

# Synchrotron Radiation

## Illuminating the NanoCosmos

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**DESY**

**IX. Research Course on New X-Ray Sciences**

**17. February 2010**

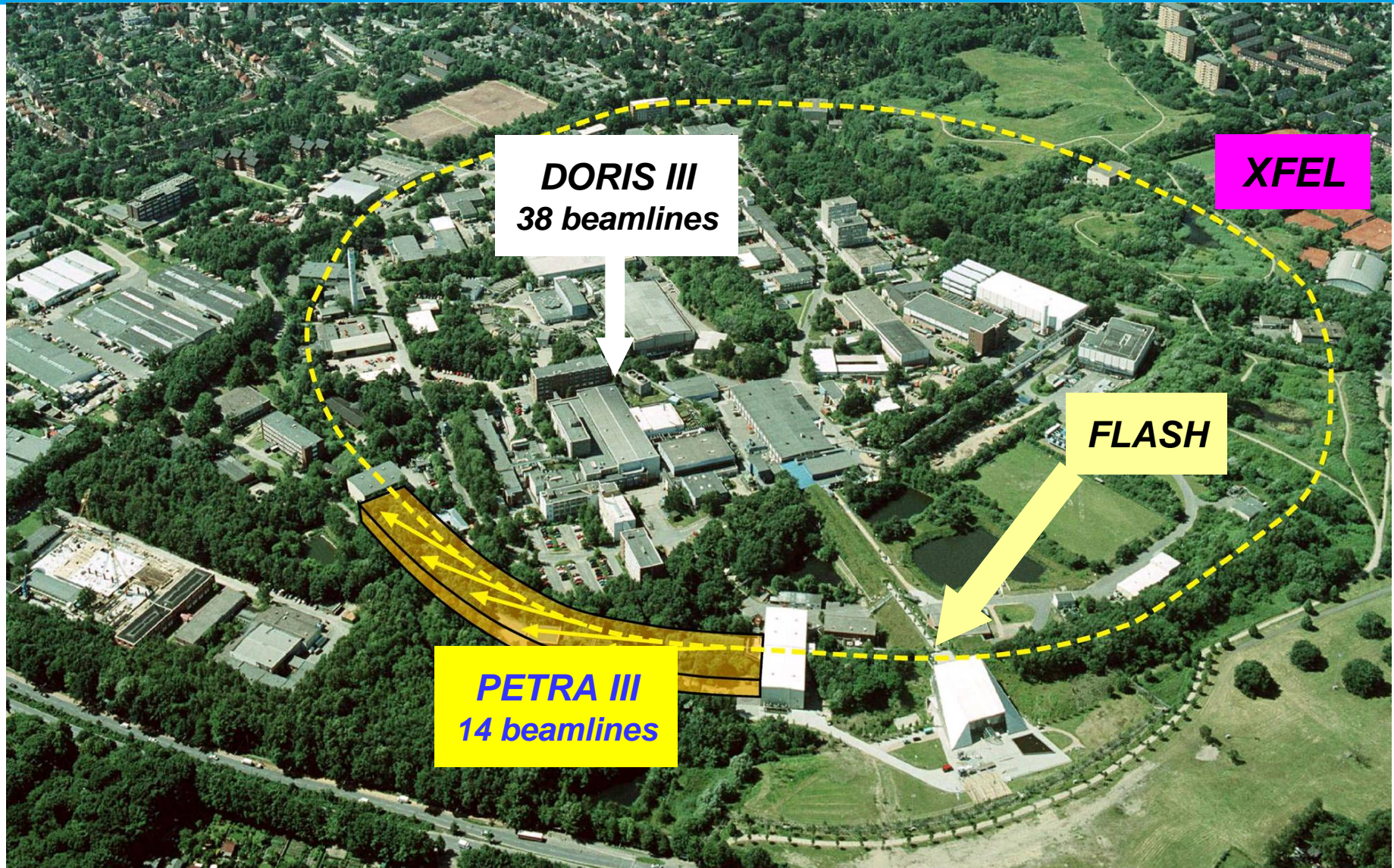
- **Generation and Properties of Synchrotron Radiation**
- **Synchrotron Radiation Sources at DESY**
- **Research Examples**

**Protein Crystallography**

**Buried Interfaces**

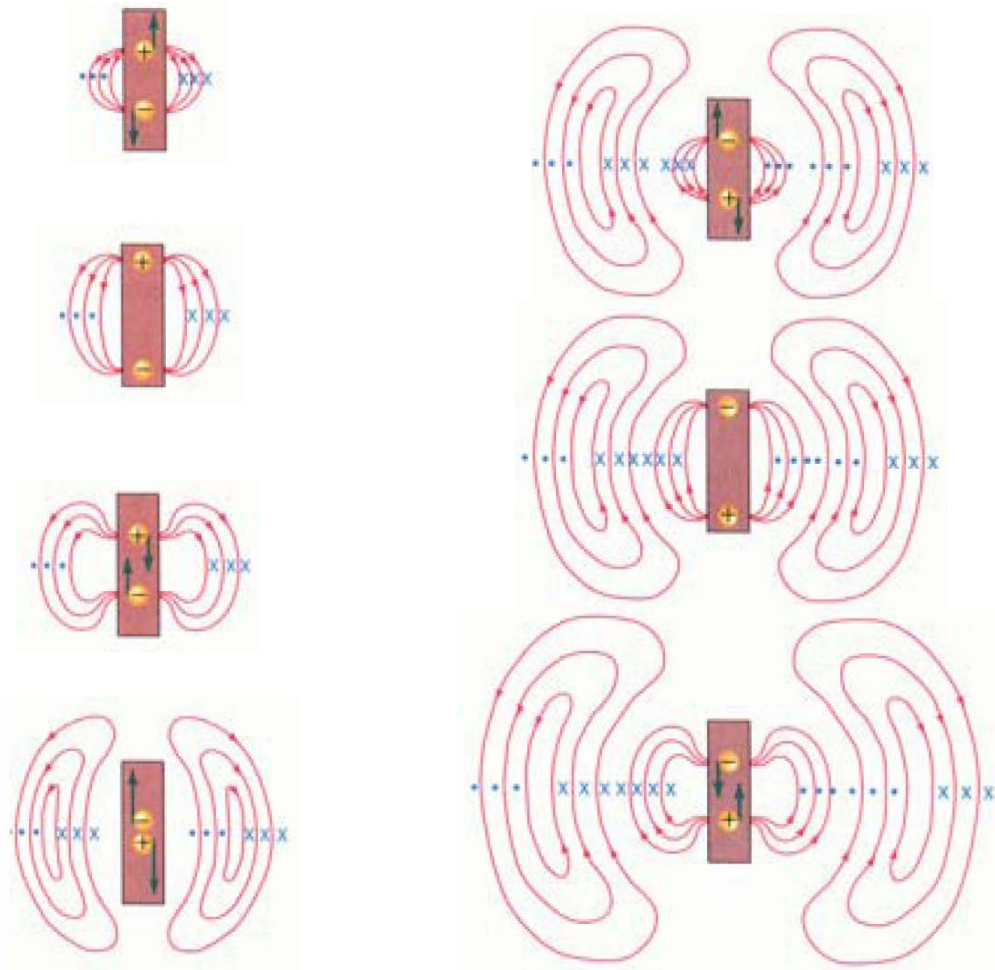


# Photon Sources at DESY



# The Electric Dipole (1)

Electric and magnetic fields around an oscillating electric dipole

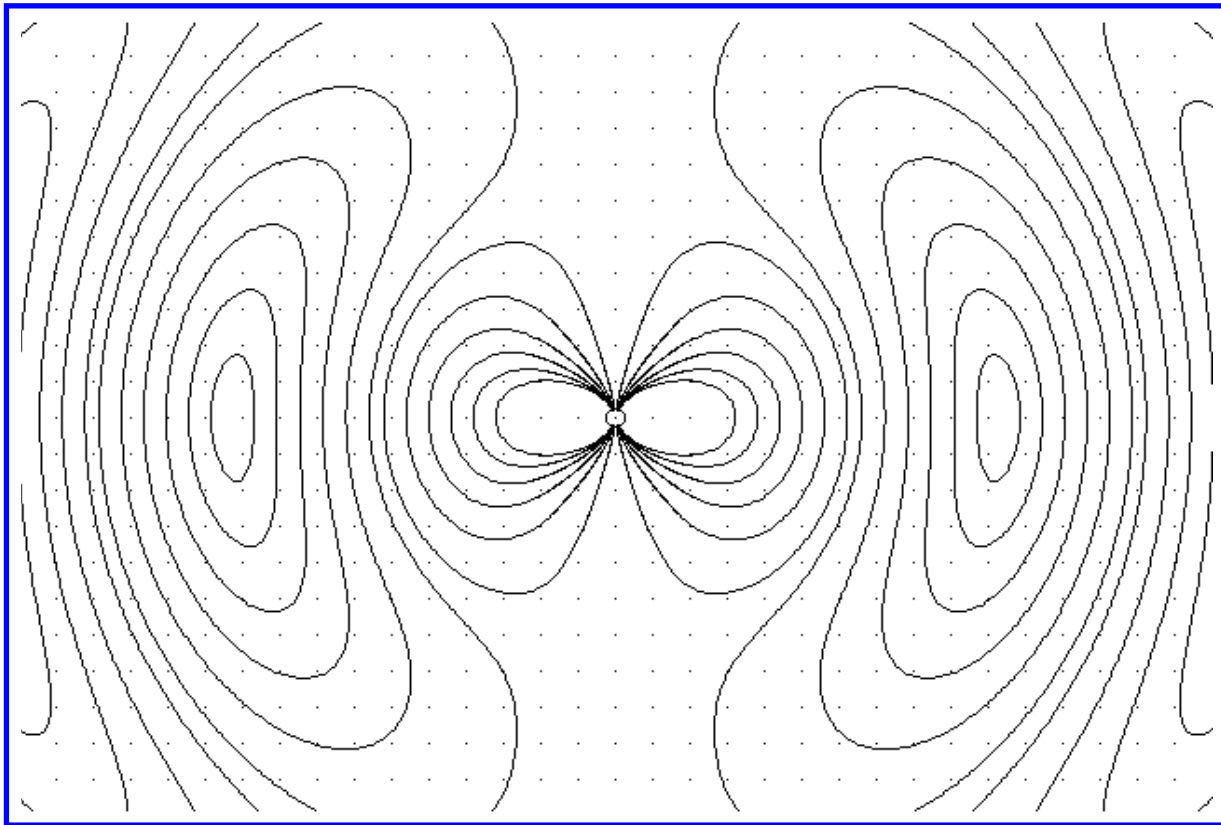


**First Halfperiod:**  
E- and B-fields  
propagate into space

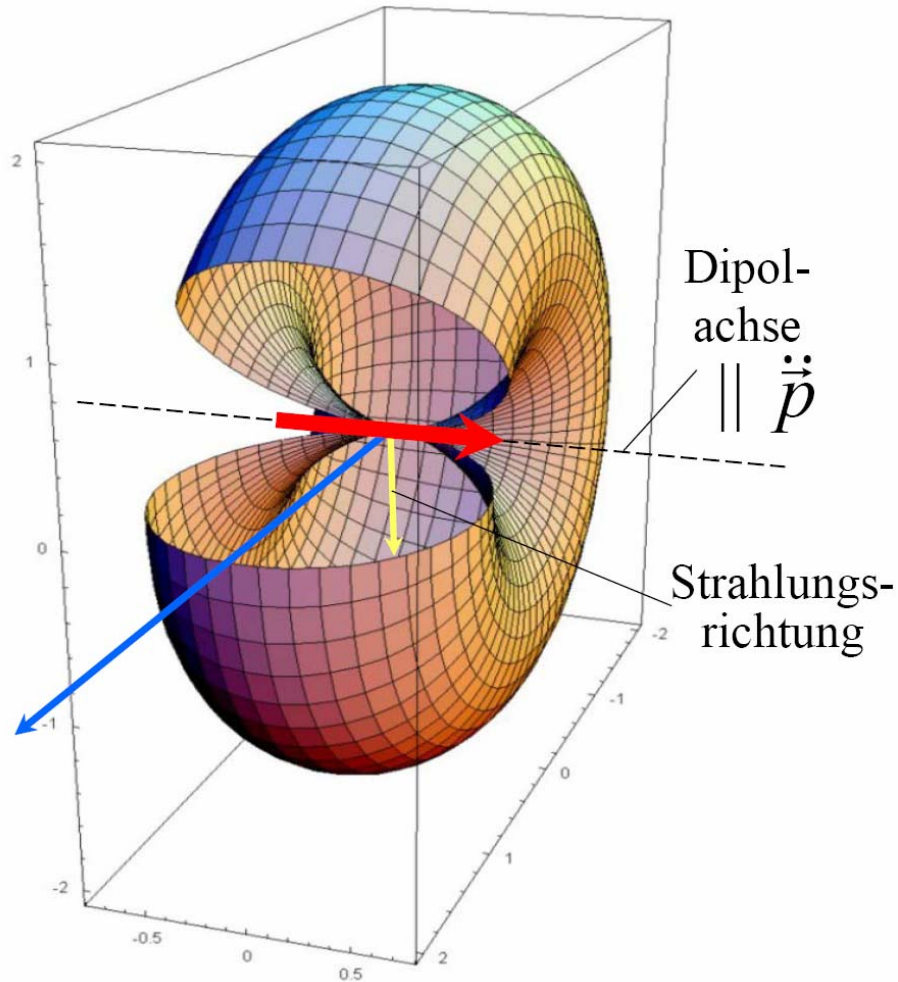
**Second Halfperiod:**  
Change of sign, the outer  
fields decouple and  
propagate freely.

# The Electric Dipole (2)

- Generation of electromagnetic waves
- Field lines around an oscillating electric dipole



# Radiation characteristic of a Hertz dipole



Every accelerated charge radiates electromagnetic waves

Radiated power

$$P = \frac{e^2}{6\pi\epsilon_0 m^2 c^3} \left( \frac{d\vec{p}}{dt} \right)^2$$

Larmor formula

Oscillatory motion:  
No radiation in direction of the oscillation.

Maximum radiated power perpendicular to the oscillation direction:

# Circular Acceleration: Synchrotron Radiation

**Radiated power** of an accelerated charged particle for nonrelativistic particles: **Larmor formula**

$$P_S = \frac{e^2}{6\pi \epsilon_0 m_0^2 c^3} \left| \frac{d\vec{p}}{dt} \right|^2$$

Lorentz transformation and application to **circular acceleration**:

$$P_S = \frac{e^2 c}{6\pi \epsilon_0} \frac{1}{(m_0 c^2)^4} \frac{E^4}{R^2}$$

$E$  = particle energy

$R$  = radius of curvature

$m_0$  = particle mass

Dependence on **particle mass**:

$$\frac{P_{S,e}}{P_{S,p}} = \left( \frac{m_p}{m_e} \right)^4 \approx 10^{13}$$

Synchrotron radiation is sufficiently intense only for **electrons/positrons !**

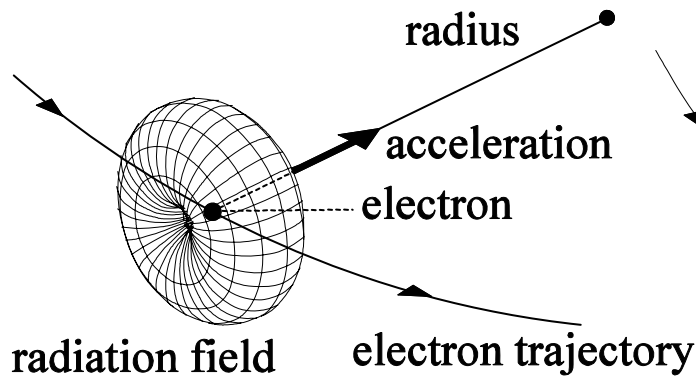


# Emission pattern for circular acceleration

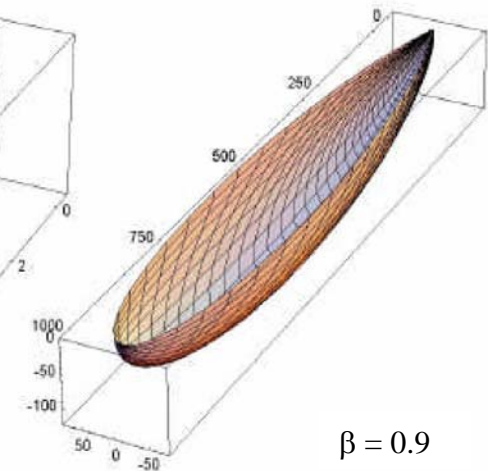
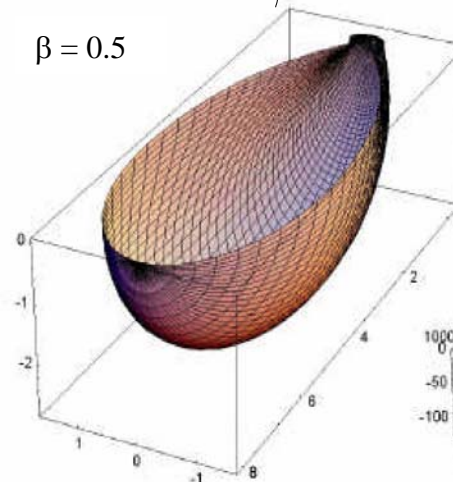
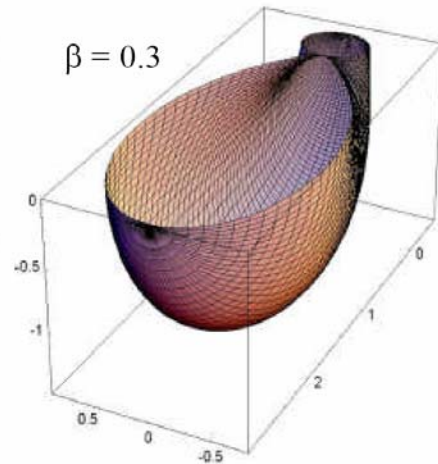
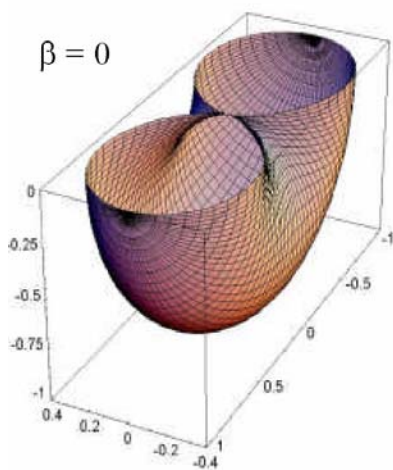
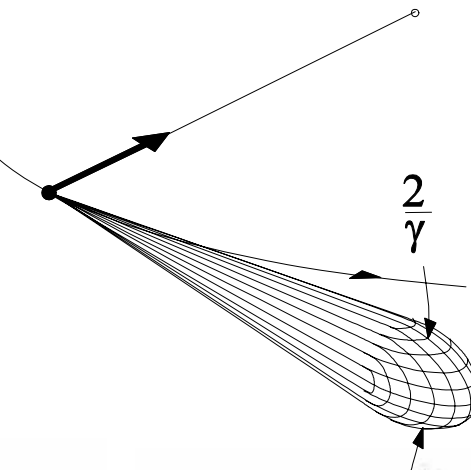
Rest frame

Lorentz transformation

Laboratory frame

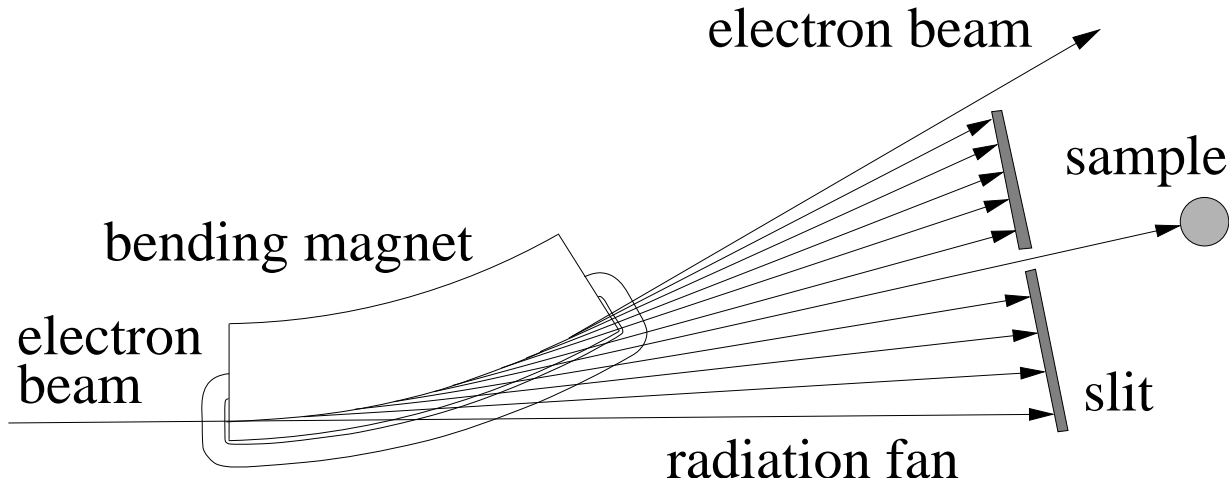


$$\gamma = \frac{1}{\sqrt{1 - \left(\frac{v}{c}\right)^2}} = \frac{E}{m_0 c^2}$$



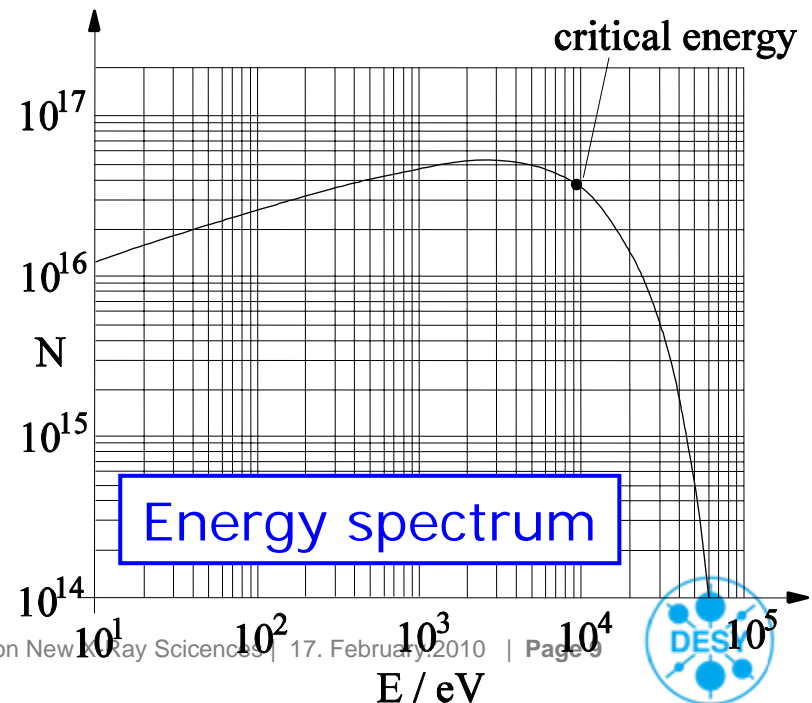


# Radiation from a bending magnet

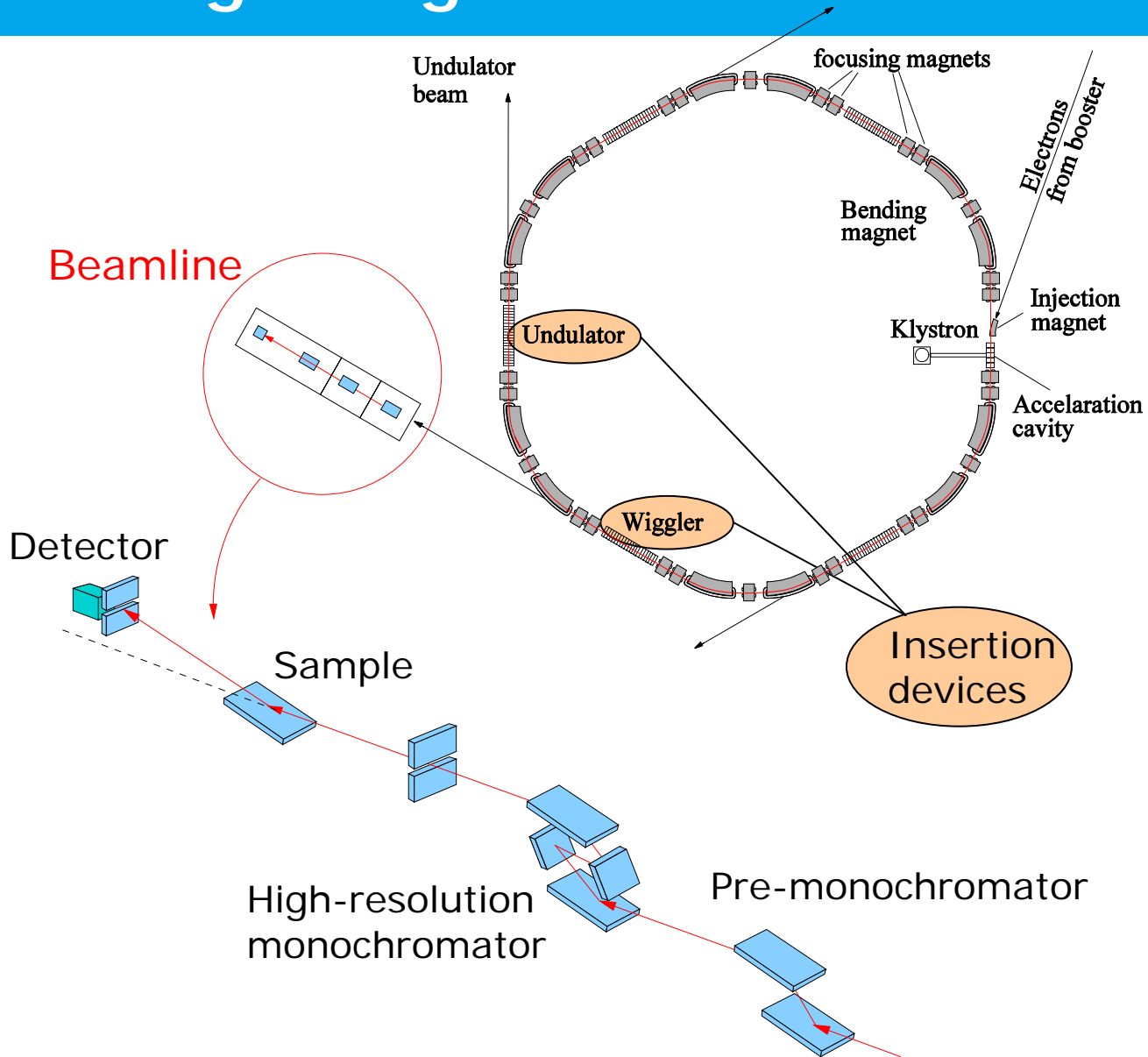


$$E = 5 \text{ GeV}$$
$$\Rightarrow \gamma = 10^4$$
$$\Rightarrow \Delta\Theta = \frac{2}{\gamma} = 0.2 \text{ mrad} \approx 40''$$

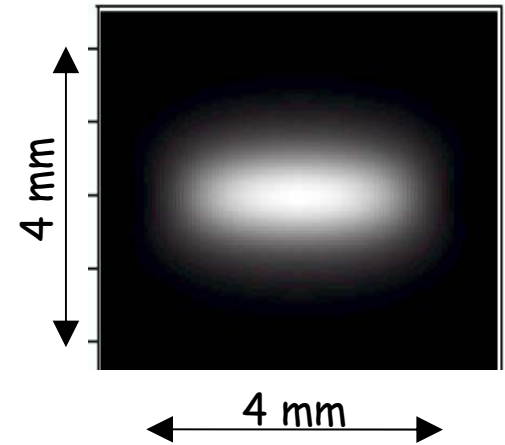
- The radiation is emitted in the plane of the orbiting particles
- The radiation is linearly polarized in the orbit plane



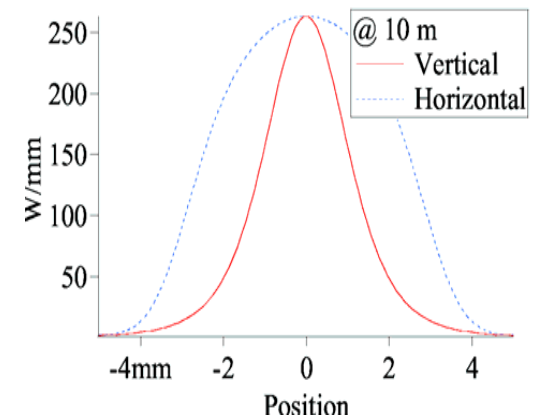
# Storage Ring and Beamlines



Photon beam profile @ 10 m distance

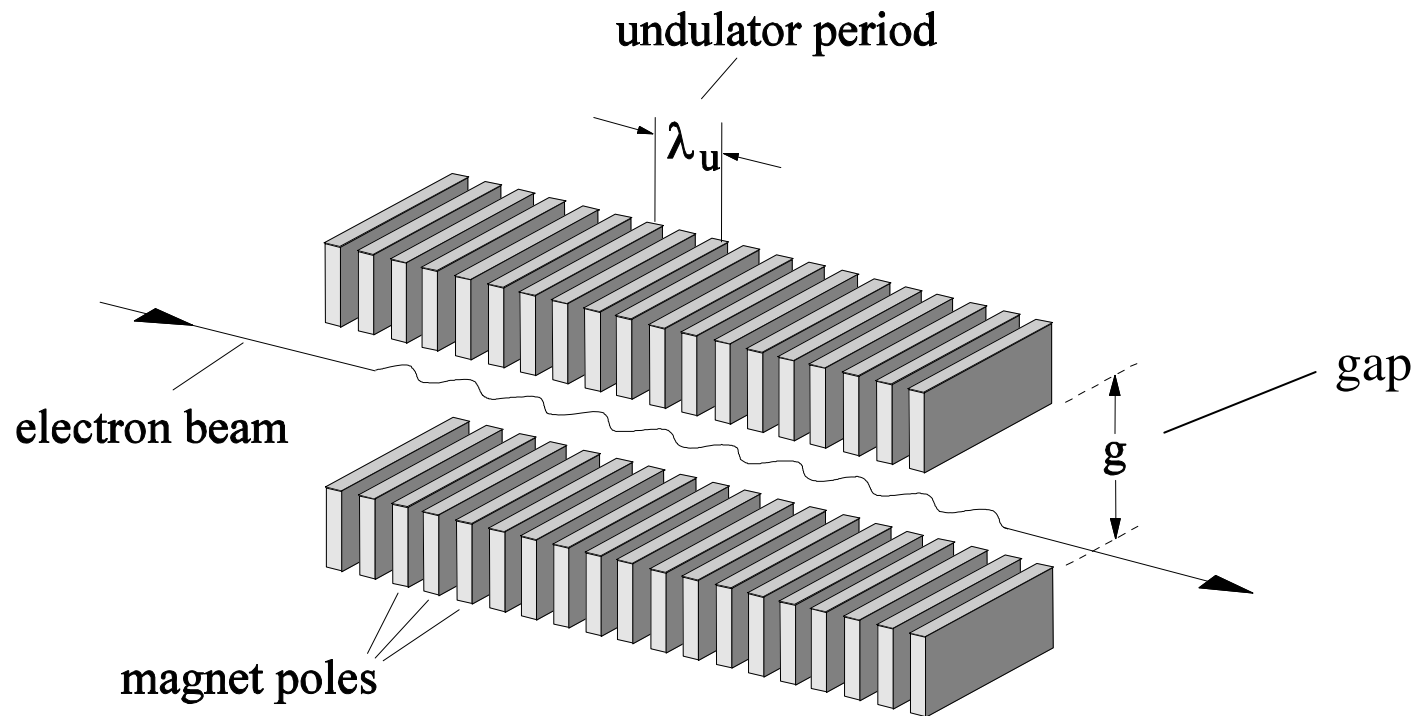


Power density



# Insertion devices: Wigglers and undulators

Electrons travelling through **periodic** magnet structures (insertion devices) :



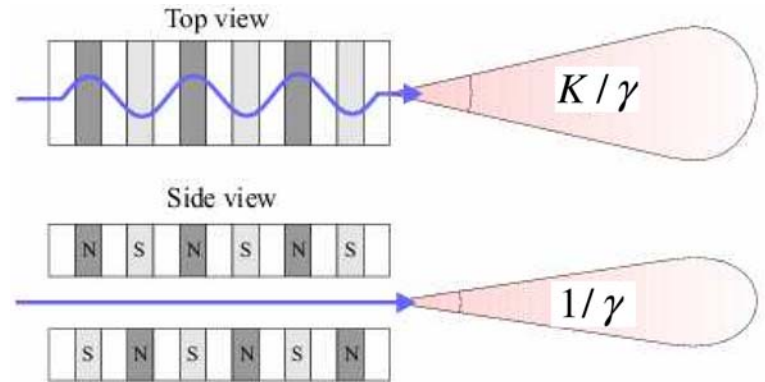
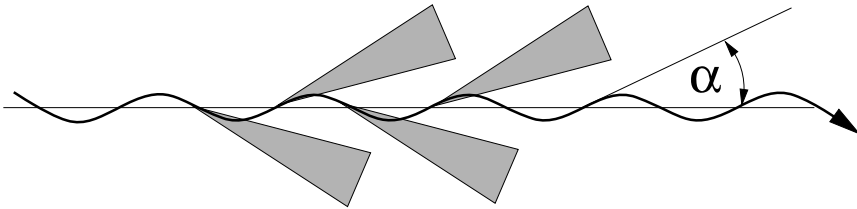
# Undulator for PETRA III



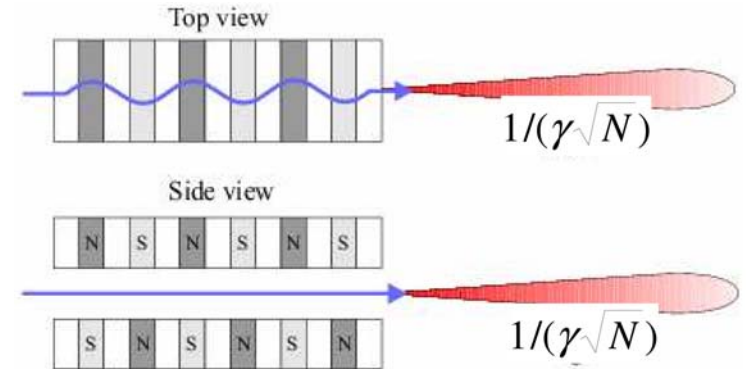
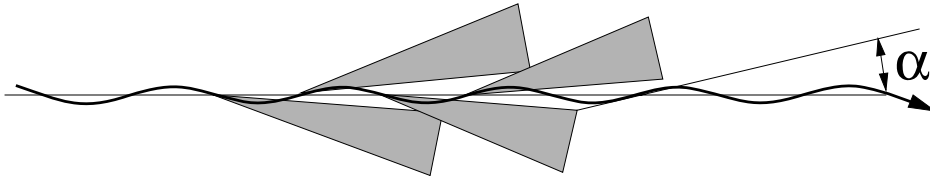
Source: Babcock  
Noell, Würzburg

# Insertion devices: Wigglers and Undulators (1)

Wiggler regime:  $\alpha > 1/\gamma$



Undulator regime:  $\alpha < 1/\gamma$



In the undulator regime the radiation cones overlap and the wave trains can interfere constructively

# Insertion devices: Wigglers and Undulators (2)

$$\alpha = \frac{K}{\gamma} \quad K : \text{deflection parameter}$$

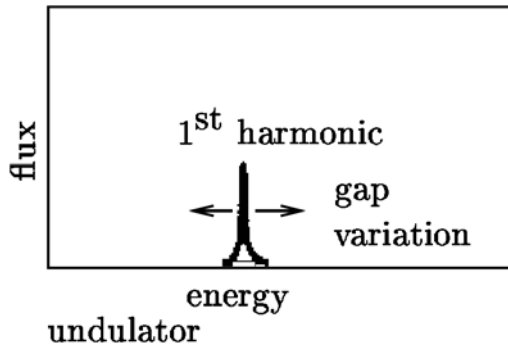
$$K = 0.934 \lambda_u(\text{cm}) B_0(\text{T})$$

$\lambda_u$  : magnetic period

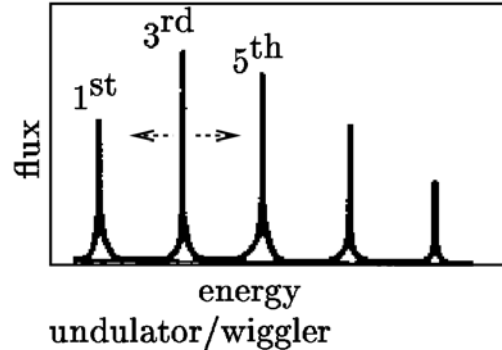
$B_0$  : magnetic field at orbit

$K$  determines the shape of the energy spectrum of an insertion device:

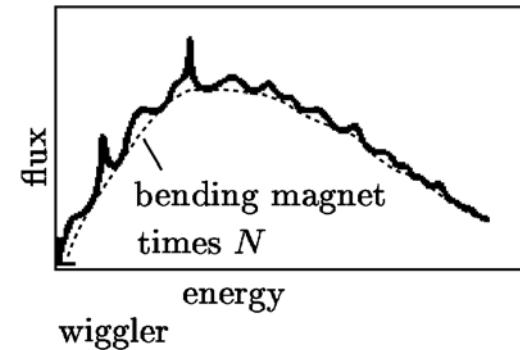
$K \ll 1, N$  large



$K \approx 1, N$  large



$K > 1, N$  smaller



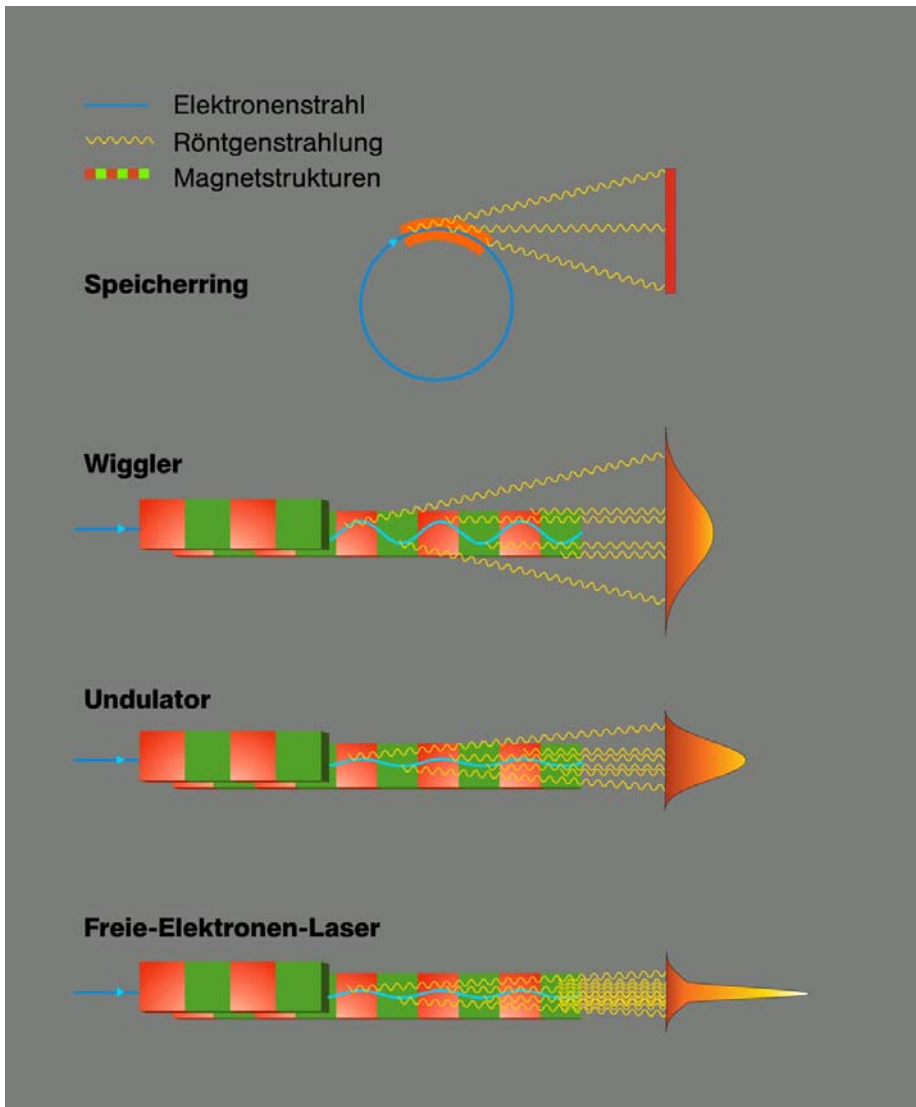
Energy of the  $n^{\text{th}}$  harmonic:

$$E_n(\text{keV}) = n \frac{0.95 E^2(\text{GeV})}{\lambda_u(\text{cm})(1 + K^2/2)}$$

Angular width of  $n^{\text{th}}$  harmonic:

$$\sigma = \frac{1}{\gamma} \sqrt{\frac{1 + \frac{1}{2}K^2}{2Nn}}$$

# Intensity of the emitted radiation



$N_p$  = Number of magnet poles

$N_e$  = Number of electrons/bunch

Incoherent superposition

$$I \sim N_e N_p$$

Partially coherent superposition

$$I \sim N_e N_p^2$$

Fully coherent superposition

$$I \sim N_e^2 N_p^2$$

Self-Amplified Spontaneous Emission (SASE) → Talk by R. Treusch

# Synchrotron Radiation: Units of Intensity

$$\text{Total flux} \equiv \frac{\text{Photons}}{\text{s}}$$

$$\text{Spectral flux} = \frac{\text{Total flux}}{0.1\% \text{ bandwidth}} \left[ \frac{\text{Photons/s}}{0.1\% \text{ bandwidth}} \right]$$

$$\text{Brightness} = \frac{\text{Total flux}}{\text{solid angle} \cdot 0.1\% \text{ bandwidth}} \left[ \frac{\text{Photons/s}}{\text{mrad}^2 \cdot 0.1\% \text{ bandwidth}} \right]$$

$$\text{Brilliance} = \frac{\text{Total flux}}{\text{solid angle} \cdot \text{source area} \cdot 0.1\% \text{ bandwidth}} \left[ \frac{\text{Photons/s}}{\text{mrad}^2 \cdot \text{mm}^2 \cdot 0.1\% \text{ bandwidth}} \right]$$

Brilliance is the figure of merit for the design of new synchrotron radiation sources

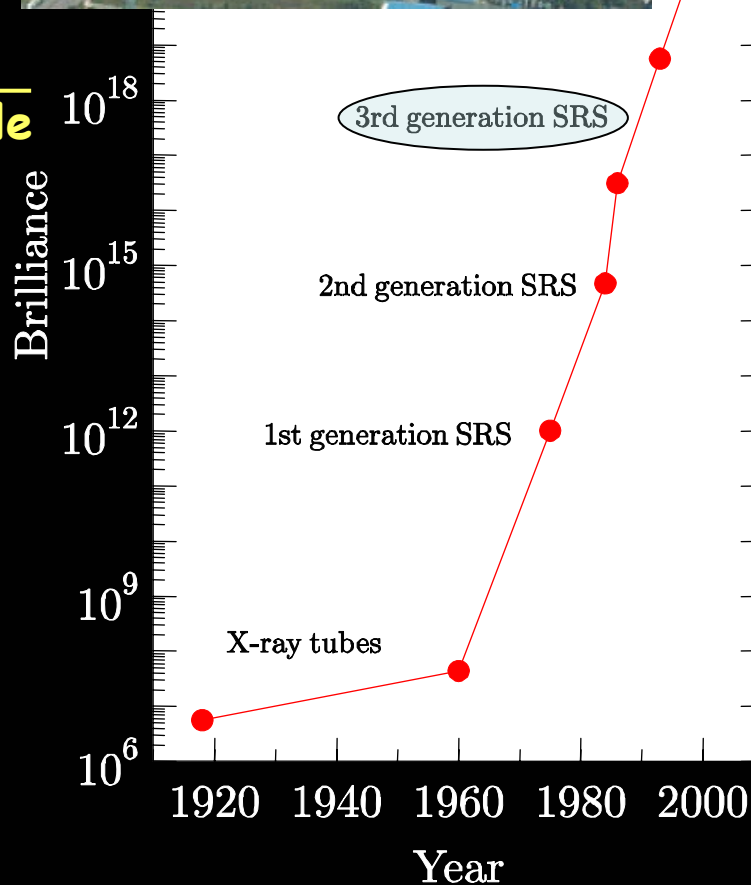




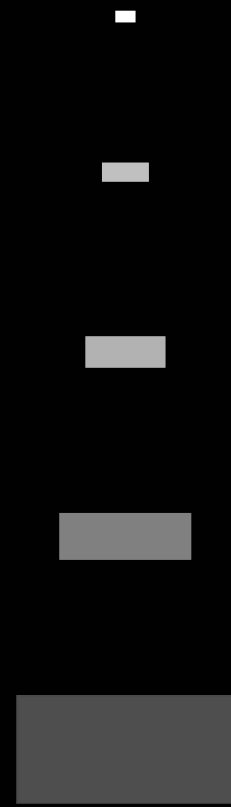
# Evolution of Source Brilliance

Brilliance =

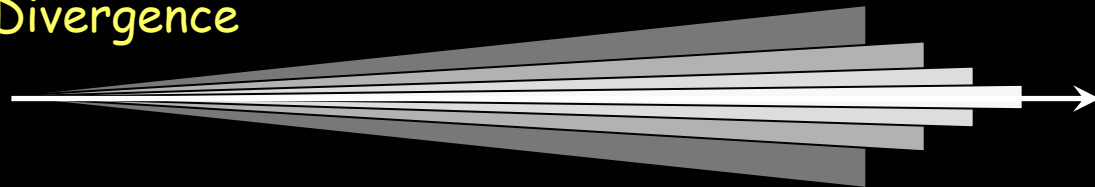
$$\frac{\text{Spectral flux}}{\text{source area} \times \text{solid angle}}$$



Source size

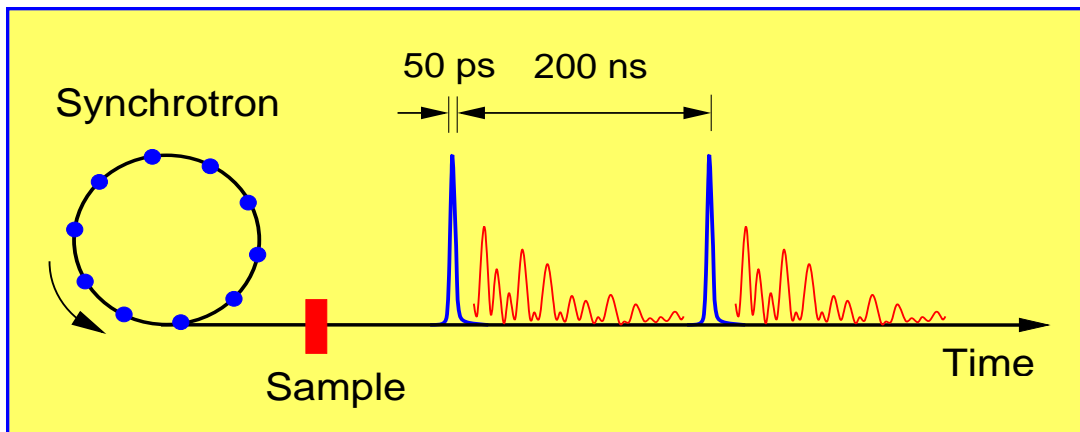
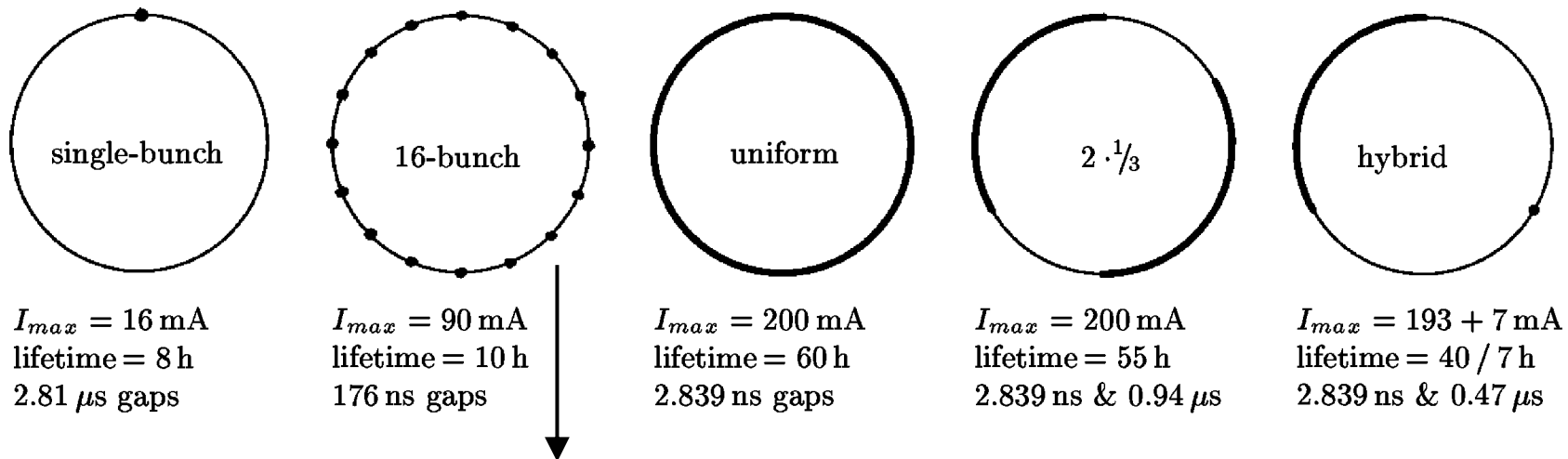


Divergence



# Time structure of synchrotron radiation (2)

Various filling modi can be realized depending on the experimental needs (example: ESRF)

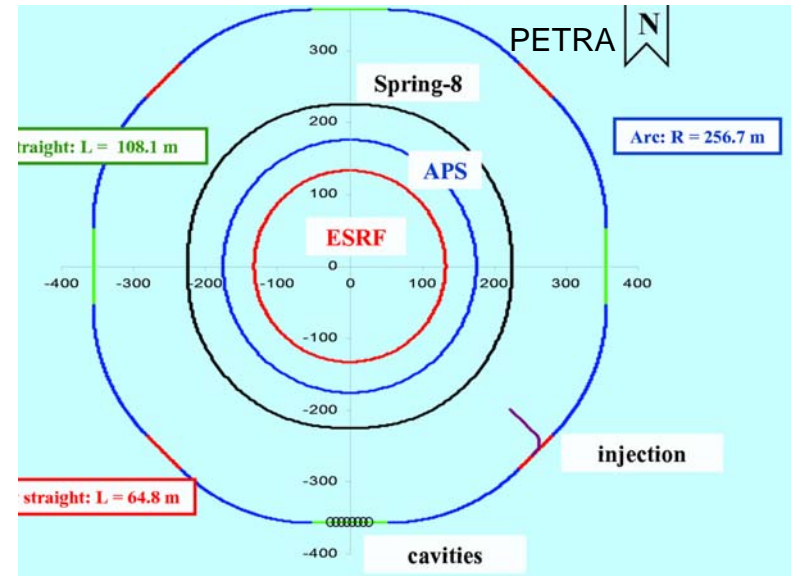
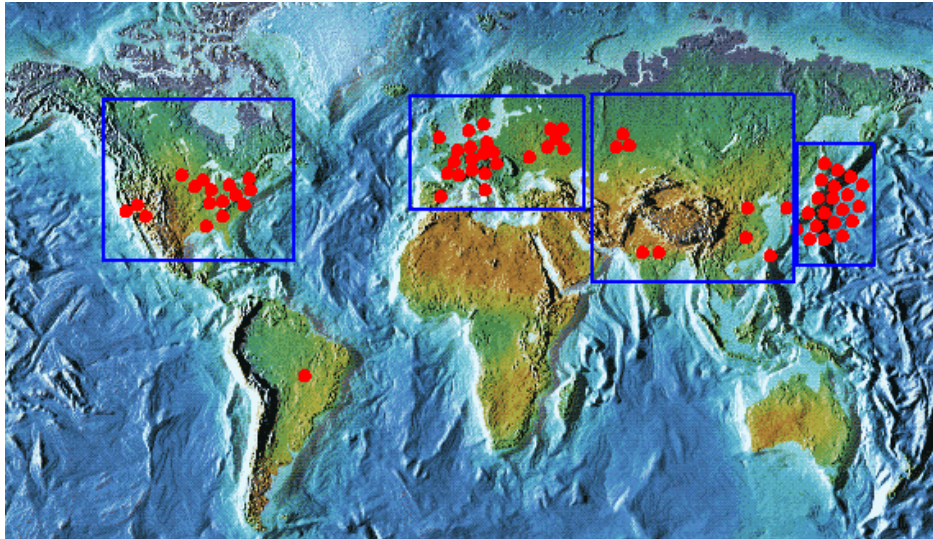


PETRA III:

950 bunches (8 ns)  
40 bunches (190 ns)

Time-resolved  
measurements

# Synchrotron radiation facilities around the world



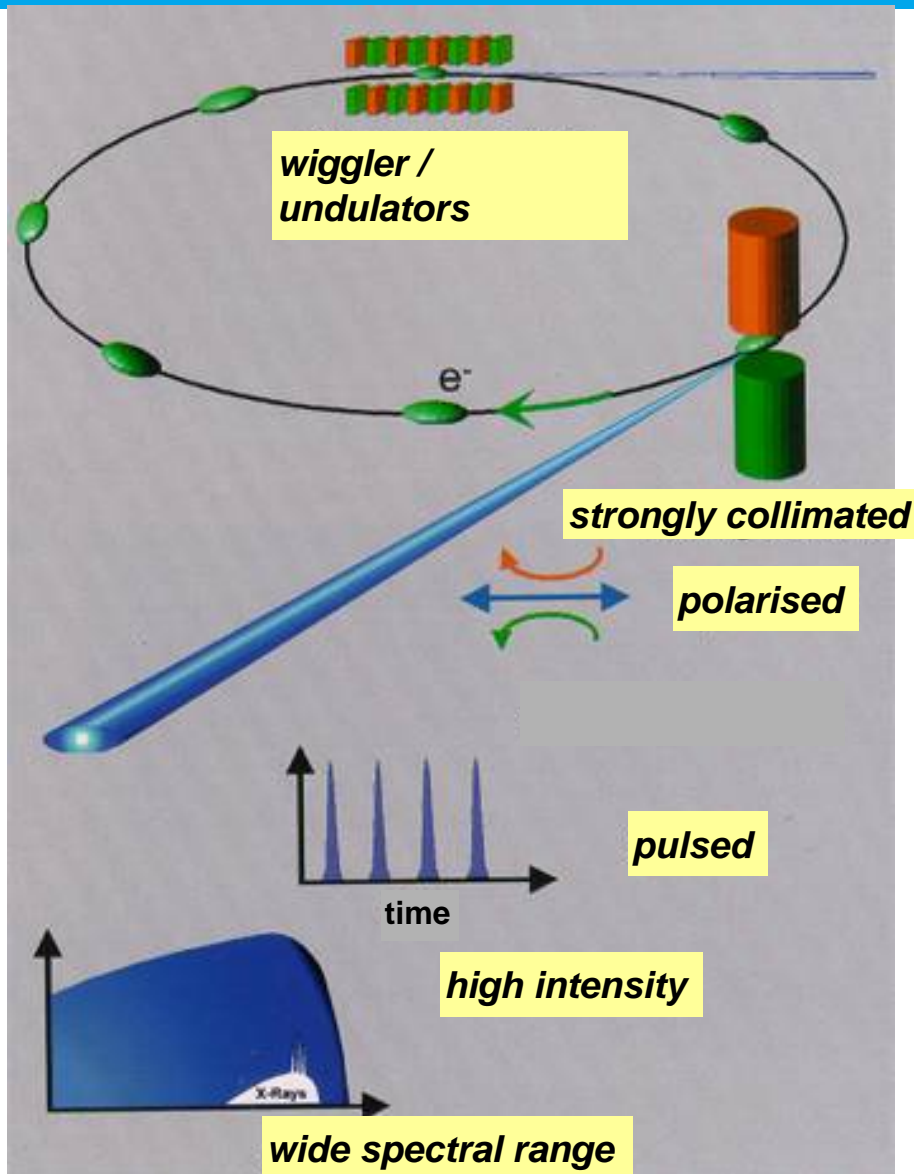
## Parameters of selected facilities

Storage Ring, Location	Particle Energy [GeV]	Circumference [m]	Orbit Period [ $\mu$ s]	Bucket Separat. [ns]	Bunch Length [ps]
ESRF, Grenoble, France	6.0	844	2.816	2.84	70
APS, Argonne, USA	7.0	1104	3.683	2.84	60
SPring8, Japan	8.0	1436	4.790	1.97	100
PETRA II, Hamburg	12.0	2304	7.680	2.00	100



European Synchrotron Radiation Facility (ESRF), Grenoble, France

# Summary: Properties of synchrotron radiation



## Properties:

- high brilliance and flux
- infrared up to hard X-rays (>100keV)
- polarization
- time structure

## Applications:

- spectroscopy
- diffraction/scattering
- imaging

## Fields:

- solid state physics
- crystallography
- structural biology
- chemistry/catalysis
- geo-/environmental science
- materials science, nano science
- medical science
- atoms, molecules and clusters
- magnetism
- engineering science

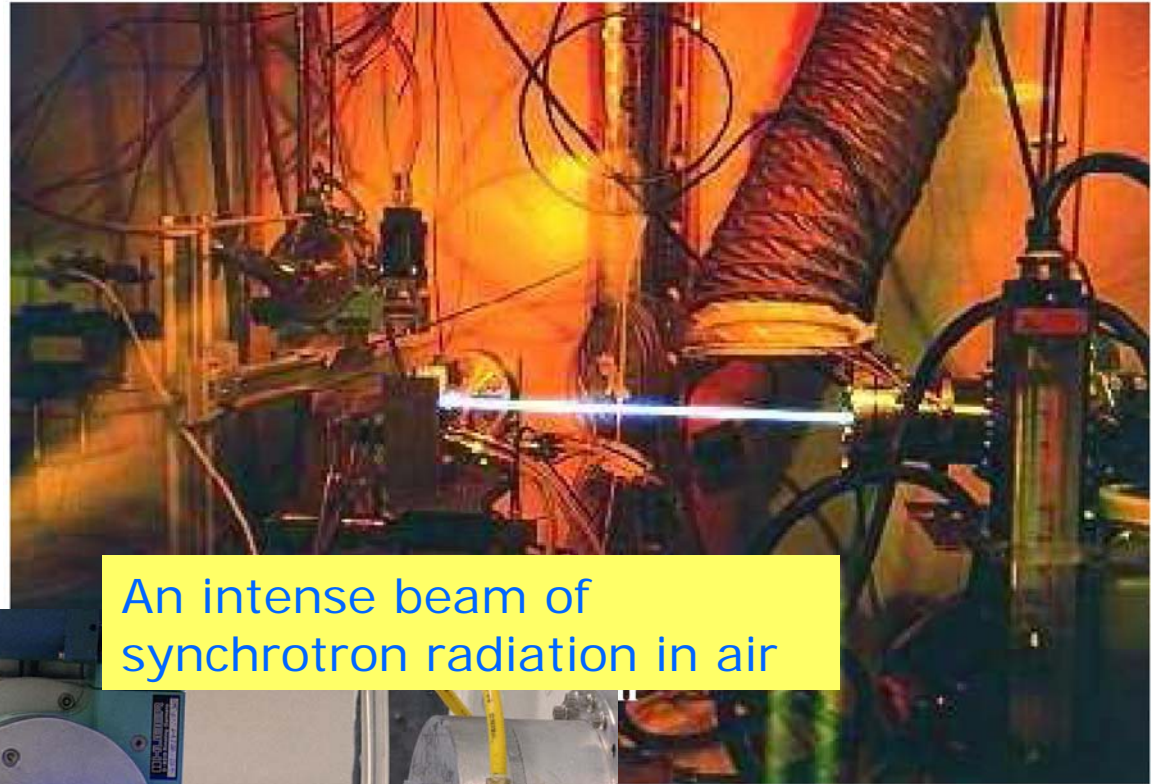
# Comparison of power densities

Sunlight on earth:

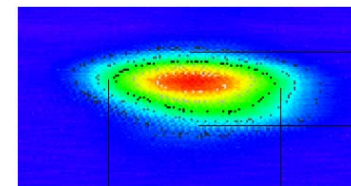
$$P_{sol} = 1 \text{ kW/m}^2$$

Synchrotron radiation  
behind undulator:

$$P_{SR} = 8000 \text{ MW/m}^2$$



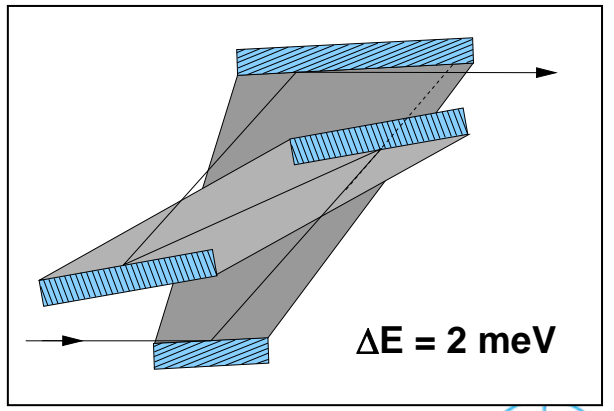
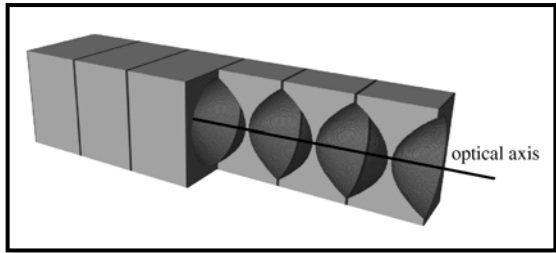
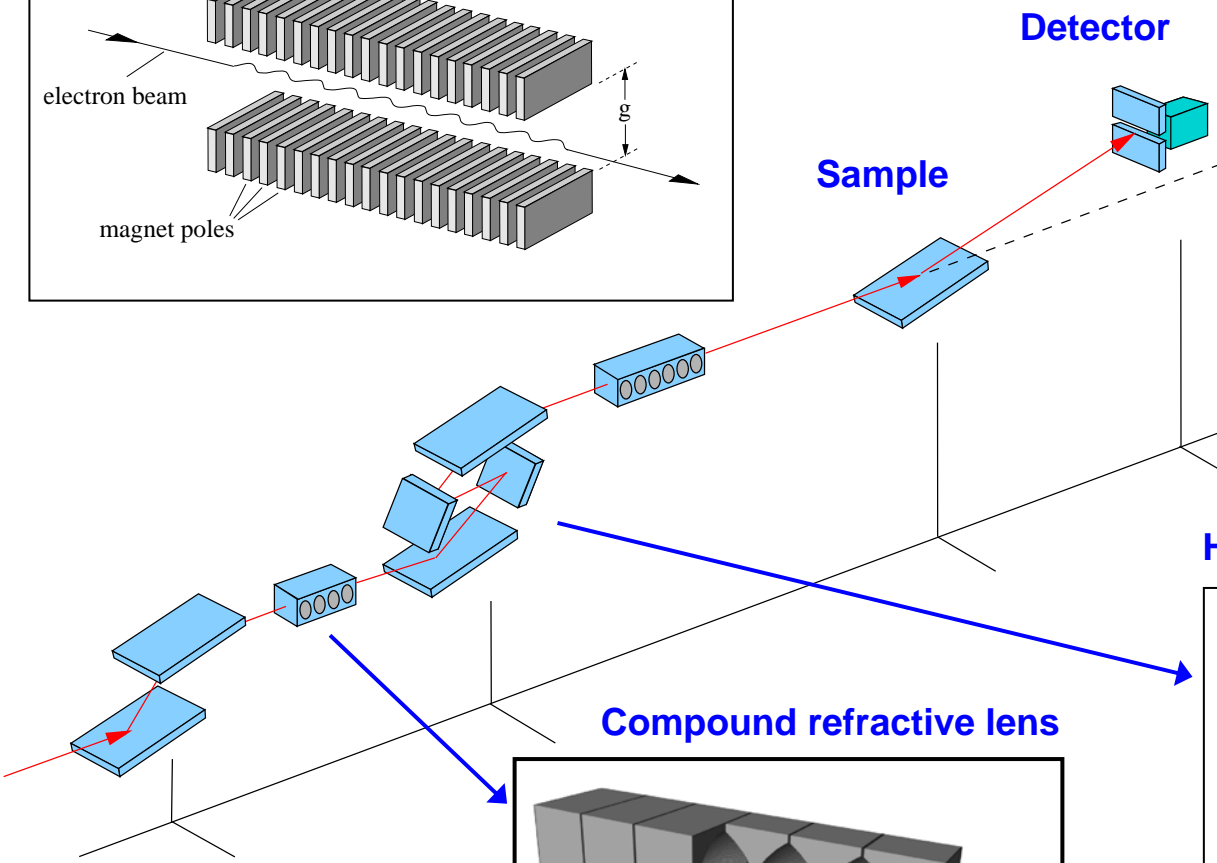
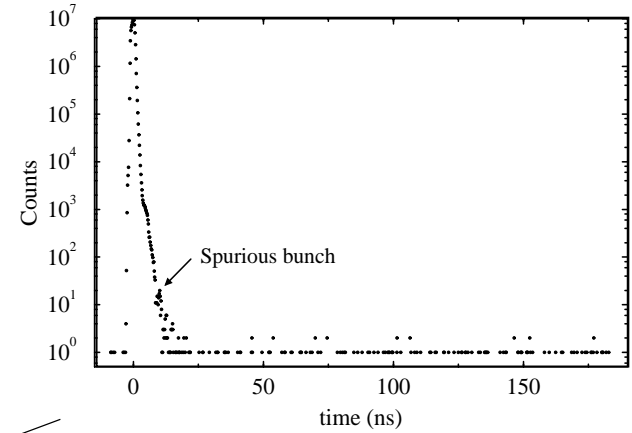
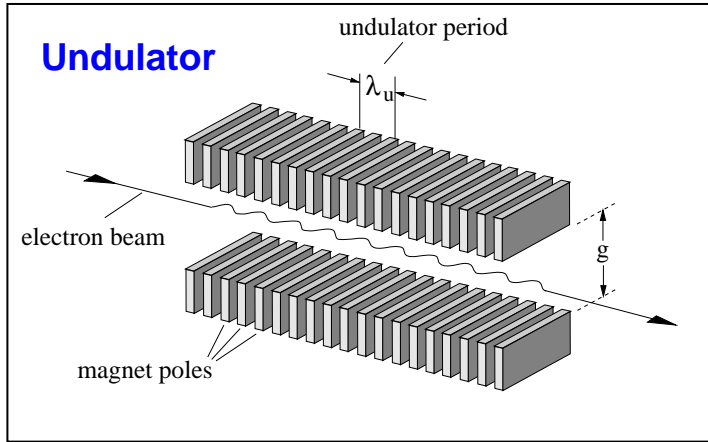
An intense beam of  
synchrotron radiation in air



20 - 100  $\mu\text{m}$

100 - 500  $\mu\text{m}$

# Handling of high-brilliance synchrotron radiation

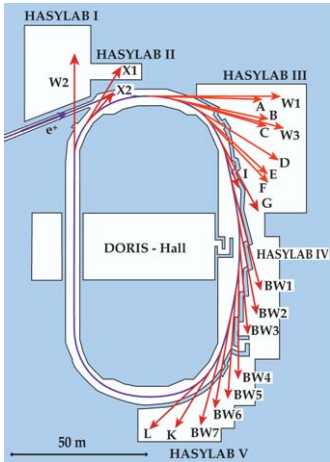


$\Delta E = 2 \text{ eV}$



# Photon Facilities at DESY

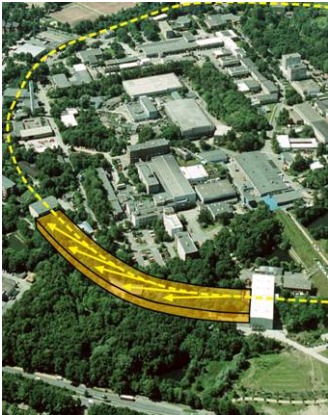
## DORIS III



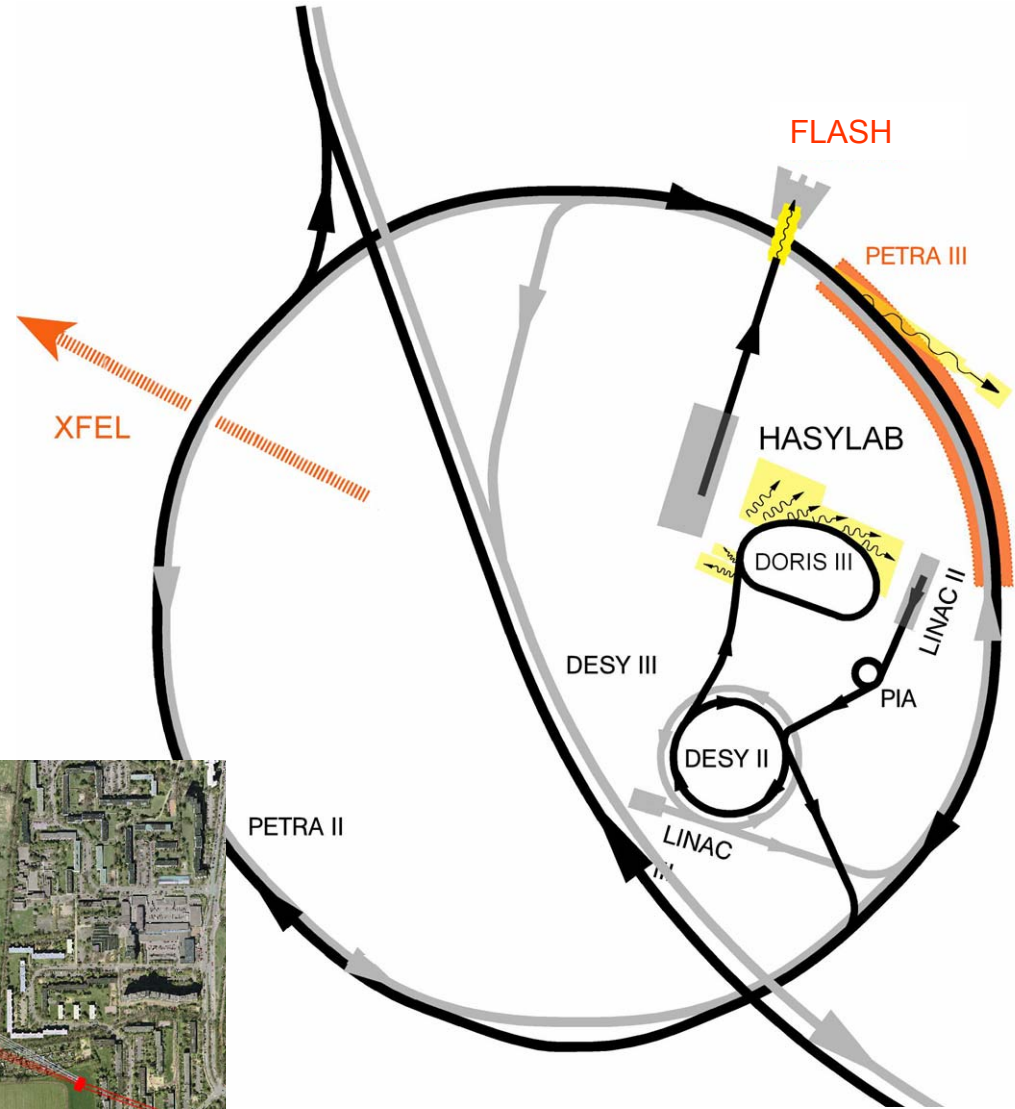
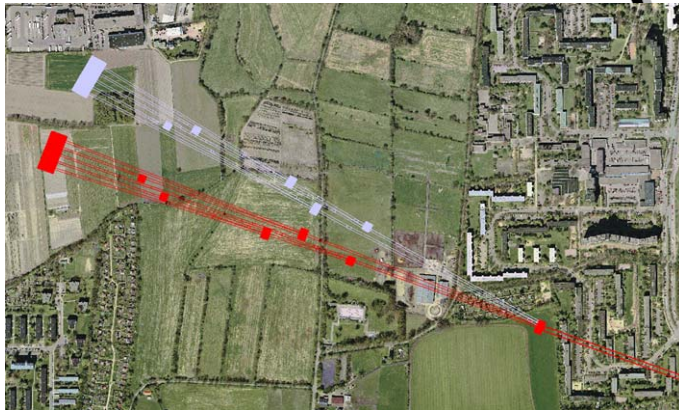
## FLASH



## PETRA III/III



## XFEL



## 38 beamlines, 70 experimental stations

### 11 Stations operated by external organizations:

- EMBL: 7
- MPG: 1
- GKSS: 1
- GFZ: 2

### 16 stations operated with support from external institutions:

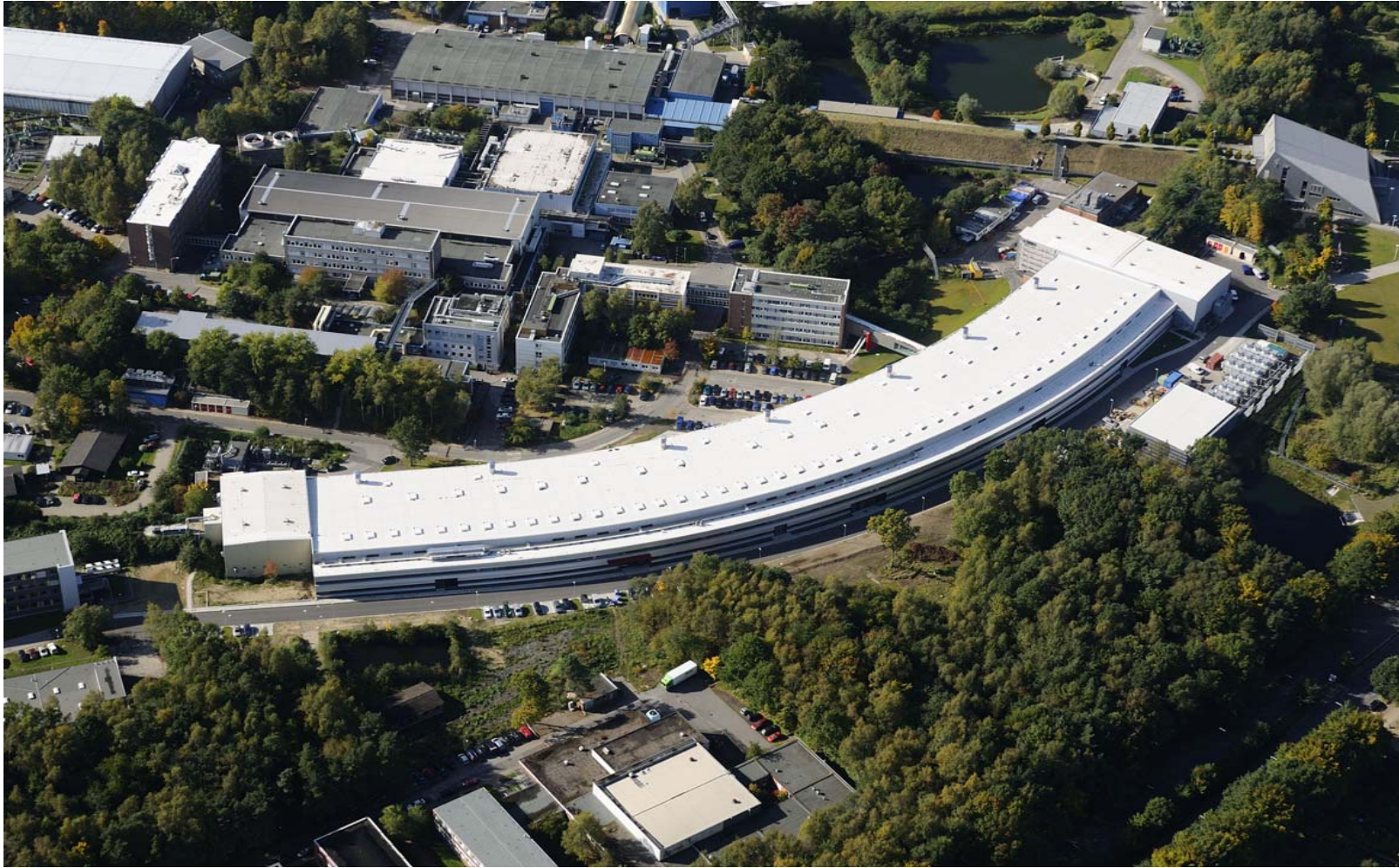
- BMBF-Verbundforschung
- FZ Jülich
- University Hamburg
- University Kiel
- University Aachen
- Debye Inst. Utrecht
- RISØ
- MPI Golm



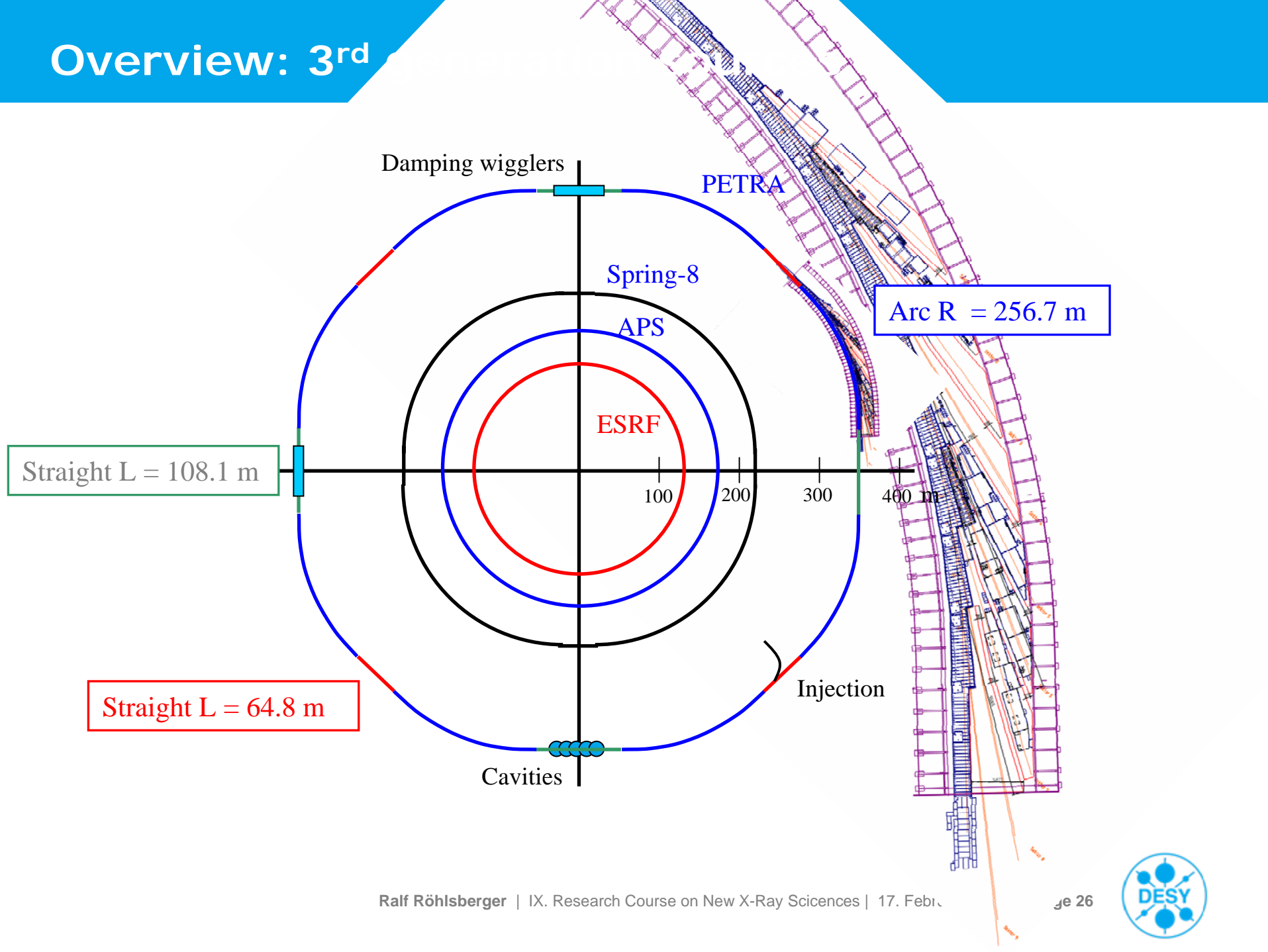


# PETRA III

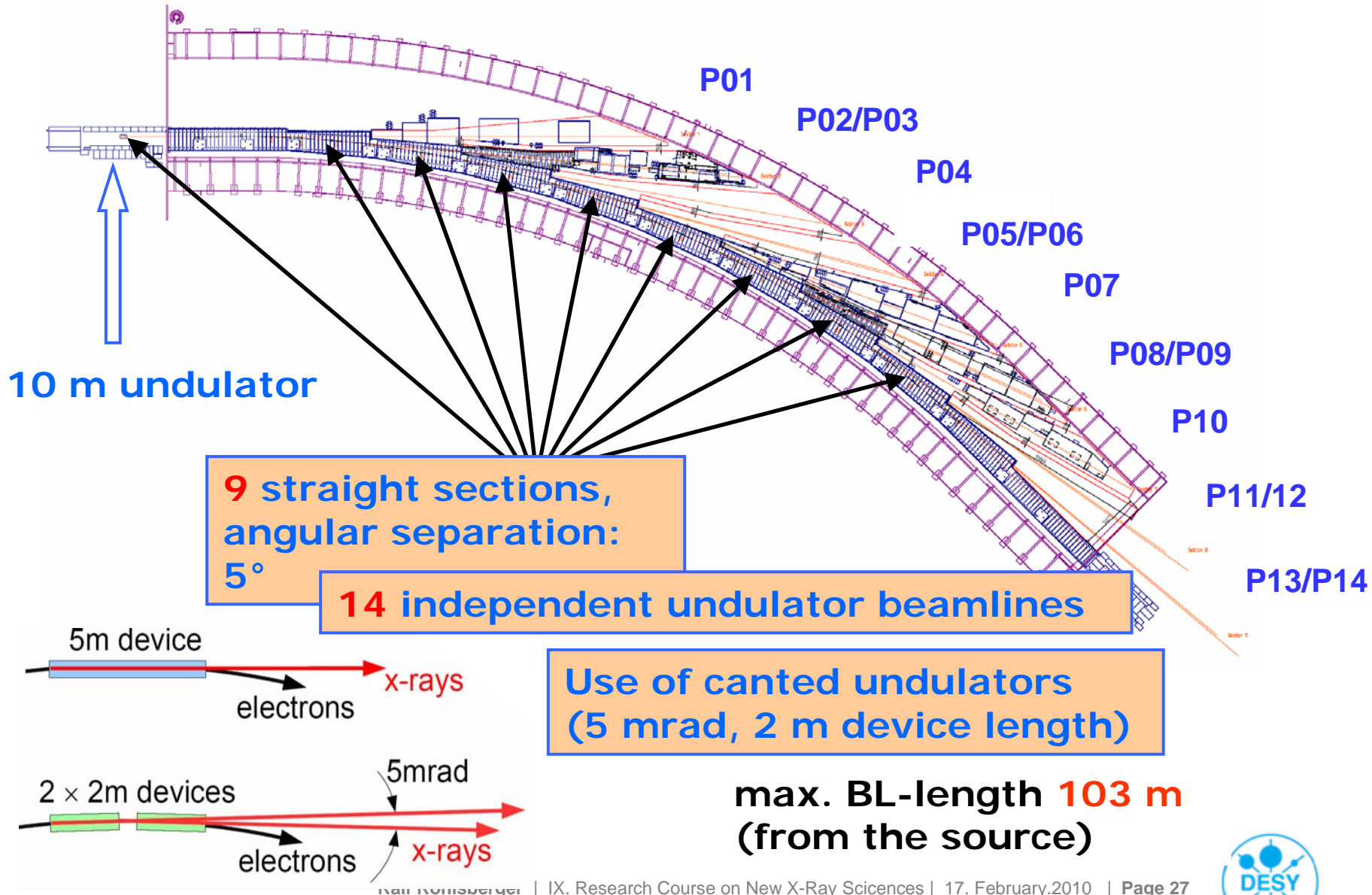
<http://petra3.desy.de>



# Overview: 3<sup>rd</sup>



# PETRA III: The experimental hall



# List of Beamlines at PETRA III

Number	Name	ID type	Energy range	Contact
P01	Dynamics beamline, IXS, NRS	10 m U32	5 - 40 keV	H.C. Wille, DESY
P02	Powder and extreme conditions	2 m U23	20 - 100 keV	H. P. Liermann, DESY
P03	Micro and Nano SAXS/WAXS	2 m U29	8 - 25 keV	S. Roth, DESY
P04	Variable Polarization XUV	5 m UE65 (APPLE)	0.2 - 3.0 keV	J. Viefhaus, DESY
P05	Micro- and nano-tomography	2 m U29	8 - 50 keV	A. Haibel, GKSS
P06	Hard X-ray nano probe, imaging	2 m U32	2.4 - 100 keV	G. Falkenberg, DESY
P07	High energy materials science	4 m U19 (IV)	50 - 300 keV	N. Schell, GKSS
P08	High resolution diffraction	2 m U29	5.4 - 30 keV	O. Seeck, DESY
P09	Resonant scattering/diffraction	2 m U32	2.4 - 50 keV	J. Stempfer, DESY
P10	Coherence applications	5 m U29	4 - 25 keV	M. Sprung, DESY
P11	Bio imaging/diffraction	2 m U32	8 - 35 keV	A. Meents, MPG, HZI, DESY
P12	BioSAXS	2 m U29	4 - 20 keV	M. Rößle, EMBL
P13	Macro molecular crystallography I	2 m U29	5 - 35 keV	M. Cianci, EMBL
P14	Macro molecular crystallography II	2 m U29	5 - 35 keV	G. Bourenkov, EMBL

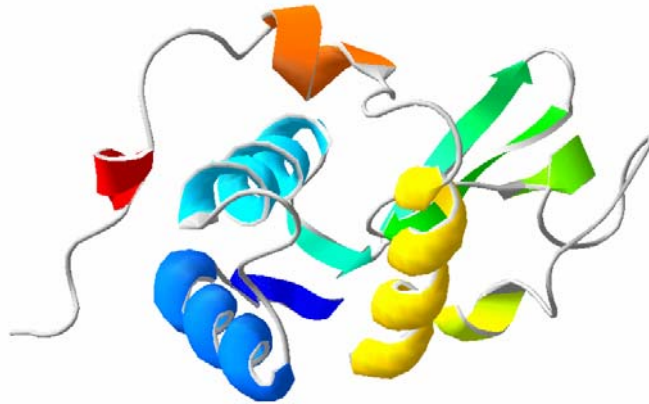
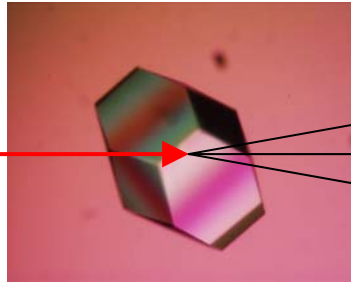
source size	
high beta section	142 x 5 $\mu\text{m}$
low beta section	35 x 6 $\mu\text{m}$



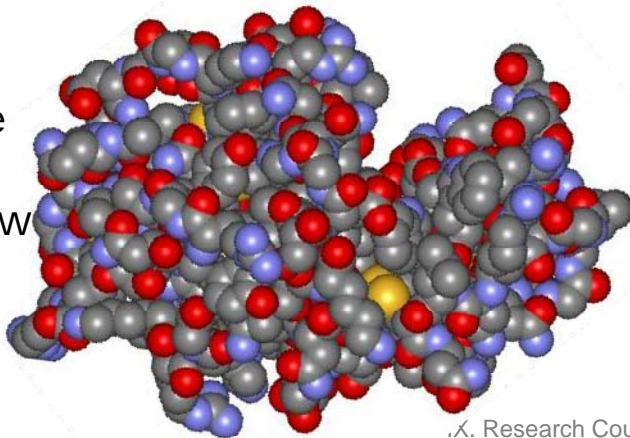
# Protein crystallography

X-rays

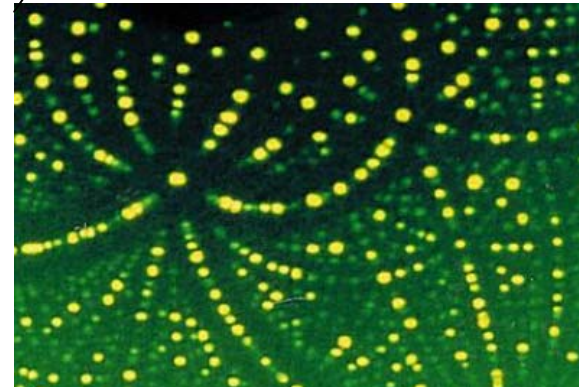
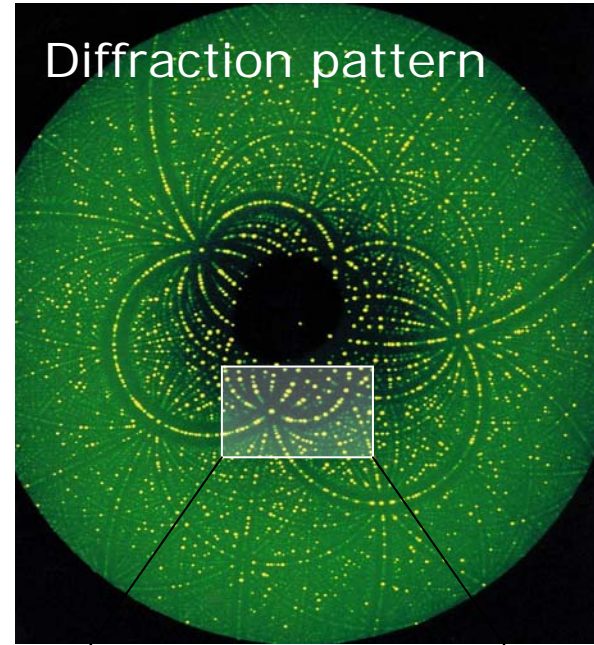
Protein crystal  
(Lysozyme)



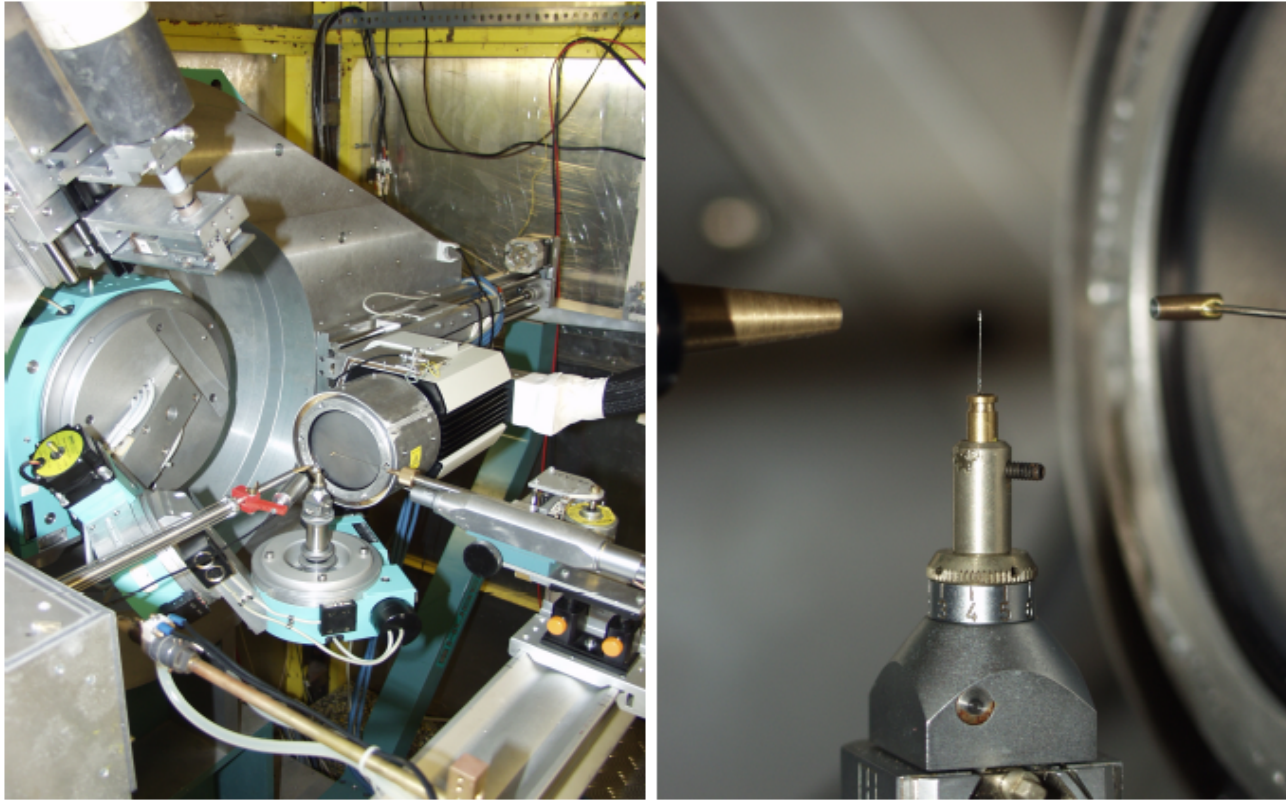
Carbon: Grey  
Nitrogen: Blue  
Oxygen: Red  
Sulphur: Yellow



Diffraction pattern



# Experimental setup

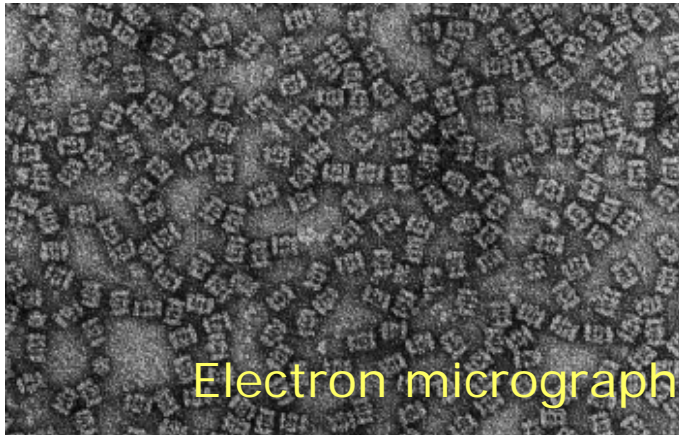


Single crystal diffractometer in  $\kappa$ -geometry with CCD and scintillation counter. Crystal mounted on a glass fiber. The  $\kappa$ -diffractometer has 3 rotations for the crystal and one for the detector.

# Protein Structure: Examples

## The proteasome

(cuts proteins into peptides and amino acids)

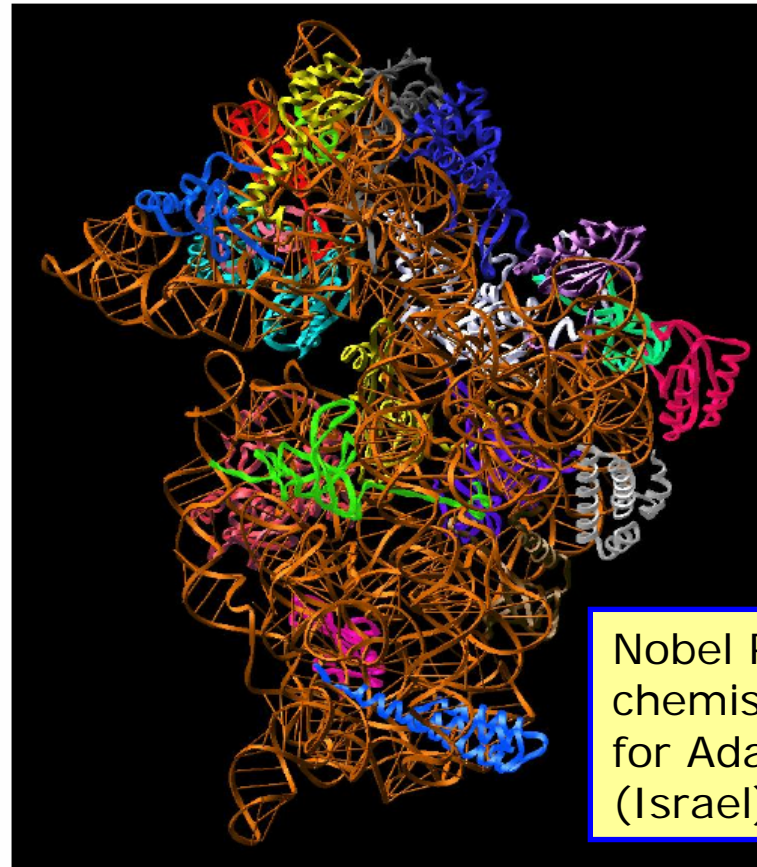


Electron micrograph

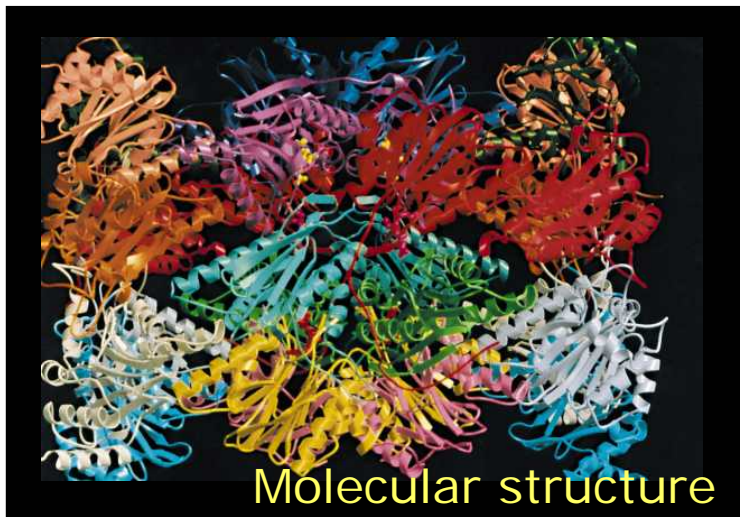
## The ribosome

(synthesis of proteins)

## The 30S subunit of the ecoli ribosome

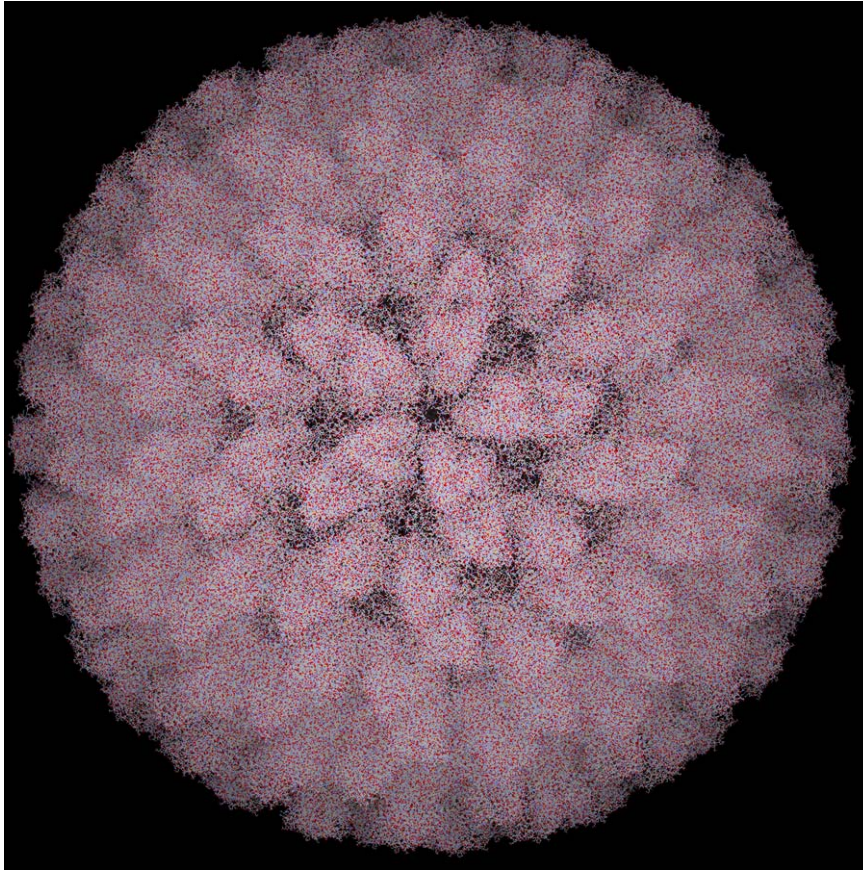


Nobel Prize in chemistry 2009 for Ada Yonath (Israel)

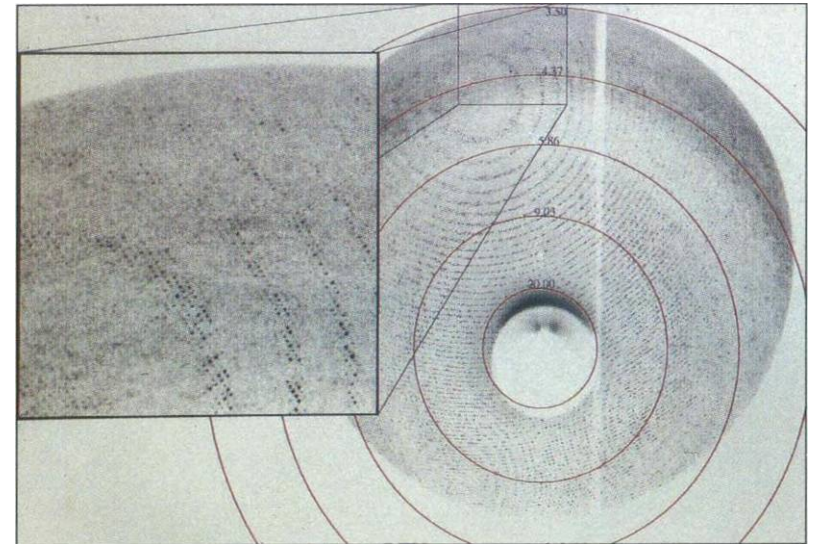


Molecular structure

# Extremely large complexes (e.g., viruses)



Example: Blue Tongue Virus



J.M. Grimes et al., *Nature* 395, 470-478 (1998)



# X-ray reflection from surfaces

Index of refraction

$$n = 1 - \delta$$

$$\delta = \frac{\rho_e r_0 \lambda^2}{4\pi}, \quad \rho_e \equiv \text{electron density}$$

$$\approx 10^{-5} - 10^{-6} \quad \text{for } \lambda = 0.1 \text{ nm}$$

For x-rays, every medium is optically thinner than vacuum !

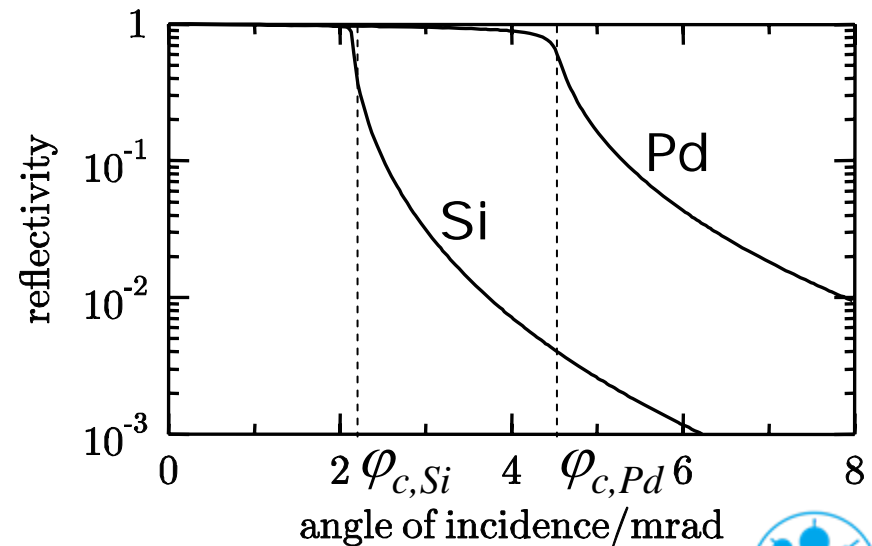
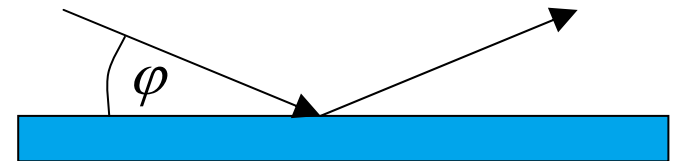
X-rays incident on a surface below the critical angle are totally reflected

Critical angle of total reflection

$$\varphi_c = \sqrt{2\delta}$$

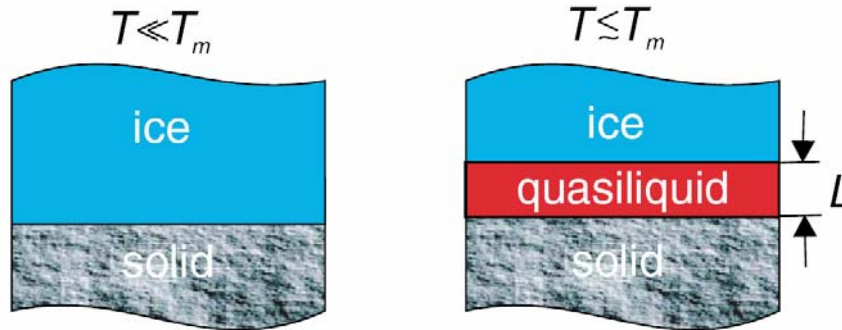
For angles  $\varphi < \varphi_c$  the penetration depth of hard x-rays is only a few nm.

X-rays can be used for the study of structures at surfaces

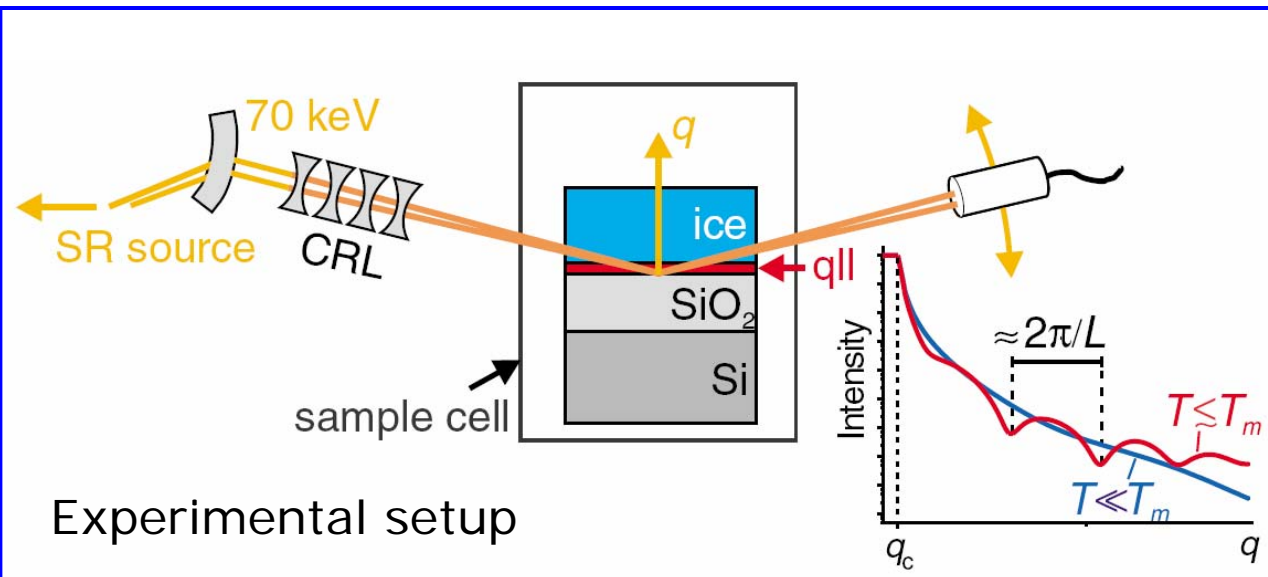


# Interfacial Melting of Ice in Contact with SiO<sub>2</sub>

## Hypothesis

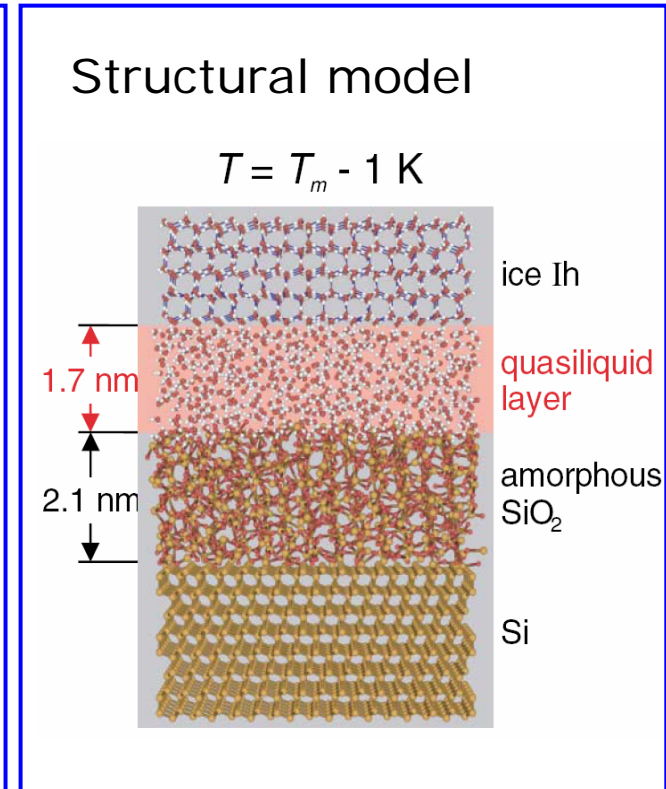
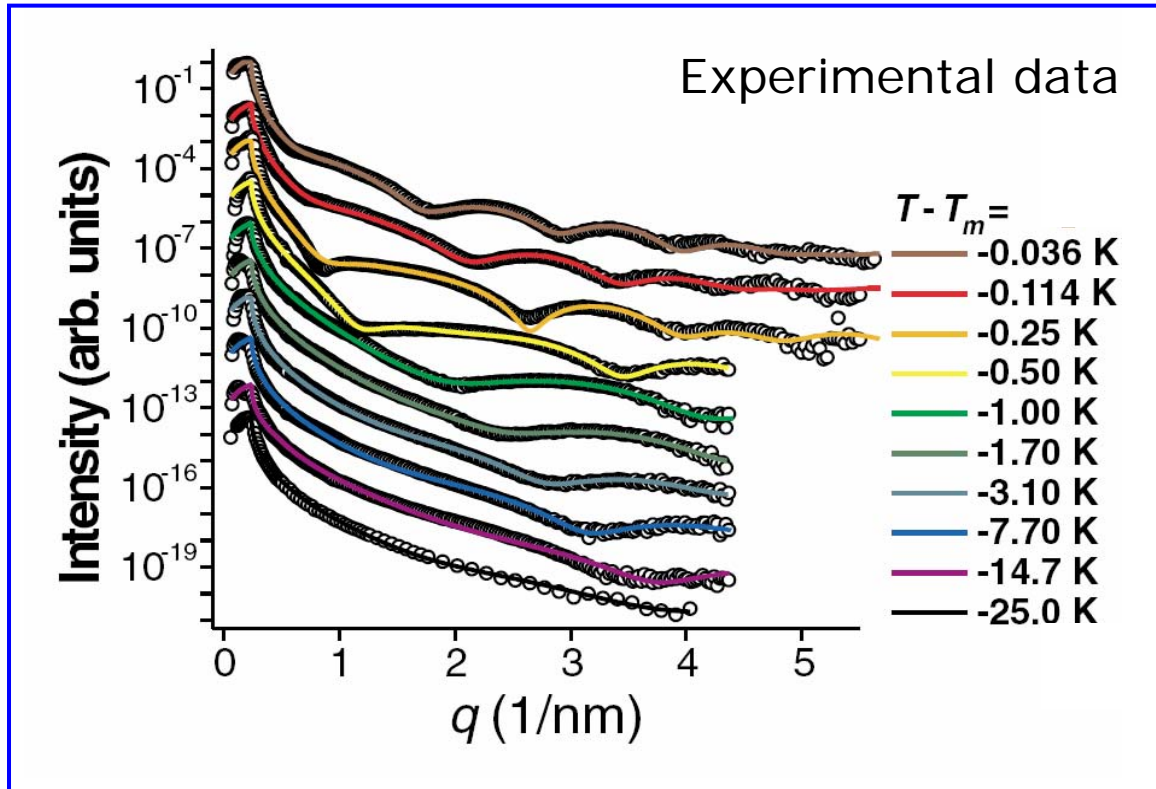


S. Engemann et al.,  
Phys. Rev. Lett. 92,  
205701 (2004)



## Experimental setup

# Interfacial Melting of Ice in Contact with SiO<sub>2</sub>



S. Engemann et al., Phys. Rev. Lett. 92, 205701 (2004)