

# Kinematic effects and ordering variables in TMD parton distributions obtained from HERA data

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# Outline

- 1 TMD evolution in XFitter: current status
- 2 Open Issues in DIS at Low  $Q^2$
- 3 The coupled DGLAP-TMD approach
- 4 Problem I: The large- $k_t$  tail issue
- 5 Problem II: The ordering variable issue
- 6 Conclusion

## Previous talk ...

- ✓ The description of the evolution package with all its different pieces was presented. In this method, DGLAP evolution equation is solved with a MC method.
- ✓ This method was applied to extract both collinear and transverse momentum dependent (TMD) quark and gluon parton densities using the precision HERA DIS data.

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## TMD evolution in XFitter: current status

Several new features implemented for usage of the TMD evolution in XFitter completely different compared to the old version.

- ✓ We can use the TMDs integrated over  $k_t$  and have that together with the coefficient function of the ME which comes from QCDNUM, to calculate  $F_2$ ,  $F_L$ , etc.
- ✓ It can work over the whole kinematic range of  $x$  and  $Q^2$ .
- ✓ We have transverse momentum dependent gluons, sea quarks and valence quarks.
- ✓ The parametrization is changed now such that TMD uses just the standard XFitter parametrization.
- ✓ We can use the whole plotting package while comes from XFitter and plot the integrated parton distribution and  $F_2$ .
- ✓ We have TMD evolution but also directly get integrated PDF's out.

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## GBW with the full TMD evolution ...

- ✓ What we had originally in our mind was a better description of small- $x$ , small- $Q^2$   $F_2$  data. We tried the CCFM evolution and GBW (the saturation ansatz). We realized that we cannot get good description of higher  $Q^2$  data for  $F_2$ .
- ✓ In parallel we had activities for coupled DGLAP-TMD evolution. The idea was that we can have a better description at small- $x$ , because in the standard approach GBW with DGLAP seems to work well (this is what many authors did), so we had problem with CCFM evolution.

The idea was to use a similar approach but with DGLAP-TMD evolution with GBW as an input to get proper description.

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- GBW with DGLAP evolution seems to work, but GBW has  $k_t$  dependence. Therefore one would need an evolution which also treats the  $k_t$  dependence (not integrated over  $k_t$ ). So we started with the coupled DGLAP-TMD evolution.
- Before one can apply that to the full cross section calculation, we have to check that it works at medium and large  $Q^2$ . We started with the standard fit using integrated TMD.
- The next step is  $F_2$  calculation with TMD. Stuck at the moment with technical difficulties!

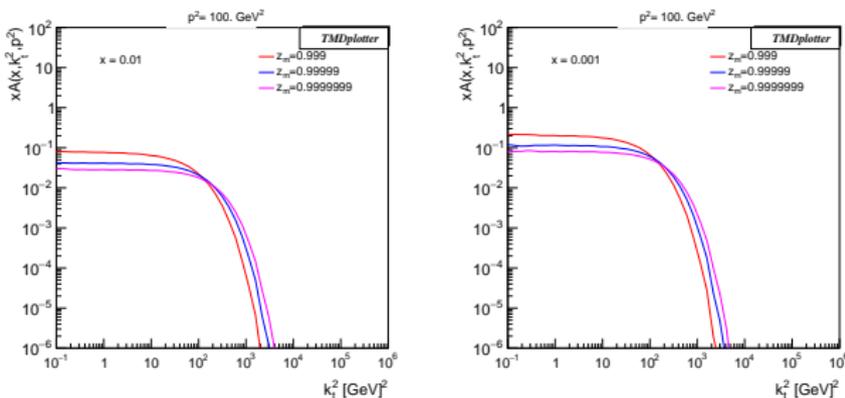
Now we discuss where the problems appear!

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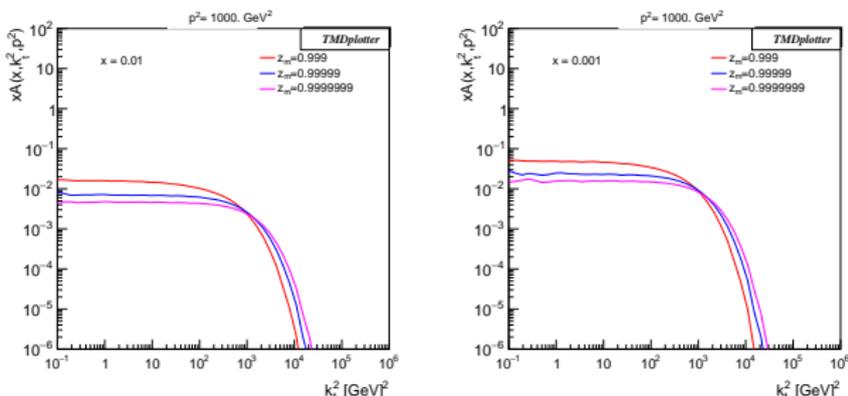
## The large- $k_t$ tail issue

At first we realize that there is an effect on  $z_{max}$  which is in the evolution, so the  $k_t$  dependence changes. We see there is a small dependence on  $z_{max}$ . The  $k_t$  distribution is different if we have smaller  $z_{max}$  or if we go to really close to one.



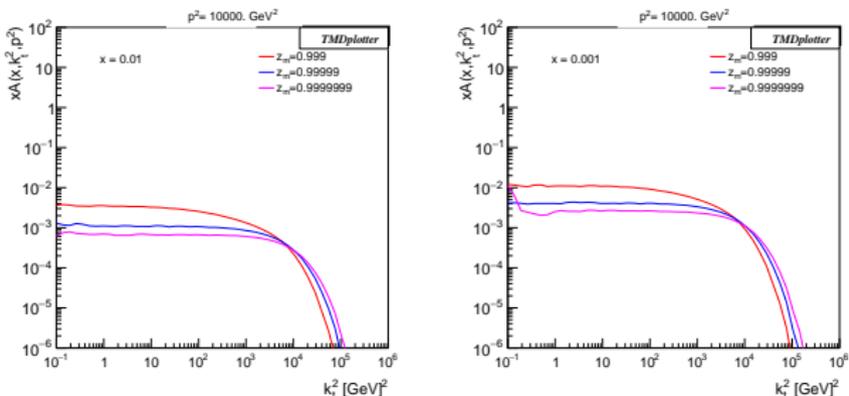
**Figure 1:** The plots show the  $k_t$  dependence as a function of the  $z_{max}$  cut applied in the splitting fct and in the sudakov factor. The important point in all the plots is that there is a tail of  $k_t$  to large values and the  $k_t$  can be larger than  $p$  (which one would naively not expect). This has quite some importance when calculating the cross section, as there are kinematic limitations and if  $k_t$  is included, then  $x' = x(1 + k_t^2/Q^2)$ .

What is even more interesting and which causes the problem is that we would normally integrate over TMD from zero- $k_t$  up to the scale. While we have to integrate over the whole  $k_t$  range which has kinematic effects. If we just include the  $k_t$ , then  $x$  changes ( $x' = x(1 + k_t^2/Q^2)$ ).



**Figure 2:** The important point in all the plots is, that there is a tail of  $k_t$  to large values and the  $k_t$  can be larger than  $p$  (which one would naively not expect). This has quite some importance when calculating the cross section, as there are kinematic limitations and if  $k_t$  is included, then  $x' = x(1 + k_t^2/Q^2)$ .

We can conclude from these plots that there is a tail to large  $k_t$  which is larger than the scale. The different sets of plots belong to the different scales. It's not a problem of one specific scale, this exists at every scale.  $k_t$  is just shifted to larger values.



**Figure 3:** The important point in all the plots is, that there is a tail of  $k_t$  to large values and the  $k_t$  can be larger than  $p$  (which one would naively not expect). This has quite some importance when calculating the cross section, as there are kinematic limitations and if  $k_t$  is included, then  $x' = x(1 + k_t^2/Q^2)$ .

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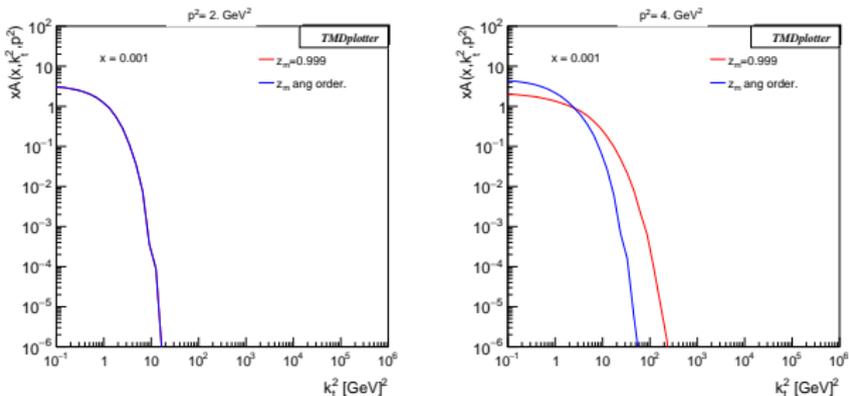
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# The ordering variable issue

In the evolution one can either have

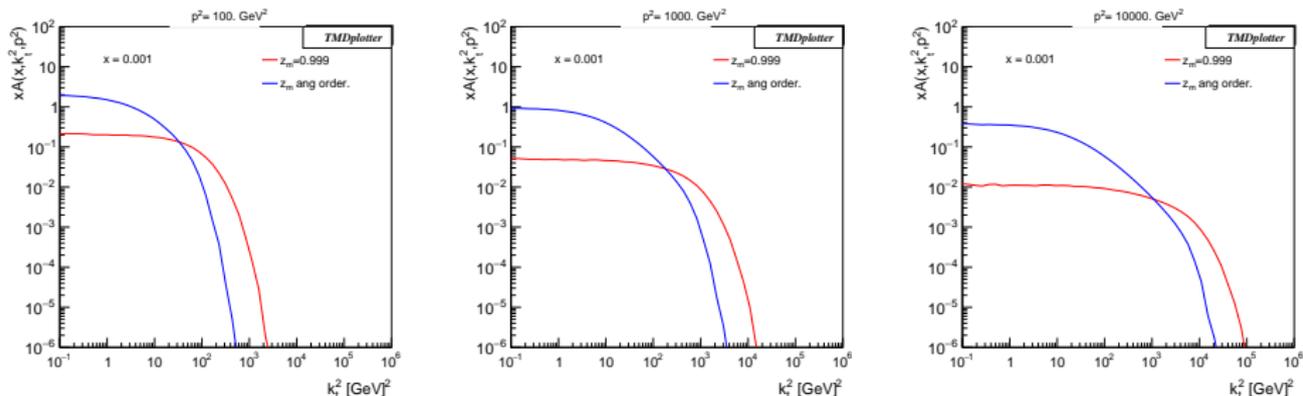
- $Q^2$  ordering with fixed  $z_{max}$  (standard DGLAP)
- angular ordering

The integrated distributions are not changed very much but the way how  $k_t$  is calculated changes. Because different evolutions have different  $k_t$  treatment, there is a significant effect of the changed ordering!



**Figure 4:** At the scale of  $2 \text{ GeV}^2$ , curves both agree, since it is at the starting scale. At  $4 \text{ GeV}^2$ , where there is some evolution, the angular ordering curve at the scale is half of the size of  $Q^2$  ordering.

The curve of angular ordering at the scale is already suppressed by the factor of two and it is half of the size of  $Q^2$  ordering curve. This also makes an effect when calculating  $F_2$  using the full TMD.



**Figure 5:** the  $k_t$  dependence for different ordering in the evolution: the standard ordering with a fixed  $z_{max}$ , the angular ordering with  $z_{max} = 1 - p^2/q_0^2$  where  $p^2$  is the evolution scale and  $q_0^2$  is a soft cutoff ( $q_0^2 = 1.9\text{GeV}^2$ ). In the angular ordering  $k_t$  is calculated as  $k_t = q(1 - z)/z$ , so it is smaller than in the other cases.

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# Conclusion

- GBW with CCFM does not lead to a good fit.
- Test performed with full coupled TMD-DGLAP evolution.
- $k_t$  dependence of TMD is significant.
- Future apply to small  $x$ .
- work in progress... stay tuned.

We are open to constructive comments and discussion.

Thanks for your paying attention.