

# Results on exotic spectroscopy at LHCb

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- 1 Introduction
  - Motivation
  - The LHCb experiment
- 2 Tetraquark candidates at LHCb
  - $X(3872)$
  - $Z(4430)$
- 3 Pentaquark candidates at LHCb
  - $\Lambda_b^0 \rightarrow J/\psi p K^-$  Decays at LHCb
  - Amplitude analysis of  $\Lambda_b^0 \rightarrow J/\psi p K^-$
  - Results
  - Interpretations
  - Implications
- 4 Summary

- Ongoing challenge: relate basic concepts of QCD to observed phenomena
  - **Effective Theories** make use of symmetries or phenomenologically motivated approximations - e.g. approximate  $SU(3)_{\text{flavor}}$  symmetry

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Volume 9, number 3

PHYSICS LETTERS

1 February 1964

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8419/TH.412

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II \*)

G. Zweig

CERN---Geneva

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- 6) In general, we would expect that baryons are built not only from the product of three  $ace$ ,  $AAA$ , but also from  $\bar{A}AAA$ ,  $\bar{A}A\bar{A}AA$ , etc., where  $\bar{A}$  denotes an anti- $ace$ . Similarly, mesons could be formed from  $\bar{A}\bar{A}$ ,  $\bar{A}AA$  etc. For the low mass mesons and baryons we will assume the simplest possibilities,  $\bar{A}\bar{A}$  and  $AAA$ , that is, "deuces and treys".

- Ongoing challenge: relate basic concepts of QCD to observed phenomena
  - **Effective Theories** make use of symmetries or phenomenologically motivated approximations - e.g. approximate  $SU(3)_{\text{flavor}}$  symmetry

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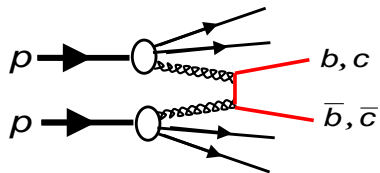
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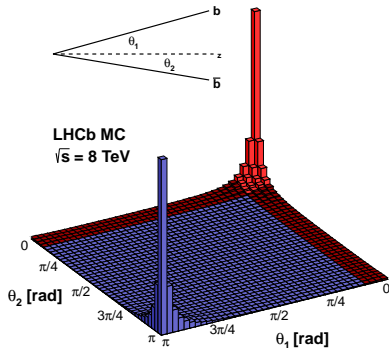
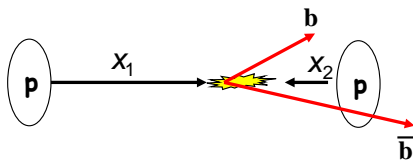
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- QCD exotics (tetra-, penta-quarks, glueballs etc.) potentially provide invaluable insight to underlying dynamics of QCD
  - hadronization, binding mechanism, color structure ...

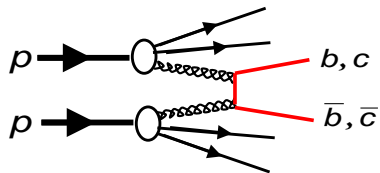
# The LHCb Experiment



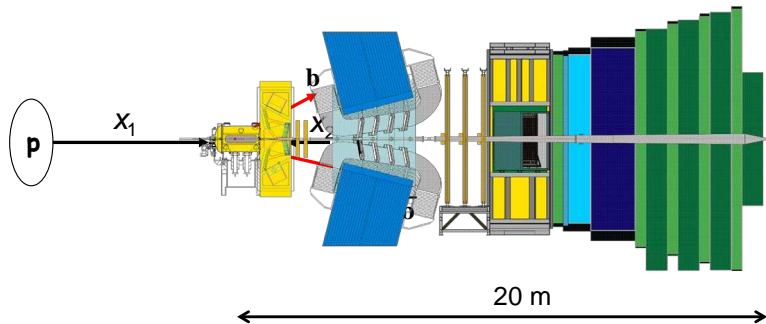
Run 2011-2012:  $3 \text{ fb}^{-1}$  (LHCb)  
200 kHz  $b\bar{b}$   $\rightarrow 2.6 \times 10^{11} b\bar{b}$   
4MHz  $c\bar{c}$   $\rightarrow 5.9 \times 10^{12} c\bar{c}$



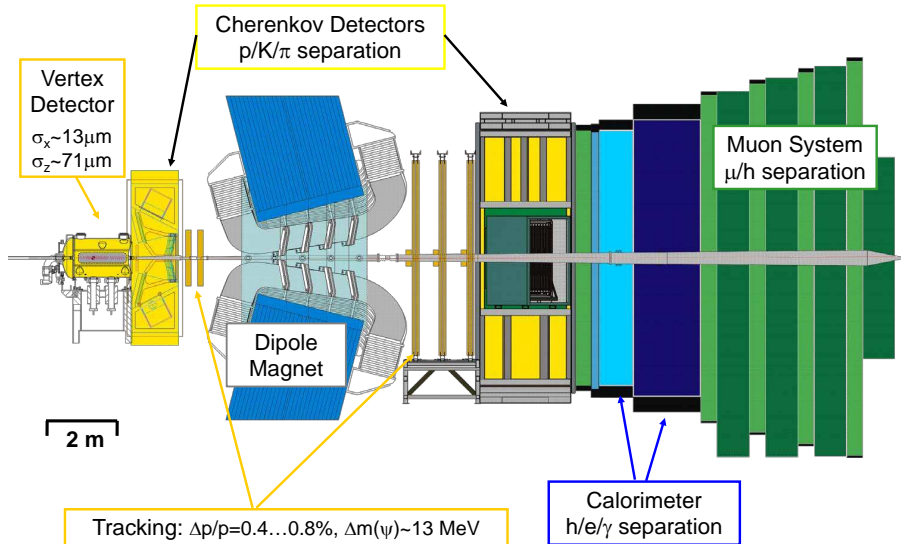
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# The LHCb Detector





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## $X(3872)$ Properties

Discovered by Belle 2003 ([PRL 91 262001](#))

in  $B^\pm \rightarrow [J/\psi\pi^+\pi^-]_{X(3872)}K^\pm$  decays

significant isospin violation

$M_0 = 3871.69 \pm 0.17$  MeV

$\Gamma_0 < 1.2$  MeV @ 90% CL

- $\sigma(pp \rightarrow X(3872) + \text{anything})$   
 $\times \mathcal{B}(X(3872) \rightarrow J/\psi\pi^+\pi^-)$   
 $= 5.4 \pm 1.3 \pm 0.8$  nb ([EPJC 72 1972](#))

# LHCb Results on the $X(3872)$

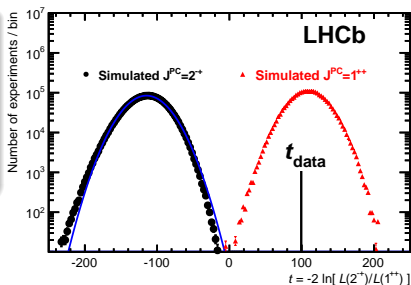
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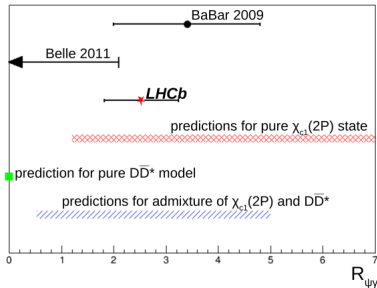
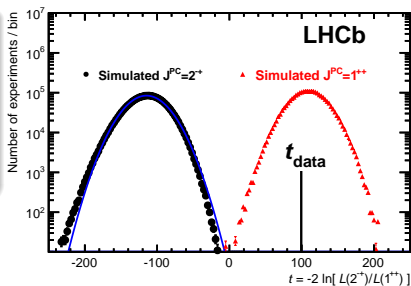
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- Quantum numbers  $I^G(J^{PC}) = 0^+(1^{++})$   
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- $\frac{\mathcal{B}(X(3872) \rightarrow \psi(2S)\gamma)}{\mathcal{B}(X(3872) \rightarrow J/\psi\gamma)} = 2.5 \pm 0.6 \pm 0.3$   
(NPB 886 665)
- D-wave fraction  $f_D < 4\% \text{ @ 95\% CL}$   
(PRD 92 011102(R))
- Results hint towards  $c\bar{c}-D\bar{D}^*$  mixture or tetraquark pictures

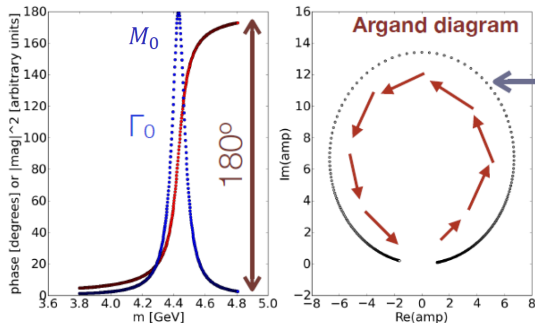


# Phase Motion of a Breit-Wigner amplitude

- Resonances (R) parametrized by relativistic Breit-Wigner amplitude

$$BW(M|M_0\Gamma_0) = \frac{1}{M_0^2 - M^2 - iM_0\Gamma(M)}$$

$$\text{where } \Gamma(M) = \Gamma_0 \left(\frac{q}{q_0}\right)^{2L_R+1} \frac{M_0}{M} B'_{L_R}(q, q_0, d)^2$$



- Circular trajectory in complex plane is characteristic of resonance
- Circle can be rotated by arbitrary phase
- Phase change of 180° across the pole

## $Z(4430)$ Properties

Discovered by Belle 2007 (PRL 100 142001)

Not confirmed by BaBar 2008 (PRD 79 112001)

dominant  $K\pi$  reflections

$$M_0 = 4478_{-18}^{+15} \text{ MeV}$$

$$\Gamma_0 = 181 \pm 31 \text{ MeV}$$

$I(J^P) = ?(1^+)$ , decay to  $\psi(2S)\pi^\pm$

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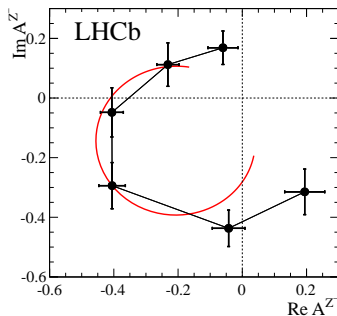
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- 4D model-dependent amplitude analysis
  - extracted resonant character
  - $J^P$  unambiguously  $1^+$
  - D-wave negligible



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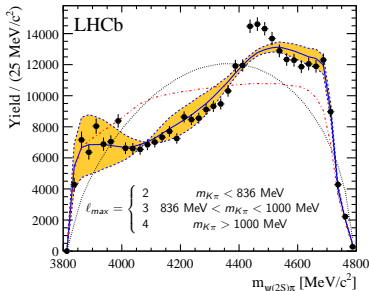
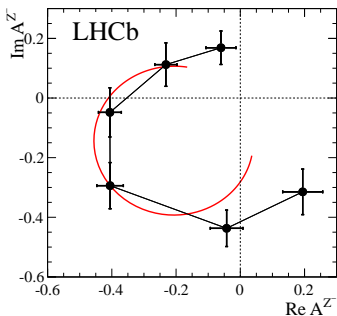
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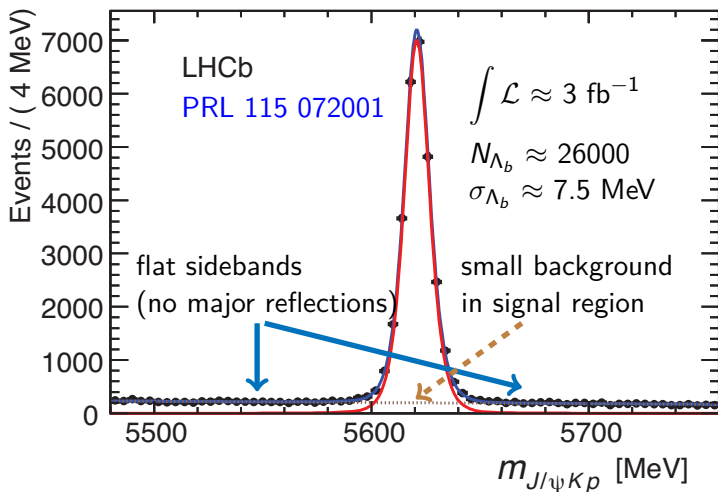
- 4D model-dependent amplitude analysis
  - extracted resonant character
  - $J^P$  unambiguously  $1^+$
  - D-wave negligible
- Model-independent moment analysis
  - Test if  $K\pi$  partial waves alone cause  $\psi(2S)\pi$  shape
  - Exclude unphysical spin  $\ell \geq 4$   $K\pi$  partial waves  $\Rightarrow S(Z) = 8\sigma$
- Tetraquark picture most plausible





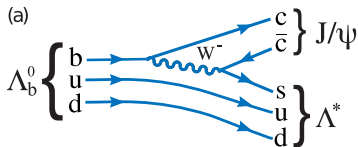
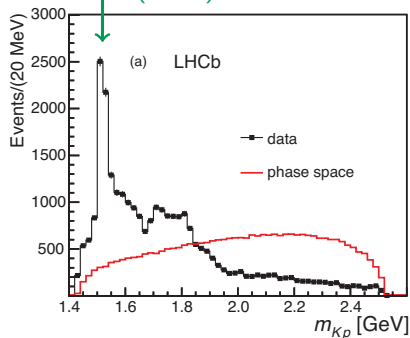
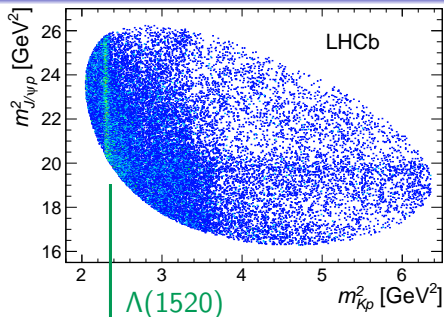
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# LHCb - The $b$ -baryon Factory

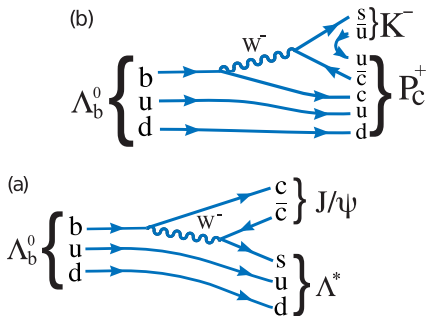
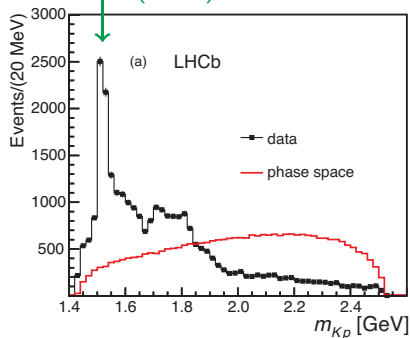
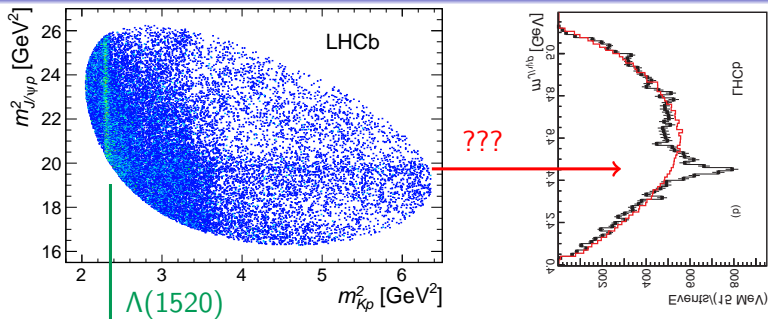


- Initial goal: measurement of  $\Lambda_b$  lifetime (PRL 111 102003)
- $\mathcal{B}(\Lambda_b^0 \rightarrow J/\psi p K^-) = (3.04^{+0.55}_{-0.43}) \times 10^{-4}$  (arXiv:1509.00292)

# An Unexpected Structure in $m_{J/\psi p}$

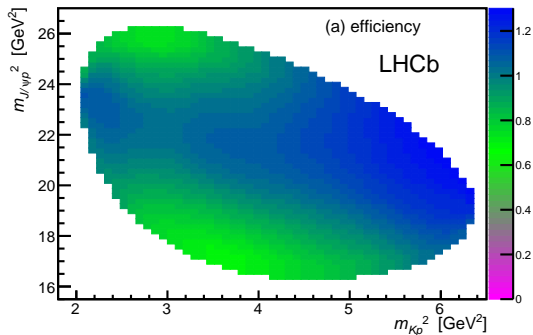


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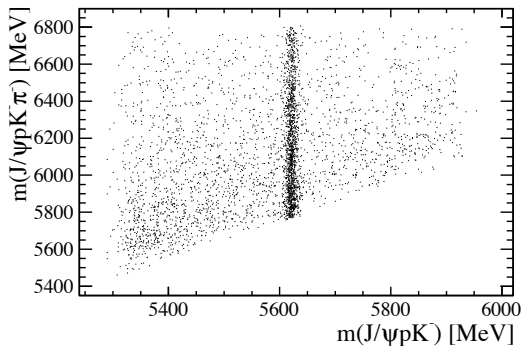
# Is the Structure due to an Artefact?

- Smooth efficiency cannot create a peak



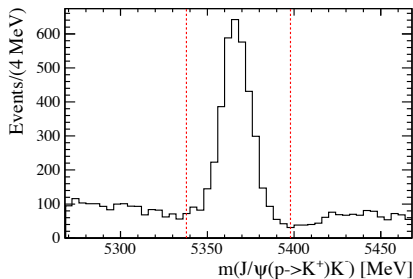
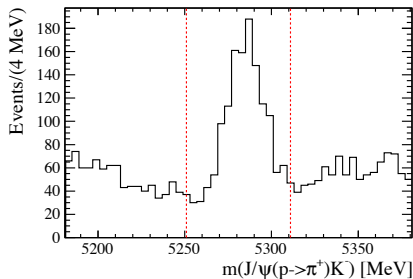
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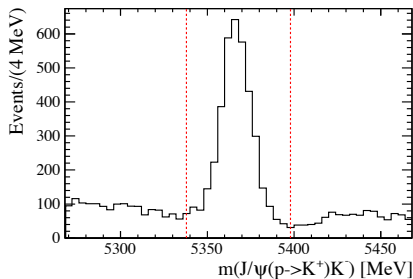
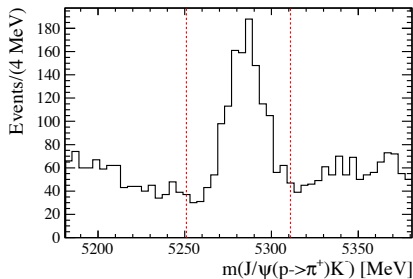
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- Tested against selection artefacts
- Cross-checked by different analysis-teams
- Checked against clones/ghost-tracks





- Fit efficiency  $\epsilon$  corrected PDF  $\mathcal{P}$  in 1+5 dimensions  $m_{Kp}, \Omega$  with parameters  $\omega$

$$\mathcal{P}_{\text{sig}}(m_{Kp}, \Omega|\omega) = \frac{1}{I(\omega)} |\mathcal{M}(m_{Kp}, \Omega|\omega)|^2 \Phi(m_{Kp}) \epsilon(m_{Kp}, \Omega)$$

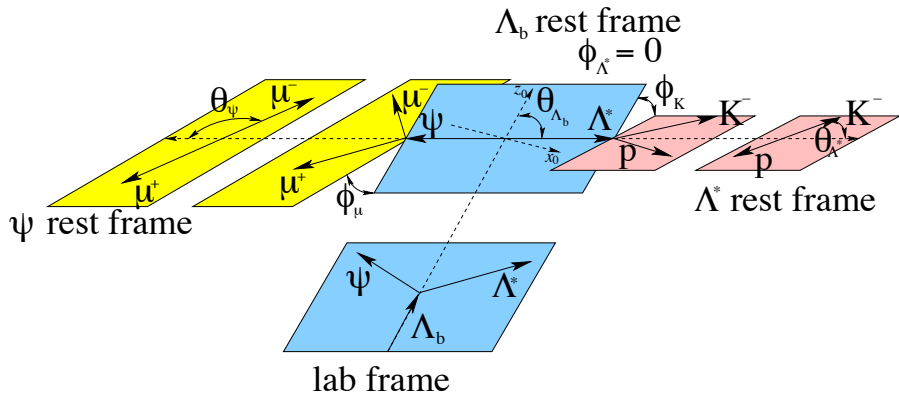
Normalization integral

Matrix element for  $\Lambda_b$  decay (on next slides)

Phase space factor

- Background handled by conventional sideband subtraction: *cFit* or signal unfolding using *sPlot* (NIM A 555, 356): *sFit*
- Fits coded independently for cross-check

# $\Lambda_b \rightarrow J/\psi \Lambda^*$ Decay Chain in the Isobar Model



Fit observables:  $m_{Kp}, \Omega = \{\theta_{\Lambda_b}, \phi_K, \phi_\mu, \theta_{\Lambda^*}, \theta_\psi\}$

# Isobar Model Helicity Amplitudes for $\Lambda_b \rightarrow J/\psi \Lambda^*$

The matrix element of the  $\Lambda_b \rightarrow J/\psi \Lambda^*$  decay chain is given by:

$$\mathcal{M}_{\lambda_{\Lambda_b}, \lambda_p, \Delta\lambda_\mu}^{\Lambda^*} = \sum_n R_n(m_{Kp}) \mathcal{H}_{\lambda_p}^{\Lambda_n^* \rightarrow Kp} \sum_{\lambda_\psi} e^{i\lambda_\psi \phi_\mu} d_{\lambda_\psi, \Delta\lambda_\mu}^1(\theta_\psi) \times$$

$$\sum_{\lambda_{\Lambda_n^*}} \mathcal{H}_{\lambda_{\Lambda_n^*}, \lambda_\psi}^{\Lambda_b \rightarrow \Lambda_n^* \psi} e^{i\lambda_{\Lambda_n^*} \phi_K} d_{\lambda_{\Lambda_b}, \lambda_{\Lambda_n^*} - \lambda_\psi}^{\frac{1}{2}}(\theta_{\Lambda_b}) d_{\lambda_{\Lambda_n^*}, \lambda_p}^{J_{\Lambda_n^*}}(\theta_{\Lambda_n^*})$$

- $\Lambda^*$  resonant amplitudes (masses/widths): Breit-Wigner
- Helicity couplings for  $\Lambda^*$  and  $\Lambda_b$  decays (4-6 complex fit parameters per amplitude)
- Angular structure of  $\Lambda_b$ ,  $J/\psi$  and  $\Lambda^*$  decays (no free parameters)

# $\Lambda^*$ Resonance Model

State	$J^P$	PDG class	Mass (MeV)	$\Gamma$ (MeV)	# Reduced	# Extended
$\Lambda(1405)$	$1/2^-$	****	$1405.1^{+1.3}_{-1.0}$	$50.5 \pm 2.0$	3	4
$\Lambda(1520)$	$3/2^-$	****	$1519.5 \pm 1.0$	$15.6 \pm 1.0$	5	6
$\Lambda(1600)$	$1/2^+$	***	1600	150	3	4
$\Lambda(1670)$	$1/2^-$	****	1670	35	3	4
$\Lambda(1690)$	$3/2^-$	****	1690	60	5	6
$\Lambda(1710)$	$1/2^+$	*	$1713 \pm 13$	$180 \pm 40$	0	0
$\Lambda(1800)$	$1/2^-$	***	1800	300	4	4
$\Lambda(1810)$	$1/2^+$	***	1810	150	3	4
$\Lambda(1820)$	$5/2^+$	****	1820	80	1	6
$\Lambda(1830)$	$5/2^-$	****	1830	95	1	6
$\Lambda(1890)$	$3/2^+$	****	1890	100	3	6
$\Lambda(2000)$	?	*	$\approx 2000$	?	0	0
$\Lambda(2020)$	$7/2^+$	*	$\approx 2020$	?	0	0
$\Lambda(2050)$	$3/2^-$	*	$2056 \pm 22$	$493 \pm 60$	0	0
$\Lambda(2100)$	$7/2^-$	****	2100	200	1	6
$\Lambda(2110)$	$5/2^+$	***	2110	200	1	6
$\Lambda(2325)$	$3/2^-$	*	$\approx 2325$	?	0	0
$\Lambda(2350)$	$9/2^+$	***	2350	150	0	6
$\Lambda(2585)$	$5/2^-?$	**	$\approx 2585$	200	0	6

- All established  $\Lambda^*$  resonances included in fit

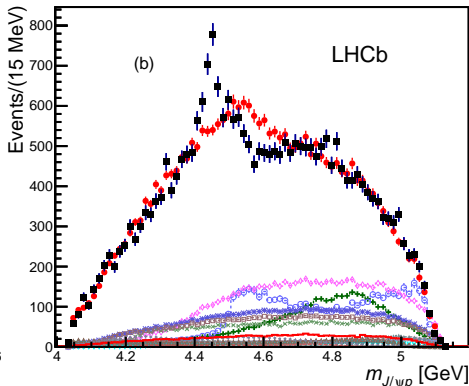
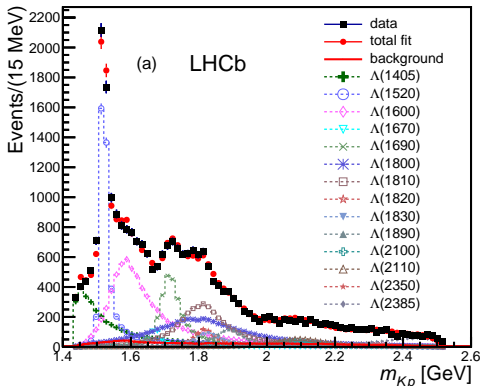
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$\Lambda(1600)$	$1/2^+$	***	1600	150	3	6
$\Lambda(1670)$	$1/2^-$	****	1670	35	3	6
$\Lambda(1690)$	$3/2^-$	****	1690	60	3	6
$\Lambda(1710)$	$1/2^+$	*	$1713 \pm 13$	$180$	3	0
$\Lambda(1800)$	$1/2^-$	***	1800	180	3	4
$\Lambda(1810)$	$1/2^+$	***	1810	180	3	4
$\Lambda(1820)$	$5/2^+$	****	1820	180	1	6
$\Lambda(1830)$	$5/2^-$	****	1830	95	1	6
$\Lambda(1890)$	$3/2^+$	*	1890	100	3	6
$\Lambda(2000)$	?	?	2000	?	0	0
$\Lambda(2020)$	?	?	$\approx 2020$	?	0	0
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Large number of free parameters (in 6D)  
 computationally expensive and challenging fit

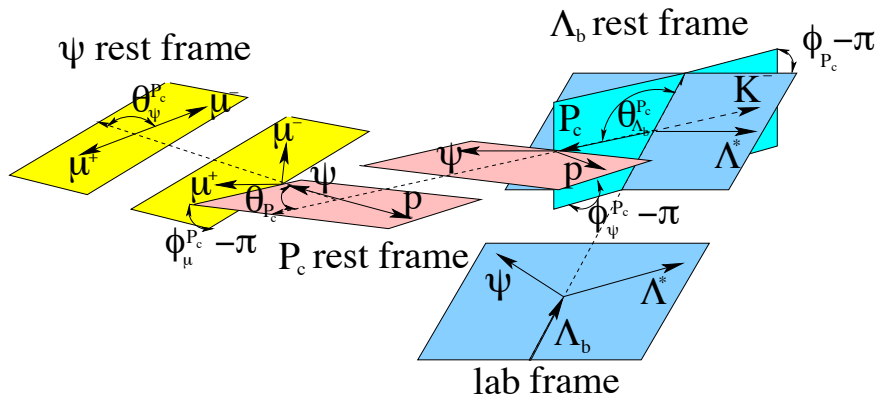
- All established  $\Lambda^*$  resonances included in fit

# Fit with $\Lambda^*$ States Only



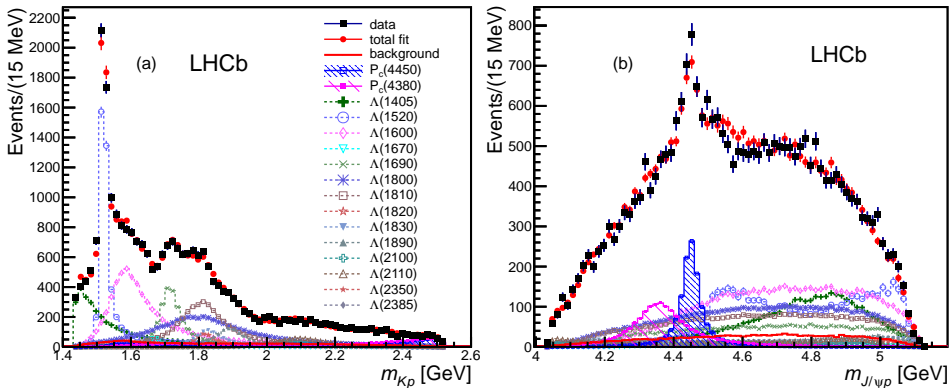
- Including non resonant components up to  $J^P=3/2^\pm$ ,  $\Sigma^*$ 's and floating masses and widths of  $\Lambda^*$ 's can also not describe  $m_{J/\psi p}$
- Next: attempt to obtain better fit by including  $m_{J/\psi p}$  resonances

# Adding the $\Lambda_b \rightarrow P_c^+ K^-$ Decay Chain



construct  $\mathcal{M}_{\lambda_{\Lambda_b}, \lambda_{P_c}, \Delta\lambda_{\mu}^{P_c}}^{P_c}$  analogous to  $\mathcal{M}_{\lambda_{\Lambda_b}, \lambda_p, \Delta\lambda_{\mu}}^{\Lambda^*}$

# Best Fit with Two $P_c$ States



- Adding 2<sup>nd</sup>  $P_c$  gives good description of data in all observables
- $\Delta(2 \ln \mathcal{L}) = 11.6^2$  from adding 2<sup>nd</sup>  $P_c$  vs. only 1  $P_c$
- Best fit has  $J^P(P_c(4380), P_c(4450)) = (3/2^-, 5/2^+)$ , also  $(3/2^+, 5/2^-)$  and  $(5/2^+, 3/2^-)$  reasonable



State	Mass (MeV)	Width (MeV)	Fit fraction (%)	Significance
$P_c(4380)^+$	$4380 \pm 8 \pm 29$	$205 \pm 18 \pm 86$	$8.4 \pm 0.7 \pm 4.2$	$9\sigma$
$P_c(4450)^+$	$4449.8 \pm 1.7 \pm 2.5$	$39 \pm 5 \pm 19$	$4.1 \pm 0.5 \pm 1.1$	$12\sigma$

- Syst. uncertainties on  $\Lambda^*$  model and  $J^P$  assignment dominate
- Significances calculated by fitting distribution of test-statistic ( $\Delta(2 \ln \mathcal{L})$ ) from toyMC experiments

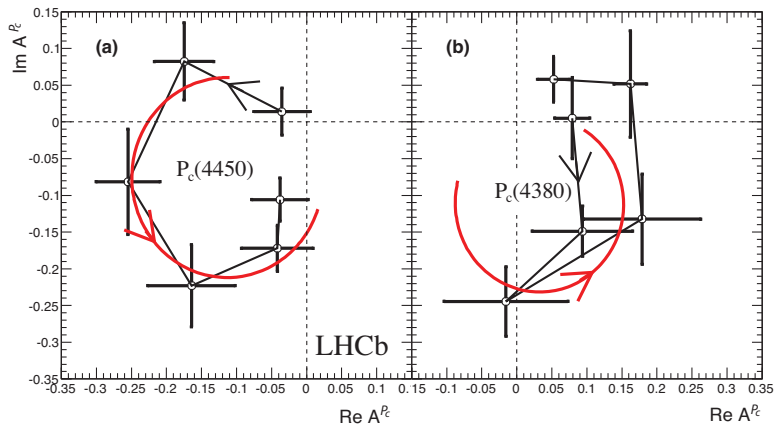
Null $\rightarrow$ Alternative Hypothesis	$\Delta(2 \ln \mathcal{L})$	Significance
$0 P_c \rightarrow 1 P_c$	$14.7^2$	$12\sigma$
$1 P_c \rightarrow 2 P_c$ 's	$11.6^2$	$9\sigma$
$0 P_c \rightarrow 2 P_c$ 's	$18.7^2$	$15\sigma$

- In a separate paper, LHCb measured ([arXiv:1509.00292](https://arxiv.org/abs/1509.00292))

$$B(\Lambda_b \rightarrow P_c^+ K^-) B(P_c^+ \rightarrow J/\psi p) = \begin{cases} (2.56 \pm 0.22 \pm 1.28_{-0.36}^{+0.46}) \times 10^{-5} & \text{for } P_c(4380)^+ \\ (1.25 \pm 0.15 \pm 0.33_{-0.18}^{+0.22}) \times 10^{-5} & \text{for } P_c(4450)^+ \end{cases}$$

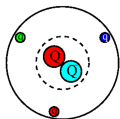
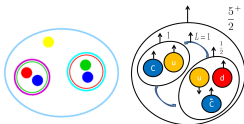
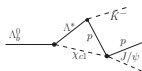
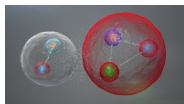
# Phase Motion

- Test resonant character of  $P_c$ 's by plotting spline-interpolated amplitude in an Argand diagram
  - Scan  $m_{J/\psi p}$  in 6 bins around  $m_0 \pm \Gamma_0$  of  $P_c$ 's
  - Fit data with full model but replace Breit-Wigner parametrization with cubic spline interpolating from 4 closest neighbouring points



# Theory Community Responding to $P_c$ candidates

- Already 81 citations!



Molecular models:

- $P_c(4450)$  as  $\Sigma_c \bar{D}^*$  molecule
- $P_c(4380)$  as  $\Sigma_c \bar{D}^*$  and  $P_c(4450)$  as  $\Sigma_c^* \bar{D}^*$
- $P_c(4380)$  as  $\Sigma_c \bar{D}^*$  and  $P_c(4450)$  as  $\Sigma_c^* \bar{D}$
- $P_c(4450)$  as  $\Sigma_c \bar{D}^*$  and  $\Sigma_c^* \bar{D}^*$  molecule
- $P_c$ 's not (colored) molecules
- $P_c(4380)$  as  $\Sigma_c^* \bar{D}$  and  $P_c(4450)$  as  $\Sigma_c \bar{D}^*$
- $P_c(4450)$  as  $\chi_{c1} p$  molecule (compositeness)

Rescattering effects:

- $\chi_{c1} p$  rescattering,  $\Lambda(1890)\chi_{c1} p$  triangle singularity
- ATS, cusp effect
- $D^* D_s^* \Sigma_c$  triangle singularity
- $P_c(4380)$  rescattering,  $P_c(4450)$  diquark model

Diquarks/Triquarks:

- Diquark-Diquark-Antiquark ( $[qq][qq]\bar{q}$ )
- Dynamical Diquark-Triquark
- Diquark-Diquark-Antiquark multiplets
- Quasi particle diquarks
- $[qq][qq]\bar{q}$  with QCD sum rules
- $P_c(4380)$  as  $J/\psi K$  reflection,  $P_c(4450)$  as  $[qq][qq]\bar{q}$
- Dynamical Diquark-Triquark multiplets

Other:

- Bound  $\bar{D}$ -soliton
- Intrinsic charm in  $\Lambda_b$  decays
- Baryocharmonium
- Phenomenology review
- $J/\psi K$  reflection
- $Z_{2,3}$  geometrical symmetries

[PRL 115 122001](#)

[PRL 115 132002](#)

[PRL 115 172001](#)

[arXiv:1507.04249](#)

[arXiv:1507.04694](#)

[arXiv:1507.05200](#)

[arXiv:1511.00870](#)

[PRD 92 071502\(R\)](#), [PLB 751 59](#)

[arXiv:1507.05359](#)

[arXiv:1507.06552](#)

[arXiv:1507.07652](#)

[PLB 749 289](#)

[PLB 749 454](#)

[arXiv:1507.08252](#)

[arXiv:1508.00356](#)

[arXiv:1508.01468](#)

[arXiv:1509.04898](#)

[arXiv:1510.08693](#)

[PRD 92 051501\(R\)](#)

[arXiv:1508.03910](#)

[PRD 92 031502\(R\)](#)

[arXiv:1509.02460](#)

[arXiv:1509.03028](#)

[arXiv:1509.06013](#)

(List may be incomplete, not listing implications)

# Implications for experiments

## Concerning $P_c(4380)$ and $P_c(4450)$

- Most important: confirmation by other experiments needed!
- Observe  $P_c \rightarrow J/\psi p$  as subsystems in different final states, e.g.:
  - $\Lambda_b \rightarrow J/\psi p \pi$
  - $\Upsilon \rightarrow J/\psi p \bar{p}$  (check for peaks at  $\chi_{c0,1,2} p$  thresholds ([PRD 92 071502\(R\)](#)))
- Observe new decay modes of  $P_c$ 's, e.g. in:
  - $\Lambda_b \rightarrow \chi_{c1} p K$  (decay of  $P_c(4450)$  in this channel rules out  $\chi_{c1} p$  rescattering ([PRD 92 071502\(R\)](#) )
  - $\Lambda_b \rightarrow \Lambda_c \bar{D}^0 K$

## Search for other types of pentaquarks

- Hidden charm partners
- Open charm pentaquarks
- Triply charged baryons
- Bottom pentaquarks
- Hidden strangeness pentaquarks

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## At distant horizons

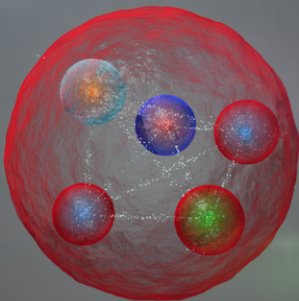
- Dibaryons?
- Hexaquarks?
- Heptaquarks?
- ...

- LHCb confirmed and measures distinct properties of the exotic  $X(3872)$  and  $Z(4430)$
- First observation of two  $J/\psi p$  resonances in amplitude analysis of  $\Lambda_b^0 \rightarrow J/\psi p K^-$
- Resonant phase motion of pentaquark candidates extracted
  - Consistent with Breit-Wigner for  $P_c(4450)^+$
  - More complicated for  $P_c(4380)^+$  (motion counter-clockwise)
- Link between  $XYZ$  states and pentaquarks potentially provides key towards some fundamental principles of QCD phenomenology
- LHCb has a broad (exotic) spectroscopy programme in meson and baryon sector

nature

The LHCb result  
leaves little doubt  
that **pentaquarks**  
are real

[bit.ly/pentaquarks](https://bit.ly/pentaquarks)

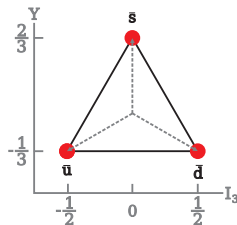
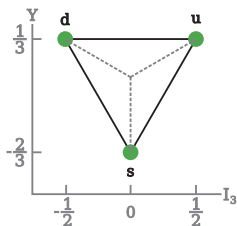


Backup slides start here



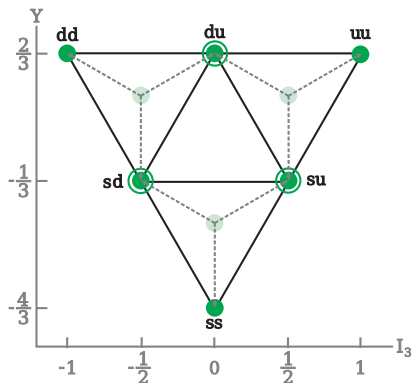
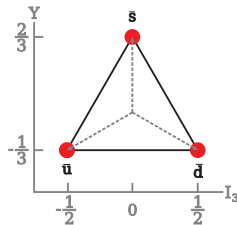
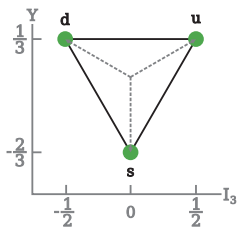
# Multiquark Exotic States from $SU(3)_{\text{flavor}}$ Symmetry

- Hadrons are physical observable color singlet bound states of quarks
- They can be labelled by their minimum (valence) quark content
  - so far  $q_1 q_2 q_3$ ,  $q_1 \bar{q}_2$  and  $q_1 q_2 \bar{q}_1 \bar{q}_3$ (?!)



# Multiquark Exotic States from $SU(3)_{\text{flavor}}$ Symmetry

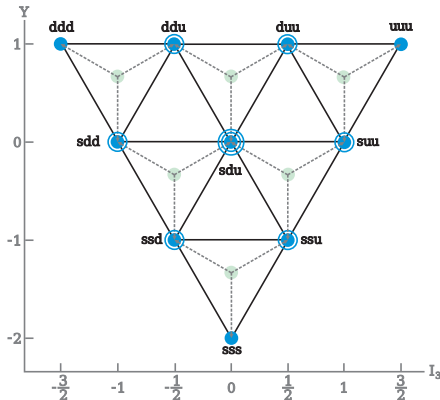
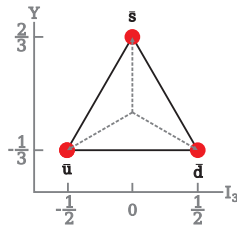
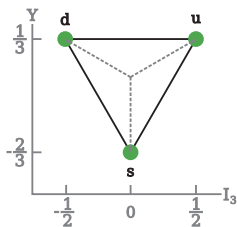
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$$3 \otimes 3 = 6 \oplus \bar{3}$$

# Multiquark Exotic States from $SU(3)_{\text{flavor}}$ Symmetry

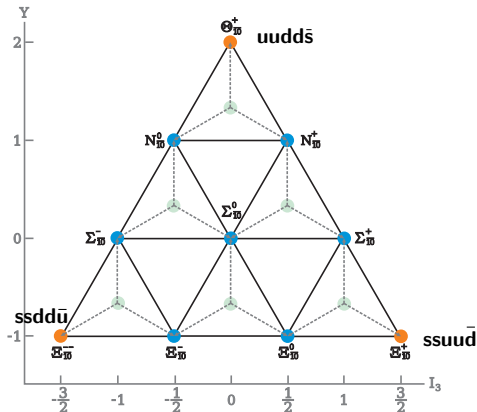
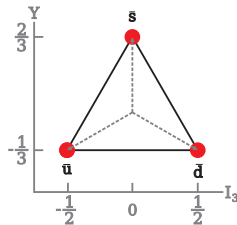
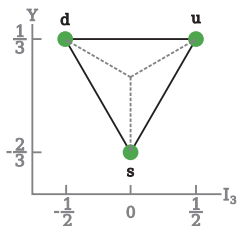
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$$\mathbf{3} \otimes \mathbf{3} \otimes \mathbf{3} = \mathbf{10} \oplus \mathbf{8}^{(2)} \oplus \mathbf{1}$$

# Multiquark Exotic States from $SU(3)_{\text{flavor}}$ Symmetry

- Hadrons are physical observable color singlet bound states of quarks
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  - so far  $q_1 q_2 q_3$ ,  $q_1 \bar{q}_2$  and  $q_1 q_2 \bar{q}_1 \bar{q}_3$  (!?)



$$3 \otimes 3 \otimes 3 \otimes 3 \otimes \bar{3} = 35 \oplus 27^{(3)} \oplus \bar{10}^{(2)} \oplus 10^{(4)} \oplus 8^{(8)} \oplus 1^{(3)}$$

# Searches for $S = +1$ Baryons

- Broad exotic  $KN$  resonances predicted 1976 (SLAC-PUB-1774)

- Resonant partial waves claimed in 70's and early 80's (PDG, RPP 1992)

- Light - current consensus:  $\Theta^+$  faked by kinematic cuts,  $t$ -channel exchanges or experimental artefacts in LEPS II result and amplitude analysis needed to settle the  $\Theta^+$  issue for good
- Searches - Amplitude analysis needs fully exclusive events or exclusive decay chain (e.g.  $\psi \rightarrow \Theta^+ \bar{N} \bar{K}$  or  $\Lambda_b^0 \rightarrow \Theta^+ \bar{K}^0 \pi^-$ )

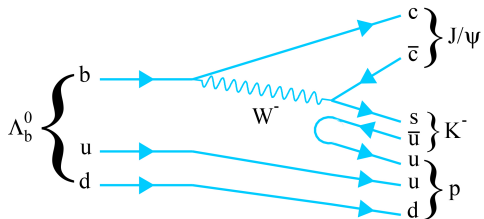
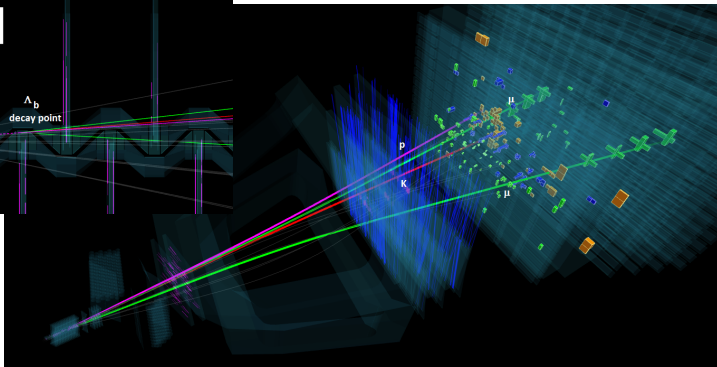
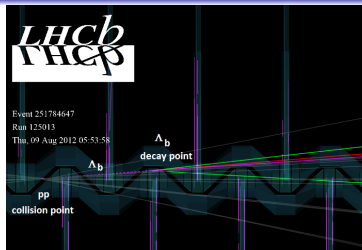
- subsequently (PDG, RPP 2008)

## Z BARYONS ( $S = +1$ )

... New partial-wave analyses<sup>4,5</sup> appeared in 1984 and 1985, and both claimed that the  $P_{13}$  and perhaps other waves resonate. However, the results permit no definite conclusion — the same story heard for 20 years. The standards of proof must simply be more severe here than in a channel

that find weak, but there is an overwhelming consensus that they do not exist. The only mention in the literature in 2003" was a paper by themselves, the phenomenologists that followed, and the eventual "undiscovery" — is a curious episode in the history of science.

# $\Lambda_b^0 \rightarrow J/\psi p K^-$ Selection



- "Standard" selection including decay chain fitting (NIM A 552 566) and Multi-Variate-Analysis

(arXiv:0703039)

- Fit efficiency  $\epsilon$  corrected PDF  $\mathcal{P}$  in 1+5 dimensions  $m_{Kp}, \Omega$

$$\mathcal{P}_{\text{sig}}(m_{Kp}, \Omega|\omega) = \frac{1}{I(\omega)} |\mathcal{M}(m_{Kp}, \Omega|\omega)|^2 \Phi(m_{Kp}) \epsilon(m_{Kp}, \Omega)$$

Normalization integral

Matrix element for  $\Lambda_b$  decay (on next slides)

Phase space factor

- Background handled by conventional sideband subtraction *cFit* or signal unfolding using *sPlot* (NIM A 555, 356) *sFit*

$$\mathcal{P}(m_{Kp,i}, \Omega_i|\omega) = (1 - \beta)\mathcal{P}_{\text{sig}}(m_{Kp}, \Omega|\omega) + \beta \mathcal{P}_{\text{bkg}}(m_{Kp}, \Omega)$$

$$-2 \ln \mathcal{L}(\omega) = -2 \sum_i \frac{w_i}{w_i^2} \sum_i w_i \ln \mathcal{P}(m_{Kp,i}, \Omega_i|\omega) \quad w_i = 1$$

- Fits coded independently for cross-check

$\beta = 5.4\%$

# $\Lambda^*$ Resonance Model

Dynamical terms  $R_n(m_{pK})$  parametrized by

- Relativistic single-channel Breit-Wigner amplitudes
- (dressed) Blatt-Weisskopf barrier factors (PRD 5 624)

$$R_n(m_{Kp}) = \tilde{B}_{L_{\psi\Lambda^*}}^{\Lambda_b} \times BW(m_{Kp} | m_0^{\Lambda_n^*}, \Gamma_0^{\Lambda_n^*}) \times \tilde{B}_{L_{pK}}^{\Lambda^*}$$

$$\text{with } BW(m | m_0 \Gamma_0) = \frac{1}{m_0^2 - m^2 - im_0 \Gamma(m)}$$

$$\text{and } \Gamma(m) = \Gamma_0 \left( \frac{q}{q_0} \right)^{2L_{\Lambda^*} + 1} \frac{m_0}{m} B'_{L_{\Lambda_n^*}}(q, q_0, d)^2$$

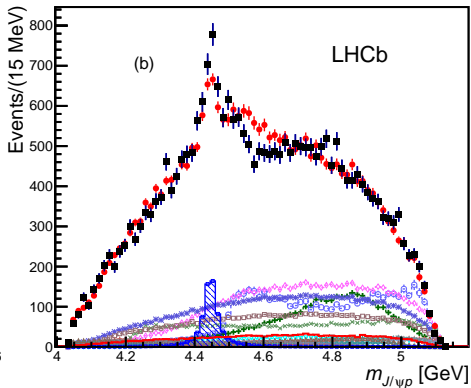
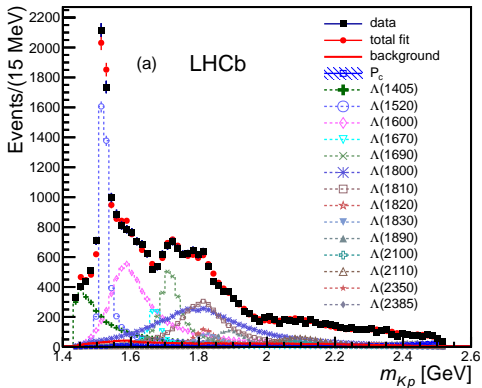
where  $p(q)$  are momenta of daughters in CM frame of mother  
and subscript-0 denotes evaluation at nominal resonance parameters (PDG)

- Exception: sub-threshold  $\Lambda(1405)$  described by Flatté-like parametrization (PLB 63 224)



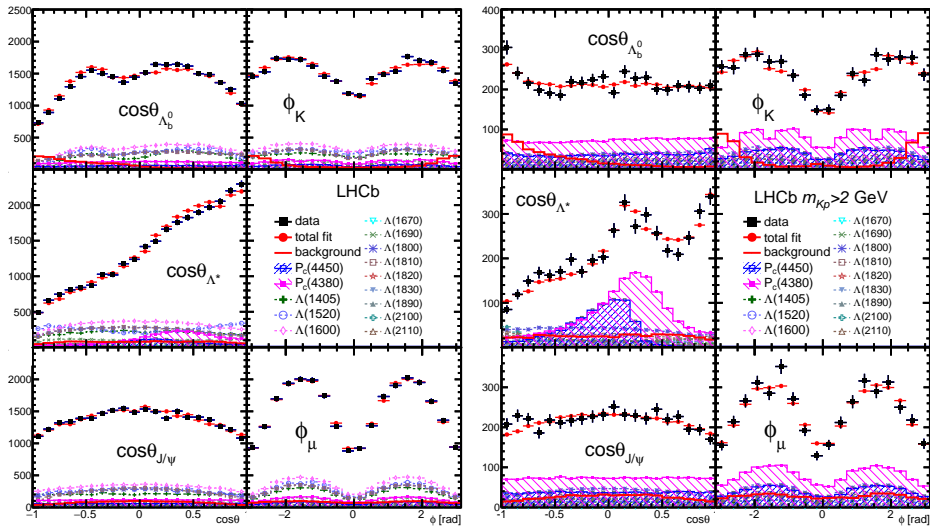


# Best Fit with Single $P_c$ State

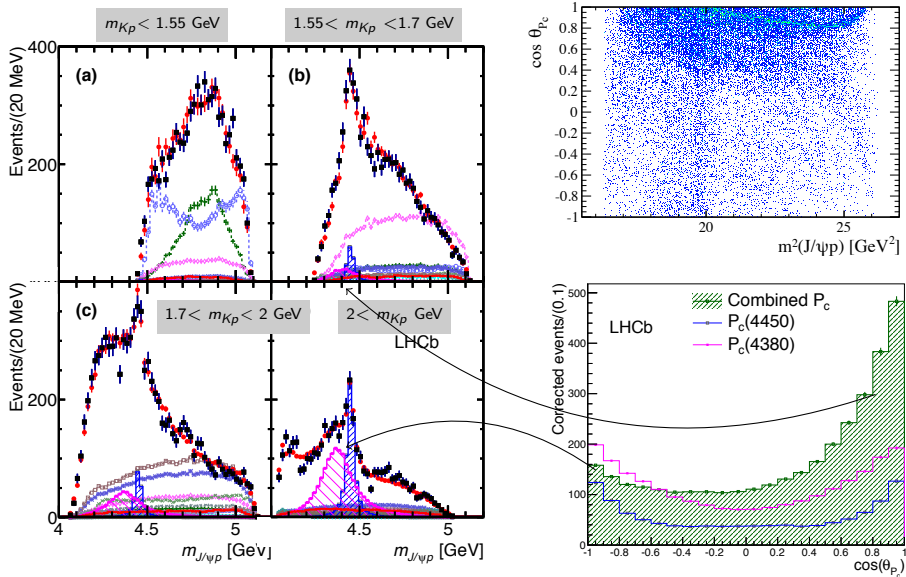


- $P_c$  of best fit has  $J^P = 5/2^+$  (tried up to  $J^P = 7/2^\pm$ )
- $\Delta(2 \ln \mathcal{L}) = 14.7^2$  when adding single  $P_c$  vs.  $\Lambda^*$  only
- Likelihood significantly improved, but still discrepancies in  $m_{J/\psi p}$

# Angular Distributions



# Preference of Opposite Parity $P_c$ States



# No Need for $m_{J/\psi K}$ Resonance

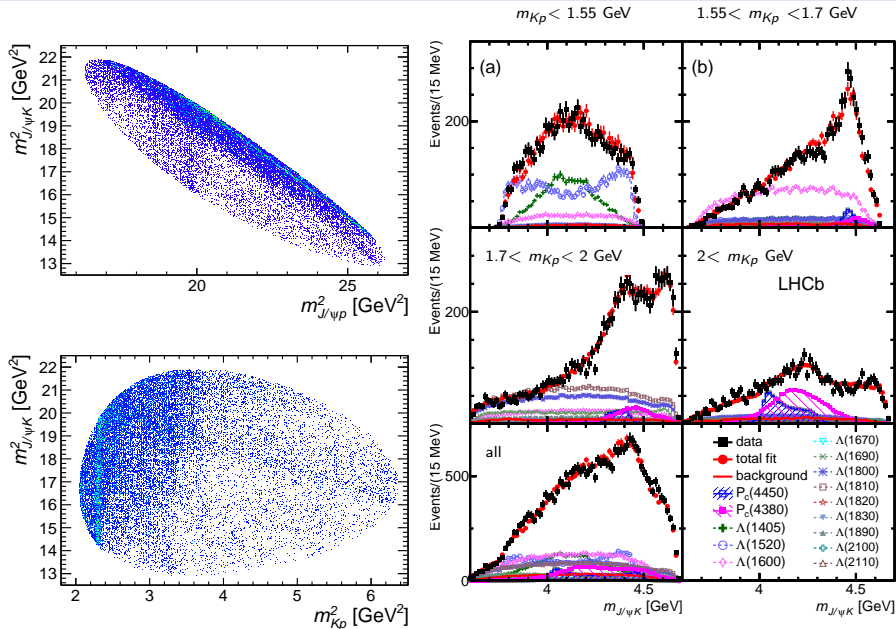


Table : Changes in fit quality using cFit from the baseline two  $P_c$  fit for different combinations of  $J^P$  states in terms of the difference  $-2\ln\mathcal{L}$ , where zero is set from cFit for the  $(3/2^-, 5/2^+)$  case. The first column is for the low mass, wider width  $P_c$  and the second for the narrower higher mass state.

Fit	$\Delta(-2\ln\mathcal{L})$	$P_c$ (Low) Mass	$P_c$ (Low) $\Gamma$	$P_c$ (High) Mass	$P_c$ (High) $\Gamma$
0	4.3799 ± 0.0064	0.205 ± 0.011	4.4498 ± 0.0017	0.0387 ± 0.0037	
0.9 <sup>2</sup>	4.3696 ± 0.0063	0.211 ± 0.012	4.4504 ± 0.0017	0.0492 ± 0.0040	
2.3 <sup>2</sup>	4.3770 ± 0.0098	0.239 ± 0.024	4.4486 ± 0.0018	0.0444 ± 0.0053	
5.9 <sup>2</sup>	4.3703 ± 0.0085	0.252 ± 0.022	4.4477 ± 0.0019	0.0367 ± 0.0043	
5.9 <sup>2</sup>	4.3505 ± 0.0058	0.163 ± 0.012	4.4458 ± 0.0017	0.0553 ± 0.0042	
6.3 <sup>2</sup>	4.3762 ± 0.013	0.253 ± 0.051	4.4484 ± 0.0019	0.0520 ± 0.0050	
6.3 <sup>2</sup>	4.3580 ± 0.0115	0.186 ± 0.026	4.4469 ± 0.0019	0.0438 ± 0.0057	
6.4 <sup>2</sup>	4.3421 ± 0.0071	0.141 ± 0.016	4.4452 ± 0.0019	0.0492 ± 0.0048	
6.8 <sup>2</sup>	4.3394 ± 0.0080	0.136 ± 0.022	4.4460 ± 0.0020	0.0563 ± 0.0063	
6.8 <sup>2</sup>	4.3862 ± 0.0095	0.252 ± 0.027	4.4483 ± 0.0019	0.0420 ± 0.0042	
7.2 <sup>2</sup>	4.3643 ± 0.0135	0.222 ± 0.052	4.4460 ± 0.0019	0.0514 ± 0.0056	
7.3 <sup>2</sup>	4.3526 ± 0.0076	0.165 ± 0.021	4.4461 ± 0.0018	0.0438 ± 0.0049	
7.4 <sup>2</sup>	4.3422 ± 0.0082	0.152 ± 0.019	4.4468 ± 0.0019	0.0499 ± 0.0059	
7.6 <sup>2</sup>	4.3423 ± 0.0063	0.112 ± 0.014	4.4459 ± 0.0019	0.0536 ± 0.0054	
7.7 <sup>2</sup>	4.3580 ± 0.0087	0.183 ± 0.020	4.4455 ± 0.0020	0.0451 ± 0.0065	
8.0 <sup>2</sup>	4.3648 ± 0.0139	0.226 ± 0.040	4.4446 ± 0.0020	0.0451 ± 0.0055	
8.3 <sup>2</sup>	4.3493 ± 0.0067	0.150 ± 0.016	4.4463 ± 0.0017	0.0467 ± 0.0042	
8.5 <sup>2</sup>	4.3443 ± 0.0098	0.148 ± 0.031	4.4447 ± 0.0021	0.0632 ± 0.0073	
8.6 <sup>2</sup>	4.3709 ± 0.0087	0.199 ± 0.019	4.4477 ± 0.0018	0.0355 ± 0.0048	
8.6 <sup>2</sup>	4.4066 ± 0.0165	0.379 ± 0.080	4.4466 ± 0.0018	0.0382 ± 0.0040	
8.9 <sup>2</sup>	4.3500 ± 0.0081	0.142 ± 0.019	4.4462 ± 0.0020	0.0568 ± 0.0054	
8.9 <sup>2</sup>	4.3396 ± 0.0098	0.138 ± 0.025	4.4451 ± 0.0020	0.0510 ± 0.0056	
8.9 <sup>2</sup>	4.3332 ± 0.0085	0.118 ± 0.022	4.4434 ± 0.0020	0.0563 ± 0.0074	
9.0 <sup>2</sup>	4.3320 ± 0.0087	0.134 ± 0.023	4.4463 ± 0.0022	0.0588 ± 0.0072	
9.4 <sup>2</sup>	4.3762 ± 0.0081	0.204 ± 0.016	4.4487 ± 0.0019	0.0339 ± 0.0048	
9.6 <sup>2</sup>	4.3645 ± 0.0090	0.157 ± 0.019	4.4496 ± 0.0020	0.0479 ± 0.0051	
9.6 <sup>2</sup>	4.3671 ± 0.0010	0.193 ± 0.023	4.4470 ± 0.0019	0.0348 ± 0.0046	
9.9 <sup>2</sup>	4.3583 ± 0.0066	0.201 ± 0.013	4.4465 ± 0.0019	0.0421 ± 0.0031	
9.9 <sup>2</sup>	4.3823 ± 0.0099	0.222 ± 0.021	4.4476 ± 0.0021	0.0407 ± 0.0061	
10.5 <sup>2</sup>	4.3397 ± 0.0068	0.114 ± 0.015	4.4459 ± 0.0019	0.0507 ± 0.0055	
10.9 <sup>2</sup>	4.3642 ± 0.0091	0.168 ± 0.019	4.4482 ± 0.0019	0.0425 ± 0.0057	
11.6 <sup>2</sup>	4.3587 ± 0.0099	0.172 ± 0.020	4.4488 ± 0.0020	0.0376 ± 0.0049	

# Systematic Uncertainties

Source	$m_0$ (MeV)		$\Gamma_0$ (MeV)		Fit fractions (%)			
	low	high	low	high	low	high	$\Lambda(1405)$	$\Lambda(1520)$
Extended vs. reduced	21	0.2	54	10	3.14	0.32	1.37	0.15
$\Lambda^*$ masses & widths	7	0.7	20	4	0.58	0.37	2.49	2.45
Proton ID	2	0.3	1	2	0.27	0.14	0.20	0.05
$10 < p_p < 100$ GeV	0	1.2	1	1	0.09	0.03	0.31	0.01
Nonresonant	3	0.3	34	2	2.35	0.13	3.28	0.39
Separate sidebands	0	0	5	0	0.24	0.14	0.02	0.03
$J^P$ ( $3/2^+$ , $5/2^-$ ) or ( $5/2^+$ , $3/2^-$ )	10	1.2	34	10	0.76	0.44		
$d = 1.5-4.5$ GeV $^{-1}$	9	0.6	19	3	0.29	0.42	0.36	1.91
$L_{\Lambda_b}^{P_c} \Lambda_b \rightarrow P_c^+(\text{low/high})K^-$	6	0.7	4	8	0.37	0.16		
$L_{P_c} P_c^+(\text{low/high}) \rightarrow J/\psi p$	4	0.4	31	7	0.63	0.37		
$L_{\Lambda_b}^{\Lambda_n^*} \Lambda_b \rightarrow J/\psi \Lambda^*$	11	0.3	20	2	0.81	0.53	3.34	2.31
Efficiencies	1	0.4	4	0	0.13	0.02	0.26	0.23
Change $\Lambda(1405)$ coupling	0	0	0	0	0	0	1.90	0
Overall	29	2.5	86	19	4.21	1.05	5.82	3.89
sFit/cFit cross check	5	1.0	11	3	0.46	0.01	0.45	0.13

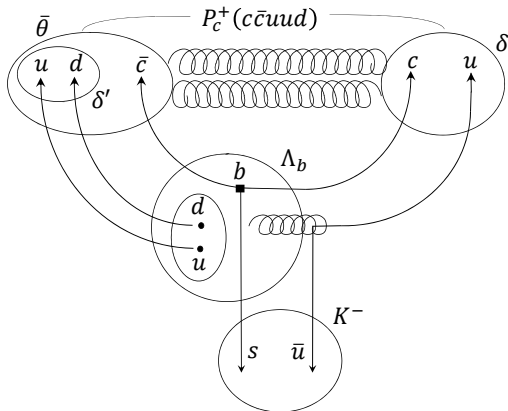
Uncertainties in  $\Lambda^*$  model dominate

Sizeable uncertainties from  $J^P$  assignment and resonance parametrization

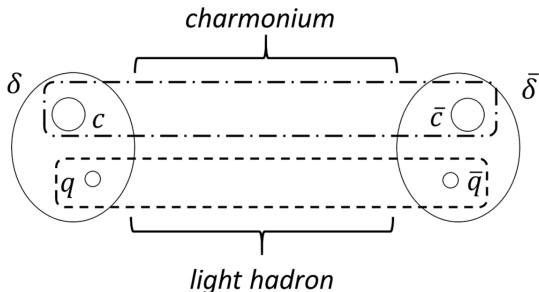
- Model provides qualitative information about tetraquark decay-widths, implies broad (or absence of) open charm tetraquarks and can incorporate hidden charm pentaquarks
- Quarks couple as  $\mathbf{3} \otimes \mathbf{3} = \mathbf{6} \oplus \bar{\mathbf{3}}$  to diquarks  $\delta$  in color-space
  - Evidence for  $0^+ \bar{\mathbf{3}}$  diquark from LQCD (PRL 97 222002)
- $\bar{\mathbf{3}}$  is attractive color-channel (coupling half as strong as color-singlet)
  - Triquark:  $[qq]_{\bar{\mathbf{3}}}\bar{q}_{\bar{\mathbf{3}}} \equiv \bar{\theta}$  is  $\bar{\mathbf{3}} \otimes \bar{\mathbf{3}} = \bar{\mathbf{6}} \oplus \mathbf{3}$  in color-space



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- $\delta_{\bar{\mathbf{3}}}\bar{\delta}_{\mathbf{3}}$  pair or  $\delta_{\bar{\mathbf{3}}}\bar{\theta}_{\mathbf{3}}$  produced at high relative momentum
- Kinetic energy between  $\delta$  and  $\bar{\delta}$  gradually converted in potential energy of color flux tube due to confinement



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- Hadronization via large  $r$  tails of mesonic wave functions, which suppresses decay widths
- Key ingredients for pentaquarks in this model
  - compact (in size  $r$ ) di-/triquarks (estimate slightly larger than mesonic  $r$  (PRD 91 094025))
  - high energy release to separate di-/triquarks
  - wave function overlap across spatially separated di-/triquarks
- Model provides qualitative information about tetraquark decay-widths, implies broad (or absence of) open charm tetraquarks and can incorporate hidden charm pentaquarks