

# $Z \rightarrow \mu\mu$ CROSS SECTION @ CMS

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# PHYSICS AT LHC STARTUP

- Physics at LHC startup:  $Z \rightarrow \mu\mu(ee)$ .
- Useful for tracker and muon system alignment and calorimeter calibration.
- $Z$  events are setting the lepton momentum and lepton energy scales.
- Result should be cross section or luminosity.

# STRATEGY FOR $pp \rightarrow Z/\gamma^* \rightarrow \mu^+ \mu^-$

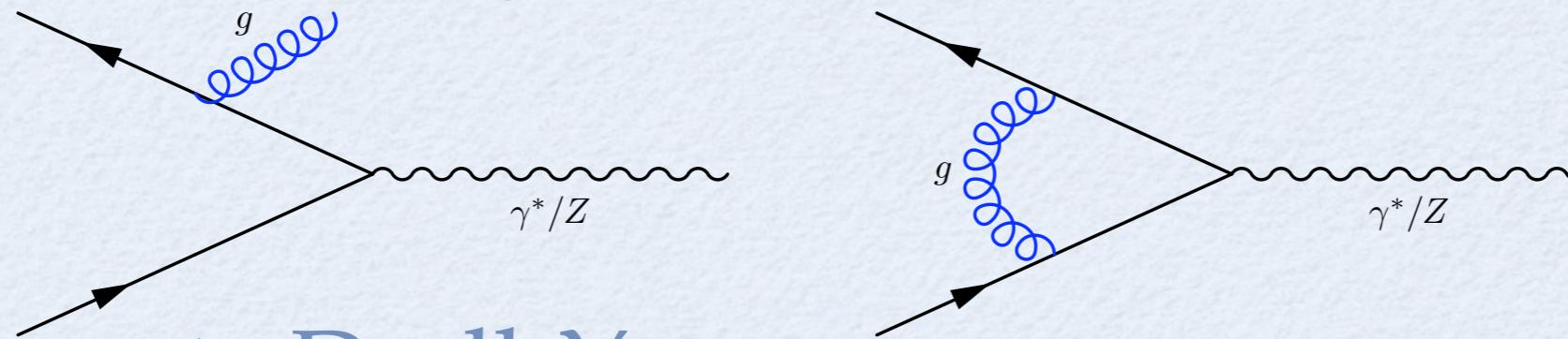
- “Master” formula to estimate **cross section** or **luminosity**:

$$\sigma(pp \rightarrow Z/\gamma^* \rightarrow \mu^+ \mu^-) = \frac{N_{\text{cand}} (1 - f_{b\bar{b}}) (1 - f_{t\bar{t}}) (1 - f_{\text{cosmics}}) (1 - f_{\tau\tau}) (1 - f_{pp \rightarrow \mu X}) (1 - f_{W \rightarrow \mu\nu})}{\epsilon_{\text{total}} \int L dt}$$

- $f_i$ : Fraction of candidate events attributed to  $b\bar{b}$  ( $t\bar{t}$ ), cosmic  $\mu$ ,  $Z \rightarrow \tau\tau$ ,  $pp \rightarrow \mu X$  and  $W \rightarrow \mu\nu$ .
- $\epsilon_{\text{total}}$  : Efficiency of selection cuts and detector acceptance.

# MC@NLO

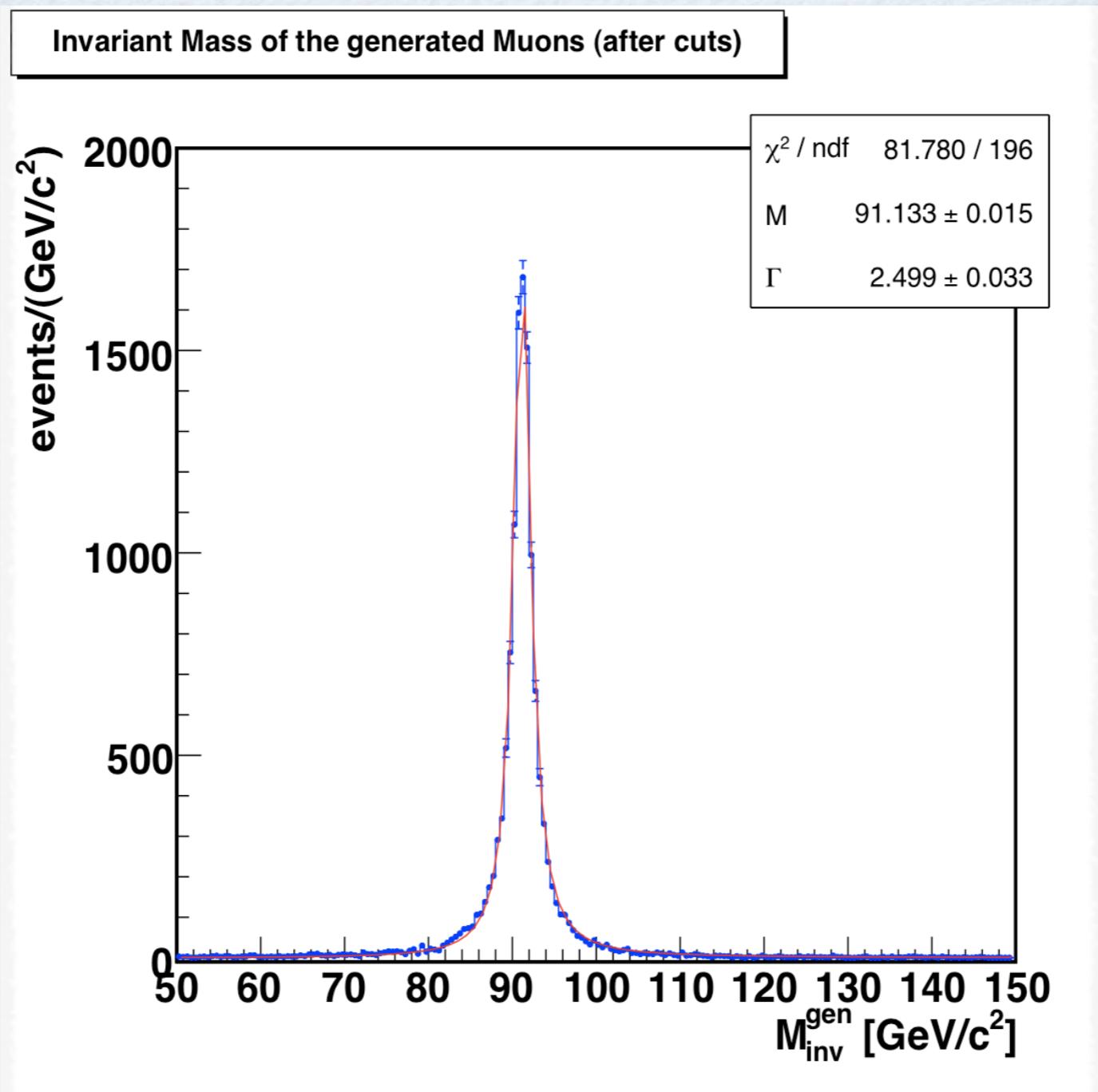
- Reminder: crucial for precision measurements.
- Using MC@NLO:  $\mathcal{O}(\alpha_s)$  (Frixione, Webber; [hep-ph/0204244](#), [hep-ph/0305252](#))
- NLO provides a more accurate answer for the integrated cross section.
- MC@NLO computes all QCD NLO diagrams before starting the shower.



- generate Drell-Yan processes ...  $Z \rightarrow \mu\mu$   
... use Herwig for showering ...  
... do full CMS detector simulation ...

# GENERATOR CHECK #1

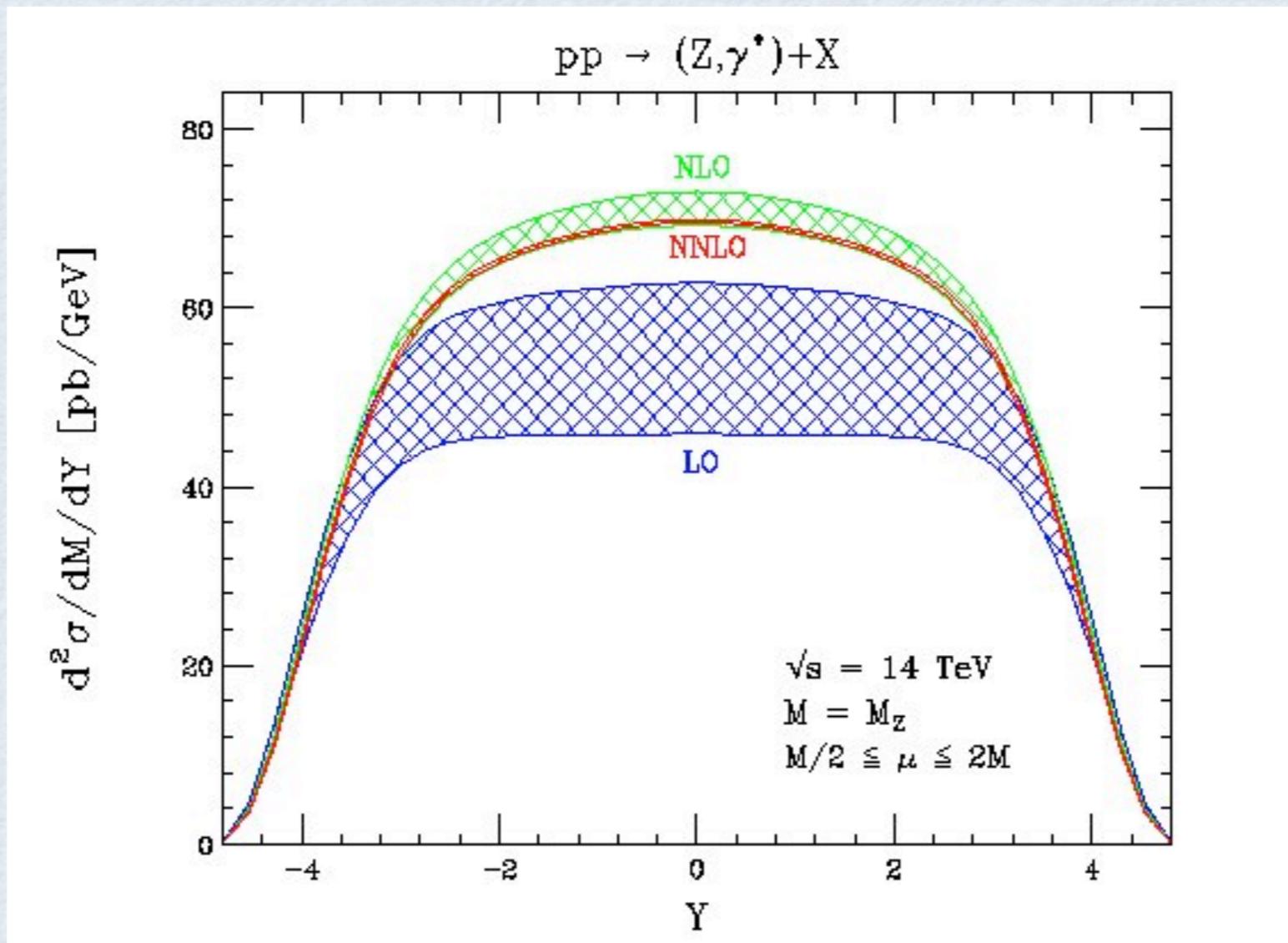
- MC@NLO: Z mass from generator



mass, width and Breit-Wigner fit okay...

# GENERATOR CHECK #2

Check MC@NLO with independent calculations:



(From Anastasiou et al,  
[hep-ph/0312266](https://arxiv.org/abs/hep-ph/0312266))

- Integration yields the total cross section times branching ratio. Assume **narrow width** approximation in  $M$  and integrate over  $\eta$  numerically ( $Y = \eta$ ).

# GENERATOR CHECK #2

- Results after integrating the plot:

LO, lower edge	$\sigma = 1.389 \text{ nb}$	very unsafe
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NLO	$\sigma = 2.011 \text{ nb}$	rather safe
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- For comparison with our simulation:

MC@NLO, NLO:  $\sigma = 1.910\text{-}2.053 \text{ nb}$  depending  
on PDF.

- Agreement nice!

- **Strategy:** Using MC@NLO as the generator  
and NNLO calculations for the cross section.

# $Z$ PRODUCTION: $\mathcal{O}(\alpha_s^2)$

- QCD **NNLO**<sup>a</sup>: Spin correlations and  $\gamma$ - $Z$  interference included.
- FEWZ is not a generator!
- Is able to calculate Xsec in LO, NLO and NNLO:
  - $\sigma_{\gamma^*/Z \rightarrow \mu\mu} = (2.031 \pm 0.002) \text{ nb } NLO$
  - $\sigma_{\gamma^*/Z \rightarrow \mu\mu} = (1.988 \pm 0.014) \text{ nb } MC@NLO$
  - ... using the same PDFs and  $66 \text{ GeV} \leq m_{\mu\mu} \leq 166 \text{ GeV}$
- $\gamma$  contribution added for MC@NLO.
- Renormalization and factorization scales equal.
- **Agreement** within  $\Delta \approx 2 \%$ .

# CROSS SECTION FOR NNLO

- Varying the renormalization  $\mu_r$  and factorization  $\mu_f$  scales.

$$\mu_r = \mu_f = m_Z$$

$$\sigma_{\gamma^*/Z \rightarrow \mu\mu} = (1.964 \pm 0.020) \text{ nb}$$

$$\mu_r = \mu_f = \frac{1}{2} m_Z$$

$$\sigma_{\gamma^*/Z \rightarrow \mu\mu} = (1.971 \pm 0.018) \text{ nb}$$

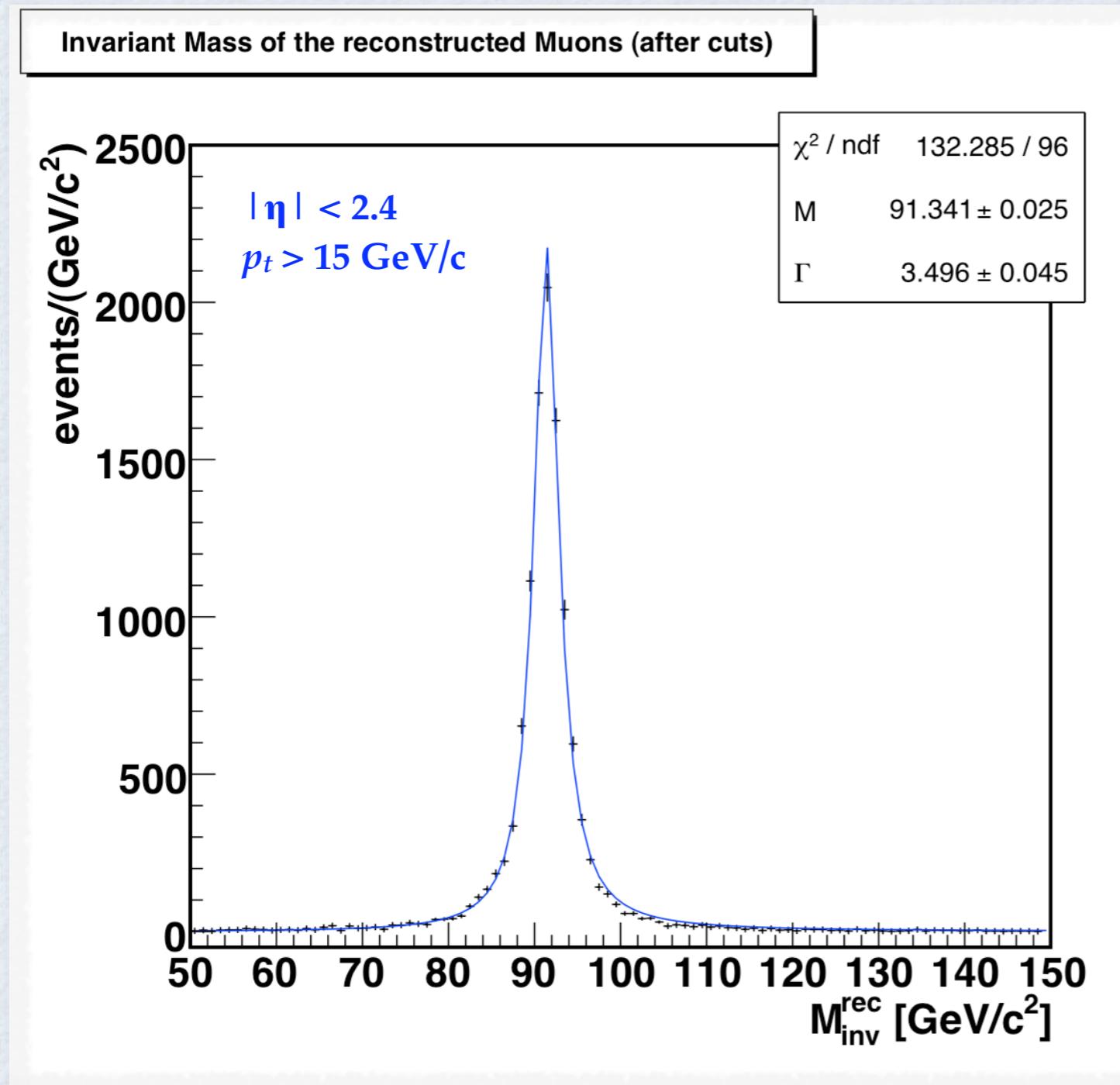
$$\mu_r = \mu_f = 2 m_Z$$

$$\sigma_{\gamma^*/Z \rightarrow \mu\mu} = (1.994 \pm 0.020) \text{ nb}$$

- Independent on scales!
- Slightly smaller than NLO from this calculation.
- Same check performed for **MC@NLO** with similar result!

# INVARIANT MASS

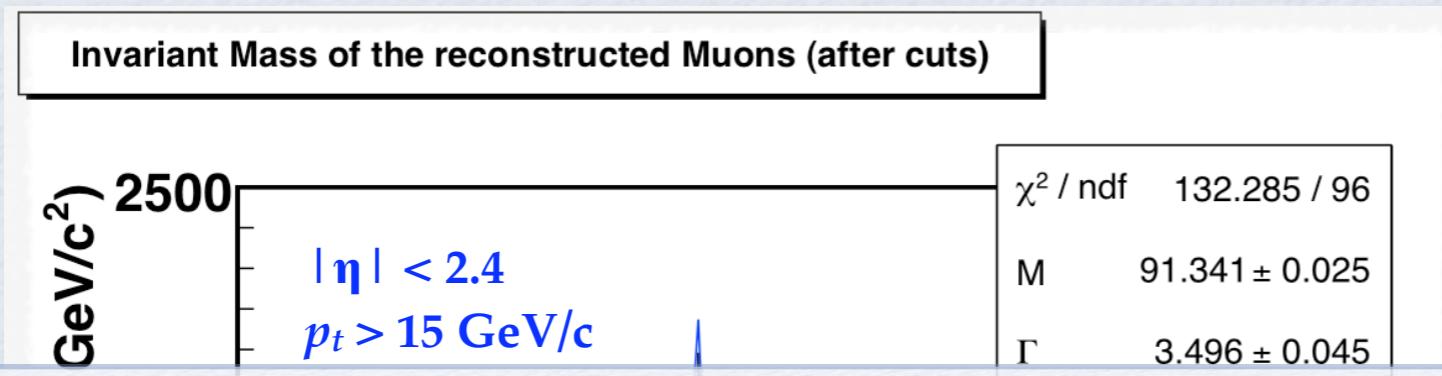
Mass Z after reconstructing 2  $\mu$ 's



- Fit is good with Breit-Wigner alone. This is in principle wrong and just by chance.

# INVARIANT MASS

Mass  $Z$  after reconstructing 2  $\mu$ 's

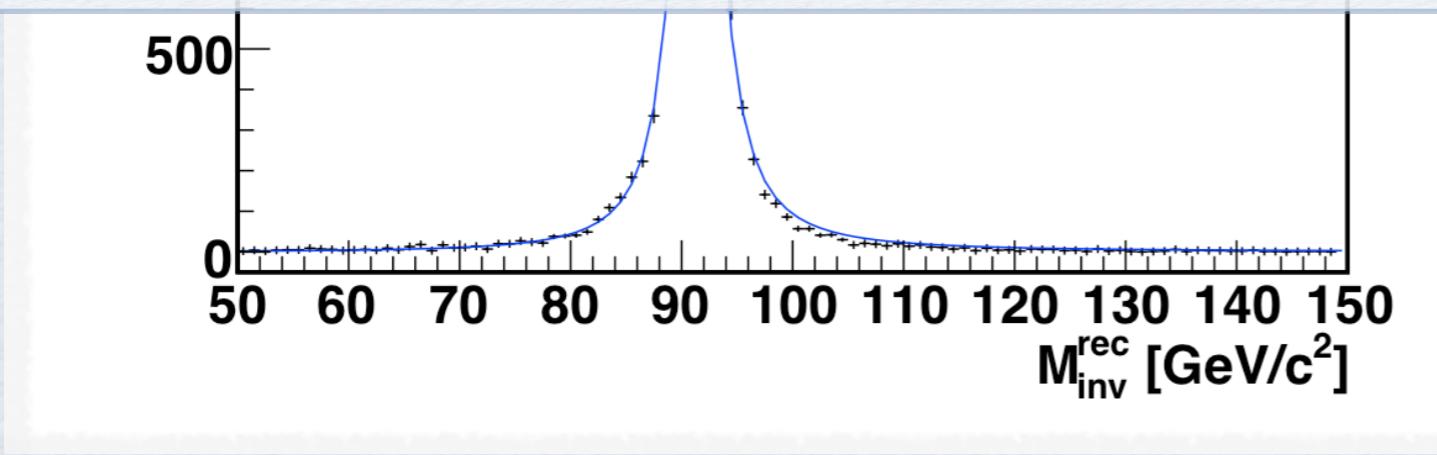


- What do we expect for the width? Important to get  $N_{cand}$  right.

$$\sigma(pp \rightarrow Z/\gamma^* \rightarrow \mu^+ \mu^-) = \frac{N_{cand} (1 - f_{b\bar{b}}) (1 - f_{t\bar{t}}) (1 - f_{\text{cosmics}}) (1 - f_{\tau\tau}) (1 - f_{pp \rightarrow \mu X}) (1 - f_{W \rightarrow \mu\nu})}{\epsilon_{total} \int L dt}$$

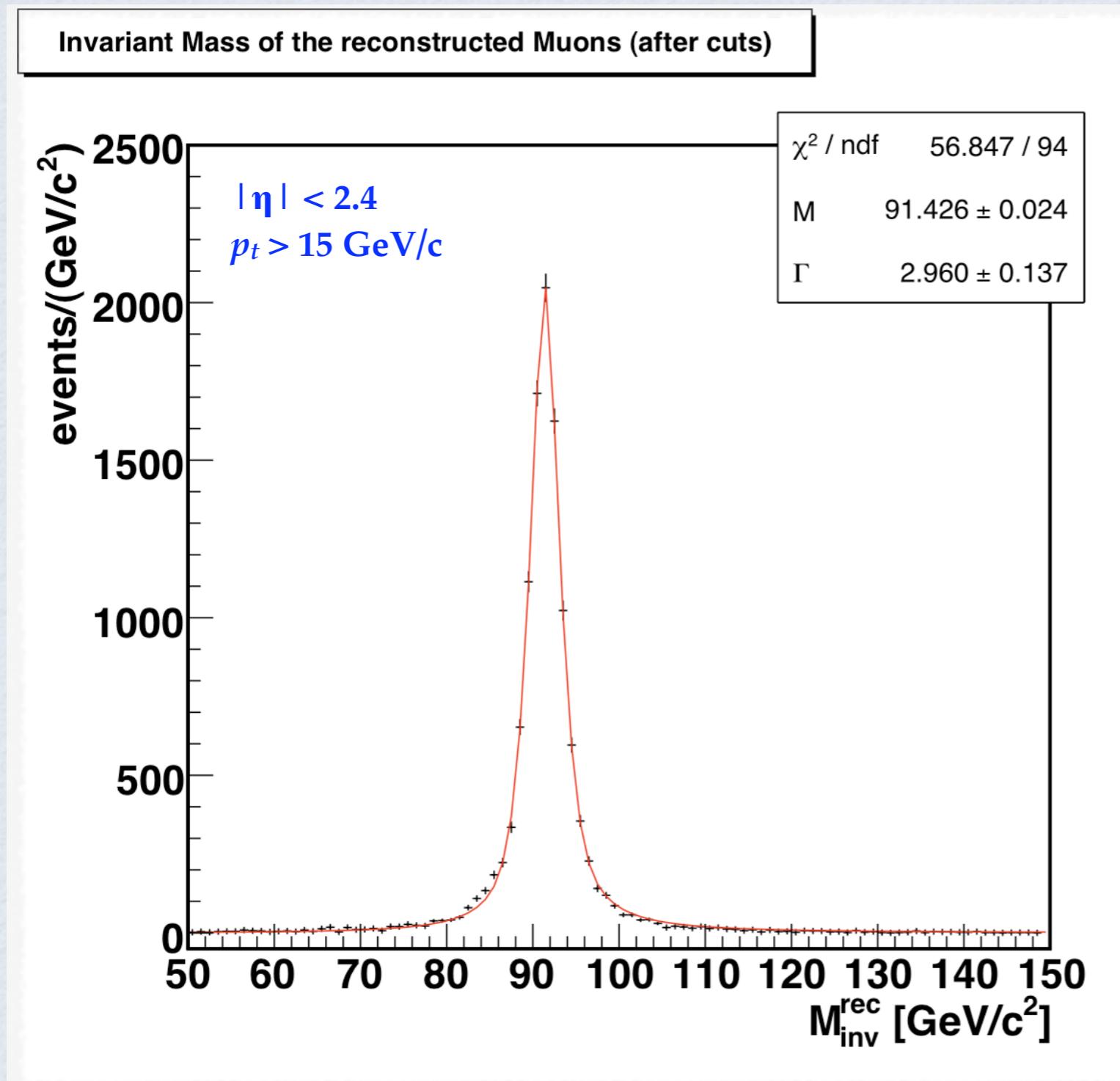


study the width into more detail...



# INVARIANT MASS

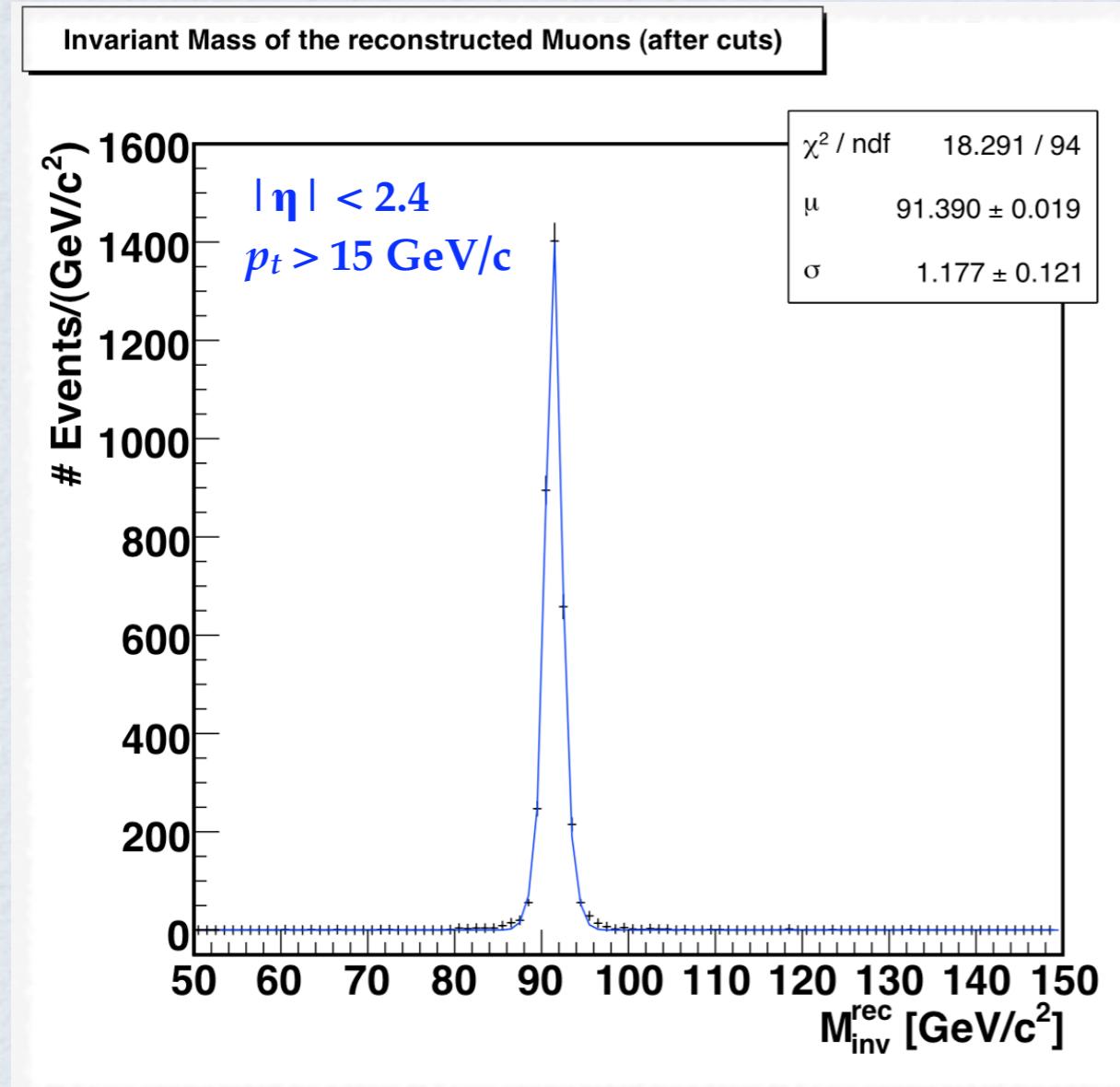
Mass  $Z$  after reconstructing 2  $\mu$ 's... another fit



- Fit in peak region okay with **Breit-Wigner + one Gaussian** (in principle one should fit more Gaussians...)
- We expect from  $Z$  width and detector resolution a width of  $2.8 \text{ GeV}/c^2$ .

# INVARIANT MASS

Mass Z after reconstructing 2  $\mu$ 's from narrow width Z



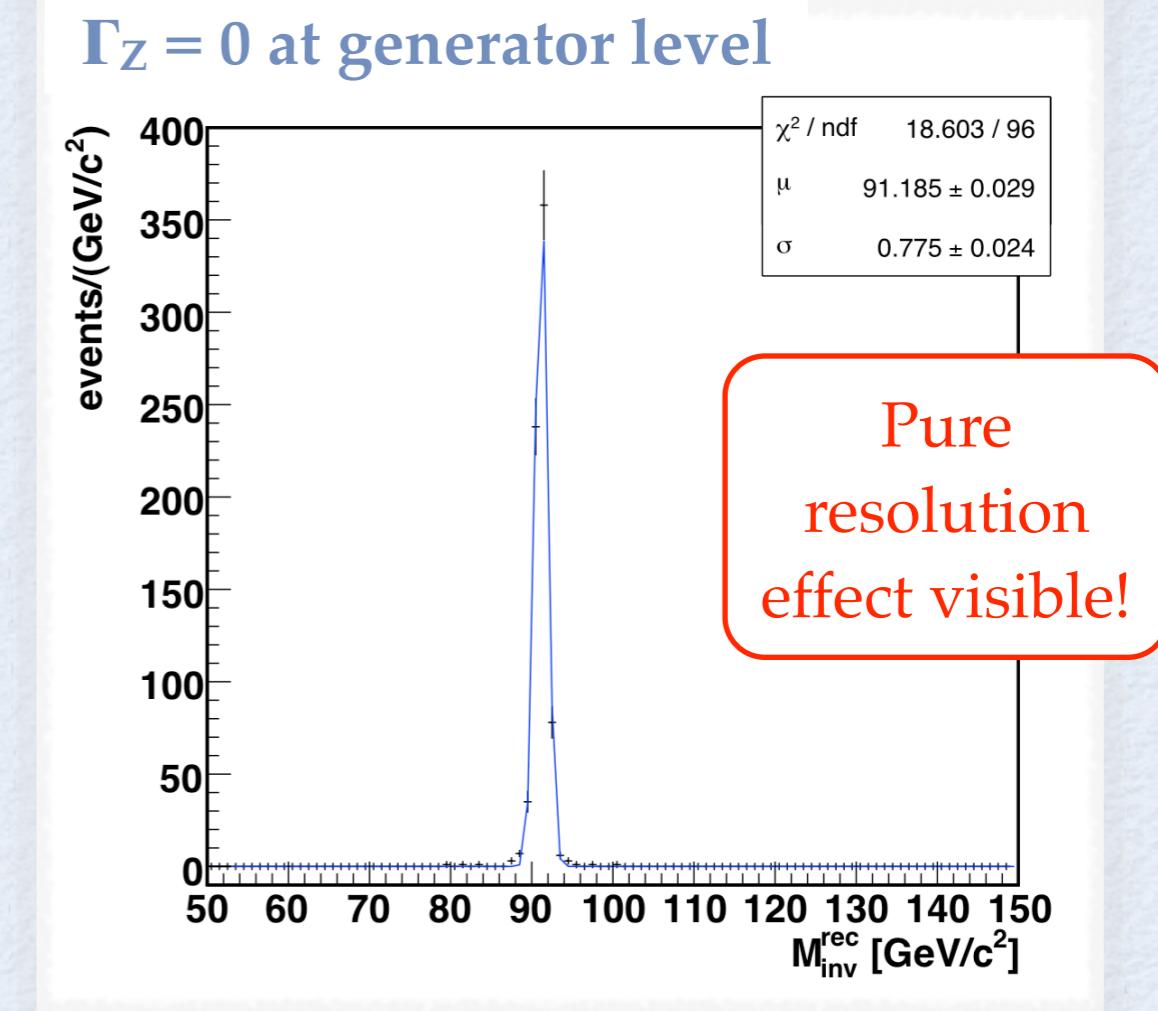
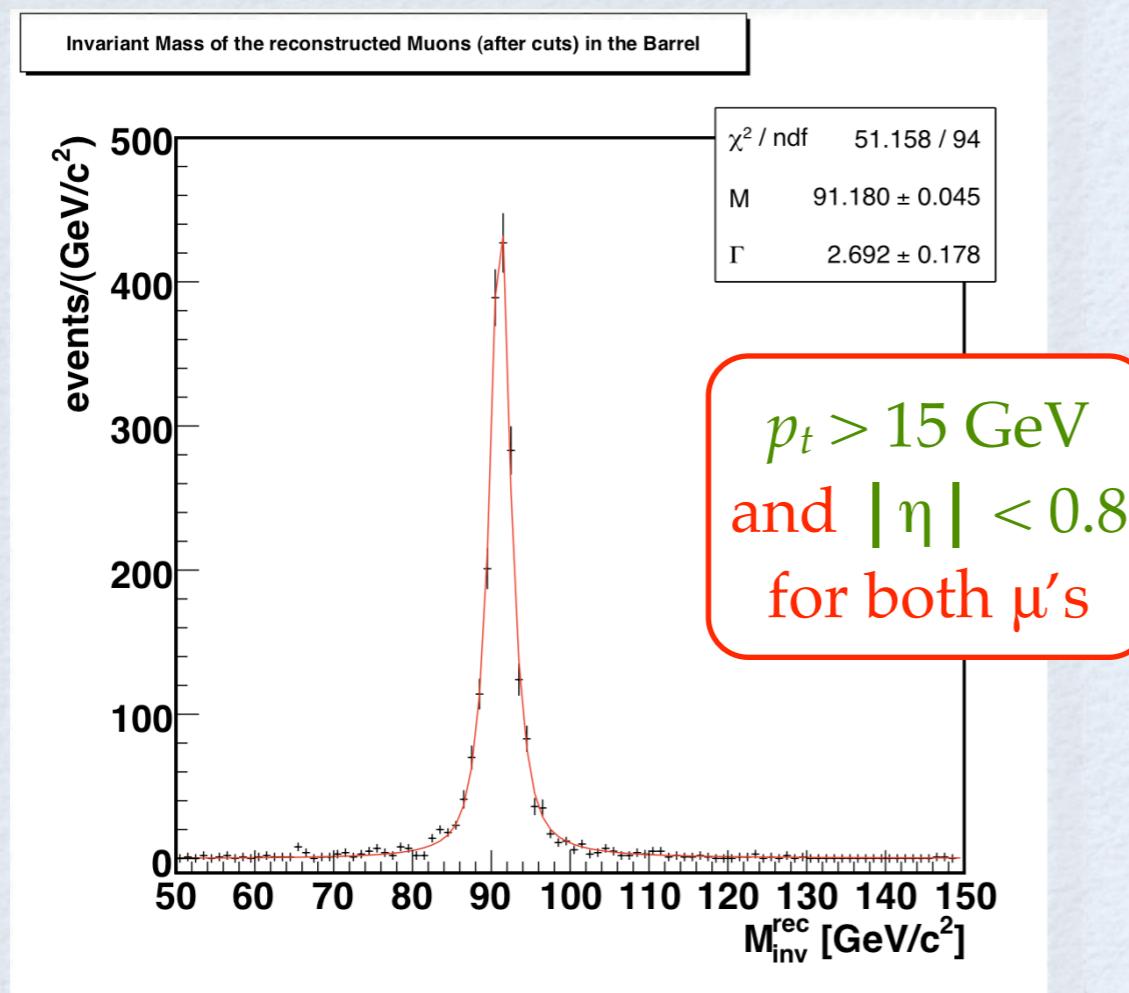
Pure  
resolution  
effect  
visible!

Width = 1.18 GeV/c<sup>2</sup>

- Fit with 2 Gaussians, detector resolution only!
- We find what we roughly expect from naive calculations.

# INVARIANT MASS

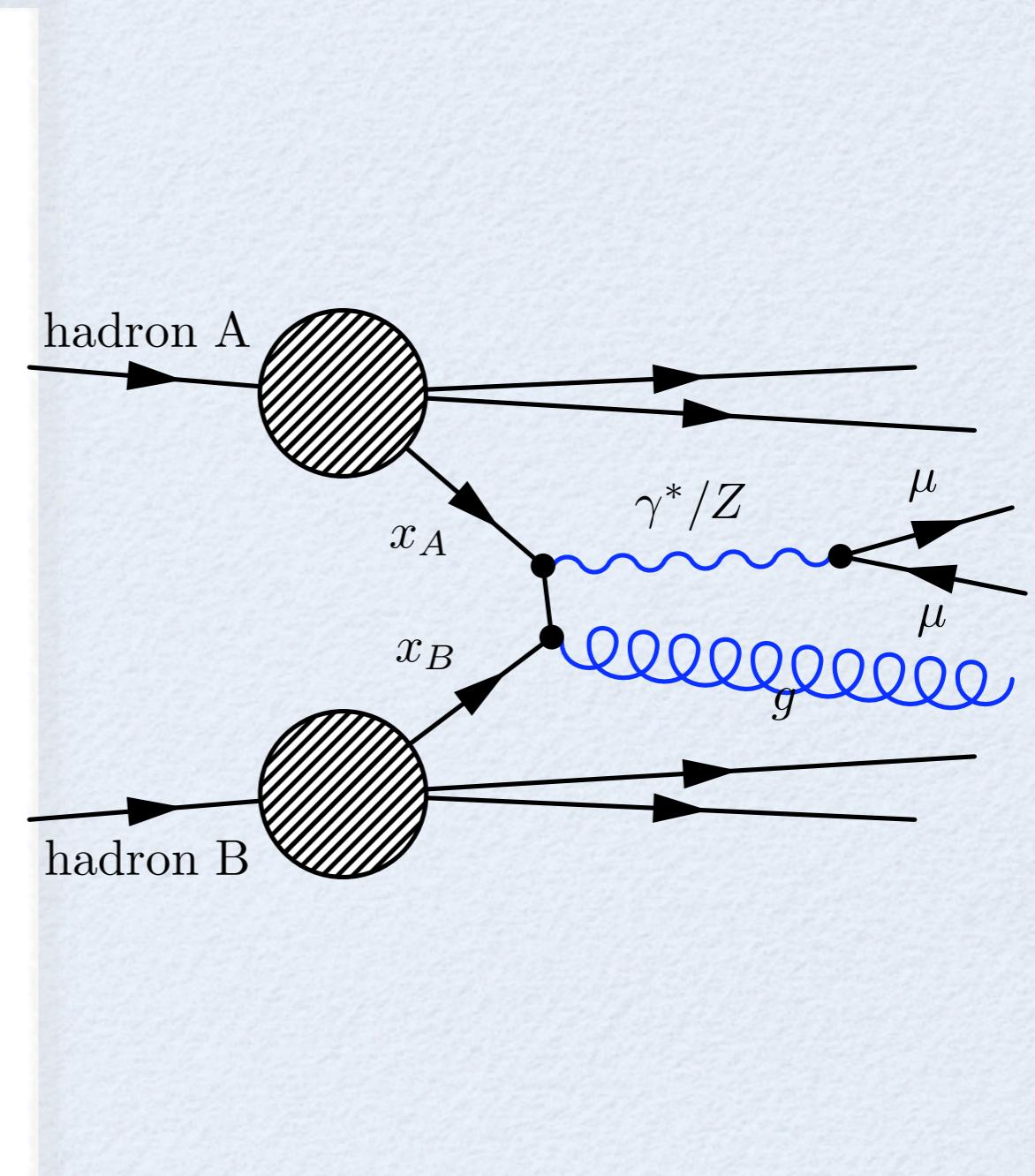
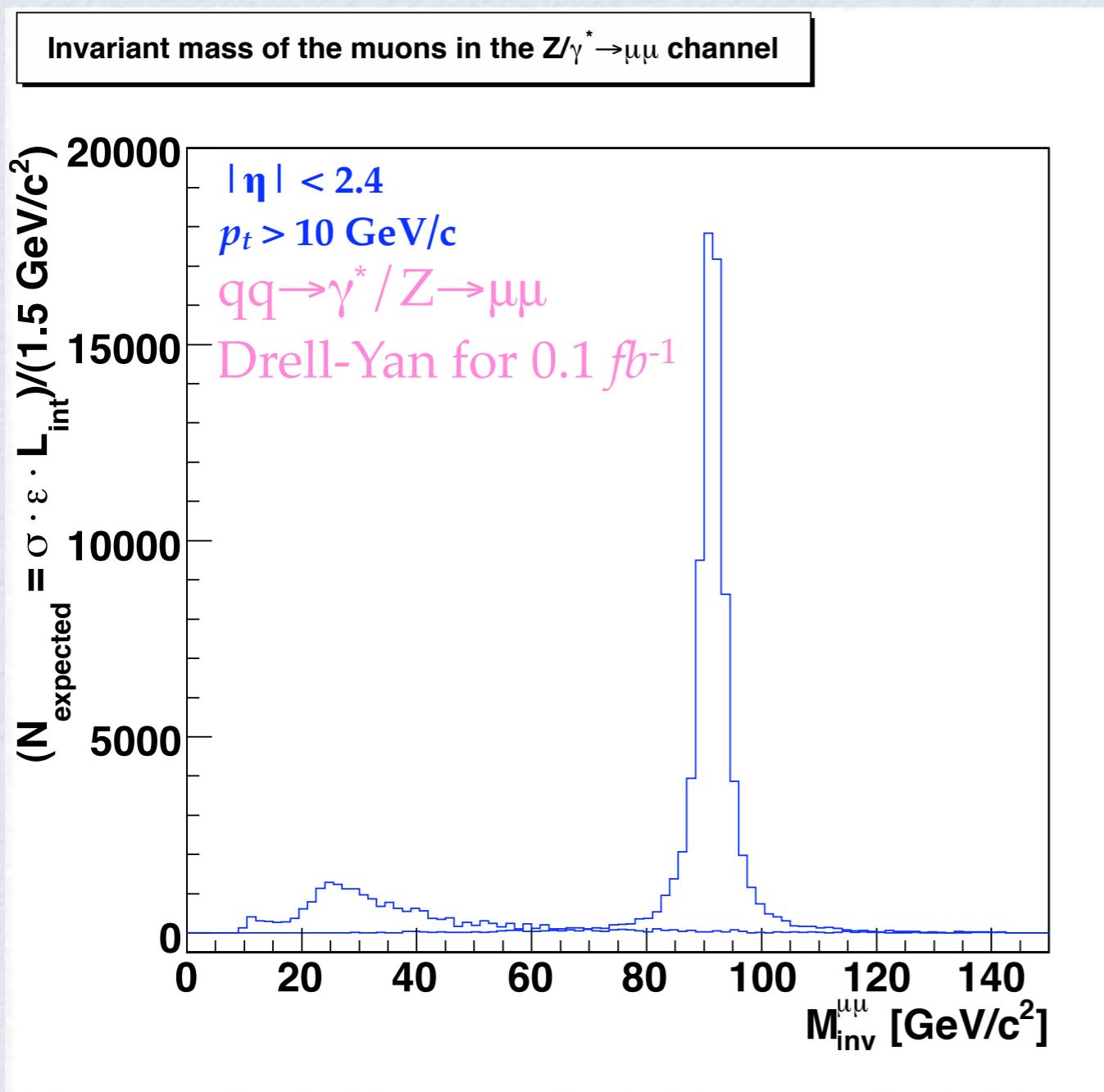
Mass Z after reconstructing 2  $\mu$ 's in **barrel** region



- Breit-Wigner and Gaussian fitted.
- Width  $2.63 \text{ GeV}/\text{c}^2$  expected in this region.
- 2 Gaussians fitted:  $\sigma = 0.78 \text{ GeV}/\text{c}^2$ .
- From the fit we obtain  $(2.69 \pm 0.18) \text{ GeV}/\text{c}^2$ !

$$pp \rightarrow \gamma^*/Z \rightarrow \mu^+ \mu^- + X$$

Expected number of  $\mu\mu$  events for  $0.1 fb^{-1}$  for the LHC with the CMS detector:



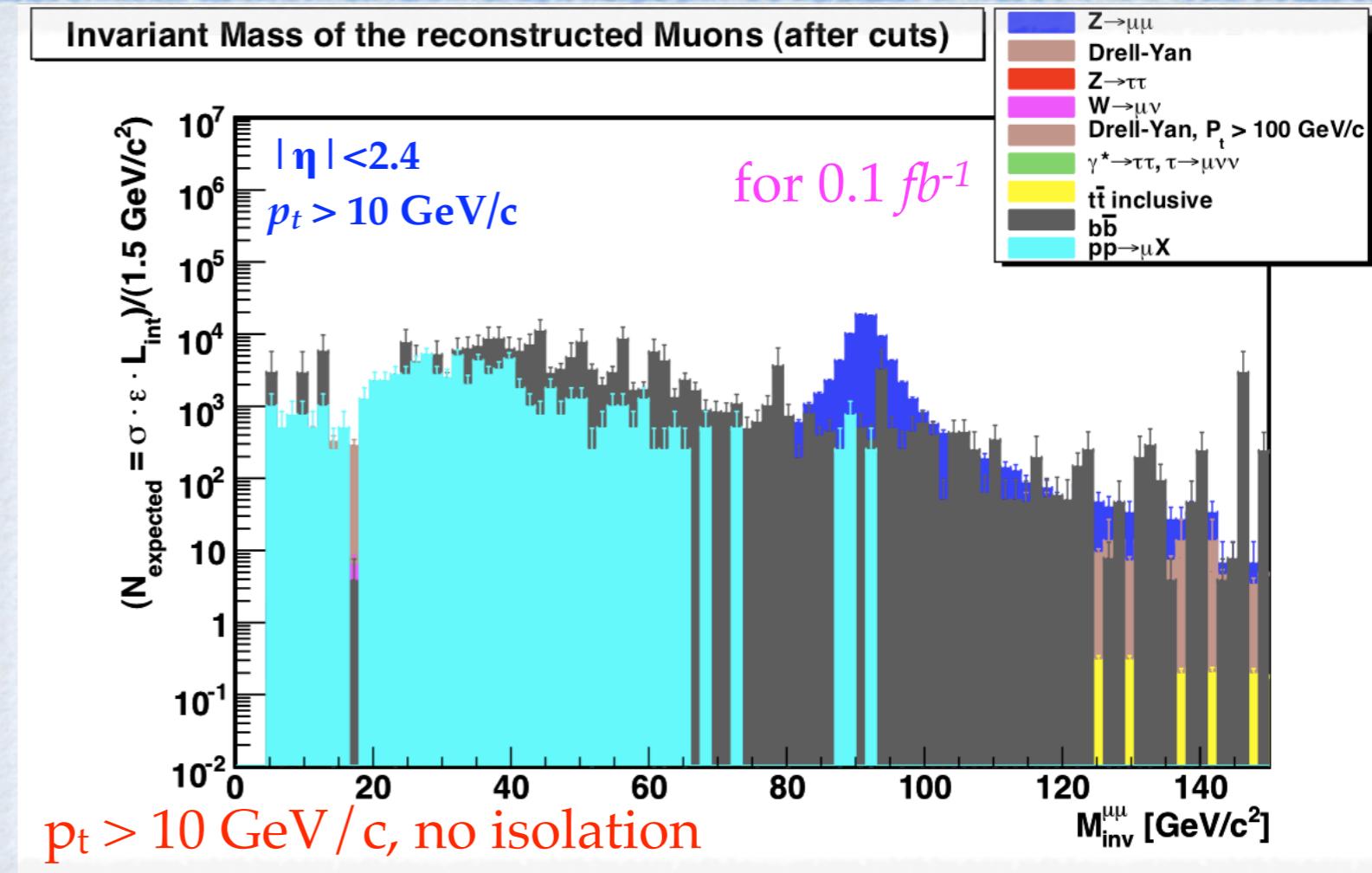
# BACKGROUND

- $f_{b\bar{b}}$  ( $f_{t\bar{t}}$ ) from data (e.g. isolation criteria).
- $f_{\tau\tau}$  irreducible (e.g. from MC)!!
- $f_{W \rightarrow \mu\nu}$  from data (e.g. # candidate events  $\geq 2\mu$ ).
- $f_{pp \rightarrow \mu X}$ : events stemming from  $qq \rightarrow qq$ ,  $gg \rightarrow gg$ ,  $gq \rightarrow gq$  and  $gg \rightarrow qq$  processes.
- $f_{\text{cosmics}}$  from data (e.g. time info!?).

$$\sigma(pp \rightarrow Z/\gamma^* \rightarrow \mu^+ \mu^-) = \frac{N_{\text{cand}} (1 - f_{b\bar{b}}) (1 - f_{t\bar{t}}) (1 - f_{\text{cosmics}}) (1 - f_{\tau\tau}) (1 - f_{pp \rightarrow \mu X}) (1 - f_{W \rightarrow \mu\nu})}{\epsilon_{\text{total}} \int L dt}$$

# SIGNAL & BACKGROUND

- Main contribution from  $b\bar{b}$  events.

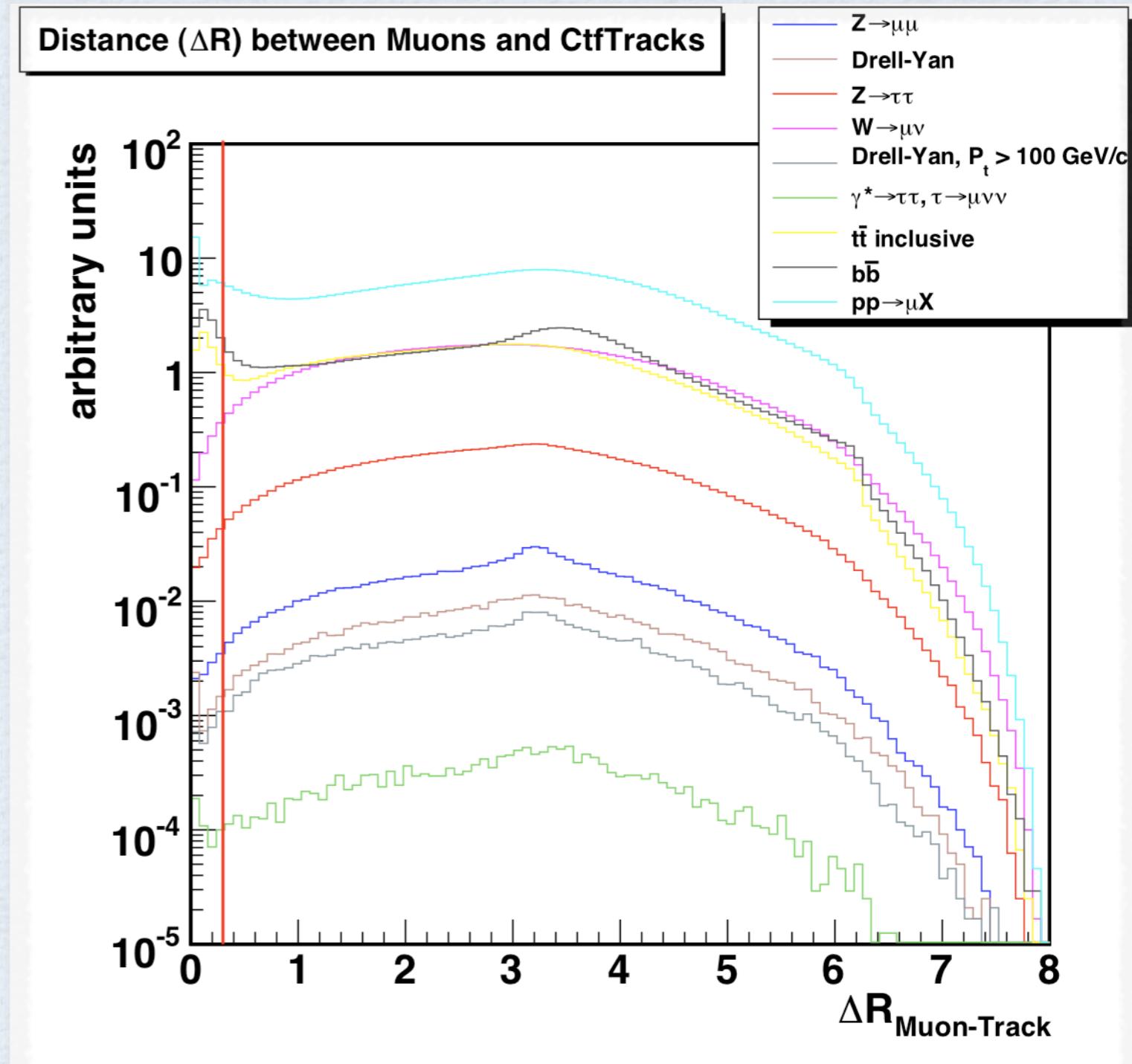


Background	$p_t > 10 \text{ GeV}/c$	$p_t > 15 \text{ GeV}/c$	$p_t > 20 \text{ GeV}/c$	$p_t > 25 \text{ GeV}/c$
$pp \rightarrow \mu + X$	$1.81 \cdot 10^{-2}$	$7.43 \cdot 10^{-3}$	$8.16 \cdot 10^{-3}$	$< 8 \cdot 10^{-3}$
$b\bar{b}$	$7.89 \cdot 10^{-2}$	$7.23 \cdot 10^{-2}$	$2.31 \cdot 10^{-2}$	$1.32 \cdot 10^{-2}$
$W \rightarrow \mu\nu$	$4.85 \cdot 10^{-4}$	$3.23 \cdot 10^{-4}$	$2.81 \cdot 10^{-4}$	$1.67 \cdot 10^{-4}$
$t\bar{t}$	$7.17 \cdot 10^{-5}$	$6.56 \cdot 10^{-5}$	$5.79 \cdot 10^{-5}$	$4.72 \cdot 10^{-5}$
$pp \rightarrow \gamma^* / Z \rightarrow \tau\tau$	$5.78 \cdot 10^{-6}$	$5.93 \cdot 10^{-6}$	$5.49 \cdot 10^{-6}$	$5.22 \cdot 10^{-6}$

Background / signal ratios  $f_i$  in  
 $85.6 \text{ GeV}/c^2 \leq M \leq 97.2 \text{ GeV}/c^2$ .

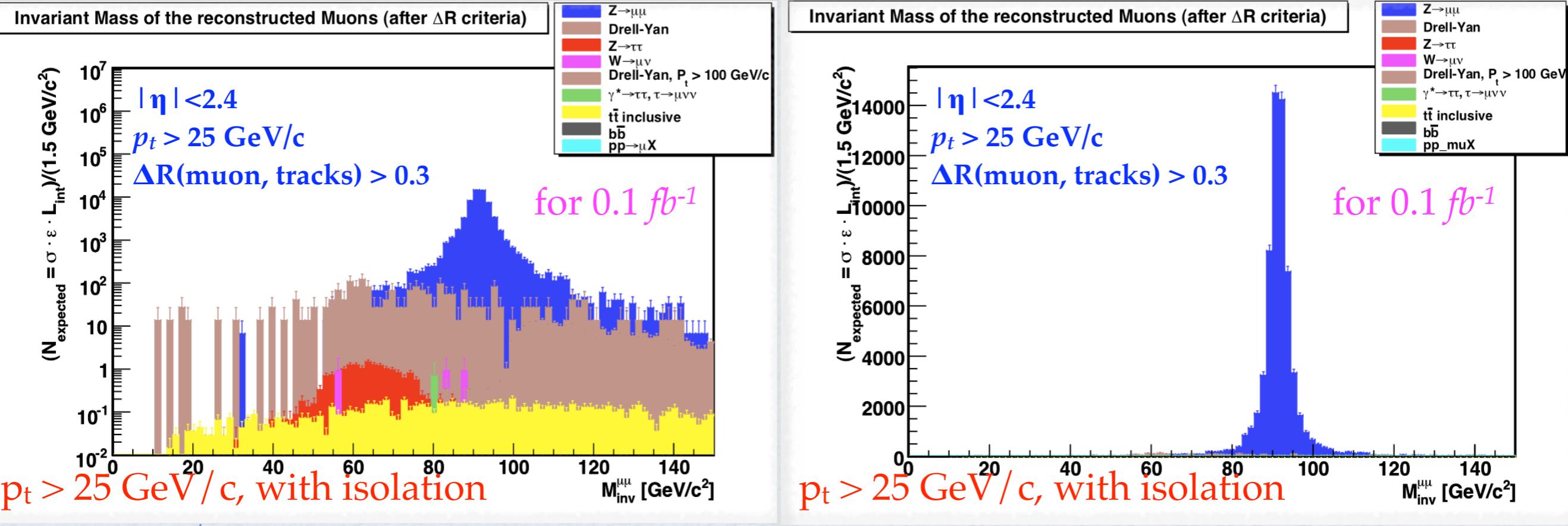
# MUON TRACK DISTANCE

- Background can be reduced by requiring **isolated** muons.
- Consider a muon isolated if no tracks are present in a cone  $\Delta R < 0.3$  around the muon.



$$\Delta R(\text{muon, track}) = \sqrt{(\eta_{\text{muon}} - \eta_{\text{track}})^2 + (\varphi_{\text{muon}} - \varphi_{\text{track}})^2}$$

# SIGNAL & BACKGROUND

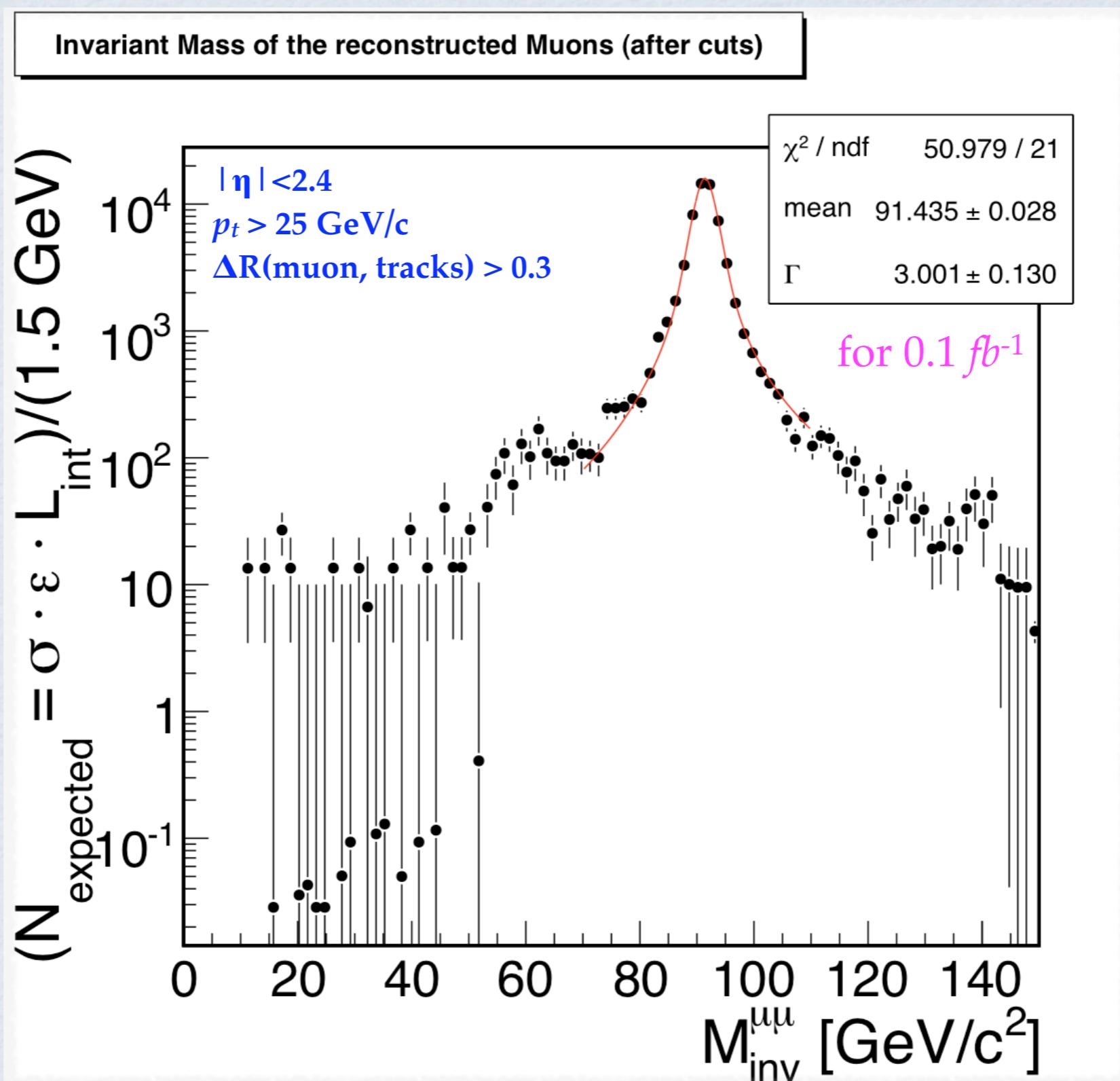


Background/signal ratios  $f_i$  in  
 $85.6 \text{ GeV}/c^2 \leq M \leq 97.2 \text{ GeV}/c^2$ :

Background	$p_t > 10 \text{ GeV}/c$	$p_t > 15 \text{ GeV}/c$	$p_t > 20 \text{ GeV}/c$	$p_t > 25 \text{ GeV}/c$
$pp \rightarrow \mu + X$	$< 10^{-3}$	$< 10^{-3}$	$< 10^{-3}$	$< 10^{-3}$
$b\bar{b}$	$< 10^{-3}$	$< 10^{-3}$	$< 10^{-3}$	$< 10^{-3}$
$W \rightarrow \mu\nu$	$4.29 \cdot 10^{-5}$	$2.93 \cdot 10^{-5}$	$1.54 \cdot 10^{-5}$	$1.65 \cdot 10^{-5}$
$t\bar{t}$	$2.58 \cdot 10^{-5}$	$2.54 \cdot 10^{-5}$	$2.32 \cdot 10^{-5}$	$2.11 \cdot 10^{-5}$
$pp \rightarrow \gamma^*/Z \rightarrow \tau\tau$	$4.56 \cdot 10^{-6}$	$4.67 \cdot 10^{-6}$	$3.76 \cdot 10^{-6}$	$4.05 \cdot 10^{-6}$

**Summary:** the number of  $\mu\mu$  pairs from other sources than  $Z$  or  $\gamma^*$  is rather small!!

# INCLUSIVE DI $\mu$ MASS



# SYSTEMATICS

Systematic uncertainties due to:

- PDFs
- Muon and Tracker alignment
- Trigger
- Magnetic field
- ...

# SYSTEMATIC ERROR

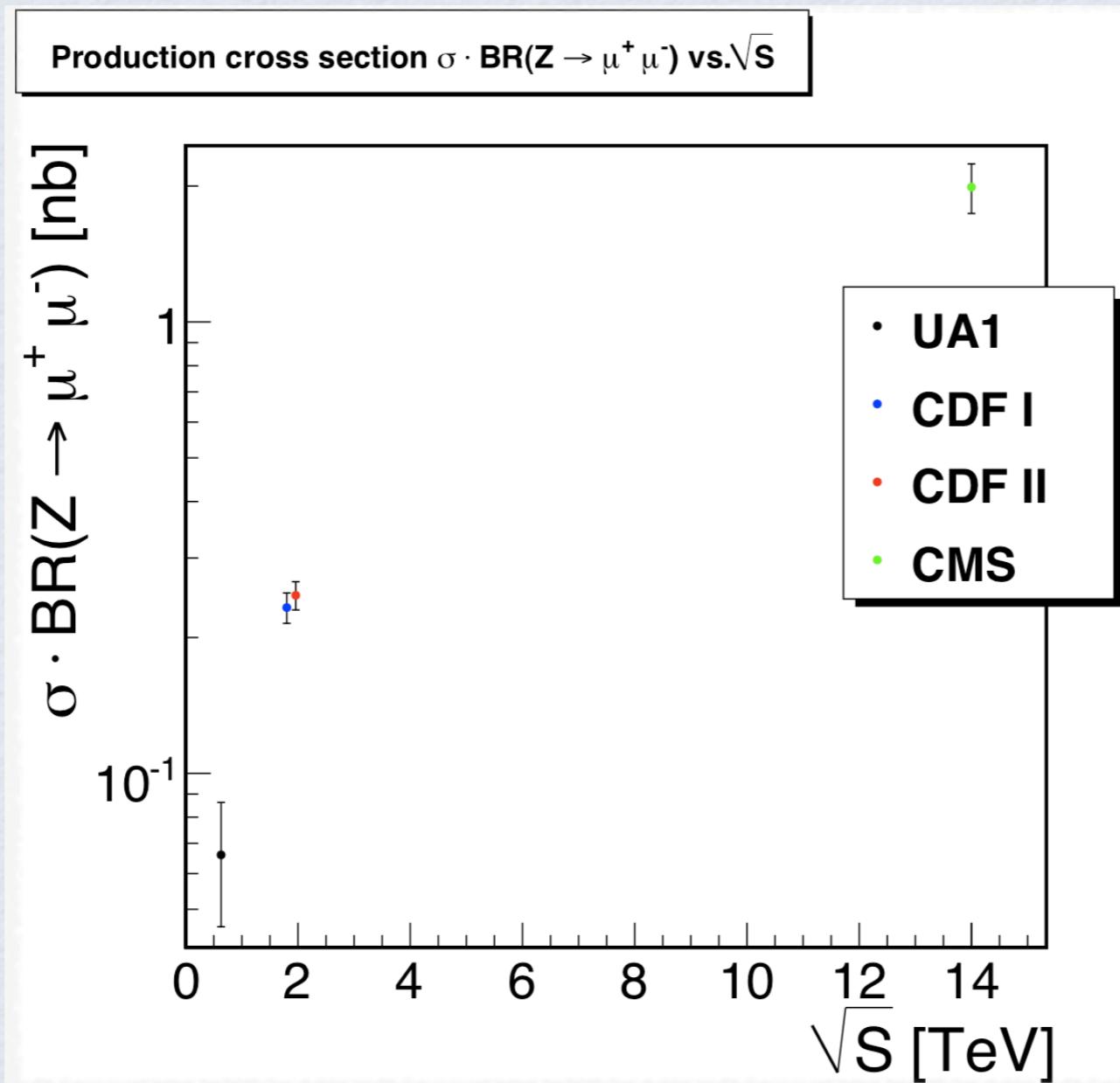
- Contributions to the total systematic uncertainty from:
  - Alignment:  $\sigma^{\text{alignment}} = 2.9\%$
  - PDF:  $\sigma^{\text{PDF}} = 3.8\%$  (cross section),  $1.9\%$  (acceptance)
  - Trigger:  $\sigma^{\text{HLT}} = 0.8\%$
  - B field:  $\sigma^{\text{B field}} = 0.5\%$  (CMS AN-2007/031)
- Total systematic uncertainty:
$$\sigma^{\text{sys}} = \sigma^{\text{alignment}} \oplus \sigma^{\text{PDF}} \oplus \sigma^{\text{HLT}} \oplus \sigma^{\text{B field}} \approx 5\% \text{ (4\%)}$$
- Finally we obtain a systematic uncertainty  $\sigma^{\text{sys}} \approx 5\%$  for luminosity and  $\sigma^{\text{sys}} \approx 4\%$  for cross section measurement.

# FINAL RESULTS

- Final results: production cross section or luminosity:
  - Cross section (with  $\epsilon = (31.19 \pm 0.56)\%$  and assuming  $L = (0.10 \pm 0.01) fb^{-1}$ ):  
$$\sigma_{pp \rightarrow \gamma^*/Z \rightarrow \mu\mu} = (1.989 \pm 0.114^{\text{stat}} \pm 0.071^{\text{sys}} \pm 0.199^{\text{lumi}}) \text{ nb.}$$
  - Luminosity (with  $\sigma_{\text{NNLO}} = (1.964 \pm 0.020) \text{ nb}$ ):  
$$L = (0.100 \pm 0.006^{\text{stat}} \pm 0.005^{\text{sys}}) \text{ fb}^{-1}.$$

# FINAL RESULTS

- Compare cross section measurement with other  $pp$  and  $p\bar{p}$  experiments:



UA1: Albajar et al,  
[Phys. Lett. B198 \(1987\)](#)  
CDF I: Abe et al, [Phys. Rev. D 59\(5\) \(Jan 1999\)](#)  
CDF II: Acosta et al,  
[Phys. Rev. Lett. 94 \(2005\)](#)

$$\sigma_{pp \rightarrow \gamma^*/Z0 \rightarrow \mu\mu} = (1.989 \pm 0.114^{\text{stat}} \pm 0.071^{\text{sys}} \pm 0.199^{\text{lumi}}) \text{ nb.}$$

# SUMMARY

- Z production in high energy  $pp$  collisions has a clean signature through e.g.  $Z \rightarrow \mu\mu$ .
- The background is very low.
- **Potential luminosity monitor:** the most important ingredient is the accuracy to which the cross section for Z production can be theoretically calculated. We find in this analysis that the accuracy of the luminosity measurement  $\approx 7\%$ .
- **Cross section:** if we determine the cross section the main uncertainty stems from the error of the luminosity, at least at the beginning of data taking.