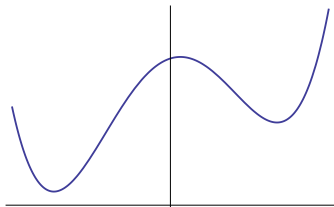


Dynamical D-term supersymmetry breaking

in particle physics and cosmology

[arxiv 1410.4641](#)



Valerie Domcke

SISSA, INFN Trieste

in collaboration with
K. Schmitz, T. Yanagida



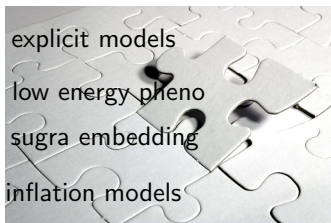
invisibles



Motivation

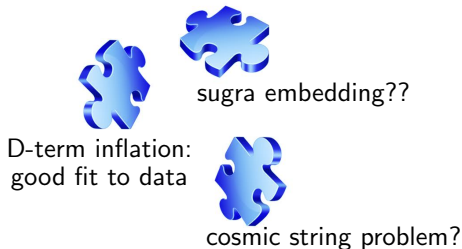
Two roads to spontaneous supersymmetry breaking:

$$\langle F \rangle \neq 0$$



O'Raifeartaigh models

$$\langle D \rangle \neq 0$$



Fayet Iliopoulos (FI) mechanism

This talk: D-terms in supergravity and their cosmology

The infamous D-term problems

D-term supersymmetry breaking in ...

- global supersymmetry: simple

[Fayet, Illiopoulos '74]

$$\mathcal{L}_{\text{FI}} = -g \xi D = -g \xi \int d^4\theta V, \quad \xi = \text{const.}$$

$$V_D = \frac{1}{2} D^2 = \frac{1}{2} g^2 (q_i |\phi_i|^2 - \xi)^2$$

- supergravity: very hard, global symmetries render theory inconsistent

[Komargodski, Seiberg '09/'10; Dienes, Thomas '10, Catino, Villadoro, Zwirner '12, ...]

- possible way out: field-dependent 'FI-term' ?

$$g \xi V \rightarrow f_{\text{GS}}(V + \Phi + \Phi^\dagger)$$

[Green, Schwarz '84]

$$\text{but stabilize modulus } \Phi \Rightarrow \xi \sim M_P^2$$

see also [Dumitrescu, Komargodski, Sudano '10, Catino, Villadoro, Zwirner '11]

This talk: Dynamical 'FI-term' generation in supergravity can overcome all of these problems.

Dynamical supersymmetry breaking

based on strong $SP(N_c)$ gauge group with $N_f = N_c + 1$ flavours.

minimal example: $SP(1) \simeq SU(2)$ [Izawa, Yanagida '96, Intriligator, Thomas '96].

- field content: 4 'quarks' $Q \xrightarrow{\Lambda} 6$ 'mesons' M ; 6 singlets Z
- deformed moduli constraint

$$Pf(M) = M_1 M_2 - M_3 M_4 + M_5 M_6 = \Lambda^2, [Pf(M)]^2 = \det(M)$$

- perturbative superpotential $W = \lambda_i \Lambda M_i Z_i$

$\Rightarrow$ Yukawas break flavour symmetry to $U(1)$, take all $\lambda_i \neq 0$

$\Rightarrow \langle M_i \rangle \neq 0 \rightarrow \langle F_{Z_i} \rangle \neq 0 \Rightarrow$ F-term susy breaking

scale Λ via dimensional transmutation:

$$\Lambda = M_P \exp\left(-\frac{8\pi^2}{b g_s(M_P)}\right)$$

$$\text{e.g. } g_s(M_P) = 1...4\pi \quad \rightarrow \quad \Lambda = 10^{10}..10^{18} \text{ GeV}$$

supersymmetry breaking by strong dynamics at scale Λ

Dynamical 'FI-term'

Weakly gauge a $U(1)$ subgroup of the flavour symmetry , $g \ll \lambda_i$

$$\begin{array}{c} \text{fields} \\ U(1) \end{array} \left\| \begin{array}{cccccc} & \overbrace{Q_1 \quad Q_2}^{M_+} & & \overbrace{Q_3 \quad Q_4}^{M_-} & Z_a^0 & Z_+ & Z_- \\ +1/2 & +1/2 & -1/2 & -1/2 & 0 & +1 & -1 \end{array} \right.$$

D-term potential:

$$V_D = \frac{1}{2} g^2 (|M_+|^2 - |M_-|^2 + \dots)^2$$

with $\langle M_{\pm} \rangle^2 \simeq \frac{\lambda_{\pm}}{\lambda_{\pm}} \Lambda^2$ (and if all other charged fields stabilized at zero):

$$\xi = \Lambda^2 \left(\frac{\lambda_+}{\lambda_-} - \frac{\lambda_-}{\lambda_+} \right) (1 - \mathcal{O}(g^2))$$

Generates effective FI-term at dynamical scale Λ

A modulus problem?

neutral fields: $\lambda_0 \gg \lambda_{\pm} \rightarrow \langle Z_a^0 \rangle = 0 = \langle M_a^0 \rangle$

charged mesons in unitary gauge: $M_{\pm} = (\langle M_{\pm} \rangle + M)e^{\pm S}$

- deformed moduli constraint eliminates M : $M_- = \Lambda^2/M_+$
- Goldstone multiplet S renders $U(1)$ vector multiplet massive

$$\begin{aligned} K &= M_+^\dagger e^{2gV} M_+ + M_-^\dagger e^{-2gV} M_- \\ &= K_0 + 2g \underbrace{(\langle |M_+|^2 \rangle - \langle |M_-|^2 \rangle)}_{-\xi} [V + (S + S^\dagger)/(2g)] + \dots \end{aligned}$$

charged singlets $X = \frac{1}{\sqrt{2}}(Z_+ + Z_-)$, $Y = \frac{1}{\sqrt{2}}(Z_+ - Z_-)$

- $\langle Y \rangle = 0$ (Dirac mass term with S)
- Goldstino multiplet X . Pseudo modulus stabilized at one-loop.

A modulus problem?

neutral fields: $\lambda_0 \gg \lambda_{\pm} \rightarrow \langle Z_a^0 \rangle = 0 = \langle M_a^0 \rangle$

charged mesons in unitary gauge: $M_{\pm} = (\langle M_{\pm} \rangle + M)e^{\pm S}$

- deformed moduli constraint eliminates M : $M_- = \Lambda^2/M_+$
- Goldstone multiplet S renders $U(1)$ vector multiplet massive

charged singlets $X = \frac{1}{\sqrt{2}}(Z_+ + Z_-)$, $Y = \frac{1}{\sqrt{2}}(Z_+ - Z_-)$

- $\langle Y \rangle = 0$ (Dirac mass term with S)
- Goldstino multiplet X . Pseudo modulus stabilized at one-loop.

$$W = \mu^2 X - mSY + \frac{m^2}{2\mu^2} S^2 X + \mathcal{O}(S^3),$$
$$m \sim \lambda\Lambda, \quad \mu^4 = 2\lambda_+\lambda_-\Lambda^4$$

A modulus problem?

neutral fields: $\lambda_0 \gg \lambda_{\pm} \rightarrow \langle Z_a^0 \rangle = 0 = \langle M_a^0 \rangle$

charged mesons in unitary gauge: $M_{\pm} = (\langle M_{\pm} \rangle + M)e^{\pm S}$

- deformed moduli constraint eliminates M : $M_- = \Lambda^2/M_+$
- Goldstone multiplet S renders $U(1)$ vector multiplet massive

charged singlets $X = \frac{1}{\sqrt{2}}(Z_+ + Z_-)$, $Y = \frac{1}{\sqrt{2}}(Z_+ - Z_-)$

- $\langle Y \rangle = 0$ (Dirac mass term with S)
- Goldstino multiplet X . Pseudo modulus stabilized at one-loop.

- 'modulus' S stabilized through F-terms.
- effective FI-term for $m_A \sim g\Lambda \ll E \ll m_S \sim \Lambda$
- supersymmetry breaking:
 $\langle F \rangle \sim \Lambda^2 > \langle D \rangle \sim g^2 \Lambda^2, \quad m_{3/2} \gtrsim \Lambda^2/M_P$

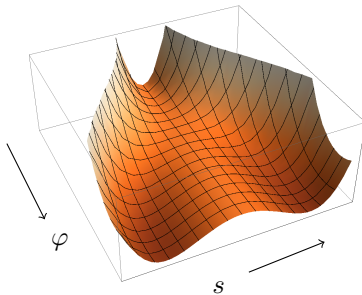
Applications in Cosmology and Particle Physics

D-term hybrid inflation: [Binetruy, Dvali '96; Halyo '96]

- $U(1)$ gauge symmetry with Fayet-Iliopoulos term ξ
- $W = \kappa \phi S_+ S_-$,

- ξ : vacuum energy
- ϕ : inflaton φ ,
tree-level flat
- $S_{\pm}$: waterfall field,
 $|S_+|$ destabilize at

$$\varphi_c = \frac{g}{\kappa} \sqrt{2\xi}$$

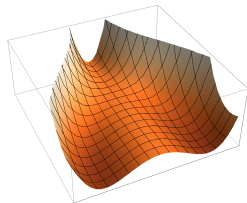


Main problems: FI-term inconsistent? Cosmic strings? n_s too large?

Dynamical D-terms for hybrid inflation

- here: cosmic string problem is avoided!
- F-term susy breaking in Minkowski vacuum after inflation
- Starobinsky limit and $m^2\phi^2$ limit

[Buchmüller, VD, Kamada '13], [Buchmüller, VD, Schmitz '14]



Outlook

- sparticle spectrum..
- $U(1)_{\text{FI}} \leftrightarrow G_{\text{GUT}}$

opens new roads for model building in
particle physics and cosmology

- dynamical susy breaking $\rightarrow$ dynamical D-term generation
- effective FI-term below dynamical scale Λ , $\Lambda \sim \Lambda_{\text{GUT}}$ possible
- gauge invariant in sugra, no moduli stabilization necessary
- F- and D-terms play a role: $\langle F \rangle > \langle D \rangle$
- one possible application: D-term inflation

[arxiv 1410.4641](#)

Thank you!

Questions?