

# New observables in quarkonium production: the case of double $J/\psi$ production

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**work done in collaboration with Hua-Sheng Shao (CERN)**

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[large NLO and NNLO correction to the  $P_T$  spectrum ; but not perfect → need a full NNLO]

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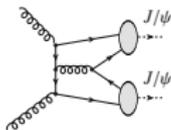
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- One of these is quarkonium-pair production

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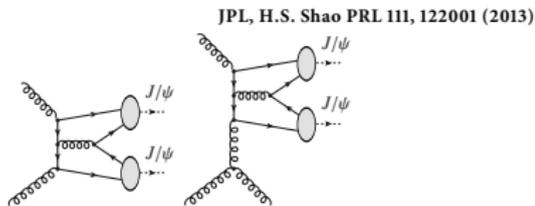
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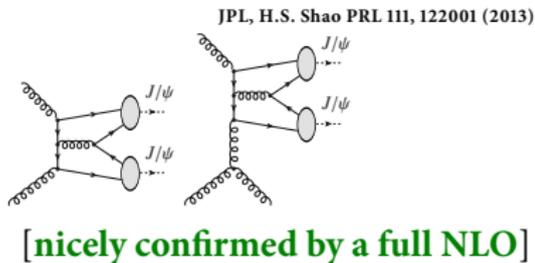
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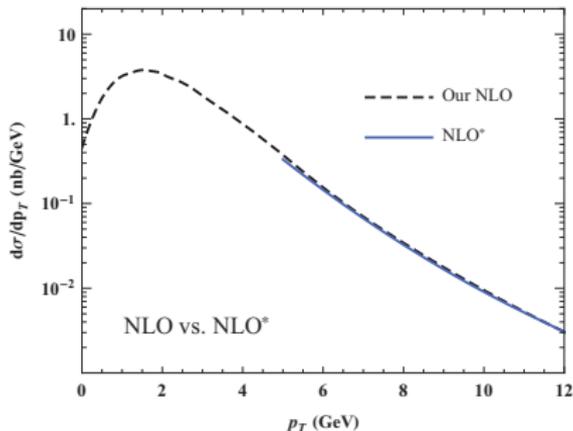


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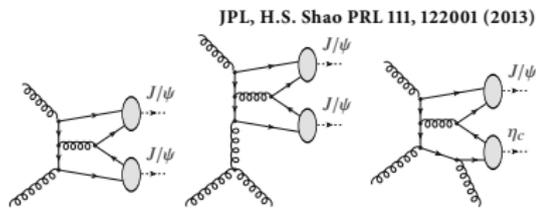


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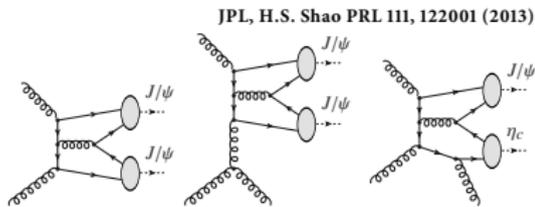


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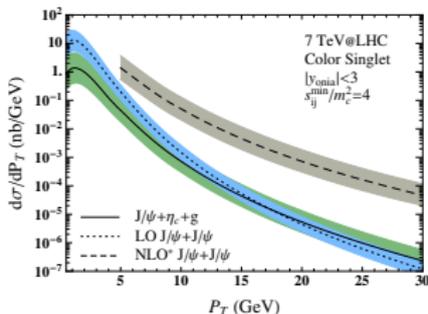
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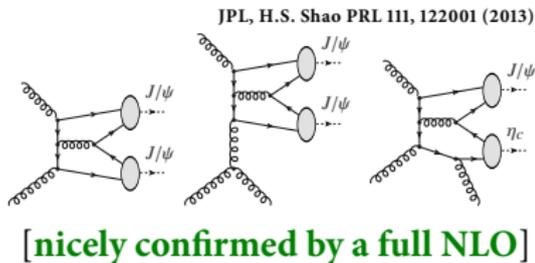
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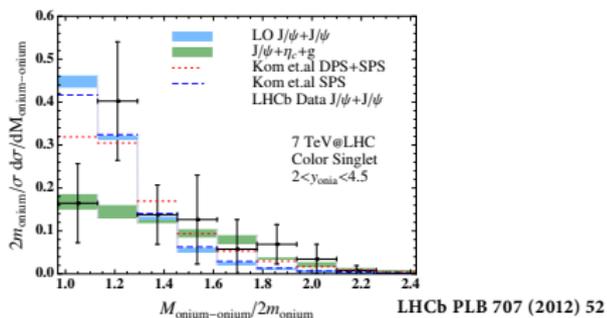
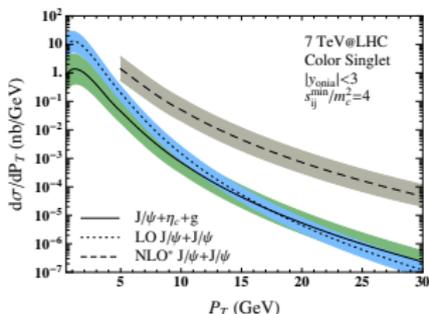


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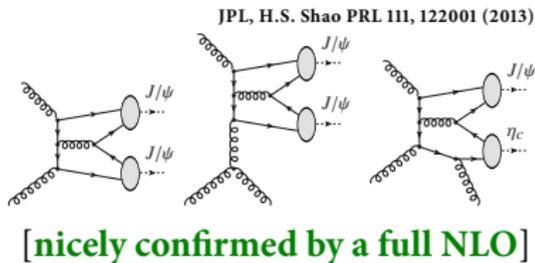
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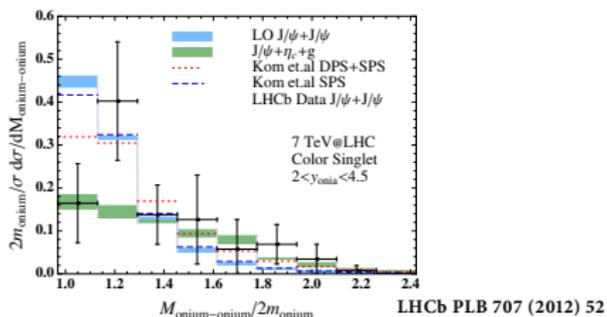
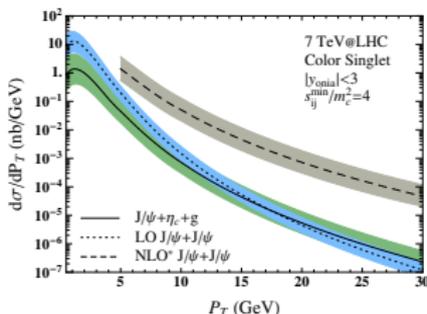
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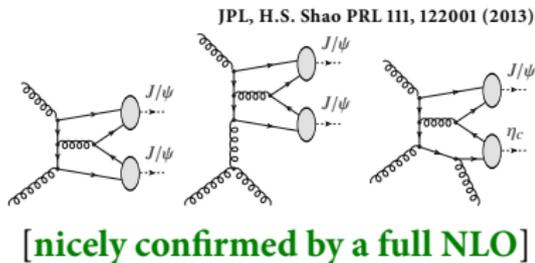
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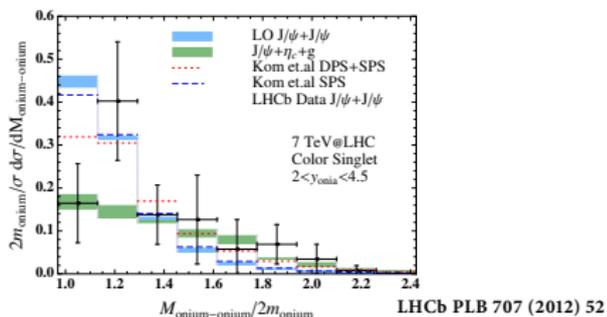
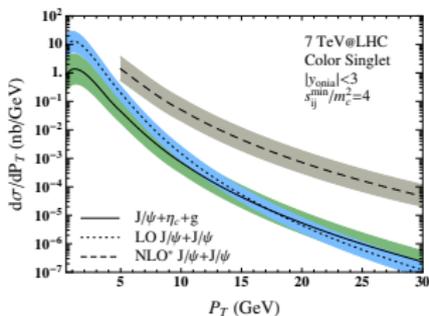
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- **Large enhancement at high  $P_T$**

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JPL, H.-S. Shao PLB 751 (2015) 479

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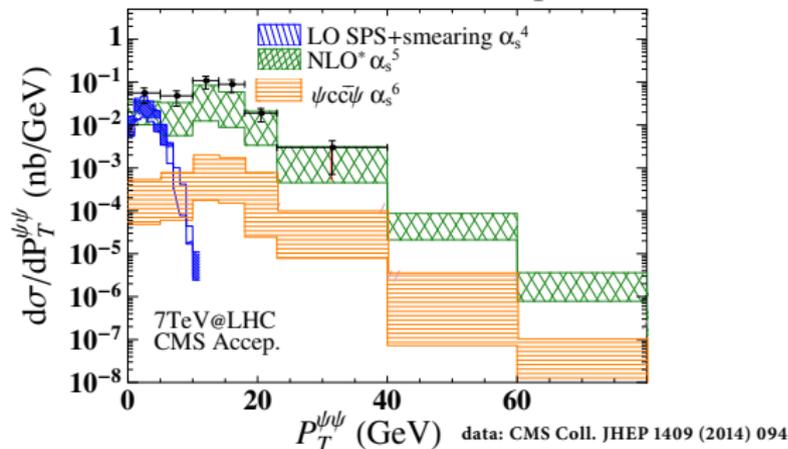
JPL, H.-S. Shao PLB 751 (2015) 479

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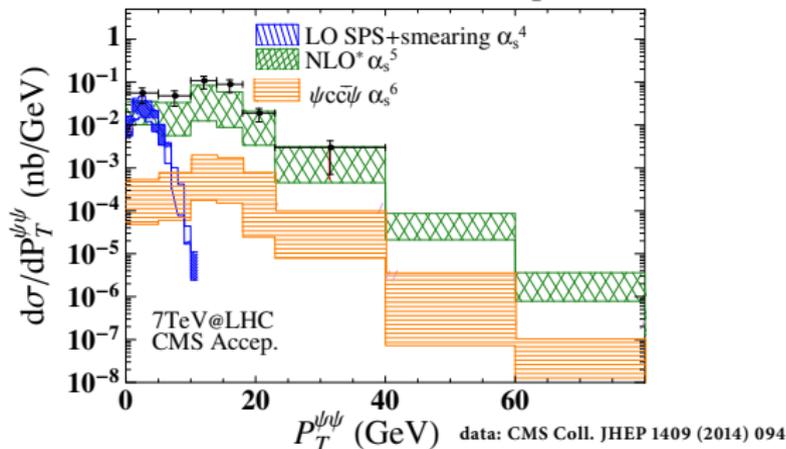
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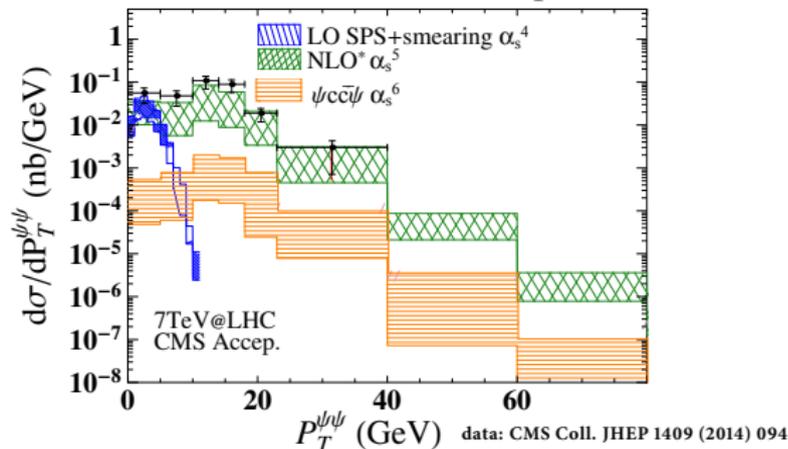


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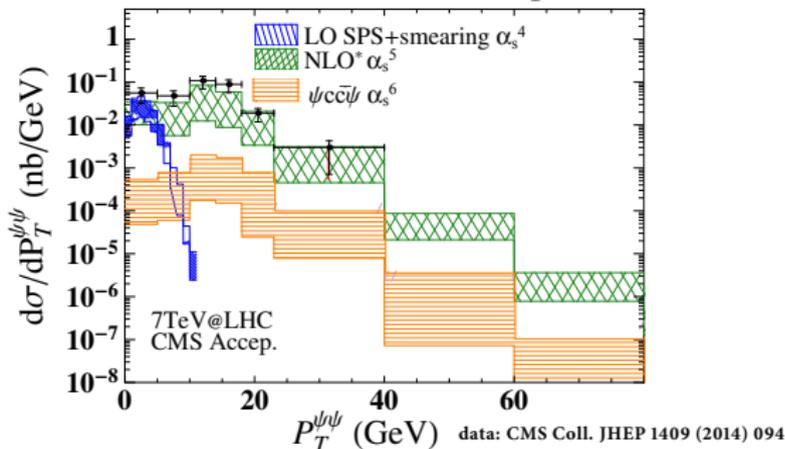


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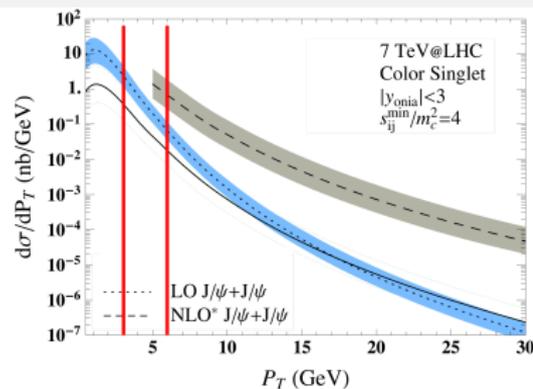
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- We do not expect NNLO ( $\alpha_s^6$ ) contributions to matter where one currently has data [the orange histogram shows one class of leading  $P_T \alpha_s^6$  contributions]

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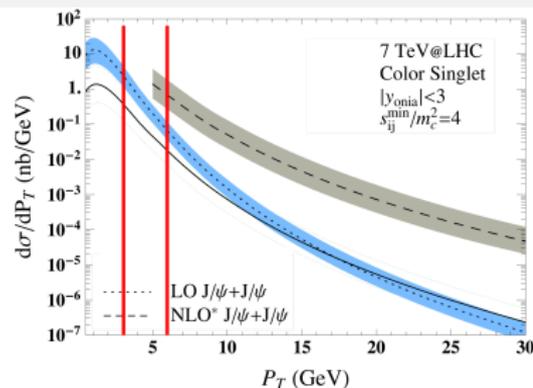
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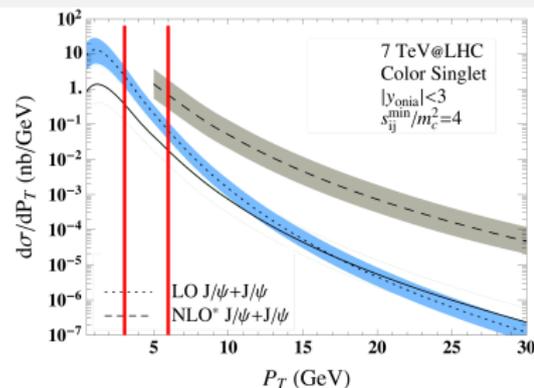
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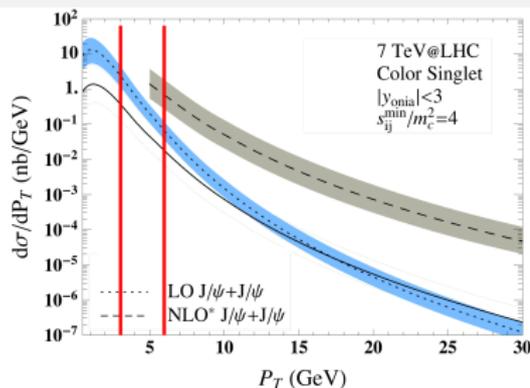
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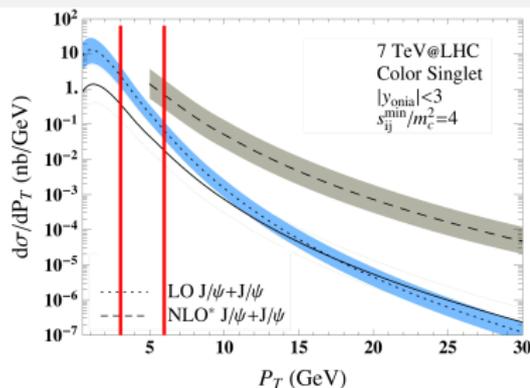
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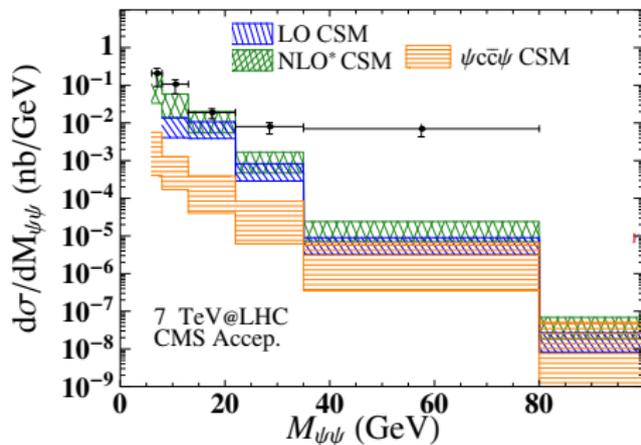
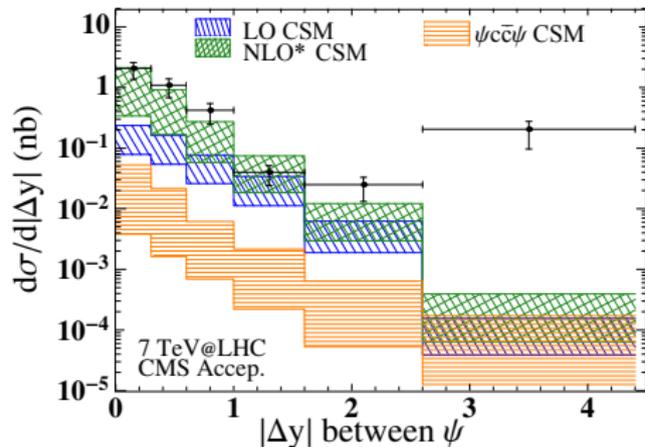
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- As we will also see, this was foreseeable (this should not have been a puzzle at all)

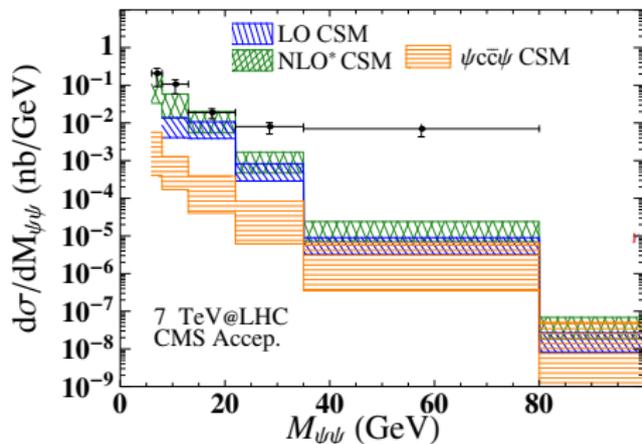
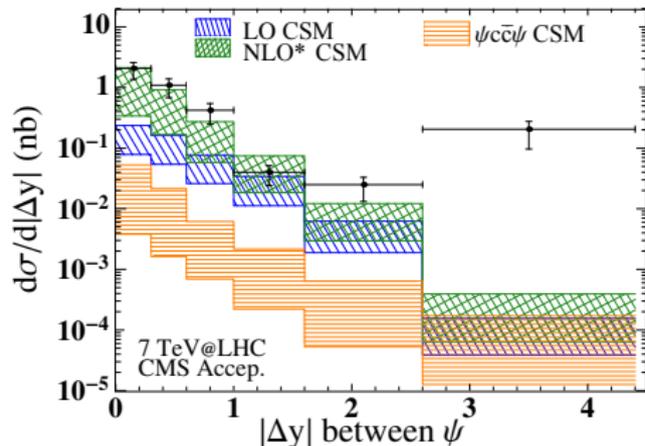


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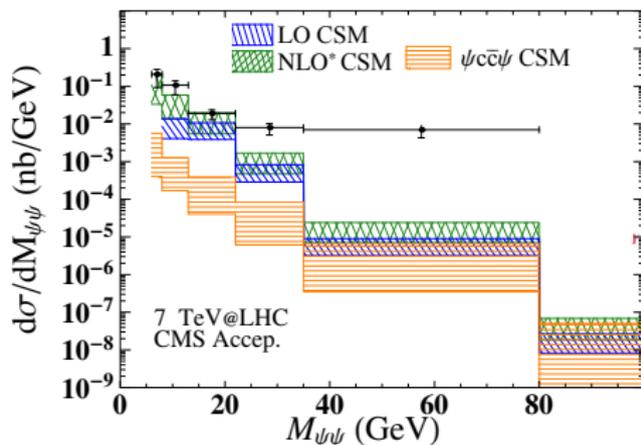
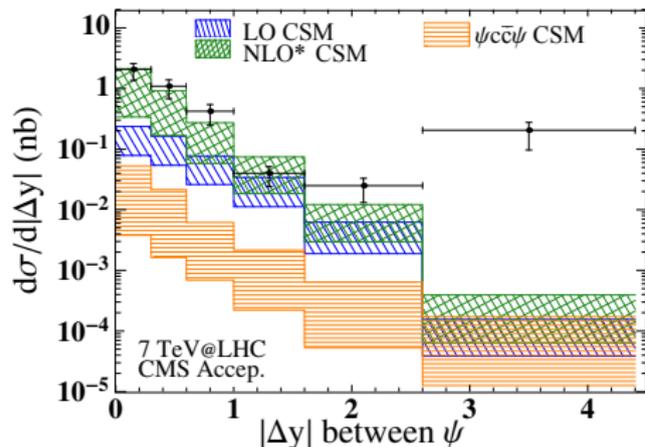


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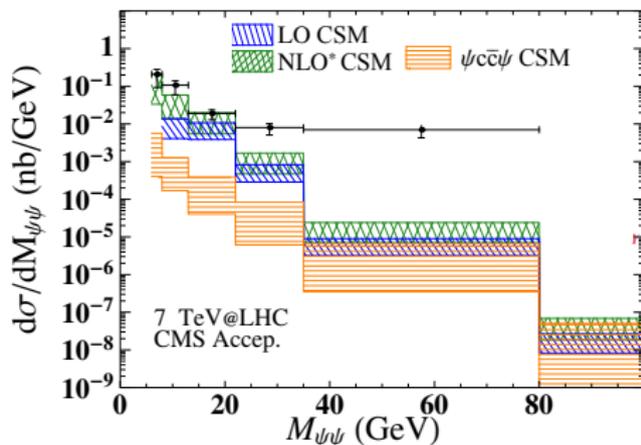
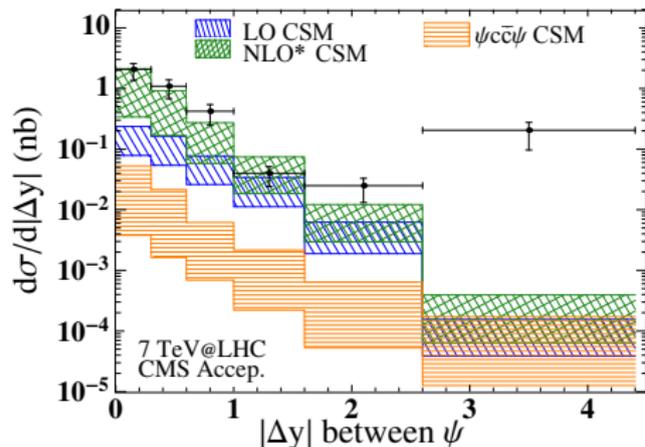
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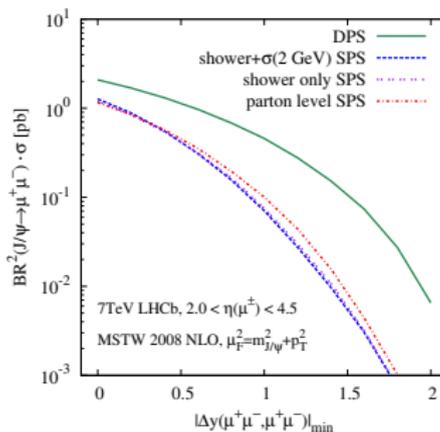
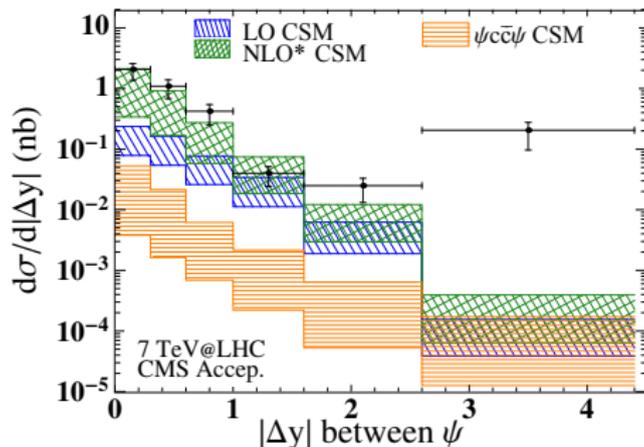
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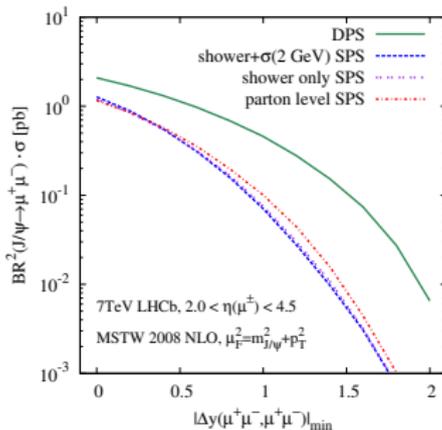
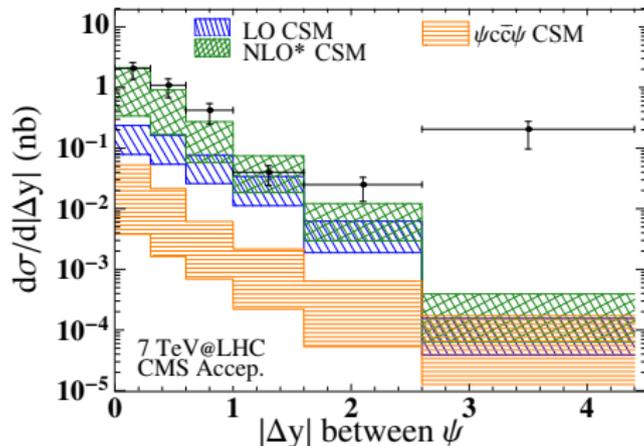
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C.H. Kom, A. Kulesza, W.J. Stirling PRL 107 (2011) 082002

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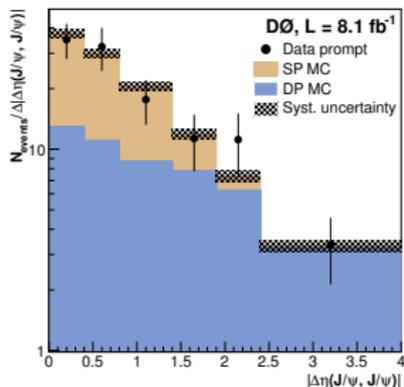
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- He & Kniehl however claimed that colour octets could also fill the gap  
→ We will come back to this later

C.H. Kom, A. Kulesza, W.J. Stirling PRL 107 (2011) 082002

Z. He, B. Kniehl PRL 115, 022002 (2015)

# On the importance of double parton scatterings at large $\Delta\eta$

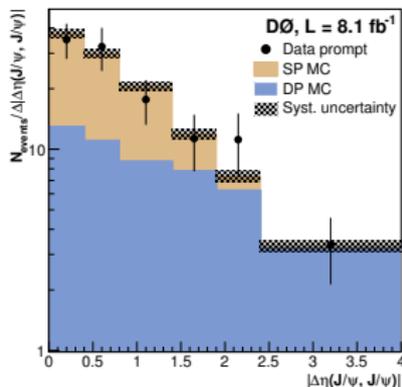
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D0 Coll. PRD 90 (2014) 111101

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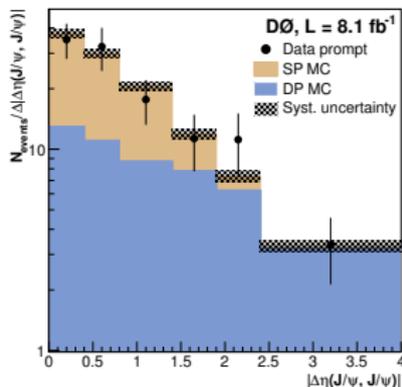


D0 Coll. PRD 90 (2014) 111101

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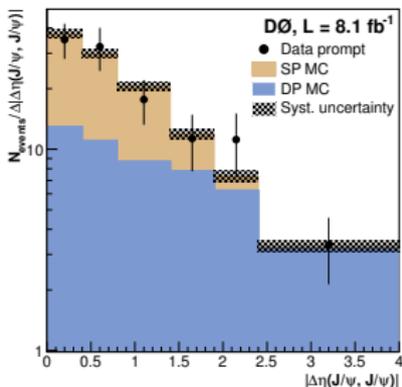


D0 Coll. PRD 90 (2014) 111101

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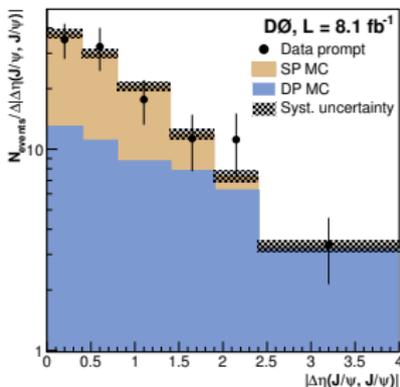


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- In turn, they obtained  $\sigma_{\text{eff}} = 4.8 \pm 2.5 \text{ mb}$
- A natural question arises: using  $\sigma^{\text{DPS}} = \frac{\sigma_{\psi} \sigma_{\psi}}{\sigma_{\text{eff}}}$  and  $\sigma_{\text{eff}} = 4.8 \pm 2.5 \text{ mb}$ , can one account for the large  $\Delta y$  CMS data?

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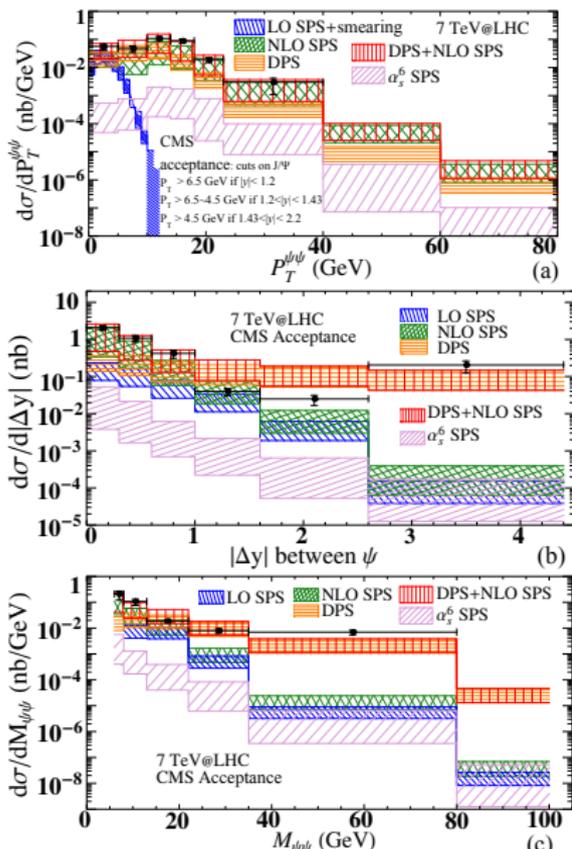
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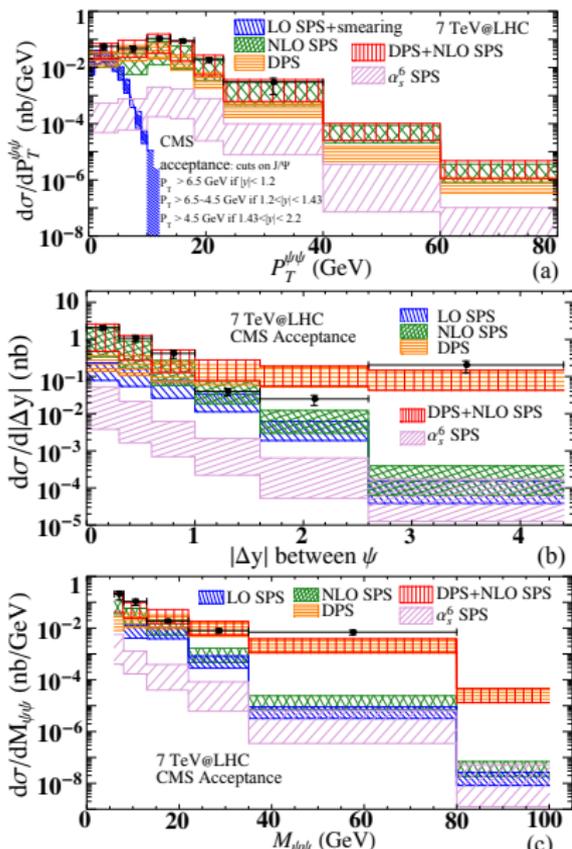
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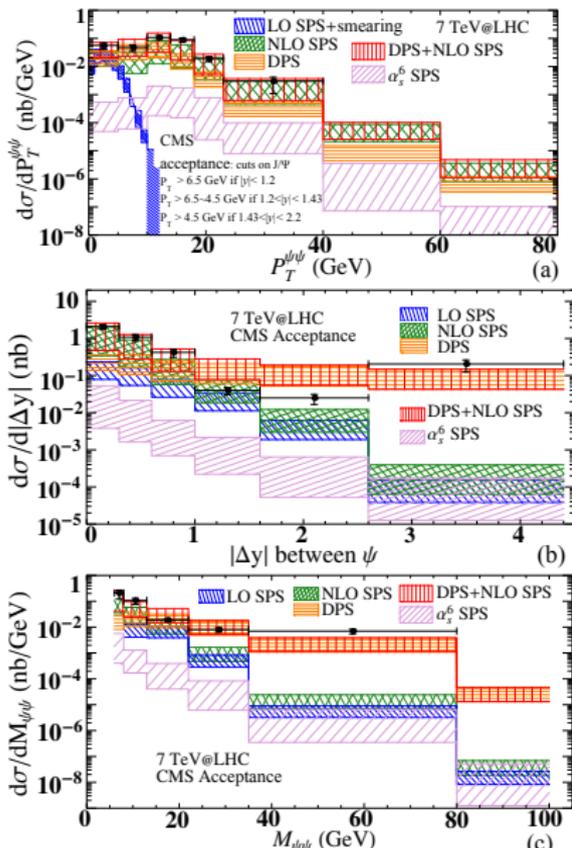
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- Agreement not altered elsewhere; improved even at low  $P_T^{\psi\psi}$  (see (a))

C.H. Kom, A. Kulesza, W.J. Stirling PRL 107 (2011) 082002

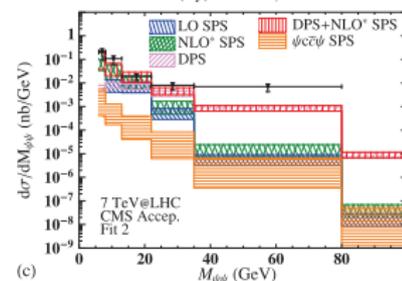
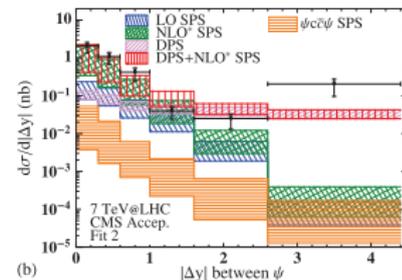
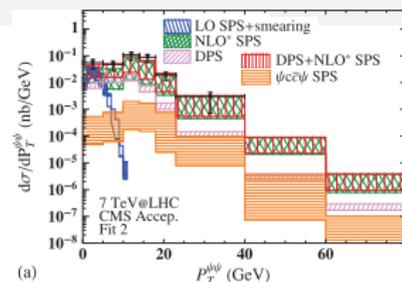


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- Conversely, fitting our own  $\sigma_{\text{eff}}$  from the CMS data should yield a value compatible with 4.8 mb

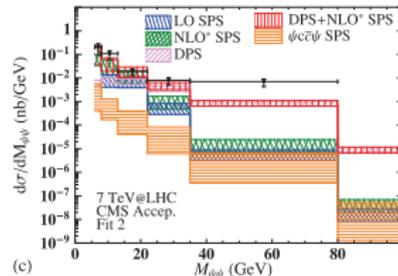
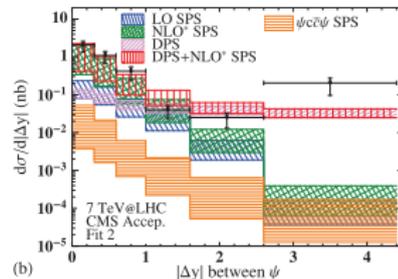
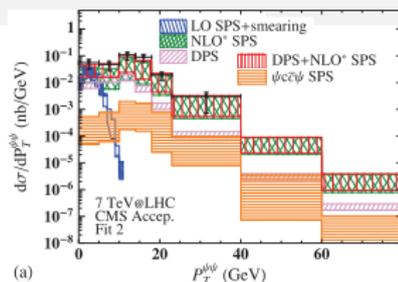


# Our fit of the double parton scatterings



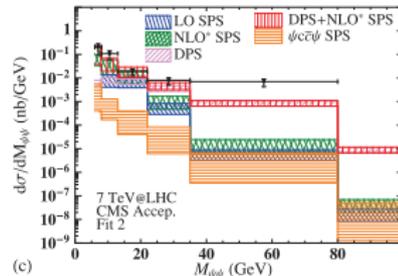
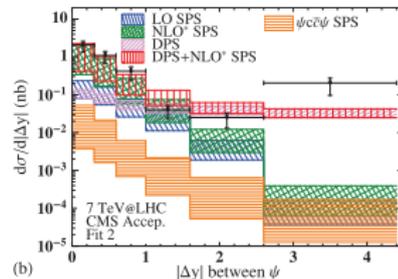
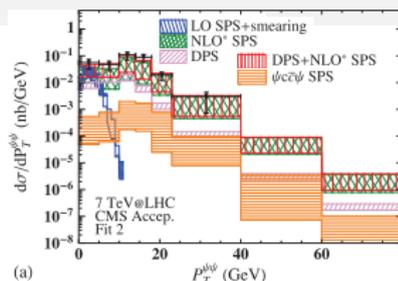
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- To assess the **systematics**, we used 3 fits of  $\sigma_\psi$ 
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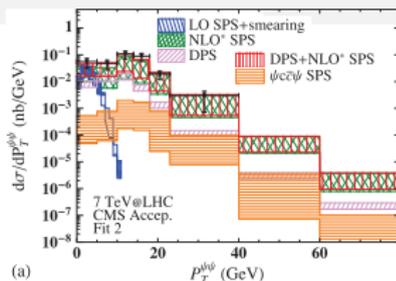


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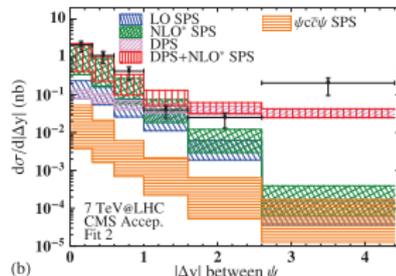
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  - Template for  $\sigma_\psi$  (see above)
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Result of the fit of the DPS yield via  $\sigma_{\text{eff}}$  on the 18 CMS values.

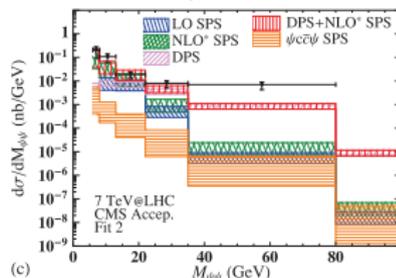
	$\sigma_{\text{eff}}$ [mb]	$\chi^2_{\text{d.o.f.}}$	d.o.f.
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$\sigma_\psi$ Fit 2	$8.2 \pm 2.2$	1.8	16
$\sigma_\psi$ Fit 3	$5.3 \pm 1.4$	1.9	16
Only LO SPS	N/A	7.6	17
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(b)



(c)

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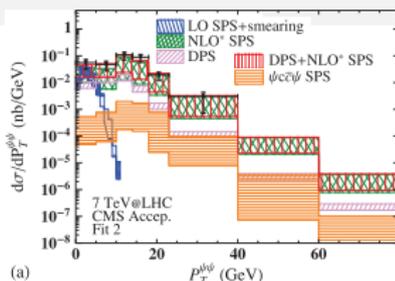
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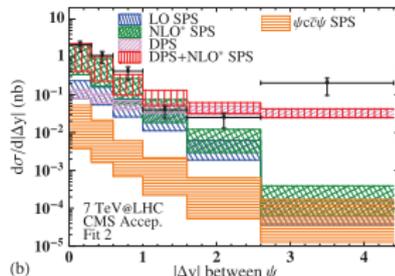
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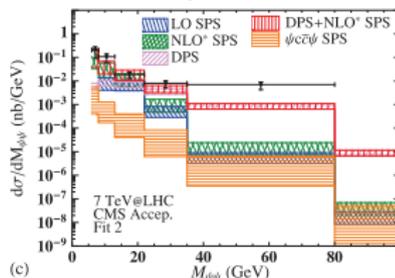
- $\sigma^{\text{DPS}}$  computed for D0 & LHCb; agreement checked:  
 $\chi_{\text{d.o.f.}}^2$  : 0.5-1.2 (LHCb) & 0.06-0.5 (D0)



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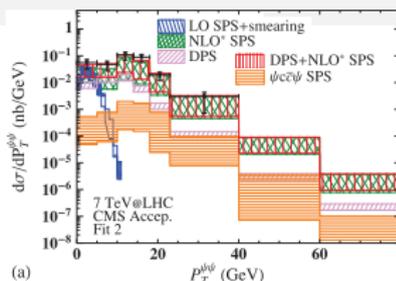
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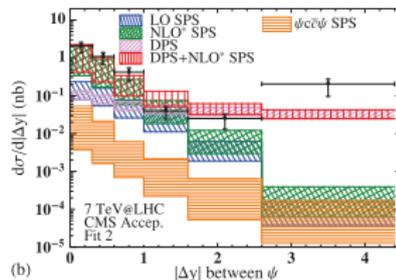
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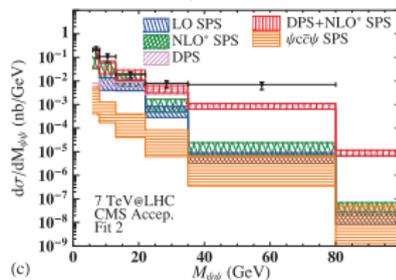
- $\sigma^{\text{DPS}}$  computed for D0 & LHCb; agreement checked:  
 $\chi^2_{\text{d.o.f.}}$  : 0.5-1.2 (LHCb) & 0.06-0.5 (D0)
- Best agreement with Fit 3 confirming the consistency:  
 $\sigma_{\text{eff}} = 4.8 \pm 2.5 \text{ mb}$  vs  $\sigma_{\text{eff}} = 5.3 \pm 1.4 \text{ mb}$



(a)

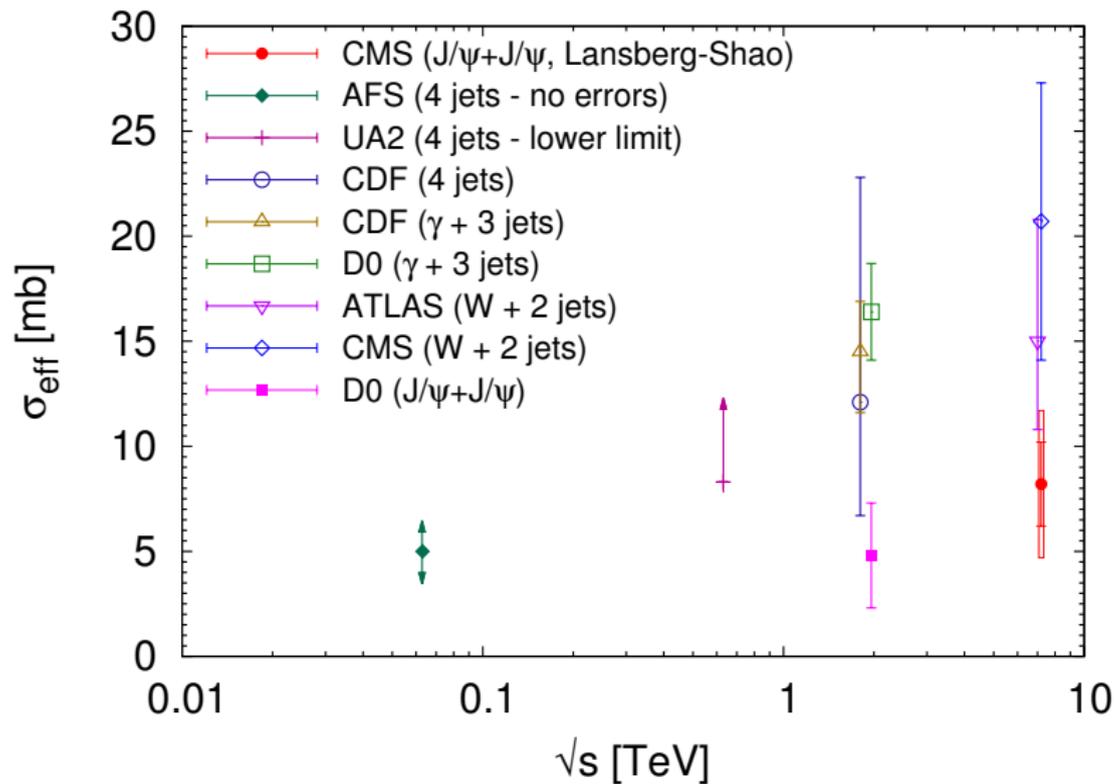


(b)



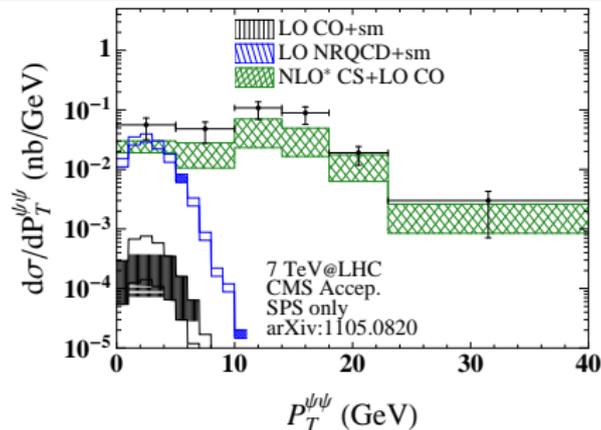
(c)

# Our fit value for $\sigma_{\text{eff}}$ : $8.2 \pm 2.0 \pm 2.9$ mb



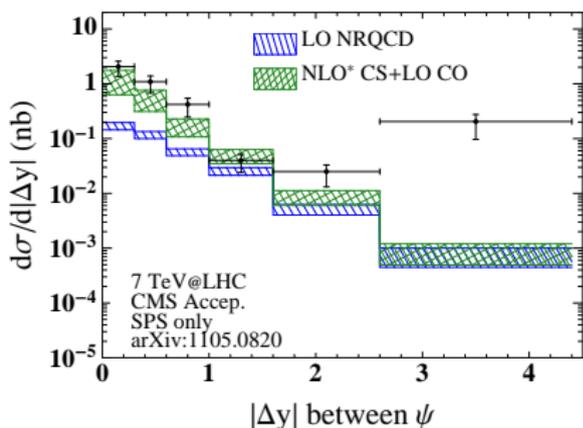
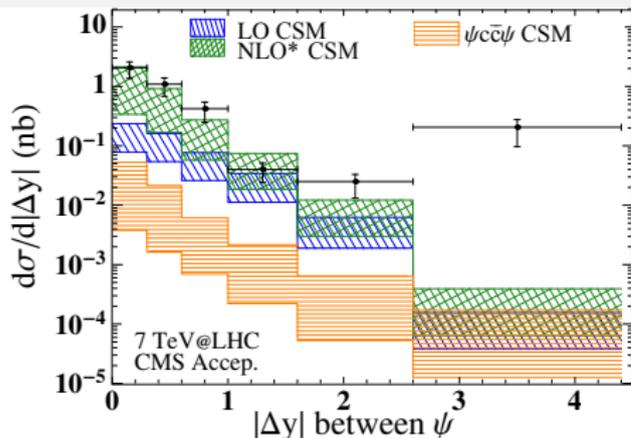
# On the (non-)importance of colour-octet channels

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Single  $J/\psi$  LDME fit: M. Butenschoen, B. Kniehl arXiv:1105.0820, PRD 84 (2011) 0515

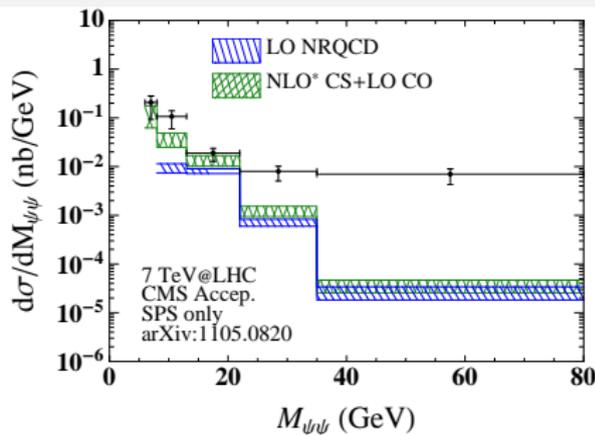
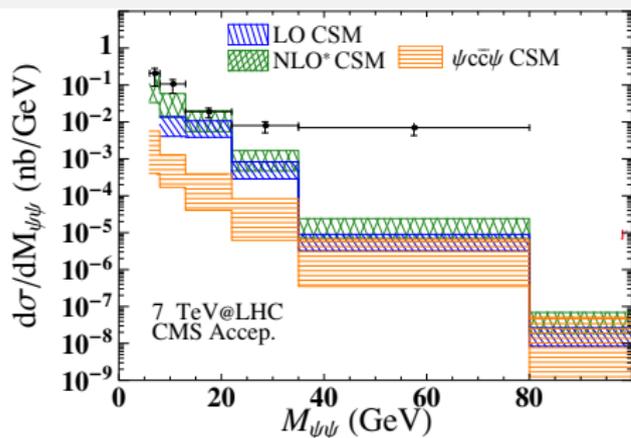
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- Adding CO using NLO LDMEs of the Hamburg group has **no impact**

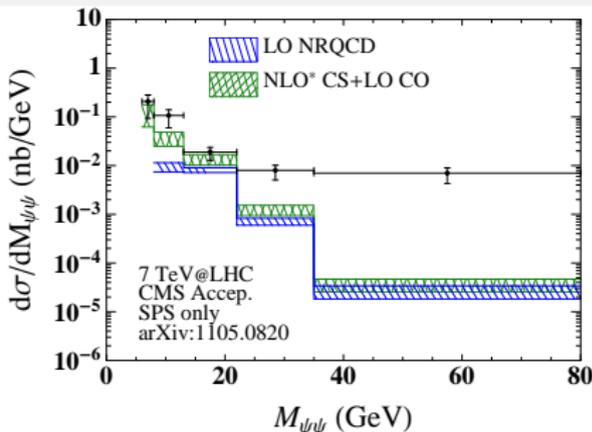
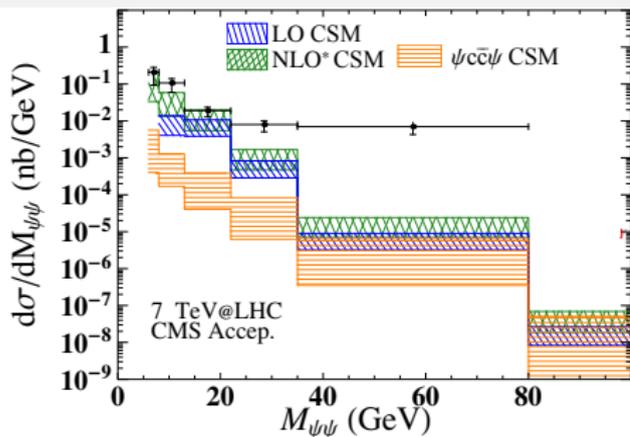
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Single  $J/\psi$  LDME fit: M. Butenschoen, B. Kniehl arXiv:1105.0820, PRD 84 (2011) 0515

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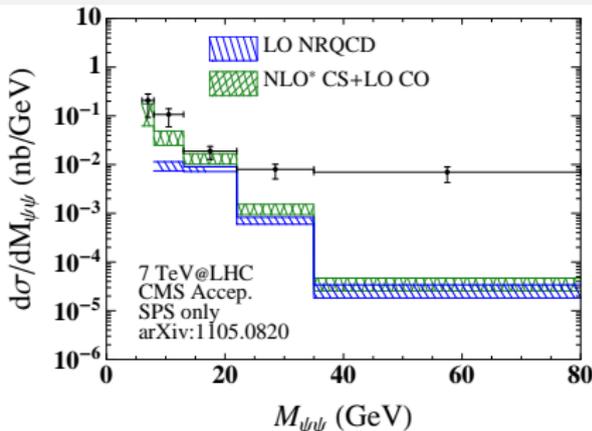
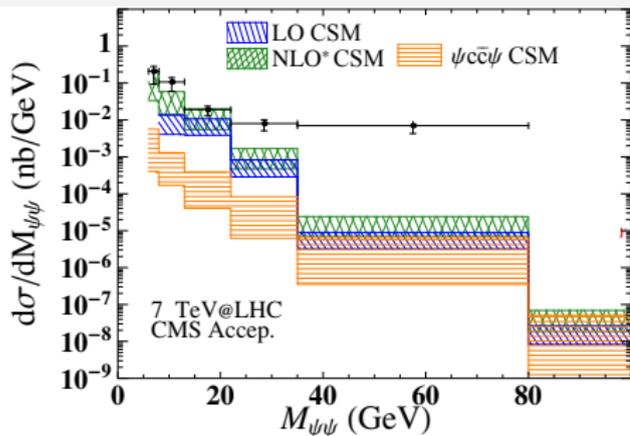


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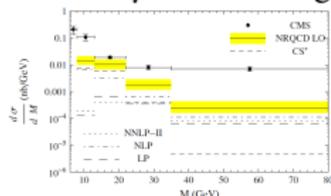
PRL 110 (2013) 042002; JHEP 1505 (2015) 103; PRL 113 (2014) 022001

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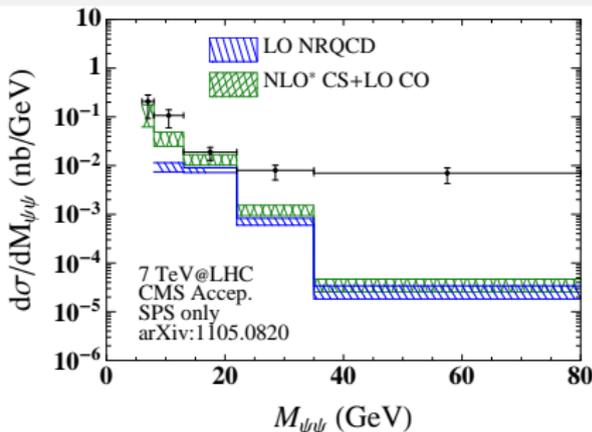
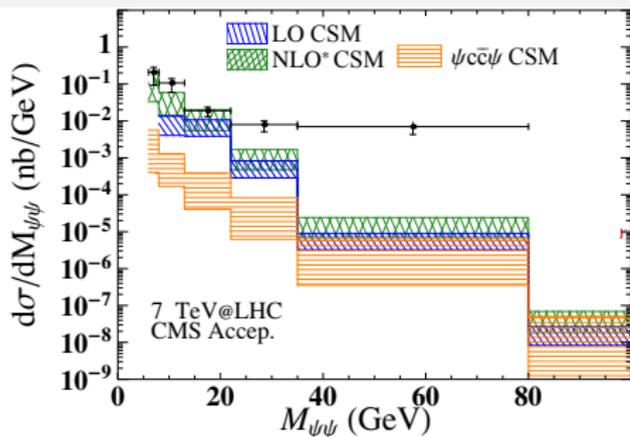


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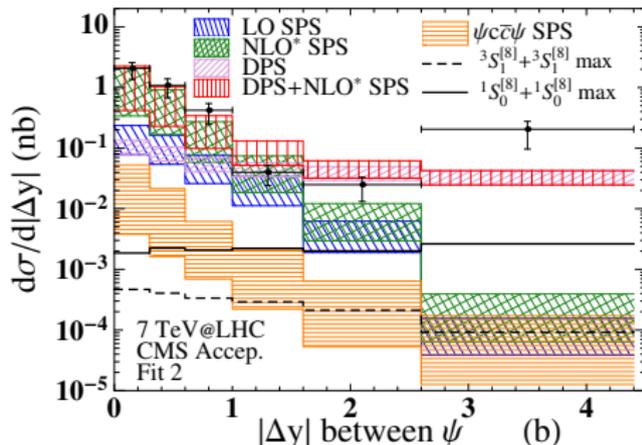
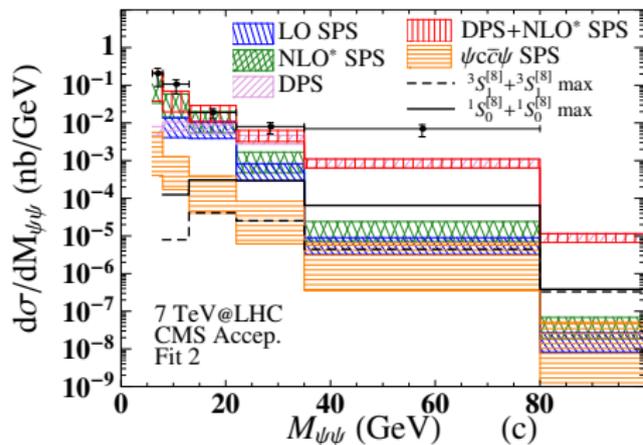
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- In terms of  $\chi_{d.o.f}^2$ :

	LO CO+ NLO* CSM w/o DPS	NLO* CSM w DPS
$\chi_{d.o.f}^2$	3.0	1.9

# Another way to see this with 2 CO channels

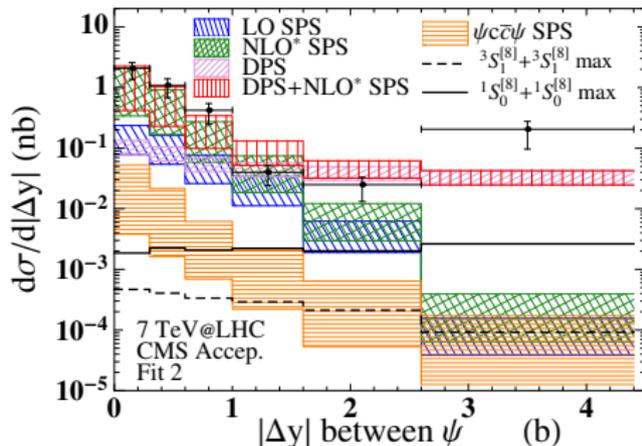
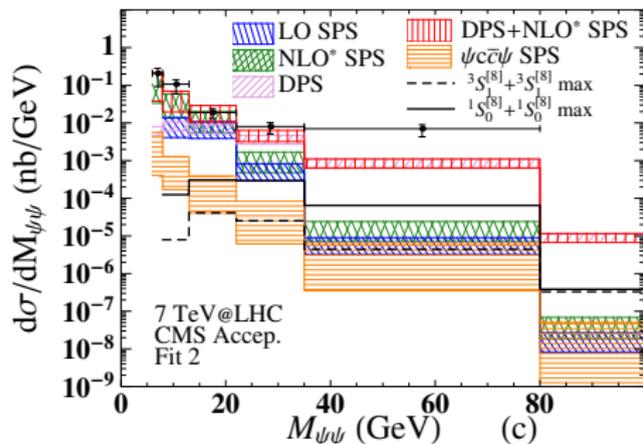
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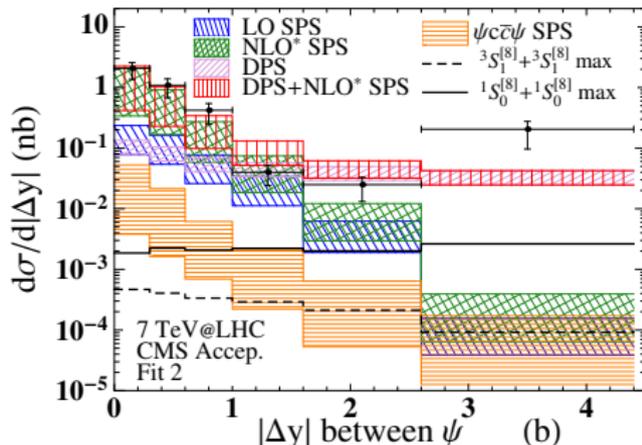
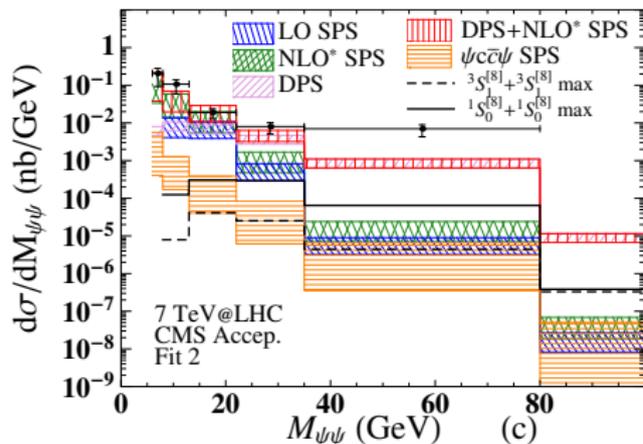


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- Ignoring all previous constraints and fitting (one channel at a time) the LDME on the CMS data one gets unrealistically large values:

$$\langle \mathcal{O}^{J/\psi}(^3S_1^{[8]}) \rangle = 0.42 \pm 0.12 \text{ GeV}^3 \quad \& \quad \langle \mathcal{O}^{J/\psi}(^1S_0^{[8]}) \rangle = 0.91 \pm 0.22 \text{ GeV}^3 \quad !!!$$

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- Overall :

	(CSM) SPS	DPS
$F_{\psi\psi}^{\psi'}$	45%	20%
$F_{\psi\psi}^{\chi_c}$	small	50%

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