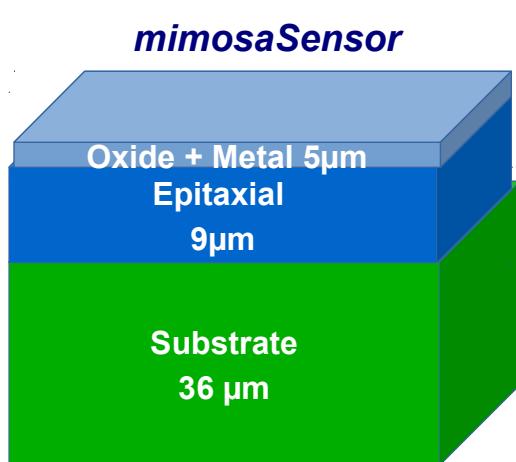


Alignment of double sided ladders and mini-vectors

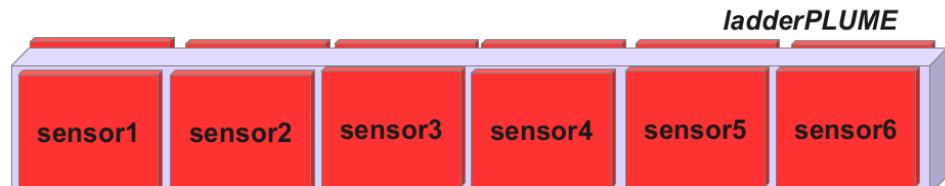


IPHC : PICSEL group - Strasbourg

COUSIN Loïc

PhD Student

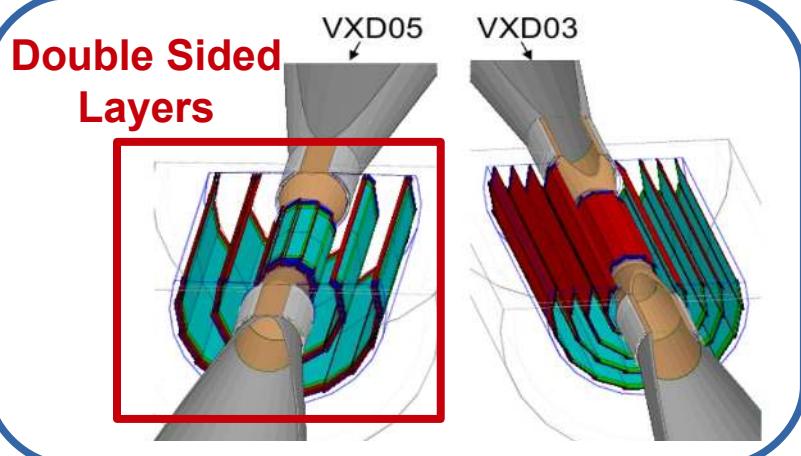
loic.cousin@iphc.cnrs.fr



Outline

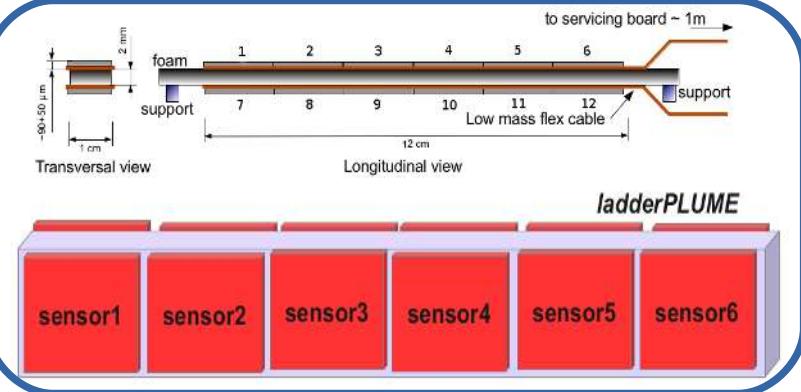
■ Motivations for double sided setup

- ↳ ILC
- ↳ Double sided layers
- ↳ Mini-vectors



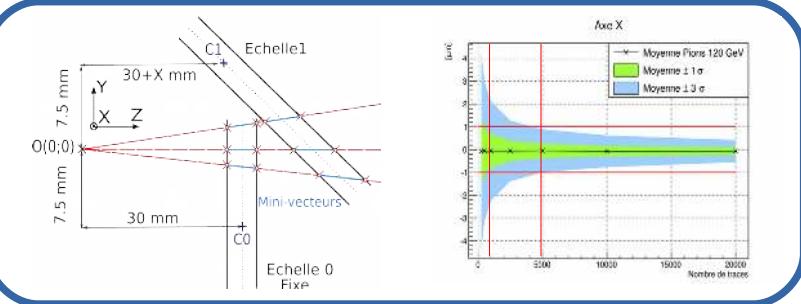
■ Simulations of double sided ladders

- ↳ Tools :
 - GEANT4
 - Charge carriage tool
 - Digitizer



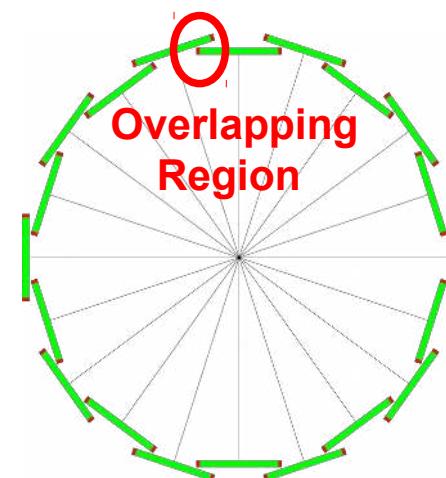
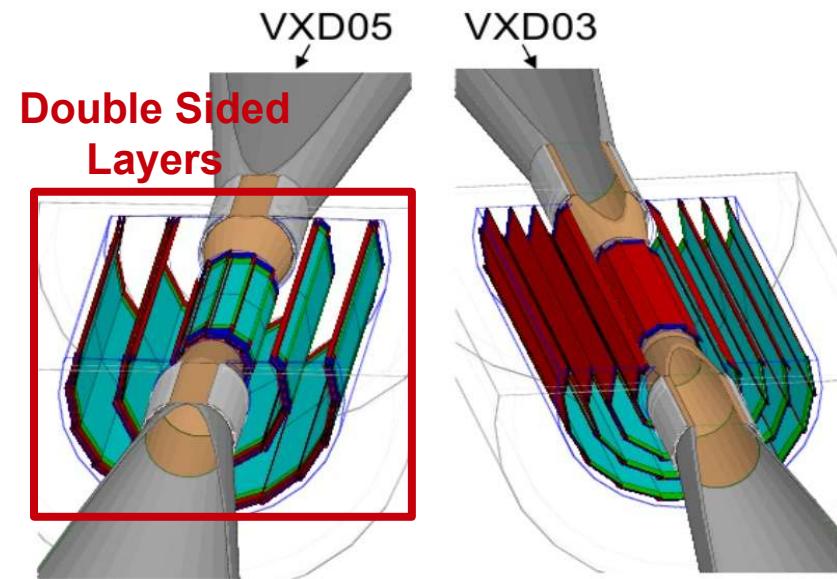
■ Alignment

- ↳ Local alignment of ladders
- ↳ Local alignment on the **overlapping region** of two **double sided layer**

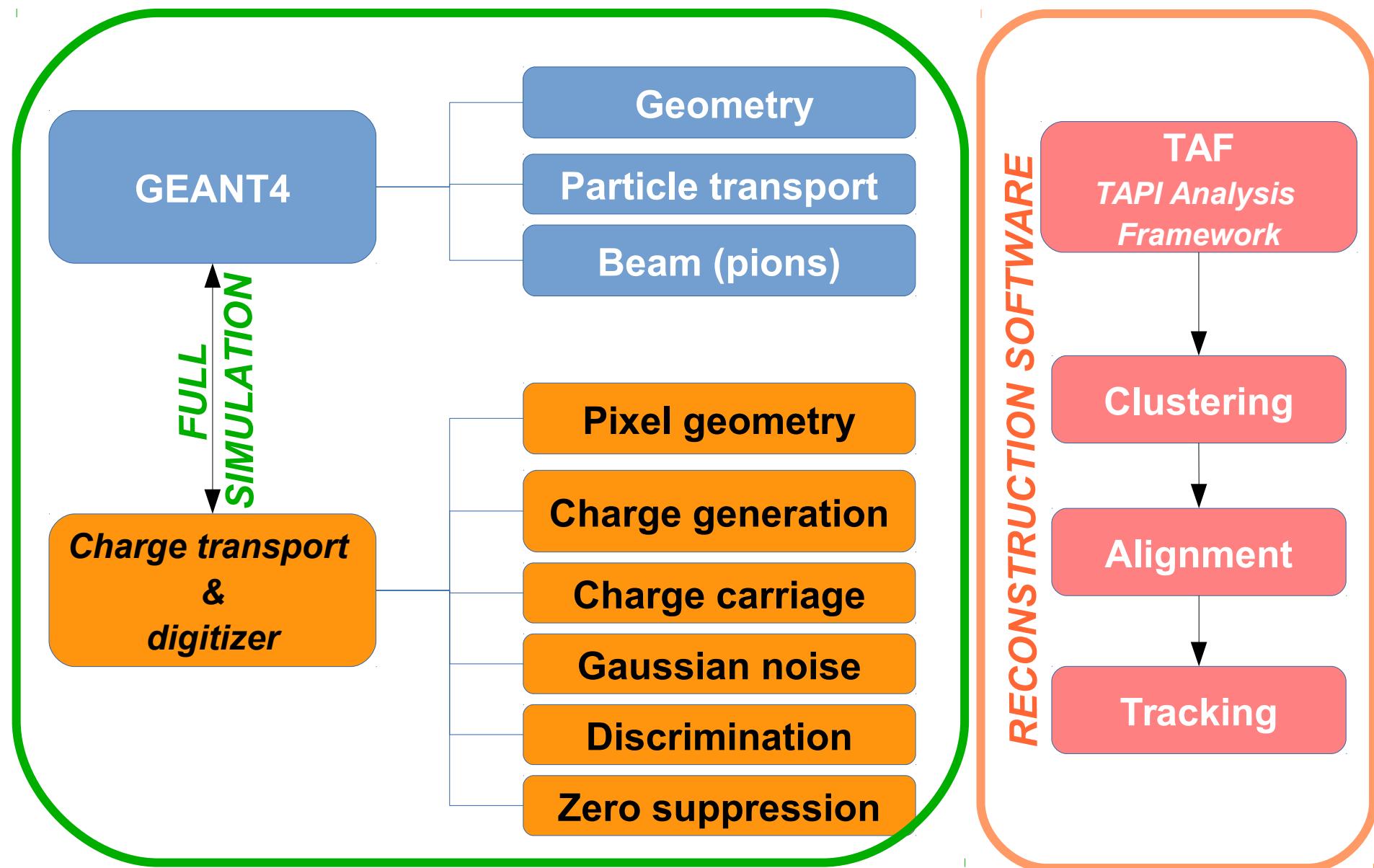


Motivations for double sided setup

- Context : ILC Vertex detector
- Geometry of the vertex detector :
 - ↳ 5 single layers OR 3 double sided layers.
- Focus on 3 **double sided layers**
 - ↳ **Material budget reduction.**
 - 1 support for 2 layers.
 - ↳ **1 track → 2 hits → 1 mini-vector**
 - ↳ **Mini-vectors : potential improvement on pattern recognition**
- Goal : Standalone alignment on the overlapping region of two consecutive ladders in the same double layer.
- Tool : **Geant4 simulation**
 - ↳ Sensor simulation
 - ↳ Double sided ladder simulation



Tool : DigiCMOS (GEANT4) + TAF (Reconstruction)



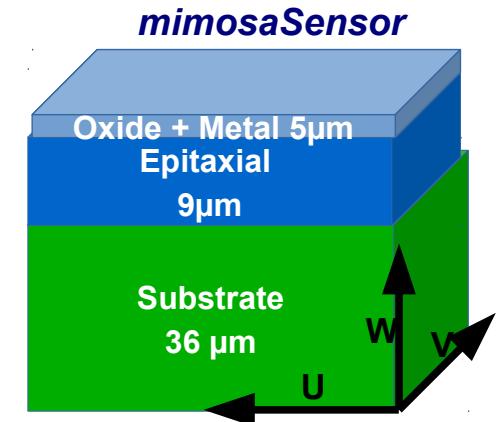
Simulation : GEANT4

■ CMOS sensors with GEANT4 :

- ↳ MIMOSA sensors : 3 layers design
 - Substrate layer (silicon) + Epitaxial layer (silicon) + Oxide+Metal layer
 - Total thickness = 50 μm
- ↳ Energy deposition { Landau ($\text{MPV} = 80\text{e-}/\mu\text{m}$) }
- ↳ Geometry modules :
 - Single sensor (MIMOSA-28 like)
 - Single and double sided ladders (PLUME)
 - Modular tool : New modules for a new geometries.
- ↳ Charge carriage & digitizer for MIMOSA-28 sensors (DIGMAPS)

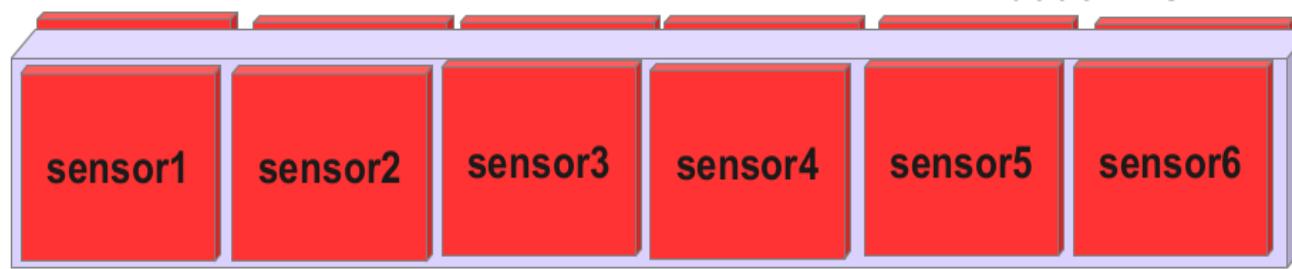
■ Double sided ladder simulation : PLUME ladder (Pixel Ladders with Ultra-low Material Embedding)

- Built with **12 sensors** MIMOSA-28 like, 6 per side
- Gap between two sensors = 420 μm
- Support = **2 mm SiC** (Density 8 %)
- **Spatial resolution = 3.5 μm** (normale incidence)



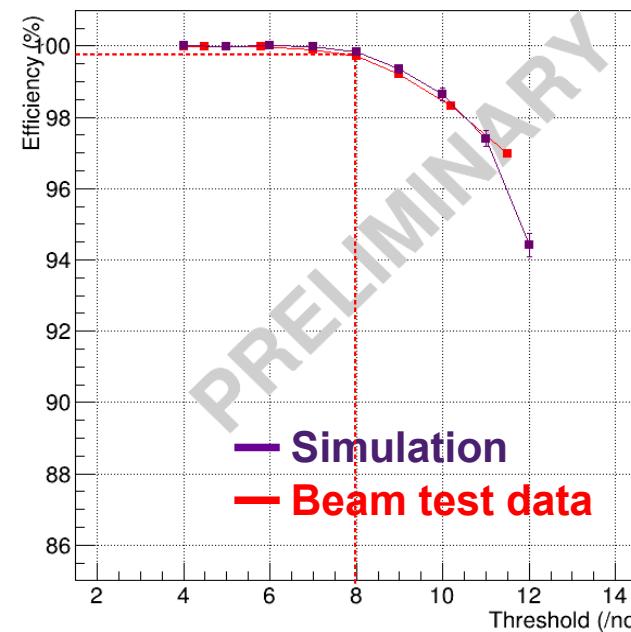
CMOS sensor simulated geometry

Real PLUME Ladder : 12 MIMOSA-26 Simulation : 12 MIMOSA-28 like (No digitizer available for MIMOSA-26 sensors)

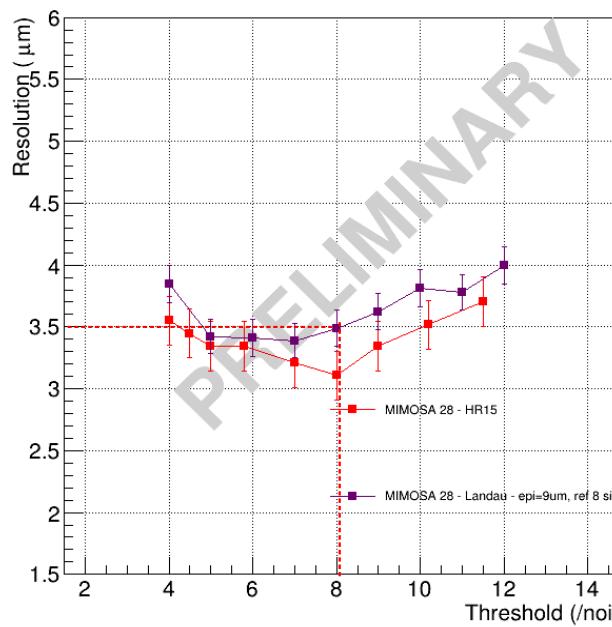


Simulation tool performances

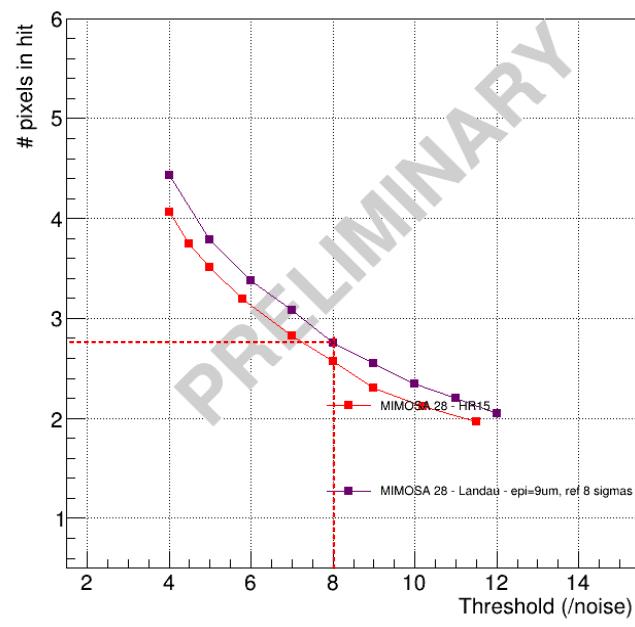
Efficiency vs Threshold



Resolution vs Threshold



Pixel multiplicity vs Threshold



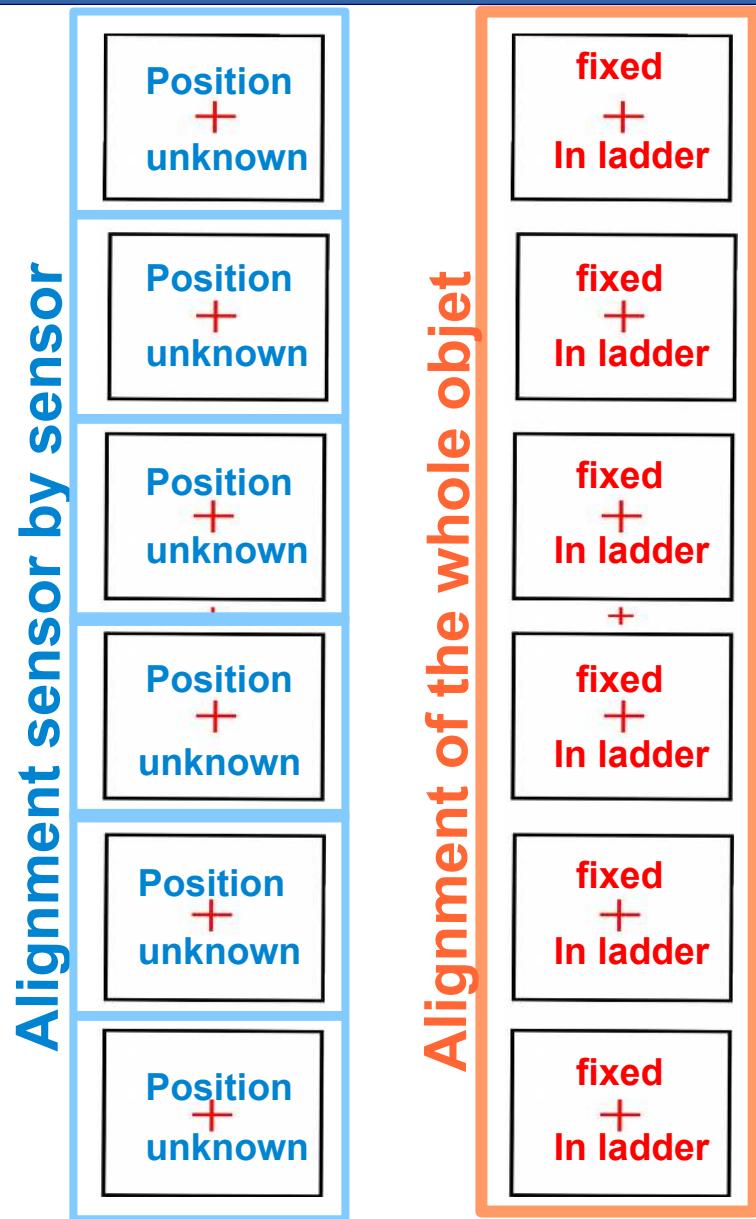
- Data based charge carriage (Due to unknown on epi thickness, dopage profil, etc...)
- Fine tuning of simulation parameters (Energy distribution, epitaxial layer, charge transport, etc...)
- Binary output (comparison with a threshold) + Zero suppression

Results :

- ↳ Comparison between simulation and test beam data of MIMOSA 28 HR15.
- ↳ **Data and simulation agreement better than 10 % (10 % for multiplicity).**
- ↳ **Single sensor model response validated.**
- ↳ Spatial resolution = **3.5 μm** (Normale incidence) | Efficiency > 99.5 %
- ↳ Mean Cluster Mult.= **2.8 px** (Normale incidence)

Alignment

- **TAF** : Framework for *test beam analysis* and *simulated data analysis*.
- *Alignment of composite objects* like PLUME ladders or SALAT planes
- 2 possible strategies of alignment :
 - ↳ *Alignment sensor by sensor* in a composite object
 - ↳ Return each sensor tilts and positions
 - ↳ *Alignment of the whole object*
 - Relative sensor position well known.
 - Return object tilts and positions
 - Already used in SALAT beam test analysis.
- Alignment description :
 - ↳ *Track based alignment* (straight tracks).
 - ↳ *Local Chi² alignment*.
 - ↳ $\chi^2 = \text{sum}(\text{residuals}(x,y,z)^2 / (\text{resolution}(x,y,z)^2))$ over tracks
 - ↳ χ^2 minimisation (ROOT : Minuit)



Alignment with mini-vectors

■ Alignment with mini-vectors

- ↳ On the *overlapping region* of two consecutive ladders
- ↳ First studies of tracking with mini-vectors → efficacy improvement at low momentum (See Georgios Voutsinas, DESY).
- ↳ **Potential improvement on pattern recognition at low momentum**
- ↳ **Idea : Standalone alignment with mini-vectors**

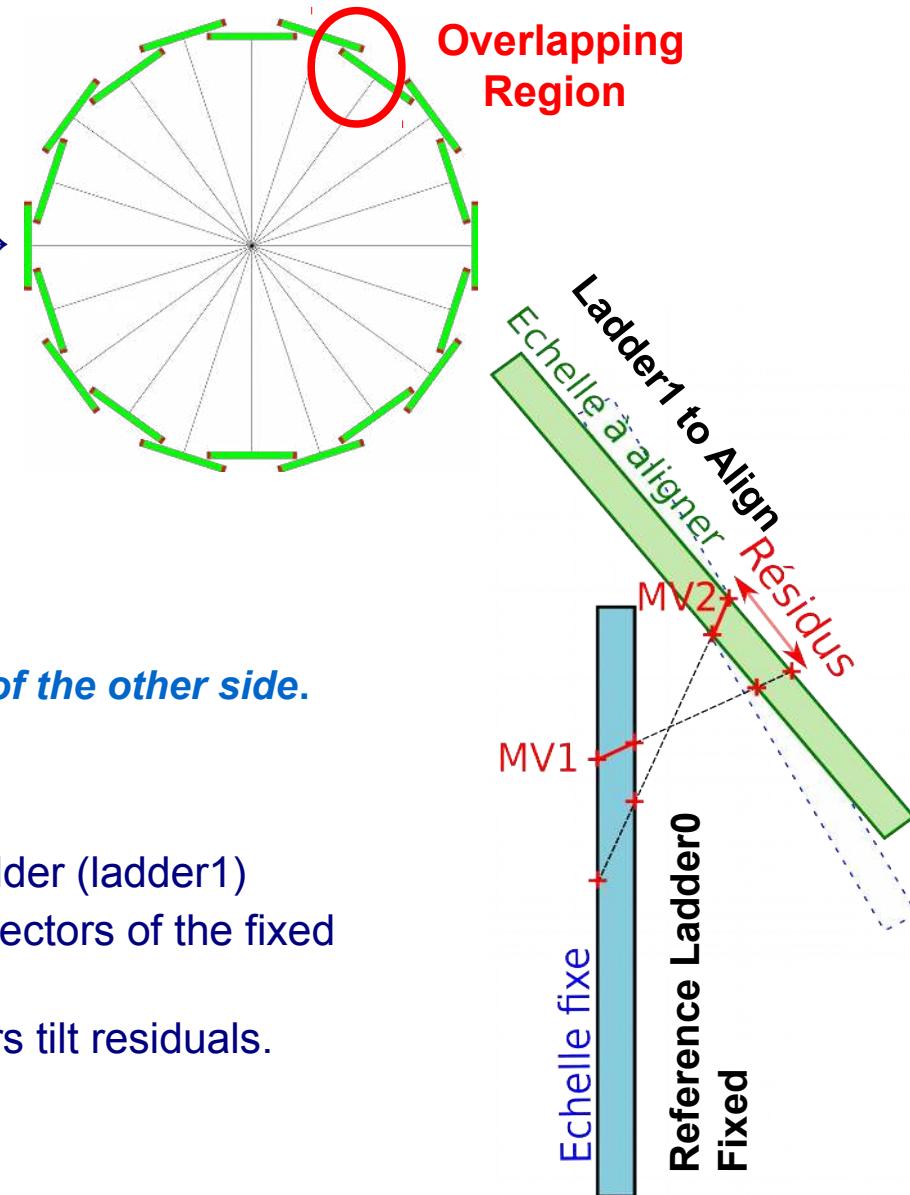
■ Reconstruction of mini-vectors

- ↳ A *hit on the first side* with the *closest hit of the other side*.

■ Method of alignment with mini-vectors

- ↳ On the **overlapping region (OR)**.
- ↳ Fixed reference (ladder0) + Misaligned ladder (ladder1)
- ↳ Spatial residuals = Projection of the mini-vectors of the fixed ladder on the other ladder
- ↳ Residuals = spatial residuals + mini-vectors tilt residuals.
- ↳ Alignment = Chi2 Minimisation.

■ Let's see the statistic ...



Statistic (Order of magnitude only)

- Order of magnitude for Statistic for 1 Overlapping Region

- We want a minimum increase of material budget so :

↳ 1 OR = 5 % Ladder Surface

- Hard processes

↳ $L = 1.8 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

↳ $e^+ e^- \rightarrow \mu^+ \mu^-$ (500 GeV) : Around $1400/2800 \mu$ per Year / OR

↳ $e^+ e^- \rightarrow q\bar{q}$ (500 GeV) : $8000/16000$ particles per Year / OR

- Very Optimistic : **Beamstrahlung** (see after)

↳ Around $7500/20000 e^-/+$ per Hour / OR

↳ But Low Momentum particles in a magnetic field

- **GigaZ option**

↳ $L = 10^{33} \text{ cm}^{-2} \text{ s}^{-1} \rightarrow 10^9/\text{Year}$

↳ Example : $Z \rightarrow \mu\mu$ (3.5%) + $Z \rightarrow ee$ (3.5%)

↳ Around $15000/25000$ particles per Month / OR

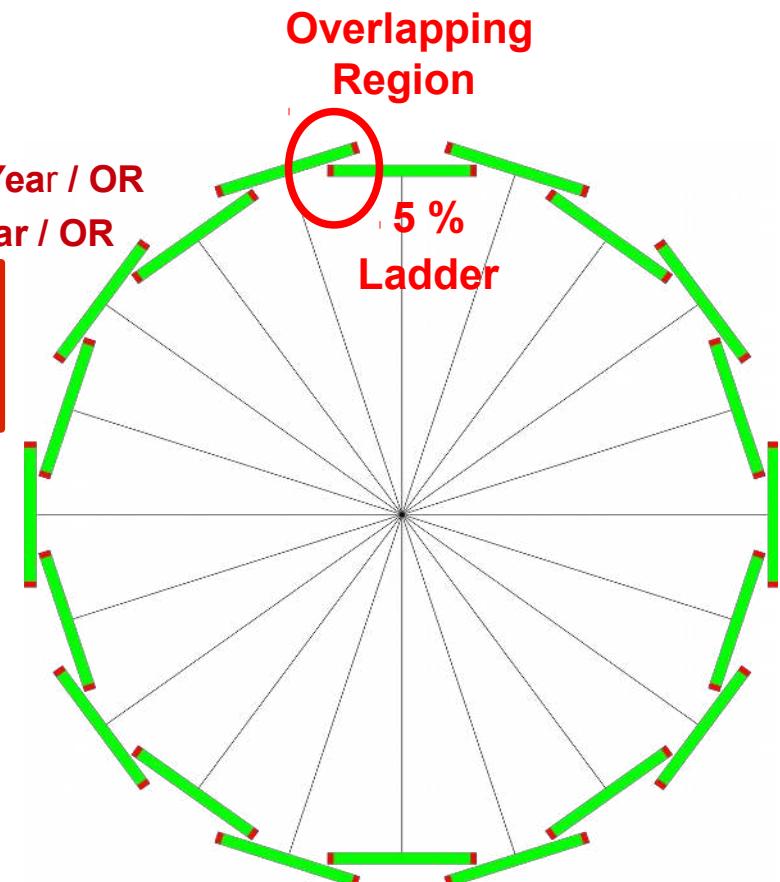
- **Photon collider option**

↳ $L = 10^{34} \text{ cm}^{-2} \text{ s}^{-1} / 500 \text{ GeV}$

↳ Ex : $\sigma(\gamma\gamma \rightarrow \mu^+\mu^-\mu^+\mu^-) \approx 150 \text{ pb}$ (TDR Tesla)

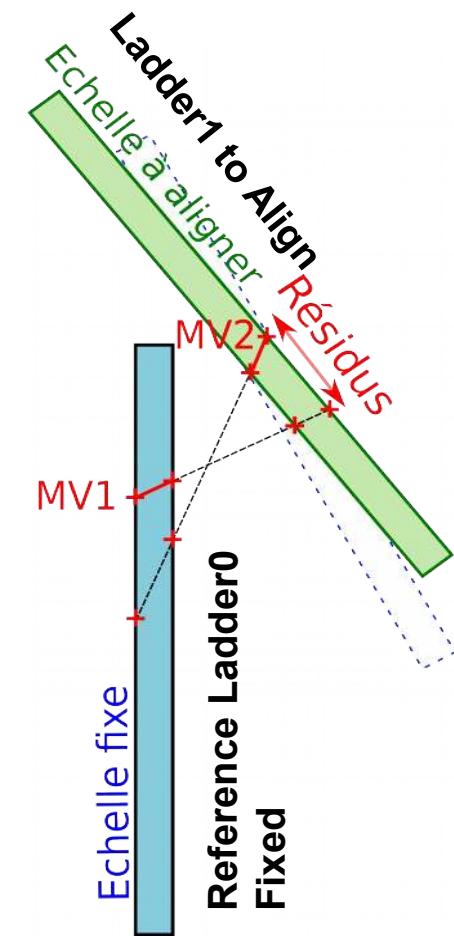
↳ Around $40000...80000 \mu$ per Month / OR

- Sum of tracks from different processes



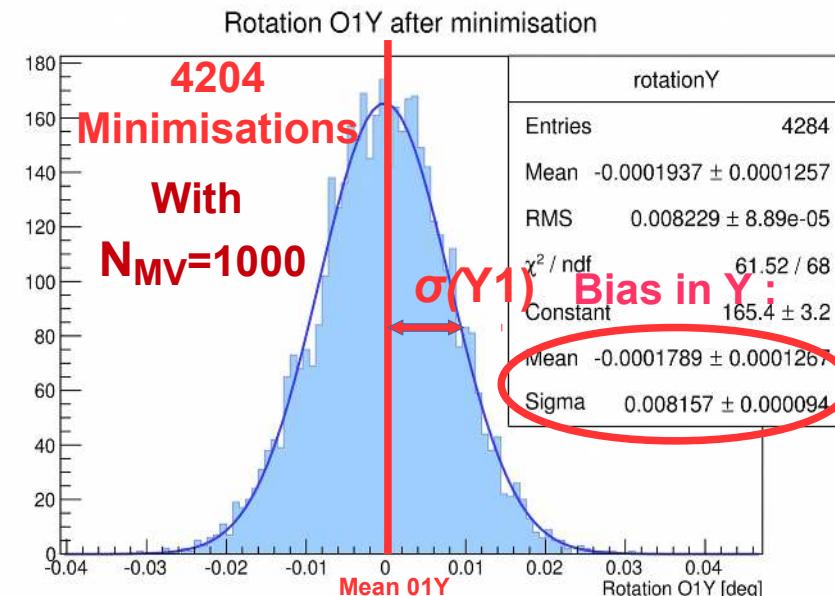
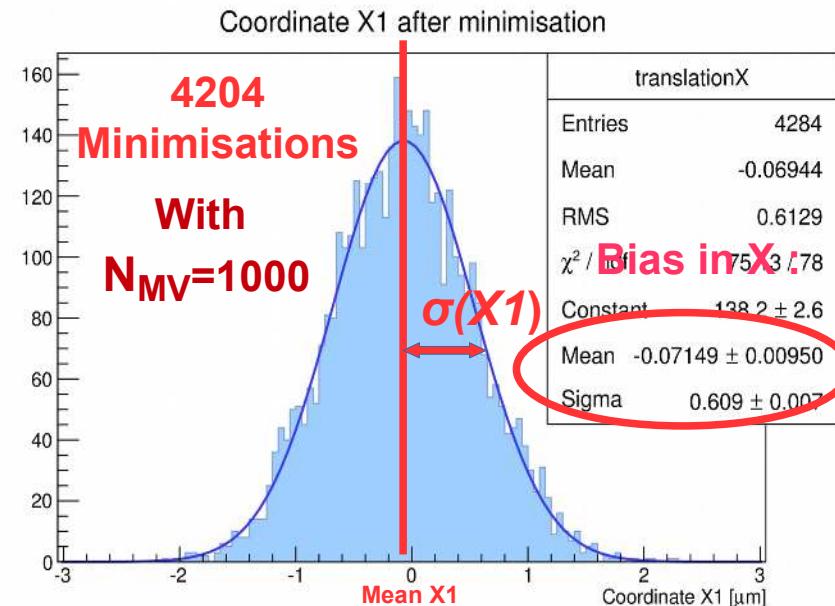
Configuration : Pions High Momentum (120 GeV/c)

- Alignment with mini-vectors : Step 1 = Proof of principle with high momentum particles.
- Relative tilt between ladders = **30 deg** (Rotation X)
- OR \approx 10 % Ladder size
- Beam
 - ↳ Negative pions 120 GeV/c
 - ↳ Distributed in a cone
 - Vertex position O(X,0,0) : random position in X axis
 - Opening angle = Random[0,15] deg
- Mini-vectors association
 - ↳ 2 mini-vectors in the overlapping region.
 - ↳ Association by pairs before minimisation
 - ↳ Proof of principle with **Perfect associations** of mini-vectors
- Monte Carlo position of ladder 0 (fixed) and 1 (ladder to align) :
 - ↳ $O_0(X_0,Y_0,Z_0) = (0-7500,30000) \mu\text{m}$
 - ↳ $O_1(X_1,Y_1,Z_1) = (0,7500,35000) \mu\text{m}$
- Relative Monte Carlo Rotations between ladder 1 and ladder 0 :
 - ↳ **RotX = 30 deg, RotY = 0 deg, RotZ = 0 deg**



Alignment with mini-vectors : alignment precision

- Alignment with 6 degrees of freedom
 - ↳ 3 Translations : X, Y, Z,
 - ↳ 3 Rotations : Rot X, Rot Y, Rot Z
- Initial misalignment :
 - ↳ Translations of the center O1 (Ladder 1)
 $\Delta X = +200 \mu\text{m}$, $\Delta Y = -200 \mu\text{m}$, $\Delta Z = +200 \mu\text{m}$
 - ↳ Rotations about the center O1 :
 $\Delta \text{Rot}X = +0.5 \text{ deg}$, $\Delta \text{Rot}Y = -0.5 \text{ deg}$,
 $\Delta \text{Rot}Z = +0.5 \text{ deg}$
- Estimation of the alignment precision :
 - ↳ ***N minimisations*** with ***different samples***
 - ↳ ***N_{MV} mini-vector pairs*** per sample.
- For each variable after 1 minimisation → 1 entry in each histogram (6 DoF = 6 Histos).
- **Bias = (Histogram Mean - Monte Carlo Values)**
- **Precision = Histogram Width (1 σ)**



Parameter X1

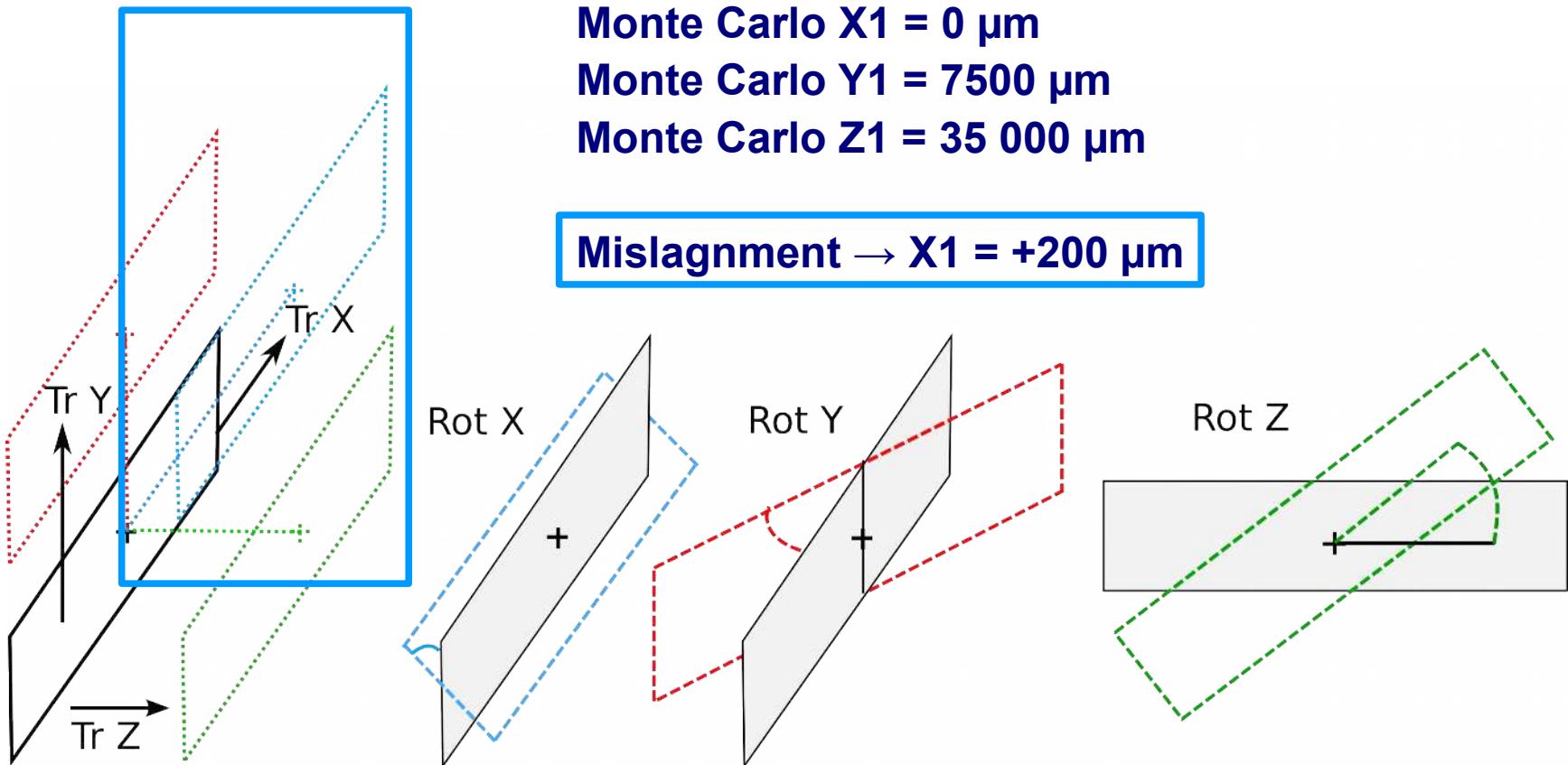
Translation Center O1(X1, Y1, Z1)

Monte Carlo X1 = 0 µm

Monte Carlo Y1 = 7500 µm

Monte Carlo Z1 = 35 000 µm

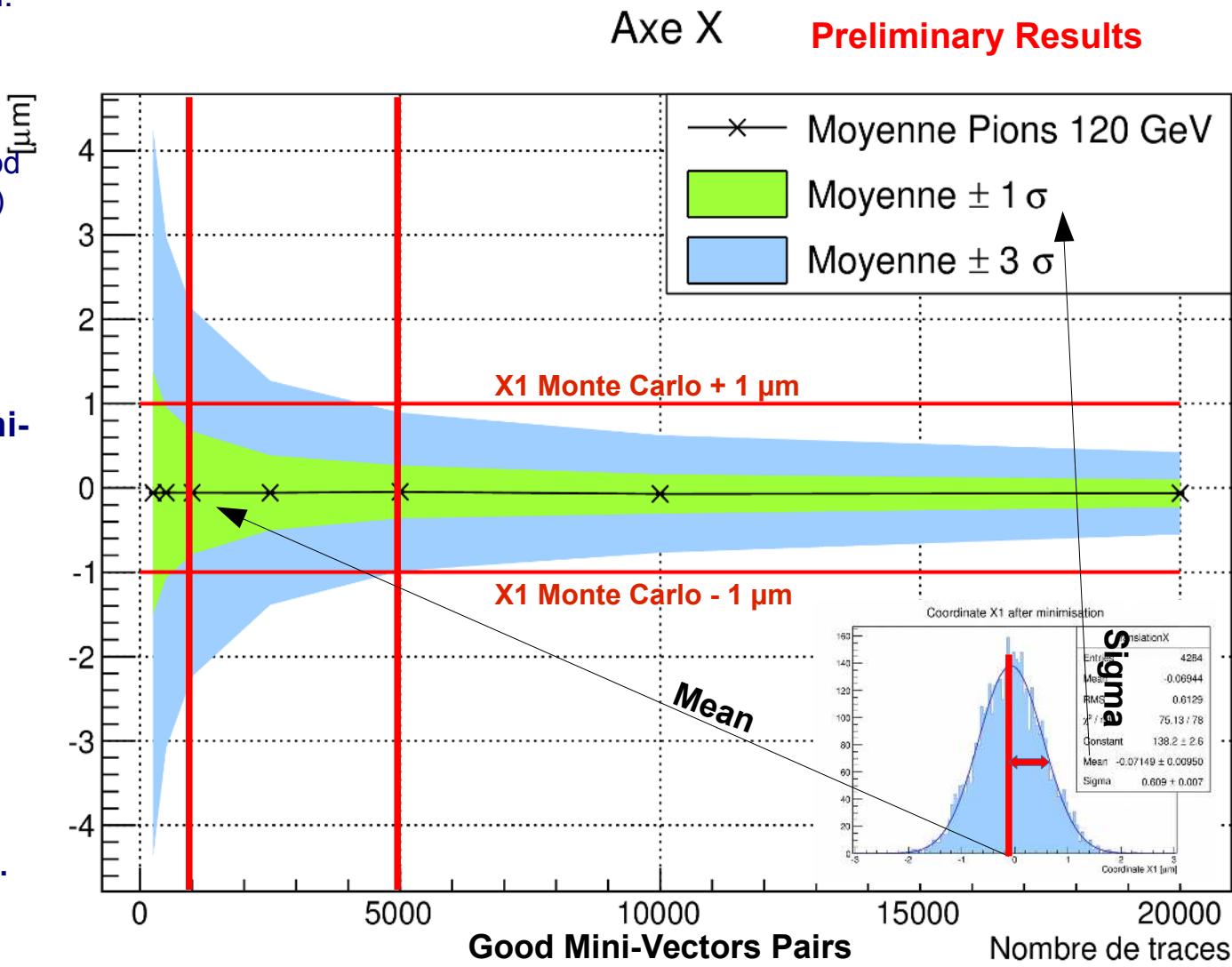
Misalignment → X1 = +200 µm



Alignment with mini-vectors : Results

Position after minimisation in function of statistics

- Ladder Center X1 position:
 - ↳ Mean vs statistic (deviation from MC values)
 - ↳ Width vs statistic (method precision : $\pm 1\sigma$, $\pm 3\sigma$.)
- Starting from **1000** good pairs of mini-vectors
 - ↳ *precision (1σ) better than $1\mu\text{m}$*
- ≤ 5000 good pairs of mini-vectors
 - ↳ *Precision (3σ) better than $1\mu\text{m}$*
- Y1 Position :
 - ↳ Similar results
- Z1 Position
 - ↳ Bias = $-10\mu\text{m} \rightarrow$ weak mode
 - ↳ Bias reduction \rightarrow increasing tiltY of MVs.
 - ↳ New Precision (1σ) < $2\mu\text{m}$ with **1000** mini-vector pairs



Parameter RotZ

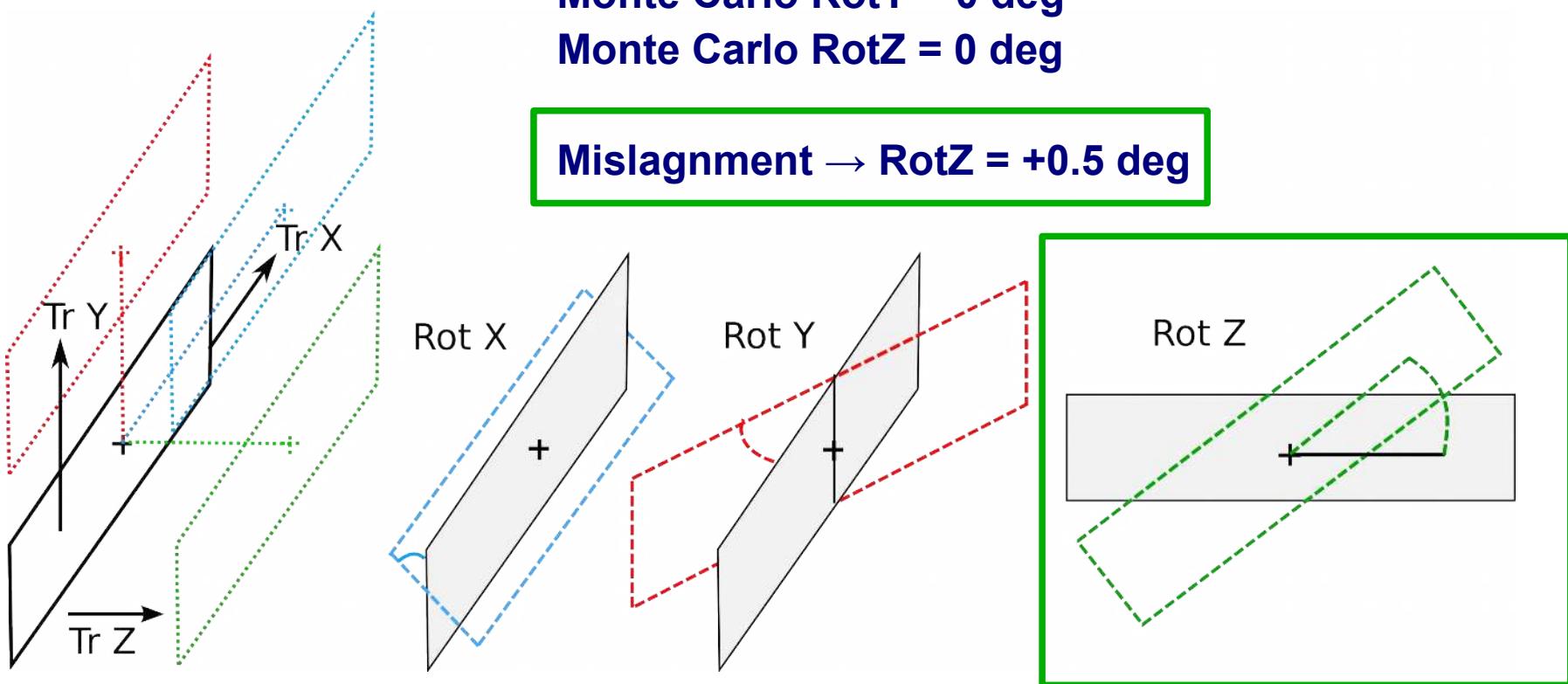
Rotation Center O1 : Rotation O1Z

Monte Carlo RotX = 0 deg

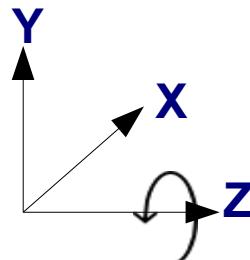
Monte Carlo RotY = 0 deg

Monte Carlo RotZ = 0 deg

Misalignment → RotZ = +0.5 deg



Alignment with mini-vectors : Results

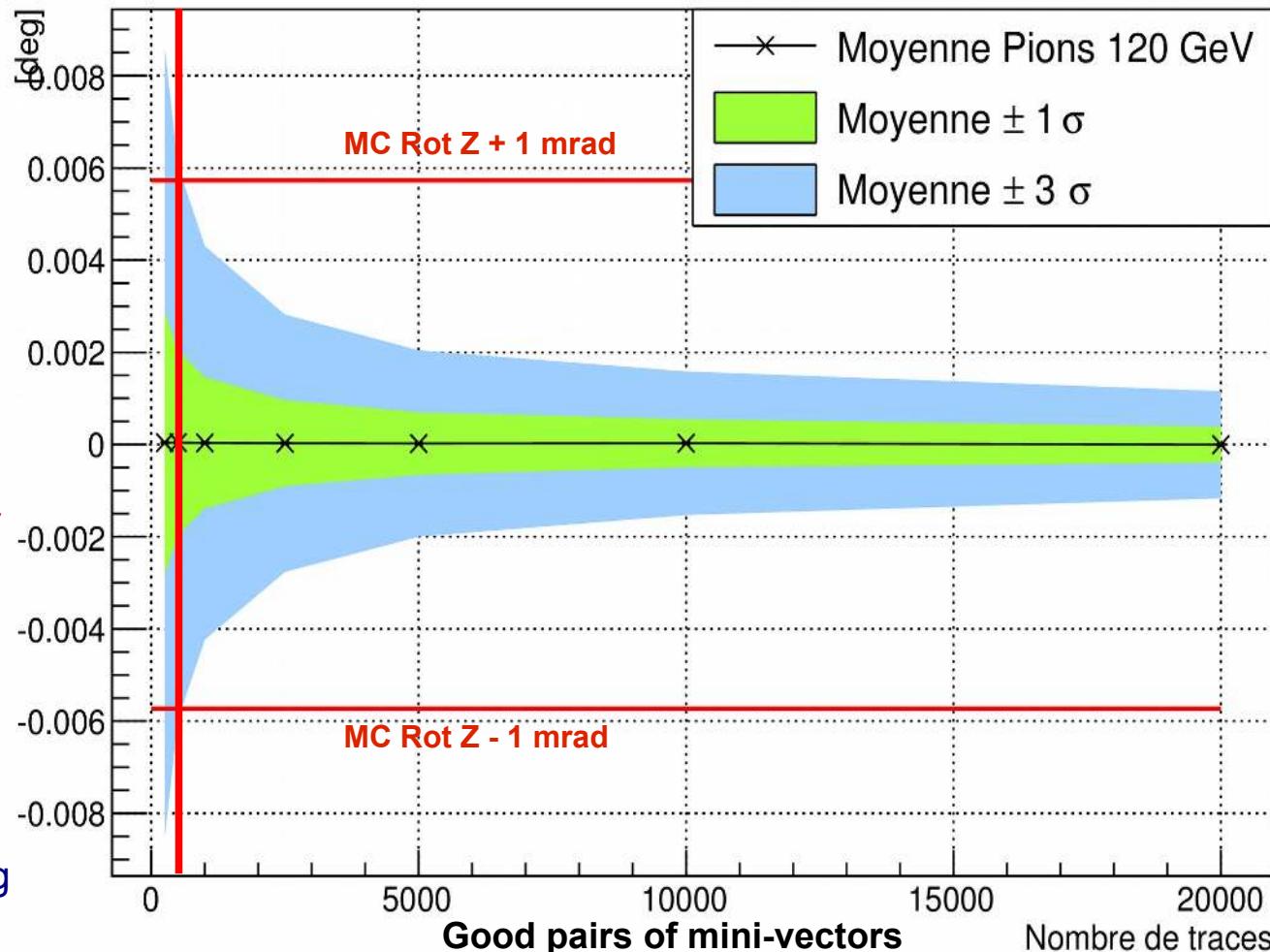


- **Rotation Axis Z :**
 - ↳ Mean vs statistic
 - ↳ Width vs statistic
- **Red lines** : Monte Carlo Value $\pm 1 \text{ mrad}$
- ≥ 500 good pairs of mini-vectors and more
 - ↳ No bias
 - ↳ ***precision (3 σ) better than 1 mrad***
- **Rotation Axis Y :**
 - ↳ No bias + precision (1σ) $< 1 \text{ mrad}$ with ≥ 2500 MV pairs
- **Rotation Axis X :**
 - ↳ Small bias = -0.01 deg
 - ↳ **Width $< 1 \text{ mrad}$ (1σ) with ≥ 2500 Mvs pairs**

Position after minimisation in function of statistics

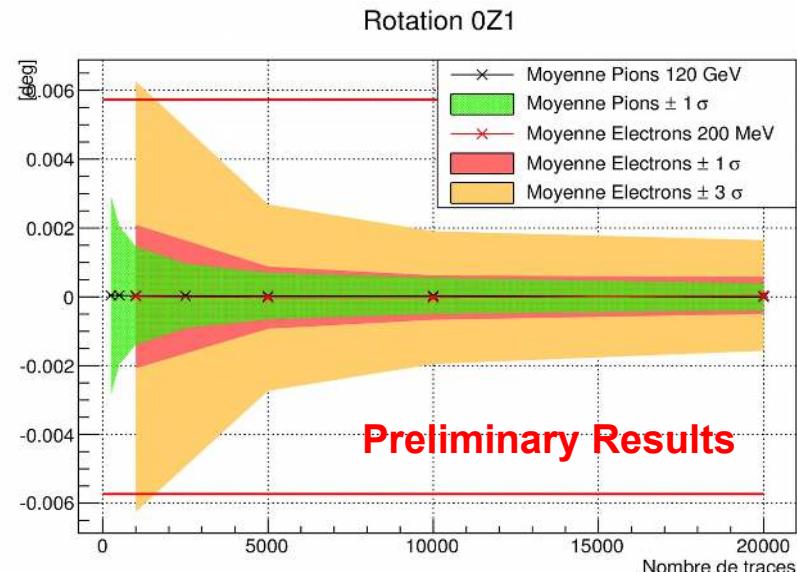
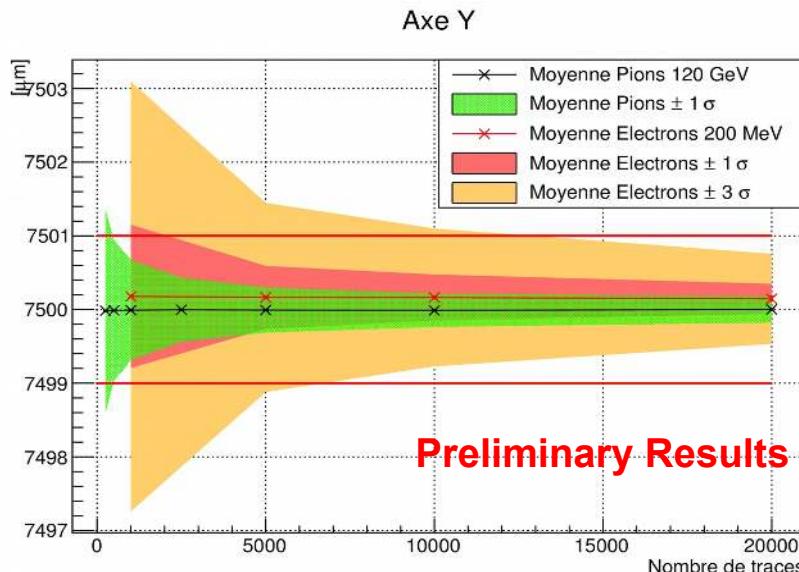
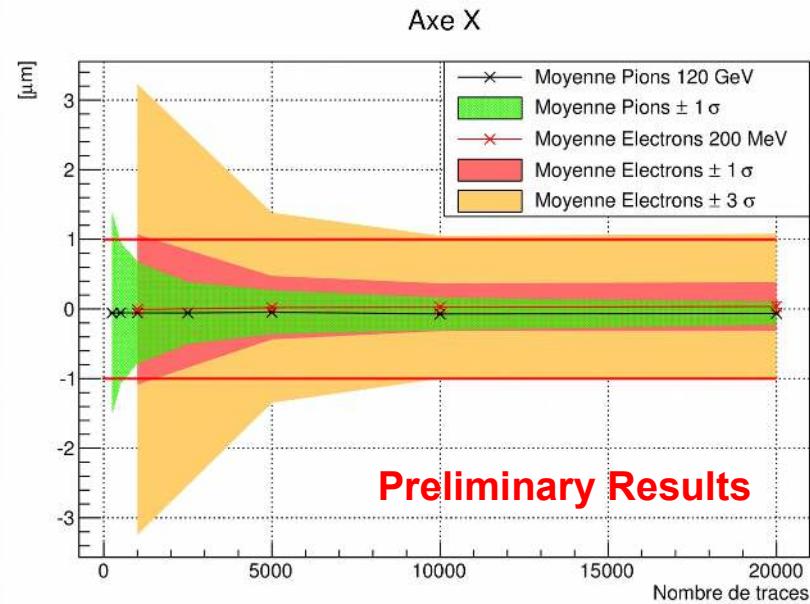
Rotation OZ1

Preliminary Results



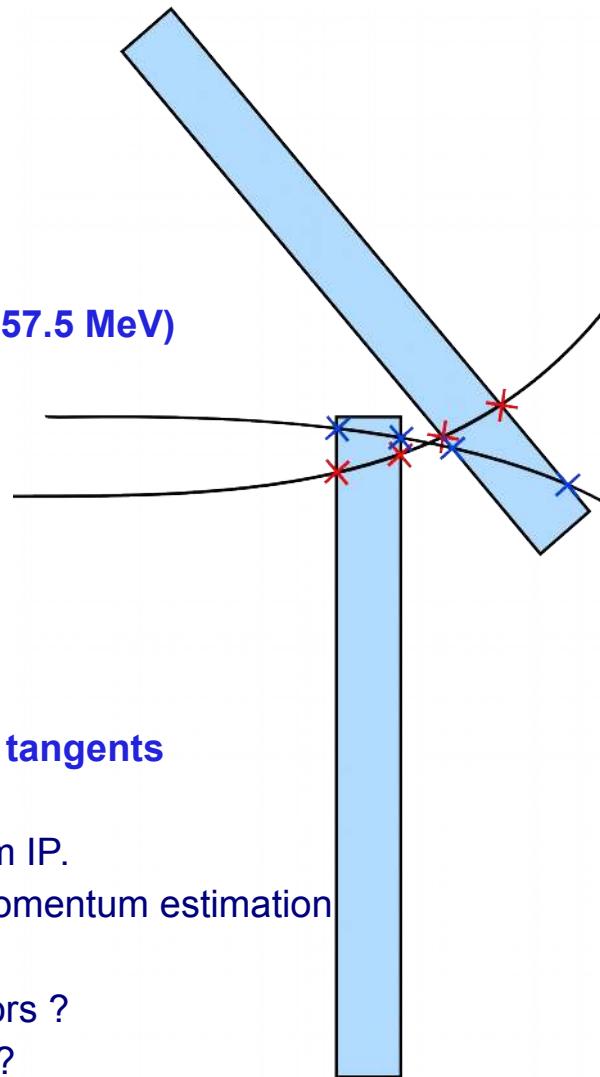
Low Momentum Electrons (200 MeV/c)

- Same configuration as before
- No magnetic Fiel B=0 and perfect mini-vectors associations
- Electrons : $P = 200 \text{ MeV}/c$ known
- Green : 120 GeV/c pions ($\pm 1 \sigma$)
- Red : 200 MeV/c electrons ($\pm 1 \sigma$), Orange ($\pm 3 \sigma$)
- Straight tracks + Multiple scattering effect :
 - ↳ No bias or small bias.
 - ↳ Small loss in precision



Alignment in real case (ILD + Beamstrahlung ?)

- Step 2 : Standalone alignment with beamstrahlung and mini-vectors
- Beamstrahlung
 - ↳ High statistic in small amount of time
 - ↳ But Low momentum
 - In Magnetic Field : Helices
 - Multiple Scattering
 - Very Low Momentum : Particles loopers.
 - ↳ Use high transverse momentum beamstrahlung (>200 MeV ?)
 - ↳ SIT projections (Layer 1 : Pt_min = 80.5 MeV Layer 2 : Pt_min = 157.5 MeV)
- Statistic :
 - ↳ $P_T > 200$ MeV : Around 10000 MVs pairs in 1 or few Hours
- Can we select these high momentum tracks with mini-vectors ?
 - ↳ Very Ambitious
- Mini-vectors
 - ↳ 2 points of measure
 - ↳ local track direction
 - ↳ 2 cluster shapes, one per side => Input and Output Tilts => Helix tangents
 - ↳ Association by couple of mini-vectors = 4 points
 - ↳ Search region for higt Pt tracks : Mostly in a cylinder of R=15 mm from IP.
 - ↳ If not standalone alignment : Pt > 200 MeV SIT + TPC information momentum estimation
- Opened questions :
 - ↳ Can we reconstruct these helices (high pt momentum) with mini-vectors ?
 - ↳ If we can, what is the resolution of the alignment with beamstrahlung ?



Summary and outlook

- Full simulation chain for :
 - ↳ Single sensors
 - ↳ Double sided ladders (PLUME)
 - ↳ SALAT sensors
 - ↳ Others ...
- Detector response based on the beam test data
- Alignment with mini-vectors : proof of principle validated
 - ↳ Precision on the center (X_1, Y_1) < 1 μm .
 - ↳ Precision on Z_1 < 2 μm .
 - ↳ Precision on tilts < 1 mrad.
 - ↳ With Few 10 000 mini-vectors pairs.
- Outlook : Studies of this alignment method with low momentum particle and magnetic field : Work In Progress.
- Outlook : Global alignment of the double sided layer

Thank you for your attention !

Thank you !

Statistic (Order of magnitude only)

- Order of magnitude for Statistic for 1 Overlapping Region

- We want a minimum increase of material budget so :

↳ 1 OR = 5 % Ladder Surface

- Hard processes

↳ $L = 1.8 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

↳ $e^+ e^- \rightarrow \mu^+ \mu^-$ (500 GeV) : Around $1400/2800 \mu$ per Year / OR

↳ $e^+ e^- \rightarrow q\bar{q}$ (500 GeV) : $8000/16000$ particles per Year / OR

- Very Optimistic : **Beamstrahlung** (see after)

↳ Around $7500/20000 e^-/+$ per Hour / OR

↳ But Low Momentum particles in a magnetic field

- **GigaZ option**

↳ $L = 10^{33} \text{ cm}^{-2} \text{ s}^{-1} \rightarrow 10^9/\text{Year}$

↳ Example : $Z \rightarrow \mu\mu$ (3.5%) + $Z \rightarrow ee$ (3.5%)

↳ Around $15000/25000$ particles per Month / OR

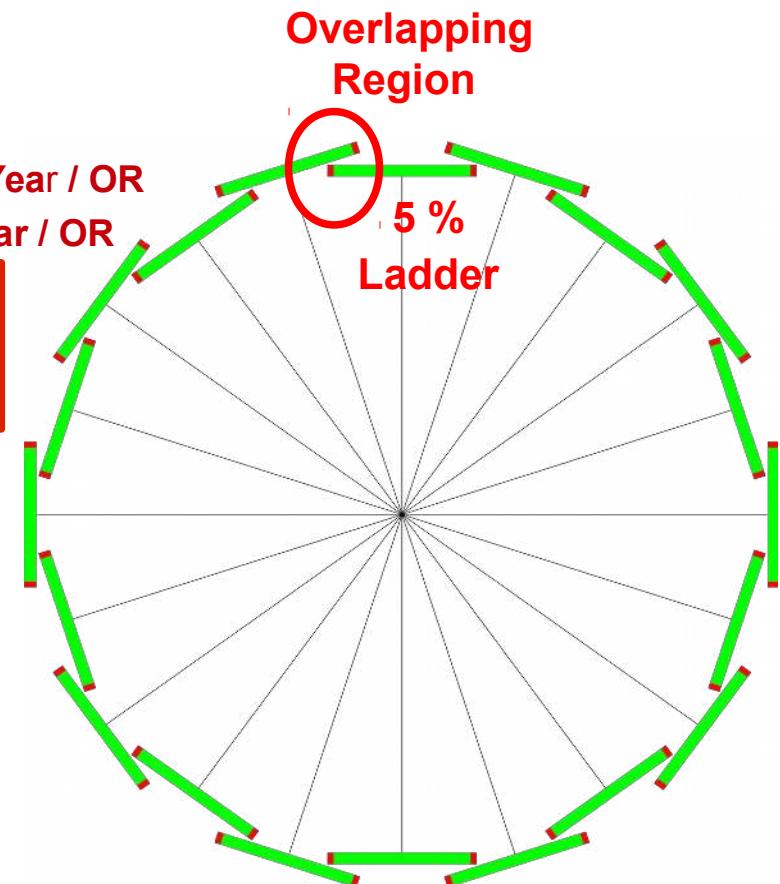
- **Photon collider option**

↳ $L = 10^{34} \text{ cm}^{-2} \text{ s}^{-1} / 500 \text{ GeV}$

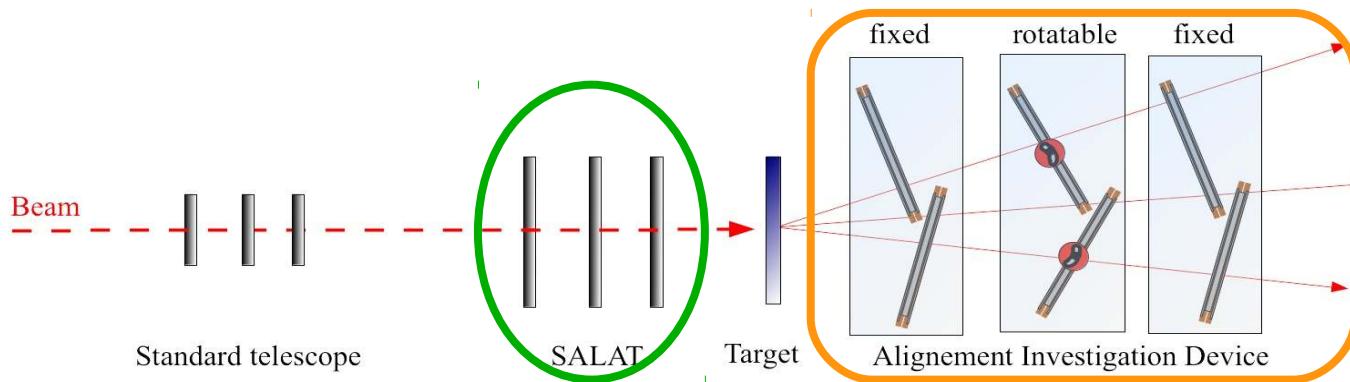
↳ Ex : $\sigma(\gamma\gamma \rightarrow \mu^+\mu^-\mu^+\mu^-) \approx 150 \text{ pb}$ (TDR Tesla)

↳ Around $40000...80000 \mu$ per Month / OR

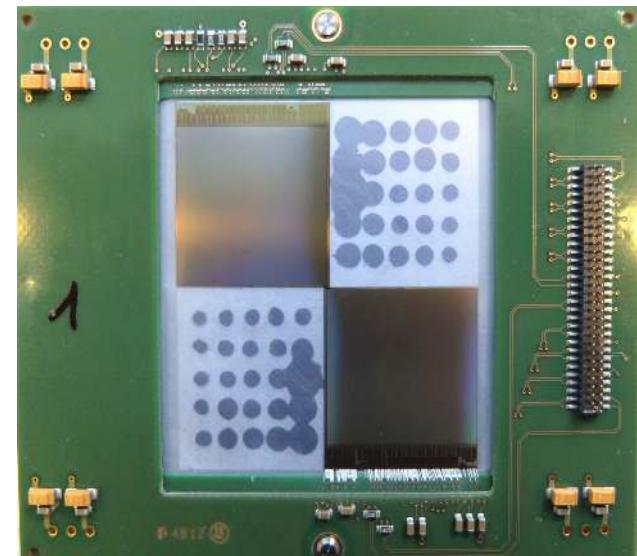
- Sum of tracks from different processes



Thesis context : AIDA beam telescope



- AIDA : R&D futur detectors
- Vertex detector context → New beam telescope
- **SALAT : Single Arm Large Area beam Telescope**
- **AID box : Alignment Investigation Device**
 - ↳ Goal : *Study of a vertex detector sector.*
 - ↳ Double sided ladders (PLUME, see latter)
- Need a Monte Carlo simulation of these objects
- Studies on alignment
 - ↳ Alignment of the whole ladder.
 - ↳ On the same layer, on the *overlapping region* between two consecutive ladders → *With mini-vectors.*



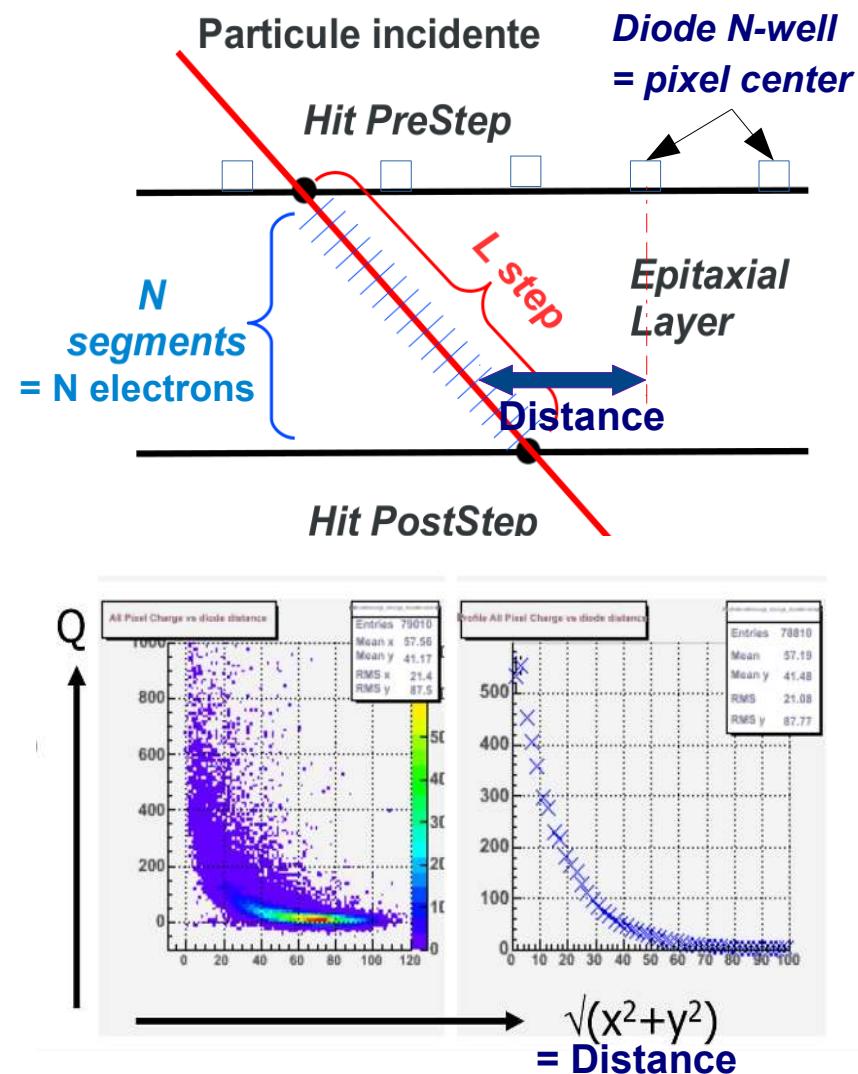
A SALAT super-plane

Charge transport simulation

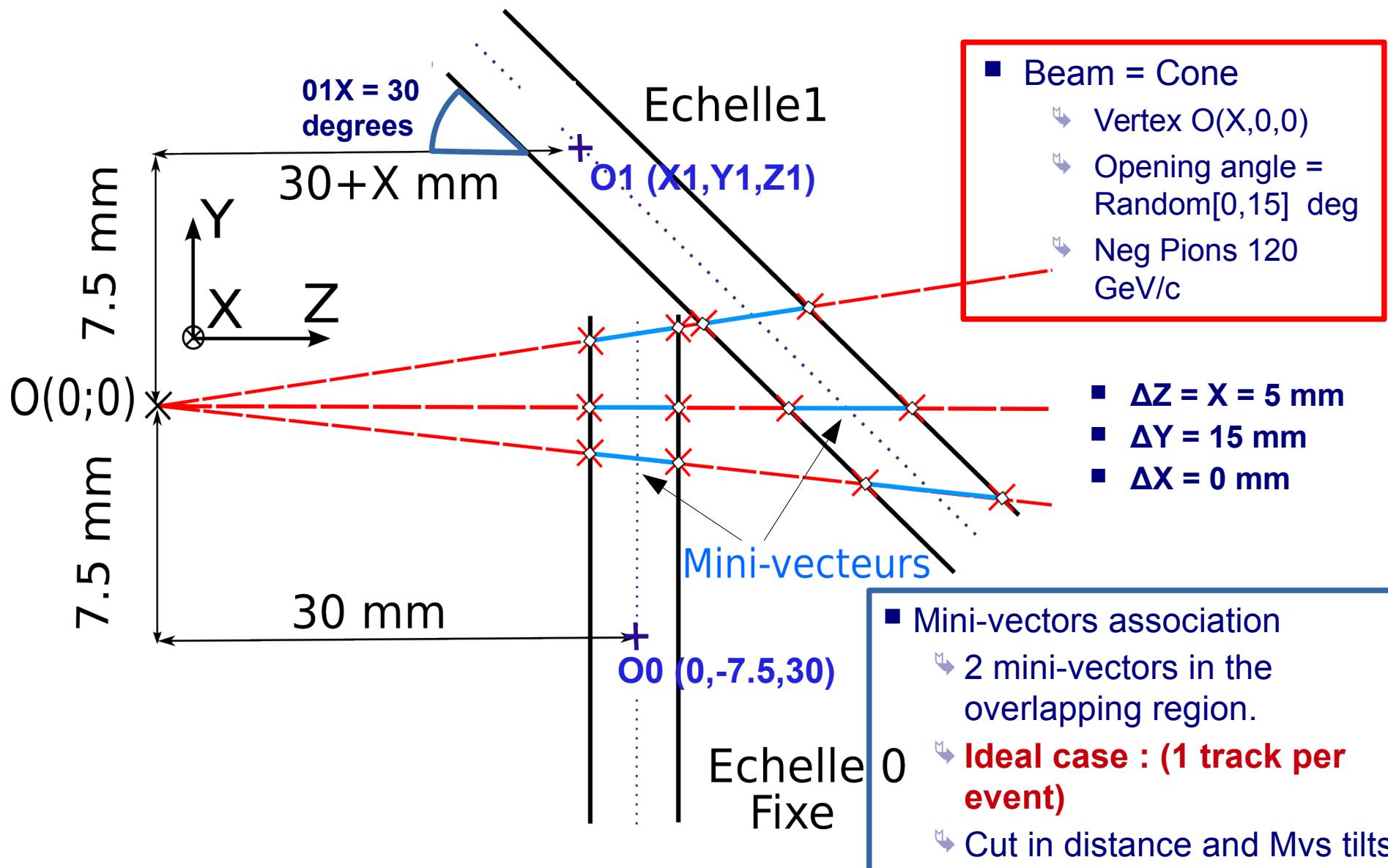
CMOS sensor response from energy deposition to digitization

■ Charge transport and digitizer

- ↳ Pixels geometry description
 - MIMOSA-28 : $20.7 \times 20.7 \mu\text{m}^2$
- ↳ Very small depleted region → thermal diffusion of the charge carriers.
- ↳ Charge carriage simulation not possible due to too many unknowns (doping profil, thicknees epi layer, etc ...)
- ↳ Data based charge transport model :
 - from previous beam tests
 - Analog and digital output sensors
- ↳ Noise = Gaussian noise (Mean = 13.7 e^-)
- ↳ Discriminator + Zero-suppression
 - pixel charge comparison with a threshold
 - Zero suppression
 - Binary Output



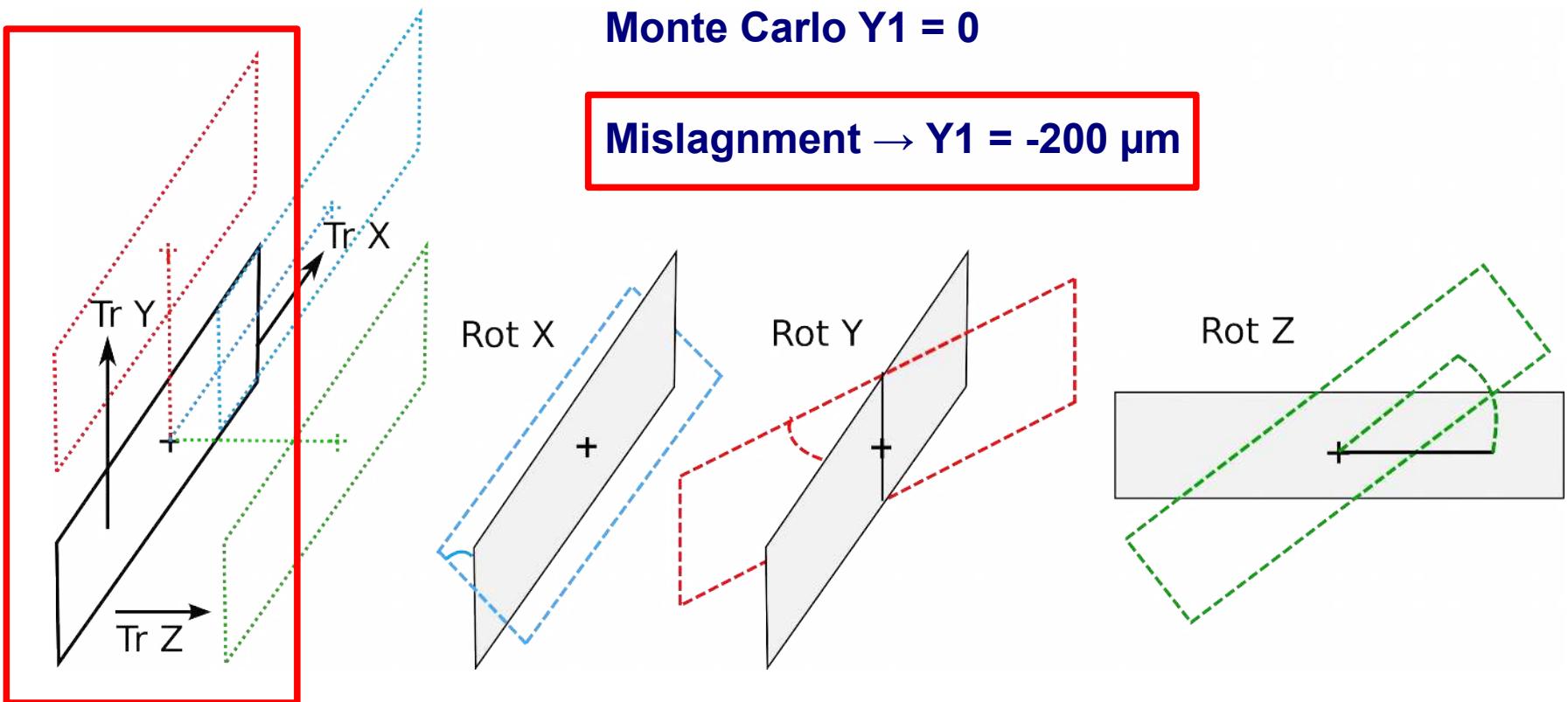
Configuration : Pions High Momentum (120 GeV/c)



Parameter Y1

Translation Center C1 : Coordinate Y1
Monte Carlo Y1 = 0

Misalignment → Y1 = -200 μm



Alignment with mini-vectors : Results

Position after minimisation in function of statistics

Axe Y

Preliminary Results

■ Position Y1 :

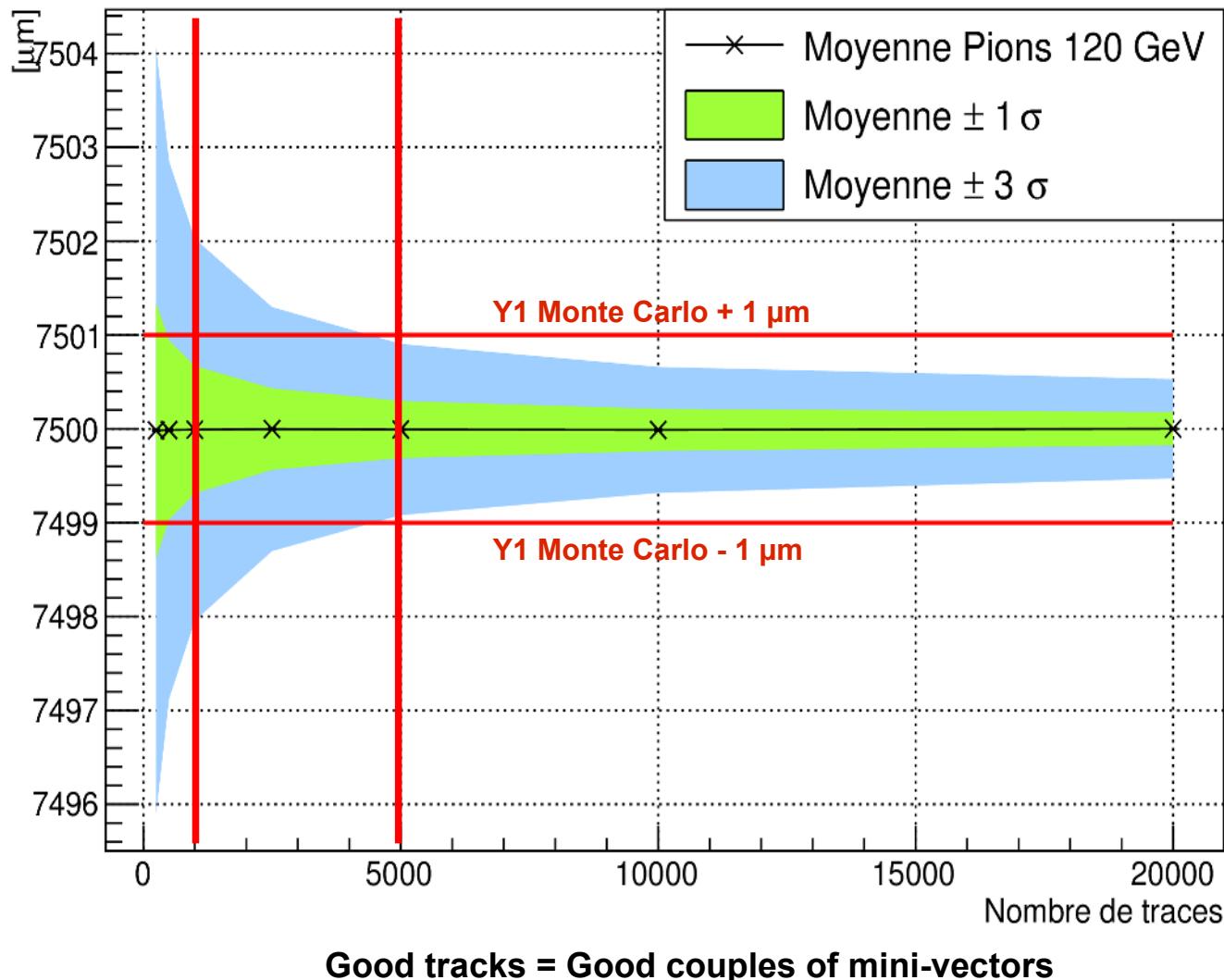
- ↳ Monte Carlo Y1 = 0
- ↳ Mean vs statistic (deviation from MC values)
- ↳ Width vs statistic (method precision : $\pm 1\sigma, \pm 3\sigma$.)

■ 1000 good couples of mini-vectors

- ↳ **precision (1σ) better than 1 μm**

■ 5000 good couples of mini-vectors

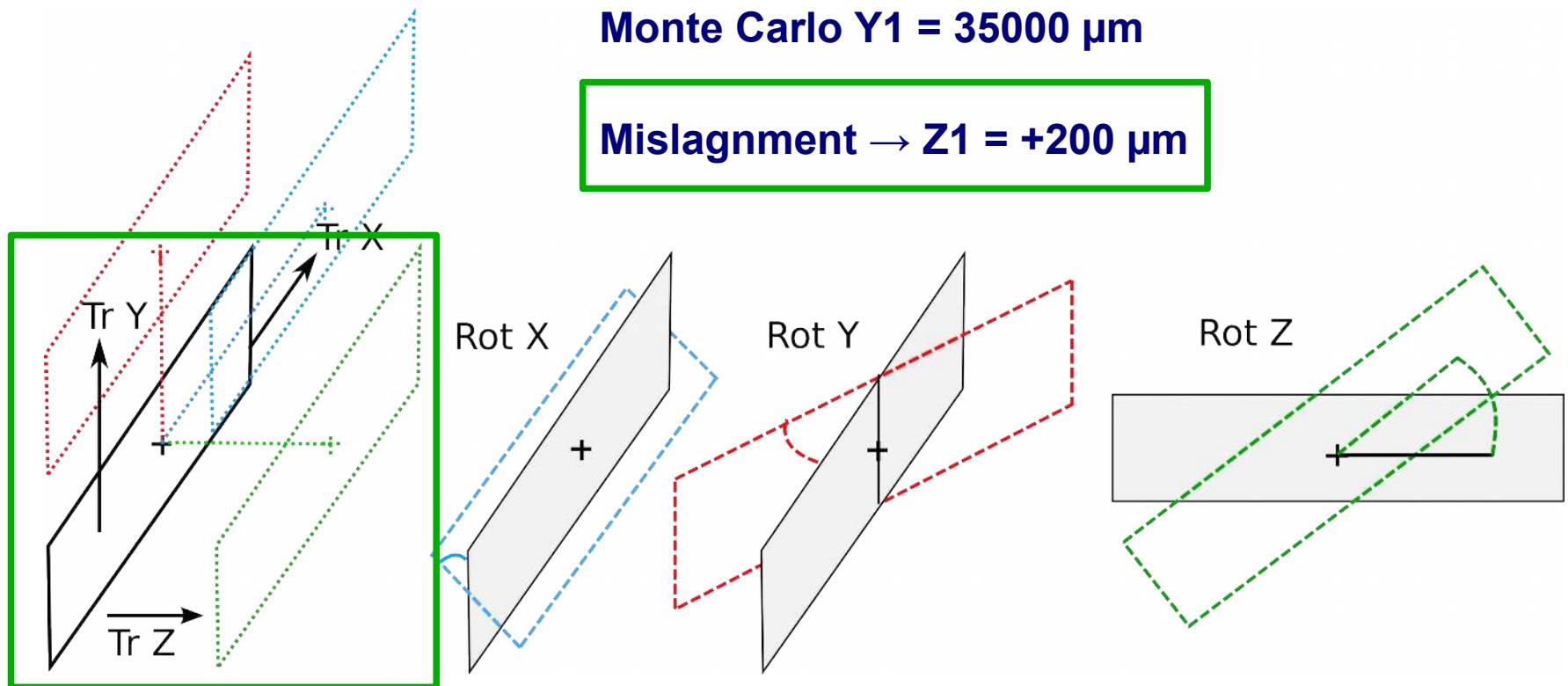
- ↳ **Precision (3σ) better than 1 μm**



Parameter Z1

Translation Center O1 : Coordinate Z1
Monte Carlo Y1 = 35000 μm

Misalignment \rightarrow Z1 = +200 μm



Alignment with mini-vectors : Results

Position after minimisation in function of statistics

■ Position Z1 :

- ↳ Monte Carlo Z1 = 0
- ↳ Mean vs statistic
- ↳ Width vs statistic
($\pm 1\sigma$, $\pm 3\sigma$.)

■ Mean = **Bias** around **-10 µm.**

- ↳ Result of a **weak mode**

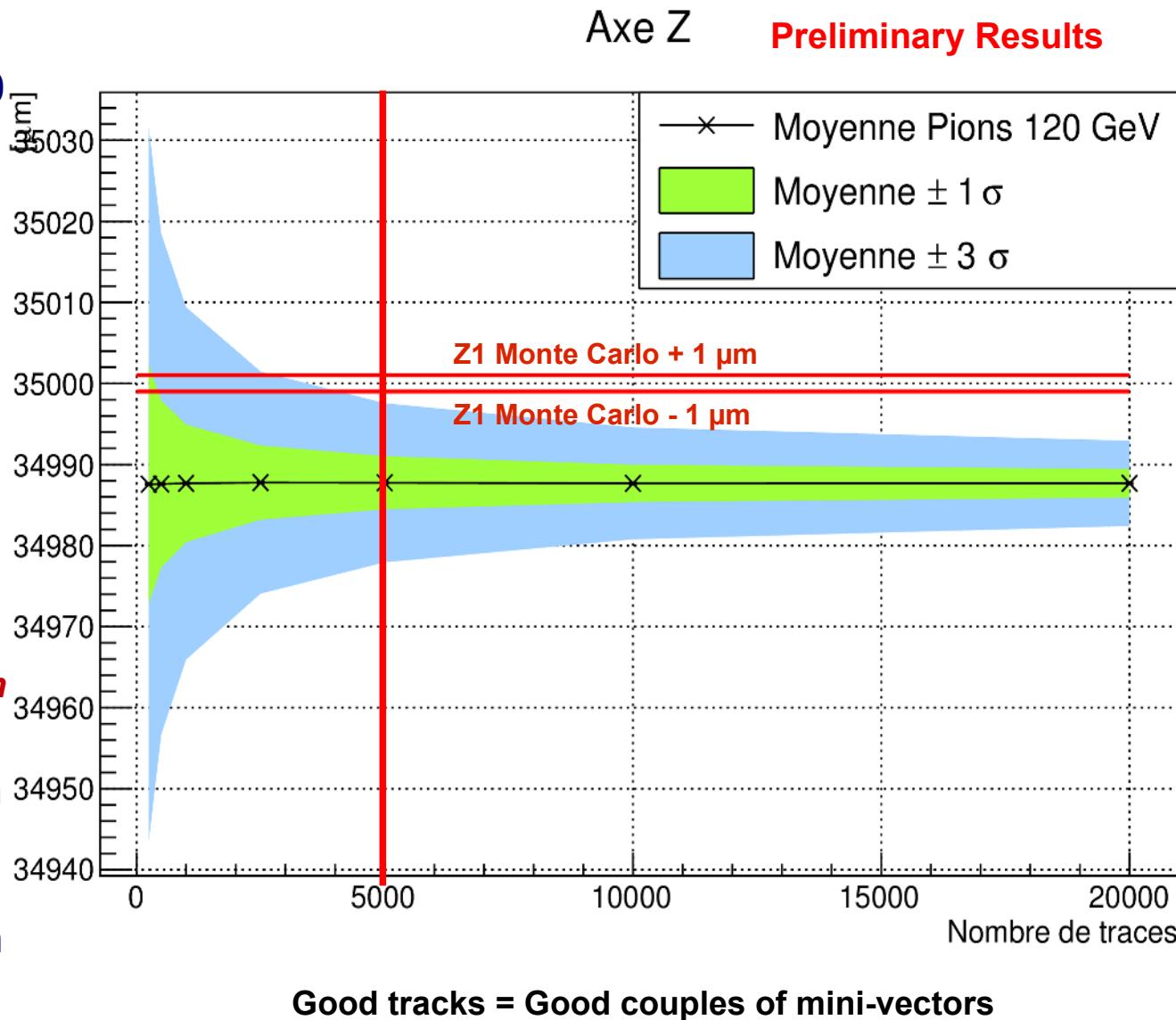
- ↳ Constant bias → can be subtracted

■ ≥ 5000 couples of MVs

- ↳ **Width (3 σ) = $\pm 10 \mu m$**

■ Bias reduction :

- ↳ More tilt in Y direction for Mini-vectors
- ↳ Bias suppression
- ↳ Precision (1σ) < $2\mu m$ with 1000 couples



Bias reduction : Z axis

- Bias on Z1

- Configuration 0

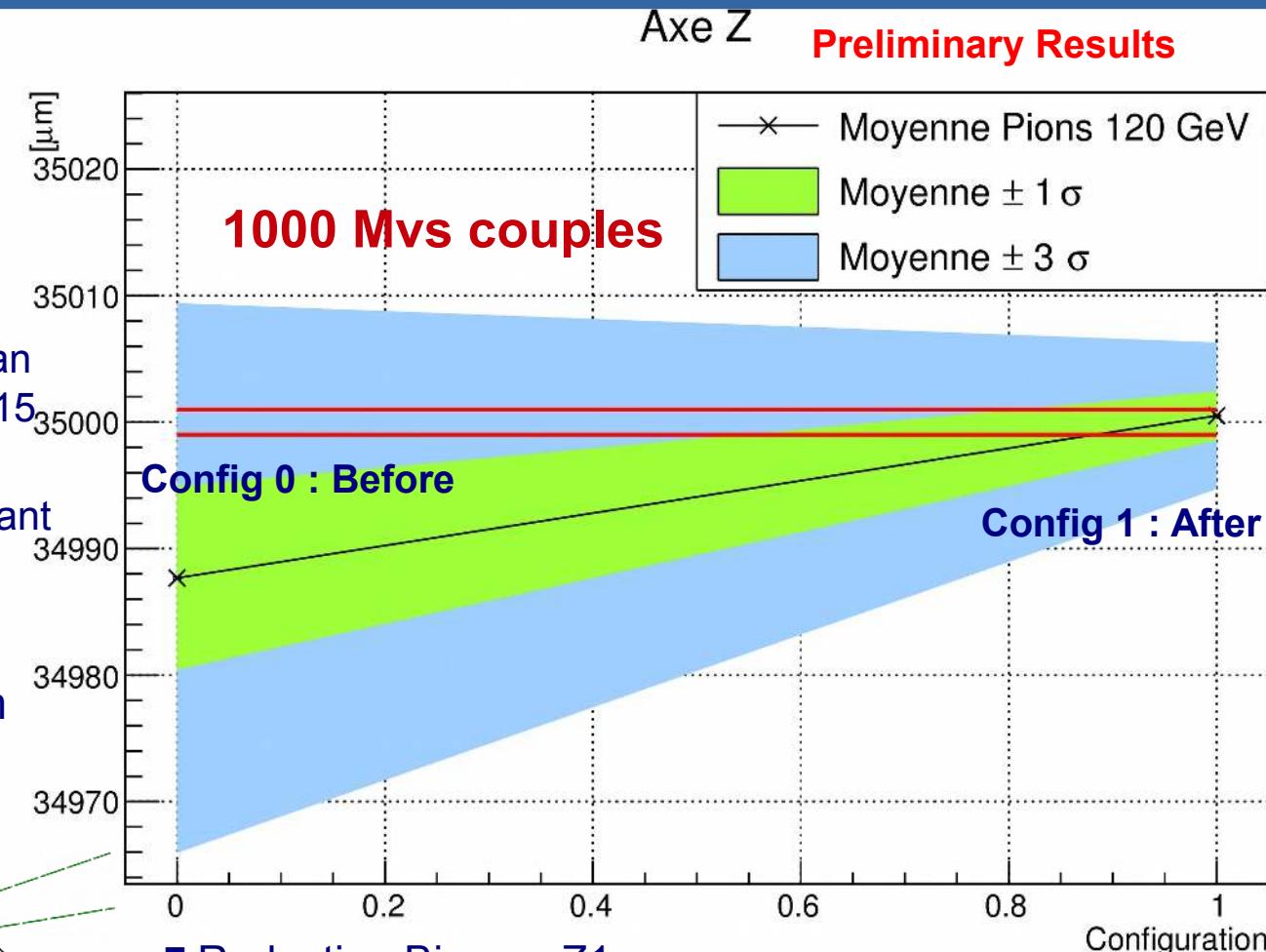
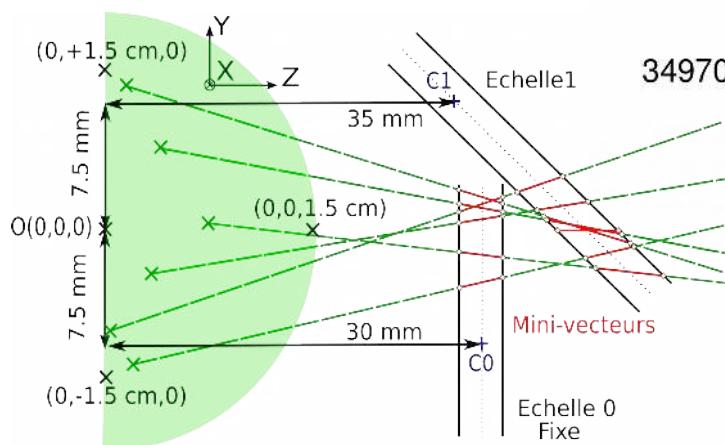
- ↳ As before (1000 Mvs couples)

- Configuration 1

- ↳ Cone Vertex : start in an half cylinder of radius 15 mm.
- ↳ MVs TiltY more important
- ↳ 1000 Mvs couples

- Bias reduction

- Weak mode suppression



- Reduction Bias on Z1 :

- ↳ With 1000 MVs couples → precision 1.5 μm

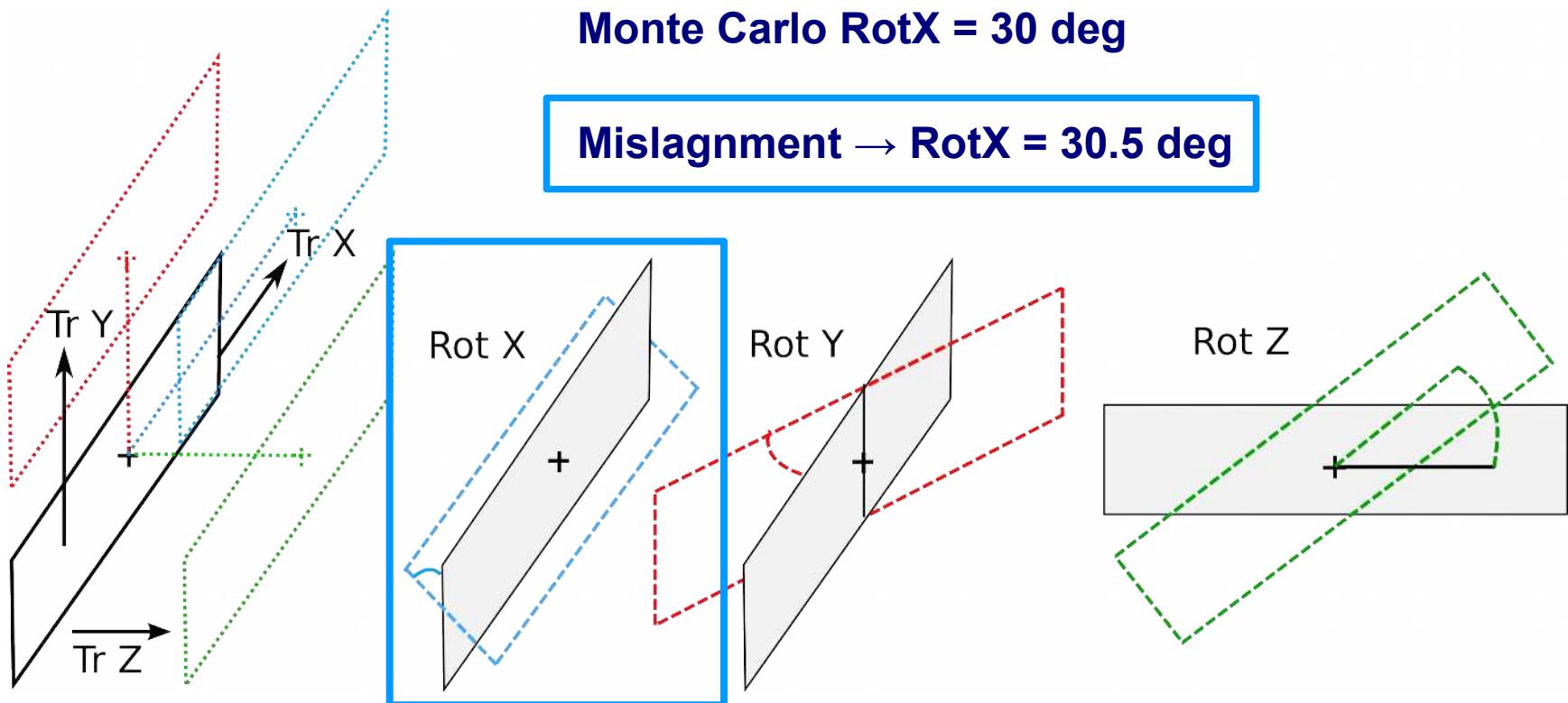
- And : Best precision in rotation O1Y

- ↳ With 1000 MVs couples : precision (3σ) : 3.5 mrad → 1.2 mrad

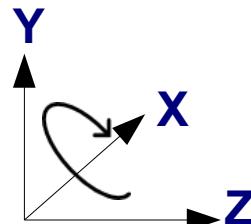
Parameter RotX

Rotation Center C1 : Rotation C1X
Monte Carlo RotX = 30 deg

Misalignment → RotX = 30.5 deg



Alignment with mini-vectors : Results



Position after minimisation in function of statistics

Rotation OX1

Preliminary Results

■ Rotation 01X :

- Deviation from MC values vs stat
- method precision : $\pm 1\sigma, \pm 3\sigma$.

■ Small bias : 0.01 deg

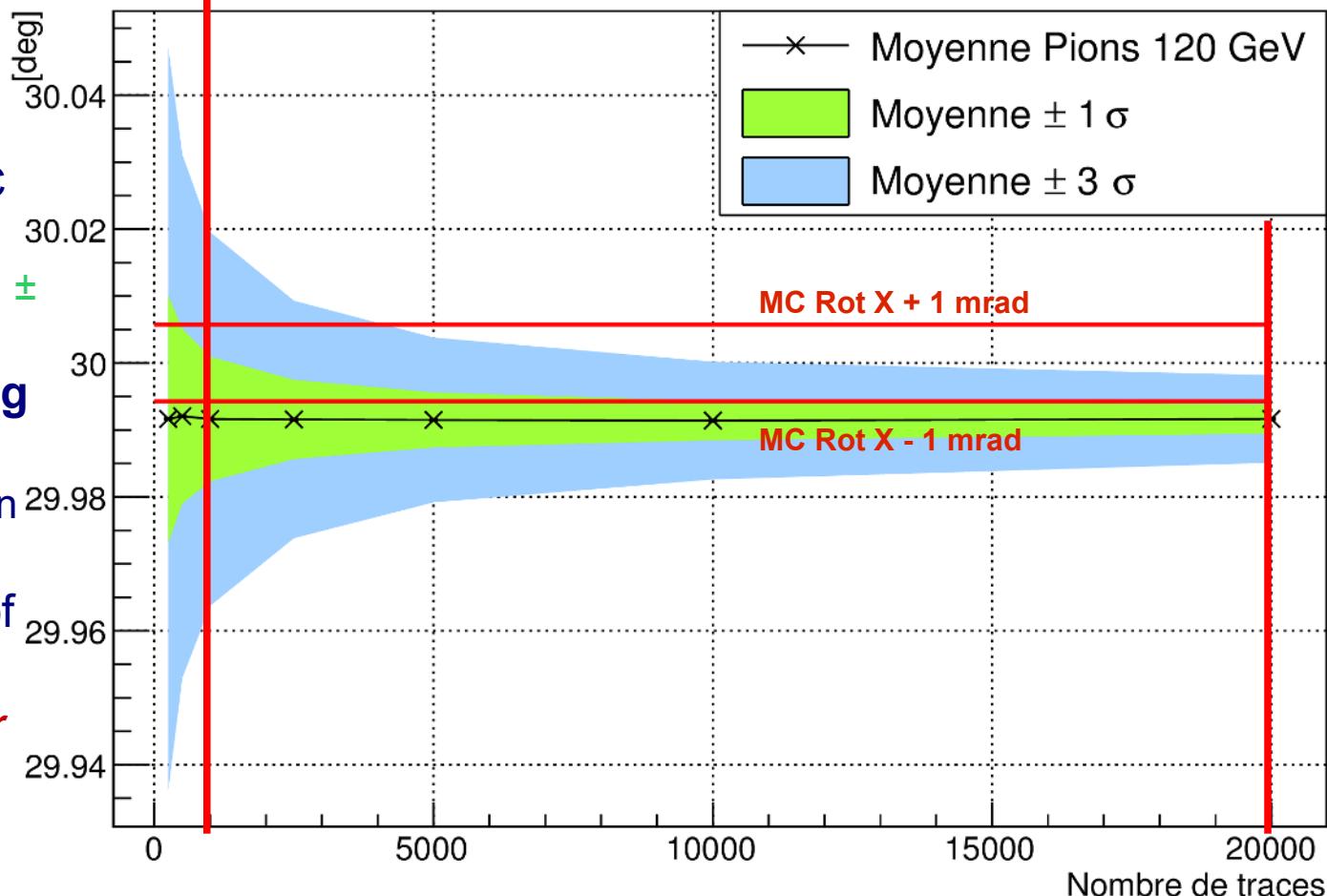
- Small weak mode.
- Constant bias : can be subtracted

■ 1000 good couples of mini-vectors

- Width (1σ) better than 1 mrad**

■ 20 000 good couples of mini-vectors

- Width (3σ) better than 1 mrad**

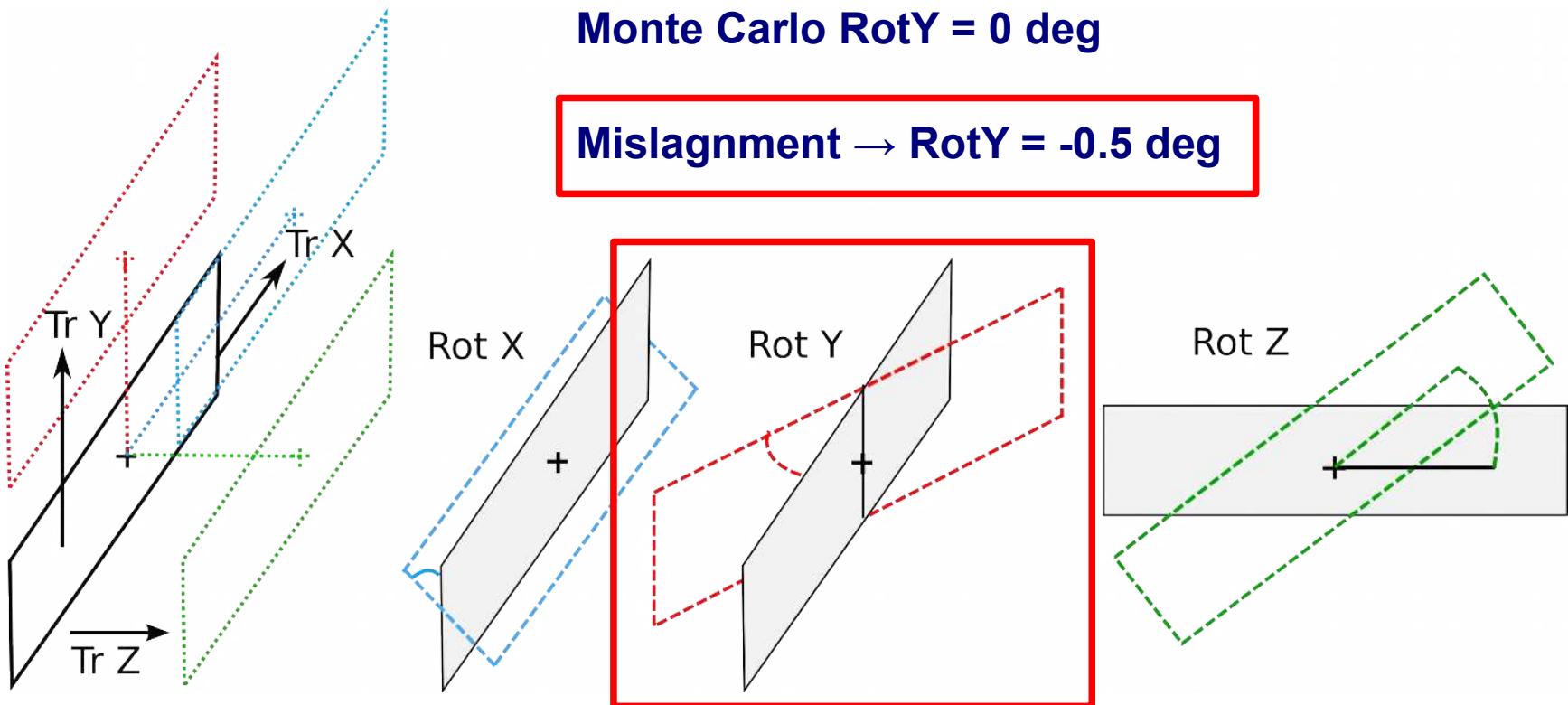


Good tracks = Good couples of mini-vectors

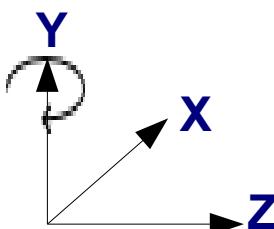
Parameter RotY

Rotation Center C1 : Rotation C1Y
Monte Carlo RotY = 0 deg

Misalignment → RotY = -0.5 deg



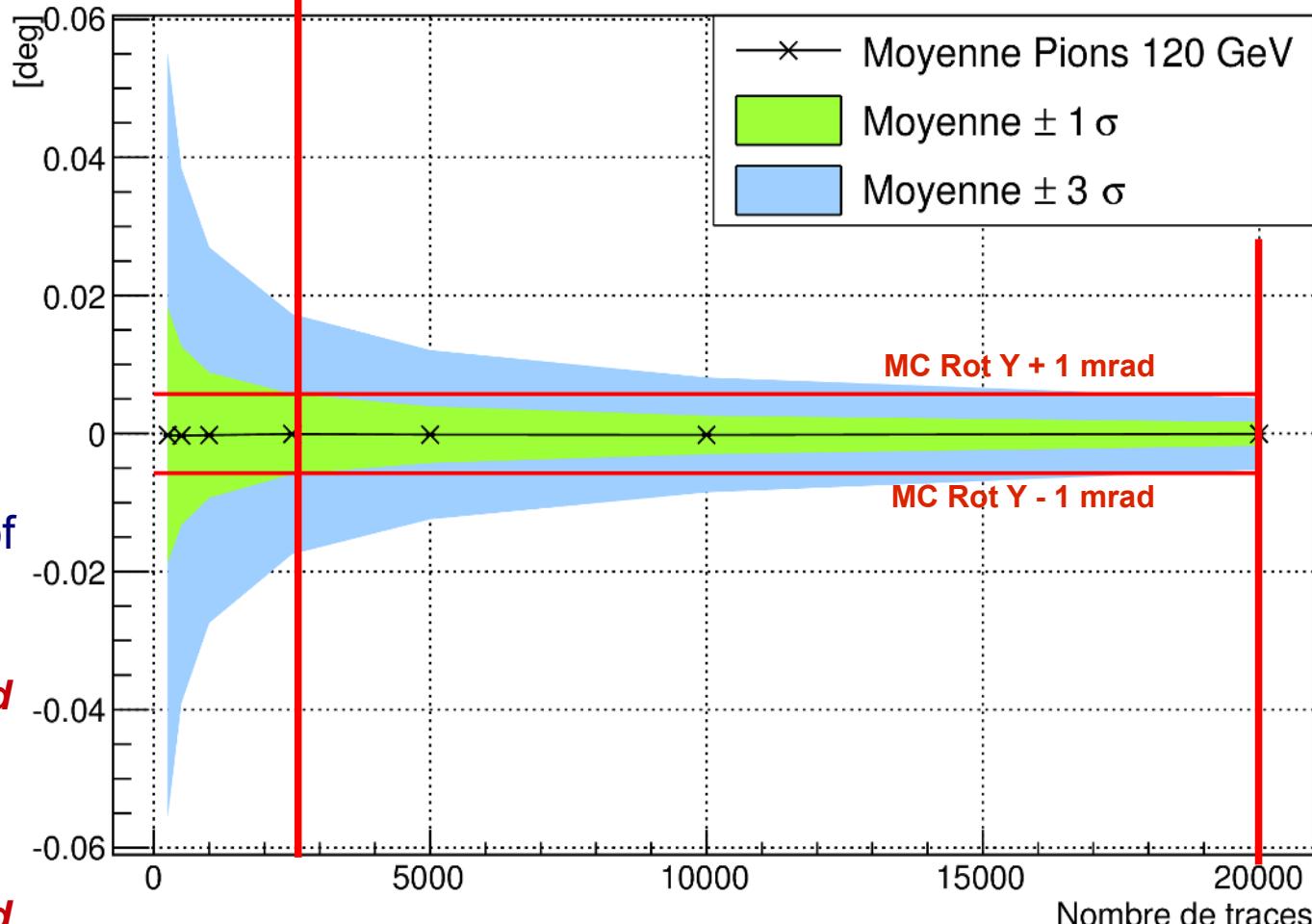
Alignment with mini-vectors : Results



Position after minimisation in function of statistics

Rotation OY1 **Preliminary Results**

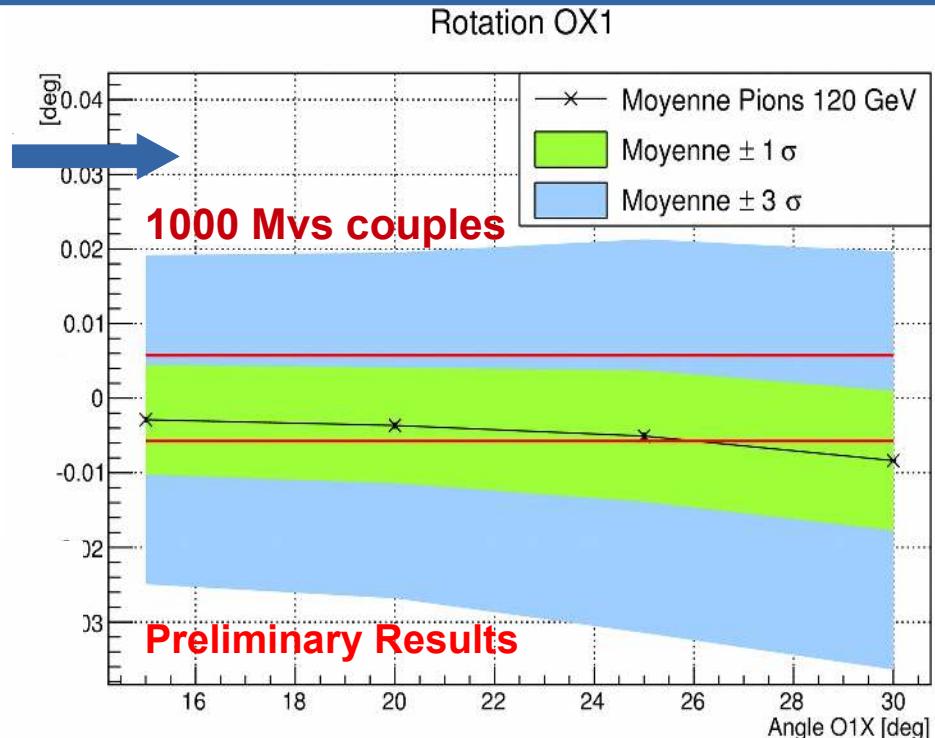
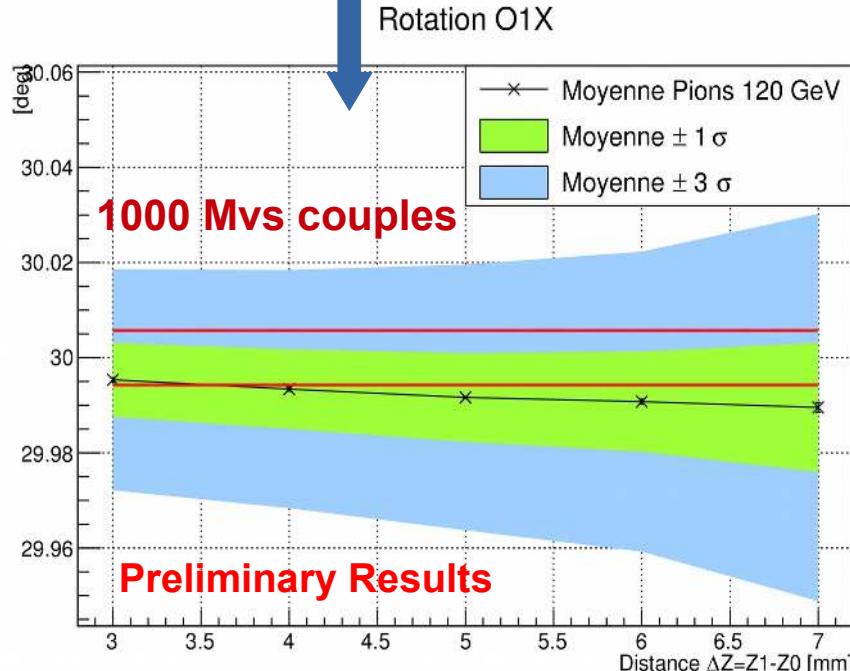
- **Rotation 01Y :**
 - ↳ Mean vs statistic (deviation from MC values)
 - ↳ Width vs statistic (method precision : $\pm 1\sigma$, $\pm 3\sigma$.)
- **2 500** good couples of mini-vectors
 - ↳ ***precision (1 σ) better than 1 mrad***
- **20 000** good couples of mini-vectors
 - ↳ ***Precision (3 σ) better than 1 mrad***



Good tracks = Good couples of mini-vectors

Bias reduction : Rotation O1X

- Bias on rotation O1X
- Reduction of the ladder1 tilt on O1X
 - ↳ Smaller distance between the two ladder
- Reduction of the distance between the 2 centers
 - ↳ Smaller distance between the two ladder



- Small bias reduction
 - ↳ Always a small weak mode
- Other solution :
 - ↳ Increase the overlapping region (In progress).
- Bias reduction strategy
 - ↳ Mixing these three solutions

SIT

- 2 Double Layer
- $R_{in} = 153 \text{ mm}$ 2 double layers
 $\pm 7.0\mu\text{m}$
- $R_{out} = 300 \text{ mm}$ Si-strip sensors
 $\pm 7.0\mu\text{m}$
- $z = 644 \text{ mm}$
- $P_{tmin} = 80.5 \text{ MeV}$
- $P_{tmax} = 157.5 \text{ MeV}$

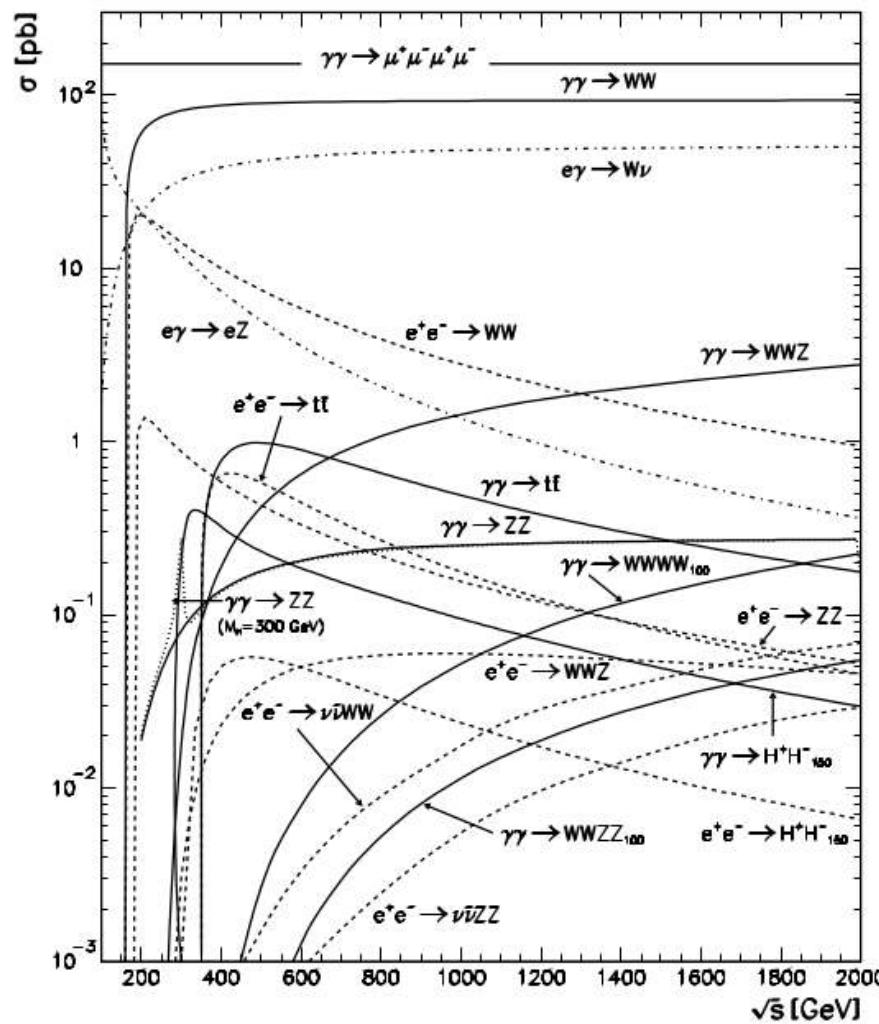
Statistic estimations : geometry

DBD/TDR values

Double Layer	Layer	Radius (mm)	z (mm)	cos(θ)	σ(μm)	Readout time (μs)
1	1	16	62,5	0,97	2,8	50
	2	18	62,5	0,96	6	10
2	3	37	125	0,96	4	100
	4	39	125	0,95	4	100
3	5	58	125	0,91	4	100
	6	60	125	0,9	4	100

Double Layer	Layer	Surface (cylinder) (cm ²)	Circumference (mm)	Ladders per double sided layer	Ladder Height (mm)	Angle (degree)
1	1	62,83	100,53	10	10	36
	2	70,69	113,10	10	10	36
2	3	290,60	232,48	12	20	30
	4	306,31	245,04	12	20	30
3	5	455,53	364,42	18	20	20
	6	471,24	376,99	18	20	20

Photon collider



MIMOSA CMOS sensors

■ Operating principle

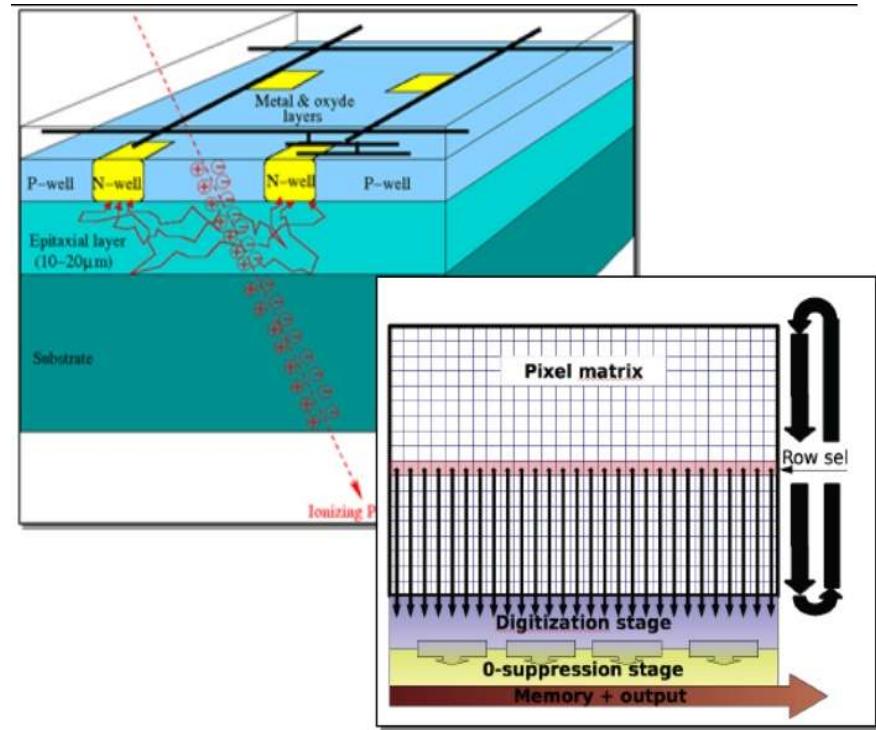
- ↳ Signal in the epitaxial layer ≈ 1000 e-.
- ↳ Thermal diffusion (very small depleted region)
- ↳ Reflection at interfaces
- ↳ Continuous collection of charges (no dead time)

■ Advantage

- ↳ Granularity : 3-4 μm with pitch of 20 μm
- ↳ Material budget : sensors thinned down to 50 μm .
- ↳ CMOS = Industrial process

■ Readout time, power consumption.

- ↳ Rolling shutter mode $\rightarrow T = T(\text{row}) * \text{Number of Row}$
- ↳ Low power consumption ($\approx \mu\text{W}$ per pixel)



■ Digitization and zero suppression

- ↳ Digitization (end column)
- ↳ Zero suppression (end column)

Chi2

$$\chi^2 = \sum_{Traces} \left(\frac{(U_{ext} - U_{MV1})^2}{\sigma_U^2} + \frac{(V_{ext} - V_{MV1})^2}{\sigma_V^2} + \frac{(\Delta R_X)^2}{\sigma_{R_X}^2} + \frac{(\Delta R_Y)^2}{\sigma_{R_Y}^2} \right)$$

$$R_X = \frac{x_2 - x_1}{z_2 - z_1} = \frac{\Delta x}{\Delta z} \quad \sigma_{R_X}^2 = \frac{2\sigma_{\Delta x}^2}{(\Delta z)^2} + \frac{(\Delta x)^2 \sigma_{\Delta z}^2}{(\Delta z)^4}$$

$$R_X = \frac{y_2 - y_1}{z_2 - z_1} = \frac{\Delta y}{\Delta z} \quad \sigma_{R_Y}^2 = \frac{2\sigma_{\Delta y}^2}{(\Delta z)^2} + \frac{(\Delta y)^2 \sigma_{\Delta z}^2}{(\Delta z)^4}$$

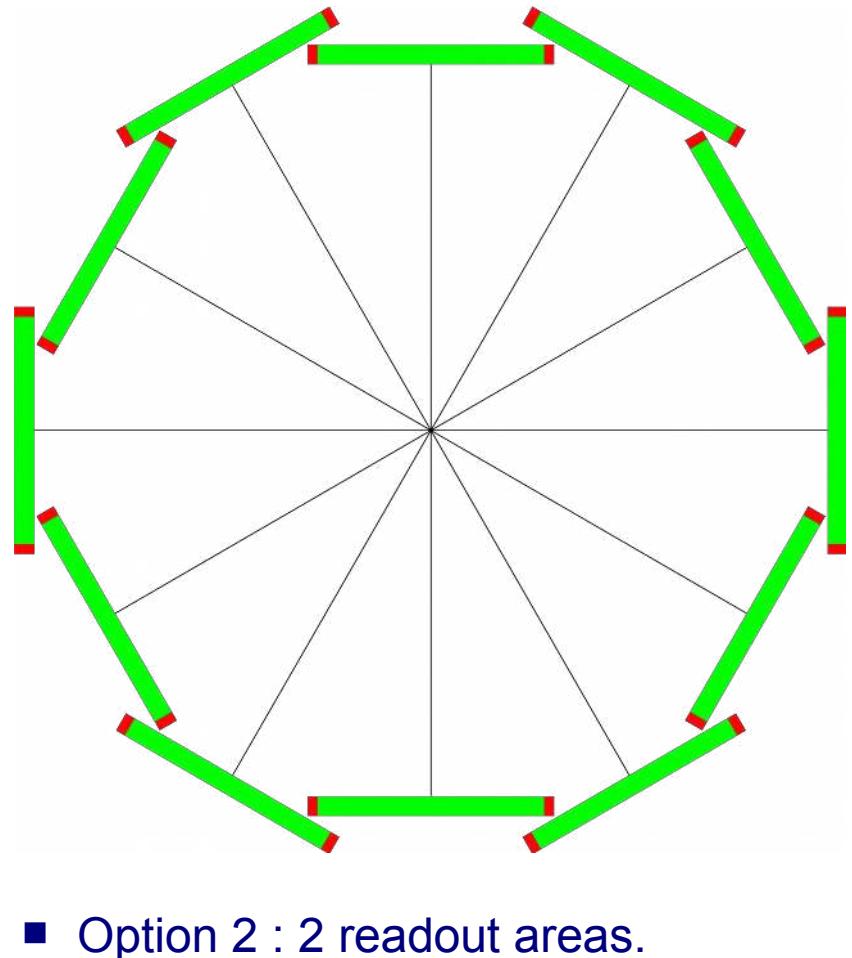
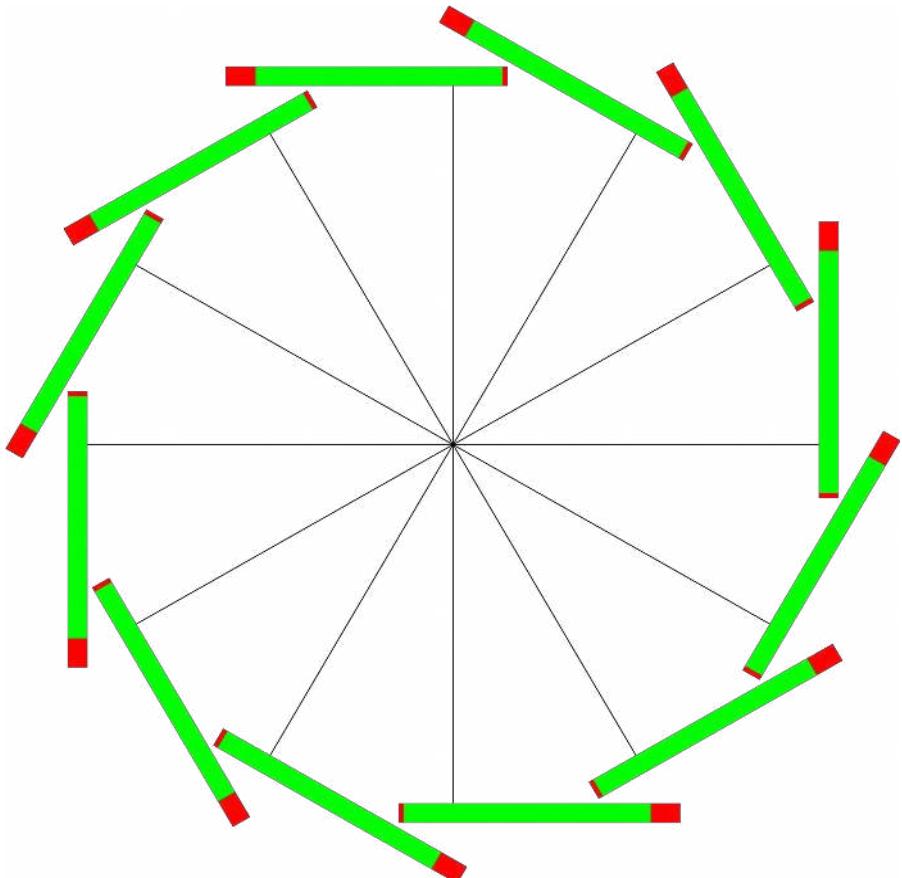
→ $\sigma_U = 3.5 \text{ } \mu\text{m}$ (Nomal incidence) or value at incidence θ_u

→ $\sigma_V = 3.5 \text{ } \mu\text{m}$ (Nomal incidence) or value at incidence θ_v

→ $\Delta x, \Delta y, \Delta z$ = mini-vector size in x, y and z.

Double Sided Layer Geometry : 2 Options

- Option 1 : 1 readout area.



- Option 2 : 2 readout areas.