

Francesca Calore

# DarkSUSY: Load it! Run it! Plot it!

**CASPAR 2014: Codes in AStroPAricle Research**  
Hamburg, 17th September 2014

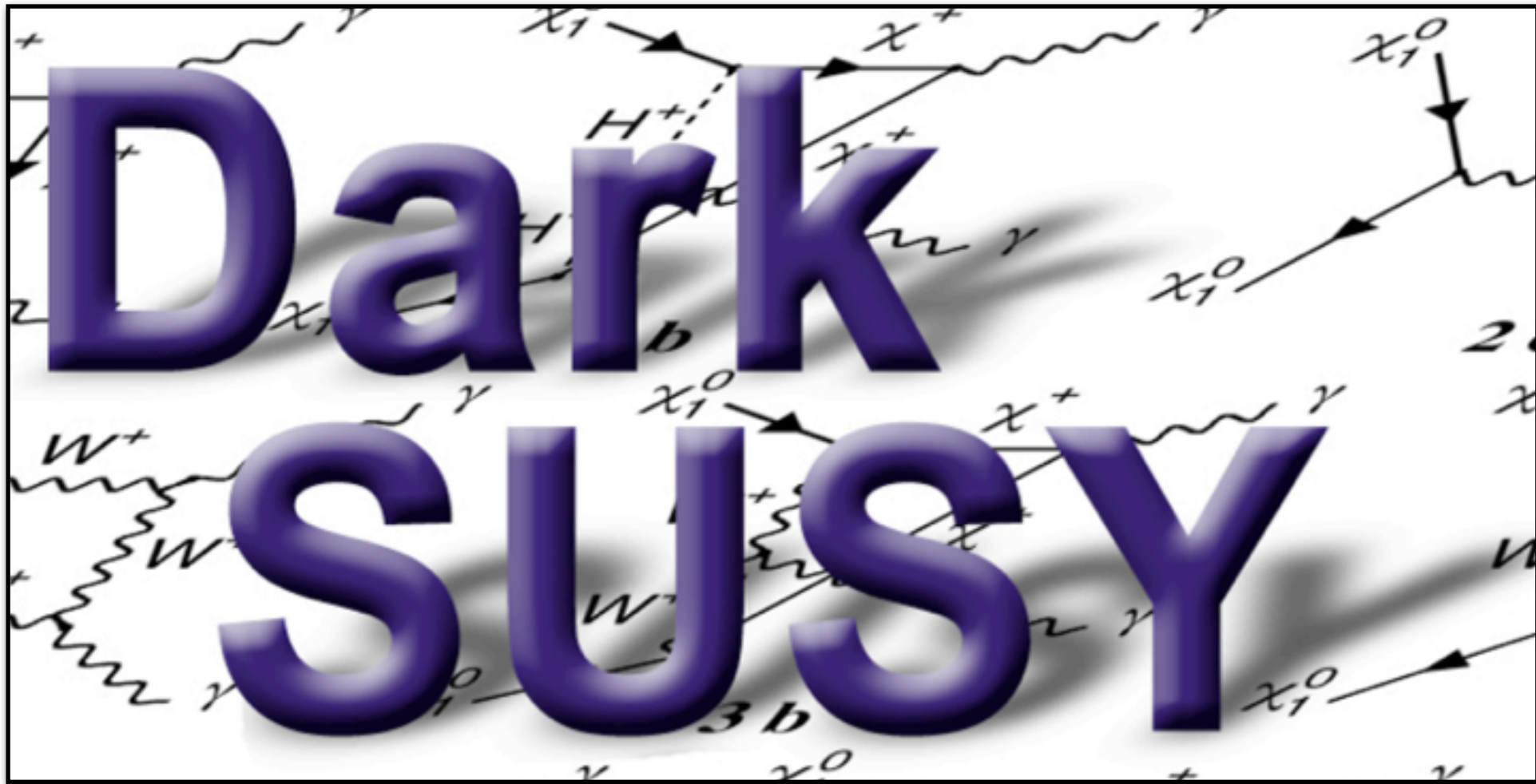


# Outline

- Introduction to DarkSUSY
- Layout of the code
- Physics set-up: SUSY models
- Relic density
- Indirect detection rates
- Direct detection rates
- Accelerator constraints

★ Exercises

# Dark SUSY

The background of the title slide features a complex network of Feynman diagrams. These diagrams illustrate various particle interactions, including the production and decay of supersymmetric particles. Labels such as  $\chi_1^+$ ,  $\chi_1^0$ ,  $\gamma$ ,  $W^+$ ,  $W^-$ ,  $H^+$ ,  $b$ , and  $3b$  are visible, representing different types of particles and interaction vertices. The diagrams are drawn with solid lines for fermions, wavy lines for gauge bosons, and dashed lines for Higgs bosons.

authors: P. Gondolo, J. Edsjö, P. Ullio, L. Bergström,  
M. Schelke, E.A. Baltz, T. Bringmann and G. Duda

**SUSY models**

**Direct detection  
rates**

# Dark USY

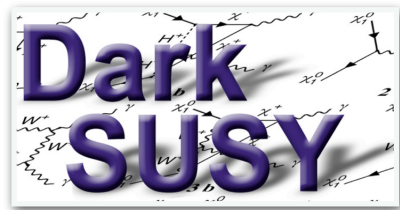
A Feynman diagram is visible in the background, showing various particles and their interactions. Labels include  $\chi_1$ ,  $\chi^+$ ,  $H^+$ ,  $\chi^0$ ,  $\gamma$ ,  $b$ ,  $W^+$ , and  $\chi_1^0$ . The diagram illustrates a complex particle interaction involving supersymmetric particles and Standard Model particles.

**Indirect detection  
rates**

**Accurate relic  
abundance  
calculation**

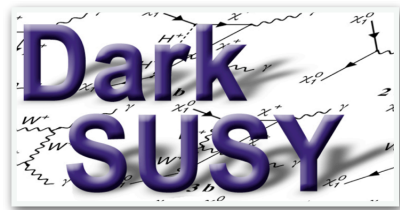
**Accelerator bounds**

authors: P. Gondolo, J. Edsjö, P. Ullio, L. Bergström,  
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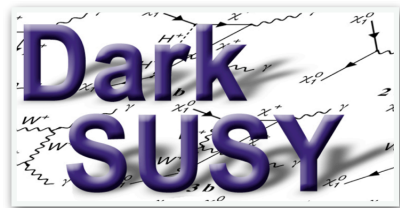
# Philosophy & Contents

- Modular structure
- Library of subroutines and functions
- Fortran compilers: gfortran, ifort
- Flexible
- Fast and accurate

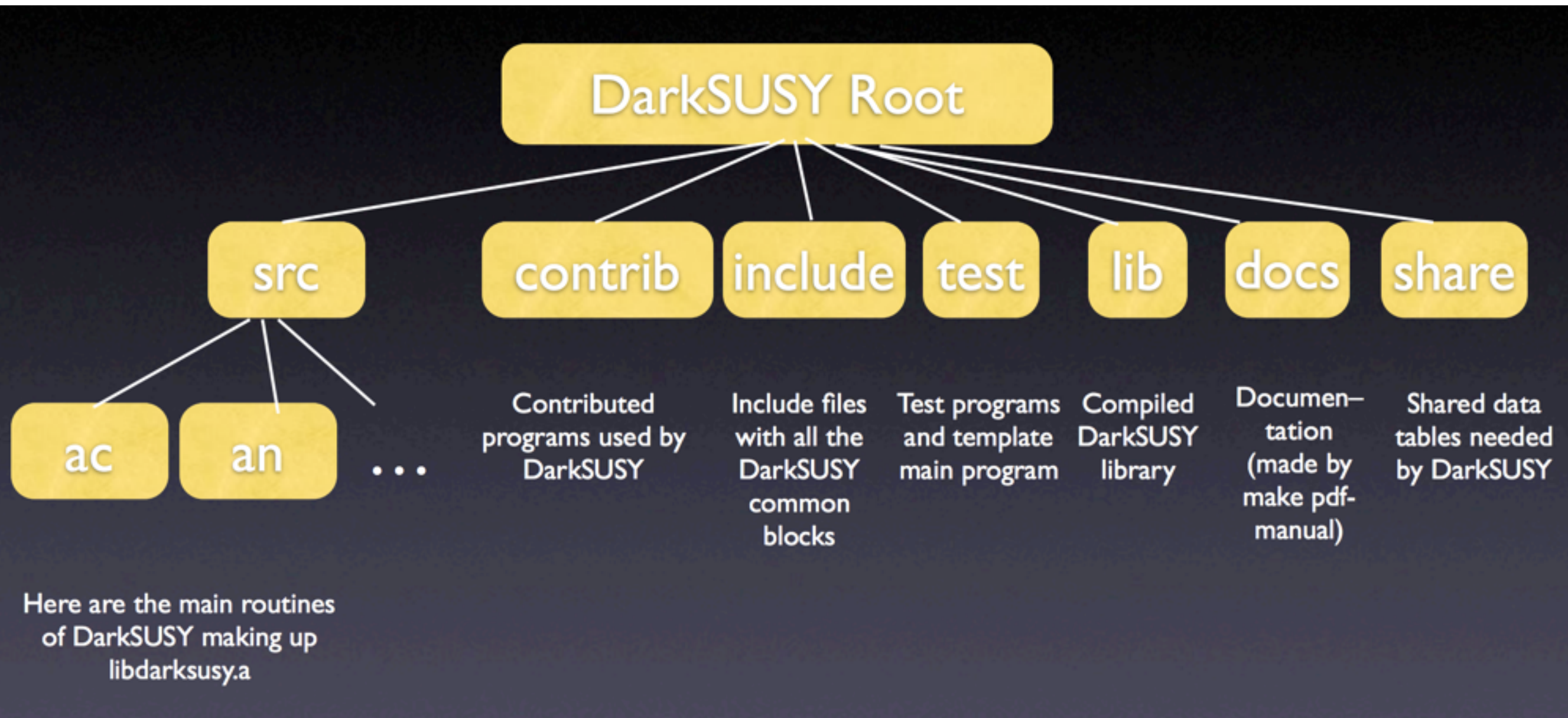


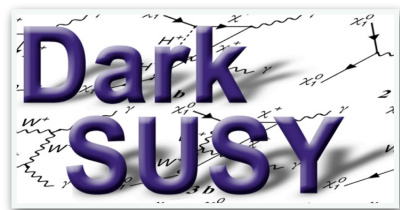
# Philosophy & Contents

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  - Flexible
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- 
- ✓ Tool for DM searches: computation of rates for indirect, direct and accelerator searches, relic abundance.
  - ✓ MSSM models: constraints and scans on generic MSSM, mSUGRA, etc.
  - ✓ Advanced indirect detection computations: signals in neutrino telescopes, gamma-ray signals, cosmic-ray positrons, antiprotons and antideuteron.

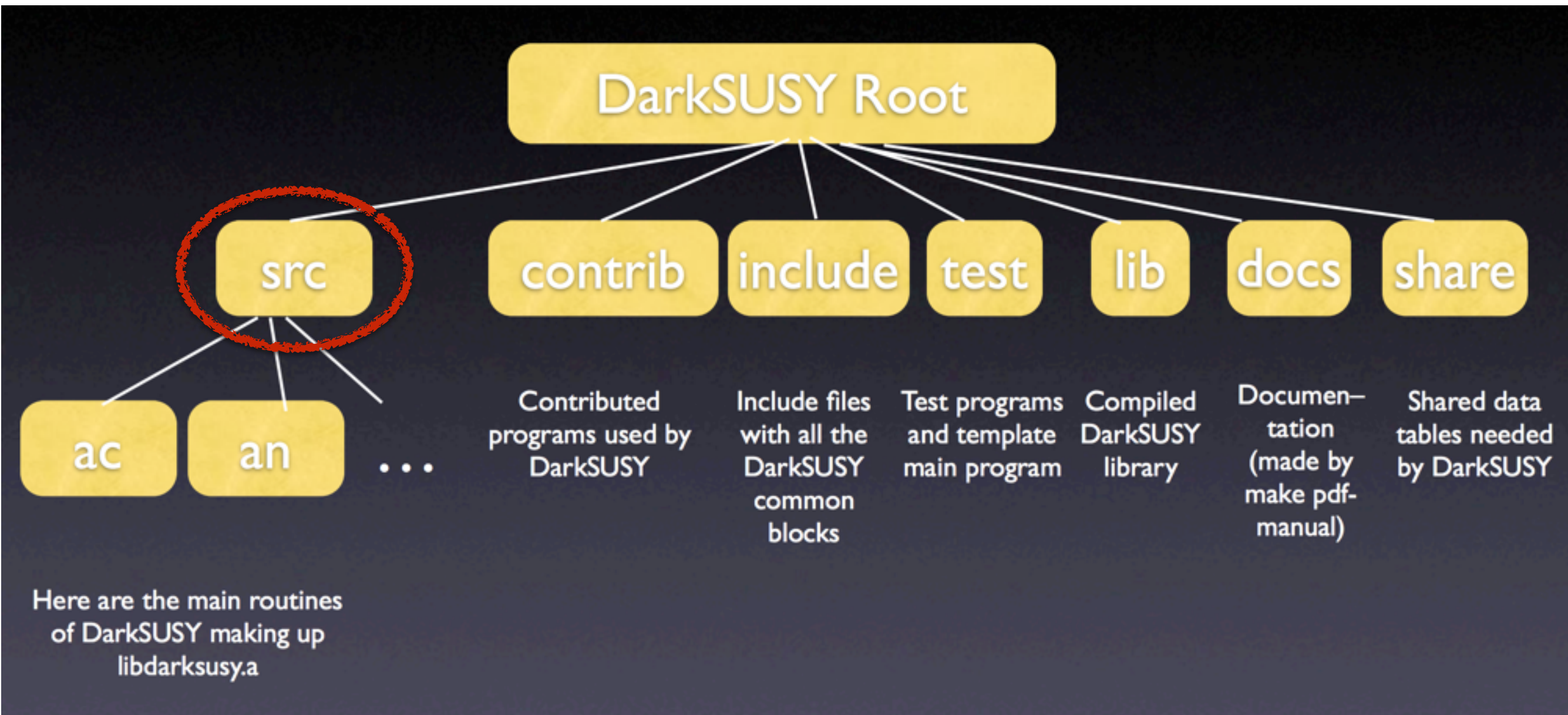


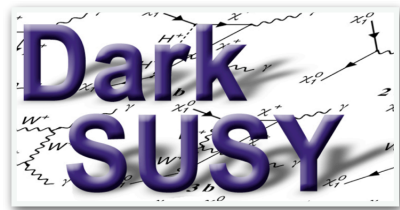
# Layout of DarkSUSY





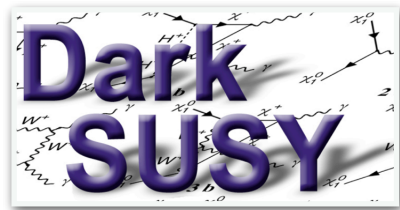
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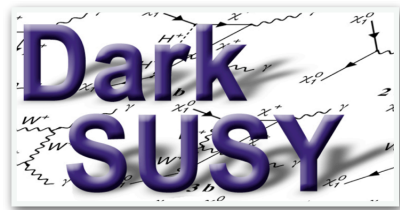
# Routines in src/ (1)

- **ac**: accelerator constraints
- **an**: annihilation cross sections for neutralino and chargino coannihilations
- **an1l**: 1-loop annihilation cross sections ( $\gamma \gamma$  and  $Z \gamma$ )
- **as**: annihilation cross sections for sfermions coannihilations
- **anstu**: auxiliary routines for neutralino and chargino coannihilations
  
- **bsg**:  $b \rightarrow s \gamma$  routines
  
- **db**: anti-deuterium
- **dd**: direct detection
- **docs**: general documentation, to be complemented by the more specific documentation in each subdirectory in src/
  
- **ep**: positron fluxes from the halo
  
- **ge**: general routines (integrators etc)



# Routines in src/ (2)

- **ha**: halo annihilation routines
- **hm**: halo models
- **hr**: rates from halo annihilation
- **ib**: internal bremsstrahlung (photons and positrons)
- **ini**: initialisation routines
- **nt**: rates from neutrino telescopes. Also includes Sun and Earth models for the capture rate calculations
- **pb**: antiproton fluxes from the halo
- **rd**: relic density routines (in general format, knows nothing about SUSY)
- **rn**: interface to relic density routines for SUSY neutralinos, these give the relic density of neutralinos
- **rge**: interface to RGE code isasugra for mSUGRA models

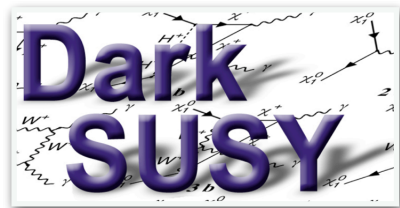


# Routines in src/ (3)

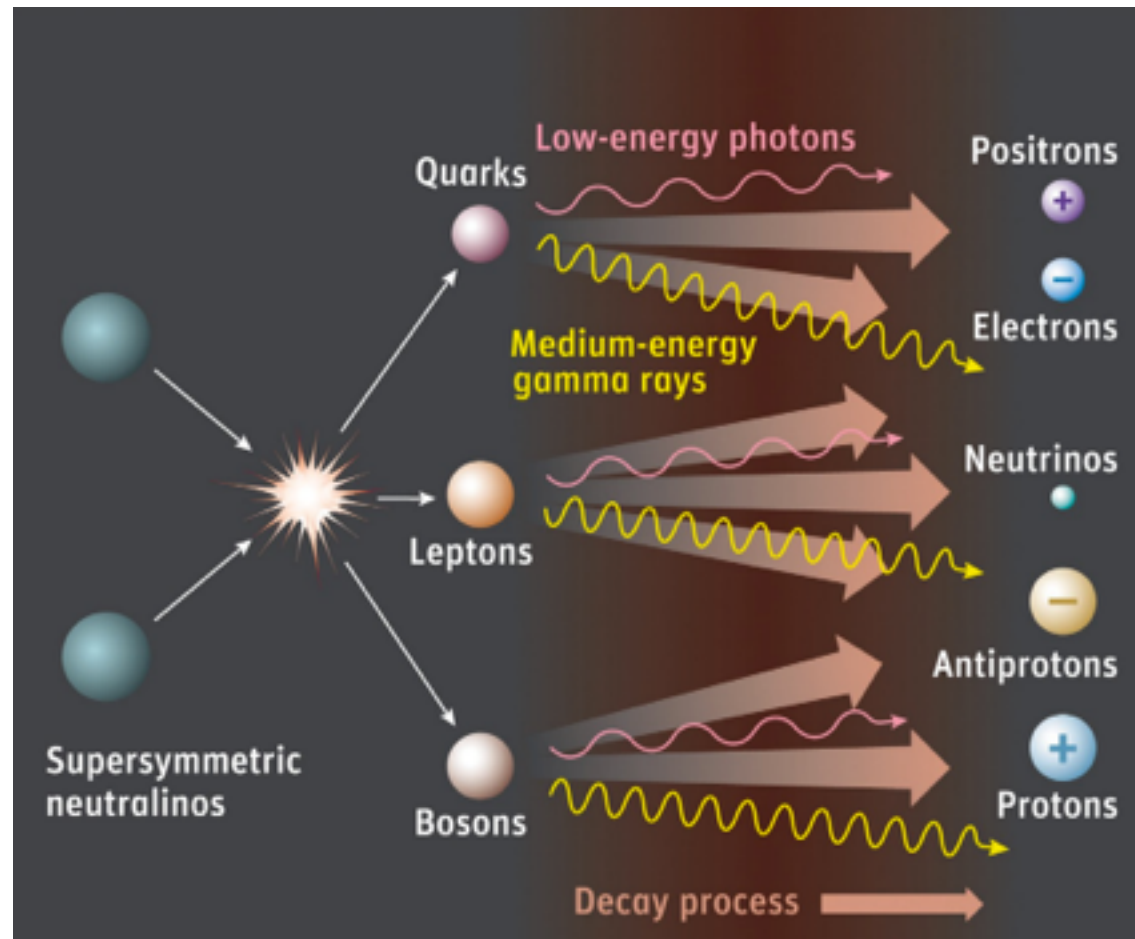
- **su**: general SUSY routines, mass spectra, vertices etc
- **wa**: WIMP annihilation routines to calculate yields of neutrinos, neutrino-induced leptons (e.g. muons) and hadronic showers from WIMP annihilation in the Earth/Sun. Note: these routines know nothing about SUSY, the interface to SUSY is done with dswasetup in the nt set of routines
- **xcern**: a few needed routines from CERNLIB
- **xcmlib**: a few needed routines from CMLIB
- **xfeynhiggs**: interface routines to FeynHiggs
- **xgalprop**: interface routines to galprop
- **xhdecay**: interface routines to HDecay

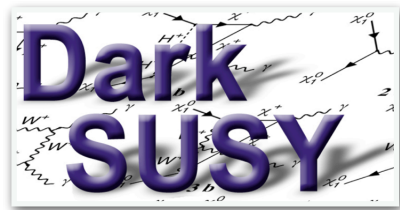


# Physics set-up

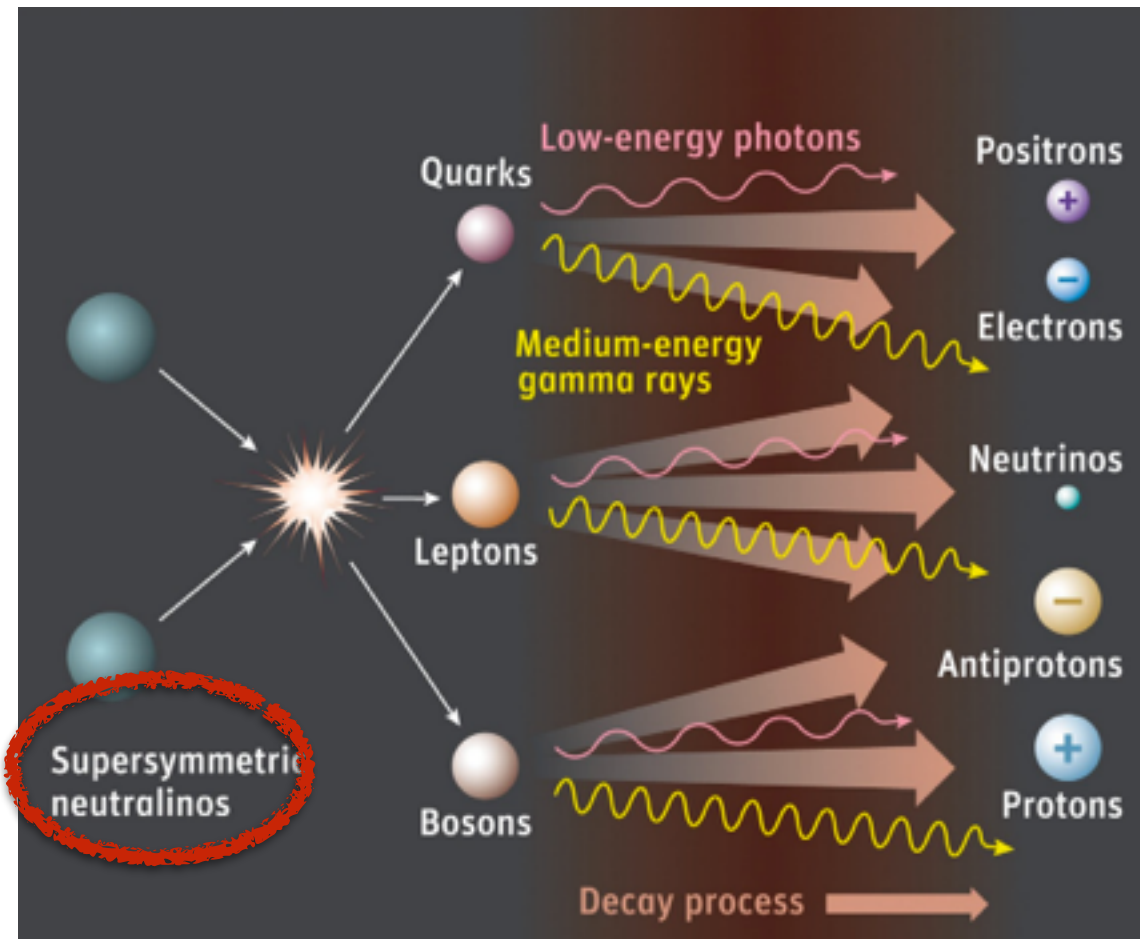


# Physic set-up: SUSY models





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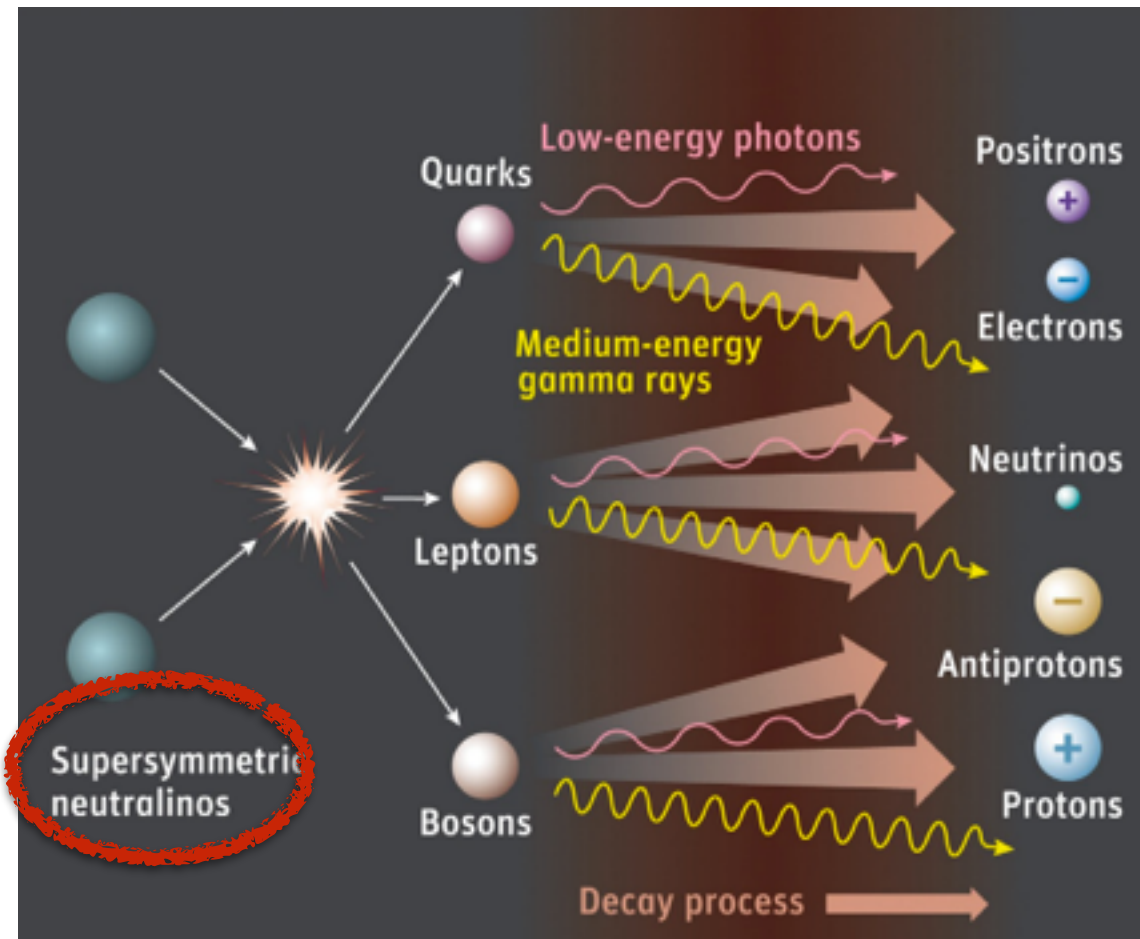


DarkSUSY has been set-up for the analysis of generic SUSY models with a large number of free parameters.

Advanced and accurate calculations in the full MSSM framework.

$$\frac{dN_X}{dE} \quad X = e^+, \bar{p}, \gamma, \nu, \dots$$

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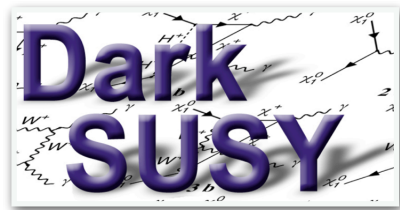
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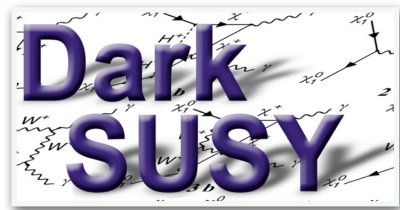
**Example:** differential energy gamma-ray flux

$$\frac{d\Phi_\gamma}{dE_\gamma}(E_\gamma, \phi, \theta, \Delta\Omega) = \frac{\langle\sigma v\rangle}{2m_\chi^2} \cdot \sum_i B_i \frac{dN_\gamma^i}{dE_\gamma} \frac{1}{4\pi} \int_0^{\Delta\Omega} d\Omega \int_{\text{l.o.s}} \rho^2(s(R, \phi, \theta)) ds$$



# Physic set-up: SUSY models

- Input parameters at EW scale (MSSM) or at GUT scale (mSUGRA)
- Higgs sector with FeynHiggs
- Higgs decay widths from literature (or from Hdecay, future FeynHiggs)
- mSUGRA interfaces: ISASUGRA
- SUSY Les Houches Accord 2 implemented (slha files)



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## Theoretical SUSY framework:

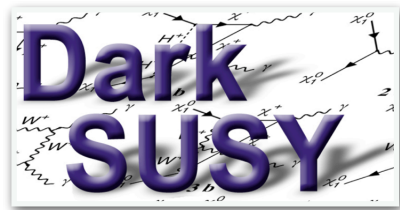
We work in the framework of the minimal  $N = 1$  supersymmetric extension of the standard model defined by, besides the particle content and gauge couplings required by supersymmetry, the superpotential

$$W = \epsilon_{ij} \left( -\hat{\mathbf{e}}_R^* \mathbf{Y}_E \hat{\mathbf{l}}_L^i \hat{H}_1^j - \hat{\mathbf{d}}_R^* \mathbf{Y}_D \hat{\mathbf{q}}_L^i \hat{H}_1^j + \hat{\mathbf{u}}_R^* \mathbf{Y}_U \hat{\mathbf{q}}_L^i \hat{H}_2^j - \mu \hat{H}_1^i \hat{H}_2^j \right) \quad (2)$$

and the soft supersymmetry-breaking potential

$$\begin{aligned} V_{\text{soft}} = & \epsilon_{ij} \left( -\tilde{\mathbf{e}}_R^* \mathbf{A}_E \mathbf{Y}_E \tilde{\mathbf{l}}_L^i H_1^j - \tilde{\mathbf{d}}_R^* \mathbf{A}_D \mathbf{Y}_D \tilde{\mathbf{q}}_L^i H_1^j + \tilde{\mathbf{u}}_R^* \mathbf{A}_U \mathbf{Y}_U \tilde{\mathbf{q}}_L^i H_2^j - B \mu H_1^i H_2^j + \text{h.c.} \right) \\ & + H_1^{i*} m_1^2 H_1^i + H_2^{i*} m_2^2 H_2^i \\ & + \tilde{\mathbf{q}}_L^{i*} \mathbf{M}_Q^2 \tilde{\mathbf{q}}_L^i + \tilde{\mathbf{l}}_L^{i*} \mathbf{M}_L^2 \tilde{\mathbf{l}}_L^i + \tilde{\mathbf{u}}_R^* \mathbf{M}_U^2 \tilde{\mathbf{u}}_R + \tilde{\mathbf{d}}_R^* \mathbf{M}_D^2 \tilde{\mathbf{d}}_R + \tilde{\mathbf{e}}_R^* \mathbf{M}_E^2 \tilde{\mathbf{e}}_R \\ & + \frac{1}{2} M_1 \tilde{B} \tilde{B} + \frac{1}{2} M_2 \left( \tilde{W}^3 \tilde{W}^3 + 2 \tilde{W}^+ \tilde{W}^- \right) + \frac{1}{2} M_3 \tilde{g} \tilde{g}. \end{aligned} \quad (3)$$

Here  $i$  and  $j$  are  $SU(2)$  indices ( $\epsilon_{12} = +1$ ),  $\mathbf{Y}$ 's,  $\mathbf{A}$ 's and  $\mathbf{M}$ 's are  $3 \times 3$  matrices in generation space, and the other boldface letter are vectors in generation space.



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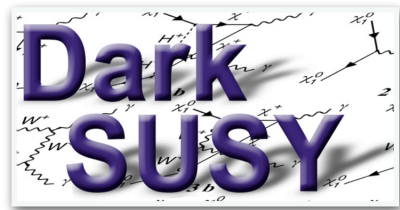
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$$\tilde{\chi}_i^0 = N_{i1} \tilde{B} + N_{i2} \tilde{W}^3 + N_{i3} \tilde{H}_1^0 + N_{i4} \tilde{H}_2^0.$$

$$\mathcal{M}_{\tilde{\chi}_{1,2,3,4}^0} = \begin{pmatrix} M_1 & 0 & -m_Z s_W c_\beta & +m_Z s_W s_\beta \\ 0 & M_2 & +m_Z c_W c_\beta & -m_Z c_W s_\beta \\ -m_Z s_W c_\beta & +m_Z c_W c_\beta & \delta_{33} & -\mu \\ +m_Z s_W s_\beta & -m_Z c_W s_\beta & -\mu & \delta_{44} \end{pmatrix},$$



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and the soft supersymmetry-breaking potential

$$V_{\text{soft}} = \epsilon_{ij} \left( -\tilde{\mathbf{e}}_R^* \mathbf{A}_E \mathbf{Y}_E \tilde{\mathbf{l}}_L^i H_1^j - \tilde{\mathbf{d}}_R^* \mathbf{A}_D \mathbf{Y}_D \tilde{\mathbf{q}}_L^i H_1^j + \tilde{\mathbf{u}}_R^* \mathbf{A}_U \mathbf{Y}_U \tilde{\mathbf{q}}_L^i H_2^j \right) \\ + H_1^{i*} m_1^2 H_1^i + H_2^{i*} m_2^2 H_2^i \\ + \tilde{\mathbf{q}}_L^{i*} \mathbf{M}_Q^2 \tilde{\mathbf{q}}_L^i + \tilde{\mathbf{l}}_L^{i*} \mathbf{M}_L^2 \tilde{\mathbf{l}}_L^i + \tilde{\mathbf{u}}_R^{i*} \mathbf{M}_U^2 \tilde{\mathbf{u}}_R^i + \tilde{\mathbf{d}}_R^{i*} \mathbf{M}_D^2 \tilde{\mathbf{d}}_R^i + \tilde{\mathbf{e}}_R^{i*} \mathbf{M}_E^2 \tilde{\mathbf{e}}_R^i \\ + \frac{1}{2} M_1 \tilde{B} \tilde{B} + \frac{1}{2} M_2 (\tilde{W}^3 \tilde{W}^3 + 2 \tilde{W}^+ \tilde{W}^-) + \frac{1}{2} M_3 \tilde{g} \tilde{g}.$$

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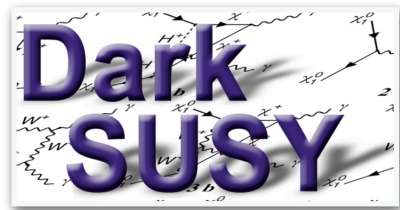
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$$\mathcal{M}_{\tilde{\chi}^\pm} = \begin{pmatrix} M_2 & \sqrt{2} m_W \sin \beta \\ \sqrt{2} m_W \cos \beta & \mu \end{pmatrix},$$

$$\tilde{\chi}_i^- = U_{i1} \tilde{W}^- + U_{i2} \tilde{H}_1^-,$$

$$\tilde{\chi}_i^+ = V_{i1} \tilde{W}^+ + V_{i2} \tilde{H}_1^+.$$



# Physic set-up: SUSY models

Low-energy phenomenological MSSM (MSSM-7)

$$\mathbf{A}_U = \text{diag}(0, 0, A_t)$$

$$\mathbf{A}_D = \text{diag}(0, 0, A_b)$$

$$\mathbf{A}_E = 0$$

$$\mathbf{M}_Q = \mathbf{M}_U = \mathbf{M}_D = \mathbf{M}_E = \mathbf{M}_L = m_0 \mathbf{1}.$$

$$M_1 = \frac{5}{3} \tan^2 \theta_w M_2 \simeq 0.5 M_2,$$

$$M_2 = \frac{\alpha_{ew}}{\sin^2 \theta_w \alpha_s} M_3 \simeq 0.3 M_3.$$

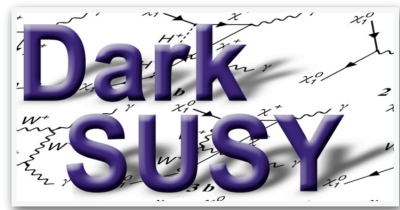
Note, however, that this specific choice is not needed by DarkSUSY, more general models are possible.

`dsgive_model`: sets an MSSM-7 model

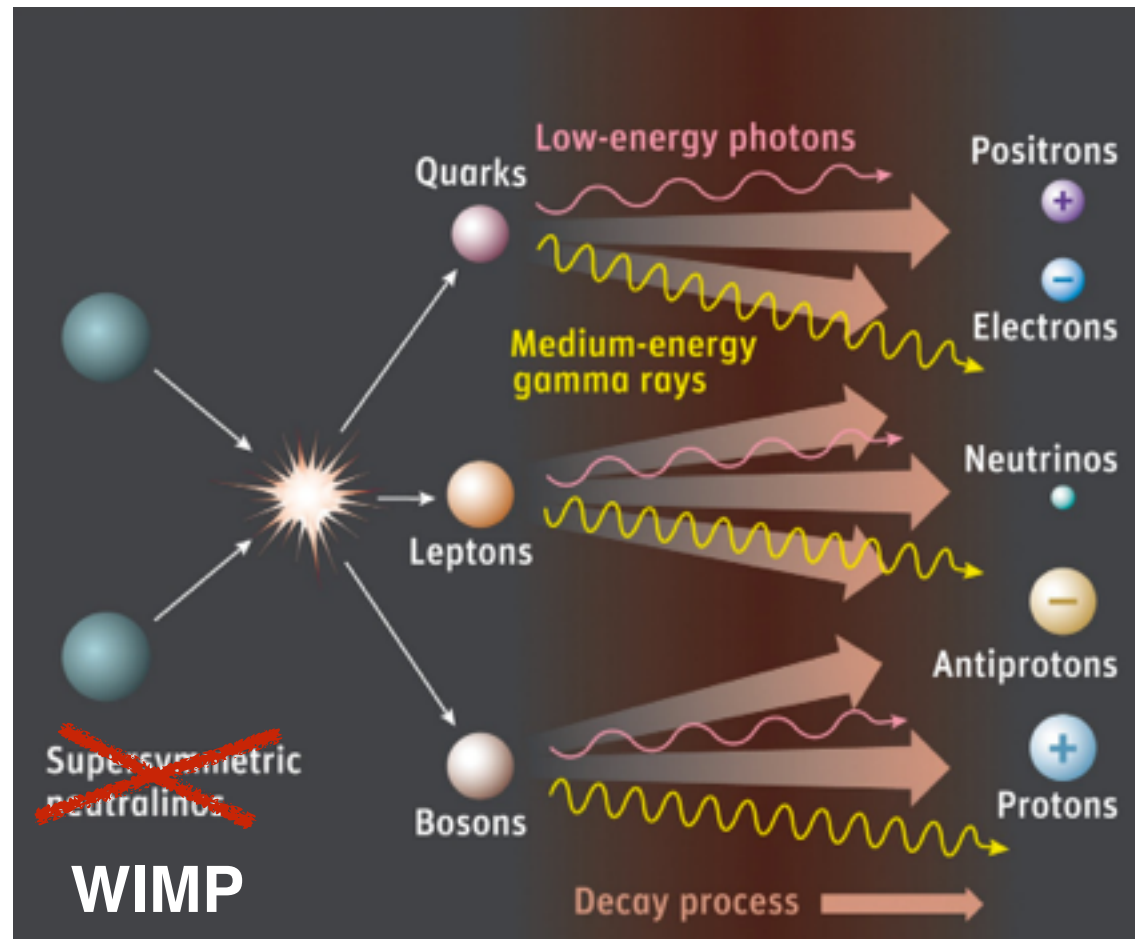
`dsgive_model13`: sets an MSSM-13 model

- One can also set these low-energy parameters with an external program, like ISASUGRA
- For consistency, in that case we use the spectrum calculation by that external program and just transfer these values to DarkSUSY

`dsgive_model_isasugra`: sets an m-SUGRA model

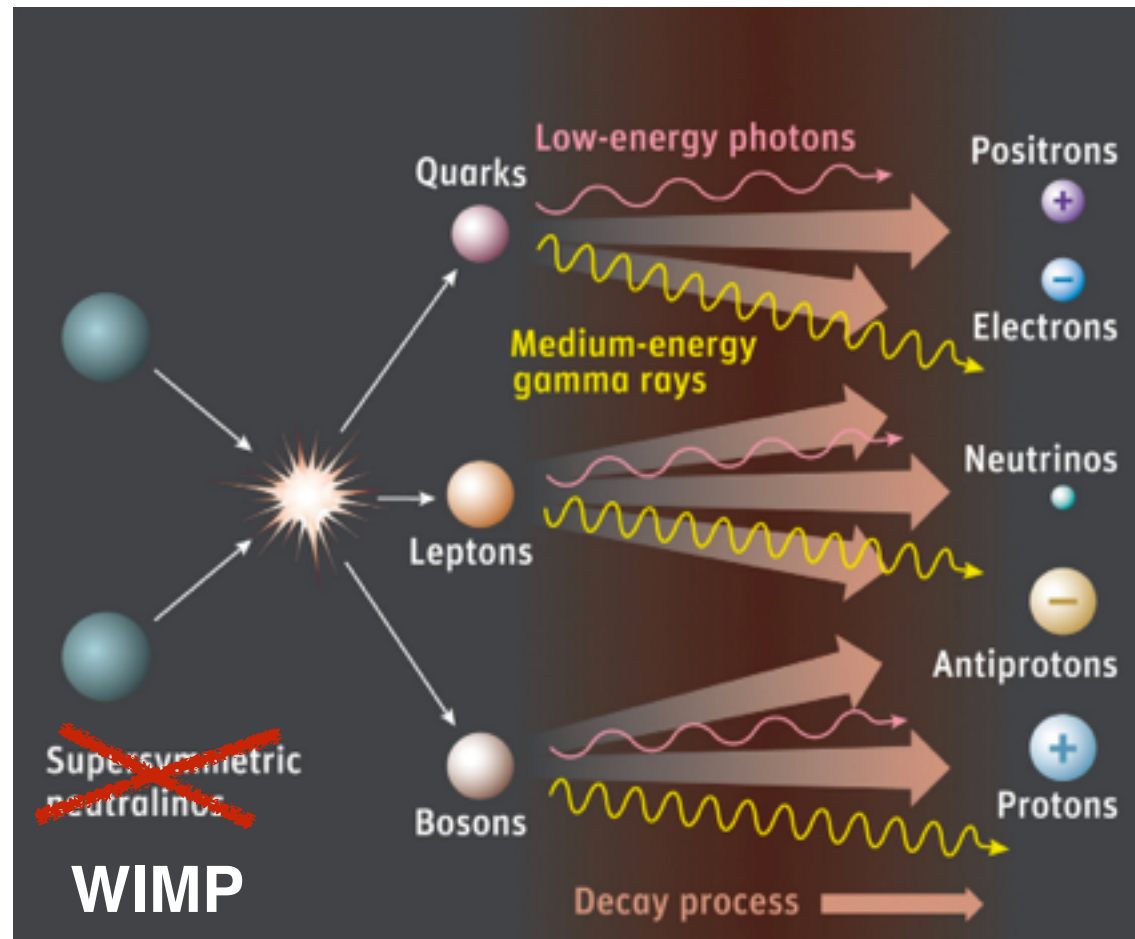


# Physic set-up: simplified models



DarkSUSY routines may be used to compute spectra and rates in the case of 100% branching ratio into a fixed final state.

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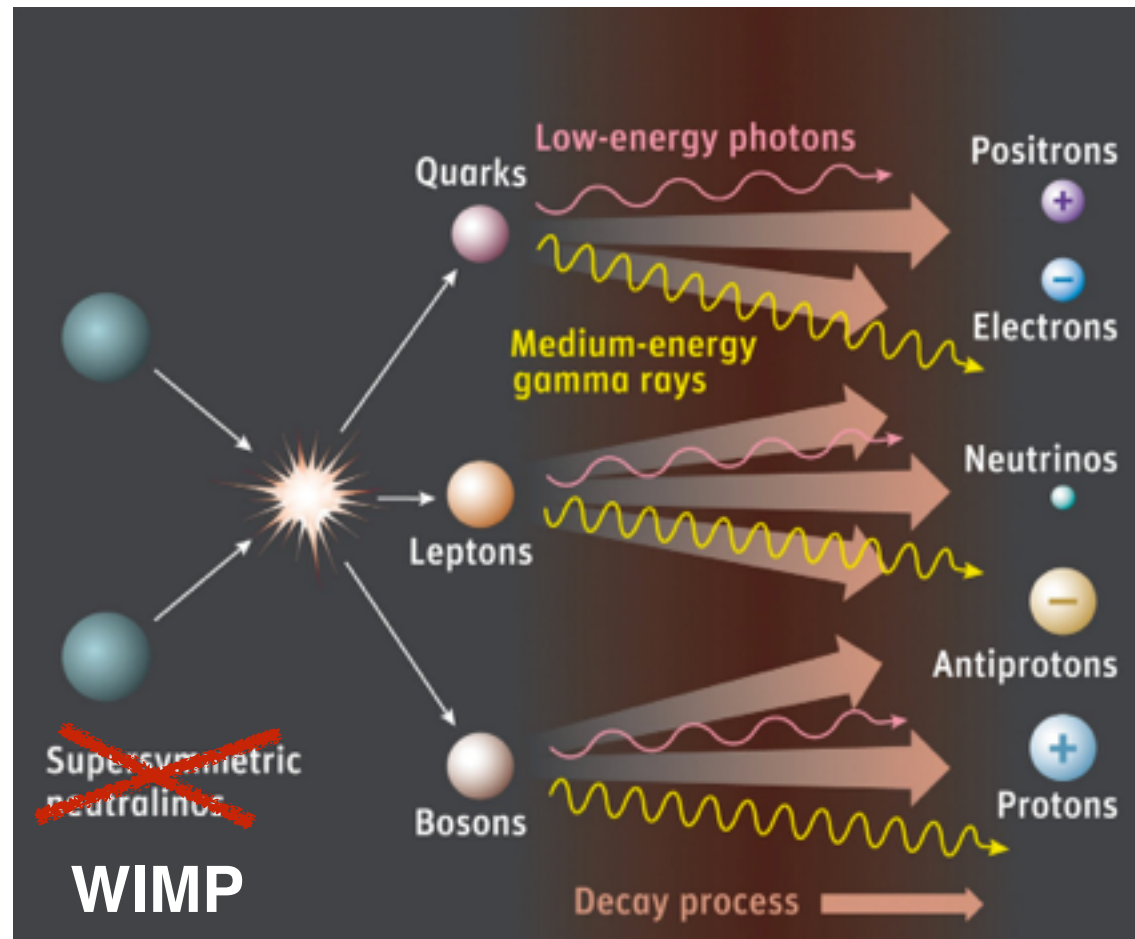


DarkSUSY routines may be used to compute spectra and rates in the case of 100% branching ratio into a fixed final state.

**Example:** differential energy gamma-ray flux

$$\frac{d\Phi_{\gamma}}{dE_{\gamma}}(E_{\gamma}, \phi, \theta, \Delta\Omega) = \frac{\langle\sigma v\rangle}{2m_{\chi}^2} \cdot \sum_i B_i \frac{dN_{\gamma}^i}{dE_{\gamma}} \frac{1}{4\pi} \int_0^{\Delta\Omega} d\Omega \int_{\text{l.o.s}} \rho^2(s(R, \phi, \theta)) ds$$

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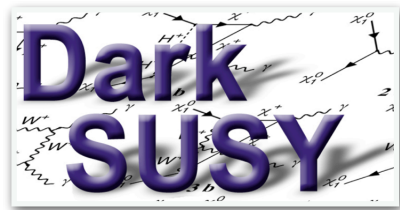
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$B_i \equiv 1$



# Relic Density



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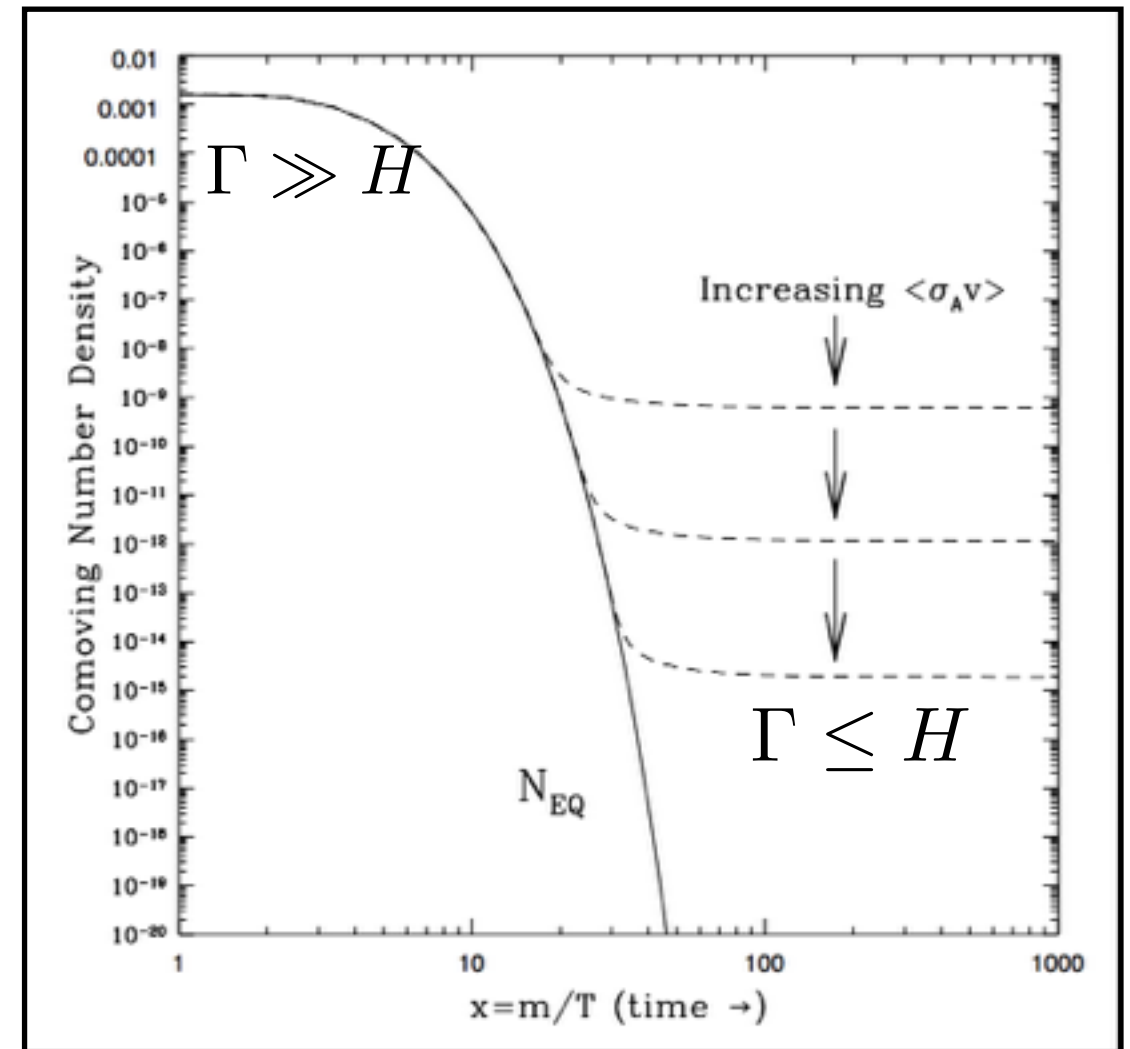
Freeze out of a thermal relic in the early Universe

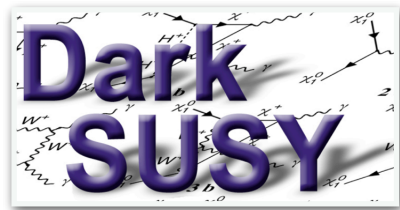
$$\Gamma = \langle \sigma_{\text{ann}} v \rangle n_\chi$$

$$H(T) = 1.66 g_*^{1/2} \frac{T^2}{M_{\text{Pl}}}$$

$$\Gamma \simeq H \rightarrow T_f \simeq \frac{m_\chi}{20}$$

$$\Omega_\chi h^2 \simeq \frac{3 \times 10^{-27} \text{cm}^3 \text{s}^{-1}}{\langle \sigma_{\text{ann}} v \rangle}$$





# Relic Density

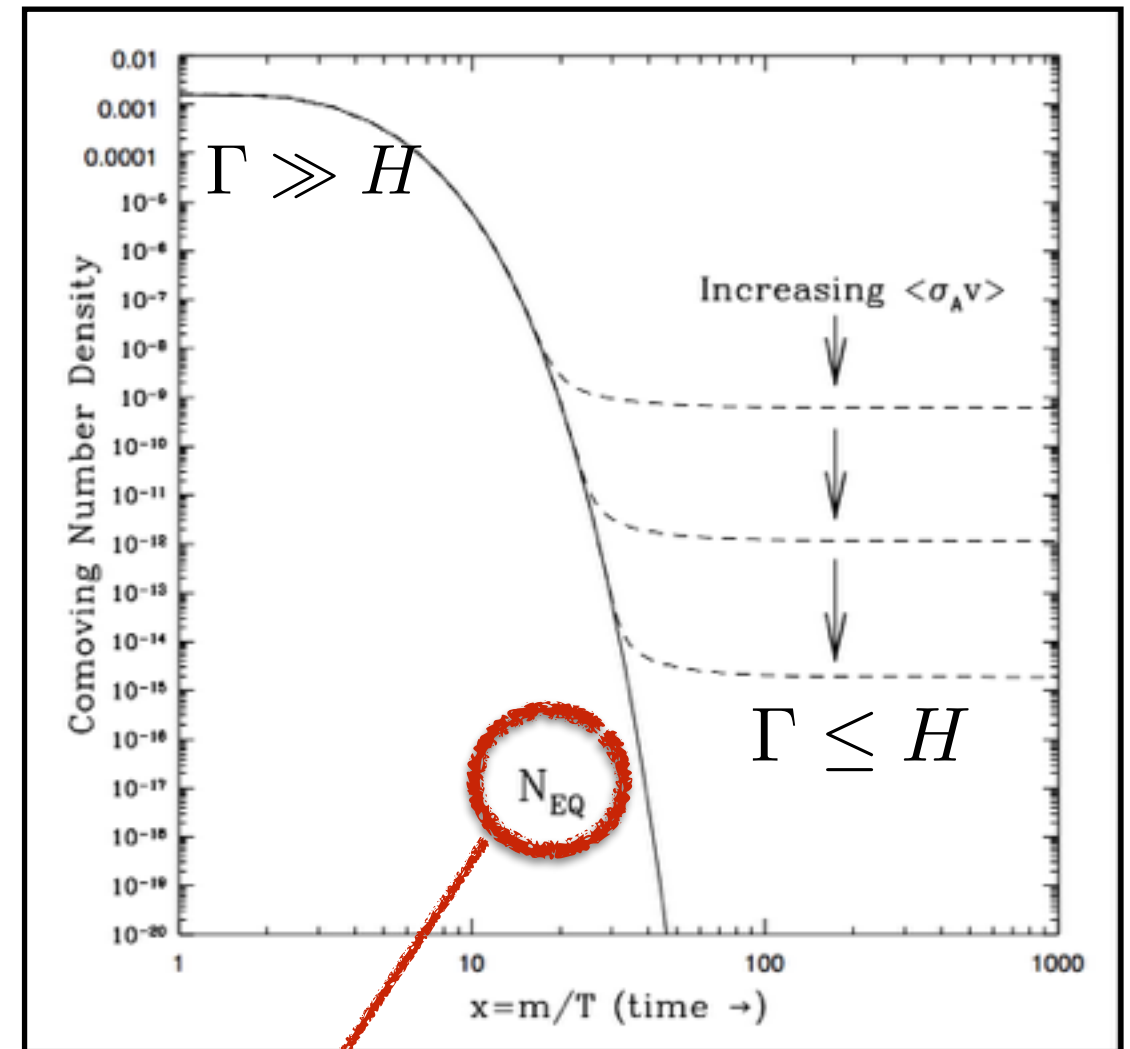
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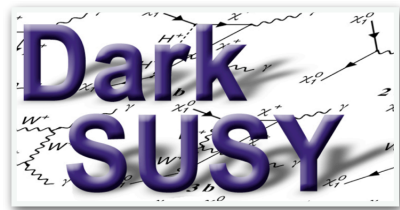
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$$n_\chi^{\text{eq}} = g_\chi \left( \frac{m_\chi T}{2\pi} \right)^{3/2} e^{-m_\chi/T}$$



# Relic Density

Freeze out of a thermal relic in the early Universe

$$\Gamma = \langle \sigma_{\text{ann}} v \rangle n_\chi$$

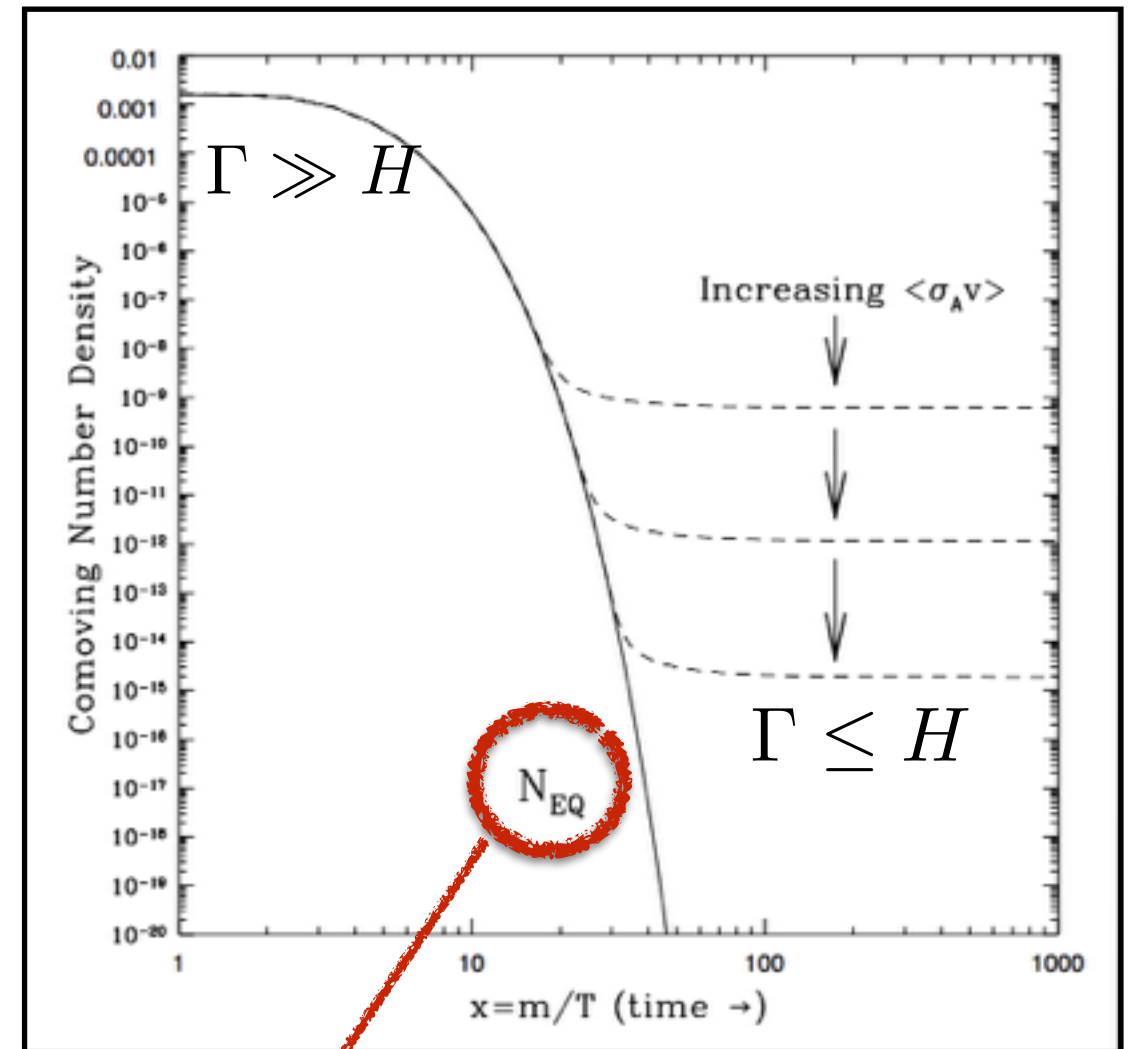
$$H(T) = 1.66 g_*^{1/2} \frac{T^2}{M_{\text{Pl}}}$$

$$\Gamma \simeq H \rightarrow T_f \simeq \frac{m_\chi}{20}$$

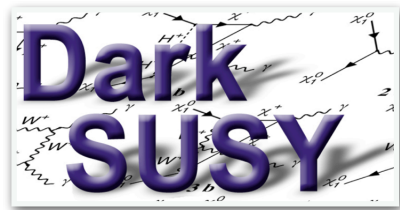
$$\Omega_\chi h^2 \simeq \frac{3 \times 10^{-27} \text{cm}^3 \text{s}^{-1}}{\langle \sigma_{\text{ann}} v \rangle}$$

Fixed by observations!

Computed by DarkSUSY!



$$n_\chi^{\text{eq}} = g_\chi \left( \frac{m_\chi T}{2\pi} \right)^{3/2} e^{-m_\chi/T}$$



# Relic Density

## How does DarkSUSY compute the relic density?

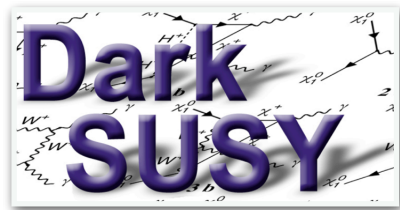
- It solves the Boltzmann equation,

$$\frac{dn}{dt} = -3Hn - \langle \sigma_{\text{ann}} v \rangle (n^2 - n_{\text{eq}}^2)$$

properly computing the thermal average  $\langle \cdot \rangle$  and including the full annihilation cross section (including all final states, resonances and thresholds).

- It includes all so-called coannihilations between all neutralinos, charginos and sfermions.

**Remark:** Only annihilation/coannihilation  
No scattering and decay  
Sum over **all** SUSY particles



# Relic Density

## DarkSUSY routines for relic density:

- The main routine for SUSY neutralinos is **dsrdomega** that calculates the relic density of neutralinos
- However, the relic density routines are more general than that and can be used for any WIMP with a call to **dsrdens**.

Call **dsrdens(wrate, npart, mgev, dof, nrs, rm, rw, nt, tm, oh2, tf, ierr, iwar)**

where you have to supply:

**wrate** – invariant effective annihilation rate (function)

**npart** – number of coannihilating particles

**mgev** – mass of these particles

**dof** – internal degrees of freedom of these particles

**nrs** – number of resonances

**rm** – mass of resonances

**rw** – width of resonances

**nt** – number of thresholds

**tm** – equivalent mass of thresholds

The routine then returns:

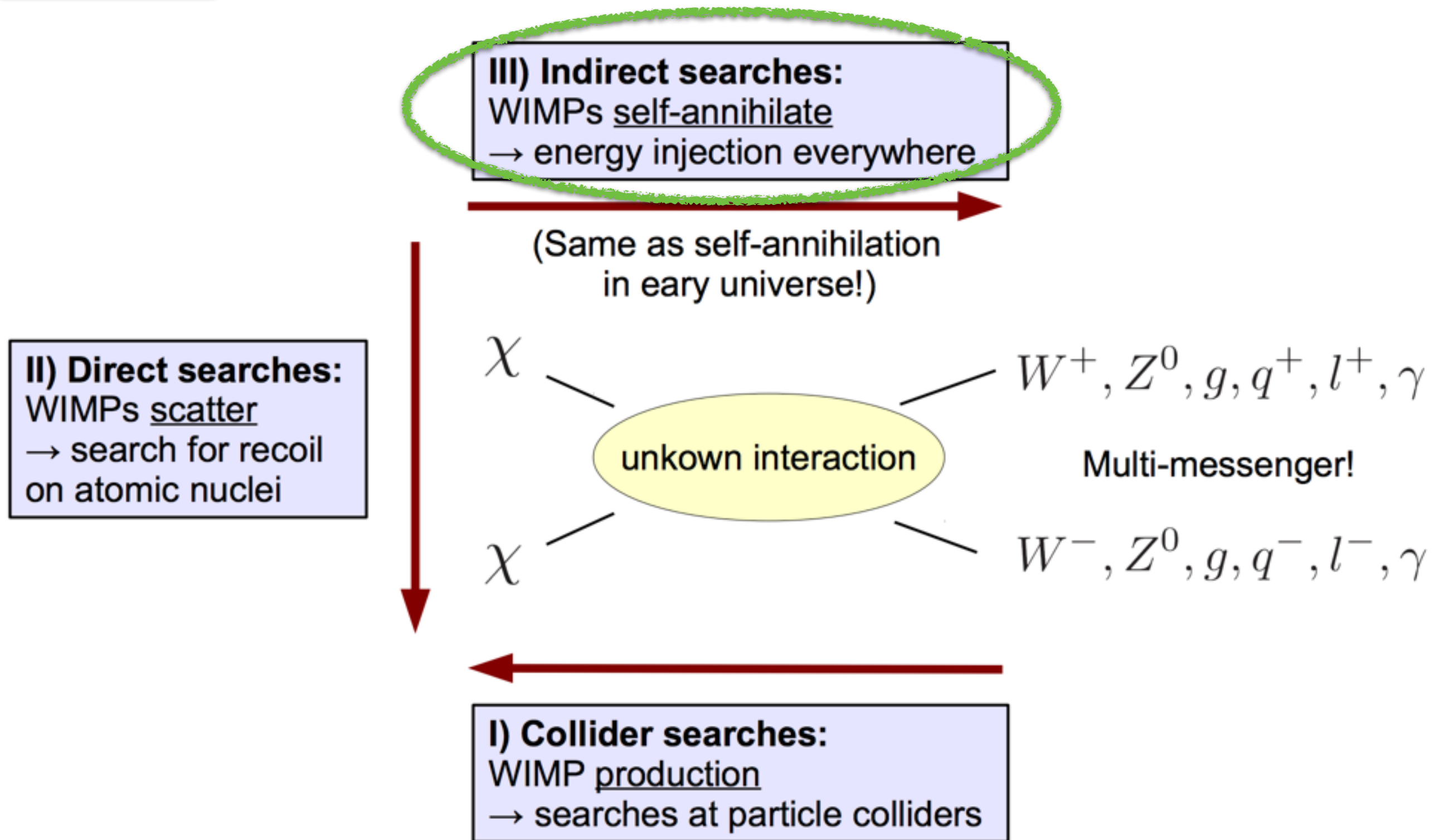
**oh2** –  $\Omega h^2$

**tf** – freeze-out temperature

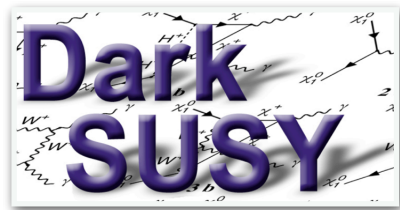


# Detection strategies with DarkSUSY

# WIMP detection strategies



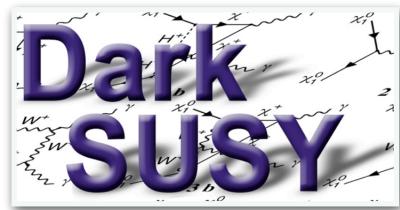
courtesy of C.Weniger



# Indirect DM detection

Indirect detection differential and integrated rates for:

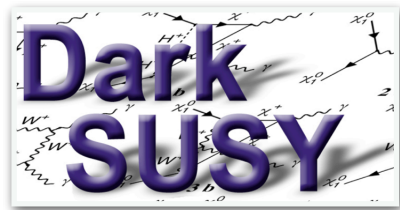
- Gamma rays from the halo
- Antiprotons from the halo
- Antideutrium from the halo
- Positrons from the halo
- Neutrinos from the Sun/Earth



# Indirect DM detection

Indirect detection differential and integrated rates for:

- Gamma rays from the halo
- Antiprotons from the halo
- Antideutrium from the halo
- Positrons from the halo
- Neutrinos from the Sun/Earth

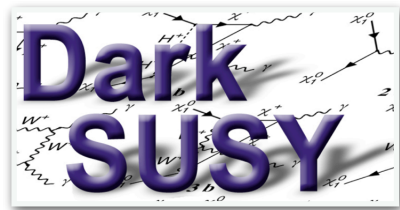


# Indirect DM detection

Indirect detection differential and integrated rates for:

- Gamma rays from the halo

$$\frac{d\Phi_\gamma}{dE_\gamma}(E_\gamma, \phi, \theta, \Delta\Omega) = \frac{\langle\sigma v\rangle}{2m_\chi^2} \cdot \sum_i B_i \frac{dN_\gamma^i}{dE_\gamma} \frac{1}{4\pi} \int_0^{\Delta\Omega} d\Omega \int_{\text{l.o.s}} \rho^2(s(R, \phi, \theta)) ds$$



# Indirect DM detection

Indirect detection differential and integrated rates for:

- Gamma rays from the halo

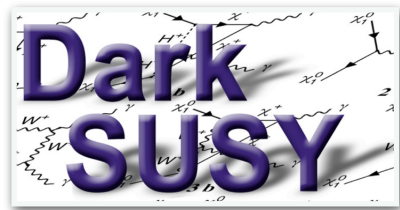
$$\frac{d\Phi_\gamma}{dE_\gamma}(E_\gamma, \phi, \theta, \Delta\Omega) = \underbrace{\frac{\langle\sigma v\rangle}{2m_\chi^2} \cdot \sum_i B_i \frac{dN_\gamma^i}{dE_\gamma}}_{\text{Particle Physics Factor}} \underbrace{\frac{1}{4\pi} \int_0^{\Delta\Omega} d\Omega \int_{\text{l.o.s}} \rho^2(s(R, \phi, \theta)) ds}_{\text{Astrophysical Factor}}$$

Particle Physics Factor  
Spectral information

$\langle\sigma v\rangle$  `src/an/dssigmav.f`  
 $\left. \begin{array}{l} \frac{dN_\gamma^i}{dE_\gamma} \\ B_i \end{array} \right\}$  `src/ha/dshayield.f`  
`src/ha/dshaloyield.f`

Astrophysical Factor  
Angular information

$\rho$  `src/hm/dshmset.f`  
 $J$  factor `src/ha/dshmj.f`  
`src/ha/dshmjave.f`



# Indirect DM detection

Indirect detection differential and integrated rates for:

- Gamma rays from the halo

$$\frac{d\Phi_\gamma}{dE_\gamma}(E_\gamma, \phi, \theta, \Delta\Omega) = \underbrace{\frac{\langle\sigma v\rangle}{2m_\chi^2} \cdot \sum_i B_i \frac{dN_\gamma^i}{dE_\gamma}}_{\text{Particle Physics Factor}} \underbrace{\frac{1}{4\pi} \int_0^{\Delta\Omega} d\Omega \int_{\text{l.o.s}} \rho^2(s(R, \phi, \theta)) ds}_{\text{Astrophysical Factor}}$$

Particle Physics Factor  
Spectral information

Astrophysical Factor  
Angular information

$\langle\sigma v\rangle$  `src/an/dssigmav.f`

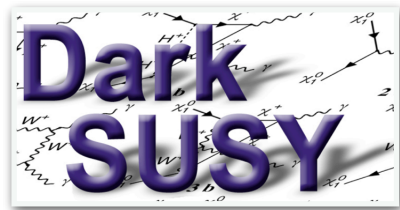
$\rho$  `src/hm/dshmset.f`

$\left. \begin{array}{l} \frac{dN_\gamma^i}{dE_\gamma} \\ B_i \end{array} \right\}$  `src/ha/dshayield.f`  
`src/ha/dshaloyield.f`

$J$  factor `src/ha/dshmj.f`  
`src/ha/dshmjave.f`



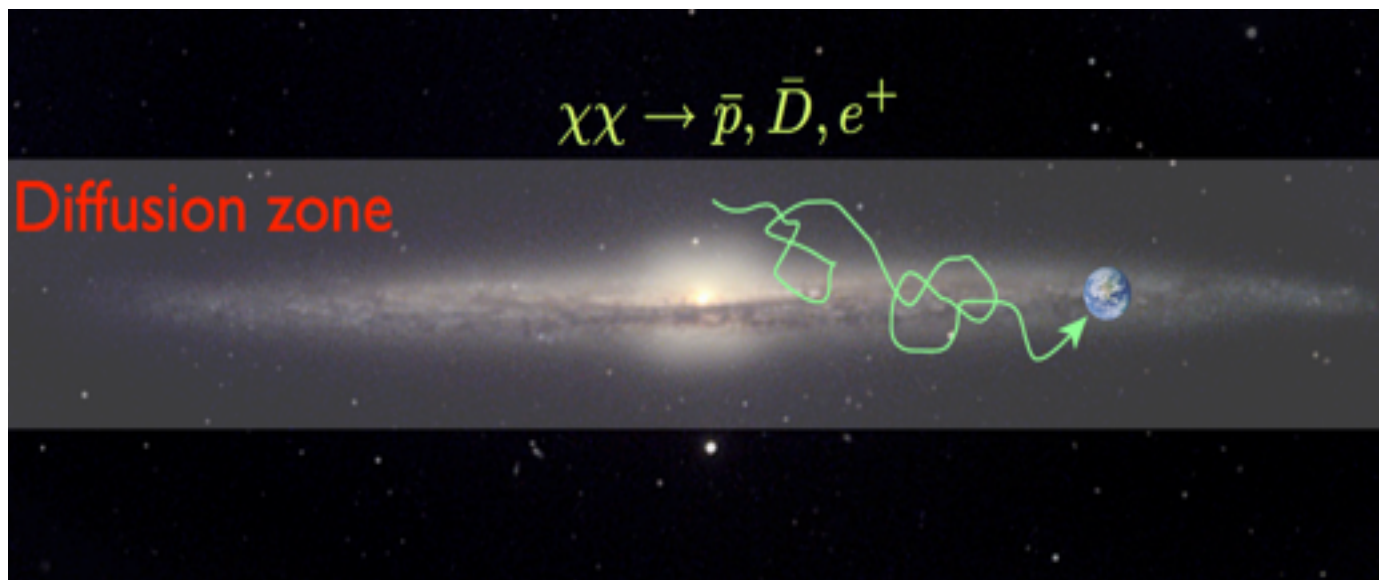
`src/an/dshrgacontdiff.f` or `src/an/dshrgacont.f`  
`src/an/dshrgaline.f`



# Indirect DM detection

Indirect detection differential and integrated rates for:

- Positrons from the halo



Spectrum at the source, then cosmic-ray propagation down to Earth:

- `src/ep/dsepset.f` sets the diffusion model, including energy losses.
- `src/ep/dsepdiff.f` calculates positron fluxes.

Prompt spectrum from DM annihilation:

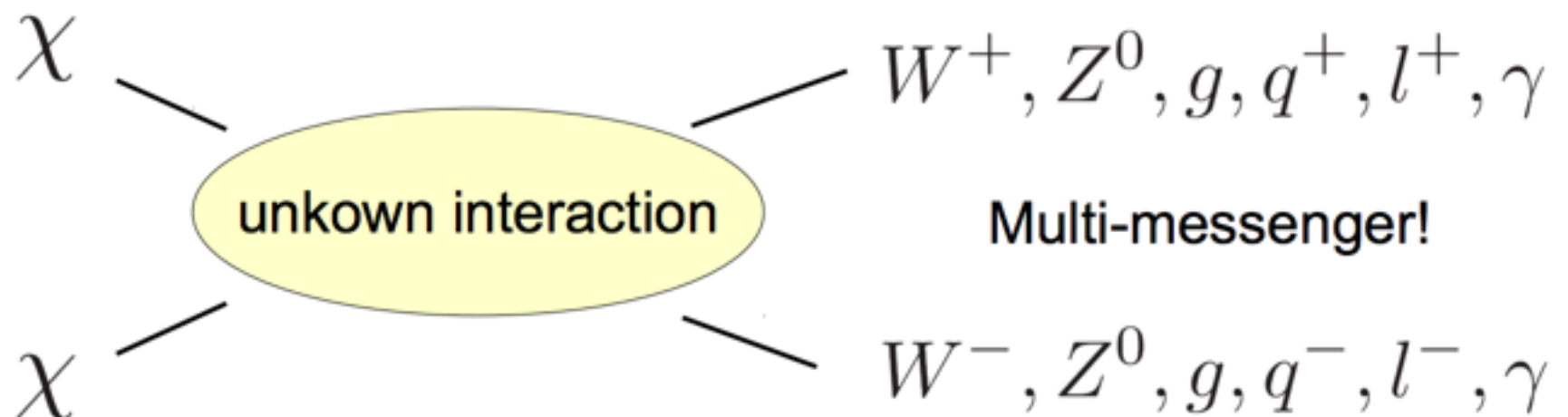
- Enhancement from IB contribution, fully implemented.
- `src/ha/dshaloyield.f` calculates the differential or integrated spectrum.

# WIMP detection strategies

**III) Indirect searches:**  
WIMPs self-annihilate  
→ energy injection everywhere

(Same as self-annihilation  
in early universe!)

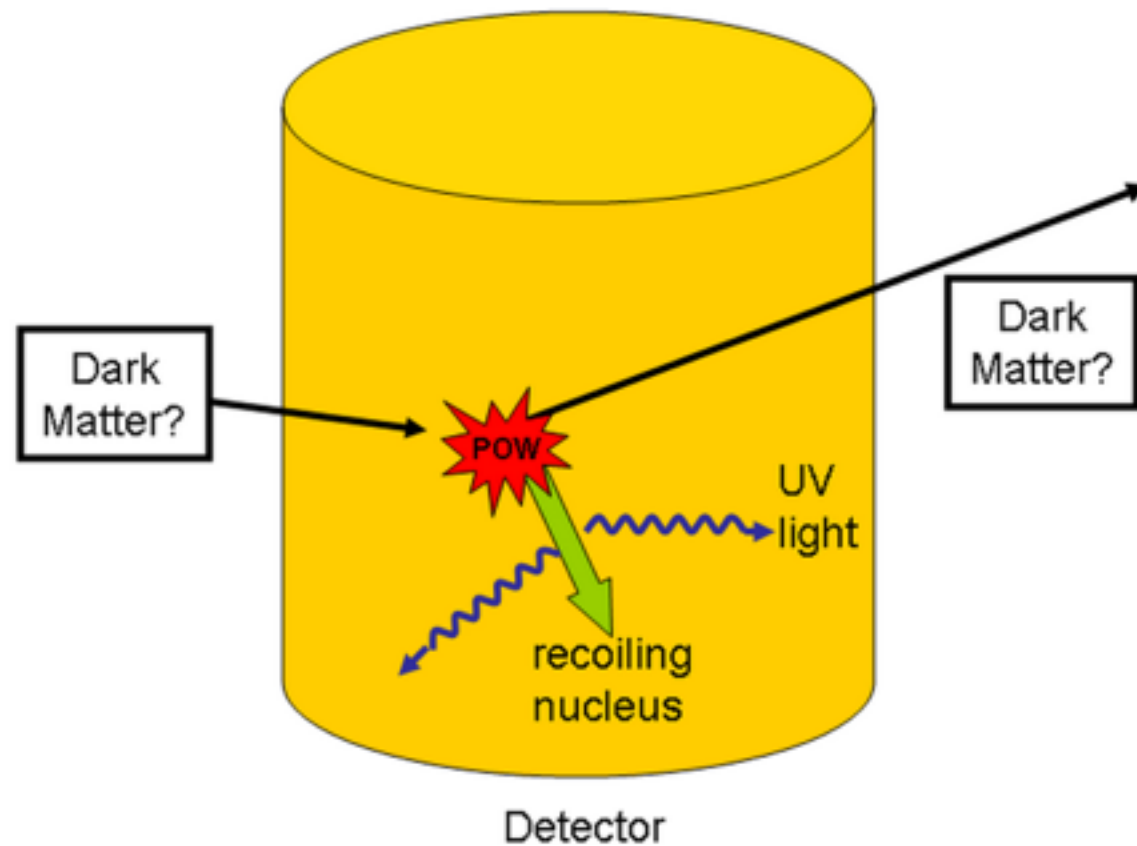
**II) Direct searches:**  
WIMPs scatter  
→ search for recoil  
on atomic nuclei



**I) Collider searches:**  
WIMP production  
→ searches at particle colliders

courtesy of C.Weniger

# Direct DM detection

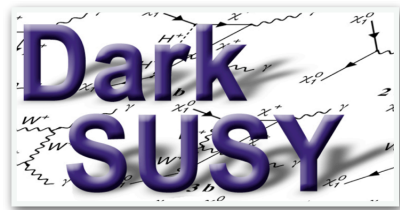


- $\text{WIMP} + \text{nucleus} \rightarrow \text{WIMP} + \text{nucleus}$
- Measure of recoil energy of the nucleus
- Suppress background enough to be sensitive to a signal
- Search for an annual modulation due to the Earth's motion in the halo (e.g. DAMA/LIBRA experiment)

Interesting quantities:

- spin-dependent and spin-independent cross sections off nucleons.
- direct detection rates in function of the recoil energy.

**Remark:** Direct detection experiments have really started to explore the MSSM parameter space!



# Direct DM detection

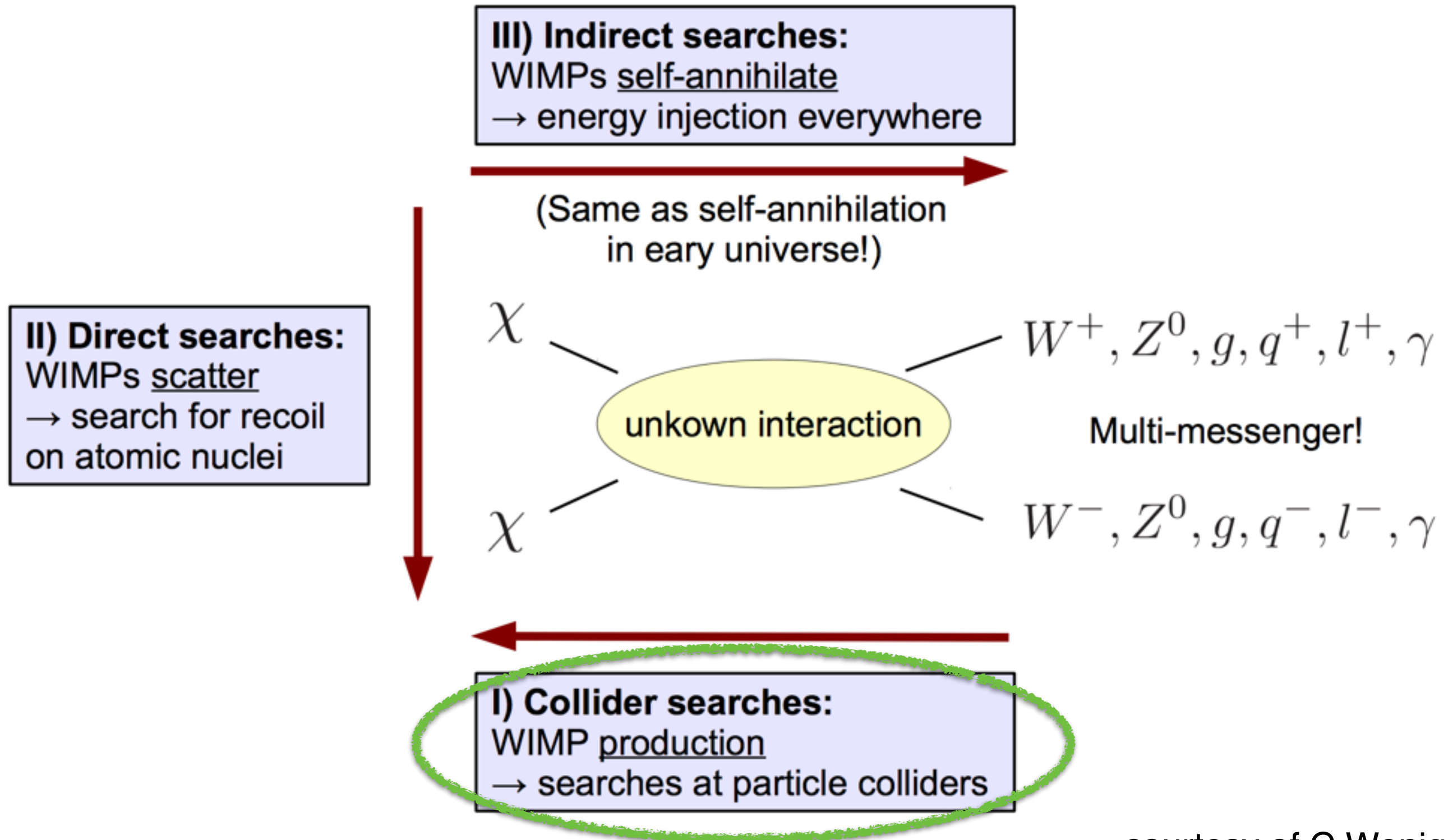
## How does DarkSUSY compute DD observables?

- DarkSUSY computes spin-independent and spin-dependent cross sections on protons and nucleons.
- Useful for the comparison with current experimental results.
- Routines for calculating the differential rate on several targets, including the form factor calculation.
- **Caveat:** large uncertainties on form factors and quark content of the nucleon.

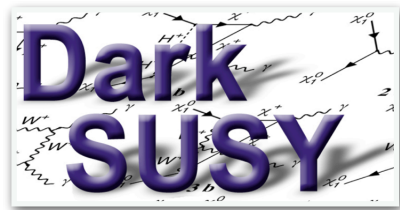
## DarkSUSY routines for direct detection:

- `src/dd/dsddneunuc.f`: computes spin-independent and spin-dependent cross sections off protons and nucleons, in units of  $\text{cm}^2$ .
- `src/dd/dsdddrde.f`: computes differential scattering rates on various targets as a function of time (it can be used to predict annual modulation signals), in units of counts/kg-day-keV.

# WIMP detection strategies



courtesy of C.Weniger



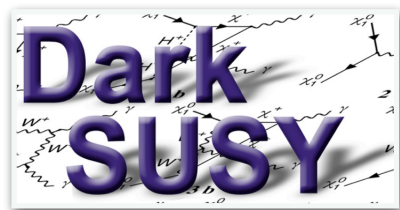
# Accelerator constraints

- Accelerator constraints are most easily checked with a call to `dsacbnd(excl)`, `excl` is non-zero if the model is excluded.
- For backwards-compatibility, DarkSUSY keeps old versions of the accelerator constraints as well, but `dsacbnd` always points to the latest set of constraints.
- Default set of constraints 'pdg2002c'. To change it, you should call `dsacset` and check its available set of options.
- See `dsacbnd9.f` for latest included bounds: lower bounds of chargino, gluino and squark masses, invisible Z width and Higgs mass bound, etc.

**Caveat:** Accelerators constraints are **not** updated to the latest accelerators results!



# DarkSUSY Tutorial

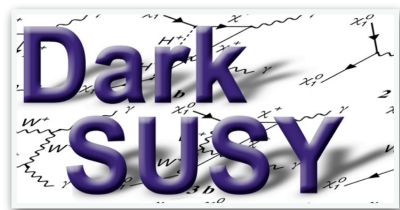


# Download & Install

<http://www.fysik.su.se/~edsjo/darksusy/>

## Current version

- **Current version:** [darksusy-5.1.1.tar.gz](#)
- **News:** Bug fixes (more automatic configure script, binary files causing problems on some systems deleted, corrected generic WIMP program in misc).
- **Release date:** March 1, 2013
- **Tested on:** Linux / Mac OS X with gfortran (version 4.2 or later required) or ifort. **Note:** g77 support is dropped.
- **System requirements:** You need to have approximately 400 MB of hard disk space. The download itself is about 100 MB. Perl is required for the make to proceed properly.



# Download & Install

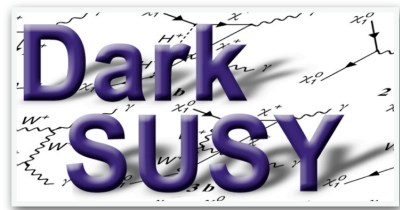
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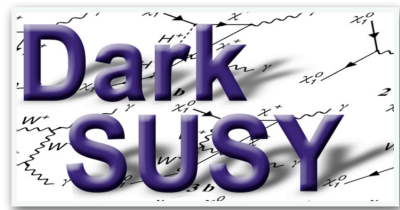
# Download & Install

<http://www.fysik.su.se/~edsjo/darksusy/>

```
$ tar -xzvf darksusy-5.1.1.tar.gz  
$ cd darksusy-5.1.1  
$ ./conf.gfortran  
$ make  
$ make install
```



**DONE?!  
READY TO GO!**



# Download & Install

<http://www.fysik.su.se/~edsjo/darksusy/>

```
$ tar -xzf darksusy-5.1.1.tar.gz
$ cd darksusy-5.1.1
$ ./conf.gfortran
$ make
$ make install
```

If you want to install DarkSUSY elsewhere (for the library and tables, usually in share), instead do:

```
$ ./configure --prefix=<install-dir>
$ make
$ make install
```

Other options can also be given at configure time, e.g:

```
$ ./configure F77=ifort FFLAGS= FOPT=-O
```

to compile with ifort instead of the default gfortran (if available).



# Manual

A quick manual (not fully up-to-date yet) is distributed with DarkSUSY and created with:

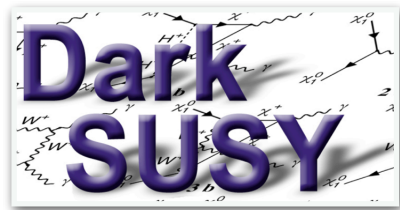
```
$ make pdf-manual
```

to make the default manual, or:

```
$ make pdf-manual-short
```

to make a short version (without subroutine headers).

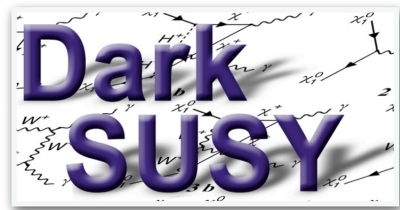
Also see the headers of various subroutines for instructions (they can be more useful than the manual sometimes).



# Typical Program

```
program ...  
implicit none  
  
real*8 ... ! definition of variables and functions called  
  
include ... ! include required modules, e.g. 'dsmssm.h'  
  
c This call initialises the DarkSUSY package.  
c Check out c src/ini/dsinit.f if you want to see what it  
c does.  
  
call dsinit  
write (*,*) 'DarkSUSY initialized'  
  
[make general settings]  
[determine your model parameters your way]  
[then calculate what you want]
```

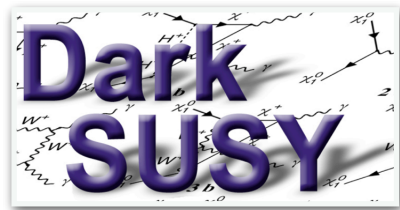
See [test/dstest.f](#) as a reference!



# Settings

## General routines setting:

- Essentially all the packages in DarkSUSY have a corresponding \*set routine that determines how those routines are going to be used, which parameter sets to use, etc.
- As an example, call dshmset ('default') chooses the default halo model (NFW).
- All these \*set routines are called with the argument 'default' by dsinit, but can be changed later by the user.



# How to run a script?

Look into **test/makefile**

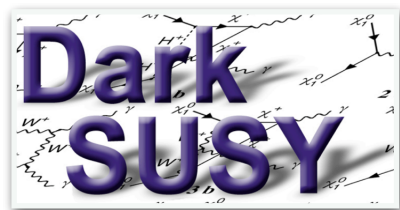
```
$ cd test  
$ nano makefile
```

- Check installation folder: **prefix=**
- Define commands for makefile:

```
dstest : dstest.f $(LIB)/libdarksusy.a $(LIB)/libisajet.a  
         $(FF) $(FOPT) $(INC) -L$(LIB) -o dstest dstest.f \  
         -ldarksusy -lHB -lFH
```

Run the script **test/dstest.f**

```
$ make dstest  
make: `dstest' is up to date.  
$ ./dstest &> out &  
$ nano out
```

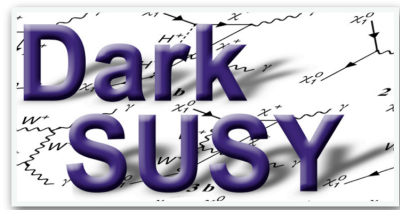


# How to run a script?

```
*****
*** Welcome to DarkSUSY version          ***
*** darksusy-5.1.1                      ***
*****

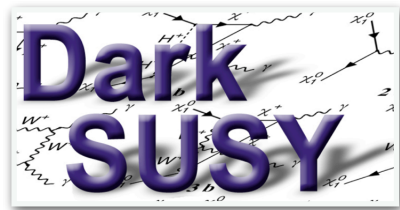
Initializing DarkSUSY...
[...]
***** MODEL: JE56A_000881 *****
[...]
Neutralino mass =    381.49536018437527
Gaugino fraction =    0.80017344515335709
H1 mass =          926.19328732872054      2.0232974526262533
H2 mass =          123.66699022930607      3.9318930663253884E-003
H3 mass =          925.90886000000000      2.1164678471354139
H+- mass =         929.64055132578301      1.9412066702012420
Calculating omega h^2 without coannihilations, please be patient...
[...]
Calculating scattering cross sections...
sigsip (pb) =       5.4014844940191810E-009
[...]
Calculating gamma ray fluxes...
fluxgacdiff =       1.9466096750513645E-012  ph/(cm^2 s GeV)
fluxgac =       5.0670561889799238E-010  ph/(cm^2 s)
fluxgaga =       5.6245800731894324E-016  ph/(cm^2 s)
fluxgaz =       3.4259181882023676E-015  ph/(cm^2 s)
nsigvgacont =       64632.998292566190
nsigvgacdiff =       32824.594649122002      GeV^-1
nsigvgaga =       7.1744512140497749E-002
nsigvgaz =       0.43699409706591746
[...]
```

```
$ make dstest
make: `dstest' is up to date.
$ ./dstest &> out &
$ nano out
```



# Exercises overview

1. Computing prompt photons and positrons spectra for DM annihilation into quarks or leptons, 100% branching ratio.
2. Plotting spectra.
3. Computing prompt photons and positrons spectra for DM annihilation for a concrete SUSY model.



# Exercise 1: spectrum 100% BR

DM model:

- 100% BR into quarks or leptons.
- Spectrum of prompt photons and positrons (or electrons).
- output: file with E, dN/dE.

Program example: Settings

```
program dmspec
implicit none

integer BRch, yieldk, istat, i
real*8 mwimp, result1, egev
real*8 dshayield

include 'dsmssm.h'
include 'dsio.h'
include 'dsidtag.h'
include 'dshacom.h'
include 'dshrcom.h'
```



# Exercise 1: spectrum 100% BR

Program example: Compute the **photon** spectrum

```
call dsinit
write (*,*) 'DarkSUSY initialized'

c    Define WIMP mass ad 100% channel
mwimp=1000.
BRch=25 ! bbar

c    Differential gamma-ray flux
yieldk=152 ! integrated above the threshold: 52

c    Open a file
open (unit=11,file='mwimp1000gev_bbar_gamma.dat')
c    Loop on energies to get the differential flux
do i=[...]
egev=[...]
result1=dshayield(mwimp,egev,BRch,yieldk,istat)
write(11,*) egev,result1
enddo
close(11)

end
```



# Exercise 1: spectrum 100% BR

Program example: Compute the **positron** spectrum

```
call dsinit  
write (*,*) 'DarkSUSY initialized'
```

```
c    Define WIMP mass ad 100% channel  
    mwimp=1000.  
    BRch=25 ! bbar
```

```
c    Differential gamma-ray flux  
    yieldk=152 ! integrated above the threshold: 52
```

```
c    Open a file  
    open (unit=11,file='mwimp1000gev_bbar_gamma.dat')
```

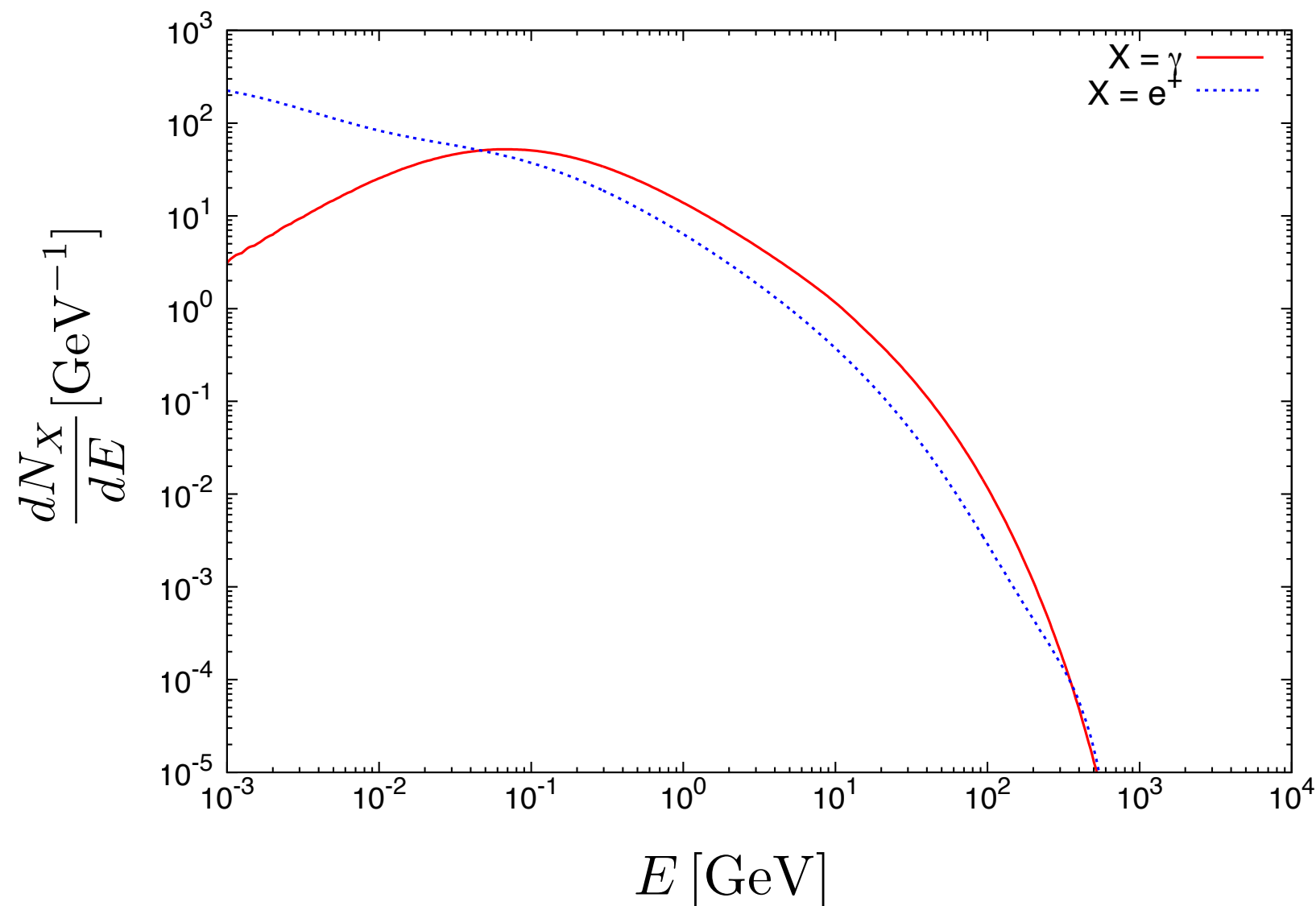
```
c    Loop on energies to get the differential flux  
    do i=[...]  
    egev=[...]  
    result1=dshayield(mwimp,egev,BRch,yieldk,istat)  
    write(11,*) egev,result1  
    enddo  
    close(11)
```

```
end
```

**Look into `src/ha/dshayield.f`  
for channels ID**

# Exercise 2: plotting spectra

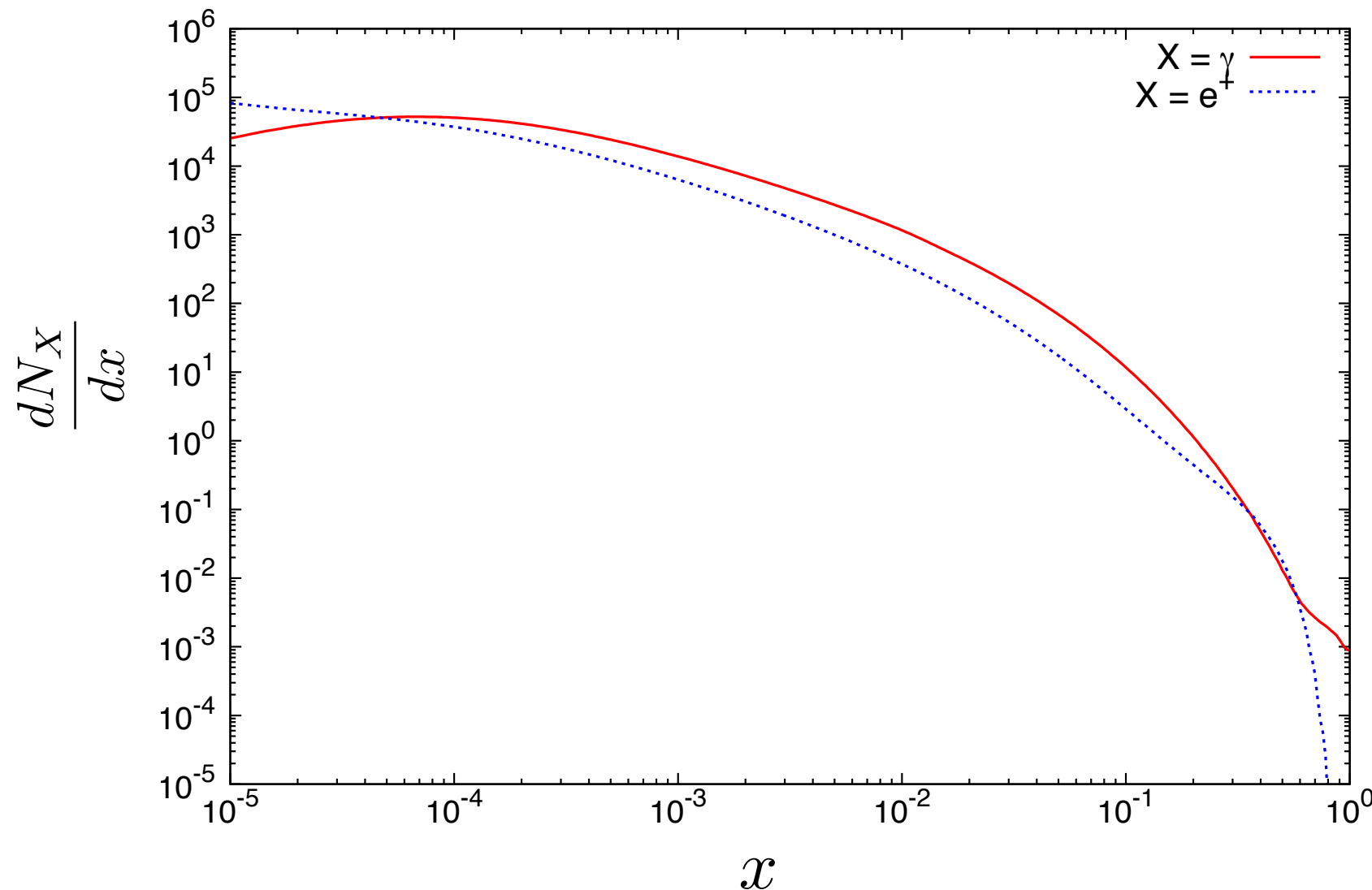
Plotting different spectral quantities from the output file (.dat file)



$$\frac{dN_X}{dE}$$

# Exercise 2: plotting spectra

Plotting different spectral quantities from the output file (.dat file)

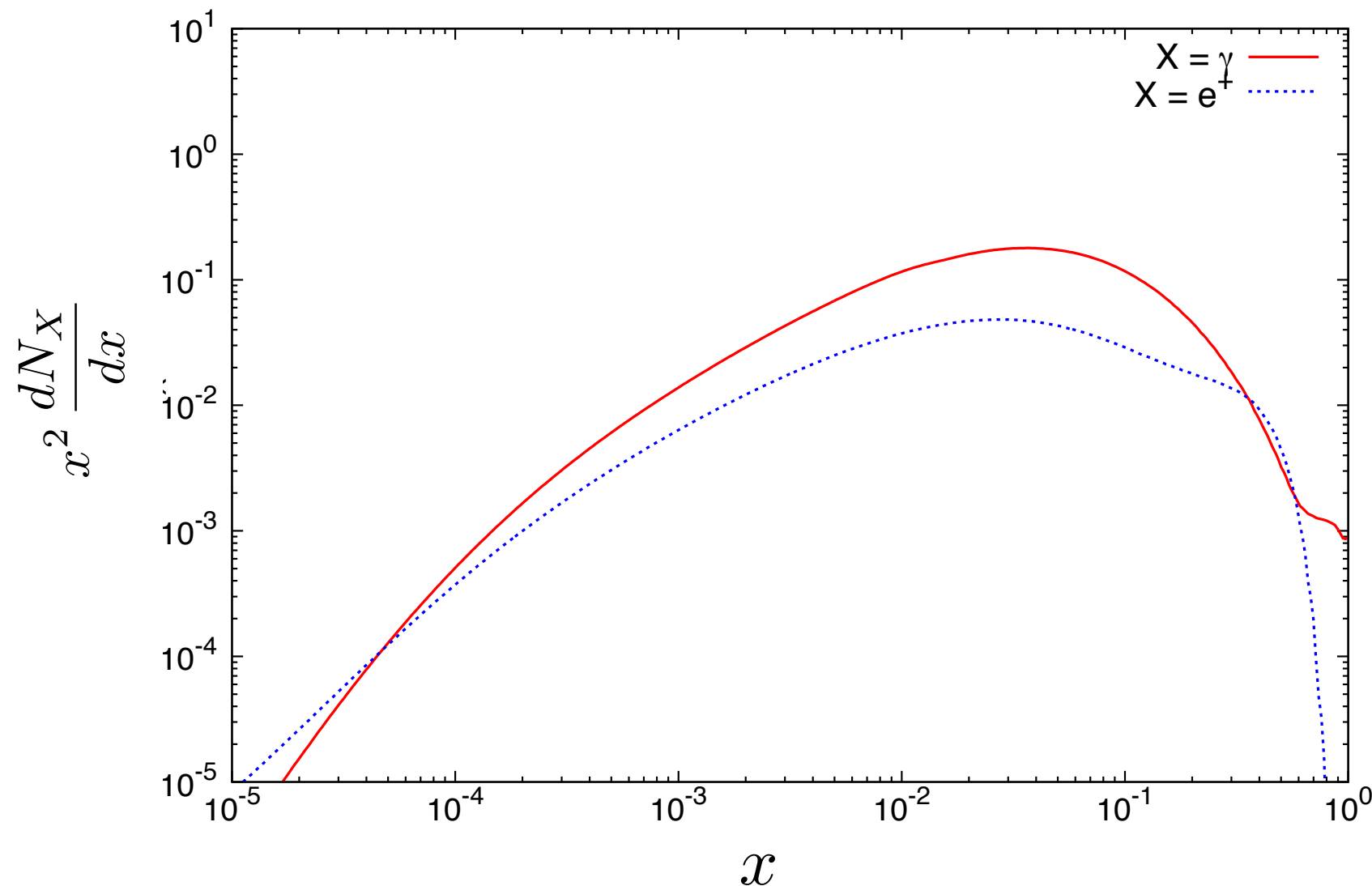


$$x \equiv \frac{E_X}{m_\chi}$$

$$\frac{dN_X}{dx} \equiv m_\chi \frac{dN_X}{dE}$$

# Exercise 2: plotting spectra

Plotting different spectral quantities from the output file (.dat file)



$$x \equiv \frac{E_X}{m_\chi}$$

$$x^2 \frac{dN_X}{dx}$$

For comparison to data, it is often plotted:

$$E^2 \frac{dN_X}{dE}$$



## Exercise 3: spectrum concrete MSSM

## DM model:

- MSSM-7 concrete model: in **test/dstest.mod** keep only JE56A\_002352
- Spectrum of prompt photons and positrons (or electrons).
- output: file with  $E$ ,  $dN/dE$ .

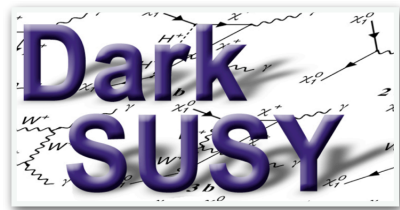
## Program example: Settings

```

program dmspec_MSSM
implicit none

[...]
integer modtype
character slhfile*80
integer iend
integer unphys,excl,hwarning

include 'dsmssm.h'
include 'dsio.h'
include 'dsidtag.h'
include 'dshacom.h'
include 'dshrcom.h'
[...]
```



## Exercise 3: spectrum concrete MSSM

Program example: Read in model in the form of .mod file

```
c      Read in models from .mod file
      open (unit=11,file='dstest.mod')
      read (11,*) ! this skips the header

      open (unit=30,file='dstest2.tmp')

      iend=0

1000  call read_model(11,0,iend,ierr)

      if (ierr.ne.0) then
        write (*,*) 'Error while reading dstest.mod'
        write (*,*) 'The DarkSUSY test cannot continue'
        stop
      else if (iend.eq.1) then
        goto 2000 ! exit program
      else
        call dswrite(0,0,'Parameters read from file dstest.mod')
      endif
```



## Exercise 3: spectrum concrete MSSM

## Program example: Read in model in the form of .mod file

```
c      Read in models from .mod file
      open (unit=11,file='dstest.mod')
      read (11,*) ! this skips the header

      open (unit=30,file='dstest2.tmp')

      iend=0
```

```
1000 call read_model(110,iend,ierr)
```

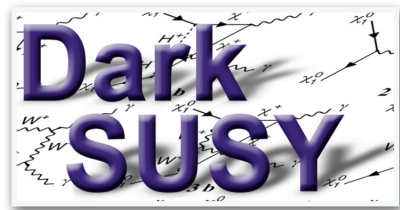
**subroutine at the end of  
test/dstest.f**

**dsgive\_model(mu,m2,ma,tanbe,mqtild,at,ab)**

```

else if (.fendreq1) then
    goto 2000 ! exit program
else
    call dswrite(0,0,'Parameters read from file dstest.mod')
endif

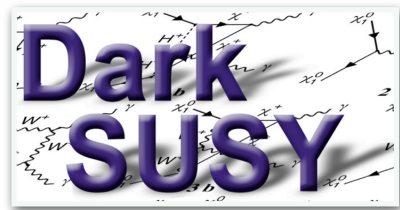
```



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Program example: Initialise model and get some interesting information

```
write(*,*) ' '  
write(*,*) '***** MODEL: ',idtag,' *****'  
  
call dssusy(unphys,hwarning)  
  
write(*,*) ' Neutralino mass mx = ',mass(kn(1))  
write(*,*) '   Gaugino fraction = ',  
&      dsabsq(neunmx(1,1))+dsabsq(neunmx(1,2))  
[...]
```



# Exercise 3: spectrum concrete MSSM

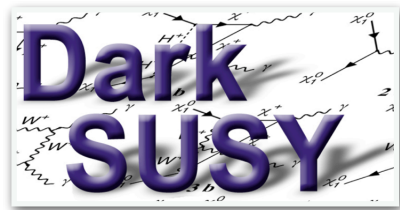
Program example: Compute the **photon** spectrum

```
c      Differential gamma-ray flux
yieldk=152 ! integrated above the threshold: 52
mwimp=mass(kn(1))

call dshasetup

open (unit=11,file='mwimp_MSSM_gamma.dat')
do i=1,501
  egev=dexp(dlog(0.001d0)
&          +(dlog(mwimp)-dlog(0.001d0))/500.d0*(i-1))
  result1=dshaloyield(egev,yieldk,istat)
  write(11,*) egev,result1
enddo
close(11)

end
```



## Exercise 3: spectrum concrete MSSM

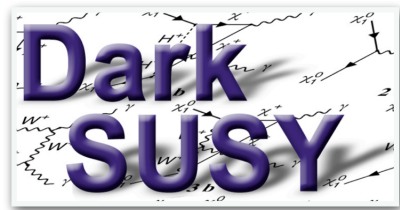
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enddo
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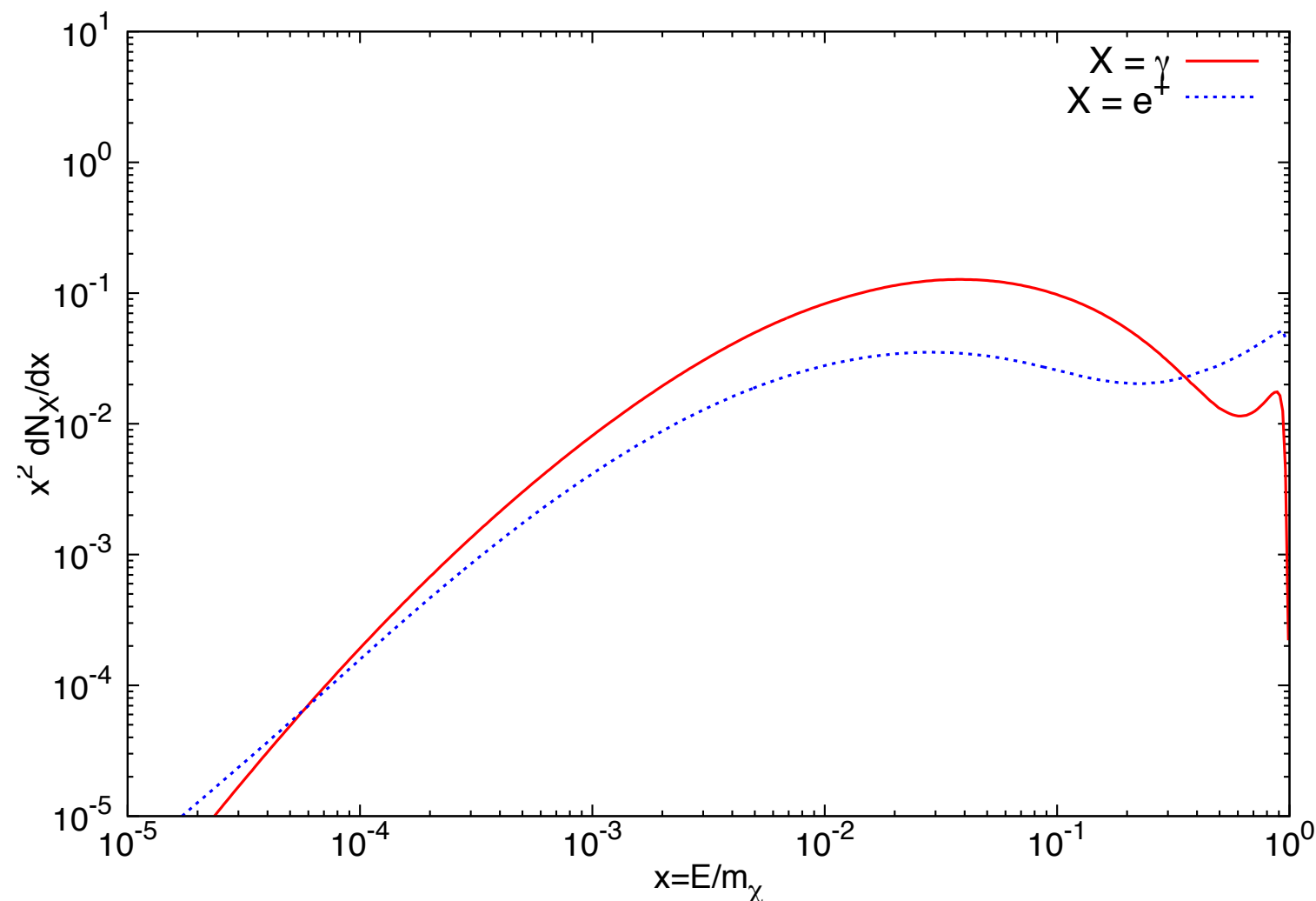
end
```



# Exercise 3: spectrum concrete MSSM

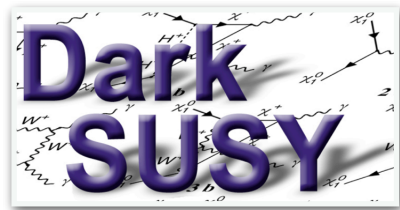
DS model: JE56A\_002352

$$\mu, \tan \beta, M_2, m_A, A_t, A_b, m_0$$



$$x^2 \frac{dN_X}{dx}$$

$$m_\chi = 988 \text{ GeV}$$



# What would you learn?

1. How DarkSUSY is structured and what we can do with this tool for DM searches.
2. How to compute prompt photons and positrons spectra for DM annihilation in the framework of:
  - Simplified models: 100% branching ratio into quarks or leptons.
  - Concrete MSSM models.
3. Plotting spectra.