

# XQCAT: Model independent analysis of heavy vector-like top partners

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# XQCAT in a nutshell

**XQCAT = eXtra Quark Combined Analysis Tool**

<https://launchpad.net/xqcat>

- 1) D. Barducci, A. Belyaev, M. Buchkremer, G. Cacciapaglia, A. Deandrea, S. De Curtis, J. Marrouche S. Moretti and **LP**, *Model Independent Framework for Analysis of Scenarios with Multiple Heavy Extra Quarks*, **arXiv:1405.0737 [hep-ph]** (submitted to JHEP)
- 2) D. Barducci, A. Belyaev, M. Buchkremer, J. Marrouche, S. Moretti and **LP**, *XQCAT: eXtra Quark Combined Analysis Tool*, **arXiv:1409.3116 [hep-ph]** (to be submitted to CPC)

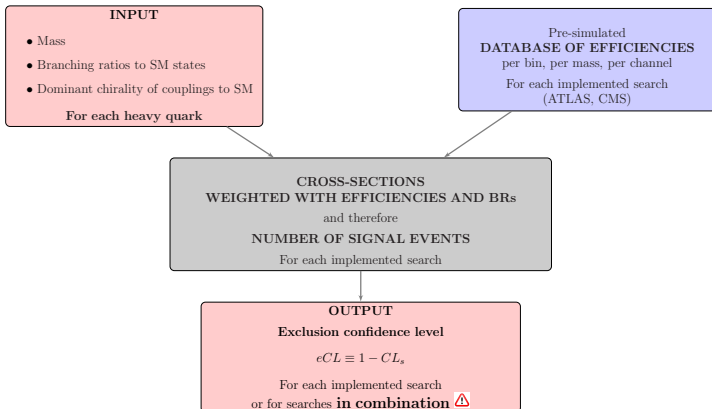
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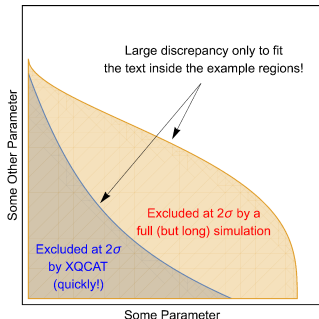
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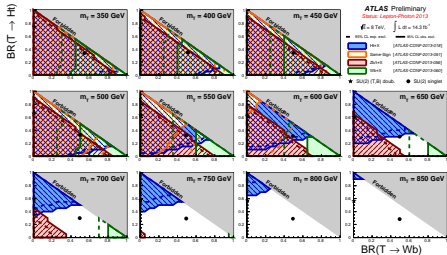
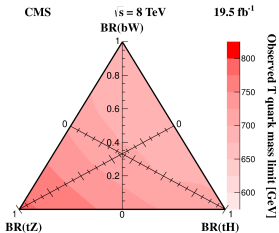
# Searches at the LHC

CMS ( $t'$ )

Phys. Lett. B 729 (2014) 149

ATLAS ( $t'$ )

ATLAS twiki: summary plots



Bounds from **pair production** in the 600-800 GeV range depending on the extra quark and on its decay channels

## Common assumptions

only one vector-like quark mixing with third generation only

Few exceptions to the common assumptions to date:

- ATLAS-CONF-2012-137: single production, mixing with first generation only (bounds above the TeV, but coupling-dependent)
- ATLAS-CONF-2014-036: pair+single production, mixing with third generation only (bounds still in the 600-800 GeV range)

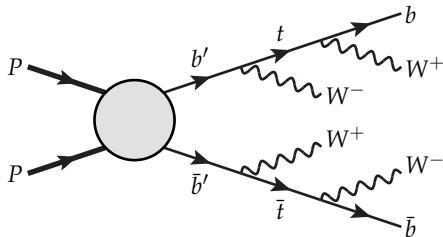
# XQCAT motivations

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New physics may be hidden where we haven't searched it yet:  
extra quarks may have different **mixing patterns**

# Allowing general mixing

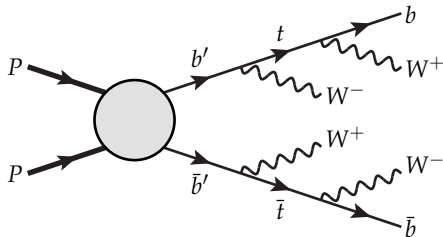
$b'$  pair production



Searches in the  
same-sign dilepton channel  
with one or more b-jets

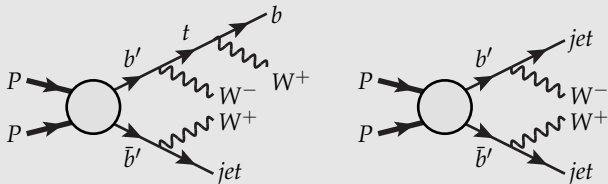
# Allowing general mixing

$b'$  pair production



Searches in the same-sign dilepton channel with one or more b-jets

If the  $b'$  decays both into  $Wt$  and  $Wq$



There can be less events in the same-sign dilepton plus b-jets channel !

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If extra quarks interact also (or only) with light generations  
can I derive bounds on their masses from experimental data?



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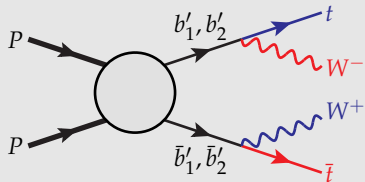
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Theoretical models predict in general **multiple new quarks**, which may have similar masses, but different charges and different mixing properties

# Allowing more than one VLQ

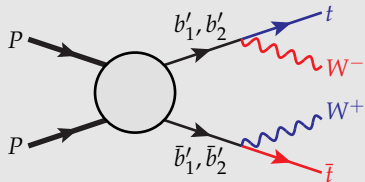
Case 1: two extra quarks of the same species



Different kinematics  
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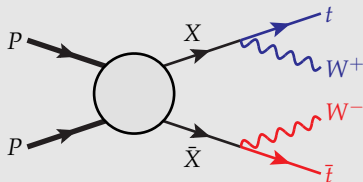
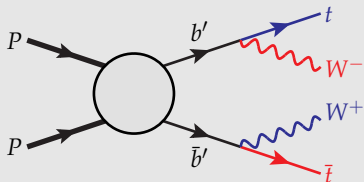
# Allowing more than one VLQ

Case 1: two extra quarks of the same species



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Case 2: two extra quarks of different species



A given final state can be fed by different channels!  
(with different kinematics)

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How can I estimate the excluded regions of parameter space of a model which contains more than one extra quark?

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**Straightforward answer to both questions**

Perform a complete simulation for each scenario that we want to test  
and apply the selection and kinematical cuts of the experimental searches

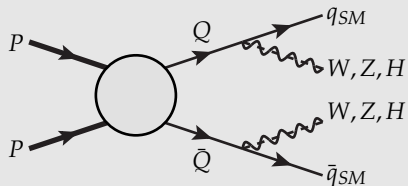
Time consuming  $\times$

Model dependent  $\times$

Not efficient for scans  $\times$

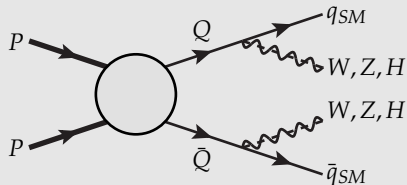
# XQCAT approach

QCD pair production + decay



# XQCAT approach

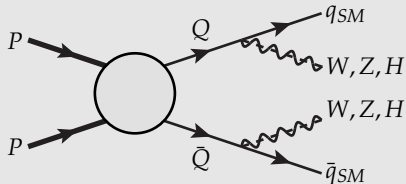
## QCD pair production + decay



- The production process depends only on the **mass** of the extra quark

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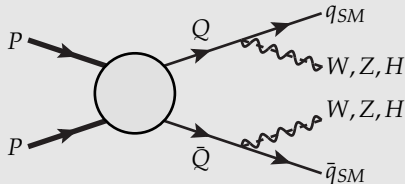


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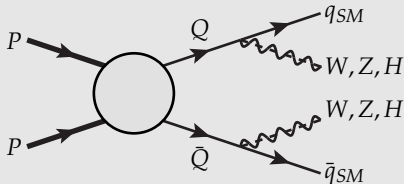


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- If one determines the **efficiencies** associated to specific **selection and kinematical cuts** for all decay channels the number of **signal events** for any spectrum can be derived through **simple algebra!**

$$N_S = L_{exp} \sum_Q \sigma_{QCD}(m_Q) \sum_{ij} BR_i(Q) BR_j(\bar{Q}) \epsilon_{ij}$$

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## QCD pair production + decay



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- Knowing (from experiment!) the **background and observed events** it is possible to determine the likelihood of the signal, and therefore its **exclusion confidence level**

$$eCL \equiv 1 - CL_s$$

## Counting the final states

$T$  pair production  $\longrightarrow$  6 possible decays:  $W^+j$   $W^+b$   $Zj$   $Zt$   $Hj$   $Ht$

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(only) 36 possible combinations of decays into SM particles!  
each one with its peculiar kinematics

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$B$  pair production  $\longrightarrow$  6 possible decays:  $W^-j$   $W^-t$   $Zj$   $Zb$   $Hj$   $Hb$

36 possible combinations of decays into SM particles

$X$  pair production  $\longrightarrow$   $W^+j$   $W^+t$

4 combinations

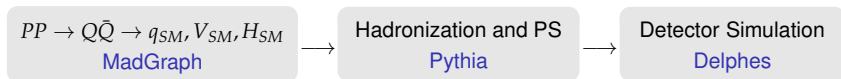
$Y$  pair production  $\longrightarrow$   $W^-j$   $W^-b$

4 combinations

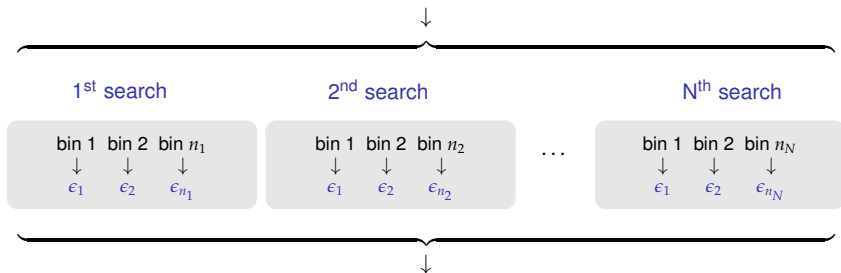
There are 80 combinations of decays of (pair produced) VLQs into SM!  
each one with its kinematic properties!

# Generation of the efficiency database

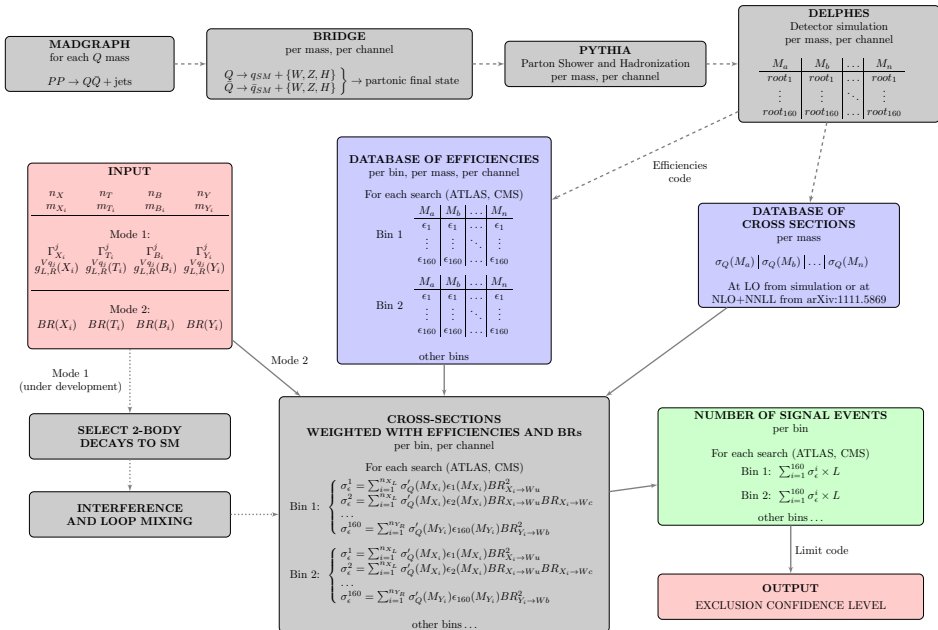
## Numerical Simulation



## Signal



## Database of Efficiencies



# First results of XQCAT

## Implemented searches (only CMS temporarily)

- Direct search of vector-like quarks

B2G-12-015 ( $t' \rightarrow Wb, Zt, Ht$  @ 8 TeV)

See Gerrit's talk for more details about this search

- SUSY searches (in combination!)

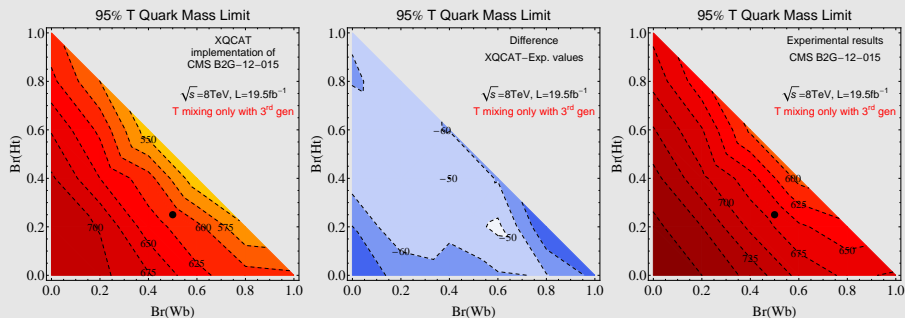
$\alpha_T$ 7 and 8 TeV	$L_P$ (monolepton) 7 TeV	SS dileptons 7 and 8 TeV	OS dileptons 7 TeV
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All these searches are SUSY-inspired, but it is ok: we only care about final states!



# First results of XQCAT: 1 T singlet

Validation plots: T mixing only with 3<sup>rd</sup> generation



We reproduce CMS 95% CL bounds within 50-60 GeV in the whole BR range

The implementation of SUSY searches **(including their combination!)** has been validated in

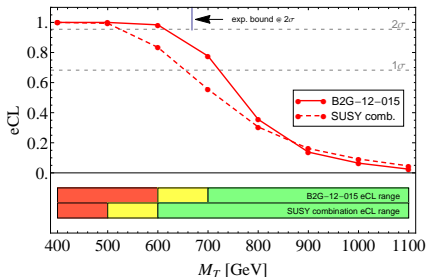
O. Buchmuller and J. Marrouche, *Int.J.Mod.Phys. A29* (2014) 1450032, arXiv:1304.2185

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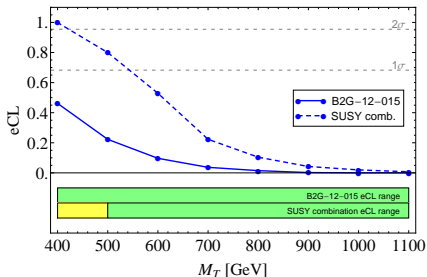
but with different mixing structure

$$BR(Zq) = BR(Hq) = 25\% \quad BR(Wq) = 50\%$$

T singlet mixing with 3<sup>rd</sup> generation

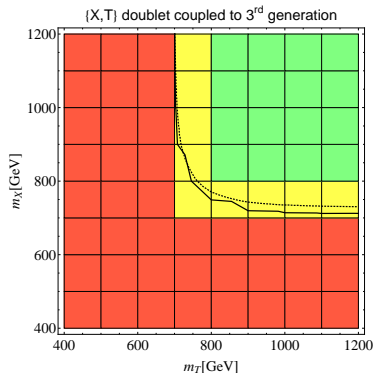
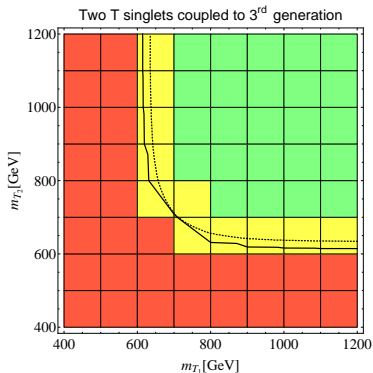


T singlet mixing with 1<sup>st</sup> generation



- 1 Stronger bounds** when mixing with 3<sup>rd</sup> generation and in the ballpark of those obtained with **direct search**! N.B. We are not using the same analysis techniques (e.g. no shape analysis), so we cannot perfectly reproduce experimental results!!
- 2** Assuming **mixing with light generation**, SUSY searches are **more sensitive** than direct searches (on a cut-and-count basis)! This gap will be closed once **new experimental direct searches** of VLQs exploring these scenarios will be available (with more refined analyses)!

# First results of XQCAT: multiple quarks



Bounds obtained using the direct VLQ search B2G-12-015

## General conclusions

- 1 The presence of multiple extra quarks can give heavier mass bounds
- 2 Dedicated searches for a given quark species may constrain other ones

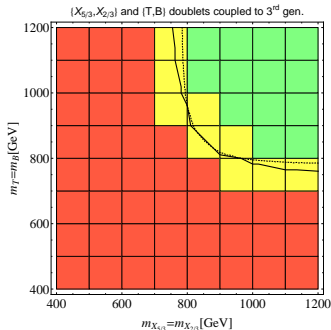
# First results of XQCAT: multiple quarks

Considering physically motivated scenarios

Composite (pseudo) Goldstone boson Higgs model

De Simone et al., *A first top partner hunters guide*, arXiv:1211.5663 [hep-ph]

$$\text{SO}(4) \text{ quadruplet} \quad \begin{pmatrix} X_{5/3} & t' \\ X_{2/3} & b' \end{pmatrix} \quad \begin{cases} BR(X_{5/3} \rightarrow Wb) = BR(b' \rightarrow Wt) = 100\% \\ BR(X_{2/3} \rightarrow Zt) = BR(X_{2/3} \rightarrow Ht) = 50\% \\ BR(t' \rightarrow Zt) = BR(t' \rightarrow Ht) = 50\% \end{cases}$$



## General conclusions

- 1 The presence of multiple extra quarks raises the bounds to the 900-1000 GeV range
- 2 Models with extra content can be more constrained

Bounds obtained using the direct VLQ search B2G-12-015

# First results of XQCAT: multiple quarks

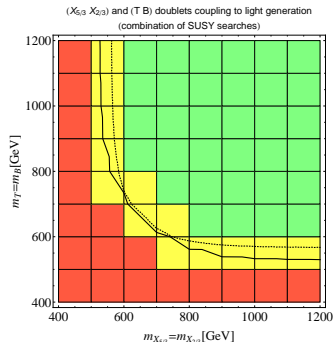
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But now let's assume mixing only with light generation!

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## General conclusions

- 1 Models with multiple extra quarks but non-standard mixing patterns can already be constrained even if no dedicated searches are available
- 2 Reinterpretation of searches not designed for extra quarks can be a powerful instrument to help designing future searches

Bounds obtained using a combination of SUSY searches

# A digression on interpolation

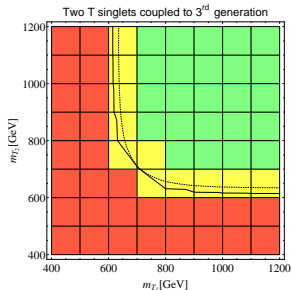
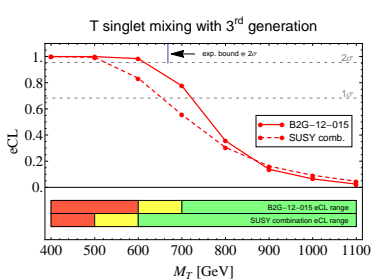
- The simulation has **discrete steps**: the mass of the extra quarks runs from 400 GeV to 2 TeV **steps of 100 GeV**
- **Information** on the efficiencies for points not simulated is **missing**
- A generic spectrum contains extra quarks with values of masses that **have not been simulated**

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How does XQCAT interpolate?

# A digression on interpolation

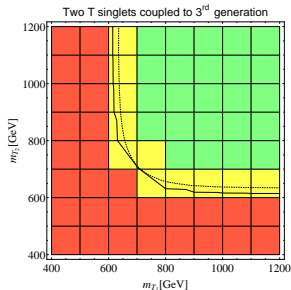
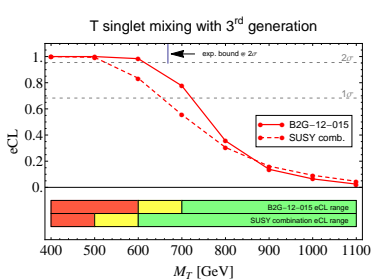


- Interpolation of efficiencies:** run XQCAT for the given spectrum, with the exact values of the extra quark masses. The code interpolates between the efficiencies of the nearest simulated masses. **Quick but fluctuations in the efficiencies have to be small between the simulated values!**

$$\epsilon(k, m_Q) = \epsilon(k, m^\downarrow) \frac{m^\uparrow - m_Q}{m^\uparrow - m^\downarrow} + \epsilon(k, m^\uparrow) \frac{m_Q - m^\downarrow}{m^\uparrow - m^\downarrow}$$



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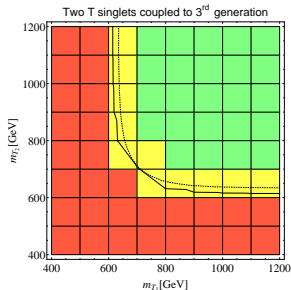
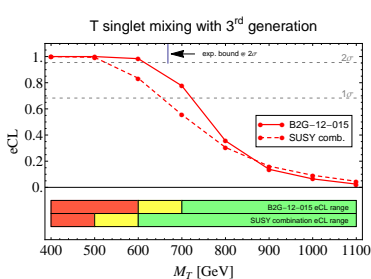


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- Determination of a range for the exclusion confidence levels:** for a given spectrum with N extra quark, compute the eCLs in all the vertices of the N-dimensional cube, corresponding to the closest simulated masses. **Longer, but the most conservative approach!**

# A digression on interpolation



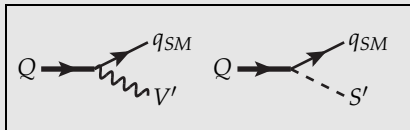
- 1 **Interpolation of efficiencies:** run XQCAT for the given spectrum, with the exact values of the extra quark masses. The code interpolates between the efficiencies of the nearest simulated masses. **Quick but fluctuations in the efficiencies have to be small between the simulated values!**

$$\epsilon(k, m_Q) = \epsilon(k, m^\downarrow) \frac{m^\uparrow - m_Q}{m^\uparrow - m^\downarrow} + \epsilon(k, m^\uparrow) \frac{m_Q - m^\downarrow}{m^\uparrow - m^\downarrow}$$

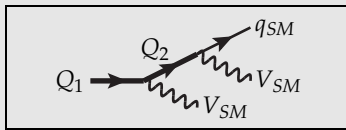
- 2 **Determination of a range for the exclusion confidence levels:** for a given spectrum with N extra quark, compute the eCLs in all the vertices of the N-dimensional cube, corresponding to the closest simulated masses. **Longer, but the most conservative approach!**
- 3 **Interpolation of the exclusion confidence levels:** the same as before, but the eCL of the test-point is the interpolation of the eCLs in the vertices of the N-dimensional cube. **Longer, and fluctuations in the efficiencies have to be small!**

# Remarks and subtleties

## Chain decays



Other new sectors besides the VLQs



Chain decays between VLQs

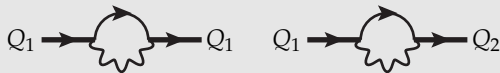
## Interferences

$$\mathcal{A}_1 = \text{Diagram with } Q_1, \bar{Q}_1, q_{SM}, \bar{q}_{SM}, V_{SM}$$

$$\mathcal{A}_2 = \text{Diagram with } Q_2, \bar{Q}_2, q_{SM}, \bar{q}_{SM}, V_{SM}$$

$$\sigma \propto |\mathcal{A}_1|^2 + |\mathcal{A}_2|^2 + 2\text{Re}[\mathcal{A}_1 \mathcal{A}_2^*]$$

## Mixing at loop level



# Conclusions and Outlook

- **XQCAT** (eXtra Quark Combined Analysis Tool) is a tool aimed to determine **exclusion Confidence Levels** for scenarios with the presence of **one or multiple extra extra quarks** which interact through Yukawa couplings with **any** of the Standard Model quarks.
- The code exploits a **database of efficiencies** for pre-simulated processes of QCD pair production and decays of the extra quarks.

<https://launchpad.net/xqcat>

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- The code exploits a **database of efficiencies** for pre-simulated processes of QCD pair production and decays of the extra quarks.

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## What's next (in pseudo-random order)

- Upgrade to **Delphes 3** and implementation of **further experimental searches**
- Inclusion of decays into **Dark Matter** particles
- Inclusion of **interference and loop effects in pair production**
- Inclusion of **single production** processes in the simulation (see Mathieu's talk)
  - check if couplings comply with **flavour bounds, EWPT...**
  - inclusion of **interference and loop effects in single production**
- (Possibly) Inclusion of **chain decays** between VLQs
- Generalisation of the procedure for **different states** (extra vectors, extra scalars, ...)





# Backup



# Mixing between VL and SM quarks

## Flavour and mass eigenstates

$$\begin{pmatrix} \tilde{u} \\ \tilde{c} \\ \tilde{t} \\ U \end{pmatrix}_{L,R} = V_{L,R}^u \begin{pmatrix} u \\ c \\ t \\ t' \end{pmatrix} \quad \text{and} \quad \begin{pmatrix} \tilde{d} \\ \tilde{s} \\ \tilde{b} \\ D \end{pmatrix}_{L,R} = V_{L,R}^d \begin{pmatrix} d \\ s \\ b \\ b' \end{pmatrix}$$

The exotics  $X_{5/3}$  and  $Y_{-4/3}$  do not mix  $\rightarrow$  no distinction between flavour and mass eigenstates

$$\mathcal{L}_{y+M} = (\bar{\tilde{u}} \bar{\tilde{c}} \bar{\tilde{t}} \bar{U})_L \mathcal{M}_u \begin{pmatrix} \tilde{u} \\ \tilde{c} \\ \tilde{t} \\ U \end{pmatrix}_R + (\bar{\tilde{d}} \bar{\tilde{s}} \bar{\tilde{b}} \bar{D})_L \mathcal{M}_d \begin{pmatrix} \tilde{d} \\ \tilde{s} \\ \tilde{b} \\ D \end{pmatrix}_R + h.c.$$

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## Mixing matrices depend on representations

- Singlets and triplets:

$$\mathcal{M}_u = \begin{pmatrix} \tilde{m}_u & & x_1 \\ & \tilde{m}_c & x_2 \\ & & \tilde{m}_t & x_3 \\ & & & M \end{pmatrix} \quad \mathcal{M}_d = \left( \frac{\tilde{V}_L^{\text{CKM}} \begin{pmatrix} \tilde{m}_d & & \\ & \tilde{m}_s & \\ & & \tilde{m}_b \end{pmatrix} \tilde{V}_R^{\text{CKM}}}{M} \begin{array}{c} x_1 \\ x_2 \\ x_3 \\ M \end{array} \right)$$

- Doubles:  $\mathcal{M}_{u,d}^{4I} \leftrightarrow \mathcal{M}_{u,d}^{I4}$

# Mixing matrices

$$\mathcal{L}_m = (\bar{u} \bar{c} \bar{t} \bar{t}')_L (V_L^u)^\dagger \mathcal{M}_u (V_R^u) \begin{pmatrix} u \\ c \\ t \\ t' \end{pmatrix}_R + (\bar{d} \bar{s} \bar{b} \bar{b}')_L (V_L^d)^\dagger \mathcal{M}_d (V_R^d) \begin{pmatrix} d \\ s \\ b \\ b' \end{pmatrix}_R + h.c.$$

$$(V_L^u)^\dagger \mathcal{M}_u (V_R^u) = \text{diag} (m_u, m_c, m_t, m_{t'}) \quad (V_L^d)^\dagger \mathcal{M}_d (V_R^d) = \text{diag} (m_d, m_s, m_b, m_{b'})$$

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Mixing in left- and right-handed sectors behave differently

$$\begin{cases} (V_L^q)^\dagger (\mathcal{M} \mathcal{M}^\dagger) (V_L^q) = \text{diag} \\ (V_R^q)^\dagger (\mathcal{M}^\dagger \mathcal{M}) (V_R^q) = \text{diag} \end{cases} \quad q_{L,R}^I \xrightarrow[V_{L,R}^q]{\times} q_{L,R}^J$$

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Singlets and triplets (case of up-type quarks)

$$V_L^u \implies \mathcal{M}_u \cdot \mathcal{M}_u^\dagger = \begin{pmatrix} \tilde{m}_u^2 + |x_1|^2 & x_1^* x_2 & x_1^* x_3 & x_1^* M \\ x_2^* x_1 & \tilde{m}_c^2 + |x_2|^2 & x_2^* x_3 & x_2^* M \\ x_3^* x_1 & x_3^* x_2 & \tilde{m}_t^2 + x_3^2 & x_3^* M \\ x_1 M & x_2 M & x_3 M & M^2 \end{pmatrix} \quad \begin{array}{l} \text{mixing in the left sector} \\ \text{present also for } \tilde{m}_q \rightarrow 0 \\ \hline \text{flavour constraints for } q_L \\ \text{are relevant} \end{array}$$

$$V_R^u \implies \mathcal{M}_u^\dagger \cdot \mathcal{M}_u = \begin{pmatrix} \tilde{m}_u^2 & & & \\ & \tilde{m}_c^2 & & \\ & & \tilde{m}_t^2 & \\ x_1 \tilde{m}_u & x_2 \tilde{m}_c & x_3 \tilde{m}_t & \sum_{i=1}^3 |x_i|^2 + M^2 \end{pmatrix} \quad \begin{array}{l} m_q \propto \tilde{m}_q \\ \hline \text{mixing is suppressed} \\ \text{by quark masses} \end{array}$$

**Doublets:** other way round

# Couplings

With  $Z$

$$\mathcal{L}_Z = \frac{g}{c_W} (\bar{q}_1 \bar{q}_2 \bar{q}_3 \bar{q}'_1)_L (V_L^q)^\dagger \left[ (T_3^q - Q^q s_w^2) \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} + (T_3^{q'} - T_3^q) \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \right] \gamma^\mu (V_L^q) \begin{pmatrix} q_1 \\ q_2 \\ q_3 \\ q' \end{pmatrix}_L Z_\mu$$

$$+ \frac{g}{c_W} (\bar{q}_1 \bar{q}_2 \bar{q}_3 \bar{q}'_1)_R (V_R^q)^\dagger \left[ (-Q^q s_w^2) \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} + T_3^{q'} \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \right] \gamma^\mu (V_R^q) \begin{pmatrix} q_1 \\ q_2 \\ q_3 \\ q' \end{pmatrix}_R Z_\mu$$

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$$\mathcal{L}_Z = \frac{g}{c_W} (\bar{q}_1 \bar{q}_2 \bar{q}_3 \bar{q}'_1)_L (V_L^q)^\dagger \left[ (T_3^q - Q^q s_w^2) \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} + (T_3^{q'} - T_3^q) \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \right] \gamma^\mu (V_L^q) \begin{pmatrix} q_1 \\ q_2 \\ q_3 \\ q' \end{pmatrix}_L Z_\mu$$

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FCNC, are induced by the mixing with vector-like quarks!

$$g_{ZL}^{JJ} = \frac{g}{c_W} (T_3^q - Q^q s_w^2) \delta^{JJ} + \frac{g}{c_W} (T_3^{q'} - T_3^q) (V_L^*)^{q'1} V_L^{q'1}$$

$$g_{ZR}^{JJ} = \frac{g}{c_W} (-Q^q s_w^2) \delta^{JJ} + \frac{g}{c_W} T_3^{q'} (V_R^*)^{q'1} V_R^{q'1}$$

The diagram shows two equivalent representations of a process. On the left, a \$u\$ quark line enters from the left, and a \$t'\$ quark line enters from the bottom. A \$Z\$ boson (represented by a wavy line) is exchanged between them. On the right, a \$u\$ quark line enters from the left, and a \$c\$ quark line enters from the bottom. They meet at a circular vertex, representing a contact interaction. The diagram is equated to the contact interaction, which is proportional to \$(V\_{L,R}^\*)^{t'u} V\_{L,R}^{t'c}\$.

# Couplings

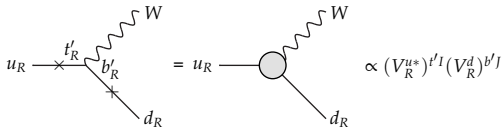
With  $W^\pm$

$$\begin{aligned} \mathcal{L}_{W^\pm} = & \frac{g}{\sqrt{2}} (\bar{u} \bar{c} \bar{t} | \bar{t}')_L (V_L^u)^\dagger \left( \begin{array}{c|c} \tilde{V}_L^{CKM} & \\ \hline & 1 \end{array} \right) \gamma^\mu V_L^d \begin{pmatrix} d \\ s \\ b \\ b' \end{pmatrix}_L W_\mu^+ \\ & + \frac{g}{\sqrt{2}} (\bar{u} \bar{c} \bar{t} | \bar{t}')_R (V_R^u)^\dagger \left( \begin{array}{c|c} 0 & \\ \hline & 1 \end{array} \right) \gamma^\mu V_R^d \begin{pmatrix} d \\ s \\ b \\ b' \end{pmatrix}_R W_\mu^+ + h.c. \end{aligned}$$

CKM matrices for left and right handed sector:

$$g_{WL} = \frac{g}{\sqrt{2}} (V_L^u)^\dagger \left( \begin{array}{c|c} \tilde{V}_{CKM} & \\ \hline & 1 \end{array} \right) V_L^d \equiv \frac{g}{\sqrt{2}} V_L^{CKM} \quad g_{WR} = \frac{g}{\sqrt{2}} (V_R^u)^\dagger \left( \begin{array}{c|c} 0 & \\ \hline & 1 \end{array} \right) V_R^d \equiv \frac{g}{\sqrt{2}} V_R^{CKM}$$

If BOTH  $t'$  and  $b'$  are present  $\rightarrow$  CC between right-handed quarks





# Couplings

## With Higgs

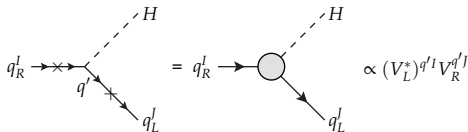
$$\mathcal{L}_h = \frac{1}{v} (\bar{q}_1 \bar{q}_2 \bar{q}_3 \bar{q}'_1)_L (V_L^q)^\dagger \left[ \mathcal{M}_q - M \begin{pmatrix} 0 & & \\ 0 & & \\ & & 1 \end{pmatrix} \right] (V_R^q) \begin{pmatrix} q_1 \\ q_2 \\ q_3 \\ q' \end{pmatrix}_R h + h.c.$$

The coupling is:

$$C = \frac{1}{v} (V_L^q)^\dagger \mathcal{M}_q (V_R^q) - \frac{M}{v} (V_L^q)^\dagger \begin{pmatrix} 0 & & \\ 0 & & \\ & & 1 \end{pmatrix} (V_R^q) = \frac{1}{v} \begin{pmatrix} m_{q1} & & \\ & m_{q2} & \\ & & m_{q3} & \\ & & & m_{q'} \end{pmatrix} - \frac{M}{v} (V_L^q)^\dagger \begin{pmatrix} 0 & & \\ 0 & & \\ & & 1 \end{pmatrix} (V_R^q)$$

FCNC induced by vector-like quarks are present in the Higgs sector too!

$$C^{IJ} = \frac{1}{v} m_I \delta^{IJ} - \frac{M}{v} (V_L^*)^{q'I} V_R^{q'J}$$



# The exclusion confidence level

Observation

310 events

Background

300 events

# The exclusion confidence level

Observation

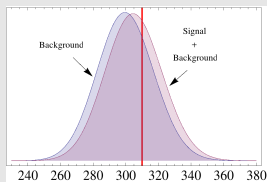
310 events

Background

300 events

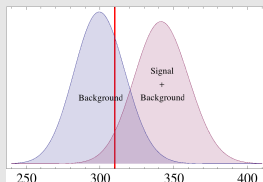
Signal

Case I: 5 events



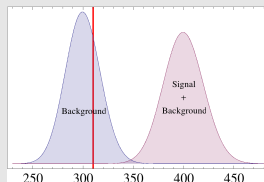
Exclusion CL  $\simeq 14\%$

Case II: 42 events



Exclusion CL  $\simeq 94\%$

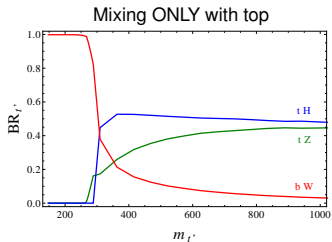
Case III: 100 events



Exclusion CL  $\simeq 99.99\%$

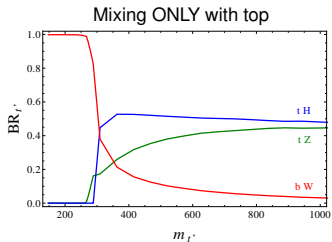
$$\text{Exclusion CL} \equiv 1 - \text{CL}_S = 1 - \frac{\text{CL}(s+b)}{\text{CL}(b)}$$

# Decays of $t'$



Equivalence theorem at large masses:  
 $BR(qH) \simeq BR(qZ)$

# Decays of $t'$



Equivalence theorem at large masses:  
 $BR(qH) \simeq BR(qZ)$

Decay to lighter generations can be sizable even with small Yukawas!

