Proton Parton Distribution Functions, LHC and HERA input

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- Motivation LHC high precision channels
- PDF extraction procedure, HERA input.
- Predictions for LHC
- Conclusions and Outlook.

LHC Discovery channels

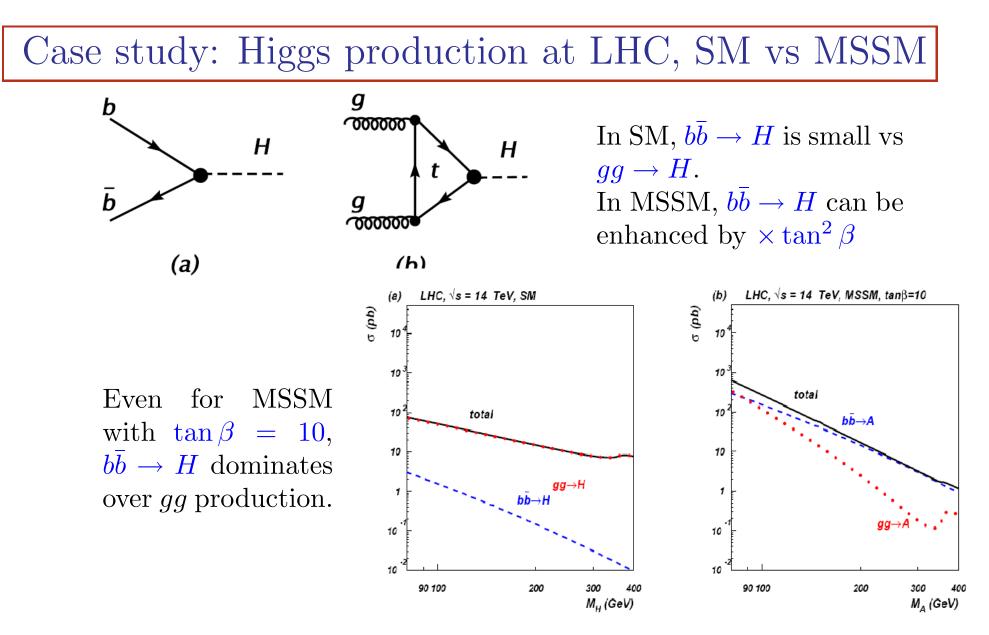
An (incomplete) list of channels to be searched at LHC

- Peak in invariant mass distribution $M_{\ell\ell}$ for high momentum leptons (Drell-Yan processes).
- Large missing p_{\perp} escaping LSP. Modeling of QCD background is the main issue.
- High p_{\perp} jets large systematic uncertainties.
- Higgs in various decay modes $(\gamma\gamma, WW \dots)$.

For experimental signatures with leptons in the final state few percent experimental counting precision is feasible (including $H \rightarrow \gamma \gamma$).

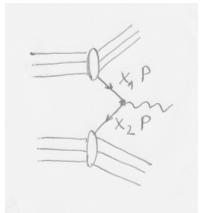
On the theory side, precision calculation are available for SM Drell-Yan processes.

Higgs production cross section is calculable to $\sim 10\%$ in SM, very different for little Higgs models, $\sim 10\%$ different for MSSM.



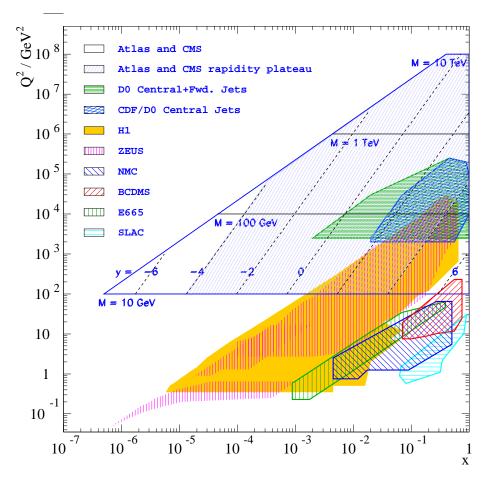
 \rightarrow production cross section measurement of Higgs is a key ingredient to disentangle new physics scenarios.





 x_1, x_2 are momentum fractions. Factorization theorem states that cross section can be calculated using universal partons \times short distance calculable partonic reaction.

$$x_{1,2} = \frac{M}{\sqrt{S}} \exp(\pm y)$$



Notation clash: y – rapidity (LHC) vs y – inelasticity (HERA, $Q^2 = Sxy$).

LHC and luminosity measurement

For a hadron collider, there is no good minimum bias QED (like $ep \rightarrow ep\gamma$) reference process which can be predicted/measured with high precision.

A better way is to normalize rate of a process of interest to a high p_{\perp} process which is calculated/can be measured with high accuracy.

The best candidates for the reference is W, Z production:

- Have high rate even at low luminosity (few Hz)
- Calculated to **NNLO** (2% precision)
- Can be measured via leptonic decays up to 1-2% precision (Z in the central rapidity region).

The Bjorken x range for W, Z production measured at |y| < 2.5is 0.0005 - 0.05; for H production with $m_H \sim 140$ GeV is 0.001 - 0.02

PDF determination

$$\frac{d^2 \sigma_{e^{\mp p}}^{NC}}{dx dQ^2} = \frac{2\pi \alpha^2 Y_+}{xQ^4} \left(F_2 - \frac{y^2}{Y_+} F_L \pm \frac{Y_-}{Y_+} xF_3 \right) \quad Y_{\pm} = 1 \pm (1-y)^2$$

Leading order relations:

$$F_{2} = x \sum e_{q}^{2}(q(x) + \bar{q}(x))$$

$$xF_{3} = x \sum 2e_{q}a_{q}(q(x) - \bar{q}(x))$$

$$\sigma_{e^{+}p}^{CC} \sim x(\bar{u} + \bar{c}) + x(1 - y)^{2}(d + s)$$

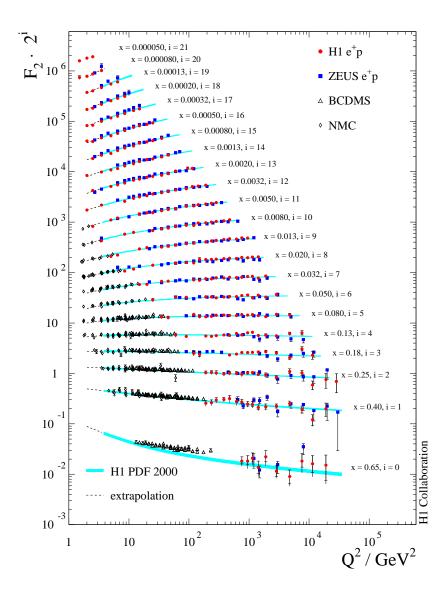
$$\sigma_{e^{-}p}^{CC} \sim x(u + c) + x(1 - y)^{2}(\bar{d} + \bar{s})$$

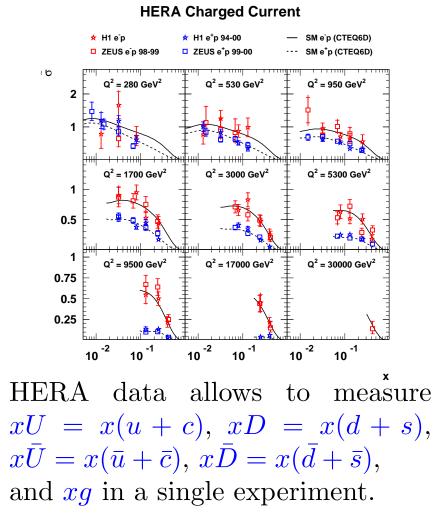
$$pp \to (\ell \bar{\ell})X \sim \sum x_{1}x_{2}q(x_{1})\bar{q}(x_{2})$$

DIS ep and ed data allows to unfold individual quark flavors. Drell-Yan data assists in determination of \overline{q} content.

Gluon is determined from F_2 scaling violation and from pp jet cross section.

The Measured Cross Sections





Treatment of experimental data

$$\chi^{2}(\{p\},\{\alpha\}) = \sum_{i} \frac{\left[F_{2}(p) - \left(F_{2}^{i} + \sum_{j} \frac{\partial F_{2}^{i}}{\partial \alpha_{j}} \alpha_{j}\right)\right]^{2}}{\sigma_{F_{2}}^{2}} + \sum_{j} \frac{\alpha_{j}^{2}}{\sigma_{\alpha_{j}}^{2}}.$$

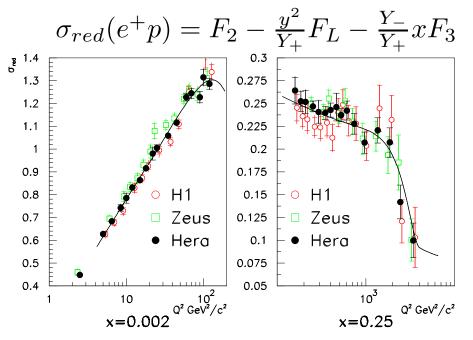
- p are parameters used to describe PDFs,
- α_j systematic uncertainty source j
- $F_2(p)$ theoretical prediction for F_2
- F_2 central value of the measured F_2
- σ_{F_2} statistical uncertainty of F_2
- σ_{α_i} uncertainty on systematic source j

Systematic uncertainties, including absolute normalizations of the data sets, are varied together with the PDF parameters. In some fits (CTEQ, H1) systematics is fitted, in others (MRST,ZEUS) central values are fixed. All fits float absolute normalizations.

Combination of Experimental Data

Before fitting to theory one can combine data in a generalized averaging procedure. Achieved by fitting χ^2 vs F_2 .

- Number of the fit parameters is equal to number of x, Q^2 points — large matrix inversion.
- + Simple quadratic dependence χ^2 unique and simple solution.



Average of H1 and Zeus data: model independent check of the consistency, $\chi^2/ndf = 534/601$. Experiments cross calibrate each other \rightarrow systematic errors reduced.

Extraction of Parton Densities

<u>Parameterization</u> of PDFs at starting scale (CTEQ case):

 $xf(x, Q_0^2) = Ax^B(1-x)^C e^{Dx}(1+Ex)^F$

For simplest minimal form D = E = F = 0. <u>Momentum sum rule:</u> $\int x (\Sigma(x) + g(x)) dx = 1$, <u>Assumptions:</u> $s = \bar{s} = 0.2(\bar{u} + \bar{d}), B_u = B_{\bar{u}} = B_d = B_{\bar{d}}$ Recent global fits follow different approaches in details:

Alekhin – NNLO DIS and DY MRST and ZEUS – float data normalizations only CTEQ and H1 – float data normalizations and syst. sources H1 – minimum set of parameters for PDFs to get good χ^2 CTEQ – maximum set of parameters still getting stable fit

 \rightarrow an estimate of the uncertainty should use errors provided by different groups but also compare central values.

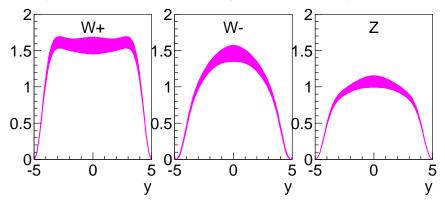
PDF predictions with uncertainties

The PDFs resulting from QCD fits are given by $N_P \sim 20$ parameters which are highly correlated among each other.

All major QCD fits provide PDF set not only for the central value, but also for diagonalized uncertainties. The uncertainty on quantity X can be calculated as

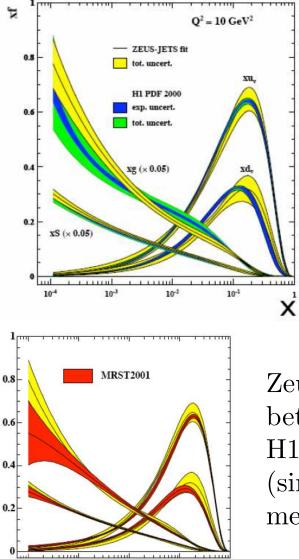
$$\Delta X = \frac{1}{2} \sqrt{\sum_{i=1}^{N_p} \left[X(S_i^+) - X(S_i^-) \right]^2}$$

where $X(S_i^{\pm})$ are the predictions based on the PDF eigenvector basis. (see e.g. hep-ph/0201195).



 $\leftarrow \text{PDF uncertainties for} \\ W, Z \text{ production based on} \\ \text{CTEQ set.} \end{cases}$

PDFs extracted by various groups



10-3

10-4

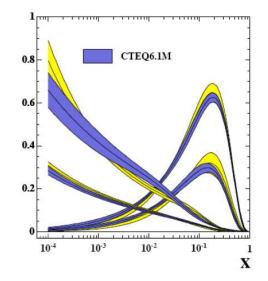
10-2

 10^{-1}

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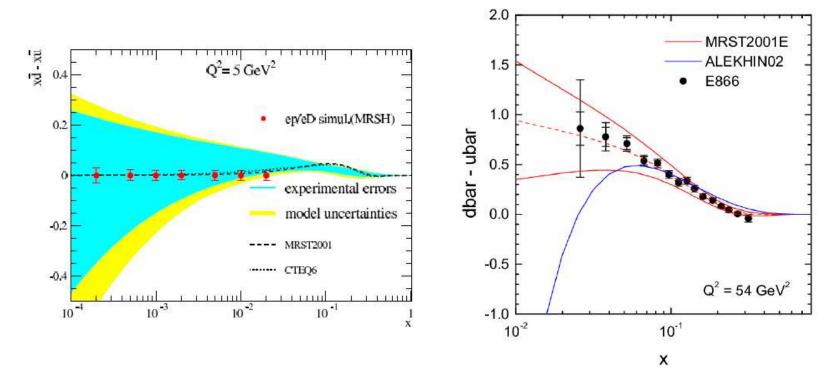
Zeus and H1 PDFs using their own data. Agree within the uncertainties.

Zeus gluon agrees better with MRST, H1 — with CTEQ. (similar data treatment ?).



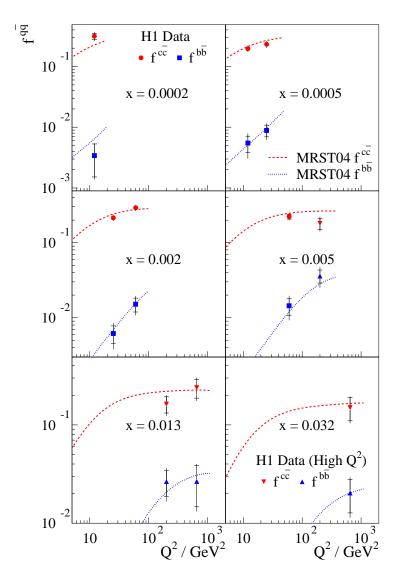
Effect of PDF constraints

Warning: relaxing low x constraints leads to large variations of PDFs



Could have been measured with ed run at HERA. Can be studied using Drell-Yan at LHC. For now assume conventional low x shape.





Sea decomposition can be studied using structure function data with tagged leading particle, using for example c, b long life times.

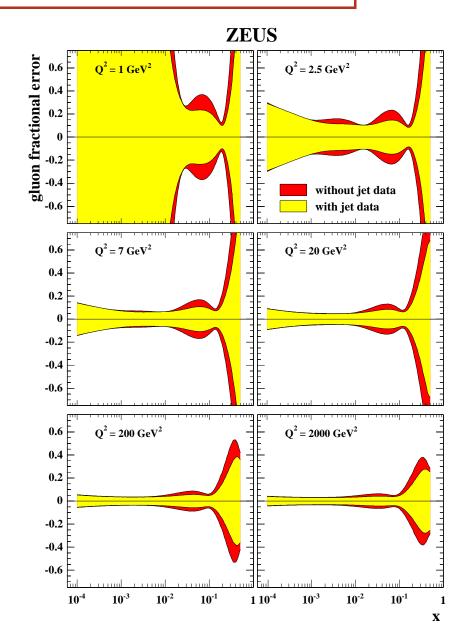
These measurements will benefit from larger HERA-II statistics. ZEUS joints H1, both detectors are now equipped with silicon vertex detectors.

Reducing Gluon uncertainties – high x

Global PDF fits (CTEQ, MRST) include Tevatron jet data to extract g(x) for high x. The data from Tevatron suffers from large systematic uncertainties (jet energy scale).

Recently Zeus collaboration included their jet data in the QCD fit.

Note that NNLO theoretical predictions are needed to make full use of the data. Pure NNLO fits (e.g. Alekhin) don't use jets data for now.

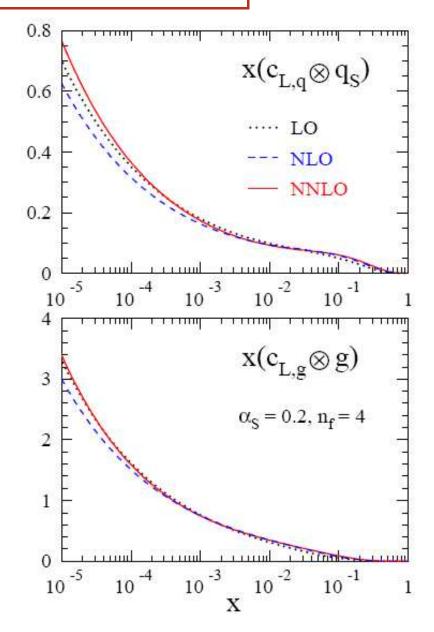


Low x Gluon and F_L predictions

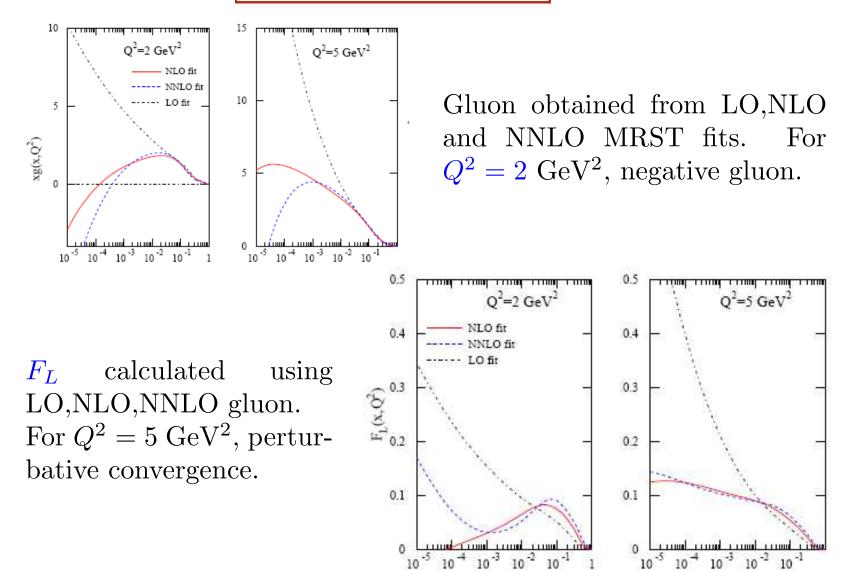
In QPM, $F_L = 0$ To lowest order of DGLAP at low x, F_L can be solved approximately.

 $xg(x) \approx \frac{8.3}{\alpha_S} F_L(0.4x)$

Recently NNLO coefficient functions has been calculated. Rather large variation from NLO to NNLO, but the same fixed PDFs are used for the plot.



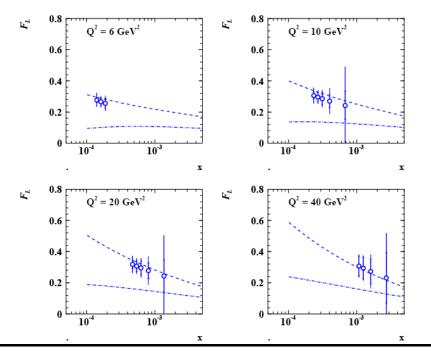


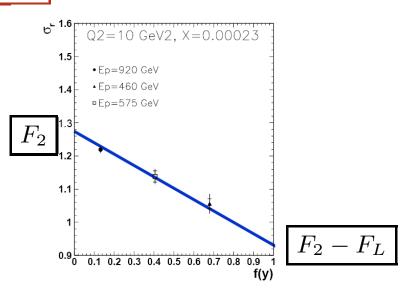


F_L measurement

$$\sigma_r(x, Q^2) = F_2(x, Q^2) - f(y)F_L(x, Q^2)$$

Measure σ_r at the same Q^2, x for different beam energies

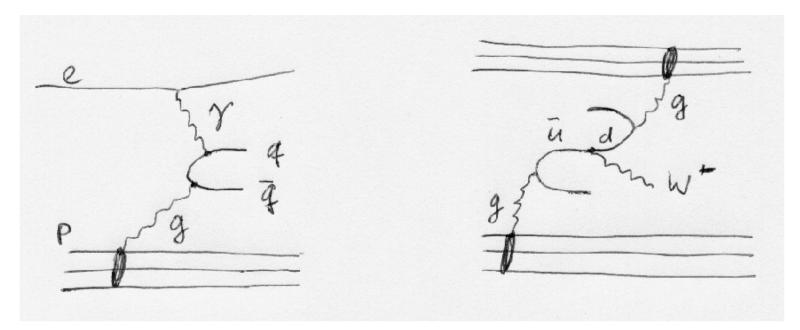




Measurement based on 10 pb⁻¹ run at $E_p = 460$ GeV allows to distinguish between different PDF fits (MRST vs CTEQ).

Measurement of F_L is planed for last 3 months of HERA operation

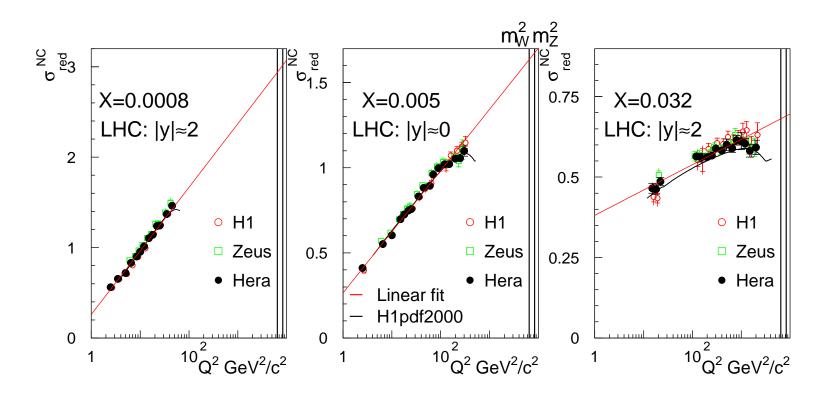
W, Z production at LHC



At low x similar boson-gluon fusion leading diagram for DIS and Drell-Yan.

One needs relation from $F_2 \sim 4/9U(x) + 1/9D(x)$ to $|V_{ud}|^2 \bar{u}(x_1) d(x_2) + |V_{cs}|^2 \bar{c}(x_1) s(x_2)$ for $W^ |V_{ud}|^2 \bar{d}(x_1) u(x_2) + |V_{cs}|^2 \bar{s}(x_1) c(x_2)$ for W^+ $\bar{u}(x_1) u(x_2) + \bar{u}(x_2) u(x_1) + \dots$ for Z

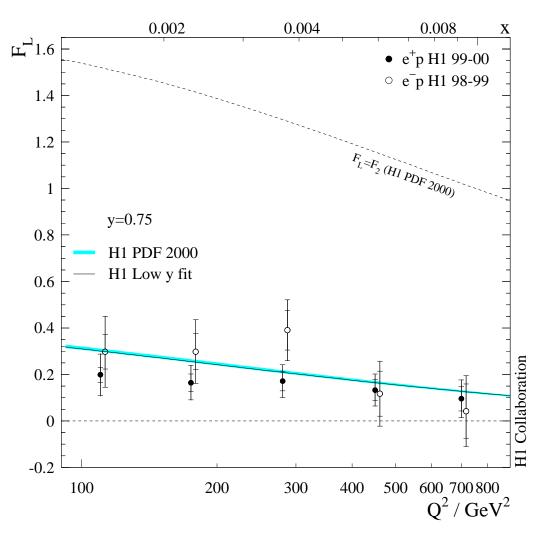
F_2 extrapolation to W, Z mass



HERA data covers complete central rapidity range of LHC for W, Z production. "Leading order" predictions can be read directly from HERA data + linear extrapolation.

Experimental part of PDF uncertainties comes from absolute F_2 normalization and the slope, $dF_2/d \log Q^2$ (gluon). Turn down of σ_{red}^{NC} for highest Q^2 (\rightarrow highest y) is due to F_L .

Consistency check: H1 F_L determination at high Q^2

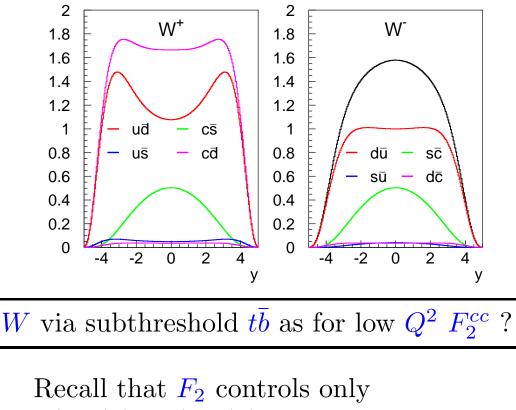


Determination of F_L as $F_L = \frac{Y_+}{y^2} \left(F_2^{fit} - \sigma_r \right)$

Important consistency check of gluon determined from F_2 scaling violation vs X-section decrease at high y.

Still large statistical uncertainties, to be improved with HERA-II

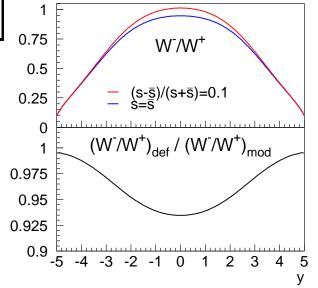
W production flavor decomposition



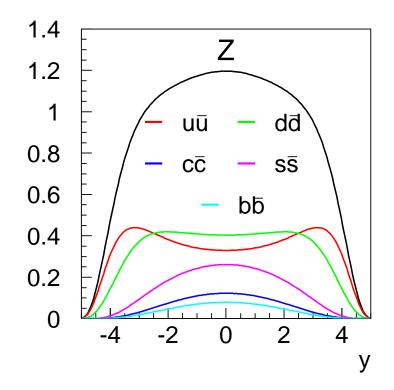
u, d, s, c quarks contribute to W^{\pm} production. Cabibbo enhanced sea $c\bar{s}$, $s\bar{c}$ by ~ 25\%, Cabibbo sea suppressed by $\sim 5\%$.

4/9U(x) + 1/9D(x), change in sea sym-

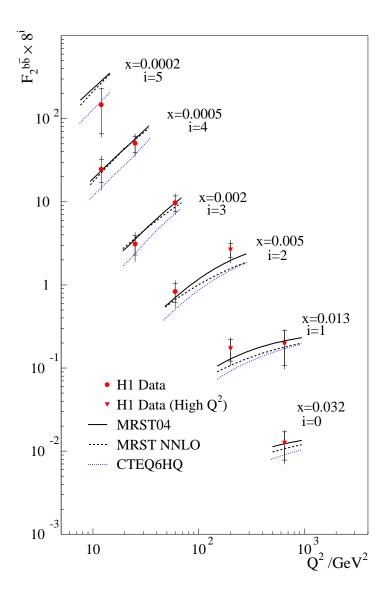
metry assumption leads to significant W^-/W^+ rate change while F_2 is not modified.

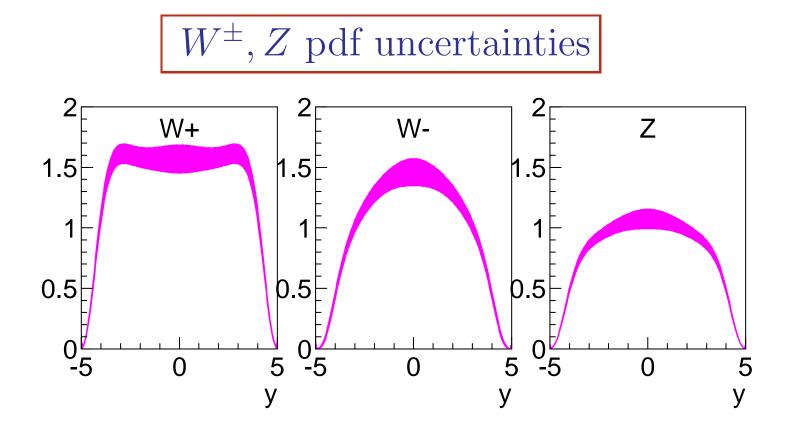


Z production flavor decomposition



Larger coupling to Z vs γ makes $b\bar{b}$ contribution more important for Z production vs inclusive F_2 . Still, F_2^{bb} is measured at HERA.



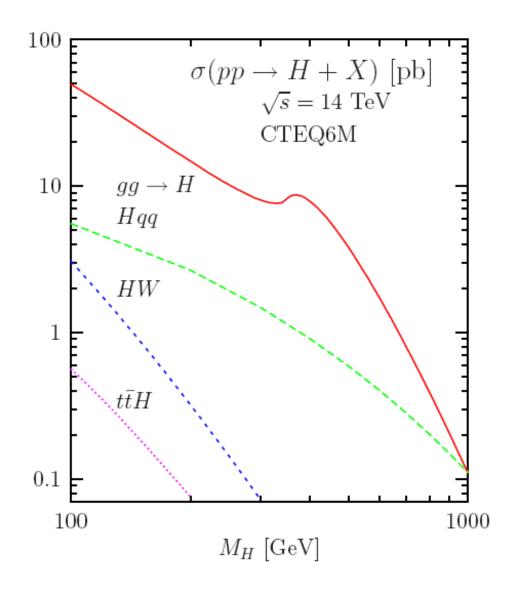


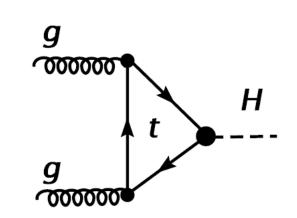
Current PDF uncertainties are $\sim 7\%$ (CTEQ). Without HERA data: > 20%.

7% is large compared to 2% theory and ultimately $\sim 2\%$ experimental precision at LHC.

 \rightarrow need for more precise HERA data for 0.001 < x < 0.03 kinematic domain.

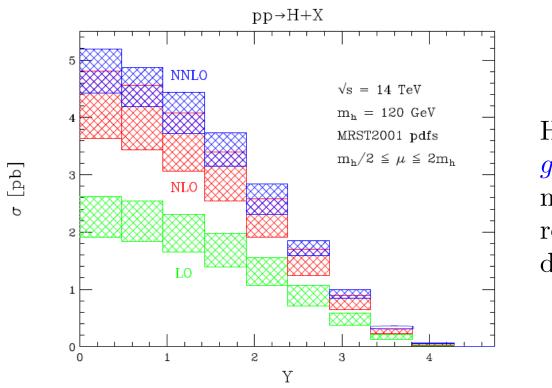
SM Higgs production





In SM, for light Higgs boson the dominant production mechanism is $gg \rightarrow H$.

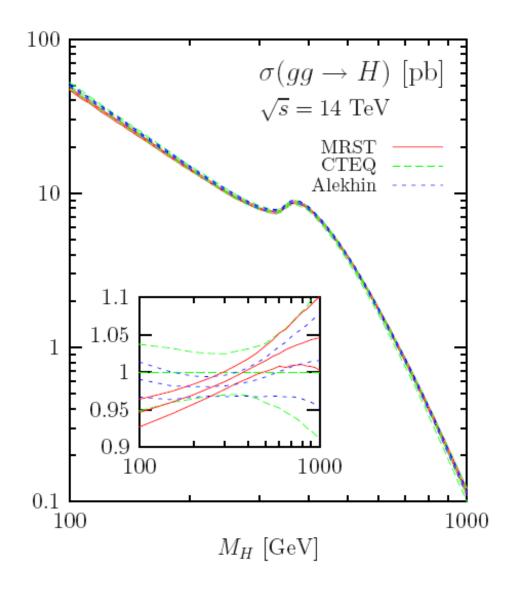
Higgs production NNLO predictions



Higgs production via $gg \rightarrow H$ receives significant positive corrections for higher orders.

Still relatively large renormalization scale uncertainty (~ 10%) even at NNLO. Larger uncertainties for H vs W, Z are similar to larger uncertainties of F_L vs F_2 , – larger sensitivity to gluon.

Higgs PDF uncertainties



PDF uncertainties for $gg \rightarrow H$ are about $\sim 8\%$ taking into account difference between central values for different PDFs.

HERA-II for LHC: What next?

LHC needs improvement of PDF determination for W, Zproduction and better understanding of gluon for Higgs production.

- $\times 5$ increase in statistics expected at HERA-II should allow to reduce uncertainties for F_2 at $Q^2 > 1000 \text{ GeV}^2$ by about factor of 2.
- For $Q^2 < 100 \text{ GeV}^2$, 2 3% uncertainty is already achieved at HERA-I. Detailed studies of systematic uncertainties show that the errors could be reduced to 1 - 1.5% level.
- Direct measurement of F_L with a low energy run will provide an important constraint for gluon at low x; theory self consistency check in a complicated low x, Q^2 domain.
- Indirect determination of $F_L \sim F_2^{QCD} \sigma_{red}$ at high Q^2 will improve with increased statistics; provides gluon universality check for Q^2 , x values closer to LHC energy.

Still a lot of work at HERA but expected $\times 2$ improvement for W, Z production prediction and better control over theory.



- Precision PDFs are important for key measurements at LHC, in particular for the Higgs production cross section.
- Precision cross section measurements at LHC require measurements of SM W and Z production as a luminosity monitor.
- HERA measurement of the inclusive cross sections are vital for PDFs needed for LHC. Current precision on W,Zproduction cross section is about 7%.
- Further improvements in PDFs are expected. They should come from higher precision inclusive cross section data, from new measurements of gluon (F_L) , from complete NNLO fits, from more rigorous treatment of the data systematic uncertainties.