

NLO effects in off-shell Top-quark pair production

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in collaboration with

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Standard Model Benchmarks at High-Energy Hadron Colliders
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Outline of the talk

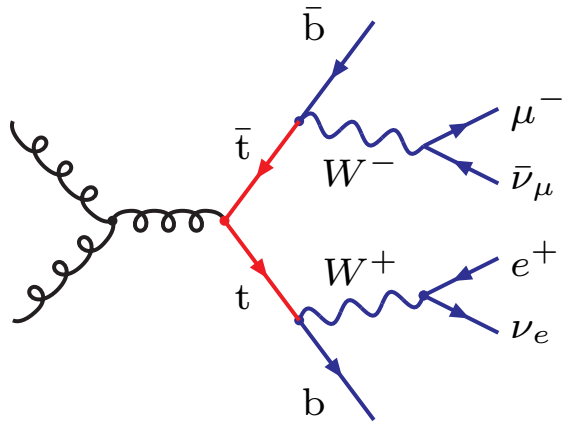
1. **Why $pp \rightarrow t\bar{t} \rightarrow W^+W^-b\bar{b}$ at NLO?**
2. **Technical aspects of the calculation**
3. **NLO predictions for Tevatron and LHC**

NLO priority list (Les Houches '05): completed $2 \rightarrow 4$ calculations

- **Two calculations for $pp \rightarrow t\bar{t}b\bar{b}$ with permille agreement**
 - arXiv:0905.0110 and arXiv:1001.4006 by Bredenstein, Denner, Dittmaier and S. P. Feynman diagrams and tensor integrals
 - arXiv:0907.4723 by Bevilacqua, Czakon, Papadopoulos, Pittau and Worek OPP reduction and HELAC
- **Two calculations for $pp \rightarrow Vjjj$**
 - arXiv:0906.1445 by Ellis, Melnikov and Zanderighi D -dimensional unitarity (leading colour)
 - arXiv:0907.1984 ($Wjjj$) and arXiv:1004.1659 ($Zjjj$) by Berger, Bern, Dixon, Febres Cordero, Forde, Gleisberg, Ita, Kosower and Maitre generalized unitarity (full colour)
- **First result for $pp \rightarrow t\bar{t}jj$**
 - arXiv:1002.4009 by Bevilacqua, Czakon, Papadopoulos and Worek OPP reduction and HELAC

- **One calculation for $pp \rightarrow WWjj$**
 - arXiv:1007.5313 and arXiv:1104.2327 by Melia, Melnikov, Rontsch and Zanderighi
 D -dimensional unitarity
- **First 7-leg result for $pp \rightarrow W + 4j$**
 - arXiv:1009.2338 by Berger, Bern, Dixon, Febres Cordero, Forde, Gleisberg, Ita, Kosower and Maitre
generalized unitarity (leading colour)
- **One calculation for $pp \rightarrow b\bar{b}b\bar{b}$**
 - arXiv:1105.3624 by Greiner, Guffanti, Reuter and Reiter
Feynman diagrams and OPP reduction (GOLEM–SAMURAI)
- **Two (almost simultaneous) calculations for $pp \rightarrow W^+W^-b\bar{b}$**
 - arXiv:1012.3975 by Denner, Dittmaier, Kallweit and S. P.
Feynman diagrams and tensor integrals
 - arXiv:1012.4230 by Bevilacqua, Czakon, van Hameren, Papadopoulos and Worek
OPP reduction and HELAC

Why $W^+W^-b\bar{b}$ production at NLO?



Full description of $t\bar{t}$ prod \times decay

- off-shell tops and non-resonant backgr.
- $W \rightarrow l\nu$ decays in spin-correlated NWA

Huge $t\bar{t}$ samples at hadron colliders

- Tevatron: few 10^4 events $\Rightarrow \frac{\delta\sigma}{\sigma} < 10\%$
- LHC at 7(14) TeV: $1.5(9) \times 10^5$ events per $\text{fb}^{-1} \Rightarrow \frac{\delta\sigma}{\sigma} = \text{few } \%$

Crucial measurements and tests

- precise studies of rich variety of (differential) observables
- checks and tuning of many theoretical/experimental tools
- $\delta m_t^{\text{exp}} \sim 1 \text{ GeV}$ measurements

Relevance for discoveries

- leptons + jets + missing E_T is a typical discovery signature (SUSY, $H \rightarrow W^+W^-$, ...)
- various BSM scenarios predict heavy resonances decaying into $t\bar{t}$

Precise predictions for hadronic $t\bar{t}$ production (and decay)

NLO QCD corrections

Beenakker, Dawson, Ellis, Frixione, Kuijf, Meng, Nason, van Neerven, Schuler, Smith

Electroweak NLO corrections

Beenakker, Bernreuther, Denner, Fücker, Hollik, Kao, Kollar, Kühn, Ladinsky, Mertig, Moretti, Nolten, Ross, Sack, Scharf, Si, Uwer, Wackerroth, Yuan

From LL to NNLL resummations

Ahrens, Beneke, Berger, Bonciani, Catani, Contopanagos, Czakon, Falgari, Ferroglia, Frixione, Kidonakis, Kiyo, Laenen, Mangano, Mitov, Moch, Nason, Neubert, Pecjak, Ridolfi, Schwinn, Sterman, Uwer, Vogt, Yang

Towards full NNLO predictions

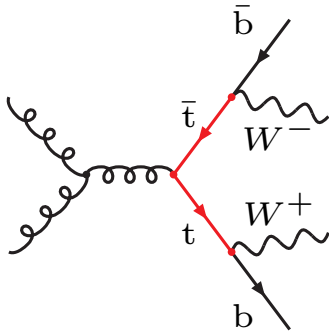
Anastasiou, Aybat, Bonciani, Czakon, Dittmaier, Ferroglia, Gehrmann, Gehrmann–De Ridder, Kniehl, Körner, Langenfeld, Maitre, Merebashvili, Mitov, Moch, Ritzmann, Rogal, Studerus, von Manteuffel, Uwer, Weinzierl

NLO $t\bar{t}$ production \times decay in spin-correlated narrow-width approx.

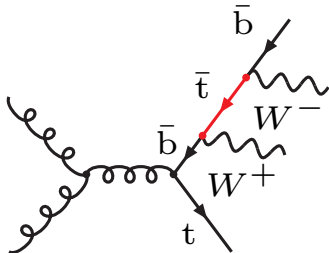
Bernreuther, Brandenburg, Melnikov, Schulze, Si, Uwer

Full $W^+W^-b\bar{b}$ description vs Narrow-Width Approximation in LO

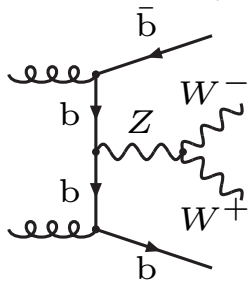
Doubly-Resonant (DR)



Singly-Resonant (SR)



Non-Resonant (NR)



Narrow-Width Approximation

- only doubly-resonant channels
- narrow-width limit of Breit-Wigner top resonances

$$\lim_{\Gamma_t \rightarrow 0} \left| \frac{1}{p_t^2 - m_t^2 + i\Gamma_t m_t} \right|^2 = \frac{\pi}{\Gamma_t m_t} \delta(p_t^2 - m_t^2)$$

Finite-width contributions to $W^+W^-b\bar{b}$

- Off-shell corrections to doubly-resonant channels
- Singly + non-resonant channels and interferences
- finite-width corrections to *inclusive* observables of order $\Gamma_t/m_t \simeq 1\%$

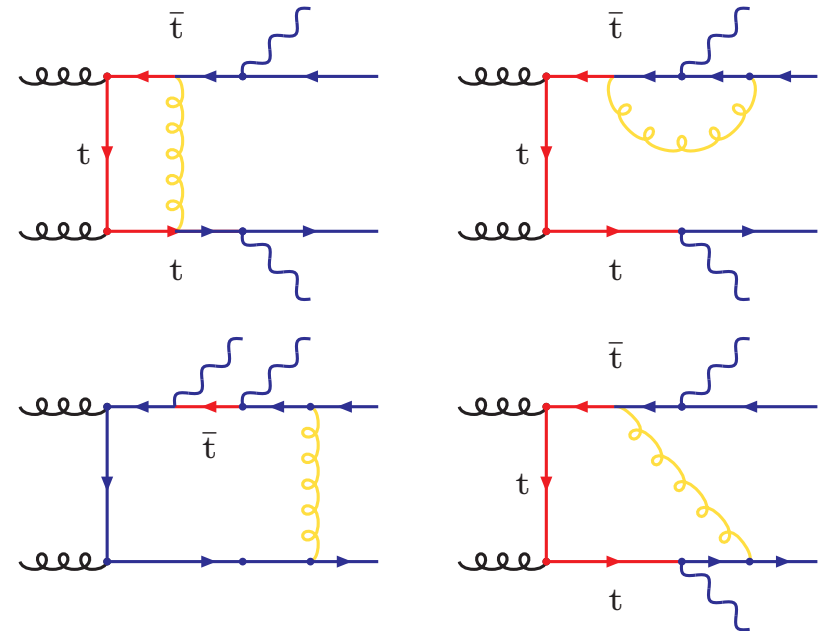
Full $W^+W^-b\bar{b}$ description vs Narrow-Width Approximation in NLO

Narrow-Width Approximation

- only factorisable corrections
- huge technical simplification

Finite-width contributions to $W^+W^-b\bar{b}$

- pentagons and hexagons
- non-factorisable and non-DR corrections



In *inclusive* observables non-fact. virtual and real $\ln(\Gamma_t/m_t)$ corr. from soft gluons cancel, and finite-width effects remain $\mathcal{O}(\Gamma_t/m_t)$ suppressed [Fadin/Khoze/Martin '94].

Finite-width effects can be important for

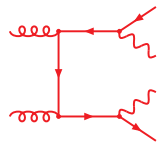
- percent-level precision in σ_{incl}
- Shape of top resonance and related observables (m_t measurement)
- cuts suppressing on-shell $t\bar{t}$ background and enhancing off-shell $W^+W^-b\bar{b}$

(2) Technical aspects of the calculation

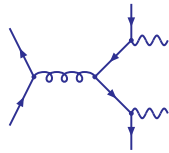
Ingredients of $pp \rightarrow W^+W^-b\bar{b}$ at NLO

Partonic channels

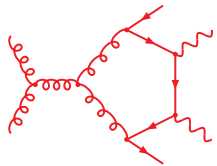
Full calculation twice and independently



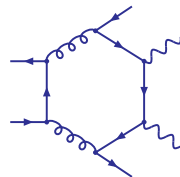
31 trees



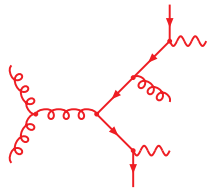
14 trees



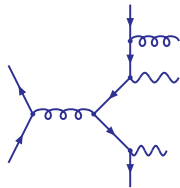
788 loops



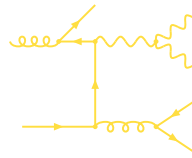
280 loops



222 NLO trees



90 NLO trees



90 NLO trees

Generation of Feynman diagrams

- FeynArts 1.0 / 3.2

Algebraic reduction

- MATHEMATICA / FormCalc [[Hahn](#)]

Tensor integrals & numerics

- Fortran77 / C++ executables: 0.25–1.2 GB

Real emission & IR Subtraction

- Madgraph & spinors
- Dipoles [[Catani/Dittmaier/Seymour/Trócsányi '97/'02](#)]
& AutoDipole [[Hasegawa/Moch/Uwer '09](#)]

Integration over 11-dim PS

- adaptive multi-channel Monte Carlo with 250–650 mappings per partonic channel

Feynman diagrams and tensor integrals

$$\sum_{\text{col,pol}} \left(\text{circle diagram with 4 external lines} \right)^* \times \text{circle diagram with 4 external lines and 2 red wavy lines} = \sum_{\text{col,pol}} \left(\text{circle diagram with 4 external lines} \right)^* \times \text{hexagon diagram with 6 external lines and 2 red wavy lines} + \mathcal{O}(1000) \text{ more diagrams}$$

Colour sums at zero cost
thanks to *colour factorisation*

$$\underbrace{\text{hexagon diagram with 6 external lines}} \times f^{a_1 b d} f^{a_2 c d} (T^c T^b)_{i_5 i_6}$$

$$\underbrace{\sum a_{i_1 \dots j_P} \epsilon_{\mu_1 \mu_2 \mu_3 \mu_4} [\bar{v}_5 \gamma_{\mu_5} \dots \gamma_{\mu_k} u_6] \{g \dots p\}_{i_1 \dots j_P}^{\mu_1 \dots \nu_P}} \int d^D q \frac{q_{\nu_1} \dots q_{\nu_P}}{N_0 \dots N_{N-1}}$$

Algebraic reduction of helicity structures

$\mathcal{O}(10^3 - 10^4)$ compact spinor chains \rightarrow fast helicity sums
completely automatic!

$$\sum T_{j_1 \dots j_P}^{(N)} \{g \dots p\}_{j_1 \dots j_P}^{\nu_1 \dots \nu_P}$$

Numerical tensor-integral reduction

$e^+ e^- \rightarrow$ 4f methods [Denner/Dittmaier'05]
completely general and numerically stable!

$$\sum d_i \text{square diagram} + c_j \text{triangle diagram} + b_k \text{circle with 2 external lines} + a_l \text{circle with 1 external line}$$

Very high CPU efficiency

First physical application up to tensor rank $P = 5$

- CPU cost of colour/helicity summed $gg \rightarrow W^+W^-b\bar{b}$ loop amplitudes very low (450ms) similarly as for $gg \rightarrow t\bar{t}b\bar{b}$ (180 ms) where $P = 4$
- σ_{NLO} with statistical accuracy of $\mathcal{O}(10^{-3})$ requires $\mathcal{O}(10^8)$ events obtained within 5–10 days on single CPU
- Total CPU cost at LHC dominated by real and virtual gg-channel corrections

Treatment of unstable particles

Regularisation of unstable-particle propagators via $\text{Im}[\Sigma(M^2)] = M\Gamma$ resummation

$$\frac{1}{p^2 - M^2 + i\epsilon} \rightarrow \frac{1}{p^2 - M^2 + iM\Gamma + i\epsilon}$$

can violate **gauge invariance**

Complex mass scheme at NLO (introduced for $e^+e^- \rightarrow 4f$ Denner/Dittmaier '05)

- Γ is absorbed into the renormalised pole mass $M^2 \rightarrow \mu^2 = M^2 - iM\Gamma$ without modifying the bare Lagrangian
- Lagrangian symmetries require (in general) complex couplings

Technical aspects

- On-shell **renormalisation with complex momenta**: $\hat{\Sigma}(p^2) = 0$ at $p^2 = \mu^2$
- Scalar **box integrals with complex masses** (subtle analytic continuations!)
 - 't Hooft/Veltman approach: $24 \rightarrow 108$ Li_2 Nhung/Ninh '09; van Hameren '10
 - Denner/Niertse/Scharf approach: $16 \rightarrow 32$ Li_2 Denner/Dittmaier '10

**(3.1) $W^+W^-b\bar{b}$ cross section at the Tevatron (1.96 TeV)
and the LHC (7 TeV)**

Setup and input parameters for Tevatron (LHC)

Particle masses and widths ($M_H = \infty$, $m_b = 0$)

$$\begin{array}{lll} m_t = 172.0 \text{ GeV} & M_W = 80.399 \text{ GeV} & M_Z = 91.1876 \text{ GeV} \\ \Gamma_{t,\text{LO}} = 1.4655 \text{ GeV} & \Gamma_{t,\text{NLO}} = 1.3376 \text{ GeV} & \Gamma_{W,\text{NLO}} = 2.0997 \text{ GeV} \end{array}$$

G_μ -scheme couplings ($G_\mu = 1.16637 \times 10^{-5} \text{ GeV}^{-2}$)

$$\sin^2 \theta_w = 1 - M_W^2/M_Z^2, \quad \alpha = \sqrt{2}G_\mu M_W^2 \sin^2 \theta_w / \pi$$

PDFs and α_S : MSTW2008NLO(LO) with $1/2 \leq \mu_{R,F}/m_t \leq 2$ variations

Anti- k_T Jet Algorithm

$$\text{QCD partons with } |\eta| < 5 \quad \Rightarrow \quad \text{jets with } \sqrt{\Delta\phi^2 + \Delta y^2} > R = 0.4 \text{ (0.5)}$$

Typical Tevatron (LHC) cuts

$$\begin{array}{lll} \text{b-jets:} & p_{T,b} > 20 \text{ (30) GeV} & |\eta_b| \leq 2.5 \\ \text{leptons:} & p_{T,l} > 20 \text{ GeV} & |\eta_l| \leq 2.5 \quad p_{T,\text{miss}} > 25 \text{ (20) GeV} \end{array}$$

Integrated $e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b}$ cross section

Predictions for $\mu_{R,F} = m_t$ and $m_t/2 \leq \mu_{R,F} \leq 2m_t$

σ	LO	NLO	NLO/LO
Tevatron	$44.31^{+19.68}_{-12.49}$ fb	$41.75^{+0.00}_{-3.79}$ fb	$0.942^{+0.000}_{-0.085}$
LHC	$662.4^{+263.4}_{-174.1}$ fb	840^{+27}_{-75} fb	$1.27^{+0.04}_{-0.11}$

Scale uncertainty at the Tevatron (LHC)

- 44% (40%) LO uncertainty is mostly due to

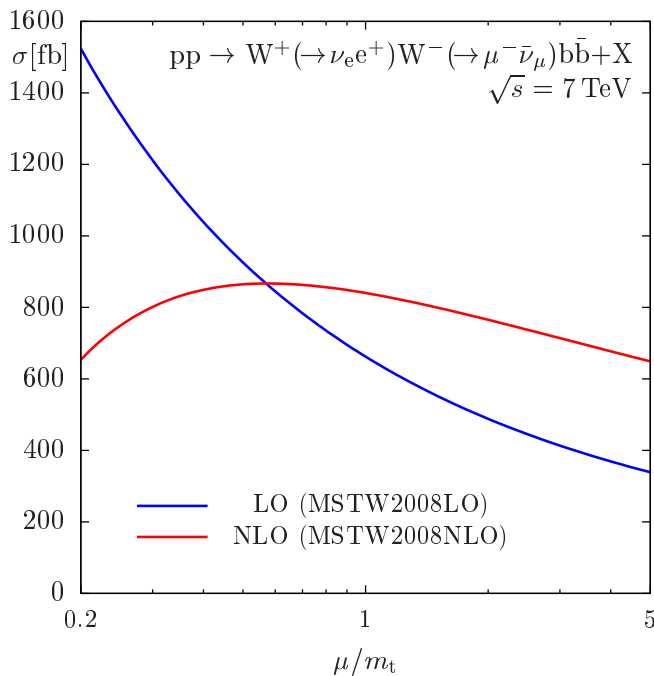
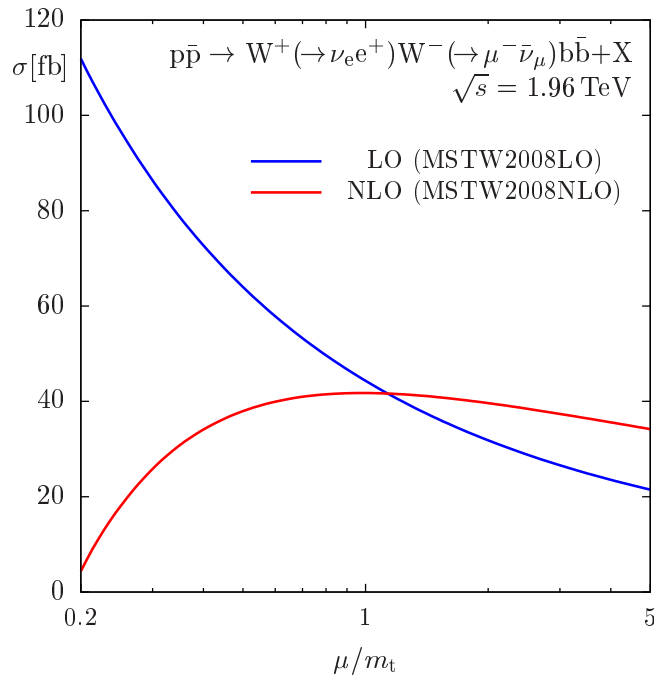
$$\frac{\Delta\sigma_{\text{LO}}}{\sigma_{\text{LO}}} \simeq \frac{\Delta\alpha_S^2(\mu)}{\alpha_S^2(\mu)} \text{ and reduces to 9\%(9\%) at NLO}$$

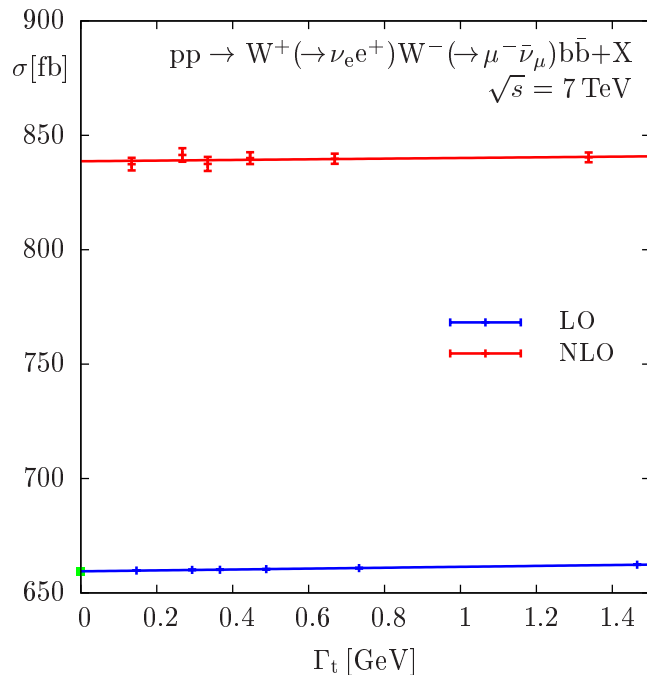
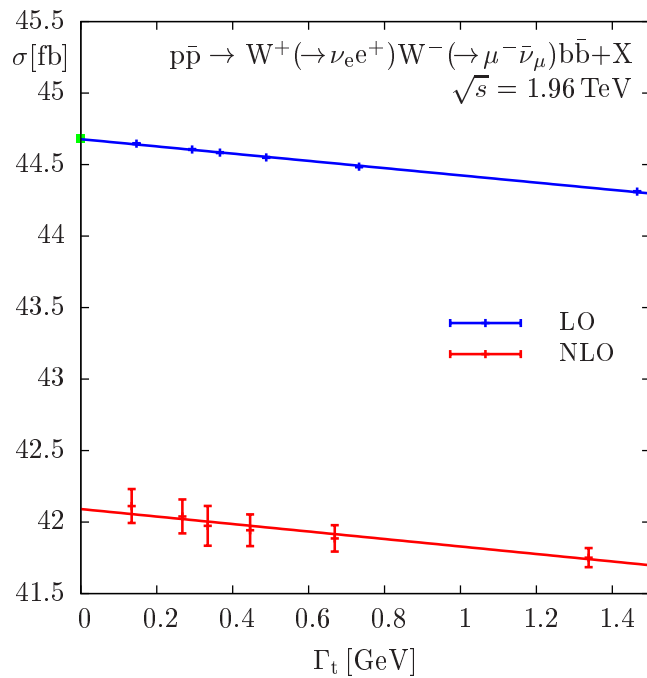
Moderate NLO corrections

- $K_{\text{Tevatron}} \simeq 0.94$ and $K_{\text{LHC}} \simeq 1.27$

Agreement with HELAC-NLO [Bevilacqua et al. '10]

σ_{Tevatron}	LO	NLO
DDKP	$44.310[3]$ fb	$41.75[5]$ fb
BCHPW	$44.32[3]$ fb	$41.86[6]$ fb





Off-shell and non-resonant contributions to $\sigma_{\text{int.}}$

Assessment of finite-width effects $\sigma(\Gamma_t) - \sigma(0)$

- numerical extrapolation to $\Gamma \rightarrow 0$ using five rescaled values $\Gamma_t \rightarrow \xi\Gamma_t$ with $0.1 \lesssim \xi \leq 1$

Cancellation of soft-gluon $\ln(\Gamma_t/m_t)$ singularities

- dipole-subtracted virtual and real parts diverge logarithmically when $\Gamma \rightarrow 0$
- **linear convergence of $\sigma(\Gamma_t) \rightarrow \sigma(0)$** provides non-trivial consistency and stability check

Finite-width effects comparable to $\Gamma_t/m_t \simeq 0.8\%$

	$\sigma_{\text{LO}}(\Gamma_t)/\sigma_{\text{LO}}(0) - 1$	$\sigma_{\text{NLO}}(\Gamma_t)/\sigma_{\text{NLO}}(0) - 1$
Tevatron	-0.8%	-0.9%
LHC	+0.4%	+0.2%

quantifies precision of NWA for σ_{incl}

**(3.2) Differential $W^+W^-b\bar{b}$ distributions
at the Tevatron (1.96 TeV) and the LHC (7 TeV)**

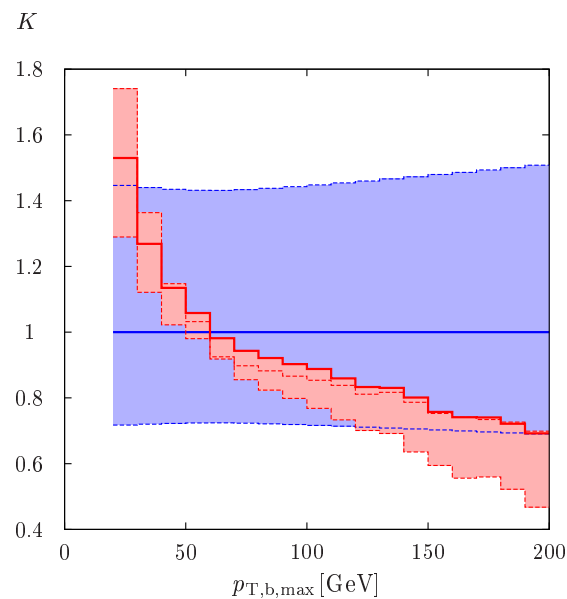
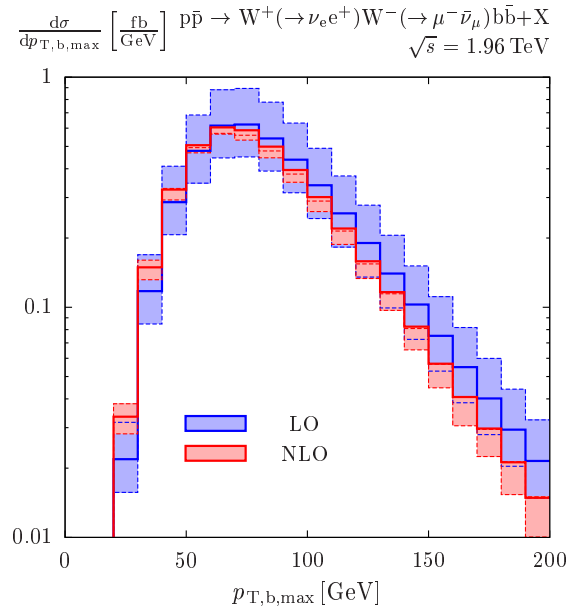
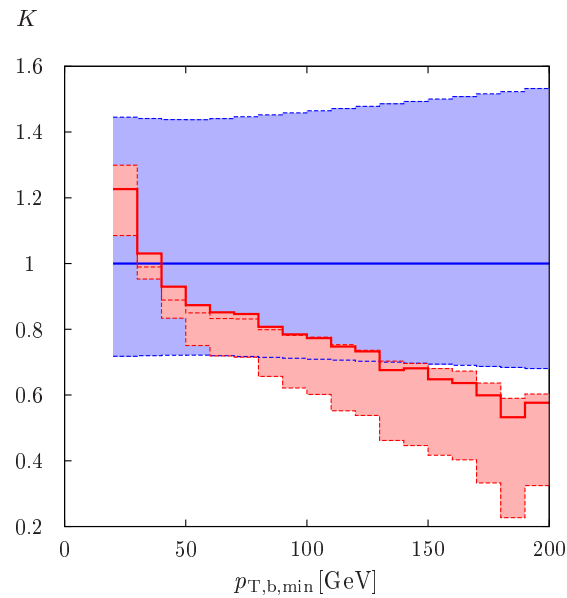
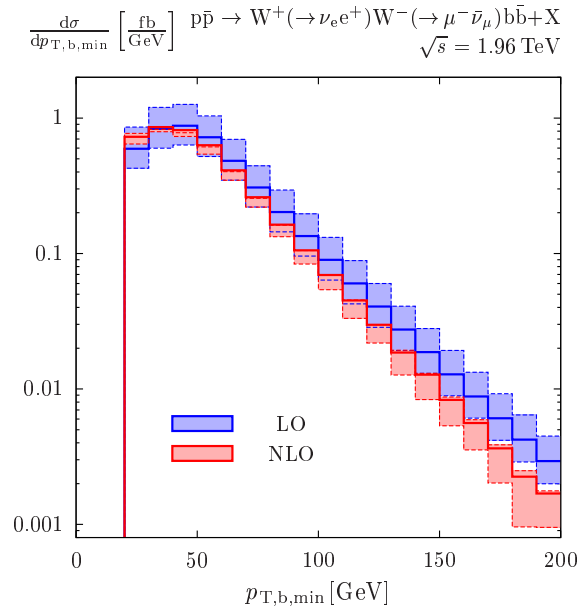
b-jet p_T at the Tevatron

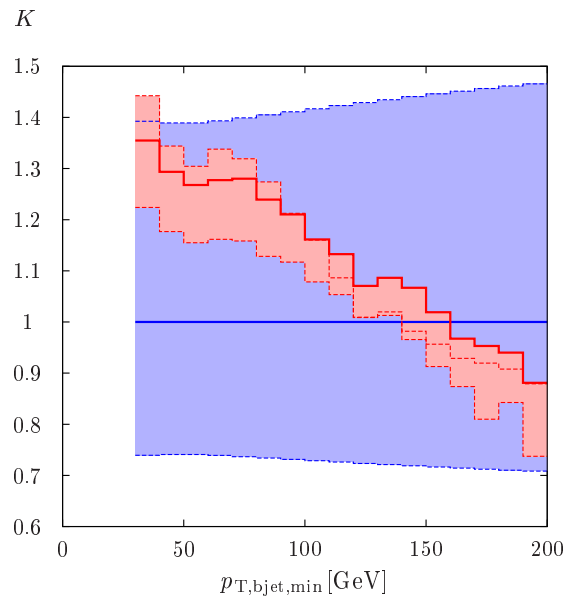
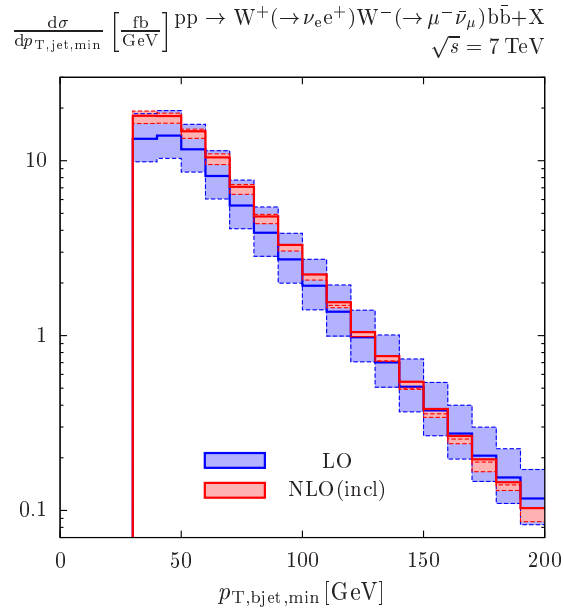
Soft b-jet (upper)

- saturates cut at 20 GeV
- +20% to -40% corrections
- strong shape distortions
(relevant for acceptance)

Hard b-jet (lower)

- peaked around 80 GeV
- +50% to -30% corrections
- strong shape distortions

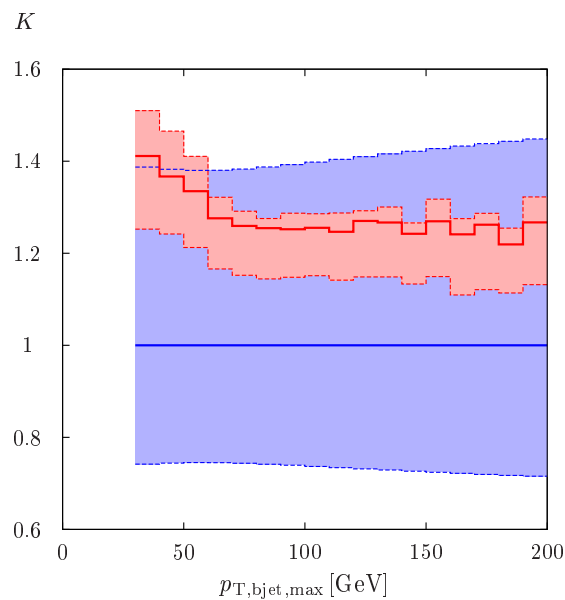
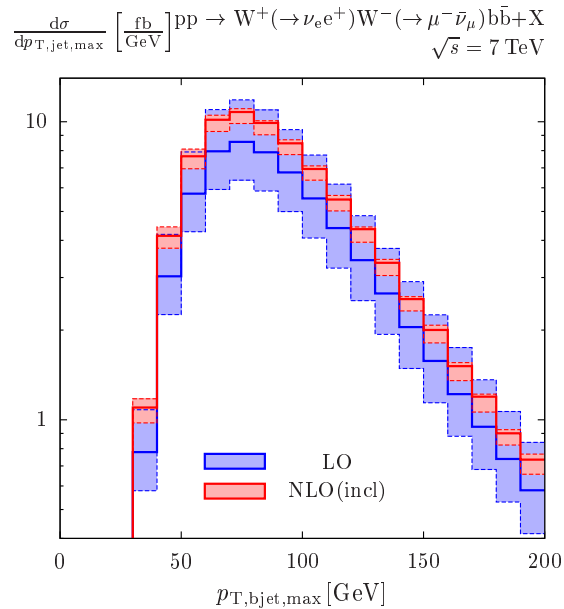




b-jet p_T at the LHC

Soft b-jet (upper)

- saturates cut at 30 GeV
- +30% to -10% corrections
- strong shape distortions
(relevant for acceptance)

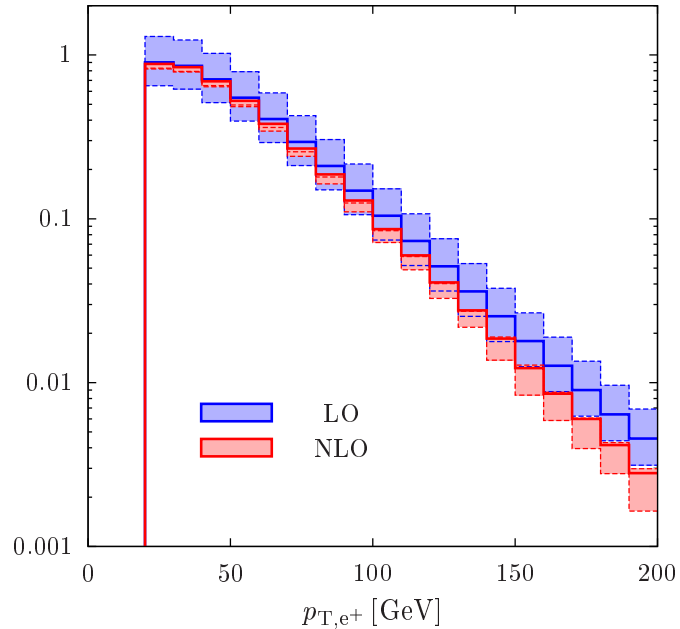


Hard b-jet (lower)

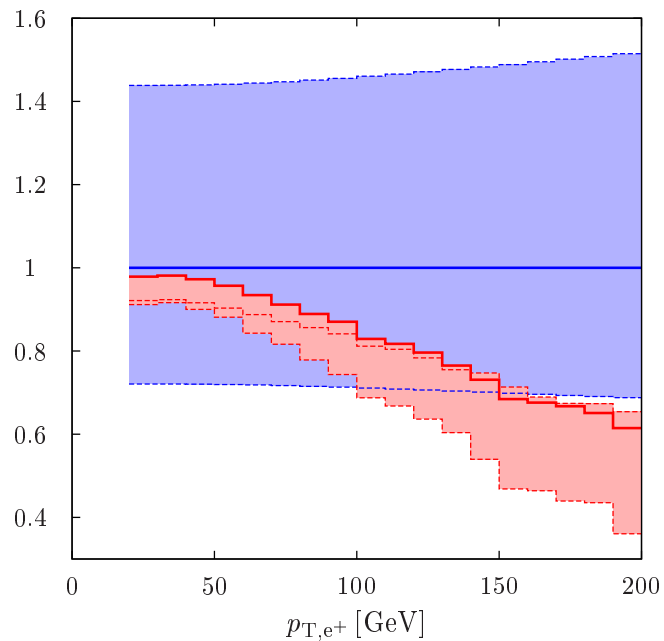
- peaked around 80 GeV
- +40% to +20% corrections
- moderate shape distortions

$$\frac{d\sigma}{dp_{T,e^+}} \left[\frac{\text{fb}}{\text{GeV}} \right] \quad p\bar{p} \rightarrow W^+(\rightarrow \nu_e e^+) W^-(\rightarrow \mu^- \bar{\nu}_\mu) b\bar{b} + X$$

$\sqrt{s} = 1.96 \text{ TeV}$



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Lepton p_T at the Tevatron

e^+ (μ^-) from W^+ (W^-) decay

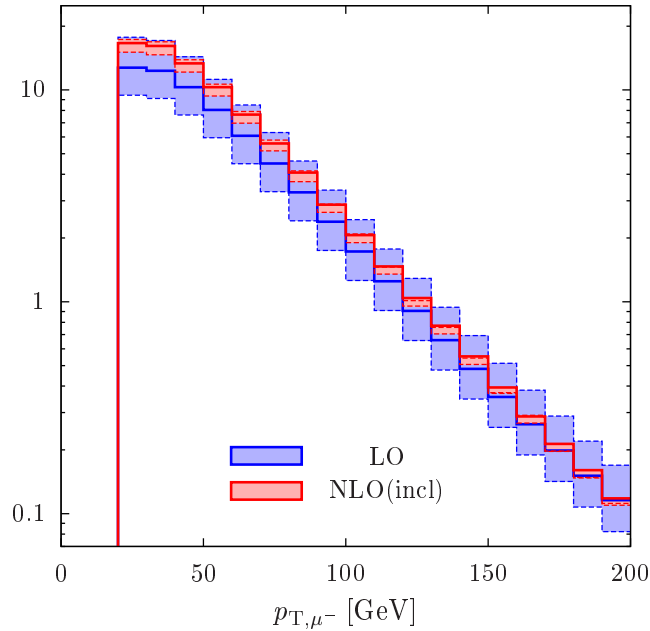
- have typically $p_T \lesssim 100 \text{ GeV}$ and tend to saturate the cut at 20 GeV
- corrections range from 0% to -40%

Shape distortion

- mild in the vicinity of the cut but **fairly strong at high p_T**
- relevant for boosted tops and NP searches
- when $p_T \gtrsim 100 \text{ GeV}$ fixed $\mu = m_t$ should be replaced by dynamical QCD scale

$$\frac{d\sigma}{dp_{T,\mu^-}} \left[\frac{\text{fb}}{\text{GeV}} \right] \quad pp \rightarrow W^+(\rightarrow \nu_e e^+) W^-(\rightarrow \mu^- \bar{\nu}_\mu) b\bar{b} + X$$

$\sqrt{s} = 7 \text{ TeV}$

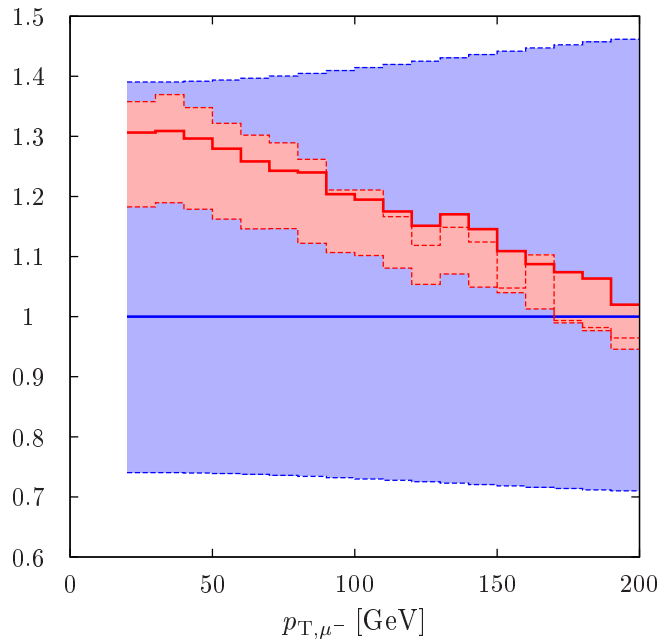


Lepton p_T at the LHC

e^+ (μ^-) from W^+ (W^-) decay

- have typically $p_T \lesssim 100 \text{ GeV}$ and tend to saturate the cut at 20 GeV
- corrections range from +30% to 0%

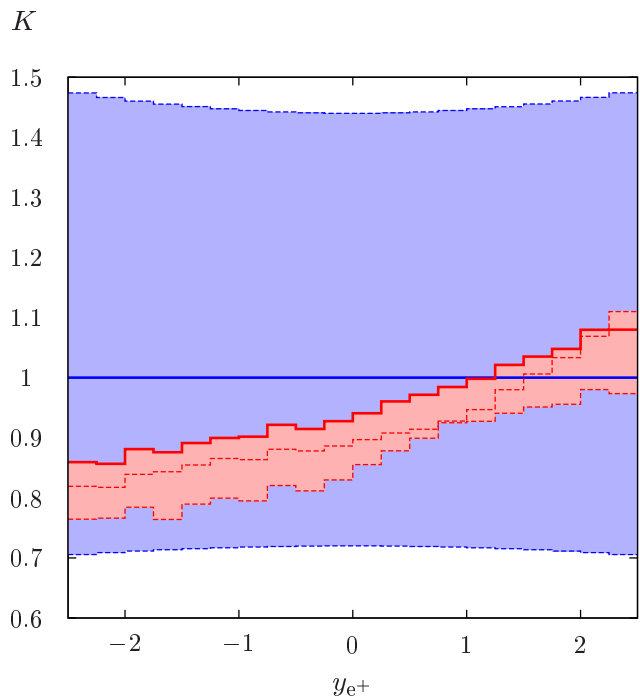
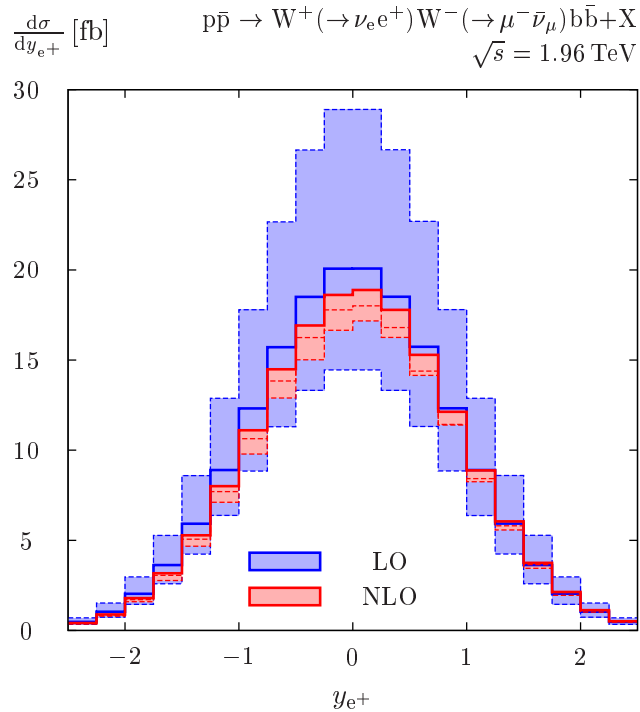
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Shape distortion

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- relevant for boosted tops and NP searches
- when $p_T \gtrsim 100 \text{ GeV}$ fixed $\mu = m_t$ should be replaced by dynamical QCD scale

Charged-lepton rapidity at the Tevatron



LO y_{e^+} distribution

- e^+ populates central region
- almost exactly symmetric due to $t \leftrightarrow \bar{t}$ invariance of $q\bar{q}/gg \rightarrow t\bar{t}$

NLO charge and FB asymmetry

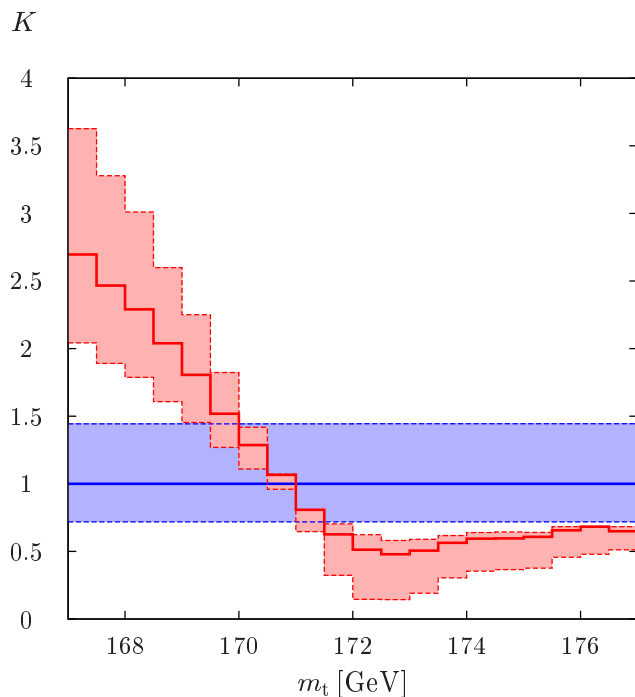
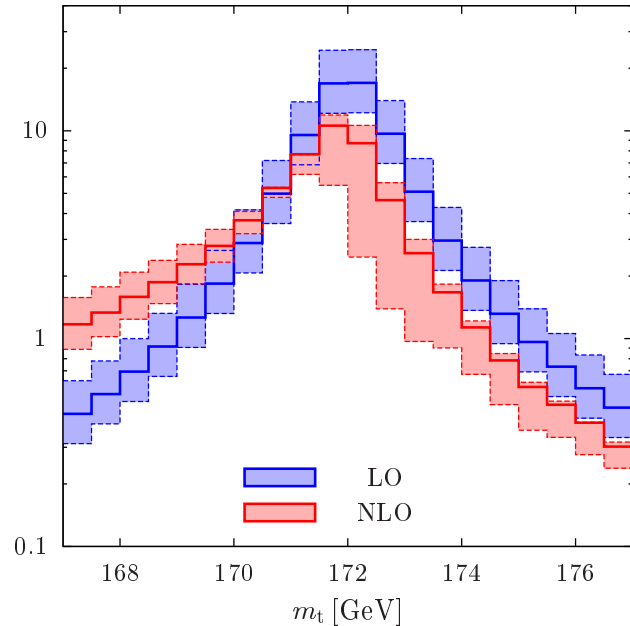
- IS–FS gluon exchange induces $t\bar{t}$ charge asymmetry
- reflected in y_{e^+} shape distortion (-15% to $+10\%$ corrections) and **FB asymmetry**

$$A_{\text{FB}} = \frac{\sigma(y_{e^+} > 0) - \sigma(y_{e^+} < 0)}{\sigma(y_{e^+} > 0) + \sigma(y_{e^+} < 0)} = 0.035(2)$$

consistent with NWA [[Bernreuther/Si '10](#)]

$$\frac{d\sigma}{dm_t} \left[\frac{\text{fb}}{\text{GeV}} \right] \quad p\bar{p} \rightarrow W^+(\rightarrow \nu_e e^+) W^-(\rightarrow \mu^- \bar{\nu}_\mu) b\bar{b} + X$$

$$\sqrt{s} = 1.96 \text{ TeV}$$



Top-quark invariant mass at the Tevatron

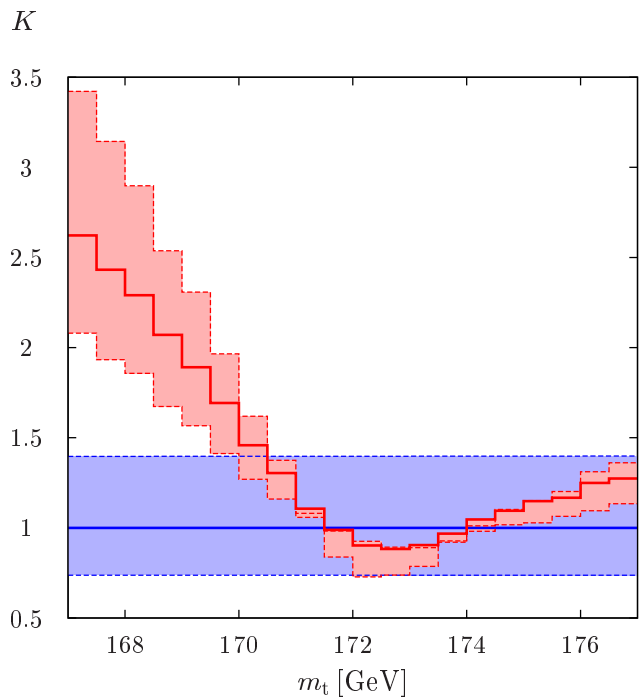
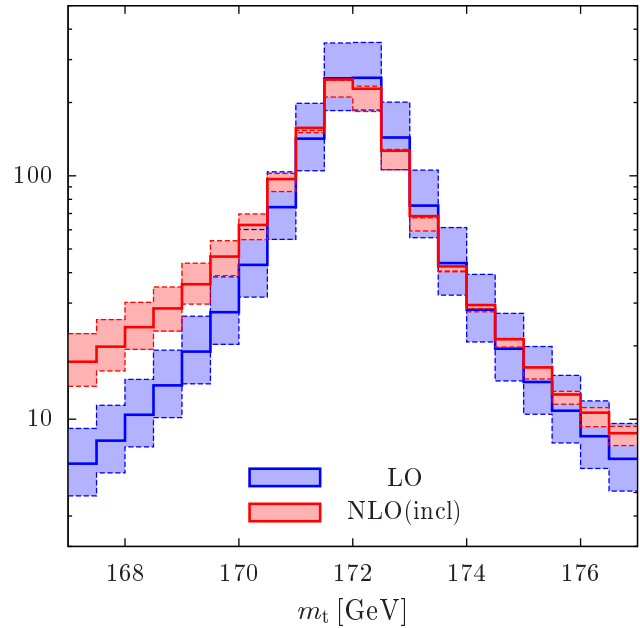
Although not observable $M_t = M_{b\bar{e}+\nu_e}$
reflects off-shell nature of $2 \rightarrow 4$ calculation

- Breit–Wigner shape in the resonance region
- $\delta\Gamma_{\text{NLO}}/\Gamma_{\text{LO}} \simeq -9\%$ crucial for consistent normalisation of $\sigma_{\text{incl.}} \sim 1/\Gamma_t^2$
- Pole of top-quark propagator not shifted in on-shell scheme, but QCD radiation leads to invariant-mass shift $\lesssim 1 \text{ GeV}$
- m_t -shift depends on jet algorithm

NLO and Γ_t effects will improve description of observables used for m_t determination

$$\frac{d\sigma}{dm_t} \left[\frac{\text{fb}}{\text{GeV}} \right] \quad pp \rightarrow W^+(\rightarrow \nu_e e^+) W^-(\rightarrow \mu^- \bar{\nu}_\mu) b\bar{b} + X$$

$$\sqrt{s} = 7 \text{ TeV}$$



Top-quark invariant mass at the LHC

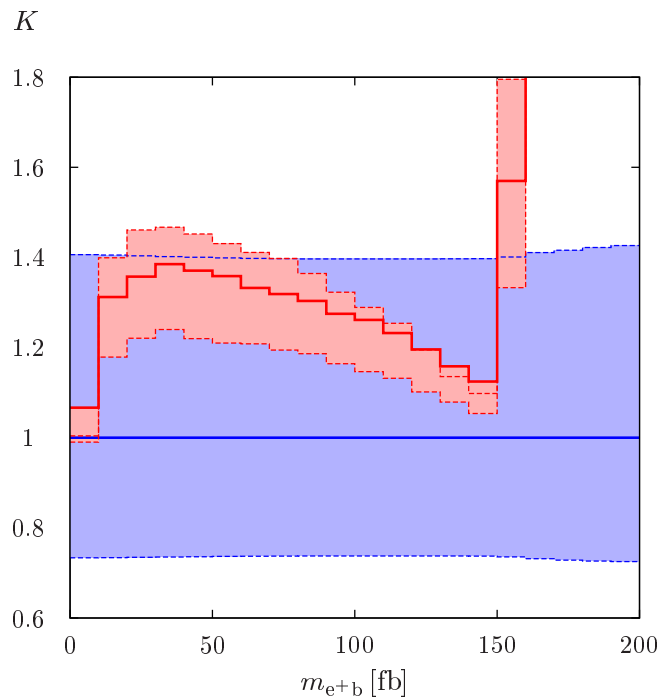
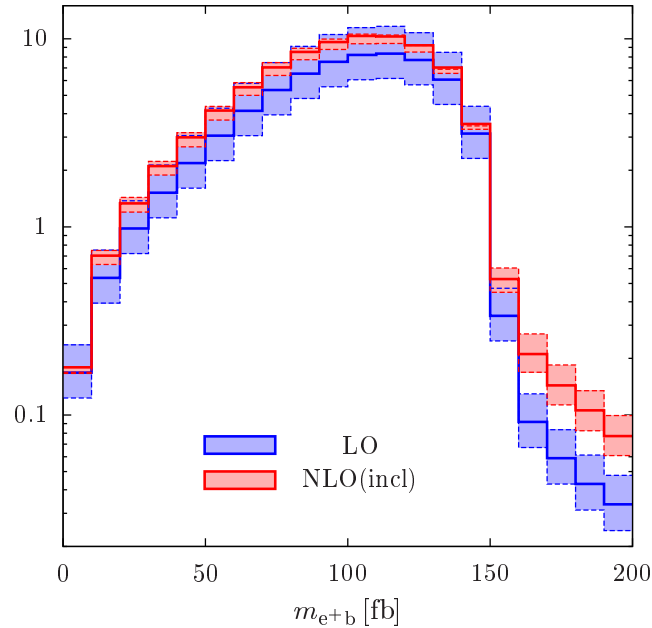
Although not observable $M_t = M_{be+\nu_e}$ reflects off-shell nature of $2 \rightarrow 4$ calculation

- Breit–Wigner shape in the resonance region
- $\delta\Gamma_{\text{NLO}}/\Gamma_{\text{LO}} \simeq -9\%$ crucial for consistent normalisation of $\sigma_{\text{incl.}} \sim 1/\Gamma_t^2$
- Pole of top-quark propagator not shifted in on-shell scheme, but QCD radiation leads to invariant-mass shift $\lesssim 1 \text{ GeV}$
- m_t -shift depends on jet algorithm

NLO and Γ_t effects will improve description of observables used for m_t determination

$$\frac{d\sigma}{dm_{e^+b}} \left[\frac{\text{fb}}{\text{GeV}} \right] \quad pp \rightarrow W^+(\rightarrow \nu_e e^+) W^-(\rightarrow \mu^- \bar{\nu}_\mu) b\bar{b} + X$$

$\sqrt{s} = 7 \text{ TeV}$



Invariant mass of b-jet–e⁺ pair at the LHC

Observable related to m_t measurement

- visible decay products in $t \rightarrow bW^+ \rightarrow be^+ \nu_e$ retain significant fraction of m_t
- good sensitivity to m_t via **kinematic bound**

$$M_{be^+}^2 \leq m_t^2 - M_W^2 \simeq (152 \text{ GeV})^2$$

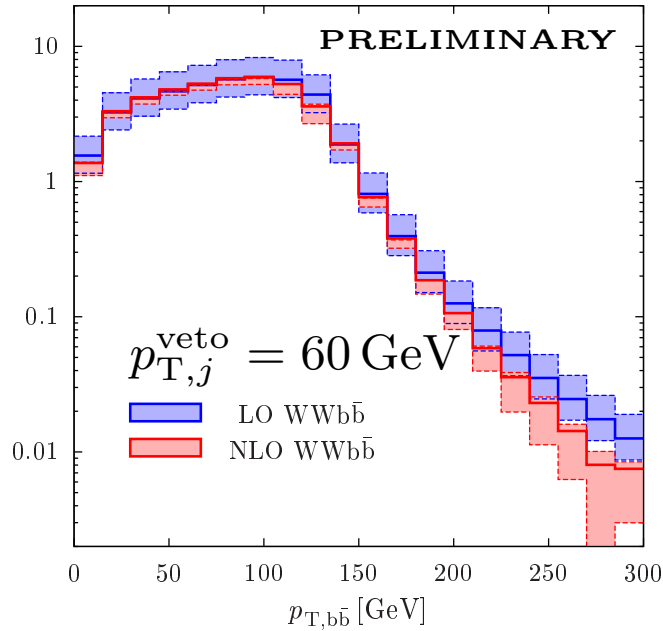
in LO and narrow-width approximation

Off-shell and NLO corrections

- M_{be^+} bound violated by LO off-shell effects
- additional violation from NLO radiation
- **strong NLO shape distortion** below the bound: from +40% to +5% corrections

$$\frac{d\sigma}{dp_{T,b\bar{b}}} \left[\frac{\text{fb}}{\text{GeV}} \right] \quad pp \rightarrow W^+(\rightarrow \nu_e e^+) W^-(\rightarrow \mu^- \bar{\nu}_\mu) b\bar{b} + X$$

$\sqrt{s} = 7 \text{ TeV}$

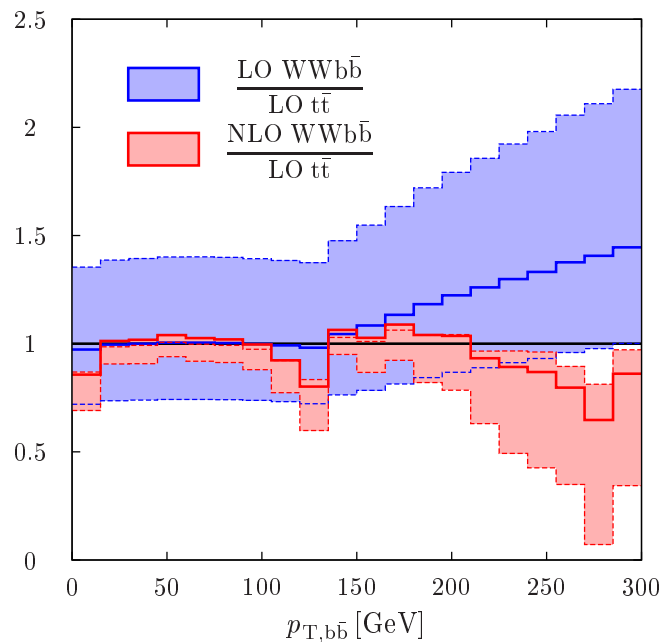


Large off-shell effects in WWb \bar{b} backg.

pp → WH → Wb \bar{b} search at the LHC

- huge QCD background suppressed with **boosted-Higgs strategy**
- $p_{T,b\bar{b}} > 200 \text{ GeV}$ and $p_{T,j}^{\text{veto}} = 30 \text{ GeV}$ yield $S/B \sim 1$ and $S/\sqrt{B} \sim 3\sigma$ with 30fb^{-1}

Butterworth et. al. (2008)



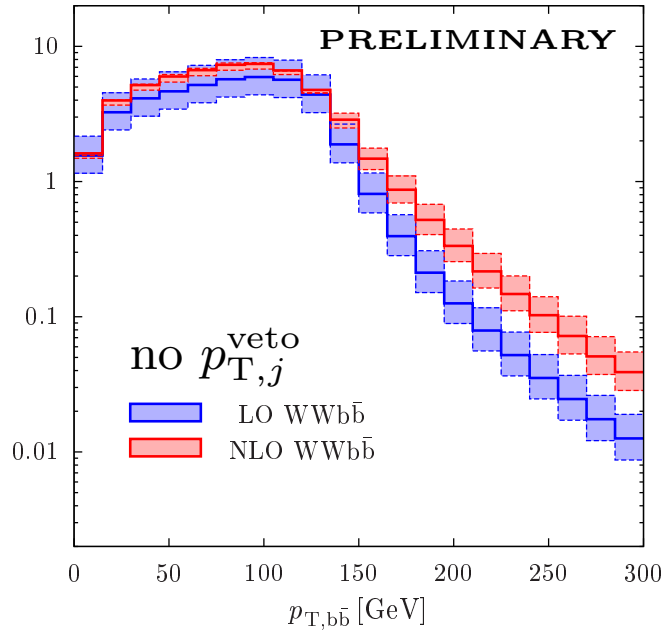
Corrections to dominant WWb \bar{b} background

- **0.4%** off-shell effects increase to $\gtrsim 30\%$
- **strong WWb \bar{b} j NLO emission very sensitive to jet veto**
- **NLO unstable for $p_{T,j}^{\text{veto}} < 60 \text{ GeV}$**

Full 2 → 4 NLO crucial to control WWb \bar{b} !

$$\frac{d\sigma}{dp_{T,b\bar{b}}} \left[\frac{\text{fb}}{\text{GeV}} \right] \quad pp \rightarrow W^+(\rightarrow \nu_e e^+) W^-(\rightarrow \mu^- \bar{\nu}_\mu) b\bar{b} + X$$

$\sqrt{s} = 7 \text{ TeV}$

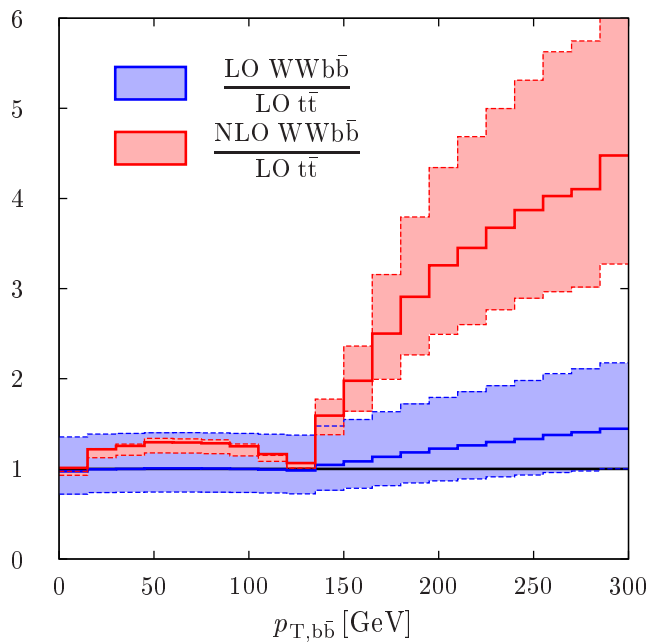


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Conclusions

NLO QCD calculation for $W^+W^-b\bar{b}$ production

- precise description of $t\bar{t}$ production and decay
- including off-shell effects, non-resonant backgrounds and interferences

Inclusive cross section at the Tevatron (LHC)

- moderate corrections $K=0.94$ (1.27) and stable NLO predictions ($\delta\sigma/\sigma \simeq 9\%$)
- quantitative assessment of finite-width effects $\lesssim \Gamma_t/m_t = 0.8\%$

NLO corrections to differential distributions

- rich and non-trivial kinematic dependence
- potentially large impact on acceptances and shape-dependent precision measurements (like m_t)
- large off-shell effects in $t\bar{t}$ background to $pp \rightarrow WH$ boosted-Higgs search

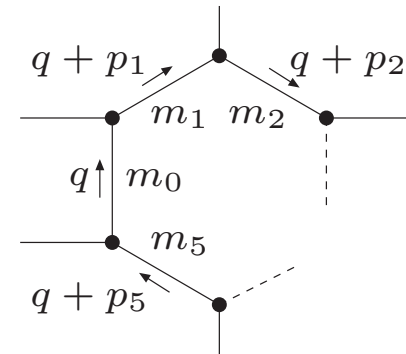
BACKUP SLIDES

Reduction of tensor integrals – *collection of* $e^+e^- \rightarrow 4f$ *methods* [Denner/Dittmaier '05]

(A) Space-time 4-dim ($N \geq 5$ prop.) simultaneous prop. & rank reduction

Melrose '65; Denner/Dittmaier '02&'05; Binoth et. al. '05

$$\begin{vmatrix} q^\mu & 2qp_1 & \dots & 2qp_5 \\ p_1^\mu & 2p_1p_1 & \dots & 2p_1p_5 \\ \vdots & \vdots & \ddots & \vdots \\ p_4^\mu & 2p_4p_1 & \dots & 2p_4p_5 \\ 0 & f_1 & \dots & f_5 \end{vmatrix} = \mathcal{O}(D - 4)$$



(B) Lorentz invariance ($N \leq 4$ prop.) reduction of rank (P)

Passarino/Veltman '79; Denner '93

$$2(D + P - N - 1) T_{00i_3 \dots i_P}^{(P)} = \sum_{k=1}^{N-1} f_k T_{ki_3 \dots i_P}^{(P-1)} + 2m_0^2 T_{i_3 \dots i_P}^{(P-2)} + \text{lower-point}$$

$$\sum_{n=1}^{N-1} Z_{mn} T_{ni_2 \dots i_P}^{(P)} = -2 \sum_{r=2}^P \delta_{mi_r} T_{00i_2 \dots \hat{i}_r \dots i_P}^{(P)} - f_m T_{i_2 \dots i_P}^{(P-1)} + \text{lower-point}$$

inversion of Gram matrix $Z_{mn} = 2p_m p_n$ **unstable** when $\det(Z) \rightarrow 0$

(C) General and robust solution of instability problems

iterative $\det(Z)$ -expansion (and various alternative methods)

$$\tilde{X}_{0j} T_{i_1 \dots i_P}^{(P)} = \det(Z) T_{ji_1 \dots i_P}^{(P+1)} + 2 \sum_{n=1}^{N-1} \tilde{Z}_{jn} \sum_{r=1}^P \delta_{ni_r} T_{00i_1 \dots \hat{i}_r \dots i_P}^{(P+1)} + \text{lower-point}$$

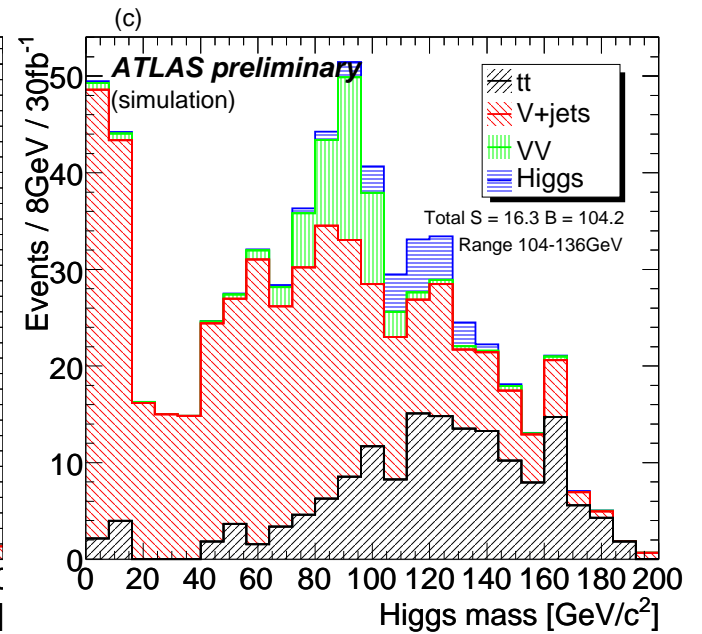
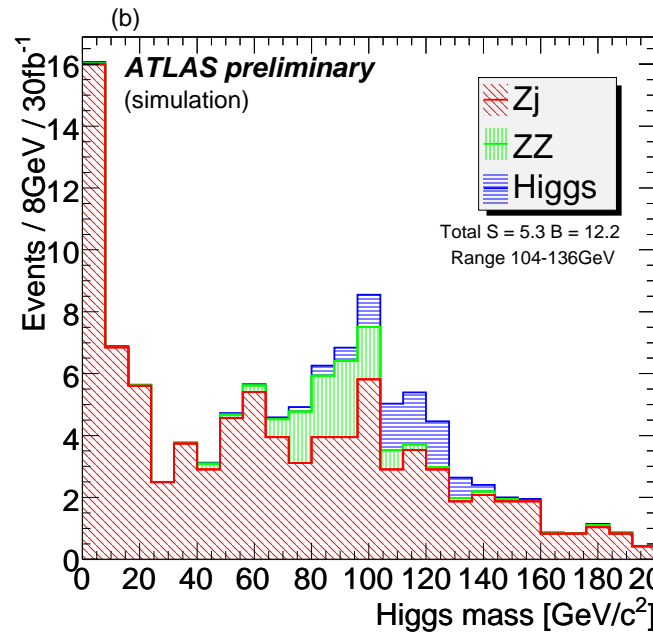
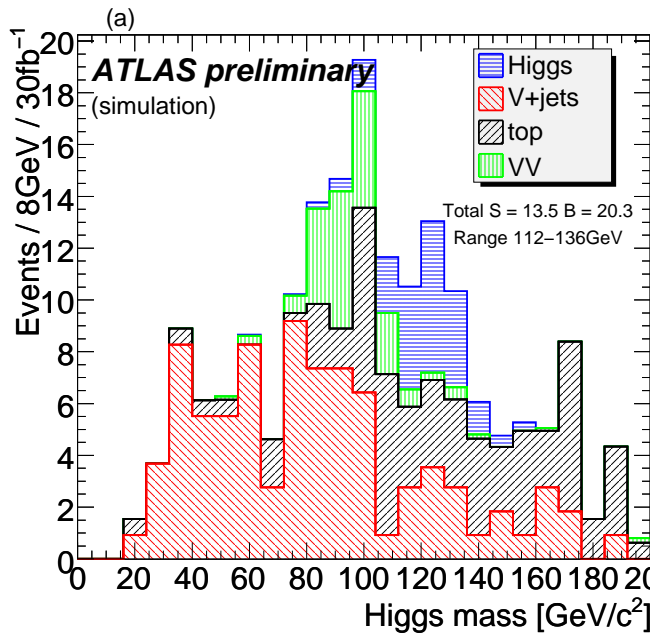
$$2\tilde{Z}_{kl} T_{00i_2 \dots i_P}^{(P+1)} = \left\{ -\det(Z) T_{kli_2 \dots i_P}^{(P+1)} + 2m_0 \tilde{Z}_{kl} T_{i_2 \dots i_P}^{(P-1)} + \sum_{n,m=1}^{N-1} \left[f_n f_m T_{i_2 \dots i_P}^{(P-1)} + 2 \sum_{r=2}^P (f_n \delta_{mi_r} + f_m \delta_{ni_r}) \right. \right. \\ \left. \left. \times T_{00i_2 \dots \hat{i}_r \dots i_P}^{(P)} + 4 \sum_{\substack{r,s=2 \\ r \neq s}}^P \delta_{ni_r} \delta_{mi_s} T_{0000i_2 \dots \hat{i}_r \dots \hat{i}_s \dots i_P}^{(P+1)} \right] \tilde{Z}_{(kn)(lm)} + \text{lower-point} \right\} (D+1+P-N + \sum_{r=2}^P \bar{\delta}_{i_r 0})^{-1}$$

Boosted-Higgs search in $pp \rightarrow VH(H \rightarrow b\bar{b})$

(a) $b\bar{b}l\nu$ channel

(b) $b\bar{b}l\bar{l}$ channel

(c) $b\bar{b}\nu\bar{\nu}$ channel



ATLAS note ATL-PHYS-PUB-2009-088 (cut-based analysis)

- $M_H = 120 \text{ GeV}$, $\sqrt{s} = 14 \text{ TeV}$, $L = 30\text{fb}^{-1}$
- $p_{b\bar{b}}^T, p_V^T > 200 \text{ GeV} \Rightarrow 5\%$ signal
- $p_{\text{jet veto}}^T = 20 \text{ GeV}$ in (a)
- $t\bar{t}$ simulated with HERWIG
- $(S/\sqrt{B})_a = 3.0$, $(S/B)_a \simeq 2/3$
- $(S/\sqrt{B})_{a+b+c} = 3.7$