



CTEQ

Beyond CT14: Hera II data and new interpretation of CT14QED photon

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On behalf of the CTEQ-TEA group

April 12, 2106

DIS 2016

DESY, Hamburg, Germany



CTEQ-TEA group

- CTEQ – Tung et al. (TEA)

in memory of Prof. Wu-Ki Tung,
who established CTEQ Collaboration in early 90's

- Current members of CTEQ-TEA group:

Sayipjamal Dulat (Xinjiang U.),

Tie-Jiun Hou, Pavel Nadolsky (Southern Methodist U.),

Jun Gao (Argonne Nat. Lab.),

Marco Guzzi (U. of Manchester),

Joey Huston, Jon Pumplin, Dan Stump, CS, C.-P. Yuan (Michigan State U.)



Outline

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- Brief overview of CT14 global analysis
Dulat et al, ArXiv:1506.07433[hep-ph]
- Impact of HERA I + II data on CT PDF analysis:
CT14HERA2
- New interpretation of CT14QED photon PDFs
and CMS data:
CT14QED (CS et al, arXiv:1509.02905[hep-ph])
- Conclusions



Overview of CT14 analysis

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- CT10 includes only pre-LHC data
- CT14 is the first CT analysis including LHC Run 1 data
- CT14 also includes the new Tevatron D0 Run 2 data on W -electron charge asymmetry
- CT14 uses a more flexible parametrization in the non-perturbative PDFs.
- We have published its results at NNLO, NLO and LO.

Produce 90% C.L. error PDF sets from Hessian method, scaled by $1/1.645$ to obtain 68% C.L. eigenvector sets.

For NNLO, $\chi^2/\text{d.o.f}$ is about 1.1 for about 3000 data points included in the fits.



Experimental Data for CT14

- Based on CT10 data set, but updated with new HERA F_L and F_2^c , and dropped Tevatron Run 1 CDF and D0 inclusive jet
- Included some LHC Run 1 (at 7 TeV) data:
ATLAS and LHCb W/Z production,
ATLAS, CMS and LHCb W-lepton charge asymmetry,
ATLAS and CMS inclusive jet
- Replace old by new D0 (9.7 1/fb) W-electron rapidity asymmetry data



Theory Analysis in CT14

- CT14 has 26 shape parameters, plus four extreme sets for describing s- and g-PDFs in small-x region. In comparison, CT10 has 24 shape parameters, plus two extreme sets for describing g-PDFs in small-x region.
- More flexible parametrization – gluon, d/u at large x, and both d/u and dbar/ubar at small x, strangeness (assuming sbar = s)
- Non-perturbative parametrization form:

$$x f_a(x) = x^{a_1} (1-x)^{a_2} P_a(x)$$

where $P_a(x)$ is expressed as a linear combination of Bernstein polynomials to reduce the correlation among its coefficients.



Theory Analysis in CT14

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- Choose experimental data with $Q^2 > 4 \text{ GeV}^2$ and $W^2 > 12.5 \text{ GeV}^2$ to minimize higher-twist, nuclear correction, etc., and focus on perturbative QCD predictions.
- PDFs are parametrized at $Q=1.3 \text{ GeV}$.
- Take $\alpha_s(M_Z) = 0.118$, but also provide α_s -series PDFs.
- Use s-ACOT- χ prescription for heavy quark partons, and take pole mass $M_c = 1.3 \text{ GeV}$ and $M_b = 4.75 \text{ GeV}$
- NNLO calculations for DIS, DY, W, Z, except jet (at NLO).
- Correlated systematic errors are taken into account.
- Check Hessian method results by Lagrangian Multiplier method which does not assume quadratic approximation in chi-square.



*Impact of HERA I + II data on CT PDF
analysis:*

CT14HERA2

PDF parametrization in CT14HERA2

- Use the CT14 PDF functional forms at initial scale Q_0 .

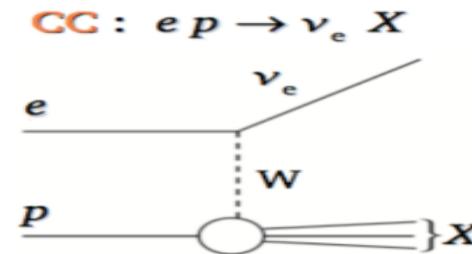
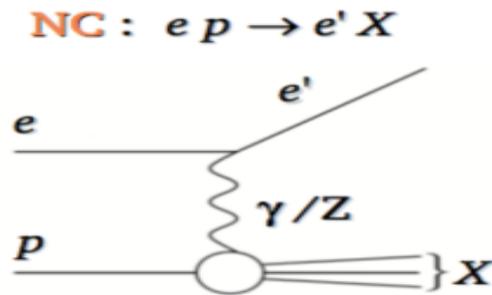
$$x f_a(x, Q_0) = x^{a_1} (1 - x)^{a_2} P_a(x)$$

Except:

- **CT14HERA2** has **27** shape parameters, plus **two** extreme sets for describing g-PDF in small-x region. In comparison, **CT14** has **26** shape parameters, plus **four** extreme sets for describing s- and g-PDFs in small-x region.
- Add one more shape parameter (in total 3) for describing **s-PDF**. ($a_1(s)=a_1(\bar{s})$ no longer tied to $a_1(\bar{u}) = a_1(\bar{d})$.)

HERA I+II data

- H1 and ZEUS experiments at HERA for neutral current and charged current e^+p , e^-p scattering collected $\sim 1/\text{fb}$ of data.
- $E_p = 920, 820, 575$ and 460 GeV and $E_e = 27.5$ GeV.



[arXiv:1506.06042](https://arxiv.org/abs/1506.06042)

Cross sections for NC interactions have been published for

$$0.045 < Q^2 < 50000 \text{ GeV}^2 \quad 6 \cdot 10^{-7} < x_{Bj} < 0.65$$

Cross sections for CC interactions have been published for

$$200 \leq Q^2 \leq 50000 \text{ GeV}^2 \quad \text{and} \quad 1.3 \cdot 10^{-2} \leq x_{Bj} \leq 0.40$$

- **HERAI+II** data has **1120** data points with
 - $Q^2 > 4 \text{ GeV}^2$ and $W^2 > 12.5 \text{ GeV}^2$,
 - 162 correlated systematic errors,
 - 7 procedural uncertainties;
 - separated into four sets, depending on whether e+ or e- beam, neutral or charged current, at various collider energies.
- **HERA-1** data has **579** data points with
 - $Q^2 > 4 \text{ GeV}^2$ and $W^2 > 12.5 \text{ GeV}^2$,
 - 110 correlated systematic errors,
 - 4 procedural uncertainties.
- CT14 with HERA1 has **about 3000** data points.

After replacing the HERA I with HERA I+II data, there are about **3300** data points in total, in which we have removed NMC muon-proton data (ID=106, with 201 data points). Its χ^2/npt is about 1.85 in CT14 fit.

Impact of the HERA +II data on the fit

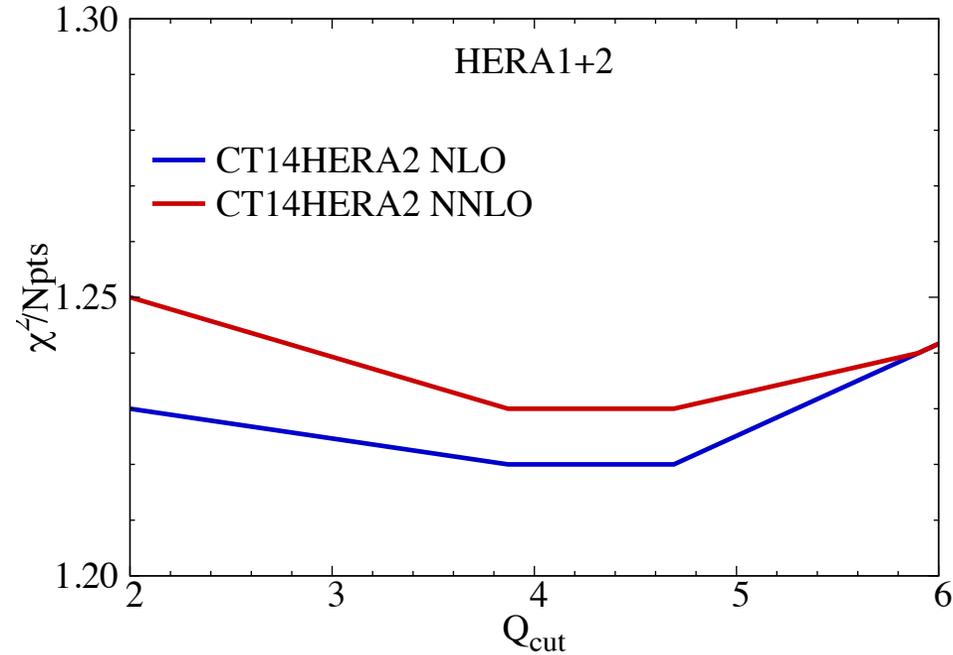
Summary of the χ^2 values for the HERA run I and HERA1+2 measurements in both CT14 and CT14HERA1+2 fits

| | $\chi^2_{\text{HERA I}}; N_{\text{pts}} = 579$ | $\chi^2_{\text{HERA1+2}}; N_{\text{pts}} = 1120$ |
|--------------------|--|--|
| CT14NLO | 590 (1.02) | 1402 |
| CT14NNLO | 591 (1.02) | 1471 |
| CT14HERA1+2(NLO) | 597 | 1374 (1.23) |
| CT14HERA1+2((NNLO) | 610 | 1403 (1.25) |

NNLO vs. NLO fits and impact of Q cut

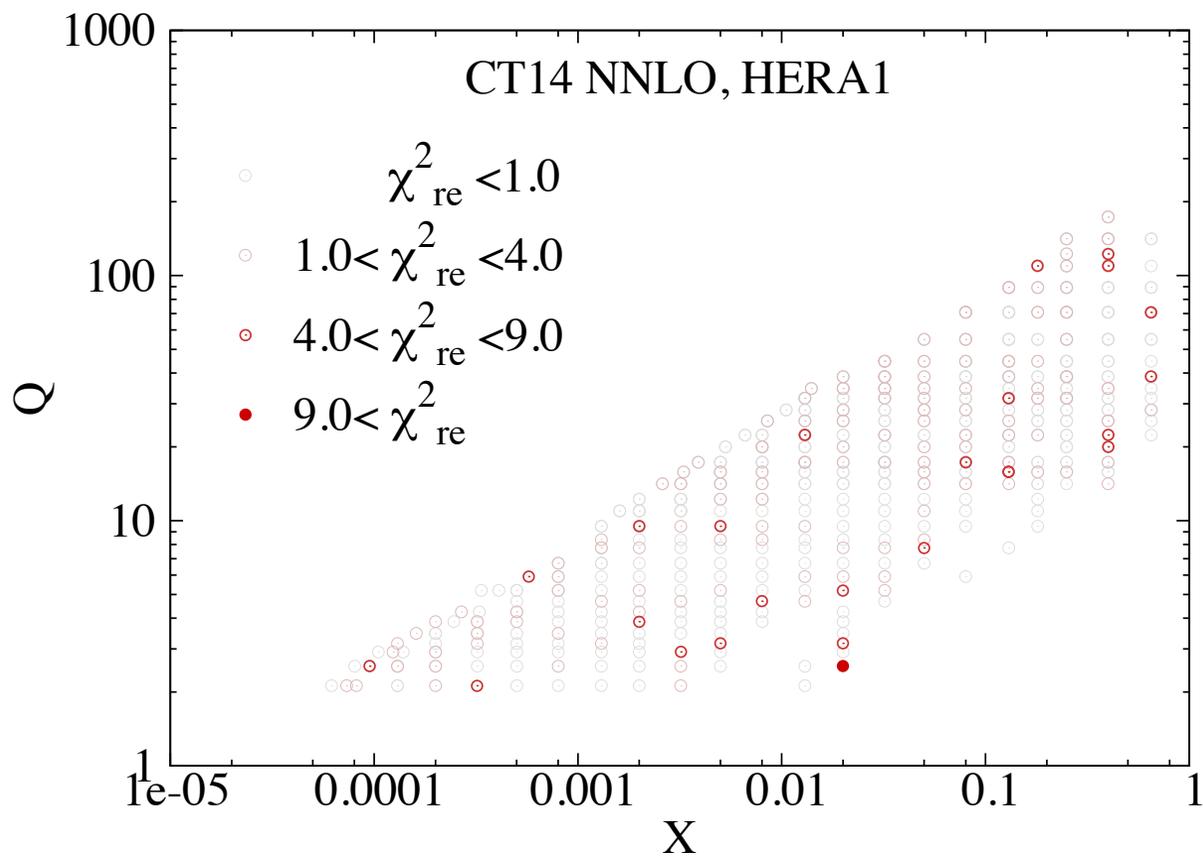
1.25 for
NNLO fit

1.23 for
NLO fit

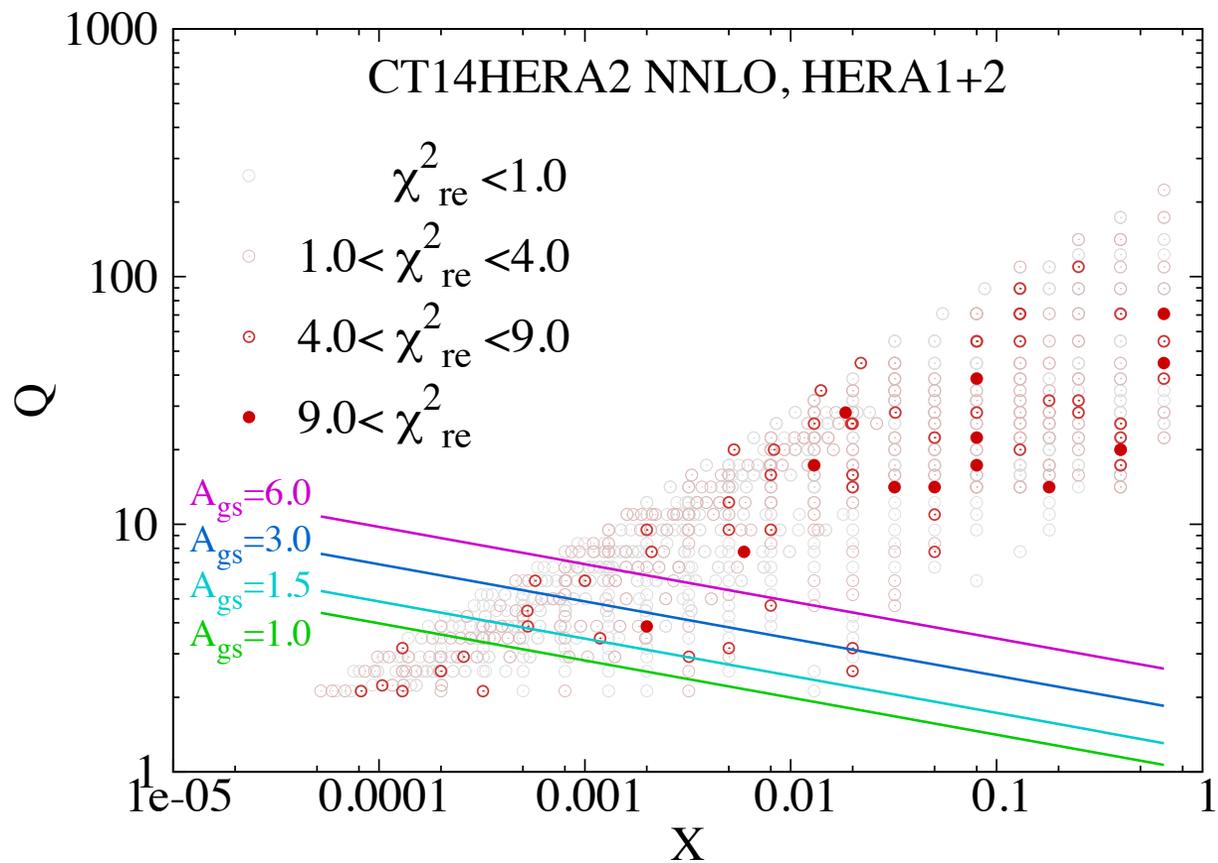


- Our nominal Q cut is 2 GeV.
- χ^2/N_{pts} increases above $Q_{cut}=5$ GeV and below 2 GeV.
- NNLO fit is slightly worse than NLO fit

The distribution of the χ^2 -residuals of HERA I and HERA2 ensembles in the (x, Q) plane for the CT14Hera2 fit.



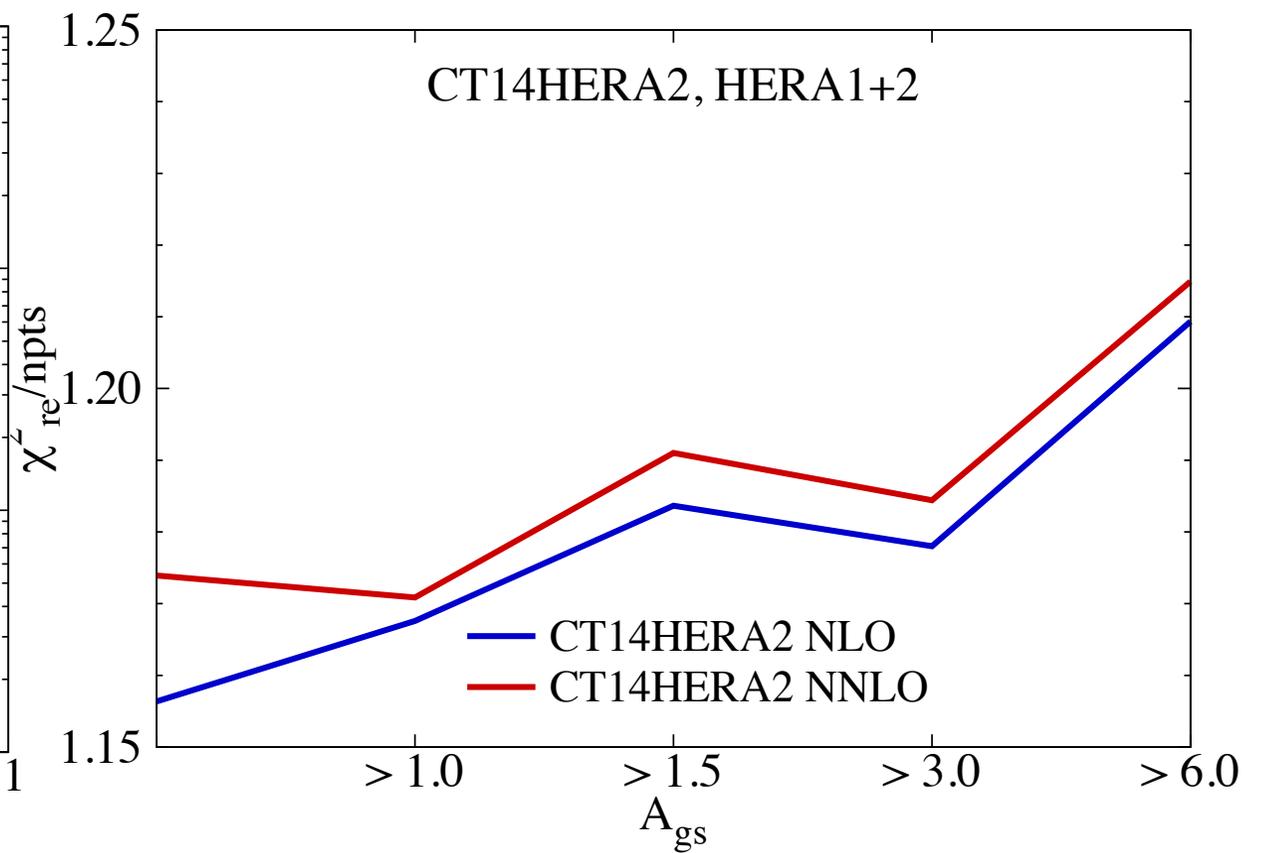
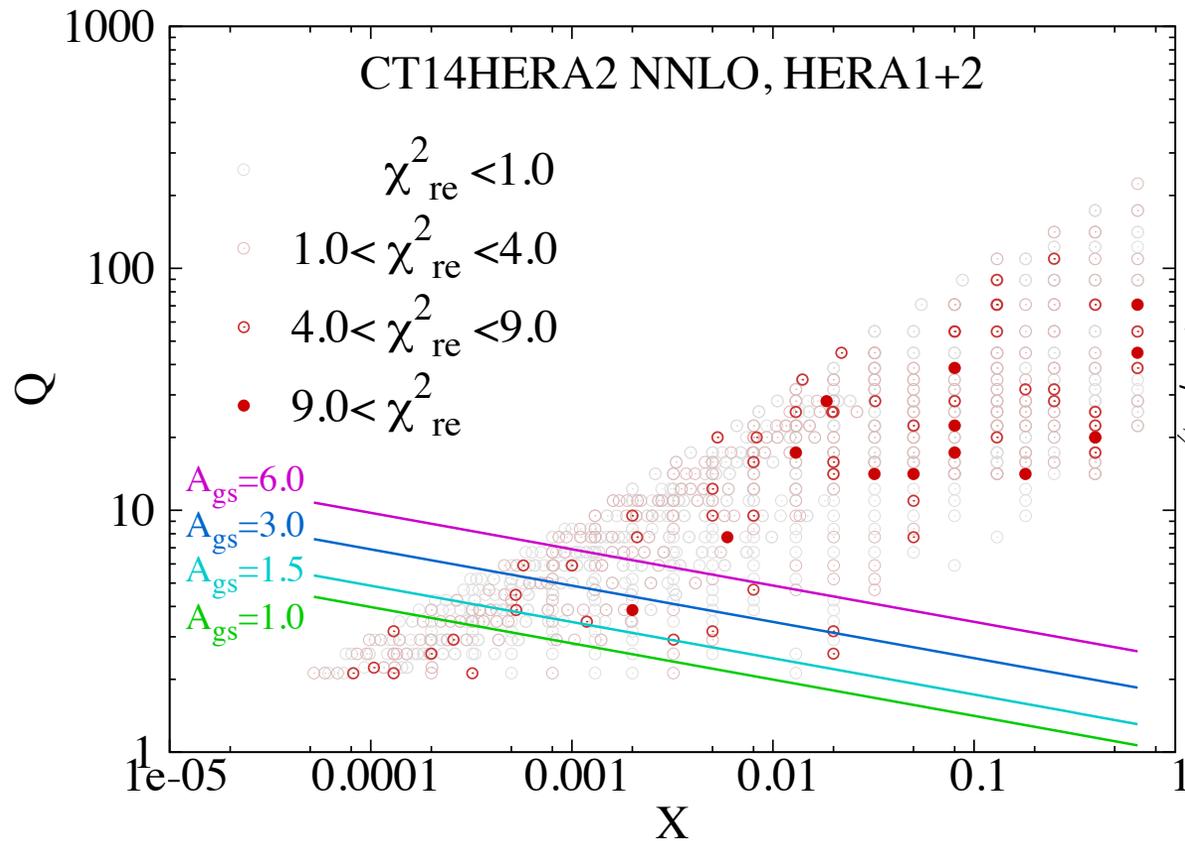
HERA I



NNLO fits

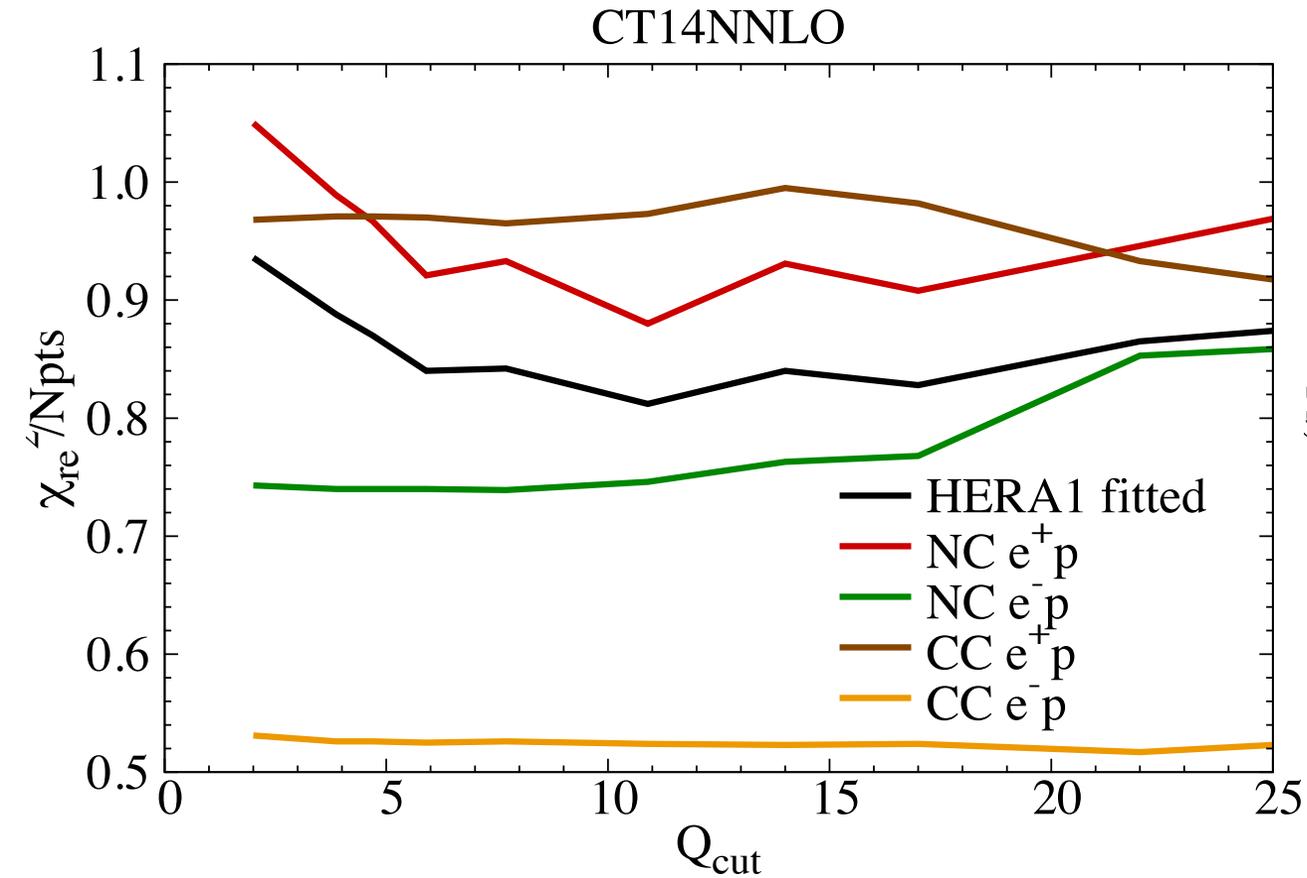
HERA I+II

Cuts on x - Q plane



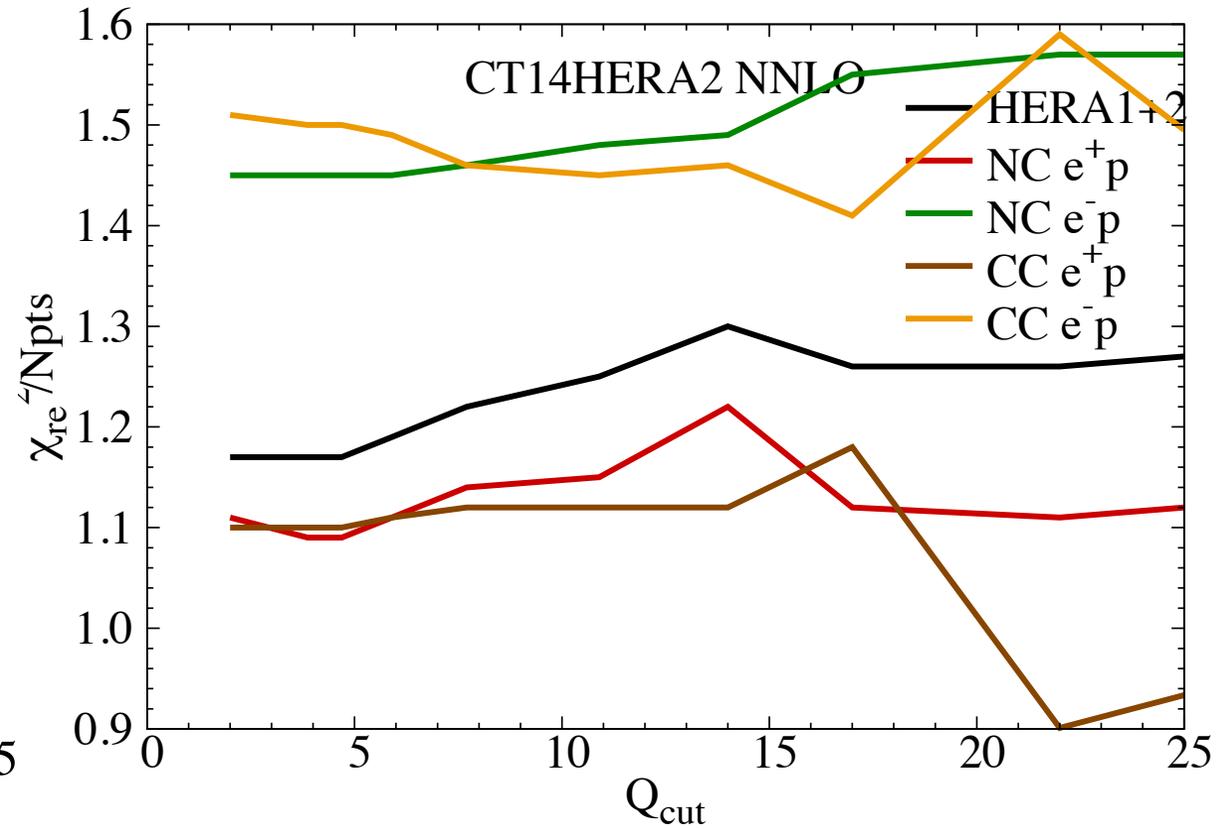
Geometric Scaling variable: $A_{\text{gs}} = Q^2 x^{0.3}$

Goodness of fit to data subsets



HERA I

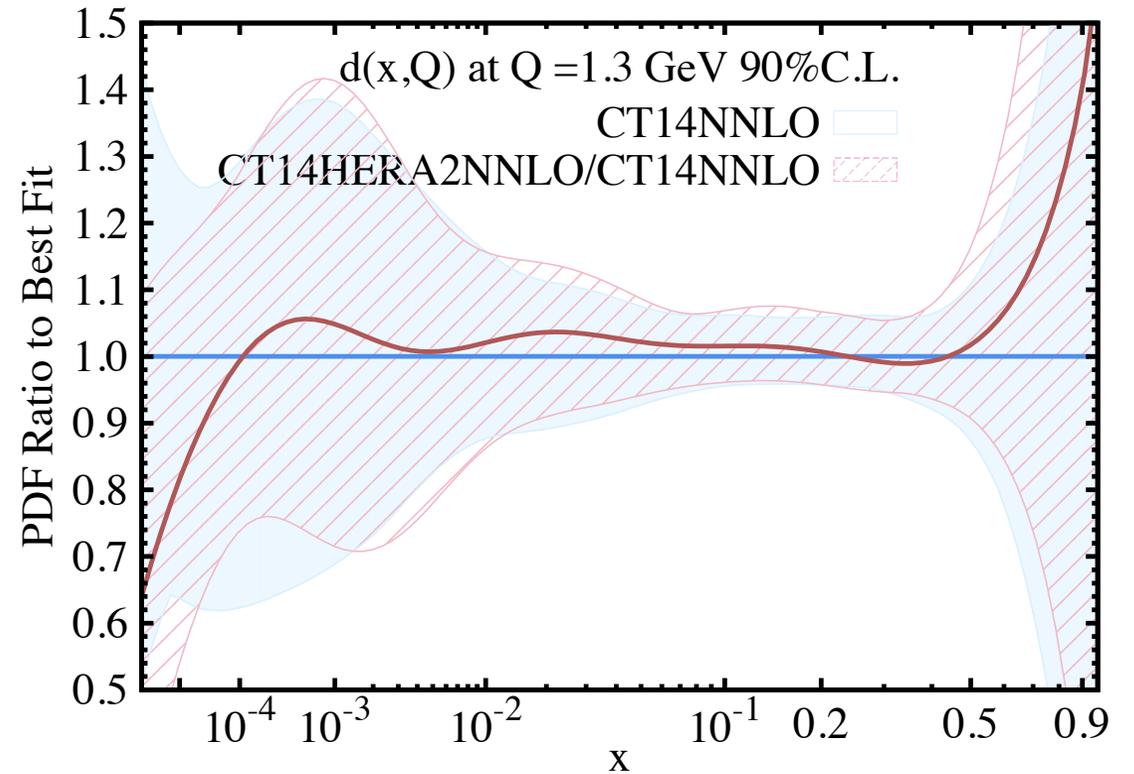
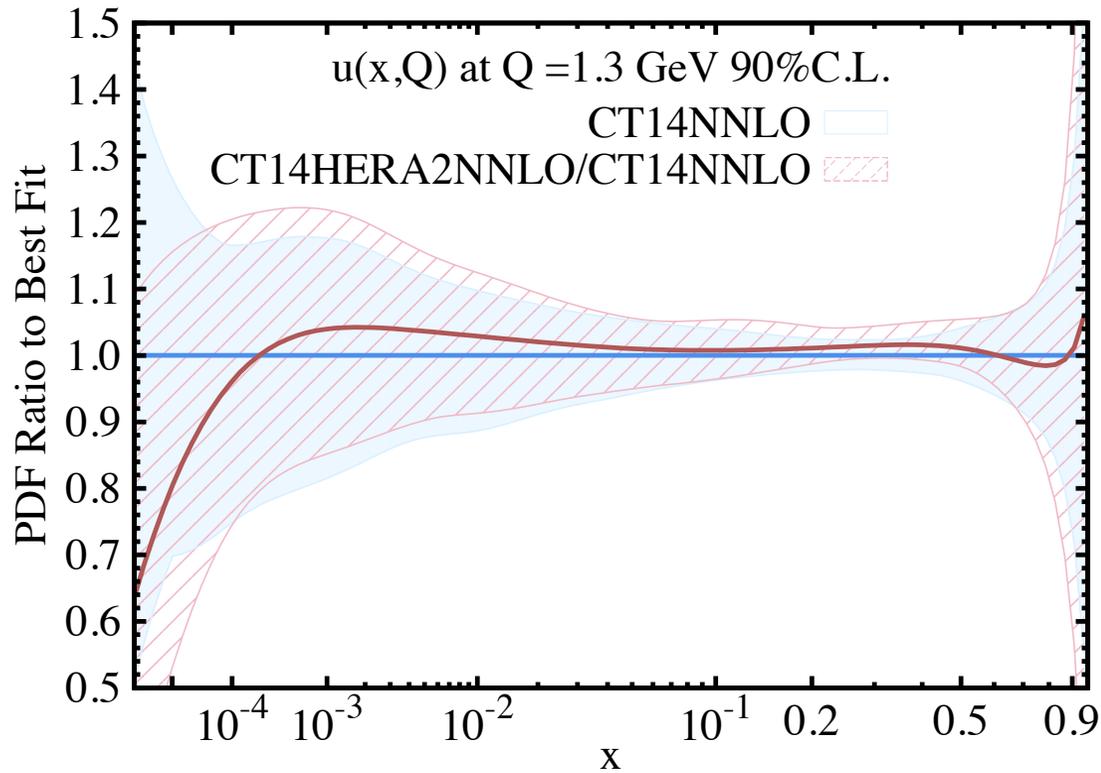
NNLO fits



HERA I+II

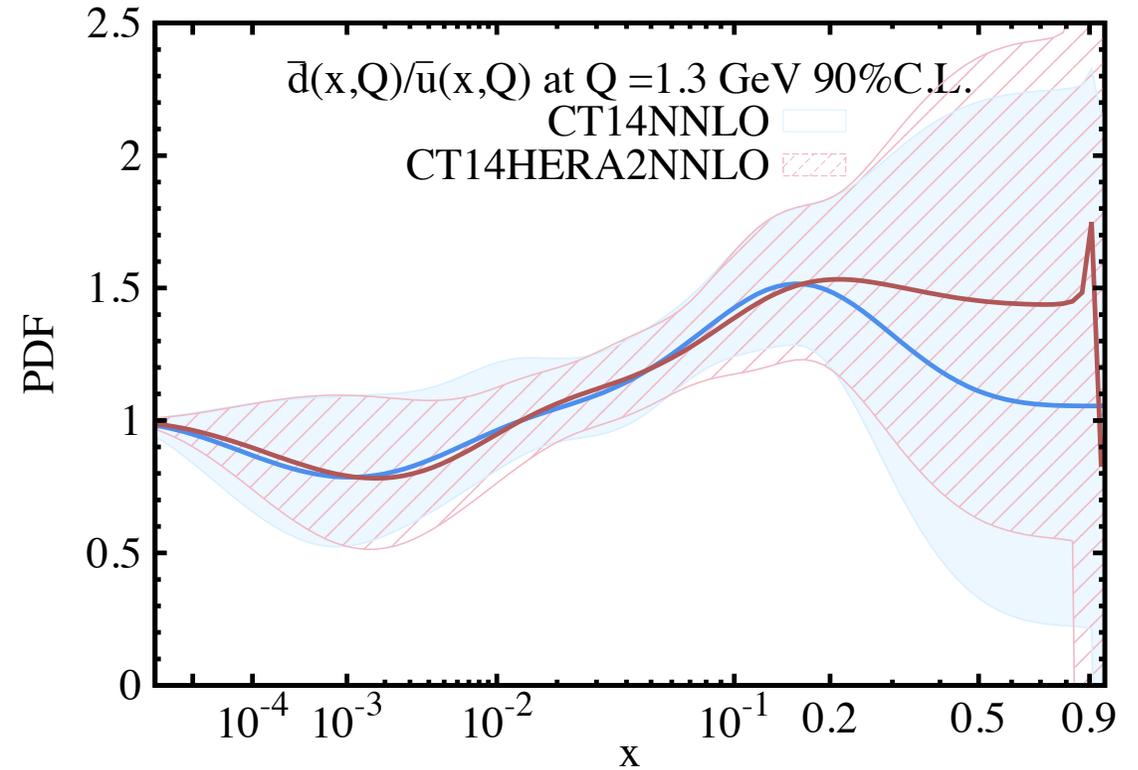
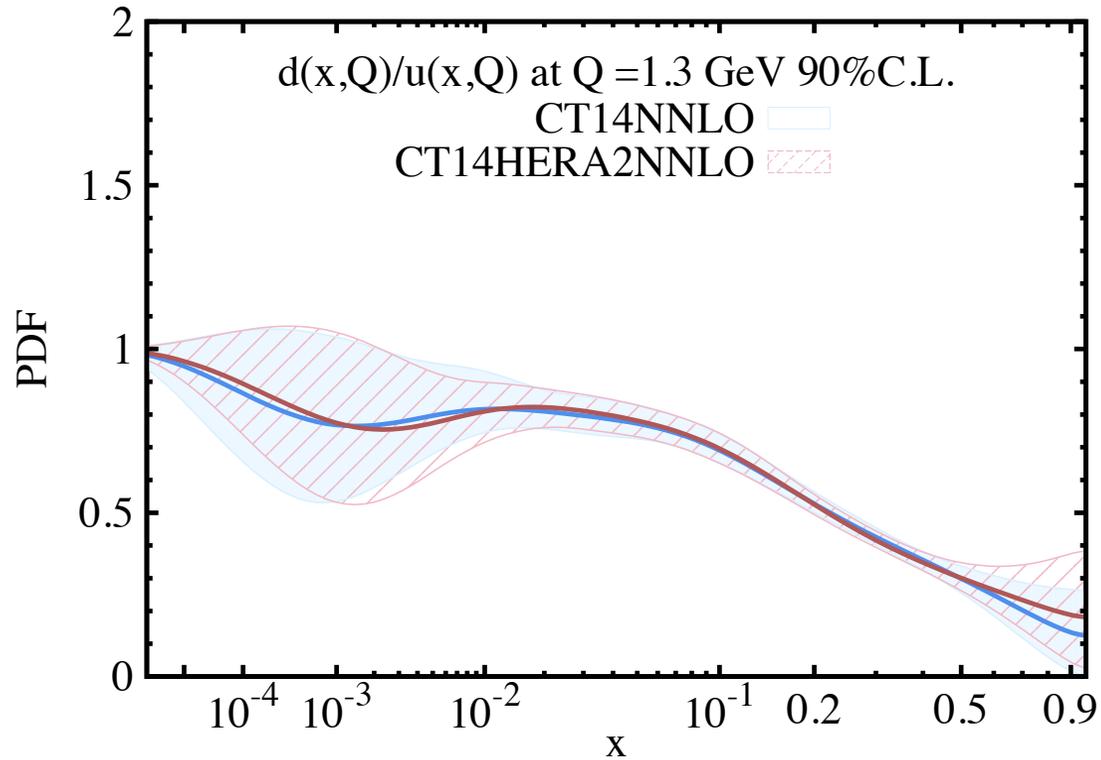
CT14HERA2 vs. CT14

u and d PDFs



HERAI+II data prefers slightly larger u and d at moderate x
Largest effect is u near $x \sim 0.3$, where new fit is near edge of old uncertainty.

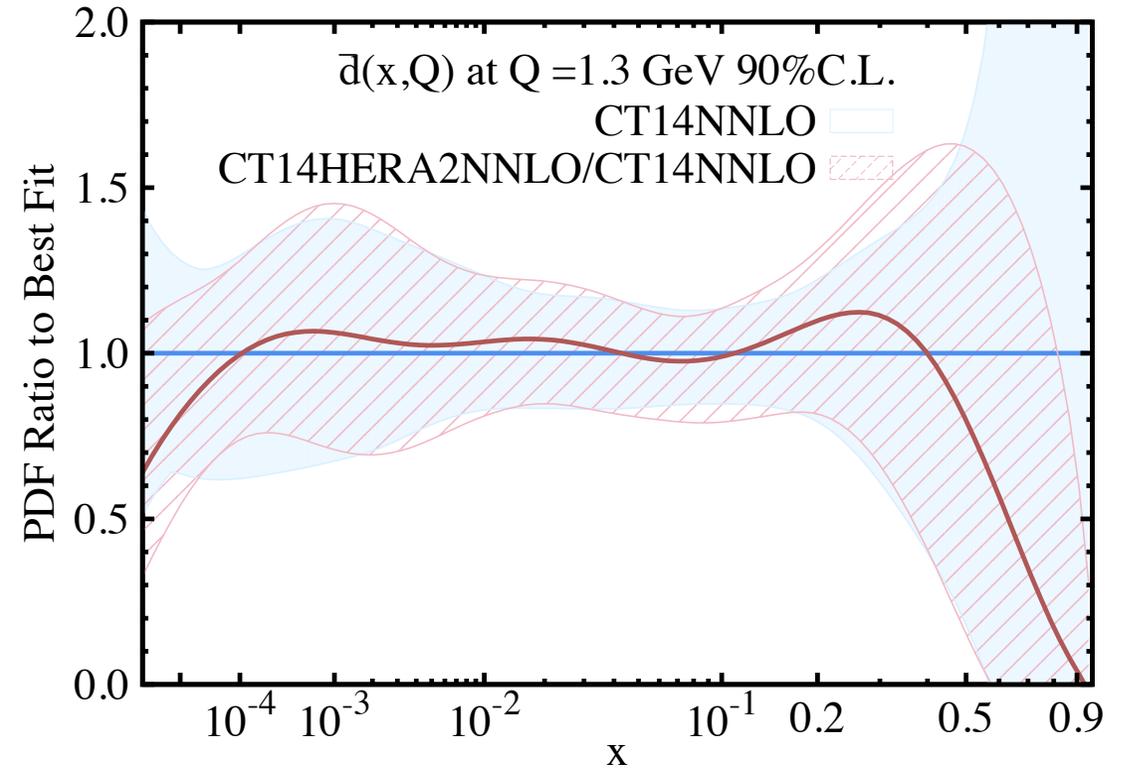
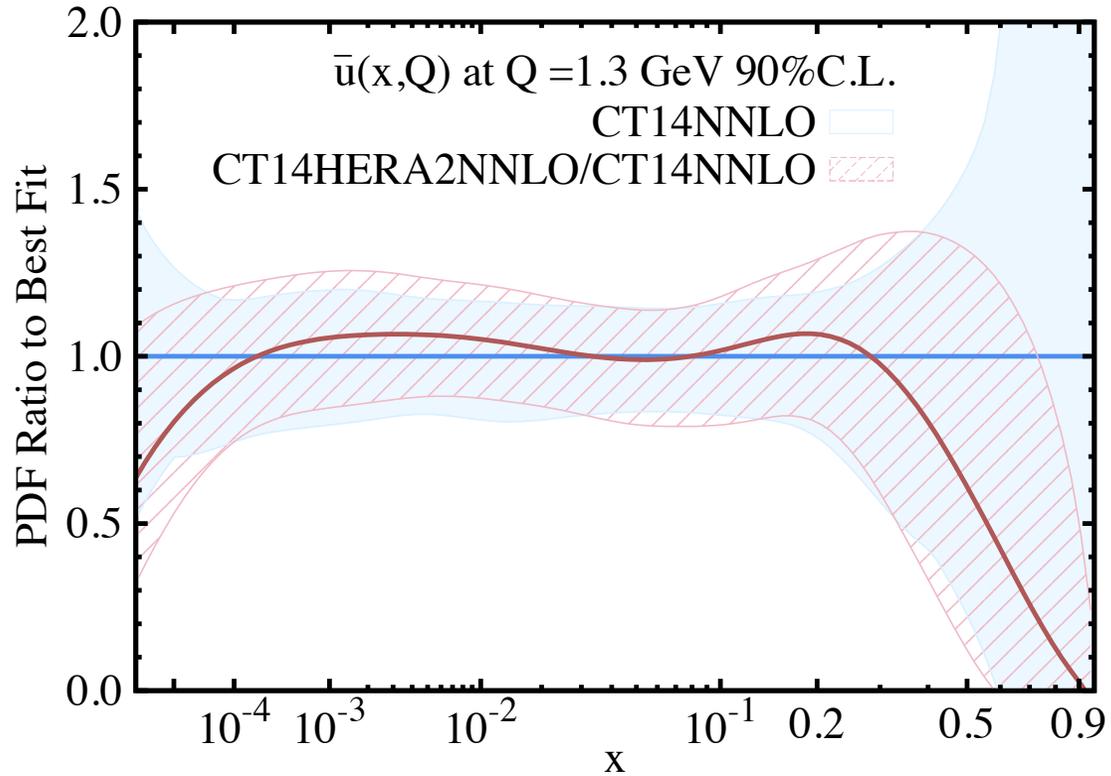
d/u and dbar/ubar PDFs



Changes are minimal, well within uncertainty bands.

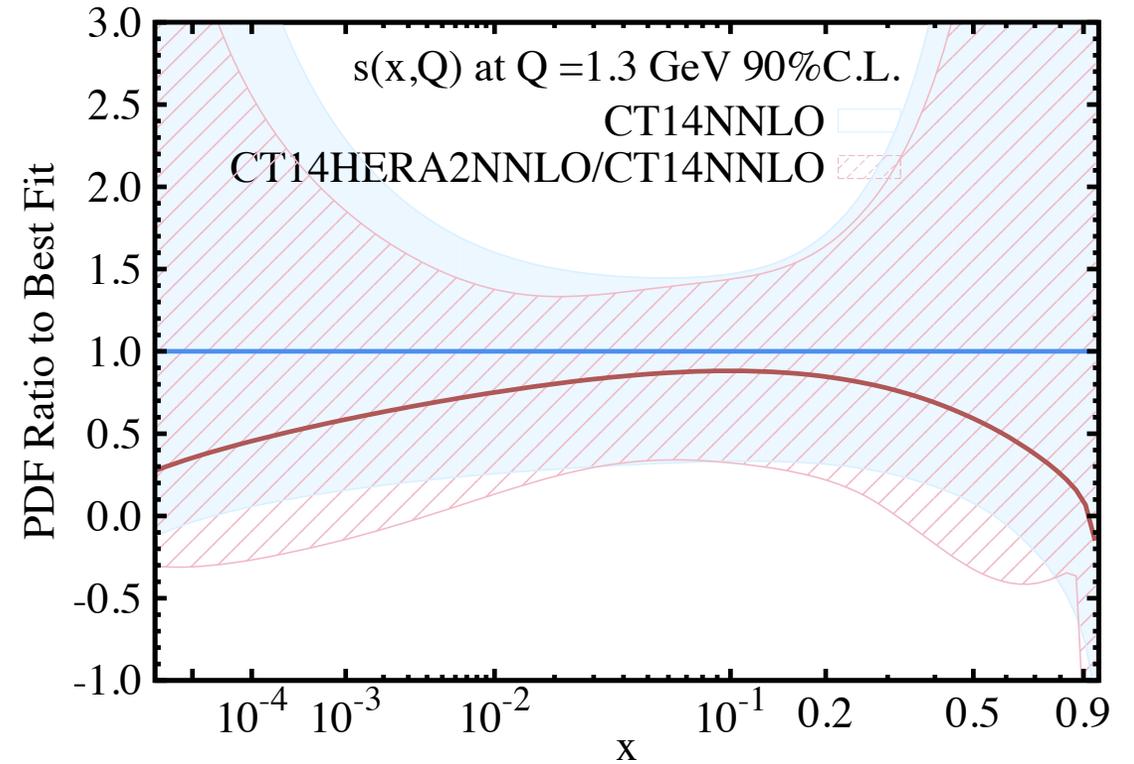
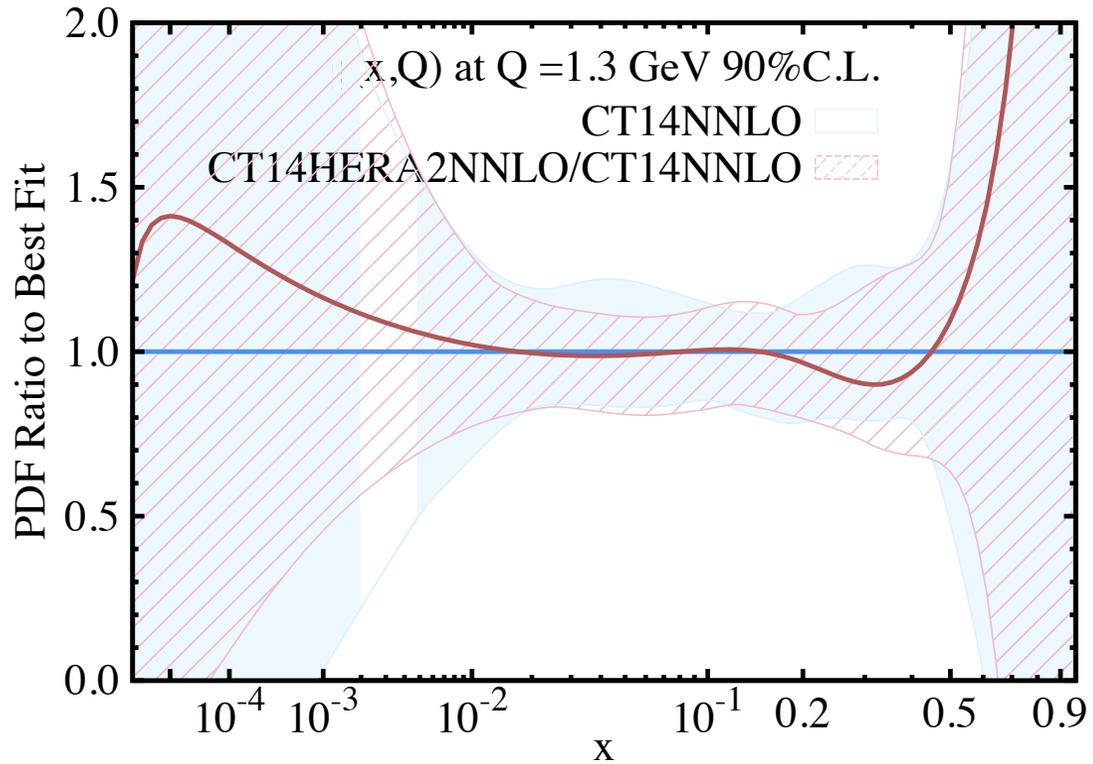
HERAI+II data prefers slightly smaller dbar/ubar around $x \sim 10^{-1}$.

ubar and dbar PDFs



Again changes are minimal, well within uncertainties.

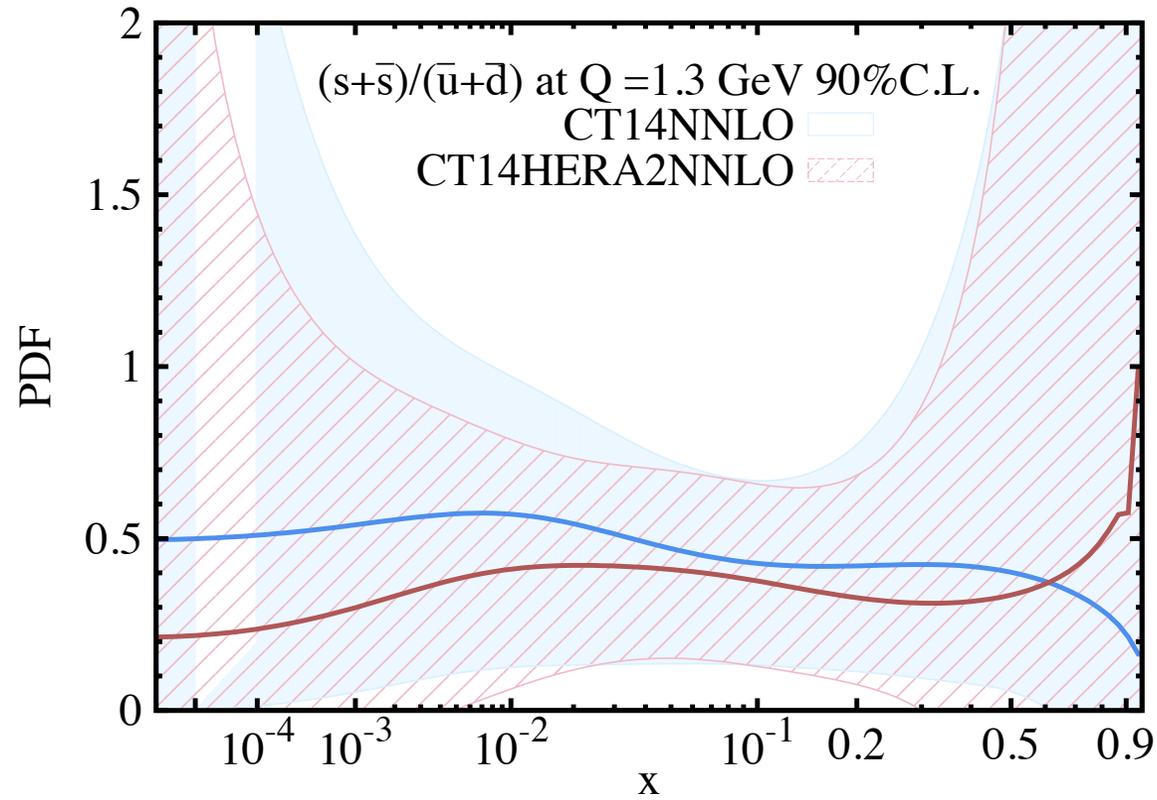
g and s PDFs



HERAI+II data prefers smaller gluon around $x \sim 0.2-0.5$.

Change in strange PDF mostly due to more flexible parametrization.

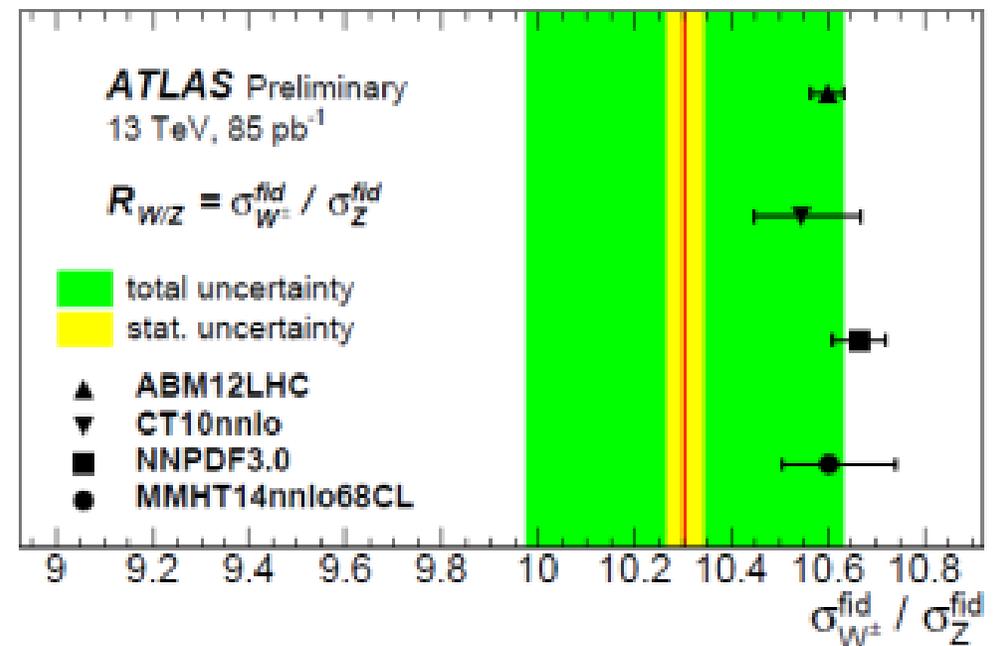
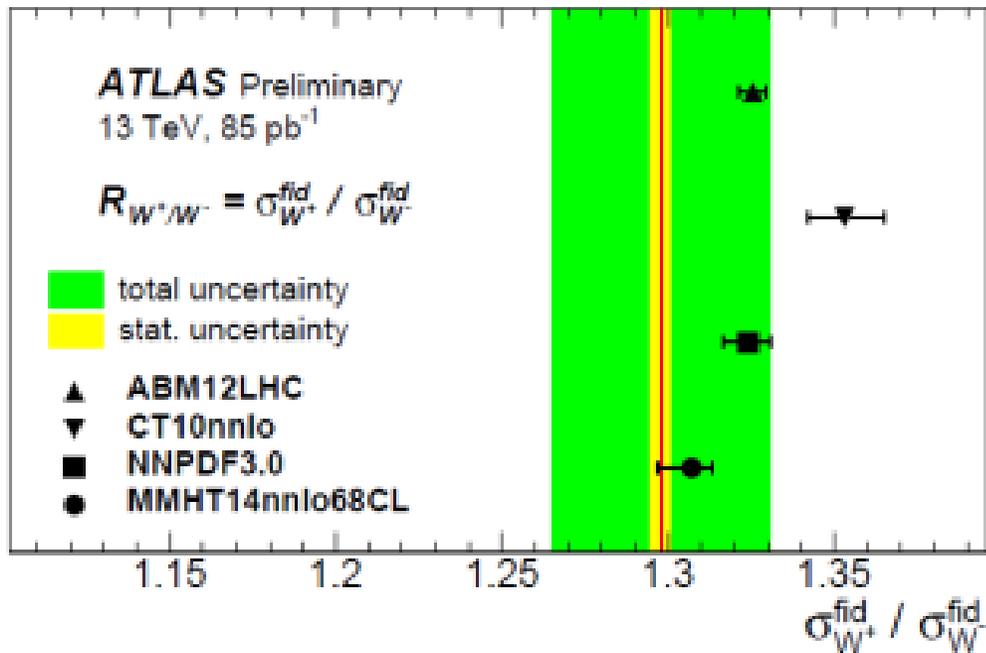
$(s+\bar{s})/(\bar{u}+\bar{d})$ PDFs



More-flexible strange PDF prefers smaller value,
but still with large uncertainty.

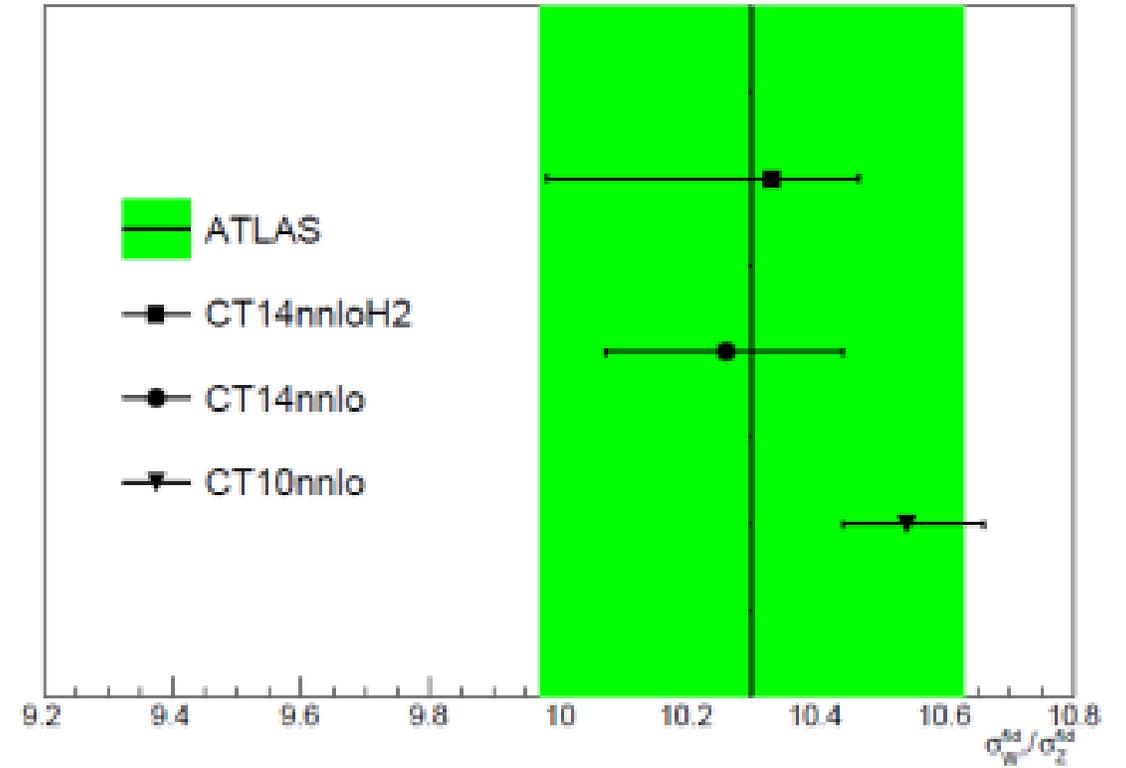
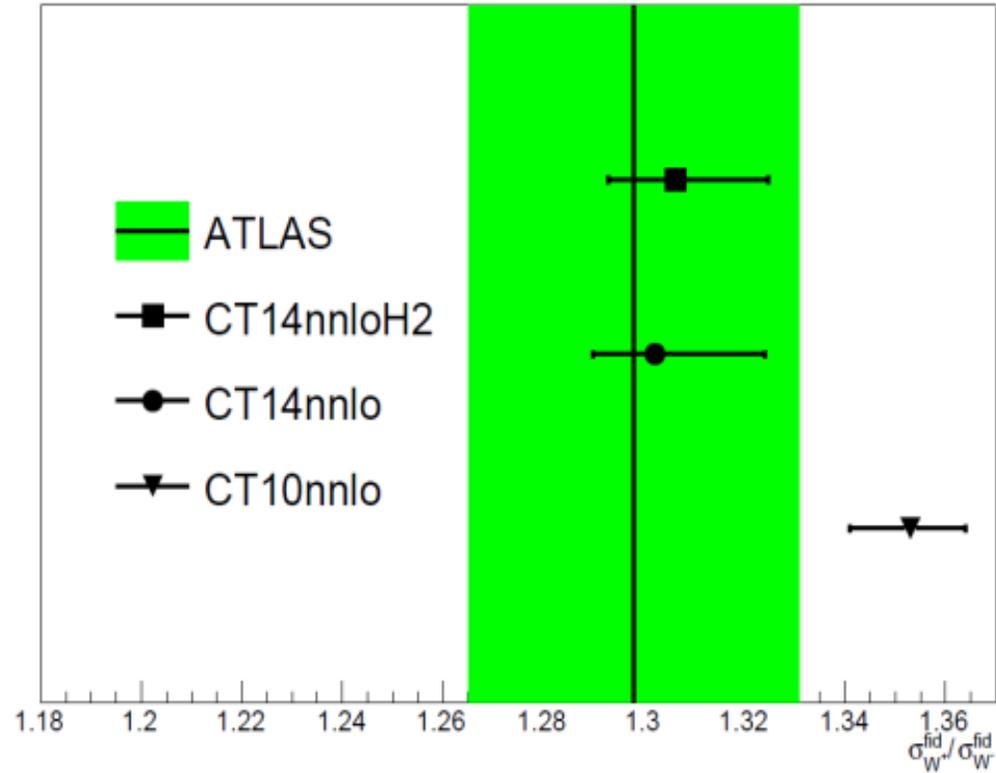
The cross section ratios: W^+/W^- and $(W^++W^-)/Z$

- Measured by the ATLAS and CMS collaboration and proved to be powerful tools to constrain PDFs
- The ratio W^+/W^- is mostly sensitive to the difference of **u valence** and **d valence** quark distributions.
- The ratio of $(W^++W^-)/Z$ constrains the **strange-quark** distribution.



The cross section ratios: W^+/W^- and $(W^++W^-)/Z$

CT14HERA2 vs. CT14



$p_T^l > 25 \text{ GeV}$, $|\eta| < 2.5$, $66 < m_{ll} < 116 \text{ GeV}$

$p_T^l > 25 \text{ GeV}$, $p_T^\nu > 25 \text{ GeV}$, $|\eta| < 2.5$, $m_T > 50 \text{ GeV}$



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***New interpretation of CT14QED Photon
PDFs and CMS data***

CT14QED



“Inclusive” Photon PDFs

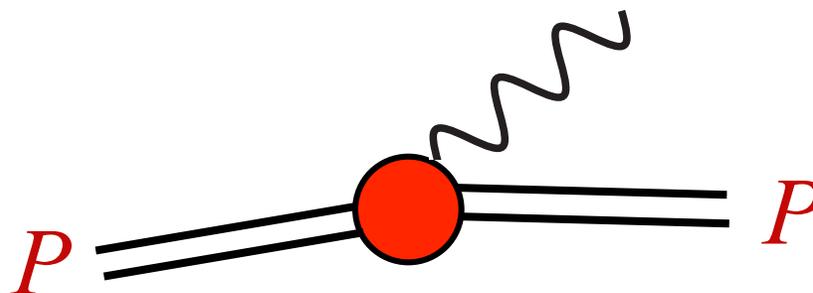
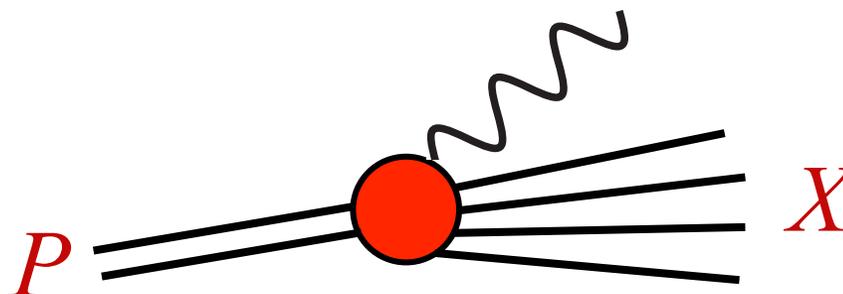
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- “Inclusive” Photon PDF contains

- “inelastic” components

and

- “elastic” components



- Martin and Ryskin: (arXiv:0909.4223v2)
 - Dominant contribution at scale Q_0 is “elastic” and calculable
 - Equivalent Photon Approximation: determined from photon form factors
 - “Elastic” photon at $Q_0=1.3$ GeV carries momentum fraction 0.15%.

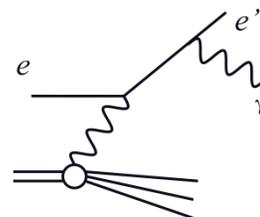


CT14QED Photon PDFs

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- CT14QED Photon PDF constrained by ZEUS DIS + isolated photon data:

- $p_0^\gamma \leq 0.14\%$ at 90 % C.L.



- CT14QED Photon PDF should be interpreted as “Inelastic” component.

- ZEUS: “At least one reconstructed track, well separated from the electron, was required, ensuring some hadronic activity which suppressed deeply virtual Compton scattering (DVCS) to a negligible level.”

- This requirement also removes “elastic” component of photon PDF.



CT14QED Photon PDFs

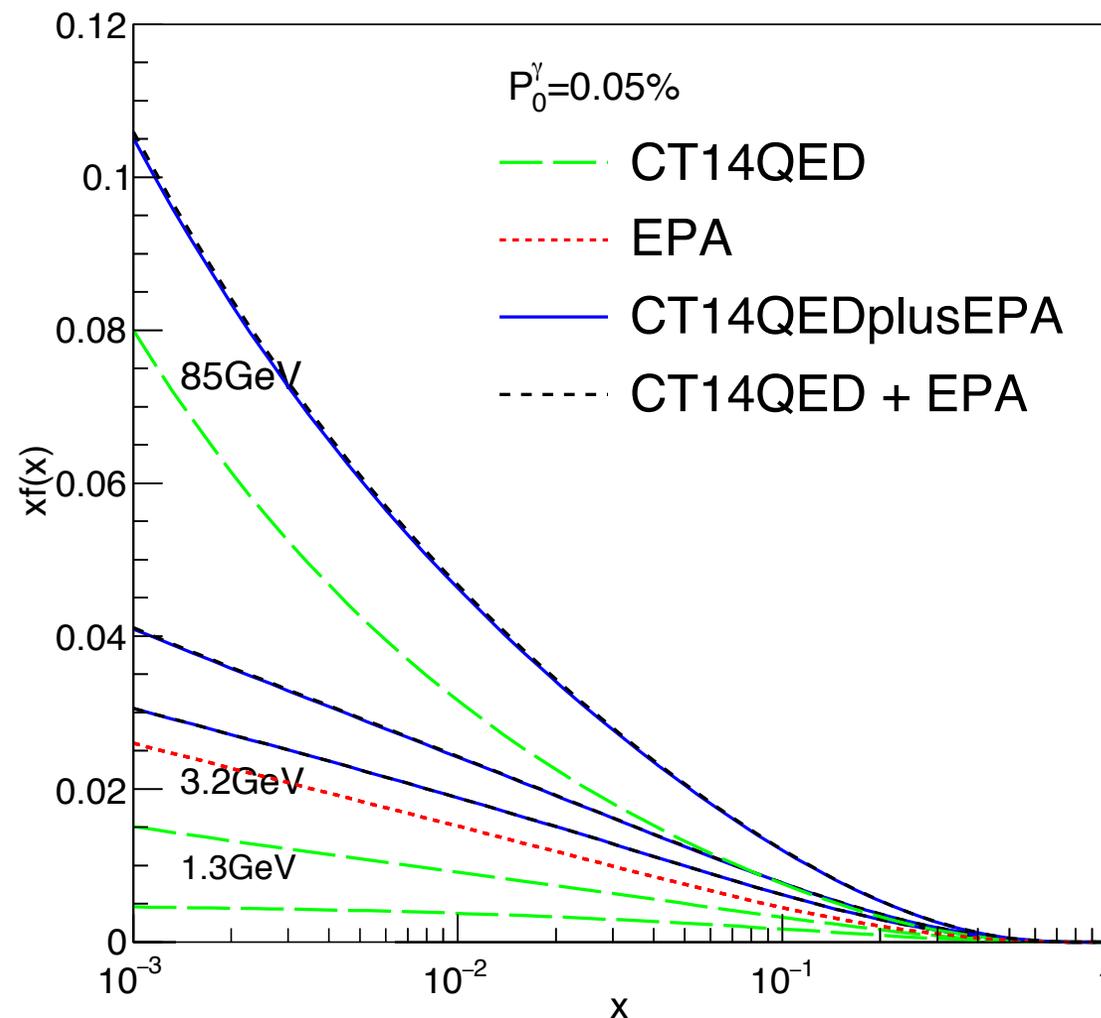
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- Important point:

$$(f_{\text{EPA}} + f_{\text{inelastic}})(x, Q) \approx f_{\text{EPA}}(x, Q) + f_{\text{inelastic}}(x, Q)$$

- $f_{\text{EPA}}(x, Q)$ changes little from Q_0 to Q because of falloff from form factor
- Up to corrections of order α , the photon PDF evolves additively:

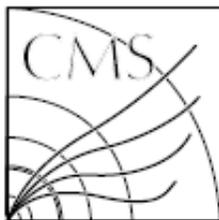
$$f(x, Q) \approx f(x, Q_0) + \int_{Q_0^2}^{Q^2} \frac{dQ^2}{Q^2} \frac{\alpha}{2\pi} P_{\gamma q} \circ \sum e_q^2 f_q(x, Q)$$





CMS $AA \rightarrow W^+ W^-$ Analysis

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CERN-PH-EP/2013-084
2013/08/22

CMS-FSQ-12-010

Study of exclusive two-photon production of W^+W^- in pp collisions at $\sqrt{s} = 7$ TeV and constraints on anomalous quartic gauge couplings

The CMS Collaboration*

(Also newer analysis at 8 TeV, 2015/06/16)



$CMS A A \rightarrow W^+ W^-$ Analysis

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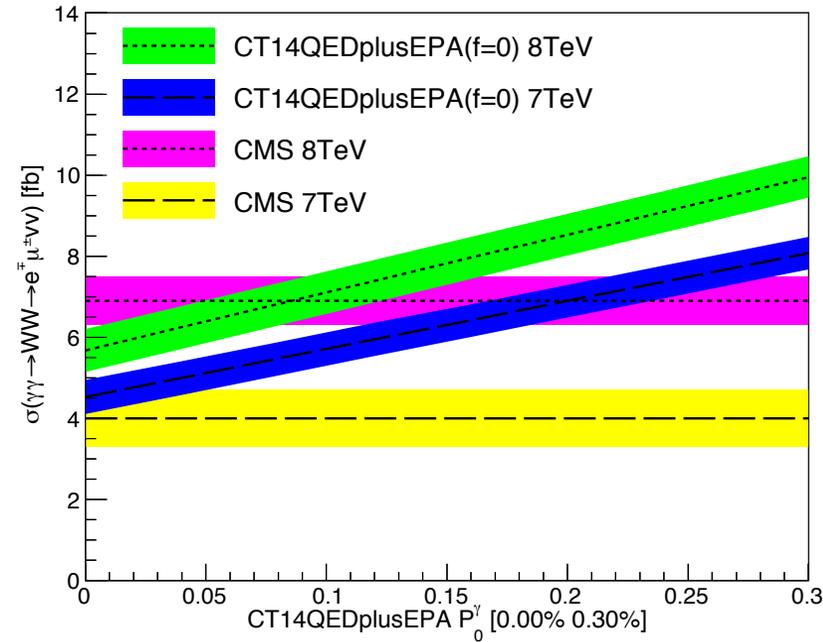
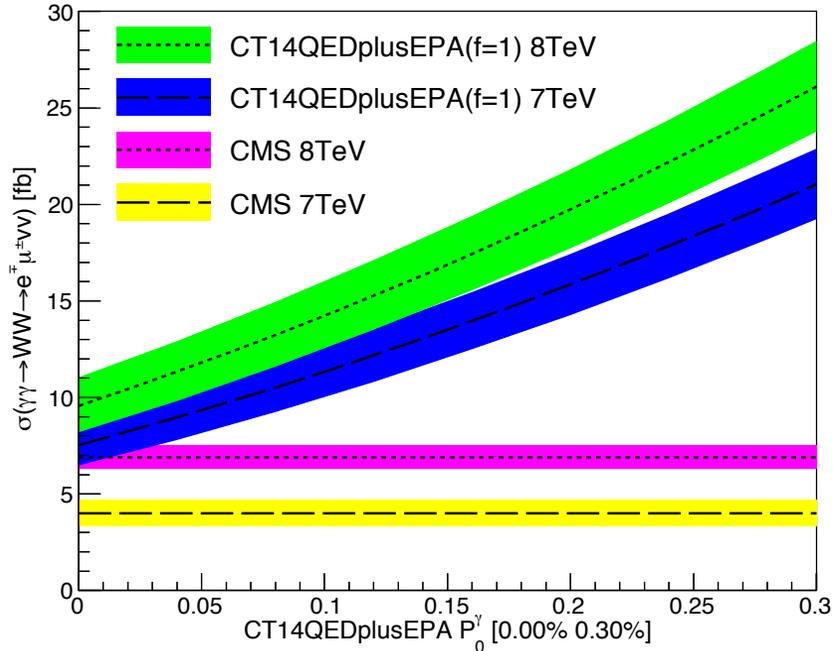
- Using off-Z-peak $\mu^+ \mu^-$ data they obtained an “effective photon luminosity” used to calculate the $W^+ W^-$ cross section
- We can compare this to our calculation using photon PDFs
- But:
 - They require zero charged tracks to isolate photon-photon production.
 - This removes some, but not all, inelastic contribution
 - Events can be divided into: elastic-elastic, elastic-inelastic, inelastic-inelastic, depending on whether 0, 1, or both protons dissociate.
- Crude approximation:
 - Assume all elastic-elastic and elastic-inelastic events pass the cut, while inelastic-inelastic are reduced by a fraction f , with $0 < f < 1$.
 - (Double-dissociative are most affected by re-scattering.)



Comparison with CMS predictions

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$f=1$



$f=0$

- Experimental error bands are 68% CL, Theory error bands are scale variation.
- Theory bands plotted as function of initial “inelastic” photon momentum
- $f=1$ is strongly disfavored, especially for the 7 TeV analysis
- Even if no double-dissociative events pass the zero-track cut, there are constraints on the initial photon momentum: $p_0^\gamma \leq 0.05\%$ (7 TeV), $p_0^\gamma \leq 0.16\%$ (8 TeV)
- Consistent with DIS + Isolated photon analysis



Photon-Photon Luminosity

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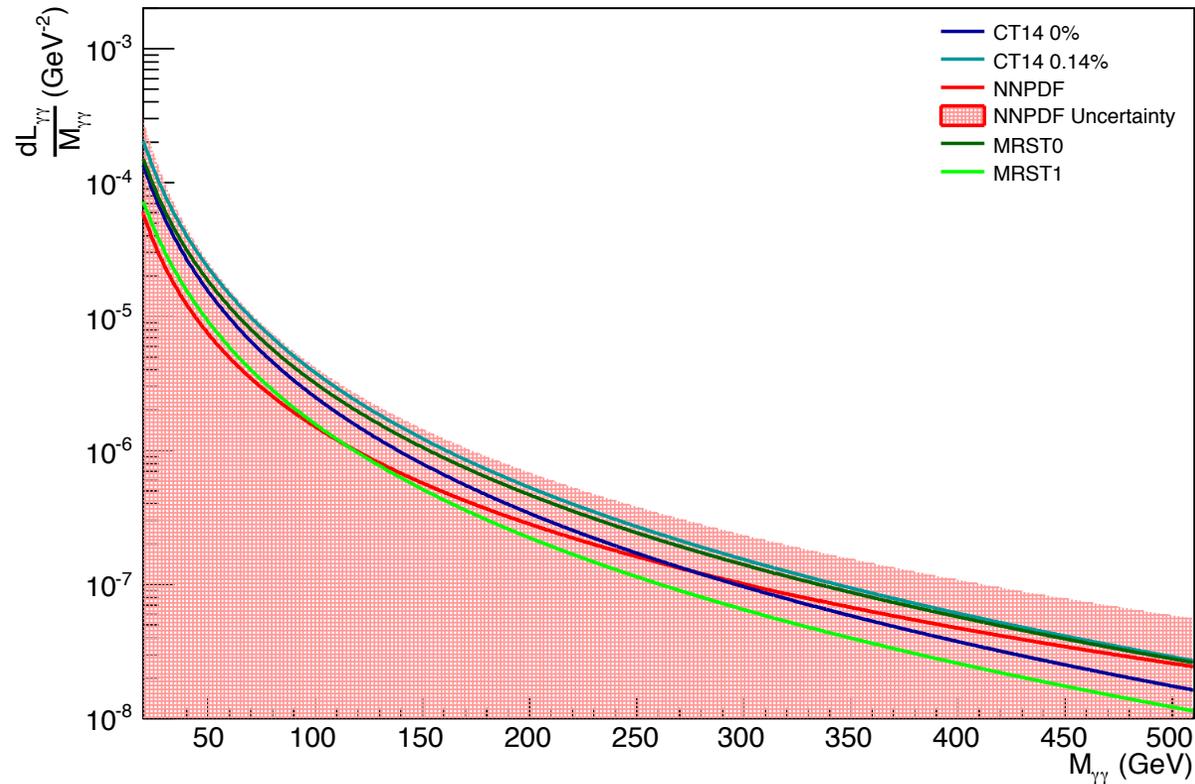


FIG. 4: Photon-photon luminosity for an invariant mass of 20 GeV to 500 GeV for 13 TeV collider energy

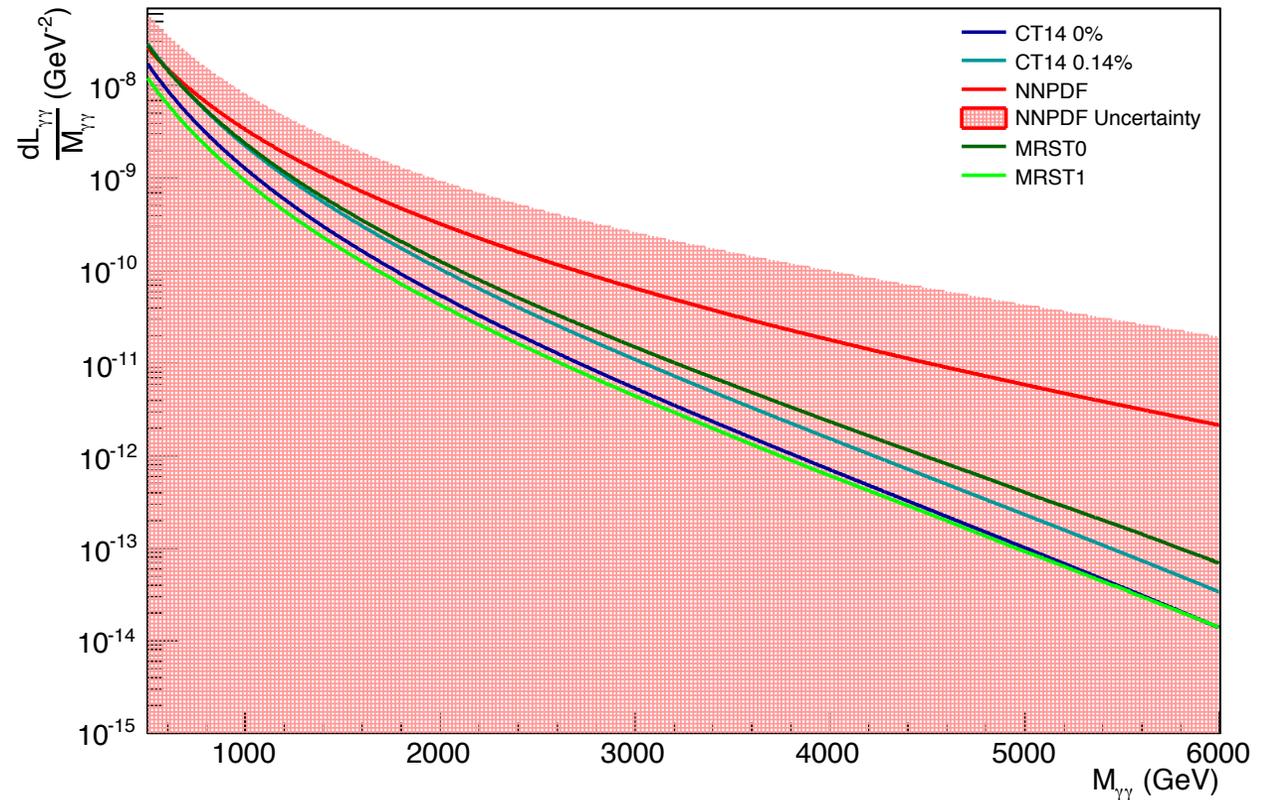


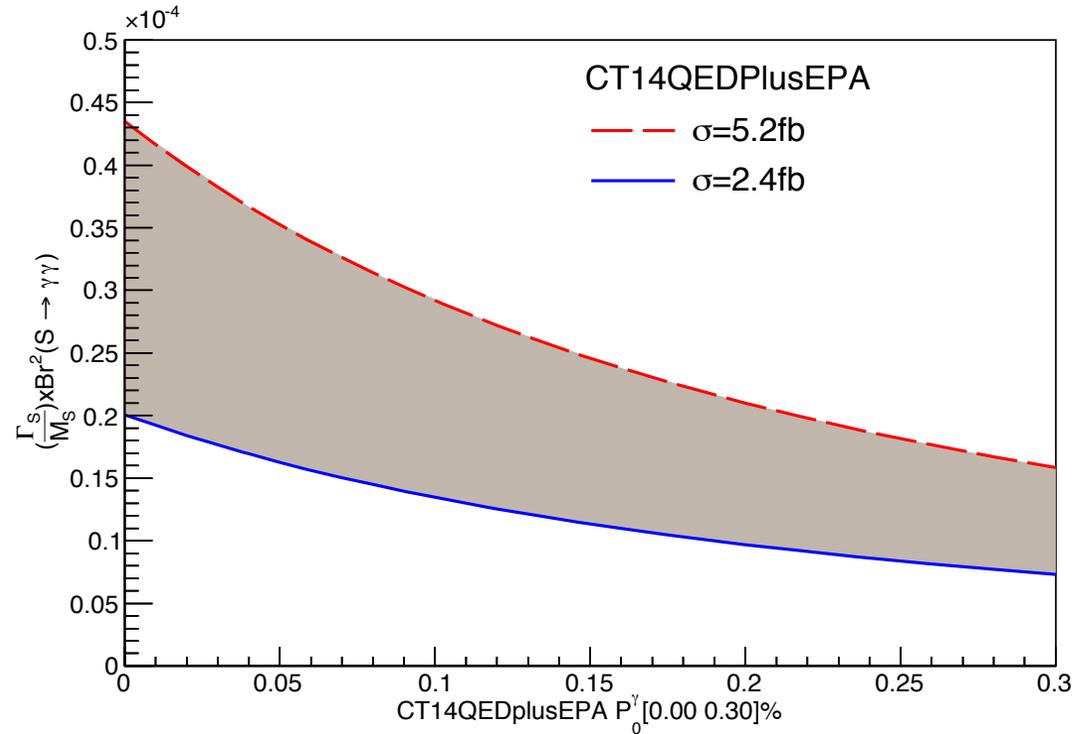
FIG. 5: Photon-photon luminosity for an invariant mass of 500 GeV to 6000 GeV for 13 TeV collider energy

- Central NNPDF photon harder at large x .



Constraints on CMS 750 GeV excess

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- If CMS 750 excess is due to resonant production in gamma-gamma channel:
 - Constraints on cross section (John Paul Chou, talk at Moriond, March 20,2016)
- From calculated photon-photon luminosities, obtain constraints on Γ/M
- Assuming $Br \sim 1$, this model requires small $\Gamma/M \sim 10^{-4}$ to fit the data.

Conclusions

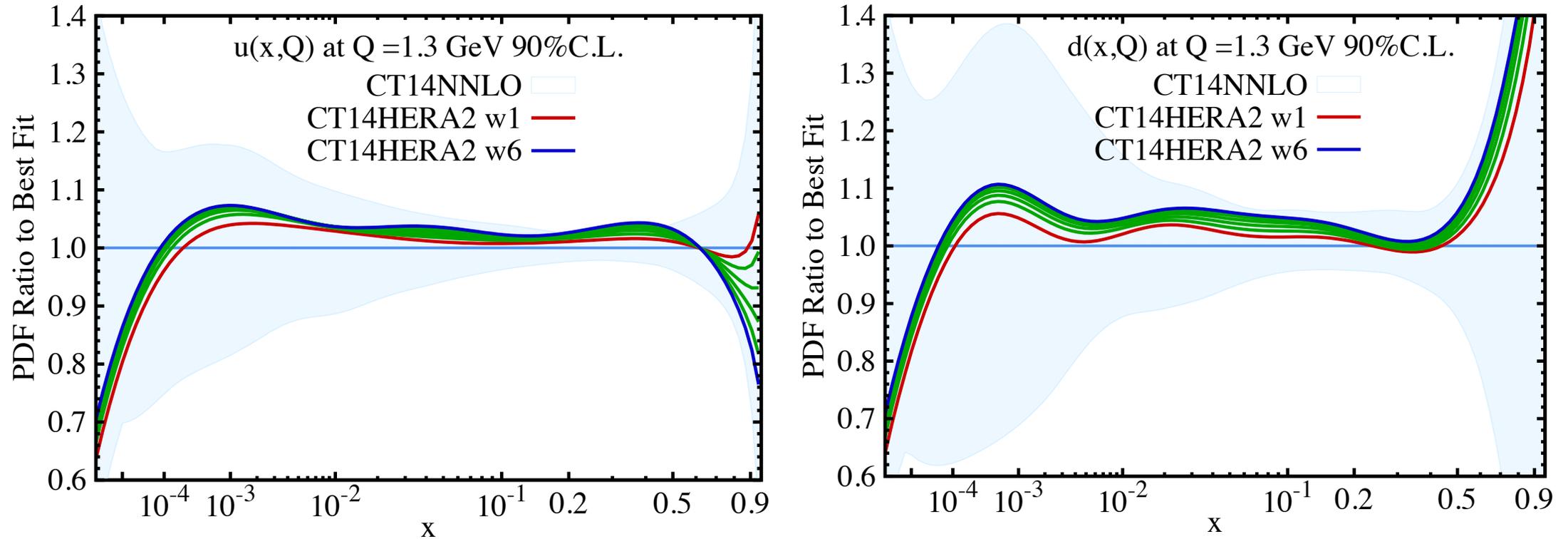
- Impact of HERA I + II data on CT PDF analysis: **(CT14HERA2)**
 - Worse fit than HERA I, especially in e^-p NC and CC channels
 - But changes to PDFs generally small
- New interpretation of CT14QED photon PDFs and CMS data:
 - **CT14QEDplusEPA**
 - CMS analysis consistent with constraints from ZEUS on inelastic contribution
 - Better understanding of Photon PDFs important for new physics analyses
- We are including more LHC data into the global analysis.



Backup Slides

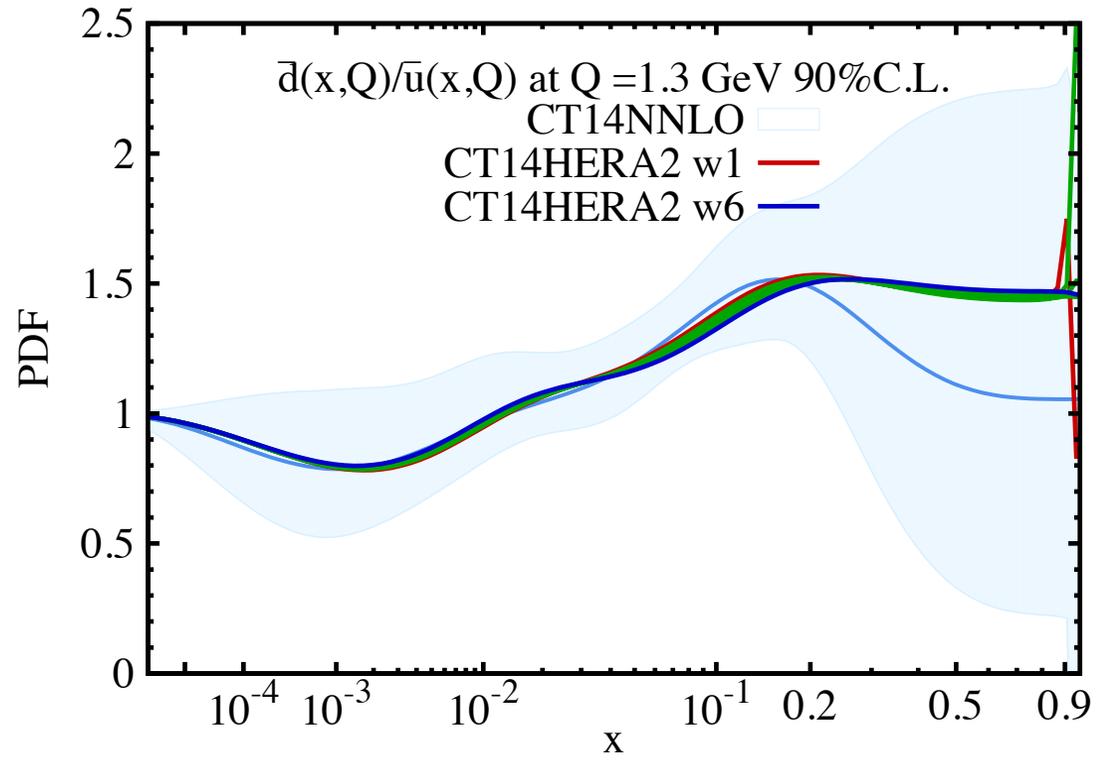
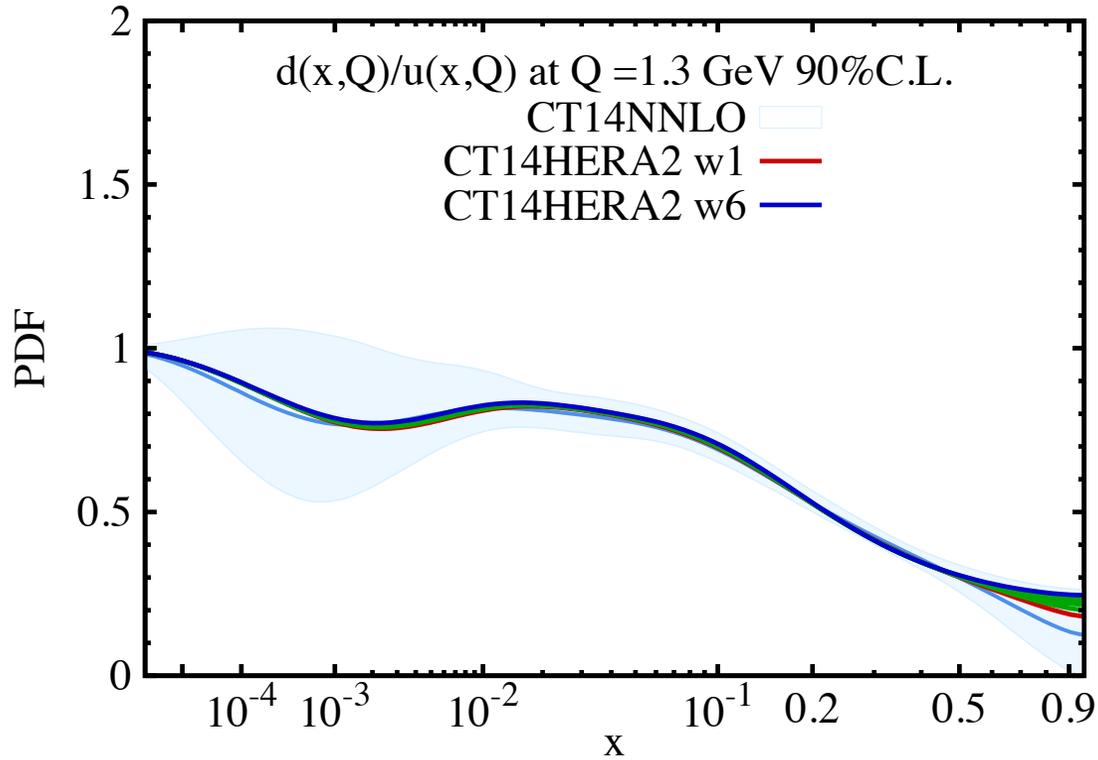
CT14HERA2 vs. CT14

u and d PDFs



HERAI+II data prefers slightly larger u and d at moderate x
Largest effect is u near $x \sim 0.3$, where new fit is near edge of old uncertainty.

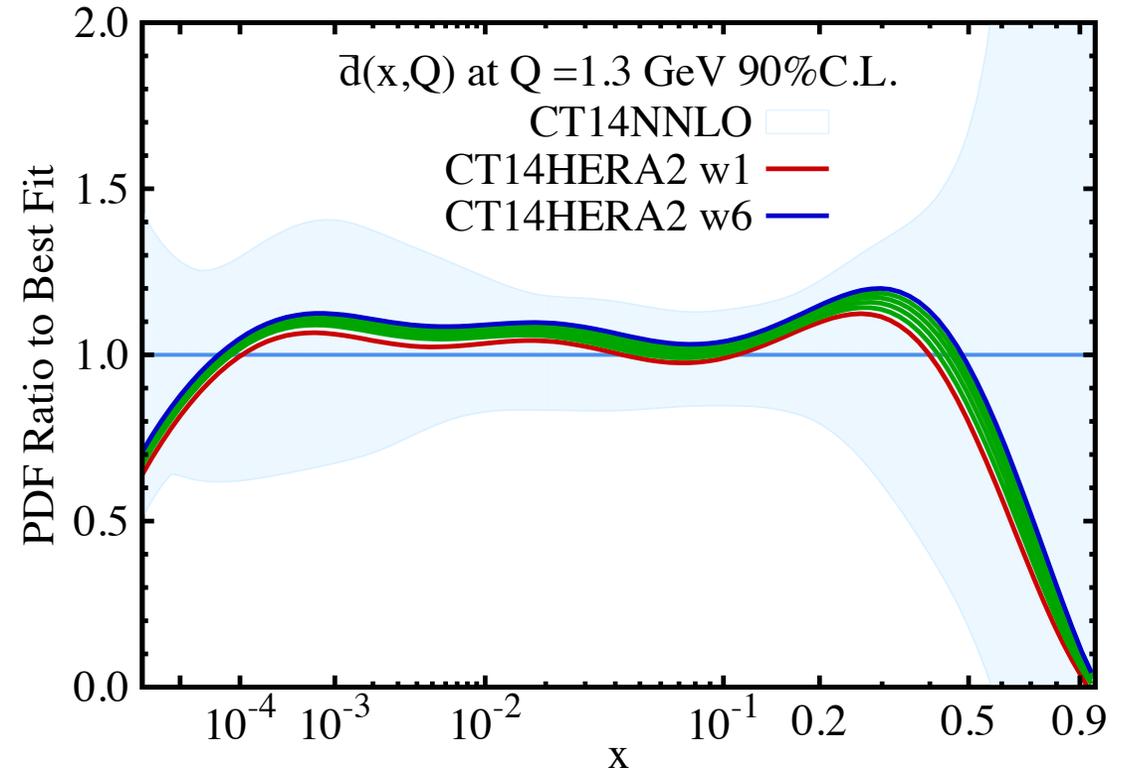
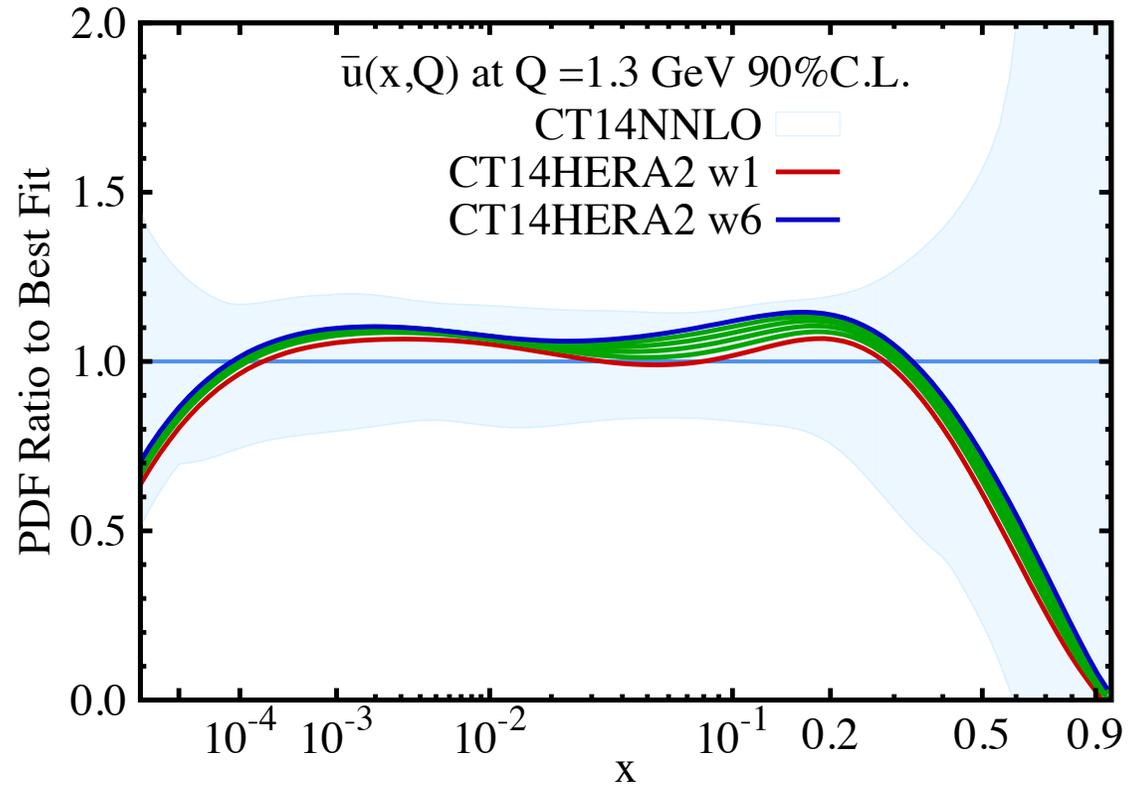
d/u and dbar/ubar PDFs



Changes are minimal, well within uncertainty bands.

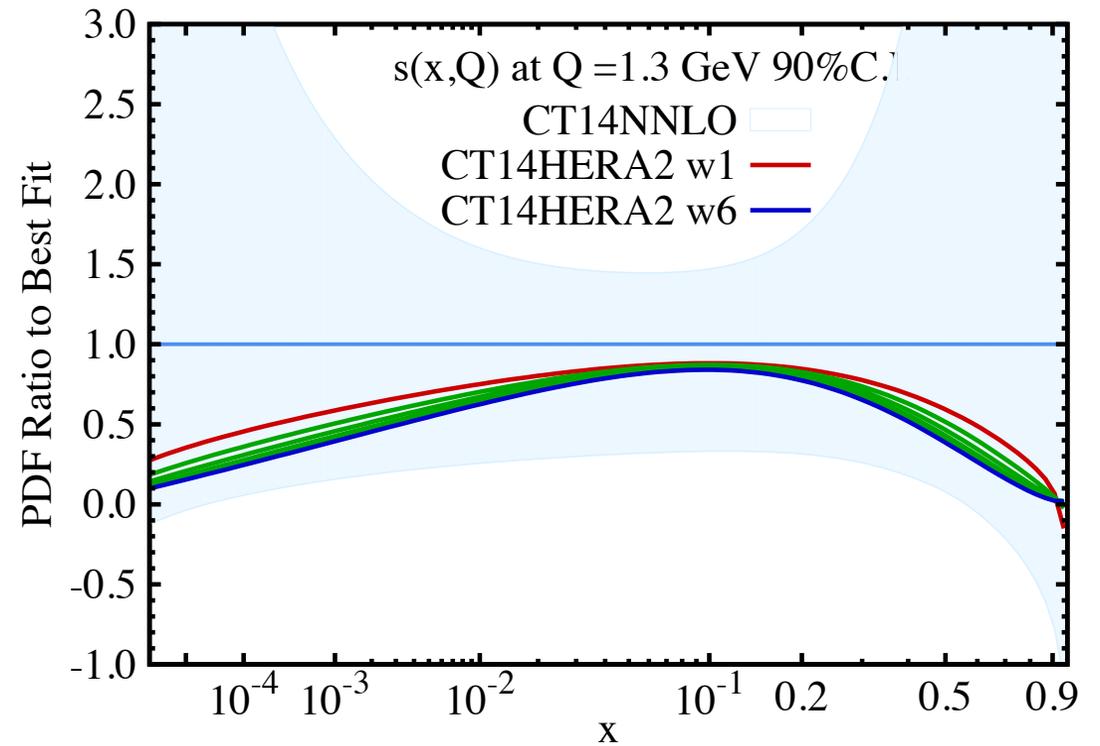
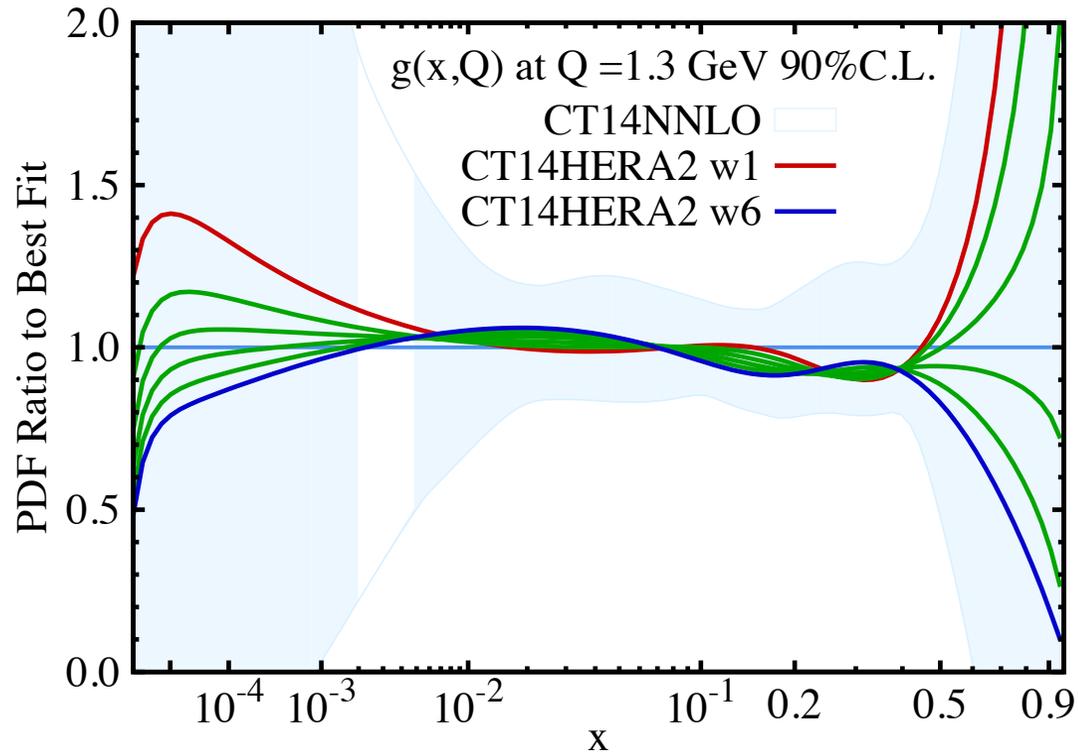
HERAI+II data prefers slightly smaller dbar/ubar around $x \sim 10^{-1}$.

ubar and dbar PDFs



Again changes are minimal, well within uncertainties.

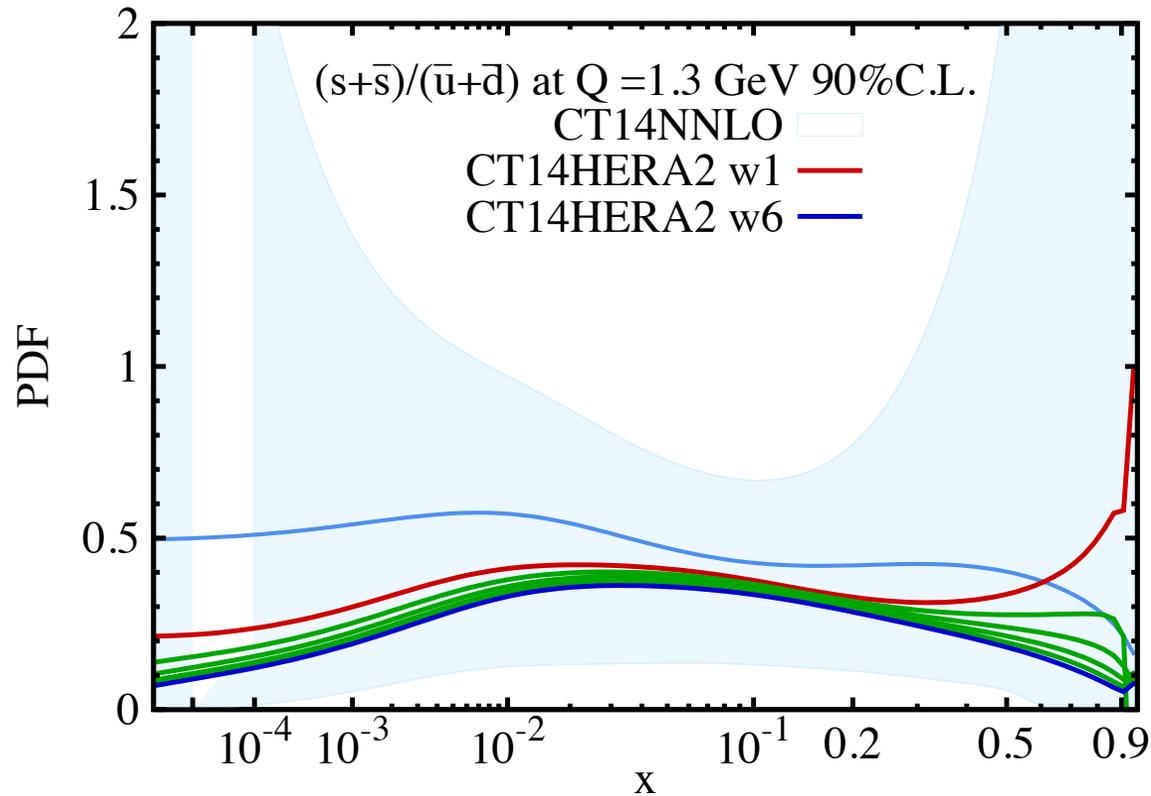
g and s PDFs



HERAI+II data prefers smaller gluon around $x \sim 0.2-0.5$.

Change in strange PDF mostly due to more flexible parametrization.

$(s+\bar{s})/(\bar{u}+\bar{d})$ PDFs



More-flexible strange PDF prefers smaller value,
but still with large uncertainty.



Photon PDFs

- 1) Previous studies
 - a) MRST Martin et al., EPJC 39 (2005) 155
 - Radiation off “primordial current quark” distributions
 - b) NNPDF Ball et al., Nuc. Phys. B 877 (2013) 290
 - parametrized fit, predominantly constrained by W, Z, γ^* Drell-Yan
 - c) Sadykov arXiv:1401.1133
 - photon evolution in QCDNum

- 2) Photon evolution at LO in α and NLO in α_s currently implemented in CTEQ-TEA global analysis package
 - a) Alternative parametrization approach
 - b) Constrain with DIS + photon data

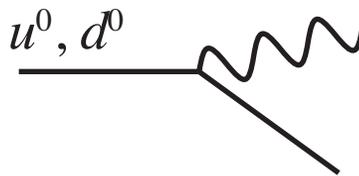


Photon PDF Parametrization

“Radiative ansatz” for initial Photon PDFs (generalization of MRST choice)

$$\gamma^p = \frac{\alpha}{2\pi} \left(A_u e_u^2 \tilde{P}_{\gamma q} \circ u^0 + A_d e_d^2 \tilde{P}_{\gamma q} \circ d^0 \right)$$

$$\gamma^n = \frac{\alpha}{2\pi} \left(A_u e_u^2 \tilde{P}_{\gamma q} \circ d^0 + A_d e_d^2 \tilde{P}_{\gamma q} \circ u^0 \right)$$



where u^0 and d^0 are “primordial” valence-type distributions of the proton.

Assumed approximate isospin symmetry for neutron.

Here, we take A_u and A_d as unknown fit parameters.

MRST choice: $A_q = \ln(Q_0^2/m_q^2)$ “Radiation from **C**urrent **M**ass” – **CM**

We use $u^0 = u^p \equiv u^p(x, Q_0)$, $d^0 = d^p \equiv d^p(x, Q_0)$

and reduce the number of parameters further (for initial study) by setting

$$A_u = A_d = A_0$$

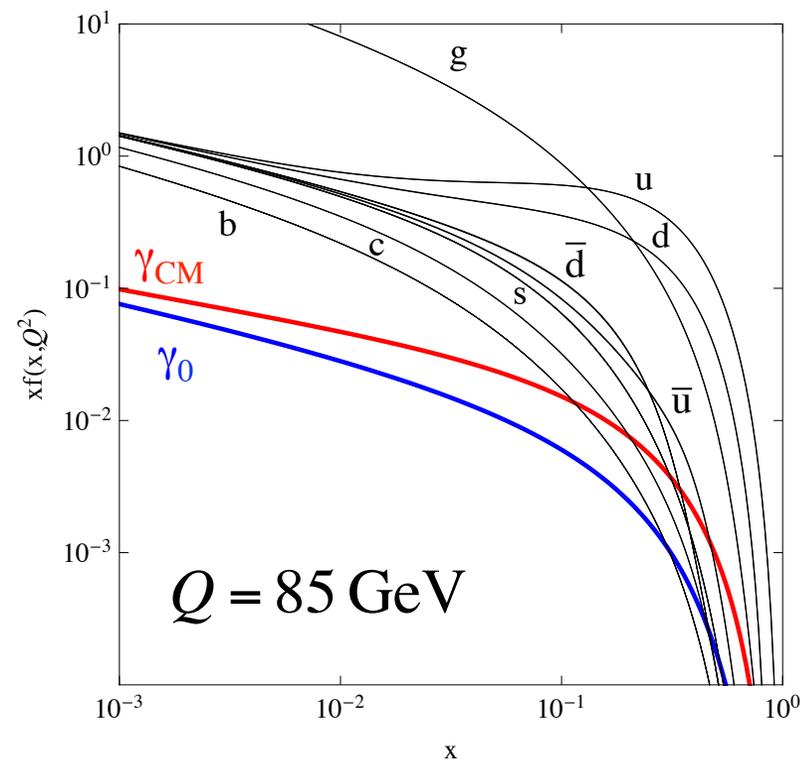
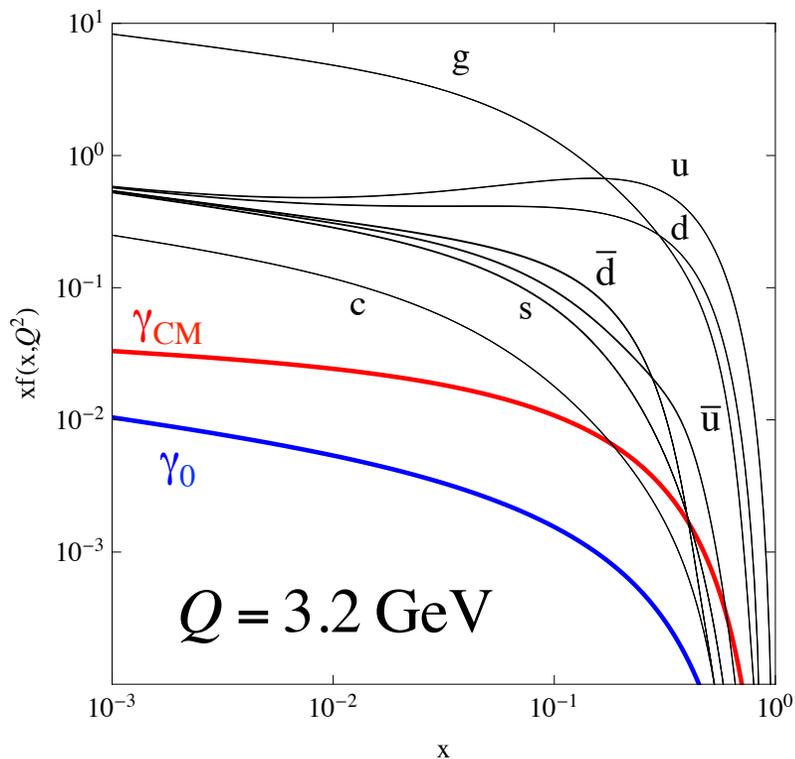
Now everything effectively specified by one unknown parameter:

$$A_0 \Leftrightarrow p_0^\gamma \equiv p^{\gamma/P}(Q_0) \quad (\text{Initial Photon momentum fraction})$$



Photon PDFs (in proton)

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γ momentum fraction:

| $p^\gamma(Q)$ | $\gamma(x, Q_0) = 0$ | $\gamma(x, Q_0)_{CM}$ |
|-----------------------|----------------------|-----------------------|
| $Q = 3.2 \text{ GeV}$ | 0.05% | 0.34% |
| $Q = 85 \text{ GeV}$ | 0.22% | 0.51% |

Photon PDF can be larger than sea quarks at large x !

Initial Photon PDF still
 ← significant at large Q .



Constraining Photon PDFs

- 1) Global fitting
 - Isospin violation, momentum sum rule lead to constraints in fit
 - We find p_0^γ can be as large as $\sim 5\%$ at 90%CL, much more than **CM** choice

- 2) Direct photon PDF probe
 - DIS with observed photon, $ep \rightarrow e\gamma + X$
 - Photon-initiated subprocess contributes at LO, and no larger background with which to compete
 - But must include quark-initiated contributions consistently
 - Treat as NLO in α , but discard small corrections, suppressed by $\alpha \gamma(x)$.



$$ep \rightarrow e\gamma + X$$

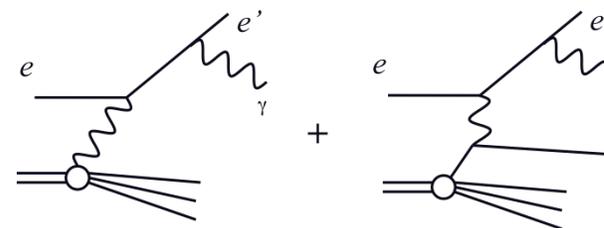
Subprocess contributions:

LL Emission off Lepton line

Both quark-initiated and photon-initiated contributions are $\sim \alpha^3$ if $\gamma(x) \sim \alpha$

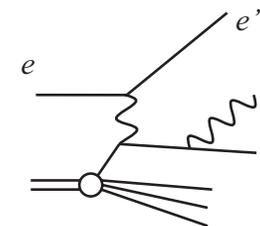
Collinear divergence cancels (in $d=4-2\varepsilon$) by treating as

$$\text{NLO in } \alpha \text{ with } \gamma^{\text{bare}}(x) = \gamma(x) + \frac{(4\pi)^\varepsilon}{\varepsilon} \Gamma(1+\varepsilon) \frac{\alpha}{2\pi} (P_{\gamma q} \circ q)(x) \quad (\overline{\text{MS}})$$



QQ Emission off Quark line

Has final-state quark-photon collinear singularity



QL Interference term

Negligible < about 1% (but still included)

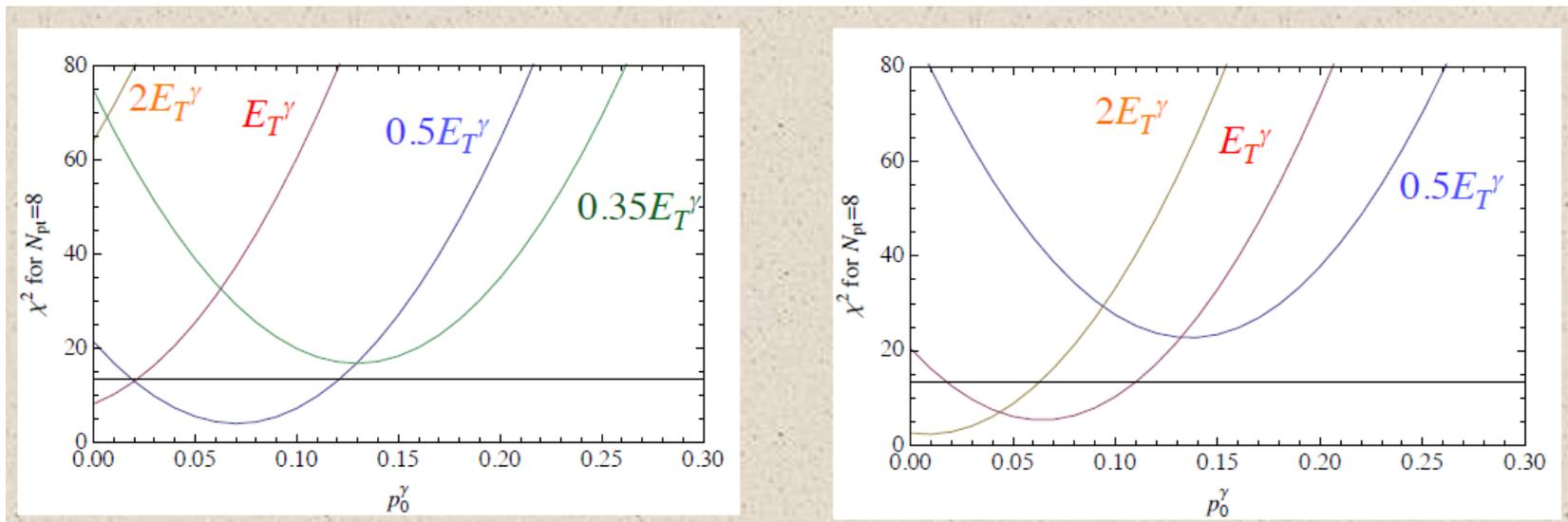
Previous calculations:

quark-initiated only – (GGP) Gehrmann-De Ridder, Gehrmann, Poulson, PRL 96, 132002 (2006)

photon initiated only – (MRST), Martin, Roberts, Stirling, Thorne, Eur. Phys. J. C 39, 155 (2005)



Limits on Photon PDF



Smooth Isolation

Sharp Isolation

- Different χ^2 curves for choice of isolation and scale μ_F
- 90% C.L. for $N_{pt} = 8$ corresponds to $\chi^2 = 13.36$
- Obtain $p_0^\gamma \leq 0.14\%$ at 90 % C.L. independent of isolation prescription

(More generally, constrains $\gamma(x)$ for $10^{-3} < x < 2 \times 10^{-2}$.)

- “Current Mass” ansatz has $\chi^2 > 45$ for any choice of isolation and scale