

# The Higgs Singlet Extension at LHC Run 2

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based on

G.M. Pruna, TR (PRD 88 (2013) 115012)

D. Lopez-Val, TR (PRD 90 (2014) 114018)

TR, T. Stefaniak (EPJC (2015) 75:105, arXiv:1601.07880)

F. Bojarski, G. Chalons, D. Lopez-Val, TR (JHEP 1602 (2016) 147)

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# Higgs Singlet extension (aka The Higgs portal)

## The model

- Singlet extension:

**simplest extension of the SM Higgs sector**

- add an **additional scalar**, singlet under SM gauge groups  
(further reduction of terms: impose additional symmetries)

⇒ potential ( $H$  doublet,  $\chi$  real singlet)

$$V = -m^2 H^\dagger H - \mu^2 \chi^2 + \lambda_1 (H^\dagger H)^2 + \lambda_2 \chi^4 + \lambda_3 H^\dagger H \chi^2,$$

- **collider phenomenology studied by many authors:** Schabinger, Wells; Patt, Wilzcek; Barger ea; Bhattacharyya ea; Bock ea; Fox ea; Englert ea; Batell ea; Bertolini/ McCullough; ...
- our approach: **minimal:** no hidden sector interactions
- equally: **Singlet acquires Vev**

# Singlet extension: free parameters in the potential

$$\text{VeVs: } H \equiv \begin{pmatrix} 0 \\ \frac{\tilde{h} + v}{\sqrt{2}} \end{pmatrix}, \quad \chi \equiv \frac{h' + x}{\sqrt{2}}.$$

- potential: 5 free parameters: 3 couplings, 2 VeVs

$$\lambda_1, \lambda_2, \lambda_3, v, x$$

- rewrite as

$$m_h, m_H, \sin \alpha, v, \tan \beta$$

- fixed, free

$$\sin \alpha: \text{mixing angle, } \tan \beta = \frac{v}{x}$$

- physical states ( $m_h < m_H$ ):

$$\begin{pmatrix} h \\ H \end{pmatrix} = \begin{pmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} \tilde{h} \\ h' \end{pmatrix},$$

# Phenomenology (in the following: focus on $m_h \sim 125$ GeV)

- SM-like couplings of **light/ heavy** Higgs:  
**rescaled by  $\sin \alpha, \cos \alpha$**
- in addition: **new physics channel:  $H \rightarrow hh$**

$$\Gamma_{\text{tot}}(H) = \sin^2 \alpha \Gamma_{\text{SM}}(H) + \Gamma_{H \rightarrow hh},$$

- **SM like decays** parametrized by

$$\kappa \equiv \frac{\sigma_{\text{BSM}} \times \text{BR}_{\text{BSM}}}{\sigma_{\text{SM}} \times \text{BR}_{\text{SM}}} = \frac{\sin^4 \alpha \Gamma_{\text{tot,SM}}}{\Gamma_{\text{tot}}}$$

- **new physics channel** parametrized by

$$\kappa' \equiv \frac{\sigma_{\text{BSM}} \times \text{BR}_{H \rightarrow hh}}{\sigma_{\text{SM}}} = \frac{\sin^2 \alpha \Gamma_{H \rightarrow hh}}{\Gamma_{\text{tot}}}$$

# Theoretical and experimental constraints on the model

**our studies:**  $m_{h,H} = 125.09 \text{ GeV}$ ,  $0 \text{ GeV} \leq m_{H,h} \leq 1 \text{ TeV}$

- ① limits from **perturbative unitarity**
- ② limits from EW precision observables through  **$S$ ,  $T$ ,  $U$**
- ③ special: **limits from W-boson mass** as precision observable
- ④ **perturbativity** of the couplings (up to certain scales\*)
- ⑤ **vacuum stability and minimum condition** (up to certain scales\*)
- ⑥ **collider limits** using HiggsBounds
- ⑦ measurement of **light Higgs signal rates** using HiggsSignals and ATLAS-CONF-2015-044 [signal strength combination]

(debatable: minimization up to arbitrary scales,  $\Rightarrow$  perturbative unitarity to arbitrary high scales [these are common procedures though in the SM case])

(\*): only for  $m_h = 125.09 \text{ GeV}$

# Results

- strongest constraints:**

$m_H \gtrsim 800 \text{ GeV}$  : **perturbativity of couplings**

$m_H \in [270; 800] \text{ GeV}$  :  **$m_W$  @ NLO**

$m_H \in [175; 270] \text{ GeV}$  : **experimental searches**

$m_H \in [120; 175] \text{ GeV}$  : **signal strength**

$m_h \lesssim 120 \text{ GeV}$  : **SM-like Higgs coupling rates (+ LEP)**

$\Rightarrow \kappa \leq 0.25$  for all masses considered here

$$\Gamma_{\text{tot}} \lesssim 0.02 m_H$$

$\Rightarrow$  **Highly (??) suppressed, narrow(er) heavy scalars**  $\Leftarrow$

$\Rightarrow$  **new (easier ?) strategies needed wrt searches for SM-like Higgs bosons in this mass range**  $\Leftarrow$

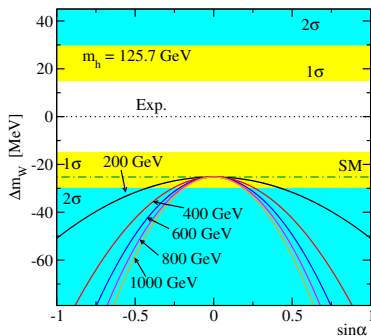
[width studies ( $\sim 2015$ ): cf. Maina ; Kauer, O'Brien; Kauer, O'Brien, Vryonidou; Ballestrero, Maina; Dawson,

# NLO corrections to $m_W$ (D. Lopez-Val, TR, PRD 90 (2014) 114018)

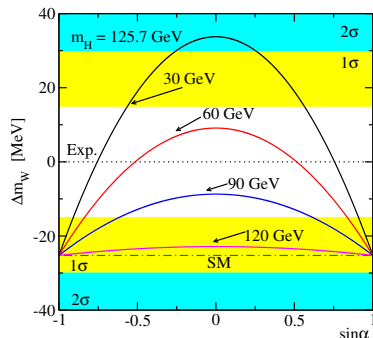
- electroweak fits: fit  $\mathcal{O}(20)$  parameters, constraining  $S, T, U$
- idea here: single out  $m_W$ , measured with error  $\sim 10^{-4}$
- **setup renormalization for Higgs and Gauge boson masses**
- EW gauge and matter sector: on-shell scheme
- Higgs sector: several choices, currently a mixture of onshell/  
 $\overline{MS}$   
(in this case:  $\delta\lambda$  only enter at 2-loop  $\implies$  not relevant here)
- first step on the road to full renormalization

# NLO corrections to $m_W$ (D. Lopez-Val, TR, PRD 90 (2014) 114018)

## Contribution to $m_W$ for different Higgs masses



$m_h = 125.7$  GeV

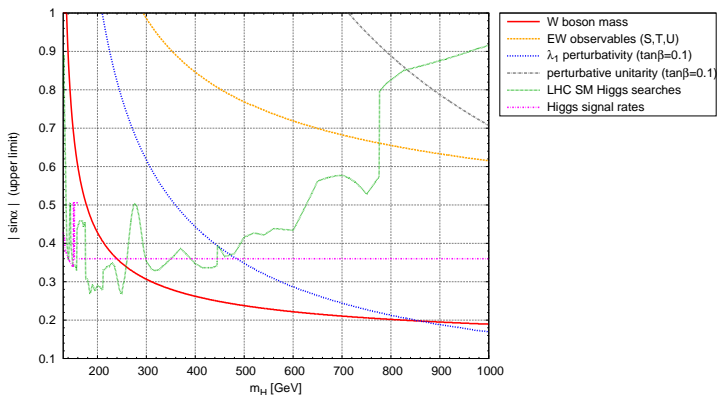


$m_H = 125.7$  GeV

$\Rightarrow$  low  $m_h$  bring  $m_W^{\text{NLO}}$  close to  $m_W^{\text{exp}}$   $\Leftarrow$



# Combined limits on $|\sin \alpha|$ (TR, T. Stefaniak, arXiv:1601.07880)



several bounds on  $|\sin \alpha|$

$m_W$ , perturbativity, LHC direct searches, Higgs Signal strength

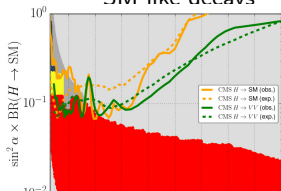
# Results from generic scans and predictions for LHC 14

(TR, T. Stefaniak, arXiv:1601.07880)

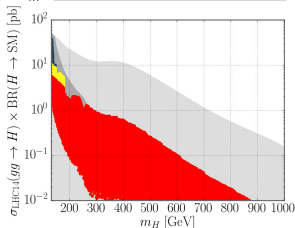
1  $\sigma$ , 2  $\sigma$ , allowed

SM like decays

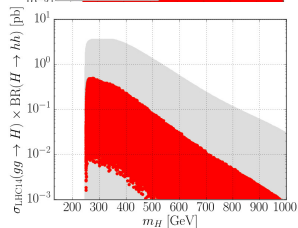
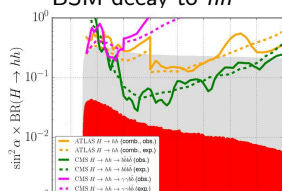
limits



pred.



BSM decay to  $hh$



# Full renormalization (1)

(F. Bojarski, G. Chalons, D. Lopez-Val, TR, JHEP 1602 (2016) 147)

- next topic: **full electroweak renormalization**
- many parts of ew sector: **follow SM prescriptions**
- **new:** renormalize

$$T_{h,H}; v; \kappa; m_{h,H}^2; Z_{h,H,hH,Hh}; m_{hH}^2$$

- ⇒ in total: **11 parameters in scalar sector**
- ⇒ need to be determined by **suitable renormalization conditions**

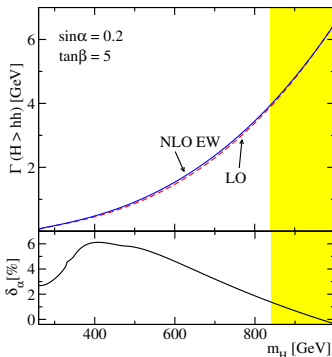
# Full renormalization (2)

## ⇒ Our choices ⇐

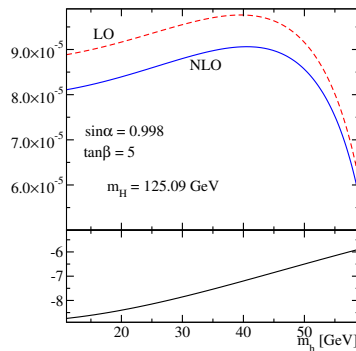
- Tadpoles:  $\delta T = -T [\hat{\tau}=0]$
- $v$ : as in SM, on-shell (ie through ew gauge sector)
- $\delta x = 0$  (not fixed by any measurement) !!! **choice** !!!  
[no UV-divergence ! ; Sperling ea, 2013]
- $\delta m_{h,H}, \delta Z_{H,h}$ : on-shell
- difficult part **off-diagonal terms**  $m_{hH}^2, \delta Z_{hH}$  !!
- we choose: **'improved on-shell scheme'** !!
- for the experts: leads to **gauge-invariant counterterms without resorting to physical measurements**; tested via SloopS (Boudjema, Semenov, Temes 2005; Baro, Boudjema, Semenov 2007/ 2008; Baro, Boudjema 2009)
- based on **'Pinch Technique'** (Cornwall 1982; Cornwall, Pappavassoliou 1989; Espinosa, Yamada, 2002; Binosi, Papavassiliou 2009;...)

# Renormalization: numerical results

... just some numerical results for allowed regions...



$m_h = 125 \text{ GeV}$

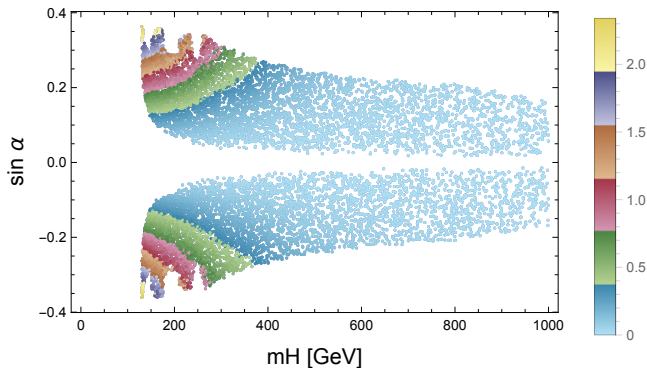


$m_H = 125 \text{ GeV}$

"typical" size of corrections

# The future...

... is colorful...



$\sigma(pp \rightarrow hH)[\text{fb}], 13 \text{ TeV LHC}$

[in collaboration with A. Papaefstathiou, J. Zurita; in preparation]

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Singlet

# Summary

- Singlet extension: **simplest extension of the SM Higgs sector**, easily identified with one of the benchmark scenarios of the HHXWG (cf. also YR3, Snowmass report)
- constraints on **maximal mixing** from  $m_W$  at **NLO** ( $m_H \in [200 \text{ GeV}; 800 \text{ GeV}]$ ), **experimental searches and fits** ( $m_{H,h} \leq 200 \text{ GeV}$ ) and/ or **running couplings** ( $m_H \geq 800 \text{ GeV}$ )
- **quite narrow widths wrt SM-like Higgses** in this mass range  $\Rightarrow$  **better theoretical handle**
- quite large suppression from current experimental/ theoretical constraints

**!!! still, large numbers could have been produced already !!!**

**$\Rightarrow$  STAY TUNED  $\Leftarrow$**

# Appendix



# Coupling and mass relations

$$m_h^2 = \lambda_1 v^2 + \lambda_2 x^2 - \sqrt{(\lambda_1 v^2 - \lambda_2 x^2)^2 + (\lambda_3 x v)^2}, \quad (1)$$

$$m_H^2 = \lambda_1 v^2 + \lambda_2 x^2 + \sqrt{(\lambda_1 v^2 - \lambda_2 x^2)^2 + (\lambda_3 x v)^2}, \quad (2)$$

$$\sin 2\alpha = \frac{\lambda_3 x v}{\sqrt{(\lambda_1 v^2 - \lambda_2 x^2)^2 + (\lambda_3 x v)^2}}, \quad (3)$$

$$\cos 2\alpha = \frac{\lambda_2 x^2 - \lambda_1 v^2}{\sqrt{(\lambda_1 v^2 - \lambda_2 x^2)^2 + (\lambda_3 x v)^2}}. \quad (4)$$

# Comments on constraints - running couplings and vacuum

## Vacuum stability and perturbativity of couplings at arbitrary scales

- clear: vacuum should be stable for large scales
- unclear: do we need ew-like breaking everywhere ?  
perturbativity ?
- ⇒ check at relative low scale (cf next slide)
- ⇒ bottom line: small mixings excluded from stability for larger scales (for  $m_H \leq 1 \text{ TeV}$  !! for the model-builders...)
- arbitrary large  $m_H$  can cure this !! cf Lebedev; Elias-Miro ea.  
Out of collider range though ( $\sim 10^8 \text{ GeV}$ )
- perturbativity of couplings severely restricts parameter space, even for low scales

# RGE running in more detail

**Question:** at which scale did we require perturbativity ?

**Answer:** "just above" the SM breakdown

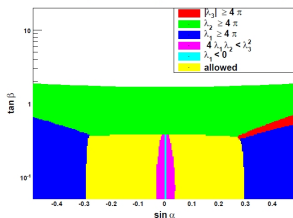
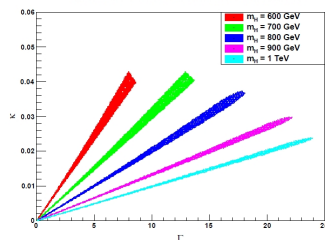
(other answers equally valid...)

- RGEs for this model **well-known** (cf eg Schabinger, Wells)
- **decoupling** ( $\lambda_3 = 0$ ): **recover SM** case
- in our setup:  $\mu_{\text{SM,break}} \sim 6.3 \times 10^{10} \text{ GeV}$   
(remark: just simple NLO running)
- **we took:**  $\mu_R \sim 1.2 \times 10^{11} \text{ GeV}$   
(higher scales  $\iff$  stronger constraints)

- **obvious:** for  $m_H \sim 125 \text{ GeV}$ , **breakdown "immediate"**  
when going to  $\mu_{\text{run}} > v$

$\Rightarrow$  disregard constraints from running in this case

# Limits for $m_H \geq 600 \text{ GeV}$

Effects of perturbativity and vacuum stability,  $t=37$ Limits in  $\sin \alpha$ ,  $\tan \beta$  plane, $m_H = 600 \text{ GeV}$  including all boundsallowed scale factor and total width,  $t=37$ limits on  $\kappa$ ,  $\Gamma$  plane from all constraints

for  $\sin \alpha \leq 0.23$ : only  $\lambda_2$  **running important**

(sideremark: here,  $1 \sigma$  constraint on mixing from  $\mu_i$ ; relaxed and improved in newer work, just as an example here)

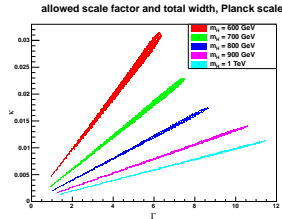
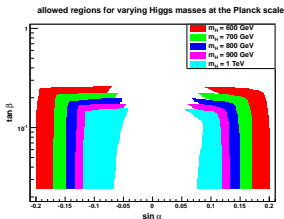
# Limits in numbers; high mass scenario

$m_H[\text{GeV}]$	$ \sin \alpha $	source upper limit	$(\tan \beta)_{\max}$
1000	[0.020; 0.16]	$\lambda_1$ perturbativity	0.21
800	[0.028; 0.20]	$m_W$ at NLO / $\lambda_1$ perturbativity	0.26
600	[0.038; 0.22]	$m_W$ at NLO	0.36
400	[0.057; 0.26]	$m_W$ at NLO	0.54
200	[0.092; 0.43]	$m_W$ at NLO	1.08
180	[0.10; 0.46]	126 GeV signal strength	1.20
160	[0.12; 0.46]	126 GeV signal strength	1.34
140	[0.17; 0.34]	$h \rightarrow \ell^+ \ell^- \ell^+ \ell^-$	1.54

- $\sin \alpha_{\min}$  always from **vacuum stability**
- $\tan \beta_{\max}$  always from **perturbativity of  $\lambda_2$**

# Limits at Planck scale

assume that the model is valid up to  $\mu_{\text{run}} \sim 10^{19} \text{ GeV}$   
(not always well motivated)



- naturally: **parameter space more restricted**
- translates to  $\kappa \lesssim 0.03$  for  $m_H = 600 \text{ GeV}$  (25 % decrease)
- now:  $\mu$  no longer relevant, only constraint from perturbativity of  $\lambda_1, \lambda_2$

# Could we have seen them ??

all numbers below:  $\sqrt{s}_{\text{hadr}} = 8\text{TeV}$ ,  $\int \mathcal{L} = 23\text{fb}^{-1}$

$m_H [\text{GeV}]$	$\kappa_{\text{max}}$	$\#gg \sim$	$\kappa'_{\text{max}}$	$\#gg \sim$
200	0.18	$3 \times 10^4$	0	0
300	0.076	$6 \times 10^3$	0.038	$3 \times 10^3$
400	0.053	$4 \times 10^3$	0.021	$1 \times 10^3$
500	0.047	$1 \times 10^3$	0.015	440
600	0.039	470	0.012	140
700	0.035	180	0.010	50
800	0.033	80	0.009	20
900	0.027	40	0.007	10
1000	0.021	15	0.005	4

[for specific final state, multiply with SM-like BR (LO approx)]

**for  $m_H \lesssim 600\text{ GeV}$ , may could already have been produced  
which are not excluded by current searches !!**

What about the “inverse” scenario, ie.  $m_H = 125.7 \text{ GeV}$

mainly ruled out by LEP and/ or  $\chi^2$  fit from HiggsSignals  
however, *still* large number produced due to large  $\sigma_{gg \rightarrow h}$

$m_h [\text{GeV}]$	$ \sin \alpha _{\text{min, exp}}$	$ \sin \alpha _{\text{min, } 2\sigma}$	$(\tan \beta)_{\text{max}}$	$\#gg \sim$
110	0.82	0.89	9.2	$10^5$
100	0.86	—	10.1	$10^5$
90	0.91	—	11.2	$10^5$
80	0.98	—	12.6	$10^4$
70	0.99	—	14.4	$10^4$
60	0.98	$\gtrsim 0.99$	16.8	$10^4$
50	0.99	$\gtrsim 0.99$	20.2	$10^4$
40	0.99	$\gtrsim 0.99$	25.2	$10^4$

**Table :** Upper limit on  $\tan \beta$  from perturbative unitarity. (— means no additional constraint)

(side remark: for  $m_h \gtrsim 60 \text{ GeV}$ ,  $\tan \beta$  irrelevant for collider observables)



# Tools which can do it ?? (incomplete list)

("it"=LO,NLO,...)

- LO: **any tool talking to FeynRules** (in principle)/ **LanHep** (in practice)
- implemented and run: **CompHep** (M. Pruna), **Sherpa** ( $\pm$ ) (would need some modification, T. Figy), privately modified codes (??)
- NLO: (mb) a modified version of **aMC@NLO** (R. Frederix) ?? (production only; might be important for VBF)
- new tool in the MadGraph environment (Artoisenet ea, 06/13): QCD-part of NLO
- complete higher orders: would need to be implemented in respective tools (I am not aware of any at the moment)

# One more word about $H \rightarrow hh$

- all above: **focuses on SM-like decays**
- **viable alternative:** search for

$$H \rightarrow hh \rightarrow \dots$$

- **widely discussed in the literature**  
(for recent work, cf Gouzevitch, Oliveira, Rojo, Rosenfeld, Salam, Sanz; Cooper, Konstantinidis, Lambourne, Wardrope; ...)
  - **HOWEVER** in our scan,  **$WW$  always dominant**
- ⇒ **would go for this first**  
(but mb more than 1 group is interested...)

# Comments on constraints (1) - Perturbativity issues

## Perturbative unitarity:

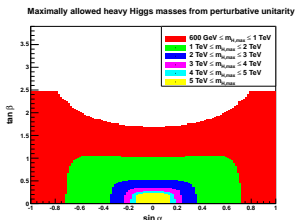
- tests combined system of all (relevant)  $2 \rightarrow 2$  scattering amplitudes for  $s \rightarrow \infty$
- we considered:

$$WW, ZZ, HH, Hh, hh \rightarrow WW, ZZ, HH, Hh, hh$$

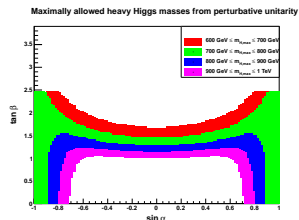
- makes sure that the largest eigenvalue for the "0"-mode partial wave of the diagonalized system  $\leq 0.5$
- "crude" check that unitarity is not violated  
(Literature: Lee/ Quigg/ Thacker, Phys. Rev. D 16, 1519 (1977))  
(in the end: all "beaten" by perturbativity of running couplings)

# Comments on constraints (1) - Perturbativity issues

- we tested: **maximal**  $m_H$  from PU  
 $\Rightarrow$  **strongest constraints from  $HH \rightarrow HH$**   $\Leftarrow$
- rule of thumb (exact for  $\alpha = 0$ ):  $\tan^2 \beta \leq \frac{16\pi v^2}{3m_H^2}$



Limits in  $\sin \alpha$ ,  $\tan \beta$  plane, maximally  
 allowed  $m_H$  from PU



Limits in  $\sin \alpha$ ,  $\tan \beta$  plane, maximally  
 allowed  $m_H \leq 1 \text{ TeV}$  from PU

$\Rightarrow$  **for realistic  $\sin \alpha$  and our  $m_H$  range,  $\tan \beta \lesssim 8$**

# Comments on constraints (2) - running couplings and vacuum

① **perturbativity:**  $|\lambda_{1,2,3}(\mu_{\text{run}})| \leq 4\pi$

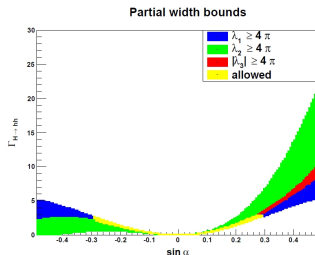
② **potential bounded from below:**  $\lambda_1, \lambda_2 > 0$

③ **potential has local minimum:**  $4\lambda_1\lambda_2 - \lambda_3^2 > 0$

$\Rightarrow$  need (2), can debate about (1), (3) at all scales  $\Leftarrow$

# Limits on $\kappa$ , $\Gamma_{\text{tot}}$

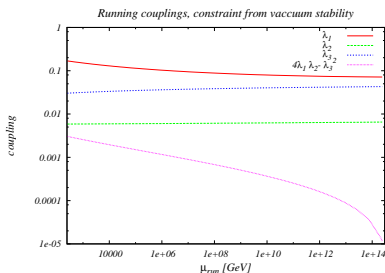
limits on  $\Gamma_{H \rightarrow hh}$ ,  $m_H = 600 \text{ GeV}$



- constraint from  $\mu$  on  $\sin \alpha$ :  $\Gamma_{H \rightarrow hh}$  already small ( $\lesssim 0.08 m_H$ )
- running of couplings: even stronger constraints

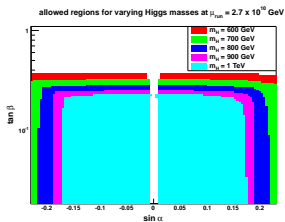
# RGE running: a caveat (1)

- important for **collider constraints**: maximal value of  $|\sin \alpha|$
- important for **vacuum stability**: minimal value of  $|\sin \alpha|$
- important here:  $4 \lambda_1 \lambda_2 \geq \lambda_3^2$
- **sometimes**: this is **(nearly) violated** for running over large scales

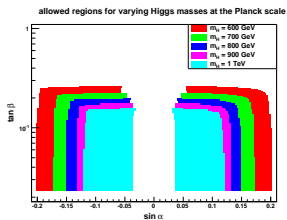


# RGE running: a caveat (2)

- ⇒ could in principle argue that **higher orders are needed**
- ⇒ one possible way to **quantify: neglect this condition**
- ⇒ now  $|\sin \alpha|_{\min}$  follows from  $\lambda_1 \geq 0$ .



low scale, third condition neglected



Planck scale, third condition neglected

⇒ **back to vacuum stability problem of SM** ⇐  
no important consequences for discovery prospects

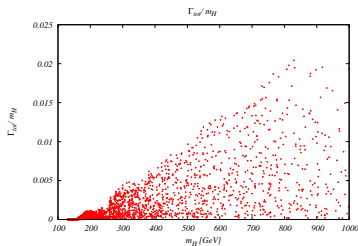


# RGE running: variation of input parameters

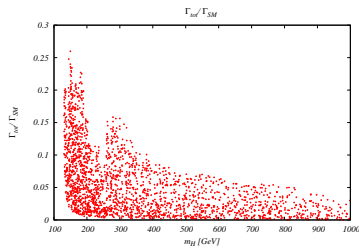
- especially in sensitive cases, but also otherwise:  
**check robustness against input parameters**
  - here: especially important in decoupling (ie SM-like) case  
(cf. various discussions in the literature...)
  - our check:  
**vary  $\alpha_s(m_Z)$ ,  $y_t(m_t)$  for  $1\sigma$  around central values**
  - main impact: **on vacuum stability**, ie  $\lambda_1 > 0$  condition
  - **no significant change in  $\kappa_{\max}(m_H)$ , ...**
- ⇒ **not relevant for collider studies** (at this stage...)

# Interim comment on total width

- Total width greatly reduced



width over mass



suppression factor of width

# Higher order corrections in the Singlet extension (3) - width and on-shellness

- is the width small enough to neglect "broadness" complications ?
- naive argument: **error**

$$\sim \frac{\Gamma_H}{m_H} \lesssim 2\%$$

⇒ **might be OK for a rough estimate**

- another point: "sideband" complications vanish

⇒ **low-mass case: interference effects ?**

(currently limited from signal strength fits (via  $\Gamma_{\text{inv}}$ ))