

The Higgs branch of $6d \mathcal{N} = (1, 0)$ theories at infinite coupling

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Based on the following work:

- ▶ [arXiv:1801.01129] with A. Hanany
- ▶ [arXiv:1707.05785] with K. Ohmori, H. Shimizu and A. Tomasiello
- ▶ [arXiv:1707.04370] with K. Ohmori, Y. Tachikawa and G. Zafrir
- ▶ [arXiv:1612.06399] with T. Rudelius and A. Tomasiello

Plan

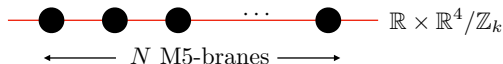
- ▶ $6d \mathcal{N} = (1, 0)$ theories on M5-branes on an ADE singularity
- ▶ Their T^2 compactification to $4d \mathcal{N} = 2$ theories
- ▶ Use lower dimensional theories to learn about the Higgs branch moduli space of $6d \mathcal{N} = (1, 0)$ theories **at infinite coupling**
- ▶ Quantify the **massless degrees of freedom** at the SCFT fixed point of a large class of $6d \mathcal{N} = (1, 0)$ theories

PART I: M5-branes on an ADE singularity

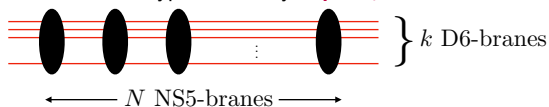
M5-branes on \mathbb{C}^2/Γ_G singularity

- ▶ The worldvolume theory of N M5-branes on flat space is $6d \mathcal{N} = (2, 0)$ theory of Type A_{N-1}
- ▶ The presence of \mathbb{C}^2/Γ_G breaks half of the amount of supersymmetry $\rightarrow 6d \mathcal{N} = (1, 0)$ theory on the worldvolume
- ▶ For $\Gamma_G = \mathbb{Z}_k$, one can conveniently find a description of the worldvolume theory in 2 steps.

1. Separate the N M5-branes

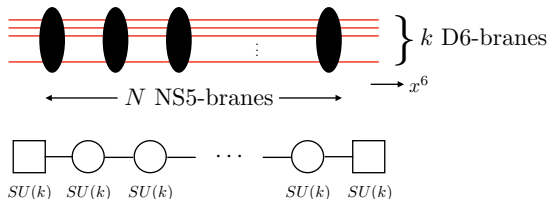


2. Reduce to the Type IIA theory [Hanany, Zaffaroni '97; Brunner, Karch '97]



A description of the theory on M5-branes on $\mathbb{C}^2/\mathbb{Z}_k$

- From the Type IIA set-up, we can write down the quiver description
[Hanany, Zaffaroni '97; Brunner, Karch '97; Ferrara, Kehagias, Partouche, Zaffaroni '98]



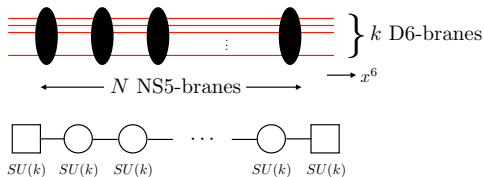
A circular node \rightarrow an $SU(k)$ vector multiplet

A square node \rightarrow an $SU(k)$ flavour symmetry

A line \rightarrow a bi-fundamental hypermultiplet + a tensor multiplet

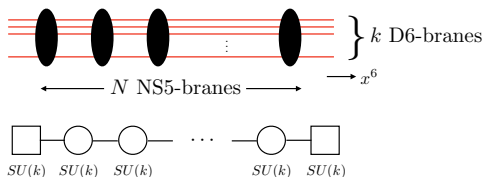
Note: Each hypermultiplet and each tensor multiplet contain a scalar component. The scalar VEVs in the h-plet parametrise the **Higgs branch** and those in the t-plet parametrise the **tensor branch** of the moduli space.

Important points



- ▶ Each NS5-brane carries a $6d \mathcal{N} = (1, 0)$ tensor multiplet (t-plet)
- ▶ The position of each NS5-brane in the x^6 -direction
 \equiv the VEV of the scalar ϕ in each t-plet
- ▶ There are $N - 1$ independent t-plets (after fixing the CoM of NS5s)
 - ▶ The VEVs of their scalars parametrise the **tensor branch** of the moduli space
- ▶ The gauge coupling $1/g_i^2$ of the i -th gauge group ($i = 1, \dots, N - 1$)
 \equiv the relative VEV $\phi_{i+1} - \phi_i$ of the scalars in the adjacent t-plets.

The infinite coupling point: SCFT



- ▶ When all NS5-branes are coincident, all gauge couplings become **infinity**

- ▶ This happens at the origin of the tensor branch, where all $\phi_{i+1} - \phi_i = 0$

- ▶ **Tensionless strings:**

The D2-branes inside the D6-branes become tensionless

(the D2-brane \equiv the instanton to the gauge field on the D6-brane)

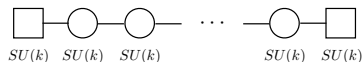
→ a critical point at the origin of the tensor branch

- ▶ Non-trivial physics: This is believed to be an **SCFT** at infinite coupling

[Hanany, Ganor '96; Seiberg, Witten '96]

The infinite coupling point: SCFT

- ▶ It should be emphasised that the quiver



provides a good description at **finite coupling**

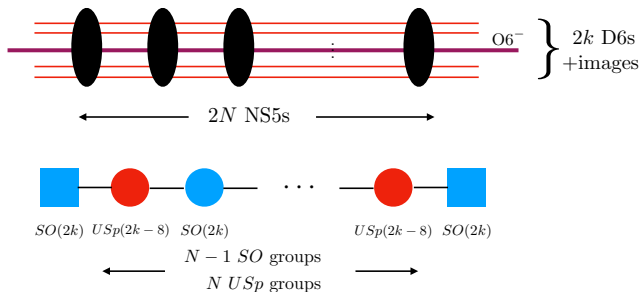
(i.e. generic VEVs of the scalars in the t-plets)

\equiv generic point of the tensor branch moduli space

- ▶ But the physics at **infinite coupling** may be different from that is described by the quiver!
- ▶ **The aim of this talk:** Show that for a number of $\mathcal{N} = (1, 0)$ theories, the Higgs branch at **infinite coupling** is *different* from that at **finite coupling**. We will also *quantify* this difference.

A description of the theory on M5-branes on \mathbb{C}^2/Γ_G (continued)

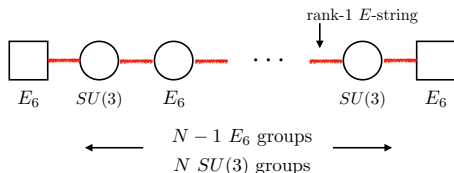
- ▶ For $G = SO(2k)$, the Type IIA description is
 [Ferrara, Kehagias, Partouche, Zaffaroni '98]



- ▶ For $G = E_{6,7,8}$, there's no known Type IIA brane construction. We need a description from F-theory
 [Aspinwall, Morrison '97; del Zotto, Heckman, Tomasiello, Vafa '14; etc.]

A description of the theory on M5-branes on \mathbb{C}^2/Γ_G (continued)

- ▶ For $G = E_6$, the quiver looks something like this



- ▶ The thick red line is *not* a fundamental hyper. It's a $6d \mathcal{N} = (1, 0)$ theory by itself, known as the **rank-1 E-string**
[Hanany, Ganor '96; Seiberg, Witten '96; Morrison, Vafa '96; Witten '96]
- ▶ A **rank-1 E-string** contains 1 tensor multiplet and at the origin of the tensor branch, it's an SCFT with E_8 global symmetry whose Higgs branch \equiv the moduli space of one E_8 instanton
- ▶ Here E_8 decomposes into $E_6 \times SU(3)$

A brief digression on F-theory quivers

- ▶ $6d$ theories can be constructed by F-theory on $\mathbb{R}^{1,5} \times$ elliptically fibred CY_3
- ▶ The base of the CY_3 is a non-compact complex 2-dimensional space with a collection of 2-cycles \mathcal{C}^i
- ▶ The size of the curves \equiv the VEVs of the scalars in $6d \mathcal{N} = (1, 0)$ t-plets
- ▶ The configuration of curves is determined by a matrix

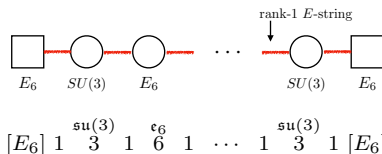
$$\eta^{ij} = -(\text{the intersection number of } \mathcal{C}^i \text{ and } \mathcal{C}^j)$$

This gives the kinetic term of tensor multiplets ϕ_i : $\eta^{ij} \partial_\mu \phi_i \partial^\mu \phi_j$

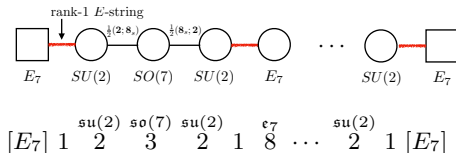
- ▶ Shrinking all curves \mathcal{C}^i simultaneously to zero size
 \Leftrightarrow taking the VEVs of the t-plets to zero \Leftrightarrow 6d SCFT

A description of the theory on M5-branes on \mathbb{C}^2/Γ_G (continued)

- ▶ $G = E_6$:



- ▶ $G = E_7$:



- ▶ $G = E_8$:

$$[E_8] \quad 1 \quad 2 \quad \overset{\text{su}(2)}{2} \quad \overset{g_2}{3} \quad 1 \quad \overset{f_4}{5} \quad 1 \quad \overset{g_2}{3} \quad \overset{\text{su}(2)}{2} \quad 2 \quad 1 \quad \overset{e_8}{12} \quad \dots \quad \overset{\text{su}(2)}{2} \quad 2 \quad 1 \quad [E_8]$$

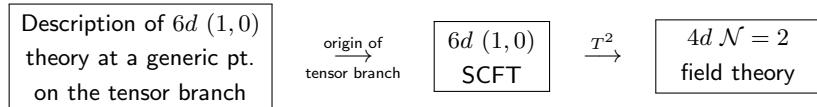
M5-branes on \mathbb{C}^2/Γ_G (continued)

- ▶ In the literature, the theory on N M5-branes on \mathbb{C}^2/Γ_G is often referred to as the **conformal matter** of type (G, G) . For $N = 1$, it's a.k.a. the **minimal conformal matter**. [del Zotto, Heckman, Tomasiello, Vafa '14]
- ▶ We have the quiver descriptions at **a generic point on the tensor branch** of these theories
 - ▶ But we want to know the physics at **infinite coupling** (e.g. extra massless degrees of freedom)
 - ▶ How do we extract such information from the quivers?

PART II: T^2 compactification

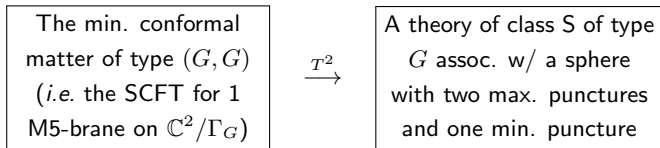
T^2 compactification

Aim: Study the Higgs branch of the $6d$ theory at infinite coupling using $4d$ theories from T^2 compactification



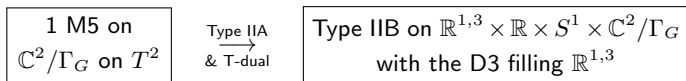
- ▶ **Working assumption:** The Higgs branch of the $6d \mathcal{N} = (1, 0)$ SCFT is the same as the Higgs branch of the $4d \mathcal{N} = 2$ theory from the T^2 compactification

T^2 compactification of the min. conformal matter theory




[Ohmori, Shimizu, Tachikawa, Yonekura (Part I) '15; del Zotto, Vafa, Xie '15]

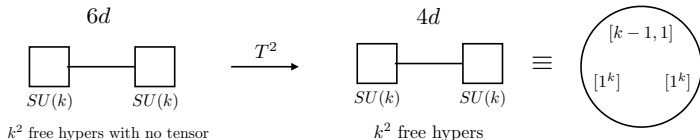
An argument using the chain of dualities



- ▶ Take the low energy limit & ignore the CoM mode of the D3
- ▶ Type IIB on $\mathbb{R} \times S^1 \times \mathbb{C}^2/\Gamma_G \rightarrow 6d (2,0)$ theory of type G on $\mathbb{R} \times S^1$
- ▶ The tension of the D3-brane becomes infinite
- ▶ The D3-brane \equiv a co-dim.-2 defect of the $\mathcal{N} = (2,0)$ theory of type G

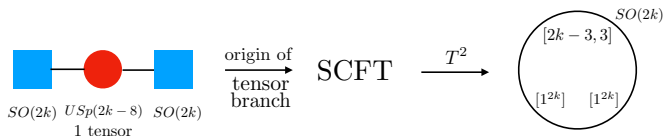
T^2 compactification of the min. conformal matter theory

- ▶ The two infinities of  $\mathbb{R} \times S^1 \equiv$ two maximal punctures
- ▶ The $4d$ theory from the T^2 compactification of the $6d$ theory \equiv a theory of class S assoc. w/ a sphere with 2 max. punctures and another puncture of type X
- ▶ To fix X , we look at $G = SU(k)$.



- ▶ Hence, X is a minimal puncture
- ▶ We'll use this class S theory to study the Higgs branch at **infinite coupling** of the $6d$ theory

Example I: 1 M5-brane on $\mathbb{C}^2/\Gamma_{D_k}$ (revisited)



- ▶ The Higgs branch dimension as computed from the **quiver description**:
 $d_{\text{Higgs}}(\text{6d quiver}) = (2k-8)(2k) - \frac{1}{2}(2k-8)(2k-7) = 2k^2 - k - 28$
- ▶ The Higgs branch dimension as computed from the *4d class S theory*:
 $d_{\text{Higgs}}(\text{4d class S}) = 2k^2 - k + 1 = d_{\text{Higgs}}(\text{6d SCFT})$
- ▶ But there is a mismatch of 29 (for all $k \geq 4$):
 $d_{\text{Higgs}}(\text{6d SCFT}) - d_{\text{Higgs}}(\text{6d quiver}) = 29$
- ▶ There are 29 extra DoFs on the Higgs branch when we go from a generic point (**finite coupling**) to the origin of the tensor branch (**infinite coupling**)
- ▶ One tensor multiplet becomes 29 hypermultiplets at **infinite coupling**

Example II: 1 M5-brane on $\mathbb{C}^2/\Gamma_{E_6}$



- ▶ The Higgs branch dimension as computed from the *4d class S theory*:

$$d_{\text{Higgs}}(\text{4d class S}) = 79 = d_{\text{Higgs}}(\text{6d SCFT})$$

- ▶ In the quiver, there's no hyper whose VEV higgses the gauge group $SU(3)$.
- ▶ But if we assume that ALL 3 tensors become 29×3 hypers at the origin of the tensor branch, we obtain the Higgs branch dimension to be

$$(29 \times 3) - 8 = 79 ,$$

in agreement with the above $d_{\text{Higgs}}(\text{6d SCFT})$.

General statements

- ▶ In the previous examples, we've seen that ALL n_T tensor multiplets become $29n_T$ hypermultiplets at the origin of the tensor branch.
- ▶ This phenomenon is known as the **small instanton transition**
[Hanany, Ganor '96; Seiberg, Witten '96; Intriligator '97; Blum, Intriligator '97; Hanany, Zaffaroni ' 97]
 - ▶ It was first discussed in the context of M5/M9 brane system
 - ▶ When an M5-brane is away from the M9-brane, there's one tensor multiplet (and no hypermultiplet)
 - ▶ When the M5 is on top of the M9, this system realises the reduced moduli space of one small E_8 instanton, whose dimension is 29.
 - ▶ Indeed, at this point, the E -string, which is an M2-brane, stretching between M5 and M9 becomes tensionless.
 - ▶ The tensor multiplet becomes 29 hypermultiplets in this set-up
- ▶ However, we'll see below that it's **NOT true** in general that *all* tensors turn into hypers at infinite coupling. There're cases in which **only some of the tensors, or even none, turn into hypers.**

PART III: The Higgs branch at infinite coupling

The SCFT Higgs branch dimension

- ▶ The **main claim** of this talk is that the Higgs branch dimension of the SCFT is given by [NM, Ohmori, Shimizu, Tomasiello '17]

$$d_{\text{Higgs}}(\text{6d SCFT}) = 29N_{T \rightarrow H} + n_H - n_V$$

where $N_{T \rightarrow H}$ is the number of the tensors that turn into hypers at the origin of the tensor branch:

$$N_{T \rightarrow H} = \sum_{i,j=1}^{n_T} \eta_{ij}^{-1} (2 - \eta^{ii})(2 - \eta^{jj}) ,$$

with n_T, n_H, n_V the numbers of tensors, hypers and vectors and η the matrix of the intersection numbers of the curves in the **F-theory quiver**.

- ▶ This formula computes a quantity at the **origin of the tensor branch** using the information from a **generic point** of the tensor branch (i.e. the F-theory quiver).
- ▶ Indeed, we'll later support this formula by an anomaly argument: $N_{T \rightarrow H}$ actually comes from the Green-Schwarz-West-Sagnotti term.

Example III: N M5-brane on $\mathbb{C}^2/\Gamma_{D_k}$

- ▶ The F-theory quiver for this theory is

$$[SO(2k)] \begin{array}{c} \text{usp}(2k-8) \\ 1 \end{array} \begin{array}{c} \text{so}(2k) \\ 4 \end{array} \cdots \begin{array}{c} \text{so}(2k) \\ 4 \end{array} \begin{array}{c} \text{usp}(2k-8) \\ 1 \end{array} [SO(2k)] ;$$

there are $n_T = 2N - 1$ tensor multiplets.

- ▶ The matrix of the intersection numbers is

$$\eta = \begin{pmatrix} 1 & -1 & 0 & 0 & 0 \\ -1 & 4 & -1 & 0 & 0 \\ 0 & -1 & \ddots & -1 & 0 \\ 0 & 0 & -1 & 4 & -1 \\ 0 & 0 & 0 & -1 & 1 \end{pmatrix}$$

$$\text{Hence, } N_{T \rightarrow H} = \sum_{i,j=1}^{n_T} \eta_{ij}^{-1} (2 - \eta^{ii})(2 - \eta^{jj}) = N$$

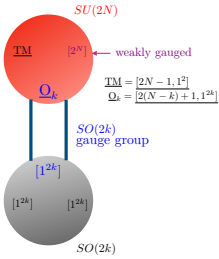
- ▶ Out of $2N - 1$ tensors, **only N tensors** turn into hypers at infinite coupling

Example III: N M5-branes on $\mathbb{C}^2/\Gamma_{D_k}$

- The Higgs branch dimension at infinite coupling is

$$\begin{aligned}
 d_{\text{Higgs}}(\text{6d SCFT}) &= 29N_{T \rightarrow H} + n_H - n_V \\
 &= 29N + 2N(2k)(2k - 4) - \left[(N - 1)k(2k - 1) \right. \\
 &\quad \left. + N(k - 1)(2k - 7) \right] \\
 &= N + \frac{1}{2}(2k)(2k - 1)
 \end{aligned}$$

- This can be checked against the Higgs branch dimension of the 4d theory from T^2 compactification [Ohmori, Shimizu, Tachikawa, Yonekura (Part II) '15; Ohmori '16]



- The resulting 4d theory is
$$\frac{S_{SU(2N)}\{\underline{\text{TM}}, [2^N], \underline{O}_k\} \times S_{SO(2k)}\{[1^{2k}], [1^{2k}], [1^{2k}]\}}{SU(N) \times \text{diag}(SO(2k) \times SO(2k))}$$
- The Higgs branch dimension is

$$d_{\text{Higgs}}(\text{4d theory}) = N + \frac{1}{2}(2k)(2k - 1)$$

Matching of certain anomaly coefficients

- ▶ Why are we able to use the effective description at finite coupling to compute a quantity at infinite coupling?

$$d_{\text{Higgs}}(\text{6d SCFT}) = 29N_{T \rightarrow H} + n_H - n_V$$

- ▶ This is because we can match the anomaly coefficients γ and δ in

$$I_8 = \alpha c_2(R)^2 + \beta c_2(R)p_1(T) + \gamma p_1(T)^2 + \delta p_2(T)$$

between the starting point and the end point of this diagram:

$$\text{6d quiver} \xrightarrow{\text{origin}} \text{6d SCFT} \xrightarrow{\text{Higgs flow}} d_{\text{Higgs}}(\text{6d SCFT}) \text{ hypers} + n \text{ tensors}$$

- ▶ Matching δ gives

$$d_{\text{Higgs}}(\text{6d SCFT}) + 29n = 29n_T + n_H - n_V$$

- ▶ Matching γ gives [Green, Schwarz, West '85; Sagnotti '92]

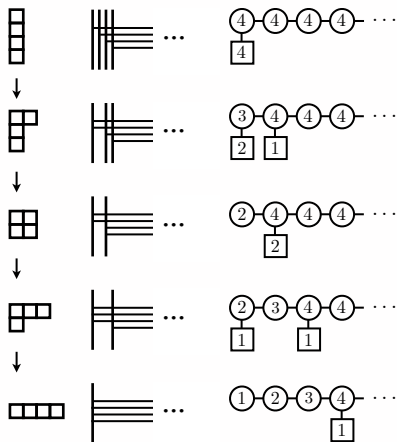
$$n_T = n_{\text{GSWS}} + n = \sum_{i,j=1}^{n_T} \eta_{ij}^{-1} (2 - \eta^{ii})(2 - \eta^{jj}) + n$$

where $n_{\text{GSWS}} = \sum_{i,j=1}^{n_T} \eta_{ij}^{-1} (2 - \eta^{ii})(2 - \eta^{jj}) = N_{T \rightarrow H}$

PART III: Applications

Example IV: T-brane theories

- ▶ Start with a theory on M5-branes on \mathbb{C}^2/Γ_G : Flavour symmetry $G \times G$
- ▶ Can turn on the nilpotent VEV to Higgs each flavour symmetry G
- ▶ **Example:** The case of $G = SU(4)$ [Kraft, Procesi '82; Gaiotto, Witten '08; del Zotto, Heckman, Tomasiello, Vafa '14; Heckman, Rudelius, Tomasiello '14; Cabrera, Hanany '16, '17]



Example IV: T-brane theories (continued)

- ▶ The Higgsing is labelled by a nilpotent orbit Y of G
 - ▶ For $G = SU(k)$, Y is specified by a partition of k
 - ▶ For $G = SO(2k)$, Y is specified by a D -partition of $2k$
 - ▶ For G an exceptional group, Y is specified by a Bala-Carter label
- ▶ Suppose that we Higgs $G \times G$ with the orbit Y_L for the first G and with the orbit Y_R for the second G .
 - ▶ The resulting theory is known as a **T-brane theory**, $T_G(Y_L, Y_R)$
 - ▶ **Example:** $G = SU(4)$, $Y_L = [2, 1^2]$ and $Y_R = [2^2]$

$$\begin{array}{ccccccc} \mathfrak{su}_3 & \mathfrak{su}_4 & \mathfrak{su}_4 & \dots & \mathfrak{su}_4 & \mathfrak{su}_4 & \mathfrak{su}_2 \\ 2 & 2 & 2 & & 2 & 2 & 2 \\ [SU(2)] & [N_f=1] & & & & [SU(2)] & \end{array}$$

- ▶ **Example:** $G = E_6$, $Y_L = E_6$ (principal orbit) and $Y_R = 0$ (trivial orbit)

$$2 \quad \mathfrak{su}_2 \quad \mathfrak{g}_2 \quad \mathfrak{f}_4 \quad \mathfrak{su}_3 \quad \mathfrak{e}_6 \quad \mathfrak{su}_3 \\ 2 \quad 2 \quad 3 \quad 1 \quad 5 \quad 1 \quad 3 \quad 1 \quad 6 \quad 1 \quad 3 \quad 1 \quad \dots \quad [E_6]$$

Example IV: T-brane theories (continued)

- ▶ The Higgs branch dimension at infinite coupling of $T_G(Y_L, Y_R)$ is

$$d_{\text{Higgs}}^{\text{CFT}} T_G(Y_L, Y_R) = \mathfrak{n} + \dim(G) + 1 - d_{Y_L} - d_{Y_R}$$

- ▶ $\mathfrak{n} = \#$ of the (-2) -curves after blowing down all (-1) -curves
 - ▶ **Blowing down a (-1) -curve:** $x \ 1 \ y \rightarrow (x-1) \ (y-1)$
 - ▶ **Field theoretically:** No matter how we try to higgs the theory at a generic point of tensor branch, there still remain \mathfrak{n} tensor multiplets which remain un-higgsed.
- ▶ d_{Y_L}, d_{Y_R} are the dimension of the orbits Y_L and Y_R
- ▶ Here, $N_{T \rightarrow H} = n_T - \mathfrak{n}$, and

$$29n_T + n_H - n_V = 30\mathfrak{n} + \dim(G) + 1 - d_{Y_L} - d_{Y_R}$$
- ▶ **Example.** $G = E_6, Y_L = E_6$ and $Y_R = 0$:

$$2 \overset{\text{su}_2}{2} \overset{\text{g}_2}{3} 1 \overset{\text{f}_4}{5} 1 \overset{\text{su}_3}{3} 1 [E_6]$$

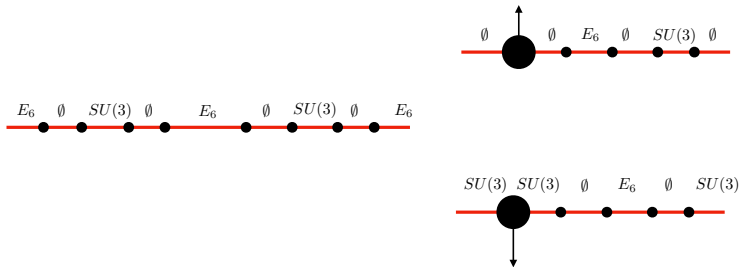
- ▶ Blow down the (-1) -curves:

$$22315131 \rightarrow 2224131 \rightarrow 222321 \rightarrow 22231 \rightarrow 2222$$
- ▶ We have $\mathfrak{n} = 4, \dim(G) = 78, d_{Y_L} = 36, d_{Y_R} = 0$
- ▶ $d_{\text{Higgs}}^{\text{CFT}} T_{E_6}(E_6, 0) = 4 + 78 + 1 - 36 - 0 = 47$

Example V: Frozen singularities

[de Boer, Dijkgraaf, Hori, Keurentjes, Morgan, Morrison, Sethi '01; Atiyah, Witten '01; Tachikawa '15]

- ▶ One can combine fractional M5-branes on a singularity in different ways
- ▶ **Example:** 2 M5-branes on $\mathbb{R} \times \mathbb{R}^4 / \Gamma_{E_6}$.
Each of the individual fractions is $1/4$ an ordinary M5



- ▶ From the E_6 conformal matter theory, we can obtain

$$[1] \begin{matrix} \mathfrak{su}(3) \\ 3 \end{matrix} 1 \begin{matrix} \mathfrak{e}_6 \\ 6 \end{matrix} [1], \quad [SU(3)] 1 \begin{matrix} \mathfrak{e}_6 \\ 6 \end{matrix} 1 [SU(3)].$$

- ▶ In the first case, E_6 is said to be **completely frozen** to $G_{\text{fr}} = \{1\}$
- ▶ In the second case, E_6 is said to be **partially frozen** to $G_{\text{fr}} = SU(3)$

Example V: Frozen singularities (continued)

- ▶ The Higgs branch dimension at infinite coupling is

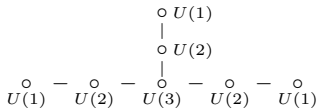
$$\dim_{\text{Higgs}}^{\text{CFT}} \mathcal{T}_{G \rightarrow G_{\text{fr}}} = n + \dim(G_{\text{fr}}) + 1$$

- ▶ Let's focus on the minimal case: $n = 0$ (i.e. the case of a single M5-brane)
- ▶ When G_{fr} is trivial (G is completely frozen), the Higgs branch dim. is 1

- ▶ The Higgs branch is \mathbb{C}^2/Γ_G
- ▶ When $\mathcal{T}_{G \rightarrow \emptyset}$ compactified on T^3 to 3d, the Coulomb branch dim. is $h_G^\vee - 1$. This is equal to (# tensors + total rank of the gauge groups) in $\mathcal{T}_{G \rightarrow G_{\text{fr}}}$

- ▶ $\mathcal{T}_{G \rightarrow \emptyset} \xrightarrow{T^3}$ 3d $\mathcal{N} = 4$ quiver theory given by an [affine Dynkin diagram](#) of G with unitary gauge groups of ranks equal to the Coxeter labels

- ▶ **Example:** $G = E_6$



with an overall $U(1)$ modded out

Example V: Frozen singularities (continued)

- ▶ **Another application:** “New” conformal matter theories of type (G, G) with G non-simply-laced. For example, starting from one M5 on $\mathbb{C}^2/\Gamma_{E_8}$

$$[E_8] \quad 1 \quad 2 \quad \overset{\mathfrak{su}(2)}{2} \quad \overset{\mathfrak{g}_2}{3} \quad 1 \quad \overset{\mathfrak{f}_4}{5} \quad 1 \quad \overset{\mathfrak{g}_2}{3} \quad \overset{\mathfrak{su}(2)}{2} \quad 2 \quad 1 \quad [E_8]$$

one can obtain the following (G_2, G_2) and (F_4, F_4) conformal matter theories by partially freezing E_8 :

$$[G_2] \quad \overset{\mathfrak{su}_2}{2} \quad 2 \quad 1 \quad \overset{\mathfrak{e}_8}{12} \quad 1 \quad 2 \quad \overset{\mathfrak{su}_2}{2} \quad \overset{\mathfrak{g}_2}{3} \quad 1 \quad \overset{\mathfrak{f}_4}{5} \quad 1 \quad [G_2] ,$$

$$[F_4] \quad 1 \quad \overset{\mathfrak{g}_2}{3} \quad \overset{\mathfrak{su}_2}{2} \quad 2 \quad 1 \quad \overset{\mathfrak{e}_8}{12} \quad 1 \quad 2 \quad \overset{\mathfrak{su}_2}{2} \quad \overset{\mathfrak{g}_2}{3} \quad 1 \quad [F_4]$$

Conclusions

- ▶ In general, the Higgs branch at infinite coupling can be different from that at finite coupling.
- ▶ A certain number of tensor multiplets become hypermultiplets at the origin of the tensor branch. We have quantified how many.
- ▶ The Higgs branch dimension of the SCFT at the infinite coupling point can be computed using the quiver data at a generic point of tensor branch.
- ▶ **Applications:** T-brane theories, and theories associated with (partially or completely) frozen singularities.
- ▶ Deeper understanding of fractional M5-branes.