

Generating fermion masses and mixing angles in extra Higgs doublet models

Ana Solaguren-Beascoa Negre

in collaboration with Alejandro Ibarra

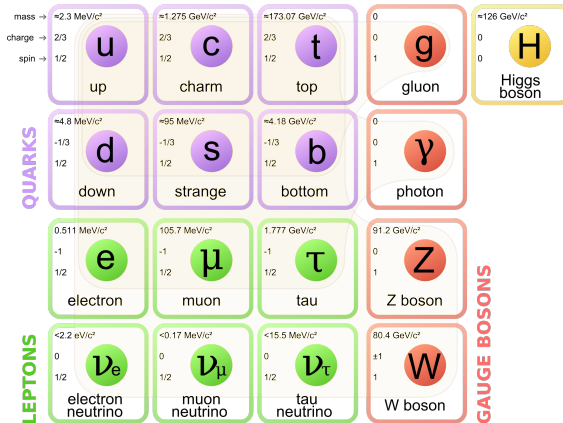
Technische Universität München & Max-Planck-Institut für Physik

DESY Theory Workshop – 30 Sept. 2015

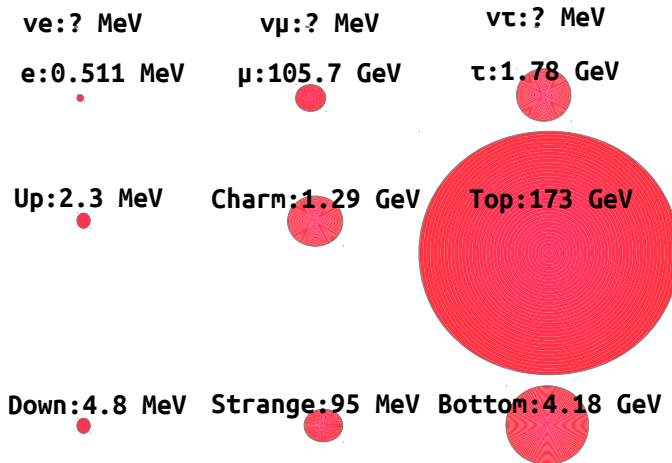


Max-Planck-Institut für Physik
(Werner-Heisenberg-Institut)

Introduction



Pattern of masses



Pattern of mixing angles

$$V_{CKM} = \begin{pmatrix} 0.974 & 0.225 & 0.0035 \\ 0.225 & 0.973 & 0.041 \\ 0.0087 & 0.04 & 0.999 \end{pmatrix}$$
$$U_{PMNS} = \begin{pmatrix} 0.822 & 0.574 & 0.156 \\ 0.355 & 0.704 & 0.614 \\ 0.443 & 0.452 & 0.774 \end{pmatrix}$$

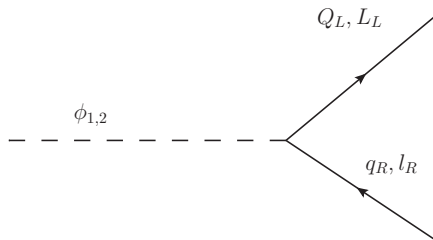
The Two-Higgs Doublet Model

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- ▶ Standard Model + one extra Higgs doublet.

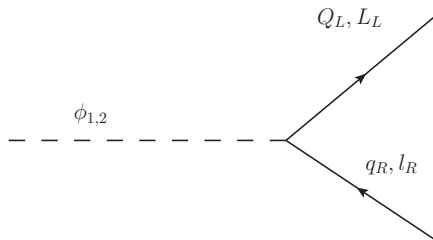
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- ▶ Interactions with fermions:



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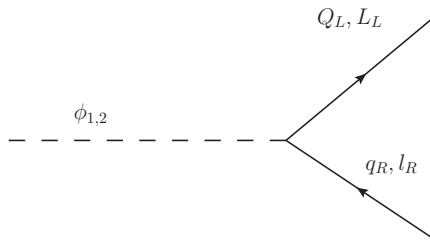
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- ▶ Interactions with SM Higgs

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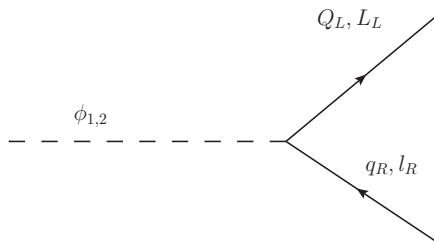
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- ▶ Interactions with SM Higgs
- ▶ Self-interactions

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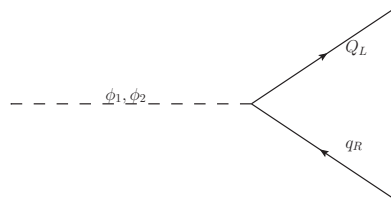


- ▶ Interactions with SM Higgs
- ▶ Self-interactions
- ▶ Decoupling limit ($M_{\phi_1} \sim 126$ GeV,
 $M_{\phi_2} \gg M_{\phi_1} \rightarrow \text{FCNC, LFV processes}$)

The Mass Sector

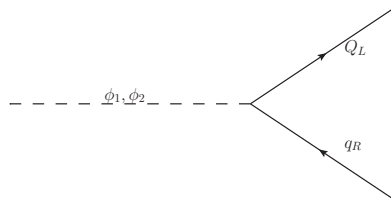
The Mass Sector

- ▶ Basis $\langle \Phi_1^0 \rangle = v/\sqrt{2}$,
 $\langle \Phi_2^0 \rangle = 0$
- ▶ Yukawa interaction
(rank-1):



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$$Y_x^{(1,2)}|_{\text{tree}} = |y_{x_L}^{(1,2)}\rangle \langle y_{x_R}^{(1,2)}|$$

The Mass Sector: Quarks

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$$Y_u^{(1)}|_{\text{tree}} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & y_u^{(1)} \end{pmatrix}, \quad Y_d^{(1)}|_{\text{tree}} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & \epsilon y_d^{(1)} \\ 0 & 0 & y_d^{(1)} \end{pmatrix}$$

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Tree Level: m_t, m_b

$$Y_u^{(2)}|_{\text{tree}} = |y_{u_L}^{(2)}\rangle \langle y_{u_R}^{(2)}|, \quad Y_d^{(2)}|_{\text{tree}} = |y_{d_L}^{(2)}\rangle \langle y_{d_R}^{(2)}|$$

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- Parametrize:

$$|y_{u_L}^{(2)}\rangle = \sqrt{y_u^{(2)}} \begin{pmatrix} e^{i\rho_{u_L}} \sin \theta_{u_L} \sin \omega_{u_L} \\ e^{i\xi_{u_L}} \sin \theta_{u_L} \cos \omega_{u_L} \\ \cos \theta_{u_L} \end{pmatrix}$$

- Neglect phases.

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Tree Level: m_τ, m_{ν_3}

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- 1-loop from β function:

$$Y_x^{(1)}|_{1\text{-loop}} \simeq Y_x^{(1)}|_{\text{tree}} + \frac{1}{16\pi^2} \beta_x^{(1)} \log \frac{\Lambda}{M_{\phi 2}}$$

Radiative Masses

Radiative Masses

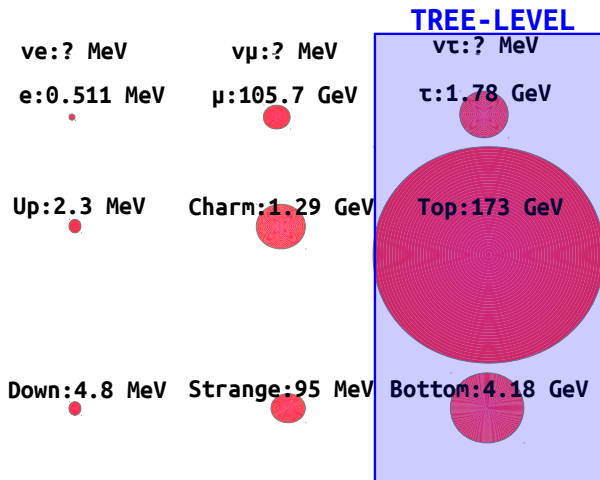
$$\frac{y_{x_2}}{y_{x_3}} \sim \left(\frac{1}{16\pi^2} \log \frac{\Lambda}{M_H} \right) \times \text{model parameters}$$

Radiative Masses

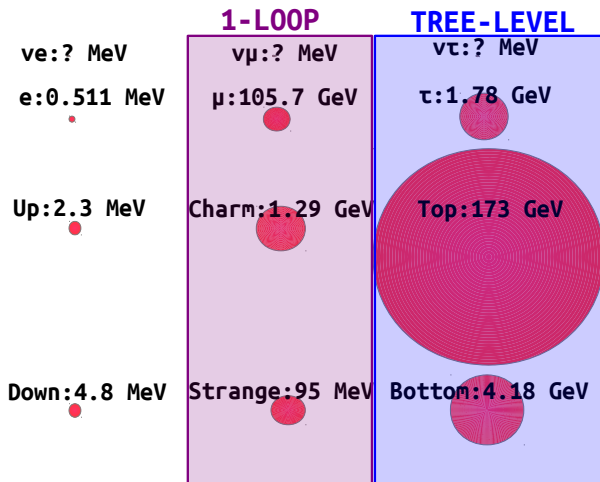
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- First generation massless.

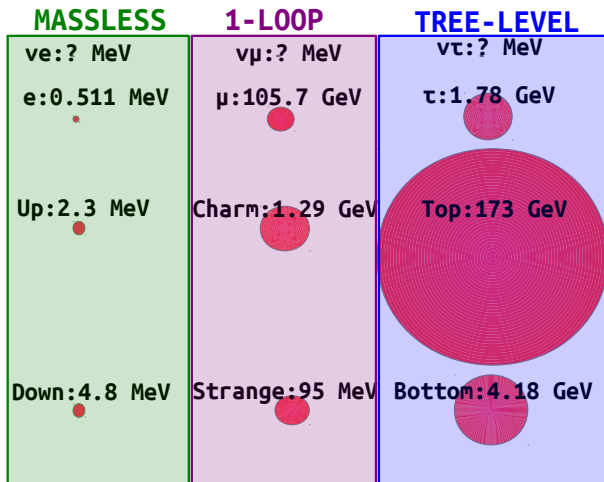
Radiative Masses



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Radiative Masses



The Mixing Sector

$$\begin{pmatrix} y_1 & 0 & 0 \\ 0 & y_2 & 0 \\ 0 & 0 & y_3 \end{pmatrix} = V_{L_x}^\dagger Y_x^{(1)} V_{R_x}$$

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$$V_{CKM} = V_{u_L}^\dagger V_{d_L} = \begin{pmatrix} 0.974 & 0.225 & 0.0035 \\ 0.225 & 0.973 & 0.041 \\ 0.0087 & 0.04 & 0.999 \end{pmatrix}$$

$$V_{PMNS} = V_{e_L}^\dagger V_{\nu_L} = \begin{pmatrix} 0.822 & 0.574 & 0.156 \\ 0.355 & 0.704 & 0.614 \\ 0.443 & 0.452 & 0.774 \end{pmatrix}$$

$$V_u = \begin{pmatrix} \mathbf{u}_L & \mathbf{c}_L & \mathbf{t}_L \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad V_d = \begin{pmatrix} \mathbf{d}_L & \mathbf{s}_L & \mathbf{b}_L \\ 0.974 & 0.225 & 0.0035 \\ 0.225 & 0.973 & 0.041 \\ 0.0087 & 0.04 & 0.999 \end{pmatrix}$$

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The Quark Sector

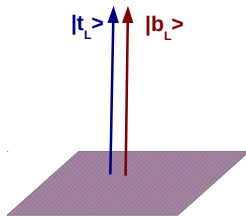
$$Y_u^{(1)}|_{\text{tree}} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & y_u^{(1)} \end{pmatrix}, \quad Y_d^{(1)}|_{\text{tree}} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & \epsilon y_d^{(1)} \\ 0 & 0 & y_d^{(1)} \end{pmatrix}$$

$$|V_{ub}|^2 + |V_{cb}|^2 \ll 1 \Rightarrow \epsilon \rightarrow 0$$

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Tree Level:

$$\Rightarrow V_{CKM} = \begin{pmatrix} ? & ? & 0 \\ ? & ? & 0 \\ 0 & 0 & 1 \end{pmatrix}$$



Quark Mixing Angles

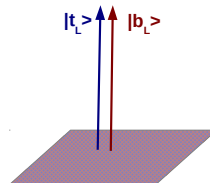
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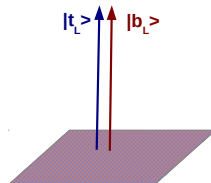
- ▶ $V_{tb} \sim 1$ @ tree-level.



Quark Mixing Angles

► $V_{CKM} = V_u^\dagger V_d$

► $V_{tb} \sim 1$ @ tree-level.



► Cabibbo angle @ 0-order in perturbation theory:

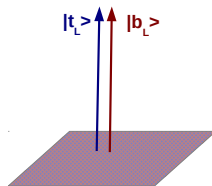
$$V_{us} \simeq -V_{cd} \simeq \frac{3 \sin \theta_{d_L} \cos \theta_{u_L} \sin(\omega_{d_L} - \omega_{u_L})}{N_d}$$

$$N_d = [9 \sin^2 \theta_{d_L} \cos^2 \theta_{u_L} + 4 \cos^2 \theta_{d_L} \sin^2 \theta_{u_L} - 3 \sin 2\theta_{d_L} \sin 2\theta_{u_L} \cos(\omega_{d_L} - \omega_{u_L})]^{1/2}$$

Quark Mixing Angles

- ▶ $V_{CKM} = V_u^\dagger V_d$

- ▶ $V_{tb} \sim 1$ @ tree-level.



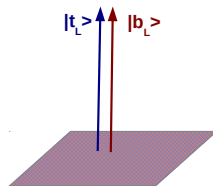
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► $V_{tb} \sim 1$ @ tree-level.



► Cabibbo angle @ 0-order in perturbation theory:

$$V_{us} \simeq -V_{cd} \simeq \text{mixing angles}$$

► @ 1st order: $V_{ub} \simeq \left(\frac{1}{16\pi^2} \log \frac{\Lambda}{M_H} \right) \frac{3y_u^{(1)} y_u^{(2)} y_d^{(2)}}{y_d^{(1)}} \times \text{mixing angles}$

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Tree-level

0th Order

↓

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↑
Tree-level

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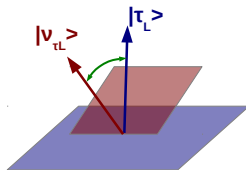
0th Order
1st Order Tree-level

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$$\Rightarrow U^{PMNS} = \begin{pmatrix} ? & ? & ? \\ ? & ? & ? \\ ? & ? & \cos \alpha \end{pmatrix}$$



PMNS Matrix

$$|U^{PMNS}| = \begin{pmatrix} 0.822 & 0.574 & 0.156 \\ 0.355 & 0.704 & 0.614 \\ 0.443 & 0.452 & 0.774 \end{pmatrix}$$

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0-Order
Tree-Level

3HDM

- ▶ SM + 2 Higgs doublets

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- ▶ $Y_x^{(a)} = \left| y_{x_L}^{(a)} \right\rangle \left\langle y_{x_R}^{(a)} \right|$ ($x = u, d, e, \nu, a = 1, 2, 3$).

3HDM

- ▶ SM + 2 Higgs doublets
- ▶ $Y_x^{(a)} = \left| y_{x_L}^{(a)} \right\rangle \left\langle y_{x_R}^{(a)} \right|$ ($x = u, d, e, \nu, a = 1, 2, 3$).
- ▶ 1 mass @ tree level for each family

3HDM

$$\blacktriangleright \frac{m_{x_2}}{m_{x_3}} \sim \left(\frac{1}{16\pi^2} \log \frac{\Lambda}{M_H} \right) \times \text{model parameters}$$

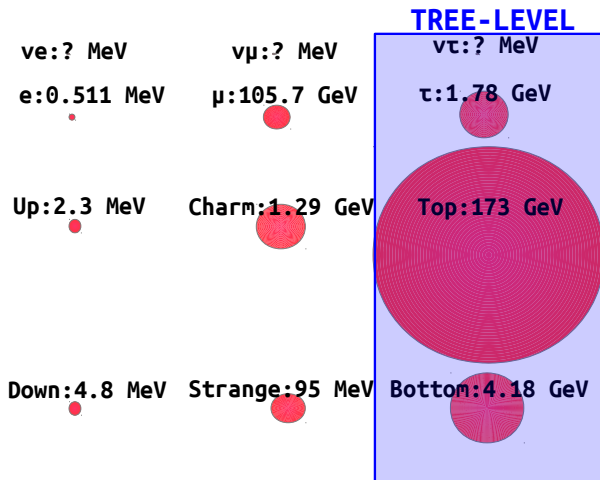
3HDM

- ▶ $\frac{m_{x_2}}{m_{x_3}} \sim \left(\frac{1}{16\pi^2} \log \frac{\Lambda}{M_H} \right) \times \text{model parameters}$
- ▶ $0 < \frac{m_{x_1}}{m_{x_2}} \sim \text{model parameters} < 1$

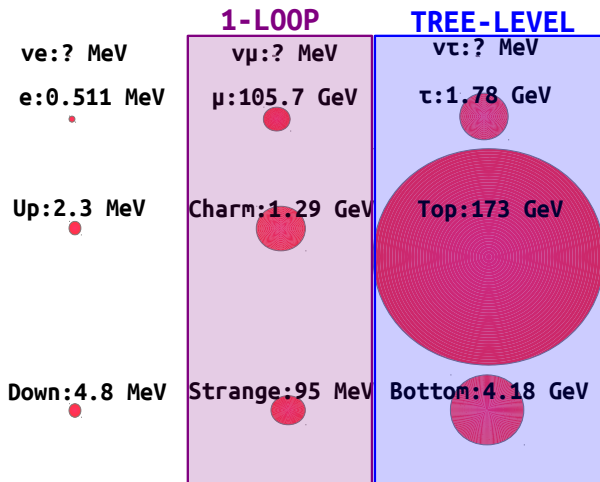
3HDM

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- ▶ $0 < \frac{m_{x_1}}{m_{x_2}} \sim \text{model parameters} < 1$
- ▶ Mixing already in a 2HDM $\Rightarrow$ no extra conditions needed

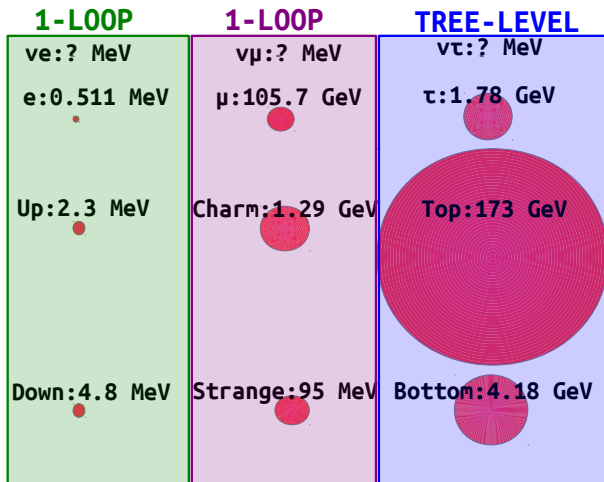
Radiative Masses – The 3HDM



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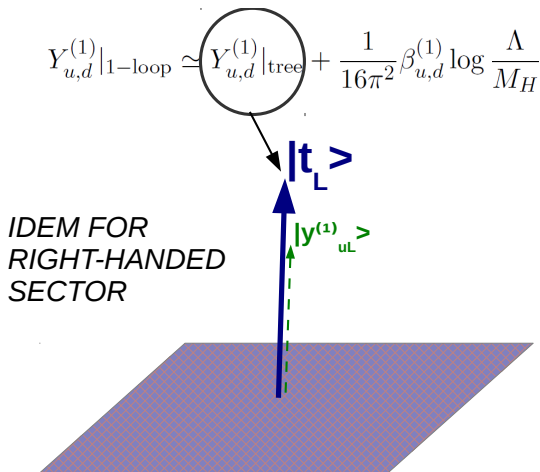


Conclusions

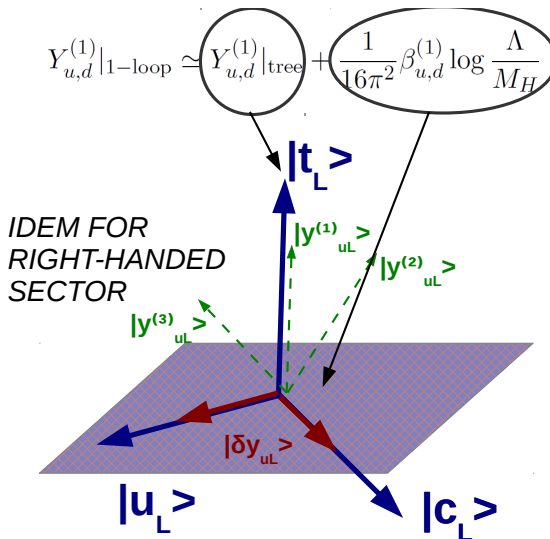
- ▶ Extend the SM with extra Higgs doublets.
- ▶ ~~Extra fermions~~ (except RH-neutrinos).
- ▶ ~~Extra symmetries~~
- ✓ Minimal model (Rank-1 Yukawa)
- ▶ Generate:
 - ✓ All 3rd generation masses @ tree level
 - ✓ All 2nd generation masses @ 1-loop
 - ✓ All 1st generation masses @ 1-loop (3HDM)
 - ✓ Hierarchical CKM
 - ✓ Anarchical PMNS

Backup Slides

2HDM

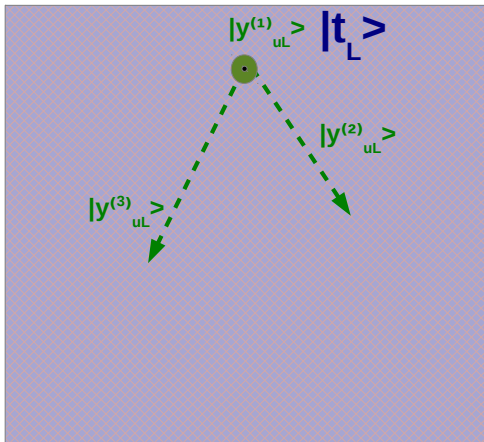


3HDM



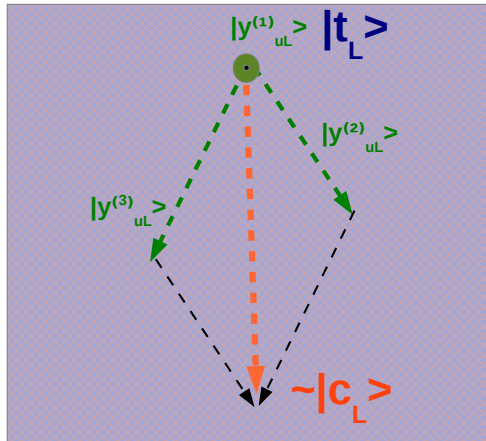
Hierarchy 1st and 2nd generation

IDEM FOR RIGHT-HANDED SECTOR



Hierarchy 1st and 2nd generation

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