

ZEUS Collaboration Meeting

September 9, 2015



Estimation of Negative Limits on the Effective Charge Radius of Quark

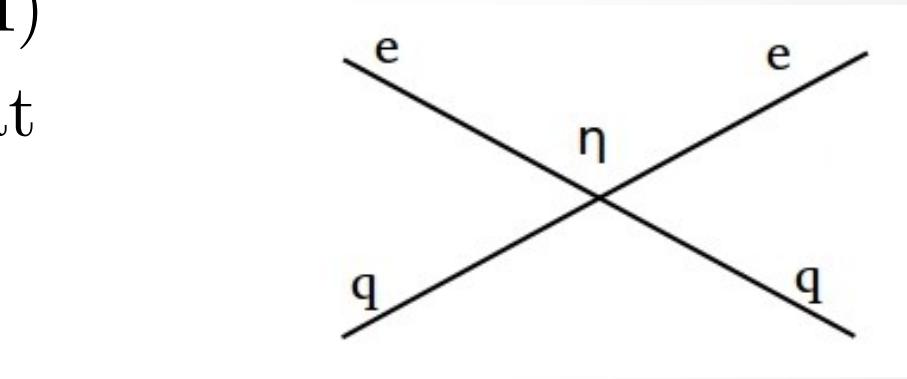
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Outline

- Quark radius model
- Probability method of setting limits
- χ^2 scan
- Model and parametrization variations
- Results
- Conclusions

Briefly about Contact Interactions

- Contact Interactions (CI)
 - an effective theory that describes low-energy effects of the BSM contributions
- To include CI into SM Lagrangian one should add additional terms:



$$L_{CI} = \sum_{\substack{i, j = L, R \\ q = u, d, s, c, b}} \eta_{ij}^{eq} (\bar{e}_i \gamma^\mu e_i) (\bar{q}_j \gamma_\mu q_j)$$

HERAFitter package (<https://www.herafitter.org>)

Input:

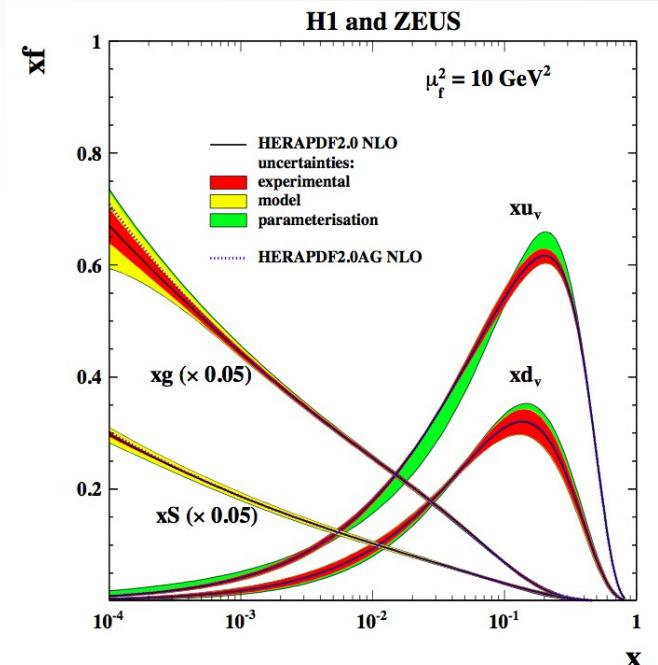
- Experimental data from HERA, Tevatron, LHC
- Different processes NC, CC, DIS, jets, diffraction, heavy quarks, Drell-Yan, W production

Together with theoretical tools:

- FastNLO, Applgrid
- DGLAP (QCDNUM)
- MSTW, CTEQ

Output:

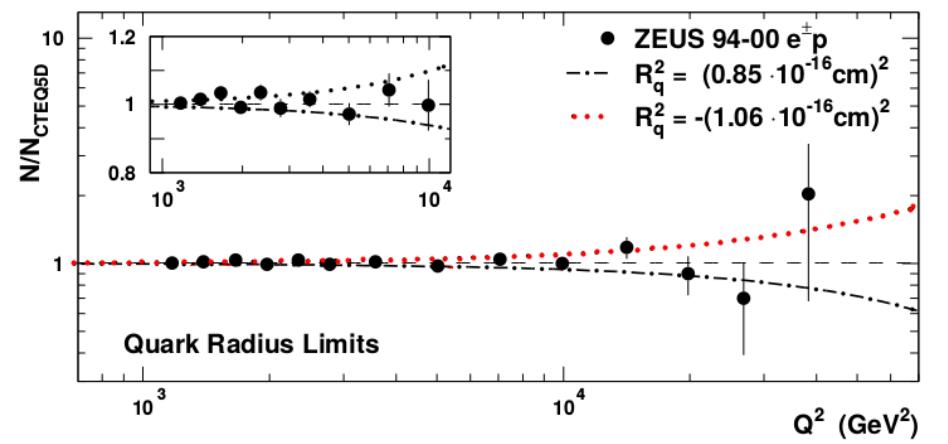
- Set of PDFs
- Constants: $\alpha_s, M_c, M_b, f_s \dots$
- Theory predictions
- Comparison of schemes



Quark Form Factor

Quark substructure can be detected by measuring the spatial distribution of the quark charge. If $Q^2 \ll 1/R_q^2$, the SM predictions for the cross sections are modified, approximately, to:

$$\frac{d\sigma}{dQ^2} = \frac{d\sigma_{SM}}{dQ^2} \left(1 - \frac{R_q^2}{6} Q^2\right)$$



Combined 1994-2000 data compared with 95% C.L. exclusion limits for the effective mean-square radius of the electroweak charge of the quark (arXiv:hep-ex/0401009)

Probability Method

“ R_q -only”:

- Choose different values of R_q^2 ^{True} and generate Monte Carlo replicas, then make fits with fixed SM PDFs.

“QCD+ R_q ”:

- Choose different values of R_q^2 ^{True} and generate Monte Carlo replicas, make fits of PDFs and R_q^2 parameter at one time for Monte Carlo replicas

Central Fitting Procedure

R_q -only

Make SM PDF fit with $R_q=0$

QCD+ R_q

Make PDF fit with included R_q^2 parameter

Perform R_q^2 fit with fixed SM PDFs

Set obtained $R_q^{2\ Data}$ as $R_q^{2\ Frac}$

Results of the Fits

- R_q -only:

$$R_q^2 \text{ } Data = (-0.385 \pm 2.68) \times 10^{-6} GeV^{-2}$$

- QCD+ R_q :

$$R_q^2 \text{ } Data = (-0.511 \pm 3.06) \times 10^{-6} GeV^{-2}$$

Preparing Monte Carlo Replicas

R_q -only

QCD+ R_q

Choose R_q^2 *True* and generate MC replicas
using PDFs fitted on data with $R_q=0$

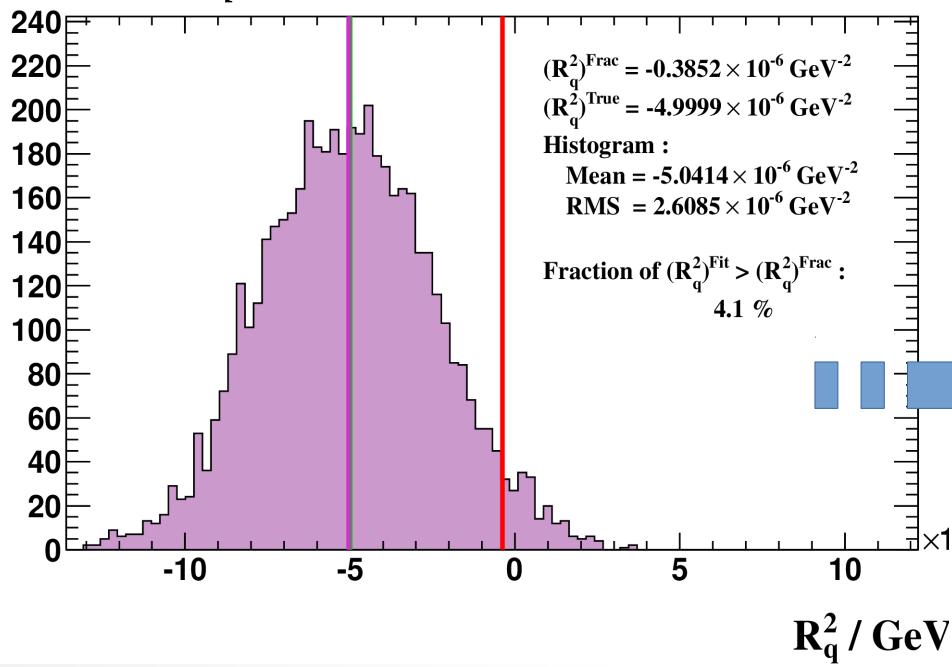
For each replica perform R_q^2 fit with
fixed PDFs

For each replica perform PDF+ R_q^2 fit

Calculate fraction of R_q^2 *Fit* > R_q^2 *Frac*

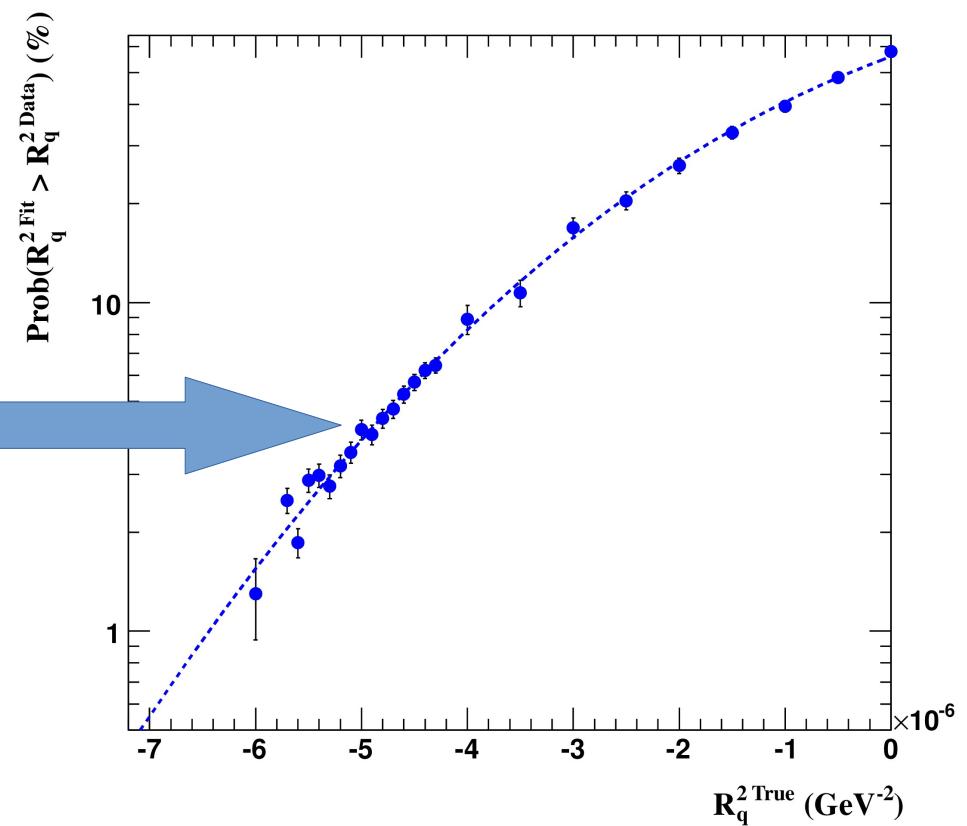
Estimating of the negative limit

R_q -only



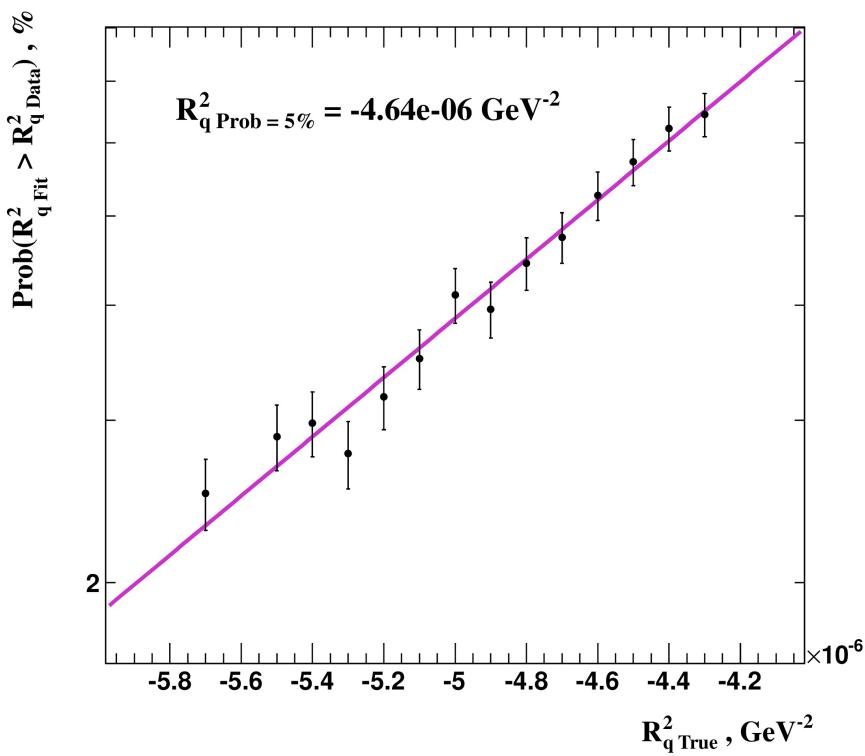
Monte Carlo replicas of cross sections are calculated as:

$$\mu^i = [M^i + \delta_{\text{tot. uncor.}}^i \cdot R_{\text{tot. uncor.}}^i \cdot D^i] \cdot (1 + \sum_j \gamma^j \cdot R_{\text{sys. sh.}}^j)$$



Final Limit

R_q -only



- Distribution is fitted with function:

$$f(x) = 5 \cdot \exp((x - A) \cdot B)$$

- Limit for central variation:

$$R_q^2 \text{ Limit} = (-4.653 \pm 0.027) \times 10^{-6} \text{ GeV}^{-2}$$

Model and Parametrization Variations

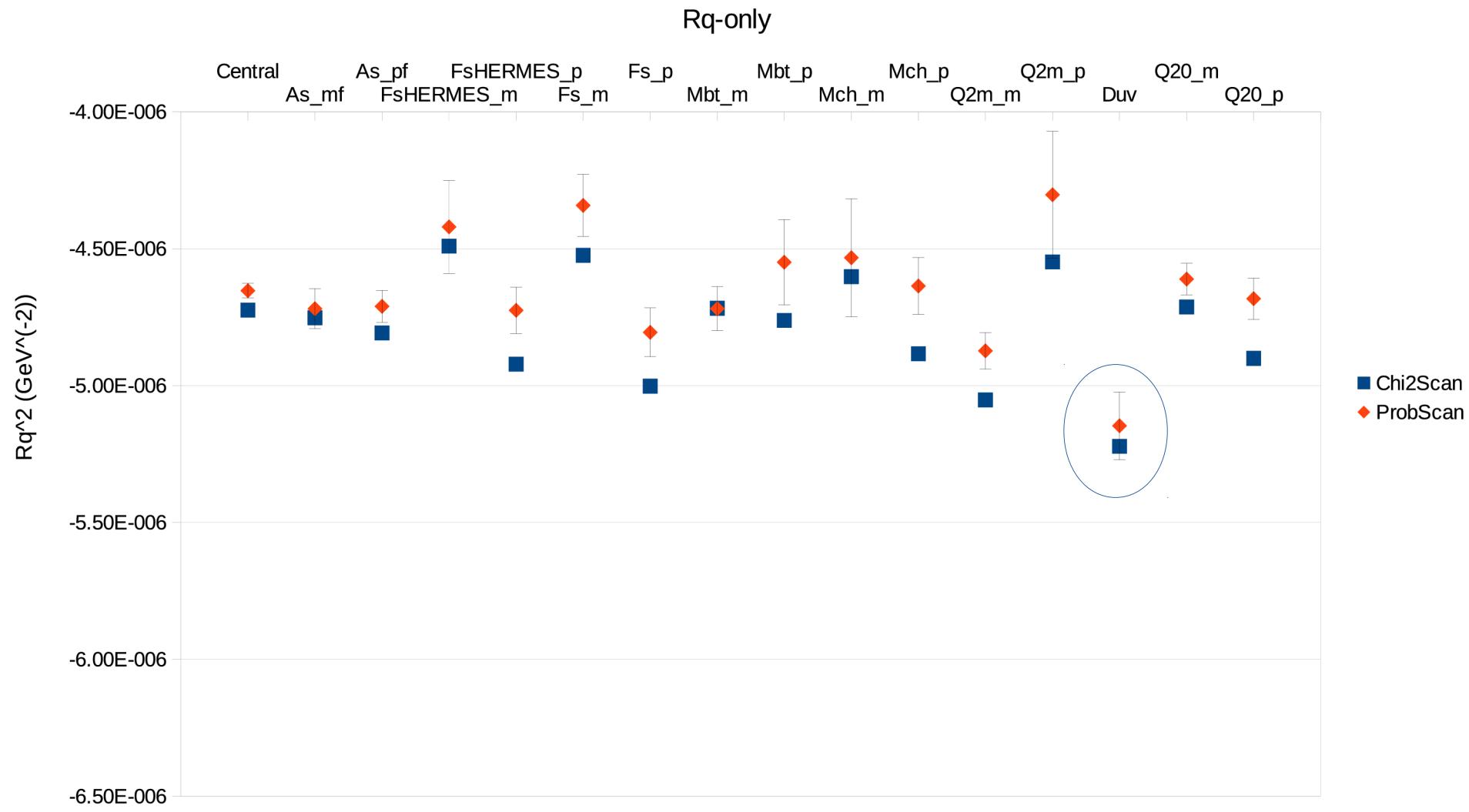
Model Variations

Variation	Standard Value	Lower Limit	Upper Limit
$Q_{min}^2 [GeV^2]$	3.5	2.5	5.0
$M_c [GeV]$	1.47	1.41	1.53
$M_b [GeV]$	4.50	4.25	4.75
f_s	0.4	0.3	0.5
$f_{s \text{ HERMES}}$	-	0.3	0.5
α_s	0.1180	0.1220	0.1146

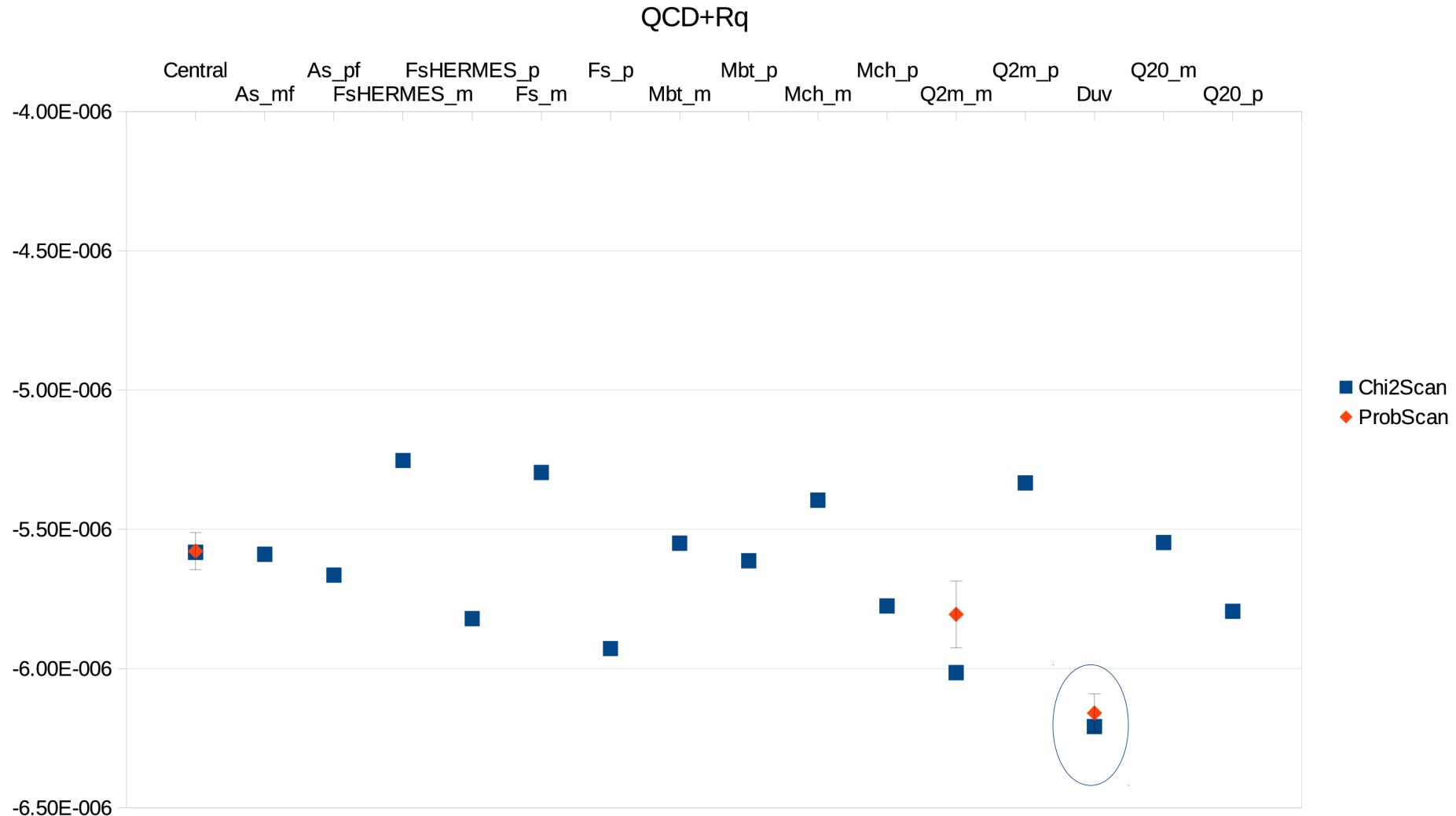
Parametrization Variations

Variation	Standard Value	Lower Limit	Upper Limit
$Q_0^2 [GeV^2]$	1.9	1.6	2.2 ($M_c = 1.53 GeV$)
D_{u_v}	-	-	+

Results of the Model and Parametrization Variations



Results of the Model and Parametrization Variations



Results of the Probability Scan

- For central variant:

$$R_q\text{-only} \quad R_q^{2 \text{ Limit}} = -((0.426 \pm 0.033) \cdot 10^{-16} \text{ cm})^2$$

$$\text{QCD} + R_q \quad R_q^{2 \text{ Limit}} = -((0.466 \pm 0.051) \cdot 10^{-16} \text{ cm})^2$$

- For variant with additional D_{u_v} parameter:

$$R_q\text{-only} \quad R_q^{2 \text{ Limit}} = -((0.447 \pm 0.069) \cdot 10^{-16} \text{ cm})^2$$

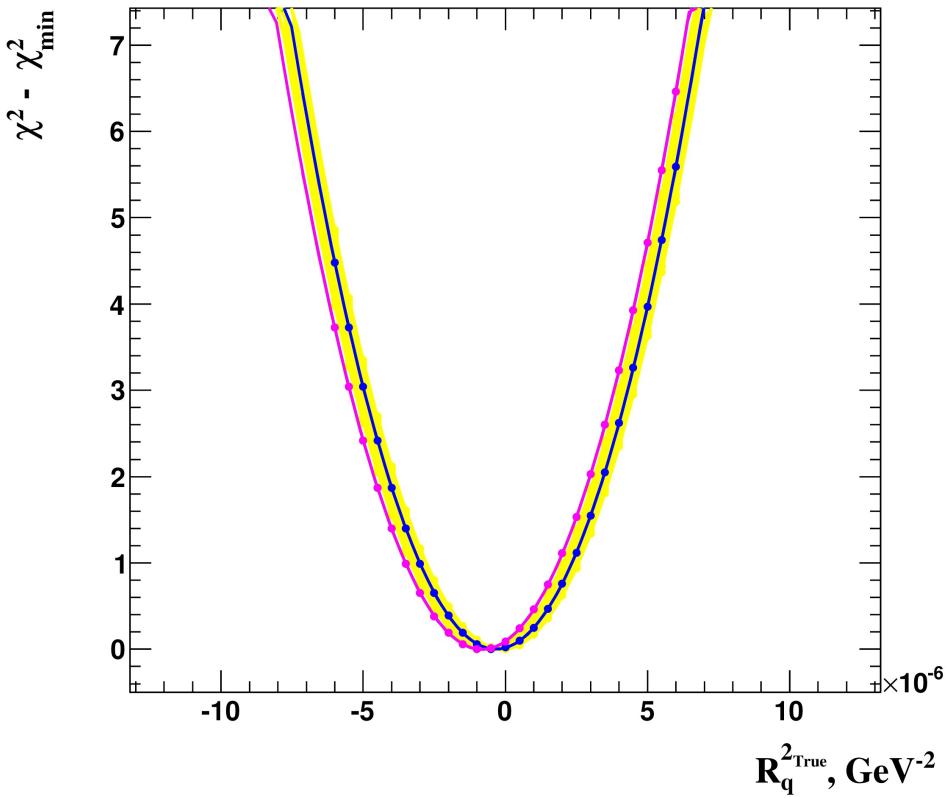
$$\text{QCD} + R_q \quad R_q^{2 \text{ Limit}} = -((0.489 \pm 0.051) \cdot 10^{-16} \text{ cm})^2$$

χ^2 Scan

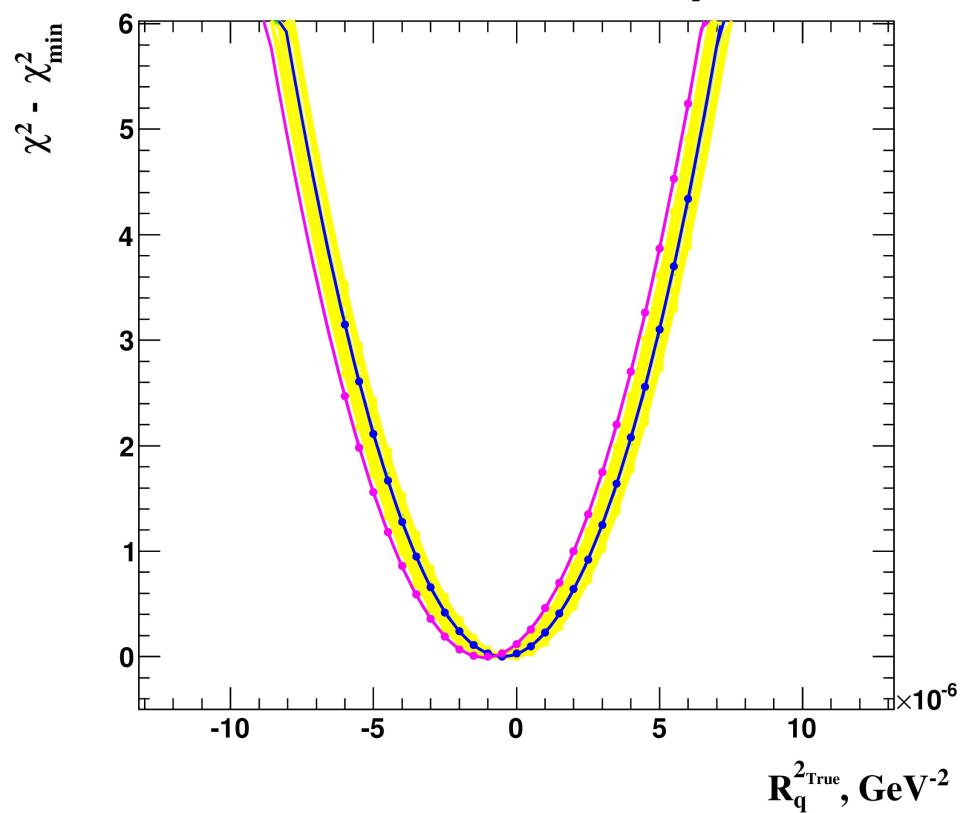
- R_q -only
 - R_q^2 fixed to $R_q^{2 \ True}$ and PDFs fixed to SM PDFs.
 - χ^2 estimated for one iteration fit on Data.
- QCD+ R_q
 - R_q^2 fixed to $R_q^{2 \ True}$ and PDFs are fitted, final χ^2 estimated.

χ^2 Scan Results

R_q -only



QCD+ R_q



Blue – central fit. Yellow – model variations. Green – parametrization variations. Magenta – D_{u_v} variation.

Probability Scan vs χ^2 Scan

- Probability Scan:

R_q -only

$$R_q^{2 \text{ Limit}} = -((0.447 \pm 0.069) \cdot 10^{-16} \text{ cm})^2$$

QCD+ R_q

$$R_q^{2 \text{ Limit}} = -((0.489 \pm 0.051) \cdot 10^{-16} \text{ cm})^2$$

- χ^2 Scan:

R_q -only

$$R_q^{2 \text{ Limit}} = -(0.451 \cdot 10^{-16} \text{ cm})^2$$

QCD+ R_q

$$R_q^{2 \text{ Limit}} = -(0.491 \cdot 10^{-16} \text{ cm})^2$$

Conclusions

- Evaluated 95% C.L. lower limit:

$$R_q^2 > - (0.489 \cdot 10^{-16} \text{ cm})^2$$

- Probability method is fully consistent with χ^2 method