

CUPS – CMS Upgrade School



Hands-on Session

DELPHES:



A modular framework for fast
simulation of a
generic collider experiment

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Outline

- ♦ Introduction to Delphes
 - ♦ What is Delphes and why do we use it?
 - ♦ Structure of the simulated detector
 - ♦ Object reconstruction
 - ♦ High-level corrections
 - ♦ Validation
 - ♦ Delphes for CMS
 - ♦ To sum up
- ♦ Analysis $H \rightarrow ZZ^* \rightarrow 4\mu$ with Delphes
- ♦ Hands-on exercise

Introduction to Delphes

Input: output of event generators (MadGraph, PYTHIA, HERWIG, ...)

DELPHES

C++ modular framework which performs a **fast** and **parametrized** multipurpose detector response simulation

- Tracking system embedded in a magnetic field
- Electromagnetic and hadronic calorimeters
- Muon identification system

Reconstruction of the physics objects (γ , $e^\pm$, $\mu^\pm$, $\tau^\pm$, jets, b-jets, MET, ...)

Output: ROOT ntuple (generated and reconstructed objects)

Introduction to Delphes

What is Delphes and why do we use it?

Very high energy particle collisions produce a large variety of final states



Multipurpose detectors are **complex** and **sophisticated**

To tune and optimize specific analysis, a **full detector simulation** is requested, with a high level of accuracy:

GEANT package, dedicated routines, complex algorithms



Large scale **computing resources** and high level **expertise**

Introduction to Delphes

What is Delphes and why do we use it?

Phenomenological studies, comparison between different upgraded or aged scenarios, big background samples production require:
less precision but a **FASTER** and **SIMPLER** tool



DELPHES

Limitations:

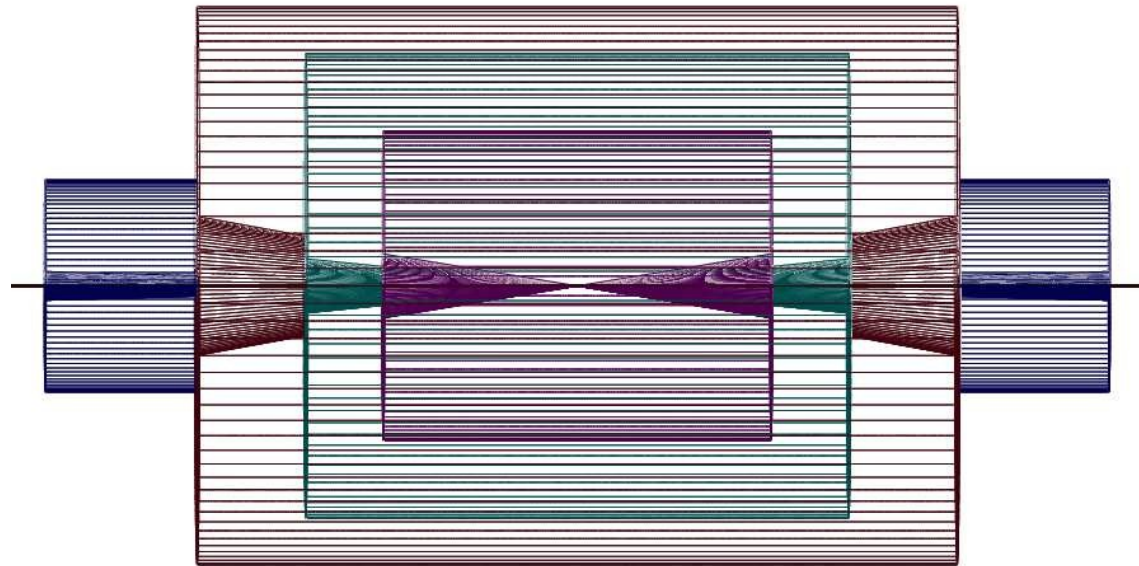
- Detector geometry is uniform, symmetric around the beam axis, without cracks or dead material
- Secondary interactions, multiple scattering, photon conversion and bremsstrahlung are not simulated

Introduction to Delphes

Structure of the simulated detector

The overall layout of a multipurpose detector is simulated thanks to a parametrization (in a DataCard^{*}):

- Central tracking system (**TRACKER**)
- Electromagnetic and hadronic calorimeters (**ECAL** and **HCAL**)
- Muon system (**MUON**)
- Two forward calorimeters (**FCAL**)



^{*} = I will talk about this in more detail later!

Introduction to Delphes

Structure of the simulated detector

- ♦ Central tracking system

Propagation of the long-lived particles in a uniform axial magnetic field along the beam direction



Neutral particles

Straight trajectory

Charged particles

Helicoidal trajectory

User-defined probability to
be reconstructed as tracks

- ♦ Particles that originate outside the tracker volume are neglected
- ♦ NO smearing applied on track parameters (except for p_T)

Introduction to Delphes

Structure of the simulated detector

- Electromagnetic and hadronic calorimeters



ECAL

Measures the energy deposit of electrons and photons

- $f_{\text{ECAL}}(e^\pm, \gamma) = 1$
- $f_{\text{ECAL}}(h) = 0$
- $f_{\text{ECAL}}(K, \Lambda) = 0.3$
- $f_{\text{ECAL}}(\mu^\pm, \nu) = 0$

HCAL

Measures the energy deposit of charged and neutral hadrons

- $f_{\text{HCAL}}(e^\pm, \gamma) = 0$
- $f_{\text{HCAL}}(h) = 1$
- $f_{\text{HCAL}}(K, \Lambda) = 0.7$
- $f_{\text{HCAL}}(\mu^\pm, \nu) = 0$

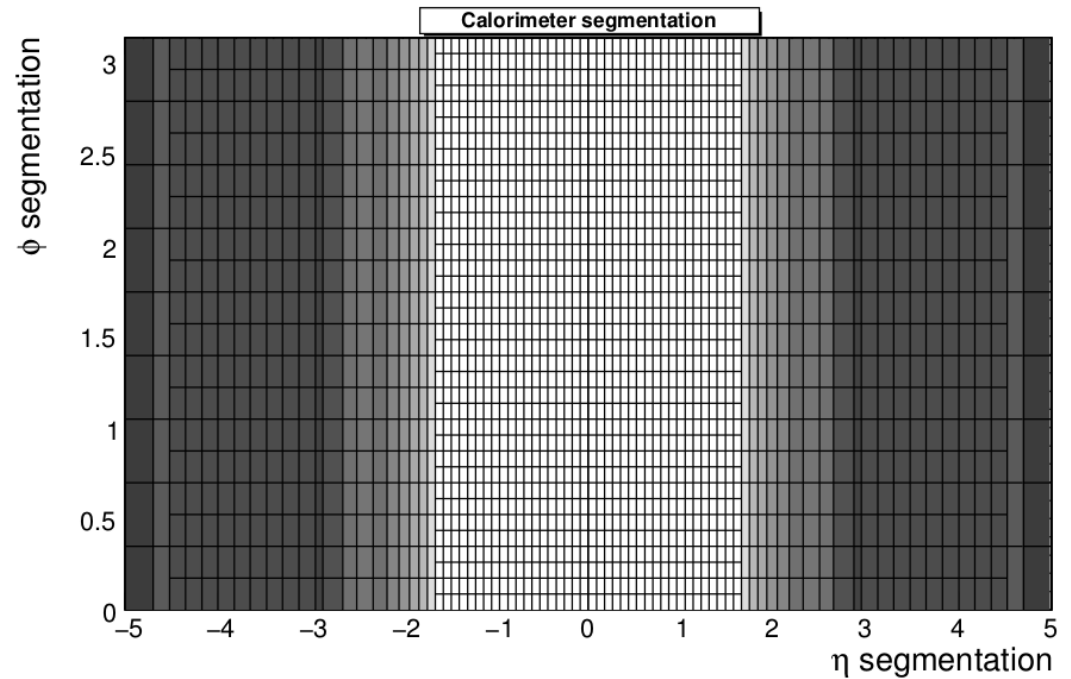
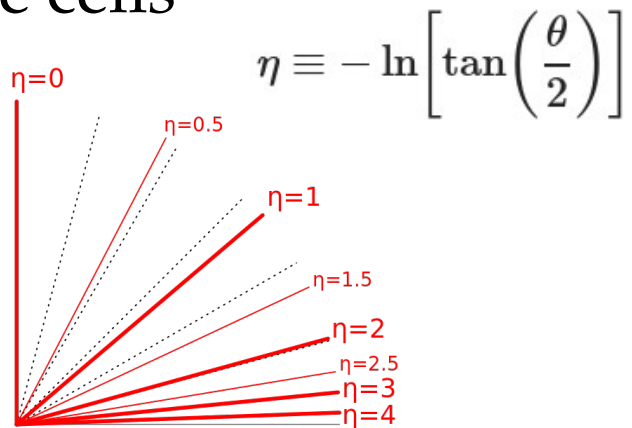
Default values, user can modify them

Introduction to Delphes

Structure of the simulated detector

- ♦ Electromagnetic and hadronic calorimeters

Segmented in the (η, ϕ) plane in user-defined size cells



- ♦ Same granularity for ECAL and HCAL
- ♦ Uniform segmentation in ϕ
- ♦ Response simulated through a Gaussian smearing of the cell energy

Introduction to Delphes

Structure of the simulated detector

- ♦ Energy-Flow

Based on Tracker and Calorimeter information with the **assumption** that the momentum resolution of the Tracker is better than the energy resolution of the Calorimeter

The algorithm counts E_{ECAL} , E_{HCAL} , $E_{\text{ECAL,trck}}$, $E_{\text{HCAL,trck}}$ and produces:

- ♦ Energy-Flow tracks from reconstructed tracks: $\text{EF_}E_{\text{Track}}$
- ♦ If $\text{EF_}E_{\text{Tower}} > 0 \implies \text{EF_}E_{\text{Tower}} = \max(0, \Delta_{\text{ECAL}}) + \max(0, \Delta_{\text{HCAL}})$

Where $\Delta_{\text{ECAL}} = E_{\text{ECAL}} - E_{\text{ECAL,trck}}$ and $\Delta_{\text{HCAL}} = E_{\text{HCAL}} - E_{\text{HCAL,trck}}$

Particle-flow track $\longrightarrow$ Charged particles, good Resolution

Particle-flow tower $\longrightarrow$ Charged+Neutral particles, lower Resolution

Introduction to Delphes

Object reconstruction

- $e^\pm, \mu^\pm, \gamma$ $\longrightarrow$ quite easy to reconstruct
- Jets, Missing Transverse Energy $\longrightarrow$ difficult to reconstruct

Accessible in the output:

- 4-momentum and related quantities
- Additional specific properties (e.g. Isolation)

- MET
$$\vec{E}_T^{miss} = - \sum_i \vec{p}_T(i)$$

From different input collections: calorimeter, energy-flow, generator-level

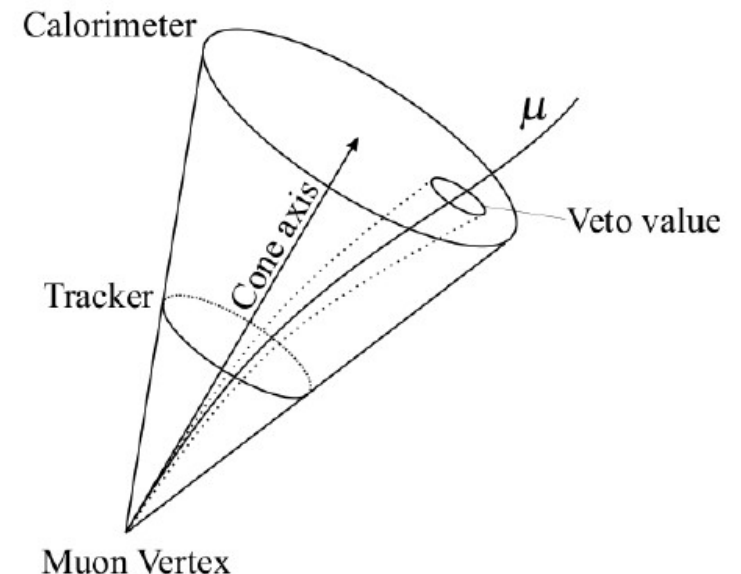
Introduction to Delphes

Object reconstruction

- ♦ Photons and charged leptons (NO τ !)

Only the final-state particles identified via generator-data and passing cuts (tracker acceptance and p_T threshold)

- ♦ Reconstructed with a user-defined Efficiency: $f(\eta, p_T)$
- ♦ NO FAKE candidates (they can be added in the analysis)



Isolation:

$e^\pm, \mu^\pm$ isolated if $I < I_{min}$ within a small cone of radius ΔR in the (η, ϕ) plane

Introduction to Delphes

Object reconstruction

- ♦ Jets

Final-states dominated by Jets: need an accurate reconstruction

It is possible to produce Jets starting from different input collections:

- ♦ Generated Jets: clustered from generator-level particles after parton-shower and hadronization
- ♦ Calorimeter Jets: use calorimeter towers
- ♦ Energy-flow Jets: result of clustering energy-flow tracks and towers

Many clustering algorithms (Longitudinally invariant k_t jet, Cambridge/Aachen jet, Anti k_t jet, CDF MidPoint, ...)

Introduction to Delphes

Object reconstruction

b-jets and τ -jets

Parametric approach:

A jet is a potential b/ τ jet if a generated b/ τ is found within some distance:

$$\Delta R = \sqrt{(\eta^{jet} - \eta^{b,\tau})^2 + (\phi^{jet} - \phi^{b,\tau})^2}$$

along the jet axis

User-defined efficiency to identify that candidate as a real b/ τ jet intervenes (Mistagging efficiency can be specified)

Introduction to Delphes

High-level corrections

Resulting collections not yet ready for the analysis

- ♦ Jet Energy scale correction

Only for Jets (not for non-composite objects) $\rightarrow f(\eta_{\text{RECO jet}}, p_{\text{T RECO jet}})$

Discrepancy between average momenta of reconstructed objects and generator-level objects

- ♦ Pile-Up Subtraction

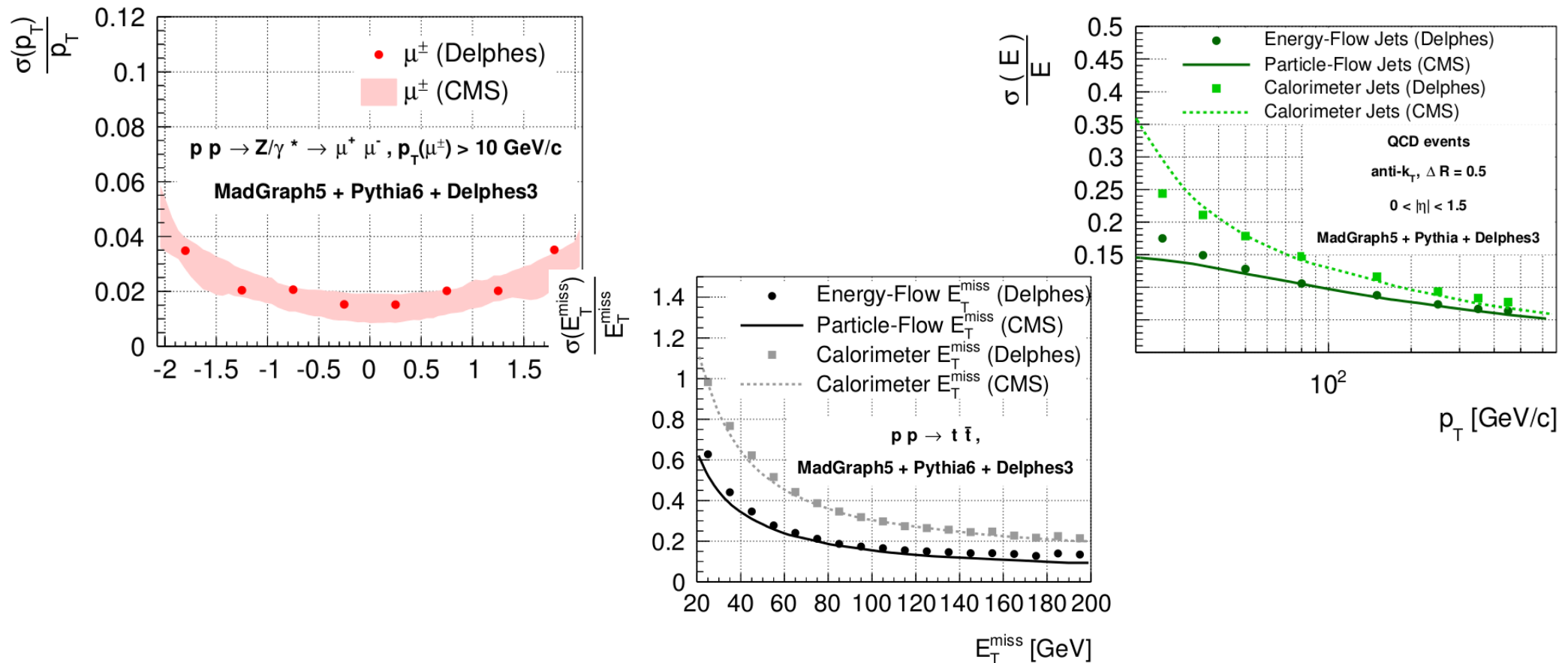
PU randomly extracted from a Minimum-Bias interactions file

Only for Jets and Isolation using vertex reconstruction (not for MET because too difficult to account for neutral contamination)

Introduction to Delphes

Validation

The simulation and reconstruction process executed by Delphes has to be validated with real experiment data (CMS and ATLAS)



Introduction to Delphes

Delphes for CMS



Many changes from the “official” Delphes:

- Timing information
- Different calorimeter configurations
- η dependent ρ correction



In general: in CMS version there are more and different modules from the official one, to adjust the simulation to the CMS detector



This is the version we are going to use!

Reference: <https://indico.cern.ch/event/294765/session/11/contribution/67>

Introduction to Delphes

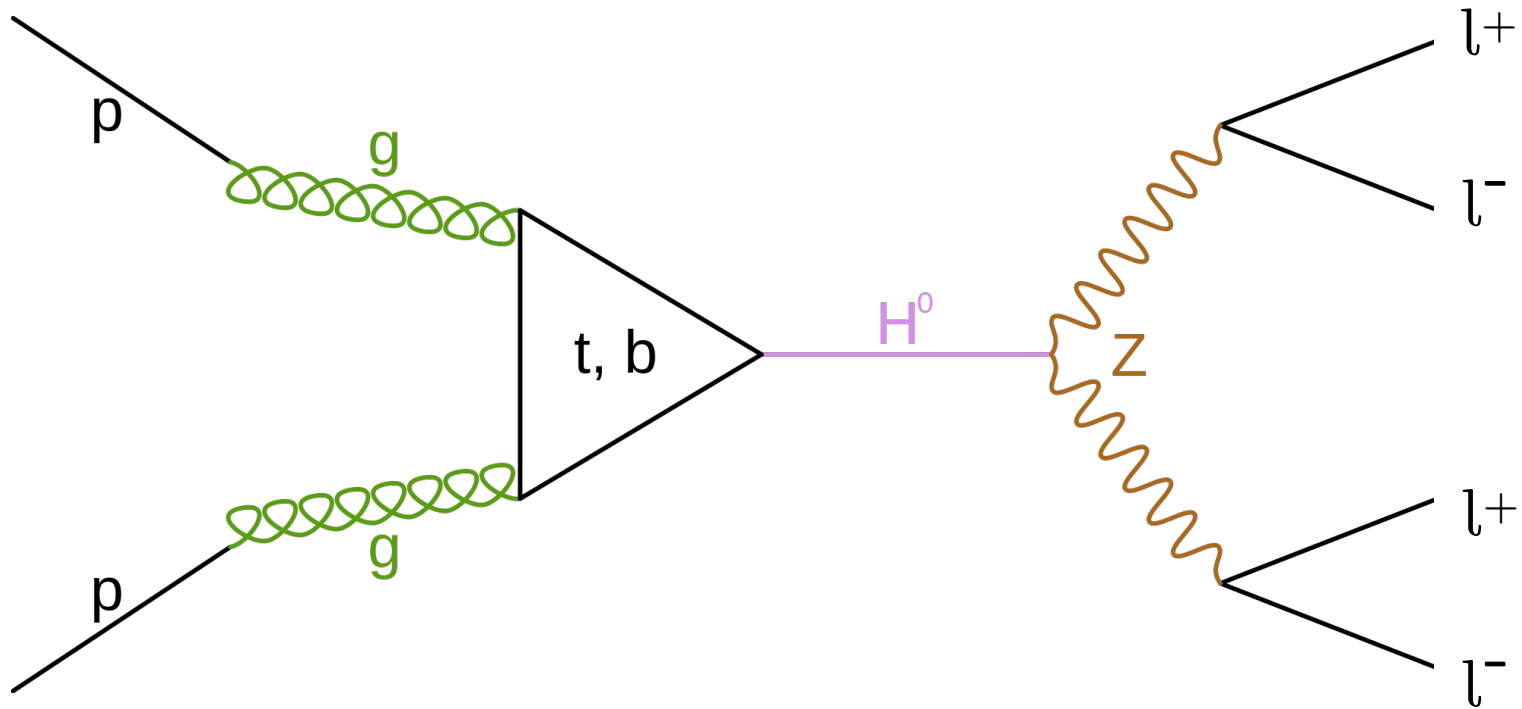
To sum up

Delphes is a modular framework that performs a fast and parametrized simulation of a multipurpose detector (e.g. CMS)

This tool has been completely validated (with CMS and ATLAS real data)

Useful in phenomenological studies and to produce big size background samples in which a fast simulation is needed

Analysis $H \rightarrow ZZ^* \rightarrow 4\mu$ with Delphes



- Higgs production mechanism: gluon-gluon fusion
- Higgs decay mode: $ZZ \rightarrow 4l$ (4μ)

Analysis $H \rightarrow ZZ^* \rightarrow 4\mu$ with Delphes

Studies of the performances of the $H \rightarrow ZZ^* \rightarrow 4\mu$ analysis with the PhaseII detector upgrade

Two detector geometries:

PhaseI (“2017”)

New tracker



FullSimulation samples:
Signal + Background



PhaseII (“2023”)

New tracker and forward ECAL
 η up to 3 or 4



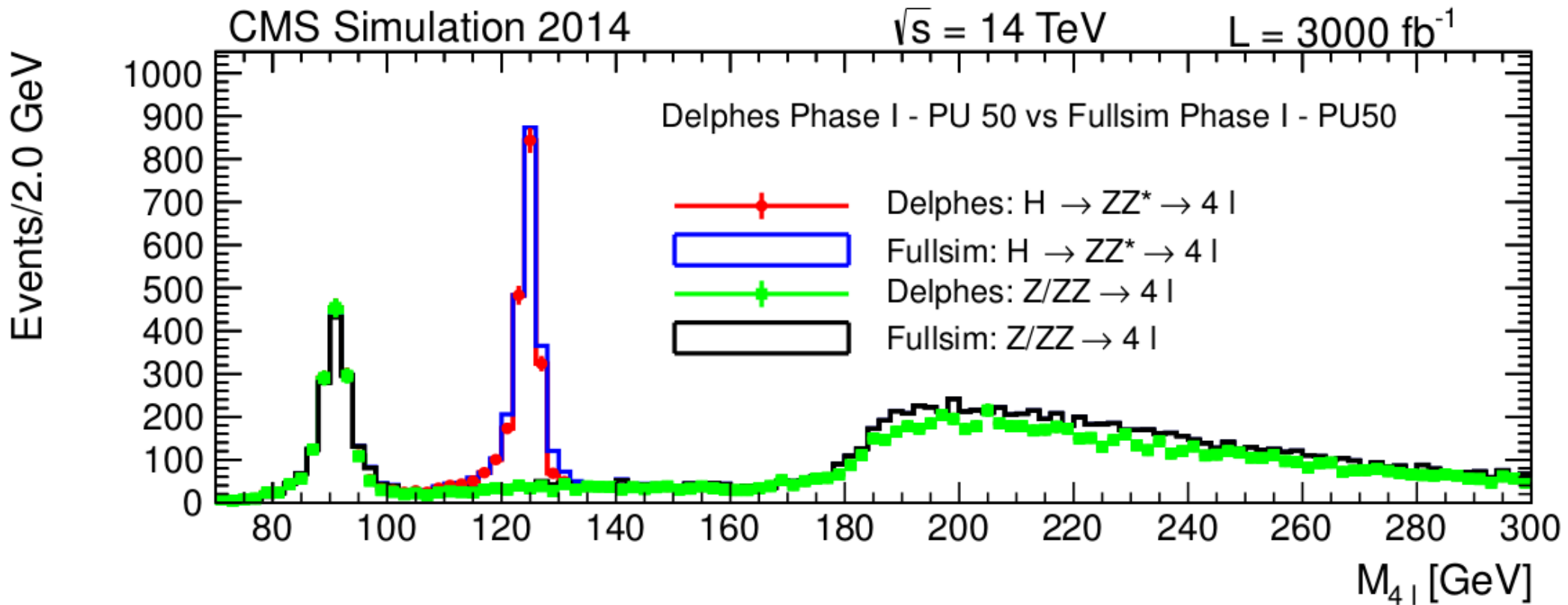
NO FullSimulation samples



DELPHES!

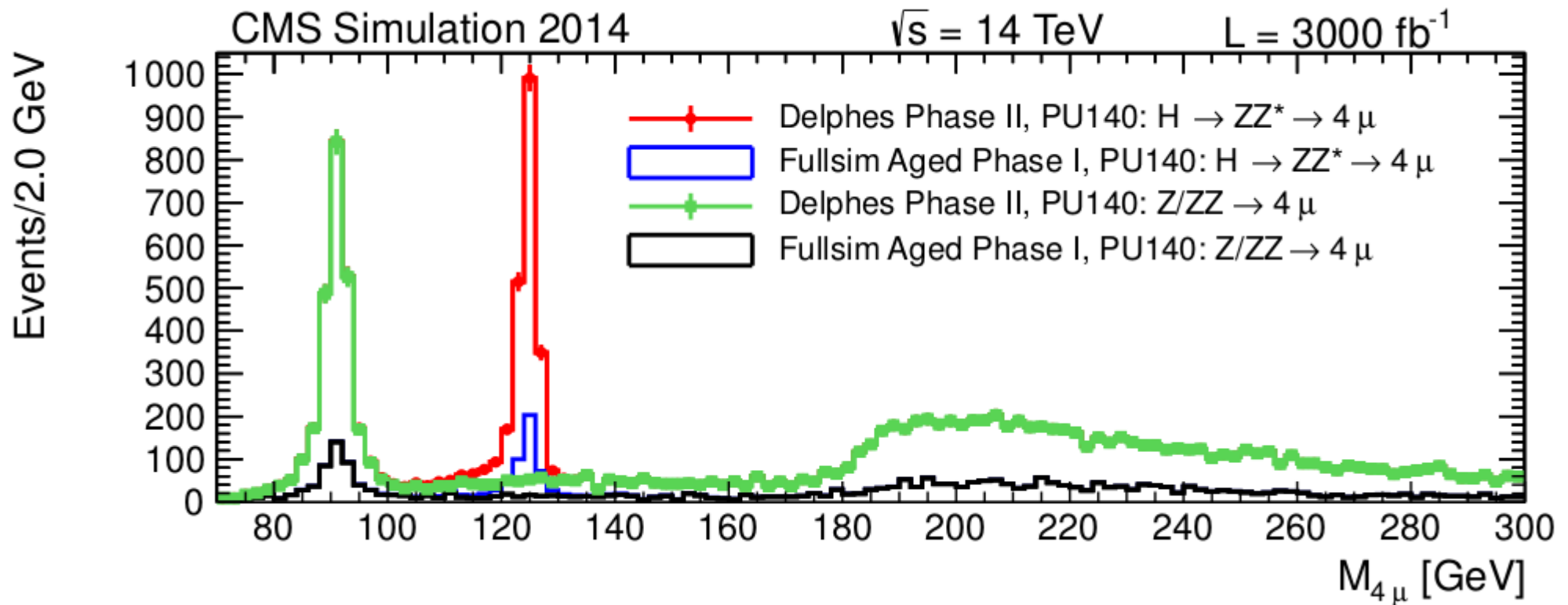
Analysis $H \rightarrow ZZ^* \rightarrow 4\mu$ with Delphes

1st step: validate Delphes vs FullSim with PhaseI “2017”
detector samples ($\sqrt{s} = 14$ TeV, PU =140)



Analysis $H \rightarrow ZZ^* \rightarrow 4\mu$ with Delphes

2nd step: use the [Delphes](#) parametrized simulation to reconstruct a hypothetical PhaseII detector ($\sqrt{s}=14$ TeV, PU =140)



Hands-on exercise

- ♦ Goals of this Hands-on Session

Basic knowledge about:

- ♦ the Delphes structure
- ♦ how Delphes works
- ♦ how to use Delphes to produce root samples of given events
- ♦ the ROOT samples structure
- ♦ how to analyze the samples with ROOT (for this part you will need a basic knowledge about ROOT).

Hands-on exercise

- ♦ Getting started with Delphes

- 1) Set the right Scientific Linux CERN version
- 2) Set the CMS environment
- 3) Download and install Delphes
- 4) You need one or more file(s) with Generated Events*
(in .hepMC format)
- 5) You need a file with Minimum Bias Events* for the PU
(MinBias.pileup)
- 6) Copy a customized Delphes DataCard* in your directory “Cards”
- 7) Copy all the macros* necessary for the analysis $H \rightarrow ZZ^* \rightarrow 4\mu$

Hands-on exercise

- ♦ Run Delphes!

General structure of
the command line:

```
./DelphesHepMC  
Cards/cardname.tcl  
somepath/outputfilename.root  
somepath/hepmcfilename.hepmc
```



Hands-on exercise

File with Generated Events (.hepMC)



- File with all the characteristics of generated events: η , p_T , E , ...
- Output of events generators

```
HepMC::Version 2.06.08
HepMC::IO_GenEvent-START_EVENT_LISTING
E 0 -1 4.6660200000000003e+01 1.4078099999999999e-01 7.7585830116479182e-03 9999 0 2024 1 2 0 1 1.0000000000000000e+00
N 1 "0"
U GEV MM
C 3.4466500000000003e+01 3.4466500000000003e+01
F -4 21 8.7436883742857147e-03 1.9855286214285714e-02 4.6660200000000003e+01 0 0 0 0
V -1 0 0 0 0 0 1 0
P 3 -4 0 0 6.1205818620000002e+01 6.1205818620000002e+01 0 21 0 0 -3 1 2 501
V -2 0 0 0 0 0 2 0
P 4 21 0 0 -1.3898700349999999e+02 1.3898700349999999e+02 0 21 0 0 -3 2 1 501 2 502
P 24 21 5.7185177904743236e+00 -6.1609436926723209e+00 -2.8704929448187880e+01 2.9910393637157195e+01 0 43 0 0 -23 2 1 507 2 501
V -3 0 0 0 0 0 2 0
P 5 25 4.0718400500000001e+01 -2.2785643319999998e+01 -7.5882461910000004e+01 1.5349401240000000e+02 1.2500036050000000e+02 22 0 0 -15 0
P 6 -4 -4.0718400500000001e+01 2.2785643319999998e+01 -1.8987229400000001e+00 4.6698809730000001e+01 7.3666614860000002e-07 23 0 0 -11 1 2 502
V -4 0 0 0 0 0 1 0
P 7 2 0 0 3.8552334991618829e+02 3.8552334991618818e+02 0 31 0 0 -6 1 1 503
V -5 0 0 0 0 0 2 0
P 8 21 0 0 -5.5383686130864440e-01 5.5383686130864385e-01 0 31 0 0 -6 2 1 504 2 505
P 15 21 -5.0817756360706540e+00 0.4407200454307436e+00 2.7410514370725580e+01 2.0280107200726172e+01 0 43 0 0 -27 2 1 505 2 506
```

Hands-on exercise

Delphes DataCard

File with ALL the settings of the simulation: efficiencies, resolutions, parameters for isolation, jets, ...

Structure:

- Function with all the list of **instructions** (different modules called one after the other)
- Descriptions of all the **modules** (Muon Momentum Smearing, Muon efficiency, Electron Energy Resolution, Muon Isolation, ...)



Last Module: **TreeWriter**
(choice of the Branches to write in the ROOT Tree)

```
#####
# Order of execution of various modules
#####
```

```
set ExecutionPath {
```

```
PileUpMerger
ModifyBeamSpot
ParticlePropagator
StatusPid
GenBeamSpotFilter
```

```
ChargedHadronTrackingEfficiency
ElectronTrackingEfficiency
MuonTrackingEfficiency
```

```
ChargedHadronMomentumSmearing
ElectronEnergySmearing
MuonMomentumSmearing
```

```
ModifyBeamSpotNoPU
ParticlePropagatorNoPU
ChargedHadronTrackingEfficiencyNoPU
ElectronTrackingEfficiencyNoPU
MuonTrackingEfficiencyNoPU
ChargedHadronMomentumSmearingNoPU
ElectronEnergySmearingNoPU
MuonMomentumSmearingNoPU
TrackMergerNoPU
CalorimeterNoPU
EFlowMergerNoPU
FastJetFinderNoPU
```

```
TrackMerger
Calorimeter
TrackPileUpSubtractor
EFlowMerger
```

```
GlobalRho
Rho
FastJetFinder
GenJetFinder
JetPileUpSubtractor
```

Execution Path

```
NeutrinoFilter
GenJetFinderNoNu
GenMissingET
```

```
EFlowChargedMerger
RunPUPPI
PuppiJetFinder
PuppiRho
PuppiJetPileUpSubtractor
PuppiMissingET
```

```
PhotonEfficiency
PhotonIsolation
```

```
ElectronEfficiency
ElectronIsolation
```

```
MuonEfficiency
MuonIsolation
```

```
MissingET
```

```
BTagging
BTaggingLoose
TauTagging
```

```
TrackPVSubtractor
IsoTrackFilter
```

```
UniqueObjectFinderGJ
UniqueObjectFinderEJ
UniqueObjectFinderMJ
```

```
ScalarHT
```

```
PileUpJetID
```

```
PileUpJetIDMissingET
```

```
ConstituentFilter
TreeWriter
```

```
module MomentumSmearing MuonMomentumSmearing {
  set InputArray MuonTrackingEfficiency/muons
  set OutputArray muons

  # set ResolutionFormula {resolution formula as a function of eta and pt}

  # resolution formula for muons

  set ResolutionFormula {
```

[illegible]

```
set ResolutionFormula {
  (abs(eta) <= 2.5) * (energy > 0.1 && energy <= 2.5e1) * (energy*0.025) + \
  (abs(eta) <= 2.5) * (energy > 2.5e1) * (energy*0.035) + \
  (abs(eta) > 2.5 && abs(eta) <= 3.0) * (energy*0.035) + \
  (abs(eta) > 3.0 && abs(eta) <= 5.0) * (energy*0.07)}
```

Resolution

Muon Efficiency

Muon Isolation

```
#####  
# Muon isolation  
#####
```

```
module Isolation MuonIsolation {  
  set CandidateInputArray MuonEfficiency/muons  
  set NeutralIsolationInputArray Calorimeter/eflowTowers  
  set ChargedIsolationInputArray TrackPileUpSubtractor/eflowTrac  
  set RhoInputArray Rho/rho  
  
  set OutputArray muons  
  
  set DeltaRMax 0.4  
  
  set PTMin 0.4  
  
  set PTRatioMax 9999.  
}
```

```
#####
```

```
File Edit Options Buffers Tools Tcl Help  
[Icons]  
#####  
# Muon efficiency  
#####  
  
module Efficiency MuonEfficiency {  
  set InputArray TrackPileUpSubtractor/muons  
  set OutputArray muons  
  
  # set EfficiencyFormula {efficiency as a function of eta and pt}  
  
  # efficiency formula for muons  
  
  set EfficiencyFormula {  
  
(pt < 5.0) * (0.00) + \  
(pt > 5.0 && pt <= 10.0) * ( abs(eta) > 0.0 && abs(eta) <= 0.5 ) * ( 0.98  
(pt > 5.0 && pt <= 10.0) * ( abs(eta) > 0.5 && abs(eta) <= 1.0 ) * ( 0.98  
(pt > 5.0 && pt <= 10.0) * ( abs(eta) > 1.0 && abs(eta) <= 1.5 ) * ( 0.97  
(pt > 5.0 && pt <= 10.0) * ( abs(eta) > 1.5 && abs(eta) <= 2.0 ) * ( 0.99  
(pt > 5.0 && pt <= 10.0) * ( abs(eta) > 2 && abs(eta) <= 2.4 ) * ( 0.9714  
(pt > 5.0 && pt <= 10.0) * ( abs(eta) > 2.4 ) * ( 0 ) + \  
(pt > 10.0 && pt <= 20.0) * ( abs(eta) > 0.0 && abs(eta) <= 0.5 ) * ( 0.9  
(pt > 10.0 && pt <= 20.0) * ( abs(eta) > 0.5 && abs(eta) <= 0.9 ) * ( 0.9  
(pt > 10.0 && pt <= 20.0) * ( abs(eta) > 0.9 && abs(eta) <= 1.1 ) * ( 0.9  
(pt > 10.0 && pt <= 20.0) * ( abs(eta) > 1.1 && abs(eta) <= 1.4 ) * ( 0.9  
(pt > 10.0 && pt <= 20.0) * ( abs(eta) > 1.4 && abs(eta) <= 2.0 ) * ( 0.9  
(pt > 10.0 && pt <= 20.0) * ( abs(eta) > 2.0 && abs(eta) <= 2.4 ) * ( 0.9  
(pt > 10.0 && pt <= 20.0) * ( abs(eta) > 2.4 ) * ( 0 ) + \  
(pt > 20.0 && pt <= 40.0) * ( abs(eta) > 0.0 && abs(eta) <= 0.5 ) * ( 0.9  
(pt > 20.0 && pt <= 40.0) * ( abs(eta) > 0.5 && abs(eta) <= 1.0 ) * ( 0.9  
(pt > 20.0 && pt <= 40.0) * ( abs(eta) > 1.0 && abs(eta) <= 1.5 ) * ( 0.9  
(pt > 20.0 && pt <= 40.0) * ( abs(eta) > 1.5 && abs(eta) <= 2.0 ) * ( 0.9  
(pt > 20.0 && pt <= 40.0) * ( abs(eta) > 2.0 && abs(eta) <= 2.4 ) * ( 0.9  
(pt > 20.0 && pt <= 40.0) * ( abs(eta) > 2.4 ) * ( 0 ) + \  
(pt > 40.0 ) * ( abs(eta) > 0.0 && abs(eta) <= 0.5 ) * ( 0.9949498 ) + \  
(pt > 40.0 ) * ( abs(eta) > 0.5 && abs(eta) <= 1.0 ) * ( 0.9952686 ) + \  
(pt > 40.0 ) * ( abs(eta) > 1.0 && abs(eta) <= 1.5 ) * ( 0.9886918 ) + \  
(pt > 40.0 ) * ( abs(eta) > 1.5 && abs(eta) <= 2.0 ) * ( 0.9919946 ) + \  
(pt > 40.0 ) * ( abs(eta) > 2.0 && abs(eta) <= 2.4 ) * ( 0.964623 ) + \  
(pt > 40.0 ) * ( abs(eta) > 2.4 ) * ( 0 )  
}
```

```

}
#####
# ROOT tree writer
#####

module TreeWriter TreeWriter {
  add Branch StatusPid/filteredParticles Particle GenParticle
  ### add Branch Delphes/allParticles Particle GenParticle

  add Branch GenBeamSpotFilter/beamSpotParticles BeamSpotParticle GenParticle

  add Branch FastJetFinder/jets RawJet Jet
  add Branch FastJetFinderNoPU/jets RawJetNoPU Jet

  add Branch GenJetFinder/jets GenJetWithNu Jet
  add Branch GenJetFinderNoNu/jets GenJet Jet
  # add Branch UniqueObjectFinderMJ/jets Jet Jet
  # add Branch UniqueObjectFinderEJ/electrons Electron Electron
  # add Branch UniqueObjectFinderGJ/photons Photon Photon
  # add Branch UniqueObjectFinderMJ/muons Muon Muon
  add Branch JetPileUpSubtractor/jets Jet Jet
  add Branch ElectronIsolation/electrons Electron Electron
  add Branch PhotonIsolation/photons Photon Photon
  add Branch MuonIsolation/muons Muon Muon

  add Branch PileUpJetIDMissingET/momentum PileUpJetIDMissingET MissingET
  add Branch GenMissingET/momentum GenMissingET MissingET
  add Branch PuppiMissingET/momentum PuppiMissingET MissingET

  add Branch MissingET/momentum MissingET MissingET
  add Branch ScalarHT/energy ScalarHT ScalarHT
  add Branch Rho/rho Rho Rho
  add Branch GlobalRho/rho GlobalRho Rho
  add Branch PileUpMerger/NPU NPU ScalarHT
  add Branch IsoTrackFilter/IsoTrack IsoTrack IsoTrack

  add Branch PuppiJetFinder/jets PuppiJet Jet

  set OffsetFromModifyBeamSpot 0

  # add Branch RunPUPPI/weightedparticles PuppiWeightedParticles GenParticle
  # add Branch Delphes/allParticles Particle GenParticle
--** CMS_PhaseI_PU50_muP0Geff.tcl (Tcl) --L1346--95%-----

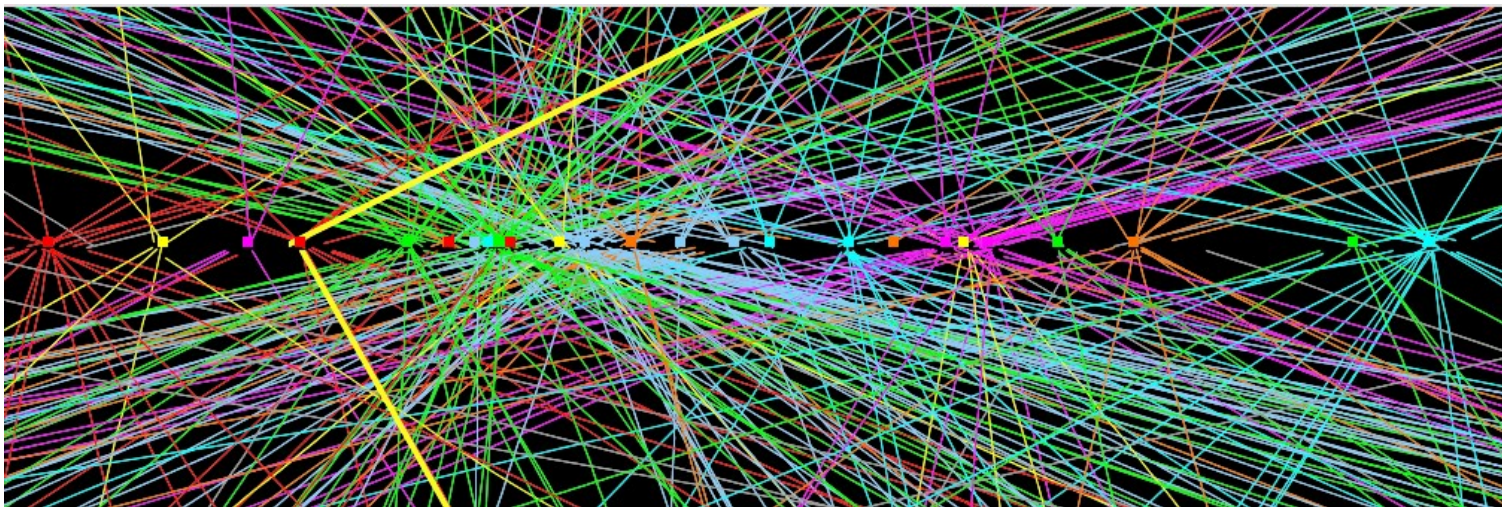
```

Root Tree Writer

Hands-on exercise

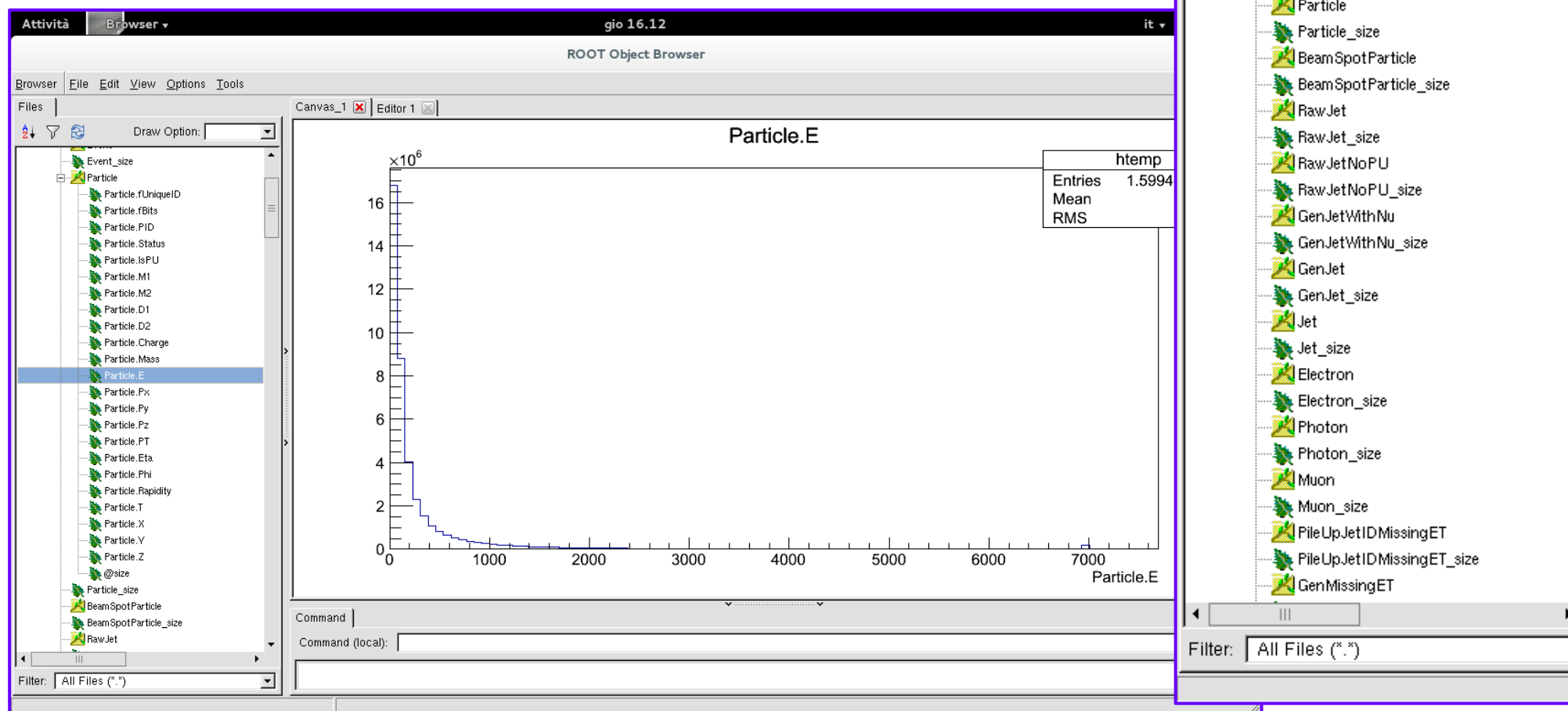
Minimum Bias Events file

- File with a collection of PU events
- Delphes accesses this file randomly for every signal event to take the selected number of PU events and superimpose them to the main one

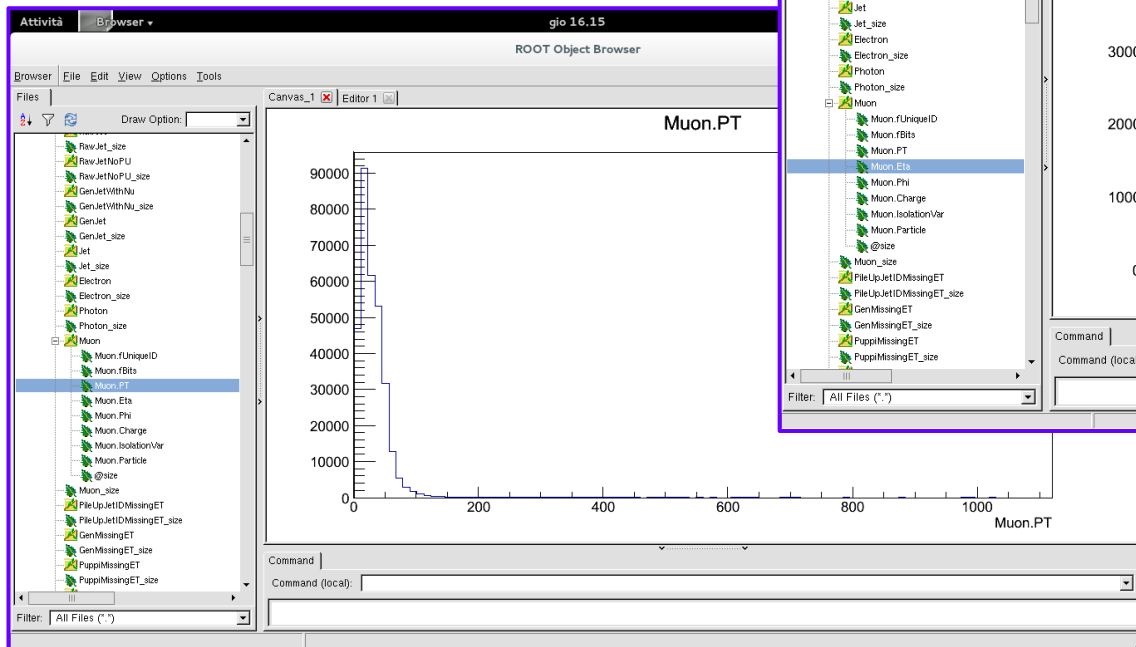
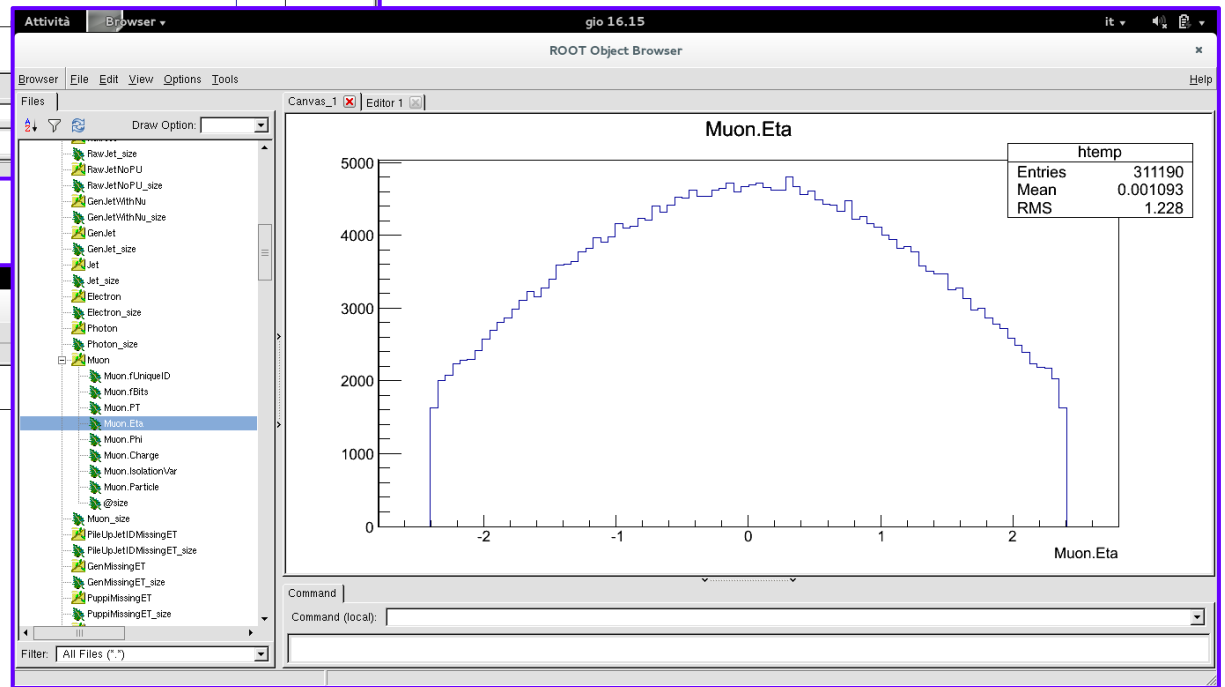
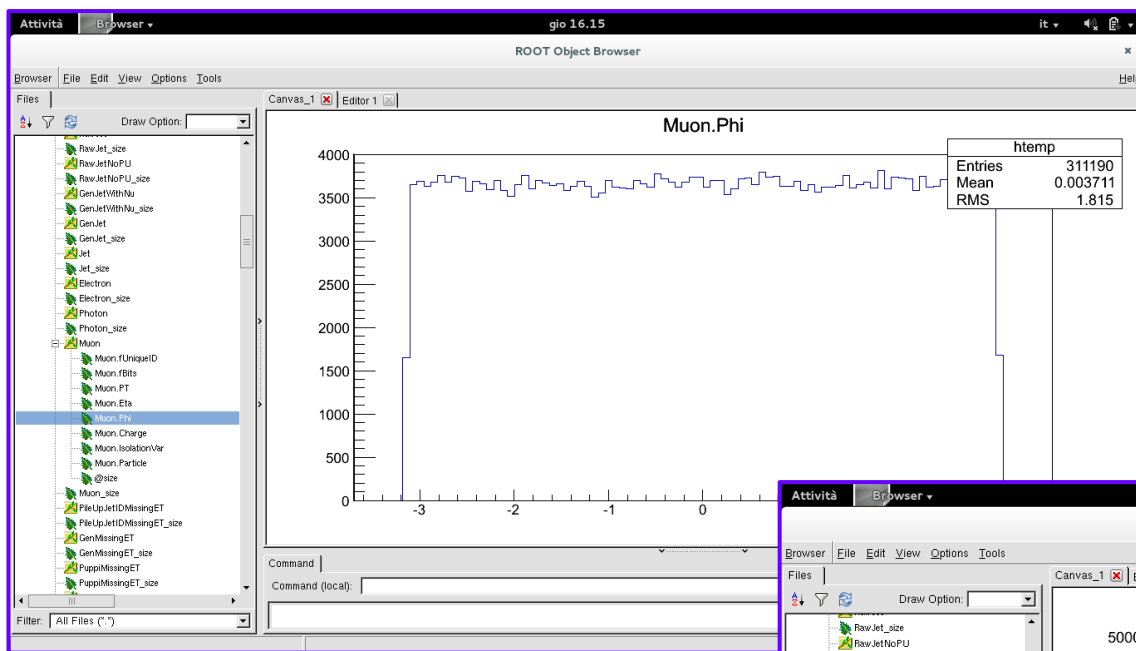


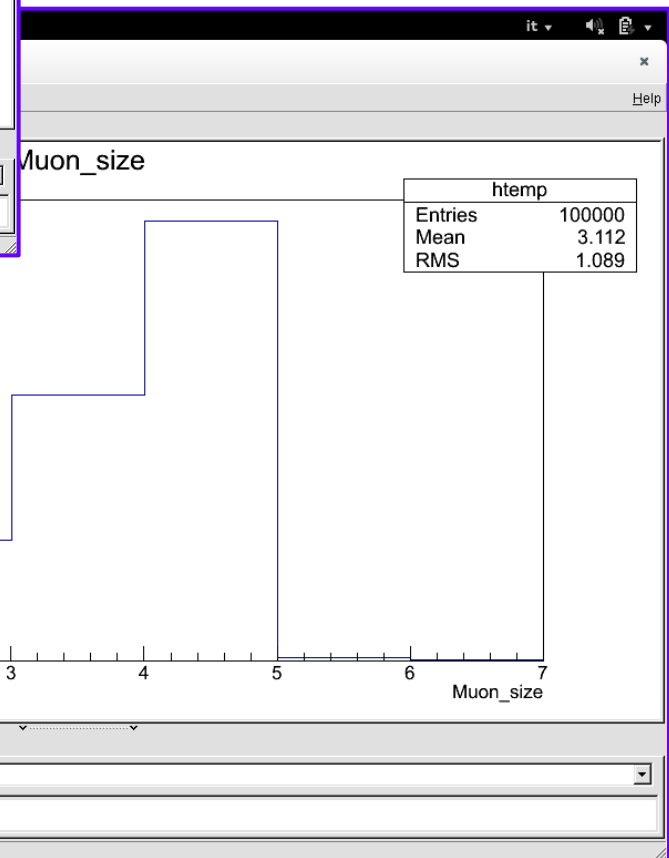
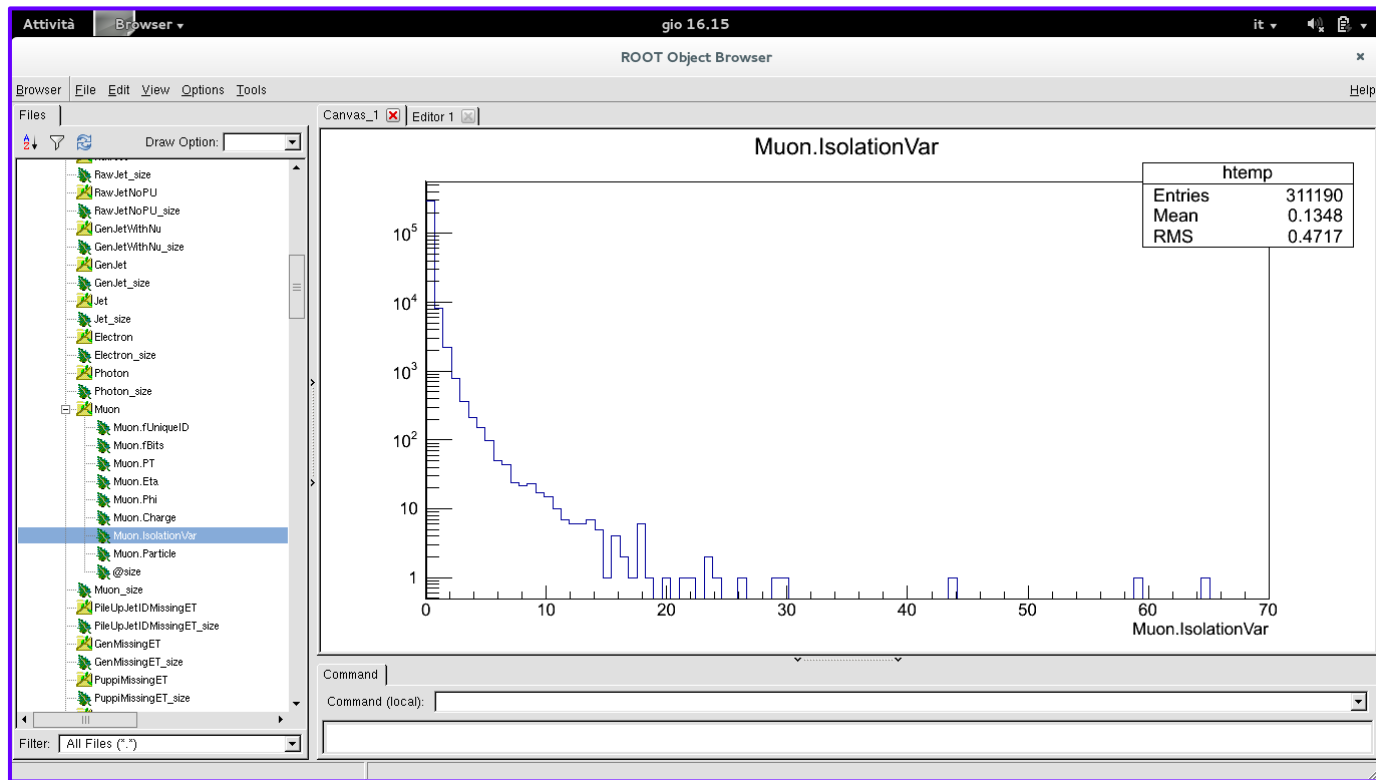
Hands-on exercise

- Delphes Tree, Branches and Leaves



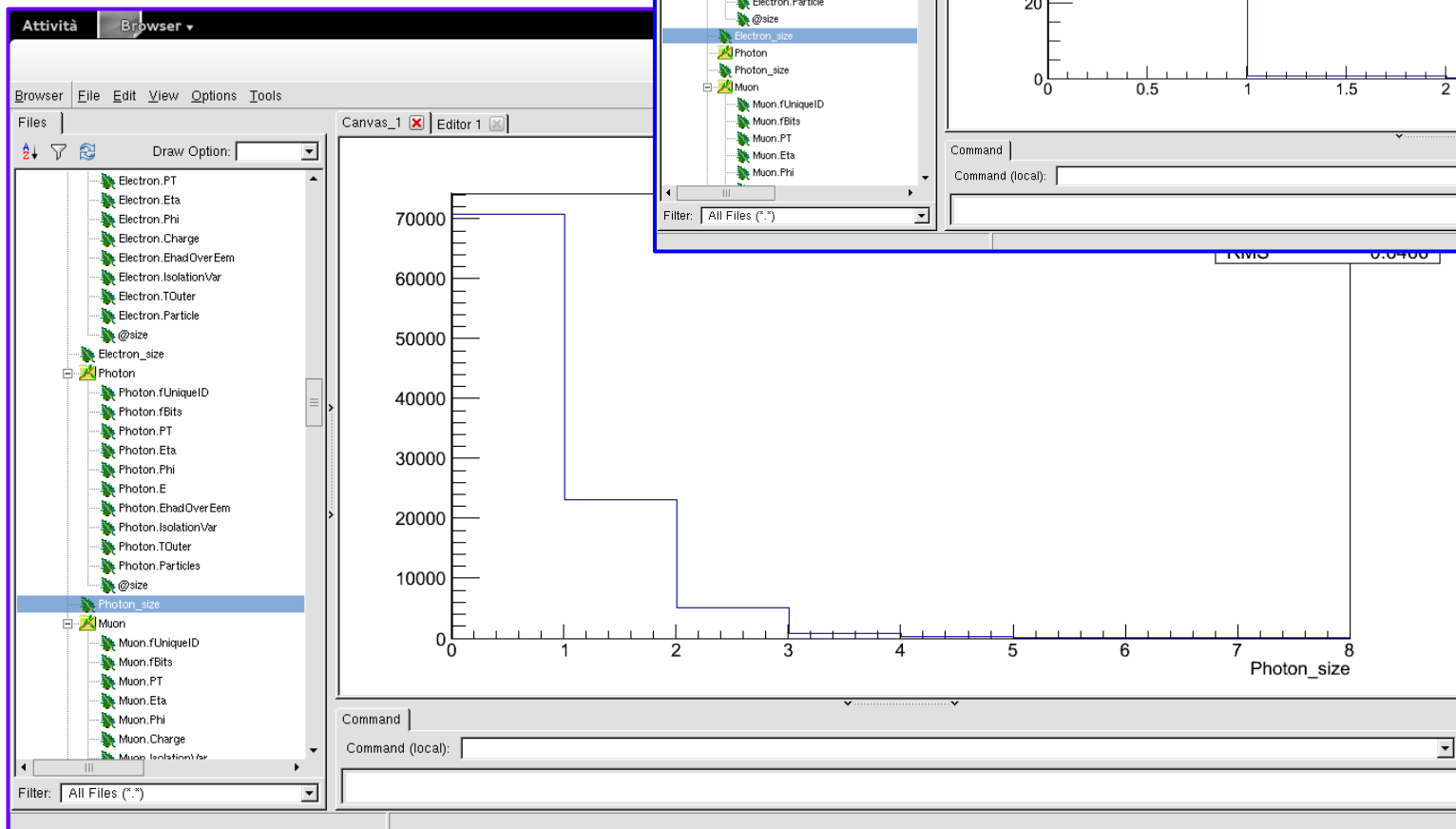
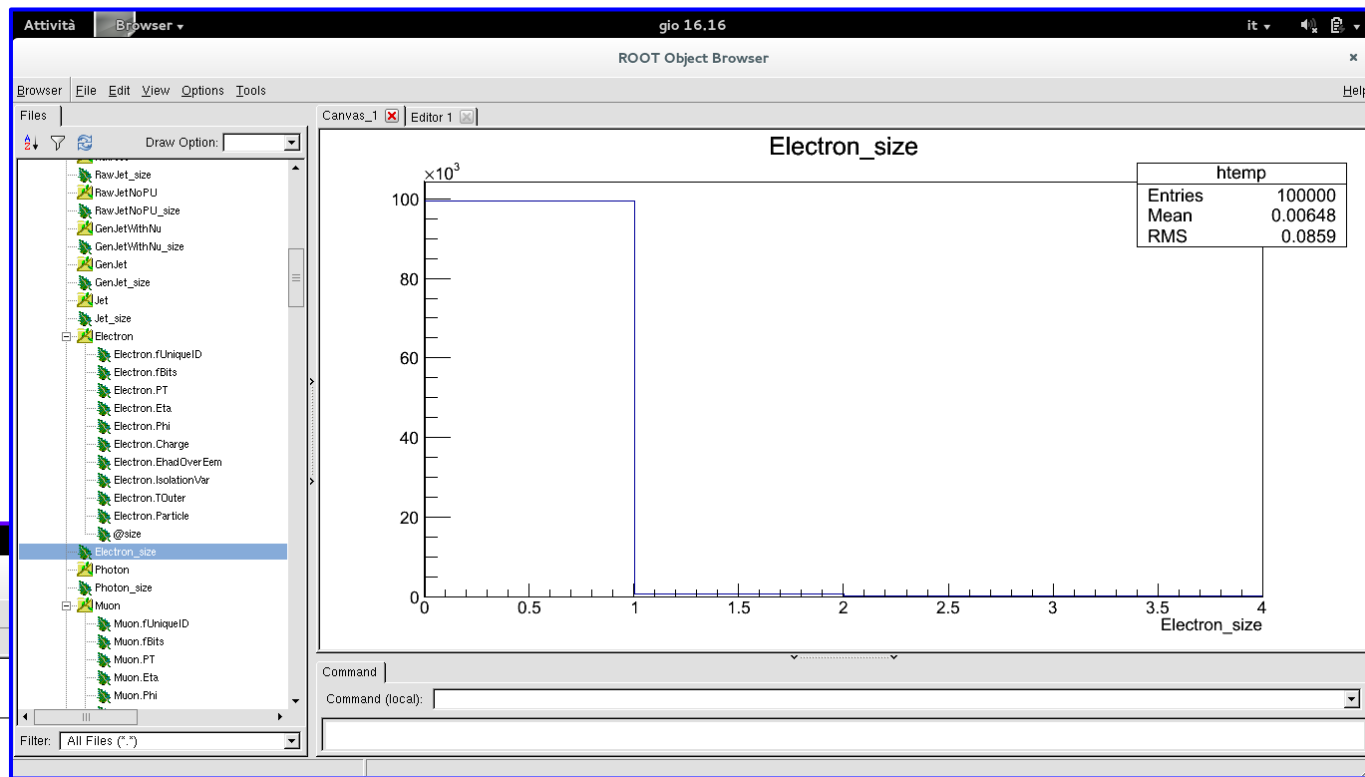
Branch Muon





**Branch
Muon**

Branch Electron



Branch Photon

Hands-on exercise

Macros for the analysis

- Simplified analysis $H \rightarrow ZZ^* \rightarrow 4\mu$
- You will learn how to:
 - a) read a Delphes Tree
 - b) access Generated Particles
 - c) access Reconstructed Muon
 - d) build an efficiency/resolution plot with “Delphes quantities”
 - e) build an invariant mass plot and a cutflow table

Hands-on exercise

- ♦ `DelphesMU_analysis.C`

- 1) Bool variables to choose configuration (REMEMBER TO CHECK ON THEM!)
- 2) Opening of the output file
- 3) Reading of the Delphes Tree
- 4) Declarations of histograms (Higgs invariant mass and Cutflow table)
- 5) Loop on every event: sequential cuts to identify events
 $H \rightarrow ZZ^* \rightarrow 4\mu$ and filling of histograms
- 6) Writing of the .histo file

Hands-on exercise

- ♦ `DelphesMU_distributions.C`

- 1) Bool variables to choose configuration (REMEMBER TO CHECK ON THEM!)
- 2) Opening of the output file
- 3) Reading of the Delphes Tree
- 4) Declarations of histograms (Efficiency as function of η and of p_T , Isolation, p_T Resolution)
- 5) Loop on every event: filling of histograms
- 6) Writing of the .histo file

Hands-on exercise

- ♦ `Plots.C`

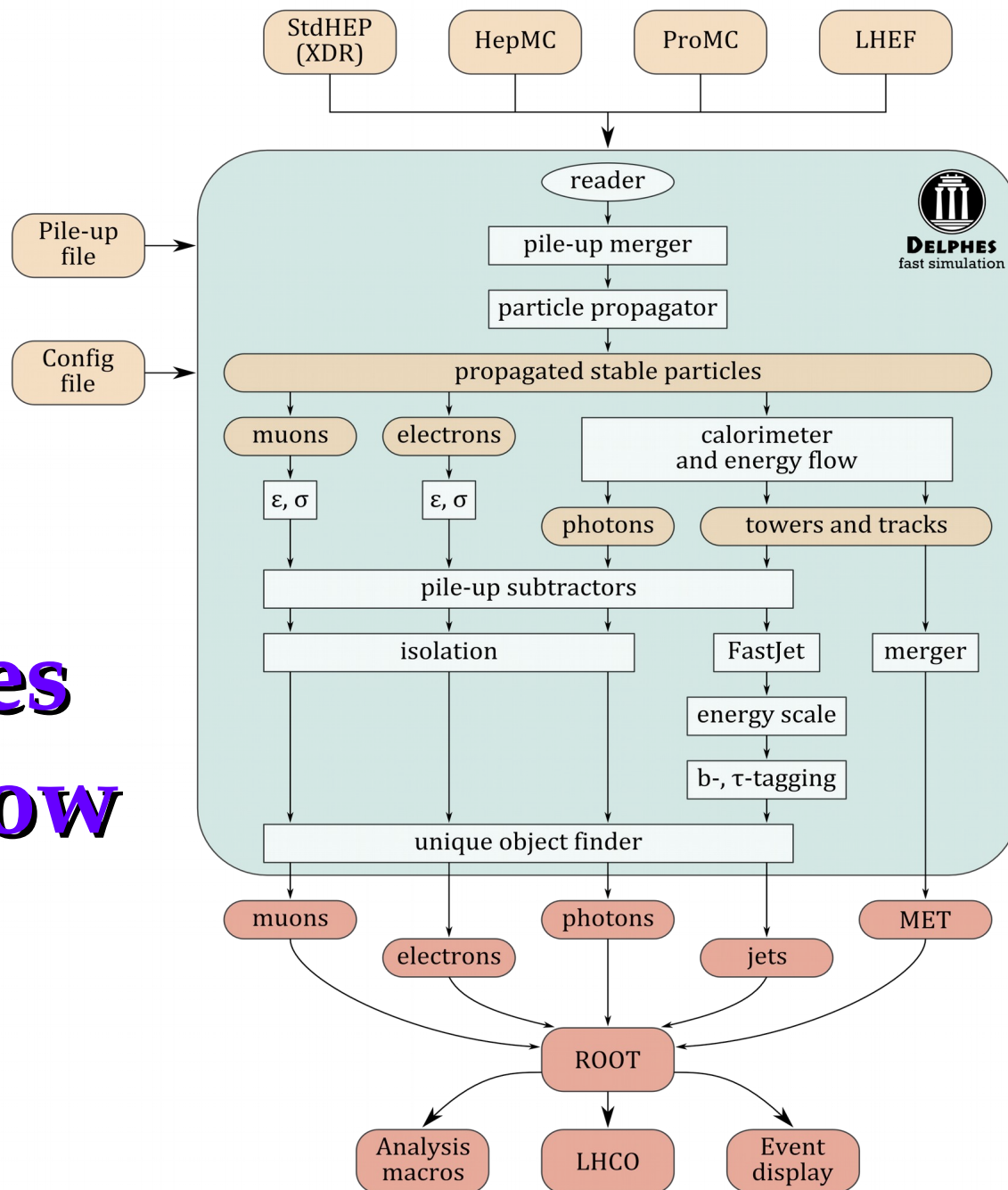
- 1) Opening of all .histo files (REMEMBER TO CHECK ON THEM!)
- 2) Reading of the leaves of the .histo
- 3) Definition of the histograms options
- 4) Definition of the legends
- 5) Drawing of the histograms
- 6) Saving of all the plots



Thank you for the attention!

Backup

Delphes work-flow chart



- ♦ Electromagnetic and hadronic calorimeters

Calorimeter response is simulated through a Gaussian smearing of the cell energy with resolution of ECAL and HCAL independently parametrized:

$$\left(\frac{\sigma}{E}\right)^2 = \left(\frac{S(\eta)}{\sqrt{E}}\right)^2 + \left(\frac{N(\eta)}{E}\right)^2 + C(\eta)^2$$

Where S: stochastic, N: noise, C constant terms

Final energy:

$$E_{Tower} = \sum_{particles} \ln \mathcal{N}(f_{ECAL} \cdot E, \sigma_{ECAL}(E, \eta)) + \ln \mathcal{N}(f_{HCAL} \cdot E, \sigma_{HCAL}(E, \eta))$$

Where $\ln \mathcal{N}(m, s)$ is the log-normal distribution with mean m and variance s

Too precise $\Rightarrow$ unique Gaussian smearing!

- ♦ Photon and charged leptons (NO !)

- $\mu^\pm$ Reconstructed thanks to user-defined efficiencies: $f(\eta, p_T)$
 p_T : Gaussian smearing of the initial 4-momentum vector
with resolution as a function of eta and p_T
- $e^\pm$ Reconstructed with user-defined efficiencies (ECAL +
tracker reconstruction): $f(\eta, p_T)$
Energy Resolution: $f(\text{TRACKER Res}, \text{ECAL Res})$
- γ Reconstructed only by the ECAL energy deposit
Pairs production neglected
 $e^\pm$ with no reconstructed tracks that reach the ECAL