

QCD and electroweak physics at the LHC

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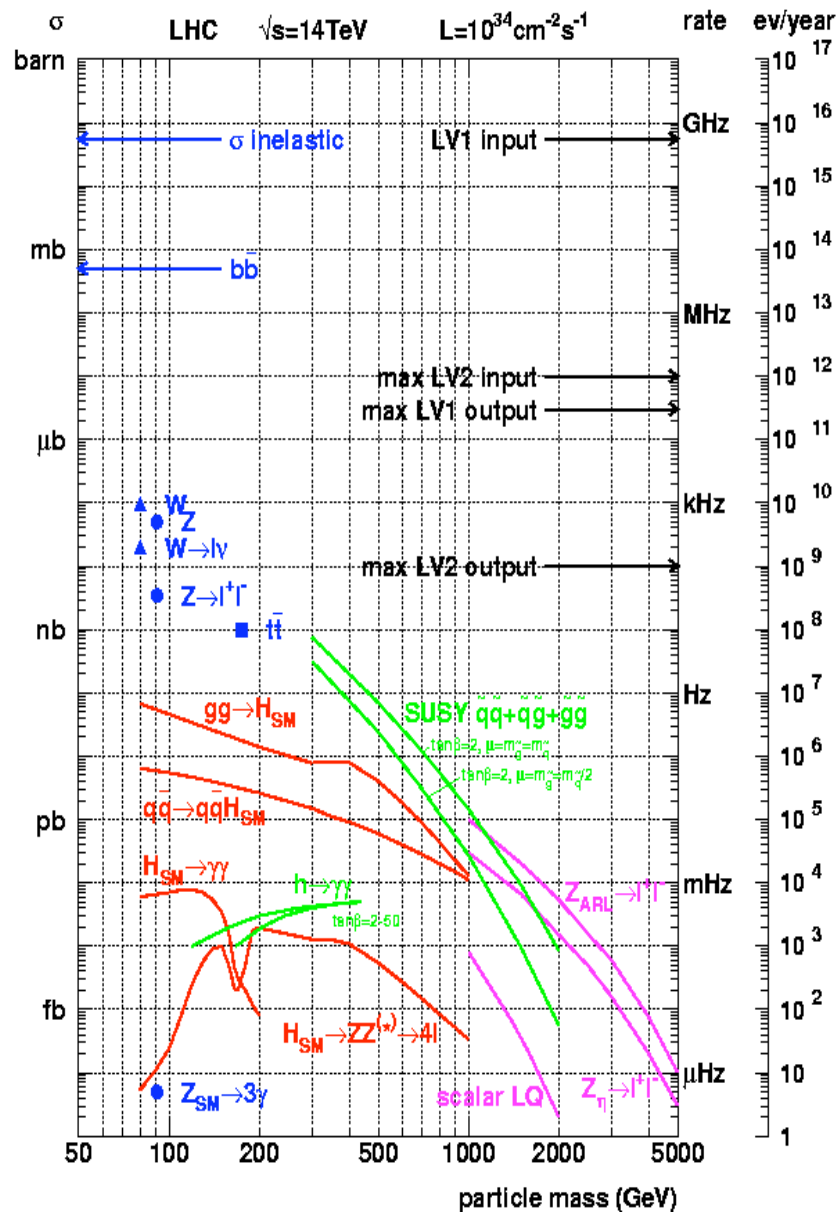
Meeting of the Helmholtz Alliance “*Physics at the Terascale*”

RWTH Aachen, November 28, 2008

Outline of the talk

- (1) **Introduction** - (some of the) activities of the EW/QCD working group
- (2) **QCD hard scattering** - from LO to NNLO
- (3) **EW corrections** - selected topics

(1) The EW/QCD working group and the LHC



SM (mostly) without Higgs and top

- gauge bosons (Drell Yan, GB pairs)
- jets

Well-known SM reactions

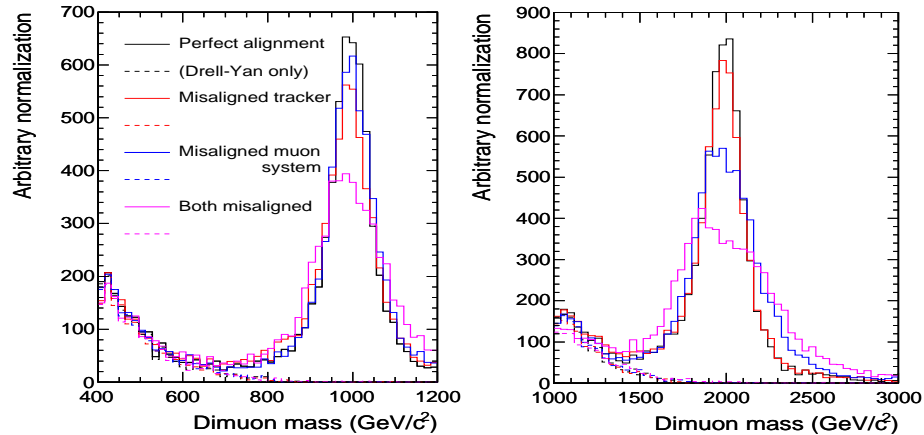
- large cross sections, clean signatures
- good theoretical description (input parameters, (N)NLO cross sections)

Importance of these reactions

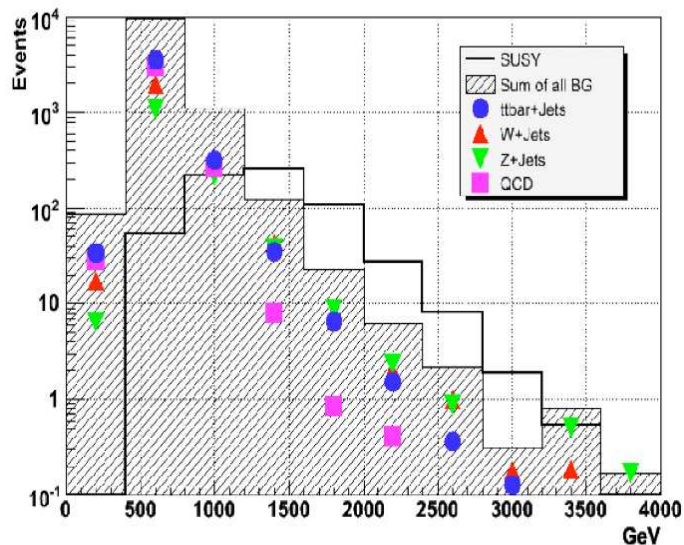
- detector calibration
- MC calibration
- measurements of luminosity, PDFs and parameters ($\alpha_S, M_W, \sin^2(\theta_{\text{eff}}), \text{TGCs}, \dots$)
- large backgrounds in NP searches

Signals and backgrounds

$Z' \rightarrow \mu^+ \mu^-$ in CMS



SUSY searches in multi-jet + \cancel{E}_T final states



Trivial backgrounds

- Two-body decays with sharp invariant-mass or Jacobian peaks
- non-hadronic final state
- background from data, role of theory prediction marginal

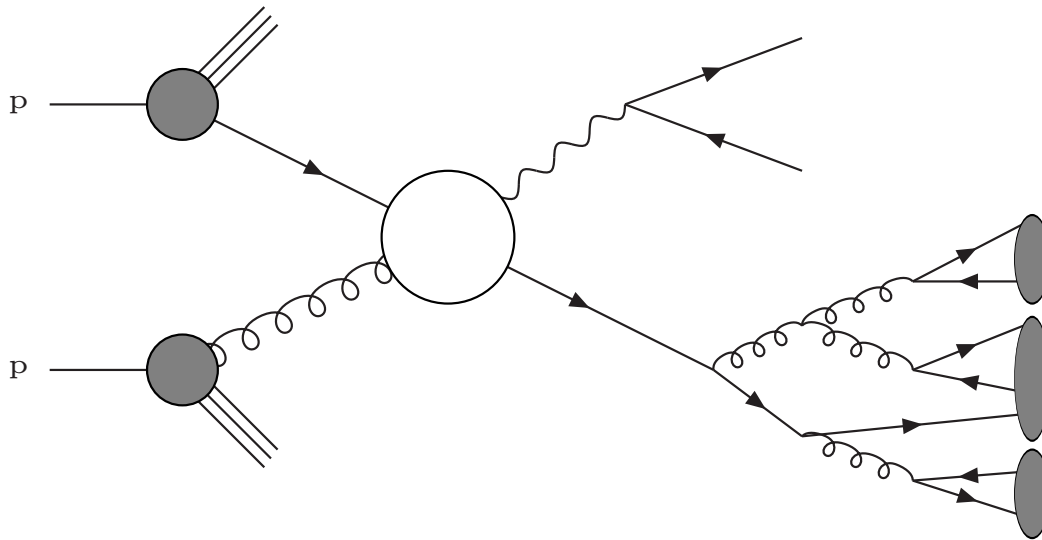
Challenging backgrounds

- jets and missing-energy in final state
- broader S distribution with shape similar as B
- requires solid prediction of B and understanding of uncertainty
- must be normalized and validated with data control samples in signal-free regions
- extrapolation into signal region driven by theory

Tools for hadronic interactions - theoretical expertise within the Helmholtz Alliance

Structure of the proton

- NNLO splitting functions [Moch/Vermaseren/Vogt](#)
- NNLO MRST PDFs [Martin/Stirling/Thorne/Watt](#)



Accurate partonic cross section

- LO, NLO, NNLO predictions (this talk)
- Resummations

Monte Carlo event generators (HERWIG, SHERPA)

- Showering and hadronization
- matching between partons and jets at LO and NLO
- Underlying events

Input parameters and fits

- precise α_S from $e^+e^- \rightarrow 3j$ at NNLO [Gehrmann-De Ridder/Gehrmann/Glover/Heinrich;Weinzierl](#)
- GFITTER

(2) QCD hard scattering

Everything involves QCD

- also purely EW reactions induced by quark scattering (at LO) receive (N)NLO QCD contributions from the gluons inside the proton

(N)NLO QCD contributions can be very large

- large gluon density at the LHC
- large size of strong coupling $\alpha_S(M_Z) \simeq 0.12$

Size of (N)NLO can be estimated

- through $\mu_{R,F}$ -dependence
- typically strong dependence from running of $\alpha_S(\mu_R)$

Importance of computing (N)NLO

- the estimates can fail (known only a posteriori)
- description of jet structure in terms of partonic constituents

Experimentalists need differential cross sections

- avoid inclusive K factors whenever possible
- experimental analysis require acceptance cuts
- cuts or jet vetos can have a strong impact on size of (N)NLO corrections and scale uncertainties

Importance of describing multi-particle final state

- signatures with many decay products from heavy unstable particles
- high probability of hard-jet emission

$\sigma(W + Nj)/\text{pb}$	$\sigma(1)$	$\sigma(2)$	$\sigma(3)$	$\sigma(4)$	$\overline{\sigma(N + 1)/\sigma(N)}$
TEVATRON	230	37	5.7	0.75	0.13
LHC	3400	1130	340	100	0.3

(2.1) LO predictions

Several automatic algorithms for multi-particle final states

- Feynman diagrams up to $2 \rightarrow 6$
(MADGRAPH, CompHEP, AMEGIC++/SHERPA, GRACE, ...)
- off-shell recursions up to $2 \rightarrow 8$ or more
(HELAC/PHEGAS, ALPHA/ALPGEN, O'MEGA/WHIZARD, ...)

Berends/Giele '88; Caravaglios/Mangano/Moretti/Pittau '99; Draggiotis/Kleiss/Papadopoulos '02

- MHV/on-shell recursions Cachazo/Svrcek/Witten '04; Britto/Cachazo/Feng/Witten '05

time [s] for 10^4 points	BG	BCF	CSW
gg \rightarrow 2g	0.28	0.33	0.26
gg \rightarrow 3g	0.48	0.51	0.55
gg \rightarrow 4g	1.04	1.32	1.75
gg \rightarrow 5g	2.69	7.26	5.96
gg \rightarrow 6g	7.19	59.1	30.6
gg \rightarrow 7g	23.7	646	195
gg \rightarrow 8g	82.1	8690	1890
gg \rightarrow 9g	270	127000	29700

CPU efficiency for colour-dressed helicity amplitudes

- MHV/on-shell methods (BCF, CSW) yields compact analytic expressions
- but off-shell recursions (BG) are faster

Duhr/Höche/Maltoni '06; Dinsdale/Ternick/Weinzierl '06

LO amplitudes

Advantages

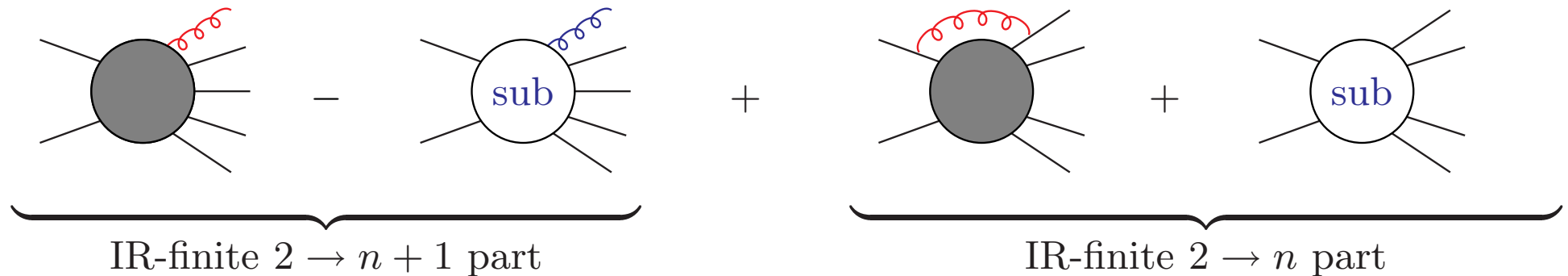
- good estimate in presence of multiple hard final states
- multi-purpose (many processes, many models)
- can be merged with parton showers (CKKW in HERWIG/SHERPA, MLM in ALPGEN)

Limitations

- large scale uncertainties
- especially from high powers of α_S associated with large jet multiplicities
- additional large uncertainties not described by scale variations (e. g. π^2 factors)

(2.2) NLO calculations

Loops and bremsstrahlung for $2 \rightarrow n$ process - treatment of IR singularities



Dipole subtraction

Frixione/Kunszt/Signer '96; Catani/Seymour '97

+ Dittmaier/Trocsanyi '02; Weinzierl/Phaf '01

- real and virtual parts divergent
- subtract local counterterm in $(n+1)$ -PS and add back to n -PS
- PL event generators, arbitrary cuts and distributions

Automatization

- universal recipe in terms of trees

- parton-level automatization

Hasegawa/Moch/Uwer; Frederix/Gehrmann/Greiner '08

- merging with parton shower

Dinsdale/Ternick/Weinzierl'07; Gleisberg/Krauss'08

Bottleneck: one-loop matrix elements

Status of NLO for $2 \rightarrow 2$ processes

- fully automatized (e.g. FeynArts/FeynCalc/FormCalc)
- available and implemented for all SM processes
(EVENT/JETRAD/MCFM/DISENT/DIPHOX/HQQB/NLOJET++/VBFNLO,etc.)
- matching with PS (MC@NLO/POWHEG) implemented for various processes

Multi-leg processes at NLO: technical challenges

Complexity of n -particle processes

- large number of diagrams [$\mathcal{O}(10^3)$] and colour structures (grows like $n!$ or faster)
- many kinematic invariants, polarization states and Dirac/helicity structures
- tensor loop integrals of high rank (from ggg-couplings and ferm. propagators)

$$\int \frac{q^{\mu_1} \dots q^{\mu_R}}{(q^2 - m_0^2) \dots ((q - p_{N-1})^2 - m_{N-1}^2)} = \sum_{i_1, \dots, i_R=1}^{N-1} T_{i_1 \dots i_R}^{(R)} p_{i_1}^{\mu_1} \dots p_{i_R}^{\mu_R} + g^{\mu_i \mu_j} \text{ terms}$$

- many particles \Rightarrow high tensor rank \Rightarrow many covariants coefficients $T_{i_1 \dots i_R}^{(R)}$

Sources of increasing complexity

- External states with colour and mass, external gluons

Numerical instabilities from inverse Gram determinants

- reduction $T^{(R)} \rightarrow T^{(R-1)}$ requires inversion of $Z_{ij} = (2p_i p_j)$
- numerical instabilities from $1/\det(Z)$ in PS regions where $\det(Z) \rightarrow 0$
- problems start at $2 \rightarrow 3$ and can become serious at $2 \rightarrow 4$

Goals for NLO programs

- reliable predictions: **numerical stability**
- **sufficient speed**: distributions require $\gtrsim 1$ event/sec!

Reduction methods

Any one-loop amplitude reducible to small set of known scalar integrals

The diagrammatic equation shows a grey circle with six external lines on the left, followed by an equals sign. To the right of the equals sign are four terms: a sum over d_i of a square diagram with two vertical internal lines; a sum over c_i of a triangle diagram with three internal lines; a sum over b_i of a circle diagram with two external lines; and a sum over a_i of a circle diagram with one external line. The entire expression is followed by a plus sign and the letter R .

$$\text{Diagram} = \sum_i d_i \text{Diagram}_1 + \sum_i c_i \text{Diagram}_2 + \sum_i b_i \text{Diagram}_3 + \sum_i a_i \text{Diagram}_4 + R$$

We need fast and stable algorithms to compute d_i, c_i, b_i, a_i and rational part R

(A) Diagrammatic approach

- express amplitude through diagrams, insert Feynman rules
- huge number of tensor integrals explicitly reduced to small set of scalar boxes, triangles, etc.

Techniques to handle multi-leg tensor loop integrals

- Reduction of tensor integrals to scalar integrals [Passarino/Veltman '79](#); [Stuart et.al. '88-90](#); [v.Oldenborgh/Vermaseren '90](#); [Ezawa et.al. '92](#); [Denner '93](#); [Campbell et.al. '96](#); [Devaraj/Stuart '97](#); [GRACE collab. '03](#); [del Aguila/Pittau '04](#); [v.Hameren et.al. '05](#); [Denner/Dittmaier '05](#);
- Alternative reductions introducing scalar integrals in $D > 4$ [Davydychev '91](#); [Bern et.al. '93](#); [Tarasov '96](#); [Fleischer et.al. '99](#); [Binoth et.al. '99/'05](#); [Duplancic/Nizic '03](#); [Giele/Glover/Zanderighi '04](#) [Ellis/Giele/Zanderighi '06](#)
- Reduction of pentagons, hexagons, etc. to boxes, triangles, bubbles [Melrose '65](#) [v.Neerven/Vermaseren '84](#); [v.Oldenborgh/Vermaseren '90](#); [Davydychev '91](#); [Bern et.al. '93](#); [Denner '93](#); [Campbell et.al. '96](#); [Suzuki et.al. '02](#); [Tramontano '02](#); [Denner/Dittmaier '02-05](#); [GRACE coll. '02-03](#);
- Numerical integration [Ferroglia et.al. '02](#); [Binoth et.al. '02-05](#); [Nagy/Soper '03](#); [de Doncker et.al. '04](#); [Kurihara/Kaneko '05](#); [Denner/Dittmaier '05](#); [Anastasiou/Beerli/Daleo '05-07](#); [Lazopoulos et.al. '07](#);

Lot of progress in the recent years

- full generality
- improved numerical stability avoiding $\det(Z)$ or expanding in small $\det(Z)$
- various groups and methods
- emphasis on efficiency, numerical stability and applications

(B) New methods based on generalized unitarity cuts

(Quadruple) branch cuts of full amplitude and its loop decomposition

The diagram shows an equation for the decomposition of a quadruple cut amplitude. On the left, a four-point amplitude is shown with four external legs and four internal propagators, all cut (indicated by red lines). This is equated to a sum of terms:

- $\sum_i d_i$ multiplied by a diagram of a box with four internal propagators, all cut (red lines), representing a specific loop topology.
- $+$ $\sum_i c_i$ multiplied by a triangle diagram with one cut propagator (red line).
- $+$ $\sum_i b_i$ multiplied by a circle diagram with two cut propagators (red lines).
- $+$ $\sum_i a_i$ multiplied by a circle diagram with one cut propagator (red line).
- $+$ R , representing the remainder.

 Brackets under the first two terms are labeled "on-shell trees" and "selects specific loop" respectively.

Bern/Dixon/Dunbar/Kosower; Britto/Cachazo/Feng; Forde; Berger/Bern/Dixon/Forde/Kosower; Anastasiou/
 Britto/Feng/Kunszt/Mastrolia; Ossola/Pittau/Papadopoulos; Ellis/Giele/Kunszt/Melnikov/Zanderighi;

In practice

- Coefficients d_i, c_i, b_i, a_i expressed in terms of on-shell tree amplitudes
- exploit compact expressions and fast algorithms for multi-leg trees
- additional tricks for cut-free (R) terms: on-shell states in $D > 4$, factorization properties,...

Status

- Proven to be powerful for $gg \rightarrow ng$ and $\gamma\gamma \rightarrow 4\gamma$ virtual amplitudes
- efficiency and numerical stability for cross sections still to be assessed
- many new ideas and strategies, first LHC applications on horizon

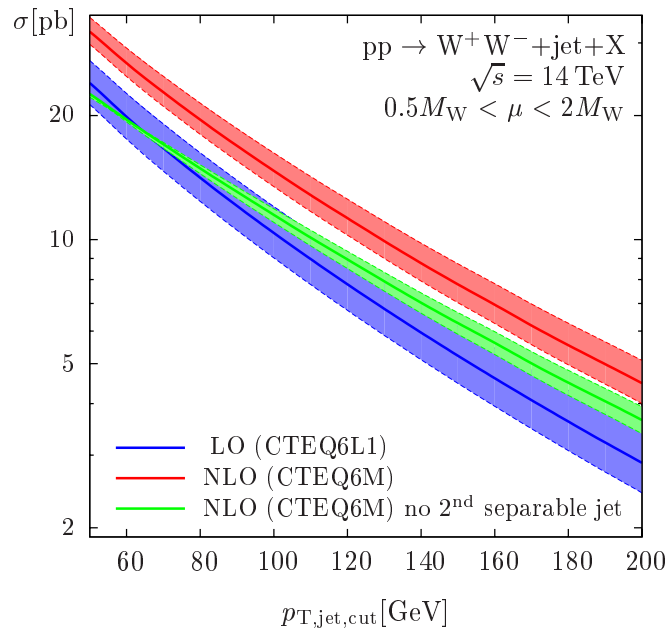
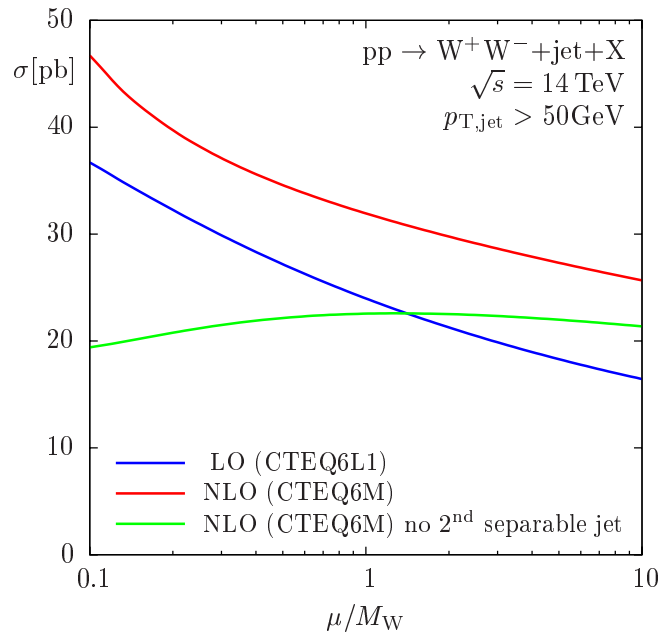
2 \rightarrow 3 NLO cross sections for LHC (*contrib. from Helmholtz Alliance)

Many signal and background calculations in the recent few years

- * $pp \rightarrow t\bar{t}H, b\bar{b}H$ Beenakker/Dittmaier/Krämer/Plümper/Spira/Zerwas;
Dawson/Reina/Wackerath/Orr/Jackson; Peng/Wen-Gan/Hong-Shen/Ren-You/Yi
- * $pp \rightarrow HHH$ Plehn/Rauch Binoth/Karg/Kauer/Rückl
- * $pp \rightarrow Hjj$ Del Duca/ Kilgore/Oleari/Schmidt/Zeppenfeld; Campbell/Ellis/Zanderighi
- $pp \rightarrow jjj$ Bern/Dixon/Kosower; Kunst/Signer/Trocsanyi; Giele/Kilgore/Nagy
- $pp \rightarrow Vjj$ Bern/Dixon/Kosower; Ellis/Veseli; Campbell/Ellis;
- * $pp \rightarrow VVj$ Dittmaier/Kallweit/Uwer; Campbell/Ellis/Zanderighi;
Binoth/Gillet/Karg/Kauer/Sanguinetti
- * $pp \rightarrow VVV$ Lazopoulos/Melnikov/Petriello; Hankele/Zeppenfeld;
Binoth/Ossola/Papadopoulos/Pittau
- $pp \rightarrow V + b\bar{b}$ Cordero/Reina/Wackerath
- * $pp \rightarrow t\bar{t}j$ Dittmaier/Uwer/Weinzierl
- $pp \rightarrow t\bar{t}Z$ Lazopoulos/McElmurry/Melnikov/Petriello

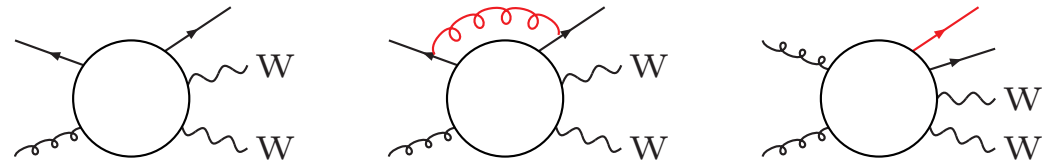
almost all based on Feynman diagrams

NLO QCD corrections to $pp \rightarrow WWj$ [Dittmaier/Kallweit/Uwer '07; Campbell/Ellis/Zanderighi '07]



Important background

- $H \rightarrow WW$ (GF/WBF) and new physics (SUSY)
- anomalous couplings in $pp \rightarrow WW$



Cross section at LHC ($p_{T,j}^{\text{max}} > p_{T,\text{cut}}, R = 1$)

- small LO scale dependence (25% for $\frac{1}{4} < \frac{\mu}{M_W} < 4$)
- not reduced at NLO!
- NLO correction $>$ LO scale uncertainty!

Stabilization through 2nd-jet veto ($p_{T,j}^{\text{min}} < p_{T,\text{cut}}$)

- reduces size of correction and NLO scale uncertainty
- NLO consistent with LO uncertainty band

Example of strong cut dependence at NLO!

- WBF cuts can increase NLO corrections up to +70% (WWj dominant BG) Campbell/Ellis/Zanderighi '07

Towards $2 \rightarrow 4$ NLO cross sections for the LHC

Very few $2 \rightarrow 4$ calculations, only for e^+e^- and $\gamma\gamma$ colliders

- $e^+e^- \rightarrow 4f$ (EW) [Denner/Dittmaier/Roth/Wieders '05](#)
- $e^+e^- \rightarrow HH\nu\bar{\nu}$ (EW) [Boudjema/Fujimoto/Ishikawa/Kaneko/Kurihara/Shimizu/Kato/Yasui '05](#)
- $\gamma\gamma \rightarrow t\bar{t}b\bar{b}$ (QCD) [Lei/Wen-Gan/Liang/Ren-You/Yi '07](#)

Results for LHC urgently needed

- most interesting signals involve heavy particles decaying into jets, leptons, photons
- many multi-particle backgrounds

$2 \rightarrow 4$ is a time consuming business

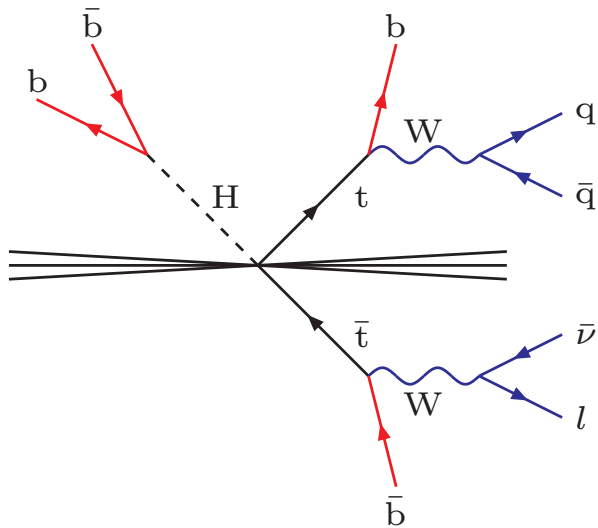
- many months of man power for a single process
- importance of setting right priorities

Les Houches '05 prioritized wishlist

	Reaction	background for	existing calculations
1.	VVj	$t\bar{t}H$, new physics	WWj: Dittmaier/Kallweit/Uwer '07; WWj: Campbell/Ellis/Zanderighi '07; WWj: Binoth/Guillet/Karg/Kauer/Sanguinetti (in progress)
2.	$t\bar{t}b\bar{b}$	$t\bar{t}H$	$q\bar{q}$-channel cross section completed Bredenstein/Denner/Dittmaier/SP '08
3.	$t\bar{t}jj$	$t\bar{t}H$	\emptyset
4.	$VVb\bar{b}$	$VBF \rightarrow H \rightarrow VV$, $t\bar{t}$, NP	\emptyset
5.	$VVjj$	$VBF \rightarrow H \rightarrow VV$	VBF : Jäger/Oleari/Zeppenfeld '06 + Bozzi '07
6.	$Vjjj$	new physics	one-loop amplitudes completed Ellis/Giele/Kunszt/Melnikov/Zanderighi '08
7.	VVV	new physics	ZZZ: Lazopoulos/Melnikov/Petriello '07; WWZ: Hankele/Zeppenfeld '07 VVV: Binoth/Ossola/Papadopoulos/Pittau '07

First (partial) results for $2 \rightarrow 4$ processes

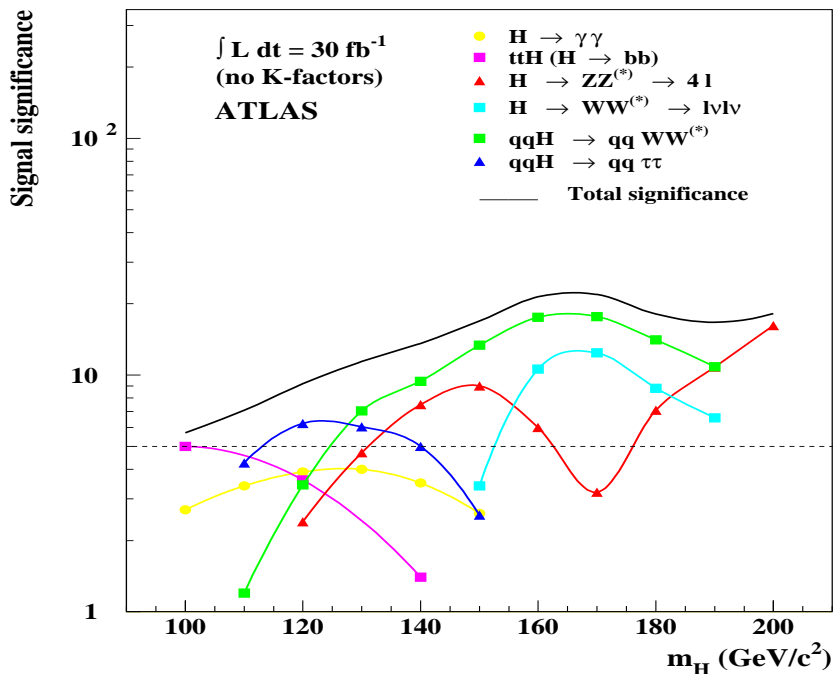
$t\bar{t}H$ production at the LHC and its $t\bar{t}b\bar{b}$ background



Associated $t\bar{t}H(H \rightarrow b\bar{b})$ production

- can be observed in $H \rightarrow b\bar{b}$ channel
- exploits large $\text{BR}(H \rightarrow b\bar{b})$ for light H
- measurement of top Yukawa coupling

ATLAS '03



Proposed analysis (ATLAS TDR)

- select final state $b\bar{b}b\bar{b}jjl\nu$ (4 b-quarks!)
- reconstruct $t\bar{t}b\bar{b}$
- select region $|m_{b\bar{b}} - M_H| < 30 \text{ GeV}$

Richter-Was/Sapinski, ATL-PHYS-98-132

Background to $pp \rightarrow t\bar{t}H$

Background processes

- $t\bar{t}b\bar{b}$ (QCD+EW), $t\bar{t}jj$
- large σ_B (underestimated in TDR)

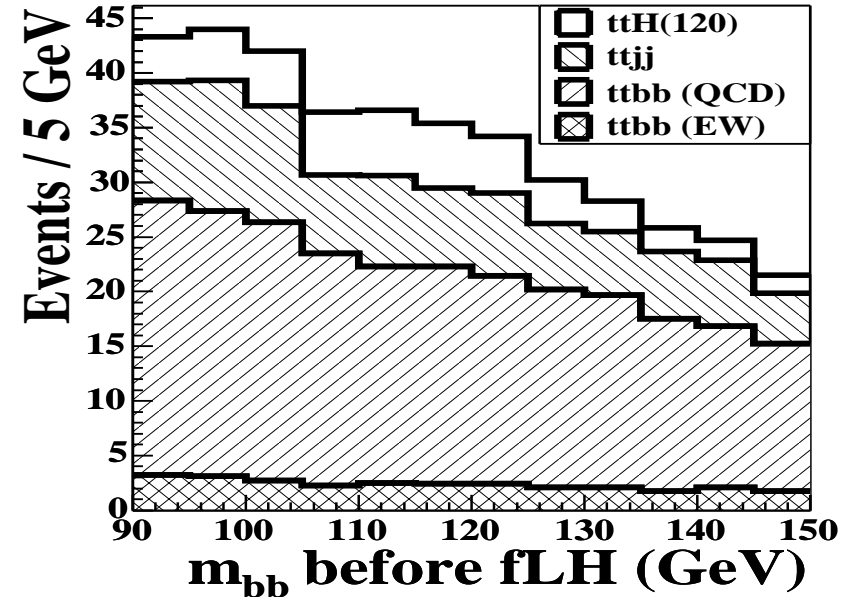
Stat. and syst. uncertainties of B

- small ΔB_{stat} with $1/\sqrt{B} < 10\%$
- small $S/B \sim 0.2$ requires $\Delta B_{\text{syst}} < 20\%$!
(not considered in TDR)

Strategy

- direct measurement of B impossible
(S and B have similar shape)
- measure B outside signal region and extrapolate with theory predictions
- theory uncertainty at LO > factor 2

$t\bar{t}H$ impossible without $t\bar{t}b\bar{b}$ at NLO

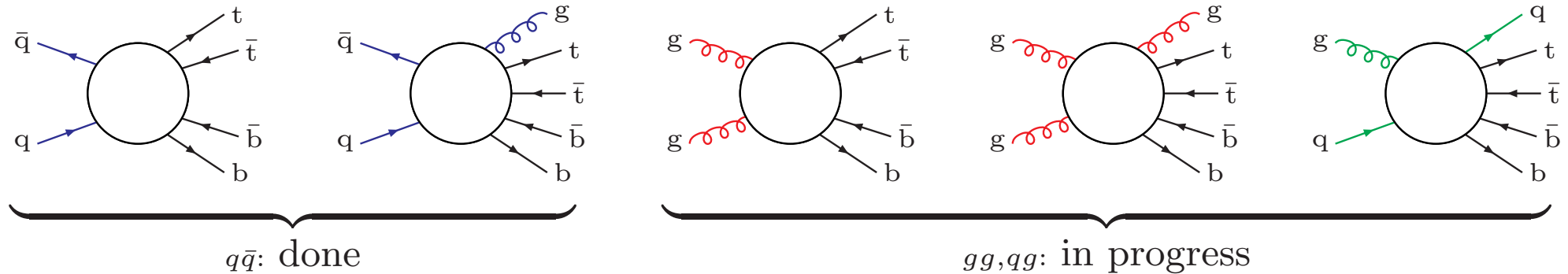


events and stat. sign. (30 fb^{-1})

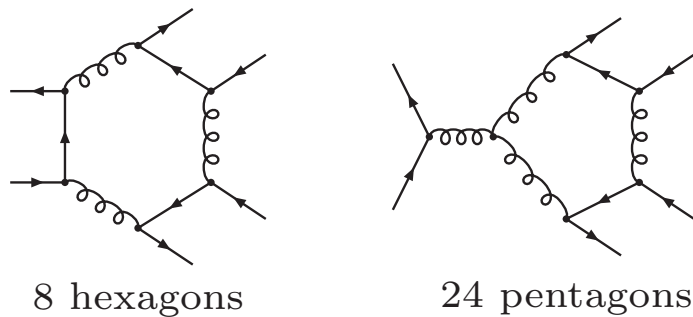
M_H (GeV)	110	120	130
$t\bar{t}H$	60.9	41.9	25.5
$t\bar{t}b\bar{b}$ (QCD)	167.3	145.8	128.7
$t\bar{t}jj$	66.2	54.6	41.6
$t\bar{t}b\bar{b}$ (EW)	21.8	18.4	15.2
S/\sqrt{B}	3.8	2.8	1.9
S/B	0.24	0.19	0.14

NLO QCD corrections to $pp \rightarrow t\bar{t}b\bar{b}$ [Bredenstein/Denner/Dittmaier/SP '08]

Quark-antiquark and gluon induced processes



Sample diagrams in the $q\bar{q}$ -channel



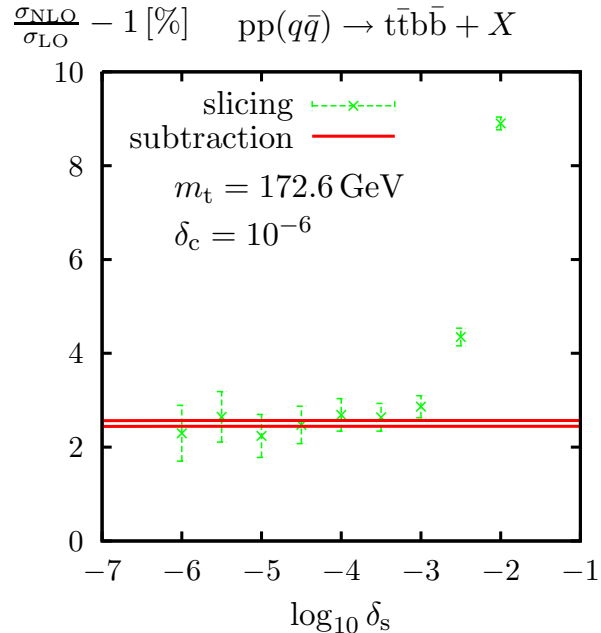
etc.

diagrams and impact on σ_{LO}

	$q\bar{q}$	gg	qg
LO	7	38	
virtual	188	1003	
real	66	393	66
σ/σ_{tot}	5%	95%	

$q\bar{q}$ channel is simpler than gg and only 5% of σ but demonstrates feasibility of NLO

Technical aspects



Precision (consistency checks)

- UV, soft and collinear cancellations
- 2 completely independent calculations
- 10-digit agreement for single PS points
- permille agreement after PS integration with $\mathcal{O}(10^8)$ events

Runtime and stat. precision $\Delta\sigma/\sigma_{\text{LO}}$

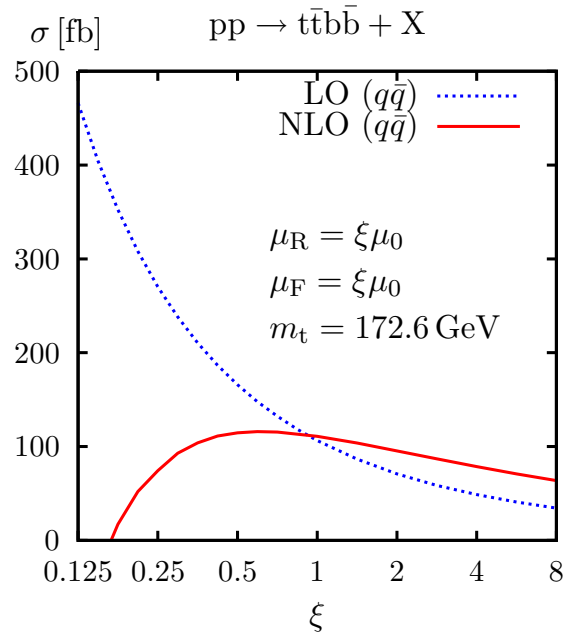
	$\sigma/\sigma_{\text{LO}}$	# events	$\Delta\sigma/\sigma_{\text{LO}}$	runtime
tree	74%	6.7×10^7	3×10^{-4}	66min
virtual	-3%	0.34×10^7	2.5×10^{-4}	12h
real	33%	13×10^7	5×10^{-4}	34h

on single 3GHZ Intel Xeon processor

Speed of calculation

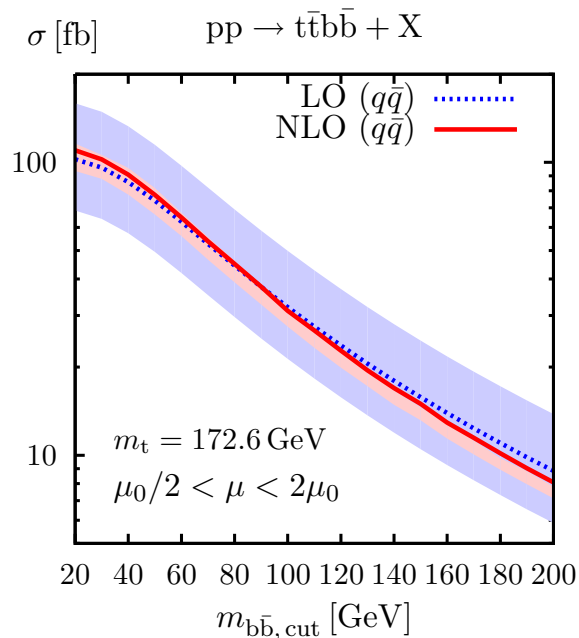
- virtual corrections @ 13 ms/event!
- for same precision ($\Delta\sigma/\sigma$) virtual corrections require less CPU-time than real corrections (scale-dependent statement!)

Reduction of scale dependence at NLO ($q\bar{q}$ channel)



Total cross section ($p_{T,b} > 20 \text{ GeV}$, $y_b < 2.5$)

- central scale $\mu_0 = m_t$
- huge LO dependence: up to factor 4 (from $\alpha_S(\mu_R)^4$)
- stabilization at NLO (close to maximum)



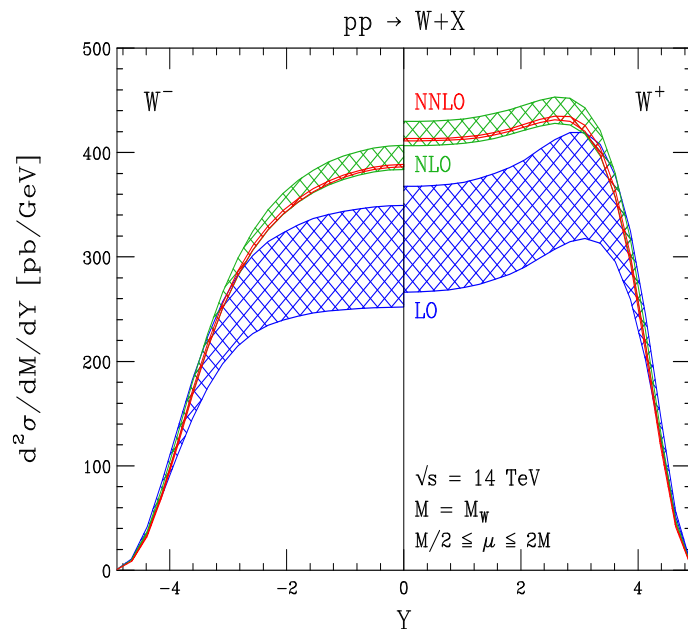
Dependence on $b\bar{b}$ invariant mass

- strong reduction of scale dependence
- NLO consistent with LO uncertainty band
- shape of $m_{b\bar{b}}$ distorted by corrections

(2.3) NNLO calculations

NNLO is important when

- NLO corrections and scale uncertainties are large
- percent precision needed for benchmark measurements



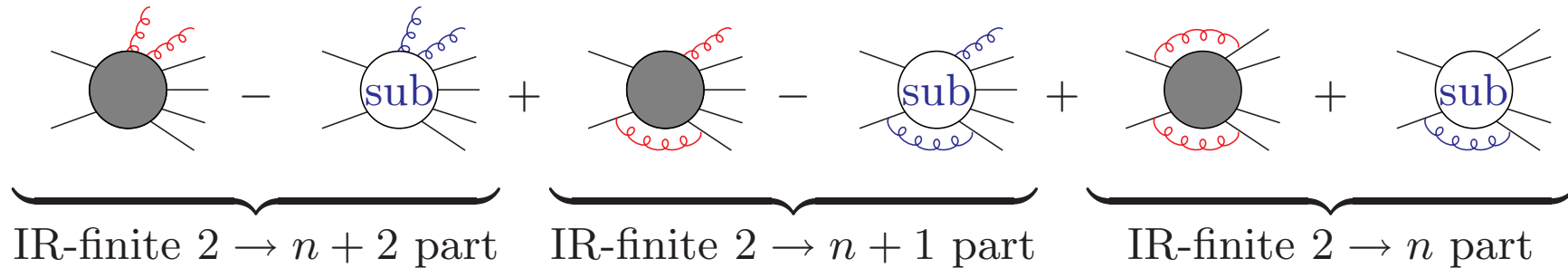
Anastasiou/Dixon/Melnikov/Petriello '04

Existing results for $pp \rightarrow H, W, Z$

- inclusive cross section
 - Harlander '00; Catani/de Florian/Grazzini '01;
 - Harlander/Kilgore '01-02; Anastasiou/Melnikov '02;
 - Ravindram/Smith/van Neerven '03
- differential distributions, selection cuts
 - Anastasiou/Melnikov/Petriello '05; Anastasiou/Dissertori/
Stöckli '07; Catani/Grazzini '07-08

IR divergences NNLO

Loops and bremsstrahlung for $2 \rightarrow n$ process



Intricate structure of IR singularities (single and double unresolved partons)

- general subtraction scheme for IR singularities not available
- but a lot of progress in this direction [Kosower, Weinzierl, Frixione, Grazzini, Gehrmann-De Ridder, Gehrmann, Glover, Daleo, Maitre, Somogyi, Trocsanyi, Del Duca](#)

Recent achievements

- full NNLO completed for $e^+e^- \rightarrow jjj$ [Gehrmann-De Ridder/Gehrmann/Glover/Heinrich '07; Weinzierl '08](#)
- full NNLO completed for $pp \rightarrow \text{singlet}$ [Catani/Grazzini '07-08](#)
- first step towards NNLO subtraction for $pp \rightarrow j + X$ [Daleo/Gehrmann/Maitre '08](#)

2-loop matrix elements for $2 \rightarrow 2$

$pp \rightarrow j + X$ Anastasiou et.al.; Bern et.al.

- important for PDFs and α_S

$pp \rightarrow t\bar{t}$ Czakon/Mitov/Moch '07; Czakon '08;

- important for precise m_t measurement
- $q\bar{q}$ -channel completed, gg -channel in progress

$pp \rightarrow WW$ Chachamis/Czakon/Eiras '08

- large BG to $H \rightarrow WW$ and relevant to search for anomalous couplings
- $M_W \rightarrow 0$ limit completed, M_W -dependence coming soon

Strategy for 2-loop master integrals $I(M)$ with $M \neq 0$ Chachamis/Czakon/Eiras '08

- remove mass-complexity computing $\lim_{M \rightarrow 0} I(M)$ (automatized MB method)
- generate system of DEs
- power expansion in M with up to 11 terms
- improve precision/check convergence with numerical solution of DE

$$\frac{\partial}{\partial M} I_i(M) = \sum_j C_{ij} I_j(M)$$

(3) EW corrections - selected topics

Typical size

- $\alpha \sim \alpha_S^2$ suggests NLO EW \sim NNLO QCD
- relevant for precision measurements: PDFs, luminosity, M_W , $\sin^2(\theta)$, ...

In some kinematic regions NLO EW strongly enhanced and this can require higher orders

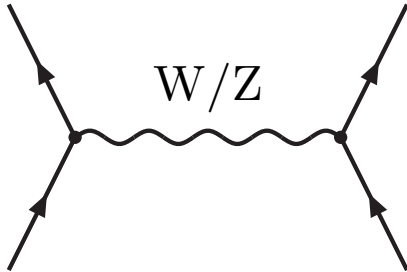
- real γ bremsstrahlung distorts leptonic distributions $\Rightarrow \ln(m_l^2/M^2)$
- Virtual W/Z effects distort tail of p_T distributions $\Rightarrow \ln(p_T^2/M_W^2)$

In the following consider two examples

- Drell-Yan
- $pp \rightarrow Vj$

(3.1) Drell-Yan processes $pp \rightarrow Z/W \rightarrow l\bar{l}/l\bar{\nu}_l$

NLO EW (and NNLO QCD) available



- for Z production: [Baur/Keller/Sakumoto '97](#); [Baur/Wackerroth '99](#); [Brein/Hollik/Schappacher '99](#); [Baur et.al '02](#); [Arbuzov et.al. '06](#);
- for W production: [Hollik/Wackerroth '97](#); [Baur/Keller/Wackerroth '98](#); [Dittmaier/Krämer '02](#); [Baur/Wackerroth '04](#); [Arbuzov et.al. '05](#); [Carloni Calame et.al. '06](#); [Brensing/Dittmaier/Krämer/Mück '08](#)

Important for measurement of luminosity from Z/W counting

(talks by Hasko Stenzel/ATLAS and Thomas Marteen/CMS)

- **5% precision** (dominated by PDF uncertainty) **might improve up to 3%**

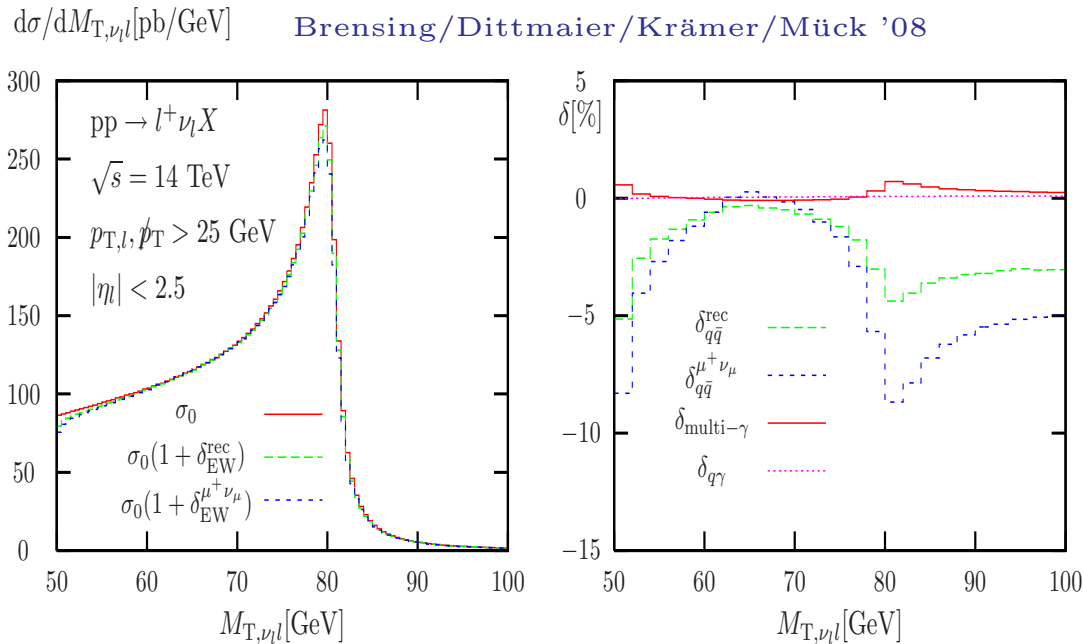
Recent progress on theory side (talk by Oleg Veretin)

- complete $\mathcal{O}(\alpha\alpha_S)$ virtual two-loop for Z production [Kotikov/Kühn/Veretin '07](#)
- must be combined with bremstrahlung counterpart

DY permits precision measurements competitive with present accuracy

- $\delta M_W \sim 15 \text{ MeV}$ and $\delta \sin^2(\theta_{\text{eff}}) \sim 14\text{--}20 \times 10^{-5}$

M_W from Jacobian peak of $M_T(W)$ distribution



NLO EW corrections

- strong distortion around peak due to $\ln(M_W^2/m_l^2)$ from collinear γ
- large shift: $\delta M_W \sim -170 \text{ MeV}$ in μ channel [Carloni Calame et.al. '06](#);

Multiple- γ emission

- parton shower [Carloni Calame et.al. '06](#) or QED resummation [Breusing/Dittmaier/Krämer/Mück '08](#)
- shift: $\delta M_W \sim 10 \text{ MeV}$ in μ channel [Carloni Calame et.al. '06](#);

Combination of EW and QCD

- EW \otimes HERWIG QCD shower (HORACE) [Vicini et. al. '07](#); [Balossini et. al. '07](#)
- Complete $\mathcal{O}(\alpha\alpha_S)$ corrections?

$M_{T,\nu_l l}/\text{GeV}$	50 $-\infty$	100 $-\infty$	200 $-\infty$	500 $-\infty$	1000 $-\infty$	2000 $-\infty$
σ_0/pb	2112.2(1)	13.152(2)	0.9452(1)	0.057730(5)	0.0054816(3)	0.00026212(1)
$\delta_{\mu+\nu_\mu}/\%$						
DK	-2.75(1)	-5.03(2)	-7.98(1)	-14.43(1)	-21.99(1)	-32.15(1)
HORACE	-2.77(1)	-5.08(1)	-8.01(1)	-14.44(1)	-21.99(1)	-32.16(1)
SANC	-2.76(2)	-5.06(2)	-7.96(2)	-14.41(2)	-21.94(2)	-32.12(2)
WGRAD	-2.69(1)	-4.84(1)	-7.96(1)	-14.48(1)	-22.03(1)	-32.3(1)

High-energy tail of $M_T(W)$ distribution

- large NLO EW effects resulting from $\ln^2(\hat{s}/M_W^2)$
- several-percent estimated uncertainty from $\ln^4(\hat{s}/M_W^2)$ two-loop terms

Studied in great detail for the case of neutral Drell-Yan (Z/γ)

- complete calculation of two-loop $\ln(\hat{s}/M_W^2)$ -terms

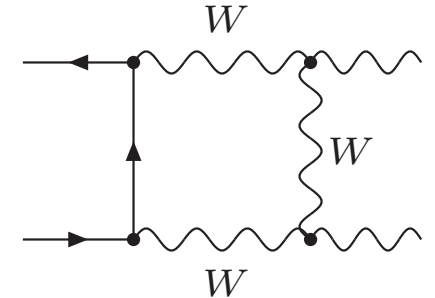
Kühn/Moch/Penin/Smirnov '00-03; Jantzen/Kühn/Penin/Smirnov '04-05; Jantzen/Smirnov '06;

- estimated residual uncertainty of $\mathcal{O}(10^{-3})$

Basic properties of EW Sudakov logarithms

Origin of $\ln(Q^2/M_W^2)$

- when $Q^2 \gg M_W^2$ the Z/W bosons behave as “quasi-massless”
- coupling to external lines produce soft/collinear logarithms



Analogies with soft/collinear singularities in QCD

- affect all hard scattering processes ($Q^2 \gg 100 \text{ GeV}$) with EW interacting particles
- universality and factorization at one loop Denner, SP '01

$$\alpha \left[C_2 \underbrace{\ln^2 \left(\frac{s}{M_W^2} \right)}_{\text{soft, coll}} + C_1 \underbrace{\ln \left(\frac{s}{M_W^2} \right)}_{\text{soft, coll}} + \tilde{C}_1 \underbrace{\ln \left(\frac{s}{\mu_R^2} \right)}_{\text{UV}} + C_0 \right]$$

practical consequence: compact formula for C_2, C_1, \tilde{C}_1 , universally applicable, easy to implement into MC!

Two-loop exponentiation

$$\begin{aligned}
 & \text{tree} + \sum_{i,j} \frac{1}{2} \text{diagram}(V_1) + \sum_{i,j,k,l} \frac{1}{2} \left[\text{diagram}(V_2, V_1) + \text{diagram}(V_1, V_2) \right] + \text{diagram}(V_1, V_2, V_3) \\
 & + \text{diagram}(V_2, V_1) + \text{diagram}(V_2, V_1) + \frac{1}{2} \text{diagram}(V_1, V_2) + \text{diagram}(V_1, V_2, k) + \frac{1}{6} \text{diagram}(V_1, V_2, V_3, k) + \frac{1}{8} \text{diagram}(V_1, V_2, k, l) = \\
 & = \exp \left[\sum_{j<i} \text{diagram}(\Delta\gamma) \right] \exp \left[\sum_{j<i} \text{diagram}(W, Z, \gamma) \right] \text{tree}
 \end{aligned}$$

Fadin/Lipatov/Martin/Melles '00; Melles '00-04; Kühn/Moch/Penin/Smirnov '00-03
 Jantzen/Kühn/Penin/Smirnov '04-05 Melles/Hori/Kawamura/Kodaira '00; Beenakker/Werthenbach '00,'02;
 Denner/Melles/SP '03; SP '04; Denner/Jantzen/SP '06-08;

- analogies with QCD
- simple formulae for practical applications at colliders

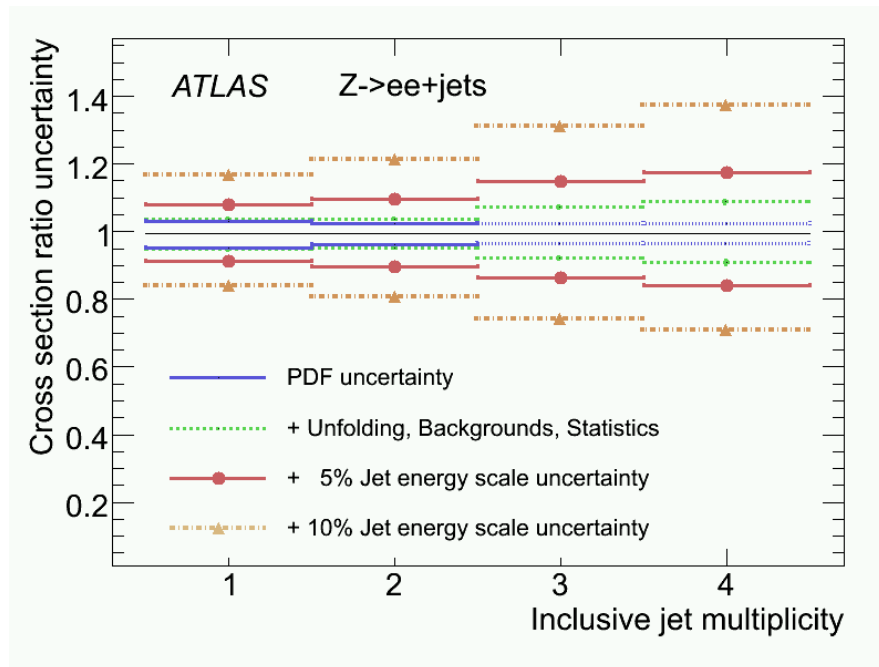
(3.2) $pp \rightarrow Vj$

ATLAS measurement of Z+jets cross section (talk by Ulla Blumenschein)

Blumenschein/Segura, Atlas Standard Model CSC Note: ATL-COM-PHYS-2008-064

Importance of $pp \rightarrow W/Z + \text{jets}$

- large BG to SM and BSM reactions
- validate/tune MC event generators



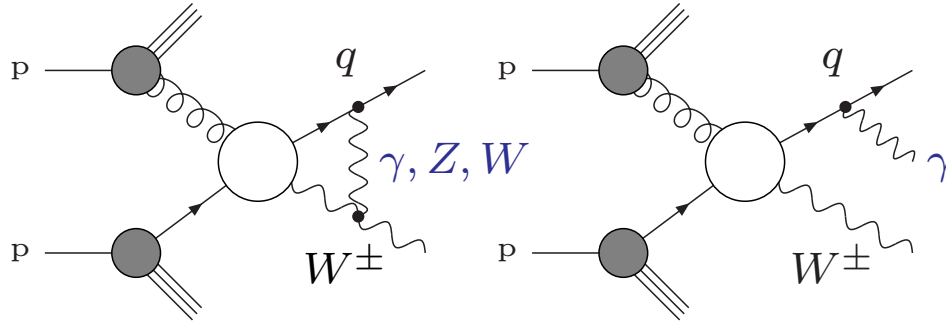
Analysis

- fully-simulated signal and background Monte Carlo samples with 1fb^{-1}
- study reconstruction of leptons and \cancel{E}_T in multi-jet final state.
- quantify stat. and syst. uncertainties
- 1fb^{-1}
- including all backgrounds (QCD, tt)
- systematics dominated by JES-uncertainty

Results assuming 5% JES resolution

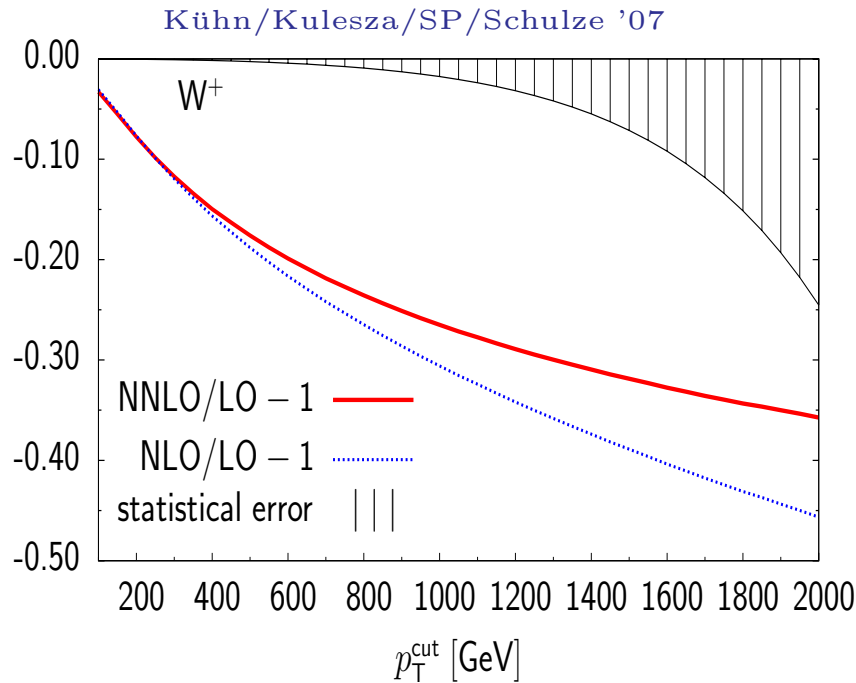
- $\delta\sigma(pp \rightarrow Z + j) \sim 8\%$
- $\delta\sigma(pp \rightarrow Z + 4j) \sim 15\%$

EW corrections to $pp \rightarrow Wj$



Two independent calculations

- NLO EW + dominant two-loop
Kühn/Kulesza/SP/Schulze '07
- NLO EW + photon-induced processes
Hollik,Kasprzik,Kniehl '07



One- and two-loop corrections to p_T distribution

- -27% + 3% = -24% at $p_T \sim 1$ TeV
- -42% + 9% = -33% at $p_T \sim 2$ TeV

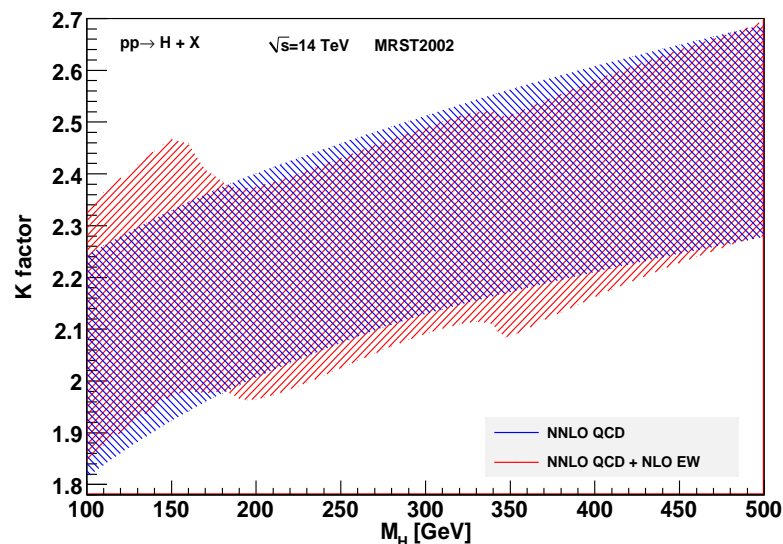
Two-loop \simeq experimental error!

Two-loop EW corrections to $pp(gg) \rightarrow H$

(talk by Sandro Uccirati [Actis/Passarino/Sturm/Uccirati 0809.1301 \[hep-ph\]](#), [0809.3667 \[hep-th\]](#))

Calculation

- all fermionic and bosonic diagrams
- exact M_H, m_t, M_W, M_Z -dependence (previous results based on M_H/M_W -expansion)
- consistent description of $W \rightarrow WW$ threshold (complex-mass scheme)



NNLO plus two-loop EW result

- combined with HNNLO code [Catani/Grazzini '07-'08](#)
- NNLO predictions shifted by $[-2\%, +6\%]$
- largest effect around WW threshold

Conclusions

QCD for multi-particle processes

- excellent LO tools
- NLO pushed up to $2 \rightarrow 3$ and will soon break the $2 \rightarrow 4$ barrier thanks to lot of theoretical progress

QCD at NNLO

- major progress from inclusive to differential $2 \rightarrow 1$ predictions
- good prospects for $2 \rightarrow 2$

EW corrections

- NLO studied for various $2 \rightarrow 2$ reactions important for benchmark measurements
- large effects in lepton distributions and high- p_T regions can require higher orders

The theoretical expertise within the Helmholtz Alliance is providing major contributions in all these areas