



Possible Field Dependence of Superconducting Properties in N-Doped Cavities

Dan Gonnella

Cornell University

December 1, 2015





- Deconvolution of R_{res} and R_{BCS}
- Fitting of field dependent data:
 - Exponential fitting
 - BCS fitting with SRIMP
 - Fitting with Xiao code
- Magnetic Field Studies
- Conclusions

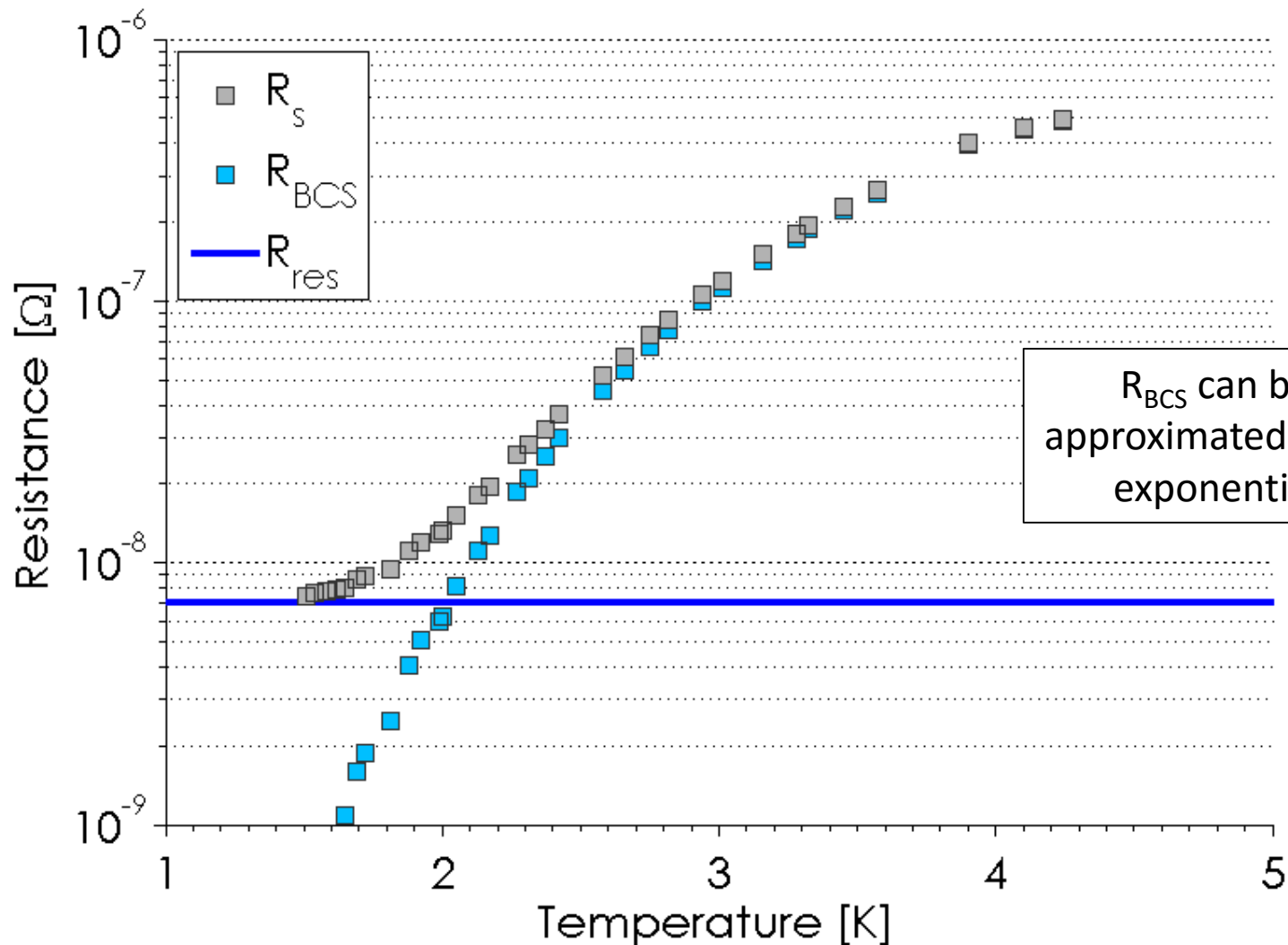




- Deconvolution of R_{res} and R_{BCS}
- Fitting of field dependent data:
 - Exponential fitting
 - BCS fitting with SRIMP
 - Fitting with Xiao code
- Magnetic Field Studies
- Conclusions



Surface Resistance

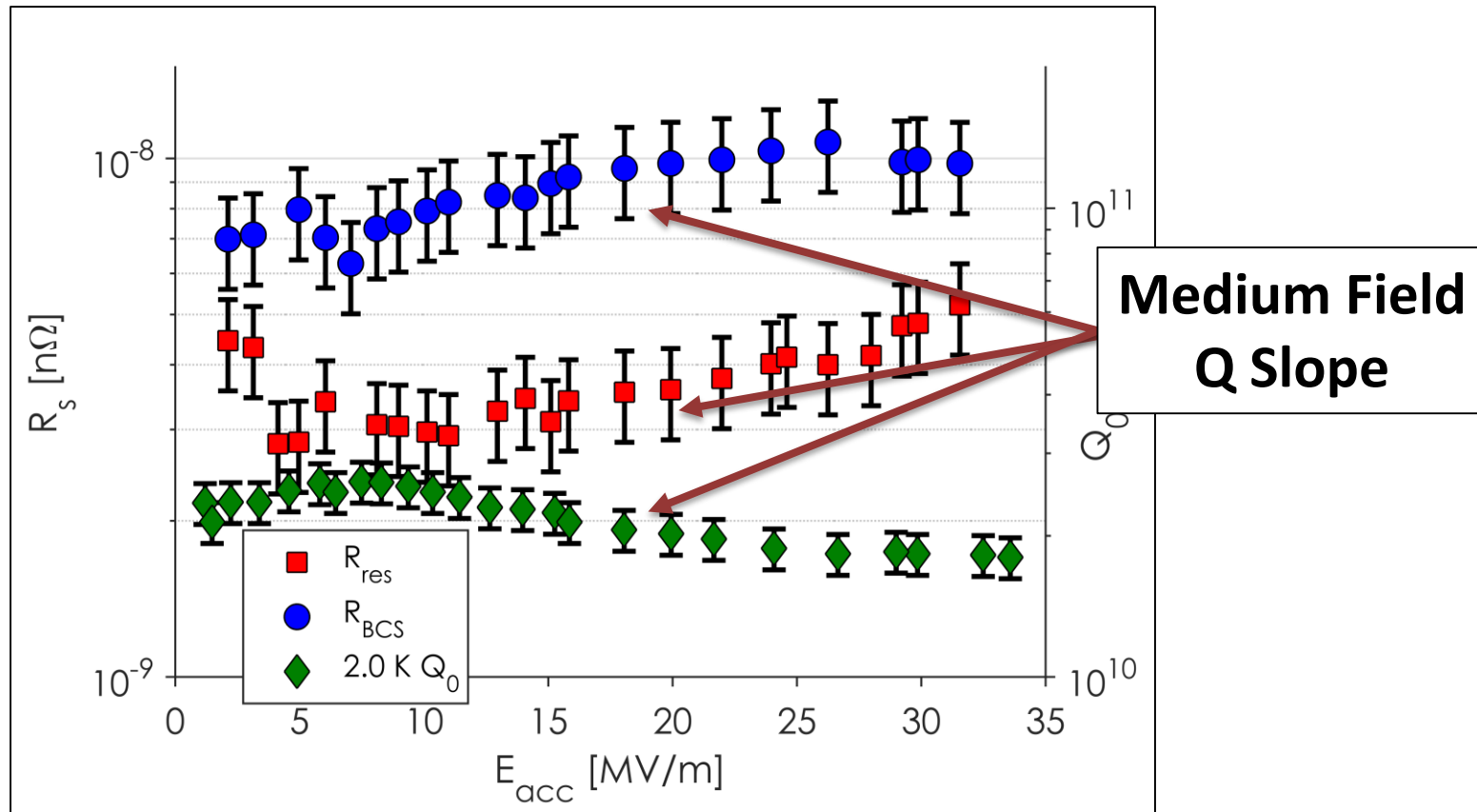




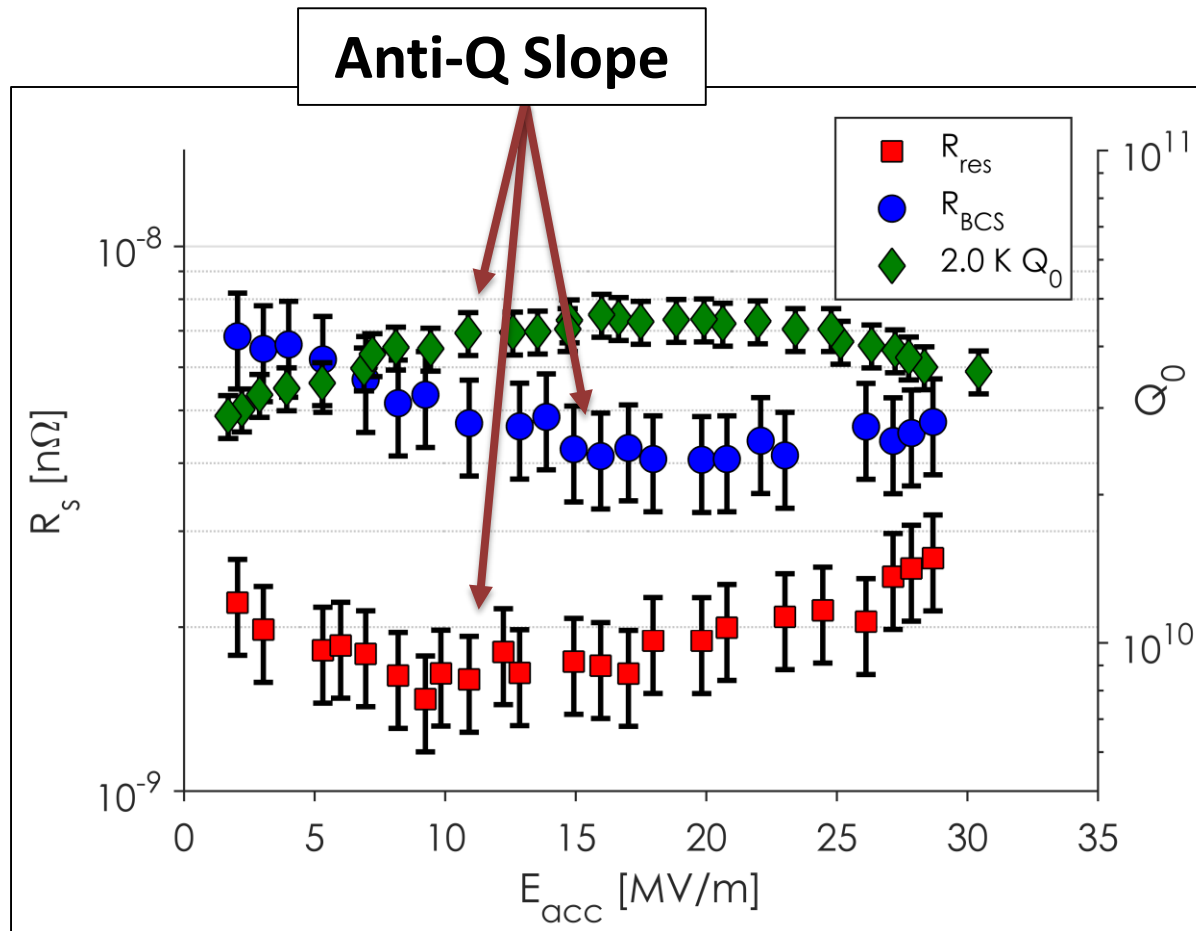
Both R_{res} and R_{BCS} have been shown to
be field dependent:

$$R_s = R_{\text{res}}(E_{\text{acc}}) + R_{\text{BCS}}(E_{\text{acc}}, T)$$





Medium field Q slope caused by a **combination** of increasing residual and BCS resistances in 120°C baked cavities



Anti-Q slope caused by a decreasing BCS resistance in N-Doped Cavities



- Deconvolution of R_{res} and R_{BCS}
- Fitting of field dependent data:
 - Exponential fitting
 - BCS fitting with SRIMP
 - Fitting with Xiao code
- Magnetic Field Studies
- Conclusions





The usual BCS equation for fitting:

$$R_{BCS} = \frac{A}{T} e^{-\epsilon/k_B T}$$

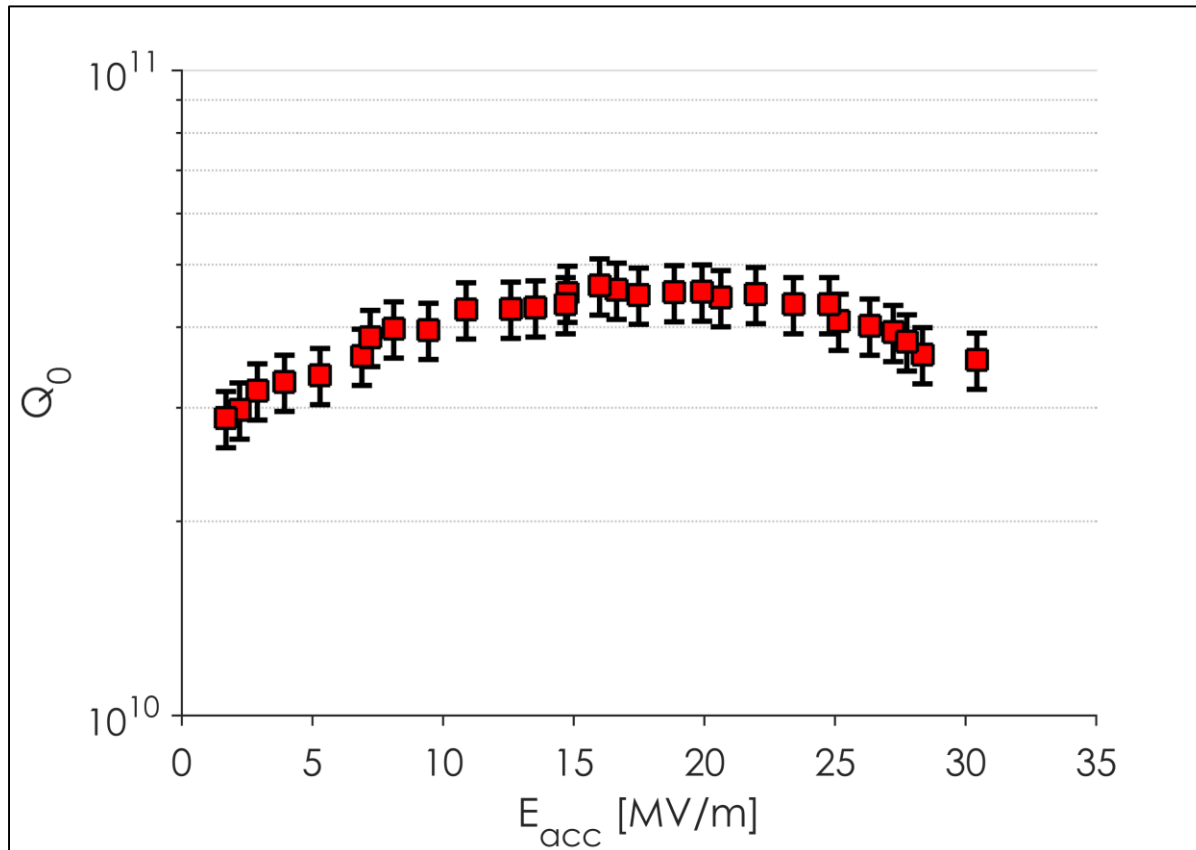
Both A and ϵ can vary with E_{acc} however fitting both together leads to sloppy fitting.

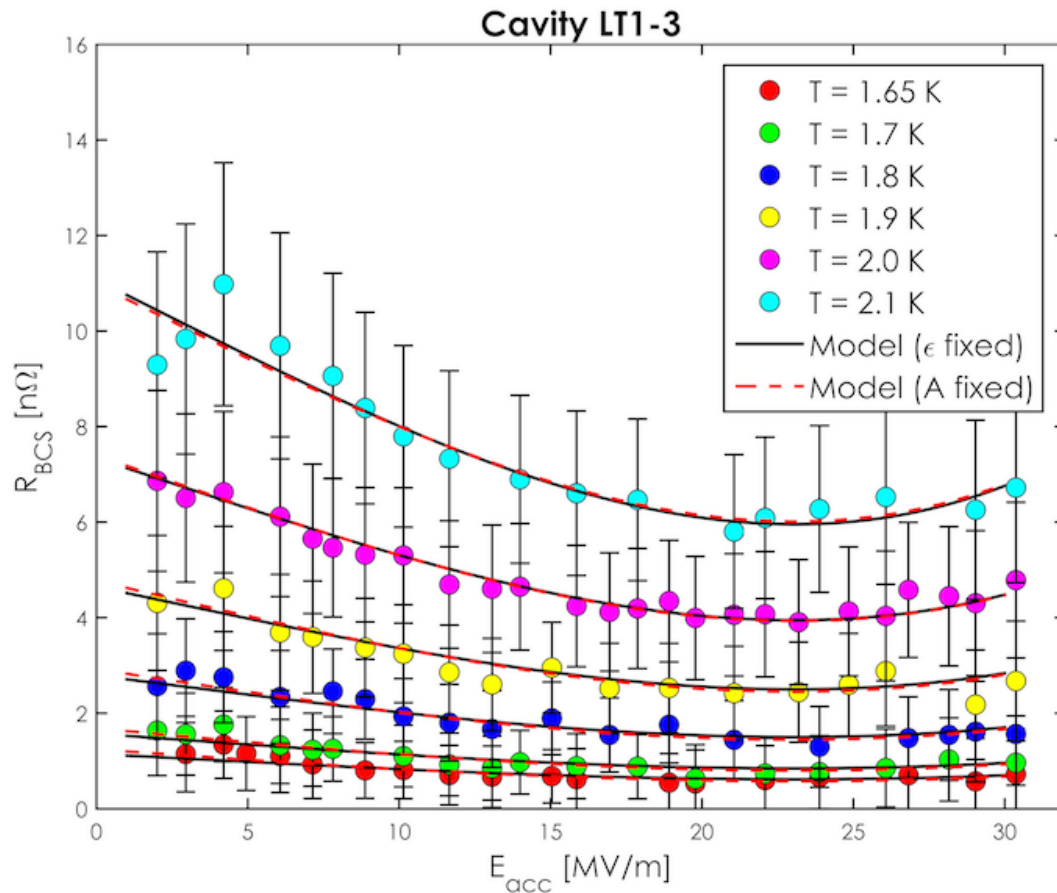
$$R_{BCS} = \frac{A(E_{acc})}{T} e^{-\epsilon/k_B T}$$

$$R_{BCS} = \frac{A}{T} e^{-\epsilon(E_{acc})/k_B T}$$



1.3 GHz Single Cell ILC shaped cavity: bulk VEP,
800°C bake in vacuum for 3 hours, 20 min in
60 mTorr of N₂ for 20 minutes, 30 minute
anneal, 12 μm VEP

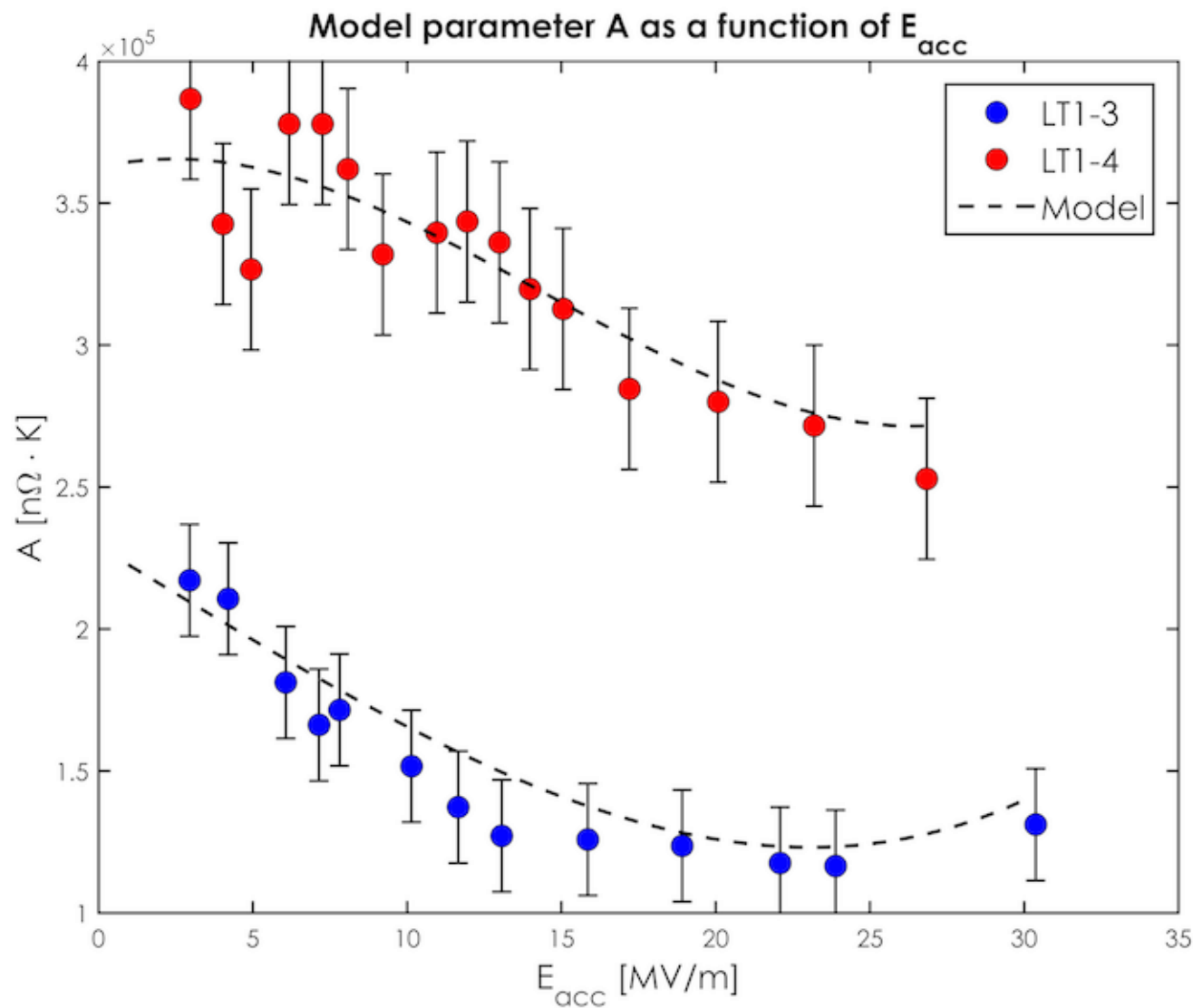




Both models can fit
the R_{BCS} data well in
the anti-Q slope
region

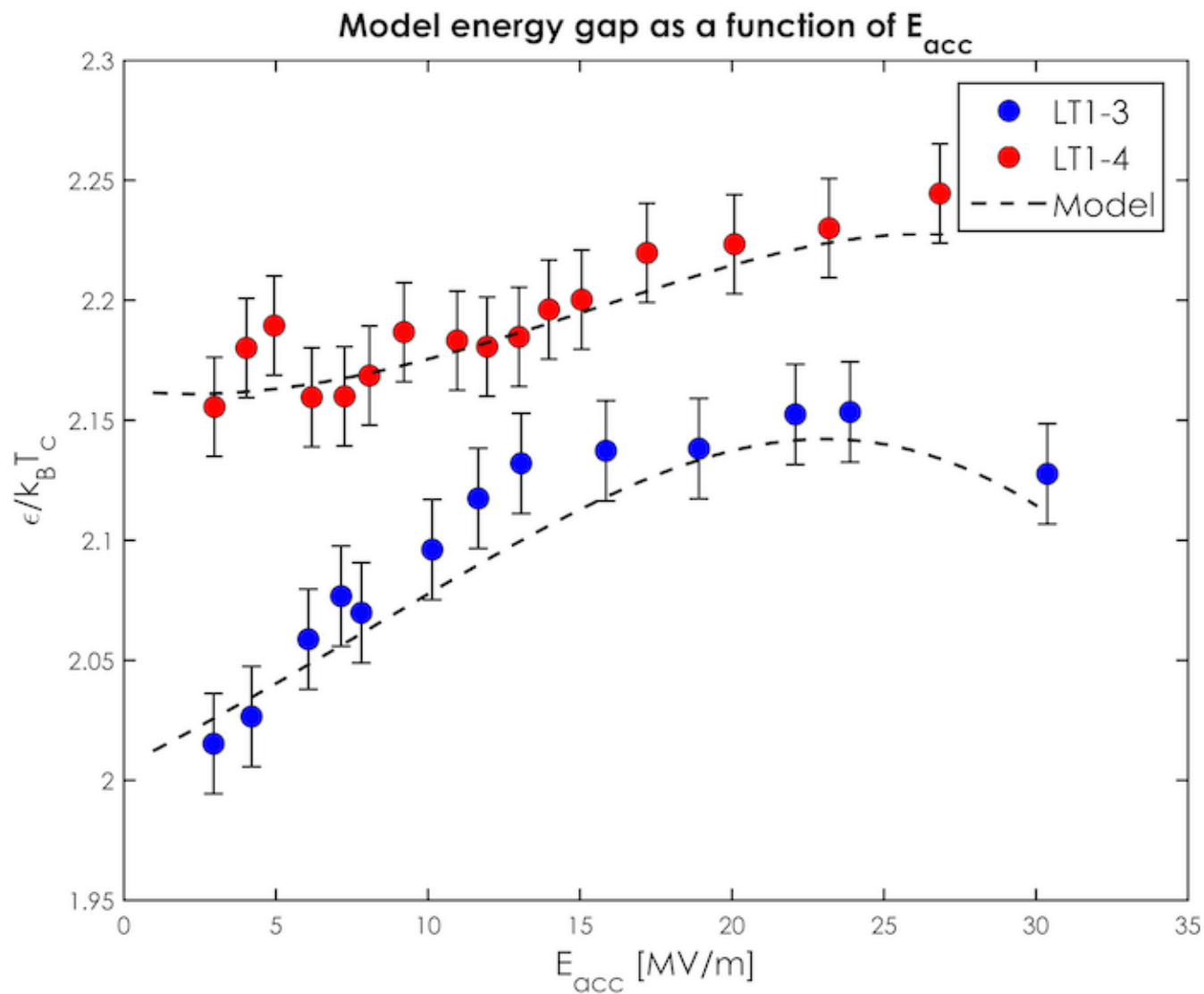


Exponential Fitting





Exponential Fitting





Exponential Fitting

- Fits with both A and ε field dependent are sloppy
- Individual fits however can fit R_{BCS} vs E_{acc} data very well
- A decreasing A with field or an increasing ε can explain the anti-Q slope observed in N-doped cavities

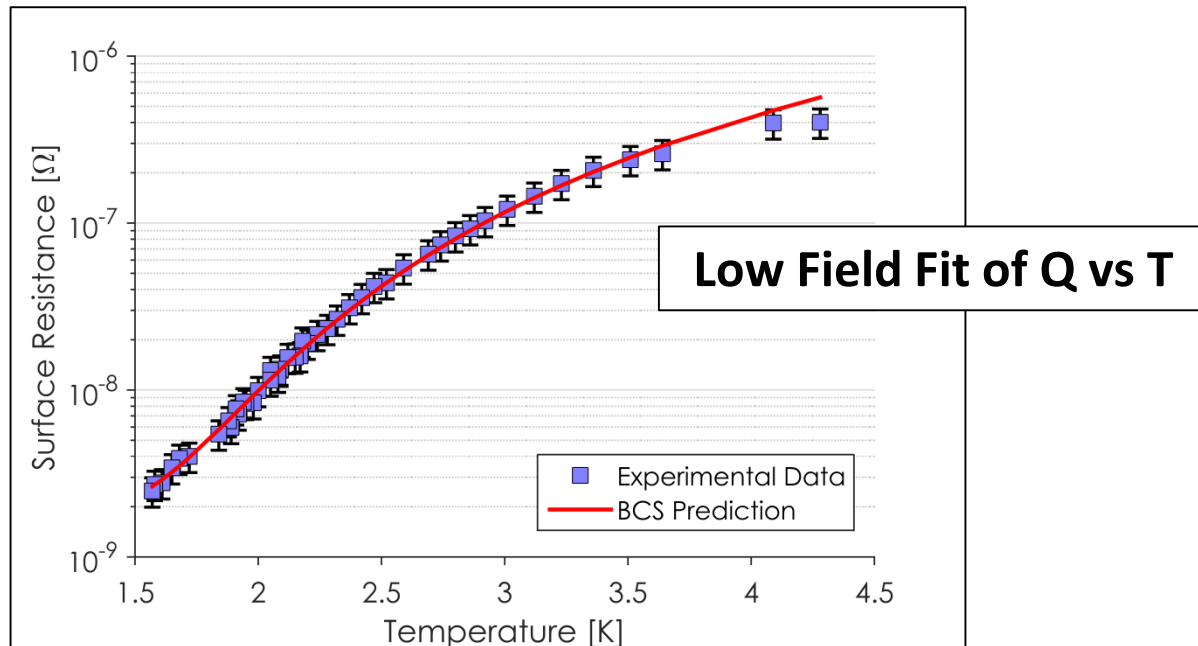




- Deconvolution of R_{res} and R_{BCS}
- **Fitting of field dependent data:**
 - Exponential fitting
 - **BCS fitting with SRIMP**
 - Fitting with Xiao code
- Magnetic Field Studies
- Conclusions

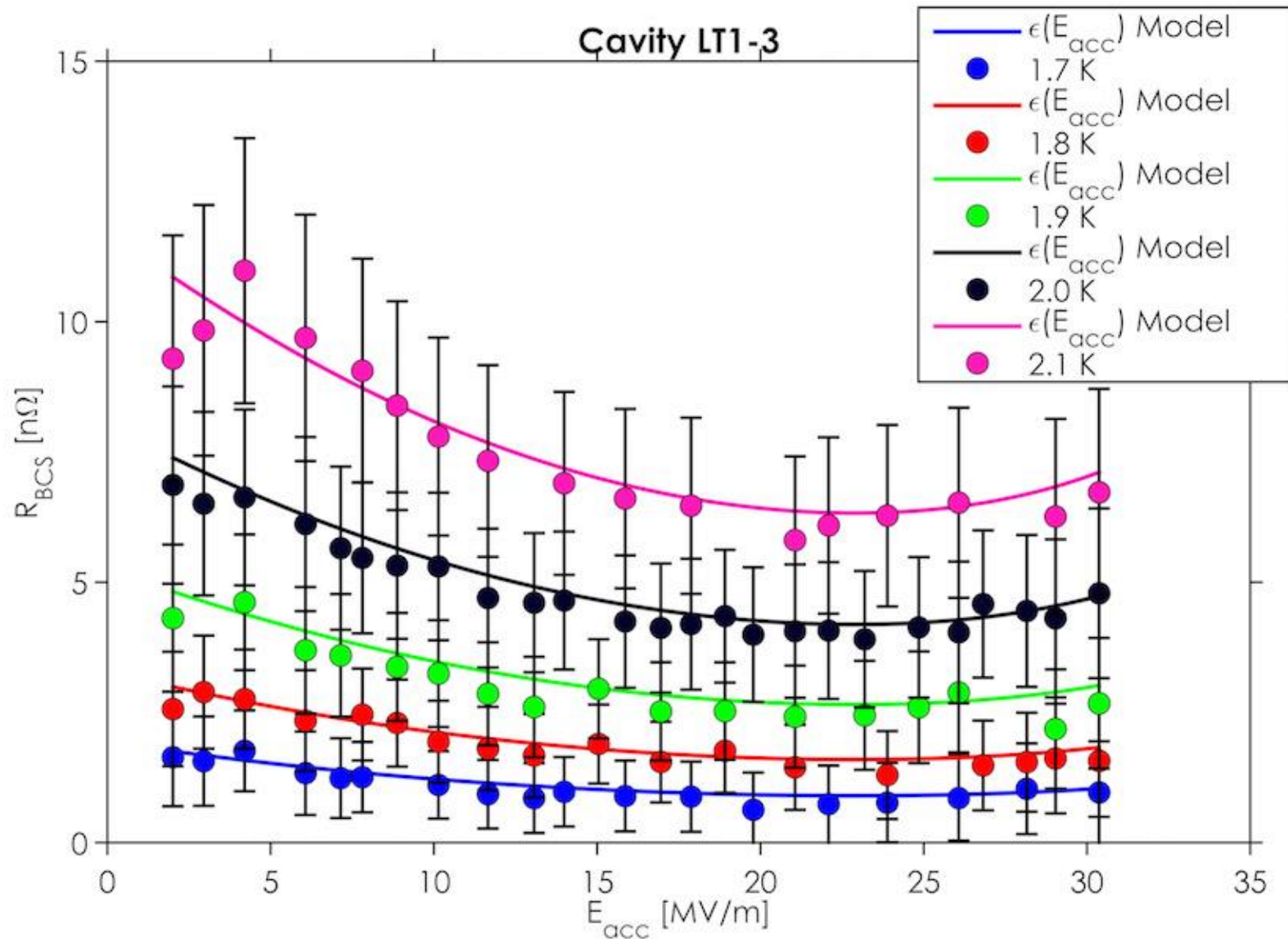


- SRIMP, a code written by Halbritter, can be used to calculate R_{BCS} based on material parameters
 - T_c , Mean Free Path, $\epsilon/k_B T_c$, coherence length, and penetration depth



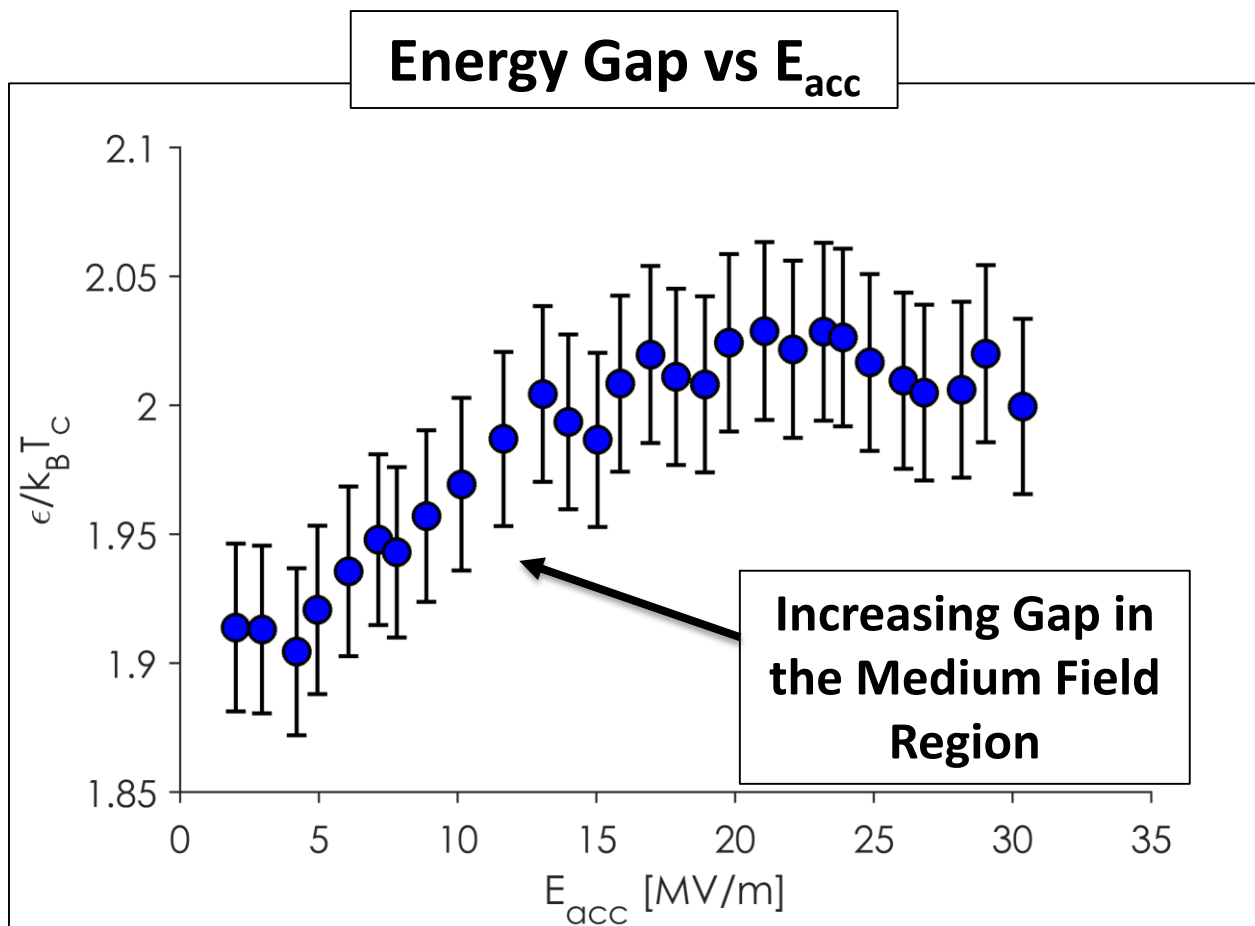


BCS Fitting with SRIMP



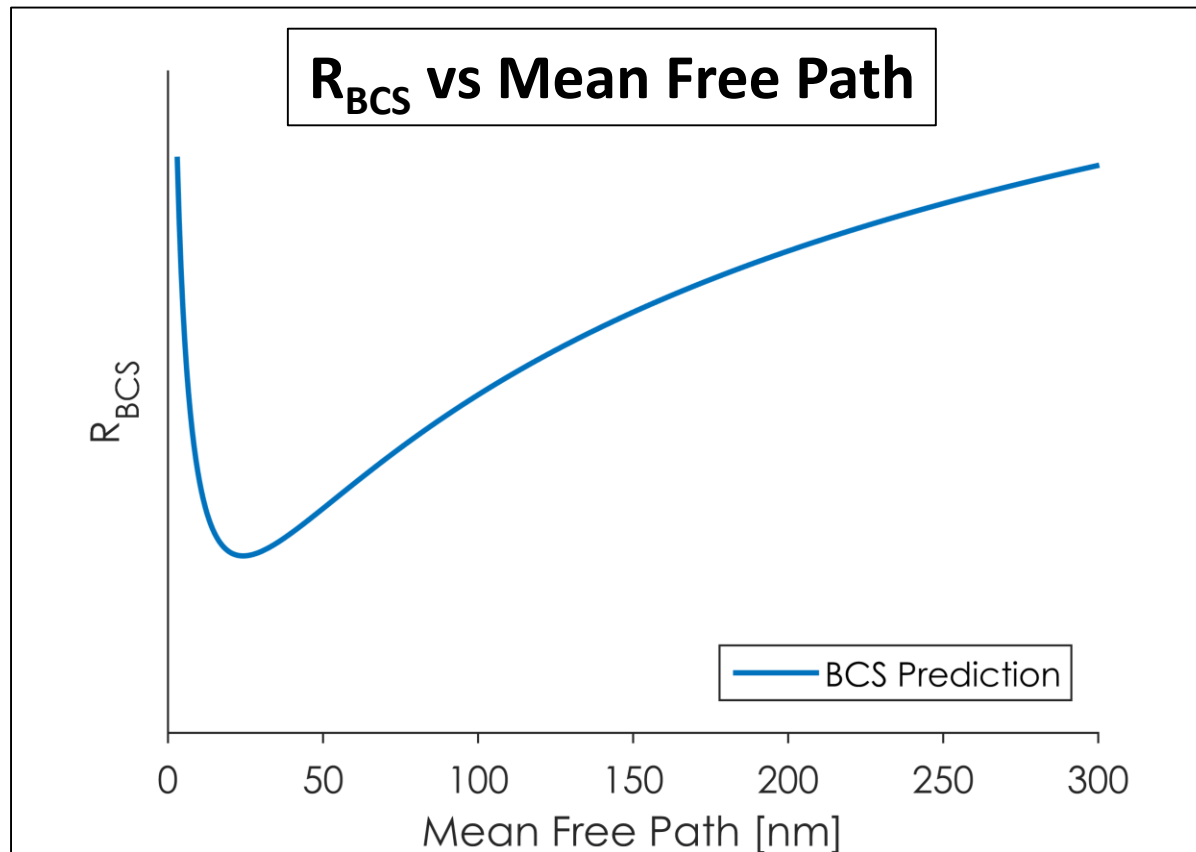


BCS Fitting with SRIMP

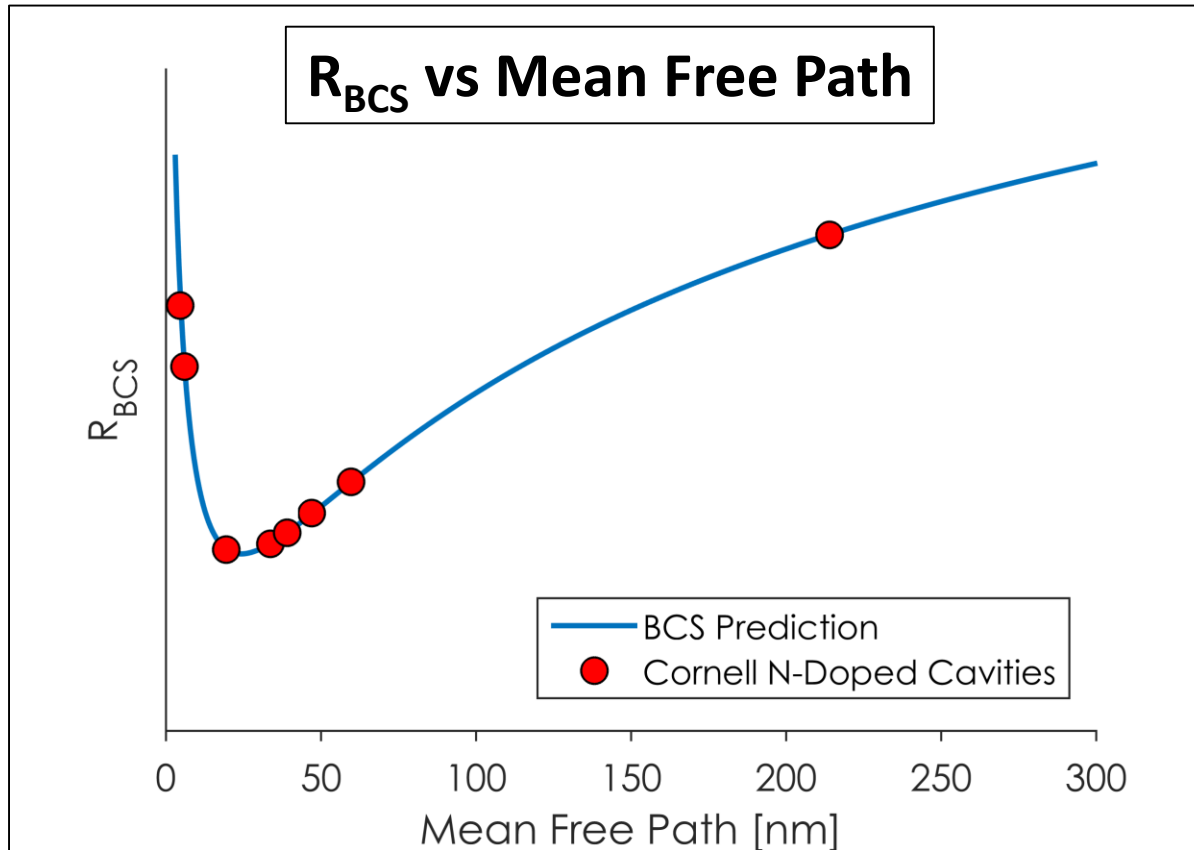




BCS Fitting with SRIMP



BCS Fitting with SRIMP



- N-Doped cavities are on both sides of the R_{BCS} vs Mean free path minimum
- Increasing or decreasing mean free path with field alone cannot explain the anti-Q slope



BCS Fitting with SRIMP

- Field dependence of BCS resistance in N-Doped cavities is related to the energy gap
- Nitrogen-doped cavities have mean free paths that are on both sides of the R_{BCS} vs mean free path minimum
 - An increasing or decreasing mean free path with accelerating field cannot explain a decreasing BCS resistance in all cavities





- Deconvolution of R_{res} and R_{BCS}
- **Fitting of field dependent data:**
 - Exponential fitting
 - BCS fitting with SRIMP
 - **Fitting with Xiao code**
- Magnetic Field Studies
- Conclusions





Fitting with Xiao Code

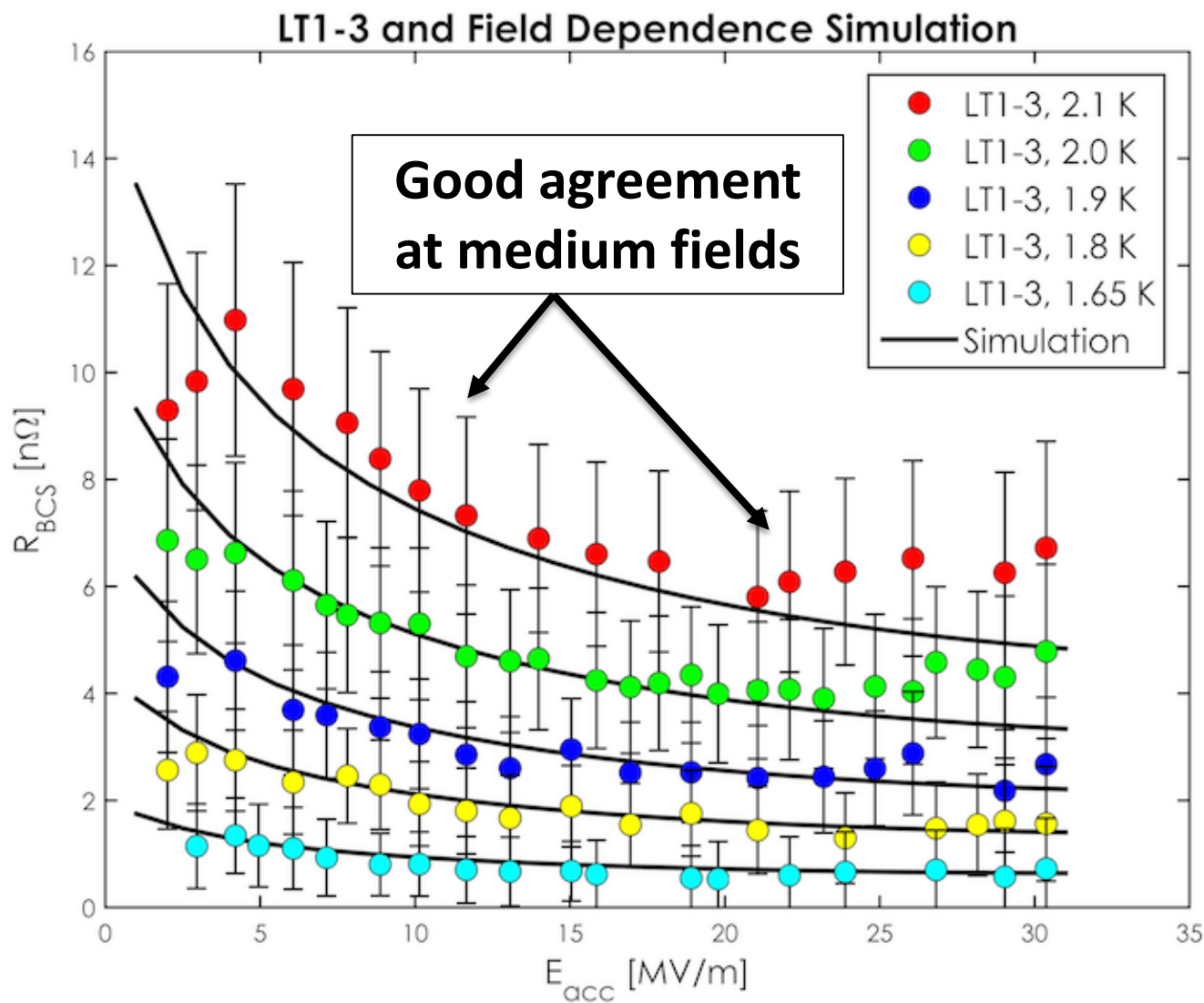
- Xiao et. al. developed a code to include field dependence in BCS theory using an extension of Mattis-Bardeen theory
- Using low field material parameters obtained from SRIMP fitting, the full field dependence of the BCS resistance can be computed at different temperatures

B. P. Xiao et. al. Superconducting surface resistance under radiofrequency field. Physica C, 490(0):26–31, 2013.



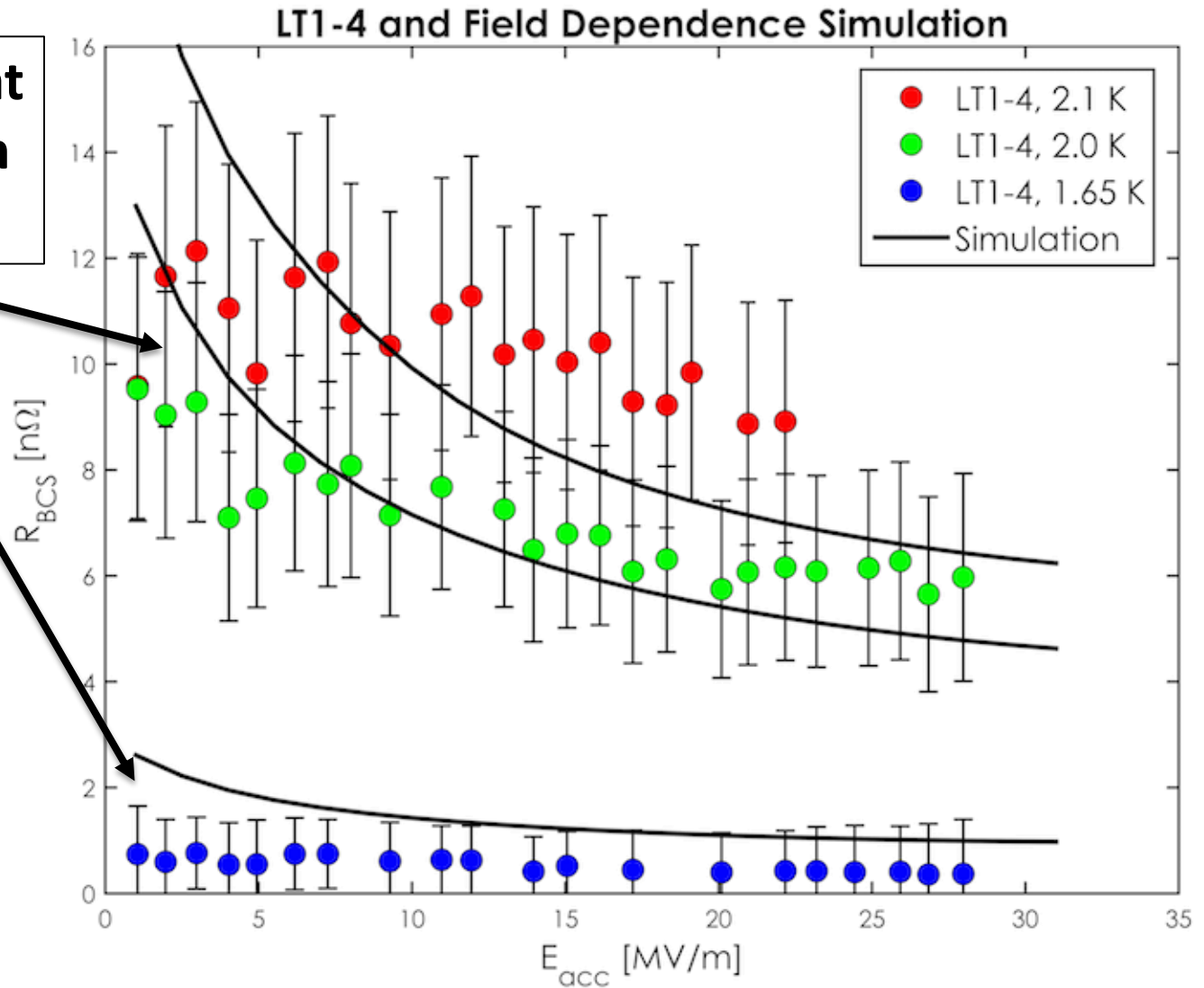


Fitting with Xiao Code



Fitting with Xiao Code

Poor agreement at
medium and high
fields





Fitting with Xiao Code

- Xiao code can accurately predict behavior of BCS resistance at medium fields in Nitrogen-doped cavities
- Theory deviates from observed behavior at low fields:
 - The theory predicts a much more drastic increase in BCS resistance than we observe



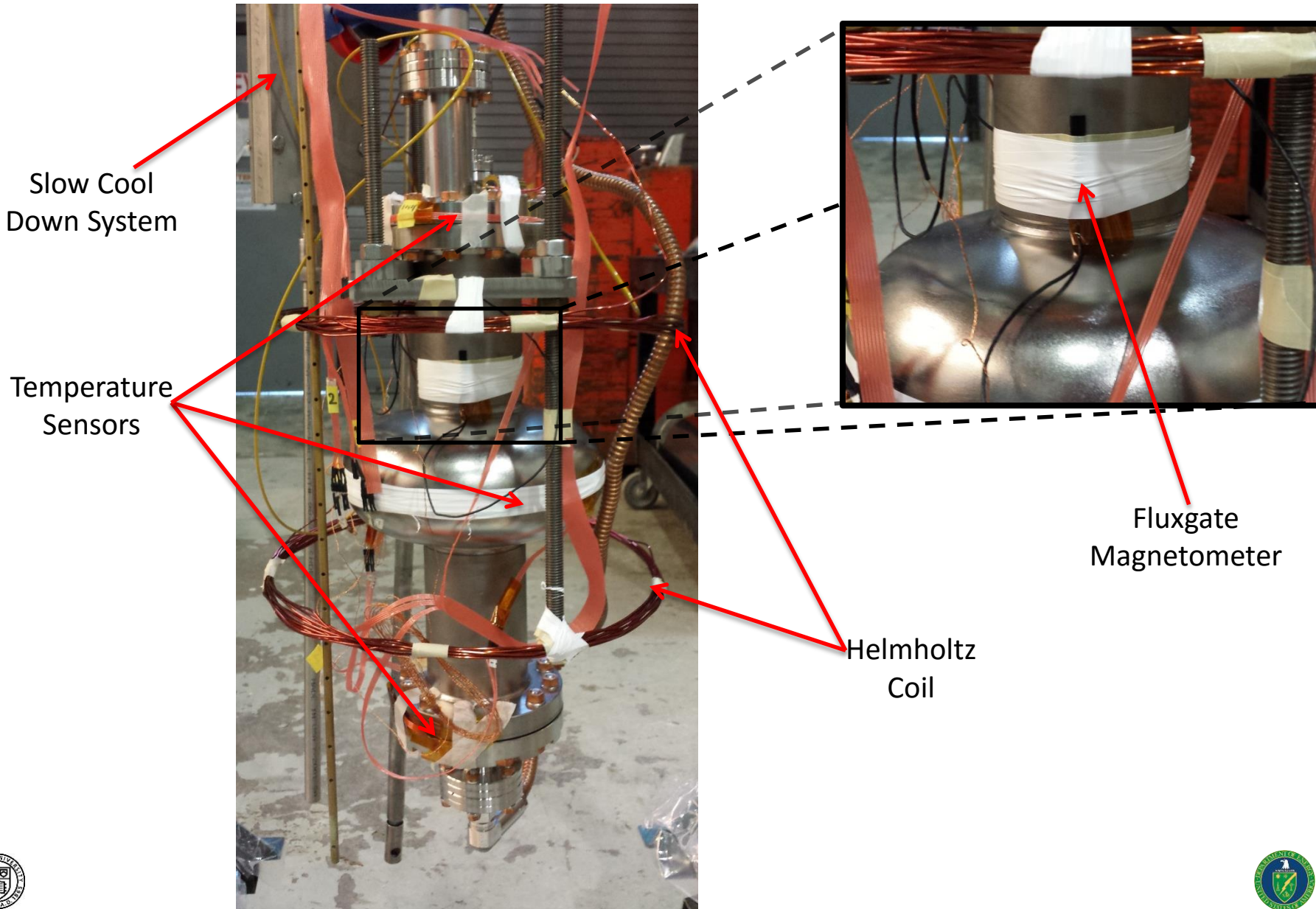


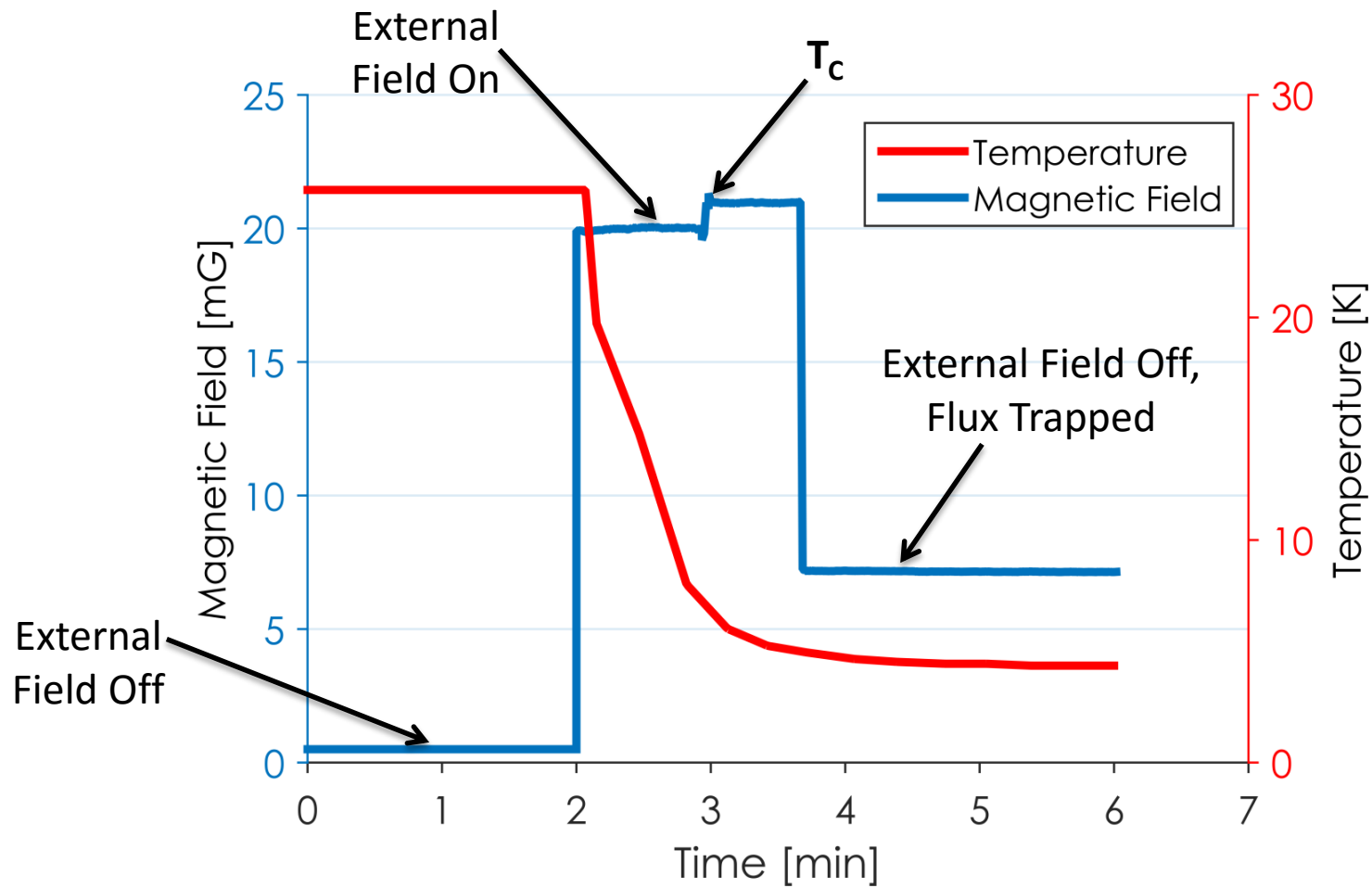
- Deconvolution of R_{res} and R_{BCS}
- Fitting of field dependent data:
 - Exponential fitting
 - BCS fitting with SRIMP
 - Fitting with Xiao code
- **Magnetic Field Studies**
- Conclusions

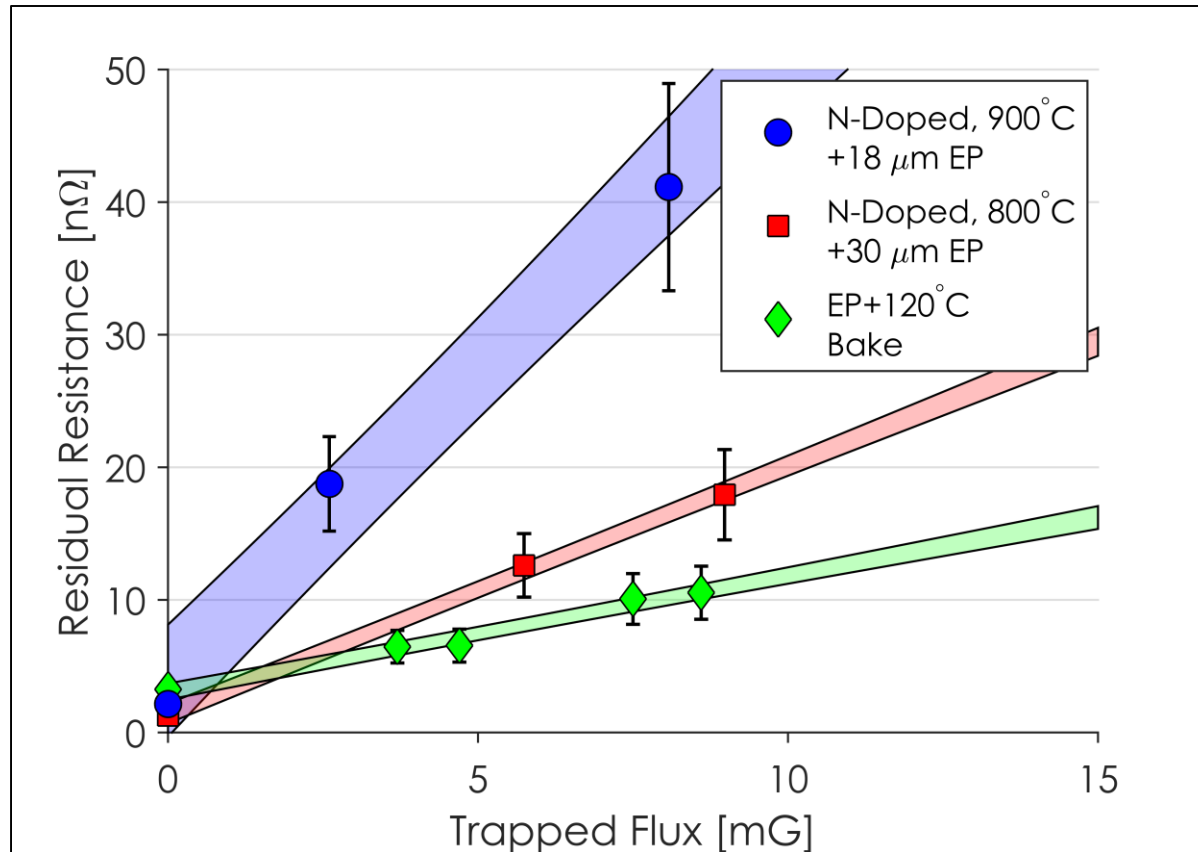




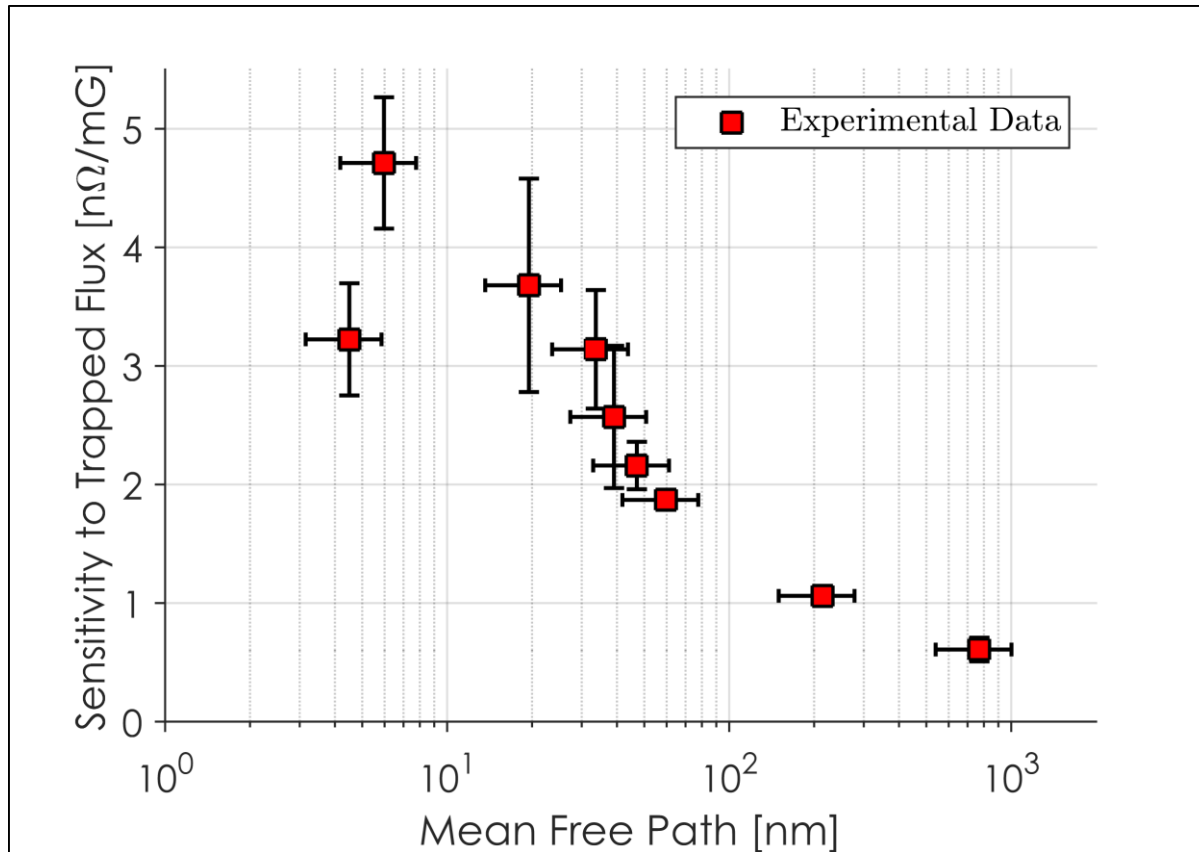
Flux Trapping Studies





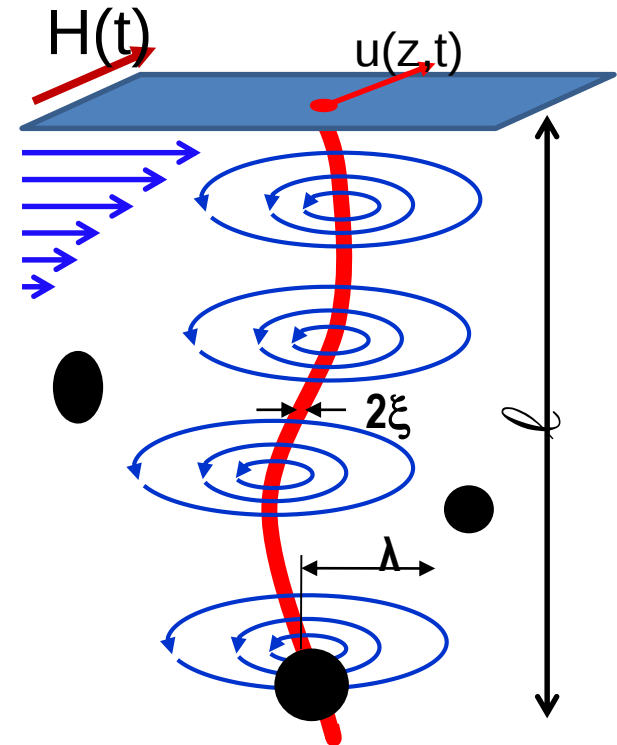
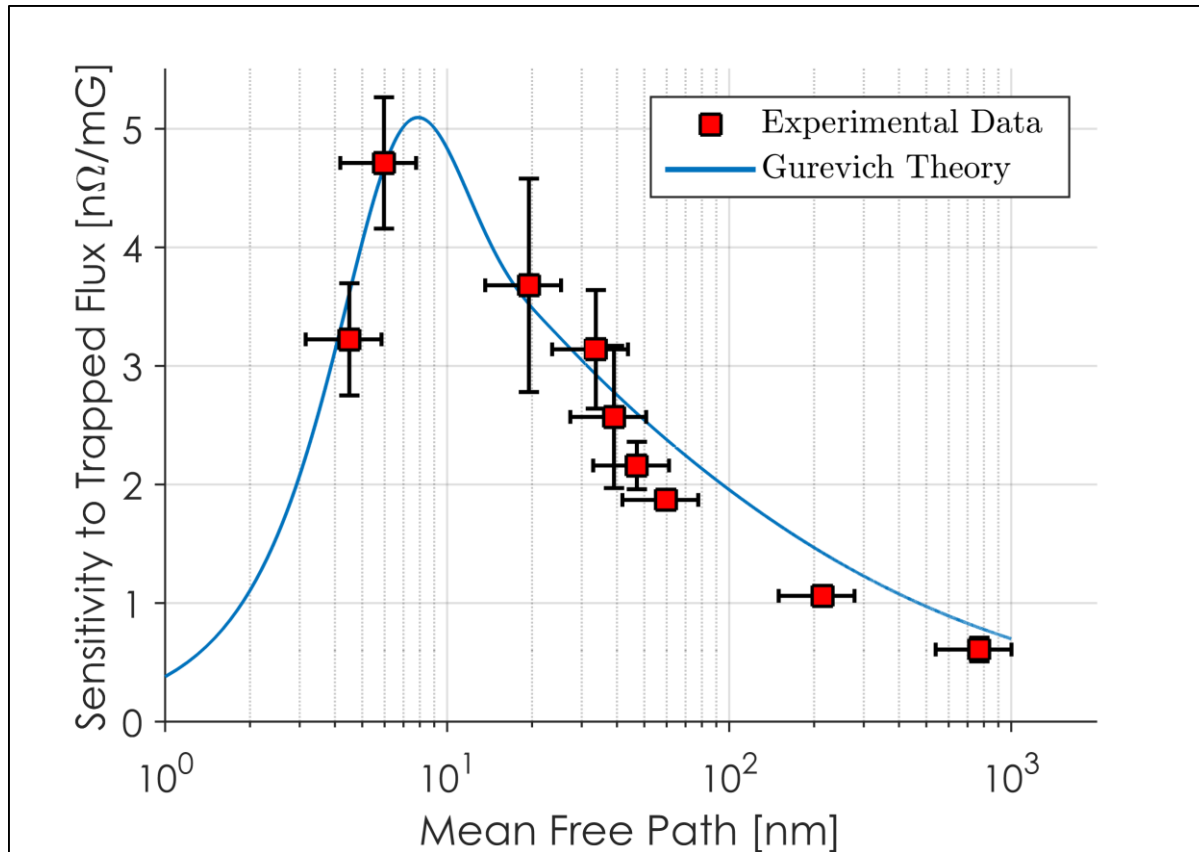


A total of 10 cavity preparations were tested, each with different mean free paths – N-doping gives us the tools needed to finely tune the mean free path



- In the clean limit, longer mean free path leads to lower sensitivity of R_{res} to trapped magnetic flux
- In the dirty limit, shorter mean free path leads to lower sensitivity

See our paper on ArXiv for full details:
Gonnella et. al. arXiv:1509.04127



See our paper on ArXiv for full details:
Gonnella et. al. arXiv:1509.04127

- This is well described by theoretical predictions proposed by Alex Gurevich (*Physical Review B*, 87(5):054502, 2013.)
- This model is heavily dependent upon mean spacing between pinning sites: we assume a linear relationship between this mean free path



- Deconvolution of R_{res} and R_{BCS}
- Fitting of field dependent data:
 - Exponential fitting
 - BCS fitting with SRIMP
 - Fitting with Xiao code
- Magnetic Field Studies
- **Conclusions**



- Medium field Q slope in 120°C cavities is caused by a combination of increasing BCS and residual resistances
- Anti-Q slope in Nitrogen-doped cavities is caused purely by decreasing BCS resistance
- This anti-Q slope can be explained in a variety of ways: decreasing A or increasing ϵ in exponential fitting and increasing $\epsilon/k_B T_c$ in full BCS fitting
 - Changing mean free path cannot solely explain the anti-Q slope since low field mean free paths are on either side of the minimum in N-Doped cavities



- Xiao code, a field-dependent derivation of Mattis-Bardeen theory can accurately predict BCS resistance at medium fields from low field material parameters but fails at low fields
- Losses due to ambient magnetic fields are heavily dependent on mean free path and are very well explained by Gurevich's theory of vortex oscillations

