



Partially Composite Dark Matter in Composite Higgs Model

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**MA, Ryuichiro Kitano
and more...**

Topics of this talk

**Composite Higgs
&
Dark Matter**

Topics of this talk

1. Brief review of

Composite Higgs

&

2. Model with

Dark Matter

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1. Brief review of

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&

2. Model with

Dark Matter

produce the Higgs potential

Composite Higgs

- **Higgs boson is a pseudo-NG boson**
arising from a Global symmetry breaking.

Minimal Composite Higgs Model (MCHM)

Agashe, Contino, Pomarol '04

$SO(5)/SO(4)$ breaking



4 NG bosons $\pi(x)$,

Higgs!!

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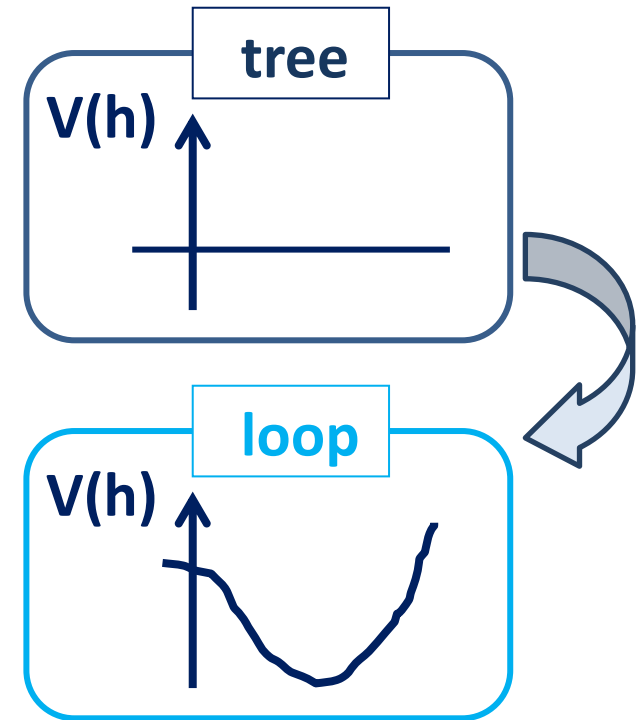
Higgs!!

NLσM: $\Sigma = e^{i\pi^a(x)X^a/f} \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \end{pmatrix} = \begin{pmatrix} \frac{\sin(h/f)}{h} \times \begin{pmatrix} h_1/h \\ h_2/h \\ h_3/h \\ h_4/h \end{pmatrix} \\ \cos(h/f) \end{pmatrix}$

Composite Higgs

- **Higgs boson is a pseudo-NG boson**
arising from a Global symmetry breaking.

- Higgs potential is protected by the **Global Symmetry**.
- EWSB scale is produced by the **Explicit Breaking**.
(**Yukawa** & gauge couplings)



[Next] How implement the top quark? →

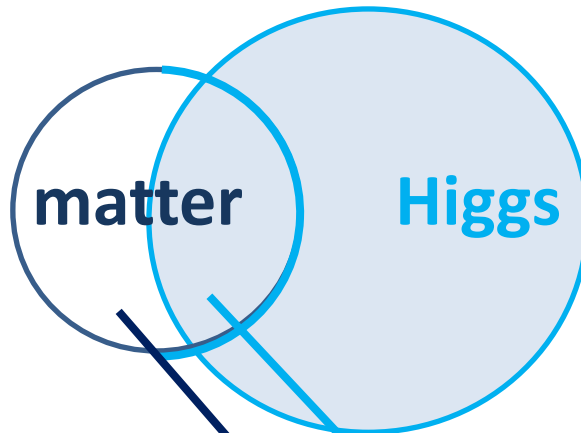
Composite Higgs

Top quark is implemented as

Partially composite fermions

Kaplan '91

Elementary
sector



Composite
sector

Elementary
-Composite mixing

$$\mathcal{L} \ni \lambda_L \psi_L \mathbf{O}_R$$

+ (L \Leftrightarrow R)

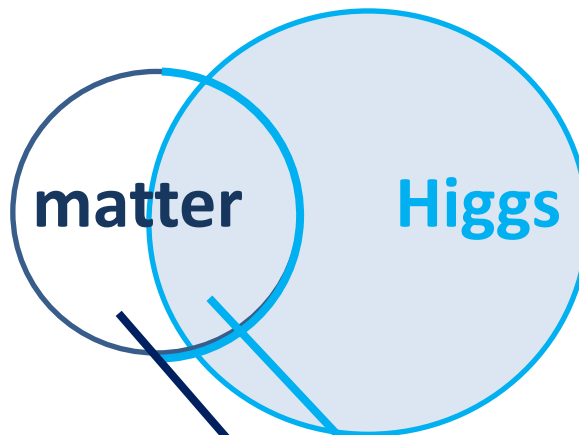
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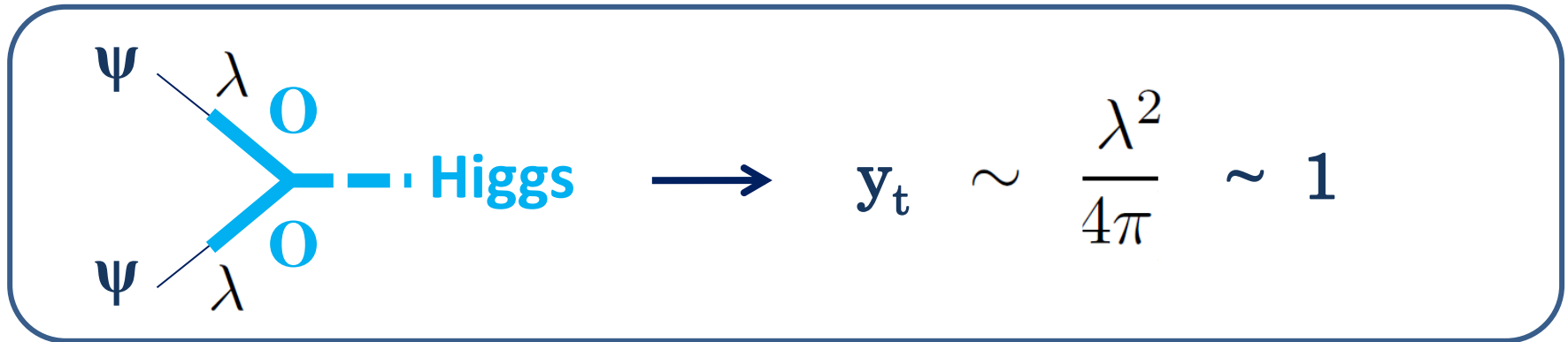
+ (L \leftrightarrow R)

Explicit breaking couplings

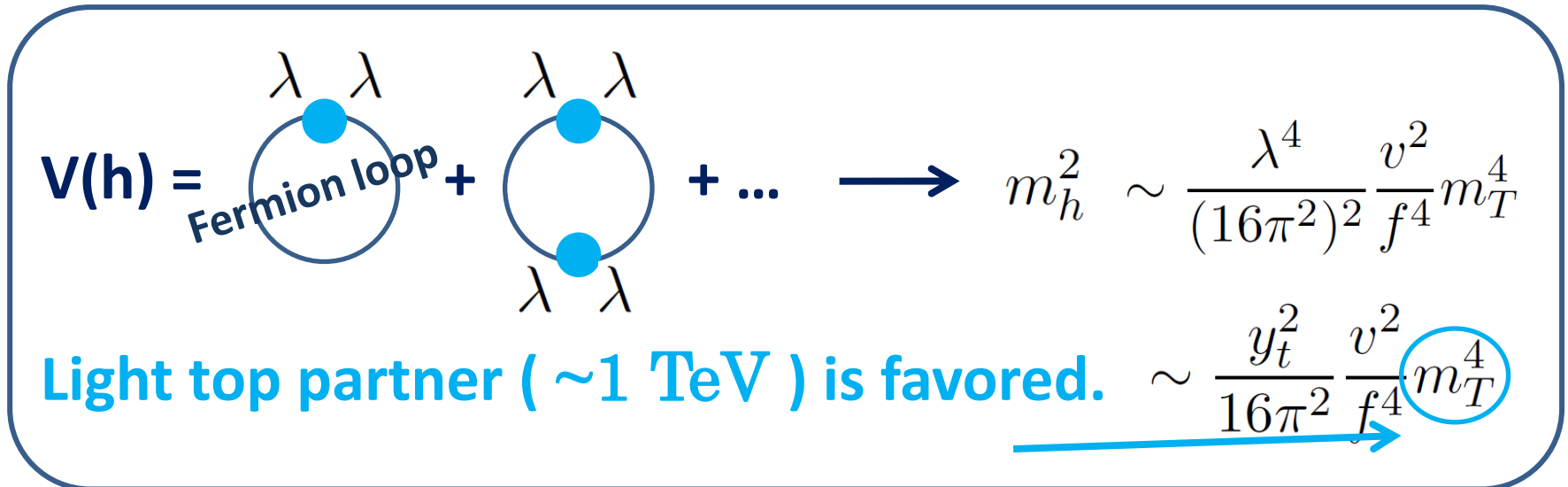
→ produce Yukawa coupling & Higgs potential.

■ Yukawa coupling

(very rough discussion)



■ Higgs potential



For current study with $m_h \sim 125$ GeV, e.g.,
 Matsedonskyi, Panico, Wulzer '12; Marzocca, Serone, Shu '12 ;...

Before Dark matter discussion,

We'll see how to get $v \sim 246\text{GeV}$.

Minimal Composite Higgs Model

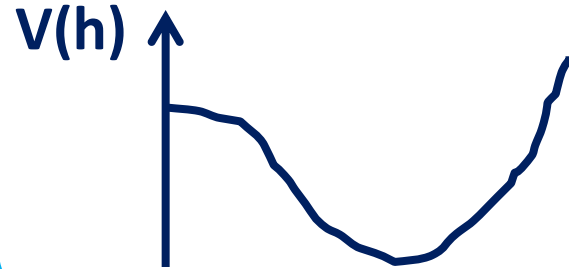
Agashe, Contino, Pomarol '04

Potential

O_t : spinorial rep. 4 of $SO(4)$

$$V(h) \simeq \alpha_t \cos \frac{h}{f} - \beta_t \sin^2 \frac{h}{f}$$

Pseudo-NG boson



$$v(h) = \text{[circle with top vertex]} + \text{[circle with top and bottom vertices]} + \dots$$

← Explicit breaking couplings

Minimal Composite Higgs Model

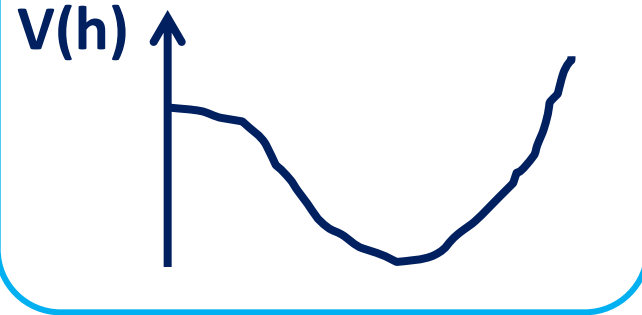
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$$\alpha_t \sim \frac{\lambda^2}{(4\pi)^2} \left[\frac{m_{t'}^4}{(4\pi)^2} \right] \quad \beta_t \sim \left(\frac{\lambda^2}{(4\pi)^2} \right)^2 \left[\frac{m_{t'}^4}{(4\pi)^2} \right]$$

$$v(h) = \text{circle with one blue dot} + \text{circle with two blue dots} + \dots$$

← Explicit breaking couplings

Minimal Composite Higgs Model

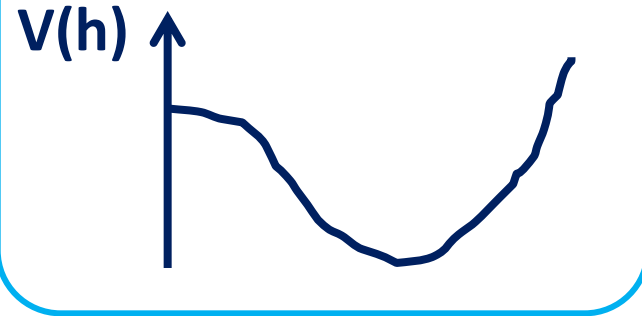
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$$\alpha_t \gg \beta_t$$

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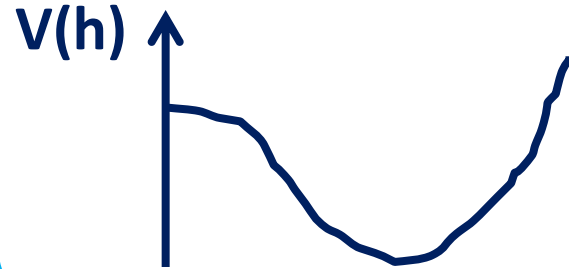
O_t : spinorial rep. 4 of $SO(4)$

$$V(h) \simeq \alpha_t \cos \frac{h}{f} - \beta_t \sin^2 \frac{h}{f}$$

$$\frac{\partial V}{\partial h} = 0$$

$$v/f = \sqrt{1 - \frac{\alpha_t^2}{4\beta_t^2}} \equiv \epsilon$$

Pseudo-NG boson



NDA

$$\alpha_t \gg \beta_t$$

Small ϵ (i.e. $v \ll f$)

is favored by experiments.

Minimal Composite Higgs Model

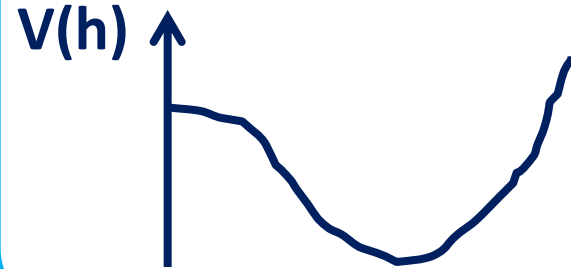
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Pseudo-NG boson



$$\epsilon \equiv v/f < 1$$

$$\alpha_t \simeq 2\beta_t$$

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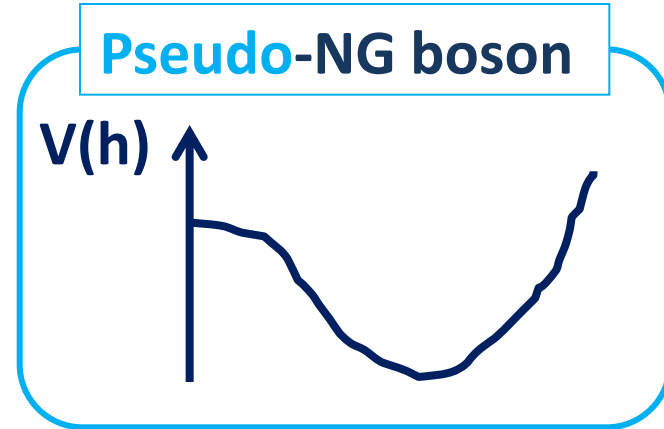
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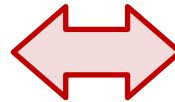


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NDA

$$\alpha_t \gg \beta_t$$



To solve the tension,

People consider, for example, another representations,

4 -> 5 or 10 or 14...

Panico, Redi Tesi, Wulzer '12

**The situation can change
by considering Dark matter!**

Dark Matter

- Dark matter exists $\Omega_{\text{DM}}h^2 = 0.12$
- We know “WIMP Miracle”
 - Observed DM relic can be explained by a DM has **weak scale mass & weak coupling**

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DM may also couple to Higgs weakly.

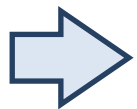
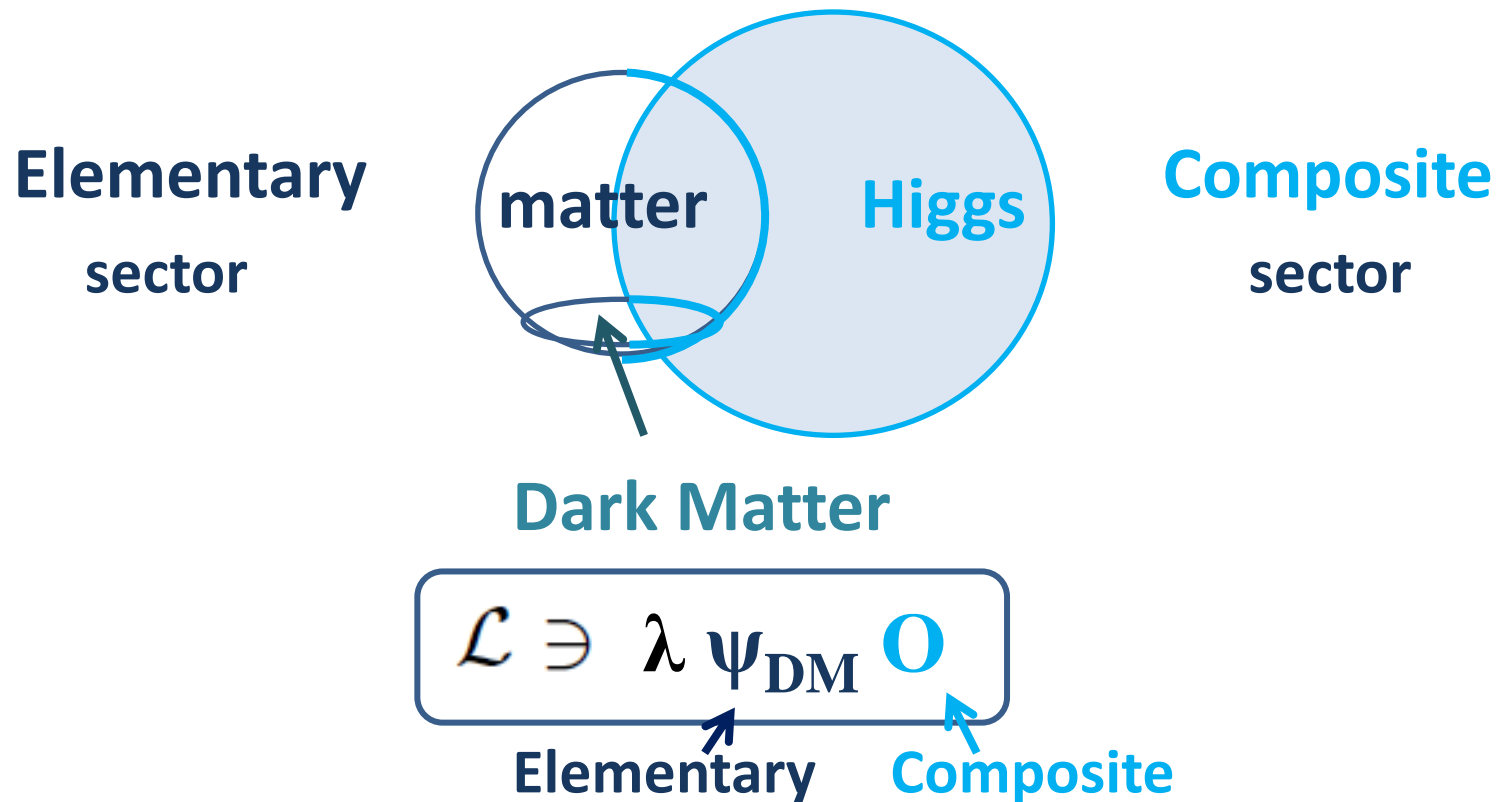
Dark Matter

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DM may also couple to Higgs (i.e. strong sector) weakly.

Dark Matter



DM is also a partially composite fermion & the explicit breaking also contributes to Higgs potential!

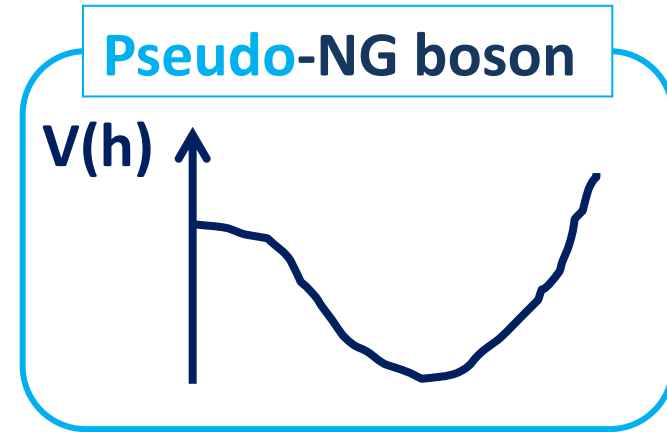
Partially composite DM

Ot: spinorial rep. 4 of SO(4)

$$V(h) \simeq \alpha_t \cos \frac{h}{f} - \beta_t \sin^2 \frac{h}{f}$$

$$v/f = \sqrt{1 - \frac{\alpha_t^2}{4\beta_t^2}} \equiv \epsilon$$

$$\boxed{\epsilon \equiv v/f < 1} \quad \alpha_t \simeq 2\beta_t \quad \longleftrightarrow \quad \boxed{\text{NDA}} \quad \alpha_t \gg \beta_t$$



Partially composite DM

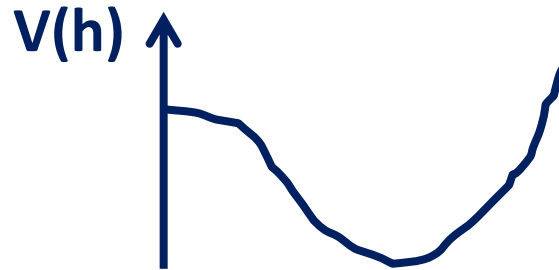
If O_{DM} is in $SO(5)$ vector representation, 5,
the leading Dark sector contribution is $\propto \sin^2(h/f)$.

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$$V(h) = \alpha_t \cos \frac{h}{f} - (\beta + \beta_t) \sin^2 \frac{h}{f}$$

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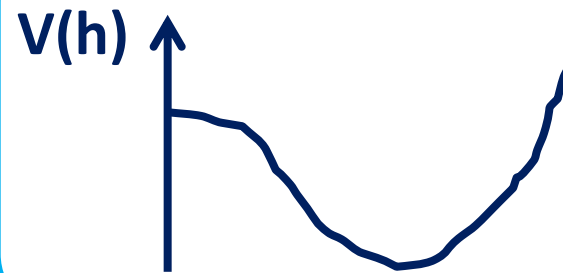
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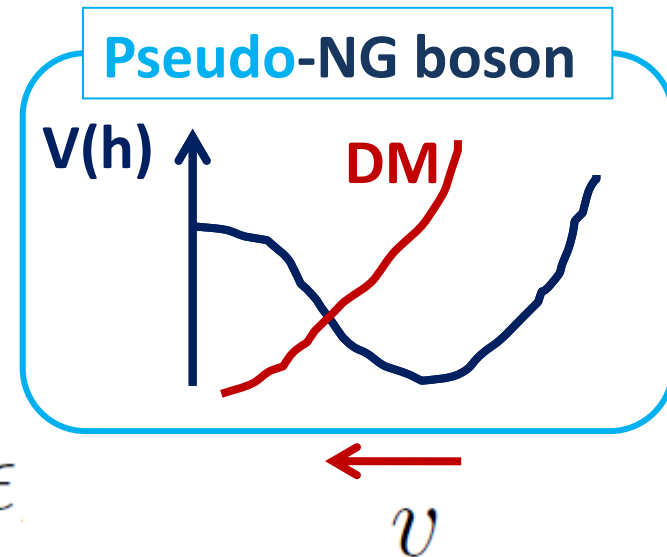
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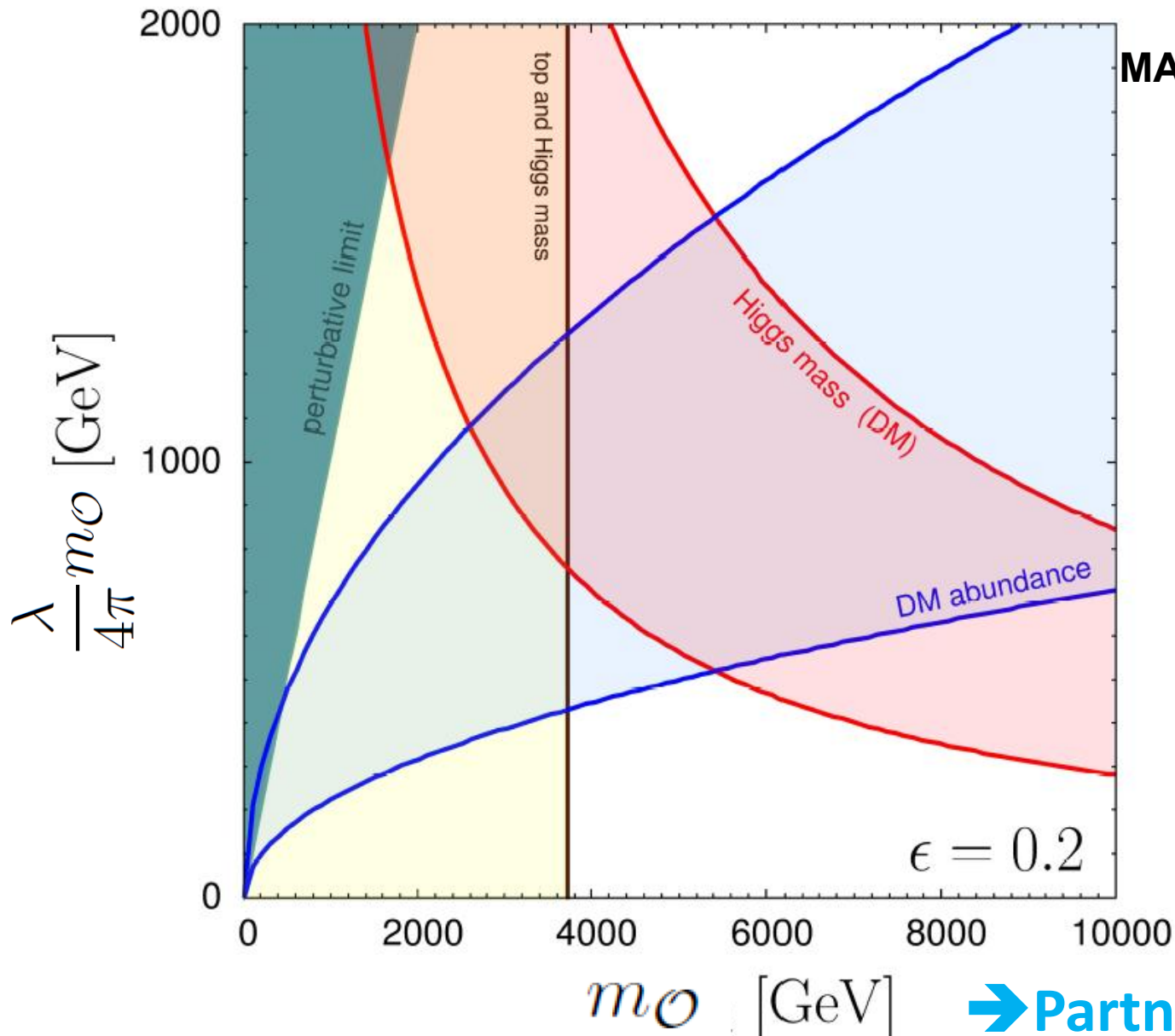
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NDA

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→ Explicit breaking



MA, Kitano '14

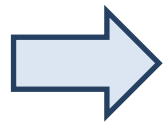
→ Partner mass

It's also consistent with DM relic!

Dark matter phenomenology

After integrating out **Composite O**,
we obtain the low-energy effective theory as

$$\mathcal{L}_{\text{eff}} = -\frac{m_{\text{DM}}}{2}\bar{\psi}_S\psi_S + \frac{\kappa}{2}\bar{\psi}_S\psi_S \sin^2 \frac{h}{f} + \frac{i\kappa_5}{2}\bar{\psi}_S\gamma_5\psi_S \sin^2 \frac{h}{f}$$



This is similar to “Higgs portal DM model”.

$$m_{\text{DM}} \sim \kappa \sim \kappa_5 = c \left(\frac{\lambda}{4\pi} \right)^2 m_{\mathcal{O}}$$

■ Annihilation cross section

$$\langle \sigma_{\text{ann.}} v \rangle \propto (\kappa^2 v^2 \text{ term}) + \underline{\kappa_5^2}$$

■ Direct detection cross section

$$\sigma_{\text{SI}} \propto \underline{\kappa^2} + (\kappa_5^2 v^2 \text{ term})$$

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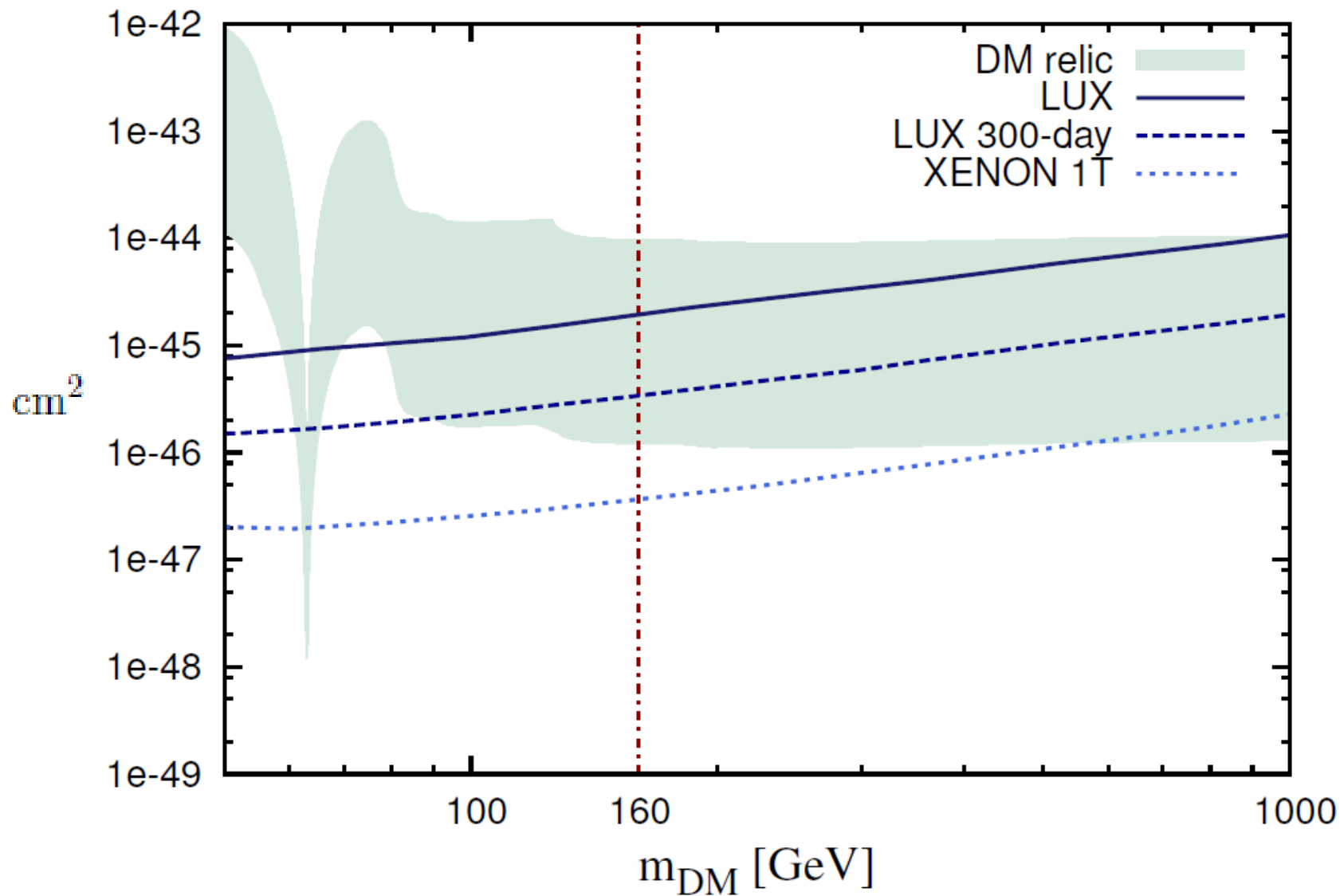
■ Direct detection cross section

$$\sigma_{\text{SI}} \propto \underline{\kappa_1^2} + (\kappa_5^2 v^2 \text{ term})$$

If \cancel{CP} in strong sector, $\kappa_1 \sim \kappa_5$, large κ_1 is not required to explain observed DM relic, then, constraints from direct detection can be mild.

Partially composite DM

MA, Kitano '14



$$1/3 < \kappa_1/\kappa_5 < 3$$

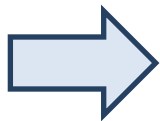
Partially composite DM

$$\mathbf{5}_0 = (\mathbf{2}, \mathbf{2})_0 + (\mathbf{1}, \mathbf{1})_0$$

Spin-1 resonance ρ^μ

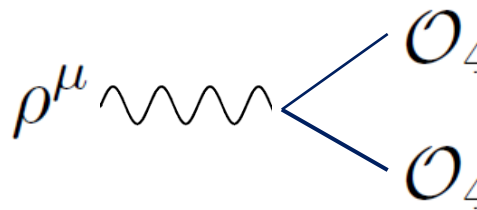
$$\mathcal{O} = \begin{pmatrix} \mathcal{O}_4 \\ \mathcal{O}_1 \end{pmatrix}$$


$$\rho^\mu \rightsquigarrow \Psi_{\text{DM}} \quad \sim g_\rho \epsilon^2 \left(\frac{\lambda}{4\pi} \right)^2 \gamma_5$$



Due to the ϵ^2 suppression, this Br is small.

If it is kinematically allowed,


$$\rho^\mu \rightsquigarrow \mathcal{O}_4 \quad \sim g_\rho$$

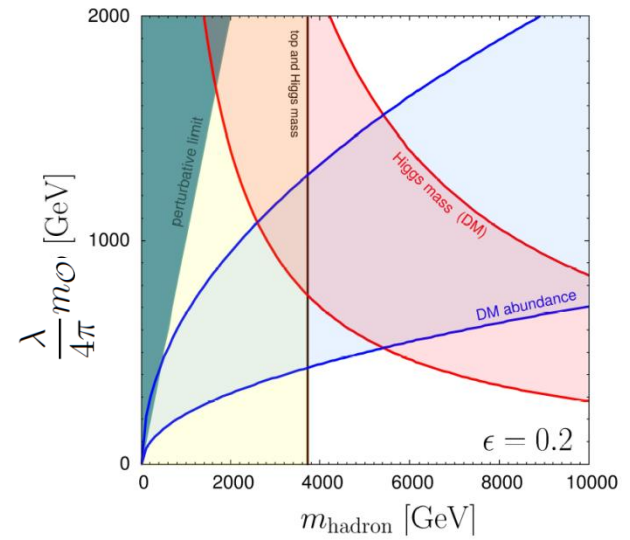
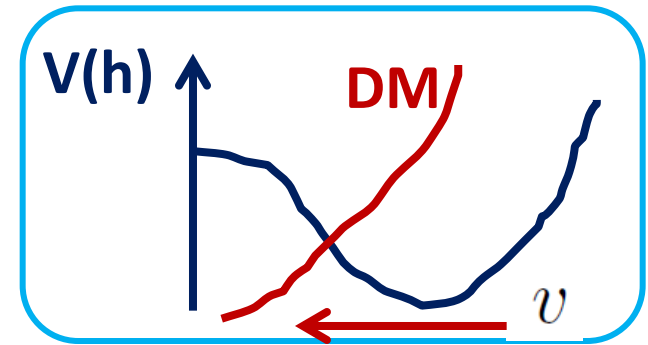
Summary

Summary

We consider a **composite Higgs scenario** in which **Dark matter** is also a **partially composite fermion**.



- **DM also contribute making Higgs potential.**
- **Parameter space consists with both Higgs & DM observables.**
- **It would be measure by DM DD in near future.**



$$\Omega_{\text{DM}} h^2 = 0.12 \qquad \kappa_5 = 160 \text{ GeV} \left(\frac{\epsilon}{0.2} \right)^{-2}$$

$$\Rightarrow \lambda f_{\mathcal{O}} = 900 \text{ GeV} \cdot c_{\kappa_5}^{-1/2} \left(\frac{m_{\mathcal{O}}}{5 \text{ TeV}} \right)^{1/2} \left(\frac{\epsilon}{0.2} \right)^{-1}$$

$$\Rightarrow m_{\text{DM}} = 160 \text{ GeV} \left(\frac{c_{\text{DM}}}{c_{\kappa_5}} \right) \left(\frac{\epsilon}{0.2} \right)^{-2}$$

$$\Rightarrow \sigma_{\text{SI}} \simeq 1.2 \times 10^{-45} \text{ cm}^2 \left(\frac{c_{\kappa}}{c_{\kappa_5}} \right)^2$$

$$m_h^2 = (126 \text{ GeV})^2 = \frac{2(\beta + \beta_t)\epsilon^2}{f^2}$$

$$m_{\mathcal{O}} = 4.9 \text{ TeV} \cdot c_\beta^{-1/2} \left(\frac{\lambda f_{\mathcal{O}}}{1 \text{ TeV}} \right)^{-1} \left(\frac{\epsilon}{0.2} \right)^{-2}$$

$$m_{t'} = 2.4 \text{ TeV} \left(\frac{c_t \cdot 2\lambda_q \lambda_u}{c_q \lambda_q^2 + c_u \lambda_u^2} \right)^{1/3} \left(\frac{\epsilon}{0.2} \right)^{-1}$$
$$\leq 2.4 \text{ TeV} \left(\frac{c_t}{\sqrt{c_q c_u}} \right)^{1/3} \left(\frac{\epsilon}{0.2} \right)^{-1}$$

$$\frac{\lambda_q \lambda_u f_{t'}^2}{m_{t'}^2} = 0.5 \cdot c_t^{-1} \left(\frac{\epsilon}{0.2} \right)^{-1} \left(\frac{m_{t'}}{2.4 \text{ TeV}} \right)^{-1}$$

Partially composite DM

MA, Kitano '14

$$\mathcal{L} \ni -\frac{m}{2}\bar{\psi}_S\psi_S + \lambda\bar{\psi}_S\mathcal{O}_5 + i\lambda'\bar{\psi}_S\gamma_5\mathcal{O}_5$$

$$\mathcal{O} = \begin{pmatrix} \mathcal{O}_1 \\ \mathcal{O}_2 \\ \mathcal{O}_3 \\ \mathcal{O}_4 \\ \mathcal{O}_5 \end{pmatrix}$$

$$\langle\psi_S(x)\bar{\psi}_S(0)\rangle = -\int\frac{d^4k}{i(2\pi)^4}\frac{e^{-ikx}}{\not{k} + \lambda^2\Pi_{55}(k)}, \quad \Pi_{ij}(q) = i\int d^4x\langle\mathcal{O}_i(x)\bar{\mathcal{O}}_j(0)\rangle e^{iqx}$$

$$= \Pi_4(q)(\delta_{ij} - \Sigma_i\Sigma_j) + \Pi_1(q)\Sigma_i\Sigma_j.$$

decompose Π 's

in terms of the unbroken $SO(4)$

$$V(h) = -\frac{1}{2}\int\frac{d^4k}{i(2\pi)^4}\text{Tr}\log[\not{k} + \lambda^2\Pi_{55}(k) + i\epsilon]$$

$$= \text{const.} - \frac{1}{2}\int\frac{d^4k}{i(2\pi)^4}\text{Tr}\left[\frac{-\lambda^2}{\not{k} + i\epsilon}(\Pi_4(k) - \Pi_1(k))\Sigma_5\Sigma_5\right] + O(\lambda^4)$$

$$\equiv \text{const.} - \beta\sin^2\frac{h}{f} + O(\lambda^4),$$

Minimal Composite Higgs Model

Agashe, Contino, Pomarol '04

Top sector A spinorial

representation of $SO(5)$, a **4** of $SO(5)$, contains two (complex) doublets, one transforming under $SU(2)_L$, the other transforming under $SU(2)_R$.

$$\Psi_q = \begin{bmatrix} q_L \\ Q_L \end{bmatrix}, \quad \Psi_u = \begin{bmatrix} q_R^u \\ \begin{pmatrix} u_R \\ d'_R \end{pmatrix} \end{bmatrix}, \quad \Psi_d = \begin{bmatrix} q_R^d \\ \begin{pmatrix} u'_R \\ d_R \end{pmatrix} \end{bmatrix}$$

$$\mathcal{L}_{\text{eff}} =$$

$$\sum_{r=q,u,d} \bar{\Psi}_r \not{p} \left[\Pi_0^r(p) + \Pi_1^r(p) \Gamma^i \Sigma_i \right] \Psi_r + \sum_{r=u,d} \bar{\Psi}_q \left[M_0^r(p) + M_1^r(p) \Gamma^i \Sigma_i \right] \Psi_r$$

$P_{\mu\nu} = \eta_{\mu\nu} - p_\mu p_\nu / p^2$ and $\Gamma^i, i = 1, \dots, 5$, are the gamma matrices for $SO(5)$