Status of Parton Shower Simulations

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DESY Theory workshop, 29.9.2015

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Outline

- 1 The role of precision simulations
- 2 Parton-level ingredients
- In State State
- 4 Multijet merging
- 5 Multijet merging at NLO
- 6 Improving the parton showers
- Concluding remarks

The inner working of event generators ...

simulation: divide et impera

• hard process: fixed order perturbation theory

traditionally: Born-approximation

- bremsstrahlung: resummed perturbation theory
- hadronisation: phenomenological models
- hadron decays: effective theories, data
- "underlying event": phenomenological models



| Ingredients | | | |
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Reminder: Ingredients of simulations

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Cross sections at the LHC: Born approximation

$$d\sigma_{N} = d\Phi_{N}\mathcal{B}_{N}$$

=
$$\sum_{a,b} \int_{0}^{1} dx_{a} dx_{b} f_{a}(x_{a}, \mu_{F}) f_{b}(x_{a}, \mu_{F}) \frac{1}{2\hat{s}} \int_{\text{cuts}} d\phi_{N} |\mathcal{M}_{ab \to N}(\phi_{N}; \mu_{F}, \mu_{R})|^{2}$$

- parton densities $f_a(x, \mu_F)$ (PDFs)
- phase space ϕ_N for *N*-particle final states
- incoming current $1/(2\hat{s})$
- squared matrix element $\mathcal{M}_{ab \rightarrow N}$

(summed/averaged over polarisations)

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- $\bullet\,$ renormalisation and factorisation scales μ_R and μ_F
- complexity demands numerical methods for large N



Reminder: Structure of an NLO calculation

sketch of cross section calculation (by now fully automated)



 subtraction terms S (integrated) and dS: exactly cancel IR divergence in R − process-independent structures

S. Frixione, Z. Kunszt & A. Signer, Nucl. Phys. B467

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S. Catani & M. Seymour, Nucl.Phys.B485

• result: terms in both brackets separately infrared finite

Probabilistic treatment of emissions

• probability for **no decay** in [t₀, t]: Sudakov form factor

$$\Delta_{ij,k}(t,t_0) = \exp\left[-\int\limits_{t_0}^t \mathrm{d}\Gamma_{ij,k}(t)
ight]$$

• decay width for parton $i(j) \rightarrow ik(j)$ (spectator j)

$$\mathrm{d}\Gamma_{ij,k}(t) = \frac{\mathrm{d}t}{t} \frac{\alpha_s}{2\pi} \int \mathrm{d}z \frac{\mathrm{d}\phi}{2\pi} \underbrace{\mathcal{K}_{ij,k}(t, z, \phi)}_{\text{splitting kernel}}$$

• evolution parameter t defined by kinematics

generalised angle (HERWIG ++) or transverse momentum (PYTHIA, SHERPA)

resums classes of higher logarithms

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- resummation of leading (and next-to leading) logarithms log t
- scale choice for strong coupling: $\alpha_{S}(k_{\perp}^{2})$
- regularisation through cut-off t_0



Emissions off a Born matrix element

• shorthand for emission off *n*-particle final state:

$$\mathcal{K}_n(\Phi_1) = \frac{\alpha_S}{2\pi} \sum_{\text{all } \{ij,k\}} \mathcal{K}_{ij,k}(\Phi_{ij,k}), \quad \Delta_n^{(\mathcal{K})}(t,t_0) = \exp\left[-\int_{t_0}^t \mathrm{d}\Phi_1 \,\mathcal{K}_n(\Phi_1)\right]$$

• consider first emission only off Born configuration

$$\mathrm{d}\sigma_{B} = \mathrm{d}\Phi_{N} \mathcal{B}_{N}(\Phi_{N}) \underbrace{\left\{ \Delta_{N}^{(\mathcal{K})}(\mu_{N}^{2}, t_{0}) + \int_{t_{0}}^{\mu_{N}^{2}} \mathrm{d}\Phi_{1} \Big[\mathcal{K}_{N}(\Phi_{1}) \Delta_{N}^{(\mathcal{K})}(\mu_{N}^{2}, t(\Phi_{1})) \Big] \right\}}_{\text{integrates to unity} \longrightarrow \text{"unitarity" of parton shower}}$$

 ${\, \bullet \, }$ further emissions by recursion with $\mu_{\rm N}^2 \longrightarrow t$ of previous emission

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| | NLO improvements | | |
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NLO improvements: Matching

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NLO matching: Basic idea

- parton shower resums logarithms fair description of collinear/soft emissions jet evolution (where the logs are large)
- matrix elements exact at given order fair description of hard/large-angle emissions jet production (where the logs are small)
- adjust ("match") terms:
 - cross section at NLO accuracy
 - correct hardest emission in PS to exactly reproduce ME at order α_{S} (\mathcal{R} -part of the NLO calculation)



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The POWHEG-trick (I): Matrix-element reweighting

M. Bengtsson & T. Sjostrand, Phys.Lett.B 185& M. Seymour, Comp.Phys.Comm.90

P. Nason, JHEP 0411 & S. Frixione, P. Nason & C. Oleari, JHEP 0711

Image: A math a math

 reminder: K_{ij,k} reproduces process-independent behaviour of *R_N/B_N* in soft/collinear regions of phase space

$$\mathrm{d}\Phi_1 \xrightarrow{\alpha_S} \mathcal{K}_{ij,k}(\Phi_1) \xleftarrow{\mathsf{IR}} \mathrm{d}\Phi_1 \xrightarrow{\mathcal{R}_N(\Phi_{N+1})} \mathcal{B}_N(\Phi_N)$$

define modified Sudakov form factor (as in ME correction)

$$\Delta_N^{(\mathcal{R}/\mathcal{B})}(\mu_N^2, t_0) = \exp\left[-\int_{t_0}^{\mu_N^2} \mathrm{d}\Phi_1 \, \frac{\mathcal{R}_N(\Phi_{N+1})}{\mathcal{B}_N(\Phi_N)}\right] \, ,$$

- assumes factorisation of phase space: $\Phi_{N+1} = \Phi_N \otimes \Phi_1$
- typically will adjust scale of α_S to parton shower scale

The POWHEG-trick (II): Local *K*-factors

P. Nason, JHEP 0411 & S. Frixione, P. Nason & C. Oleari, JHEP 0711

• start from Born configuration Φ_N with NLO weight:

("local K-factor")

$$\begin{split} \mathrm{d}\sigma_{N}^{(\mathrm{NLO})} &= \mathrm{d}\Phi_{N}\,\bar{\mathcal{B}}(\Phi_{N}) \\ &= \mathrm{d}\Phi_{N}\left\{\mathcal{B}_{N}(\Phi_{N}) + \underbrace{\mathcal{V}_{N}(\Phi_{N}) + \mathcal{B}_{N}(\Phi_{N})\otimes\mathcal{S}}_{\tilde{\mathcal{V}}_{N}(\Phi_{N})} \right. \\ &+ \int \mathrm{d}\Phi_{1}\left[\mathcal{R}_{N}(\Phi_{N}\otimes\Phi_{1}) - \mathcal{B}_{N}(\Phi_{N})\otimes\mathrm{d}S(\Phi_{1})\right] \right\} \end{split}$$

by construction: exactly reproduce cross section at NLO accuracy

• note: second term vanishes if $\mathcal{R}_N \equiv \mathcal{B}_N \otimes \mathrm{d}S$

(relevant for MC@NLO)

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NLO accuracy in radiation pattern

• generate emissions with $\Delta_N^{(\mathcal{R}/\mathcal{B})}(\mu_N^2, t_0)$:

$$d\sigma_{N}^{(\text{NLO})} = d\Phi_{N} \bar{\mathcal{B}}(\Phi_{N}) \\ \times \underbrace{\left\{ \Delta_{N}^{(\mathcal{R}/\mathcal{B})}(\mu_{N}^{2}, t_{0}) + \int_{t_{0}}^{\mu_{N}^{2}} d\Phi_{1} \frac{\mathcal{R}_{N}(\Phi_{N} \otimes \Phi_{1})}{\mathcal{B}_{N}(\Phi_{N})} \Delta_{N}^{(\mathcal{R}/\mathcal{B})}(\mu_{N}^{2}, k_{\perp}^{2}(\Phi_{1})) \right\}}$$

integrating to yield 1 - "unitarity of parton shower"

- radiation pattern like in ME correction
- possible pitfall, again: choice of upper scale μ_N^2

(this is vanilla POWHEG!)

• apart from logs: which configurations enhanced by local K-factor

(K-factor for inclusive production of X adequate for $X + \text{ jet at large } p_{\perp}$?)

Improved POWHEG: Constraining the phase space

S. Alioli, P. Nason, C. Oleari, & E. Re, JHEP 0904

--- POWHEG h→∞ --- POWHEG h=m_H=400 GeV

• split real-emission ME as

$$\mathcal{R} = \mathcal{R}\left(\underbrace{\frac{h^2}{p_{\perp}^2 + h^2}}_{\mathcal{R}^{(S)}} + \underbrace{\frac{p_{\perp}^2}{p_{\perp}^2 + h^2}}_{\mathcal{R}^{(F)}}\right)$$

• differential event rate up to first emission

$$d\sigma = d\Phi_B \bar{\mathcal{B}}^{(\mathbb{R}^{(S)})} \left[\Delta^{(\mathcal{R}^{(S)}/\mathcal{B})}(s, t_0) + \int_{t_0}^{s} d\Phi_1 \frac{\mathcal{R}^{(S)}}{\mathcal{B}} \Delta^{(\mathcal{R}^{(S)}/\mathcal{B})}(s, k_{\perp}^2) \right] + d\Phi_R \mathcal{R}^{(F)}(\Phi_R)$$

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Resummation in MC@NLO

S. Frixione & B. Webber, JHEP 0602

S. Hoeche, FK, M. Schoenherr, & F. Siegert, JHEP 1209

• divide \mathcal{R}_N in soft ("S") and hard ("H") part:

$$\mathcal{R}_N = \mathcal{R}_N^{(S)} + \mathcal{R}_N^{(H)} = \mathcal{B}_N \otimes \mathrm{d}\mathcal{S}_1 + \mathcal{H}_N$$

• identify subtraction terms and shower kernels $\mathrm{d}\mathcal{S}_1\equiv\sum_{\{ij,k\}}\mathcal{K}_{ij,k}$

(modify ${\cal K}$ in $1^{{\mbox{st}}}$ emission to account for colour)

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$$d\sigma_{N} = d\Phi_{N} \underbrace{\tilde{\mathcal{B}}_{N}(\Phi_{N})}_{\mathcal{B}+\tilde{\mathcal{V}}} \left[\Delta_{N}^{(\mathcal{K})}(\mu_{N}^{2}, t_{0}) + \int_{t_{0}}^{\mu_{N}^{2}} d\Phi_{1} \mathcal{K}_{ij,k}(\Phi_{1}) \Delta_{N}^{(\mathcal{K})}(\mu_{N}^{2}, k_{\perp}^{2}) \right] \\ + d\Phi_{N+1} \mathcal{H}_{N}$$

• effect: only resummed parts modified with local K-factor



Example results: inclusive Z- p_{\perp} and $Zb\bar{b}$

snapshot of upcoming HERWIG ++ 3.0

 MC@NLO vs. POWHEG implemented in HERWIG ++ with two different parton showers (ang.ordered & CS dipole)



| | MEPs@Lo | | |
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Multijet merging

Multijet merging: basic idea

S. Catani, FK, R. Kuhn, & B. Webber, JHEP 0111 & L. Lonnblad, JHEP 0205 & FK, JHEP 0208

- parton shower resums logarithms fair description of collinear/soft emissions jet evolution (where the logs are large)
- matrix elements exact at given order fair description of hard/large-angle emissions jet production (where the logs are small)
- combine ("merge") both: result: "towers" of MEs with increasing number of jets evolved with PS
 - multijet cross sections at Born accuracy
 - maintain (N)LL accuracy of parton shower





Separating jet evolution and jet production

 separate regions of jet production and jet evolution with jet measure Q_J

("truncated showering" if not identical with evolution parameter)

- matrix elements populate hard regime
- parton showers populate soft domain
- plot from first practical implementation for hadron colliders

FK, A. Schaelicke, S. Schumann, G. Soff, Phys.Rev.D70



Di-photons @ ATLAS: $m_{\gamma\gamma}$, $p_{\perp,\gamma\gamma}$, and $\Delta\phi_{\gamma\gamma}$ in showers

arXiv:1211.1913 [hep-ex]



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Aside: Comparison with higher order calculations

arXiv:1211.1913 [hep-ex]



| | | MEPs@NLO | |
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Multijet merging at NLO

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Multijet-merging at NLO: MEPS@NLO, FxFx, & UNLOPS

S. Hoeche, FK, M. Schoenherr, & F. Siegert, JHEP 1304, arXiv 1207.5030

R. Frederix & S. Frixione, JHEP 1212, arXiv 1209.6215

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L. Lonnblad & S. Prestel, arXiv 1211.7278

- basic idea like at LO: towers of MEs with increasing jet multi (but this time at NLO)
- combine them into one sample, remove overlap/double-counting

maintain NLO and LL accuracy of ME and PS

towers of MC@NLO simulations without double-counting

(possibly further supplemented with LO simulations for even higher final state multiplicities)

First emission(s) in NLO-merged samples

$$d\sigma = d\Phi_N \tilde{\mathcal{B}}_N \left[\Delta_N^{(\mathcal{K})}(\mu_N^2, t_0) + \int_{t_0}^{\mu_N^2} d\Phi_1 \mathcal{K}_N \Delta_N^{(\mathcal{K})}(\mu_N^2, t_{N+1}) \Theta(Q_J - Q_{N+1}) \right] \\ + d\Phi_{N+1} \mathcal{H}_N \Delta_N^{(\mathcal{K})}(\mu_N^2, t_{N+1}) \Theta(Q_J - Q_{N+1})$$

$$+\mathrm{d}\Phi_{N+1}\,\tilde{\mathcal{B}}_{N+1}\left(1+\frac{\mathcal{B}_{N+1}}{\tilde{\mathcal{B}}_{N+1}}\int_{t_{N+1}}^{\mu_N^2}\mathrm{d}\Phi_1\,\mathcal{K}_N\right)\Theta(Q_{N+1}-Q_J)$$

$$\cdot \Delta_{N}^{(\mathcal{K})}(\mu_{N}^{2}, t_{N+1}) \cdot \left[\Delta_{N+1}^{(\mathcal{K})}(t_{N+1}, t_{0}) + \int_{t_{0}}^{t_{N+1}} \mathrm{d}\Phi_{1} \,\mathcal{K}_{N+1} \Delta_{N+1}^{(\mathcal{K})}(t_{N+1}, t_{N+2}) \right]$$

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$$+\mathrm{d}\Phi_{N+2}\,\mathcal{H}_{N+1}\Delta_{N}^{(\mathcal{K})}(\mu_{N}^{2},t_{N+1})\Delta_{N+1}^{(\mathcal{K})}(t_{N+1},t_{N+2})\Theta(Q_{N+1}-Q_{J})+\ldots$$







• first emission by MC@NLO , restrict to $Q_{n+1} < Q_{cut}$

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- first emission by MC@NLO, restrict to Q_{n+1} < Q_{cut}
- MC@NLO $pp \rightarrow h + \text{jet}$ for $Q_{n+1} > Q_{\text{cut}}$

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- first emission by MC@NLO, restrict to Q_{n+1} < Q_{cut}
- MC@NLO $pp \rightarrow h + \text{jet}$ for $Q_{n+1} > Q_{\text{cut}}$
- restrict emission off $pp \rightarrow h + \text{jet to}$ $Q_{n+2} < Q_{\text{cut}}$

p_{\perp}^{H} in MEPs@NLO



- first emission by MC@NLO , restrict to $Q_{n+1} < Q_{cut}$
- MC@NLO $pp \rightarrow h + \text{jet}$ for $Q_{n+1} > Q_{\text{cut}}$
- restrict emission off $pp \rightarrow h + \text{jet to}$ $Q_{n+2} < Q_{\text{cut}}$
- MC@NLO $pp \rightarrow h + 2jets$ for $Q_{n+2} > Q_{cut}$

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p_{\perp}^{H} in MEPs@NLO



- first emission by MC@NLO, restrict to Q_{n+1} < Q_{cut}
- MC@NLO $pp \rightarrow h + \text{jet}$ for $Q_{n+1} > Q_{\text{cut}}$
- restrict emission off $pp \rightarrow h + \text{jet to}$ $Q_{n+2} < Q_{\text{cut}}$
- MC@NLO $pp \rightarrow h + 2jets$ for $Q_{n+2} > Q_{cut}$
- iterate

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p_{\perp}^{H} in MEPs@NLO



- first emission by MC@NLO, restrict to Q_{n+1} < Q_{cut}
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- first emission by MC@NLO, restrict to Q_{n+1} < Q_{cut}
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- restrict emission off $pp \rightarrow h + \text{jet to}$ $Q_{n+2} < Q_{\text{cut}}$
- MC@NLO $pp \rightarrow h + 2jets$ for $Q_{n+2} > Q_{cut}$
- iterate

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• sum all contributions



- first emission by MC@NLO, restrict to Q_{n+1} < Q_{cut}
- MC@NLO $pp \rightarrow h + \text{jet}$ for $Q_{n+1} > Q_{\text{cut}}$
- restrict emission off $pp \rightarrow h + \text{jet to}$ $Q_{n+2} < Q_{\text{cut}}$
- MC@NLO $pp \rightarrow h + 2jets$ for $Q_{n+2} > Q_{cut}$
- iterate
- sum all contributions
- eg. p⊥(h)>200 GeV has contributions fr. multiple topologies

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Differences between MEPS@NLO, FxFx, & UNLOPS

| | MEPs@Nlo | FxFx | UNLOPS |
|----------------|---|-----------------------|----------------------|
| | in SHERPA | with aMC@NLO_MADGRAPH | in Pythia/Herwig |
| ME | \mathcal{V} external | all internal | all external |
| | $\mathcal{B}, \mathcal{R}, \mathcal{S}$ fromCOMIX or AMEGIC++ | aMC@NLO_MADGRAPH | LH event files |
| | ${\cal V}$ from OpenLoops, BlackHat, Njet, \ldots | | |
| shower | internal | external | internal |
| | CS Shower from SHERPA | HERWIG or PYTHIA | Pythia/Herwig |
| Δ_N | from PS | analytical | from PS |
| $\Theta(Q_J)$ | per emission | a-posteriori | per emission |
| Q_{J} -range | > Sudakov regime | relatively high | pprox Sudakov regime |
| | | (but changed) | |

MEPs@NLO: validation in W+jets

S. Hoeche, F. Krauss, M. Schoenherr & F. Siegert, JHEP 1304









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FxFx: validation in Z+jets

(Data from ATLAS, 1304.7098, aMC@NLO_MADGRAPH with HERWIG++)

(green: 0, 1, 2 jets + uncertainty band from scale and PDF variations, red: MC@NLO)



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FxFx: validation in Z+jets

(Data from ATLAS, 1304.7098, aMC@NLO_MADGRAPH with HERWIG++)

(green: 0, 1, 2 jets + uncertainty band from scale and PDF variations, red: MC@NLO)



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Multijet merging in HERWIG ++: validation in W+jets

Merging algorithm from S. Platzer, JHEP 1308





Aside: merging without Q_J - the MINLO approach

K.Hamilton, P.Nason, C.Oleari & G.Zanderighi, JHEP 1305

- based on POWHEG + shower from PYTHIA or HERWIG
- up to today only for singlet S production, gives NNLO + PS
- basic idea:
 - use S+jet in POWHEG
 - push jet cut to parton shower IR cutoff
 - scale setting like in multijet merging
 - apply analytic NNLL Sudakov rejection weight for intrinsic line in Born configuration

(kills divergent behaviour at order α_S)

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- don't forget double-counted terms
- reweight to NNLO fixed order

NNLOPS for H production

K. Hamilton, P. Nason, E. Re & G. Zanderighi, JHEP 1310



Alternative NNLO+PS: UN²LOPS

S. Hoche, Y. Li, & S. Prestel, Phys.Rev.D90 & D91

• building on UNLOPS logic: add and subtract terms in parton shower



| | | PS improvements | |
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Improving the parton showers

Going dipoles

- first parton showers in PYTHIA and HERWIG based on $1\to 2$ splittings evolution parameters given by invariant mass (ang.veto) or angle
- \bullet antenna shower based on $2 \rightarrow 3$ in ARIADNE:

also in VINCIA (W. Giele, D. Kosover & P. Skands, Phys.Rev.D78)

- no discrimination of splitter & spectator
- transverse momentum as ordering parameter
- for $e^-e^+
 ightarrow$ hadrons and DIS only
- extension to initial states in J. Winter & FK, JHEP 0807
- dipole showers based on subtraction kernels:
 - $\bullet\,$ based on $2 \rightarrow 3$ kinematics with splitter–spectator identification
 - transverse momentum as ordering parameter
 - first proposed to alleviate NLO matching (MC@NLO)

Z. Nagy & D. Soper, JHEP 0510

 $\bullet\,$ implemented stand-alone and as part of SHERPA and HERWIG $++\,$

M. Dinsdale, M. Ternick, & S. Weinzierl, Phys.Rev.D76

S. Schumann & FK, JHEP 0803 & S. Platzer & S. Gieseke, Eur.Phys.C72

A new hybrid shower between dipole and parton shower

S. Hoeche & S. Prestel, arXiv 1506.05057

• use transverse momentum defined in soft instead of collinear regime: amounts to dynamical rescaling of trivial k_\perp

the exact inverse of soft eikonal

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- enforce collinear anomalous dimensions
- two independent implementations in SHERPA and PYTHIA
- LO multijet merging already available

Validation of DIRE in $e^-e^+ \rightarrow$ hadrons

S. Hoche, Y. Li, & S. Prestel, Phys.Rev.D90 & D91

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| | | PS improvements | |
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Validation of DIRE in Drell-Yan

S. Hoche, Y. Li, & S. Prestel, Phys.Rev.D90 & D91



usually small contribution (see next slide) – ▲□▶ ▲圖▶ ▲屋▶ ▲屋▶ F. Krauss Status of Parton Shower Simulations

Including higher orders in $1/N_c$

Ingredients

- parton showers are formulated in the large- N_c limit
- sum over external colour factors for gluon emission

$$\sum_{j\neq i} \mathbf{T}_i \mathbf{T}_j^{\dagger} = |\mathbf{T}_i|^2$$

only relevant for observables driven by non-global logarithms

PS improvements

Merging algorithm from S. Platzer, JHEP 1308

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- comparing soft matrix elements for various accuracies in $1/N_c$ (left)
- average p_{\perp} distribution w.r.t. an axis orthogonal to event plane



Including higher logarithms

S. Hoeche, FK, S. Prestel, M. Schonherr, in prep

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- compare with Q_T resummation in Collins–Soper–Sterman scheme:
 - Sudakov form factor given by

$$\Delta(t,t_0) = \exp\left\{-\int_{t_0}^t \frac{\mathrm{d}k_\perp^2}{k_\perp^2}\left[A(k_\perp^2)\log\frac{k_\perp^2}{t_0} + B(k_\perp^2)\right]\right\}$$

where A and B have expansion in α_S

- parton showers usually include terms $A^{(1,2)}$ and $B^{(1)}$ ("NLL") in differential form, all process-independent
- can try to include $A^{(3)}$ process-independent parts of $B^{(2)}$

Effect of higher logarithms in Drell-Yan

S. Hoeche, FK, S. Prestel, M. Schonherr, in prep



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Effect of higher logarithms in $gg \rightarrow H$

S. Hoeche, FK, S. Prestel, M. Schonherr, in prep



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Adding spin correlations, weak emissions

• can also add spin correlations - needs large matrix multiplications

Z. Nagy & D. Soper, JHEP 1206 & HERWIG ++, in prep.

- attempts to include electroweak emissions in shower:
 - photon in shower are trivial, multijet merging available

S. Hoeche, S. Schumann, & F. Siegert, Phys.Rev.D81

- W and Z emission more tricky, due to spin structure
- emission of single boson ok, second boson much harder
- some implementations in PYTHIA and SHERPA

J. R. Christiansen & T. Sjostrand, JHEP 1404 & FK, P. Petrov, M. Schoenherr, & M. Spannowsky, Phys.Rev.D89

Summary

- Systematic improvement of event generators by including higher orders has been at the core of QCD theory and developments in the past decade:
 - multijet merging ("CKKW", "MLM")
 - NLO matching ("MC@NLO", "POWHEG")
 - MEPS@NLO ("SHERPA", "UNLOPS", "FxFx")
 - NNLOPS feasible for simple processes



"So what's this? I asked for a hammer! A hammer! This is a crescent wrench! ... Well, maybe it's a hammer. ... Damn these stone tools."

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(first 3 methods are well understood and used in experiments)

- multijet merging at NLO for relevant signals and backgrounds
- complete automation of NLO calculations done

 $\longrightarrow must \ benefit \ from \ it! \qquad {\tiny (it's \ the \ precision \ and \ trustworthy \ \& \ systematic \ uncertainty \ estimates!)}$

(last method need validation etc.)

• first steps towards systematic improvement of parton showers: 1/N corrections spin correlations higher logarithms