

# Hadronization models and Colour Reconnection

arXiv:1412.6259 [hep-ph] and arXiv:1507.02091 [hep-ph]

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# Introduction

- Hadronization models central for non-perturbative QCD.
- String model(s) (eg. Pythia 6+8) challenged by many MPIs.
- Many MPIs  $\Rightarrow$  High density of strings  $\Rightarrow$  Interference effects.
- Rope model: Change of string tension, based on lattice QCD.
- Universality is a requirement.
  - 1 Introduction to strings.
  - 2 The Rope model.
  - 3 The DIPSY event generator.
  - 4 Junction handling.
  - 5 Results.

## Strings: A simple model for mesons

- Strings predates QCD, leading Regge trajectories,  $\alpha' \approx 0.9 \text{ GeV}^{-2}$ :

$$J(s) = J(0) + \alpha' s$$

- *What kind of force law could reproduce this?* Revolving string.
- String of length  $l$ , massless ends moving with  $c$ , string tension in rest is  $\kappa$ .

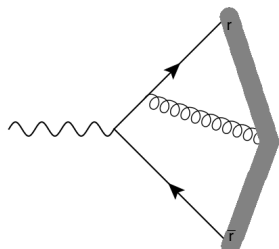
$$E = \frac{\pi l \kappa}{2}, \quad J = \frac{l^2 \pi \kappa}{8}$$

$$\Rightarrow \kappa = \frac{1}{2\pi\alpha'} \approx 0.180 \text{ GeV}^2 = 0.91 \text{ GeV/fm.}$$

- Later confirmed on the lattice.

- Non-perturbative phase of final state.
- *Breaking*/tunneling with  $\mathcal{P} \propto \exp\left(-\frac{\pi m_{\perp}^2}{\kappa}\right)$  gives hadrons.
- Left-right symmetry in the breaking gives

$$f(z) \propto z^{-1}(1-z)^a \exp\left(\frac{-bm_{\perp}}{z}\right).$$



- $a$  and  $b$  related to total multiplicity.
- Flavours determined by relative probabilities:

$$\rho = \frac{\mathcal{P}_{\text{strange}}}{\mathcal{P}_{\text{u or d}}}, \xi = \frac{\mathcal{P}_{\text{diquark}}}{\mathcal{P}_{\text{quark}}}$$

- Probabilities are related to  $\kappa$  via tunneling equation.

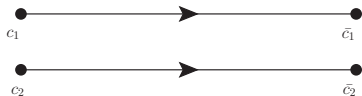
# Change of string tension

- Field changes when strings overlap - Simple Regge:  $2\pi E/l = \kappa$ .
- Effective string tension:  $\kappa \mapsto \tilde{\kappa} = h\kappa$  from number of overlapping strings.
- Electrodynamics: Principle of superposition, simple.
- QCD: Not so simple. Secondary Casimir operator of multiplet.

$$\kappa \propto C_2 \Rightarrow h = \tilde{\kappa}/\kappa = \frac{C_2(\text{multiplet})}{1 \text{ GeV/fm}}$$

- Confirmed on the lattice, static case.

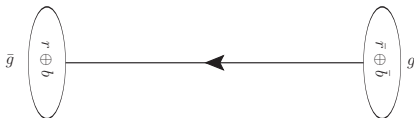
- The simplest example: Two  $q\bar{q}$  pairs act coherently.
- Two distinct possibilities:



Case (a),  $c_1 = c_2$  :

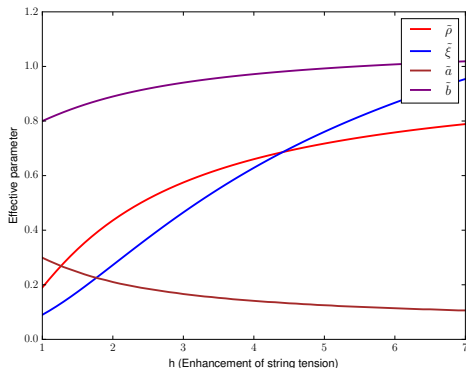


Case (b),  $c_1 \neq c_2$  :



# Effect on hadronization parameters

- All parameters related through string tension.
- $\rho$  (strange) and  $\xi$  (baryon) are very sensitive.



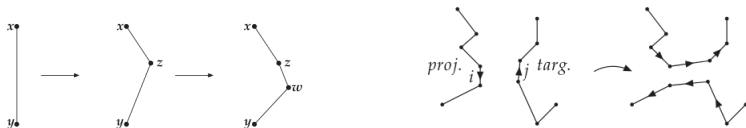
- Large effect on hadronic flavours.
- Smaller effect on hadron  $p_{\perp}$  and multiplicity (tunable).

# The DIPSY model arXiv:1103.4321 [hep-ph]

- Full  $\vec{b}$ -space information: Mueller dipoles (with corrections).
- MPIs  $\Leftrightarrow$  Dipole Chain Loops  $\Leftrightarrow$  Pomeron loops.
- A dipole  $(\vec{x}, \vec{y})$  can emit a gluon at position  $\vec{z}$  with probability ( $P$ ) per unit rapidity ( $Y$ ); dipoles  $i$  and  $j$  interacts with probability  $2f_{ij}$ :

$$\frac{dP}{dY} = \frac{3\alpha_s}{2\pi^2} d^2\vec{z} \frac{(\vec{x} - \vec{y})^2}{(\vec{x} - \vec{z})^2(\vec{z} - \vec{y})^2}$$

$$f_{ij} = \frac{\alpha_s^2}{8} \left[ \log \left( \frac{(\vec{x}_i - \vec{y}_j)^2 (\vec{y}_i - \vec{x}_j)^2}{(\vec{x}_i - \vec{x}_j)^2 (\vec{y}_i - \vec{y}_j)^2} \right) \right]^2$$

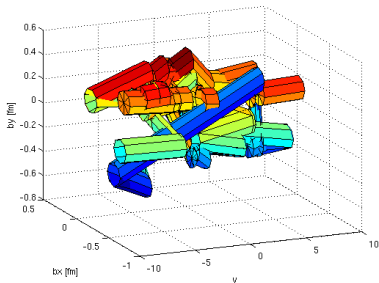
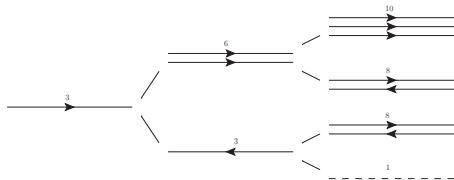


- Follow position through final state emissions.
- Full space-time information on all strings.



# Building the rope

- Spatial overlap calculated for individual dipoles.
- Rope built from  $m, n$  fundamental strings.
- SU(3) multiplet structure decided by random walk.

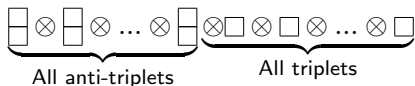


- Three options
  - 1 Highest multiplet.
  - 2 Lower multiplet (junction structure).
  - 3 Singlet.

# Highest multiplet

- All higher multiplets represents a coherent interaction.
- Fundamental quantum numbers  $p$  and  $q$  from recursion relations.
- Number of random (anti)-triplets added decided by overlaps.

$$\{p, q\} \otimes \vec{3} = \{p+1, q\} \oplus \{p, q+1\} \oplus \{p, q-1\}$$



- Transform to  $\tilde{\kappa} = \frac{2p+q+2}{4}\kappa$  and  $2N = (p+1)(q+1)(p+q+2)$ .
- $N$  (multiplicity of the multiplet) serves as a state's weight.
- String hadronized with  $\tilde{\kappa}$ .

# Junction handling

- Extra junctions handled through simplistic, popcorn-based approach.



- Extra parameter for colour fluctuations (no data handle).
- Better: Dynamical handling in a "swing".

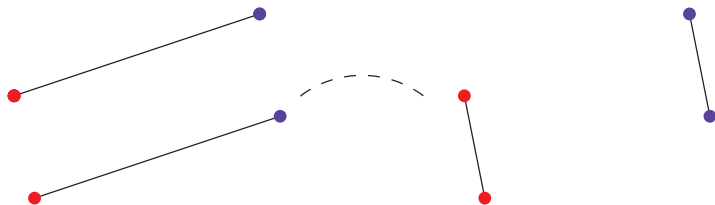


- Related: recent Pythia 8 model [arXiv:1505.01681](https://arxiv.org/abs/1505.01681) [hep-ph]

# The singlet swing

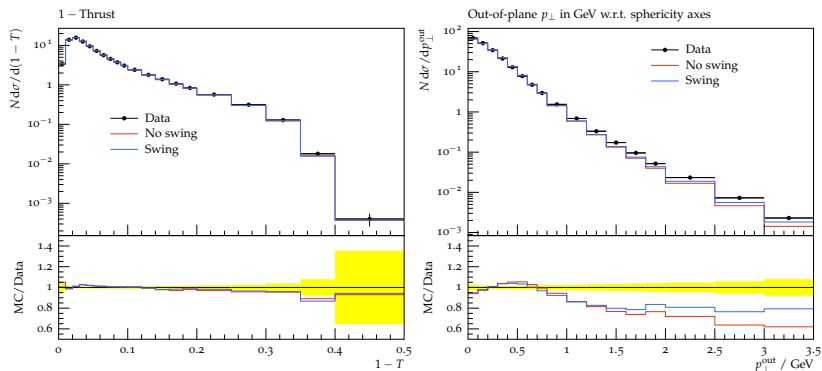
- Singlets are handled already in the FS shower (Ariadne).
- Matching colours *swings* with each other, competing w. emission.

$$\frac{dP_e}{d\ln(p_{\perp}^2)} \approx dy \frac{C_F \alpha_s}{2\pi} \quad \text{and} \quad \frac{dP_r}{d\ln(p_{\perp}^2)} = \lambda \frac{(\vec{p}_1 + \vec{p}_2)^2 (\vec{p}_3 + \vec{p}_4)^2}{(\vec{p}_1 + \vec{p}_4)^2 (\vec{p}_2 + \vec{p}_3)^2}$$



# Singlet swing and LEP Data: DELPHI

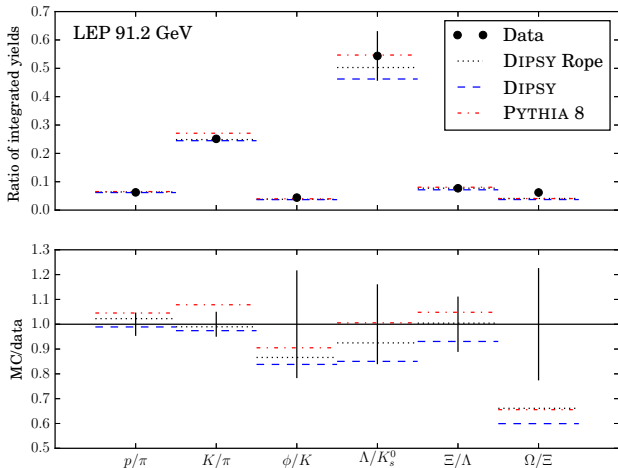
- Comes in already at perturbative level.
- Retuning of shower is necessary.
- No large difference,  $p_{\perp}^{out}$  somewhat improved.



# Flavour ratios - LEP

Data: SLD, LEP and PDG Avg.

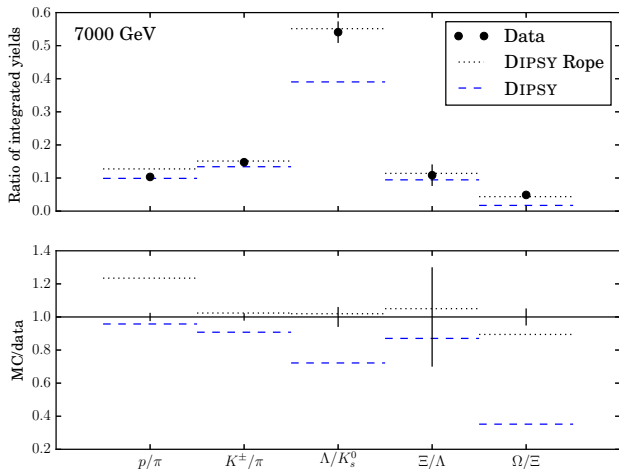
- String at LEPs. Agreement with data.
- Jet universality: Gain predictive power in  $pp$  by fixing parameters here.



# Flavour ratios - LHC

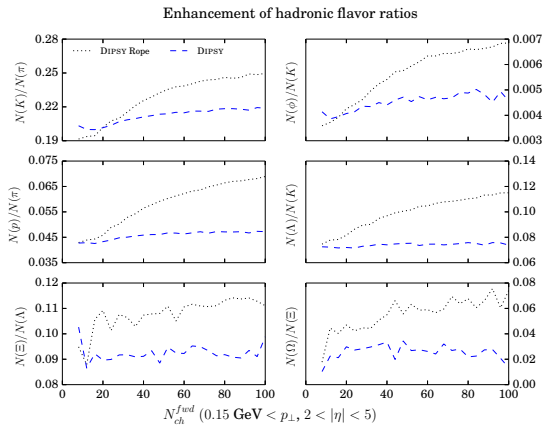
Data: CMS and ALICE

- Ropes at LHC. Overall better agreement, problem with  $p/\pi$ .
- Integrated quantities, need per event quantities as function of activity.



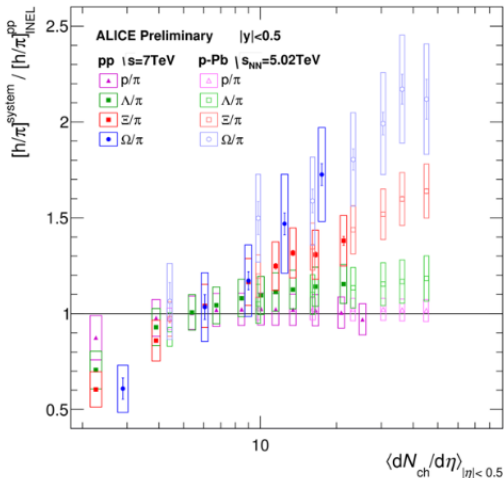
# Multiplicity dependence

- Rise of ratios with event multiplicity.
- Even more exclusive: ratios(mult) in jets vs. bulk.





- Strange enhancement is confirmed, baryonic is not.
- Further work: Baryon enhancement and junctions.



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# Conclusions and future

- Corrections to string hadronization improves description of flavour data.
- Space-time picture important to go differential.
- Rise as function of activity confirmed.
- No rise of baryon/meson seen in data.
- Particle ratios in jets vs. bulk.
- Application to pA and AA.

*Thank you!*