

# *NLO QCD corrections to off-shell $t\bar{t}j$ production at the LHC*

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# *Plan*

- Motivation for  $t\bar{t}j$  production at the LHC
- Motivation for top-quark off-shell effects based on  $t\bar{t}$  production
- Status of theoretical predictions for  $t\bar{t}j$
- Complete off-shell effects with **HELAC-NLO** for  $t\bar{t}j$
- Results for LHC @ 8 TeV
- Summary & Outlook

*Collaborators:*

*G. Bevilacqua (University of Debrecen)*  
*H. B. Hartanto (RWTH Aachen University)*  
*M. Kraus (RWTH Aachen University)*

# Motivation for $ttj$

- @ LHC tops are produced with large energies & high transverse momenta
- Increase probability for additional (hard) radiation of gluons  $\rightarrow ttj$  final state
- How big is the contribution of  $ttj$  in the inclusive  $tt$  sample ?
- NNLO  $tt$  cross section for  $m_t = 173.2 \text{ GeV}$  @  $\text{LHC}_{13 \text{ TeV}}$  with CT14 PDF set:

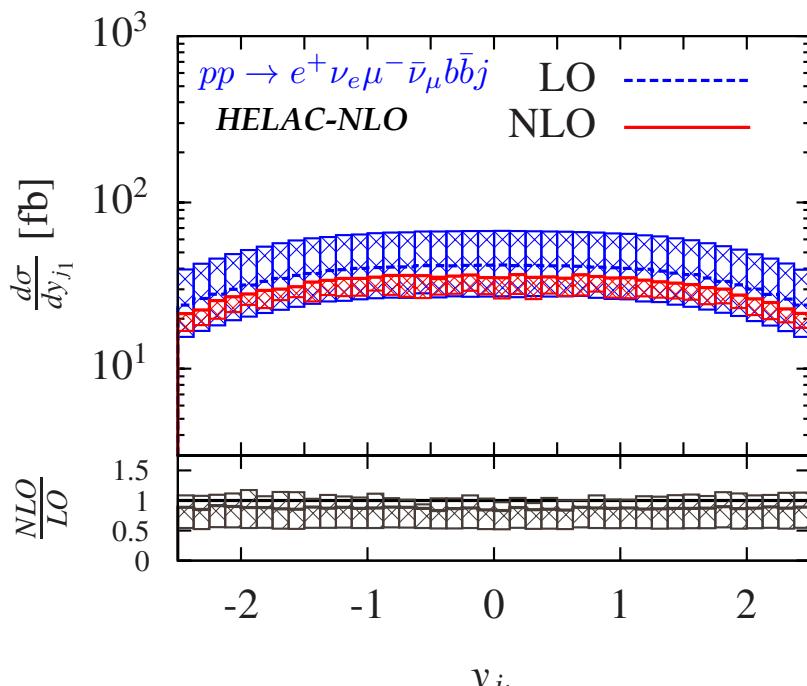
$$\sigma(tt) = 807 \text{ pb}$$

*TOP++, Czakon, Mitov '14*

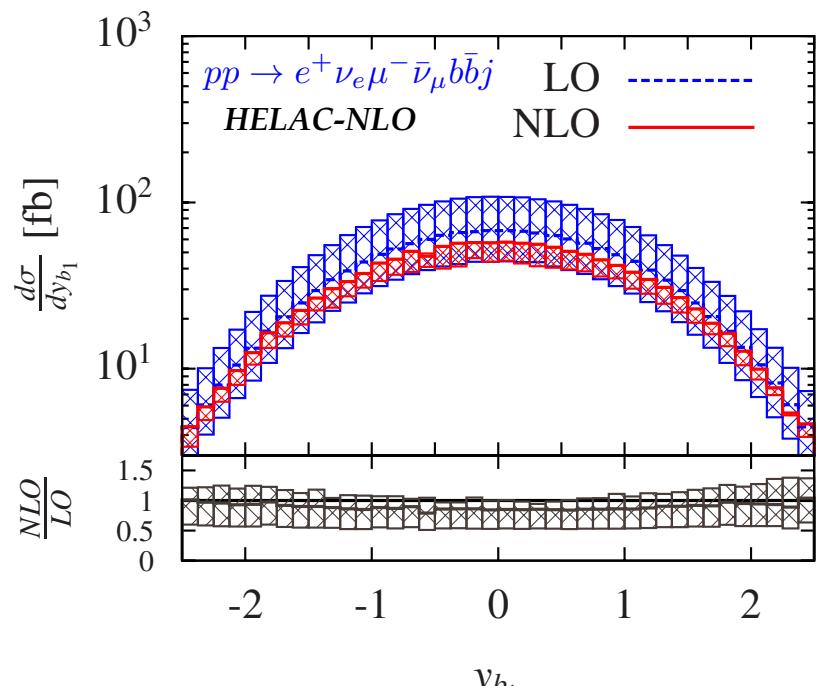
Jet $p_T$ cut [GeV]	$\sigma(ttj)$ [pb]	$\sigma(ttj)/\sigma(tt)$ [%]
40	$296.97 \pm 0.29$	37
60	$207.88 \pm 0.19$	26
80	$152.89 \pm 0.13$	19
100	$115.60 \pm 0.14$	14
120	$89.05 \pm 0.10$	11

# Motivation for $t\bar{t}j$

- Background to SM Higgs production in VBF:  $qq \rightarrow Hqq \rightarrow WWqq$
- 2 tagging jets:  $\Delta y_{jj} = |y_{j1} - y_{j2}| > 4$  &  $y_{j1} \times y_{j2} < 0$
- $\downarrow$  tt background:  $tt \rightarrow WWbb$  &  $\uparrow$  ttj background:  $ttj \rightarrow WWbbj$



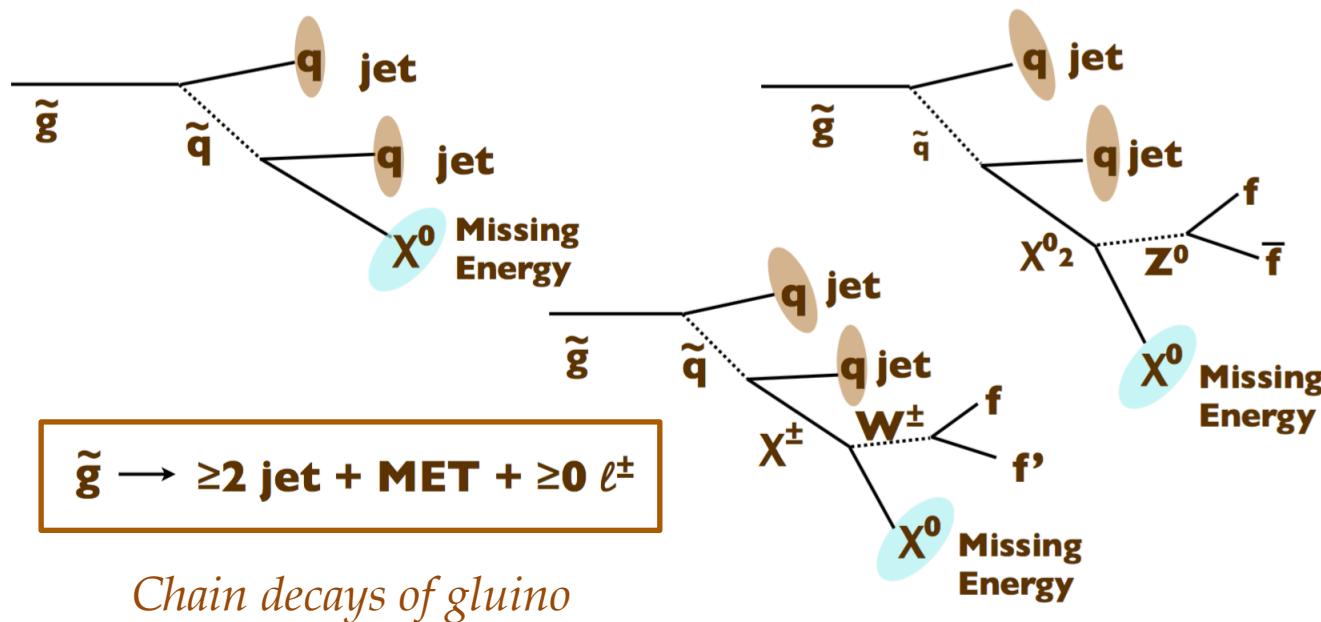
forward/backward light-jets



b-jets from tops are central

# Motivation for $t\bar{t}j$

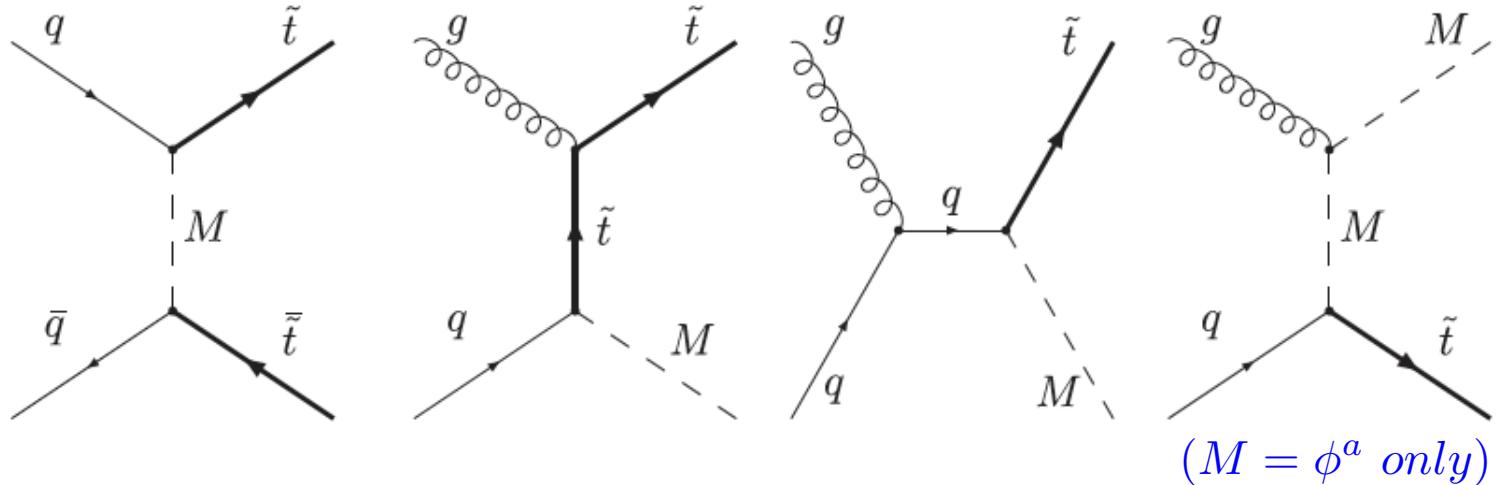
- Background to supersymmetric particle production
- Top decays into W and b-quark → SM :  $t \rightarrow Wb \approx 100\%$
- *Decay channels*: di-leptons ( $\mathcal{Br} = 4\%$ ), lepton+jet ( $\mathcal{Br} = 30\%$ ), all-jets ( $\mathcal{Br} = 46\%$ )
  - ★  *$t\bar{t}j$  signature*: jets, charged leptons &  $p_T^{\text{miss}}$  from invisible neutrinos
  - ★ *Typical signals*: jets, charged leptons &  $p_T^{\text{miss}}$  due to escaping lightest supersymmetric particle (neutralino)



# Motivation for $t\bar{t}j$

- Background to production of top flavor violating resonances  $pp \rightarrow Mt \rightarrow t\bar{t}j$

*M. I. Gresham, I.-W. Kim, K. M. Zurek '11*



$\tilde{t} = t$  for  $M = W', Z'_H$  and  $\tilde{t} = \bar{t}$  when  $M = \phi^a$  (color triplet or sextet)

- $W'$  signal:  $W' \rightarrow \bar{t}q$
- Production processes:  $pp \rightarrow W't \rightarrow t\bar{t}j$

$m_{W'} \in \{200, \dots, 600\} \text{ GeV}$

$\sigma_{7\text{TeV}} \in \{40, \dots, 4\} \text{ pb}$

- ATLAS:**  $m_{W'} > 430 \text{ GeV}$

*arXiv:1209.6593*

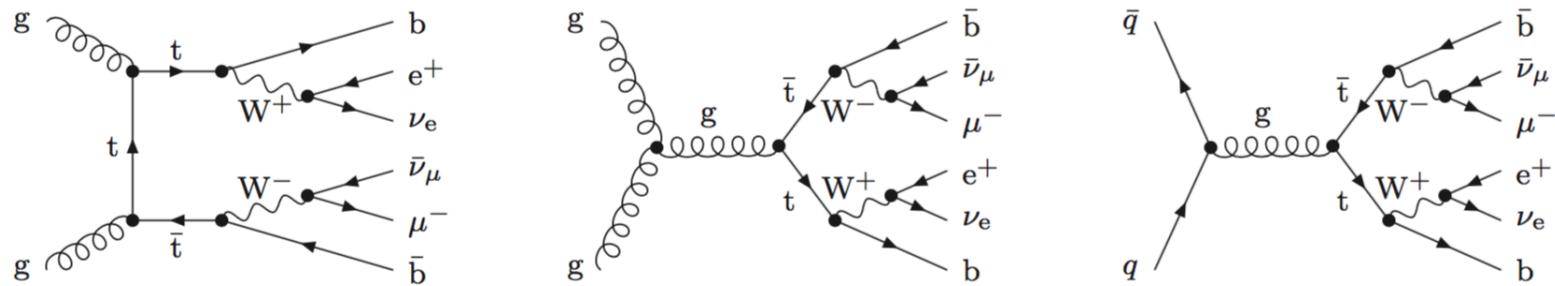
$$\mathcal{L}_{W'} = \frac{1}{\sqrt{2}} \bar{d} \gamma^\mu g_R P_R t W'_\mu + \text{H.c.},$$

$$\mathcal{L}_{Z'_H} = \frac{1}{\sqrt{2}} \bar{u} \gamma^\mu g_R P_R t Z'_{H\mu} + \text{H.c.},$$

$$\mathcal{L}_\phi = \bar{t}^c T_r^a (g_L P_L + g_R P_R) u \phi^a + \text{H.c.},$$

# NWA Vs. Off-shell Effects

- NWA → Tops are restricted to on-shell states
- Approximation is controlled by the ratio:  $\Gamma_t/m_t \approx 10^{-2}$
- Contributions from diagrams involving two top-quark resonances



- Should be accurate for sufficiently inclusive observables
- Indeed → *top-quark off-shell effects for  $\sigma$  at few % level for:*

★  $pp \rightarrow tt$

*A. Denner et al. '11, G. Bevilacqua et al. '11, A. Denner et al. '12  
R. Frederix '14, F. Cascioli et al. '14, G. Heinrich et al '14*

★  $pp \rightarrow ttH$

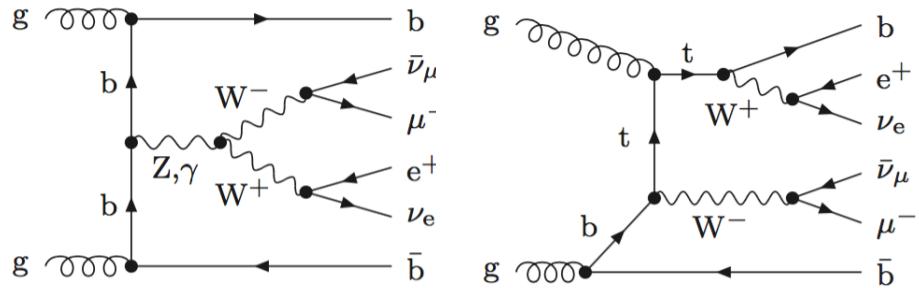
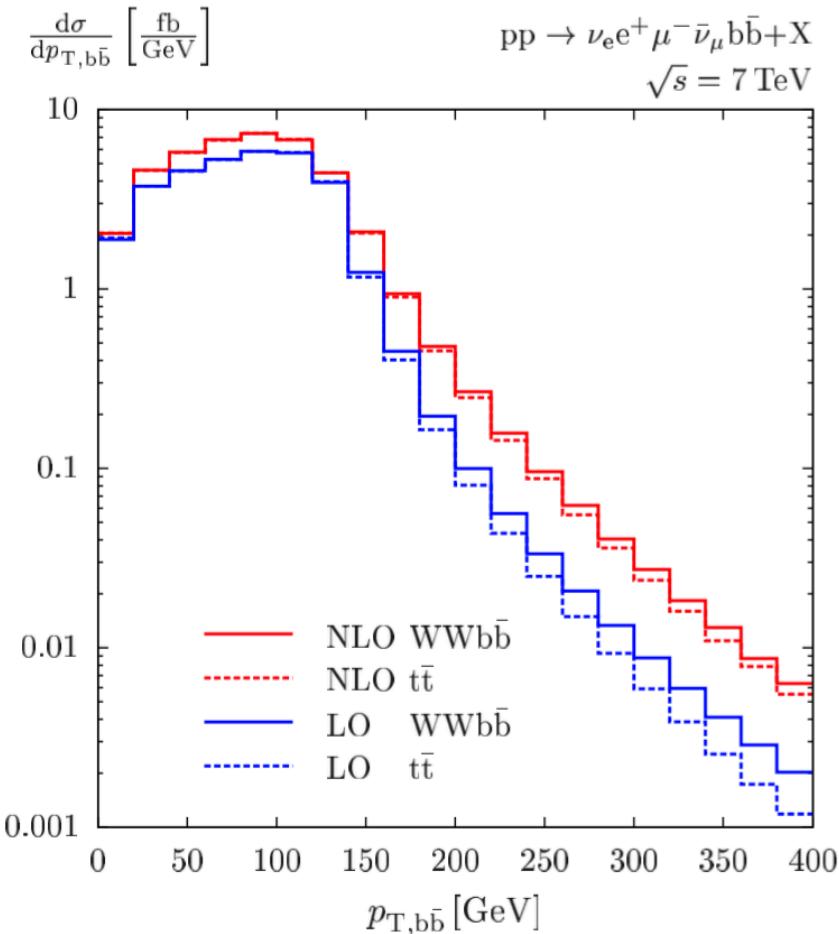
*A. Denner, R. Feger '15*

★  $pp \rightarrow ttj$

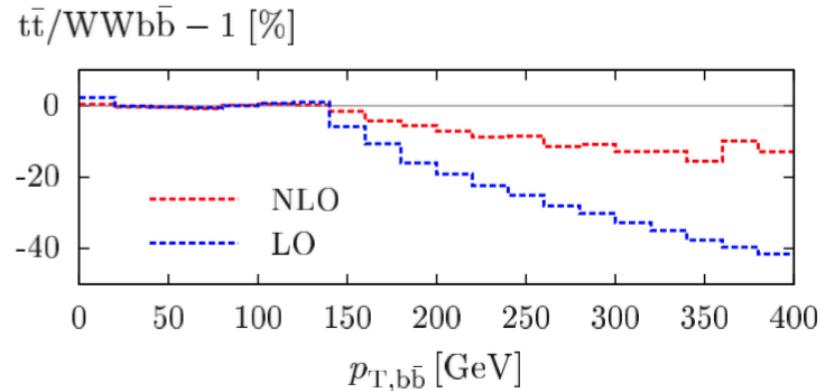
*G. Bevilacqua, H. B. Hartanto, M. Kraus, M. Worek '16*

# NWA Vs. Off-Shell Effects

- Larger impact on differential distributions
- Full NWA ( $t\bar{t}$ ) versus full calculation (WW $b\bar{b}$ ) for  $p_T(b\bar{b})$

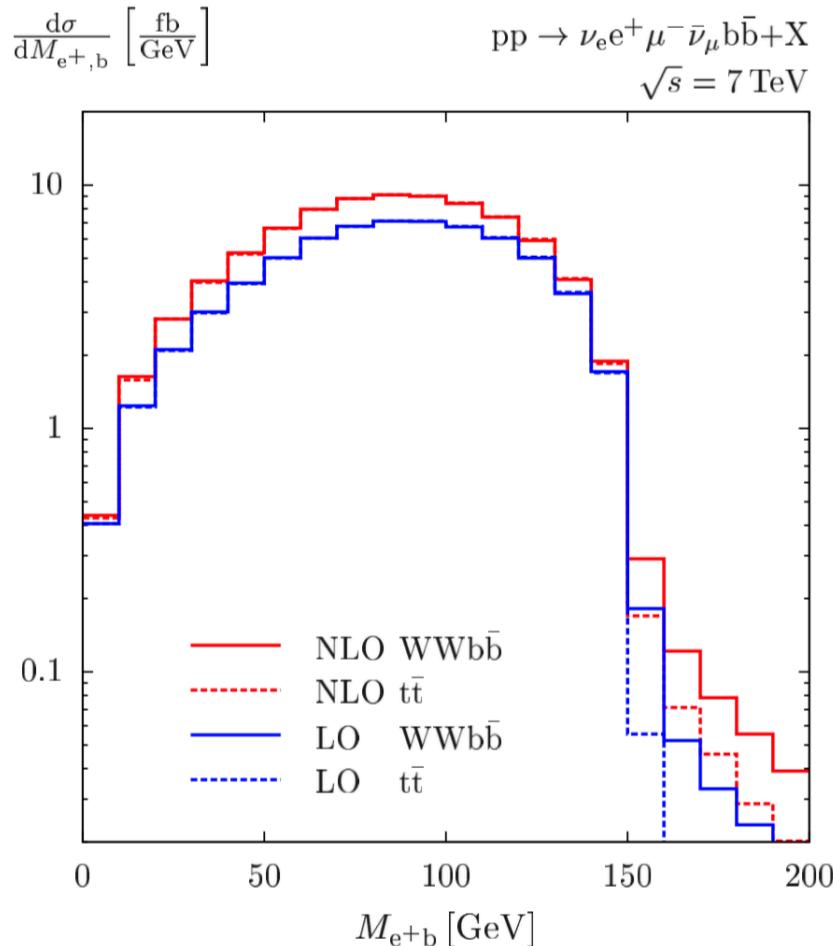


...also diagrams with one or no top-quark resonances

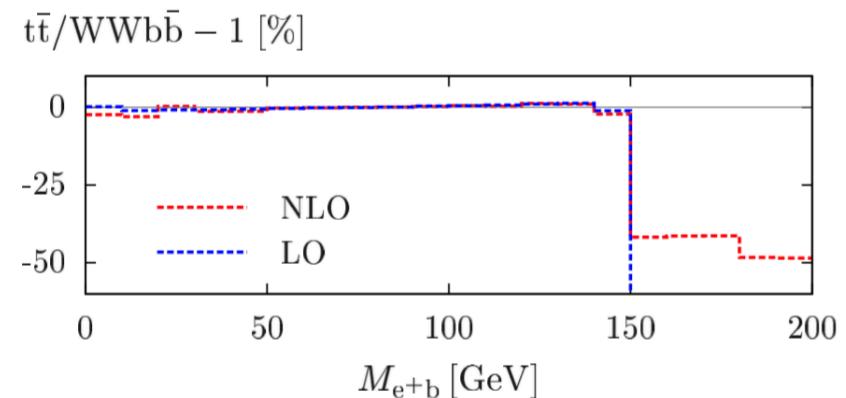


# NWA Vs. Off-Shell Effects

- Full NWA ( $t\bar{t}$ ) versus full calculation (WW $b\bar{b}$ ) for  $M_{e+b}$



- If both top and W decay on-shell  
 $\rightarrow$  end-point given by sharp cut
- $M_{\ell b} = \sqrt{m_t^2 - m_W^2} \approx 152 \text{ GeV}$
- Additional radiation & off-shell effects introduce smearing



# *Theoretical Predictions for $t\bar{t}j$*

- NLO QCD corrections to on-shell  $t\bar{t}j$  production

*S. Dittmaier, P. Uwer, S. Weinzierl '07 '09*

- NLO QCD correction to on-shell  $t\bar{t}j$  production with LO decays

*K. Melnikov, M. Schulze '10*

- NLO QCD corrections to  $t\bar{t}j$  in NWA (with jet radiation in top-quark decays)

*K. Melnikov, M. Schulze '12*

- **NLO QCD corrections to  $t\bar{t}j$  with full top-quark and W off-shell effects**

*G. Bevilacqua, H. B. Hartanto, M. Kraus, M. Worek '16*

- NLO QCD correction to on-shell  $t\bar{t}j$  production + PS

★ **POWHEG + PYTHIA**, no spin correlations

*A. Kardos, C. G. Papadopoulos, Z. Trocsanyi '11*

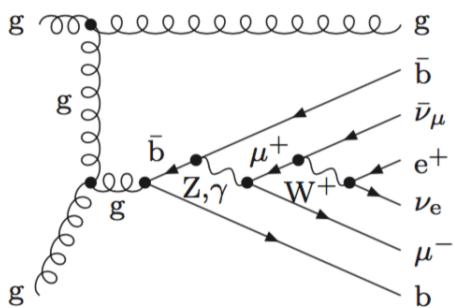
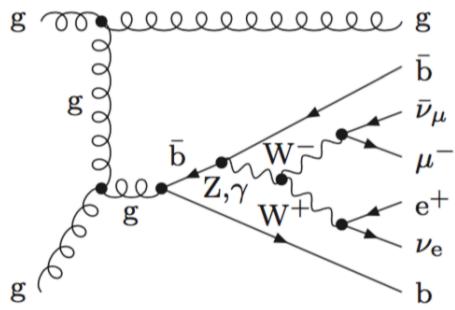
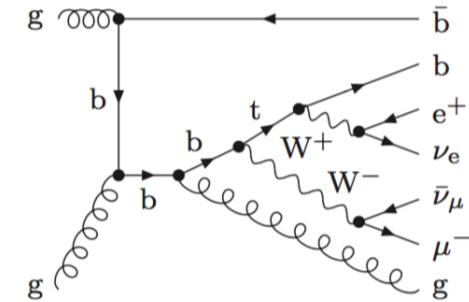
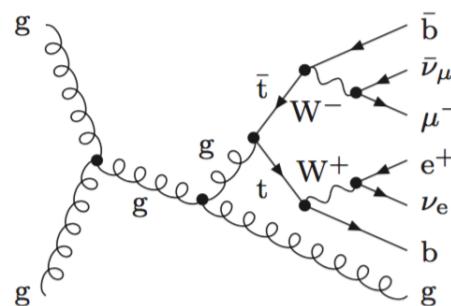
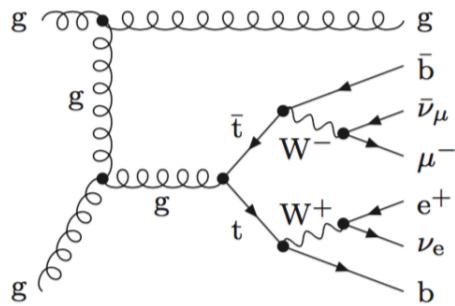
★ **POWHEG + PYTHIA/HERWIG** with spin-correlations @ LO

*S. Alioli, S. Moch, P. Uwer '12*

★ **MC@NLO + DEDUCTOR**, without top-quark decays

*M. Czakon, H. B. Hartanto, M. Kraus, M. Worek '15*

# Off-Shell Effects for $t\bar{t}j$



$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} j + X$$

- $t\bar{t}j$  with leptonic decays at  $\mathcal{O}(\alpha_s^4 \alpha^4)$
- $2 \rightarrow 5$  process from the QCD point of view
- Diagrams with complete off-shell effects for top & W gauge boson for gg initial state:
  - ★ LO: 508
  - ★ Real emission: 4447

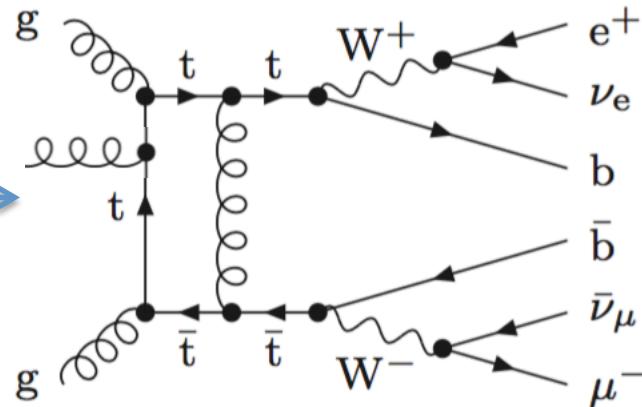
# Off-Shell Effects for $t\bar{t}j$

- $gg$  channel comprises 39 180 one-loop diagrams → according to QGRAF

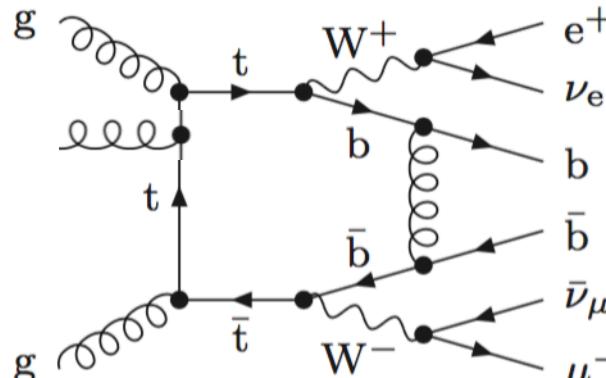
P. Nogueira '93

- The most complicated ones are 1155 hexagons & 120 heptagons
- Tensor integrals up to rank six

NWA for  $t\bar{t}j$  (on-shell top-quark production)  
- up to pentagons !



Full calculations for  $t\bar{t}j$   
- up to heptagons !



# Intermediate Top Resonances

- Putting simply  $\Gamma_t \neq 0$  violates gauge invariance
- Gauge-invariant treatment  $\rightarrow$  complex-mass scheme
- $\Gamma_t$  incorporated into top mass via:

$$\mu_t^2 = m_t^2 - i m_t \Gamma_t$$

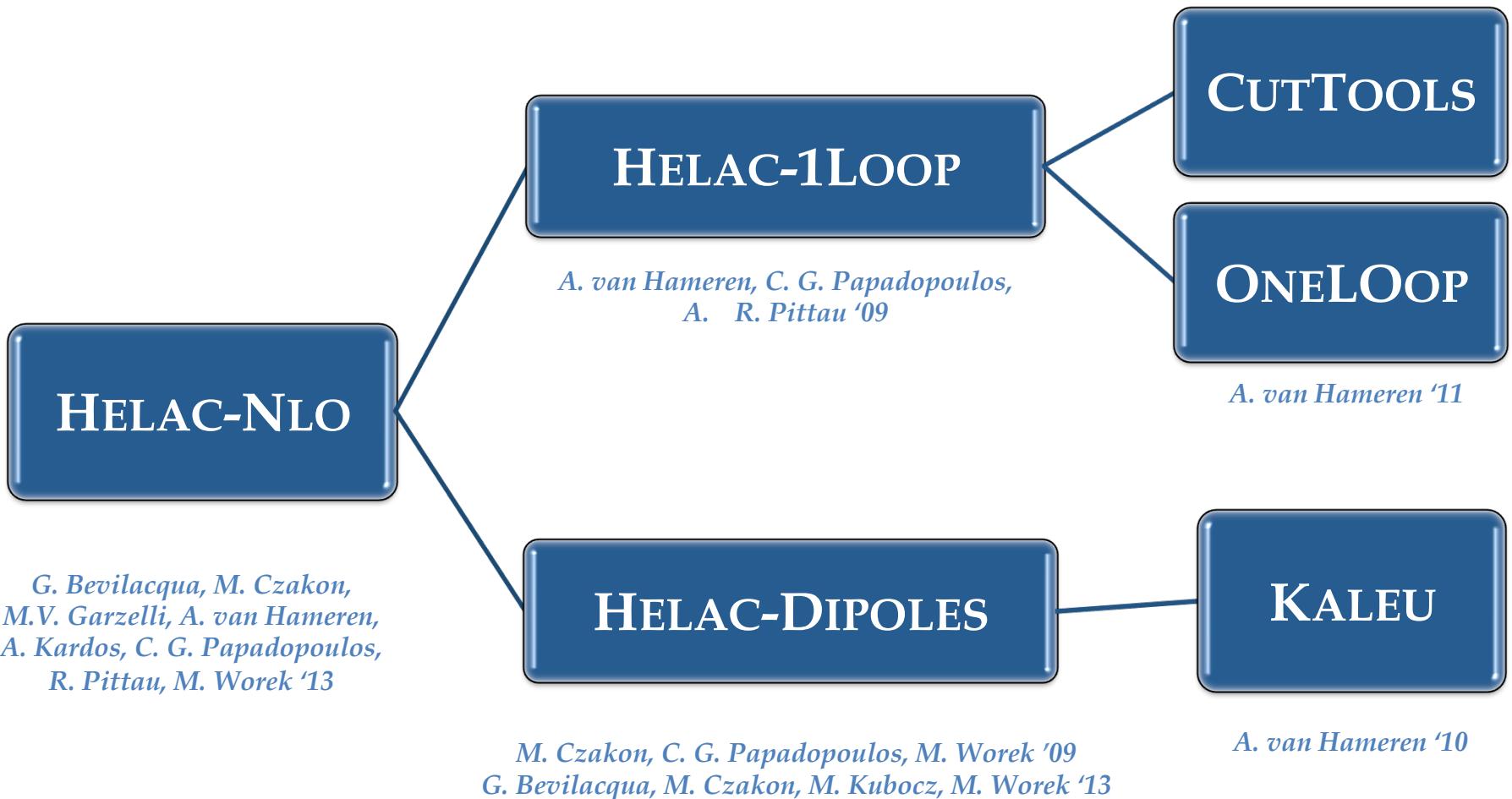
A. Denner, S. Dittmaier, M. Roth, D. Wackerlo '99  
A. Denner, S. Dittmaier, M. Roth, L. H. Wieders '05

- All matrix elements evaluated using complex masses
- $\mu_t^2$  identified with the position of pole of top-quark propagator
- Top-mass counter-term  $\delta\mu_t$  related to top-quark self-energy at:  $p_t^2 = \mu_t^2$
- *Another non trivial aspect:* evaluation of one-loop scalar integrals in presence of complex masses !
- Scalar integrals with complex masses  $\rightarrow$  supported e.g. by **ONELOOP**

A. van Hameren '11

# *HELAC-NLO*

*G. Ossola, C. G. Papadopoulos,  
R. Pittau '08*



# *HELAC-NLO*

- **HELAC-1LOOP** → Virtual corrections in 't Hooft-Veltman version of dimensional regularization
- **CUTTOOLS** → Ossola-Papadopoulos-Pittau (OPP) reduction technique
- **ONELOOP** → Evaluation of scalar integrals with complex masses
- **HELAC-DIPOLES** → The singularities from soft or collinear parton emissions isolated via subtraction methods for NLO QCD:
  - ★ Catani-Seymour dipole subtraction
  - ★ Nagy-Soper subtraction scheme
  - ★ Both for massive and massless cases
  - ★ Restriction on the phase space of the subtraction →  $\alpha_{\max}$
- Reweighting & unweighting techniques, helicity, and color sampling methods for optimization
- **KALEU** → Phase-space integration
  - ★ Multi-channel Monte Carlo techniques
  - ★ Adaptive weight optimization
  - ★ Dedicated additional channels for each subtraction term for both subtractions

# Results for $t\bar{t}j$

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} j + X$$

- Different lepton generations → Effects at the level of 0.5% → checked @ LO
- Diagrams for gg initial state @ LO: 508 for  $e^+\mu^-$  → 1240 for  $e^+e^-$
- SM Parameters in  $G_\mu$  scheme:

$$G_F = 1.16637 \cdot 10^{-5} \text{ GeV}^{-2}, \quad m_t = 173.3 \text{ GeV},$$

$$m_W = 80.399 \text{ GeV}, \quad \Gamma_W = 2.09974 \text{ GeV},$$

$$m_Z = 91.1876 \text{ GeV}, \quad \Gamma_Z = 2.50966 \text{ GeV},$$

$$\Gamma_t^{\text{LO}} = 1.48132 \text{ GeV}, \quad \Gamma_t^{\text{NLO}} = 1.3542 \text{ GeV}.$$

- MSTW2008 set of PDF &  $\mu_R = \mu_F = \mu_0 = m_t$
- All light quarks including *b-quarks* and leptons *are massless*
- Suppressed *contribution from b quarks* in the initial state *neglected*
- Amounts to 0.8% @ LO

# Top Width

- Finite W width contributions included in matrix elements & in  $\Gamma_t$
- Top width for unstable W bosons, neglecting bottom quark mass @ LO & NLO*

$$\Gamma_t^{\text{LO}} = \frac{G_\mu m_t^5}{16\sqrt{2}\pi^2 M_W^2} \int_0^1 \frac{dy \gamma_W}{(1 - y/\bar{y})^2 + \gamma_W^2} F_0(y)$$

M. Jezabek, J. H. Kühn '89  
A. Denner, et al. '12

$$\gamma_W = \Gamma_W/M_W, \bar{y} = (M_W/m_t)^2 \quad F_0(y) = 2(1-y)^2(1+2y)$$

$$\Gamma_t^{\text{NLO}} = \frac{G_\mu m_t^5}{16\sqrt{2}\pi^2 M_W^2} \int_0^1 \frac{dy \gamma_W}{(1 - y/\bar{y})^2 + \gamma_W^2} \left[ F_0(y) - \frac{2\alpha_s}{3\pi} F_1(y) \right]$$

$$\begin{aligned} F_1(y) = & 2(1-y)^2(1+2y) [\pi^2 + 2 \operatorname{Li}_2(y) - 2 \operatorname{Li}_2(1-y)] \\ & + 4y(1-y-2y^2) \ln(y) + 2(1-y)^2(5+4y) \ln(1-y) \\ & - (1-y)(5+9y-6y^2). \end{aligned}$$

- In the limit  $\gamma_W \rightarrow 0$

$$\frac{\gamma_W}{(1 - y/\bar{y})^2 + \gamma_W^2} \rightarrow \pi \bar{y} \delta(y - \bar{y}).$$

# Cuts

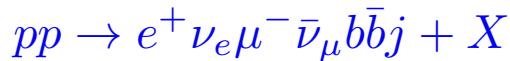
$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} j + X$$

- *Jets:*
  - ★ Final-state quarks and gluons with pseudo-rapidity  $|y| < 5$  converted into infrared-safe jets using *anti- $k_T$  jet* algorithm with  $R=0.5$
- *Requirement:*
  - ★ exactly 2 b-jets, at least one light-jet, 2 charged leptons, and missing  $p_T$
- *Final states:*
  - ★ have to fulfill the following kinematical requirements (fairly inclusive cuts)

$$\begin{array}{ll} p_{T\ell} > 30 \text{ GeV}, & p_{Tj} > 40 \text{ GeV}, \\ p_T^{\text{miss}} > 40 \text{ GeV}, & \Delta R_{jj} > 0.5, \\ \Delta R_{\ell\ell} > 0.4, & \Delta R_{\ell j} > 0.4, \\ |y_\ell| < 2.5, & |y_j| < 2.5, \end{array}$$

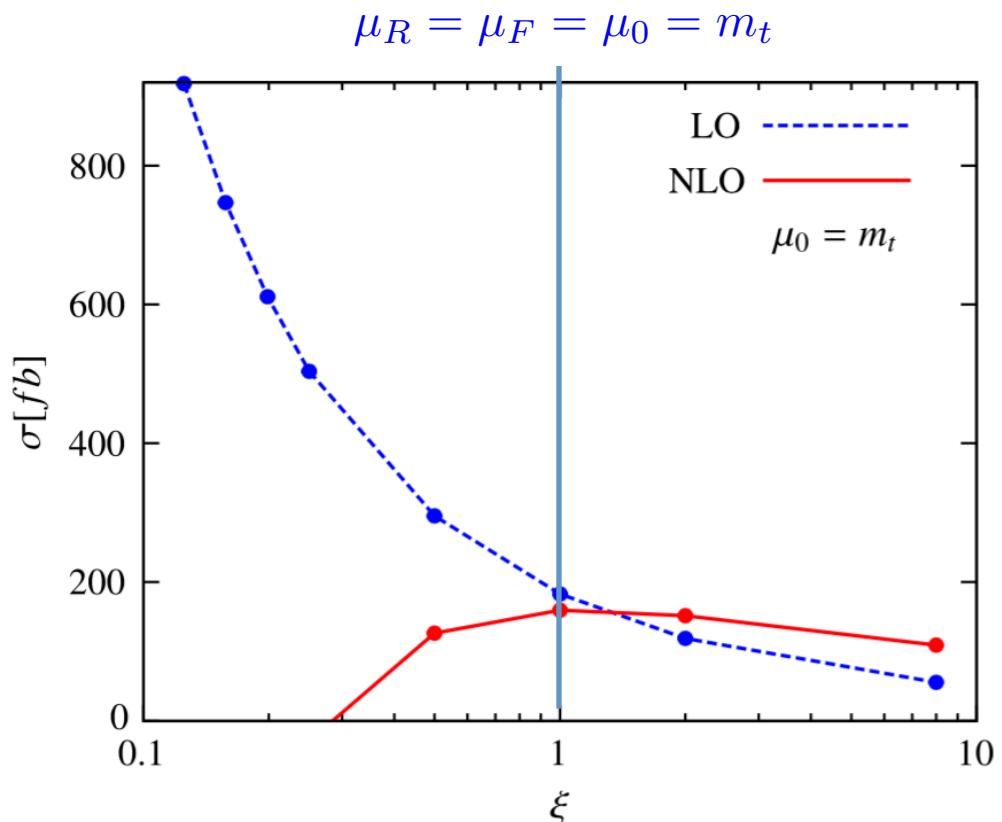
# Scale Dependence

- Total cross section @ LHC with 8 TeV (MSTW2008 PDF)



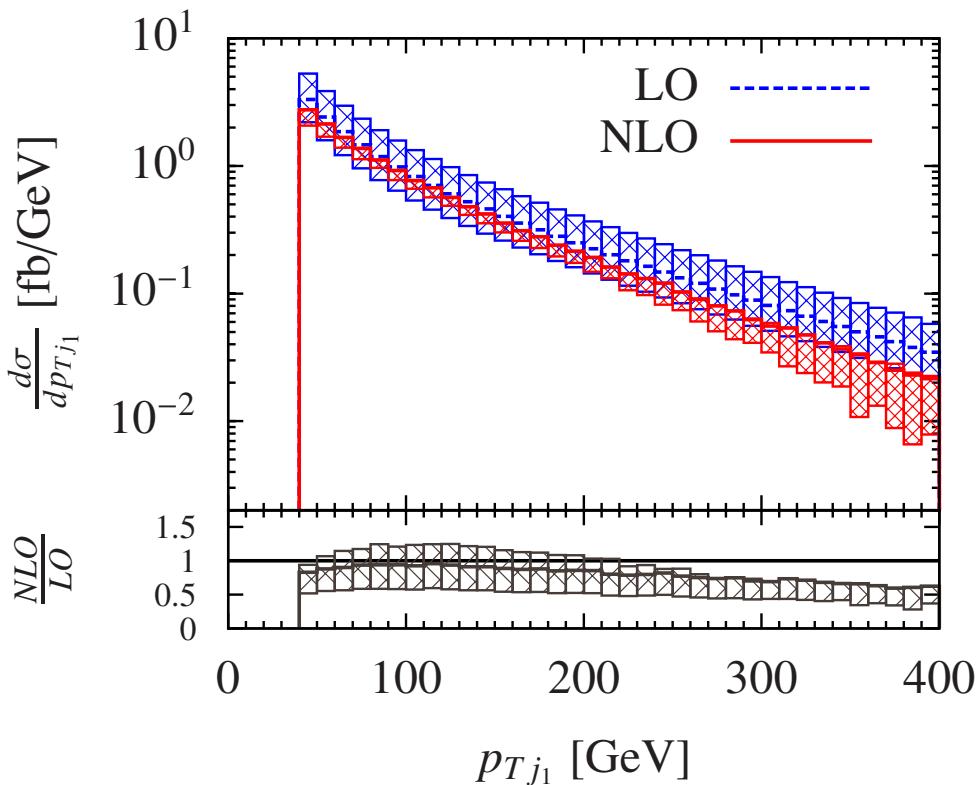
$\sigma_{\text{HELAC-NLO}}^{\text{LO}} = 183.1^{+112.2(61\%)}_{-64.2(35\%)} \text{ fb},$ 
 $\sigma_{\text{HELAC-NLO}}^{\text{NLO}} = 159.7^{+33.1(21\%)}_{-7.9(5\%)} \text{ fb}.$

- NLO corrections: -13%
- Theoretical uncertainties:
  - ★ 61% (48%) @ LO
  - ★ 21% (13%) @ NLO



# Hardest Light-Jet

- Upper panel: distributions and scale dependence bands:  $\{0.5m_t, m_t, 2m_t\}$
- Lower panel: differential K-factor

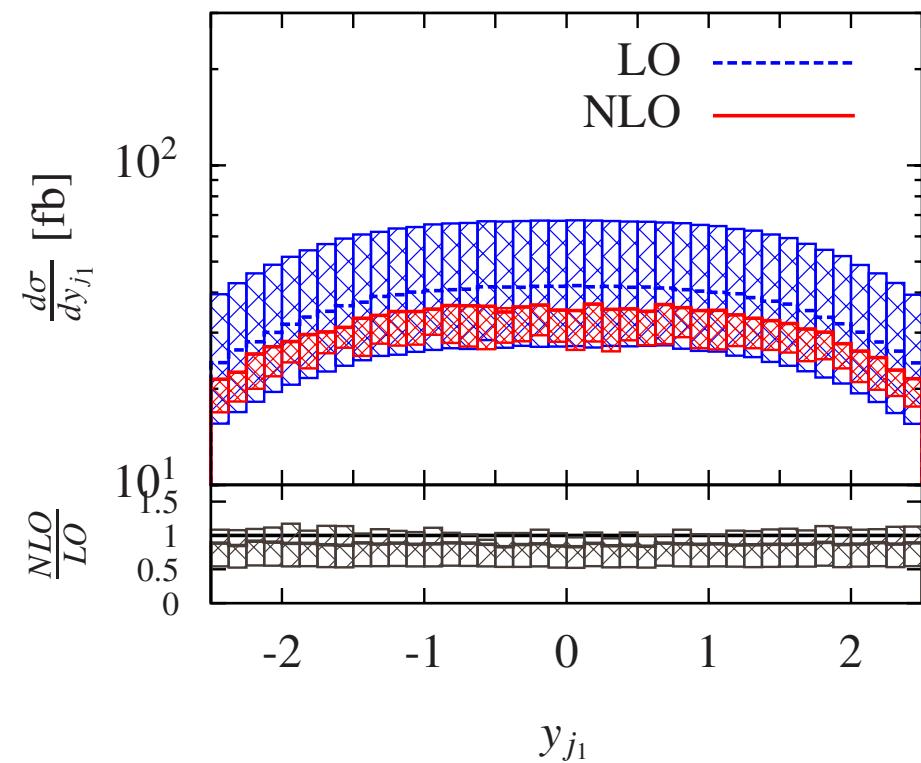


- NLO do not rescale shape of LO
- Distortions up to 50% with  $\mu_0 = m_t$
- Properly described only via NLO
- Negative NLO in  $p_T$  tails  
→ LO higher than NLO
- The *dynamic scale should depend on hardest jet  $p_T$*  ↑
- Asymptotic freedom →  $\alpha_s \downarrow$  in tails
- Dependence on  $\alpha_s$  @ LO >> @ NLO
- Would drive positive NLO/LO ratio in this region

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} j + X$$

# Hardest Light-Jet

- Upper panel: distributions and scale dependence bands
- Lower panel: differential  $K$ -factor

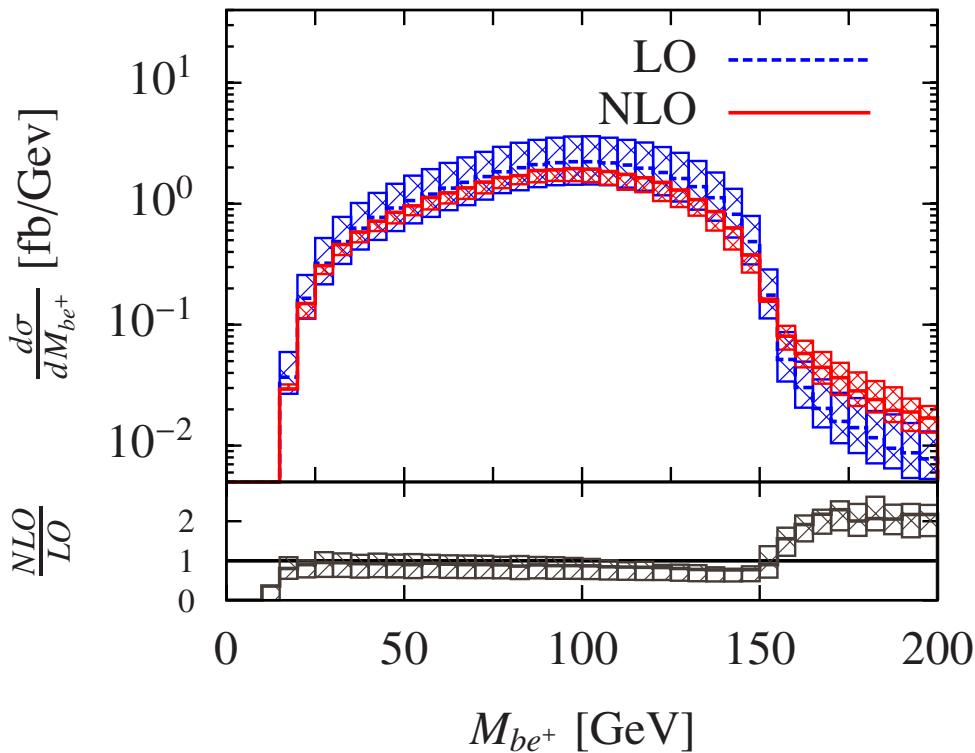


- Negative, moderate but ... quite stable NLO corrections
- Dimensionless nature of  $y_j$
- Receives contributions from various scales → also from these sensitive to threshold for  $t\bar{t}j$  production
- For  $\mu_0 = m_t$  effects of phase-space regions close to  $t\bar{t}j$  threshold dominate

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}j + X$$

# Lepton and $b$ -Jet

- Upper panel: distribution and scale dependence bands
- Lower panel: differential  $K$ -factor
- $be^+$  pair that returns the smallest invariant mass



$$M_{be^+} = \sqrt{m_t^2 - m_W^2} \approx 153 \text{ GeV}$$

- If both top and W decay on-shell  
→ end-point given by sharp cut
- Additional radiation & off-shell effects introduce smearing
- Highly sensitive to the details of the description of the process



# *Summary*

- Complete description for  $t\bar{t}j$  process with “resonant” and “non-resonant” contributions at NLO QCD
- First calculation of  $2 \rightarrow 5$  process with HELAC-NLO
- Further studies are needed:
  - ★ Look for judicious choice of a dynamical scale
  - ★ PDF uncertainties
  - ★ Bottom-mass effects
  - ★ Off-shell effects for differential distributions (comparison to NWA)
- Phenomenological applications  $\rightarrow m_t$  extraction
- Shape-based  $m_t$  measurement relies on precise modeling of differential distributions
- $m_t$  extraction  $< 1 \text{ GeV}$   $\rightarrow$  Predictions should go beyond simple approximation of factorizing top production & decays

# Outlook

- Alternative method for  $m_t$
- $m_t$  from normalized differential cross section for  $t\bar{t}j$

*S. Alioli, et al. '13*

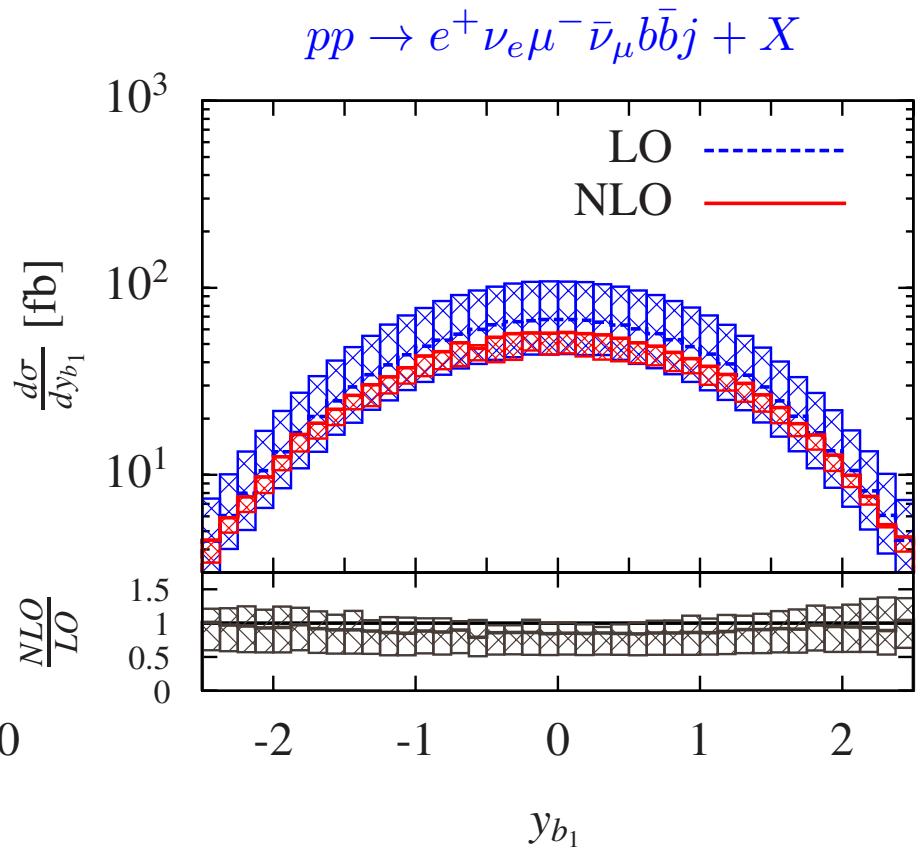
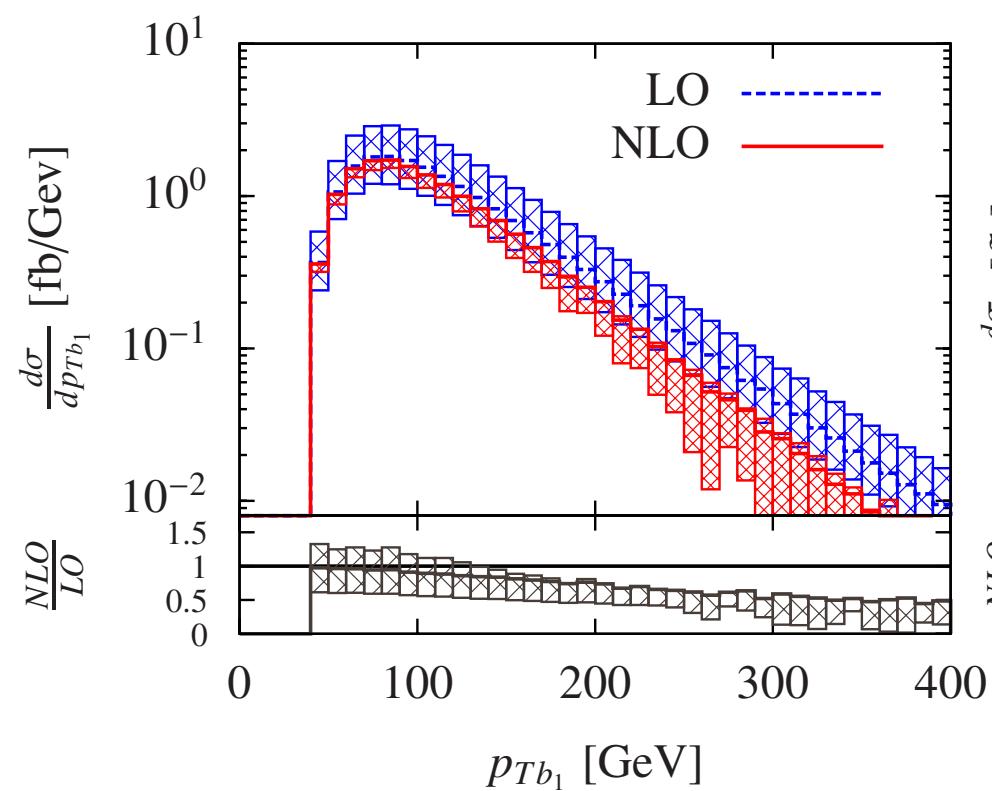
$$\mathcal{R}(m_t^{\text{pole}}, \rho_s) = \frac{1}{\sigma_{t\bar{t}+1\text{-jet}}} \frac{d\sigma_{t\bar{t}+1\text{-jet}}}{d\rho_s}(m_t^{\text{pole}}, \rho_s),$$
$$\rho_s = \frac{2m_0}{\sqrt{s_{t\bar{t}+1\text{-jet}}}},$$

- $\mathcal{R}$  has been calculated using  $t\bar{t}j$  @ NLO + POWHEG matched with PYTHIA  
→ top-quark decays via PS only with spin correlations @ LO
- Theoretical uncertainties & PDF uncertainties should affect  $m_t$  extraction  $< 1 \text{ GeV}$
- **For now:** *ATLAS @ 7 TeV:  $m_t = 173.7 \pm 2.2 \text{ GeV}$*  *ATLAS, arXiv:1507.01769*
- Worth looking at with complete off-shell effects included...

*Backup slides...*

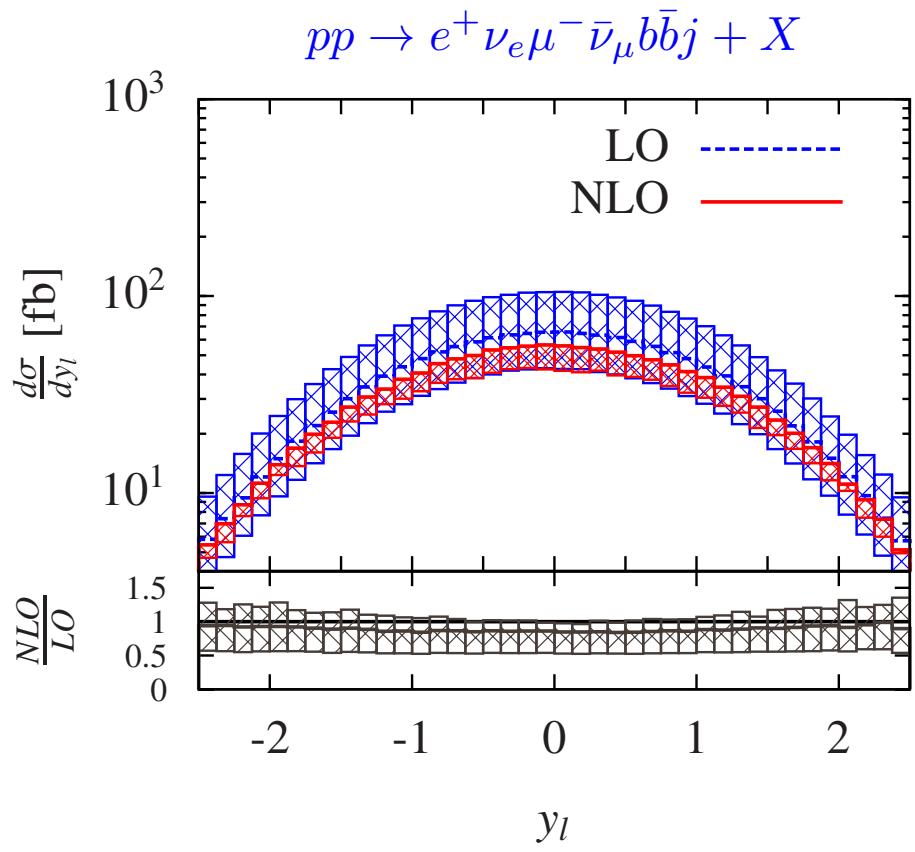
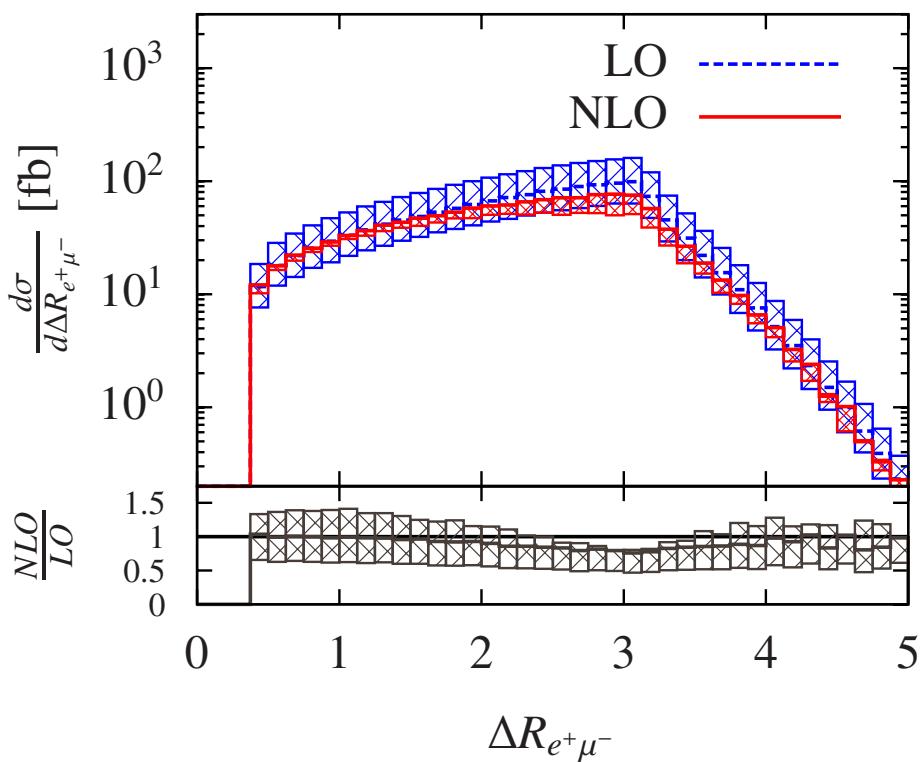
# *b-Jet*

- Upper panels: distributions and scale dependence bands
- Lower panels: differential *K*-factors



# Leptons

- Upper panels: distributions and the scale dependence bands
- Lower panels: differential  $K$ -factors



G. Bevilacqua, H. B. Hartanto, M. Kraus, M. Worek '16

# NWA for $t\bar{t}j$

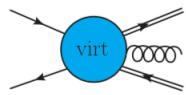
- Inclusive NLO  $\sigma(t\bar{t}j)$  in NWA convolution of production  $\sigma(t\bar{t}+nj)$  &  $\Gamma(t\bar{t}+nj)$   $n \leq 2$

$$d\sigma_{\text{incl}} = \Gamma_{t,\text{tot}}^{-2} (d\sigma_{t\bar{t}+0j} + d\sigma_{t\bar{t}+1j} + d\sigma_{t\bar{t}+2j} + \dots) \\ \otimes (d\Gamma_{t\bar{t}+0j} + d\Gamma_{t\bar{t}+1j} + d\Gamma_{t\bar{t}+2j} + \dots).$$

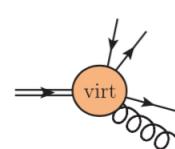
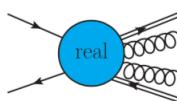
K. Melnikov, M. Schulze '12

- Expanded version with terms up to  $\alpha_s^4$  only

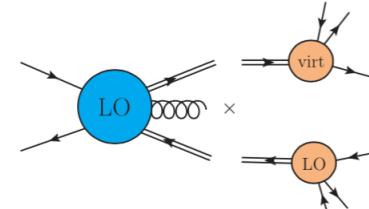
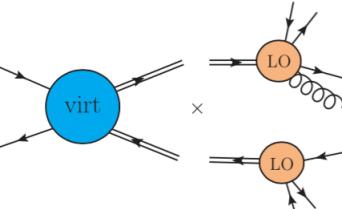
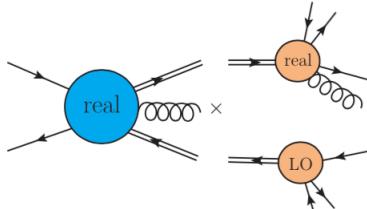
$$d\sigma_{t\bar{t}+1j}^{\text{NLO}} = \Gamma_{t,\text{tot}}^{-2} (d\sigma_{t\bar{t}+1j}^{\text{LO}} d\Gamma_{t\bar{t}}^{\text{LO}} + d\sigma_{t\bar{t}}^{\text{LO}} d\Gamma_{t\bar{t}+1j}^{\text{LO}} + \underbrace{(d\sigma_{t\bar{t}+1j}^{\text{virt}} + d\sigma_{t\bar{t}+2j}^{\text{real}}) d\Gamma_{t\bar{t}}^{\text{LO}}}_{(a)} + \underbrace{d\sigma_{t\bar{t}}^{\text{LO}} (d\Gamma_{t\bar{t}+1j}^{\text{virt}} + d\Gamma_{t\bar{t}+2j}^{\text{real}})}_{(b)} \\ + \underbrace{d\sigma_{t\bar{t}+1j}^{\text{real}} d\Gamma_{t\bar{t}+1j}^{\text{real}} + d\sigma_{t\bar{t}}^{\text{virt}} d\Gamma_{t\bar{t}+1j}^{\text{LO}} + d\sigma_{t\bar{t}+1j}^{\text{LO}} d\Gamma_{t\bar{t}}^{\text{virt}}}_{(c)}).$$



(a) jet emission in production

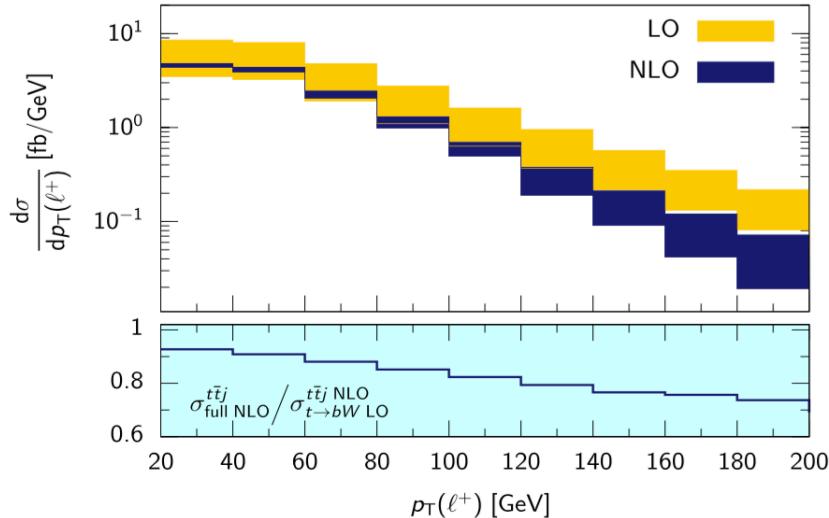


(b) jet emission in decay



(c) mixed contribution

# *NWA for $t\bar{t}j$*



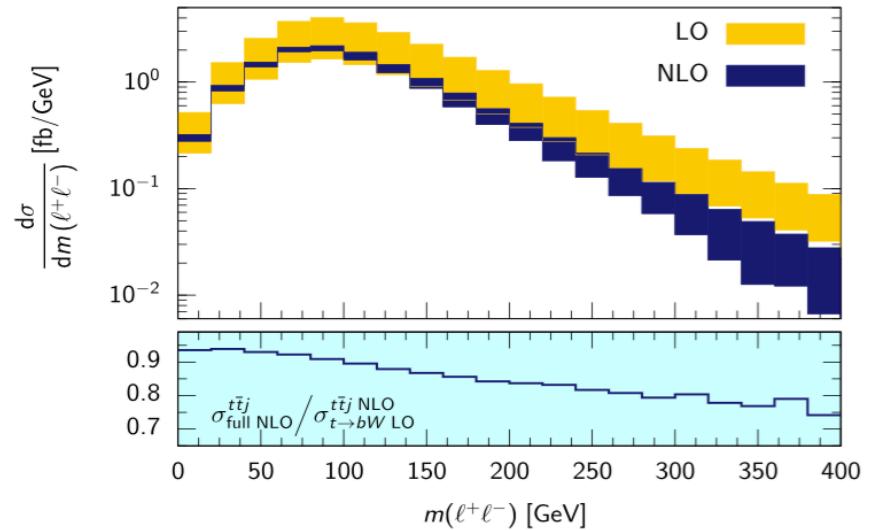
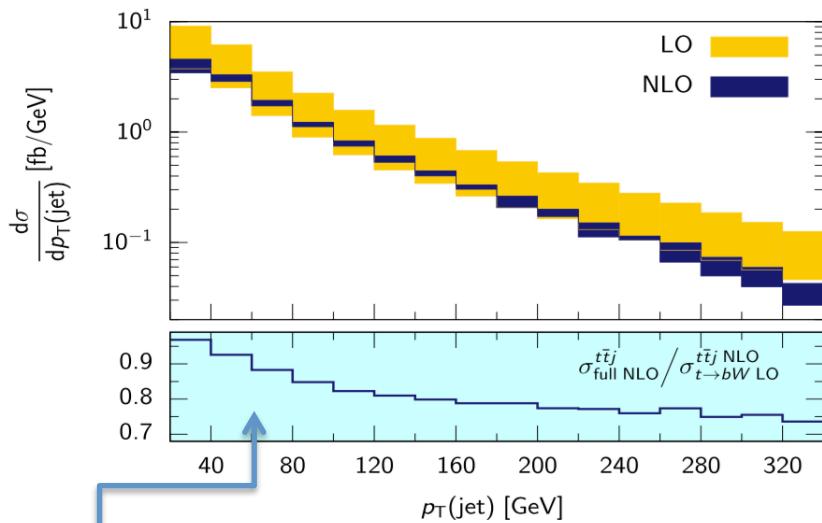
LHC @ 7 TeV with inclusive cuts

$$\sigma_{\text{LO}} = 316.9(\text{Pr}) + 33.4(\text{Dec}) = 350.3 \text{ fb},$$

$$\sigma_{\text{NLO}} = 323(\text{Pr}) + 40.5(\text{Dec}) - 75.5(\text{Mix}) = 288 \text{ fb}.$$

$\longleftrightarrow$   $14\%$   $\longleftrightarrow$   $26\%$

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Full NWA versus NWA with LO decays