



Top quark simulations at LC



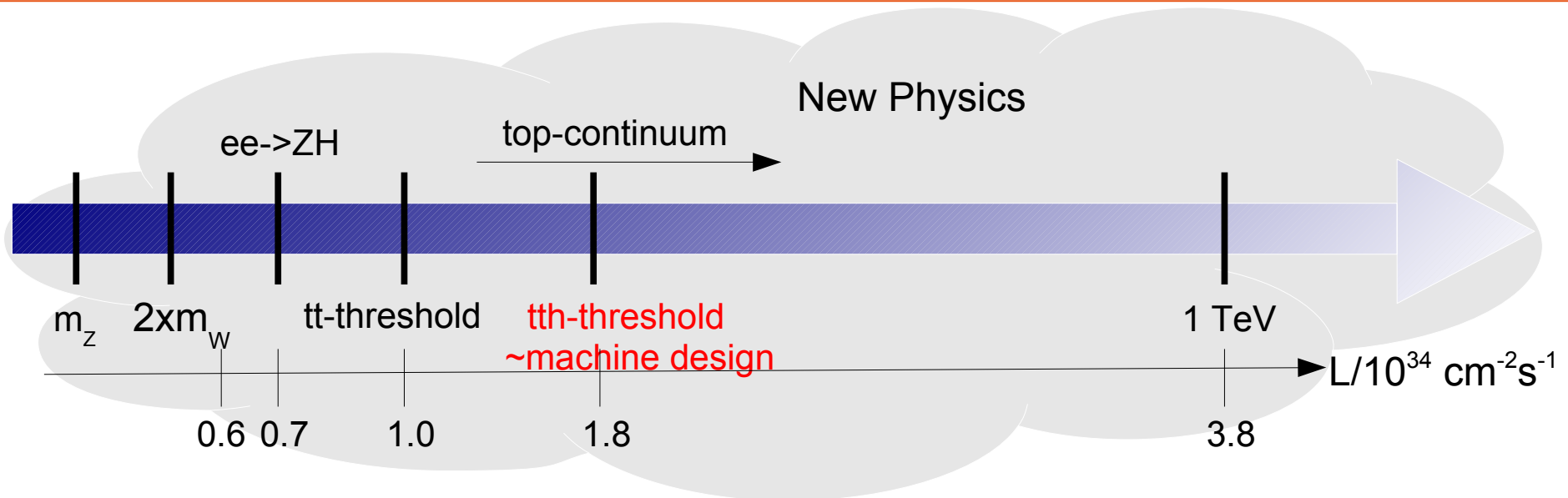
Roman Pöschl



With major contributions from



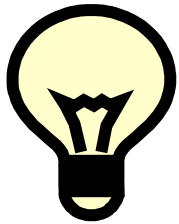
2nd WHIZARD Workshop Würzburg – March 2015



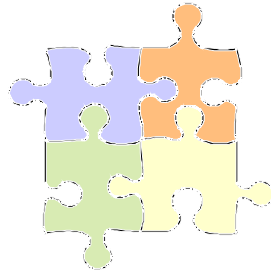
- All Standard Model particles within reach of (I)LC
 - High precision tests of Standard Model over wide range to detect onset of New Physics
- Machine settings can be “tailored” for specific processes
 - Centre-of-Mass energy
 - Beam polarisation

$$\sigma_{P,P'} = \frac{1}{4} [(1 - PP')(\sigma_{LR} + \sigma_{RL}) + (P - P')(\sigma_{RL} - \sigma_{LR})]$$

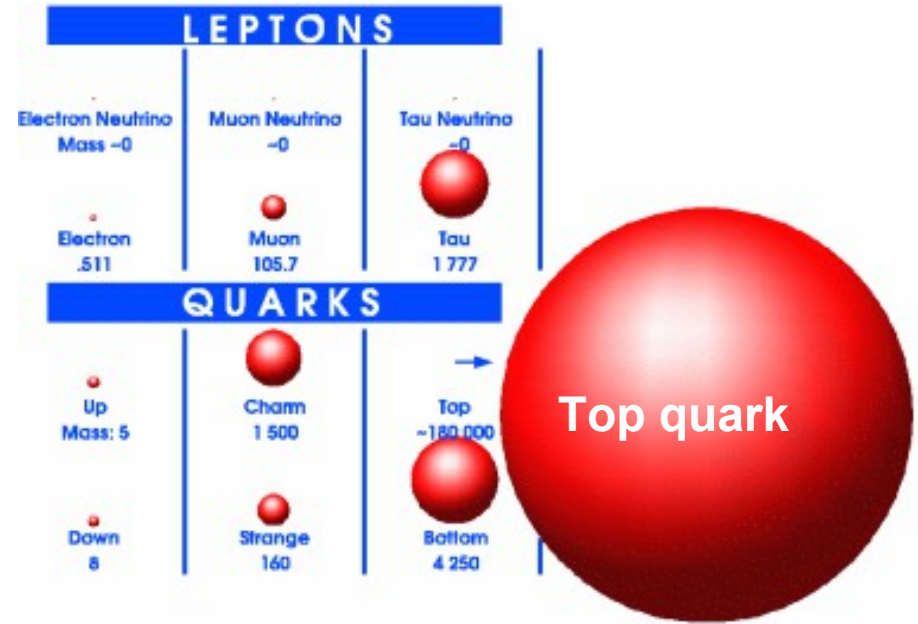
- “Background free” searches for BSM through beam polarisation



Elementary Scalar?



Composite object?



- Higgs and top quark are intimately coupled!

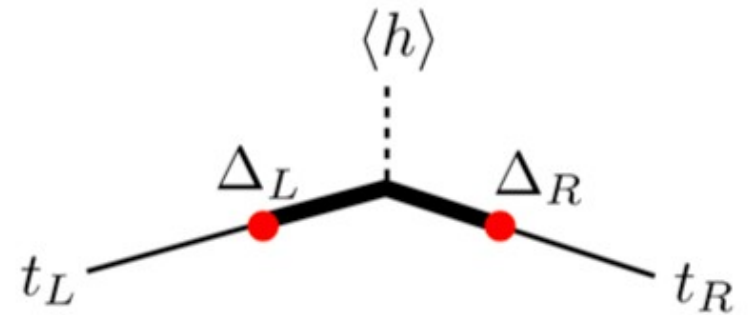
Top Yukawa coupling $O(1)$!

=> Top mass important SM Parameter

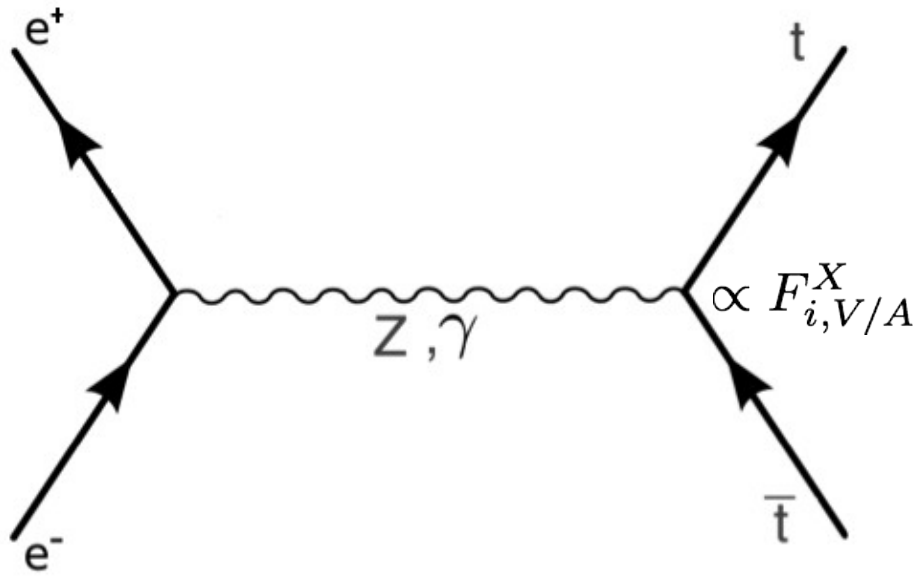
- New physics by compositeness?

Higgs and top composite objects?

- LC perfectly suited to decipher both particles



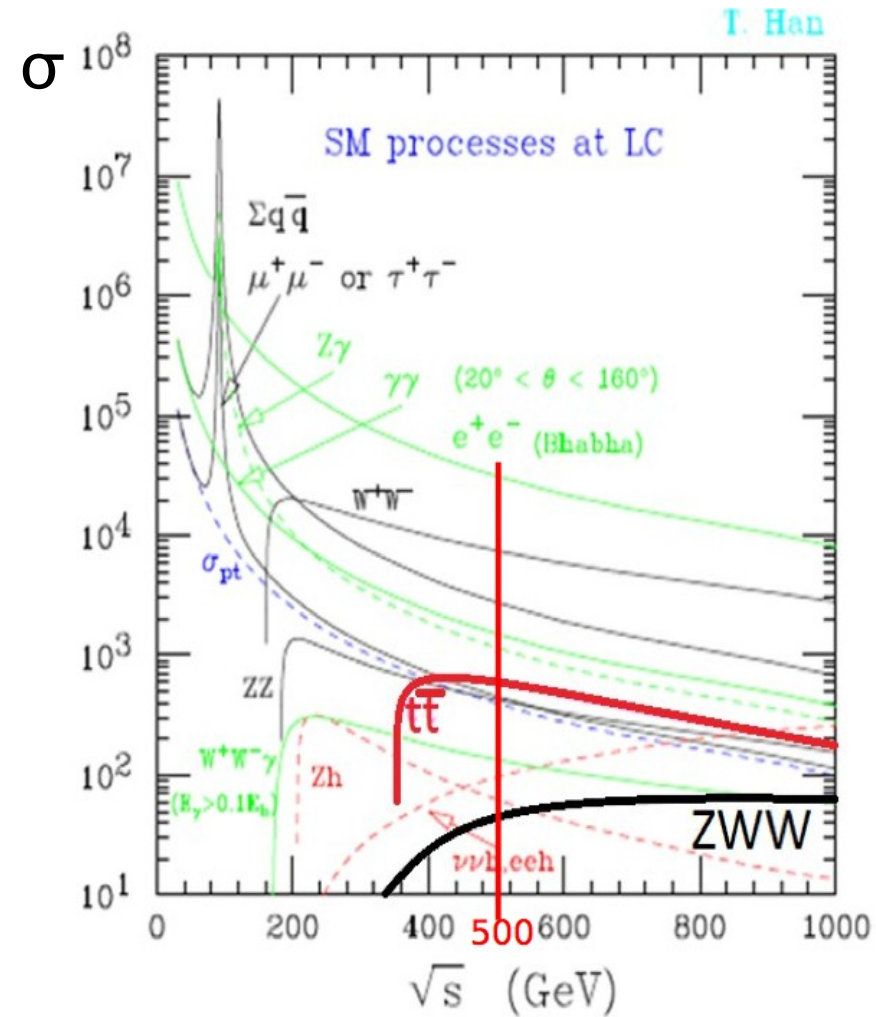
Courtesy of S. Rychkov



- Top quark production through electroweak processes
no competing QCD production => Small theoretical errors!

- High precision measurements

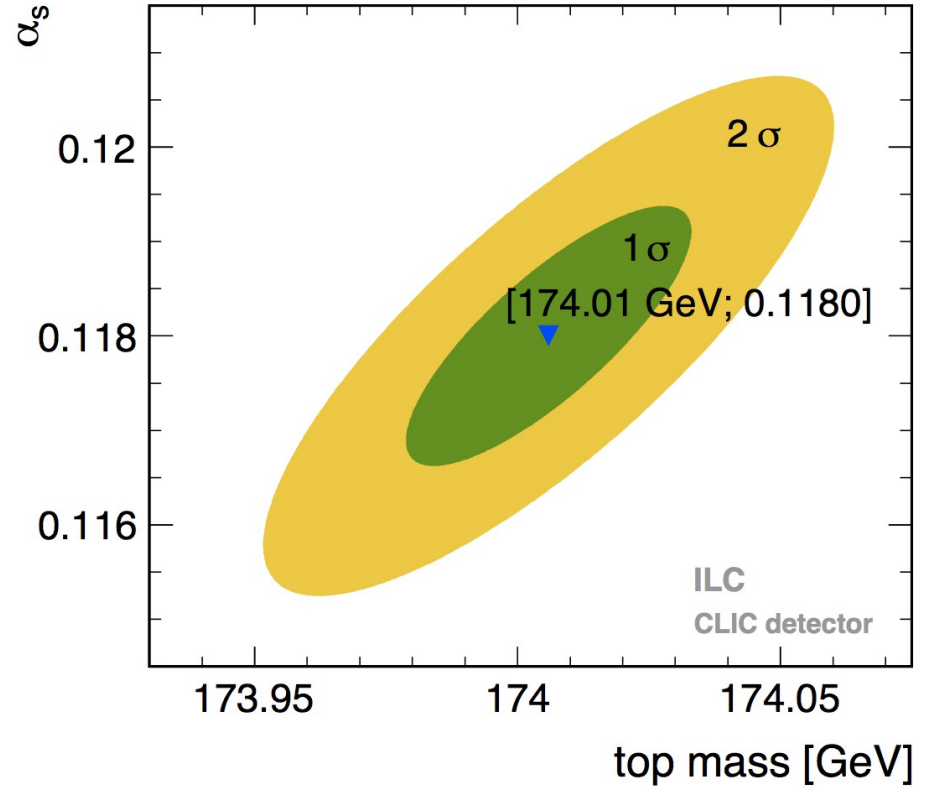
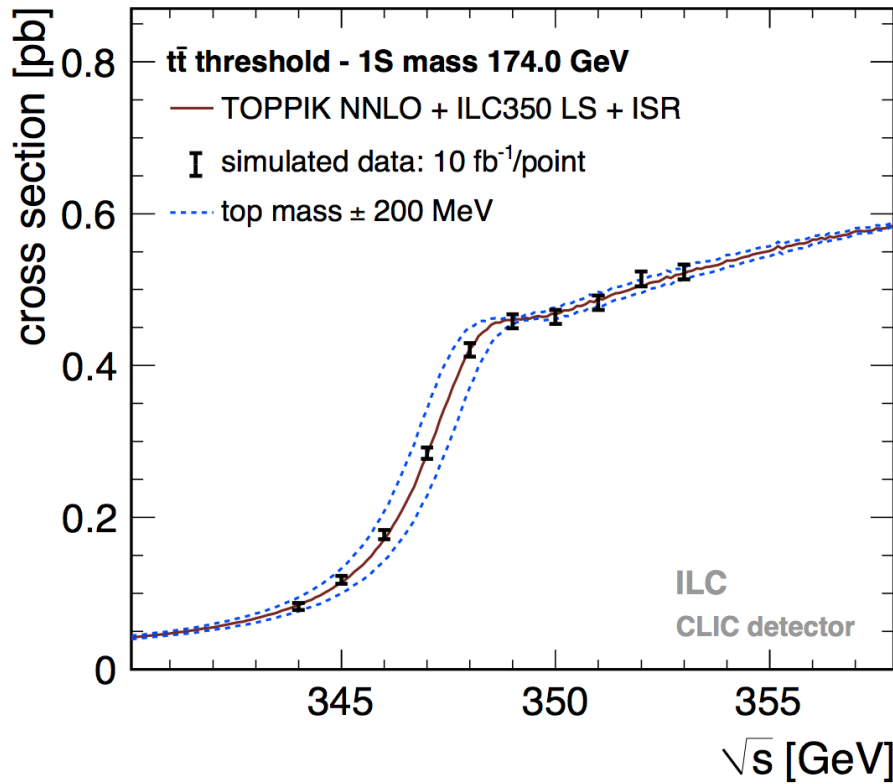
- Top quark mass at ~ 350 GeV through threshold scan
- Polarised beams allow testing chiral structure at $t\bar{t}X$ vertex
=> Precision on form factors F





Mass and α_s

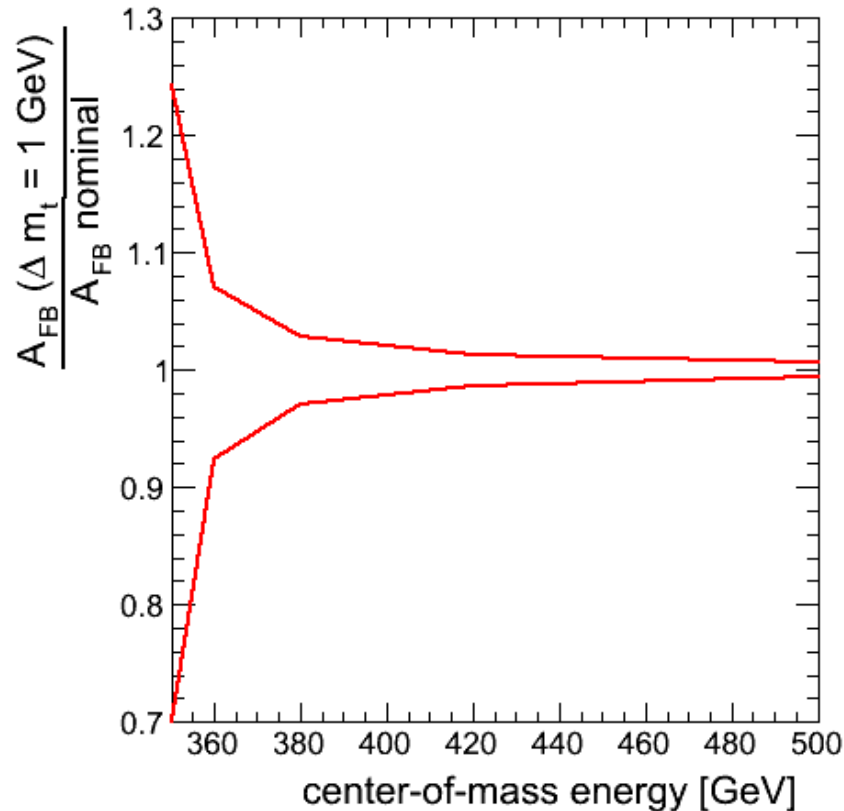
EPJC C73 (2013) 2530



~100 MeV

1S top mass and α_s combined 2D fit

m_t stat. error	27 MeV
m_t theory syst. (1%/3%)	5 MeV / 9 MeV
α_s stat. error	0.0008
α_s theory syst. (1%/3%)	0.0007 / 0.0022



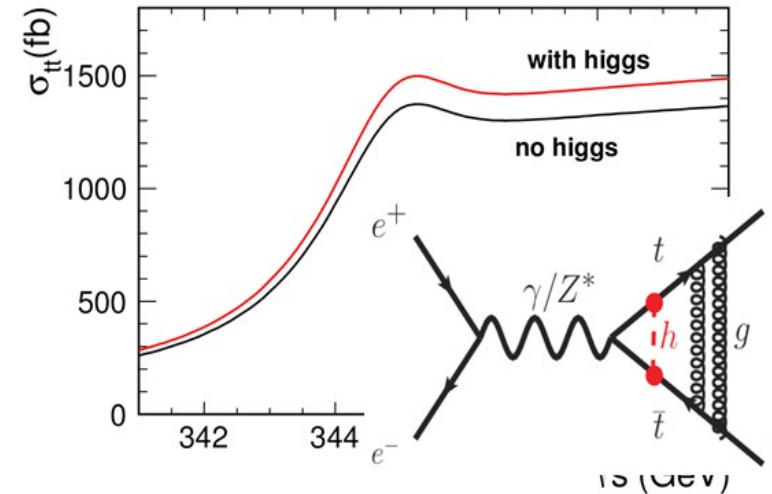
Influence of the top quark mass on x-sec and A_{FB}

- very pronounced below $\sqrt{s} = 360$ GeV
- 2.9%/GeV at $\sqrt{s} = 380$ GeV
- 1.3%/GeV at $\sqrt{s} = 420$ GeV
- 0.6%/GeV at $\sqrt{s} = 500$ GeV

With the assumption of a 100 MeV pole mass measurement at threshold, the remaining uncertainty is one per mil or less above 420 GeV

The template is prepared by floating top mass and width. Since the measurement of δy_t is extracted from normalization of σ_{tt} , the normalization is also used for σ_{tt} fit.

- 2+1 param : **2D fit** of m_t and Γ_t , y_t is measured individually.
- 3 param : **3D fit** of m_t , Γ_t and y_t .

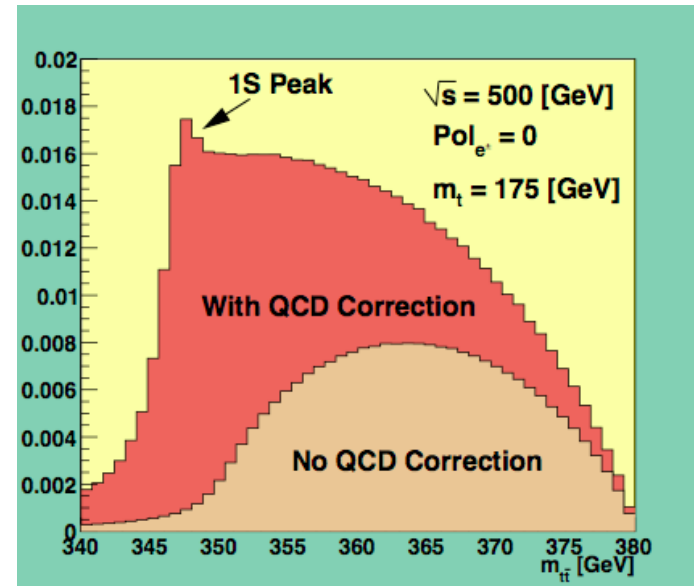
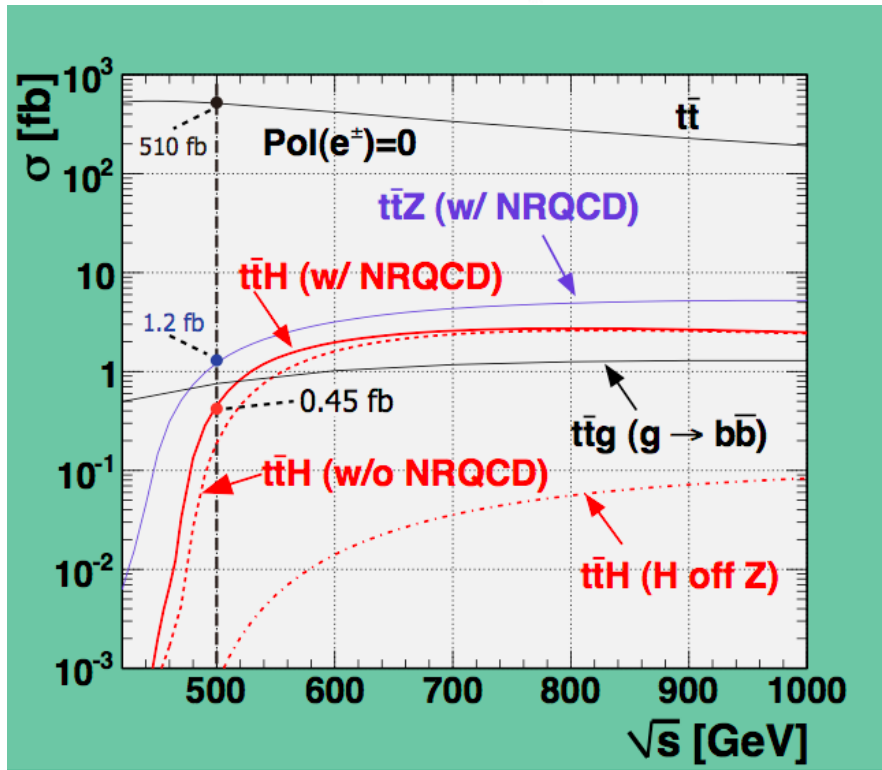
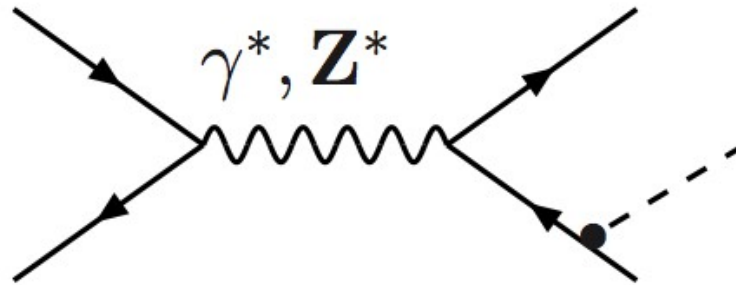


$$\int \mathcal{L} dt = \mathbf{100 fb^{-1}}$$

	(2 + 1) param fit	3 param fit
m_t	19 MeV	29 MeV
Γ_t	38 MeV	39 MeV
y_t	4.6%	5.9%

Stat. Uncertainties
'add'
Theoretical
uncertainties ~ 70 MeV

Total expected precision on $m_t \sim 100$ MeV
(very conservative estimation!!!)

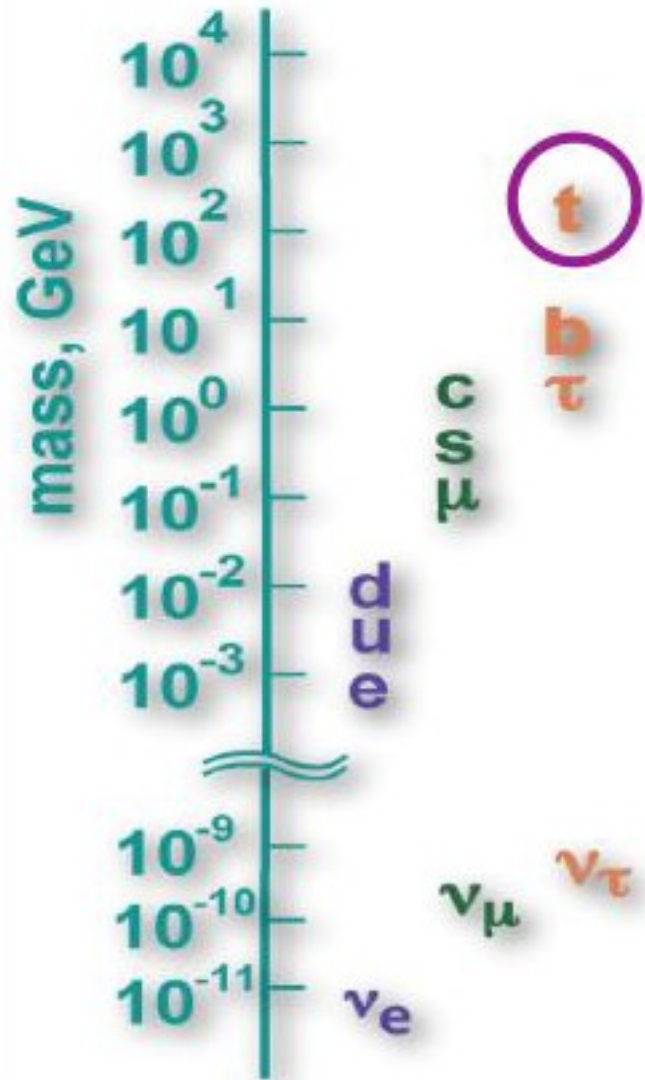


~ Factor 2 enhancement
From QCD bound states

R. Yonamine et al.
T. Tanabe, T. Price

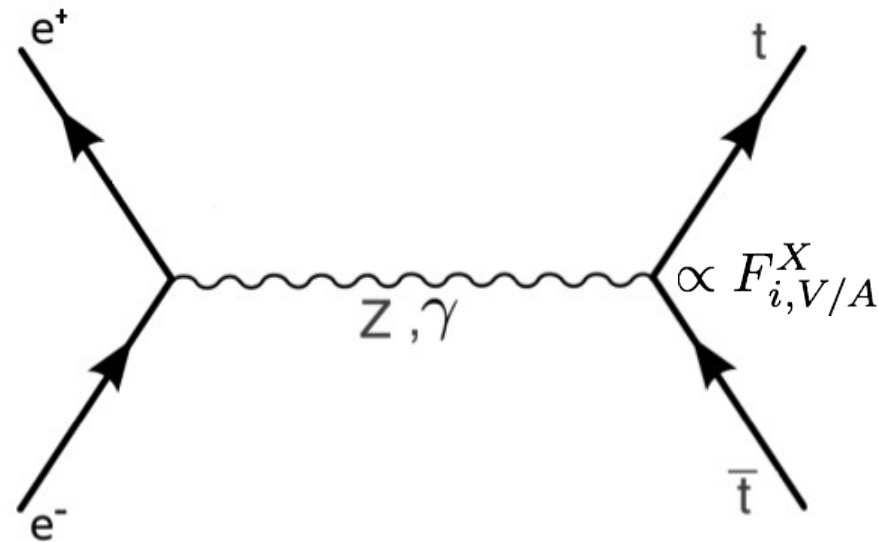
$\Delta g_{ttH} / g_{ttH}$	500 GeV	500 GeV + 1 TeV
Canonical	14%	3.2%
LumiUP	7.8%	2.0%

← ILC TDR
← Technically possible



- SM does not provides no explanation for mass spectrum of fermions (and gauge bosons)
- Fermion mass generation closely related to the origin electroweak symmetry breaking
- Expect residual effects for particles with masses closest to symmetry breaking scale
 - A_{FB} anomaly at LEP for b quark

Strong motivation to study chiral structure of top vertex in high energy e^+e^- collisions



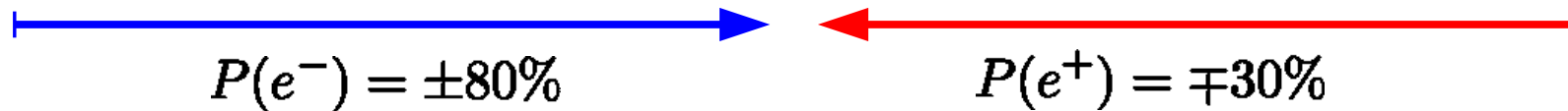
$$\Gamma_{\mu}^{t\bar{t}X}(k^2, q, \bar{q}) = ie \left\{ \gamma_{\mu} (F_{1V}^X(k^2) + \gamma_5 F_{1A}^X(k^2)) - \frac{\sigma_{\mu\nu}}{2m_t} (q + \bar{q})^{\nu} (iF_{2V}^X(k^2) + \gamma_5 F_{2A}^X(k^2)) \right\}$$

Pure γ or pure Z^0 : $\sigma \sim (F_i)^2 \Rightarrow$ No sensitivity to sign of Form Factors

Z^0/γ interference : $\sigma \sim (F_i) \Rightarrow$ Sensitivity to sign of Form Factors

At ILC **no** separate access to ttZ or tty vertex, but ...

ILC 'provides' two beam polarisations



There exist a number of observables sensitive to chiral structure, e.g.

$$\sigma_I \quad A_{FB,I}^t = \frac{N(\cos\theta > 0) - N(\cos\theta < 0)}{N(\cos\theta > 0) + N(\cos\theta < 0)} \quad (F_R)_I = \frac{(\sigma_{t_R})_I}{\sigma_I}$$

x-section

Forward backward asymmetry

Fraction of right handed top quarks



Extraction of relevant unknowns

$$F_{1V}^\gamma, F_{1V}^Z, F_{1A}^\gamma = 0, F_{1A}^Z \quad \text{or equivalently} \quad g_L^\gamma, g_R^\gamma, g_L^Z, g_R^Z$$

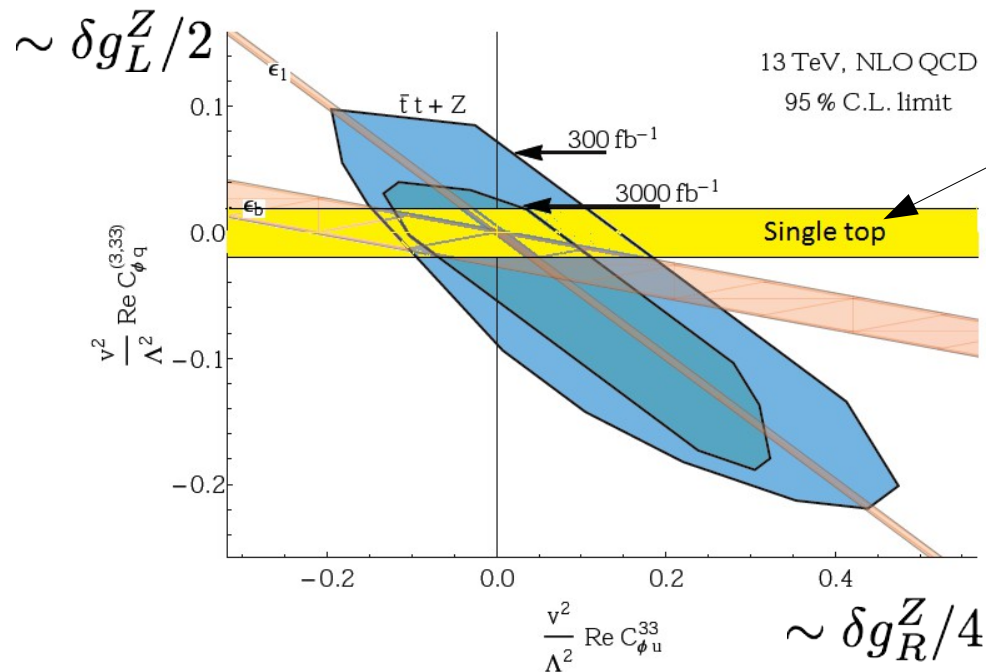
$$F_{2V}^\gamma, F_{2V}^Z$$

Precision cross section $\sim 0.5\%$,

Precision $A_{\text{FB}} \sim 2\%$,

ArXiv: 1307.8102
Precision $\lambda_t \sim 3-4\%$

Accuracy on SM Z couplings compared with other experiments



- ILC with polarised beams outperforms all present and future experiments (Stringent limits only from LEP)

- Before ILC single top at LHC and B factories can deliver complementary information

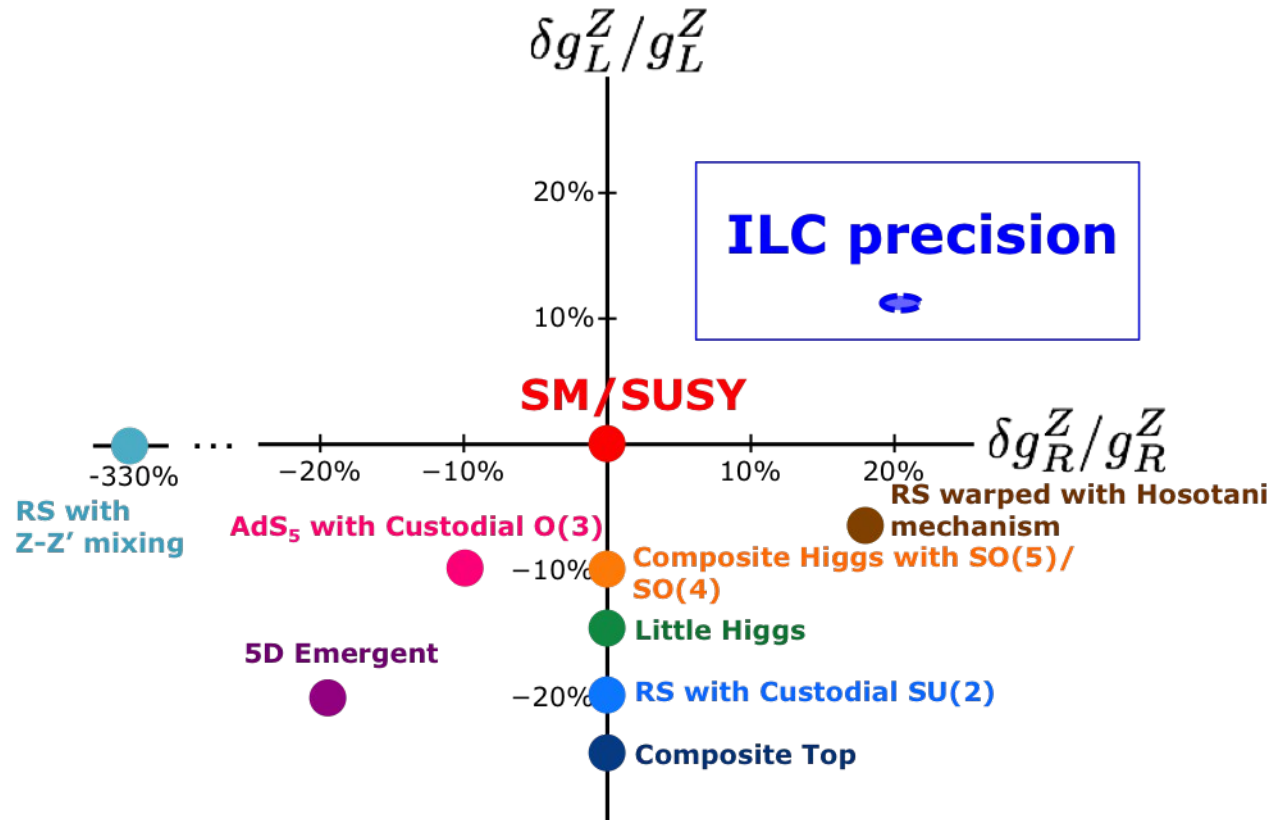
- In particular g_R can only be constrained by ILC!

- Maintaining this high level still requires substantial experimental and theoretical work

LHC 300. 3000 from 1404.1005
Flavor from 1408.0792
LHC Single top added by F. Richard

ILC promises to be high precision machine for electroweak top couplings

Top is primary candidate to be a messenger new physics in many BSM models
Incorporating compositeness and/or extra dimensions

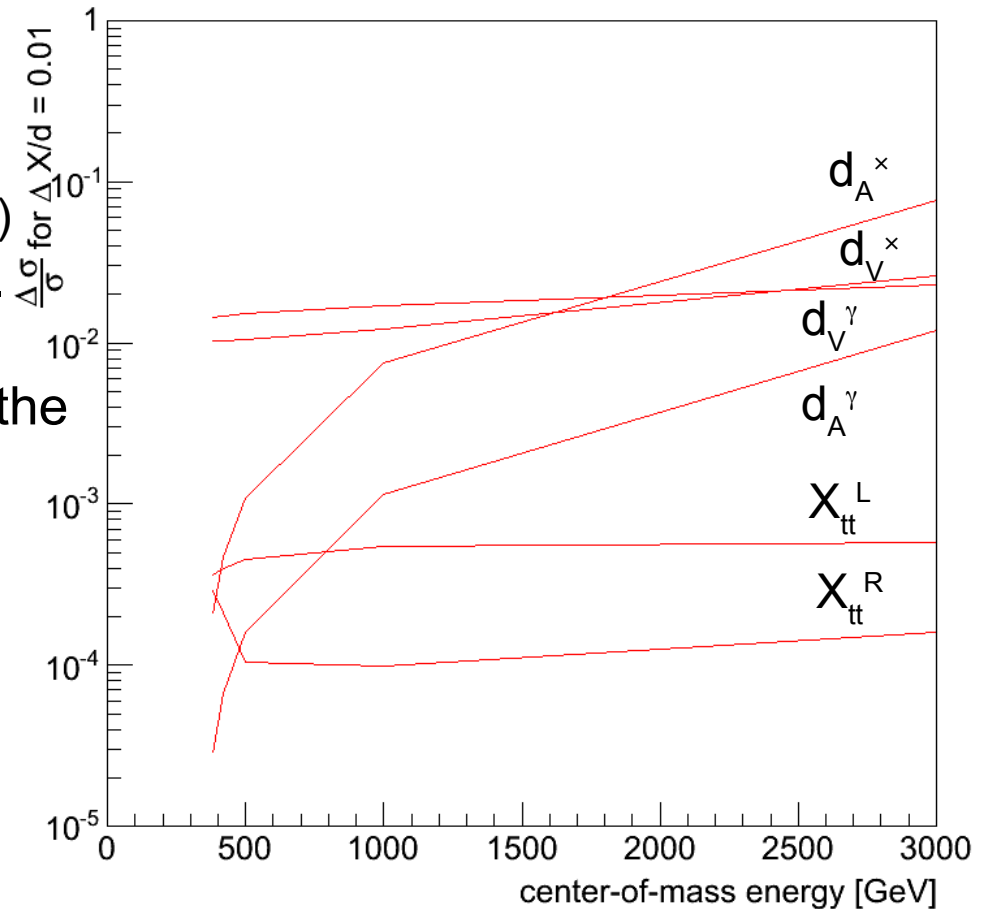


Precision expected for top quark couplings will allow to distinguish between models

Dimension 6 effective operators
(~equivalent role to anomalous form factors)
have been implemented in WHIZARD...

Allow to map the dependence on \sqrt{s} of the
impact of new physics on given
observable

May help to explore the sensitivity of
new/additional observables





- Event generator **WHIZARD (v1.95!!!)** interfaced to **PYTHIA**
 $e^+e^- \rightarrow 6f$: 250 fb⁻¹ for two beam polarisations: $e_L^- e_R^+$ and $e_R^- e_L^+$

Events were generated with full simulation and results were scaled for realistic beam polarisation

$$\sigma_{P,P'} = \frac{1}{4} [(1 - PP')(\sigma_{LR} + \sigma_{RL}) + (P - P')(\sigma_{RL} - \sigma_{LR})]$$

Full Standard Model background
Common samples for ILD and SiD studies

- **GEANT4** and **ILCSoft** for detector simulation and reconstruction
- **ILD** features a full software suite
 - Mokka as geometry interface to GEANT4
 - MARLIN as analysis framework for event reconstruction
 - Interface to toolkits such as PandoraPFA or LCFIVertex
- **Detector simulation is based on input from worldwide detector R&D**

- Worry was that hard gluon radiation (not implemented in WHIZARD 1.95) deteriorates results
- WHIZARD 2.2.2 allow for additional hard gluon radiation and test sensitivity of “our” observables to hard gluon emission (from top leg!?)
Observables are cross section and forward-backward asymmetry

The generated samples are:

$$\textit{inclusive } e^+e^- \rightarrow t\bar{t}$$

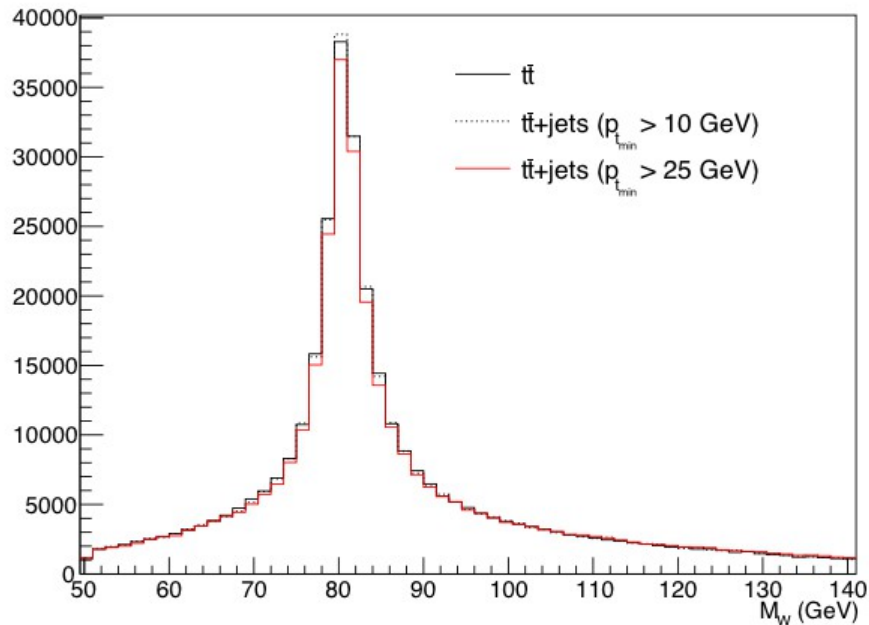
for both polarisations
 $e_L^-e_R^+$ and $e_R^-e_L^+$

$$e^+e^- \rightarrow t\bar{t} + t\bar{t}j + t\bar{t}jj + t\bar{t}jjj$$

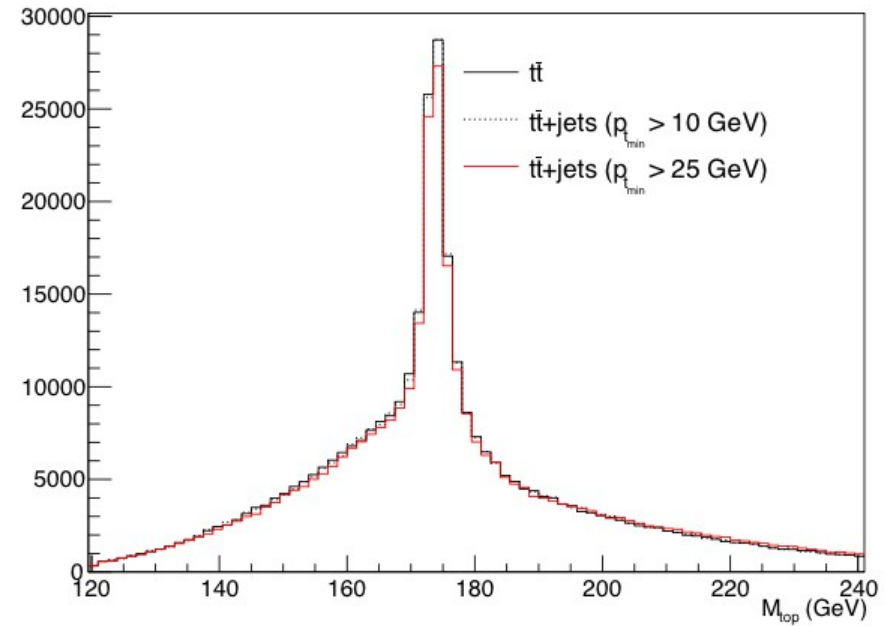
for different \mathbf{p}_t of the additional jets
($p_{t_{min}} > 10, 15, 20, 25$ GeV) for $e_L^-e_R^+$
 $p_{t_{min}} > 10$ for $e_R^-e_L^+$

1 million of events per sample

- Events are passed to PYTHIA8 for parton showering and hadronisation

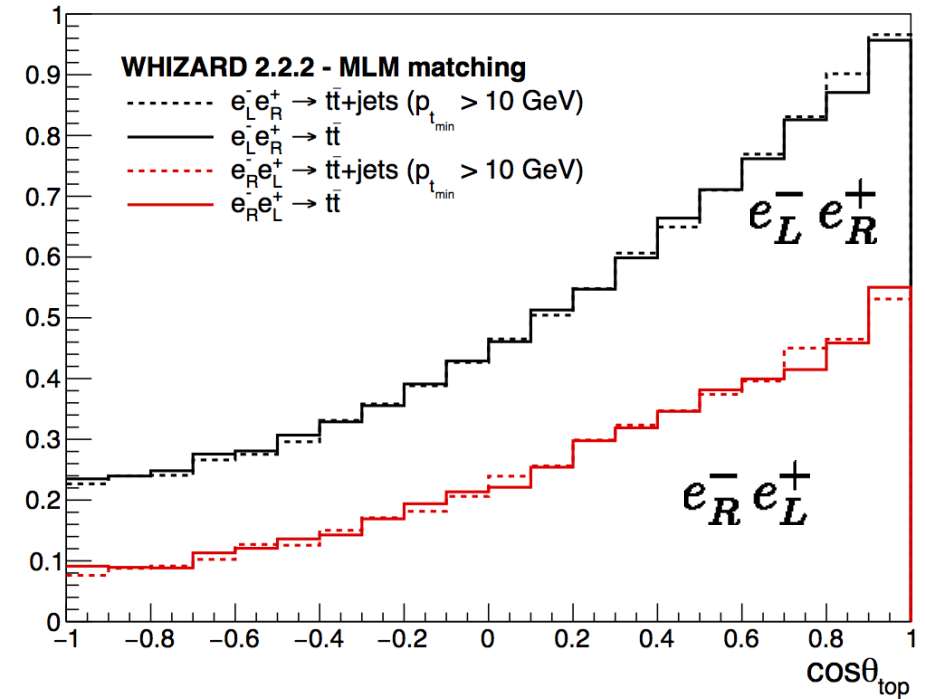
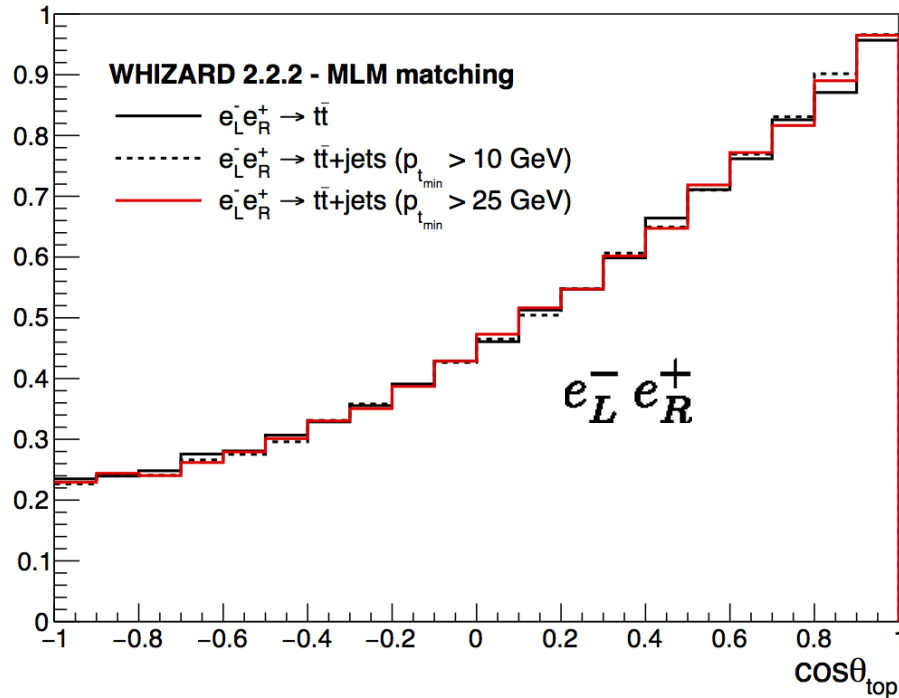


Reconstructed W mass



Reconstructed top mass

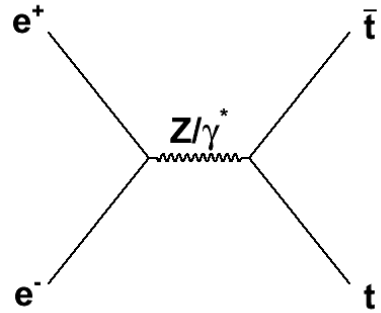
- No notable differences between different matched and unmatched distributions



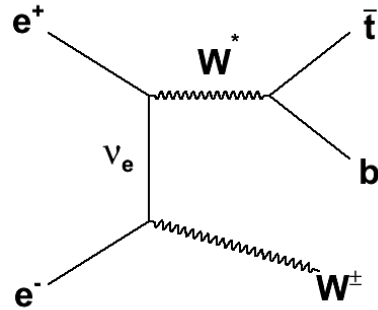
$\sqrt{s}=500 \text{ GeV}$

Difference between inclusive AFB and those with additional jets are small

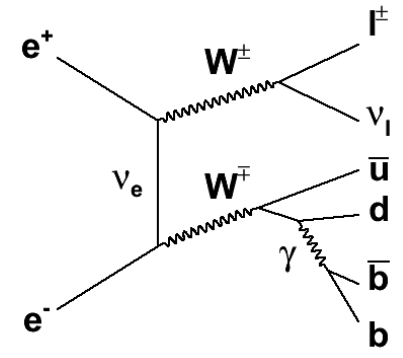
=> Results with WHIZARD 1.95 are sufficiently accurate



Top quark pair production...



...Single top quark production...



...WW γ /Z/h...

...

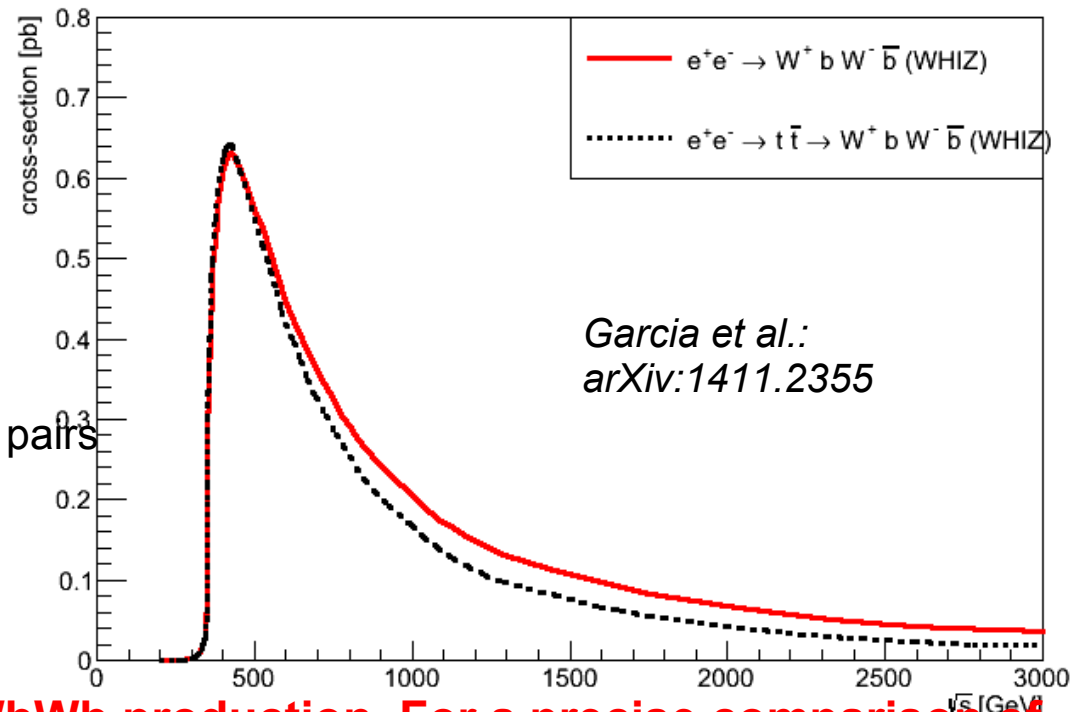
...

Maximum x-section for pair production ~ 0.6 pb
peak well above threshold ~ 420 GeV
300.000 pairs after 4 years at 500 GeV

$e^+e^- \rightarrow WbWb \rightarrow 6$ fermions has several
 non-negligible sources
 (at 500 GeV: $tt \sim 90\%$, single top $\sim 9\%$, $WW\gamma/Z/h \sim 1\%$)

At 500 GeV single top is \sim indistinguishable from pairs

The x-sec for $WbWb$ is 5 to 50% larger than tt



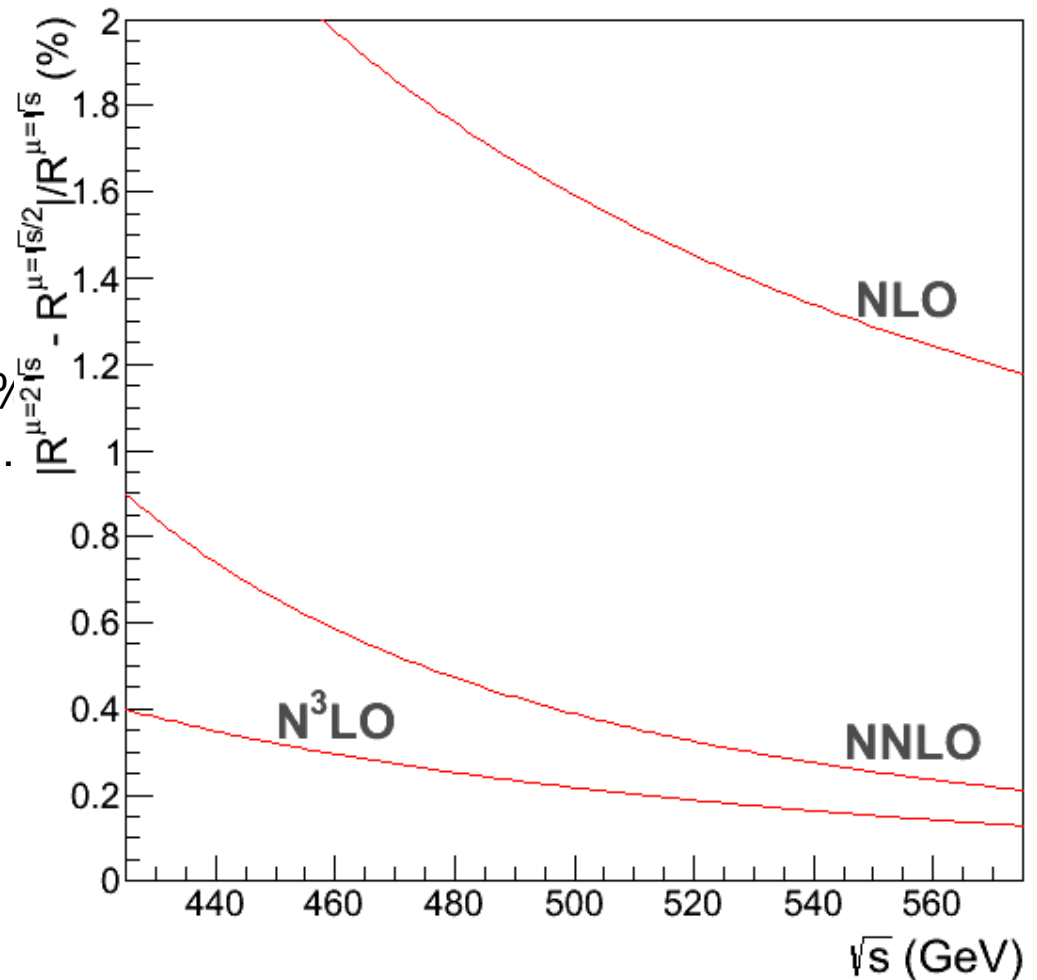
Must measure rate and properties of $WbWb$ production. For a precise comparison of data and prediction more theory work is needed!

Precise calculations exist for $e^+e^- \rightarrow tt$

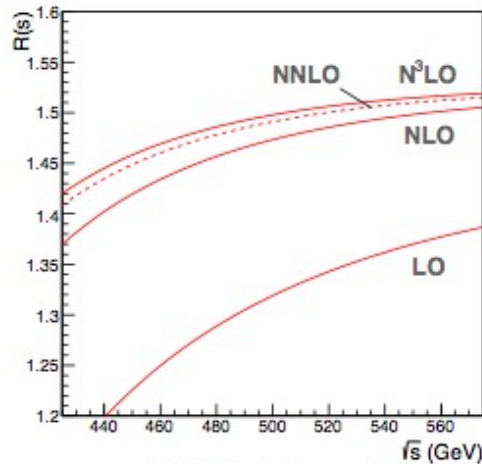
QCD corrections calculated to N²LO
 Scale variations at N³LO estimated at $\sim 0.3\%$
 Electroweak corrections are sizable, though.

LO Monte Carlo exists for $e^+e^- \rightarrow 6$ fermions

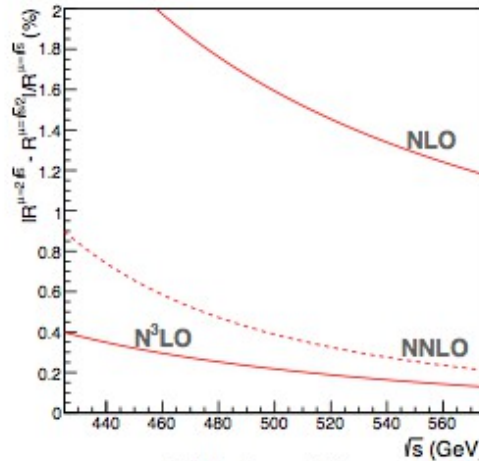
WHIZARD-GoSam may bring this to NLO



*QCD corrections are known up to N³LO



(a) Perturbation series

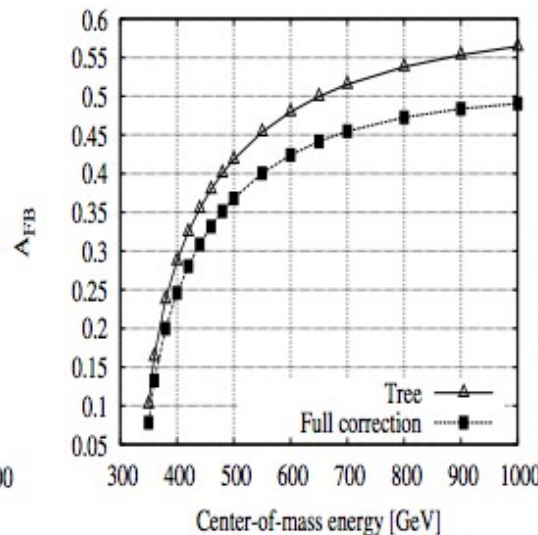
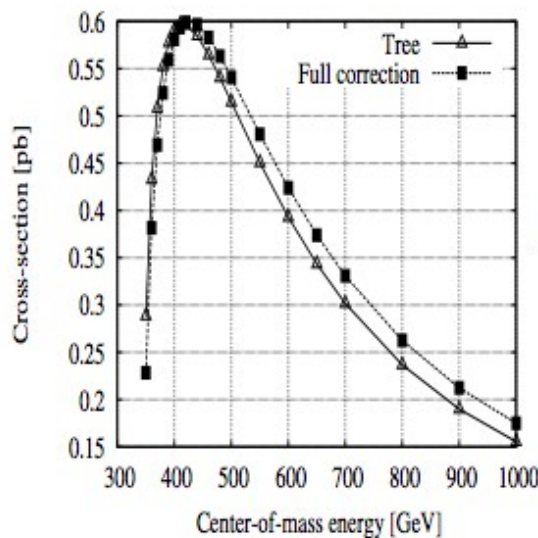


(b) Scale variations

QCD correction (N³LO) is at the per mil level

Kiyo, Maier, Maierhofer, Marquard, NCP B823 ('09)
Bernreuther, Bonciani, Gehrmann, Heinesch, Leineweber, NPB750 ('06)
Hoang, Mateu, Zebarjad, NPB813 ('09)

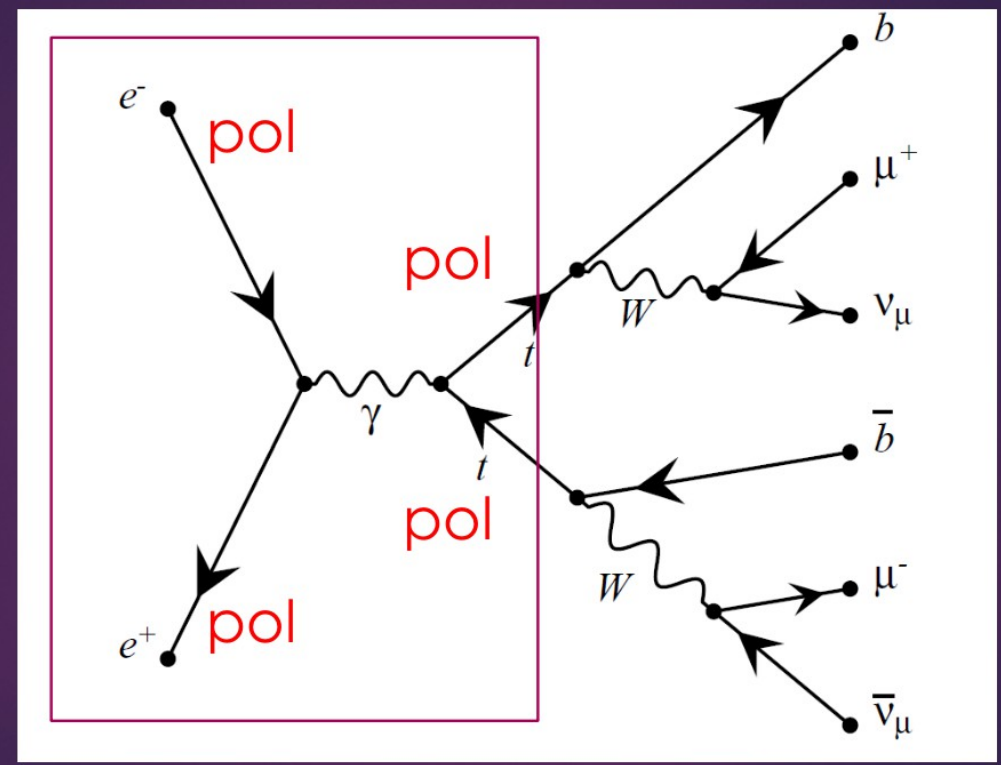
*Electroweak corrections are known at one-loop level



EW correction at one-loop is
~5% for cross section
~10% for A_{FB}

Fleischer, Leike, Riemann, Werthenbach, EJPC31 ('03)
Kheim, Fujimoto, Ishikawa, Kaneko, Kato, arXiv:1211.1112

Elw. Corrections for polarised beams

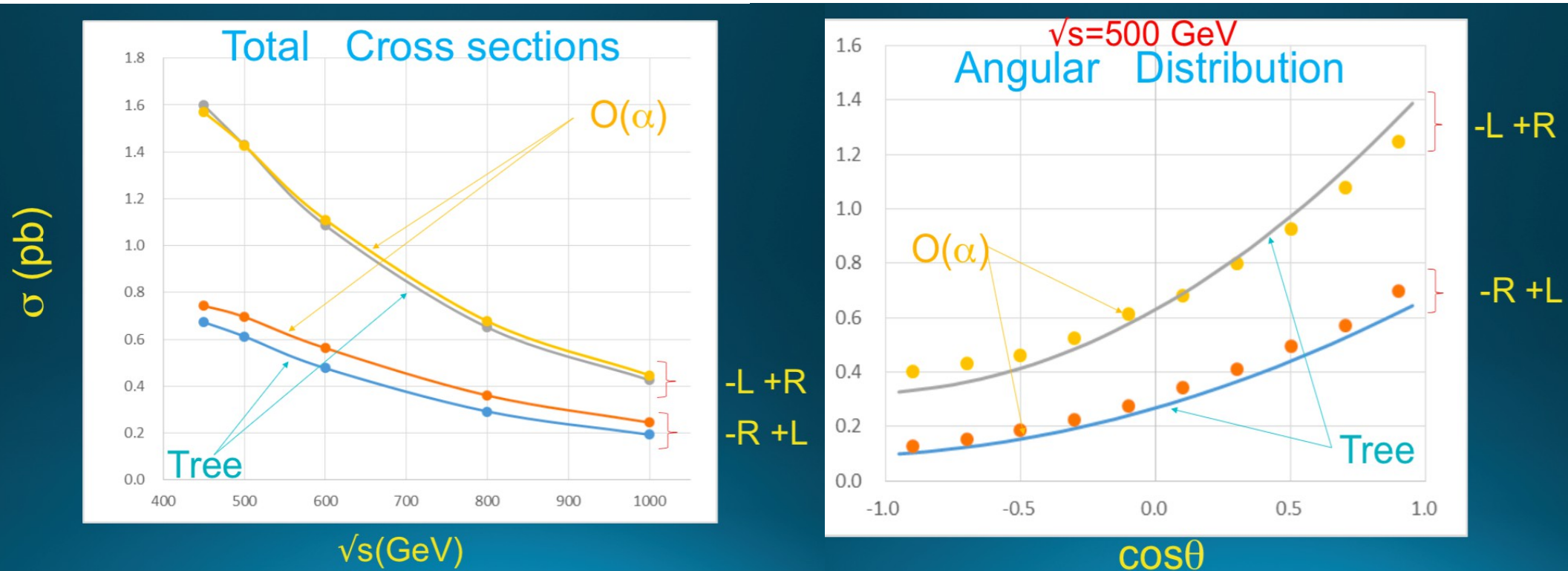


Target:

- $e^+e^- \rightarrow t\bar{t} \rightarrow b\bar{b}f\bar{f}f\bar{f}$ @ ILC
- Full $O(\alpha)$ electroweak corrections
- Beam polarization effects
- Finite width effects of top-quarks
- Matrix elements
- Event generation ?
- $O(\alpha^2)$ electroweak corrections ???

Goal for accuracy < 1%

Collaboration within French-Japanese TYL/FJPPL research programme



- Corrections on x-section more pronounced for: $e_R^- e_L^+$
- Higher orders deform angular distribution: $e_L^- e_R^+$

Beam polarisation essential to disentangle impact/origin of higher order corrections

Future

Decay Loop

Decay-Loop connection

Effects of a top-width

Higher order estimation

- Theoretical uncertainty

- A LC is **the** machine for precision top physics

First machine to produce top pairs in electroweak production!!!
Essential pillar of LC physics program

- Rich program of top quark physics with 'exciting' prospects

- Precision on top mass ~ 50 MeV \Rightarrow 'Final word' on vacuum stability of the universe
- Test of models with extra dimensions and/or compositeness
- Top elw. Measurements are complementary to Higgs coupling measurements

- Exploitation of potential requires huge experimental and theoretical efforts, **Event generators play vital role in the endeavour**

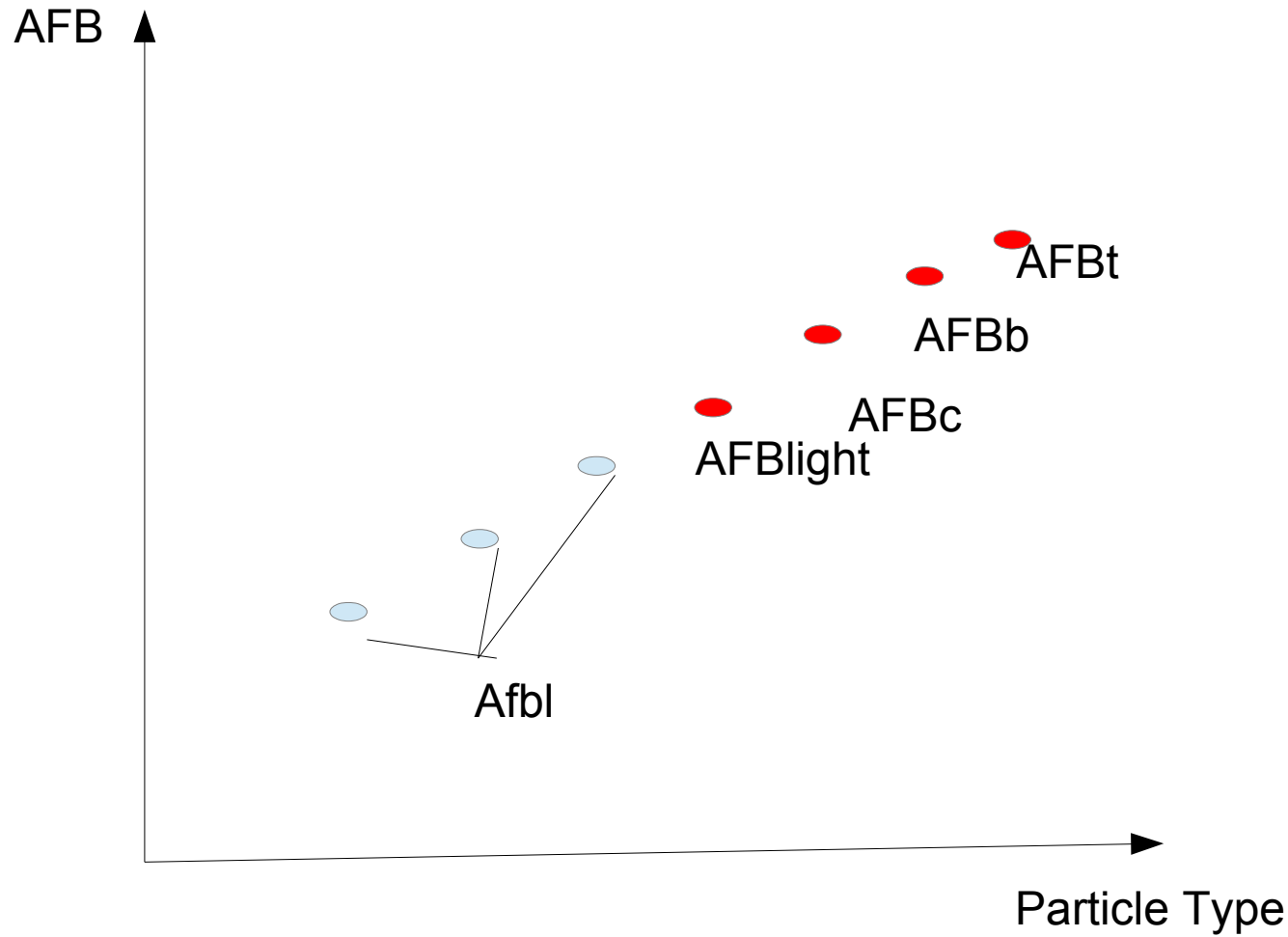
- Theoretical uncertainty on top mass \gg Experimental uncertainty
- Matchin between QCD dominated phase space region and continuum
- $t\bar{t}$ production is in reality six-fermion final state
- Uncertainty of theoretical prediction of AFB
NLO with polarised beams
NNLO would be 10 years of work !!!

3rd workshop on LC Top Physics in Week 27 2015 (Week of 29/6/15)
at IFIC Valencia

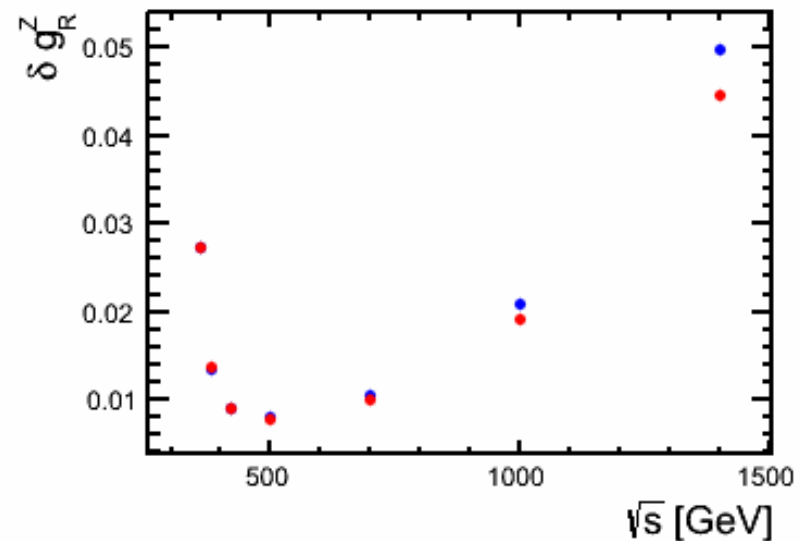
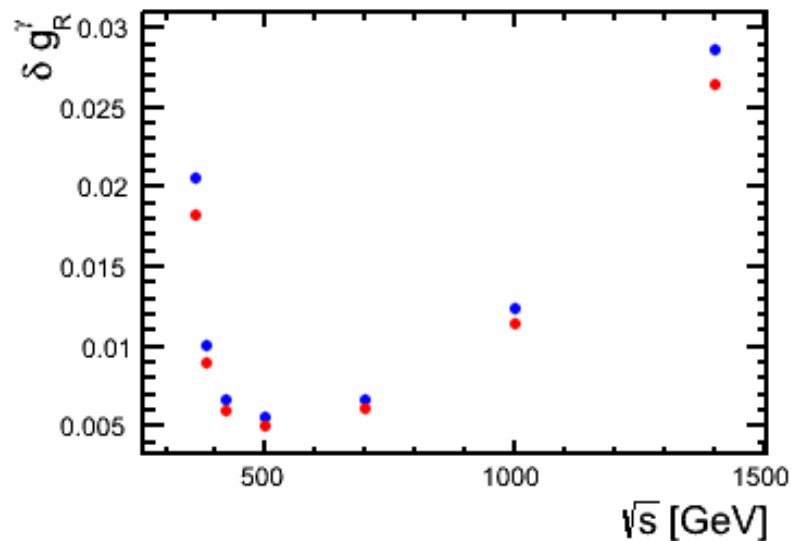
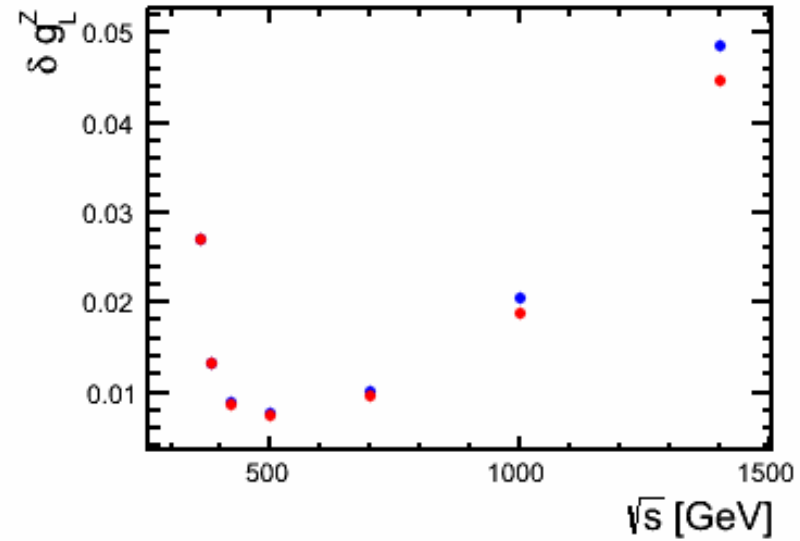
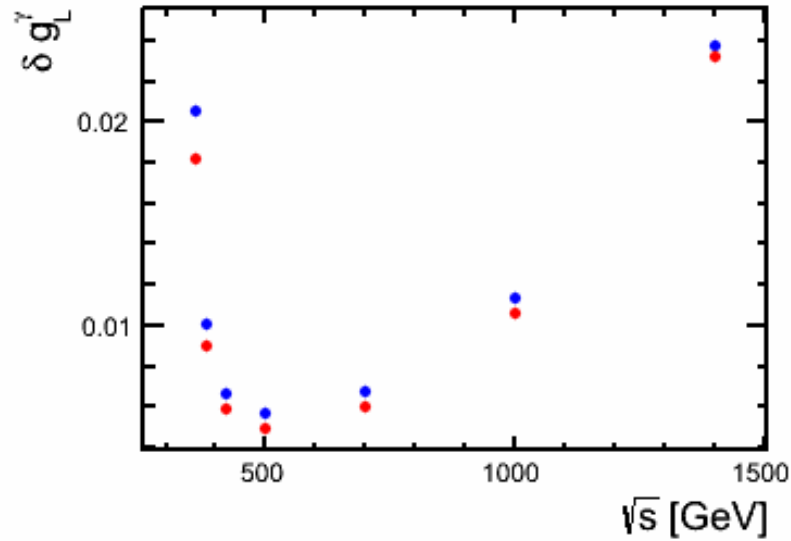
Mark your calendars and stay tuned

Backup

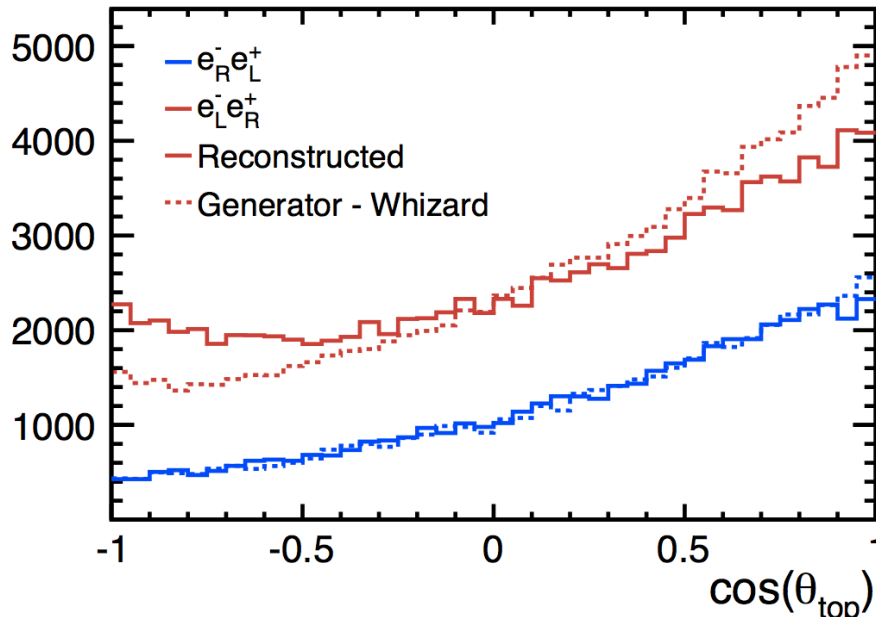
Question to theoreticians: What would you say if in ~two years from now we offer you something like this



The “Higgs plot” for asymmetries



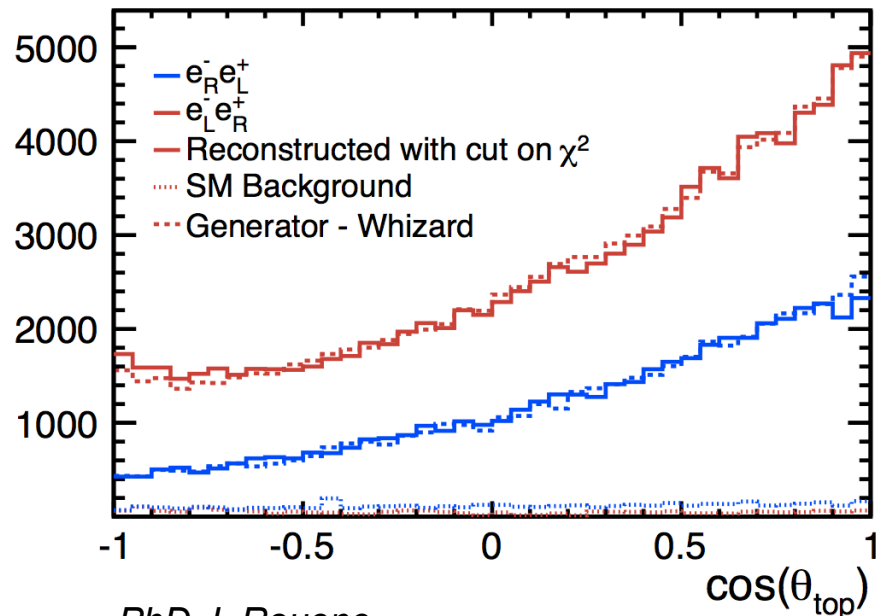
When do we run into QCD uncertainties at small energies?



← Ambiguities in case of **left** handed electron beams
Due to V-A structure at ttX vertex

← Precise reconstruction of θ_{top}
in case of **right** handed electron beams

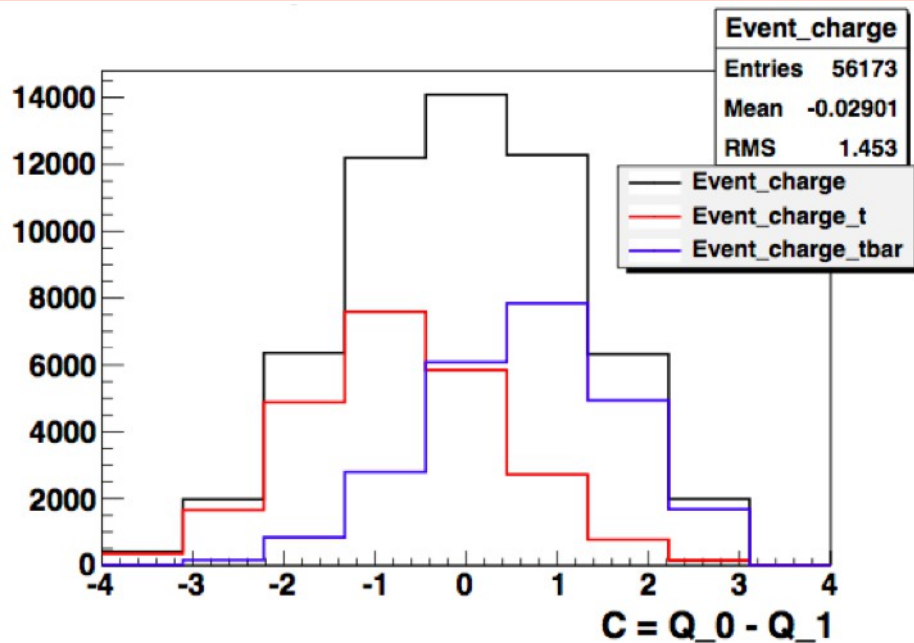
Remedy to address ambiguities:
Select cleanly reconstructed events by χ^2 analysis
or
Reconstruction of b quark charge



Precise reconstruction for both beam polarisations

- Efficiency Penalty for e_L
- ϵ_{tot} : $e_R \sim 50\%$, $e_L \sim 30\%$

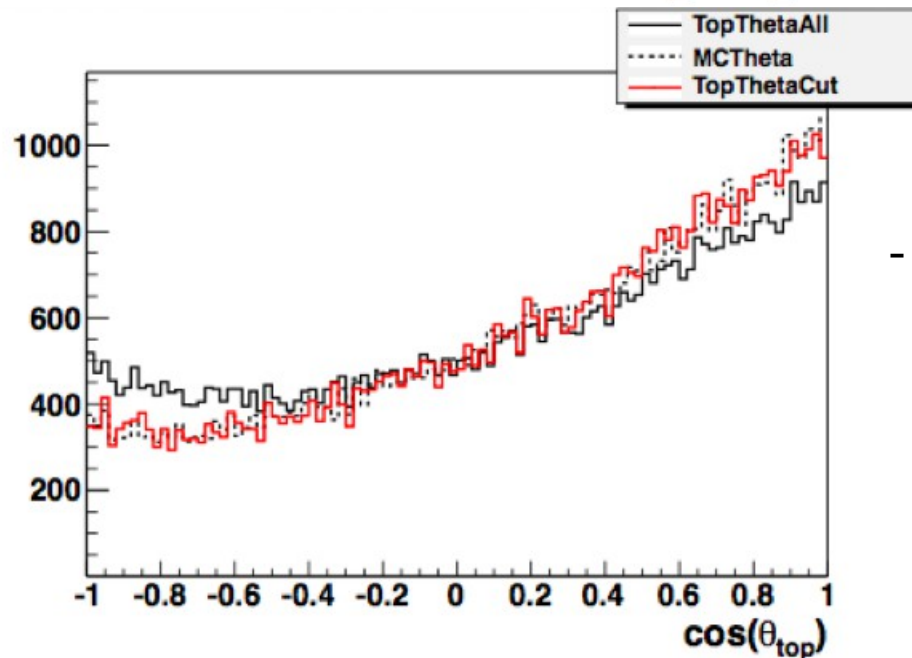
Precision on $A_{FB} \sim 2\%$



Event charge $C = b_1 - b_2$

In SL can compare charge C with lepton charge to select clean sample

Use only events with correct C or $C=0$
(plus another cut on the Lorentz Factor)



- Clean reconstruction of top quark direction
 $\epsilon \sim 30\%$
Will improve with improving charge reconstruction

- b quark hadronises to about

~40% to charged B mesons

~50% to neutral B mesons

~10% to Baryons

=> 64% cases where there is at least one charged b => Should be recognisable

- neutral B mesons decay to about

~ 50% into charged D Mesons => measurable

~ 50% into neutral D mesons

~64% of these D neutral undergo prong decays => charged particles => measurable

=> Out of 36% cases remaining above ~75% can (in principle) be retrieved

=> 91% of the charges from top quark decays lead to signatures that are in principle measurable

Two tasks:

1) Understand why final state with charged B Meson are wrongly reconstructed
Exact fraction depends on final state, looks as if SL is somewhat easier than fully hadronic

2) Tertiary vertices for neutral B Mesons

-> Talks by Sviatoslav and Masakazu

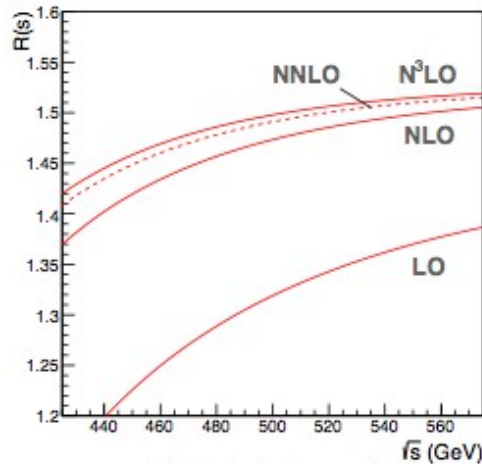
LIA TYL ILC-top (one aspect of it)

$$e^+e^- \rightarrow t\bar{t} \rightarrow \mu^+\mu^-b\bar{b}\nu_\mu\bar{\nu}_\mu$$

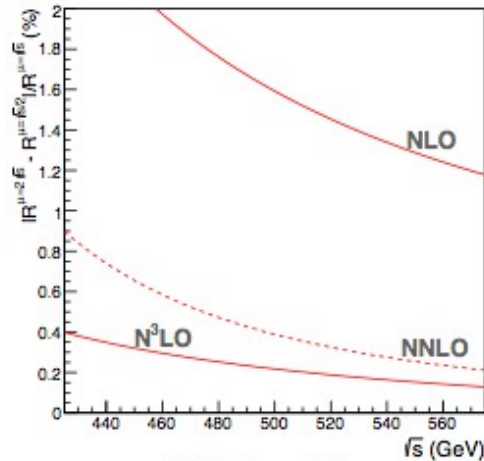
The Matrix Element Method
Conjugate (optimal) variables
Results
Kinematics
Conclusion

See talk by Francois LeDiberder

*QCD corrections are known up to N³LO



(a) Perturbation series

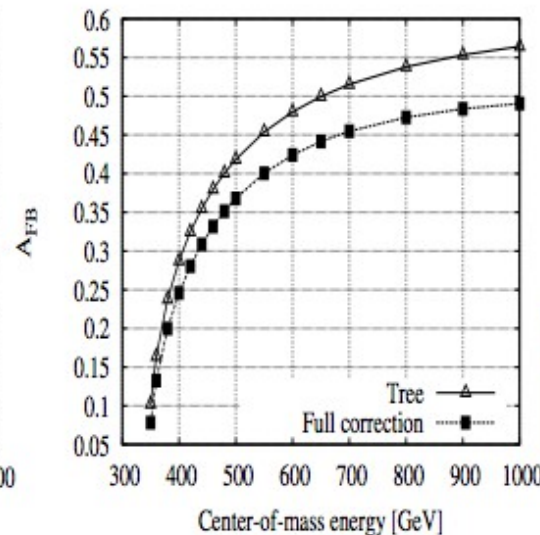
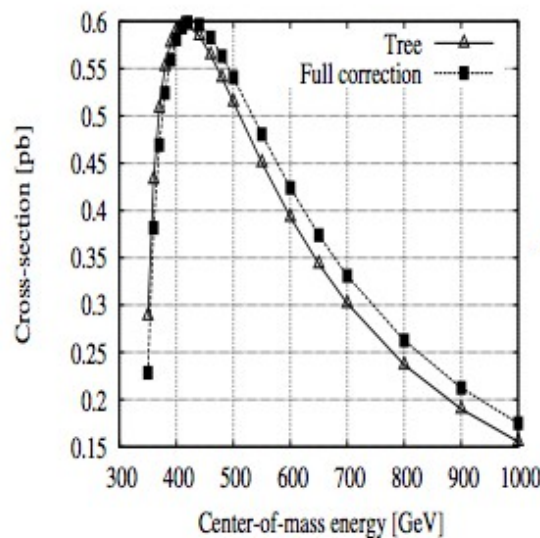


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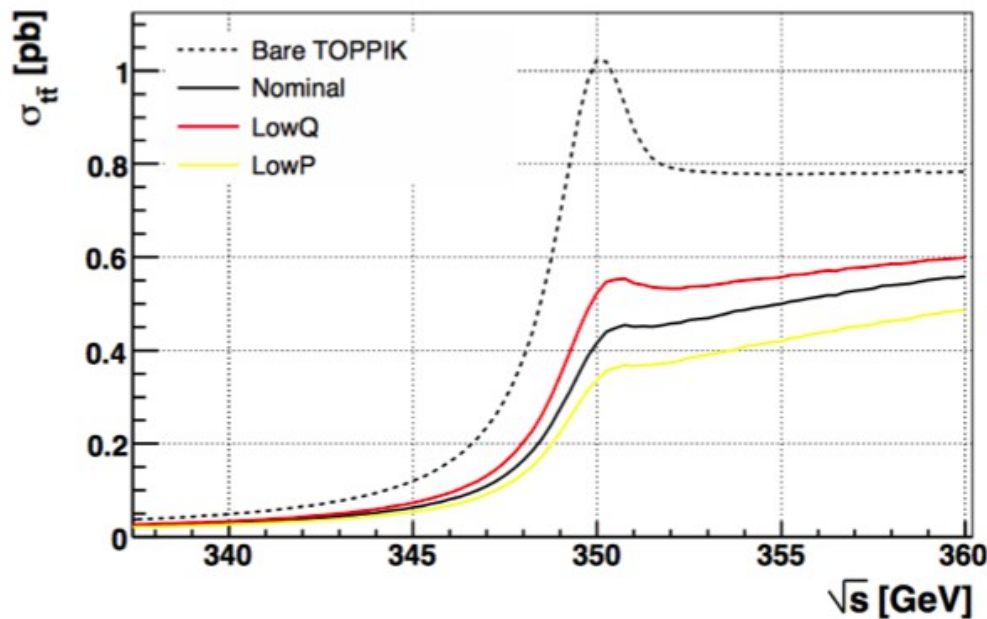


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Fleischer, Leike, Riemann, Werthenbach, EJPC31 ('03)
*Kheim, Fujimoto, Ishikawa, Kaneko, Kato,
arXiv:1211.1112*



- Experimental study of matrix element method (Fully leptonic channel)
- Continuation of fully hadronic channel (would benefit massively from b charge and PiD)
- Studies at 1 TeV and higher (partially done by IFIC)
- CPV measurement at ~380 GeV
380 GeV and > 1 TeV now addressed in CLIC study
- Influence of higher order corrections
Note Spanish Master thesis that claims that elw. NLO are no big deal!
- More on interpretation
Note also studies by Roentsch et al. arXiv: 1501.05939
- Everything that I have forgotten



Principle: m_t from $\sigma_{t\bar{t}}(m_t)$

Advantages:

- ▷ count number of $t\bar{t}$ events
- ▷ color singlet state
- ▷ background is non-resonant
- ▷ physics well understood
(renormalons, summations)
- Top decay protects from non-pert effects

Much of the discriminating power of the approach related to the strong mass-dependence ($t\bar{t}$ resonance).

Peak position very stable in theory predictions (threshold mass scheme).

Typical results:

$$\rightarrow \delta m_t^{\text{exp}} \simeq 50 \text{ MeV}$$

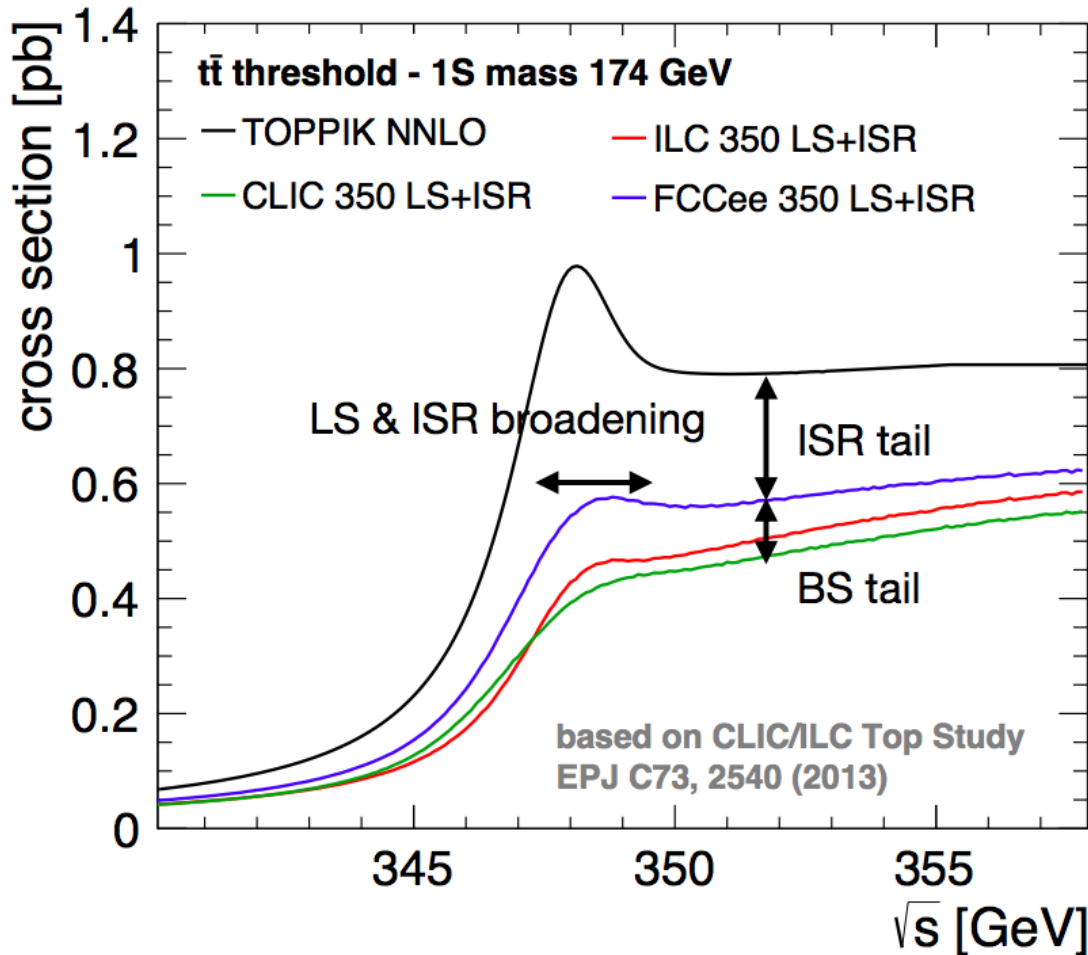
$$\rightarrow \delta m_t^{\text{th}} \simeq 100 \text{ MeV}$$

What mass?

$$\sqrt{s}_{\text{rise}} \sim 2m_t^{\text{thr}} + \text{pert.series}$$

(short distance mass: $1S \leftrightarrow \overline{MS}$)

A. Hoang



- **Initial State Radiation**
Lowers effective L at top energy
- **BeamStrahlung**
Lowers effective L at top energy
Not at FCCee Gaussian spectrum
- **Luminosity spectrum & Initial State Radiation broadening**
Smearing of cross section
Due to beam energy spread
ILC and FCCee comparable
Worse at CLIC

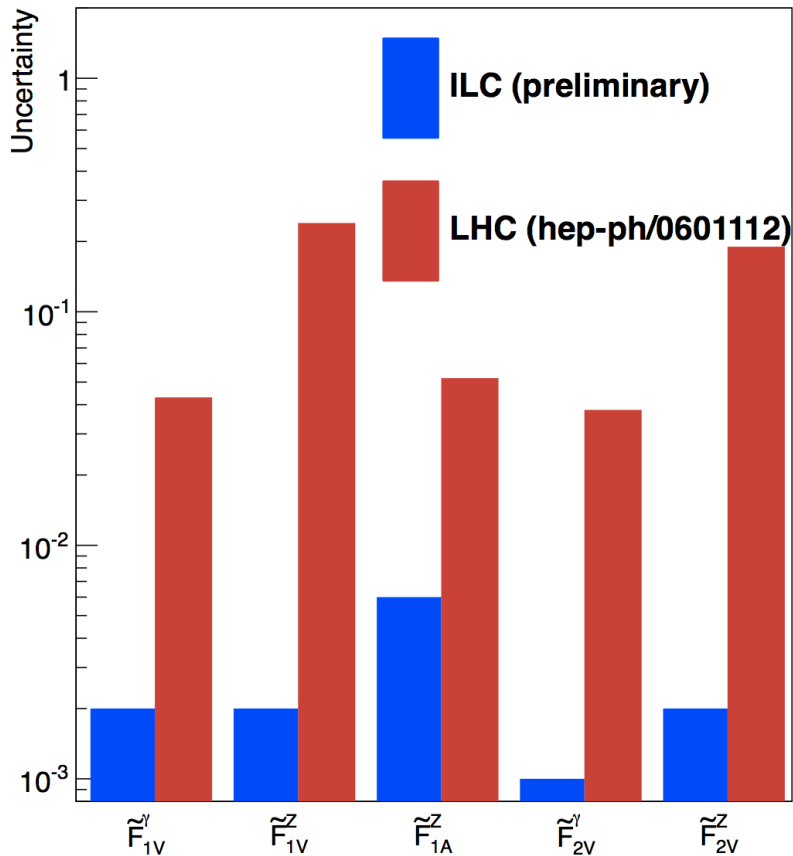
- 1) Main effect on L spectrum is ISR
=> Reduces Luminosity, smears out 1s bound state peak
- 2) LC somewhat smaller L due to BeamStrahlung

Precision: cross section $\sim 0.5\%$,

Precision $A_{FB} \sim 2\%$,

Precision $\lambda_t \sim 3-4\%$

Accuracy on CP conserving couplings

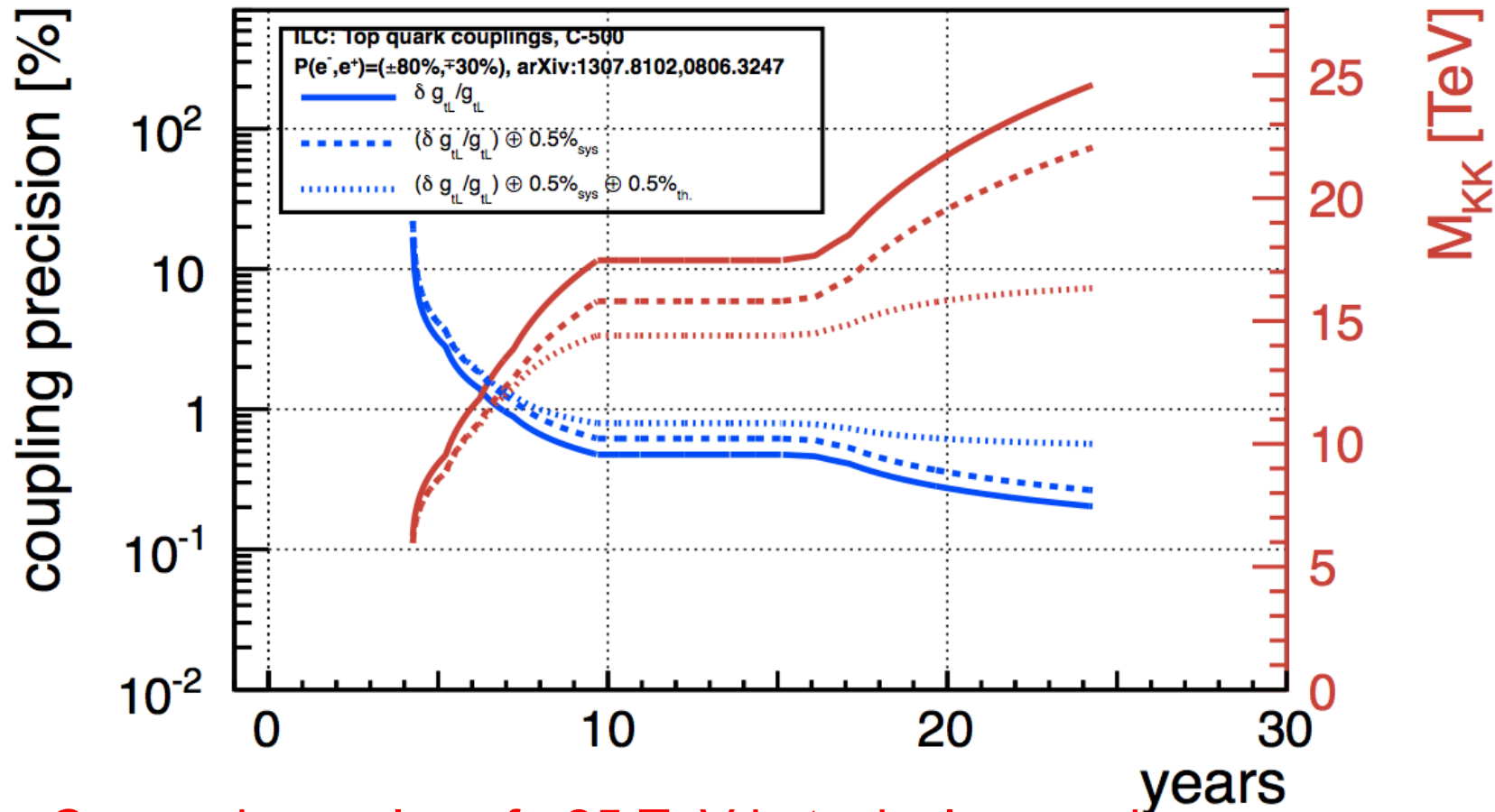


- ILC might be up to two orders of magnitude more precise than LHC ($\sqrt{s} = 14$ TeV, 300 fb^{-1})
Disentangling of couplings for ILC
One variable at a time For LHC
However LHC projections from 8 years old study
- Need to control experimental (e.g. Top angle) and theoretical uncertainties (e.g. Electroweak corrections)
-> Dedicated work has started
- Potential for CP violating couplings at ILC under study

ILC promises to be high precision machine for electroweak top couplings

New physics reach for typical BSM scenarios with composite Higgs/Top and or extra dimensions

Based on phenomenology described in Pomerol et al. arXiv:0806.3247



Can probe scales of ~25 TeV in typical scenarios

(... and up to 80 GeV for extreme scenarios)

=> Important guidance for e.g. 100 TeV pp-collider