

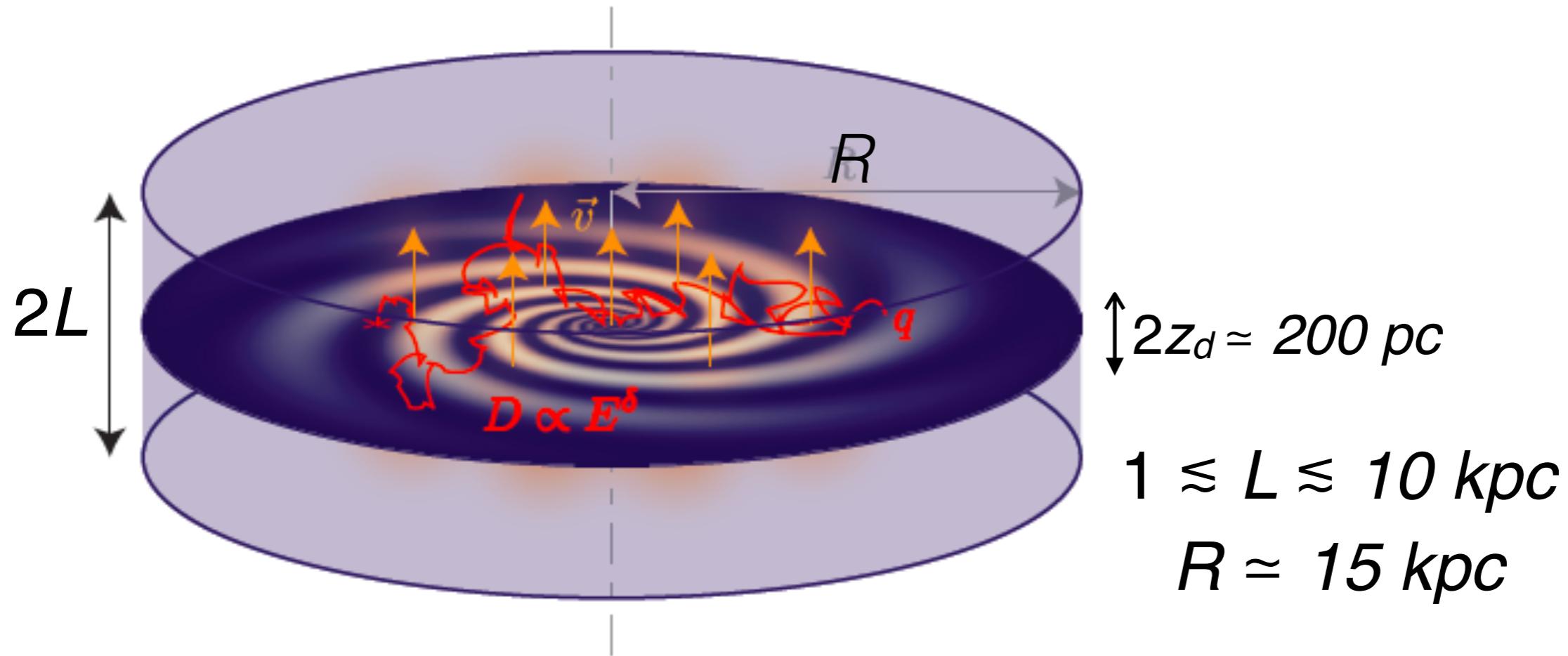
Cosmic ray propagation with DRAGON

few recipes to cook good models

D. GRASSO (INFN, Pisa)

CASPAR school, DESY 15-19 Sep. 2014

Geometry of the galactic CR pool



Our position: $R \approx 8.3 \text{ kpc}$ $z \approx 0$

CR nuclei

The transport equation (2d)

(Ginzburg & Syrovatsky, 1964)

Diffusion tensor

$$D(E) = D_0 (\rho/\rho_0)^\delta$$

ρ = rigidity $\sim p/Z$

Convection term

Energy loss

Reacceleration

$$D_{pp} \propto \frac{p^2 v_A^2}{D}$$

$$\begin{aligned} \frac{\partial N^i}{\partial t} - \nabla \cdot (D \nabla - v_c) N^i + \frac{\partial}{\partial p} \left(\dot{p} - \frac{p}{3} \nabla \cdot v_c \right) N^i - \frac{\partial}{\partial p} p^2 D_{pp} \frac{\partial}{\partial p} \frac{N^i}{p^2} = \\ = Q^i(p, r, z) + \sum_{j>i} c\beta n_{\text{gas}}(r, z) \sigma_{ji} N^j - c\beta n_{\text{gas}} \sigma_{\text{in}}(E_k) N^i \end{aligned}$$

SN source term.

We assume everywhere
a power law energy spectrum

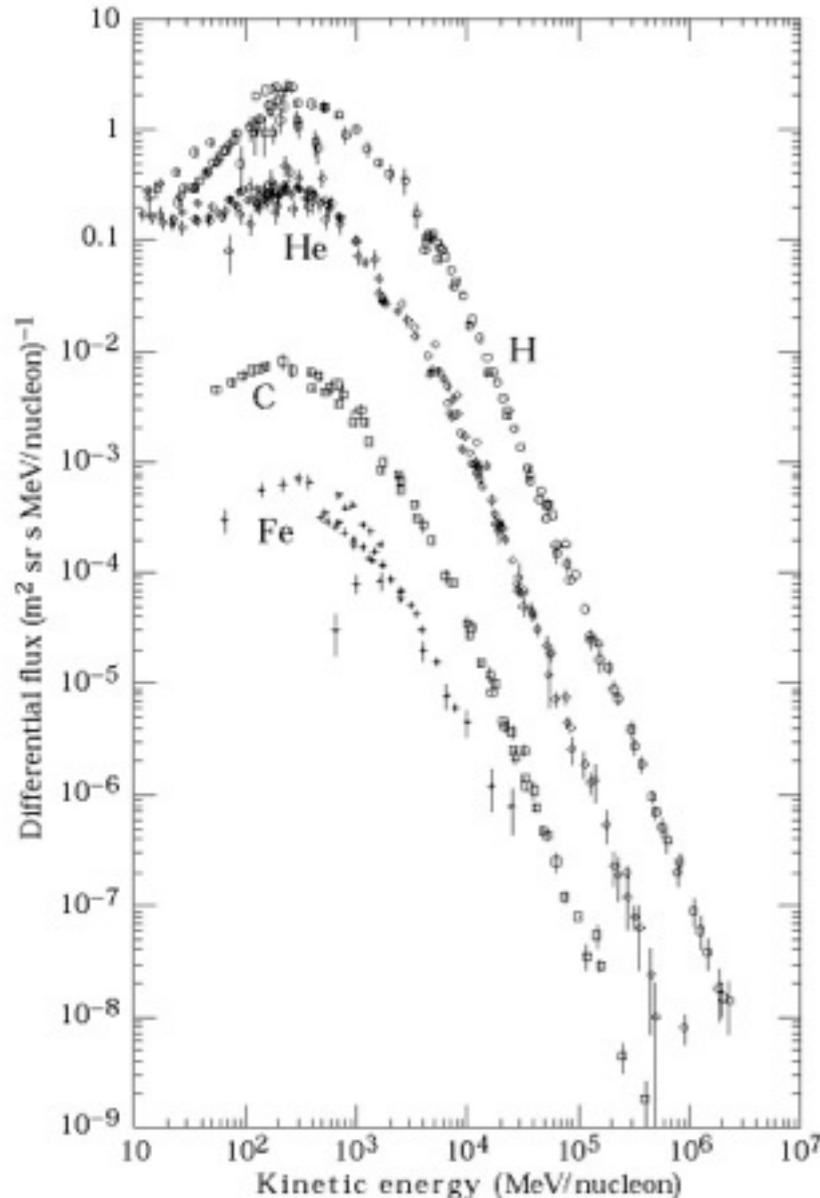
Spallation cross
section. Appearance
of nucleus i due to
spallation of nucleus j

Total inelastic cross
section.
Disappearance of
nucleus i

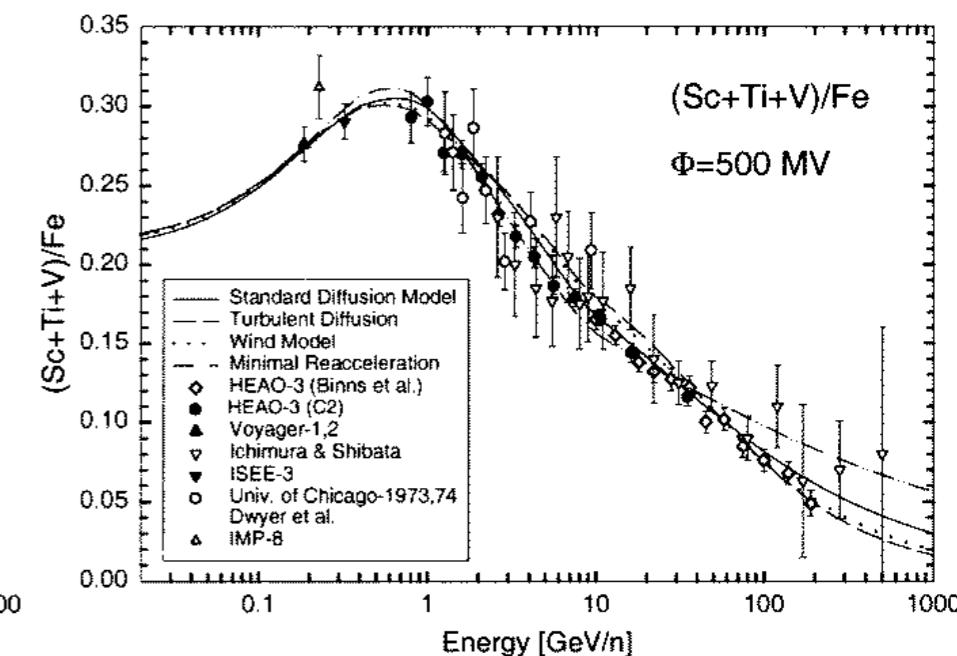
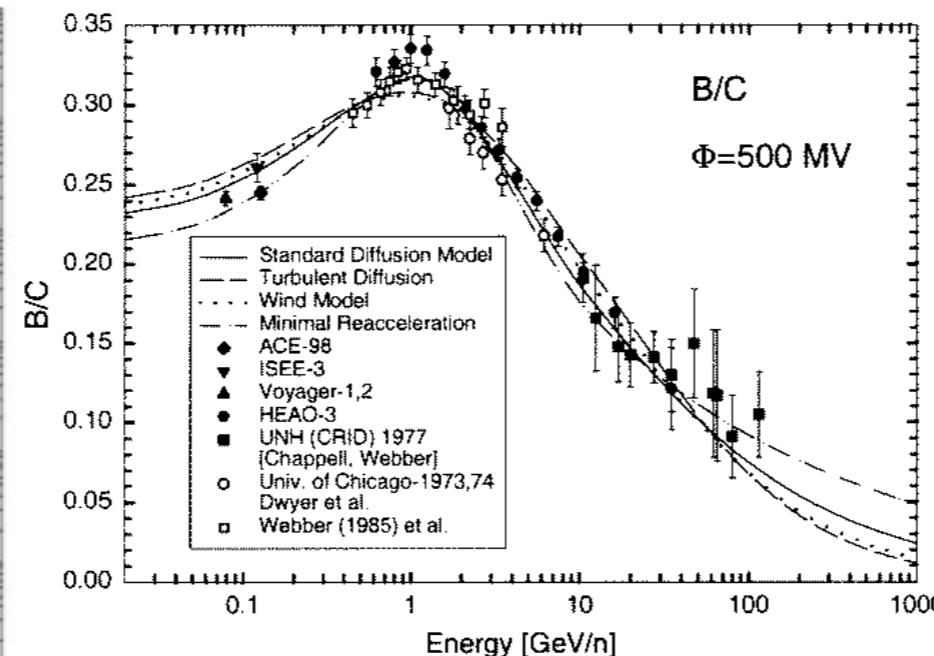
boundary condition: $N^i(r, z) = 0$ either for $r = R$ or $|z| = L$

A large number of parameters to be fixed against multichannel CR data !

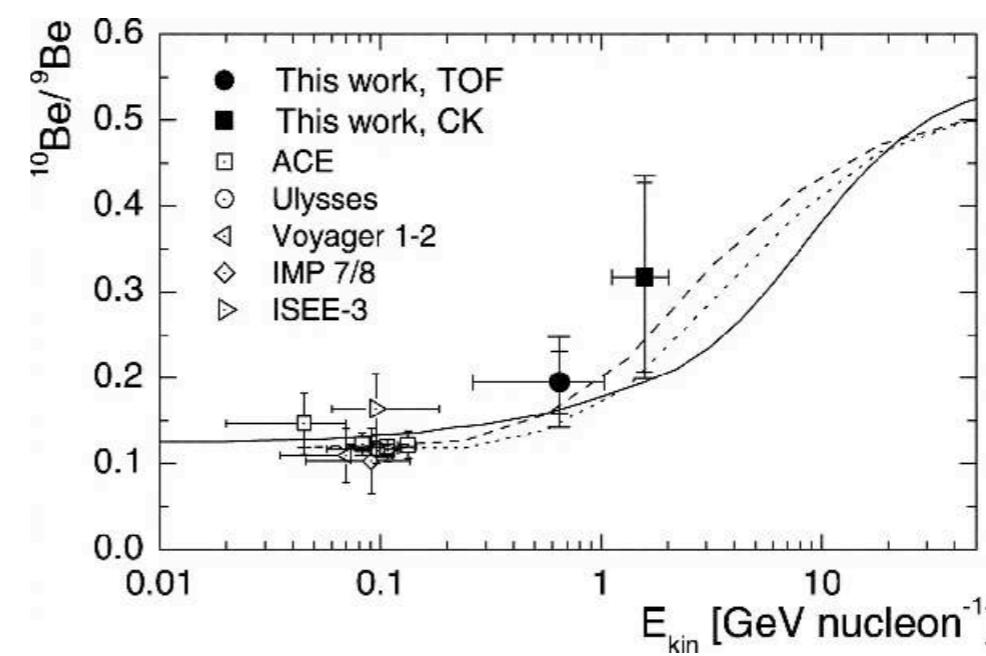
CR nuclei data



primary spectra



primary/secondary ratio of stable nuclei



primary/secondary ratio of unstable nuclei

Source term

- **Spatial dependence**

we assume sources trace SNRs

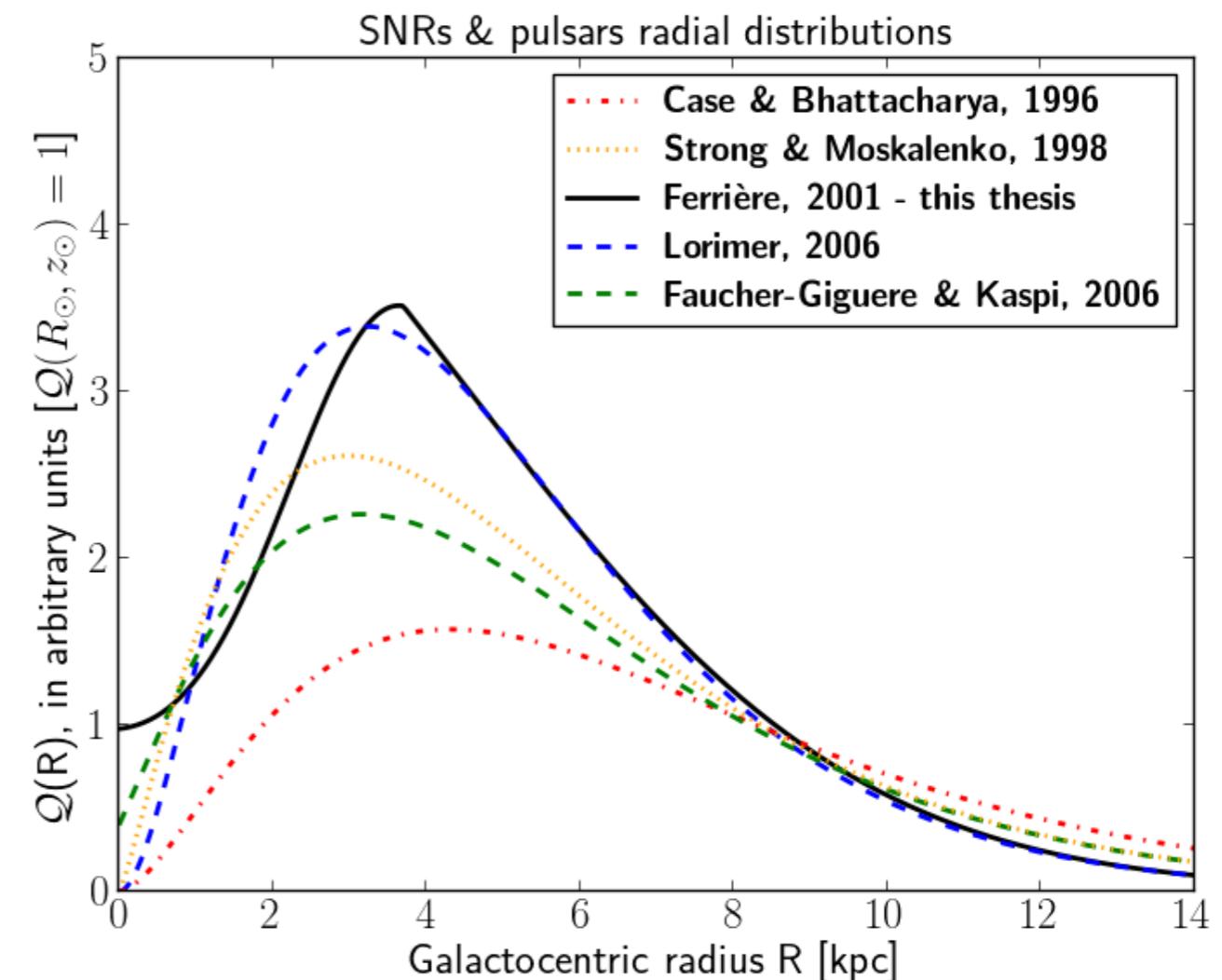
distributions implemented in
DRAGON: Galprop, Ferriere

in DRAGON 3D we can also account
for spiral arms

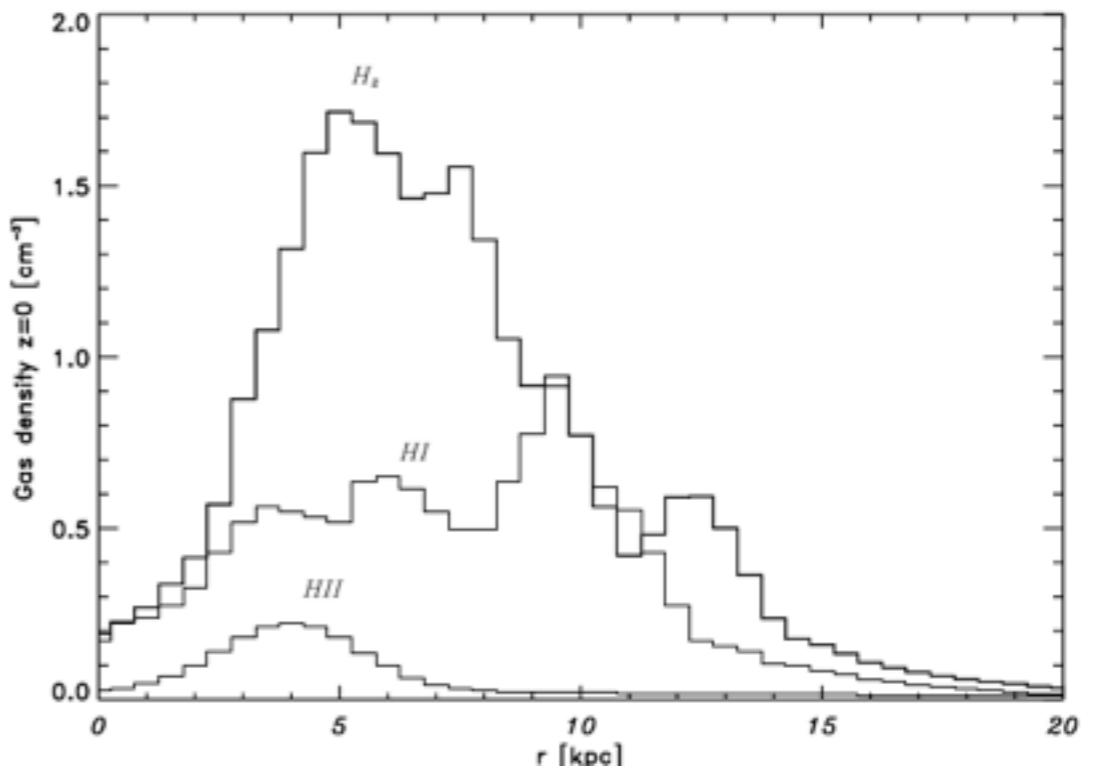
- **Rigidity dependence**

$$Q(\mathbf{x}, \rho) = Q_0(\mathbf{x}) \left(\frac{\rho}{\rho_0} \right)^{-\gamma}$$

we allow for several spectral
breaks (3 in the present version)



Gas distribution



$$n_{\text{H}_1}(R, z) = \frac{1}{n_{\text{GB}}} Y(R) \times \begin{cases} \sum_{i=1,2} A_i e^{-\ln 2 (z^2/z_i^2)} + A_3 e^{-|z|/z_3}, & R \leq 8 \text{kpc} \\ \text{interpolato,} & 8 < R < 10 \text{kpc} \\ n_{\text{DL}} \exp(-z^2 e^{-0.22R}/z_4^2), & R \geq 10 \text{kpc} \end{cases} \quad \text{Gordon \& Burton 1976}$$

$$n_{\text{H}_2}(R, z) = 3.24 \times 10^{-22} X Q_{\text{co}}(R) \exp \left(-\ln 2 \left[\frac{(z - z_0)^2}{z_{1/2}^2} \right] \right) \quad \text{Bronfman, 1998}$$

$$X \equiv \frac{n_{\text{H}_2}}{Q_{\text{co}}} = 1.9 \times 10^{20} \text{moli cm}^{-2}/(\text{K km s}^{-1}),$$

see Ferriere review, 2001

Diffusion equation

Particle flux, 1-dim. $J = nv - D \frac{\partial n}{\partial x_i}$ \Rightarrow 3-dim. $J_i = nv_i - \sum_{j=1}^3 D_{ij} \frac{\partial n}{\partial x_i}$

Particle number conservation \Rightarrow $\frac{\partial n}{\partial t} = - \frac{\partial J_i}{\partial x_i}$

$$\boxed{\frac{\partial n}{\partial t} + \frac{\partial}{\partial x_i} (nv_i) + \frac{\partial}{\partial x_i} \left(D_{ij} \frac{\partial n}{\partial x_j} \right) = q(\vec{x}, t)}$$

$q(\vec{x}, t)$: source term

In the presence of a regular magnetic field one expects isotropy to be broken and

$$D_{ij}(\vec{x}) = (D_{\parallel}(\vec{x}) - D_{\perp}(\vec{x})) b_i(\vec{x}) b_j(\vec{x}) + D_{\perp}(\vec{x}) \delta_{ij} \quad : \text{diffusion tensor}$$

$b_i(\vec{x})$: regular magnetic field versor

$$[D_{ij}] = : \text{length}^2 / \text{time}$$

Diffusion equation

for uniform and isotropic diffusion $D_{ij}(\mathbf{x}) = D \ \delta_{ij}$

and a bursting source $q(E, \vec{x}, t) = q(E)\delta(\vec{x}; t)$

$$N(E, r, t) = \frac{q(E)}{\pi^{3/2} R_{\text{diff}}^3} \exp\left(-\frac{r^2}{R_{\text{diff}}^2}\right)$$

$$R_{\text{diff}}(t) = 2\sqrt{Dt} \quad : \text{diffusion length}$$

$$t_{\text{diff}}(L) \simeq \frac{L^2}{D} \quad : \text{diffusion time on a length L}$$

smaller/larger D \Rightarrow slower/faster diffusion out of the source region

Diffusion coefficient

Here we assume isotropic diffusion

note that for azimuthal symmetry only one component (D_{\perp}) is relevant anyhow

$$D(\mathbf{x}, \rho) = D_0(\mathbf{x}) (\rho/\rho_0)^{\delta}$$

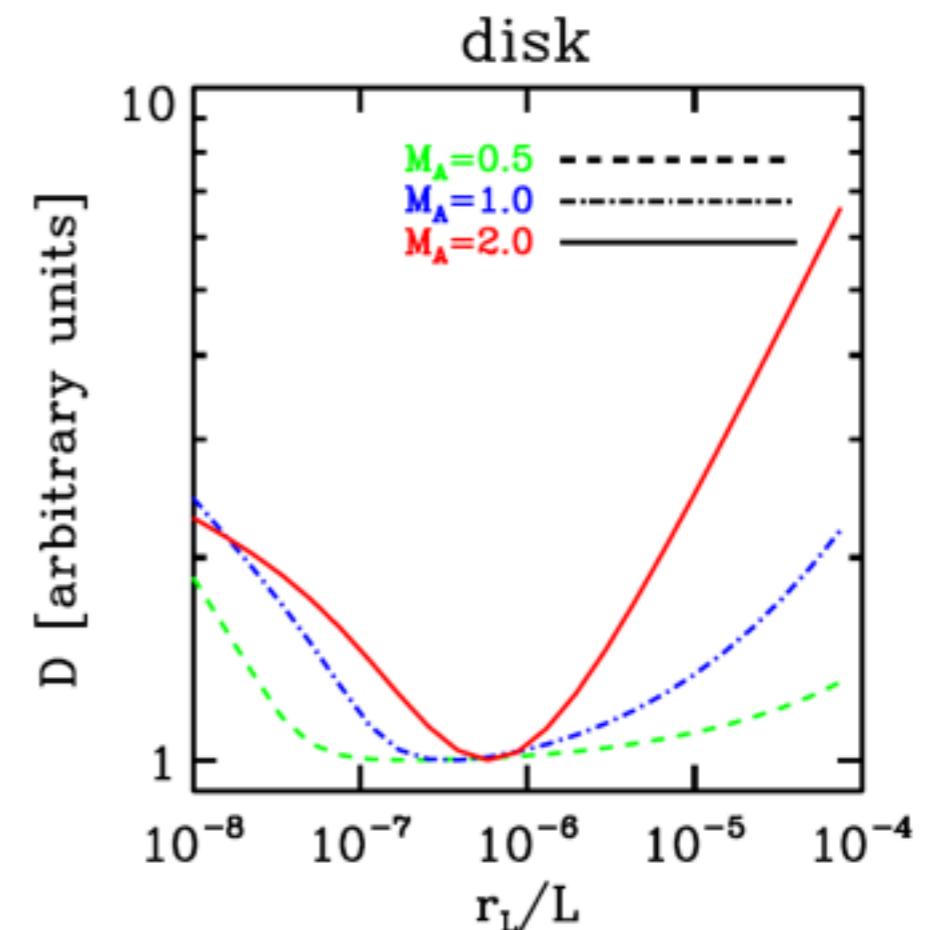
where $\rho = p/Ze$: magnetic rigidity

At low energy dissipation of MHD turbulence may come in (see e.g. Ptuskin et al. ApJ 2006; Evoli & Yan 2013) giving rise to faster CR escape

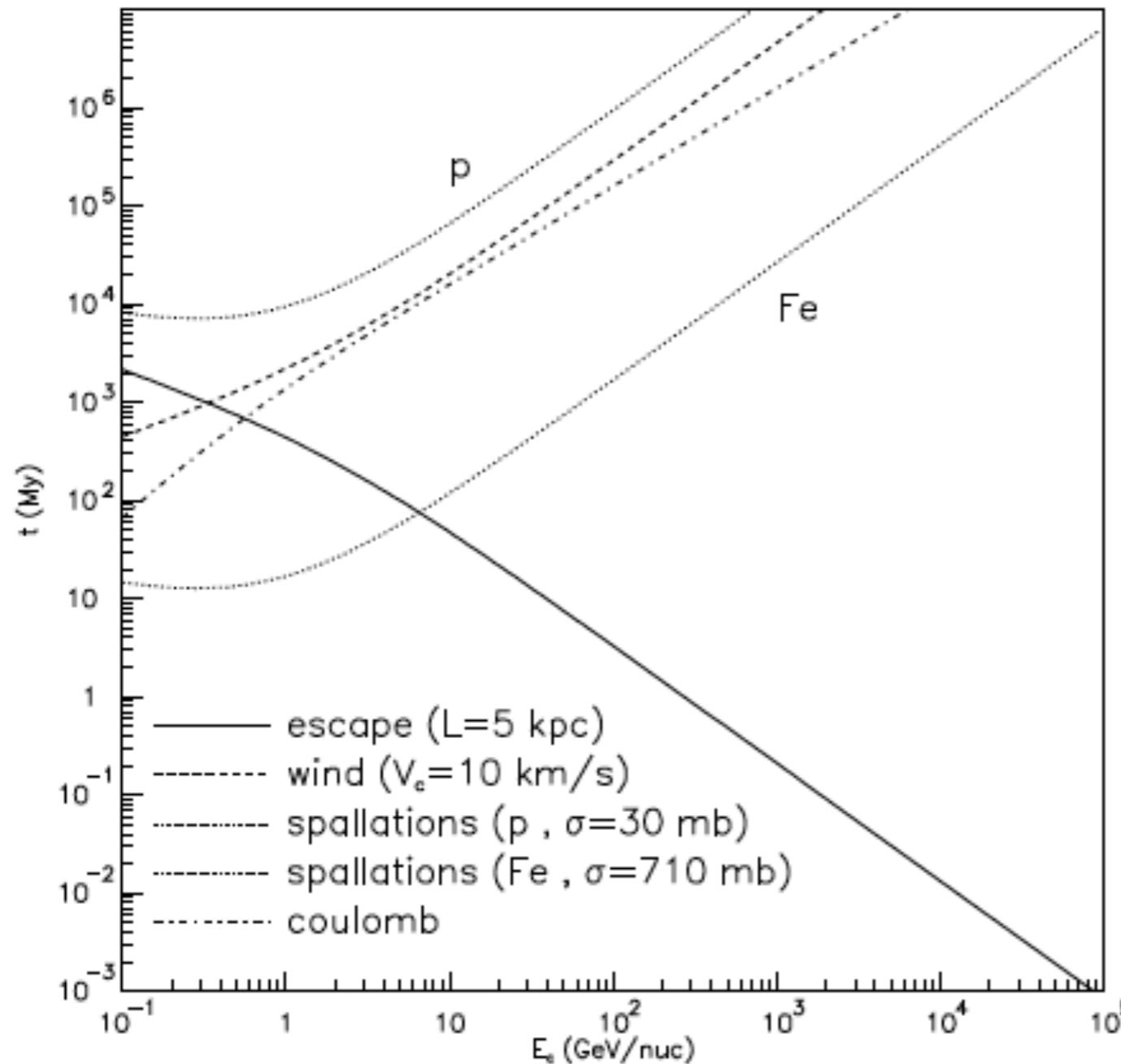
This is often parametrized introducing

$$D(\mathbf{x}, \rho) = D_0(\mathbf{x}) (\rho/\rho_0)^{\delta} \beta^{\eta}$$

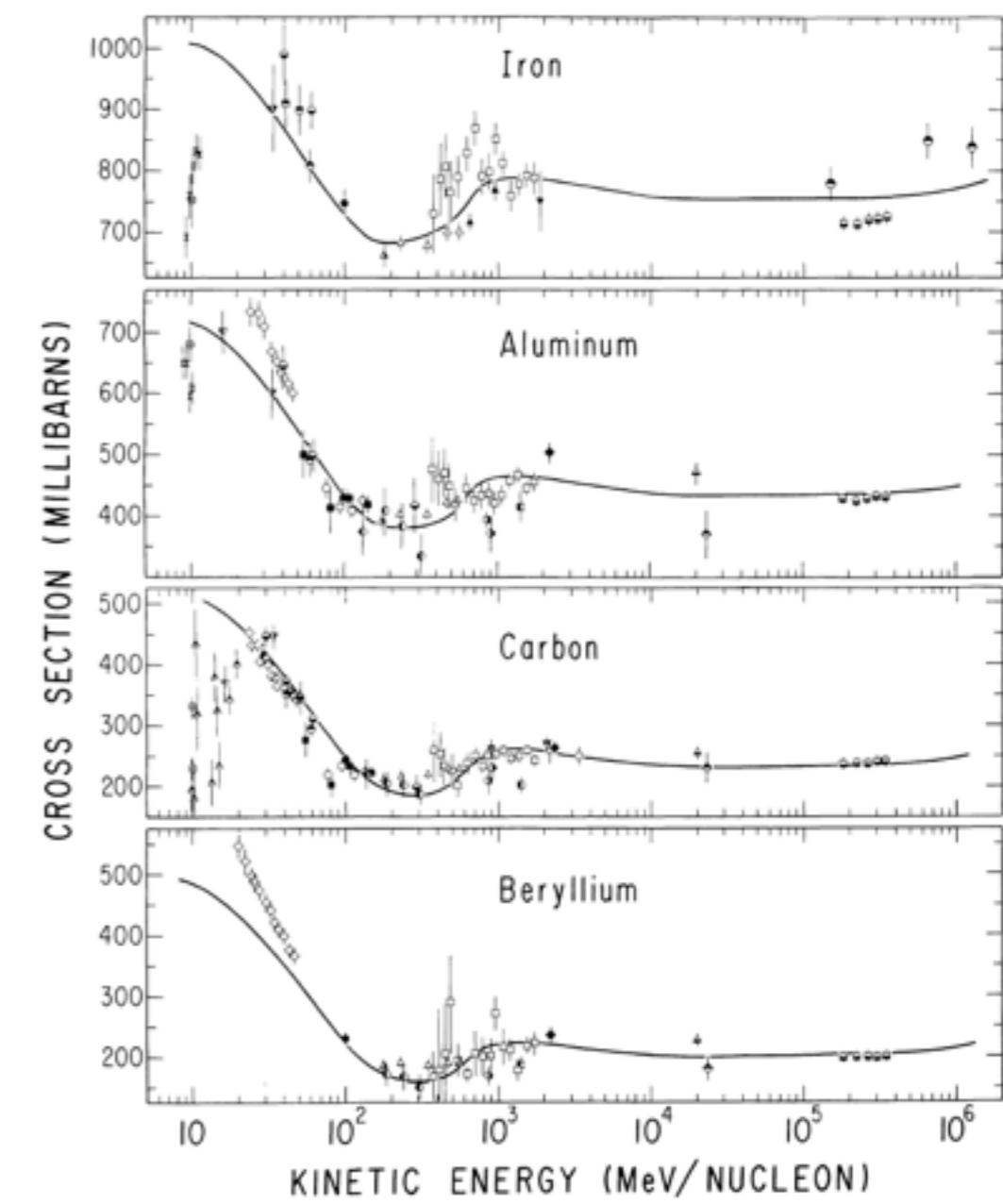
where $\eta < 0$ $\beta = v/c$



Nuclei losses



some spallation cross sections



$$\text{for } E_k \geq 2 \text{ GeV/n} \quad \sigma_{\text{tot}}^{\text{in}} = 45 A^{0.7} [1 + 0.016 \sin(5.3 - 2.63 \ln A)] \text{ mb} \quad \text{Letaw et al. '83}$$

see also Tang & Ng 1983

Nuclei losses

Castellina & Donato 2005

above $\sim 100 \text{ GeV/n}$
 energy losses become energy independent (other effect are also negligible at those energies, see below), hence CR spectra are determined by diffusion. Hence from a simple leaky box model

for primary nuclei spectra

$$N_i(E) \equiv \frac{dN_i}{dE} \propto Q_i(E) \tau_{\text{esc}}(E) \propto E^{-(\alpha_i + \delta)}$$

for primary/secondary ratio

$$\frac{N_p(E)}{N_s(E)} \propto E^{-\delta}$$

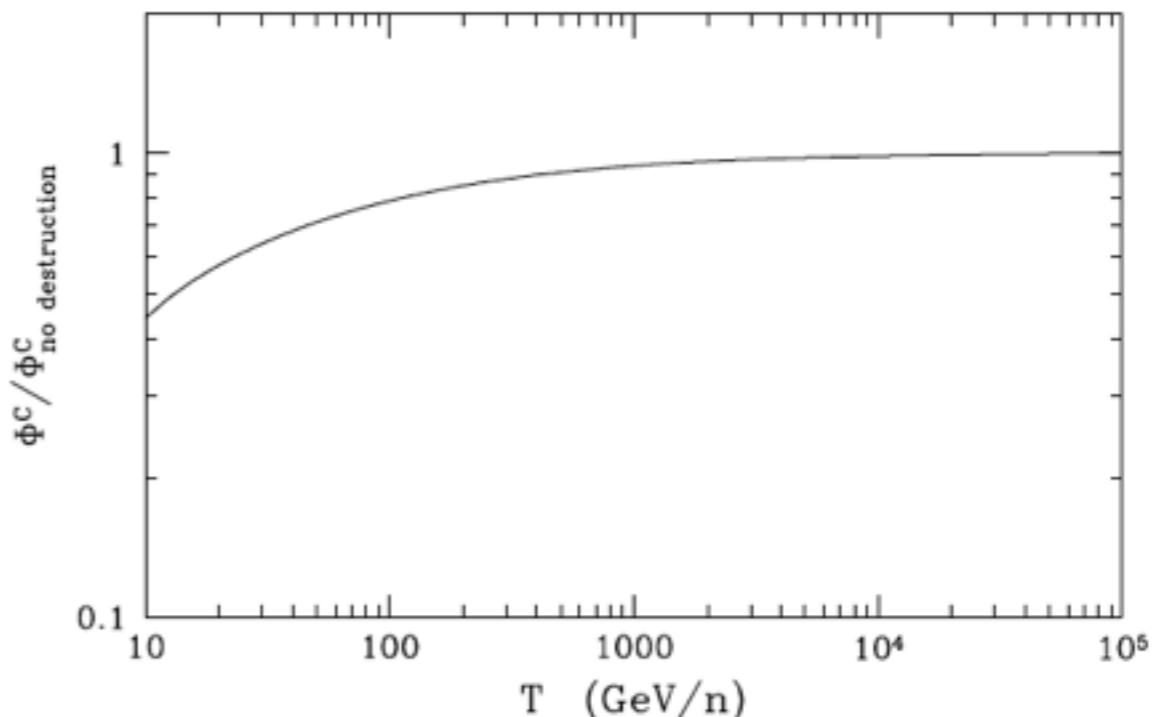
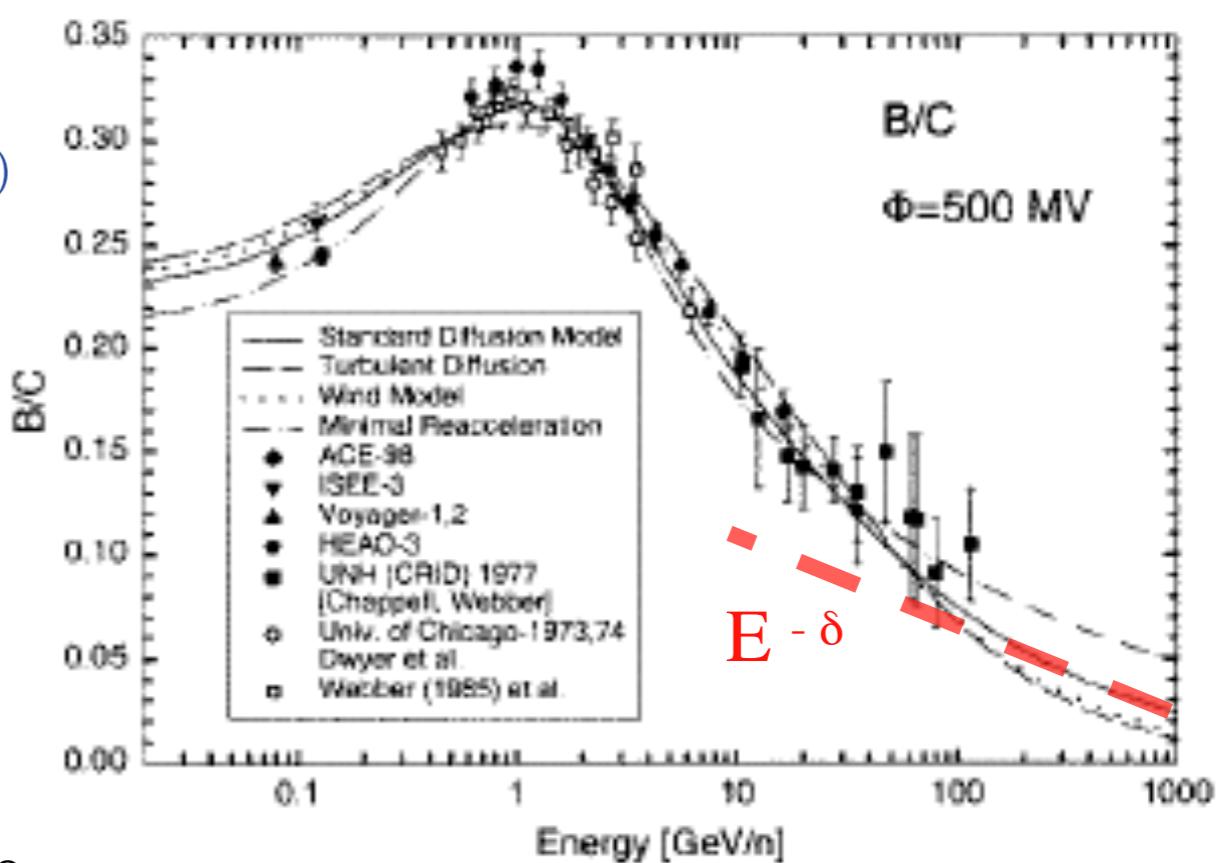


Fig. 4. Ratio of calculated carbon fluxes from the same propagation model, where nuclear destructions have been turned off at the denominator.



Reacceleration and convection

- Reacceleration

due to stochastic scattering onto MHD waves (Fermi 2nd order acc.)

For a given detection energy it increases the residence time respect to the no reaccelerating case (more secondaries)

in the quasi-linear theory $D_{pp} = p^2 V_A^2 / (9 D)$

$V_A = B^2 / (4\pi \rho_{\text{plasma}}) \approx 10 \text{ km}^2/\text{s}$ in the ISM (large uncertainty)

Berezinsky et al. 1990, Schlickeiser 2002

- Convection

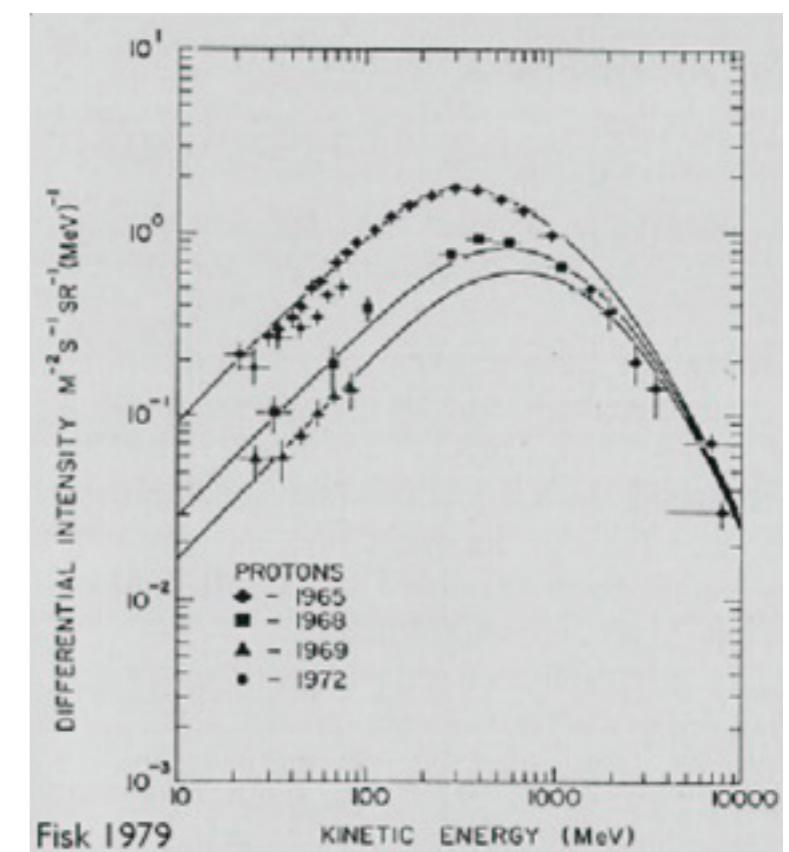
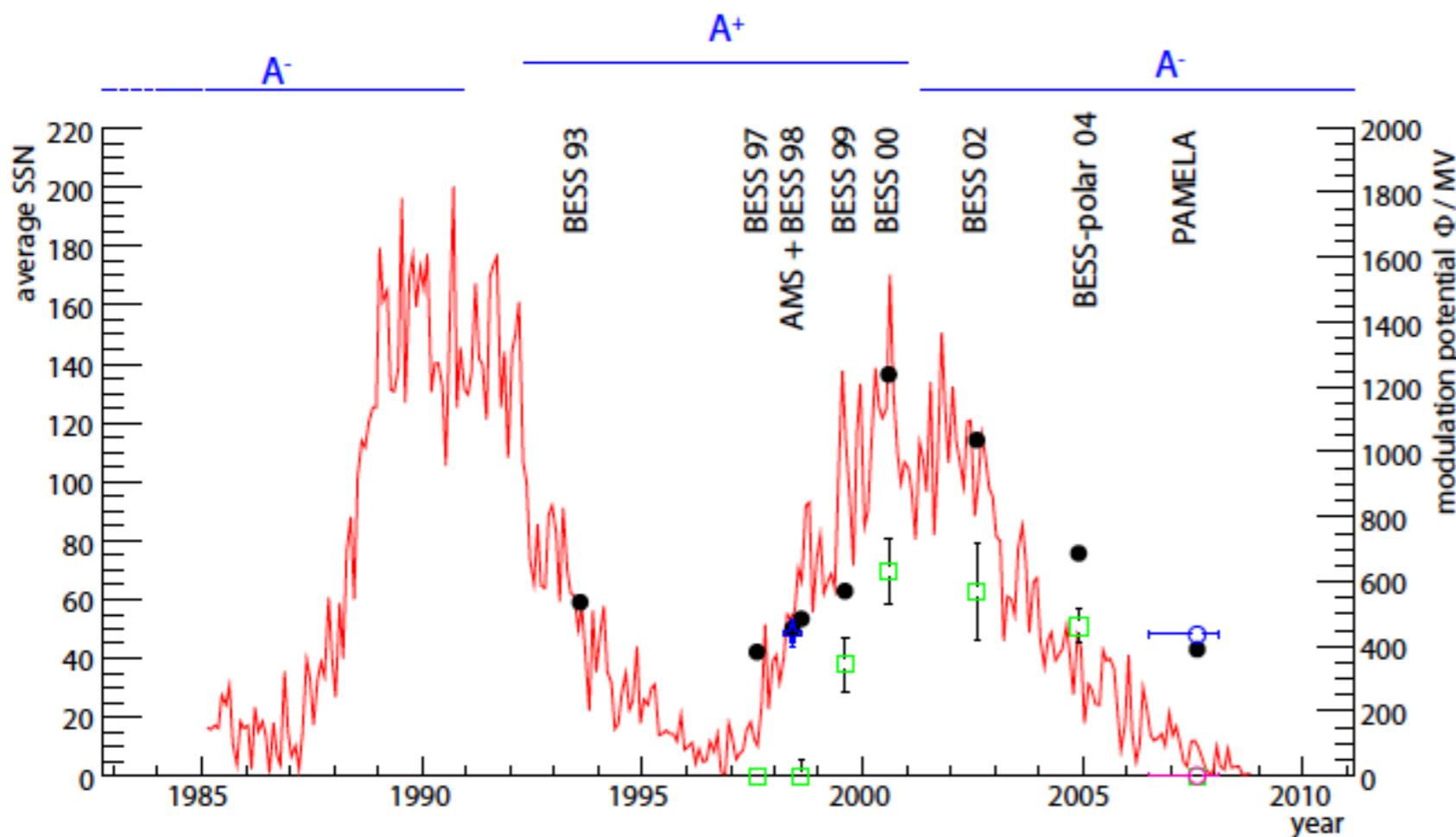
$$\frac{dE}{dt} = -\frac{2}{3} \frac{nV}{N} E (\nabla \cdot v) = -\frac{2}{3} (\nabla \cdot v) E$$

evidence of winds are observed with speed as high as 100 km/s

They should transport and induce adiabatic cooling of low energy CR

Take in mind that V_C may also depend on R

Solar modulation

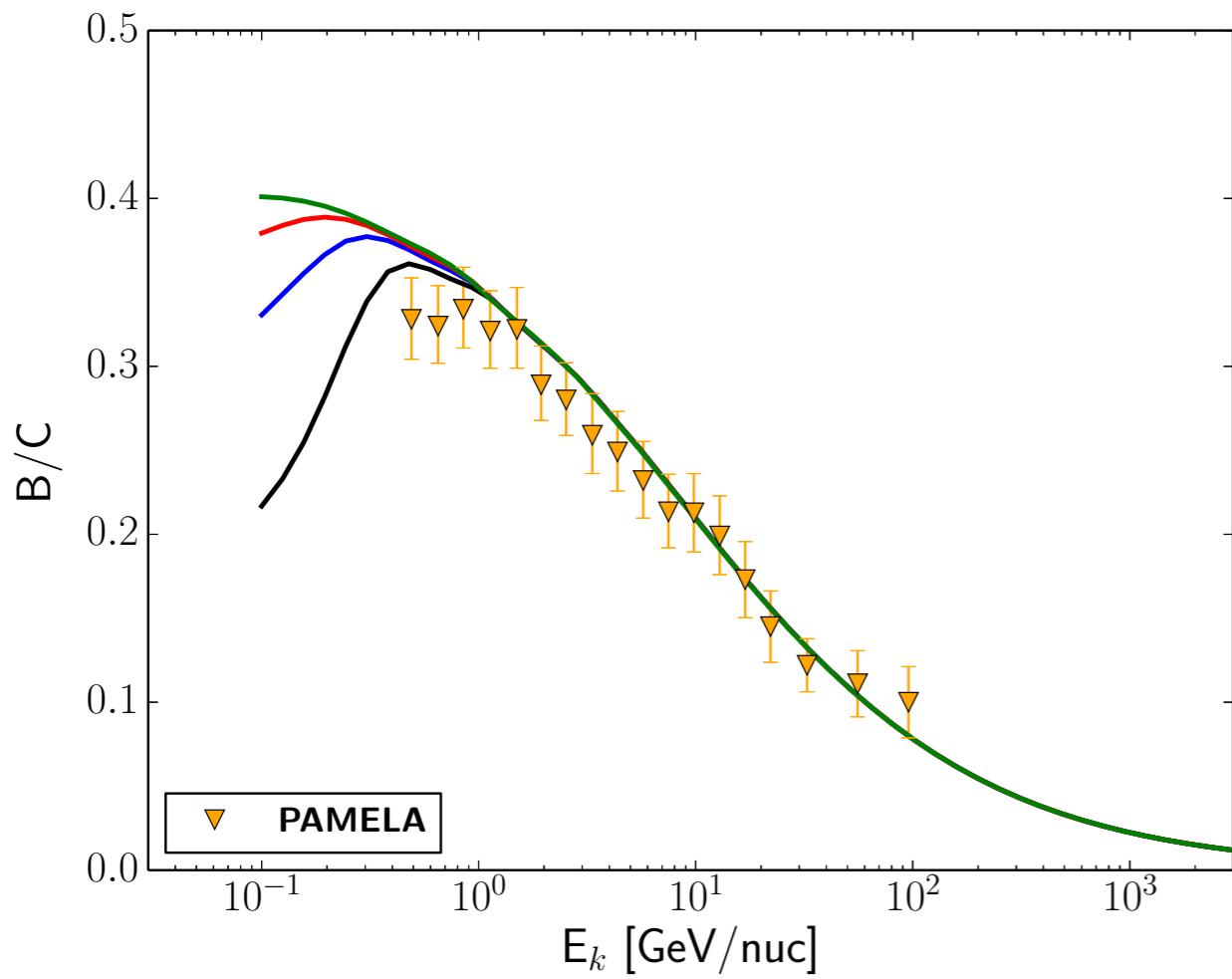


Solar modulation (force field approximation)

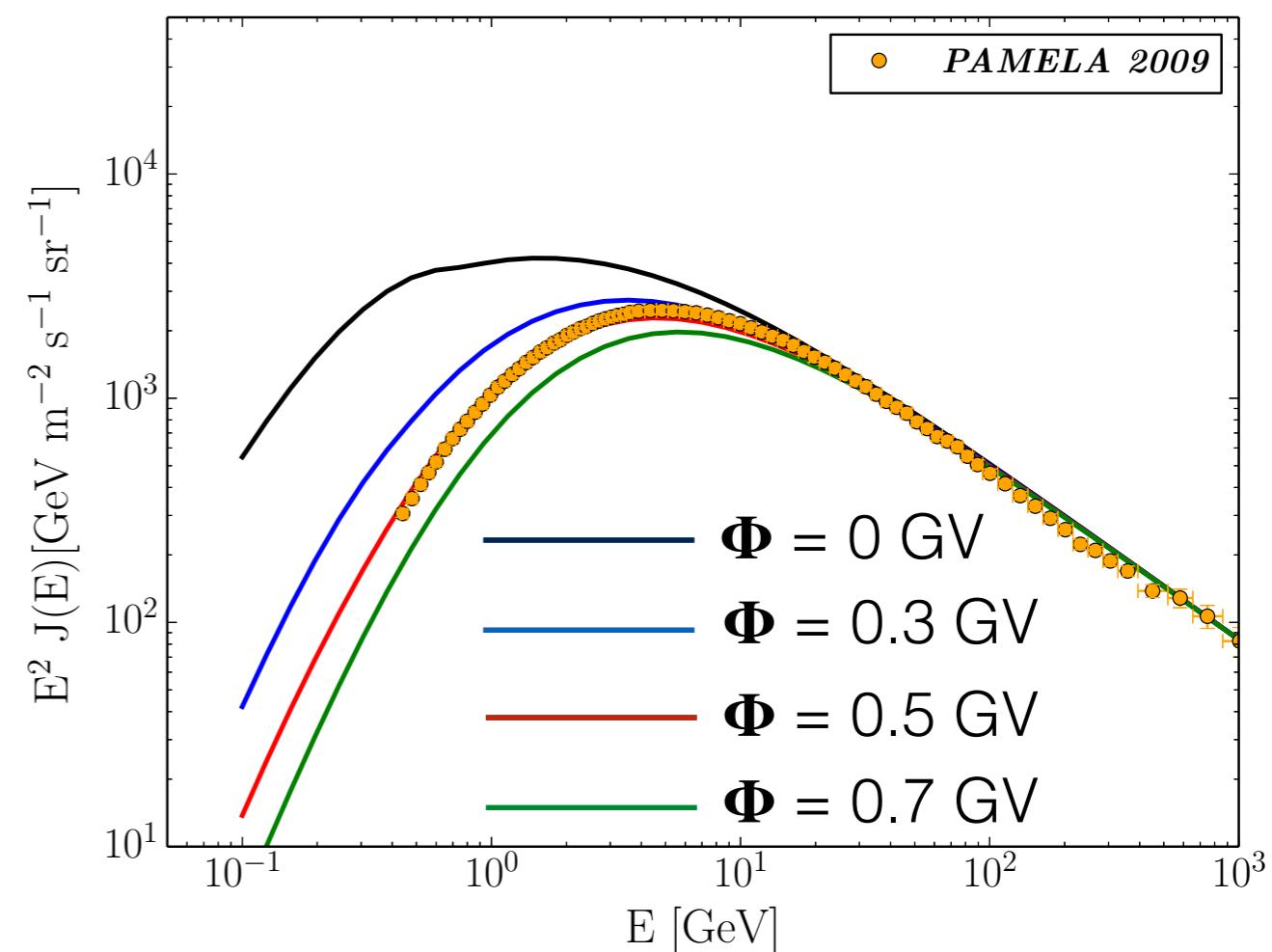
Gleeson & Axford 1968

$$J(E_k, Z, A) = \frac{(E_k + m)^2 - m^2}{\left(E_k + m + \frac{Z|e|}{A}\Phi\right)^2 - m^2} J_{\text{LIS}}(E_k + \frac{Z|e|}{A}\Phi, Z, A)$$

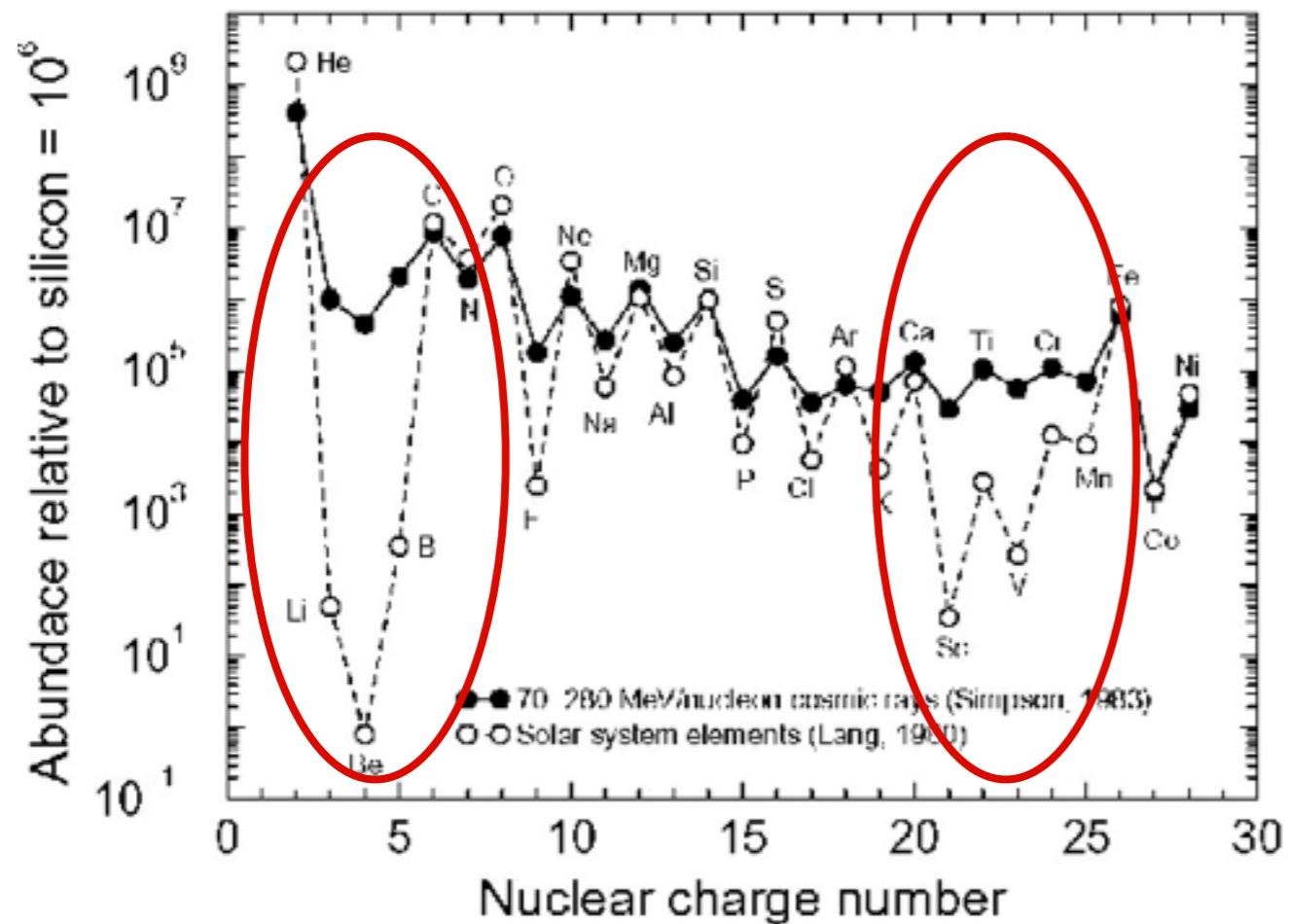
modulated spectrum



DRAGON output



Diffusion parameters from secondary-primary ratio



In order to reproduce the measured abundances of stable nuclei, CRs should have traversed: $\sim 10 \text{ g cm}^{-2}$ of material:

Primary species are present in sources (CNO, Fe). Produced by stellar nucleosynthesis. Acceleration in SN shocks ($\geq 10^4 \text{ yr}$).

Secondary species are absent of sources (LiBeB, SubFe). Produced during propagation of primaries.

J.A. Simpson, Ann. Rev. Nucl. Part. Sci. 33 (1983) 323

Plain diffusion - uniform D

$D - L$ are **almost** degenerate

(for spherical symmetry $\tau_{esc} \propto \frac{R^2}{D}$)

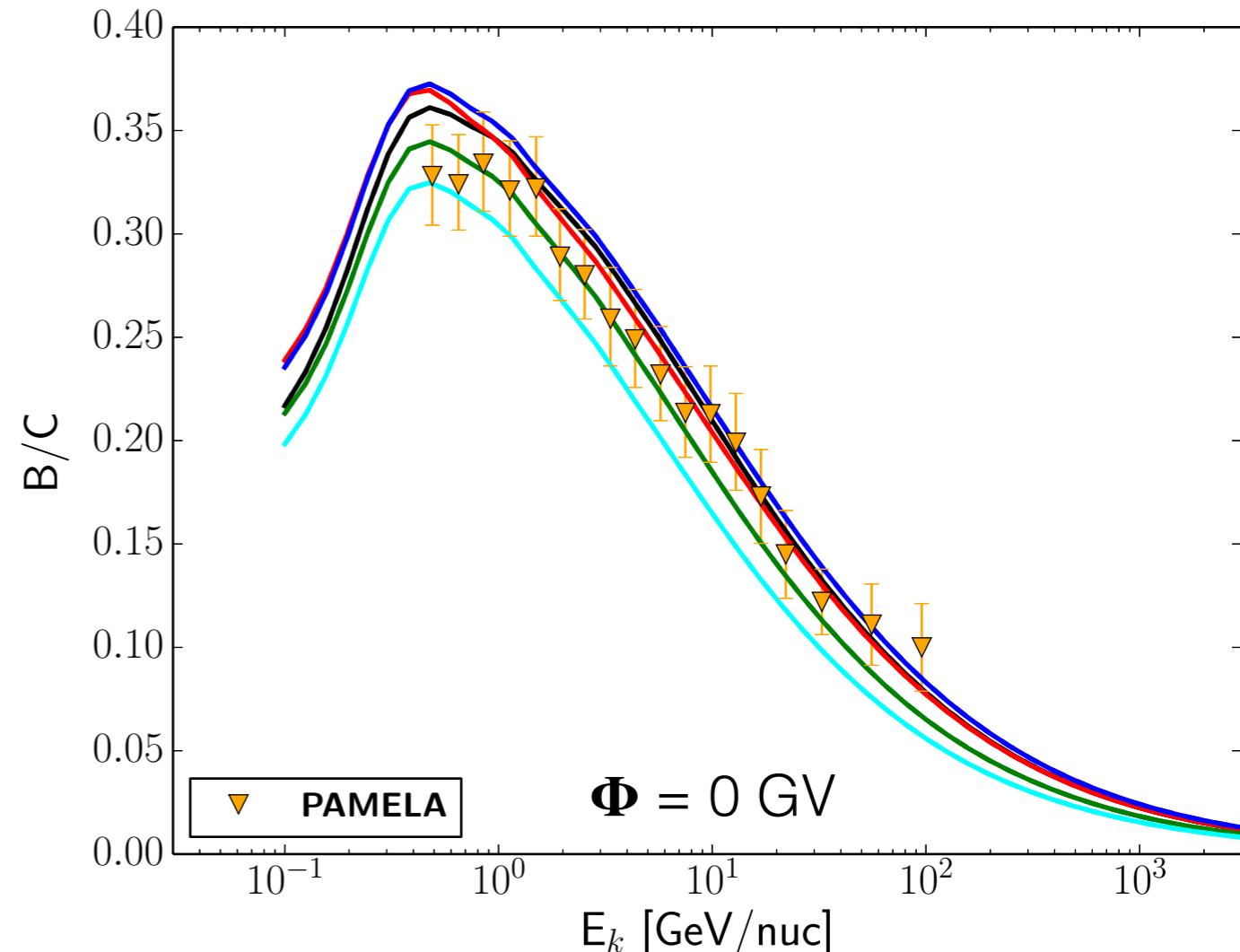
In the plot $D_0/L = 0.675 = \text{const}$

where D_0 is in units of $10^{28} \text{ cm}^2/\text{s}$ and
 L “ “ of kpc

good degeneracy only for low L !

($Z_{\max} = 14$ is enough for modeling B/C)

for the models in the plot
 $\delta = 0.6, v_A = 0, v_C = 0, \eta = 1$; dimensions = 2
 $\Phi = 0$



- $L = 1 \text{ kpc}$
- $L = 2 \text{ kpc}$
- $L = 4 \text{ kpc}$
- $L = 6 \text{ kpc}$
- $L = 8 \text{ kpc}$

Plain diffusion - uniform D

$D - L$ are **almost** degenerate

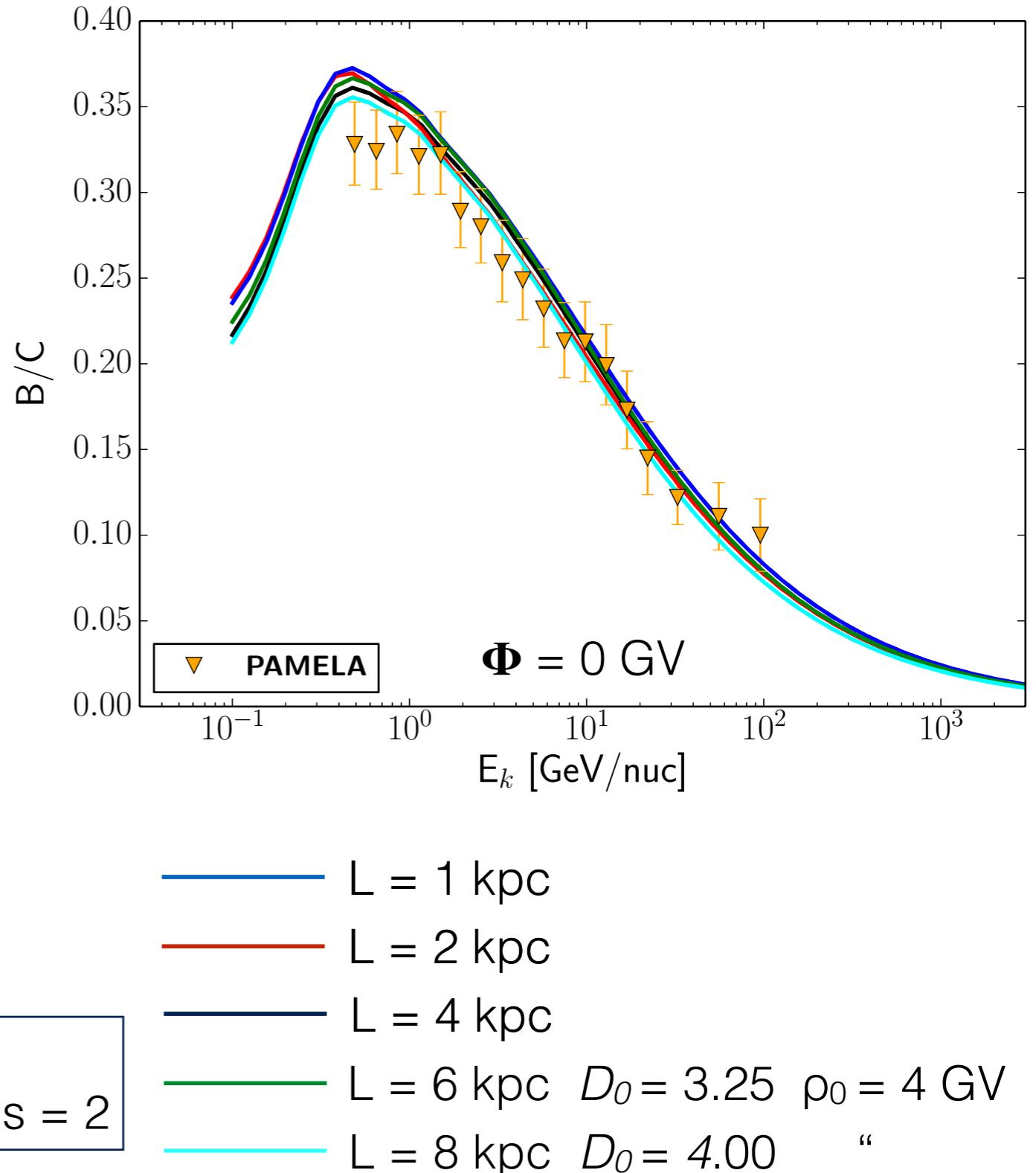
(for spherical symmetry) $\tau_{esc} \propto \frac{R^2}{D}$)

In the plot $D_0/L = 0.675$
only for $L = 1, 2, 4$ kpc

where D_0 is in units of $10^{28} \text{ cm}^2/\text{s}$ and
 L " " of kpc

degeneracy is restored after rescaling
 D_0 , \rightarrow we cannot use the B/C to
 constrain L !

for the models in the plot
 $\delta = 0.6, v_A = 0, v_C = 0, \eta = 1$; dimensions = 2



Plain diffusion - uniform D

$D - L$ are **almost** degenerate

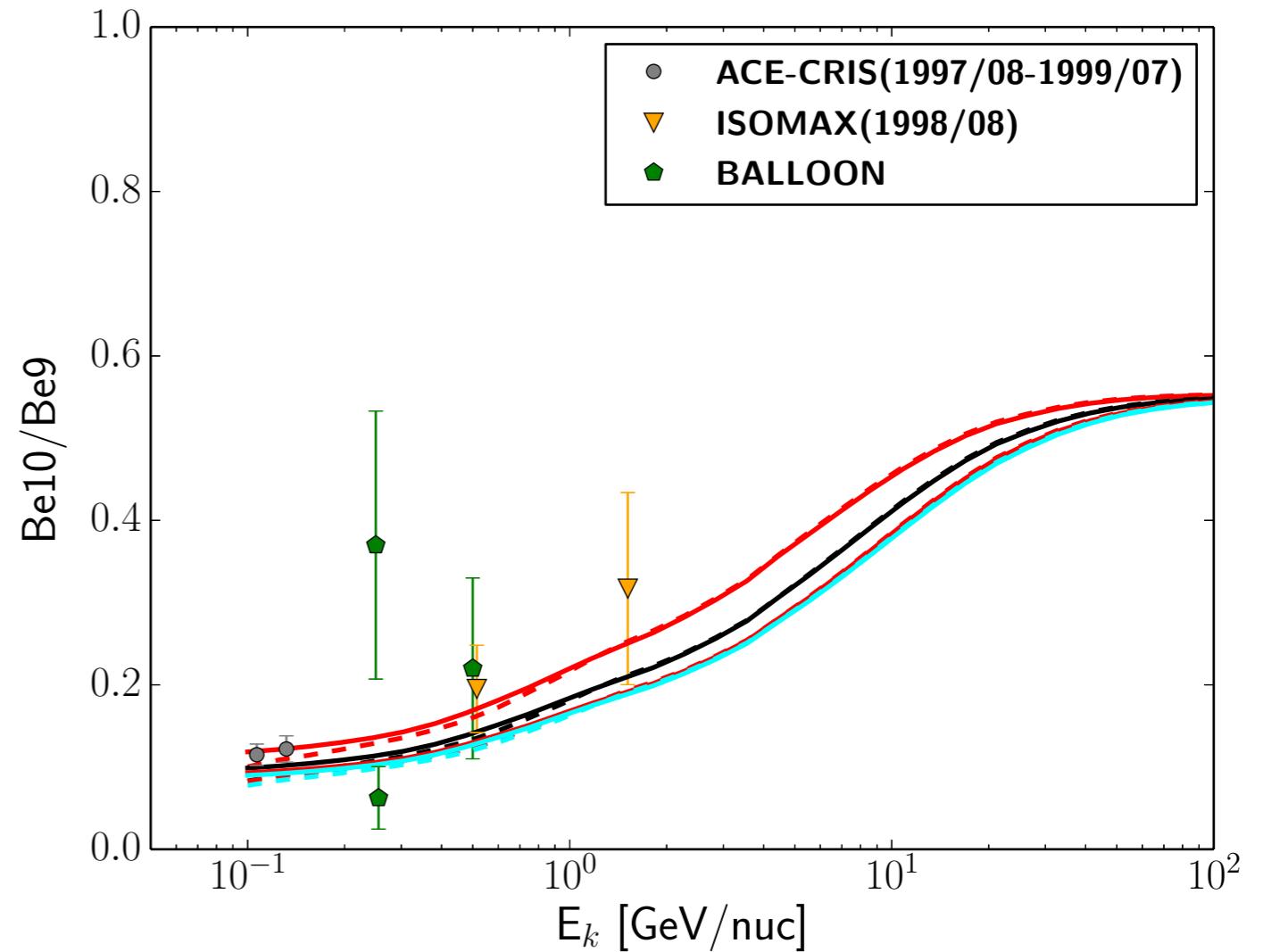
(for spherical symmetry)

$$\tau_{esc} \propto \frac{R^2}{D}$$

In the plot $D_0/L = 0.675$
only for $L = 1, 2, 4$ kpc

where D_0 is in units of $10^{28} \text{ cm}^2/\text{s}$ and
 L " " of kpc

degeneracy is restored after rescaling
 D_0 , → we cannot use the B/C to
 constrain L !



for the models in the plot
 $\delta = 0.6, v_A = 0, v_C = 0, \eta = 1$; dimensions = 2

$\text{--- } L = 2 \text{ kpc}$ $\text{--- } L = 4 \text{ kpc}$ $\text{--- } L = 6 \text{ kpc } D_0 = 3.25 \rho_0 = 4 \text{ GV}$ $\text{--- } L = 8 \text{ kpc } D_0 = 4.00 \text{ "}$
--

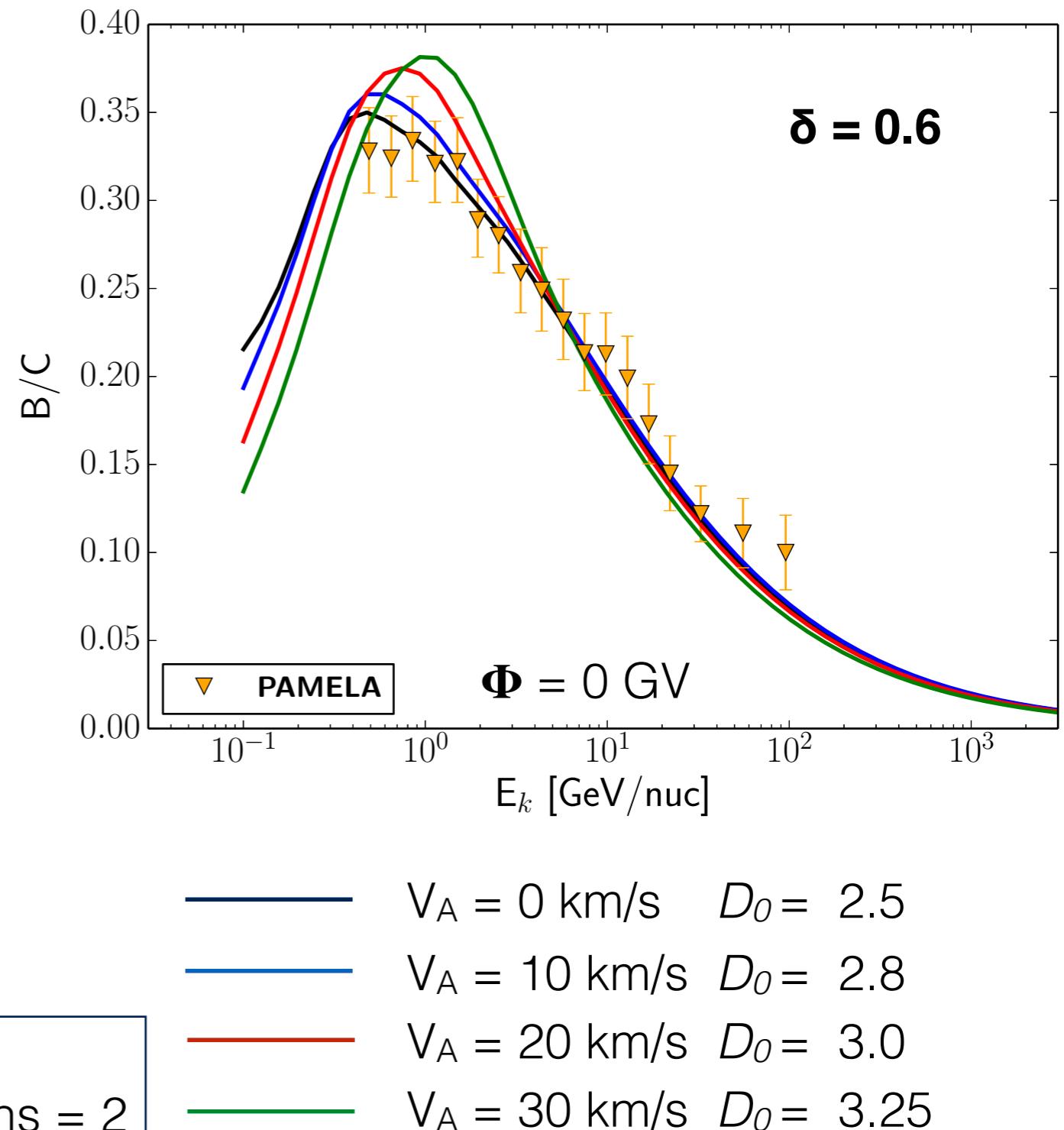
The effect of reacceleration

Generally this is parametrized in terms of V_A entering in D_{pp}

increasing V_A , particles detected at a given E have spent some time at lower energy, hence they had a larger residence time with respect to the case with $V_A = 0 \rightarrow$ more secondaries !

When changing V_A , D_0 has to be rescaled

to reproduce the B/C above 10 GeV/n
(above that energy the effects of
reacceleration are negligible for realistic V_A)



for the models in the following plots

δ = 0.6, $L = 4 \text{ kpc}$, $v_C = 0$, $\eta = 1$; dimensions = 2
 $D(z)$ exponential;

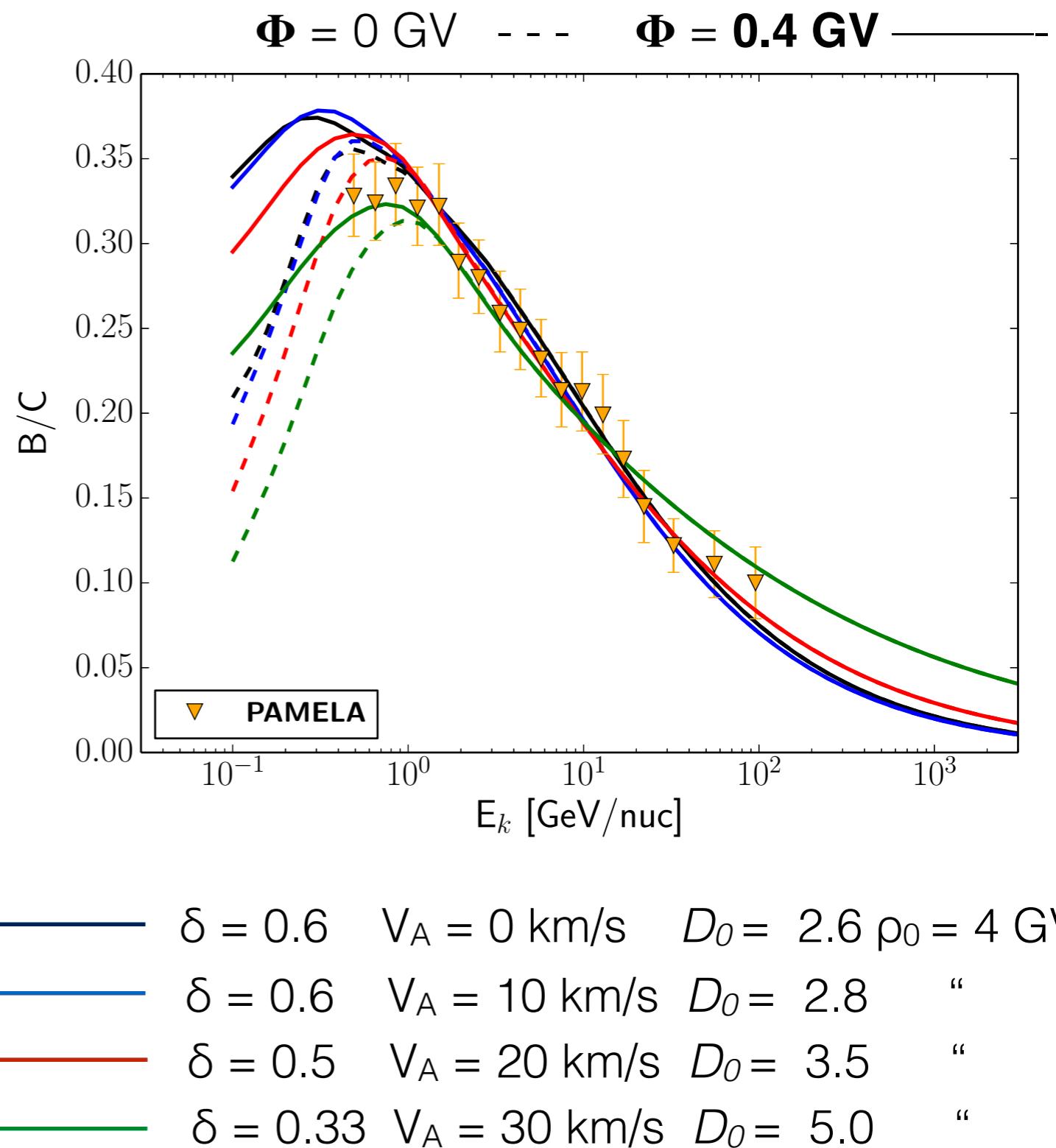
The effect of reacceleration

when increasing V_A the diffusion coefficient rigidity dependence (δ) has to be changed !

note that the source spectral index has to be changed so to leave $a_i + \delta$ constant

in the literature high values of V_A were introduced to match the B/C below 1 GeV/n

a_i : source spectral index of nuclei



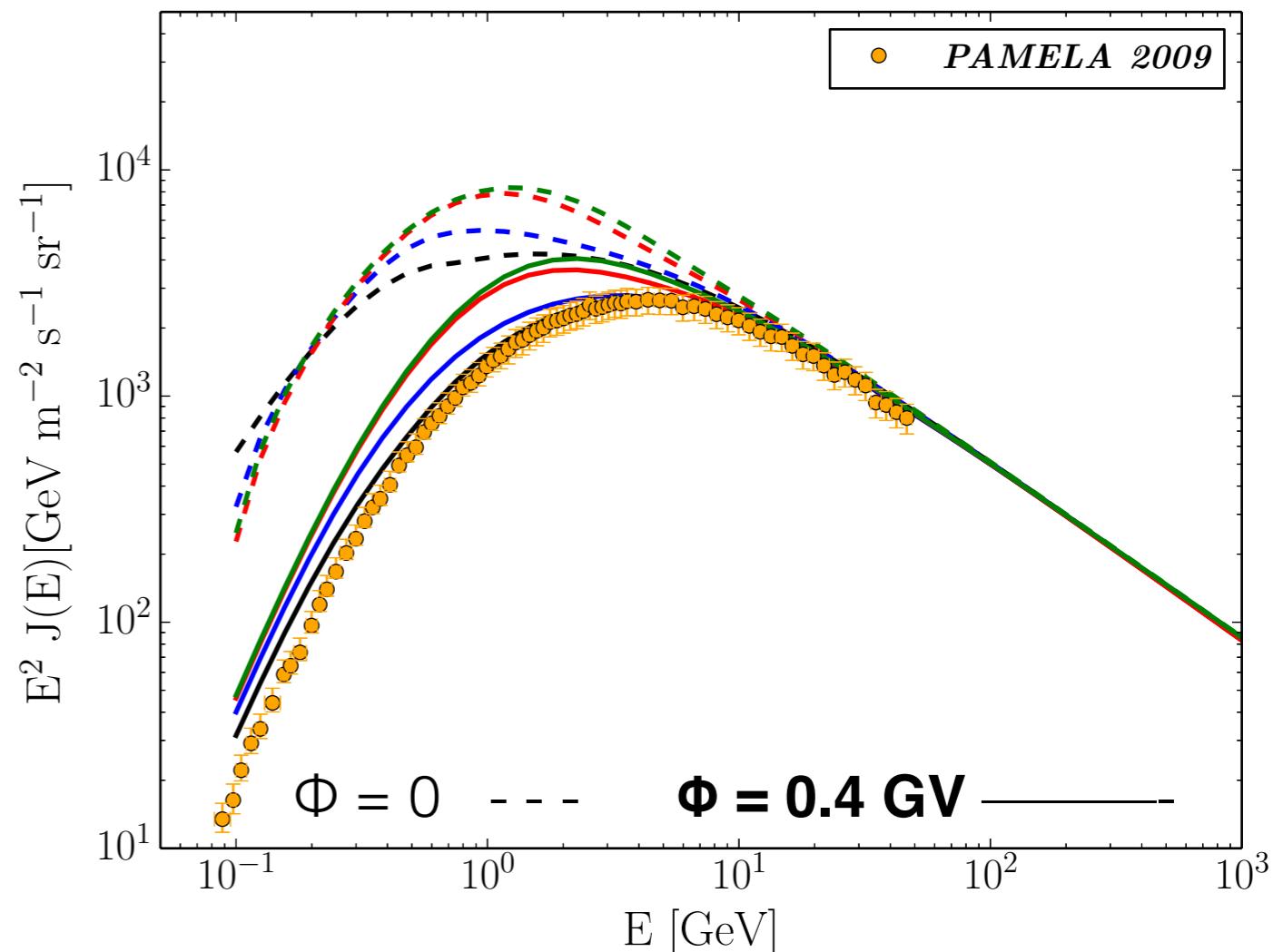
The effect of reacceleration (proton spectrum)

when increasing V_A the diffusion coefficient rigidity dependence (δ) has to be changed !

note that the source spectral index has to be change so to leave $a_i + \delta$ constant

in the literature high values of V_A were introduced to match the B/C below 1 GeV/n

large V_A result in more peaked spectra at about 1 GeV/n



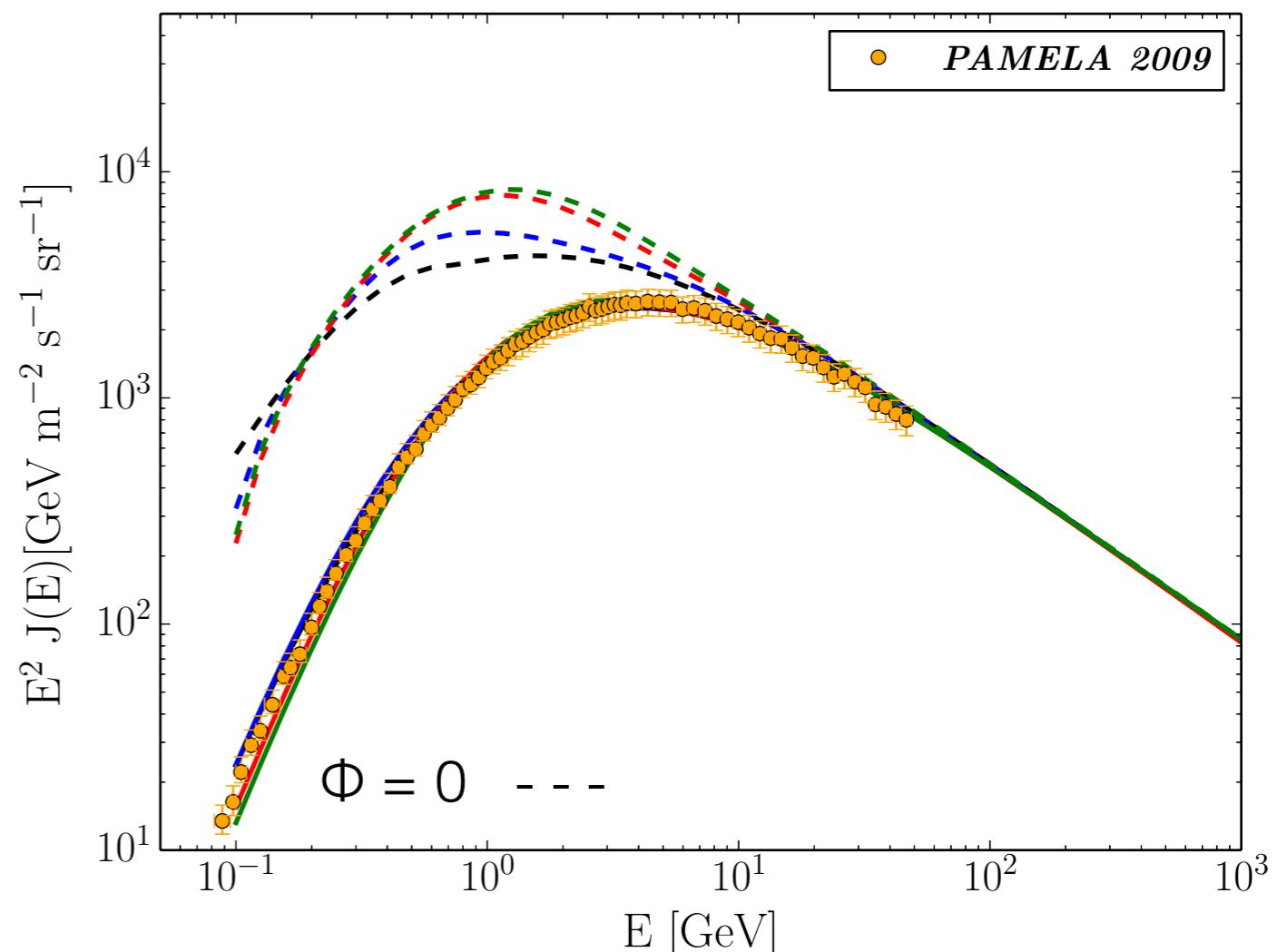
—	$\delta = 0.6$	$V_A = 0 \text{ km/s}$	$D_0 = 2.6$	$\Phi = 0.35 \text{ GV}$	$a = 2.2$
—	$\delta = 0.6$	$V_A = 10 \text{ km/s}$	$D_0 = 2.8$	$\Phi = 0.35 \text{ GV}$	$a = 2.2$
—	$\delta = 0.5$	$V_A = 20 \text{ km/s}$	$D_0 = 3.5$	$\Phi = 0.35 \text{ GV}$	$a = 2.3$
—	$\delta = 0.33$	$V_A = 30 \text{ km/s}$	$D_0 = 5.0$	$\Phi = 0.35 \text{ GV}$	$a = 2.47$

The effect of reacceleration (proton spectrum)

larger V_A result in more peaked spectra at about 1 GeV/n

this may be compensated increasing the modulation potential

⇒ degeneration $V_A - \Phi$!



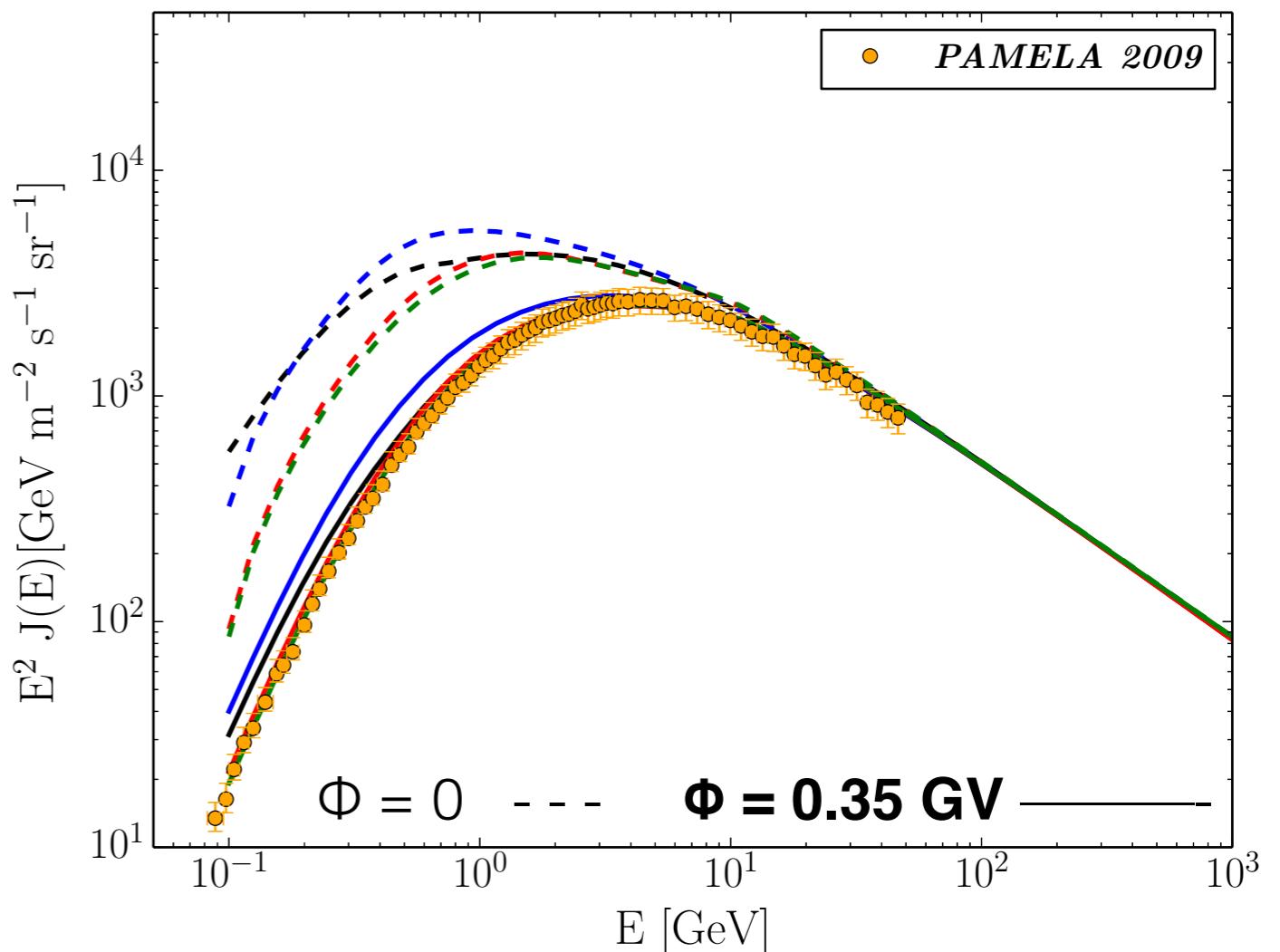
—	$\delta = 0.6$	$V_A = 0 \text{ km/s}$	$D_0 = 2.6$	$\Phi = 0.4 \text{ GV}$
—	$\delta = 0.6$	$V_A = 10 \text{ km/s}$	$D_0 = 2.8$	$\Phi = 0.45 \text{ GV}$
—	$\delta = 0.5$	$V_A = 20 \text{ km/s}$	$D_0 = 3.5$	$\Phi = 0.60 \text{ GV}$
—	$\delta = 0.33$	$V_A = 30 \text{ km/s}$	$D_0 = 5.0$	$\Phi = 0.65 \text{ GV}$

The effect of reacceleration (proton spectrum)

large V_A result in more peaked spectra at about 1 GeV/n

this may be compensated increasing the modulation potential

or introducing a break in the p source spectrum at ~ 10 GeV
(marginal effect on the B/C)



---	$\delta = 0.6$	$V_A = 0 \text{ km/s}$	$D_0 = 2.6$	$\Phi = 0.35 \text{ GV}$	$a = 2.2$
---	$\delta = 0.6$	$V_A = 10 \text{ km/s}$	$D_0 = 2.8$	$\Phi = 0.35 \text{ GV}$	$a = 2.2$
---	$\delta = 0.5$	$V_A = 20 \text{ km/s}$	$D_0 = 3.5$	$\Phi = 0.35 \text{ GV}$	$a = 2.0/2.3 \quad b/a \text{ 11 GeV}$
---	$\delta = 0.33$	$V_A = 30 \text{ km/s}$	$D_0 = 5.0$	$\Phi = 0.35 \text{ GV}$	$a = 2.1/2.45 \quad b/a \text{ 11 GeV}$

The effect of changing D(E) at low energy

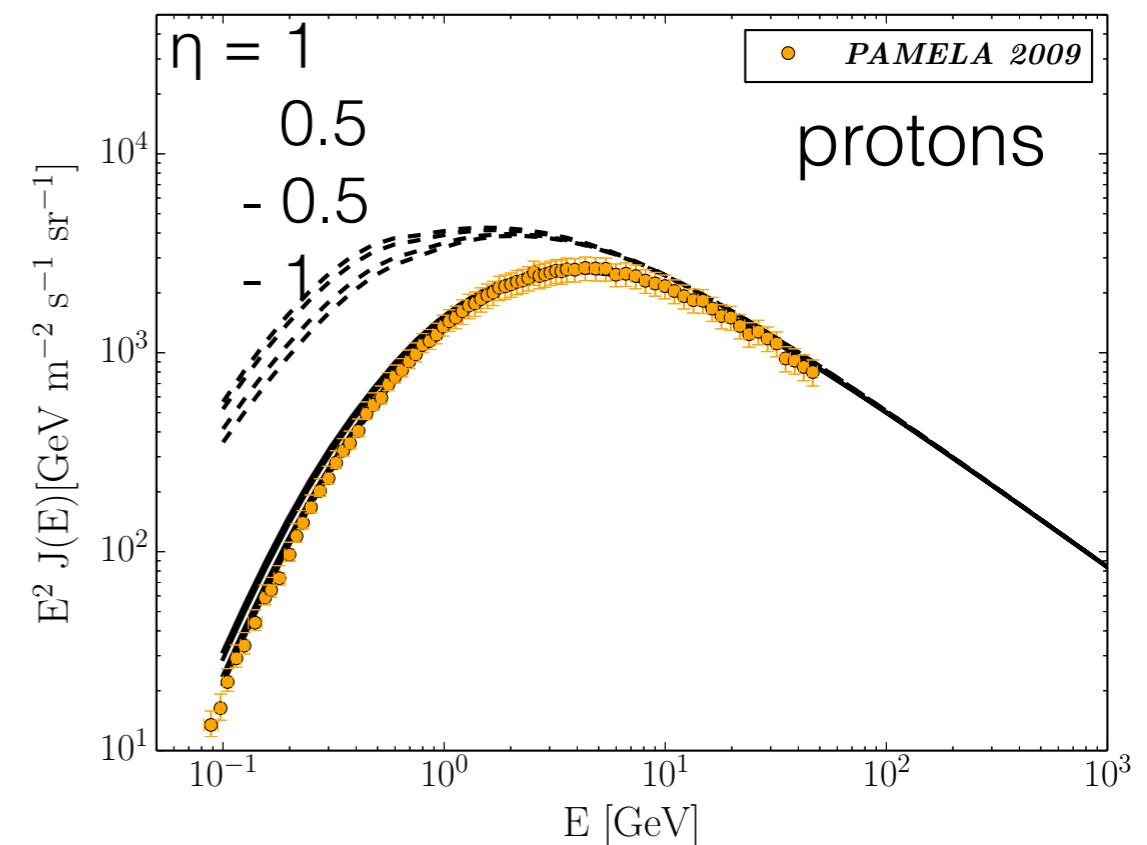
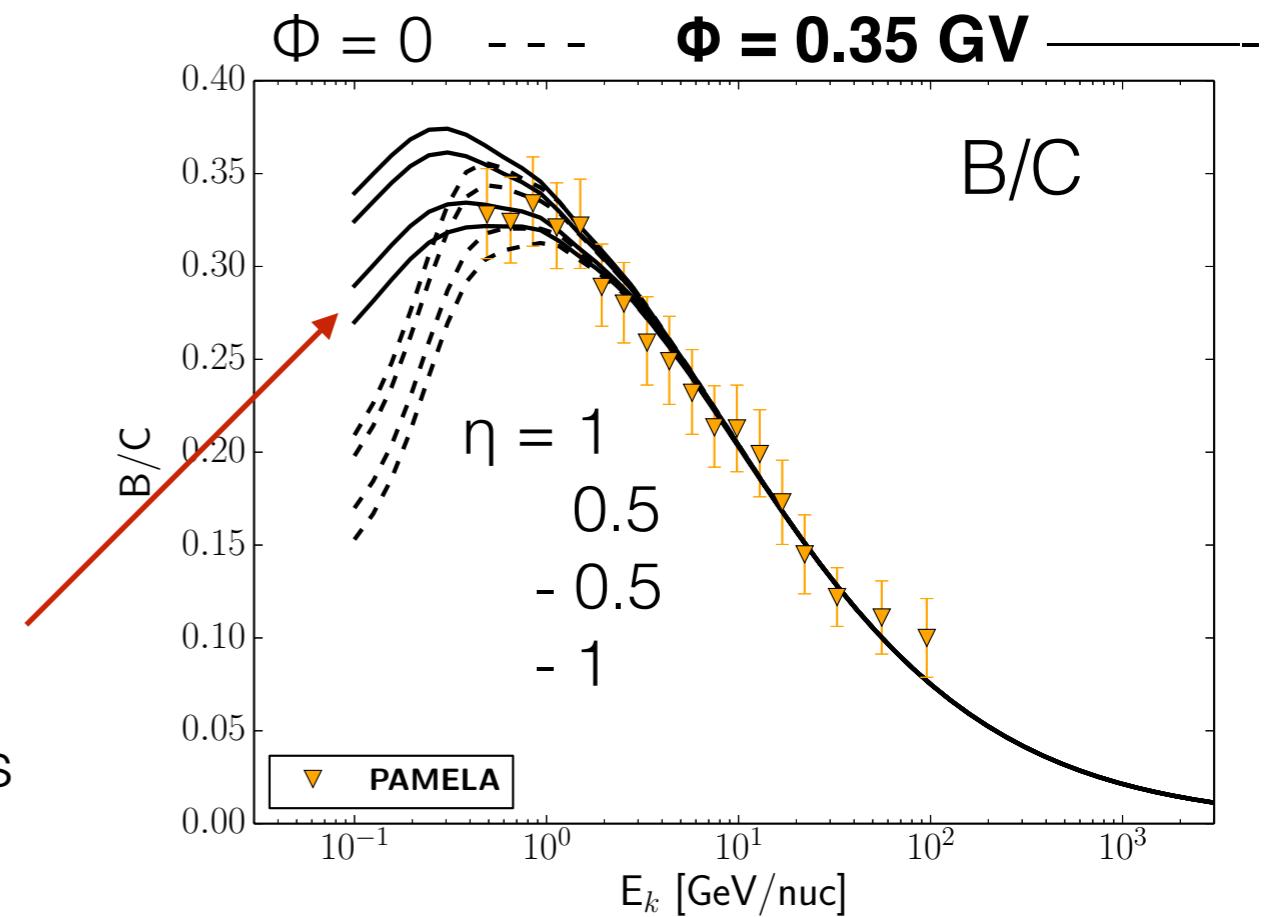
This may be parameterized in the form

$$D(\rho) = D_0 \beta^\eta \left(\frac{\rho}{\rho_0} \right)^\delta$$

The effect may help to reproduce the B/C below 1 GeV for low reacceleration models

the effect on the proton spectrum is small and almost degenerate with solar modulation

models in the plots
 $\delta = 0.6$, $v_C = 0$; $D_0 = 2.6$ $z_t = 4$ kpc



The effects of convection

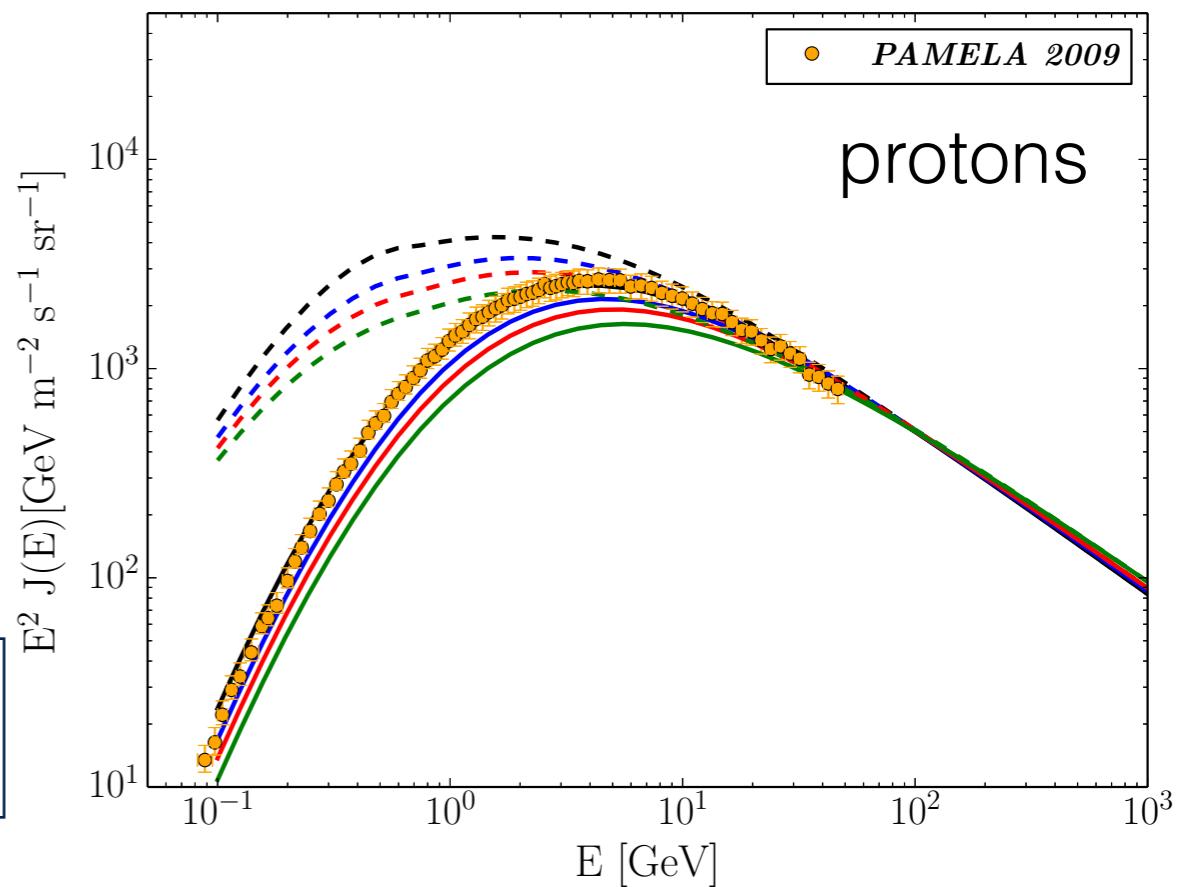
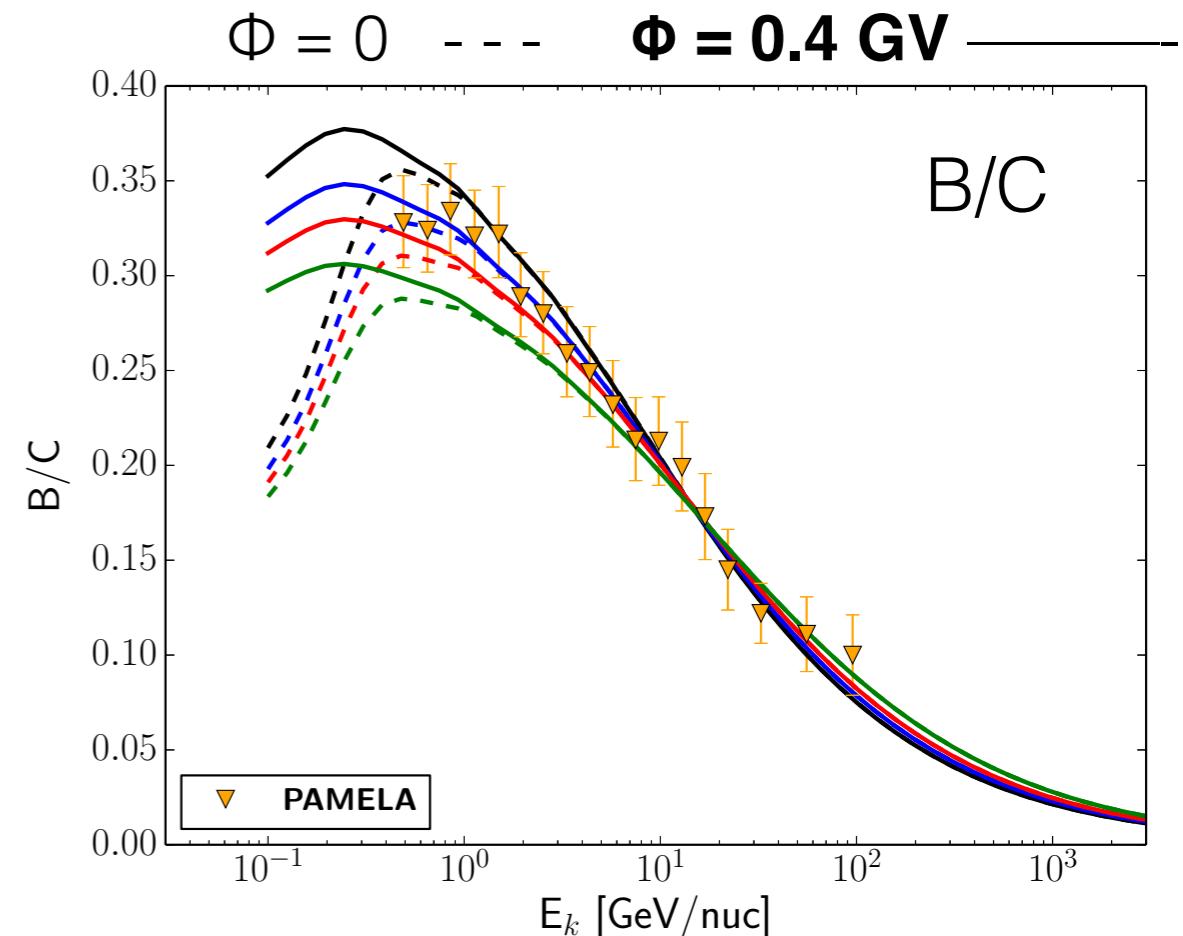
We assume $V_c = 0$ at $z = 0$ and it grows specularly with z with constant dV_c/dz

The effect is negligible above ~ 20 GeV/n

D_0 has to be rescaled when changing dV_c/dz

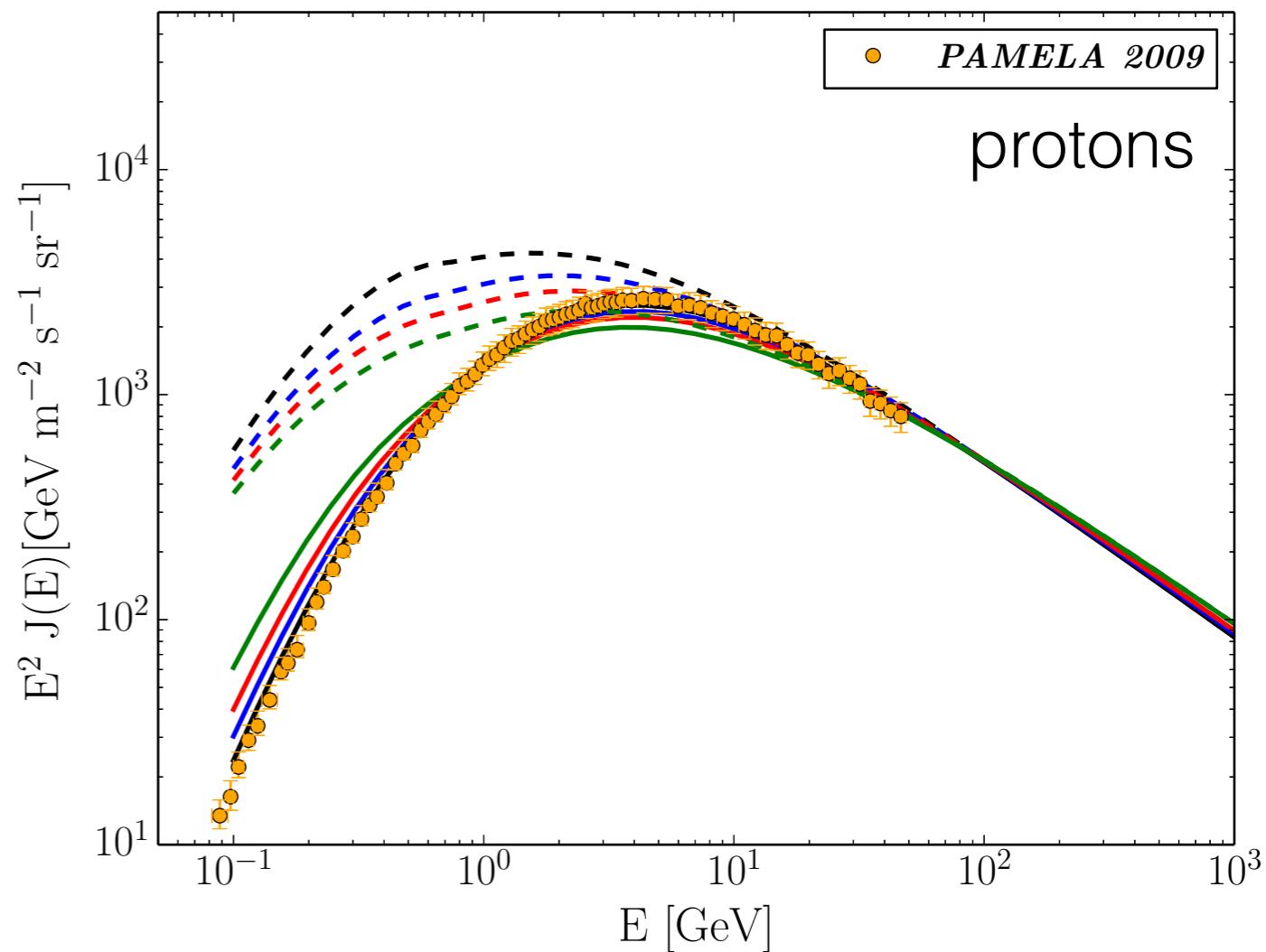
—	$dV_c/dz = 0$ km/s/kpc	$D_0 = 2.6$
—	$dV_c/dz = 5$ km/s/kpc	$D_0 = 2.4$
—	$dV_c/dz = 10$ km/s/kpc	$D_0 = 2.2$
—	$dV_c/dz = 20$ km/s/kpc	$D_0 = 1.8$

for all models in these plots
 $\delta = 0.6$, $V_A = 0$; $z_t = 4$ kpc



The effects of convection

proton data can hardly be matched
lowering the modulation potential and
only for small values of dV_c/dz



$dV_c/dz = 0 \text{ km/s/kpc}$	$D_0 = 2.6$	$\Phi = 0.4 \text{ GV}$
$dV_c/dz = 5 \text{ km/s/kpc}$	$D_0 = 2.4$	$\Phi = 0.3 \text{ GV}$
$dV_c/dz = 10 \text{ km/s/kpc}$	$D_0 = 2.2$	$\Phi = 0.23 \text{ GV}$
$dV_c/dz = 20 \text{ km/s/kpc}$	$D_0 = 1.8$	$\Phi = 0.15 \text{ GV} !!$

for all models in these plots
 $\delta = 0.6$, $V_A = 0$; $z_t = 4 \text{ kpc}$

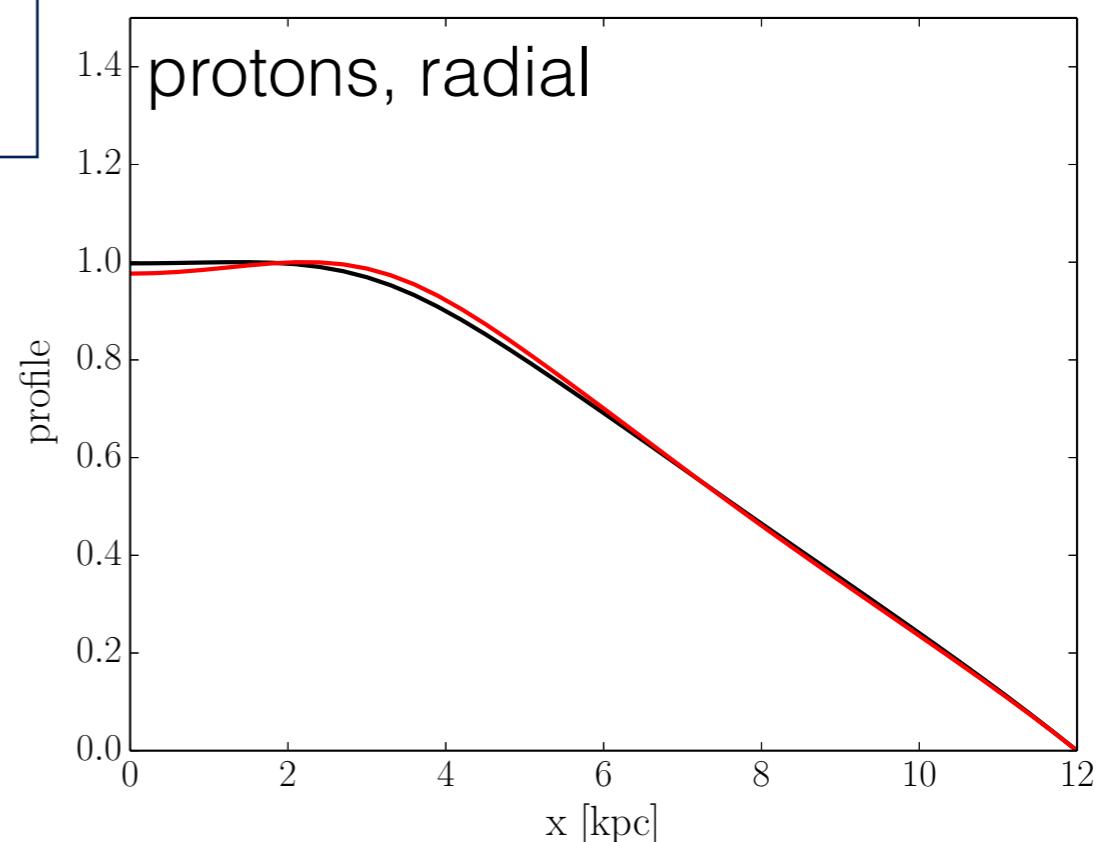
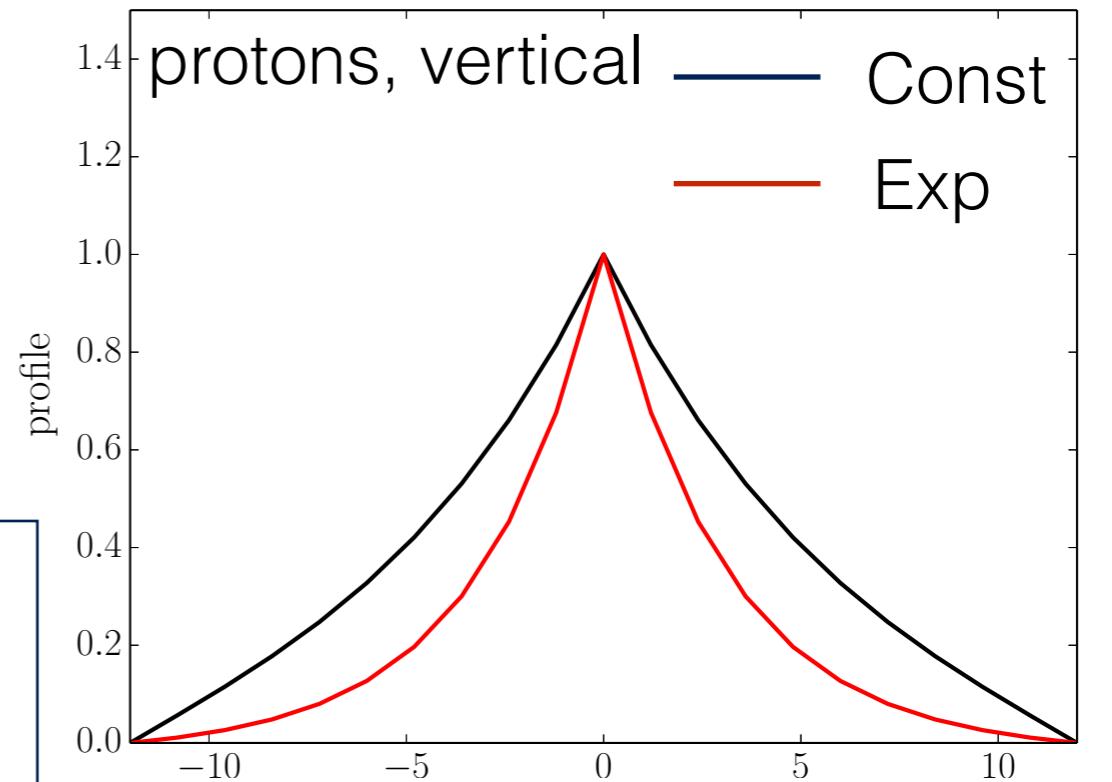
The CR spatial distribution (Constant vs Exp)

Const: $D(z) = \text{const}$

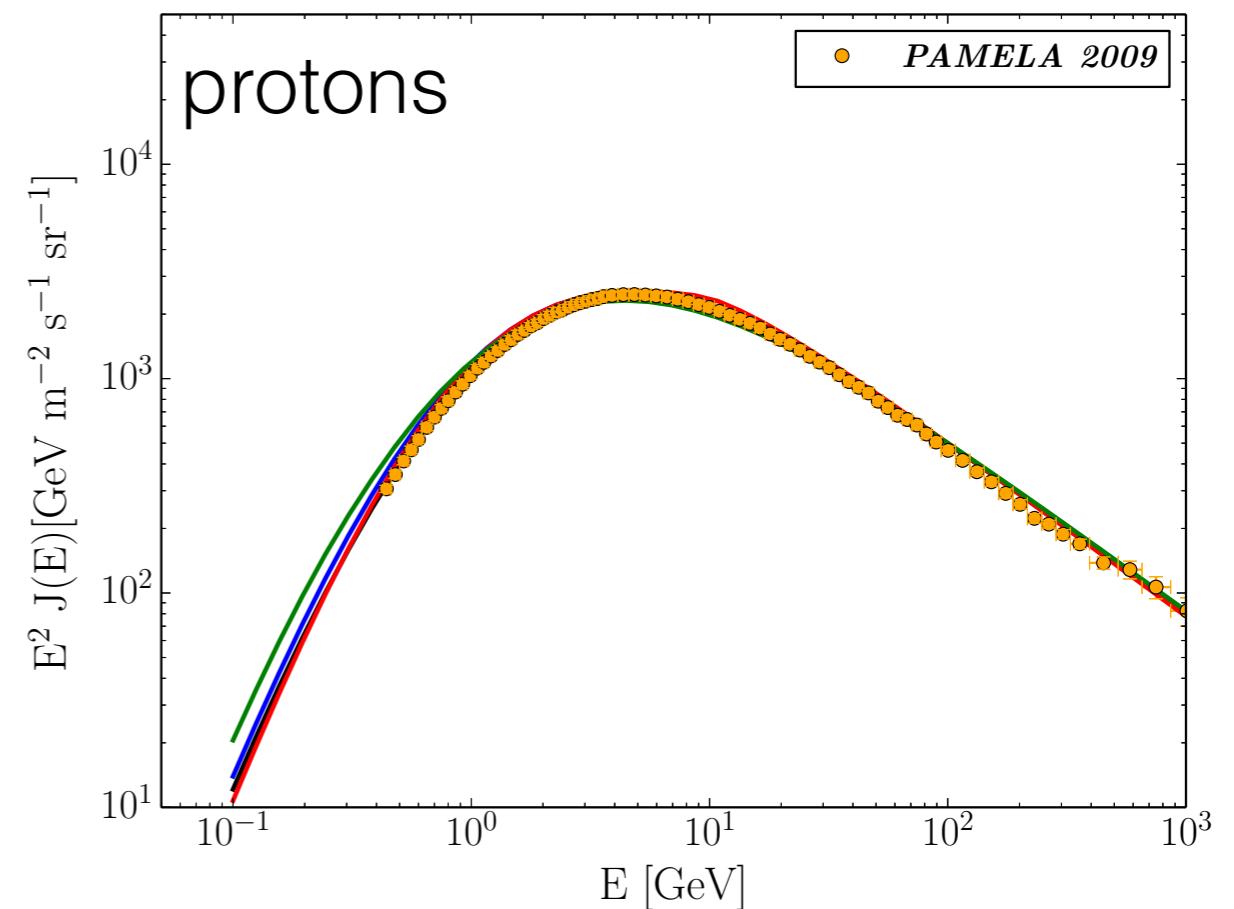
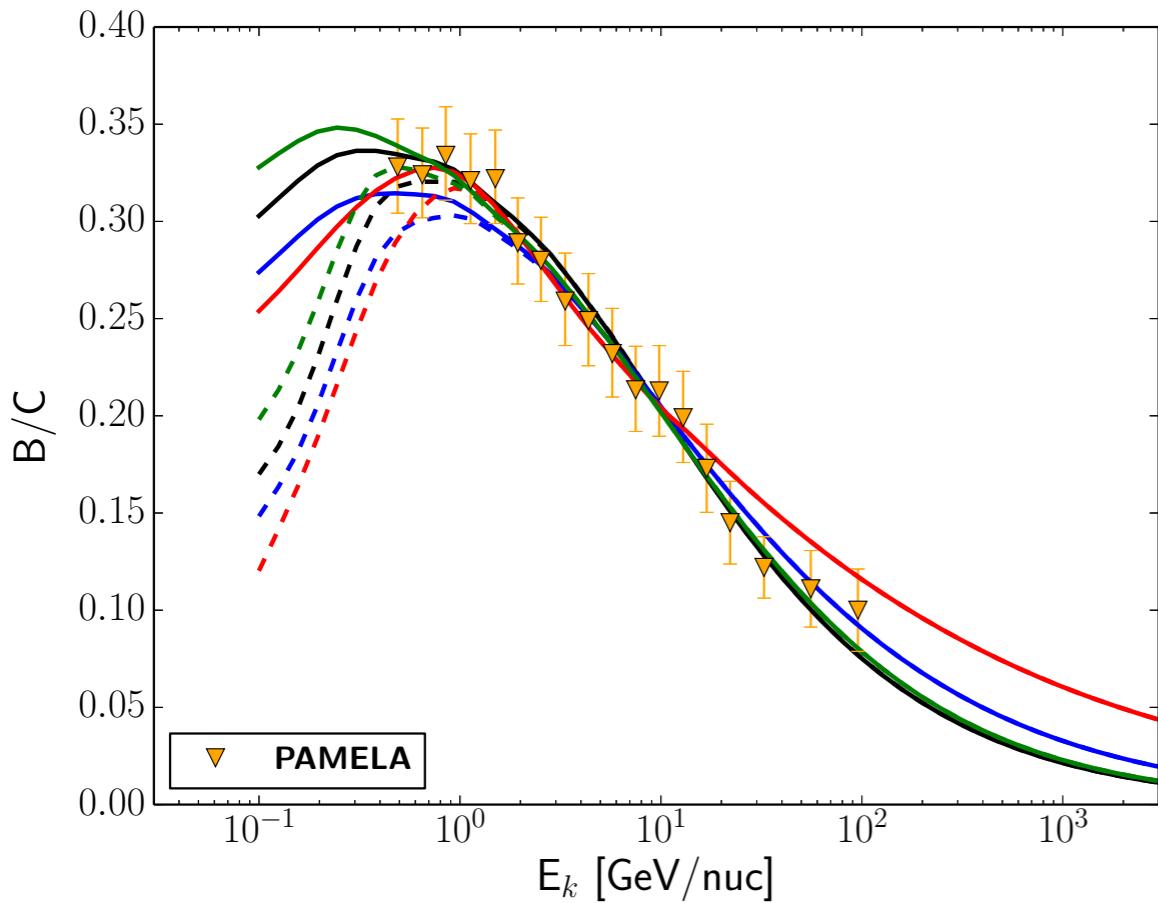
Exp: $D(z) \propto \exp\left(\frac{z}{z_t}\right)$

in these plots
 $D_0 = 2.6$, **$z_t = 4 \text{ kpc}$**

$E = 1 \text{ GeV}$
almost coincident for higher energies as proton energy losses are almost energy independent

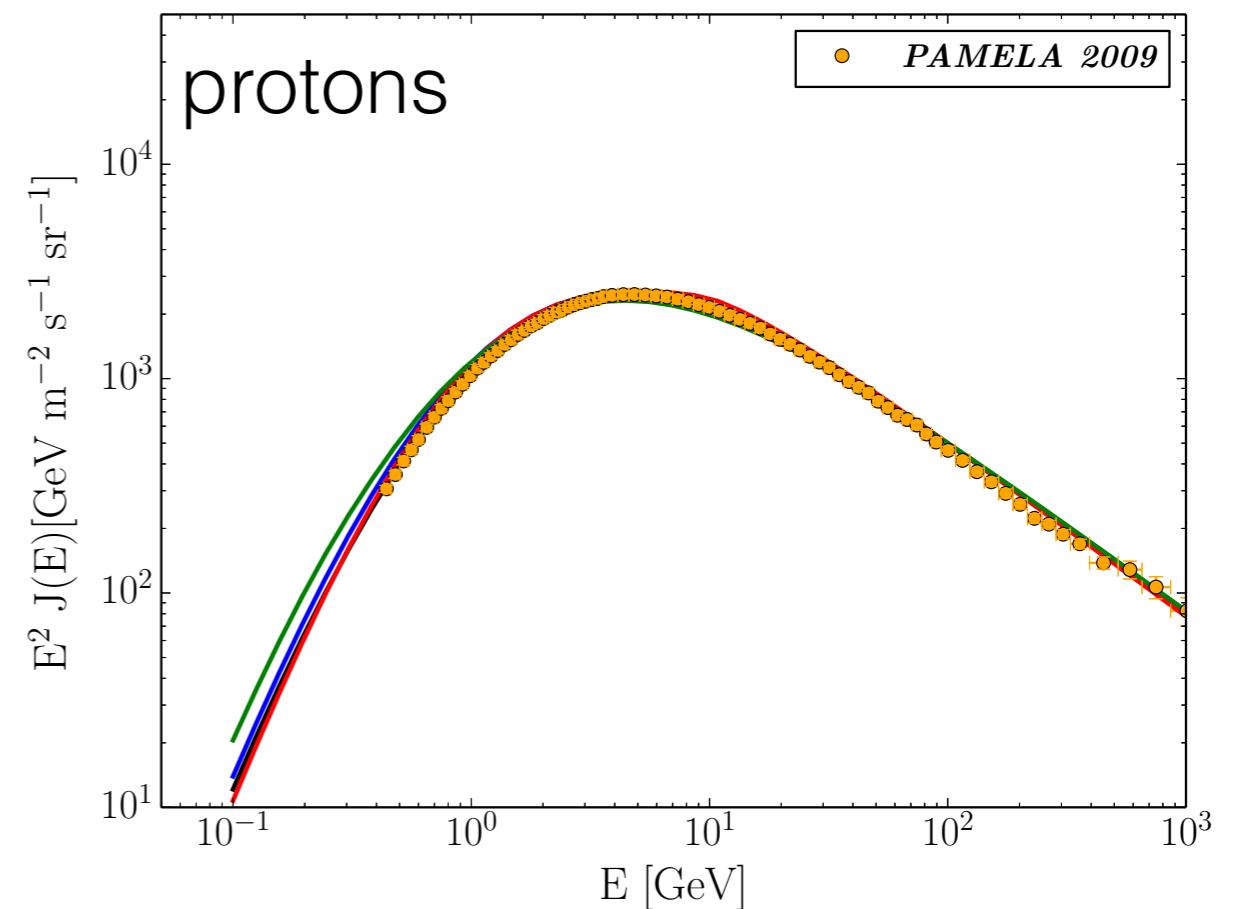
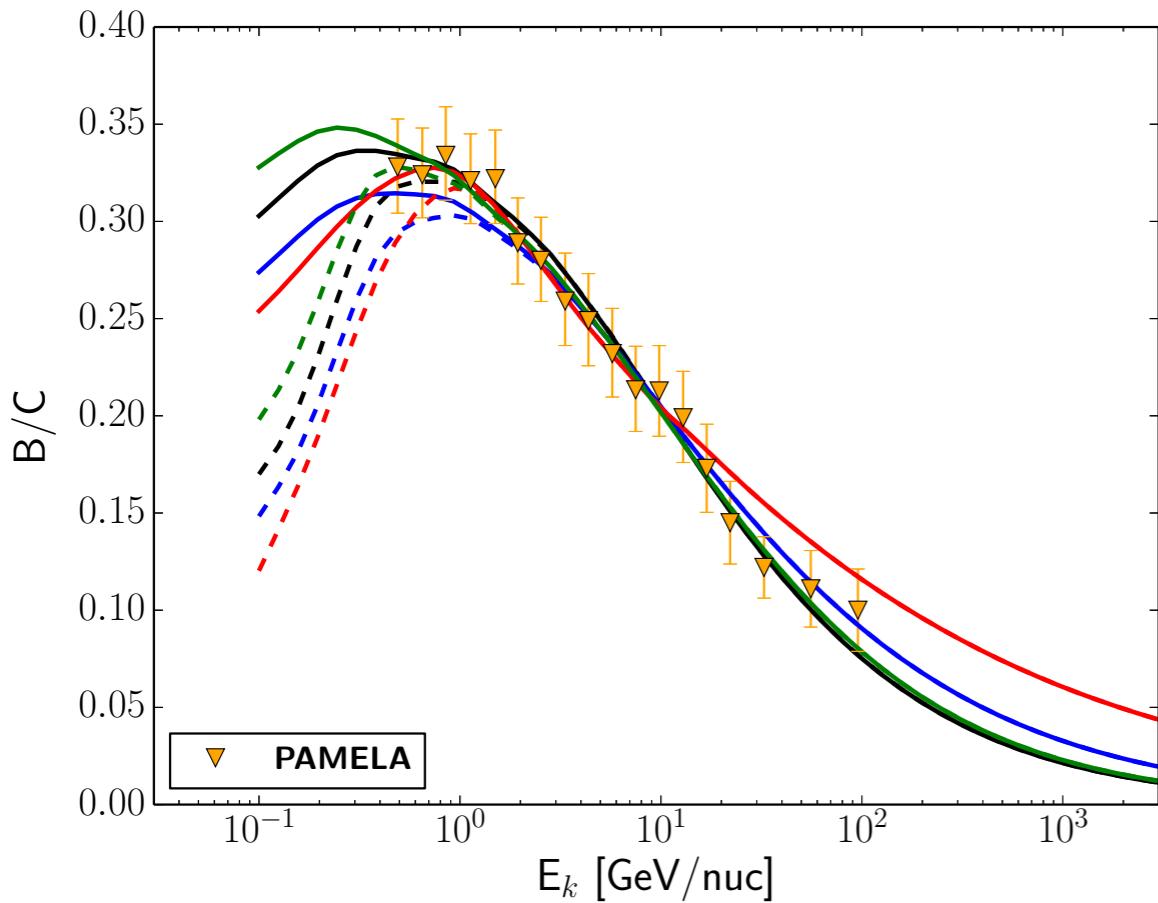


The “fantastic” four



---	$\delta = 0.6$	$V_A = 0$ km/s	$D_0 = 2.6$	$\eta = -0.5$	$a = 2.22$	$dV_c/dz = 0$	$\Phi = 0.5$	PD
---	$\delta = 0.5$	$V_A = 10$ km/s	$D_0 = 3.1$	$\eta = -0.5$	$a = 2.32$	$dV_c/dz = 0$	$\Phi = 0.65$	KRA
---	$\delta = 0.33$	$V_A = 30$ km/s	$D_0 = 4.6$	$\eta = 1$	$a = 2.1/2.49$	$dV_c/dz = 0$	$\Phi = 0.5$	KOL
---	$\delta = 0.6$	$V_A = 0$ km/s	$D_0 = 2.4$	$\eta = 1$	$a = 2.22$	$dV_c/dz = 5$	$\Phi = 0.5$	CONV

The “fantastic” four

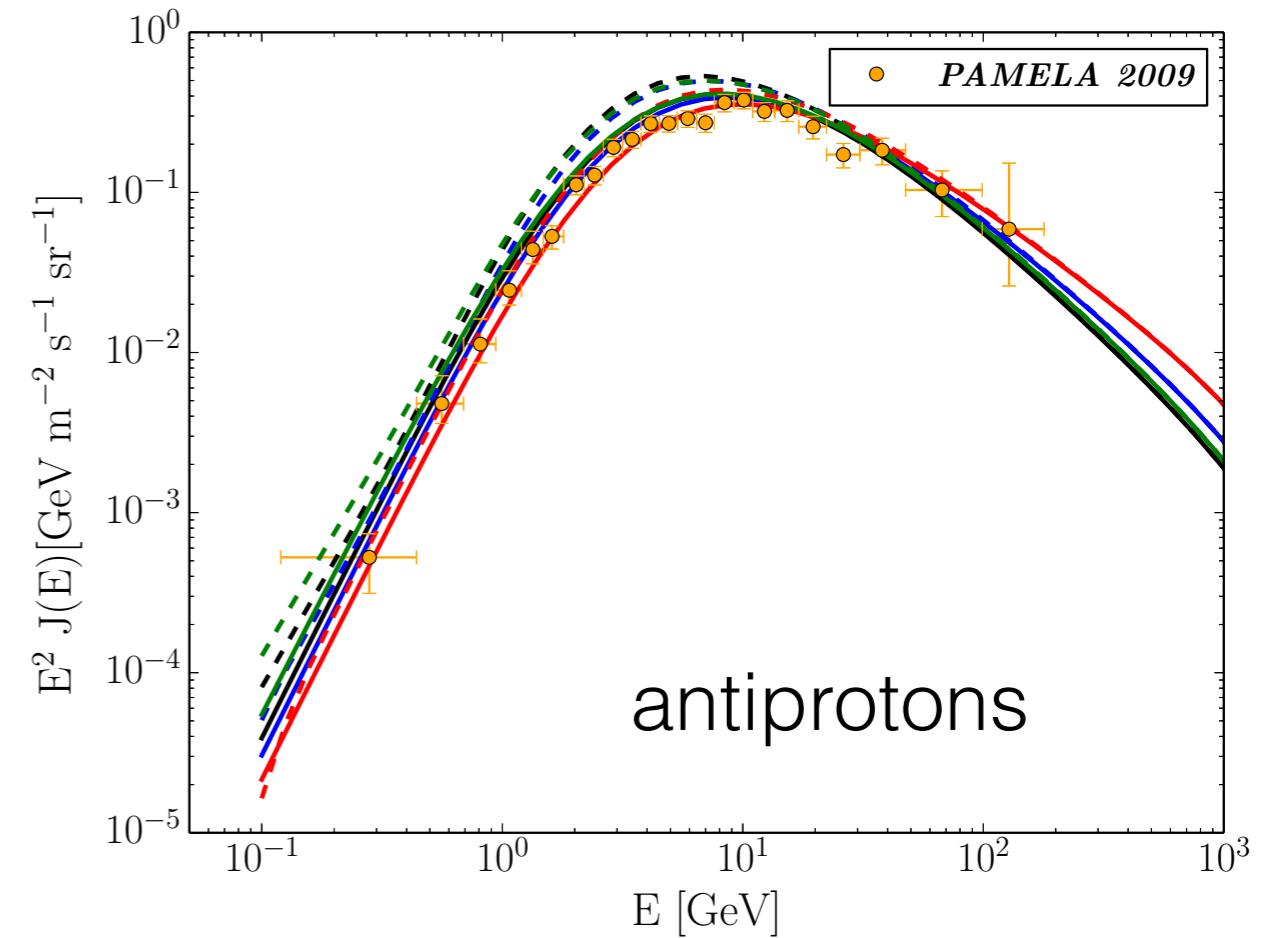
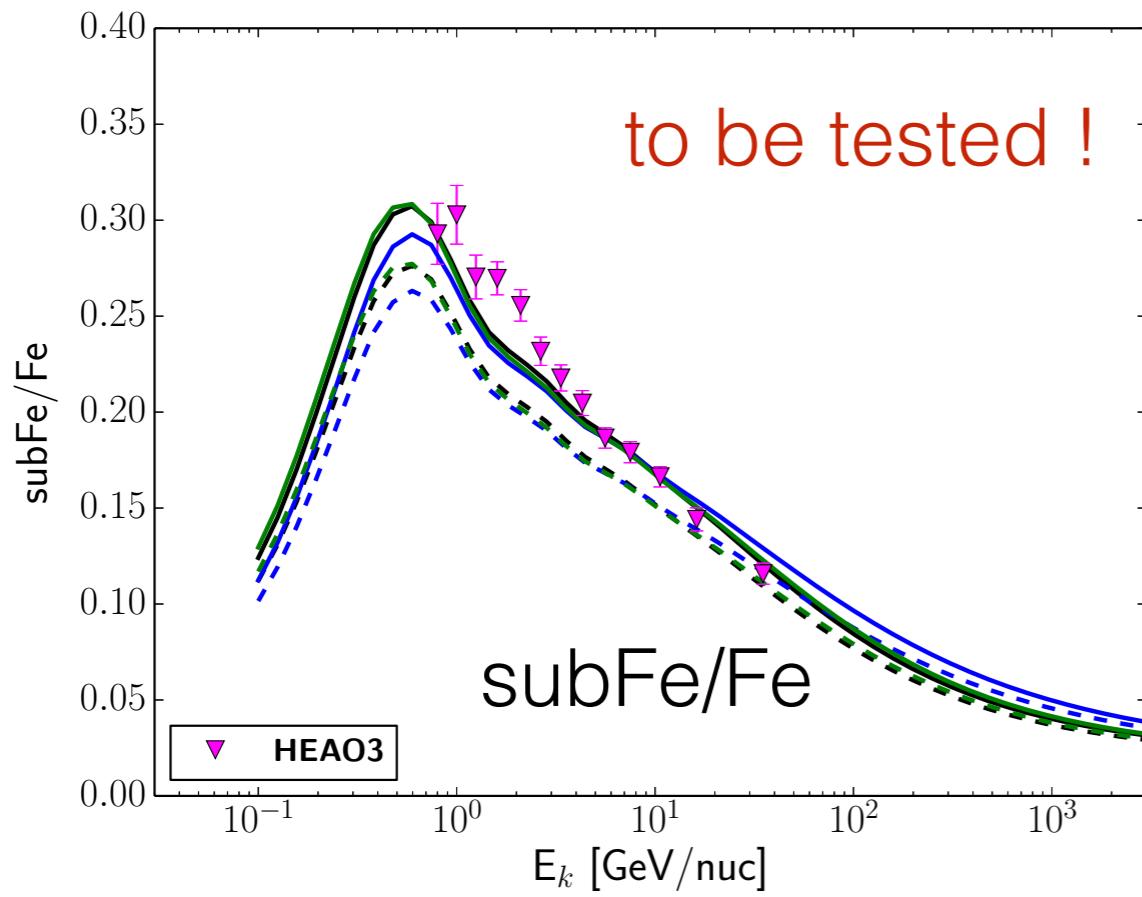


---	$\delta = 0.6$	$V_A = 0 \text{ km/s}$	$D_0 = 2.6$	$\eta = -0.5$	$a = 2.22$	$dV_c/dz = 0$	$\Phi = 0.5$	PD
---	$\delta = 0.5$	$V_A = 10 \text{ km/s}$	$D_0 = 3.1$	$\eta = -0.5$	$a = 2.32$	$dV_c/dz = 0$	$\Phi = 0.65$	KRA
---	$\delta = 0.33$	$V_A = 30 \text{ km/s}$	$D_0 = 4.6$	$\eta = 1$	$a = 2.1/2.49$	$dV_c/dz = 0$	$\Phi = 0.5$	KOL
---	$\delta = 0.6$	$V_A = 0 \text{ km/s}$	$D_0 = 2.4$	$\eta = 1$	$a = 2.22$	$dV_c/dz = 5$	$\Phi = 0.5$	CONV

which one is ?



The “fantastic” four



—	$\delta = 0.6$	$V_A = 0 \text{ km/s}$	$D_0 = 2.6$	$\eta = -0.5$	$\alpha = 2.22$	$dV_c/dz = 0$	$\Phi = 0.5$	PD
—	$\delta = 0.5$	$V_A = 10 \text{ km/s}$	$D_0 = 3.1$	$\eta = -0.5$	$\alpha = 2.32$	$dV_c/dz = 0$	$\Phi = 0.65$	KRA
—	$\delta = 0.33$	$V_A = 30 \text{ km/s}$	$D_0 = 4.6$	$\eta = 1$	$\alpha = 2.1/2.49$	$dV_c/dz = 0$	$\Phi = 0.5$	KOL
—	$\delta = 0.6$	$V_A = 0 \text{ km/s}$	$D_0 = 2.4$	$\eta = 1$	$\alpha = 2.22$	$dV_c/dz = 5$	$\Phi = 0.5$	CONV

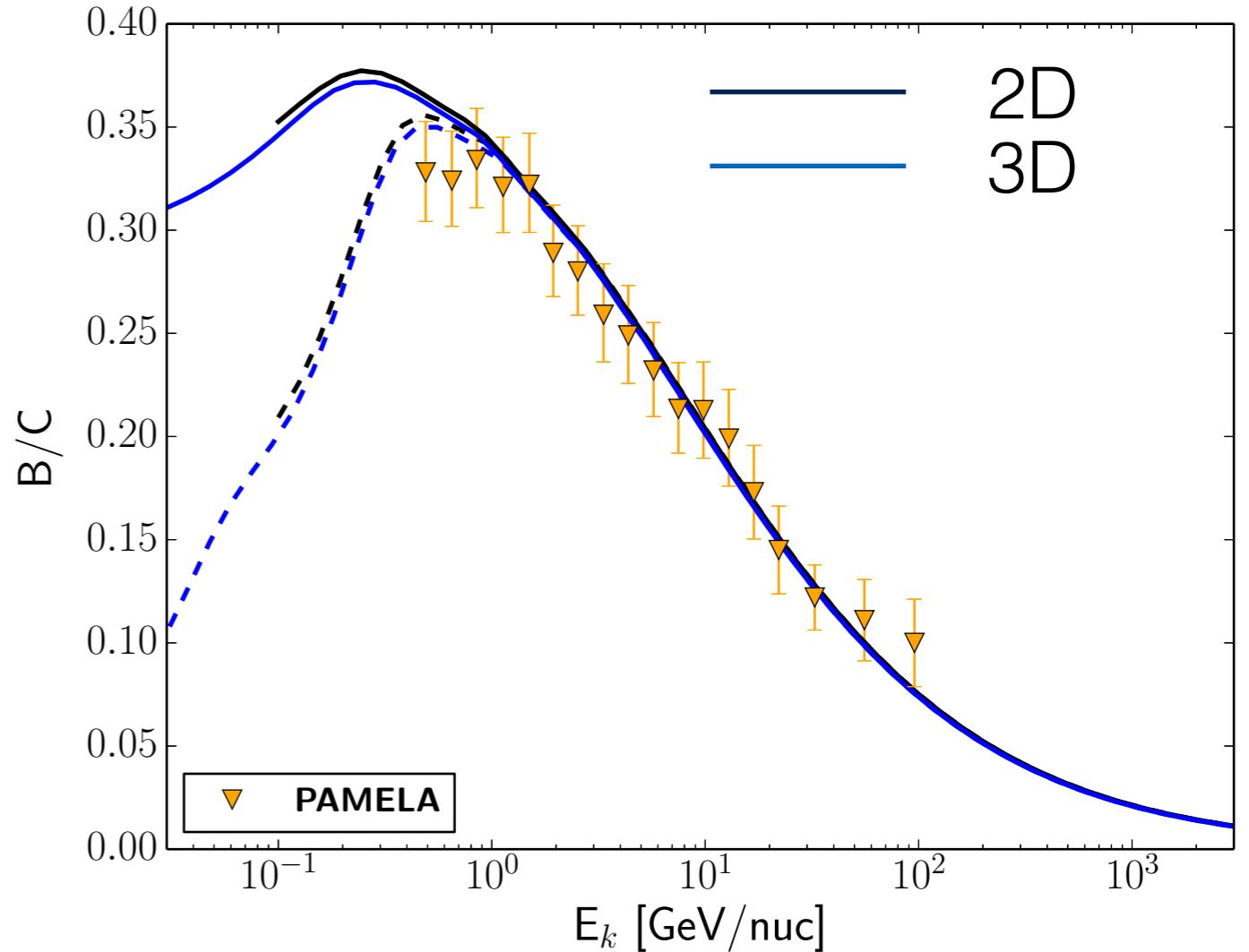
(Note that $Z_{\max} > 32$ for correctly modeling sub Fe/Fe
 sub Fe = Sc + V + Ti)

Cosmic rays in 3D

We consider a 3D grid (x,y,z)

If the same source, gas, MF,
distributions are adopted

same results !

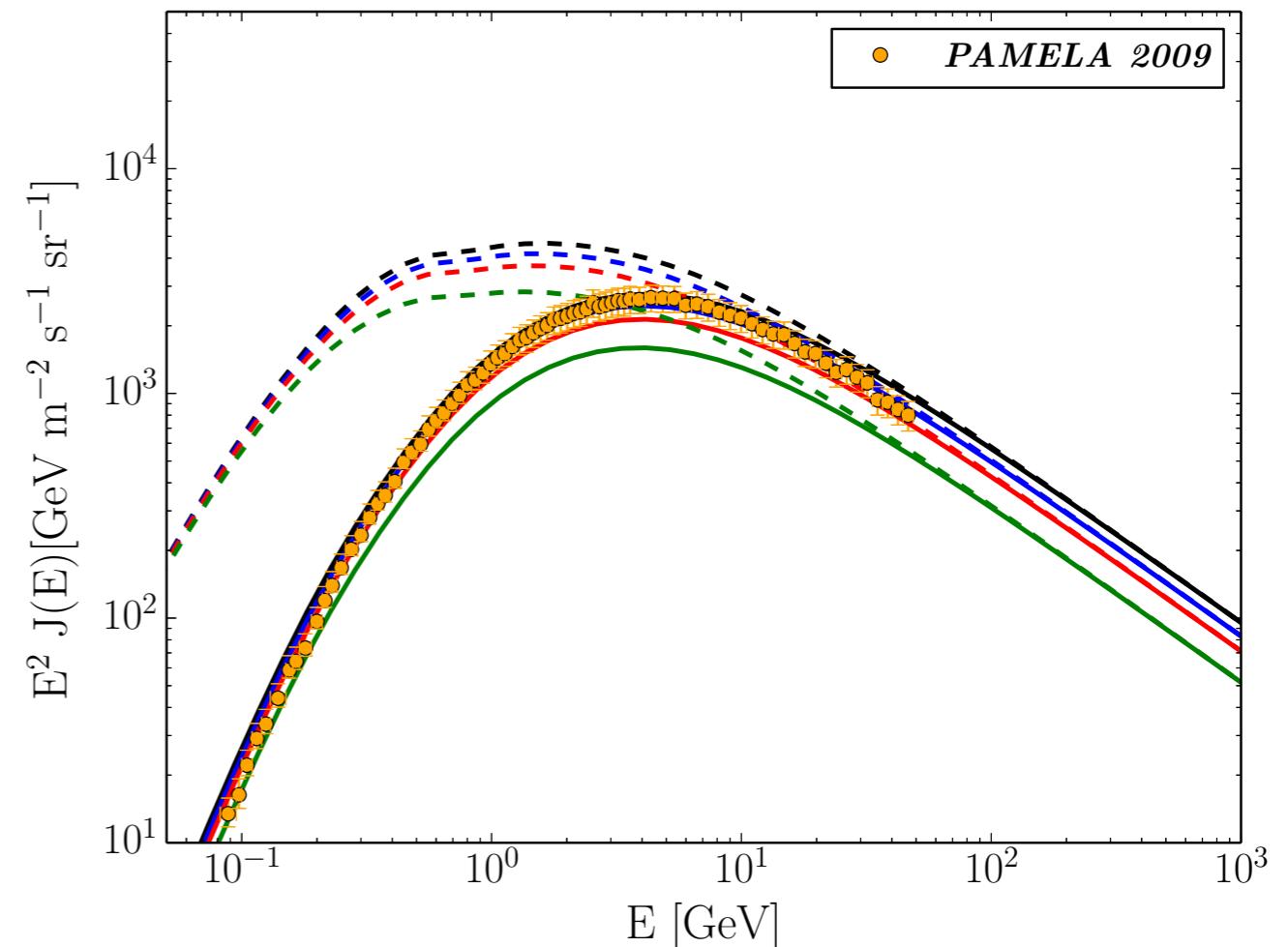


for the models in the plot

$$\delta = 0.6, L = 4 \text{ kpc}, V_A = V_C = 0, \eta = 1; D_0 = 2.6$$

D(z) exponential;

Where the primary and secondary CR reaching the Earth are produced ?

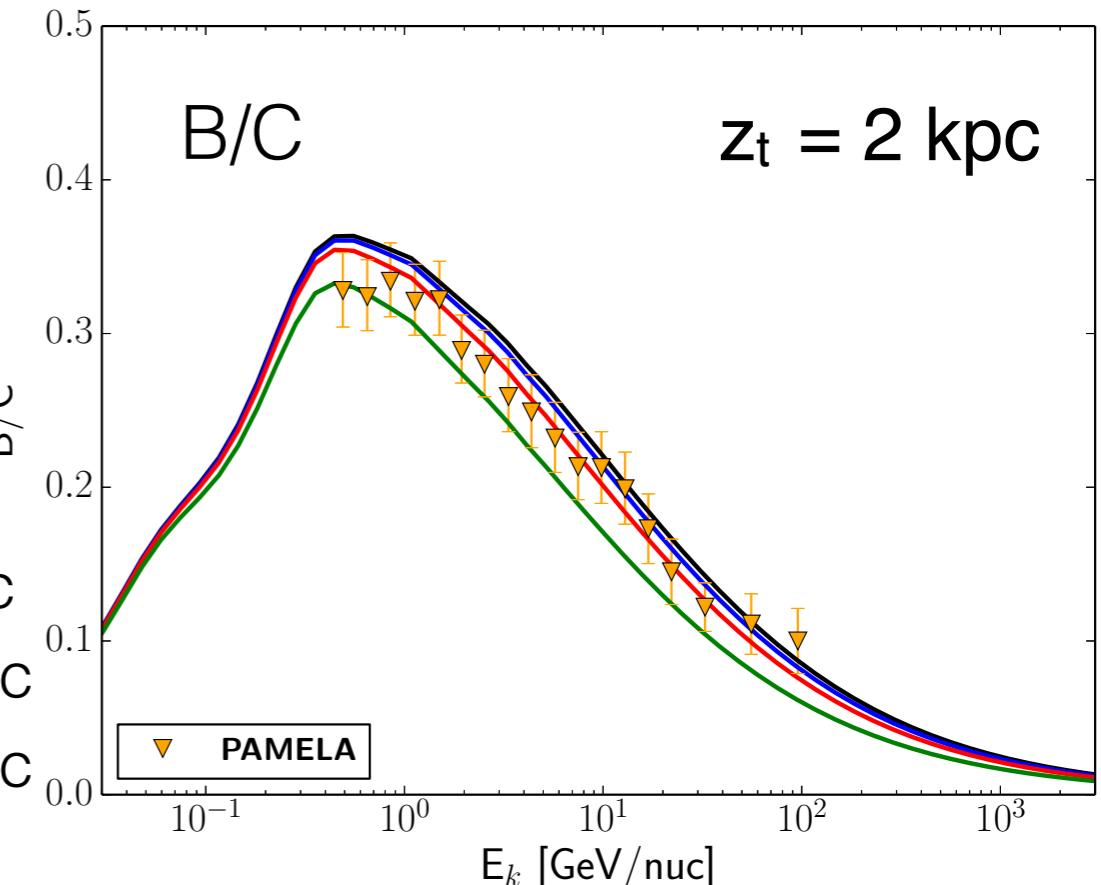
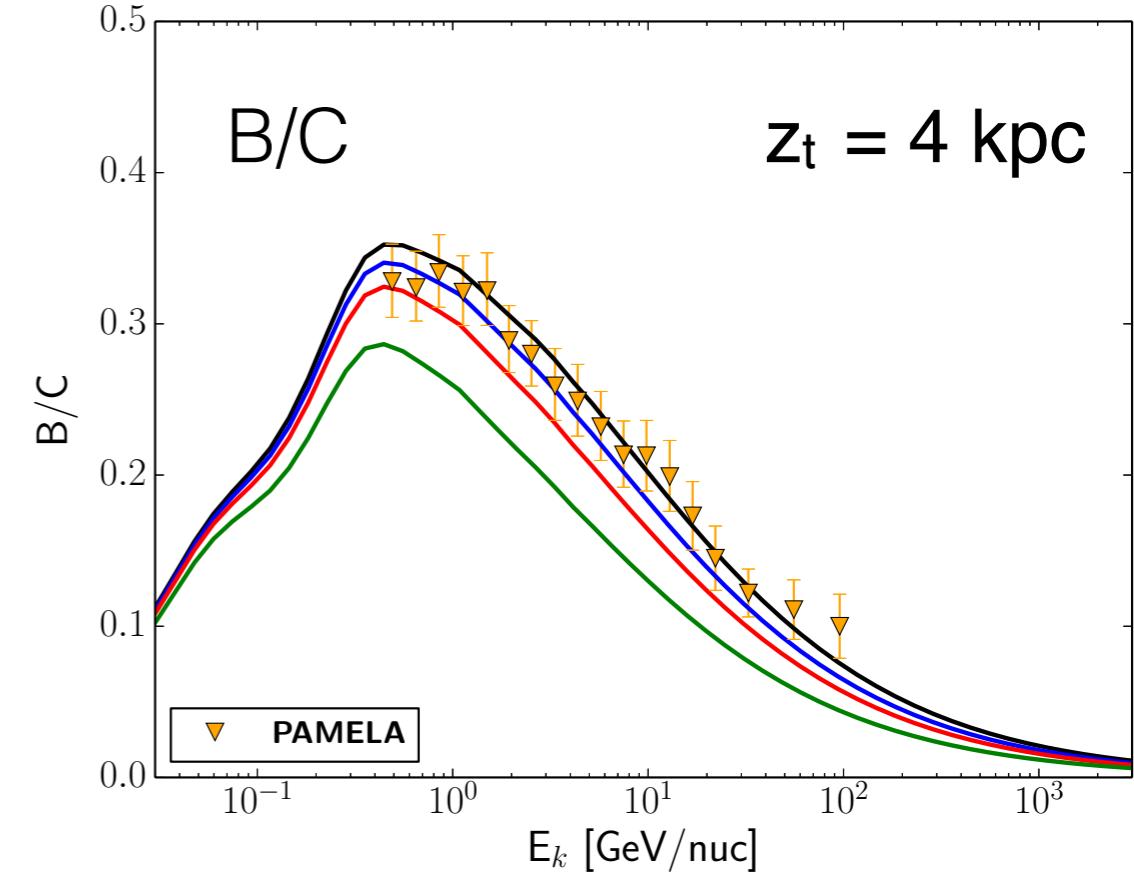


$z_t = 4 \text{ kpc}$

- sources only within $d < R_{\text{cut}}$
- $R_{\text{cut}} = R_{\text{max}}$
 - $R_{\text{cut}} = 7 \text{ kpc}$
 - $R_{\text{cut}} = 5 \text{ kpc}$
 - $R_{\text{cut}} = 3 \text{ kpc}$

Where the primary and secondary CR reaching the Earth are produced ?

Light secondary stable nuclei are produced in a region of size slightly larger than z_t



sources only within $d < R_{\text{cut}}$

$R_{\text{cut}} = R_{\text{max}}$

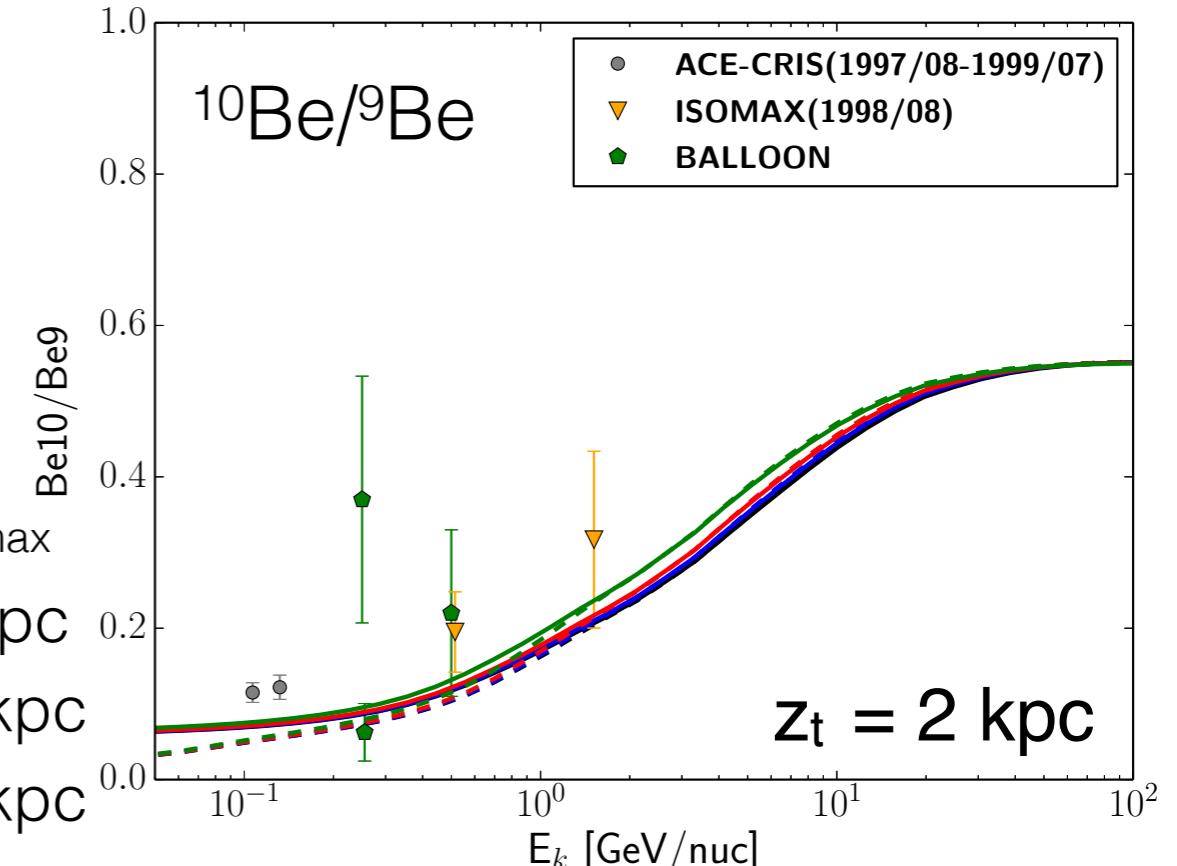
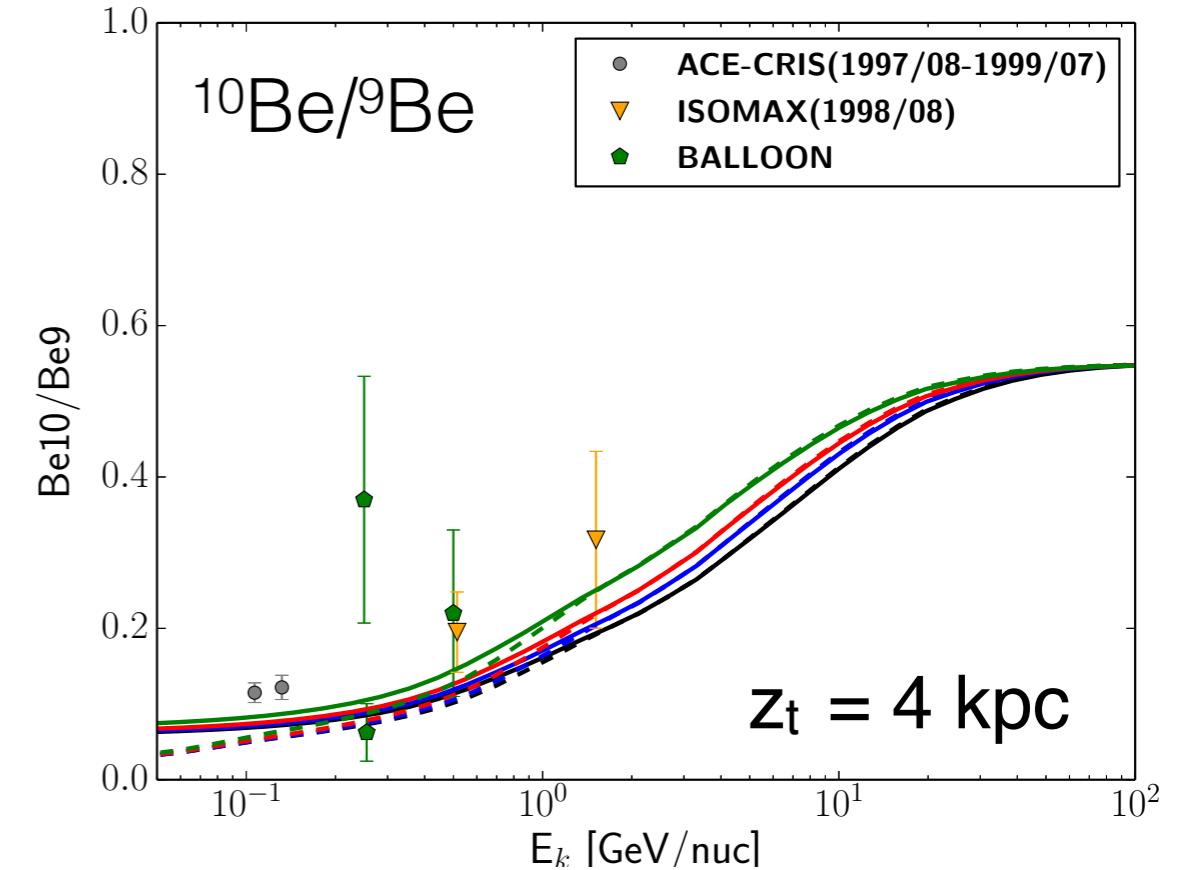
$R_{\text{cut}} = 7$ kpc

$R_{\text{cut}} = 5$ kpc

$R_{\text{cut}} = 3$ kpc

Where the primary and secondary CR reaching the Earth are produced ?

the ^{10}Be is produced almost locally, hence it is almost independent on R_{cut} , while ^9Be decreases increasing R_{cut} up to z_t



sources only within $d < R_{\text{cut}}$

$R_{\text{cut}} = R_{\text{max}}$

$R_{\text{cut}} = 7 \text{ kpc}$

$R_{\text{cut}} = 5 \text{ kpc}$

$R_{\text{cut}} = 3 \text{ kpc}$

$R_{\text{cut}} = R_{\text{max}}$

$R_{\text{cut}} = 7 \text{ kpc}$

$R_{\text{cut}} = 5 \text{ kpc}$

$R_{\text{cut}} = 3 \text{ kpc}$

Short summary

- D and L are almost degenerate. The value of L does not affect the secondary/primary ratios (after D rescaling). When relevant (e.g. for DM) L should be determined from other measurements.
- strong reacceleration need string (ad hoc ?) breaks in the source spectral index
- low reacceleration models may need a change in the low energy dependence of D (modulation may also do the job)
- exponential $D(z)$ give more physically reasonable CR profiles, still this is not necessary for what concerns only nuclei

Electrons and positrons

e^\pm energy losses and transport equation

$$\frac{d}{dt}N_e(E) = D(E)\nabla^2 N_e + \frac{\partial}{\partial N} (b(E)N_e(E)) + Q(E)$$

above 1 GeV

$$b = -\frac{dE}{dt} = \beta E^2 = \frac{4}{3} \frac{\sigma_T c}{(m c^2)^2} \left(\frac{B}{8\pi^2} + \rho_{\text{rad}} \right) E^2$$

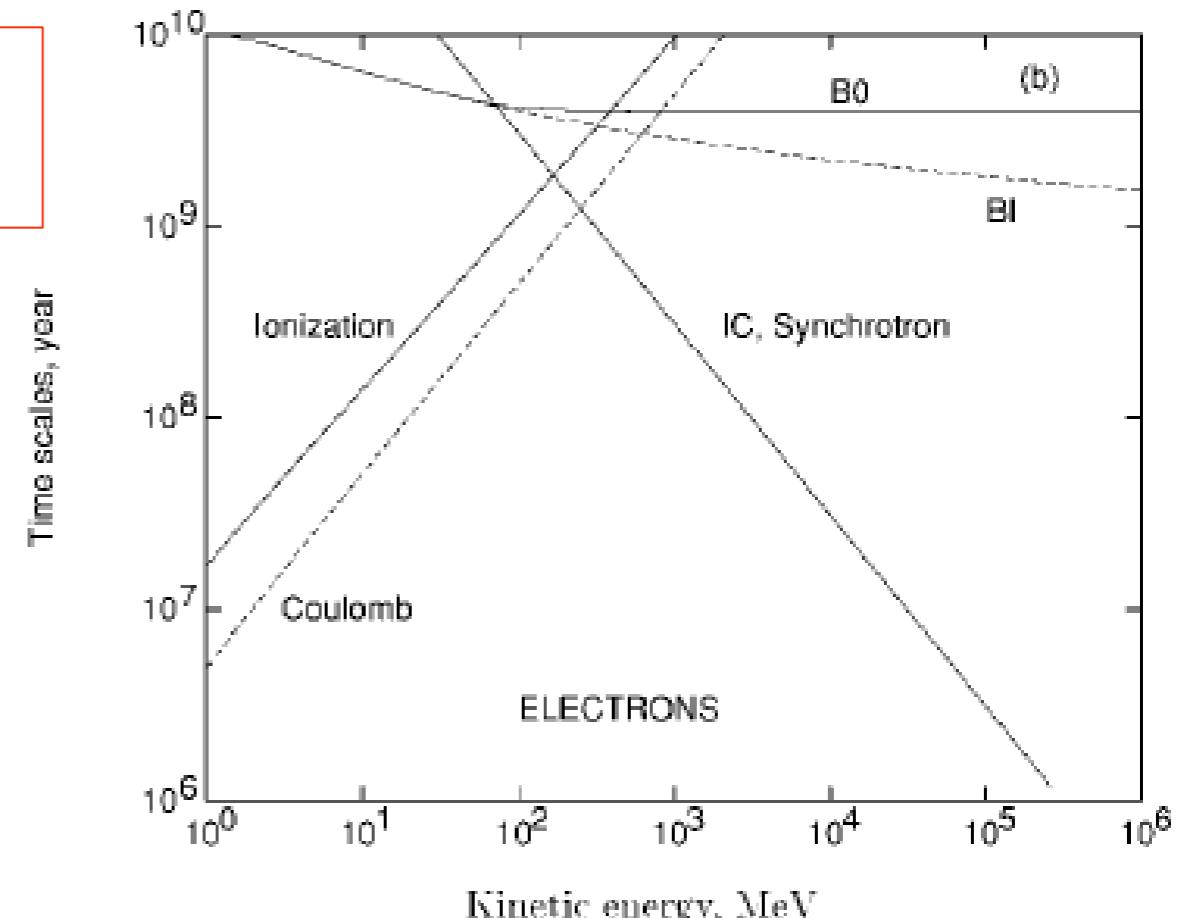
↑ ↑
synchro IC

at the solar system $b \approx 1 \times 10^{-16} \text{ GeV}^{-1} \text{ s}^{-1}$

below 0.1 GeV

$$\tau_{\text{loss}}^{ion} = \left(-\frac{1}{E} \frac{dE}{dt} \right)^{-1} = 10^8 \left(\frac{E}{1 \text{ GeV}} \right) \left(\frac{n_{\text{gas}}}{1 \text{ cm}^{-3}} \right)^{-1} \text{ yr}$$

ionization losses



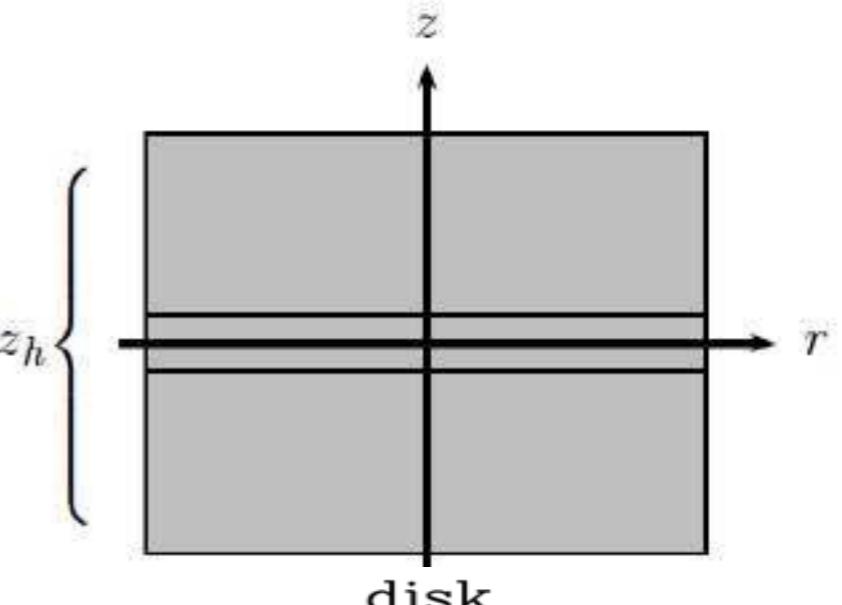
$$\tau_{\text{loss}}(1 \text{ GeV}) \sim 10^8 \text{ yr} ; \quad \tau_{\text{loss}}(100 \text{ GeV}) \sim 10^6 \text{ yr}$$

The effects of energy losses

Bulanov & Dogel 74, Berezinsky et al. 1990

Diffusive loss length

$$\lambda_{\text{loss}}(E) = \left(\int_0^{\tau_{\text{loss}}(E)} D(E') dE' \right)^2 = \left(\int_0^E \frac{D(E')}{b(E')} dE' \right)^2$$



This has to be compared with the halo scale height z_t

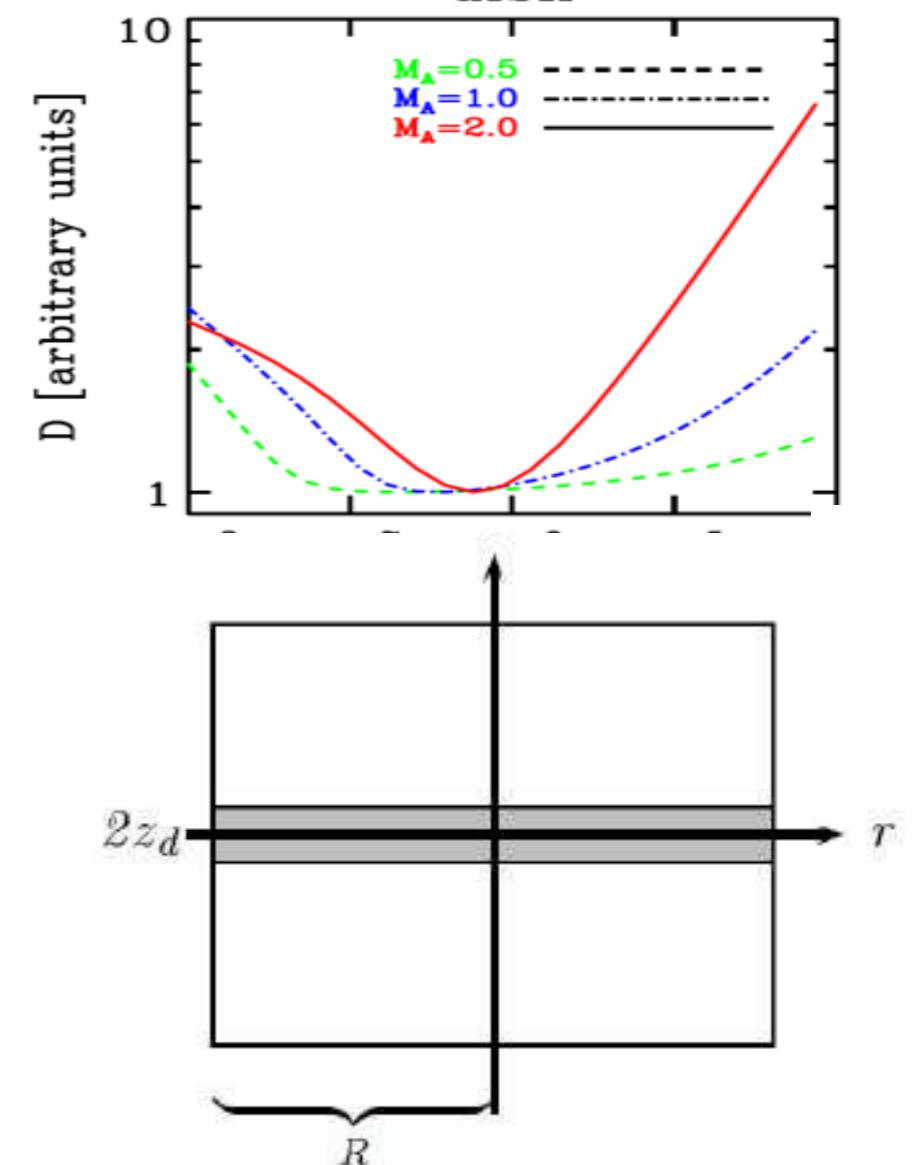
λ_{loss} become smaller than z_t for

$$E > E_* \simeq \frac{10}{1-\delta} \left(\frac{D_0}{10^{28} \text{ cm}^2/\text{s}} \right) \left(\frac{z_t}{1 \text{ kpc}} \right)^{-2} \text{ GeV}$$

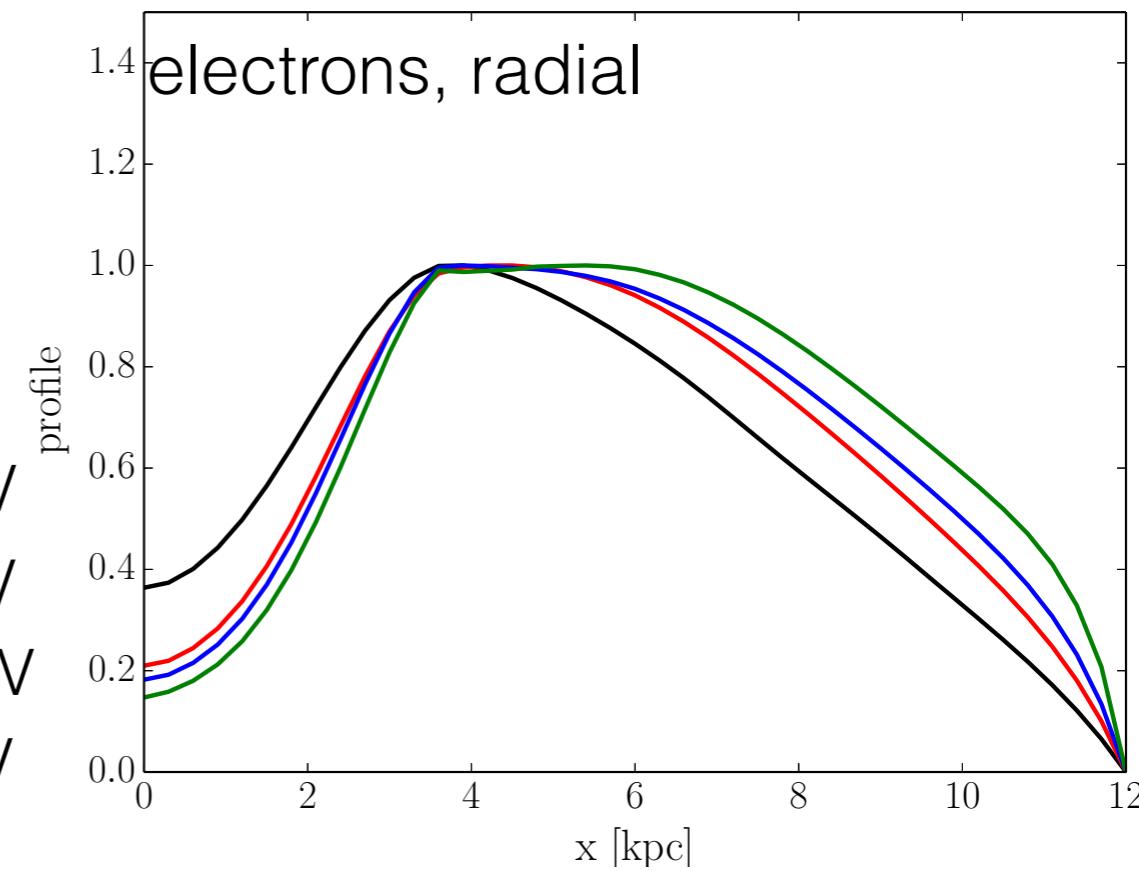
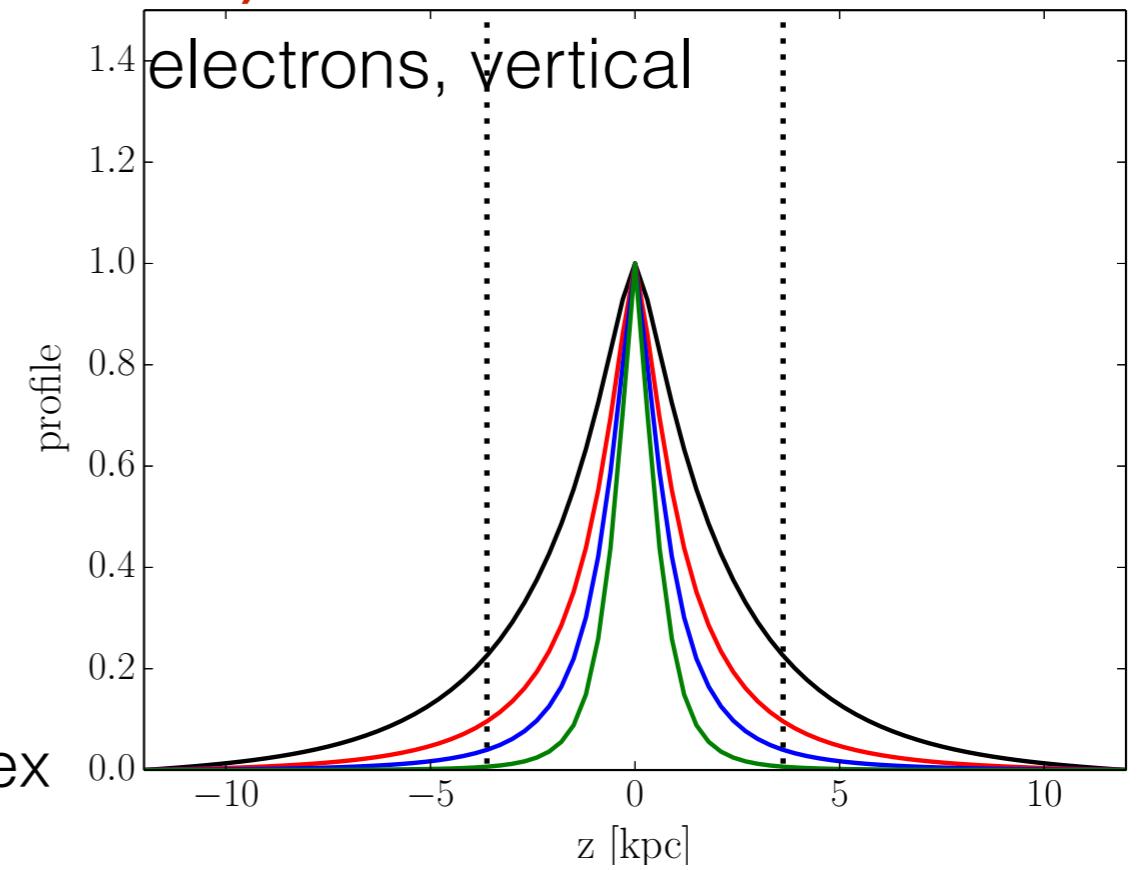
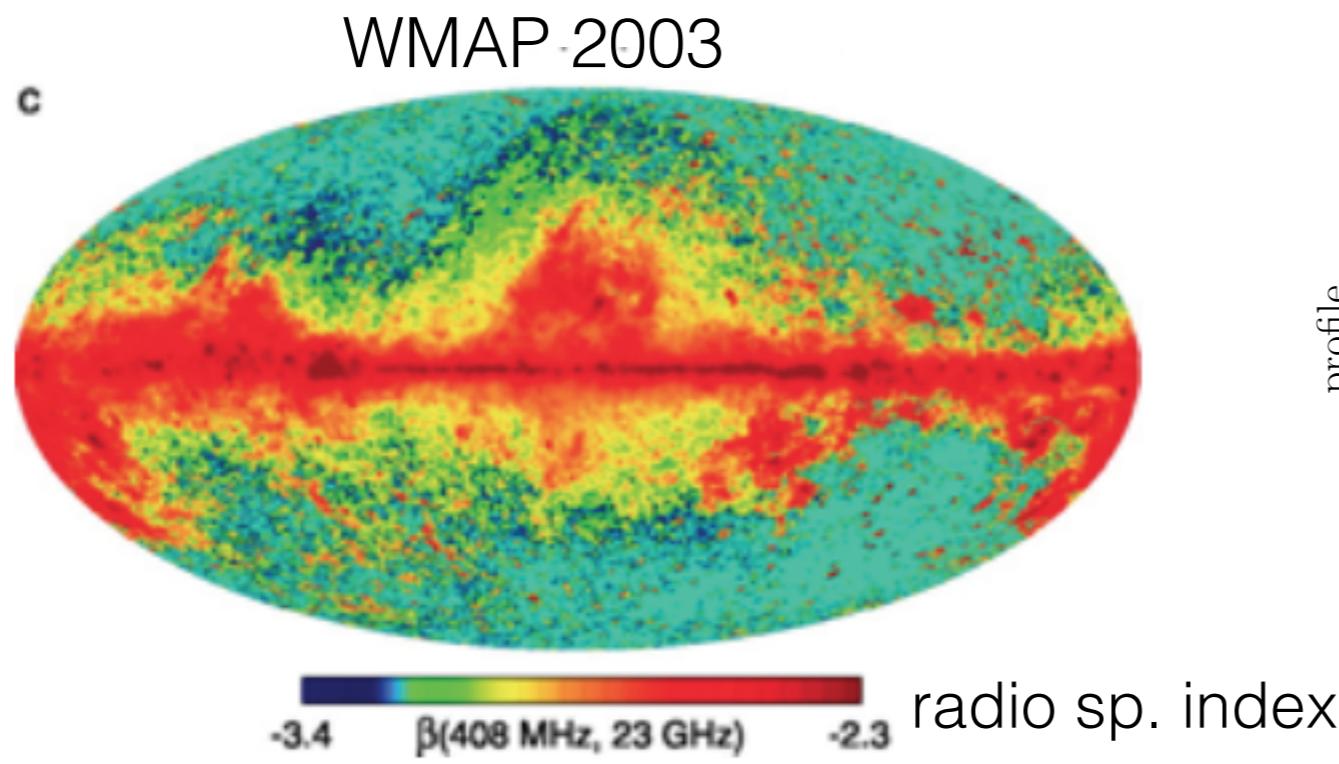
this few GeV for the models considered.

Electrons do not escape the disk ($z_d \sim 100$ pc) only above several TeV.

Note that $z_d \simeq$ mean separation between SNRs



The effect of energy losses (no arms case)



in these plots
 $D_0 = 2.6$, **$z_t = 4 \text{ kpc}$**
plain diffusion

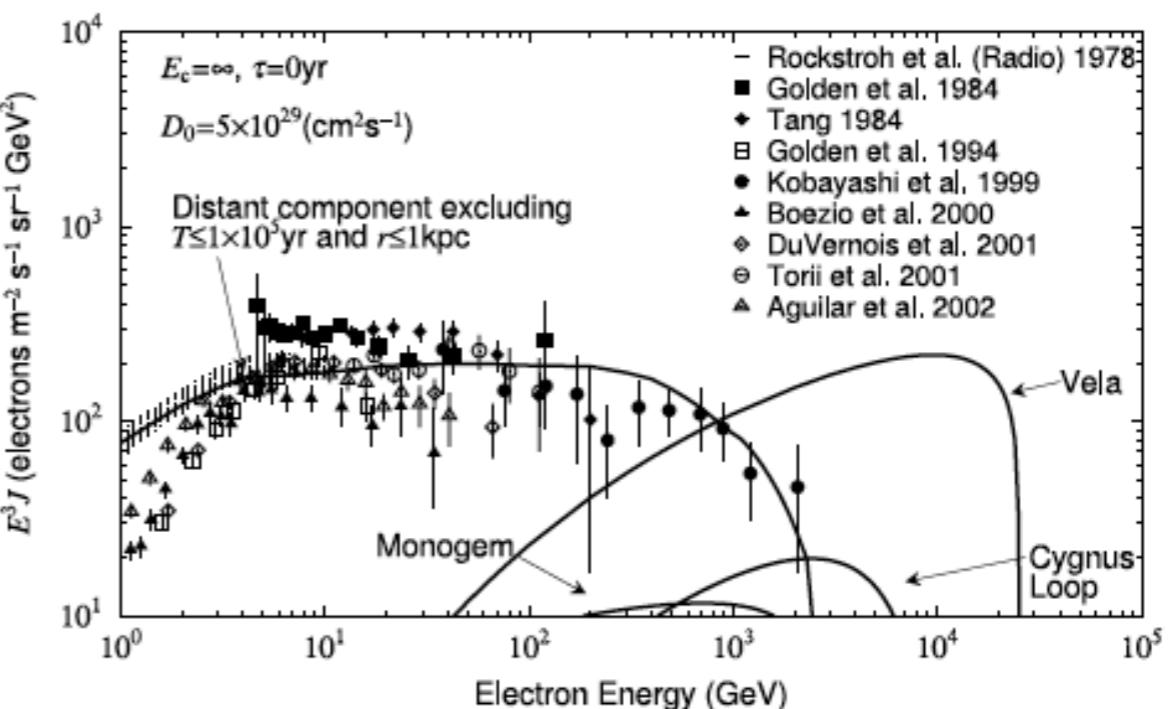
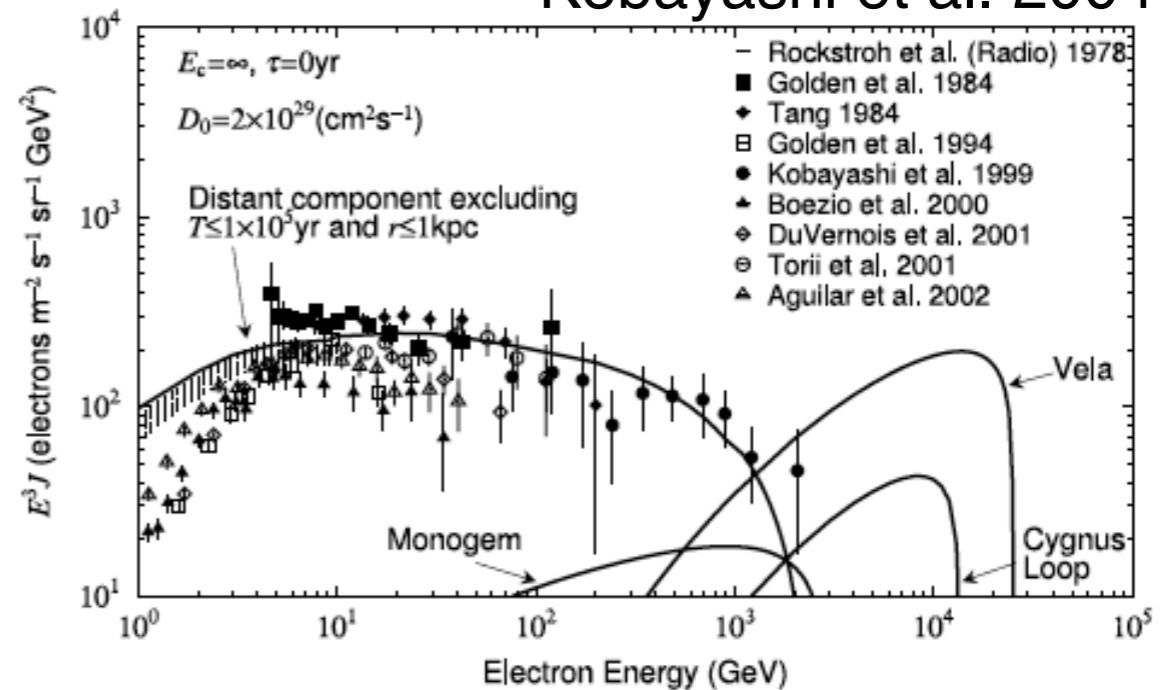
- $E = 1 \text{ GeV}$
- $E = 10 \text{ GeV}$
- $E = 100 \text{ GeV}$
- $E = 1 \text{ TeV}$

The effect of energy losses (source stochasticity)

Above/near the TeV only a few prominent sources may contribute to the e^\pm flux reaching the Earth

therefore above/near that energy to assume a continuous source distribution may be inadequate !

Kobayashi et al. 2004



Primary and secondary e^\pm

This is assuming that e^+ are only secondary products of CR interaction with the ISM

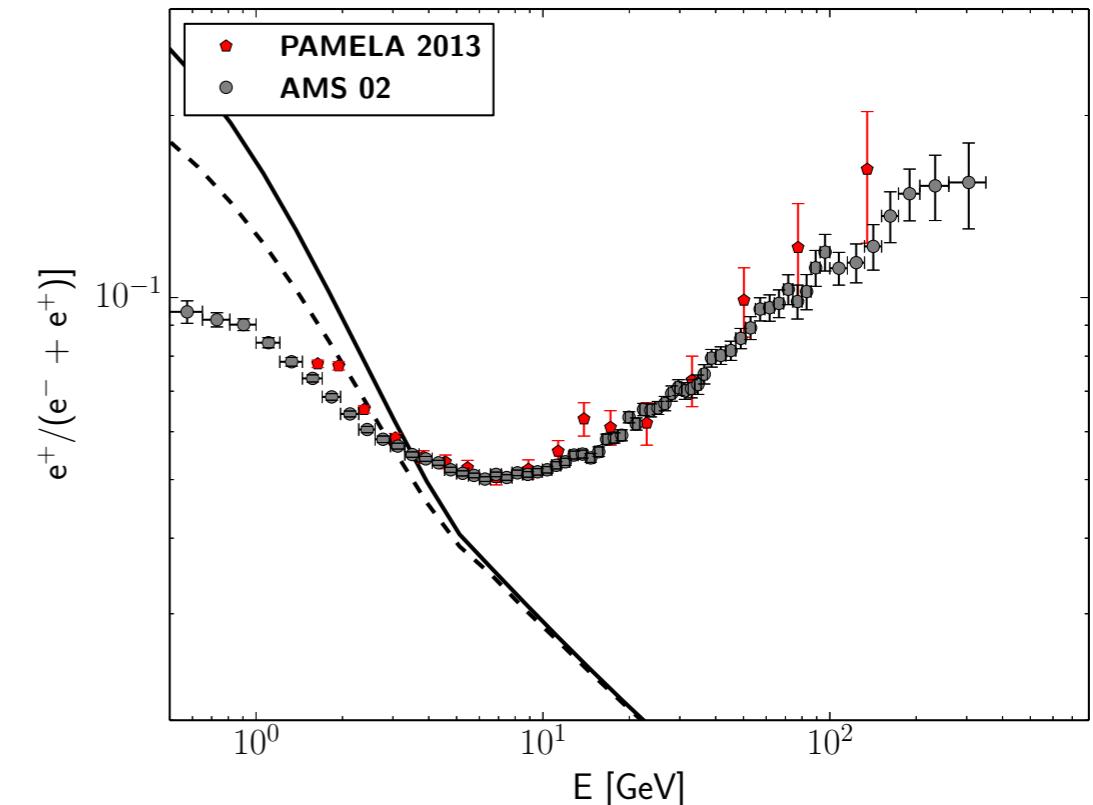
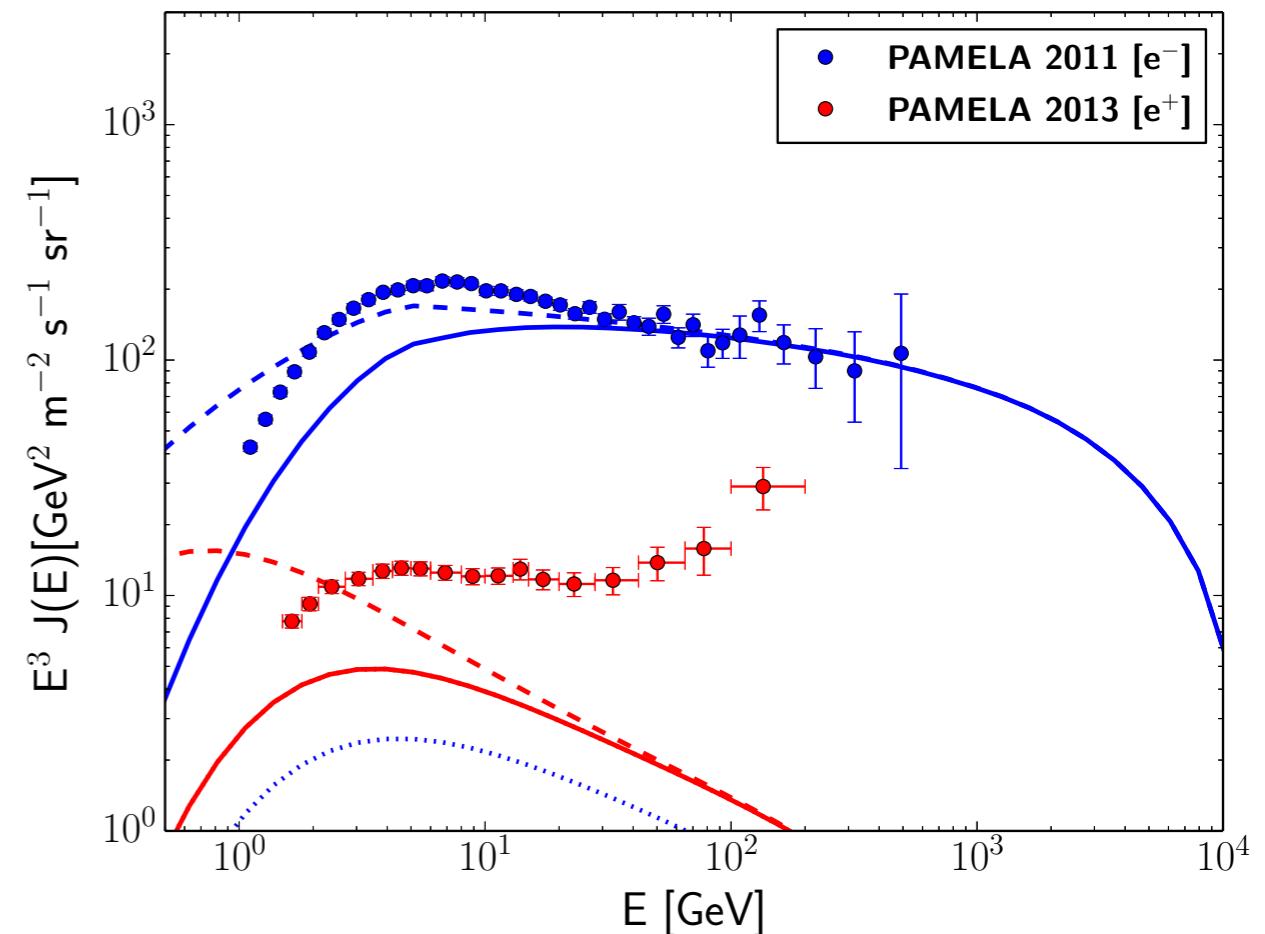
In this plots the e^- source spectral index is

$$\alpha(e^-) = 1.6/2.3 \quad a/b \text{ 4 GeV}$$

plain diffusion model which match light nuclei with $L = 4 \text{ kpc}$

- total modulated e^-
- - - total unmodulated e^-
- secondary e^-
- secondary = total e^+

$$\Phi = 0.4 \text{ GV}$$



Primary and secondary e^\pm

This is assuming that e^+ are only secondary products of CR interaction with the ISM

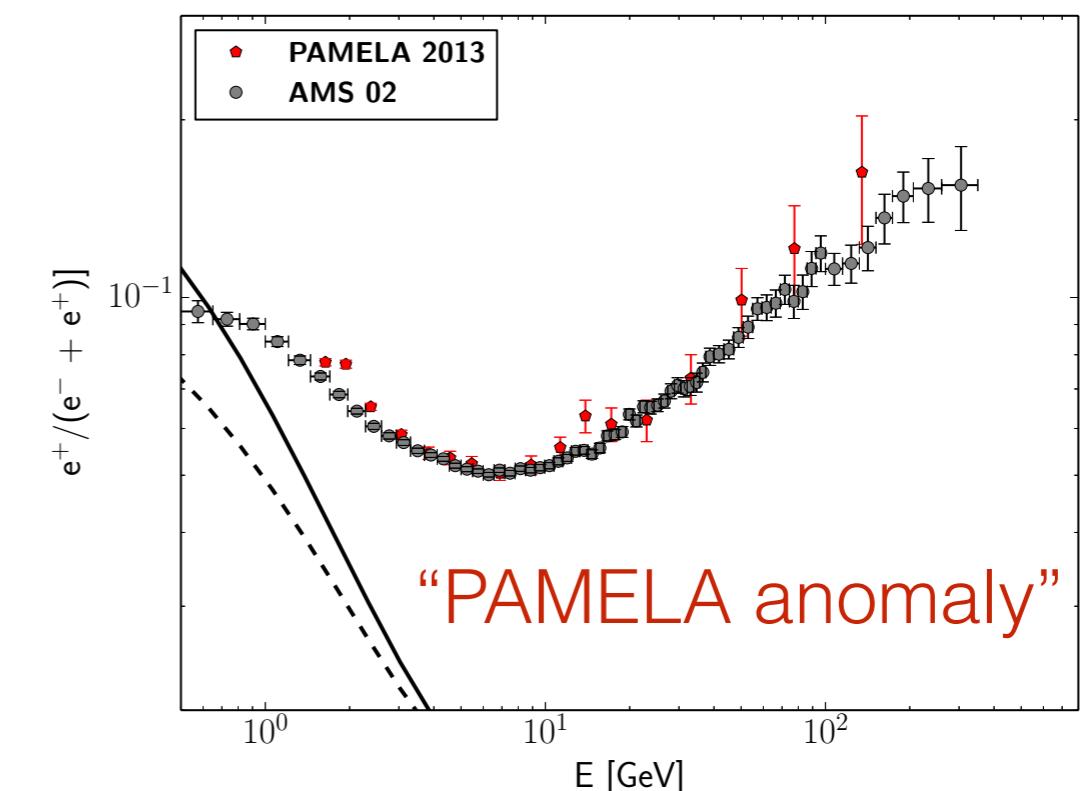
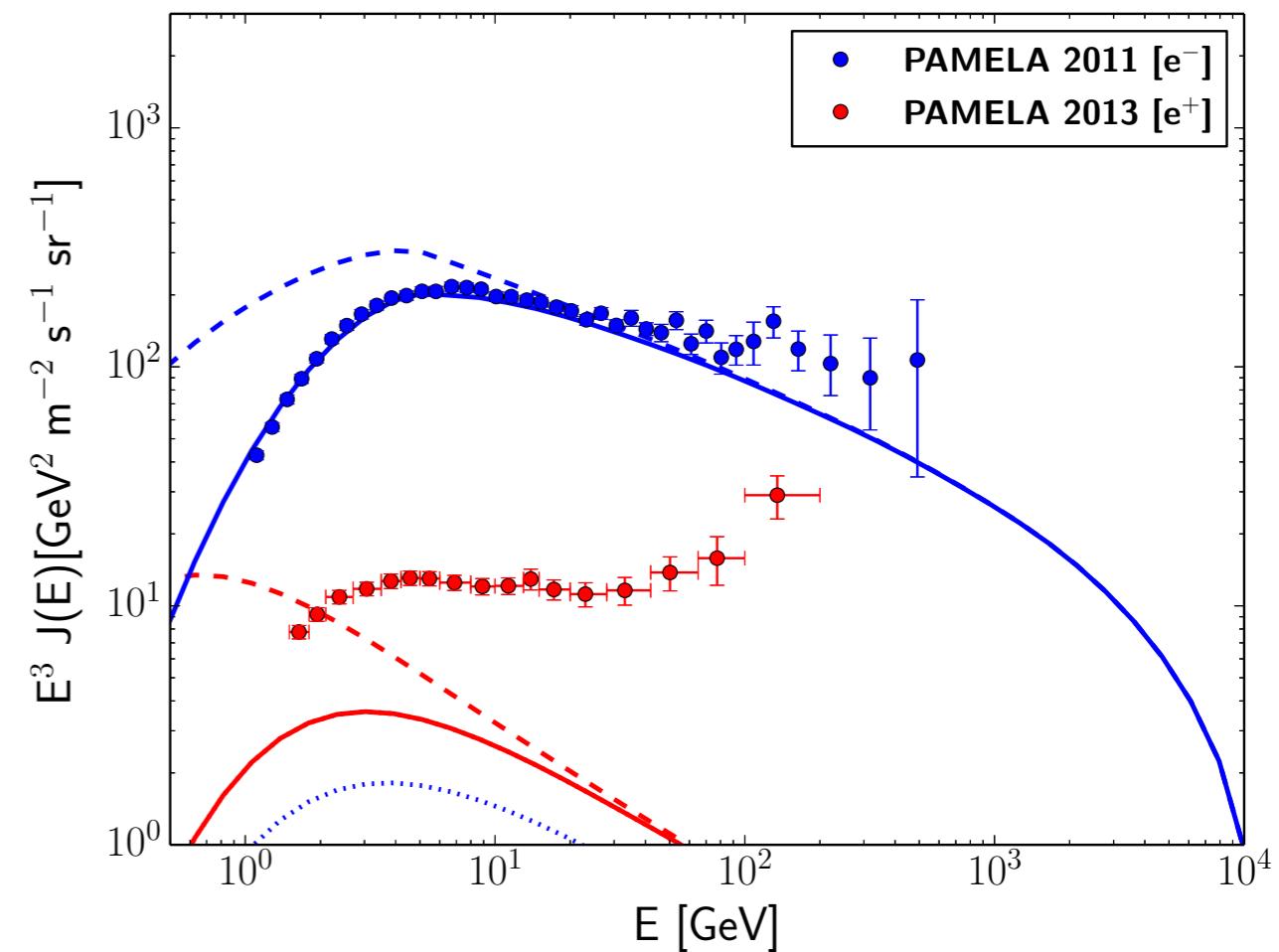
In this plots the e^- source spectral index is

$$\alpha(e^-) = 1.6/2.5 \quad a/b \text{ 4 GeV}$$

plain diffusion model which match light nuclei with $L = 4 \text{ kpc}$

- total modulated e^-
- - - total unmodulated e^-
- secondary e^-
- secondary = total e^+
- - - unmodulated “ e^+

$$\Phi = 0.4 \text{ GV}$$



Primary and secondary e^\pm

for several propagation setups

This is assuming that e^+ are only secondary products of CR interaction with the ISM

Propagation setups in this plots

PD4 $(\alpha(e^-) = 1.6/2.65)$

KRA4 $(\alpha(e^-) = 1.6/2.65)$

KOL4 $(\alpha(e^-) = 1.6/2.65)$

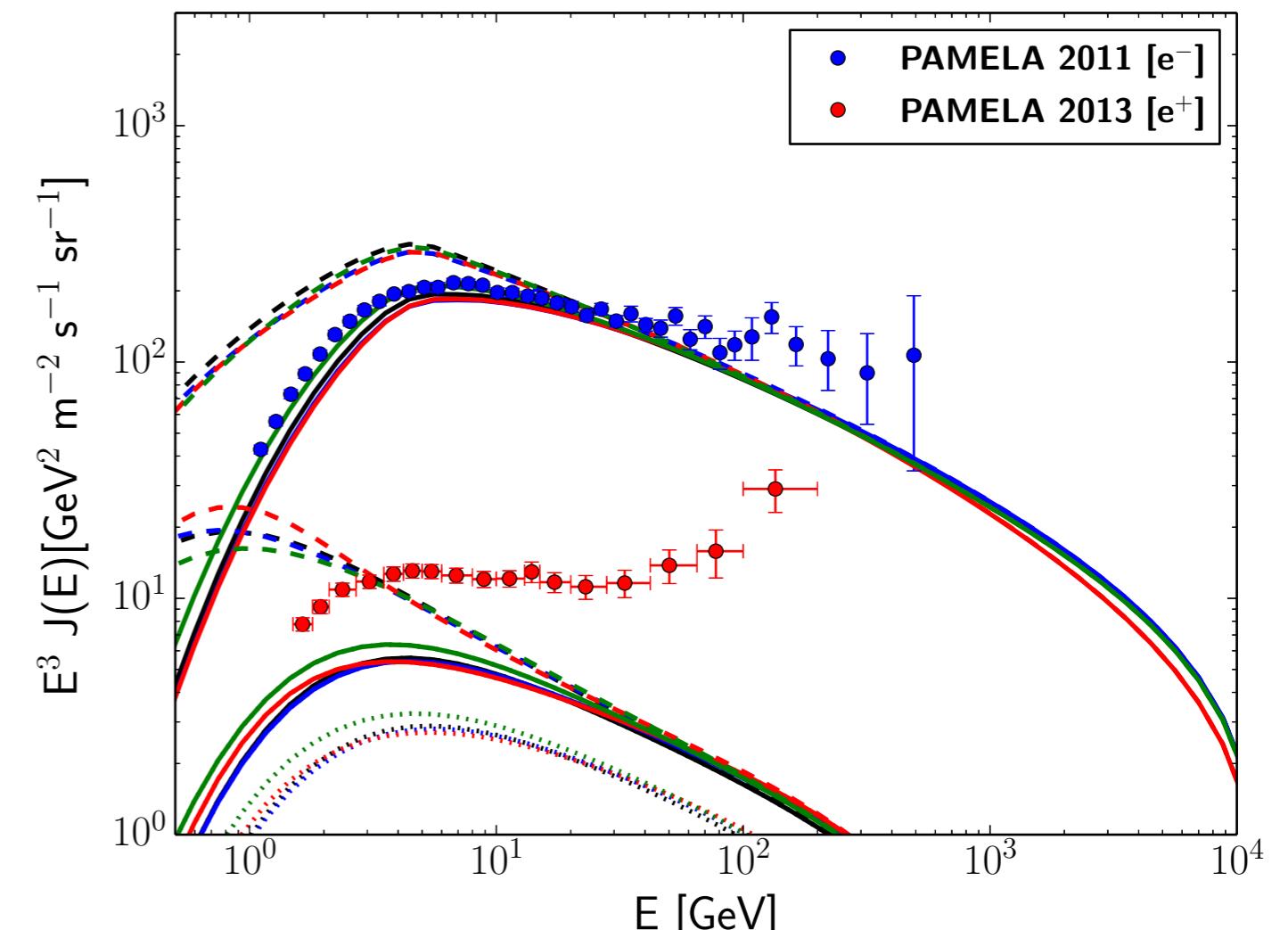
CONV4 $(\alpha(e^-) = 1.6/2.7)$

— total modulated e^-

- - - total unmodulated e^-

..... secondary mod. e^-

— secondary = total e^+



(for all these models Exp profile for D with **$z_t = 4 \text{ kpc}$**)

PAMELA anomaly is independent on the choice of the propagation setup !

Primary and secondary e^\pm

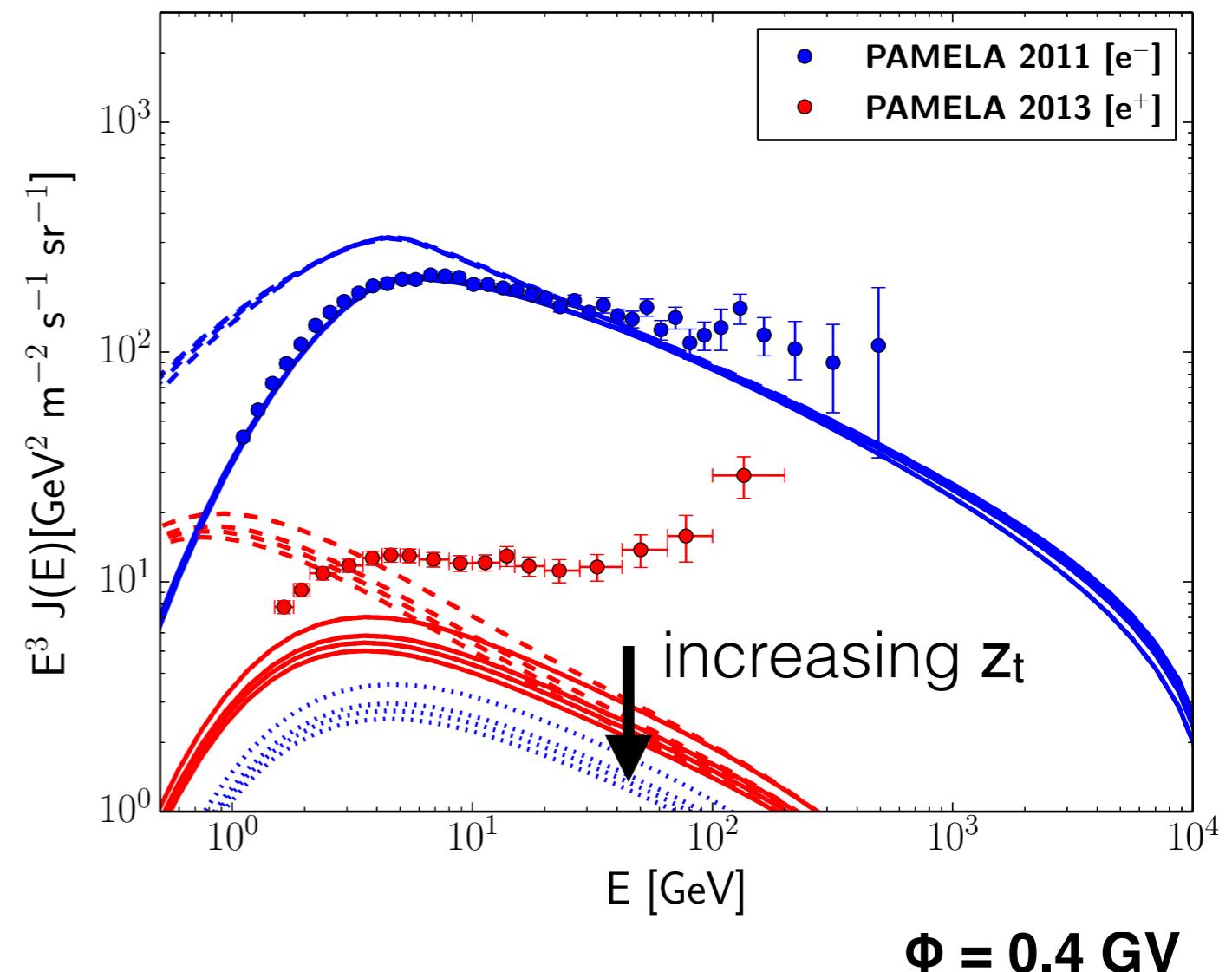
the effect of changing the halo height

This is assuming that e^+ are only secondary products of CR interaction with the ISM

Propagation setups in this plots

PD2
PD4
PD6
PD8

- total modulated e^-
- - - total unmodulated e^-
- secondary mod. e^-
- secondary = total e^+

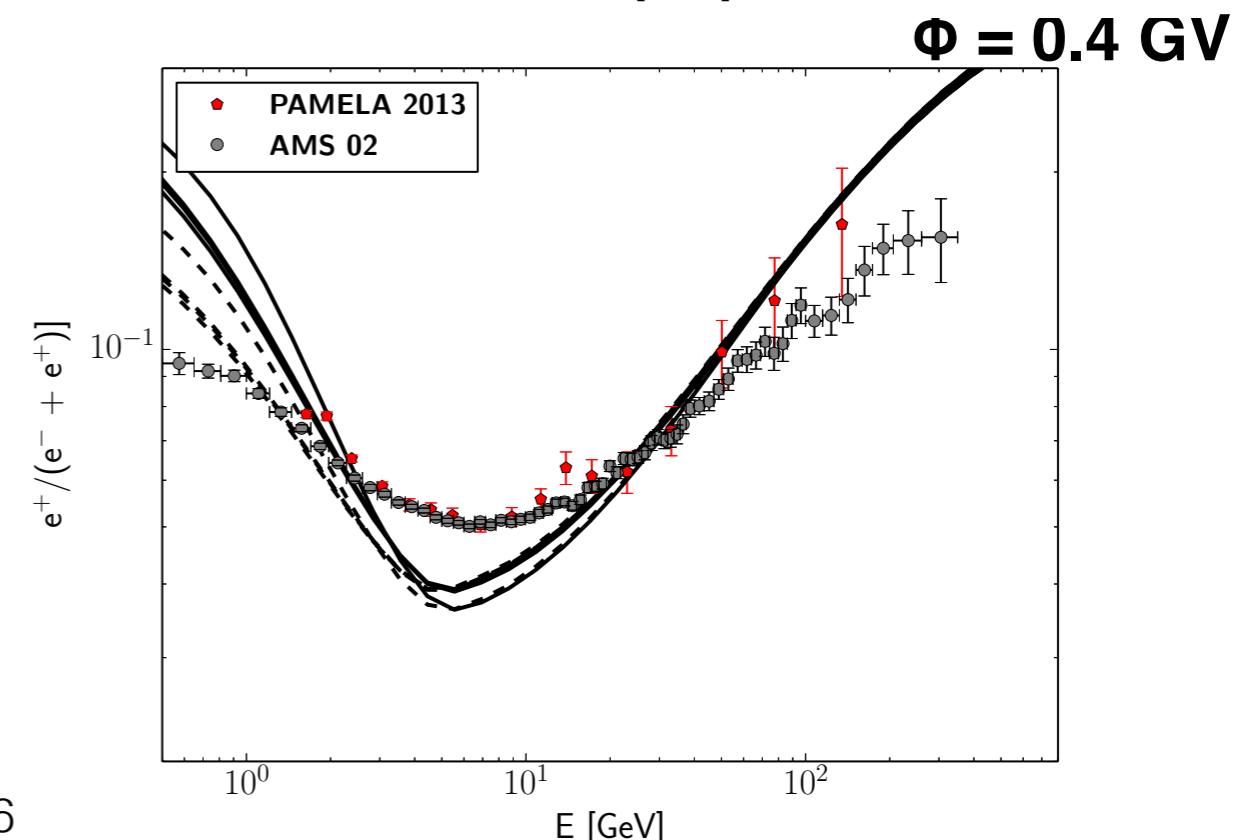
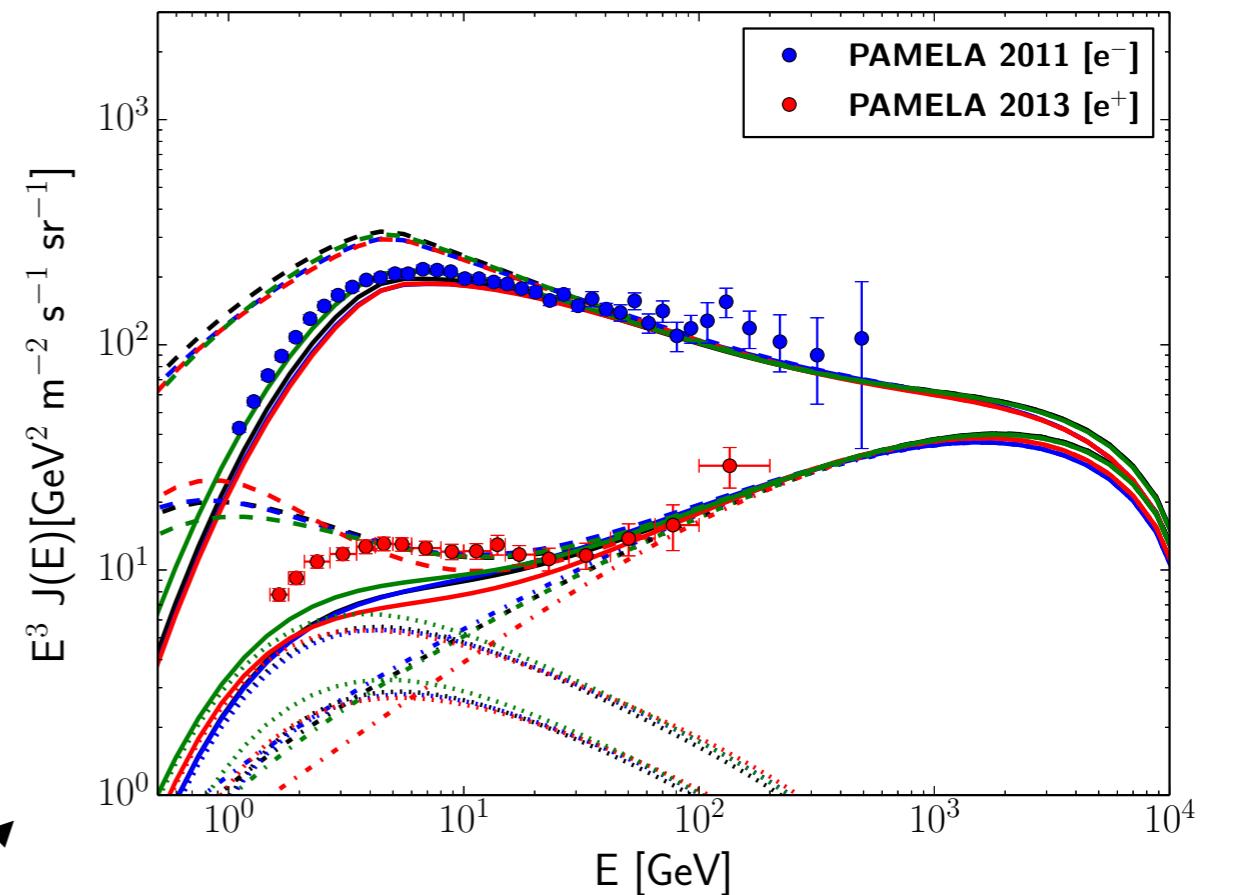
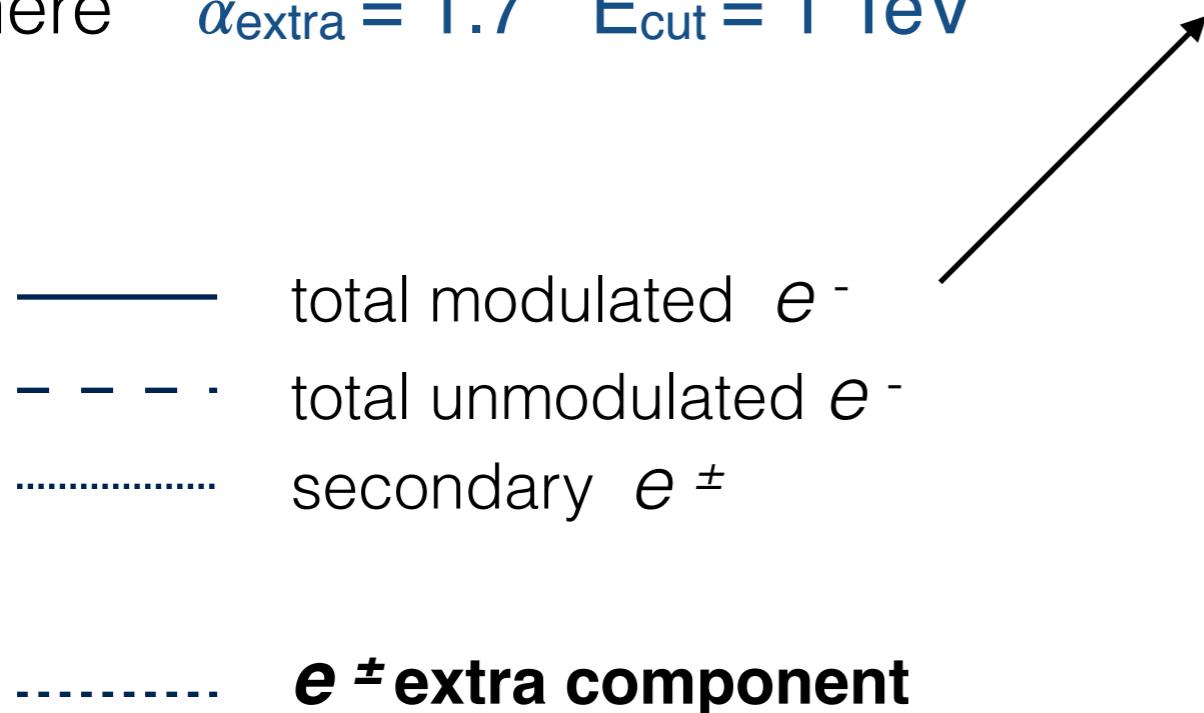


The extra component paradigm

This is assuming a charge symmetric e^\pm extra component with a continuous source distribution tracing SNR (pulsar) (no arms) and source spectrum

$$J(e^\pm) \propto E^{-\alpha_{\text{extra}}} \exp(-E/E_{\text{cut}})$$

here $\alpha_{\text{extra}} = 1.7$ $E_{\text{cut}} = 1 \text{ TeV}$



The effect of spiral arms

Star formation take place mainly in spiral arms

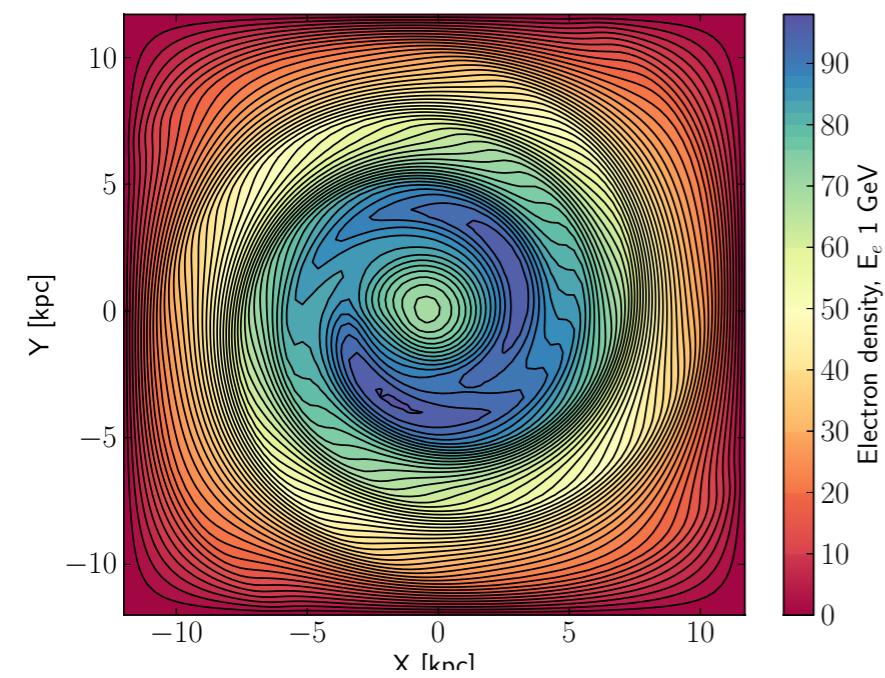
distance between arms
 $\simeq 1 \text{ kpc}$

we are in a low density region between two arms

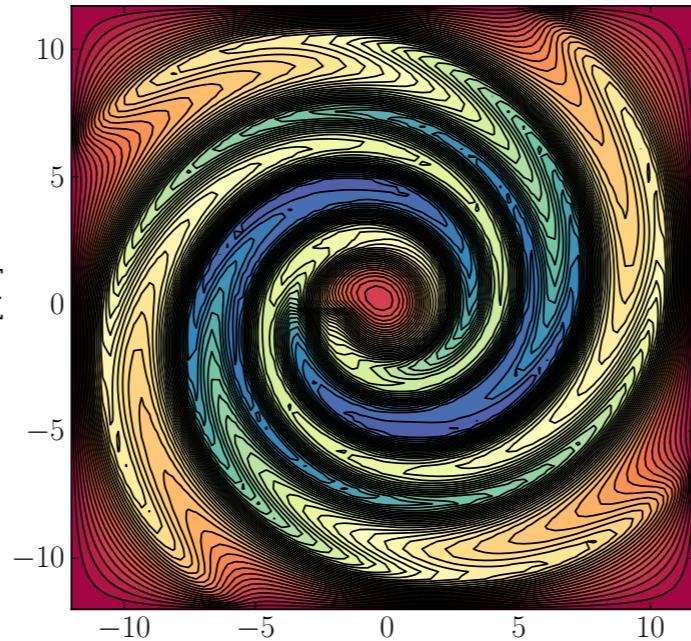


arms make the difference !

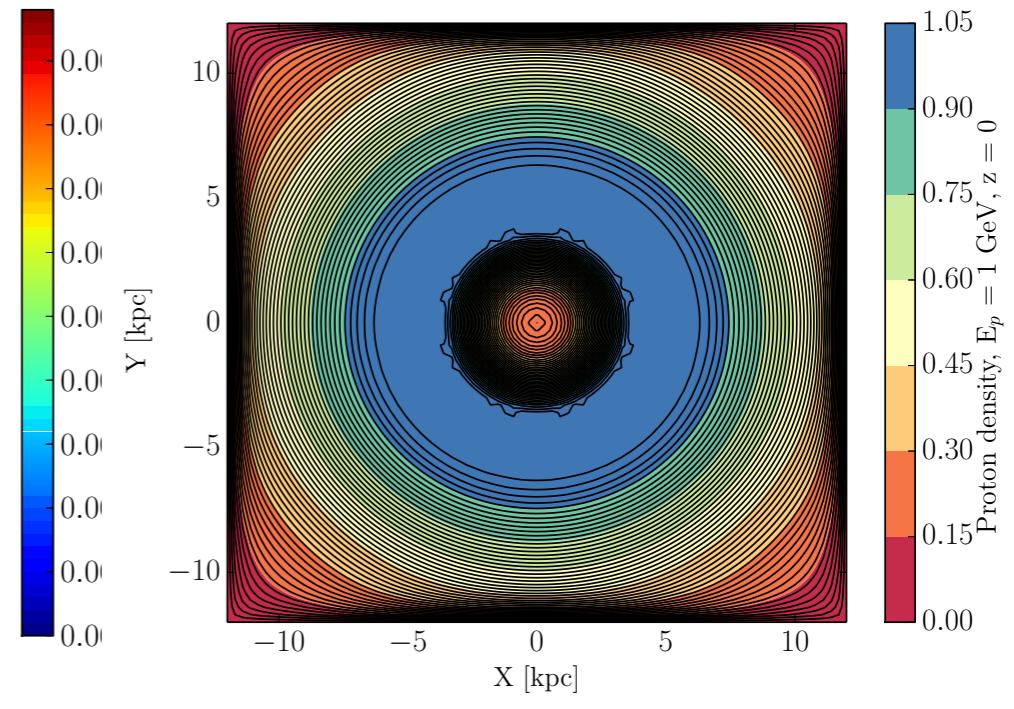
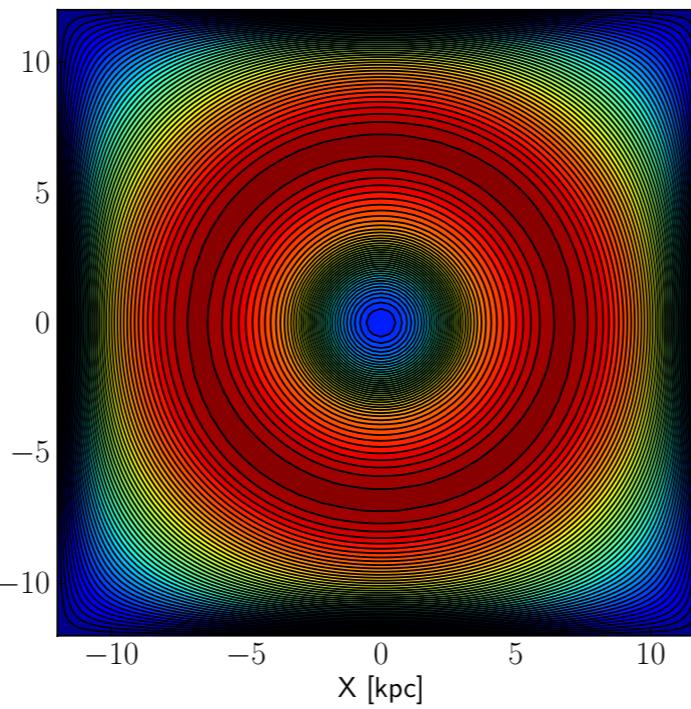
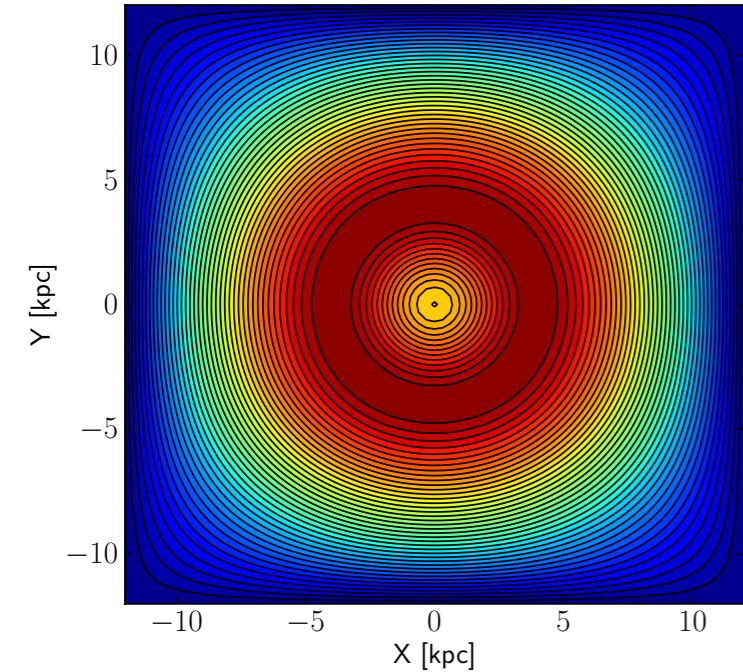
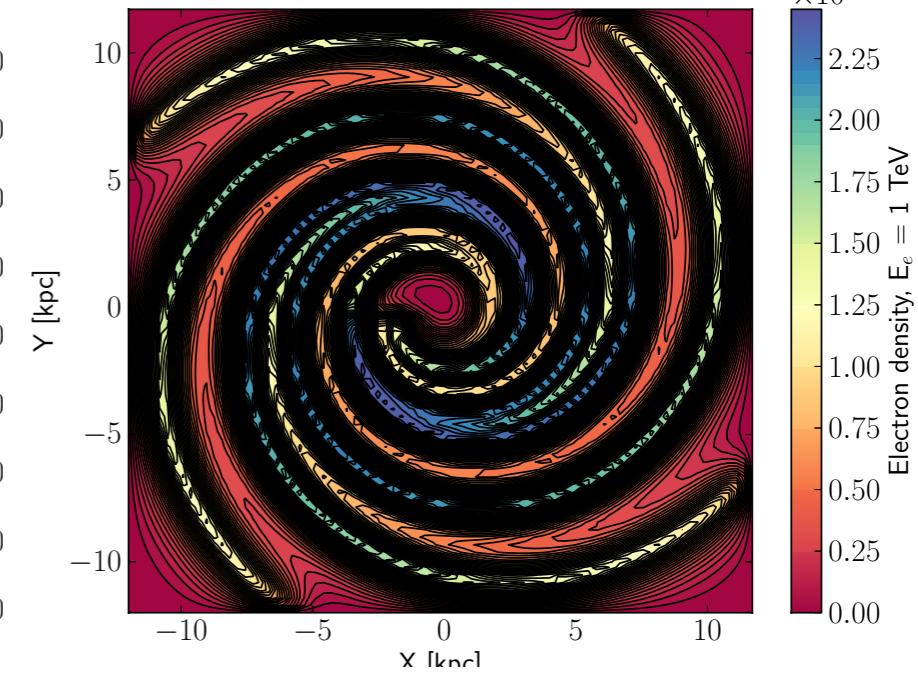
10 GeV



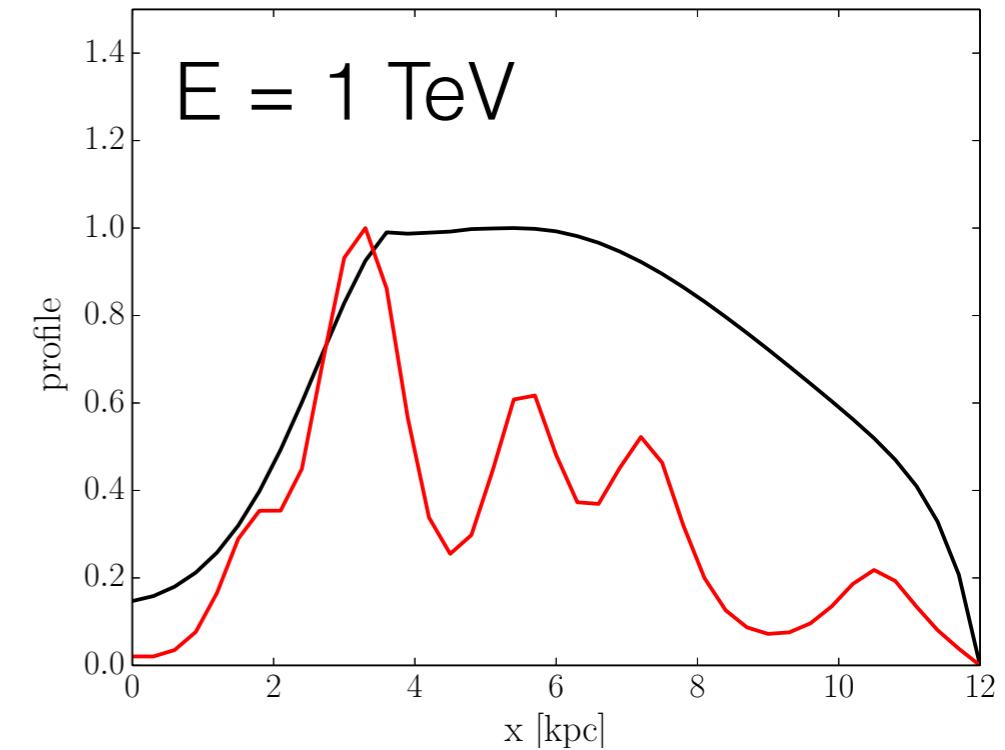
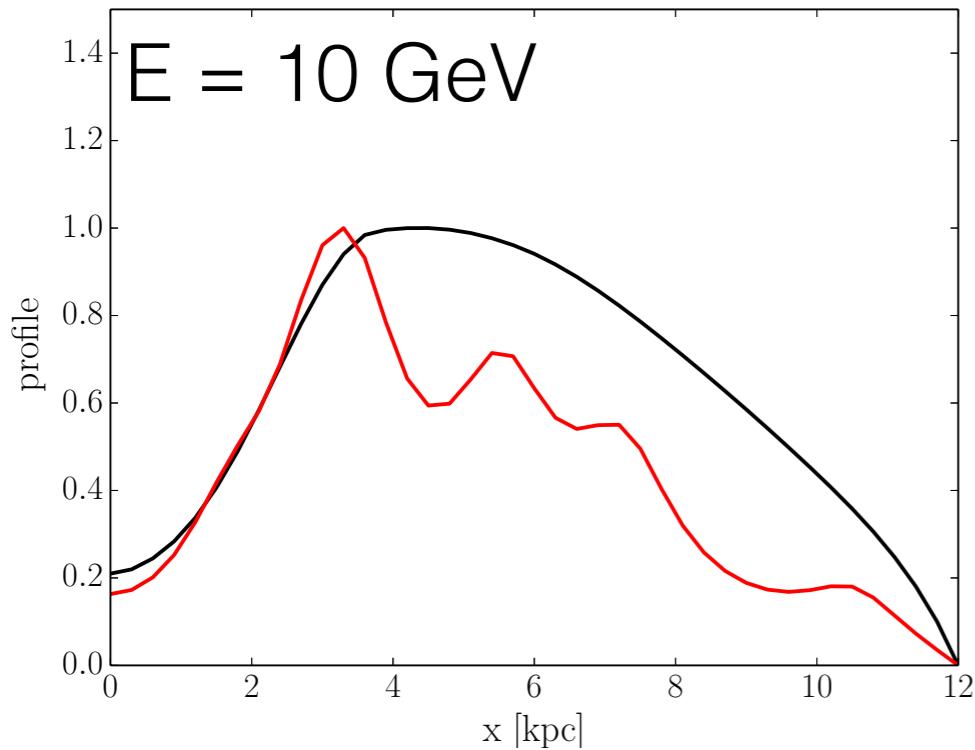
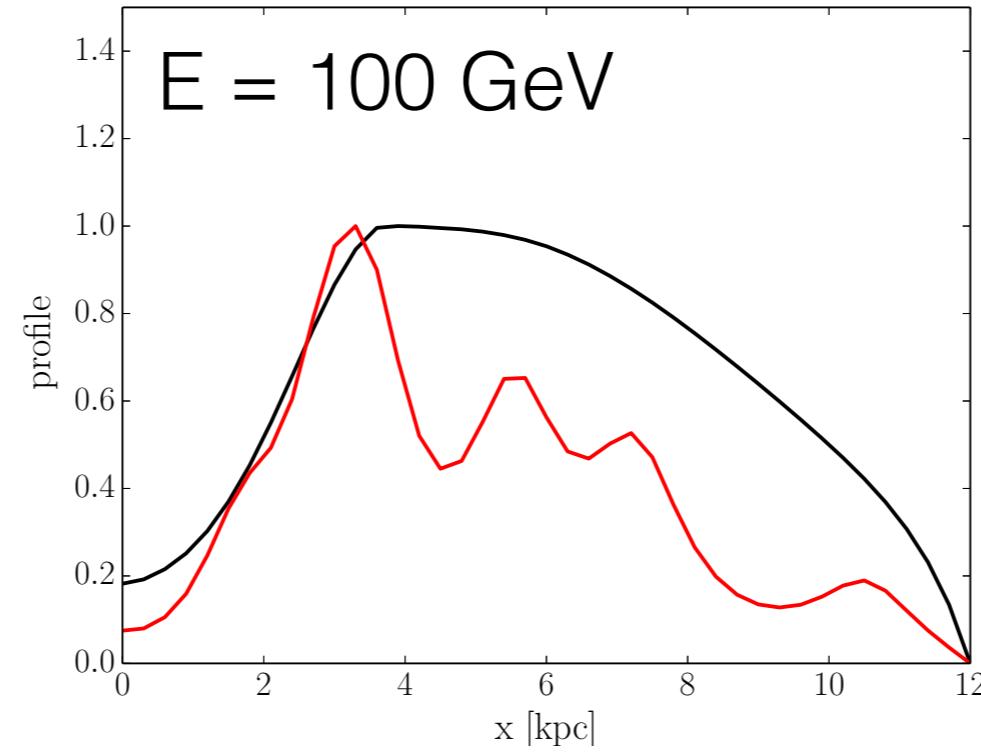
100 GeV



1 TeV

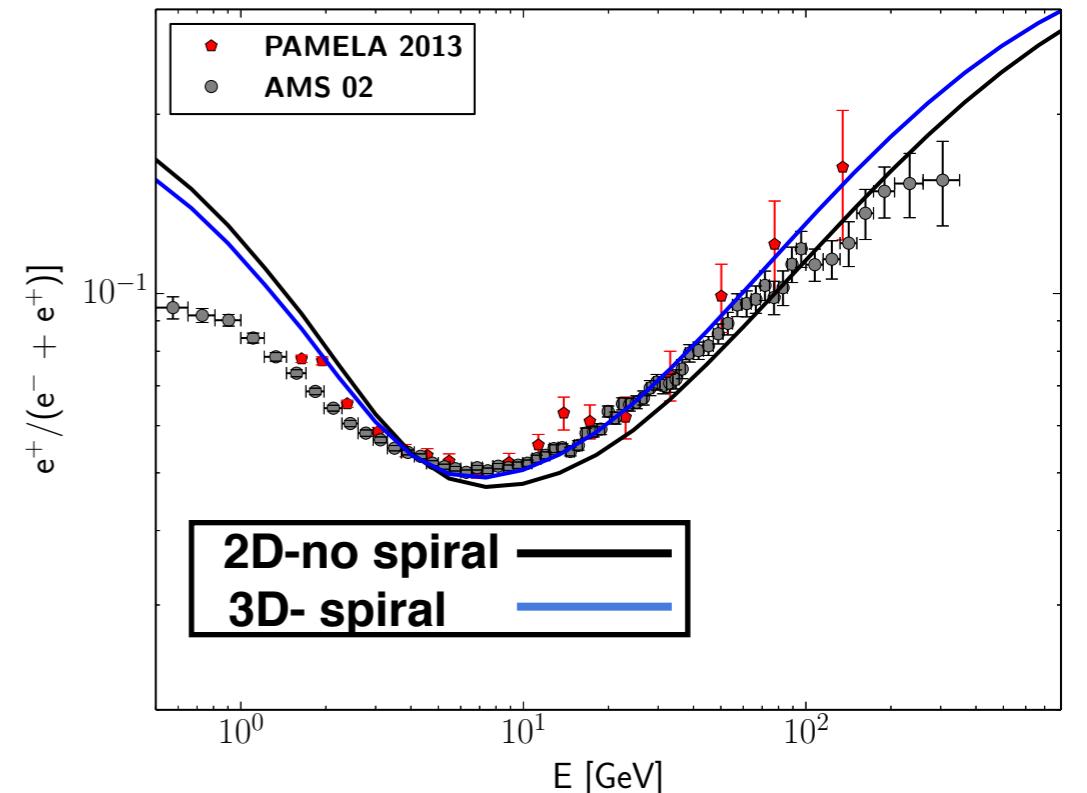
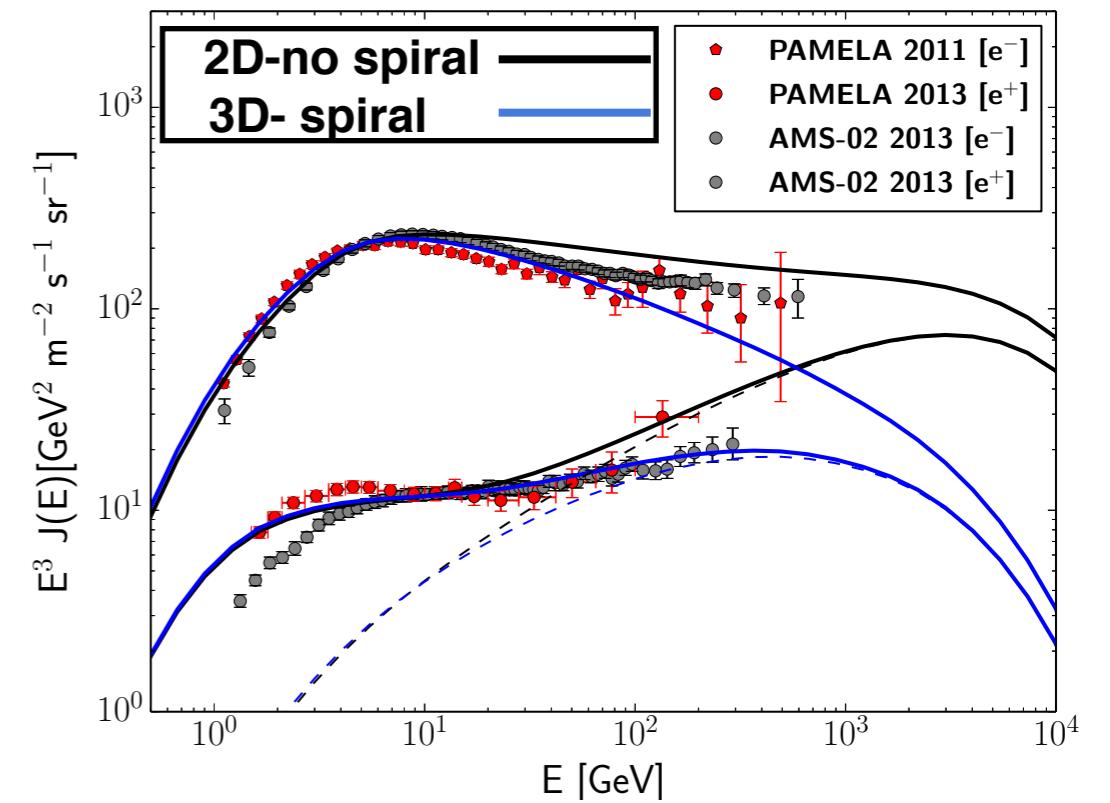


Arms make the difference ! (radial profile)



The effect of the spiral arms on the lepton spectra

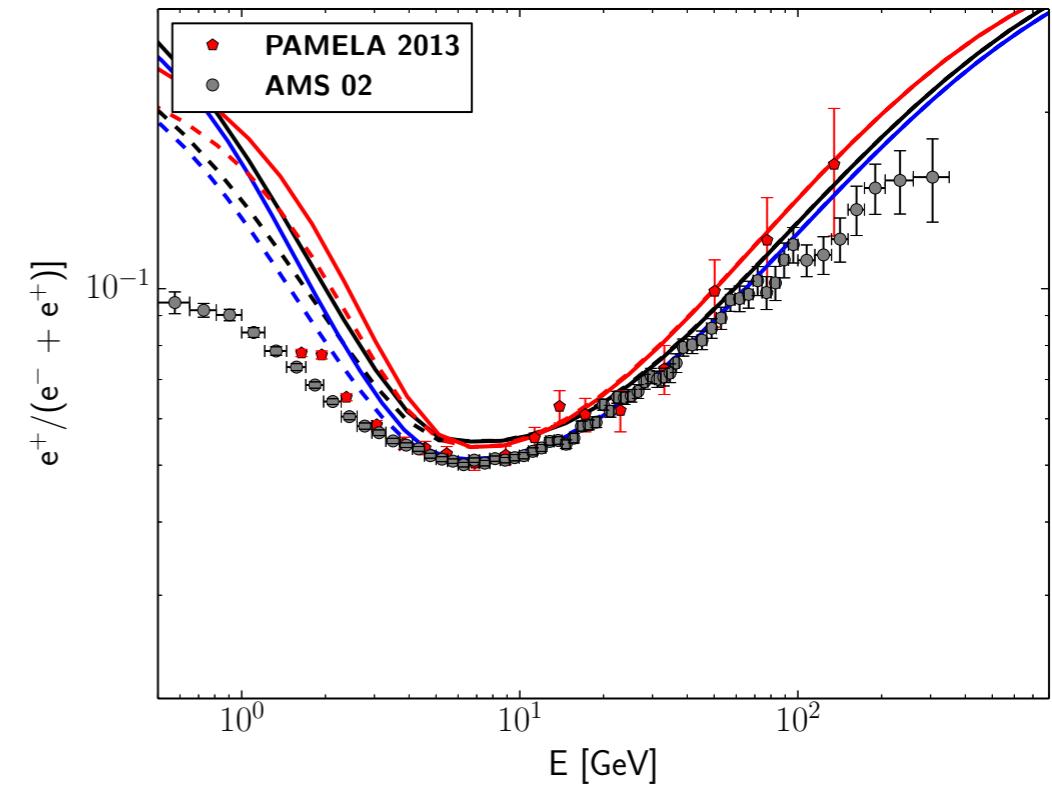
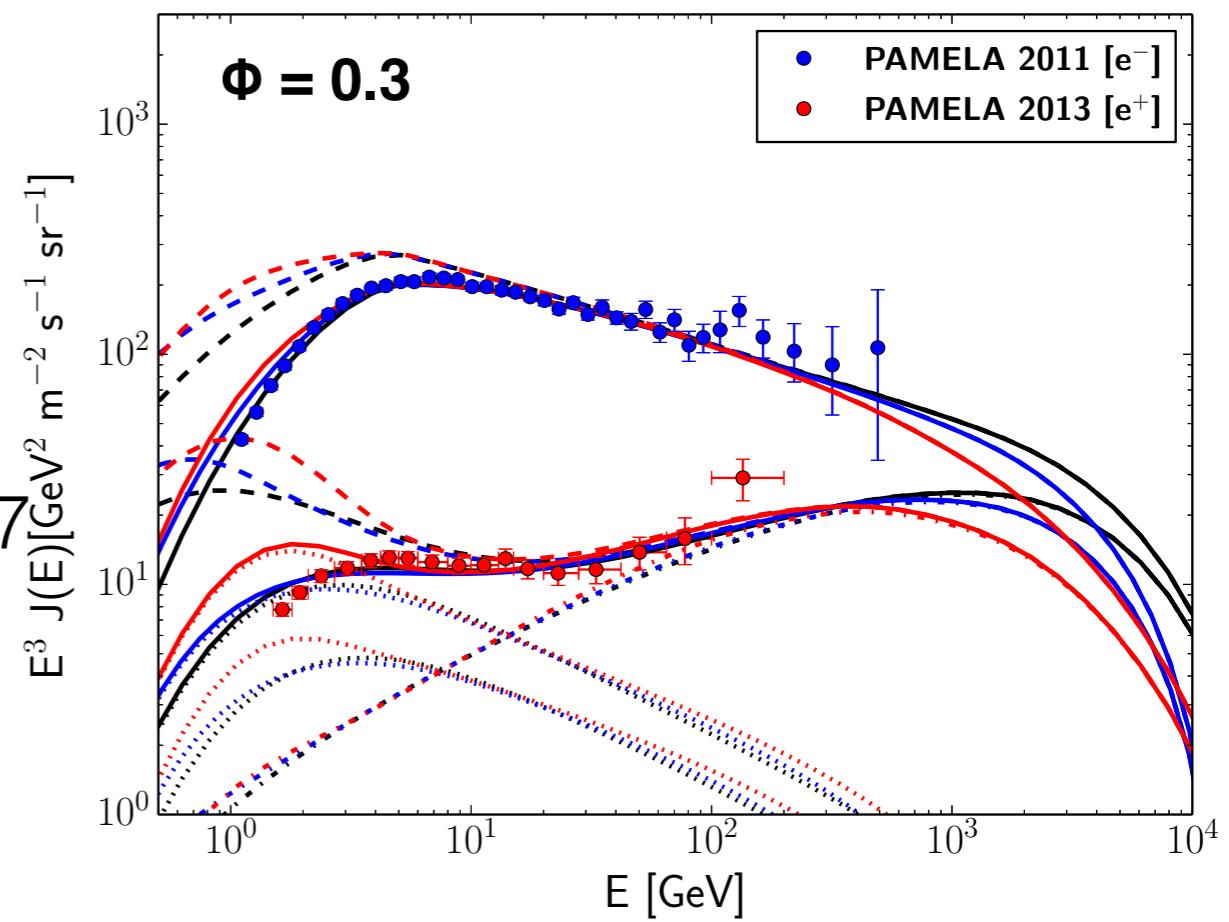
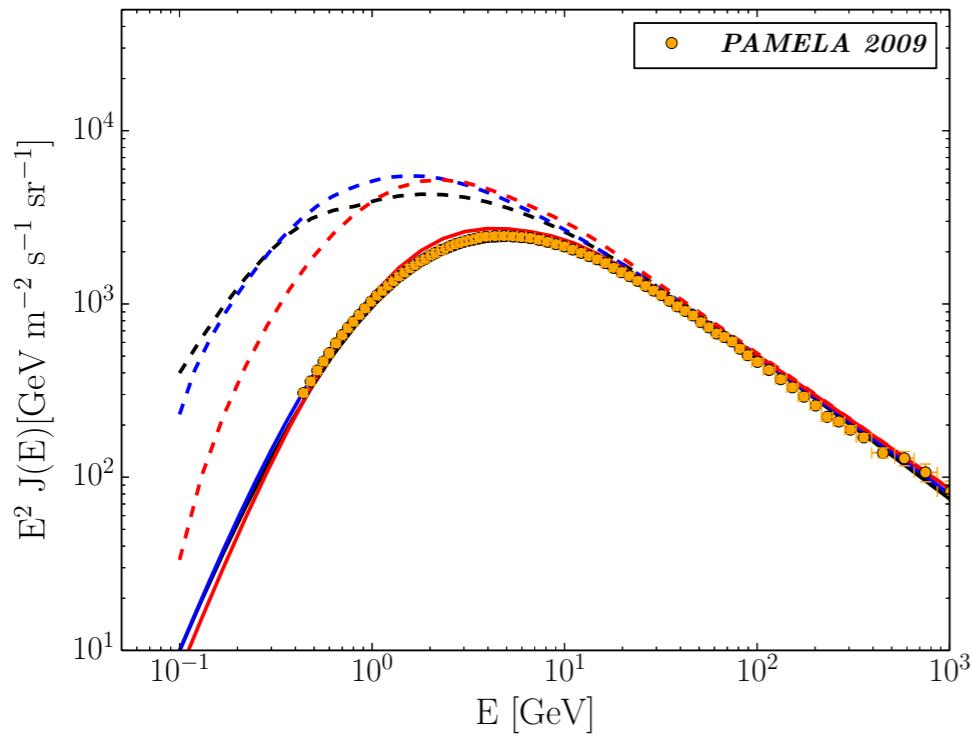
- Energy losses in the inter-arm region change dramatically the e^- and e^+ spectra above 20 GeV
- the effect is almost absent in the positron fraction (PAMELA pf and FERMI $e^- + e^+$ were reproduced in 2D)
- even if the extra-component is due to DM (not affected by arms), the e^- background computed in 2D is unrealistic



3 (almost) good models in 3D

PD $\alpha_p = 2.22$ $\alpha_{e^-} = 1.6/2.5$ $\alpha_{\text{extra}} = 1.7$
KRA $\alpha_p = 2.32$ $\alpha_{e^-} = 1.7/2.5$ $\alpha_{\text{extra}} = 1.7$
KOL $\alpha_p = 2.1/2.45$ $\alpha_{e^-} = 1.8/2.5$ $\alpha_{\text{extra}} = 1.7$

$z_t = 4 \text{ kpc}$



The possible effect of nearby sources

So far we modeled local source contributions adding to DRAGON output the analytical solution of diffusion/loss equation (using the same parameters we have in DRAGON in the local region).

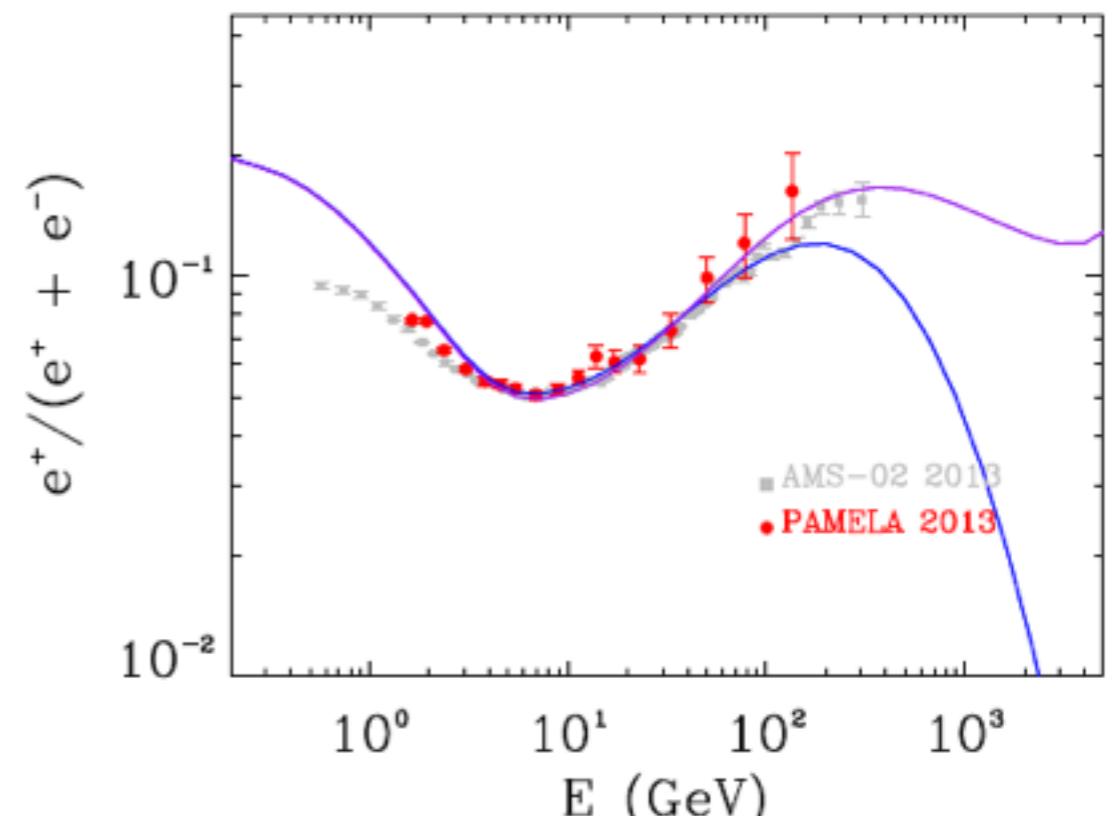
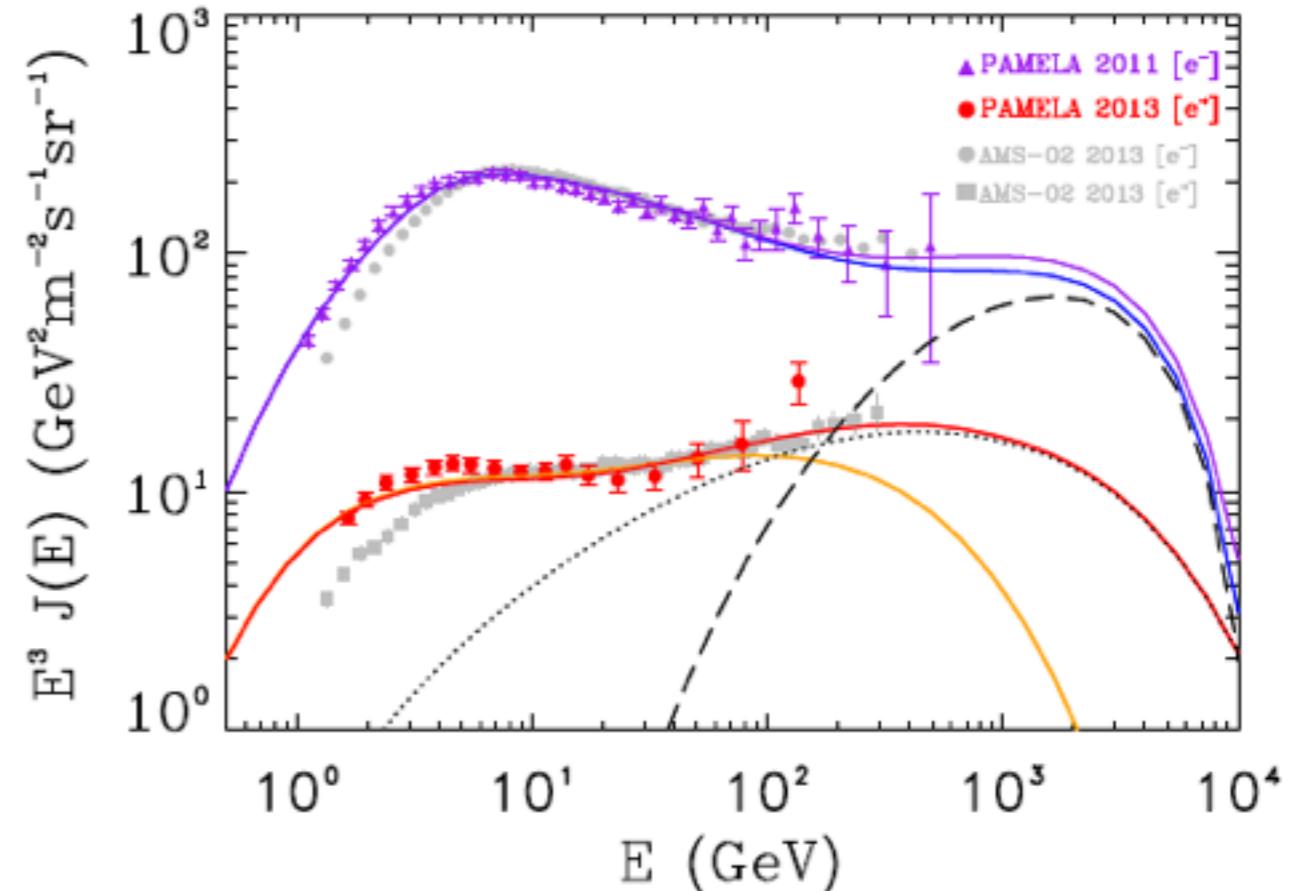
This is done with IDL/Python routines

In these figures:

Vela SNR, $d = 300$ pc, $T = 10^4$ yrs

$$\gamma_{\text{SNR}}(e^-) = 2.4 \quad E_{\text{cut}}(\text{SNR}) = 5 \text{ TeV}$$

$$E_{\text{SNR}}(e^-) = 2 \cdot 10^{48} \text{ erg}$$



The possible effect of nearby sources

So far we modeled local source contributions adding to DRAGON output the analytical solution of diffusion/loss equation (using the same parameters we have in DRAGON in the local region).

This is done with IDL/Python routine

In these figures: Vela SNR +

Monogem pulsar $d = 280$ pc, $T = 10^5$ yrs

Geminga pulsar $d = 160$ pc, $T = 3 \cdot 10^5$ yrs

for both we assume 15% e^\pm conversion effic.

$$\gamma_{\text{pulsars}}(e^\pm) = 1.9 \quad E_{\text{cut}} = 1 \text{ TeV}$$

