

Higgs theory at NNLO

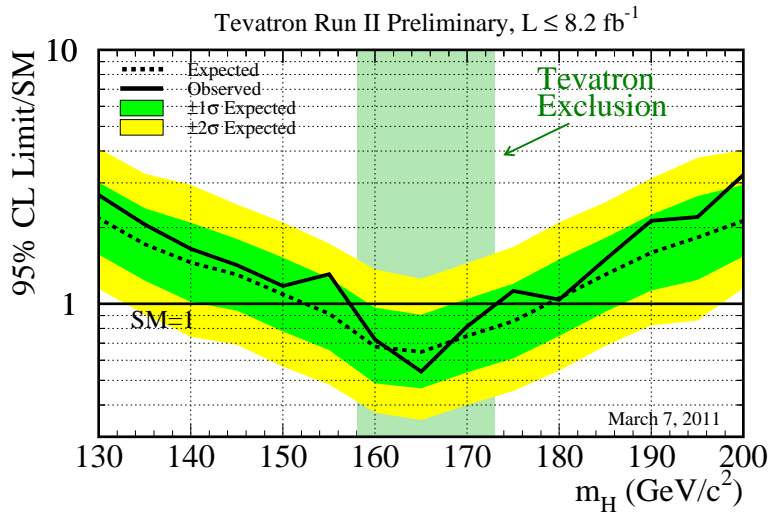
Robert Harlander

BU Wuppertal

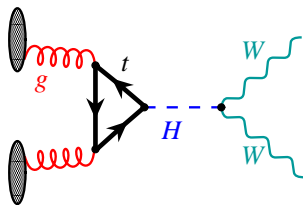
Standard Model Benchmarks at High-Energy Hadron Colliders
DESY Zeuthen, 17 June 2011

*Supported by: BMBF, DFG, Helmholtz Alliance "Physics at the Terascale",
LHCPhenoNet*

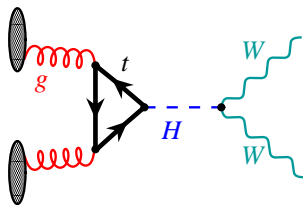
Higgs search at the Tevatron



Gluon Fusion

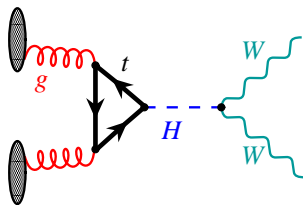


Gluon Fusion



- dominant production mode
- sensitive to heavy particle spectrum

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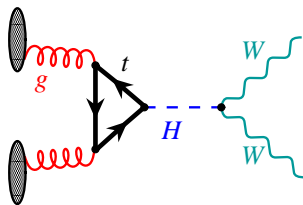


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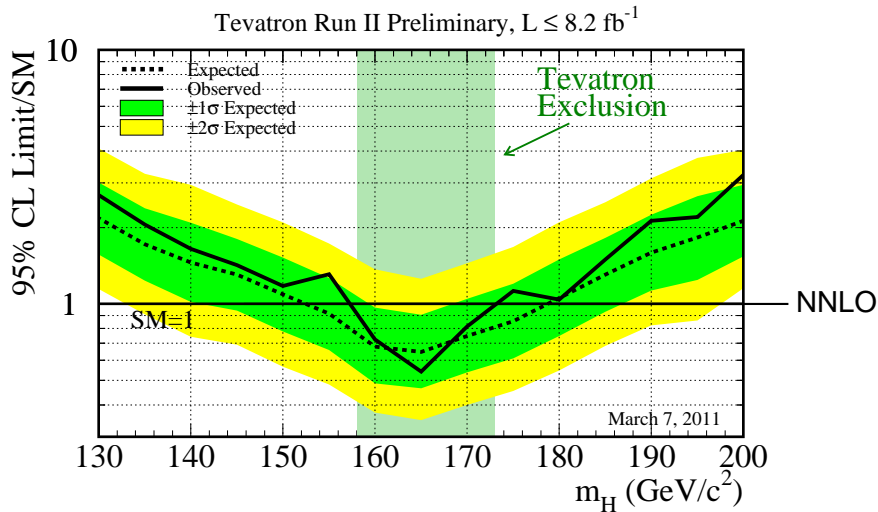


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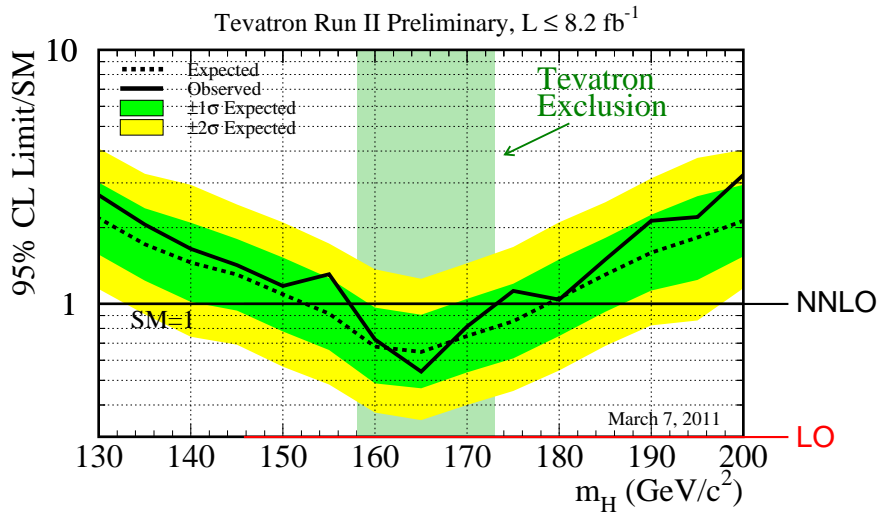
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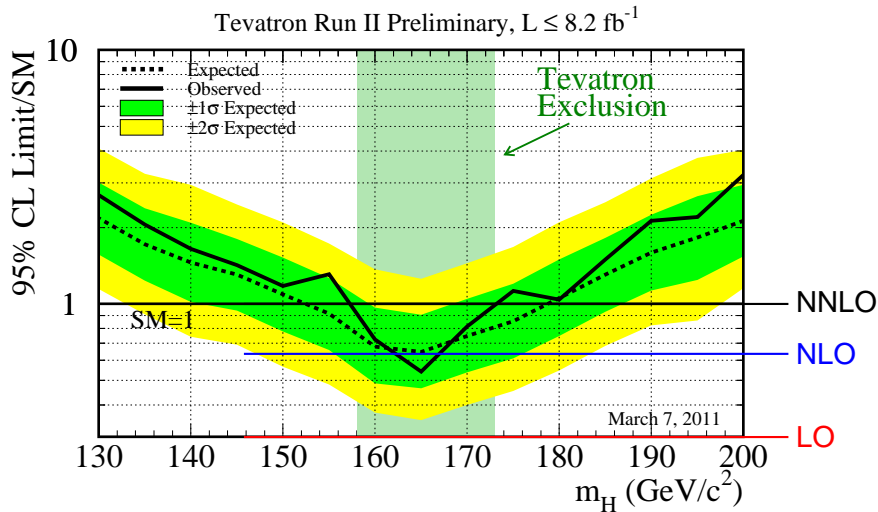
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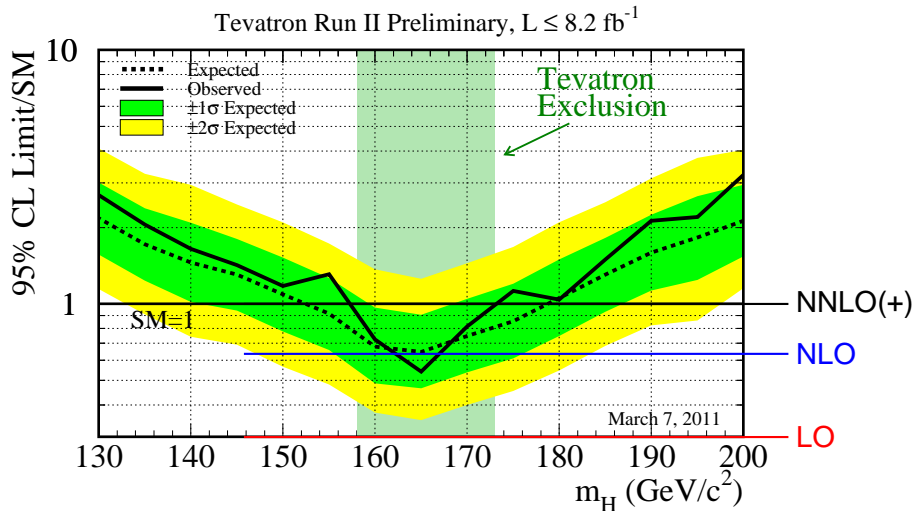
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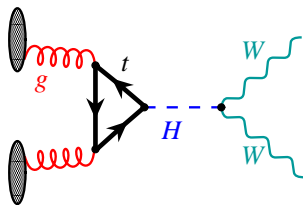
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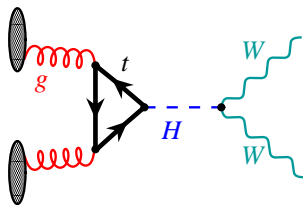


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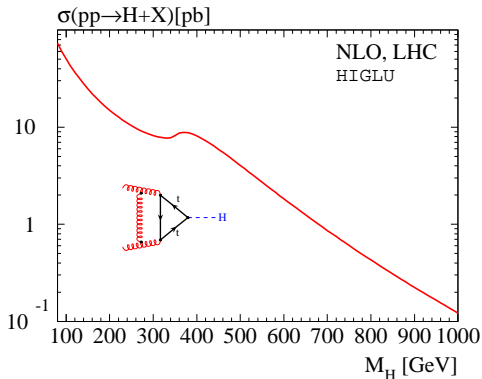
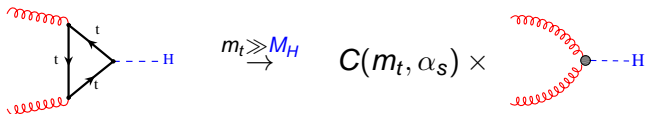
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Gluon fusion

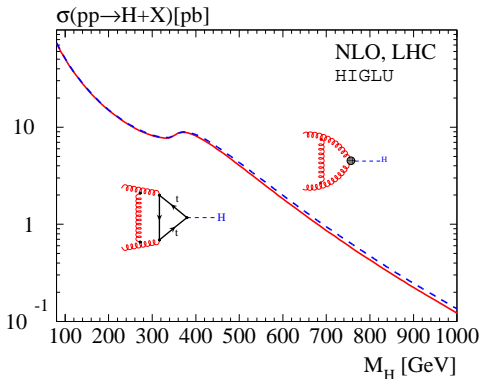
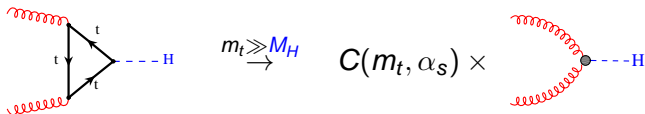
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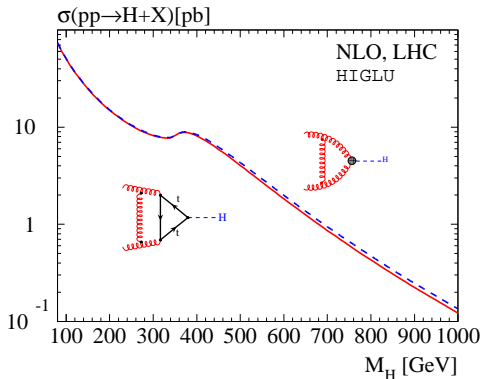
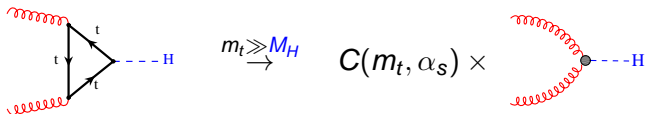
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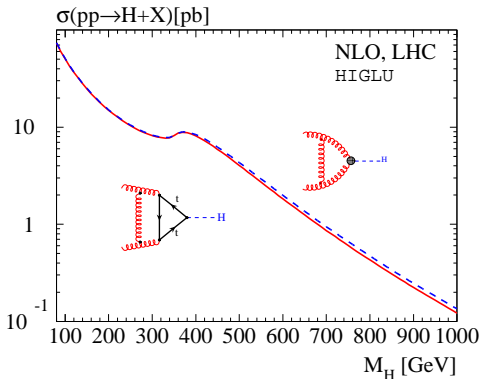
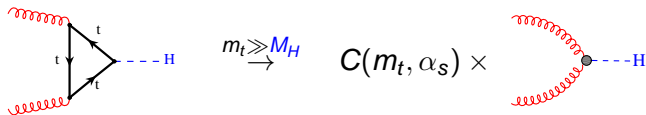
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NNLO?

Results in the heavy-top limit

- NNLO QCD inclusive

[RH, Kilgore '02], [Anastasiou, Melnikov '02], [Ravindran, Smith, van Neerven '03]

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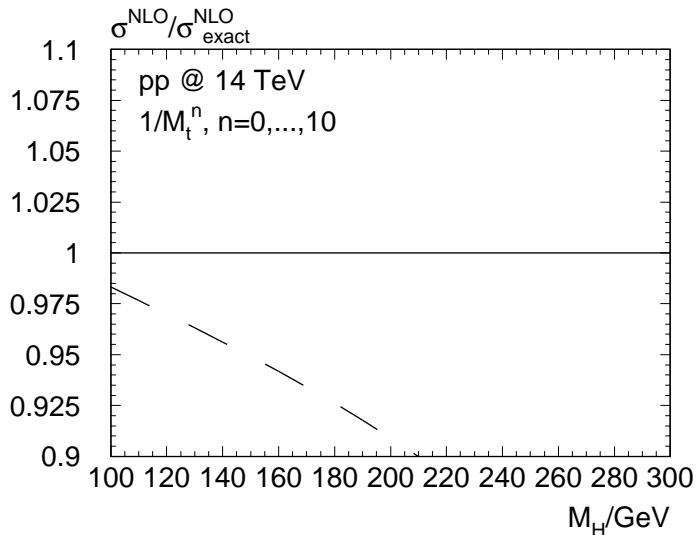
[Anastasiou, Melnikov, Petriello '05], [Catani, Grazzini '07]

Test: subleading terms in $1/m_t$

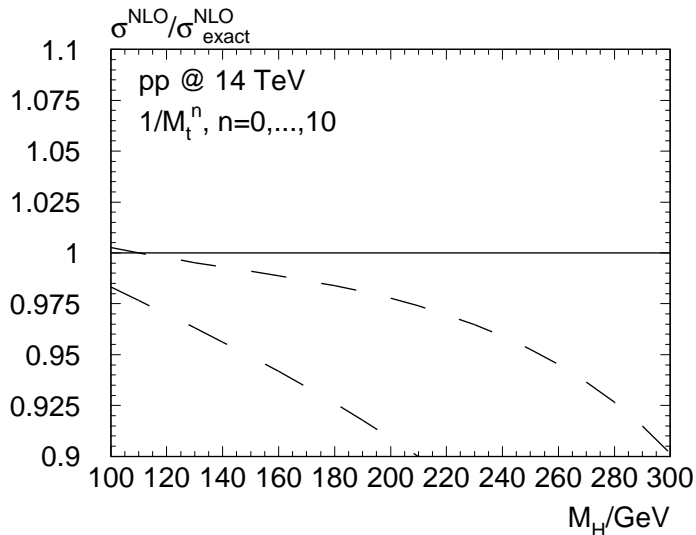
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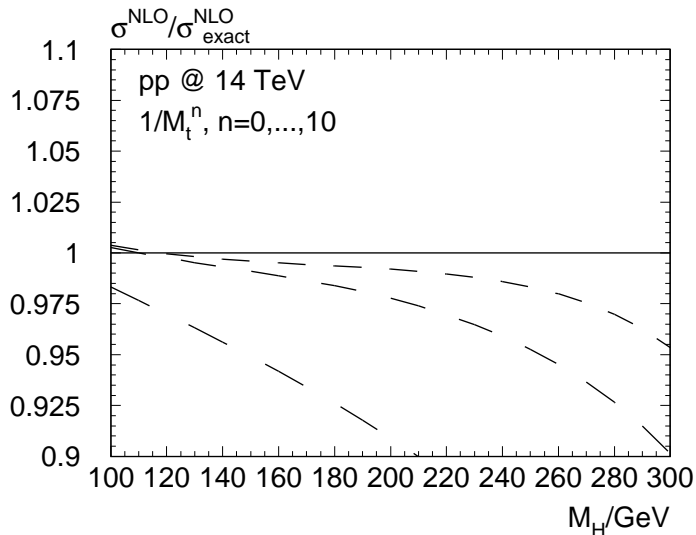
Convergence of $1/m_t$ expansion at NLO



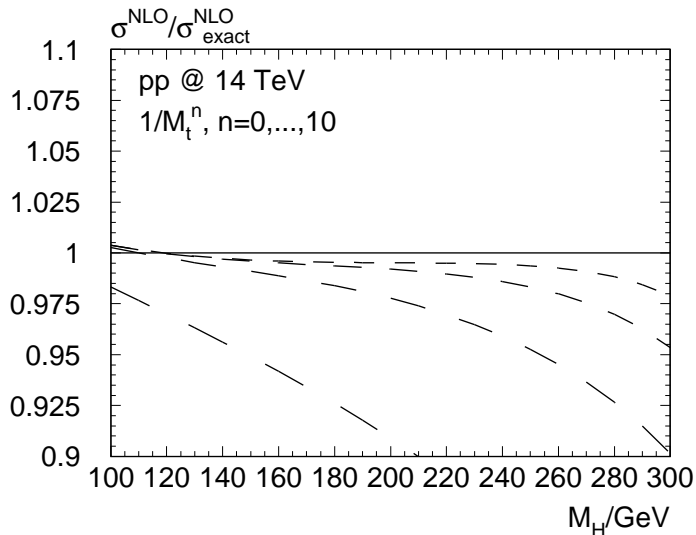
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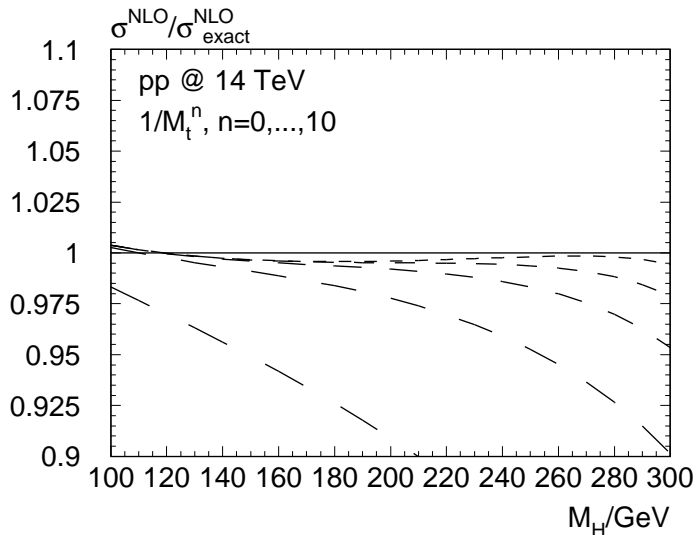
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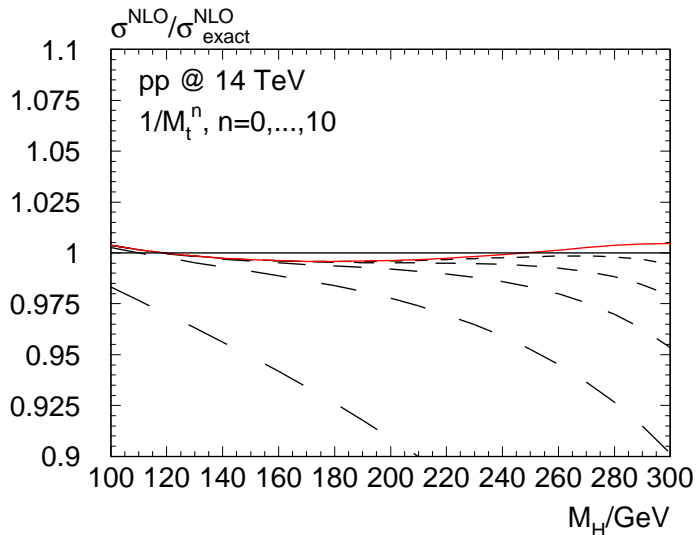
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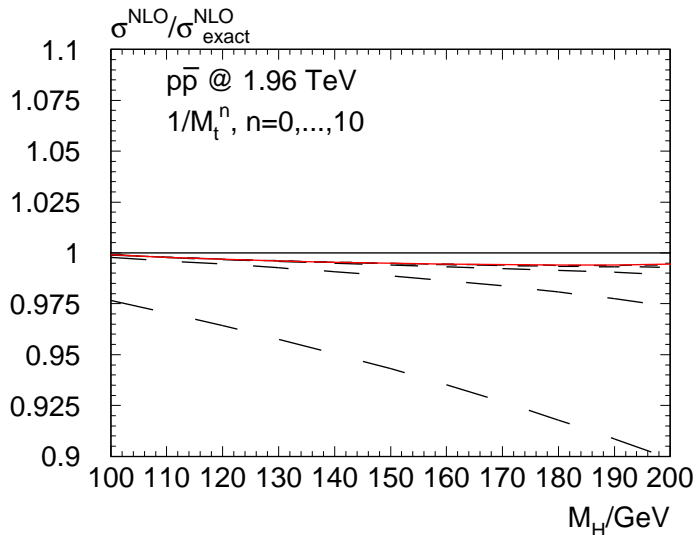
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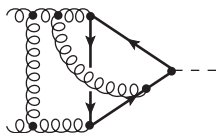
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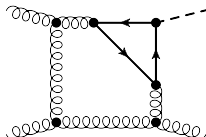
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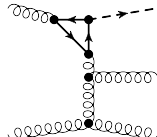
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623



327



114

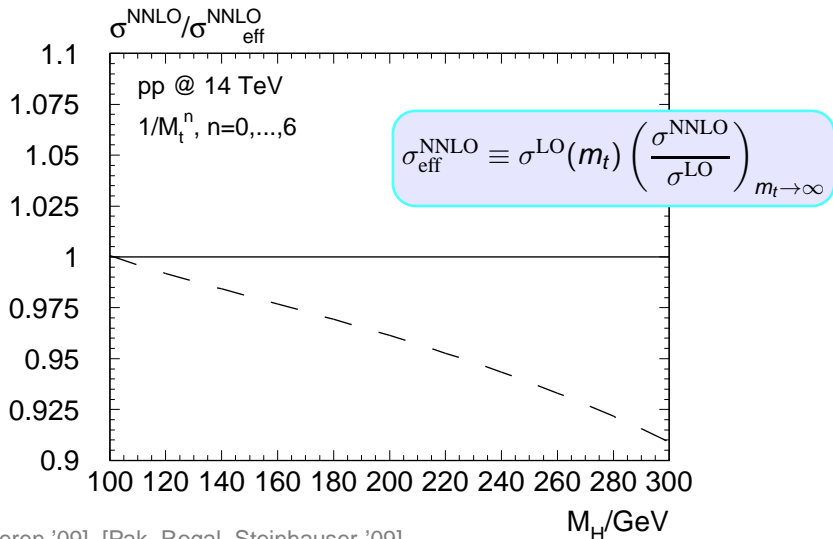
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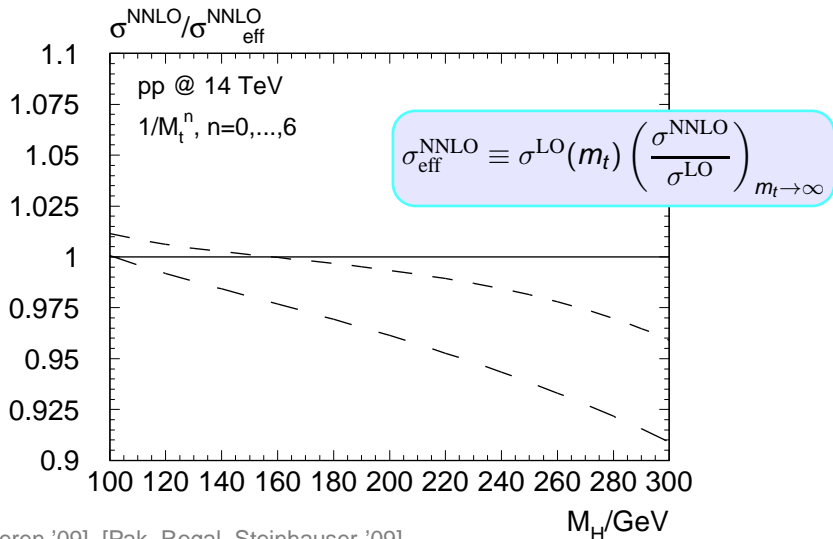
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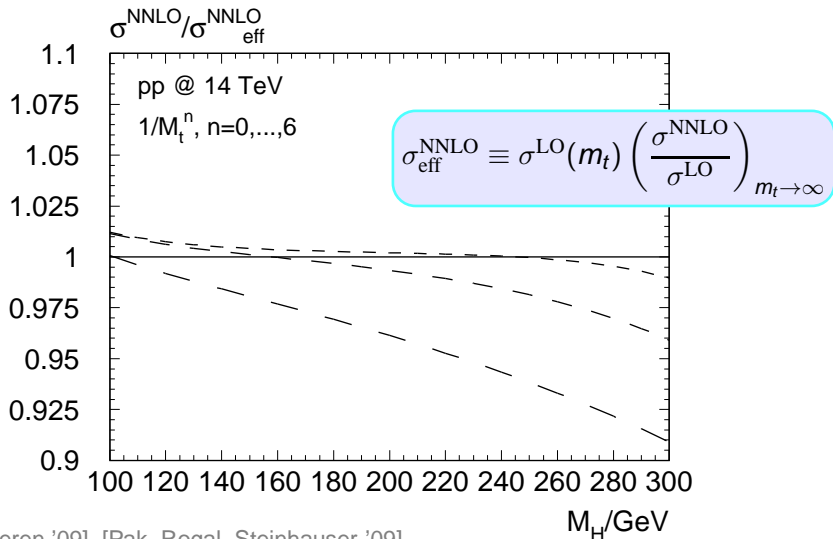
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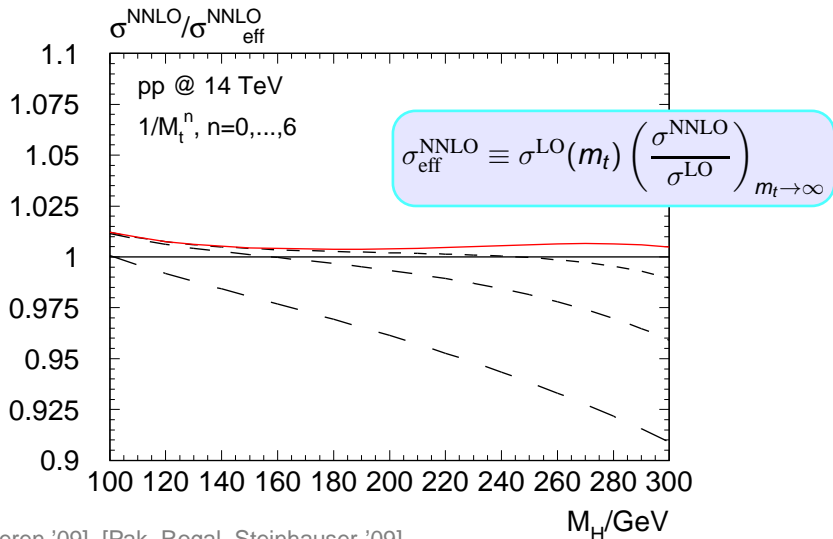
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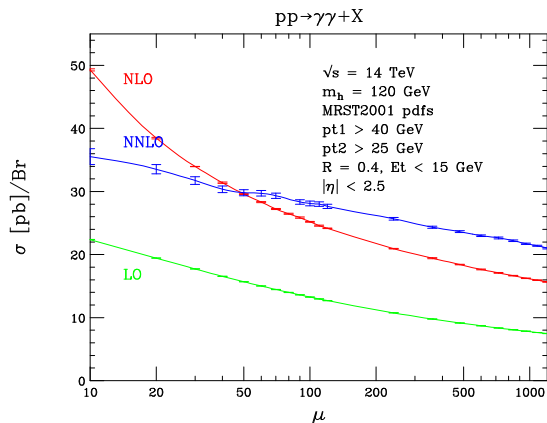
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[Catani, Grazzini '08]

Summary of numerical effects (Tevatron)¹

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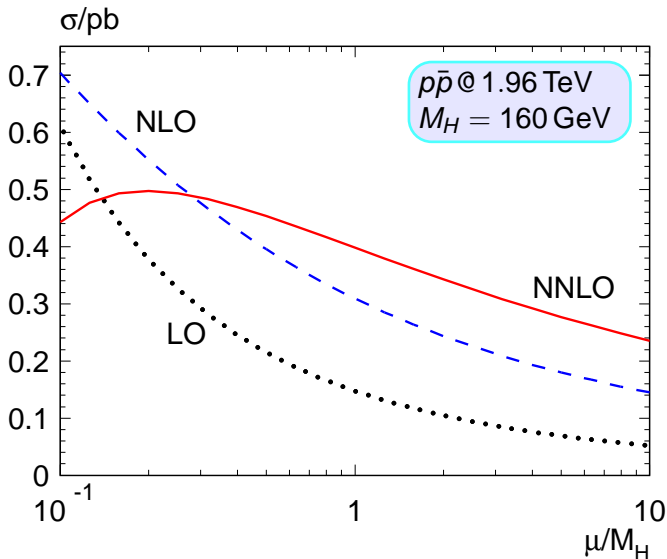
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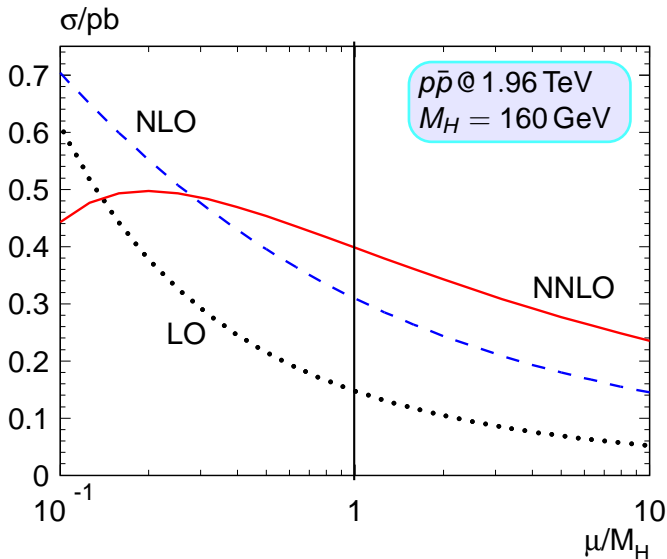
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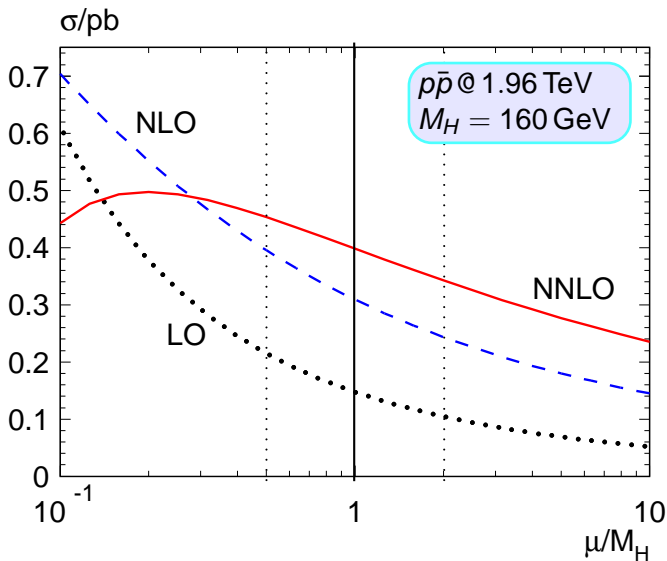
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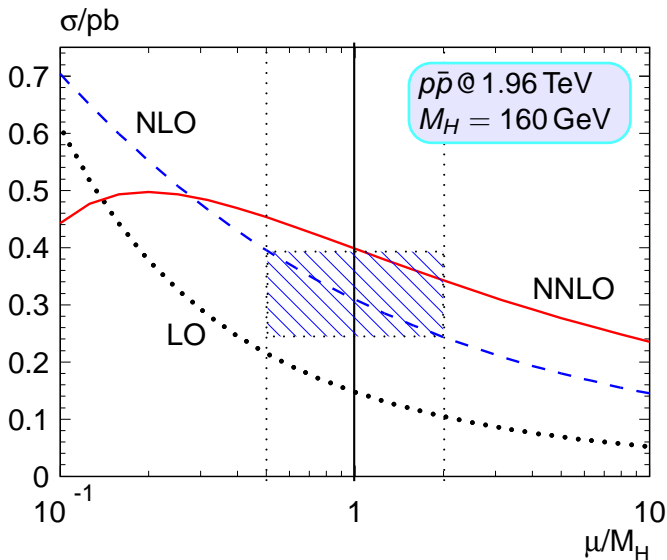
- estimate higher orders from scale variation
- range of μ variation is (at best) a convention —
often: $M/2 < \mu < 2M$

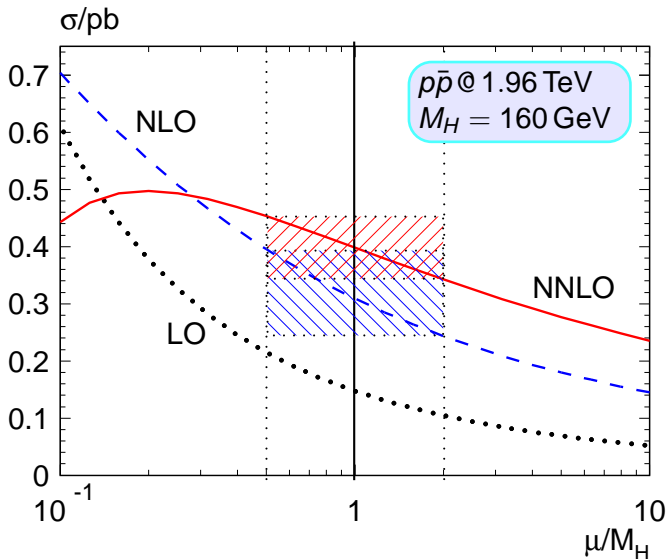


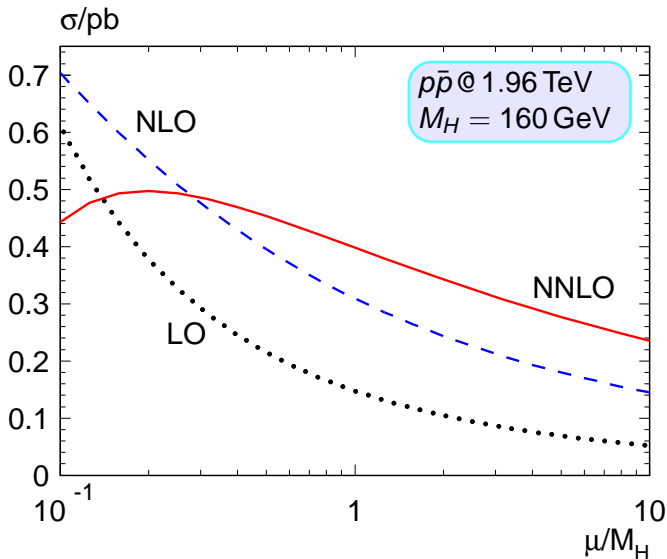


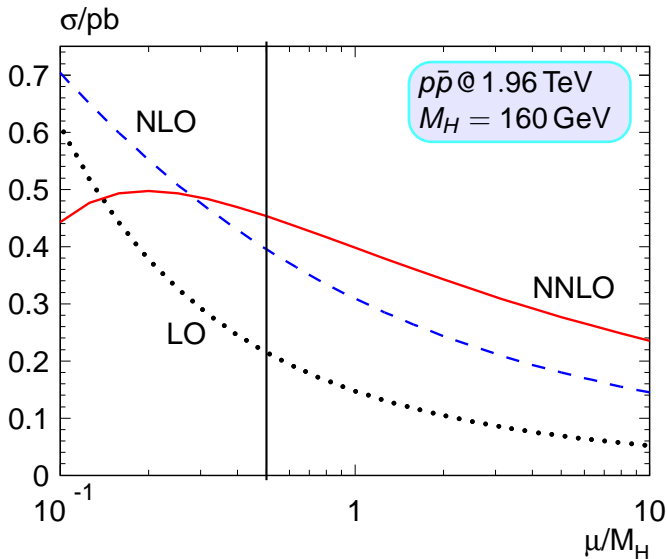


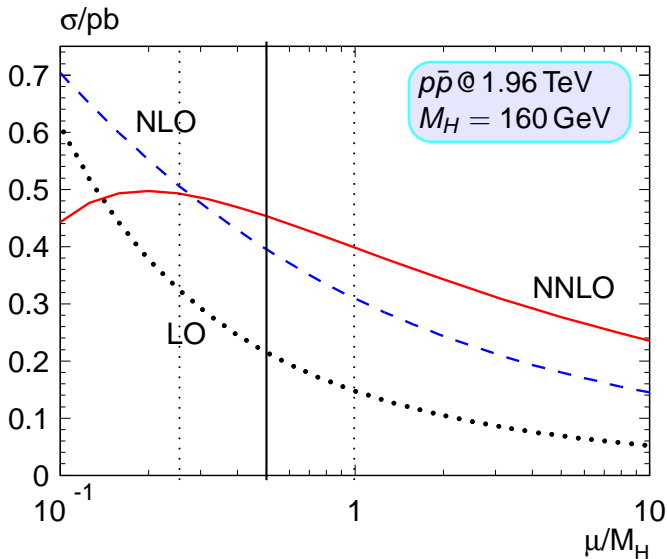
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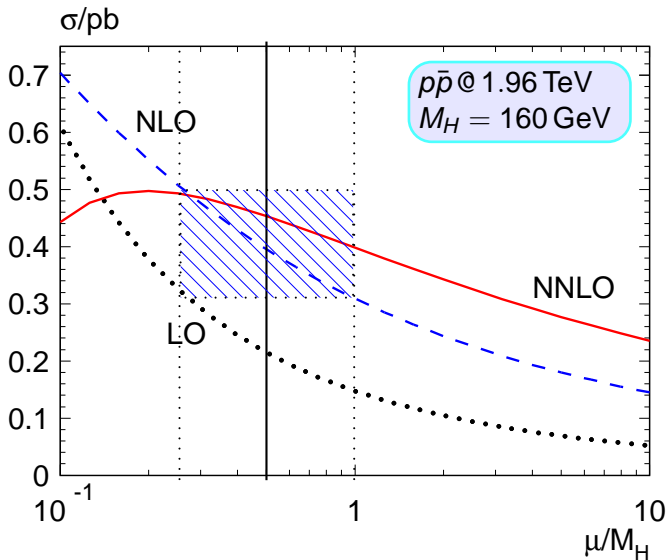


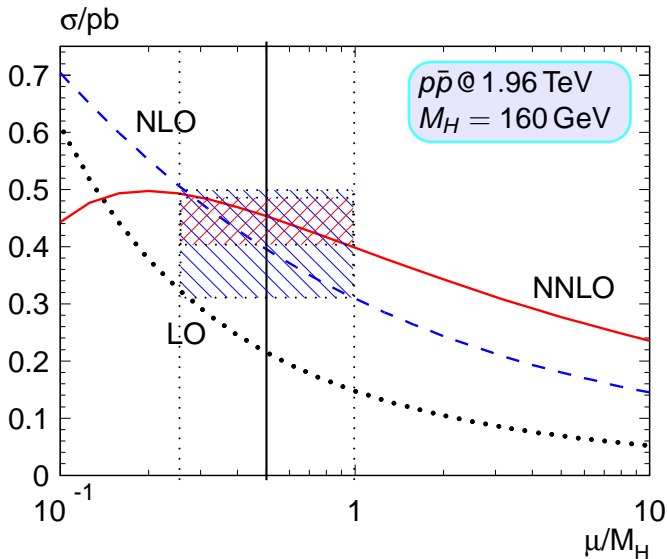




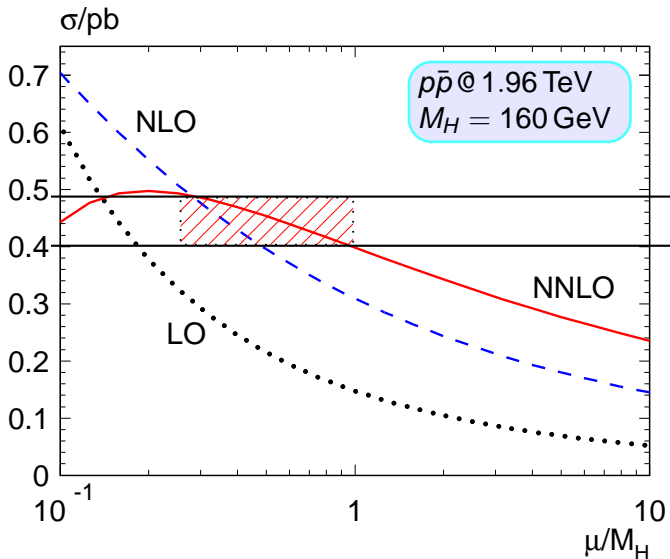


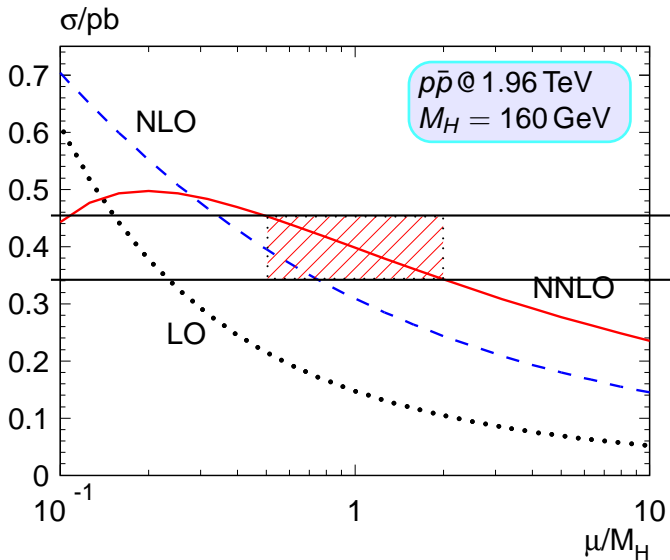






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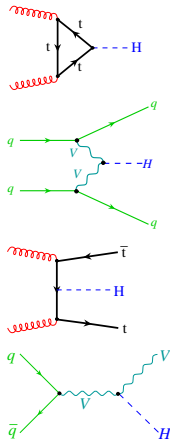
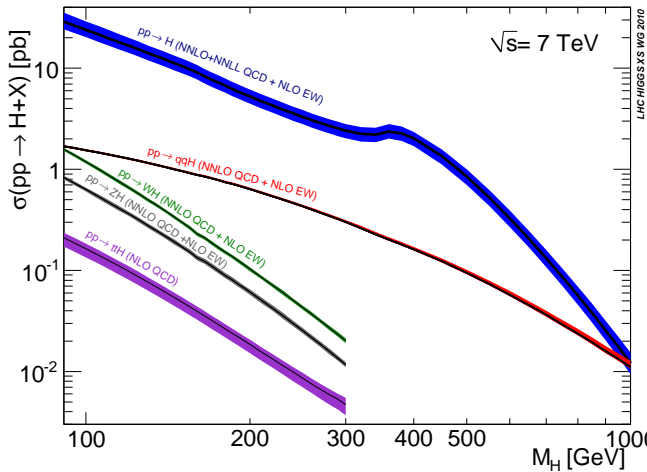
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- how does Tevatron exclusion depend on $\Delta_{\text{th}}\sigma$?

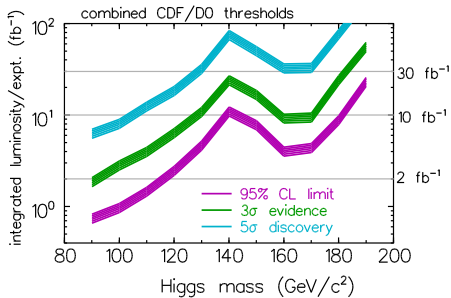
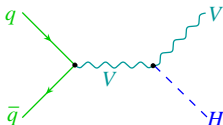
Theory uncertainties

- μ dependence (renormalization/factorization scales)
- PDF uncertainties
 - parametrization
 - data
 - heavy quark effects
 - α_s
 - ...
- $m_b(m_b)$ vs. $m_b(M_H)$ vs. M_b^{pole}
- ...
- combining errors: quadratically?
- how does Tevatron exclusion depend on $\Delta_{\text{th}}\sigma$?
- my opinion:
 - provide exclusion for a “central” theory prediction
 - decouple “theory error” from experimental error
 - equivalently: don’t normalize to SM

Higgs cross sections



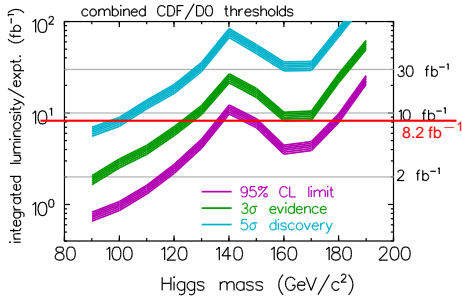
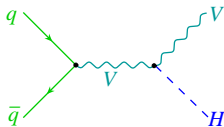
Higgs Strahlung



[Tev Higgs WG '00]

- used to be
- main search mode for Tevatron

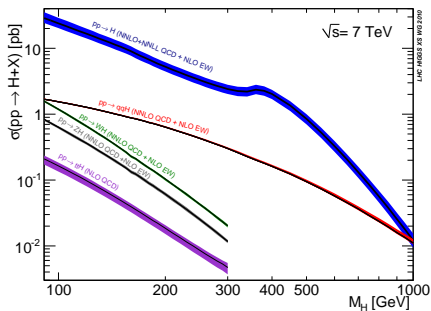
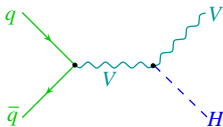
Higgs Strahlung



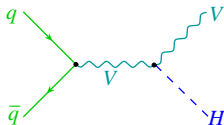
[Tev Higgs WG '00]

- used to be
- main search mode for Tevatron

Higgs Strahlung



- used to be
 - main search mode for Tevatron
 - considered useless for Higgs search at LHC

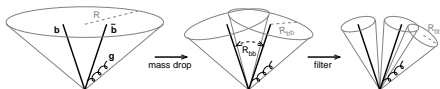


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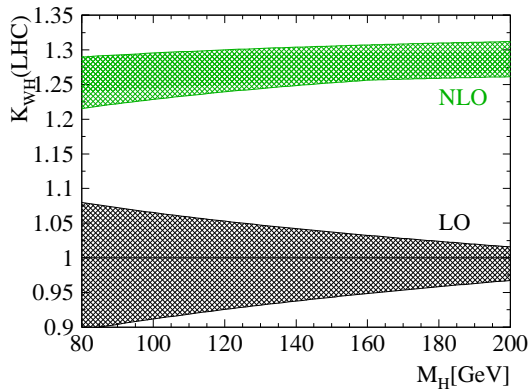
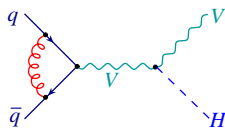
- use jet sub-structure:

[Butterworth *et al.* 08]

promising for $M_H \approx 120$ GeV

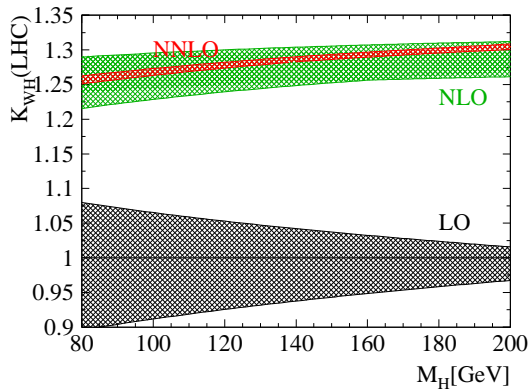
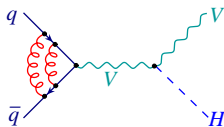


Higgs Strahlung



[Han, Willenbrock '90]

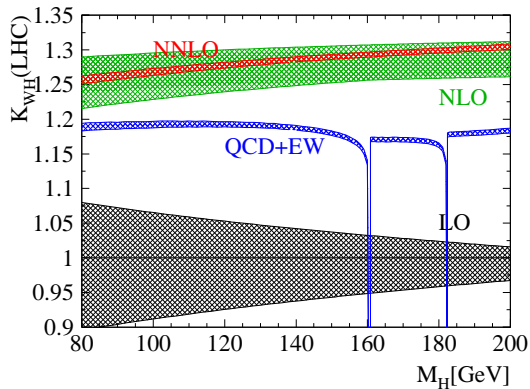
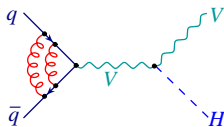
Higgs Strahlung



[Brein, Djouadi, R.H. '03]

[Han, Willenbrock '90]

Higgs Strahlung

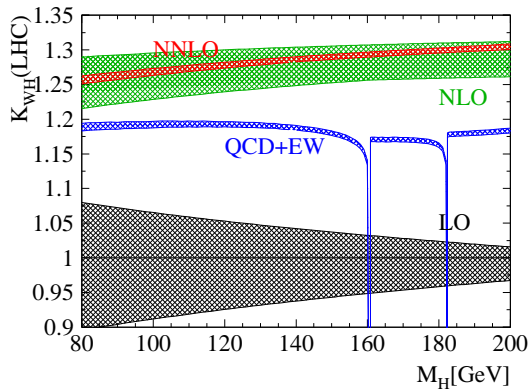
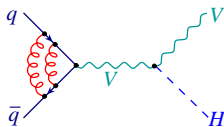


[Brein, Djouadi, R.H. '03]

[Han, Willenbrock '90]

[Ciccolini, Dittmaier, Krämer '03]

Higgs Strahlung



[Brein, Djouadi, R.H. '03]

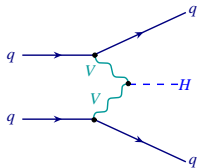
[Han, Willenbrock '90]

[Ciccolini, Dittmaier, Krämer '03]

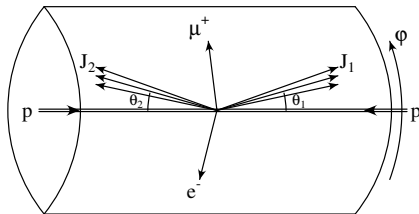
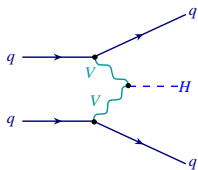
update:

[Brein, R.H., Wieseemann, Zirke '11]

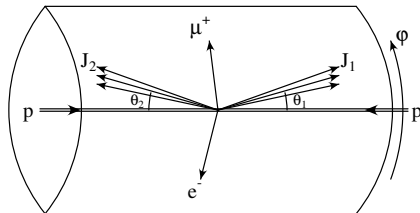
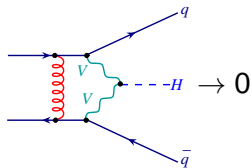
Weak Boson Fusion



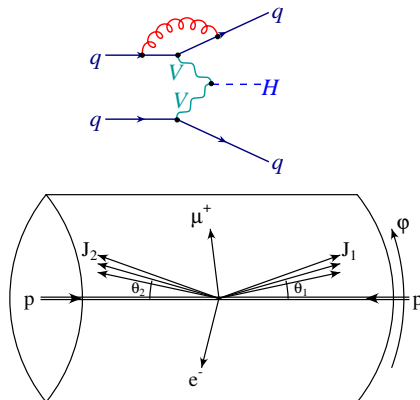
Weak Boson Fusion



Weak Boson Fusion



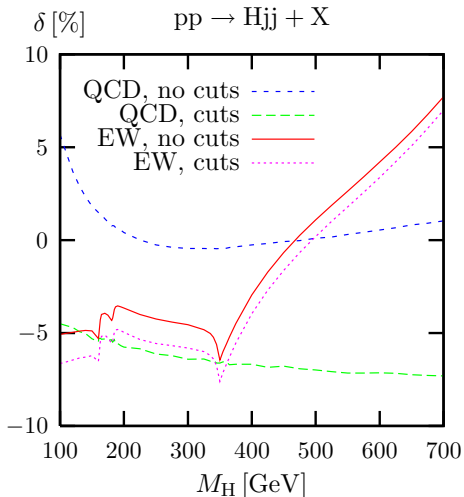
Weak Boson Fusion



NLO QCD: [Figy, Oleari, Zeppenfeld '03]

+ EW: [Ciccolini, Denner, Dittmaier '08]

WBF: QCD+EW corrections



[Ciccolini, Denner, Dittmaier '08]

- gluon fusion/WBF interference

[Andersen, Binoth, Heinrich, Smillie '07], [Andersen, Smillie '08]

[Bredenstein, Hagiwara, Jäger '08]

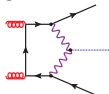
WBF: other corrections

- gluon fusion/WBF interference

[Andersen, Binoth, Heinrich, Smillie '07], [Andersen, Smillie '08]

[Bredenstein, Hagiwara, Jäger '08]

- gluon induced WBF [R.H., Vollinga, Weber '08]



part of NNLO

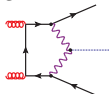
WBF: other corrections

- gluon fusion/WBF interference

[Andersen, Binoth, Heinrich, Smillie '07], [Andersen, Smillie '08]

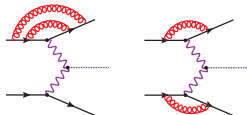
[Bredenstein, Hagiwara, Jäger '08]

- gluon induced WBF [R.H., Vollinga, Weber '08]



part of NNLO

- DIS-like NNLO (inclusive) [Bolzoni, Maltoni, Moch, Zaro '10]



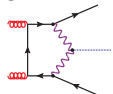
WBF: other corrections

- gluon fusion/WBF interference

[Andersen, Binoth, Heinrich, Smillie '07], [Andersen, Smillie '08]

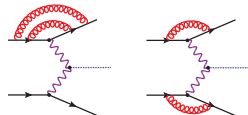
[Bredenstein, Hagiwara, Jäger '08]

- gluon induced WBF [R.H., Vollinga, Weber '08]

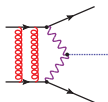


part of NNLO

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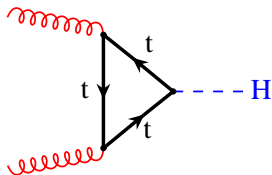


- missing:



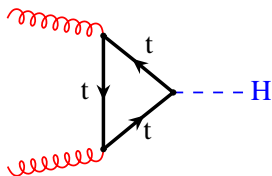
BSM Higgs

Gluon Fusion: 4th generation



- sensitive to heavy particle spectrum

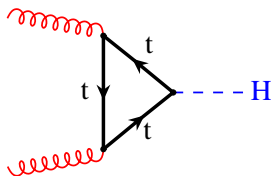
Gluon Fusion: 4th generation



- sensitive to heavy particle spectrum

$$\sigma \xrightarrow{m_t \gg M_H} \frac{\pi}{256\sqrt{2}} \left(\frac{\alpha_s}{\pi}\right)^2 \left(\frac{y_t}{m_t}\right)^2$$

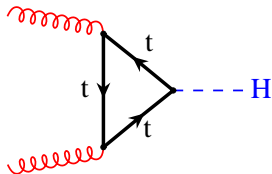
Gluon Fusion: 4th generation



- sensitive to heavy particle spectrum

$$\sigma \xrightarrow{m_t \gg M_H} \frac{\pi}{256\sqrt{2}} \left(\frac{\alpha_S}{\pi}\right)^2 \left(\frac{y_t}{m_t} + \frac{y_{t'}}{m_{t'}} + \frac{y_{b'}}{m_{b'}}\right)^2$$

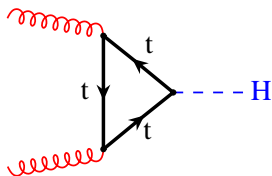
Gluon Fusion: 4th generation



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Gluon Fusion: 4th generation

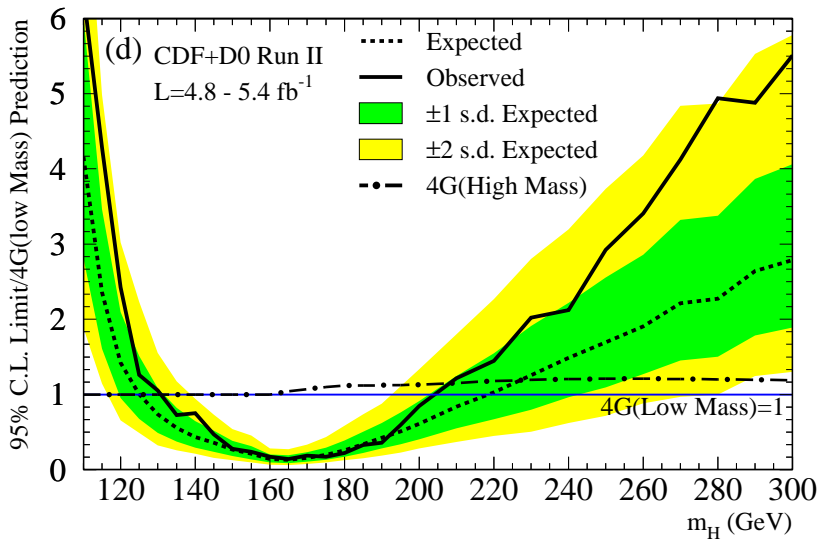


- sensitive to heavy particle spectrum

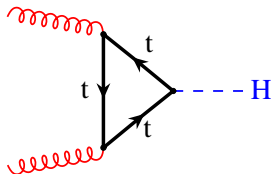
$$\sigma \xrightarrow{m_t \gg M_H} \frac{\pi}{256\sqrt{2}} \left(\frac{\alpha_S}{\pi}\right)^2 \left(\frac{m_t}{m_t} + \frac{m_{t'}}{m_{t'}} + \frac{m_{b'}}{m_{b'}}\right)^2 = 9 \frac{\pi}{256\sqrt{2}} \left(\frac{\alpha_S}{\pi}\right)^2$$

NNLO: [Anastasiou, Buehler, Furlan, Herzog, Lazopoulos '11]

Higgs with 4th generation

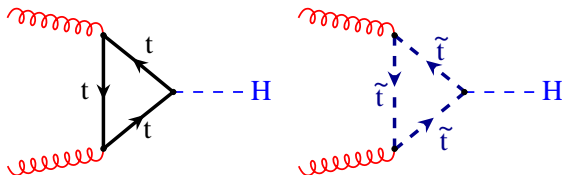


Gluon Fusion



- sensitive to heavy particle spectrum

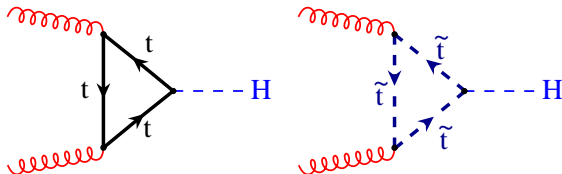
$$\sigma \xrightarrow{m_t \gg M_H} \frac{\pi}{256\sqrt{2}} \left(\frac{\alpha_s}{\pi}\right)^2 \left(\frac{y_t}{m_t}\right)^2$$



- sensitive to heavy particle spectrum

$$\sigma \xrightarrow{m_t \gg M_H} \frac{\pi}{256\sqrt{2}} \left(\frac{\alpha_s}{\pi}\right)^2 \left(\frac{y_t}{m_t} + \frac{\tilde{y}_t^2}{\tilde{M}_t^2}\right)^2 \left(\frac{\cos \alpha}{\sin \beta}\right)^2$$

Gluon Fusion

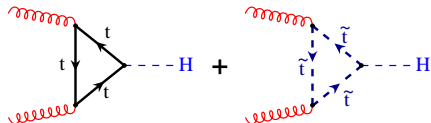


- sensitive to heavy particle spectrum

$$\sigma \xrightarrow{m_t \gg M_H} \frac{\pi}{256\sqrt{2}} \left(\frac{\alpha_s}{\pi}\right)^2 \left(\frac{m_t}{m_t} + \frac{m_t^2}{2\tilde{M}_t^2}\right)^2 \left(\frac{\cos\alpha}{\sin\beta}\right)^2$$

Effects of SUSY

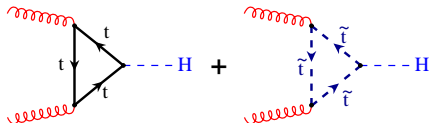
[Djouadi 98], [Carena *et al.* 99]



may interfere destructively!

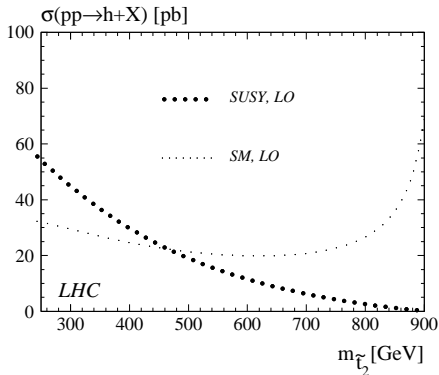
Effects of SUSY

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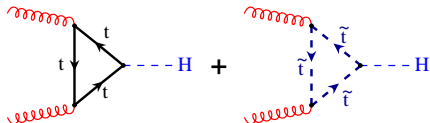
$$\begin{aligned}
 m_{\tilde{t}_1} &= 200 \text{ GeV} \\
 m_{\tilde{g}} &= 1 \text{ TeV} \\
 \tan \beta &= 10, \\
 \alpha &= 0, \\
 \theta_t &= \frac{\pi}{4}
 \end{aligned}$$



- [R.H., Steinhauser '04]
- [Anastasiou *et al.* '06/'08]
- [Mühlleitner, Rzehak, Spira '07/'08]
- [Aglietti, Bonciani, Degrassi, Vicini '06]
- [Degrassi, Slavich '08]

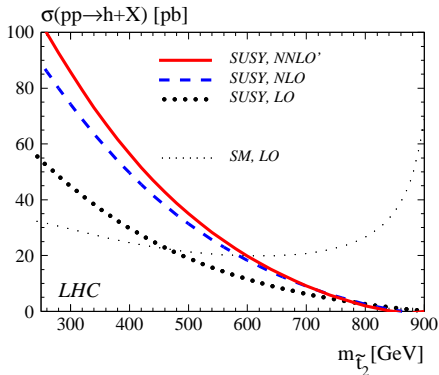
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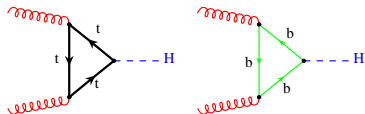
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Known components

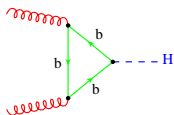
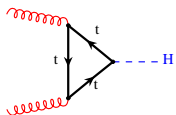


NLO

[Spira, Djouadi, Graudenz, Zerwas '95]
[RH, Kant '05]

...

Known components

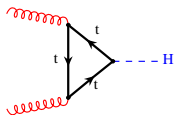


NLO

[Spira, Djouadi, Graudenz, Zerwas '95]

[RH, Kant '05]

...



NNLO

[RH, Kilgore '02]

[Anastasiou, Melnikov '02]

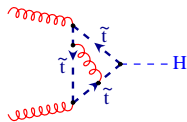
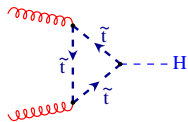
[Ravindran, Smith, van Neerven '03]

[Marzani, Ball, del Duca,
Forte, Vicini '08]

[RH, Marzani, Mantler, Ozeren '10]

[Pak, Rogal, Steinhauser '10]

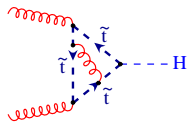
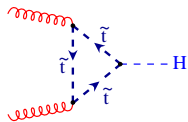
Known components



NLO

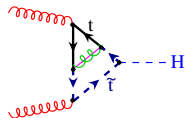
[RH, Steinhauser '03]
[Anastasiou *et al.* '07]
[Aglietti *et al.* '07]
[Mühlleitner, Spira '07]

Known components



NLO

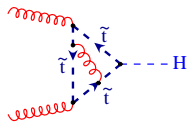
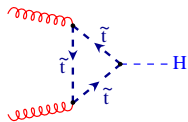
[RH, Steinhauser '03]
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[Aglietti *et al.* '07]
[Mühlleitner, Spira '07]



NLO

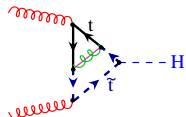
[RH, Steinhauser '03]
[Anastasiou, Beerli, Daleo '08]
[Degrassi, Slavich '08]

Known components



NLO

[RH, Steinhauser '03]
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[Aglietti *et al.* '07]
[Mühlleitner, Spira '07]



NLO

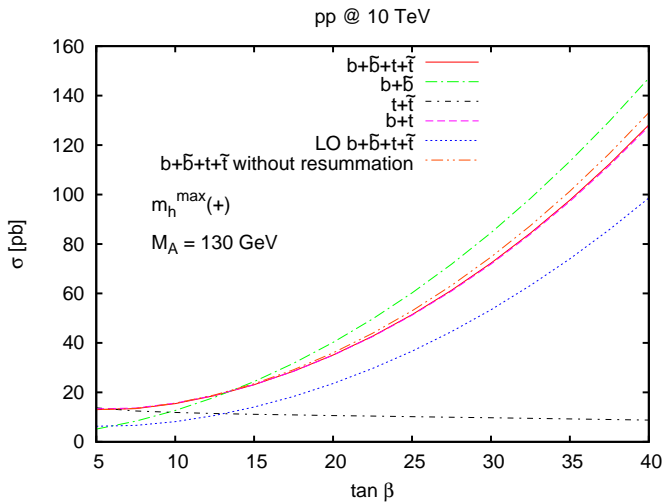
[RH, Steinhauser '03]
[Anastasiou, Beerli, Daleo '08]
[Degrassi, Slavich '08]

bottom/sbottom

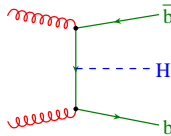
NLO

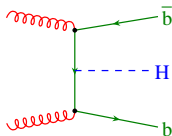
[Degrassi, Slavich '10]
[RH, Hofmann, Mantler '10]

Effects of SUSY

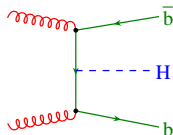


[RH, Hofmann, Mantler '10]

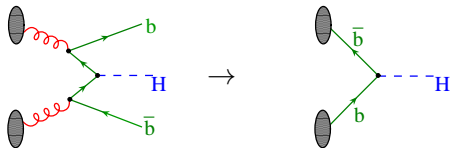




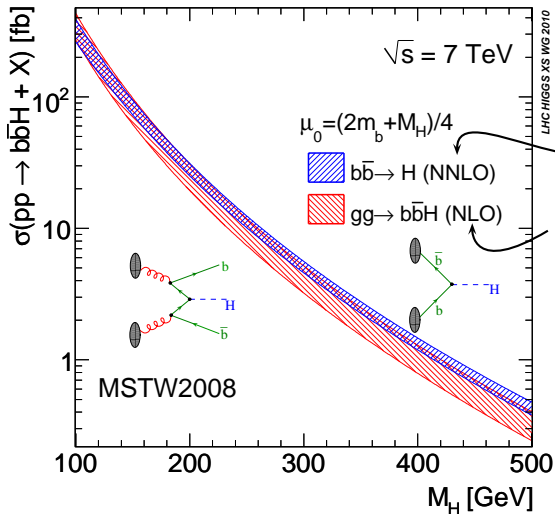
- collinear logarithms: $\sim \alpha_s \ln(m_b/M_H) \sim \alpha_s \ln(5/200)$



- collinear logarithms: $\sim \alpha_s \ln(m_b/M_H) \sim \alpha_s \ln(5/200)$
- resummation: **bottom quarks as partons**



$$pp \rightarrow H + b\bar{b}$$



LHC HIGGS XS WG 2010

[RH, Kilgore '03]

[Dittmaier, Krämer, Spira '04]

[Dawson, Jackson, Reina, Wackerath '04]

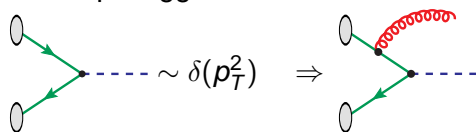
electro-weak:

[Dittmaier, Krämer, Mück, Schlüter '06]

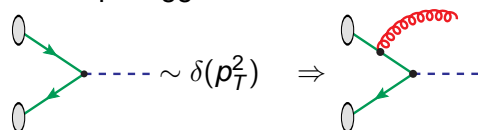
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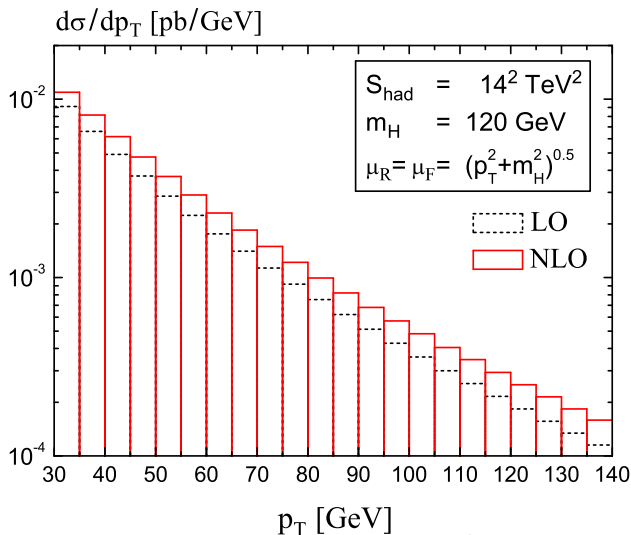
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consistent treatment requires NLO



[RH, Ozeren, Wiesemann '10]

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[RH, Kilgore '03]

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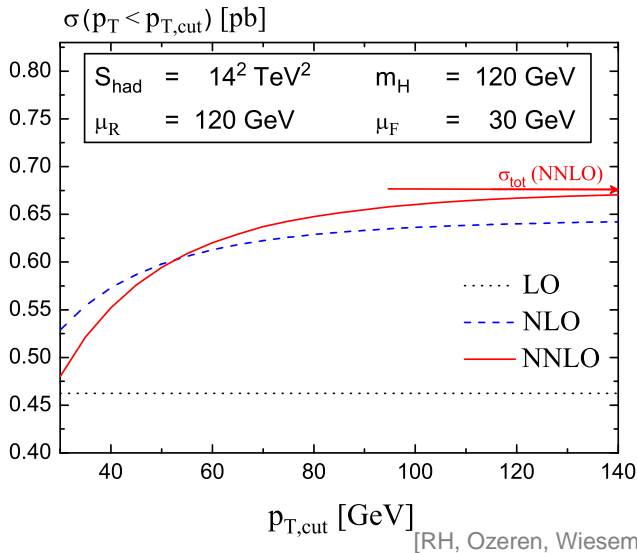
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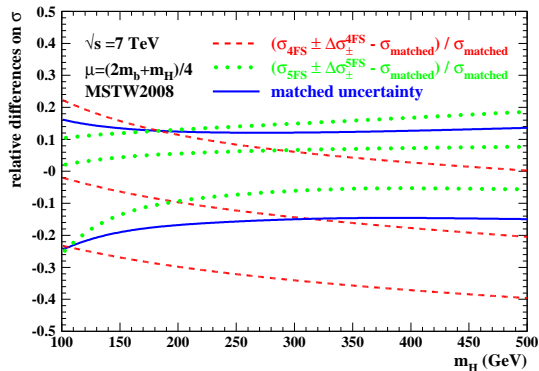
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- **vbf@nnlo**, **HNNLO**, **FEHiP**, ...

- [Anastasiou, Boughezal, Petriello '09]
- [de Florian, Grazzini '09]
- [Ahrens, Becher, Neubert, Yang '10]
- [Baglio, Djouadi '10]
- [Demartin, Forte, Mariani, Rojo, Vicini '10]
- [C.F. Berger, Marcantonini, Stewart, Tackmann, Waalewijn '10]
- [Alekhin, Blümlein, Jimenez-Delgado, Moch, Reya '10]
- [Baglio, Djouadi, Ferrag, Godbole '11]
- [...]

Backup Slides

Santander matching



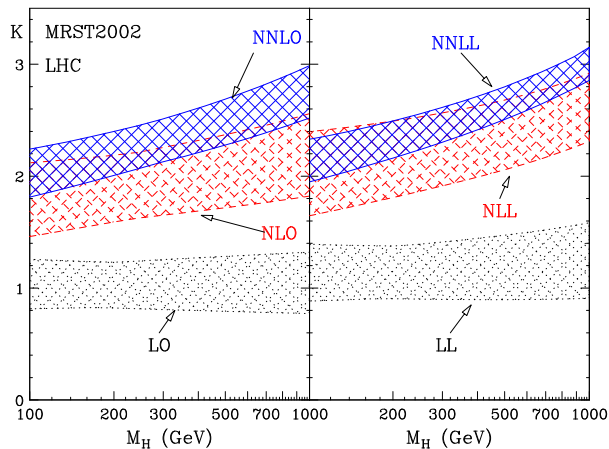
$$\sigma = \frac{\sigma_{4\text{FS}} + W\sigma_{5\text{FS}}}{1 + W}$$

$$\Delta\sigma = \frac{\Delta\sigma_{4\text{FS}} + W\Delta\sigma_{5\text{FS}}}{1 + W}$$

$$W = \ln \frac{m_H}{m_b} - 2$$

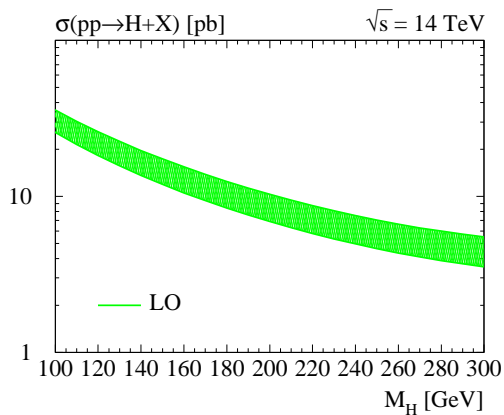
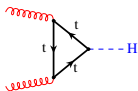
[R.H., Krämer, Schumacher '11]

Soft gluon resummation

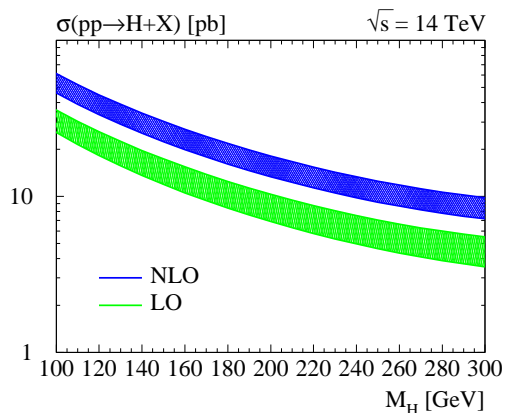
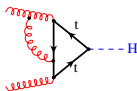


[Catani, de Florian,
Grazzini, Nason ('03)]

Gluon fusion: theory prediction



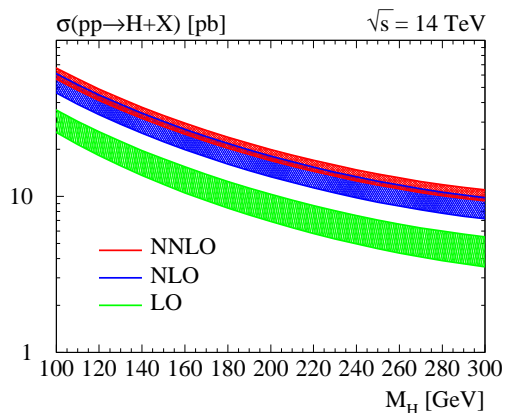
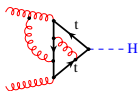
Gluon fusion: theory prediction



[Spira, Djouadi, Graudenz,
Zerwas '91/'93]

[Dawson '91]

Gluon fusion: theory prediction



- [R.H., Kilgore '02]
- [Anastasiou, Melnikov '02]
- [Ravindran, Smith, v. Neerven '03]
- [Spira, Djouadi, Graudenz, Zerwas '91/'93]
- [Dawson '91]

Higgs Cross Section

M_H (GeV)	ABM10 [8]	ABKM09 [9]	JR [10]	MSTW08 [11]	HERAPDF [12]
100	1.438 ± 0.066	1.380 ± 0.076	1.593 ± 0.091	1.682 ± 0.046	1.417
110	1.051 ± 0.052	1.022 ± 0.061	1.209 ± 0.078	1.265 ± 0.038	1.055
115	0.904 ± 0.047	0.885 ± 0.055	1.060 ± 0.072	1.104 ± 0.034	0.917
120	0.781 ± 0.042	0.770 ± 0.050	0.933 ± 0.067	0.968 ± 0.031	0.800
125	0.677 ± 0.038	0.672 ± 0.045	0.823 ± 0.062	0.851 ± 0.029	0.700
130	0.588 ± 0.034	0.589 ± 0.041	0.729 ± 0.058	0.752 ± 0.026	0.615
135	0.513 ± 0.031	0.518 ± 0.037	0.647 ± 0.054	0.666 ± 0.024	0.541
140	0.449 ± 0.028	0.456 ± 0.034	0.576 ± 0.050	0.591 ± 0.022	0.479
145	0.394 ± 0.025	0.403 ± 0.031	0.514 ± 0.047	0.527 ± 0.020	0.424
150	0.347 ± 0.023	0.358 ± 0.028	0.461 ± 0.044	0.471 ± 0.018	0.377
155	0.306 ± 0.020	0.318 ± 0.026	0.413 ± 0.041	0.421 ± 0.017	0.336
160	0.271 ± 0.019	0.283 ± 0.024	0.371 ± 0.039	0.378 ± 0.016	0.300
165	0.240 ± 0.017	0.253 ± 0.022	0.335 ± 0.036	0.341 ± 0.014	0.269
170	0.213 ± 0.015	0.226 ± 0.020	0.302 ± 0.034	0.307 ± 0.013	0.241
175	0.190 ± 0.014	0.203 ± 0.019	0.274 ± 0.032	0.278 ± 0.012	0.217
180	0.169 ± 0.013	0.182 ± 0.017	0.248 ± 0.030	0.251 ± 0.012	0.195
185	0.151 ± 0.012	0.164 ± 0.016	0.225 ± 0.028	0.228 ± 0.011	0.176
190	0.136 ± 0.011	0.148 ± 0.015	0.205 ± 0.027	0.207 ± 0.010	0.159
200	0.109 ± 0.009	0.121 ± 0.013	0.170 ± 0.024	0.172 ± 0.009	0.131

Higgs Cross Section

