Hype – a simple tool for hypothesis evaluation

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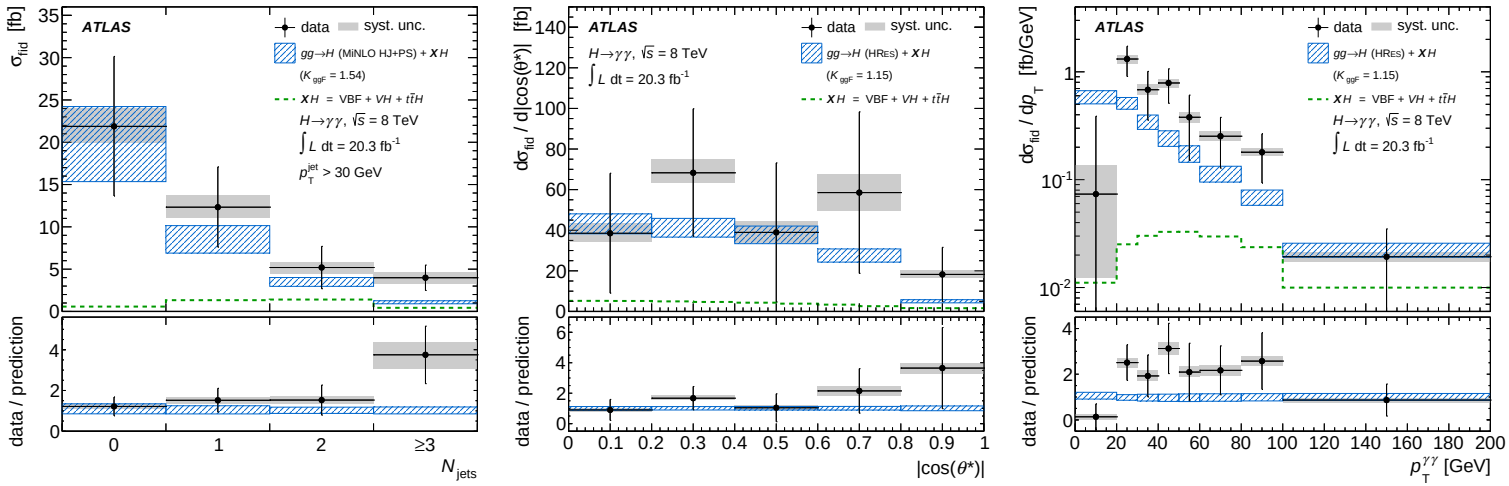
New interesting results from the *ATLAS* experiment about the Higgs available:



* Differential Cross sections in $H \to 4\ell$ and $H \to \gamma\gamma$

[JHEP09(2014)112] [Physics Letters B 738 (2014) 234-253]

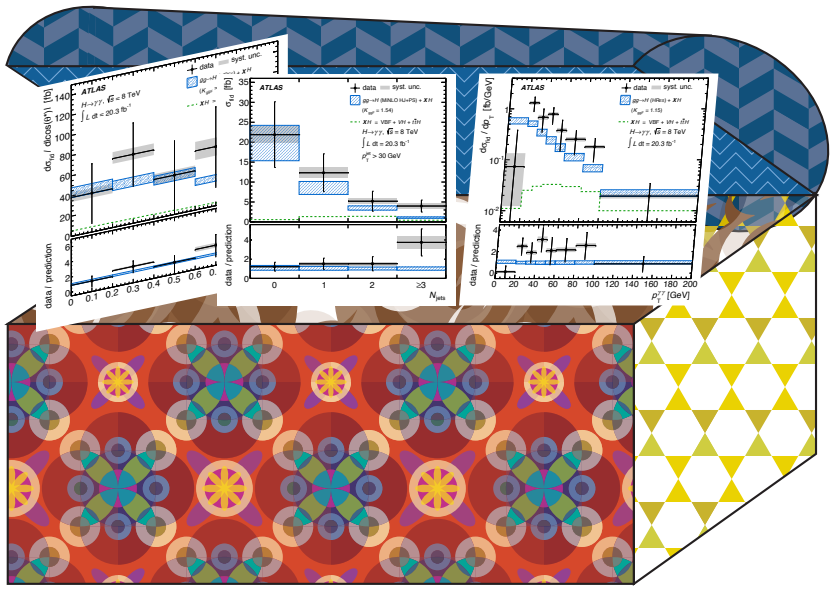
$\to$ Measured values published in **HepData**; unfolded to **particle level**

1. Minimal *underlying* physics dependence

   unfolding into truth fiducial region closely related to measured fiducial selection

2. Full set of *systematic* bin-by-bin cross correlations

Treasure chest for *theorists and phenomenologists*:



Do you have a new physics model and it impacts kinematics in the Higgs sector? Why not test it!

Like you know what a certain **dim-6 operator** makes the Higgs more boosted? Allowed **Spin** 2^+ coefficients?

→ Both measurements provide Rivet routines for **particle level fiducial regions**

→ Non-perturbative correction factors included to map parton to particle level predictions

Hype – (Hyp)othesis (e)valuator for unfolded distributions

Software package that aims to provide simple path to hypotheses tests

The Hype Team:
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Features:

i. **Easily** test between zero and alternative hypotheses
ii. Additional **Plug-ins**: B *vs* S+B,..
iii. Can directly import **Hep-Data** measurements
iv. Can **interface custom code**
v. Very performant: 1M toys in about 3s with fast toy option

Say, you have two hypothesis: SM and alternative theory

Neyman-Pearson Lemma: Likelihood ratio of both Hypothesis

$$\mathcal{L}_{\text{alt}}/\mathcal{L}_{\text{zero}}$$

most powerful discriminator *(called a test statistic)* you can build.

Applied to binned data: $-2\ln\left(\mathcal{L}_{\text{alt}}/\mathcal{L}_{\text{zero}}\right) = \chi^2_{\text{alt}} - \chi^2_{\text{zero}} = \Delta\chi^2$ where

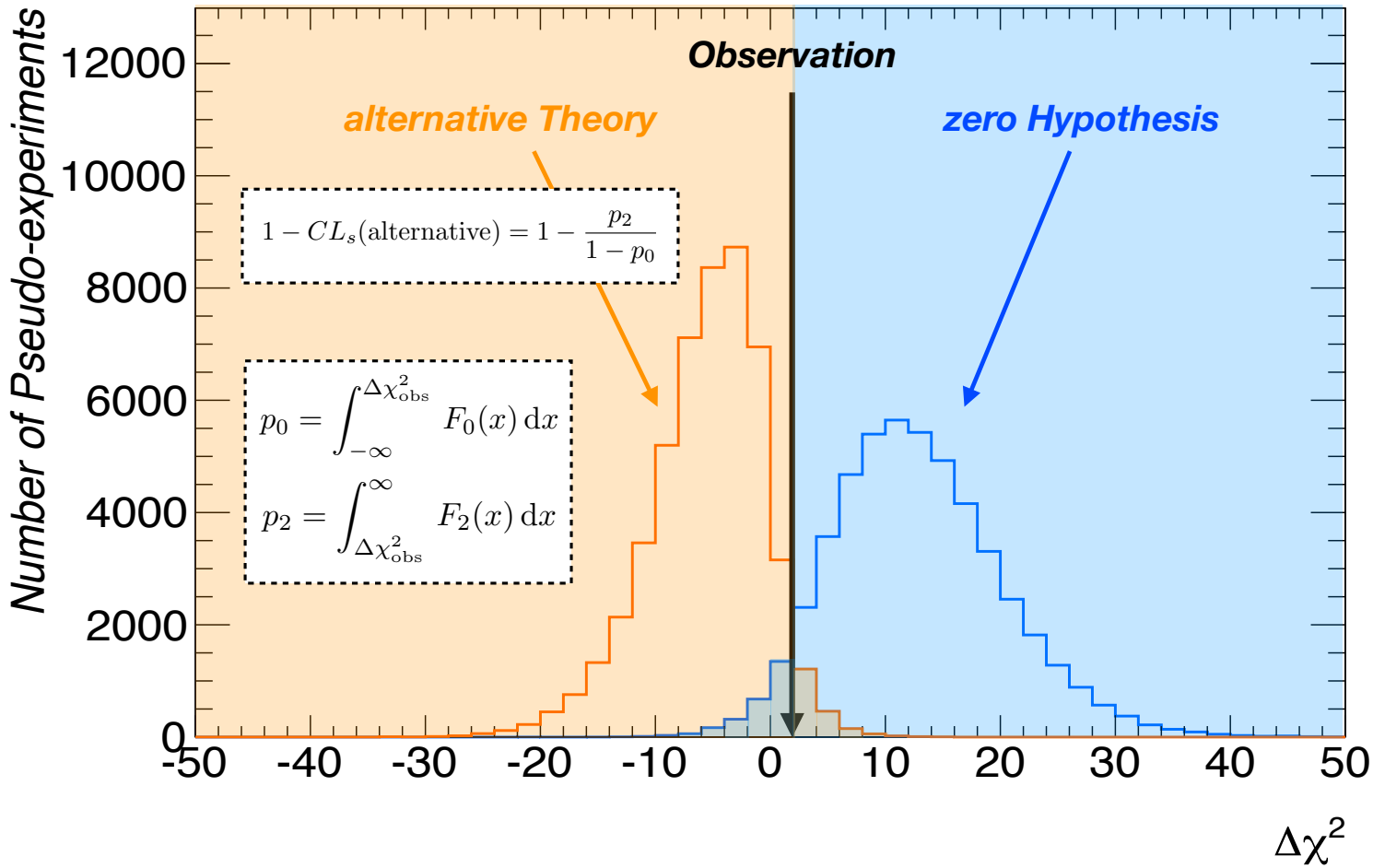
$$\chi^2_{hypo} = \left(\vec{x}_{\text{data}} - \vec{x}_{\text{hypo}}\right) C^{-1}_{\text{hypo}} \left(\vec{x}_{\text{data}} - \vec{x}_{\text{hypo}}\right) .$$

To interpret an observed value of $\Delta\chi^2$ in data:

* Need to know how test statistic is distributed given either zero or alternative theory is the true underlying theory.
* Can be done using Monte Carlo Method with **pseudo-experiments**

Used Test Statistic and CL_s(alternative)

Example test statistic distribution for zero and alternative hypothesis:



Hype automatically determines needed number of pseudo-experiments

to achieve numerical accuracy depending on the observation.

The Hype Approach to Pseudo-Experiments

Besides this normal implementation, Hype has a fast toy option:

$$\chi^2_{hypo} = (\vec{x}_{\text{data}} - \vec{x}_{\text{hypo}})\, C^{-1}\, (\vec{x}_{\text{data}} - \vec{x}_{\text{hypo}})\ .$$

This option makes use of the asymptotic behaviour of $\Delta\chi^2$

* Reduces the problem of generating pseudo-experiments with N bins to the *two* or *more* relevant degrees of freedom

→ Cross terms cancelation in $\Delta\chi^2$; given fixed normalization test statistic normal distributed.

* Breaks down when floating normalization: $\vec{x}_{\text{hypo}} \to \mu_{\text{hypo}} \cdot \vec{x}_{\text{hypo}}$

→ Problem now non-linear, normalization depends on pseudo-experiment.

→ Can be diagonalized in a new set of variables and solved for each pseudo-experiment; leaves only 2 effective degrees of freedom

Reduces toy-generation effort from $2\,N_{\text{bins}}$ to 4 random numbers.

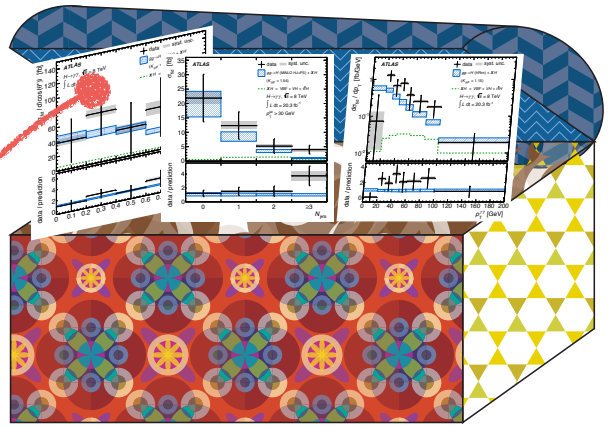
Can also be generalized for cases where $C \to C_{\text{hypo}}$.

With this options it takes **3s** to produce 1M pseudo-experiments.

It is activated automatically when the covariances are identical, and it's accuracy checked on the fly with normal pseudo-experiments.

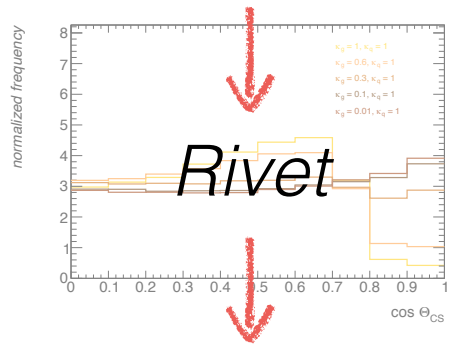
Flow of a typical Hype analysis:

Measurements

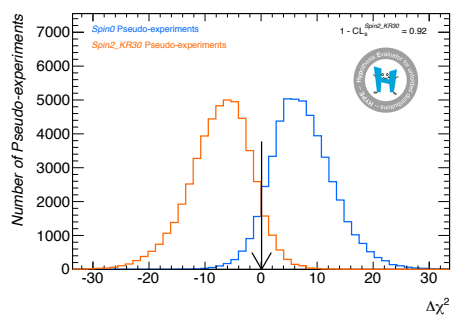


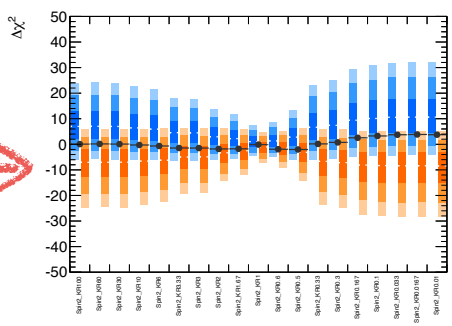
Predictions

(MG5_)[a]MC@NLO+ PS



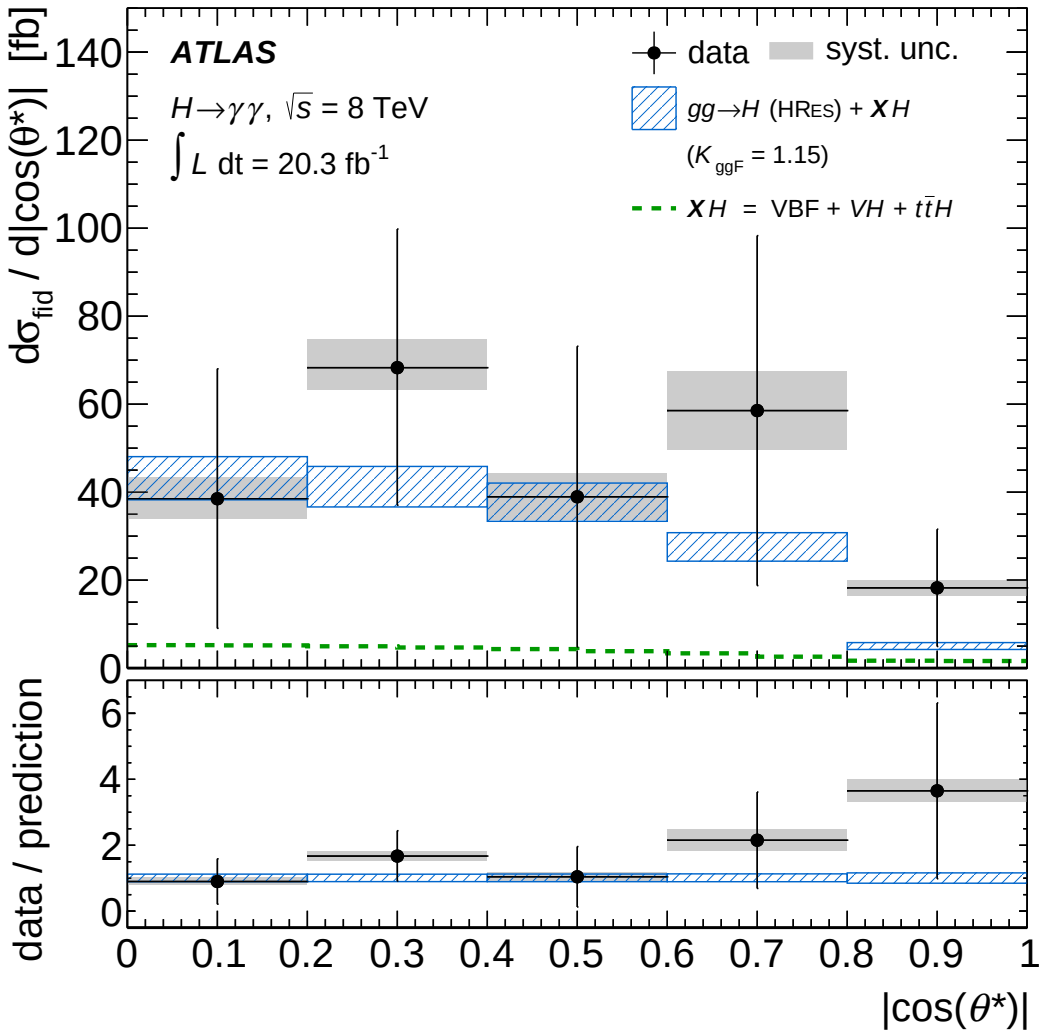

```
# Spin0 hypothesis predictiona and uncertainty covariance
Spin0.XSec:        4.28232 4.25835 ....
Spin0.XSecUncert:  0. 0. 0. 0. 0. 0. 0. 0. 0. 0.
Spin0.FullyUncorrelatedUncertainties: 1

# Spin2 hypothesis predictiona and uncertainty covariance
Spin2.XSec:    3.04068 3.12015 ....
Spin2.XSecUncert:  0. 0. 0. 0. 0. 0. 0. 0. 0. 0.
Spin2.FullyUncorrelatedUncertainties: 1
```





Example Analysis: **Spin analysis with $H \to \gamma\gamma$ ATLAS Run 1 data**

Measured distribution sensitive to Spin of Higgs: $|\cos(\theta^*)|$



Actually measured in 10 bins, here merged to 5

Example Analysis: **Spin analysis with $H \to \gamma\gamma$ ATLAS Run 1 data**

Zero Hypothesis: **SM** from MiNLO HJ + Py8 (ggF) + Powheg + Py8(VBF) + Py8(VH & $t\bar{t}H$)

Alternative Hypothesis: Spin 2^+

Effective Lagrangian of alternative hypothesis: *arXiv:1306.6464v3*

$$\mathcal{L} = -\frac{\kappa}{\Lambda} \sum_{f=q,\ell} \kappa_f \, T^f_{\mu\nu} \, X_2^{\mu\nu} - \frac{\kappa}{\Lambda} \sum_{V=Z,W,\gamma,g} \kappa_V \, T^V_{\mu\nu} \, X_2^{\mu\nu}$$

$H \to \gamma\gamma$ sensitive to variations in κ_q & κ_g

* Explore models with *free* parameter to change overall normalization: κ/Λ

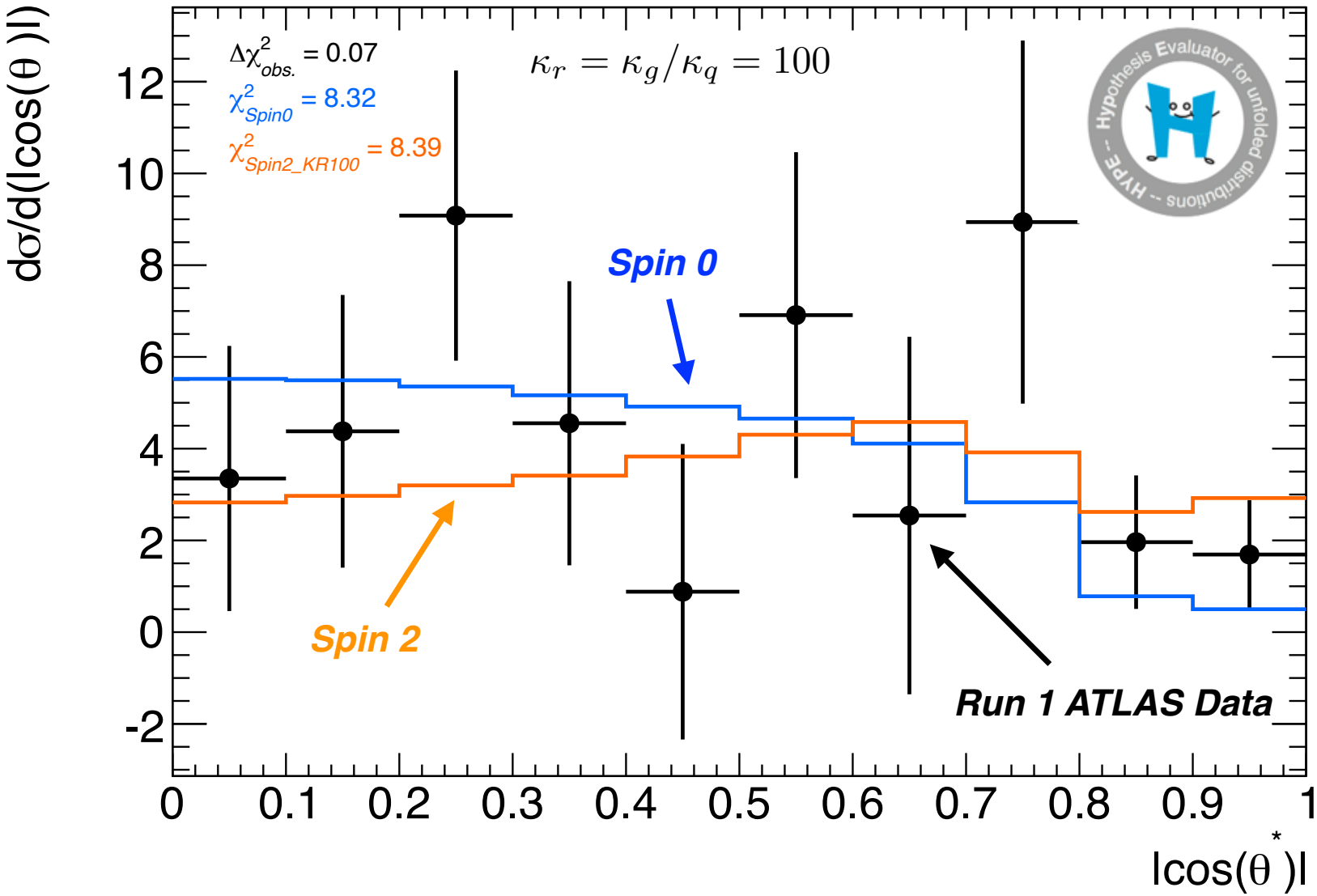
$\to$ only relevant degree of freedom between various models: $\kappa_r = \kappa_g/\kappa_q$

* Perform a scan over 19 working points in κ_r ranging from **0.01 to 100**

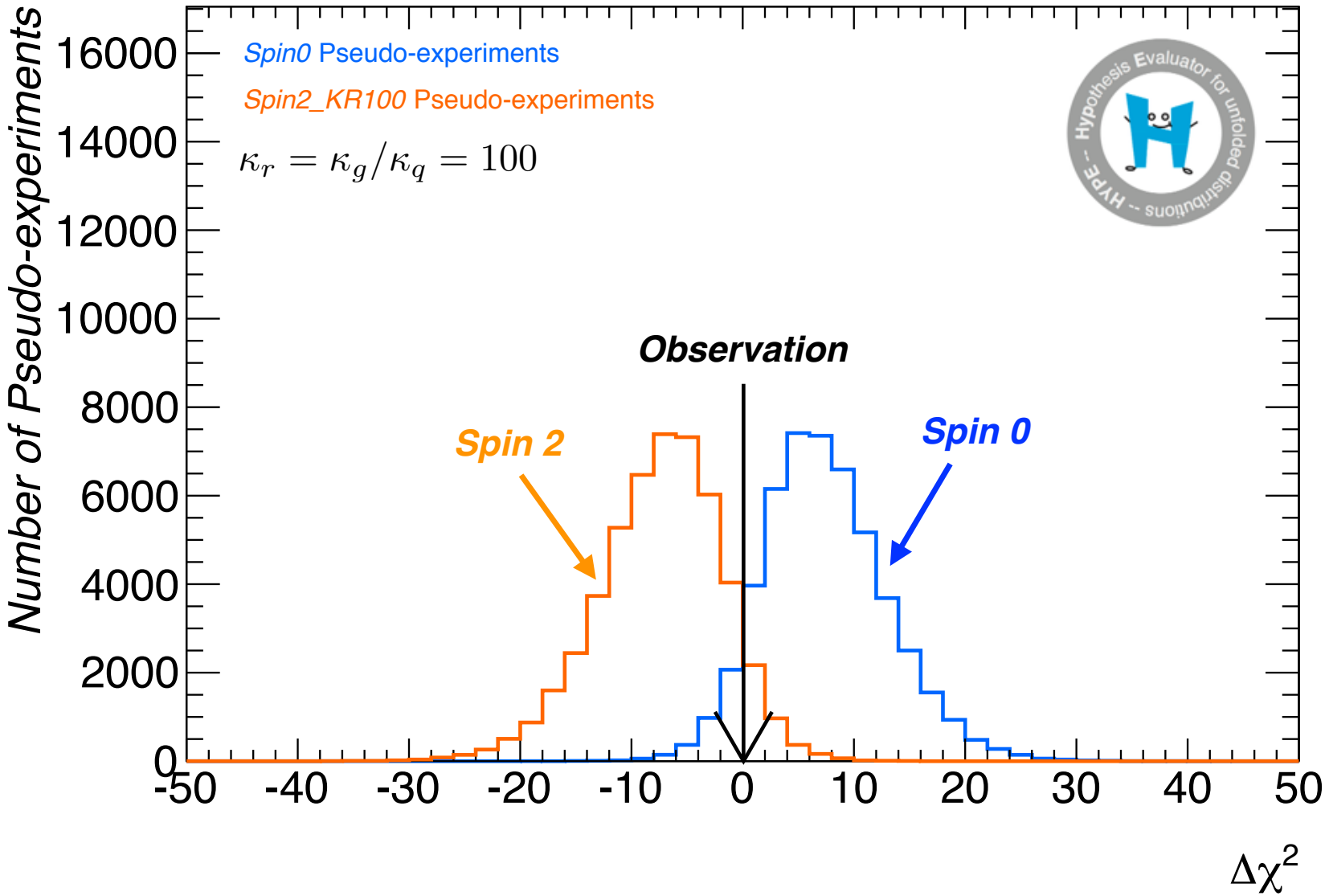
Predictions generated with with with aMC@NLO + Herwig++

Caveats: No theory uncertainties, no interference with background taken into account, private MC production

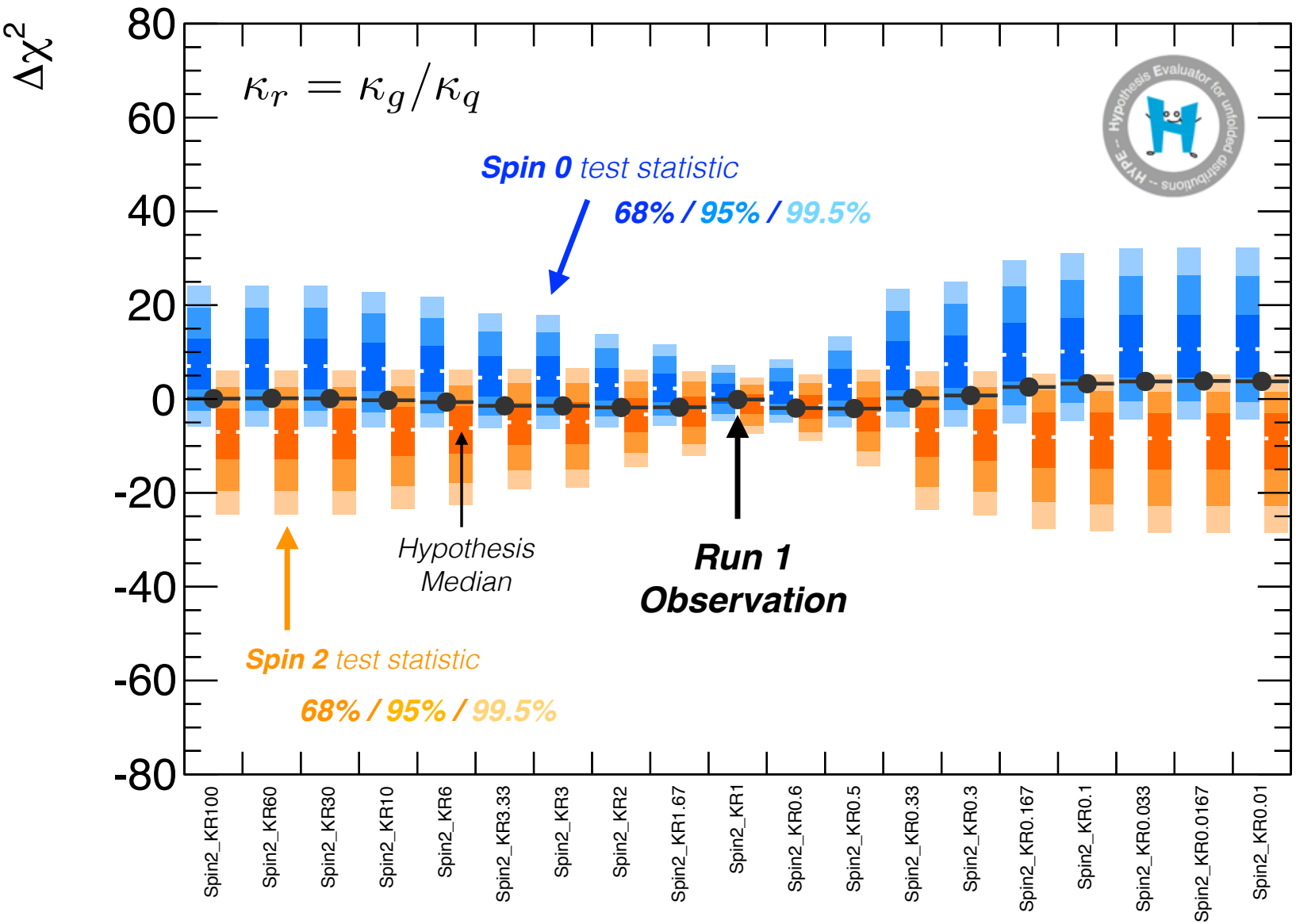
Fit result for $\kappa_r = 100$:



Test statistic for $\kappa_r = 100$:

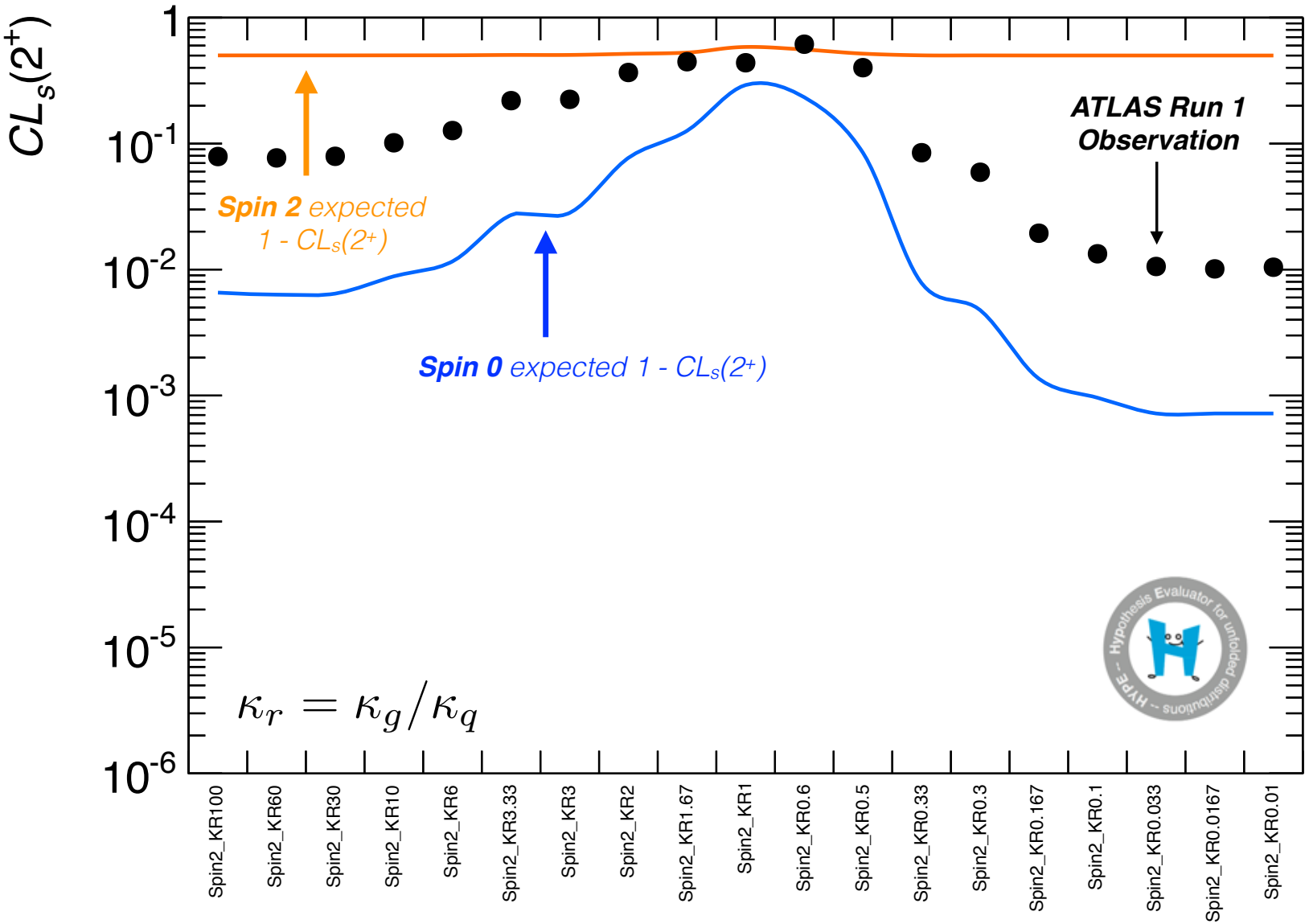


Scan for statistic for $\kappa_r = [100, 0.01]$:



Ratio scan from 100 to 0.01

$CL_s(2^+)$ for $\kappa_r = [100, 0.01]$:



Summary

Hype easy tool to be used to constrain alternative models, e.g. in the Higgs sector or at other places.

Current status:

* Core code written, extensively tested, rewritten, nicer rewritten and documented.
* Finalizing the code & documentation.

→ Hype will be made available around December on **Hepforge** with number of example analyses.

→ Fast toy option makes this very fast computationally

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Thank you!

Backup

Other observables – make your pick!