

Automated NLO QCD+EW corrections for the LHC



**Universität
Zürich^{UZH}**

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work in collaboration with:

S. Kallweit, P. Maierhöfer, S. Pozzorini, M. Schönherr

[arXiv:1412.5157 , arXiv:1505.05704]

DESY Theory Workshop 2015
DESY, Hamburg, 30th of September 2015

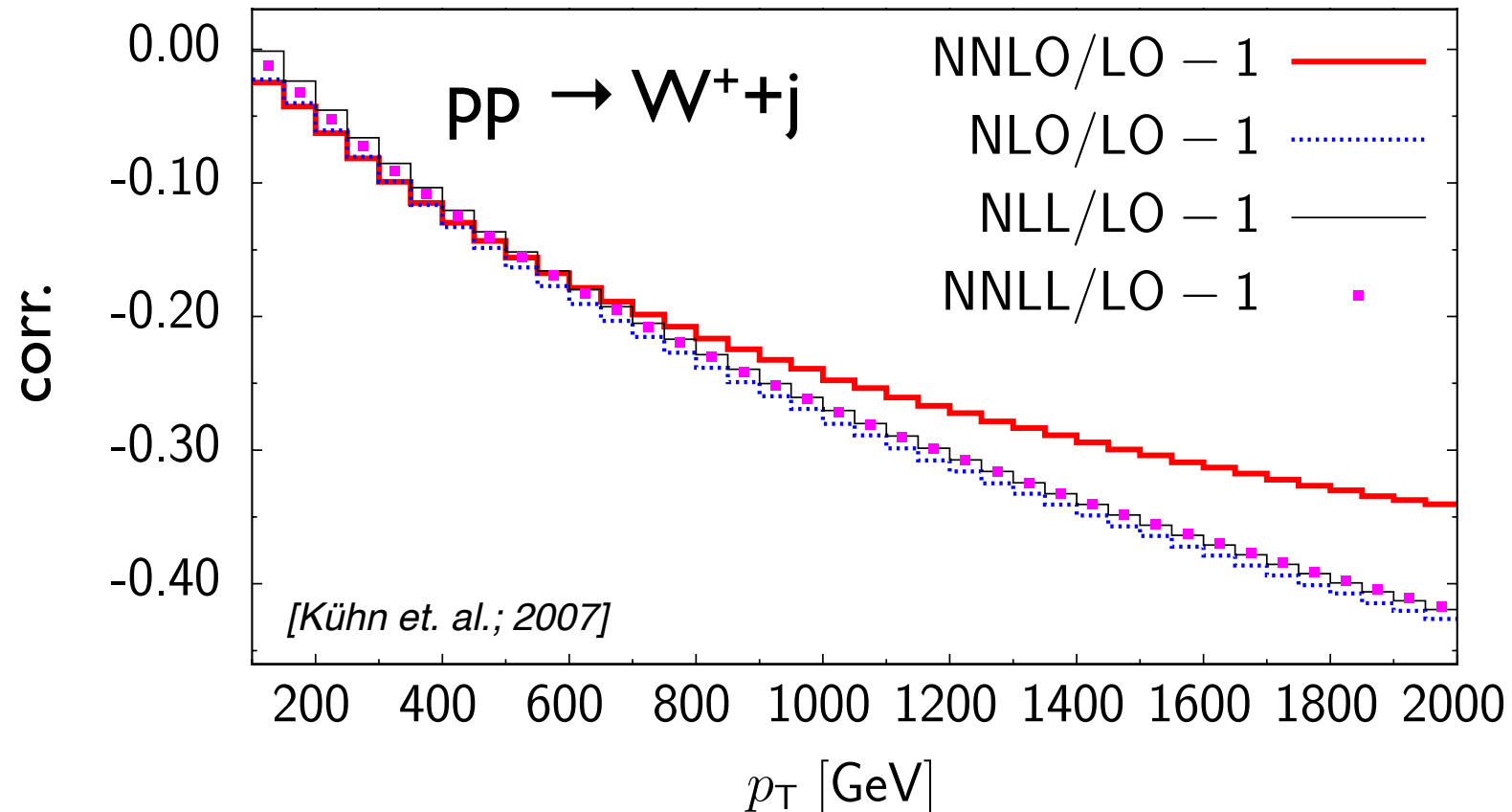
Why EW corrections?

- Formally suppressed by α/α_s with respect to QCD and numerically $\mathcal{O}(\alpha) \sim \mathcal{O}(\alpha_s^2) \Rightarrow$ **NLO EW \sim NNLO QCD**

- Possible large (negative) enhancement due to universal virtual **Sudakov logs** at high energies (i.e. in the tails of the distributions):

$$\text{NLO EW} \sim -\alpha \log^2 \left(\frac{M_V^2}{\hat{s}} \right)$$

[Ciafaloni, Comelli, '98;
 Lipatov, Fadin, Martin, Melles, '99;
 Kuehen, Penin, Smirnov, '99;
 Denner, Pozzorini, '00]



What are EW corrections?

Perturbative power counting

LO subleading Born contributions

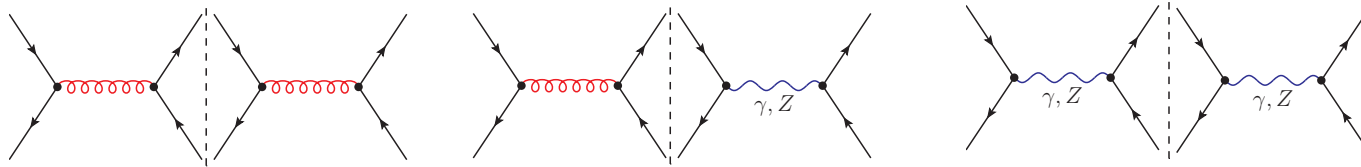
$$d\sigma = d\sigma(\alpha_s^n \alpha^m) + d\sigma(\alpha_s^{n-1} \alpha^{m+1}) + \sigma(\alpha_s^{n-2} \alpha^{m+2}) + \dots$$

Perturbative power counting

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subleading Born contributions

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Illustrative example: $q\bar{q} \rightarrow q\bar{q}$

Perturbative power counting

LO subleading Born contributions

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$$\dots + \sigma(\alpha_s^{n+1} \alpha^m) + d\sigma(\alpha_s^n \alpha^{m+1}) + \sigma(\alpha_s^{n-1} \alpha^{m+2}) + \sigma(\alpha_s^{n-2} \alpha^{m+3}) + \dots$$

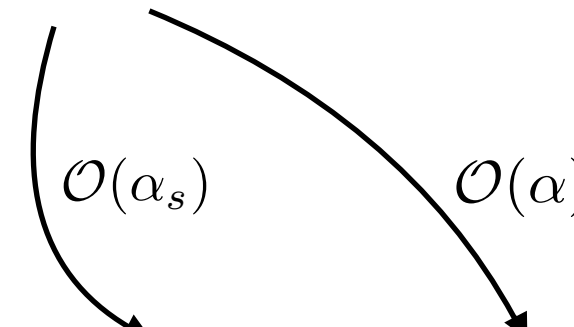
“NLO **QCD**” “NLO **EW**”

Perturbative power counting

LO

subleading Born contributions

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“NLO **QCD**”

“NLO **EW**”

“subleading one-loop contributions”

Perturbative power counting

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subleading Born contributions

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$\mathcal{O}(\alpha_s)$

$\mathcal{O}(\alpha)$

$$\dots + \sigma(\alpha_s^{n+1} \alpha^m) + d\sigma(\alpha_s^n \alpha^{m+1}) + \sigma(\alpha_s^{n-1} \alpha^{m+2}) + \sigma(\alpha_s^{n-2} \alpha^{m+3}) + \dots$$

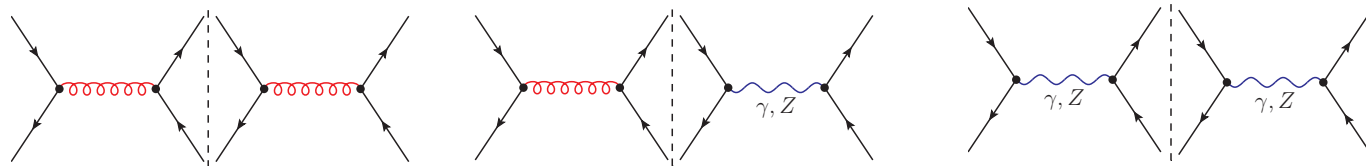
“NLO QCD”

“NLO EW”

Perturbative power counting

LO subleading Born contributions

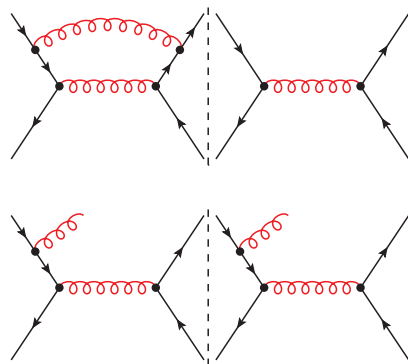
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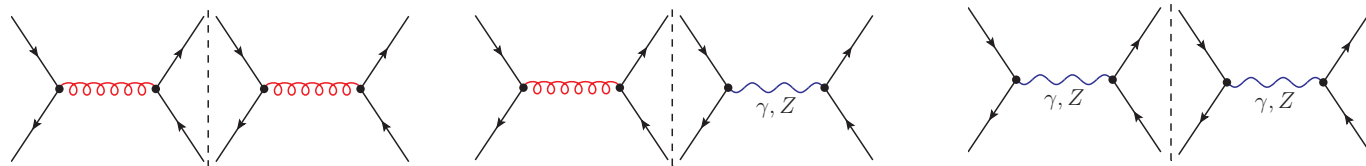


Perturbative power counting

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subleading Born contributions

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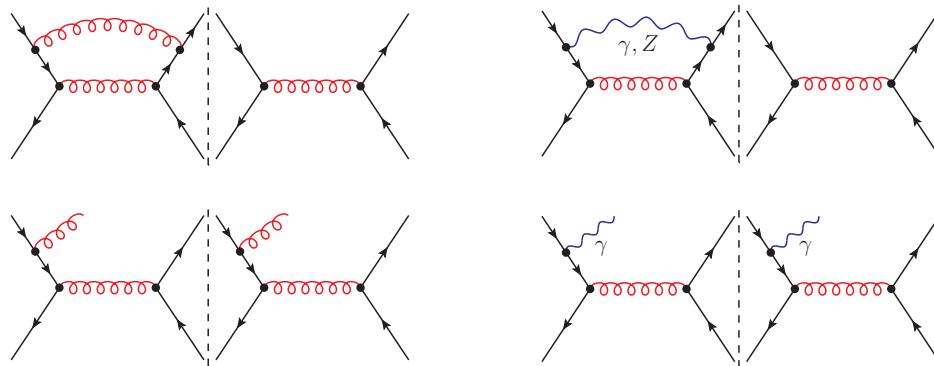


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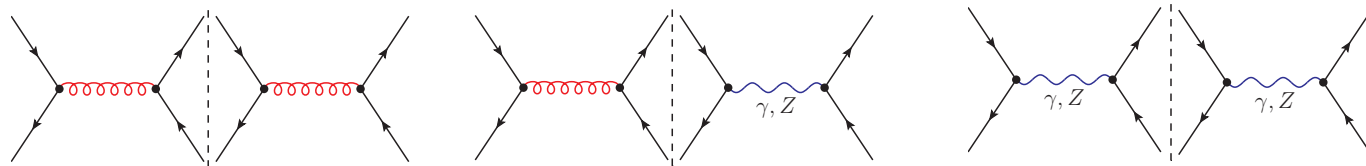


Perturbative power counting

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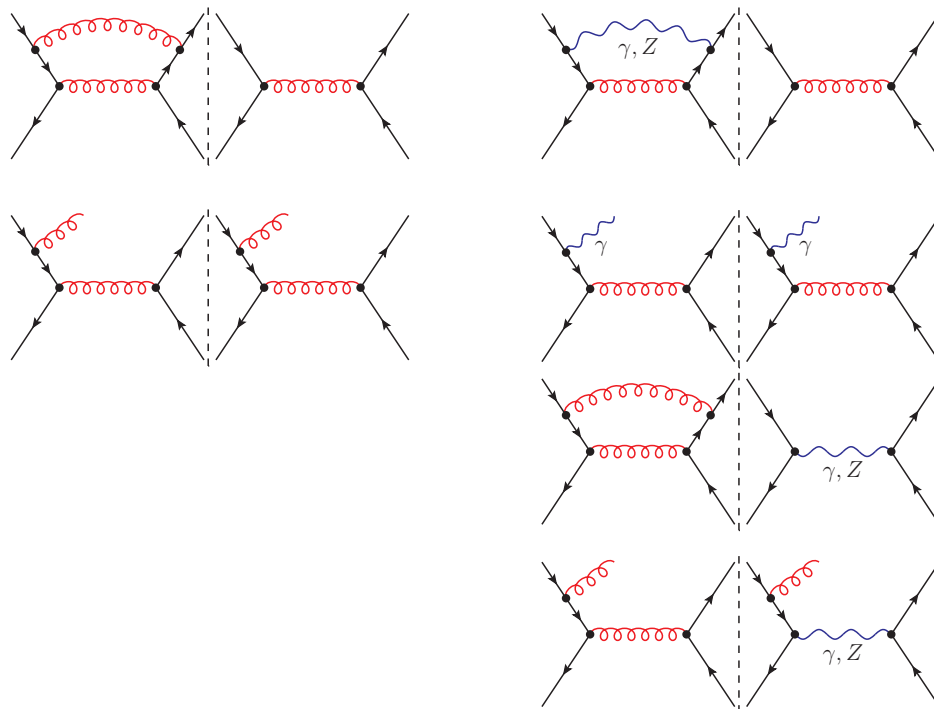


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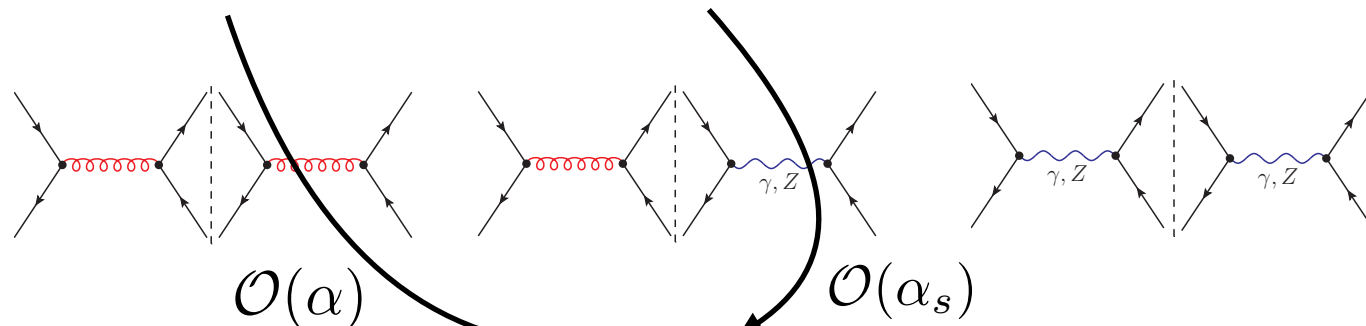


Perturbative power counting

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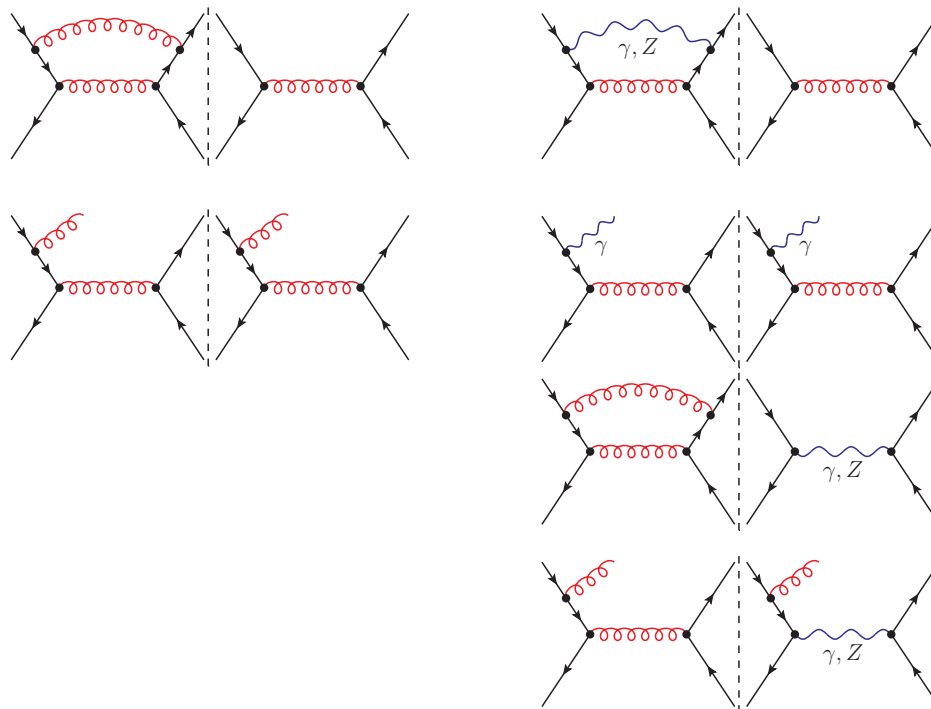
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“NLO **QCD**”

“NLO **EW**”

“subleading one-loop contributions”



Note:

- No diagrammatic separation in NLO **QCD** and **EW**
- An IR finite & gauge invariant result is only obtained including all virtual and real contributions of a given perturbative order.

Perturbative power counting

LO

subleading Born contributions

$$d\sigma = d\sigma(\alpha_s^n \alpha^m) + d\sigma(\alpha_s^{n-1} \alpha^{m+1}) + \sigma(\alpha_s^{n-2} \alpha^{m+2}) + \dots$$

The diagram shows two curved arrows originating from the first two terms of the top equation. The first arrow, labeled $\mathcal{O}(\alpha_s)$, points from $d\sigma(\alpha_s^n \alpha^m)$ to the first term of the bottom equation, $\dots + \sigma(\alpha_s^{n+1} \alpha^m)$. The second arrow, labeled $\mathcal{O}(\alpha)$, points from $d\sigma(\alpha_s^{n-1} \alpha^{m+1})$ to the second term of the bottom equation, $+ d\sigma(\alpha_s^n \alpha^{m+1})$.

$$\dots + \sigma(\alpha_s^{n+1} \alpha^m) + d\sigma(\alpha_s^n \alpha^{m+1}) + \sigma(\alpha_s^{n-1} \alpha^{m+2}) + \sigma(\alpha_s^{n-2} \alpha^{m+3}) + \dots$$

“NLO **QCD**”

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“subleading one-loop contributions”

✓ **Automation** requires universal power counting and bookkeeping in α and α_s including different interference effects for all contributions: virtual, real, subtraction.

Input:

1. Born process and desired order $\alpha_s^n \alpha^m$
2. type of correction, i.e. “NLO **QCD**” $\equiv \alpha_s^{n+1} \alpha^m$ or “NLO **EW**” $\equiv \alpha_s^n \alpha^{m+1}$

Automation of NLO QCD

$$\sigma^{\text{NLO}} = \int d\Phi_B (B + V + I) + \int d\Phi_R (R - S)$$

OpenLoops

[JML, Maierhöfer, Pozzorini]

Monte-Carlo-Framework:

Sherpa

[Gleisberg, Höche, Krauss, Schönherr, Schumann, Siegert, Winter et. al.]

MUNICH:

MUlti-**cha**Nnel Integrator at swiss (CH) precision

[Kallweit]

POWHEG-**BOX**

[Alioli, Nason, Oleari, Re, et. al.]

Herwig++/Matchbox

[Bellm, Gieseke, Grellscheid, Papaefstathiou, Plätzer, Richardson, Seymour, Siodmok, et al.]

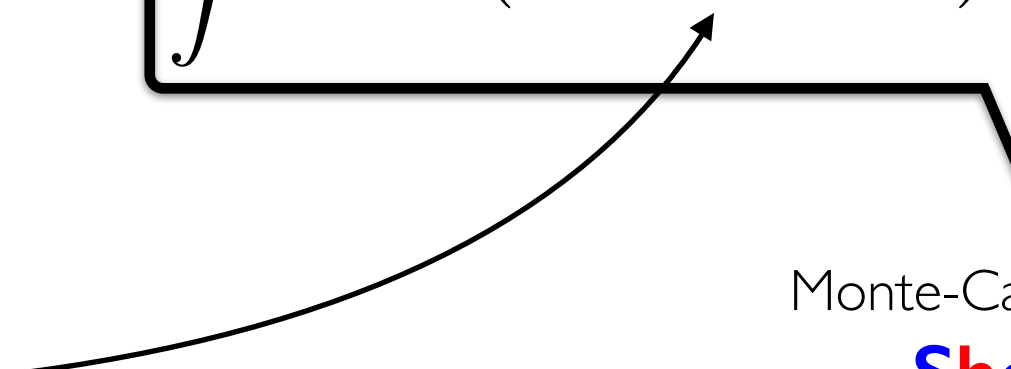
Whizard

[Kilian, Ohl, Reuter, Bach, Chokoufe Nejad, Weiss, et.al.]

OpenLoops with NLO QCD is publicly available at

<http://openloops.hepforge.org>

Automation of NLO QCD+EW

$$\sigma^{\text{NLO}} = \int d\Phi_B (B + V + I) + \int d\Phi_R (R - S)$$


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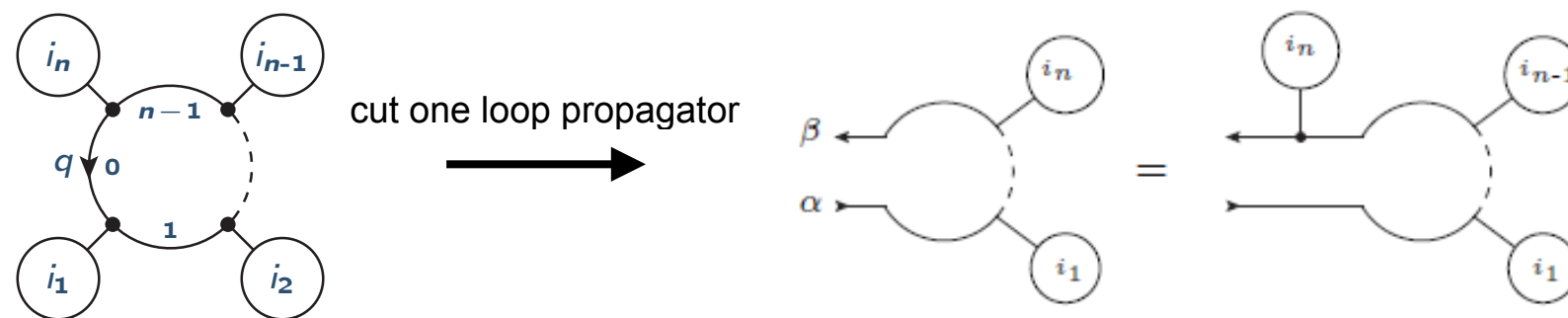
[Kallweit]

- NLO corrections in the full SM (QCD & EW) are implemented in OpenLoops together with Sherpa and MUNICH (will be included in upcoming public releases)
- missing: PS matching & merging (work in progress)

The OpenLoops program

[F. Cascioli, JML, P. Maierhöfer, S. Pozzorini, '14]

- ▶ **FAST** and flexible implementation of the Open Loops algorithm [F. Cascioli, P. Maierhöfer, S. Pozzorini, '12]:
a process- and model-independent numerical recursion for the calculation of one-loop amplitudes



- ▶ Publicly available at **<http://openloops.hepforge.org>**
- ▶ Amplitudes for any $2 \rightarrow 4(5)$ NLO **QCD** process in the SM available:
tree & (renormalized) virtual amplitudes, color correlations, spin correlations
- ▶ Installation (Requirements: gfortran ≥ 4.6 , Python 2.x, x ≥ 4): `$ cd ./OpenLoops && ./scons`
- ▶ Interfaces to reduction/scalar integral libraries:
 - **CutTools** [Ossola, Papadopolous, Pittau; '07] + **OneLOop** [van Hameren], **COLLIER** [Denner, Dittmaier, Hofer], **Samurai** [Mastrolia, Ossola, Reiter, Tramontano; '10]

The OpenLoops NLO **QCD** process library

- Public library includes > 100 LHC processes including $t\bar{t}+0,1,2\text{ j}$, $t\bar{t}V+0,1\text{ j}$, $t\bar{t}h+0,1\text{ j}$, **$H+0,1,2,3\text{ j}$** ...
- List of available process will grow continuously

OpenLoops is hosted by Hepforge, IPPP Durham

- Home
- Download & Installation
- Change Log
- Process Library
- Documentation
 - Getting started
 - Native Fortran interface
 - Native C/C++ interface
 - BLHA interface
 - OpenLoops+Sherpa
 - OpenLoops+Herwig++
 - Parameters
 - Stability system
- Pheno studies
- Third party tools
- Contact

OpenLoops Process Library

<http://openloops.hepforge.org>

The following libraries are available within OpenLoops and contain all relevant matrix elements to compute NLO QCD corrections, including color- and helicity-correlations. NLO electroweak corrections will be supported soon as well.

Note: the set of available processes will be significantly extended in the near future. However, please do not hesitate to send us an **email** if the process you want to study is not (yet) available.

Library	Process	Category	Description
pptt	$pp \rightarrow t\bar{t}$	$pp \rightarrow t\bar{t}+\text{jets}$	Top-quark pair production.
ppttj	$pp \rightarrow t\bar{t}j$	$pp \rightarrow t\bar{t}+\text{jets}$	Top-quark pair production with an additional jet.
ppttjj	$pp \rightarrow t\bar{t}jj$	$pp \rightarrow t\bar{t}+\text{jets}$	Top-quark pair production with two additional jets.
ppjj	$pp \rightarrow jj$	$pp \rightarrow \text{jets}$	Production of two jets.
ppjjj	$pp \rightarrow jjj$	$pp \rightarrow \text{jets}$	Production of three jets.
ppatt	$pp \rightarrow A t\bar{t}$	$pp \rightarrow V t\bar{t}+\text{jets}$	Photon plus t t-bar production.
ppattj	$pp \rightarrow A t\bar{t}j$	$pp \rightarrow V t\bar{t}+\text{jets}$	Photon plus t t-bar jet production.
pplltt	$pp \rightarrow l\bar{l} t\bar{t}$	$pp \rightarrow V t\bar{t}+\text{jets}$	Off-shell Z/A boson plus t t-bar production with leptonic decays (l+l- and nn)
ppllttj	$pp \rightarrow l\bar{l} t\bar{t}j$	$pp \rightarrow V t\bar{t}+\text{jets}$	Off-shell Z/A boson plus t t-bar jet production with leptonic decays (l+l- and nn)
pplntt	$pp \rightarrow l\bar{l} n\bar{n}$	$pp \rightarrow V t\bar{t}+\text{jets}$	Off-shell W+/W- boson plus t t-bar production with leptonic decays
pplnttj	$pp \rightarrow l\bar{l} n\bar{n}j$	$pp \rightarrow V t\bar{t}+\text{jets}$	Off-shell W+/W- boson plus t t-bar jet production with leptonic decays
ppwtt	$pp \rightarrow W t\bar{t}$	$pp \rightarrow V t\bar{t}+\text{jets}$	W+/W- plus t t-bar production.
ppwttj	$pp \rightarrow W t\bar{t}j$	$pp \rightarrow V t\bar{t}+\text{jets}$	W+/W- plus t t-bar jet production.
ppztt	$pp \rightarrow Z t\bar{t}$	$pp \rightarrow V t\bar{t}+\text{jets}$	Z plus t t-bar production.
ppzttj	$pp \rightarrow Z t\bar{t}j$	$pp \rightarrow V t\bar{t}+\text{jets}$	Z plus t t-bar jet production.
ppllll	$pp \rightarrow l\bar{l} l\bar{l}$	$pp \rightarrow V V+\text{jets}$	Production of four leptons (all combinations of leptons and neutrinos).
pplll2	$gg \rightarrow l\bar{l} l\bar{l}$	$pp \rightarrow V V+\text{jets}$	Loop-induced production of four leptons (all combinations of leptons and neutrinos) in gluon fusion.
			Production of four leptons (all combinations of leptons and

- Install (for example for Z+1,2,3 production) :

```
./openloops libinstall ppzj ppzjj ppzjjj
```

Technical implementation of NLO EW

✓ Virtuals with **OpenLoops**:

- ▶ Fast numerical routines for all tree+loop vertices in the full SM
- ▶ $\mathcal{O}(\alpha)$ renormalization [Denner, '92] + R_2 rational terms
- ▶ Treatment of unstable particles: complex-mass-scheme / narrow-width approximations

✓ Real radiation, subtraction, subprocess bookkeeping

✓ **Sherpa** [Höche, Schönherr, in preparation]



✓ **MUNICH**: MUlti-chaNnel Integrator at swiss (CH) precision [Kallweit, in preparation]



- ▶ Based on the well established NLO **QCD** dipole subtraction frameworks with replacements for **QCD** \rightarrow **QED**

$$\alpha_s \longrightarrow \alpha, \quad C_F \longrightarrow Q_f^2, \quad T_R \longrightarrow N_{c,f} Q_f^2, \quad T_R N_f \longrightarrow \sum_f N_{c,f} Q_f^2, \quad C_A \longrightarrow 0$$

$$\frac{\mathbf{T}_{ij} \cdot \mathbf{T}_k}{\mathbf{T}_{ij}^2} \longrightarrow \begin{cases} \frac{Q_{ij} Q_k}{Q_{ij}^2} & \text{if the emitter } ij \text{ is a (anti)fermion} \\ \kappa_{ij,k} & \text{if the emitter } ij \text{ is a photon,} \end{cases}$$

- ▶ Mixed QCD-QED I-operator requires a non-trivial interplay between different Born orders

$$I \propto \sum \int_1 V_{\text{QED}} \otimes \text{diagram} + \int_1 V_{\text{QCD}} \otimes \text{diagram}$$

The diagrams show two types of Born-order processes. The first diagram (for QED) shows a fermion line with a self-energy loop (red wavy line) and a vertex correction (red wavy line). The second diagram (for QCD) shows a fermion line with a self-energy loop (red wavy line) and a vertex correction (blue wavy line labeled γ, Z).

Technical implementation of NLO EW

✓ Virtuals with **OpenLoops**:

- ▶ Fast numerical routines for all tree+loop vertices
- ▶ $\mathcal{O}(\alpha)$ renormalization [Denner, '97]
- ▶ Treatment of unstable particles

✓ Real radiation

All ingredients carefully validated:
 ✓ OpenLoops vs. private code by S. Pozzorini
 ✓ MUNICH vs. Sherpa



... (CH) precision

... QCD dipole subtraction frameworks with replacements for

$$T_F \longrightarrow Q_f^2, \quad T_R \longrightarrow N_{c,f} Q_f^2, \quad T_R N_f \longrightarrow \sum_f N_{c,f} Q_f^2, \quad C_A \longrightarrow 0$$

$$\frac{-ij \cdot \mathbf{T}_k}{\mathbf{T}_{ij}^2} \longrightarrow \begin{cases} \frac{Q_{ij} Q_k}{Q_{ij}^2} & \text{if the emitter } ij \text{ is a (anti)fermion} \\ \kappa_{ij,k} & \text{if the emitter } ij \text{ is a photon,} \end{cases}$$

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The diagrams show a loop structure with a red wavy line (photon) and a blue wavy line (gluon or photon/Z boson).

Combination of NLO QCD and EW & Setup

Two alternatives:

$$\sigma_{\text{QCD}+\text{EW}}^{\text{NLO}} = \sigma^{\text{LO}} + \delta\sigma_{\text{QCD}}^{\text{NLO}} + \delta\sigma_{\text{EW}}^{\text{NLO}}$$

$$\sigma_{\text{QCD}\times\text{EW}}^{\text{NLO}} = \sigma_{\text{QCD}}^{\text{NLO}} \left(1 + \frac{\delta\sigma_{\text{EW}}^{\text{NLO}}}{\sigma^{\text{LO}}} \right) = \sigma_{\text{EW}}^{\text{NLO}} \left(1 + \frac{\delta\sigma_{\text{QCD}}^{\text{NLO}}}{\sigma^{\text{LO}}} \right)$$

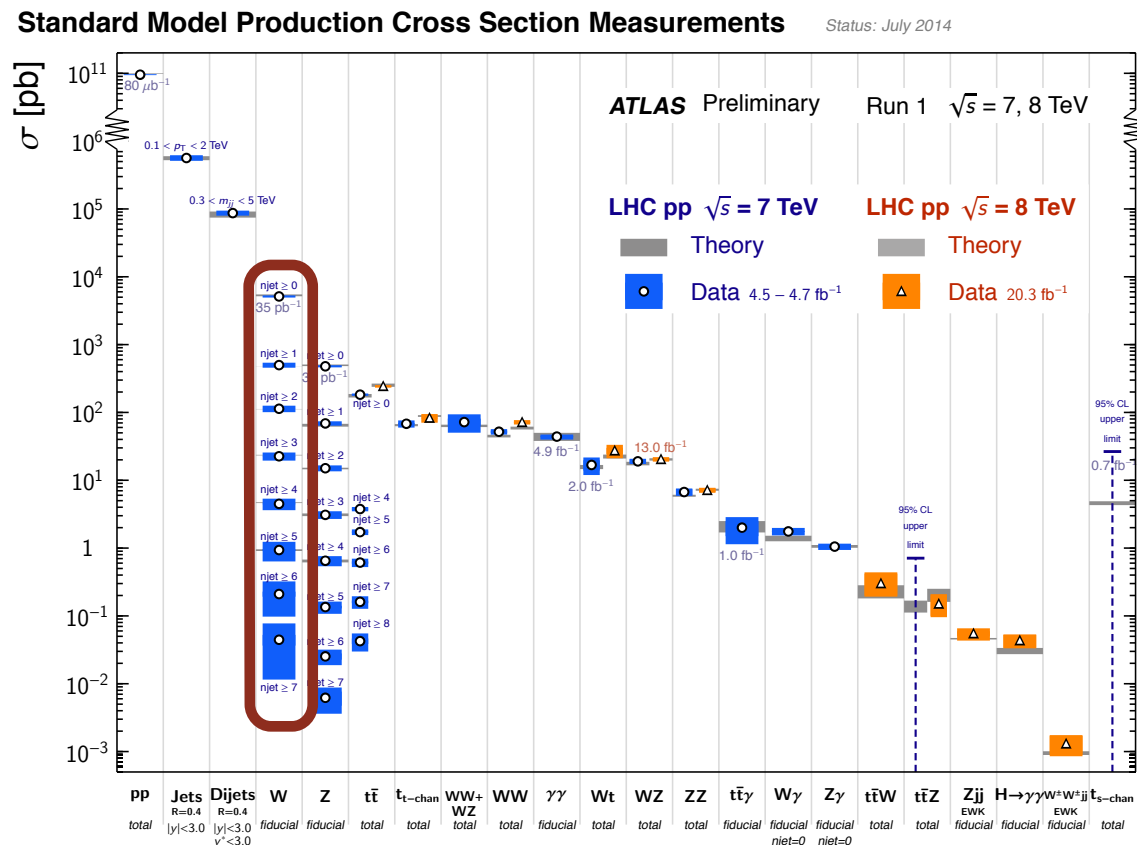
Difference between the two approaches indicates uncertainties due to missing two-loop EW-QCD corrections of $\mathcal{O}(\alpha\alpha_s)$

Relative corrections w.r.t. NLO QCD:

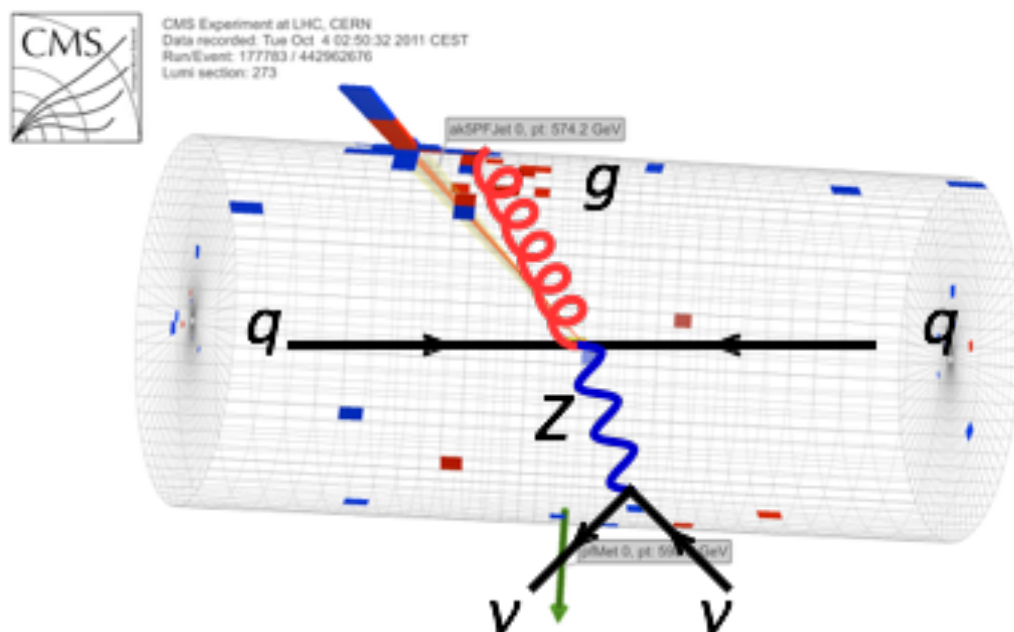
$$\frac{\sigma_{\text{QCD}+\text{EW}}^{\text{NLO}}}{\sigma_{\text{QCD}}^{\text{NLO}}} = \left(1 + \frac{\delta\sigma_{\text{EW}}^{\text{NLO}}}{\sigma_{\text{QCD}}^{\text{NLO}}} \right) \quad \text{suppressed by large NLO QCD corrections}$$
$$\frac{\sigma_{\text{QCD}\times\text{EW}}^{\text{NLO}}}{\sigma_{\text{QCD}}^{\text{NLO}}} = \left(1 + \frac{\delta\sigma_{\text{EW}}^{\text{NLO}}}{\sigma^{\text{LO}}} \right) \quad \text{“usual” NLO EW w.r.t. LO}$$

-
- ▶ $\alpha = \frac{\sqrt{2}}{\pi} G_\mu M_W^2 \left(1 - \frac{M_W^2}{M_Z^2} \right)$ in **G_μ-scheme** with $G_\mu = 1.16637 \times 10^{-5} \text{ GeV}^{-2}$
 - ▶ or: $\alpha(0) = 1/137.036$ in **on-shell-scheme**
 - ▶ PDFs: **NNPDF 2.3QED** with $\alpha_s(M_Z) = 0.118$ for LO and NLO QCD/EW

Motivation: $V + \text{multijet}$ production



- Large cross-sections and clean leptonic signatures
- Precision QCD at LHC
- Playground to probe different aspects of higher-order calculations (LO+PS, NLO+PS, NLO-Merging, NLO EW,...)



- Important/dominant background for various **BSM searches** (lepton + jets + missing E_T)
- Dominant background for monojet **DM searches**
- Dominant background for **top physics**
- Important background for **Higgs physics**, e.g. $VH(\rightarrow b\bar{b})$

$W^+ + 1 \text{ jet: inclusive}$

Setup:

$$\sqrt{S} = 13 \text{ TeV}$$

$$p_{T,j} > 30 \text{ GeV}, \quad |\eta_j| < 4.5$$

$$\mu_0 = \hat{H}_T/2 \text{ (+ 7-pt. variation)}$$

inclusive

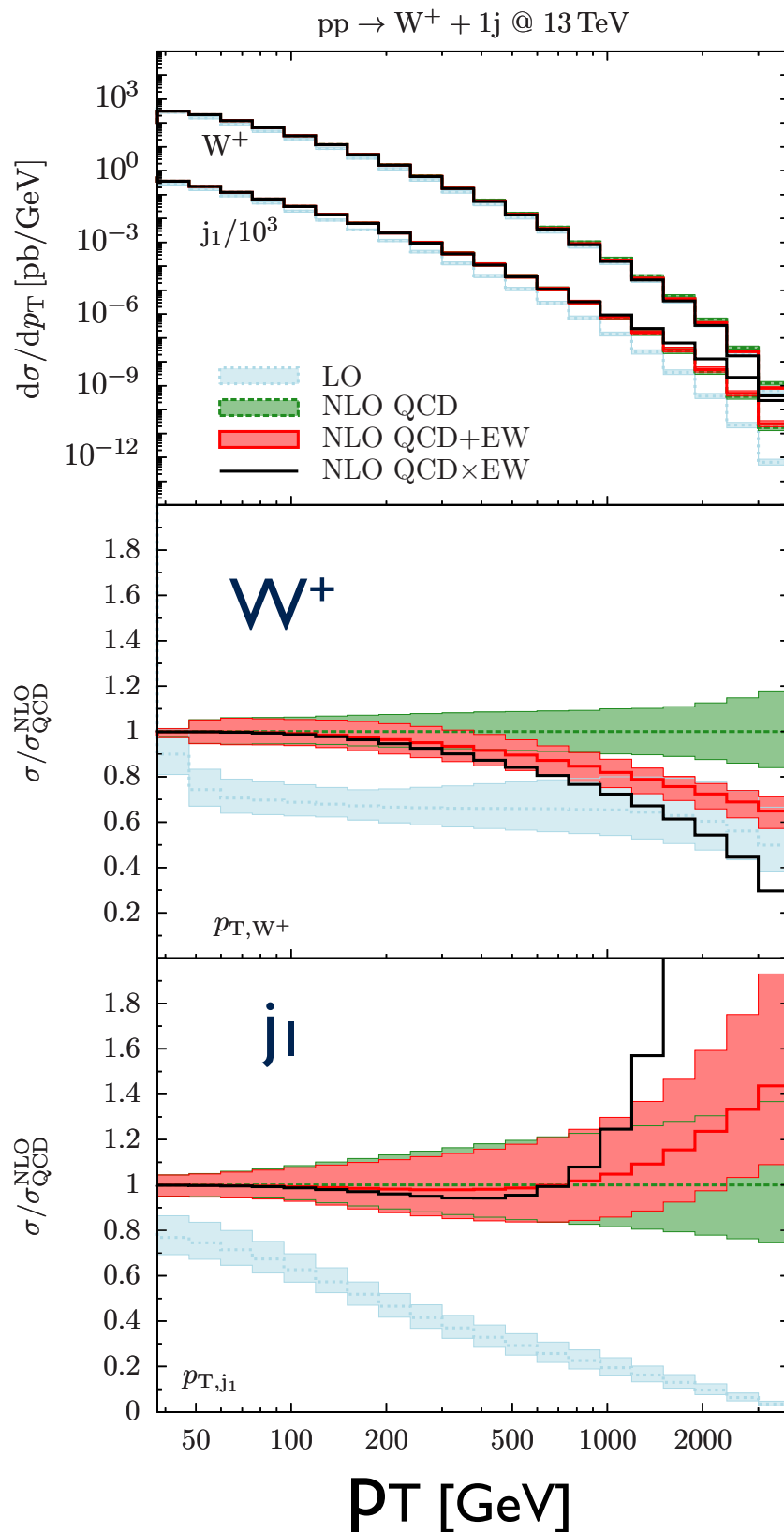
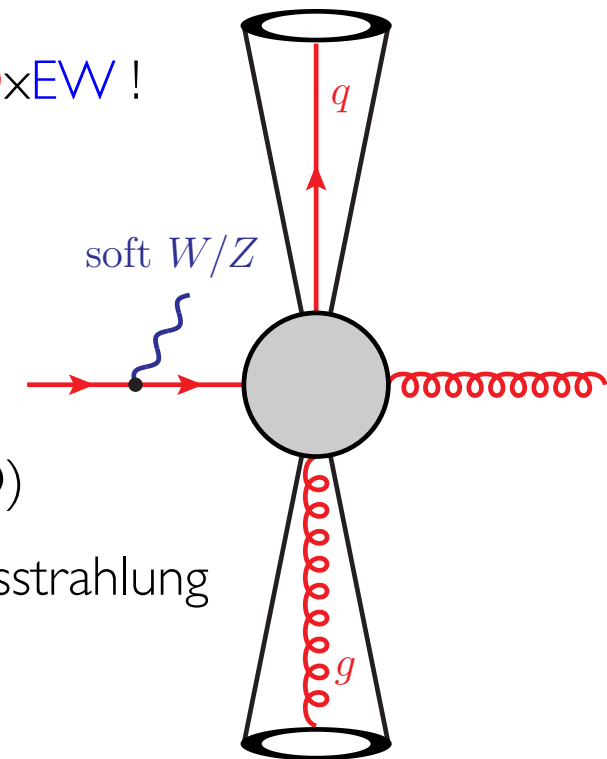
$\approx 1\%$ EW corrections

p_T of W-boson

- ▶ +100 % **QCD** corrections in the tail
- ▶ large negative **EW** corrections due to **Sudakov behaviour**: -20–35% corrections at 1-4 TeV
- ▶ sizeable difference between **QCD+EW** and **QCDxEW** !

p_T of jet

- ▶ factor-10 NLO **QCD** corrections in the tail!
- ▶ dominated by **dijet configurations** (effectively LO)
- ▶ positive 10-50% EW corrections from quark bremsstrahlung



NNLO **QCD**: [Boughezal, Focke, Liu, Petriello '15]

$W^+ + 1 \text{ jet: inclusive}$

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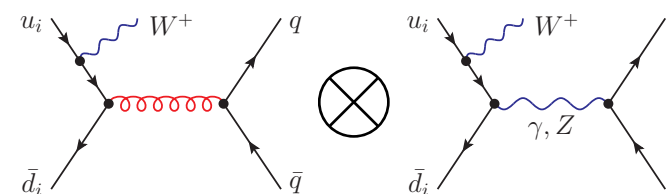
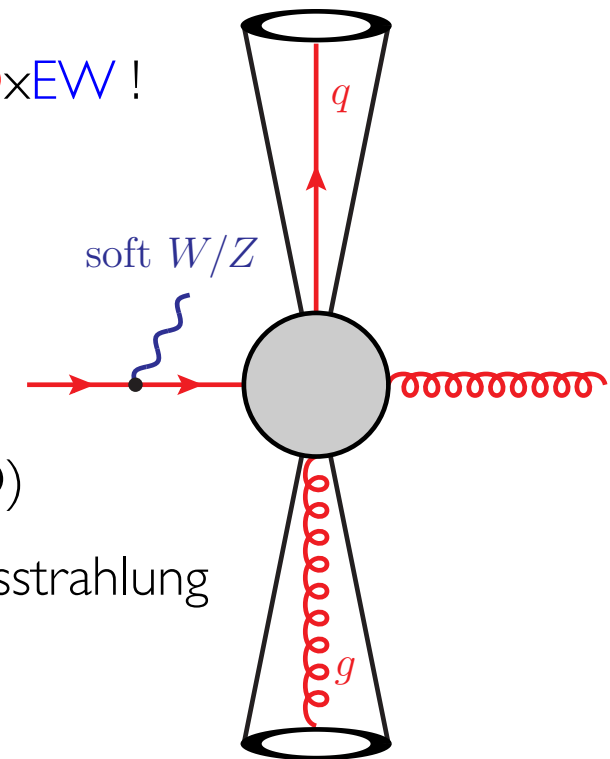
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\Rightarrow pathologic with large uncertainties!

$W^+ + 1 \text{ jet: exclusive}$

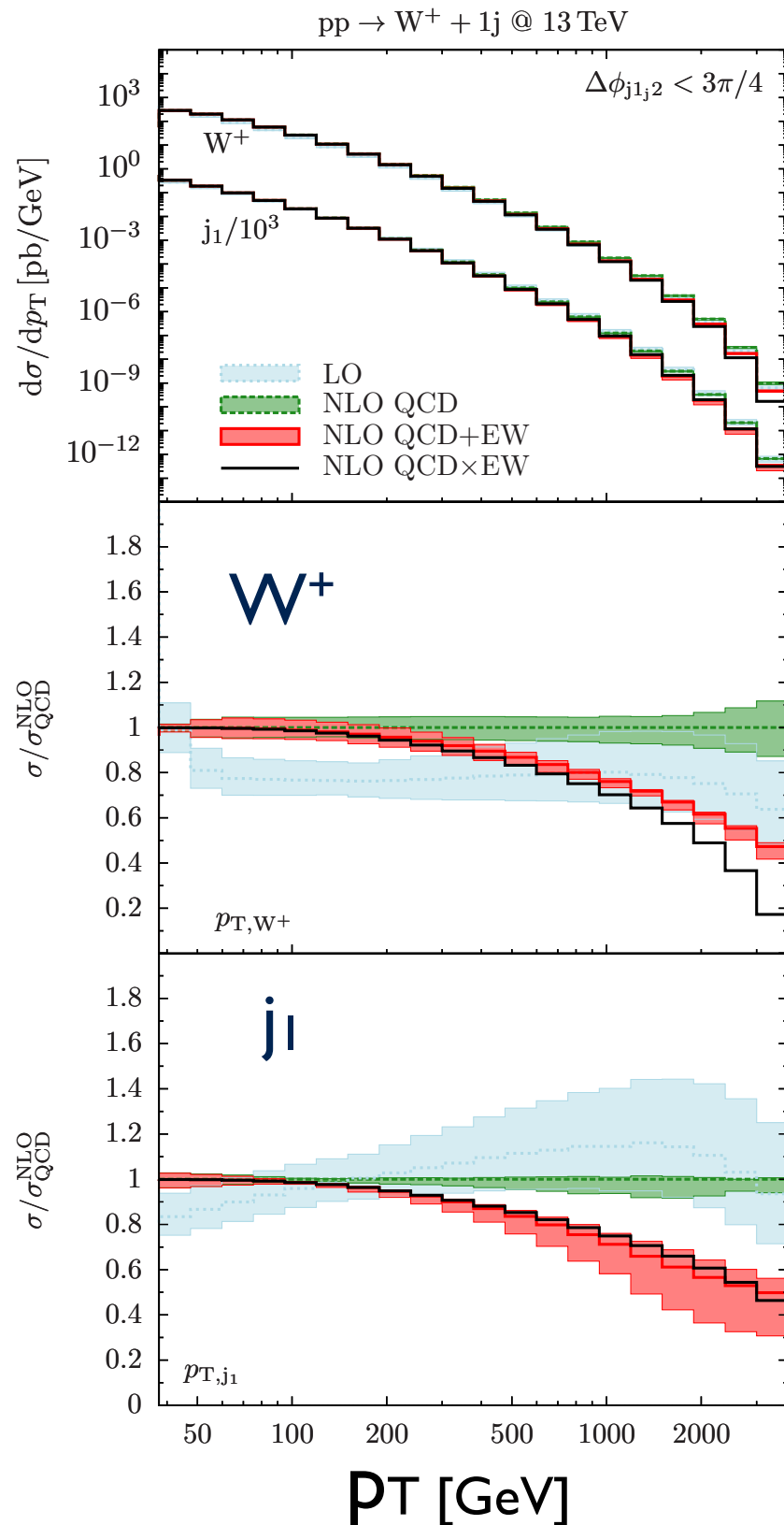
$\Delta\phi_{j1j2} < 3\pi/4$
(veto on dijet configurations)

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$$\sqrt{S} = 13 \text{ TeV}$$

$$p_{T,j} > 30 \text{ GeV}, \quad |\eta_j| < 4.5$$

$$\mu_0 = \hat{H}_T/2 \text{ (+ 7-pt. variation)}$$



QCD corrections

- ▶ mostly moderate and stable QCD corrections

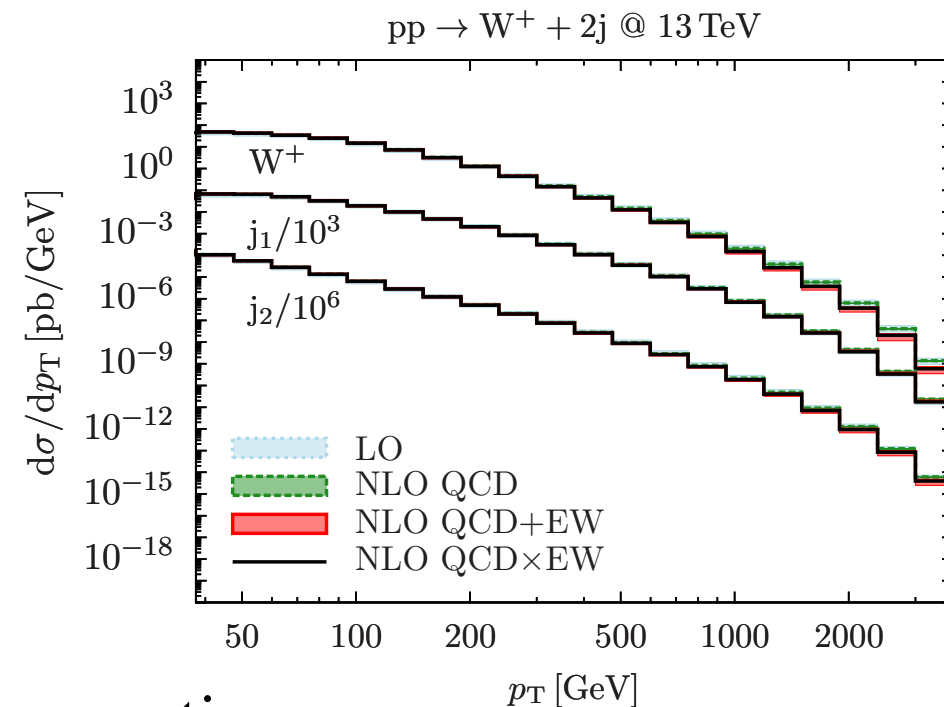
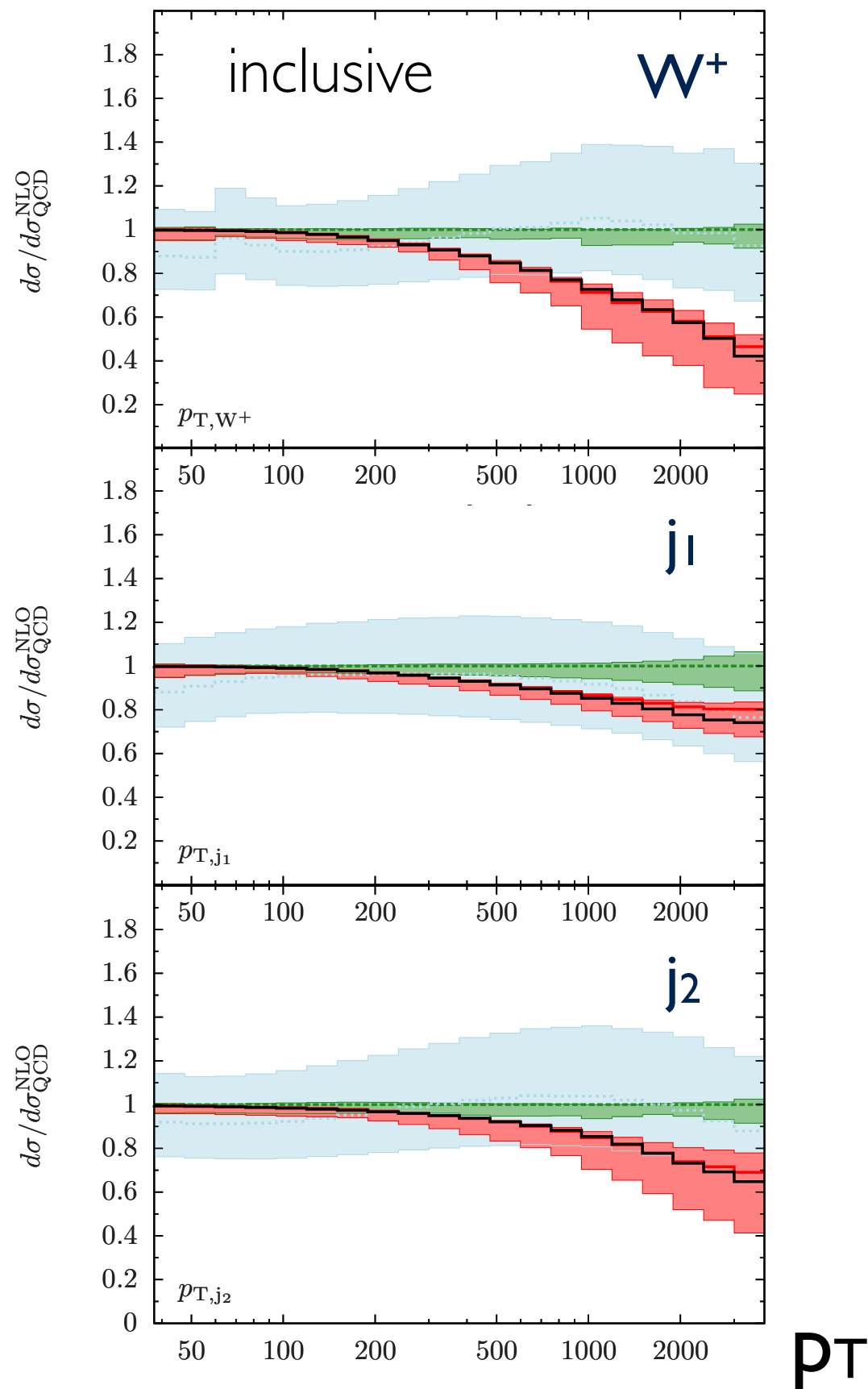
EW corrections

- ▶ **Sudakov behaviour** in both tails:
-20–50% EW corrections at 1–4 TeV
- ▶ EW corrections larger than QCD uncertainties for $p_{T,W^+} > 300 \text{ GeV}$

\Rightarrow exclusive $W^+ 1\text{jet}$ ok!

\Rightarrow inclusive $W^+ 1\text{jet}$ requires $W^+ 2 \text{ jets}$ at NLO QCD+EW!

$W^+ + 2 \text{ jets: NLO EW}$



QCD corrections

- ▶ small and very stable
- ▶ $\approx 10\%$ scale uncertainties

EW corrections

- ▶ **Sudakov behaviour** in all p_T tails:

- -30–60% for W-boson at 1–4 TeV
- -15–25% for 1st and 2nd jet at 1–4 TeV

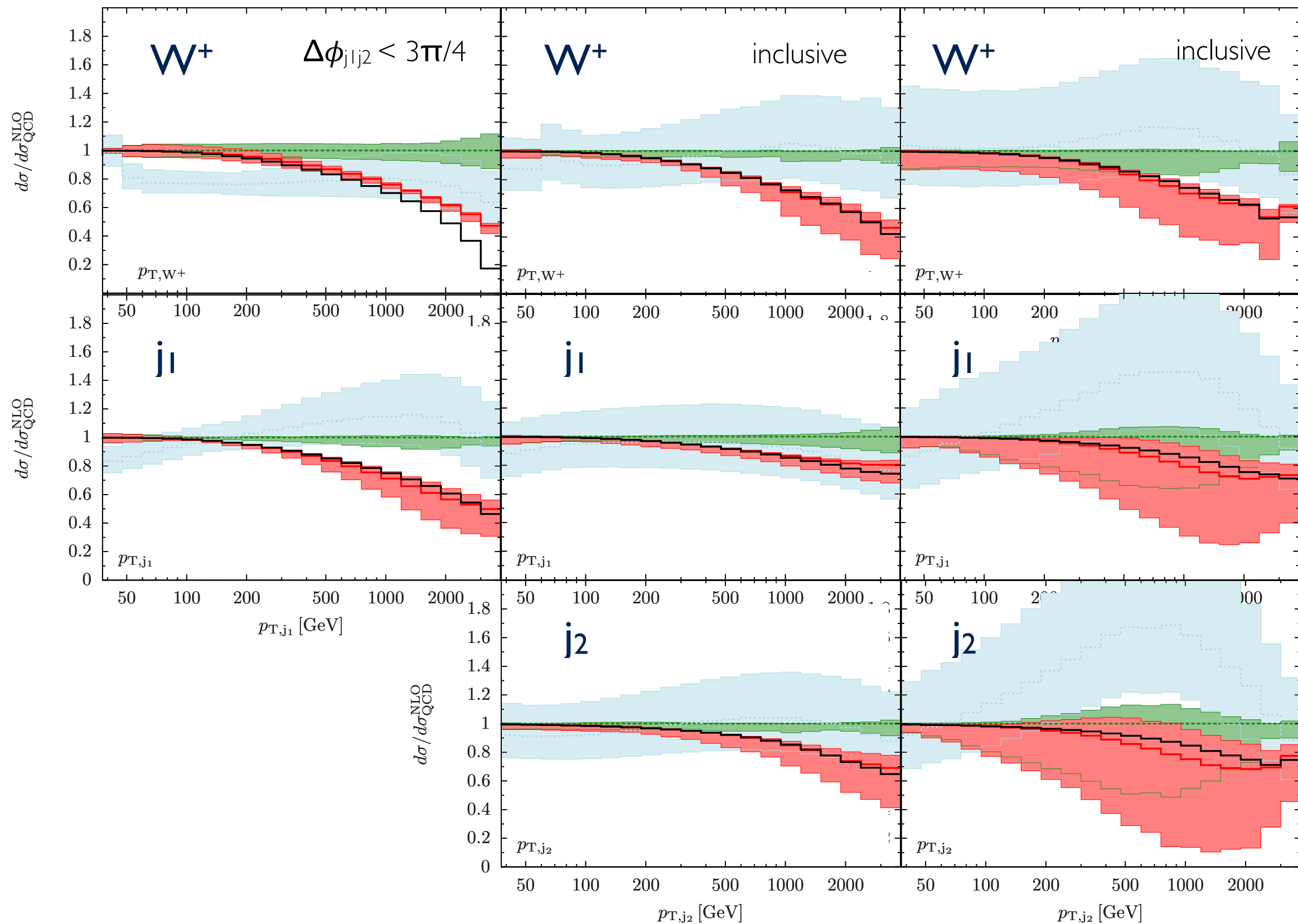
different!

- ▶ Might need resummation of leading EW Sudakov logs

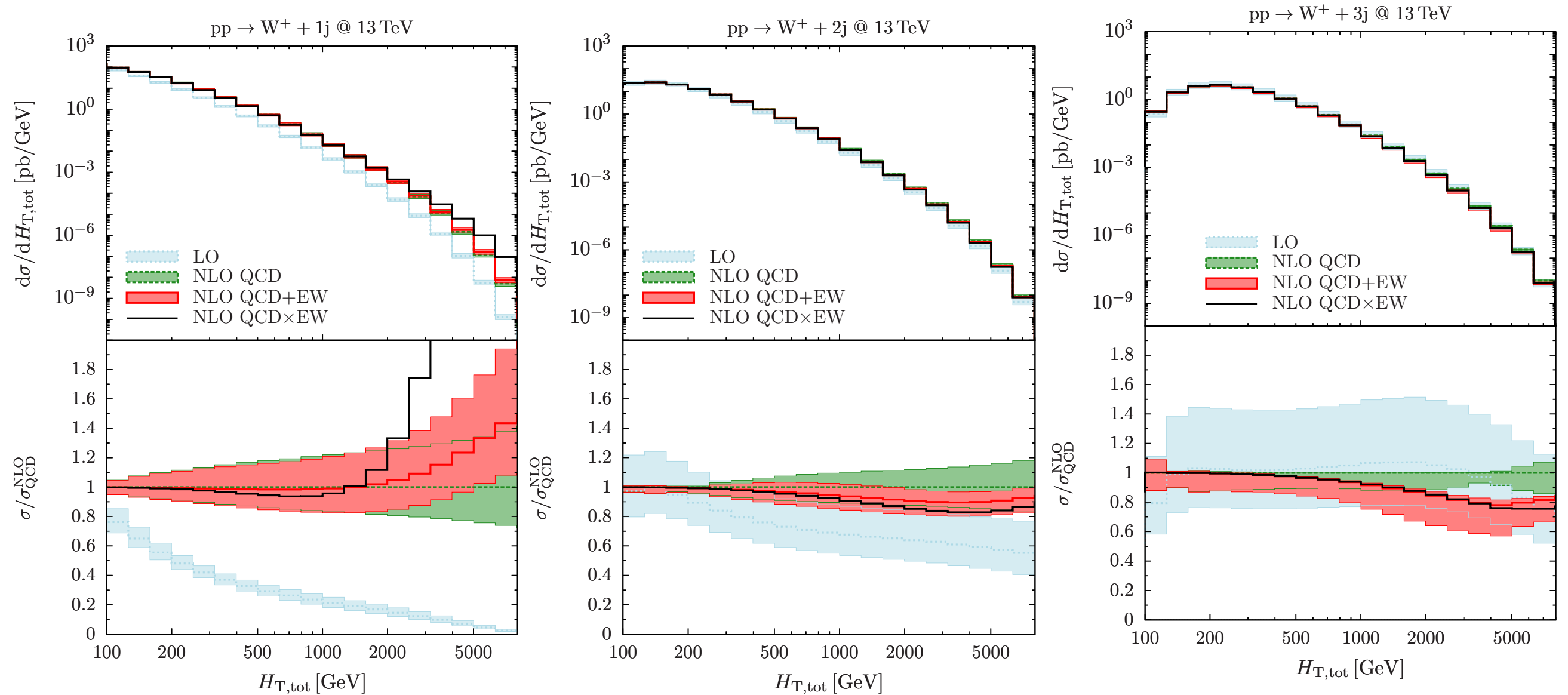
$W^+ + 1 \text{ jets}$

$W^+ + 2 \text{ jets}$

$W^+ + 3 \text{ jets}$



$H_{T,\text{tot}}$ for $W^+ + 1, 2, 3$ jets



QCD corrections

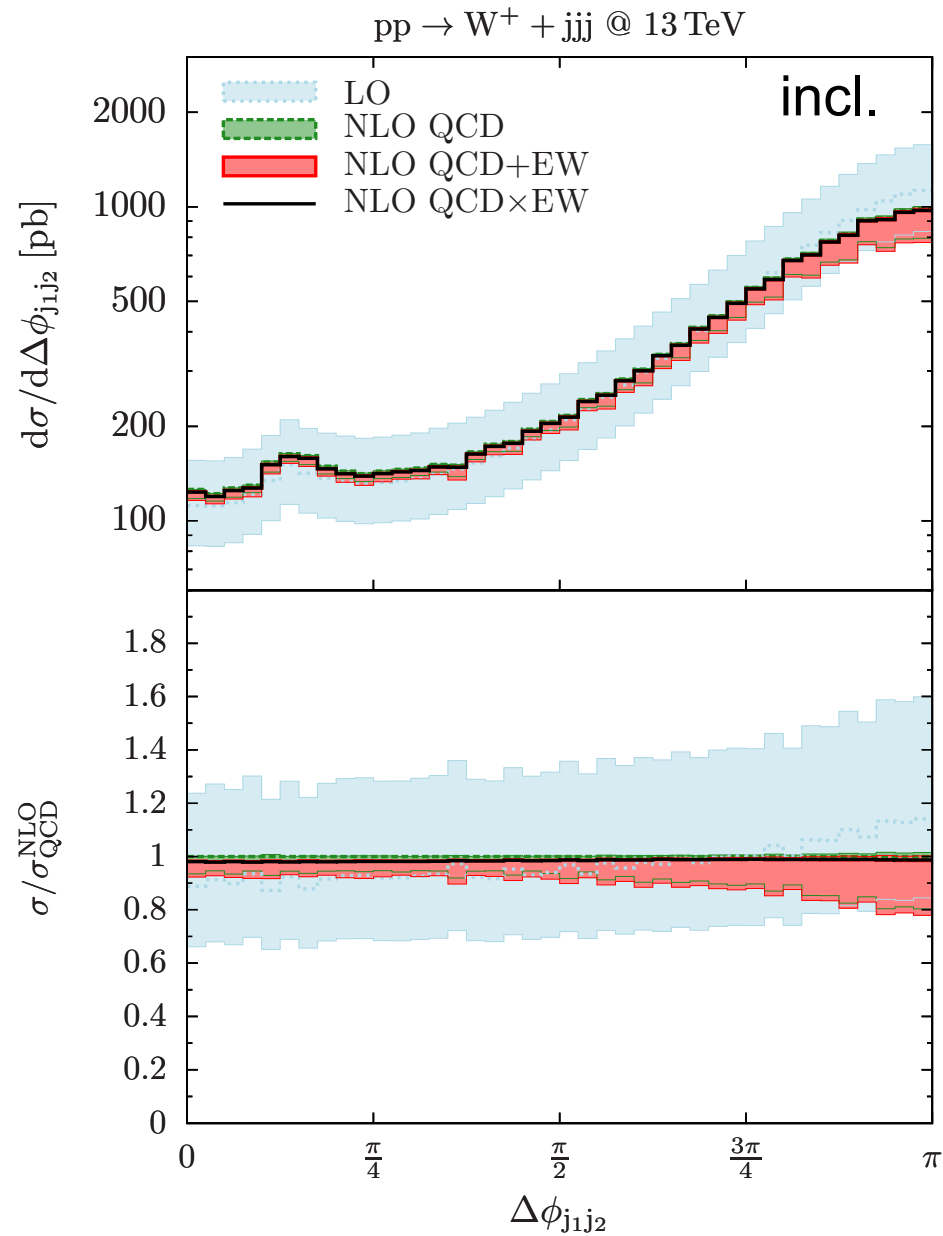
- ▶ for $W+2j$: large QCD corrections (80-100%)
- ▶ starting to be stable only for $W+3$ jets

EW corrections

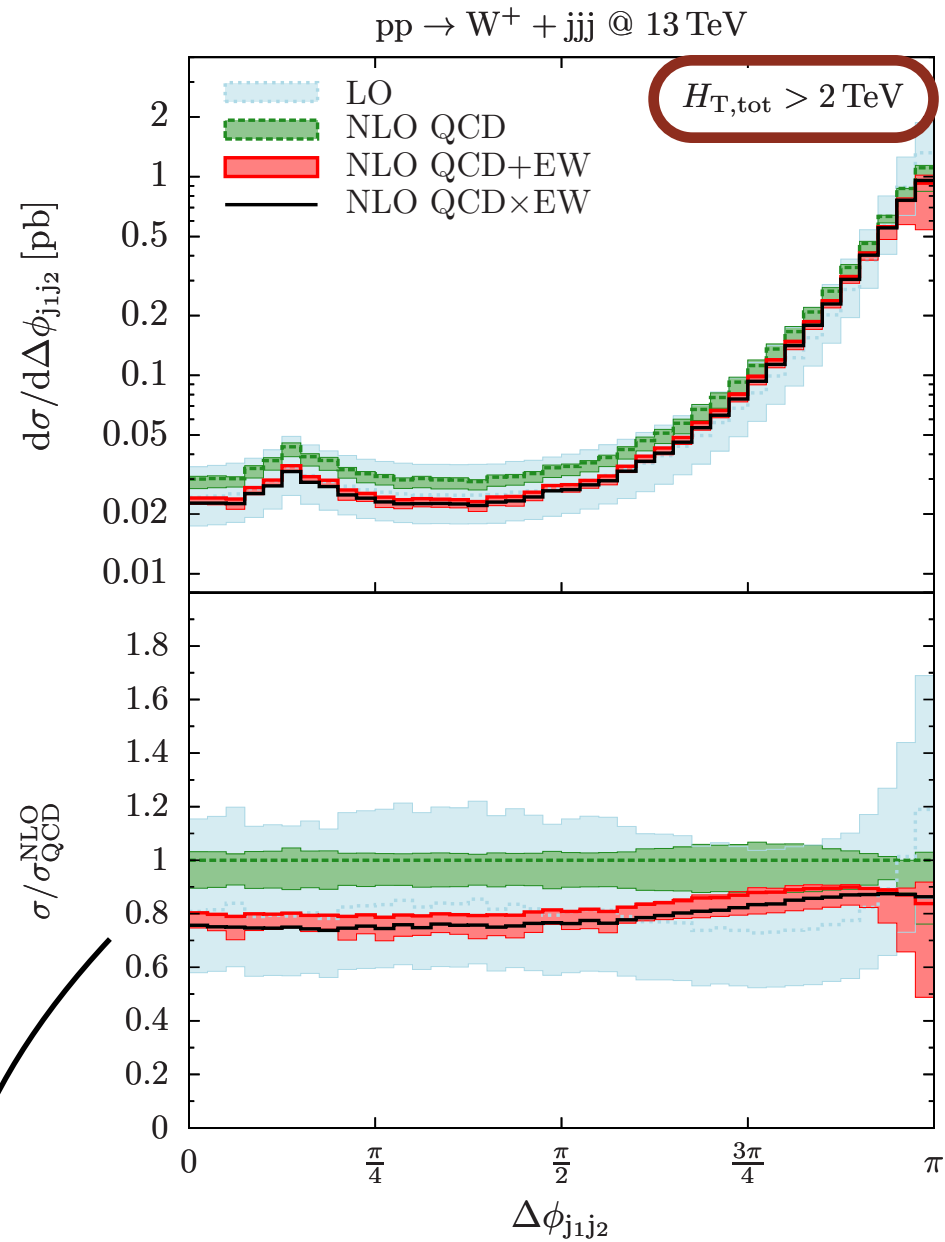
- ▶ moderate EW corrections: -20-30 % in the tail

\Rightarrow calls for NLO QCD+EW multi-jet merging!

$W^+ + 3 \text{ jets}$: topology of EW corrections

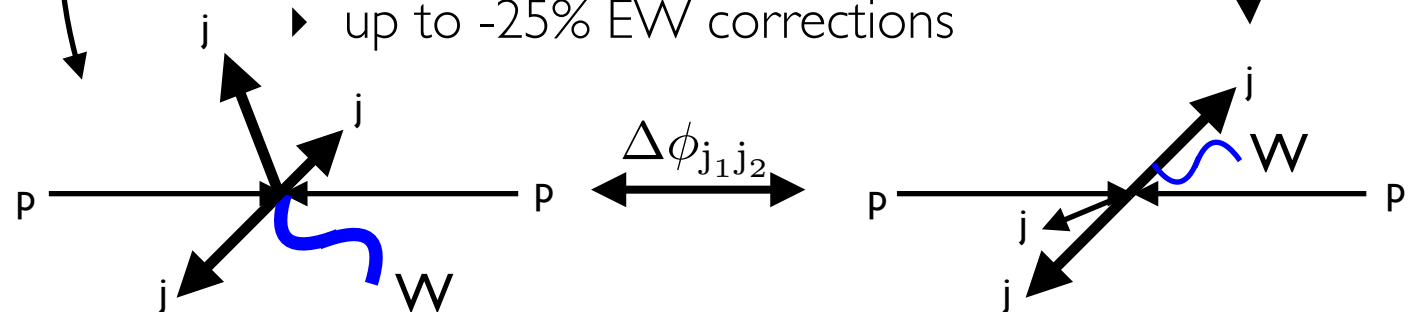


► negligible EW corrections

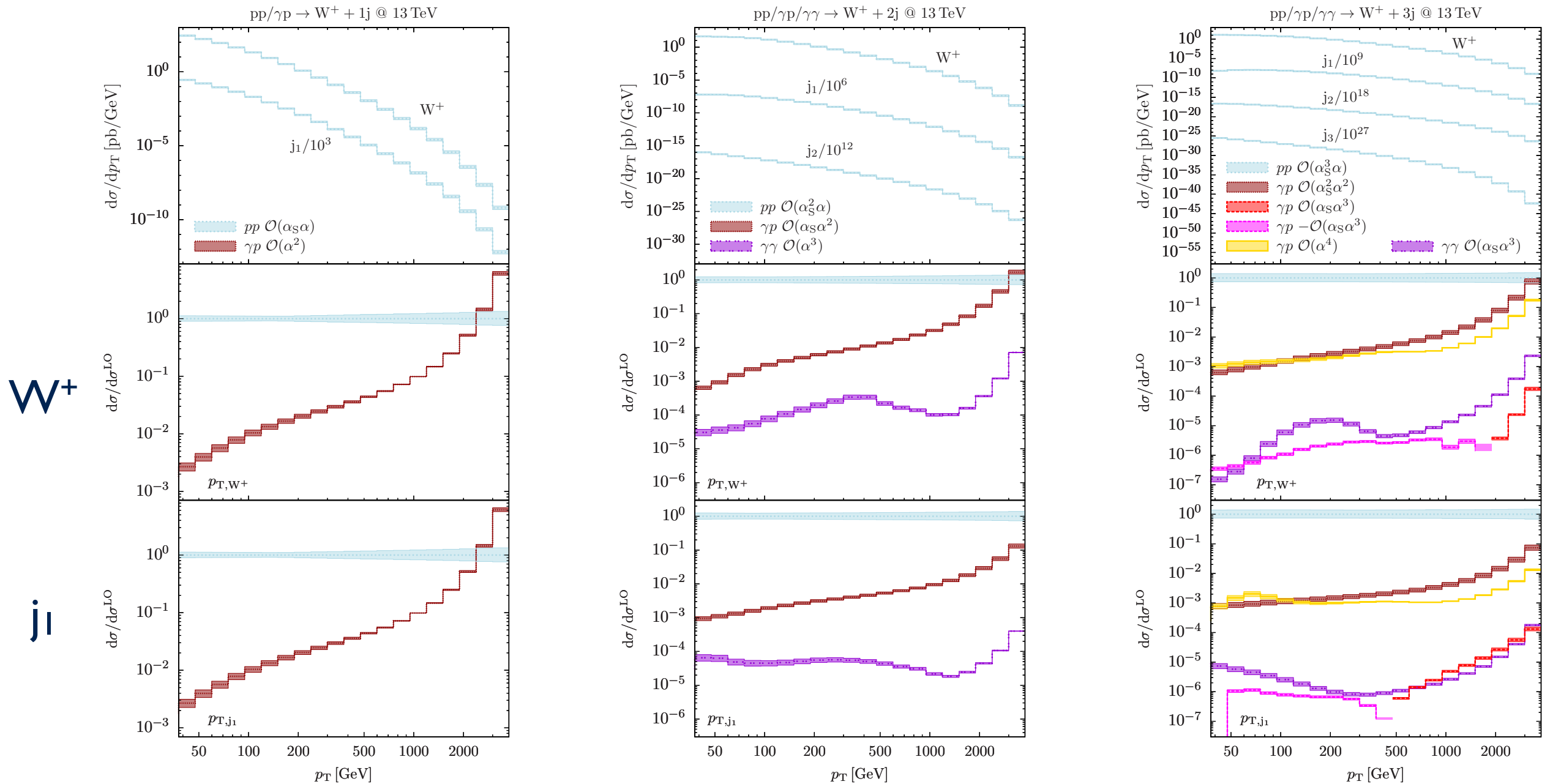


► stable QCD corrections

► up to -25% EW corrections

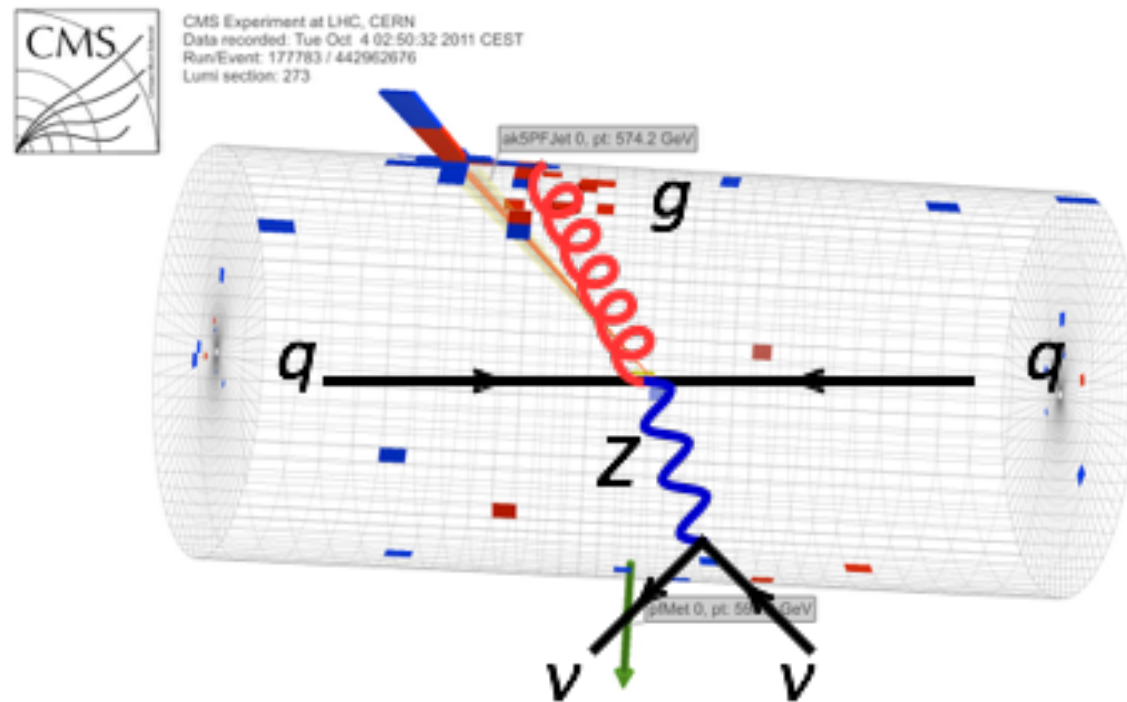


W + 1,2,3 jets @ sub-LO: γ -induced



- ▶ As large as 5 - 100% at $p_{T,W^+} = 1-4$ TeV
- ▶ However: giant γ -PDF uncertainties at large x !

Motivation: $V + \text{multijet}$ production



- ▶ $Z(\rightarrow \nu\bar{\nu}) + \text{jets}$ irreducible background for monojet/multijet **Dark Matter searches**
- ▶ can be determined from $\gamma + \text{jets}$ and/or $W + \text{jets}$ measurements together with *theoretical predictions* for $Z + \text{jets}/\gamma + \text{jets}$ and $Z + \text{jets}/W + \text{jets}$ ratios

Z/ γ + 1 jet: exclusive

Setup:

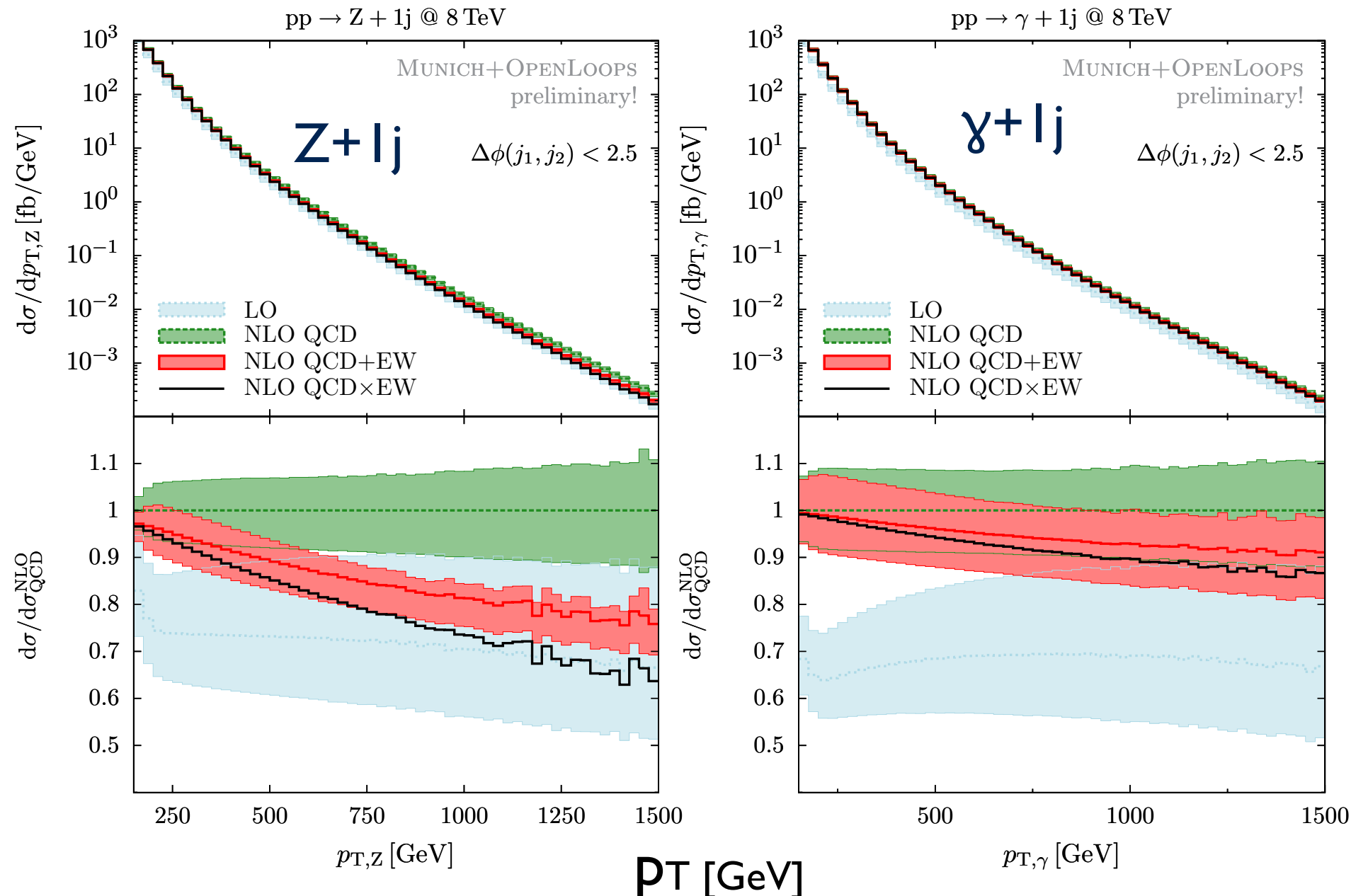
$$\sqrt{S} = 8 \text{ TeV}$$

$$p_{T,j} > 110 \text{ GeV}, \quad |\eta_j| < 2.4$$

$$\mu_0 = \hat{H}_T/2 \text{ (+ 7-pt. variation)}$$

$$\Delta\phi_{j1j2} < 2.5$$

Frixione-Isolation with $dR=0.3$



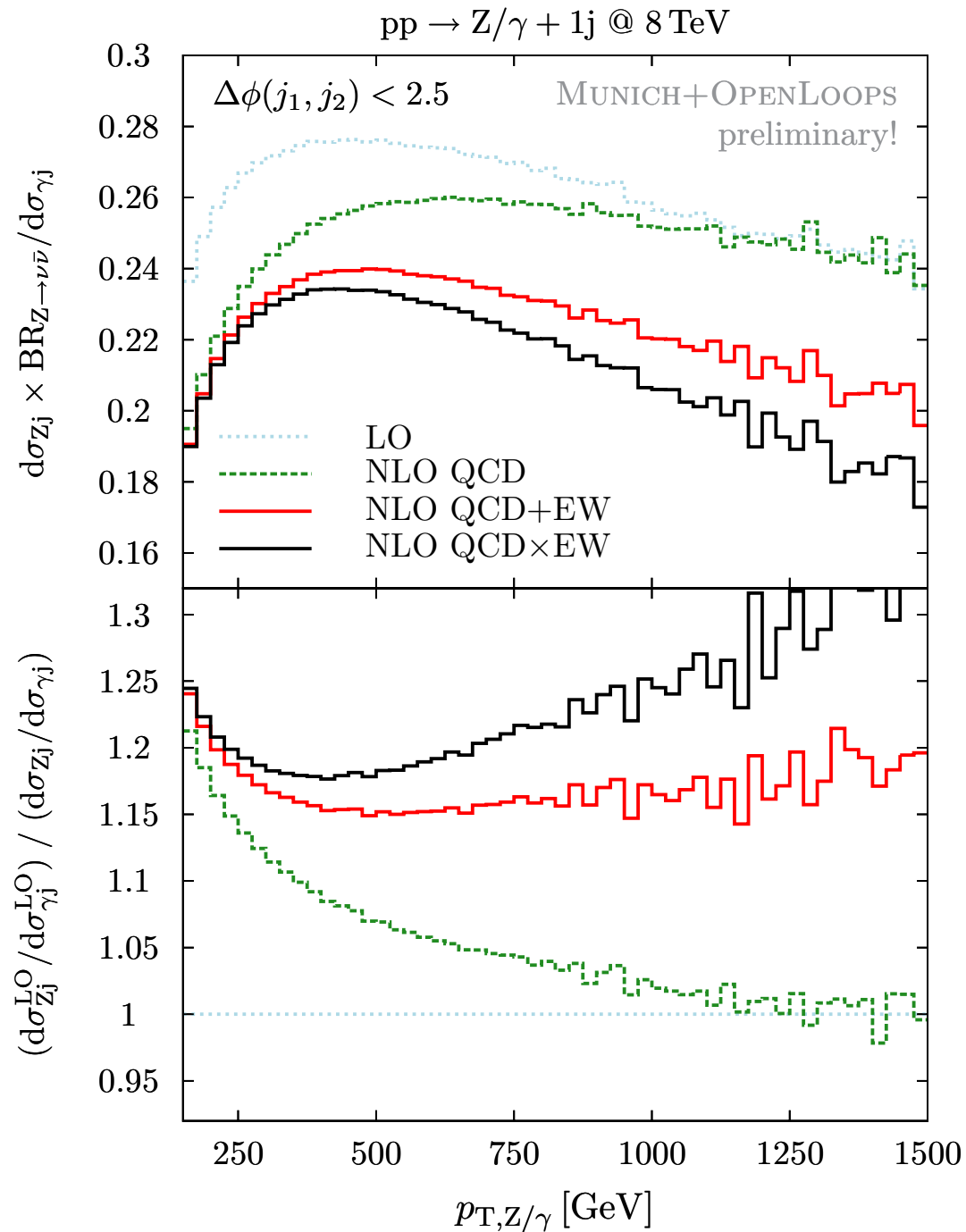
QCD corrections

- ▶ mostly moderate and stable QCD corrections
- ▶ (almost) identical QCD corrections in the tail, sizeable differences for small p_T

EW corrections

- ▶ correction in $p_T(Z) >$ correction in $p_T(\gamma)$
- ▶ **-20/-8% EW for Z/ γ at 1 TeV**
- ▶ EW corrections $>$ QCD uncertainties for $p_{T,Z} > 350 \text{ GeV}$

$Z/\gamma + 1 \text{ jet: } p_T\text{-ratio}$



Overall

- mild dependence on the boson p_T

QCD corrections

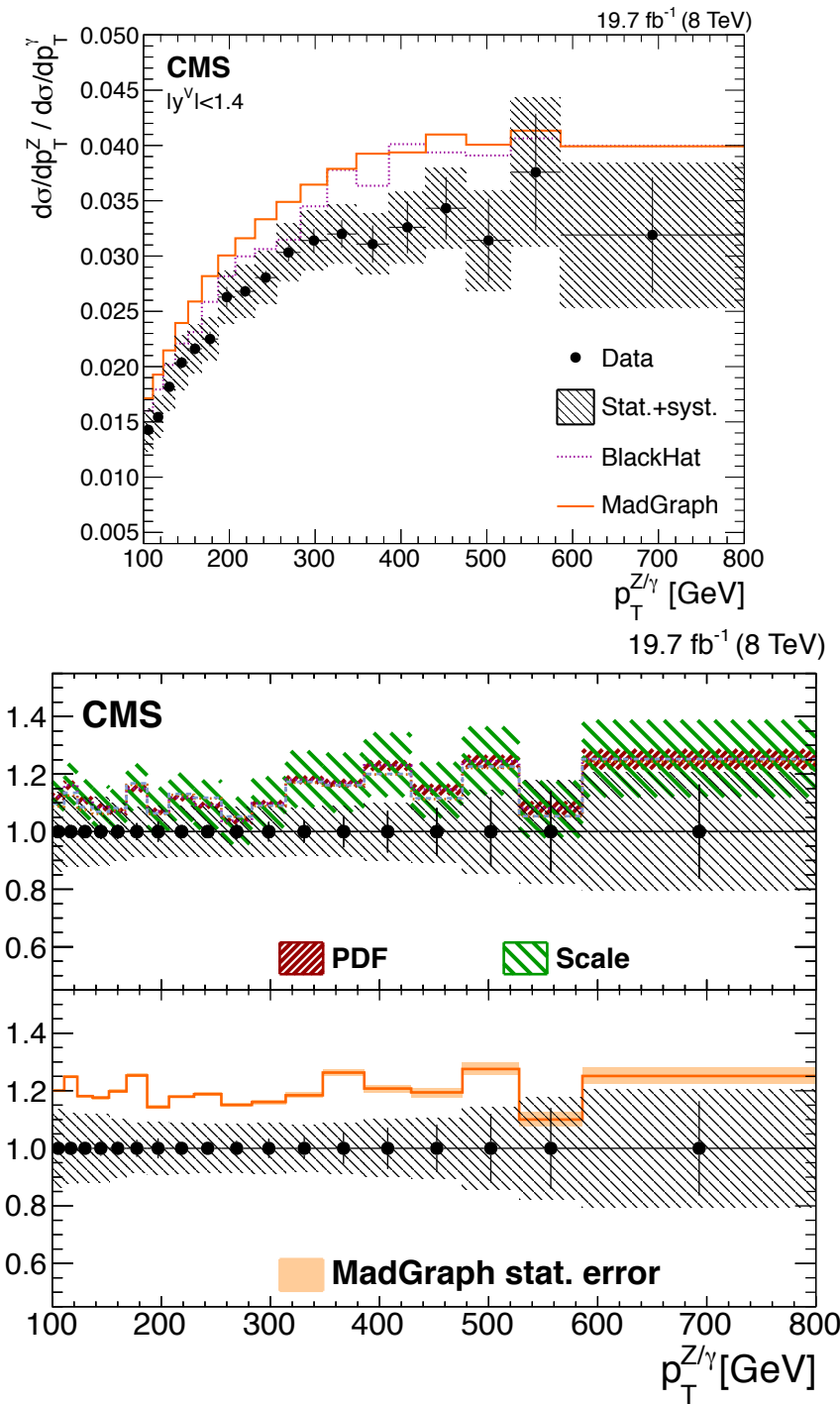
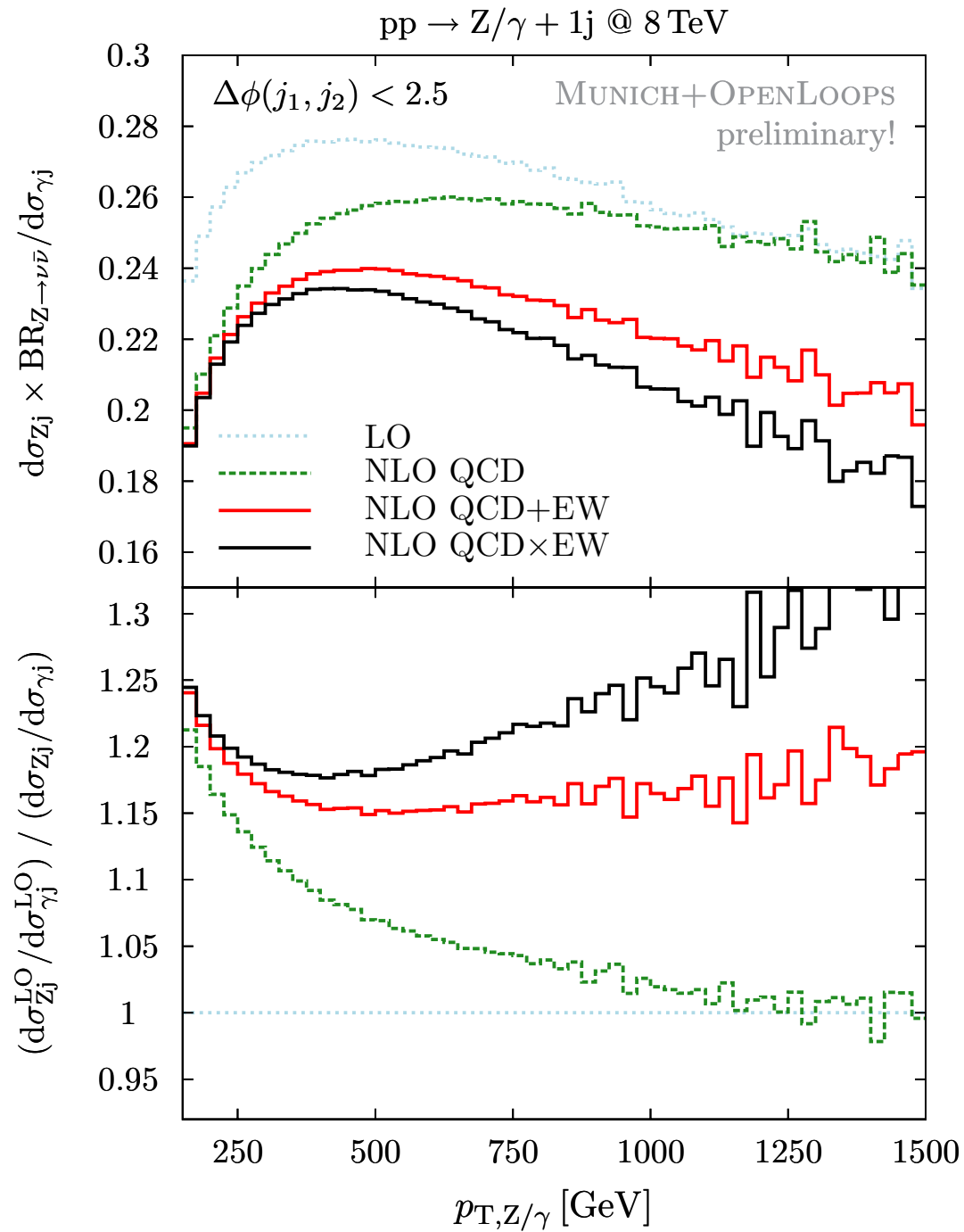
- $\approx 10\%$ above 300 GeV

EW corrections

- result in an almost constant shift between LO and NLO **QCD+EW** of $\sim 15\%$
- sizeable difference between **QCD+EW** & **QCD \times EW**

Z/ γ + 1 jet: pT-ratio

[CERN-PH-EP-2015-089]



Note: fiducial regions not identical!

Conclusions

► V + multijets at QCD+EW:

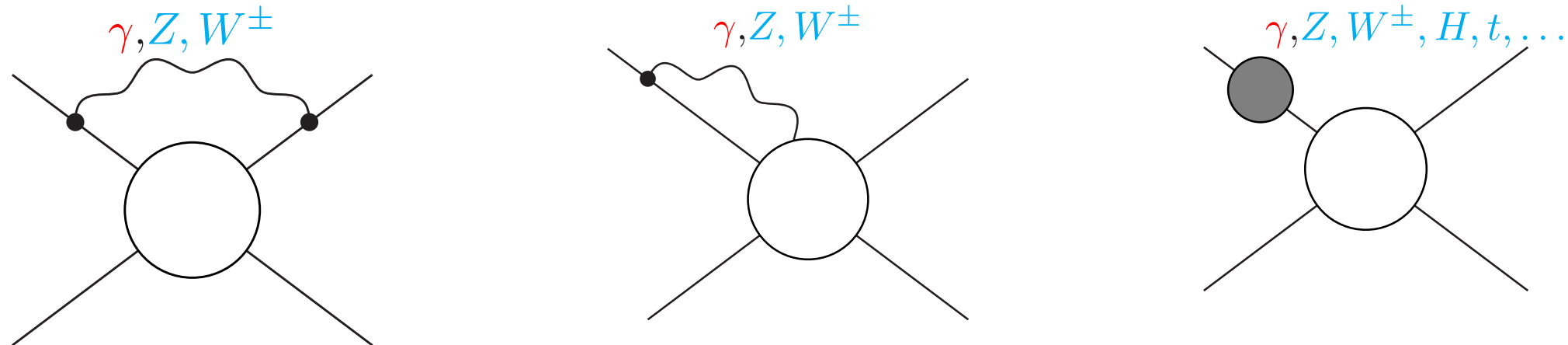
- 2 → 4 NLO EW feasible!
- inclusion of EW corrections *crucial* at the TeV scale (up to 50%)
- non-trivial interplay between QCD and EW
- multi-jet final states genuinely different from V+1jet
- Z+jets / γ +jets ratio sensitive to EW corrections *below* TeV scale

► Outlook:

- **decays** of V's (ll+jets, ln+jets)
- PS matching & **multi-jet merging**
- NLO corrections in the full SM (QCD & EW) publicly available in OpenLoops+Sherpa

Origin of electroweak Sudakov logarithms

Originate from soft/collinear virtual EW bosons coupling to on-shell legs



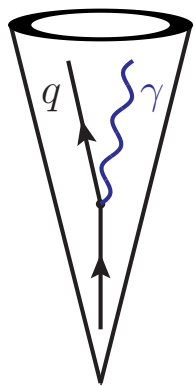
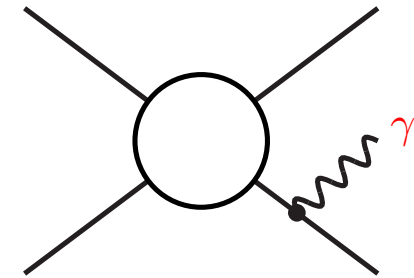
Universality and factorisation similar as in QCD [Denner, Pozzorini; '01]

$$\delta_{\text{LL+NLL}}^{1\text{-loop}} = \frac{\alpha}{4\pi} \sum_{k=1}^n \left\{ \frac{1}{2} \sum_{l \neq k} \sum_{a=\gamma, Z, W^\pm} I^a(k) I^{\bar{a}}(l) \ln^2 \frac{s_{kl}}{M^2} + \gamma^{\text{ew}}(k) \ln \frac{s}{M^2} \right\}$$

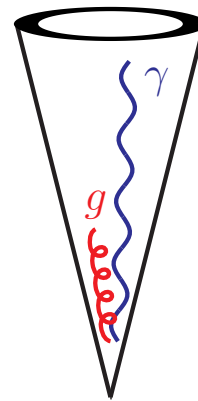
- process-independent and simple structure
- tedious implementation (ALPGEN [Chiesa et al. '13]) due to nontrivial $SU(2) \times U(1)$ features (P-violation, mixing, soft $SU(2)$ correlations, Goldstone modes, ...)
- 2-loop extension and resummation partially available

Treatment of Photons

- ▶ QED IR subtraction [Catani,Dittmaier,Seymour,Trocsanyi; Frixione, Kunszt, Signer]
- ▶ Problem of IR safeness in presence of FS QCD partons and photons:
 - ▶ Democratic jet-algorithm approach (jets \equiv photons)



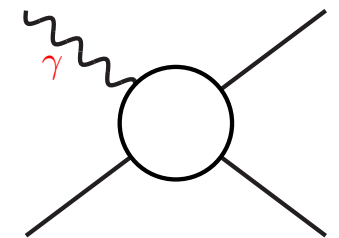
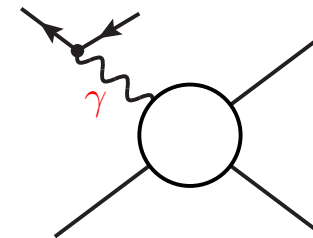
collinear $q \rightarrow q\gamma$ singularities
cancelled clustering q, g, γ on
same footing



soft gluon singularities \leftrightarrow hard photons
inside jets: cancelled in jet-production
(NLO **EW**) + γ -production (NLO **QCD**)

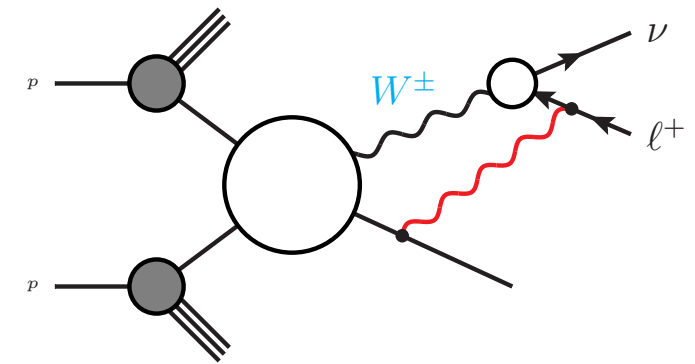
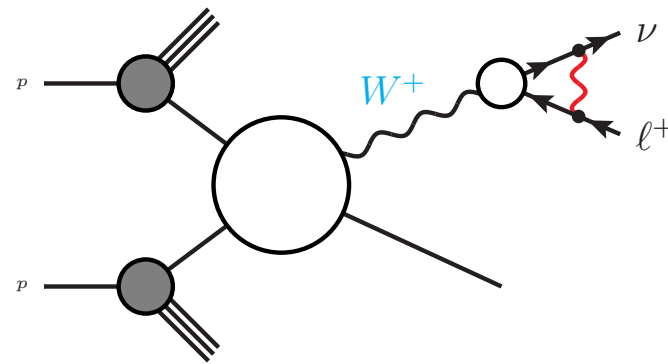
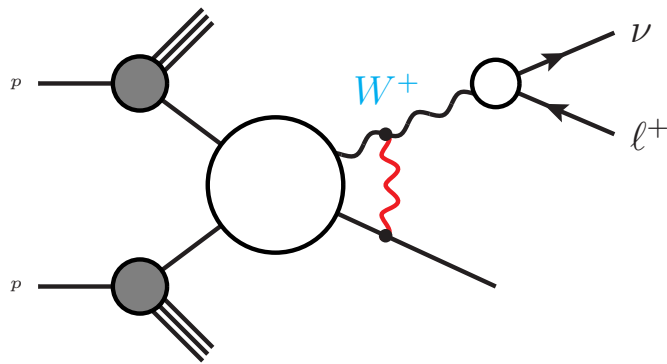
- ▶ Separation of jets from photons through $E_\gamma/E_{\text{jet}} < z_{\text{thr}}$ inside jets
 - *rigorous approach:* absorb $q \rightarrow q\gamma$ singularity into fragmentation function
 - *approximation:* cancel singularity via $q\gamma$ recombination in small cone $\Delta R_{q\gamma} < 0.1$
difference < 1% for typical z_{thr} !

- ▶ QED factorisation for IS photons and PDF evolution [MRST2004, NNPDF2.3]
- ▶ γ -induced processes \rightarrow possible TeV scale enhancements
(However large uncertainties!)



Decays of heavy particles

- ▶ Leptonic decays of gauge bosons are trivial at NLO QCD. At NLO EW corrections in production, decay and non-factorizable contributions have to be considered.

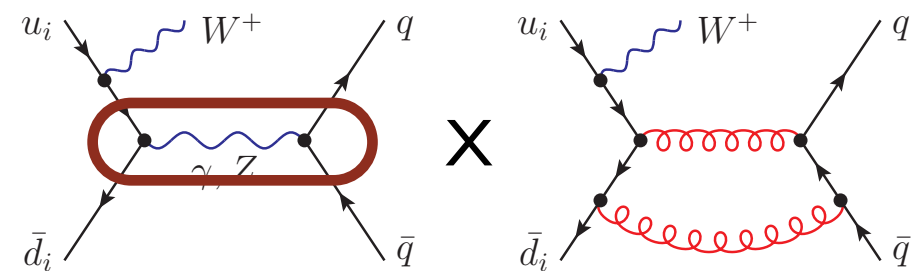
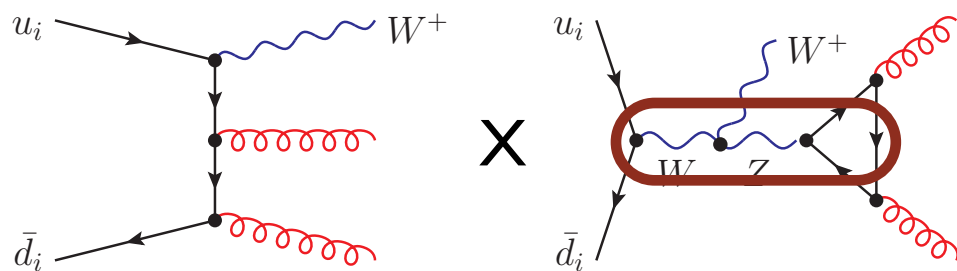


- ▶ Scheme of choice: **complex-mass-scheme** [Denner, Dittmaier]
 - gauge invariant and exact NLO
 - **computationally very expensive**: one extra leg per two-body decay
- ▶ Pragmatic choice: **Narrow-width-approximation (NWA)**
 - gauge invariant in strict on-shell limit of NWA
 - **allows to capture all Sudakov effects** (not present in decay)
 - **allows to go to higher jet multiplicities**
 - not applicable to all processes at all perturbative orders

Technical note: pseudo-singularities for W+2,3 jets

gluonic channels

fermionic channels



- At the considered order **only effects QCD-EW interferences**
- Complex-mass-scheme can not be used with on-shell/stable W's
- NWA: finite width $\Gamma_{\text{reg.}}$ in potentially s-channel propagators for W, Z, t, H
- Smooth **gauge-invariant limit** and negligible numerical dependence for $\Gamma_{\text{reg.}} \rightarrow 0$

$$\Rightarrow \frac{Q^2 - M^2}{(Q^2 - M^2)^2 + \Gamma_{\text{reg}}^2 M^2}$$

Goal:

- Investigation of technical performance at highest possible jet multiplicity
- Investigate dependence of EW corrections on number of jets

Performance of NLO EW OpenLoops amplitudes

- Performance study for $pp \rightarrow t\bar{t} + n \text{ jets}$ with $n=0,1,2$

$t\bar{t} + 0, 1, 2j$	$n_{\text{loop diag}}$		$t_{\text{compile}} [\text{s}]$		size [MB]		$t_{\text{run}} [\text{ms/point}]$	
	QCD	EW	QCD	EW	QCD	EW	QCD	EW
$d\bar{d} \rightarrow t\bar{t}$	11	33	2.1	3.5	0.1	0.2	0.27	0.69
$gg \rightarrow t\bar{t}$	44	70	3.6	3.7	0.2	0.3	1.6	2.8
$d\bar{d} \rightarrow t\bar{t}g$	114	360	3.5	5.9	0.4	0.9	4.8	13
$gg \rightarrow t\bar{t}g$	585	660	8.2	8.8	1.4	1.6	40	56
$d\bar{d} \rightarrow t\bar{t}u\bar{u}$	236	1274	5.3	16	0.8	2.8	12	48
$d\bar{d} \rightarrow t\bar{t}d\bar{d}$	472	2140	9.5	56	1.4	1.4	30	99
$d\bar{d} \rightarrow t\bar{t}gg$	1507	4487	20	47	3.5	8.2	133	327
$gg \rightarrow t\bar{t}gg$	8739	7614	105	79	18	16	1458	1557

Timings on i7-3770K with gcc 4.8 -O0 dynamic and unpolarised $t\bar{t}$ (significantly faster with decays!) using **COLLIER** for reduction

- 1-loop **EW** similarly fast as highly competitive 1-loop **QCD** timings up to $t\bar{t} + 2 \text{ jets}$
- code size, compilation- & runtime reflect a **moderate increase of complexity w.r.t. QCD**
- $2 \rightarrow 4$ NLO QCD+EW feasible!

Z/ γ + l jet: exclusive

Setup:

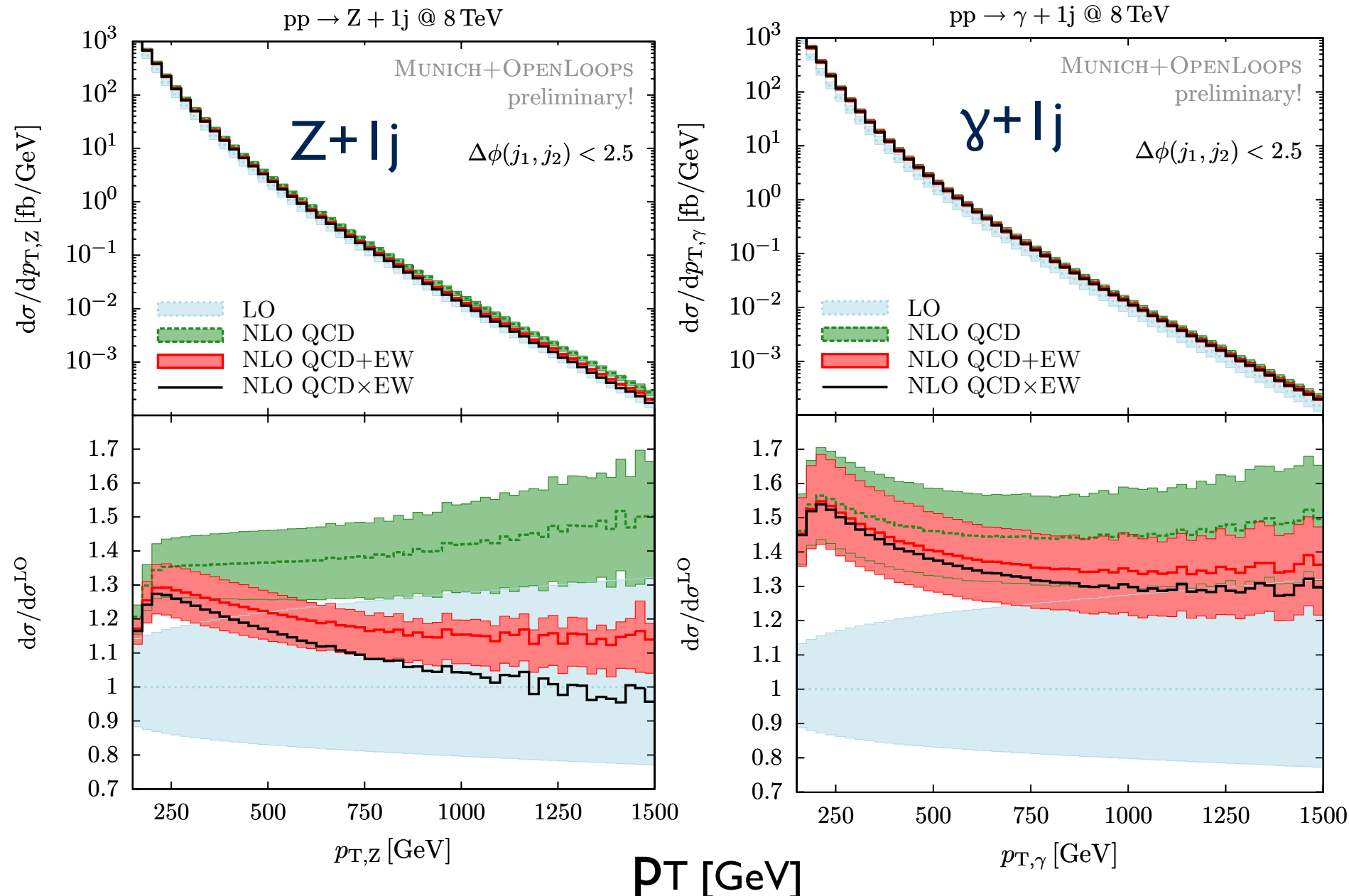
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Frixione-Isolation with $dR=0.3$



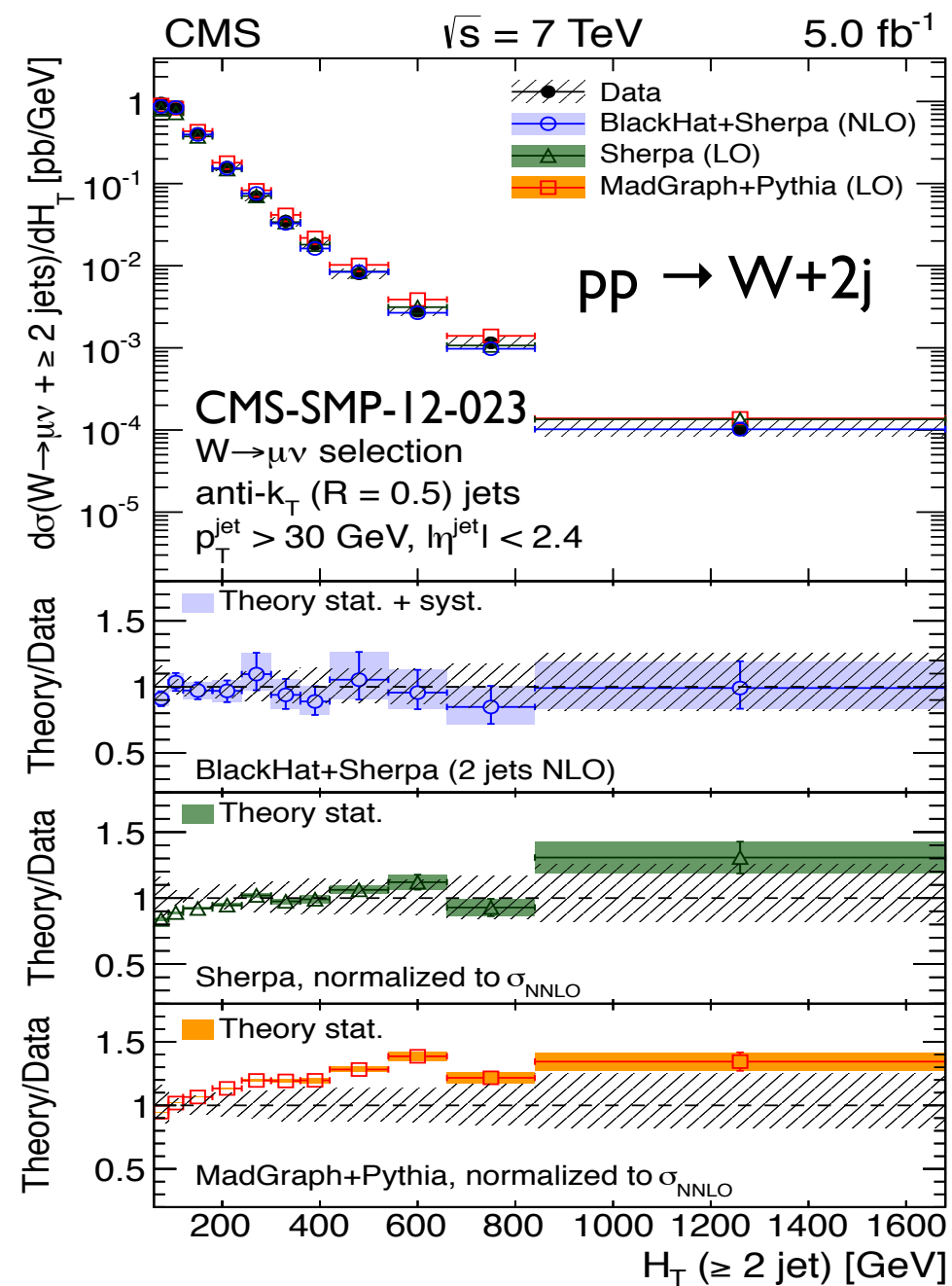
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- ▶ mostly moderate and stable QCD corrections
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- ▶ correction in $p_T(Z) >$ correction in $p_T(\gamma)$
- ▶ **-20/-8% EW for Z/ γ at 1 TeV**
- ▶ EW corrections $>$ QCD uncertainties for $p_{T,Z} > 350 \text{ GeV}$

W + multijet production



- W+2j production badly described by LO+PS (merged)
- H_T @ NLO QCD small uncertainties ($\sim 10\%$)

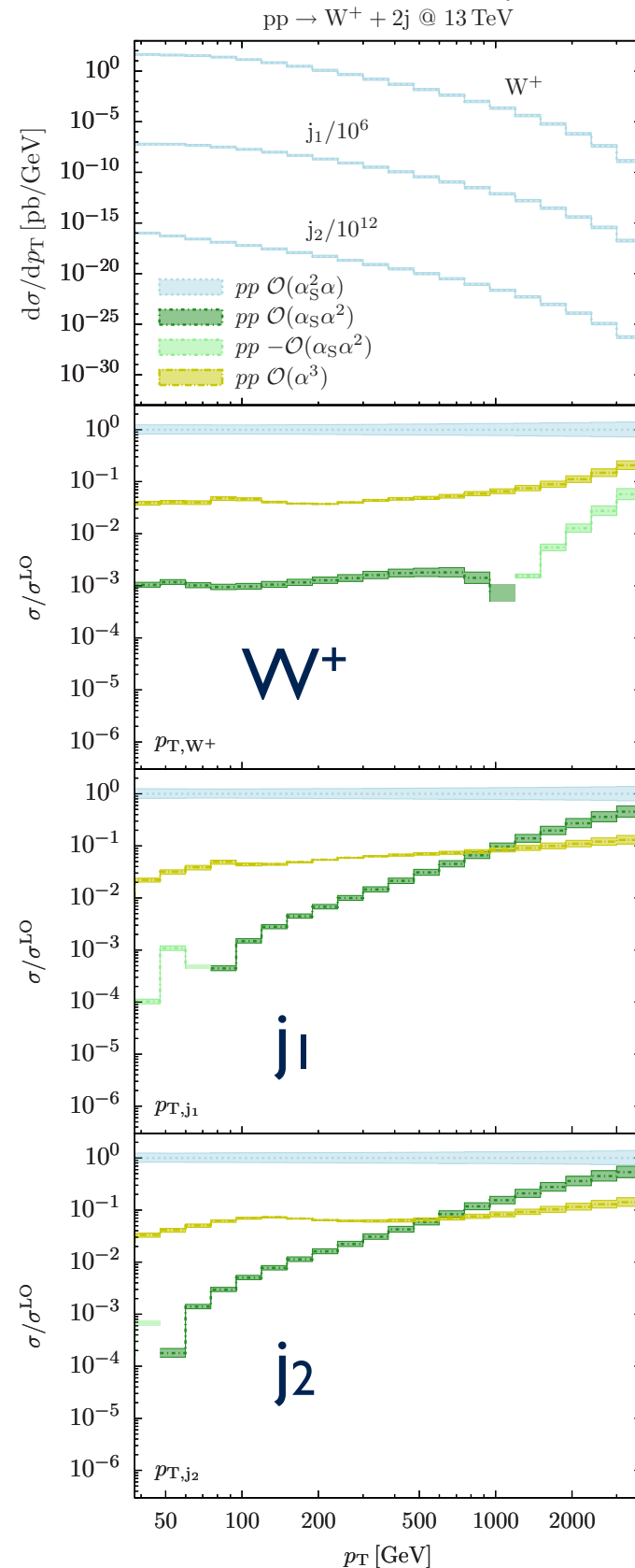
W + 2 jets @ sub-LO: QCD-EW interplay

Setup:

$$\sqrt{S} = 13 \text{ TeV}$$

$$p_{T,j} > 30 \text{ GeV}, \quad |\eta_j| < 4.5$$

$$\mu_0 = \hat{H}_T/2 \text{ (+ 7-pt. variation)}$$

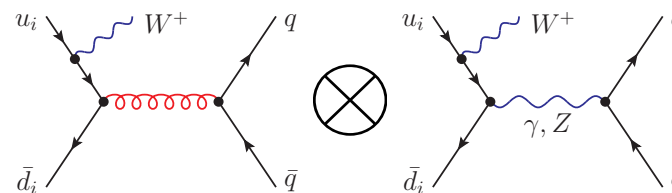


Inclusive

- ▶ Subleading contributions highly suppressed

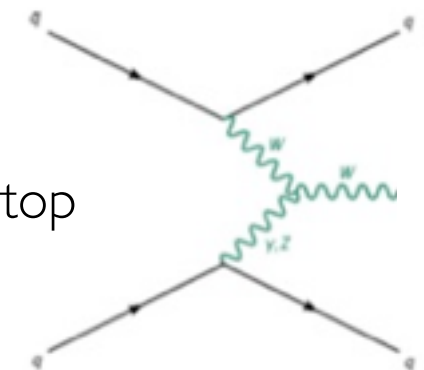
$\mathcal{O}(\alpha_S\alpha^2)$ mixed QCD-EW contribution

- ▶ large impact at large jet-pT (10-50% at 1-4 TeV)!



$\mathcal{O}(\alpha^3)$ pure EW contribution

- ▶ includes contributions from WW, WZ, VBF, single-top
- ▶ 10-20% at 1-4 TeV



Photon PDF comparison at 10^4 GeV^2

