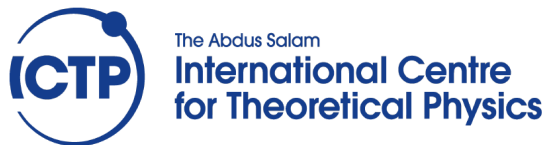


SUSY and the Higgs

or “A SM Higgs Guide to Find SUSY”

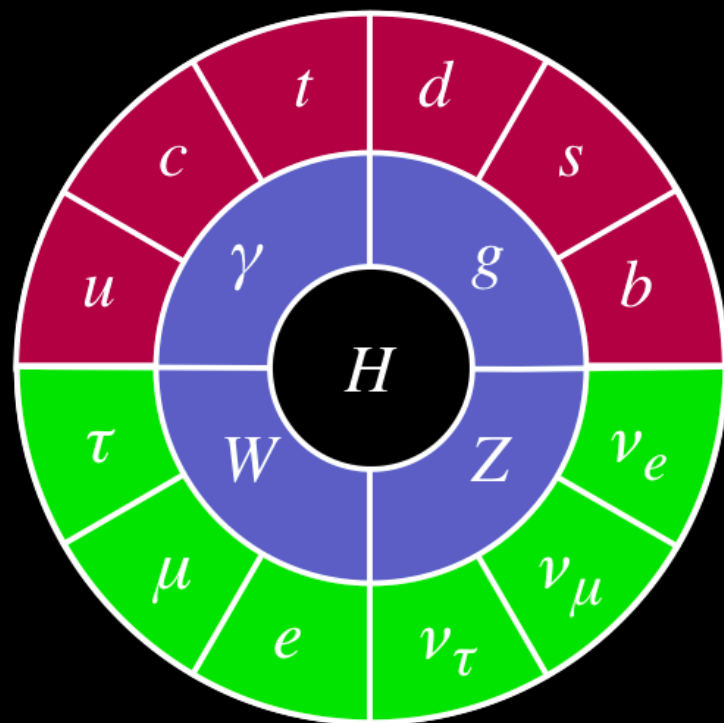
Giovanni Villadoro

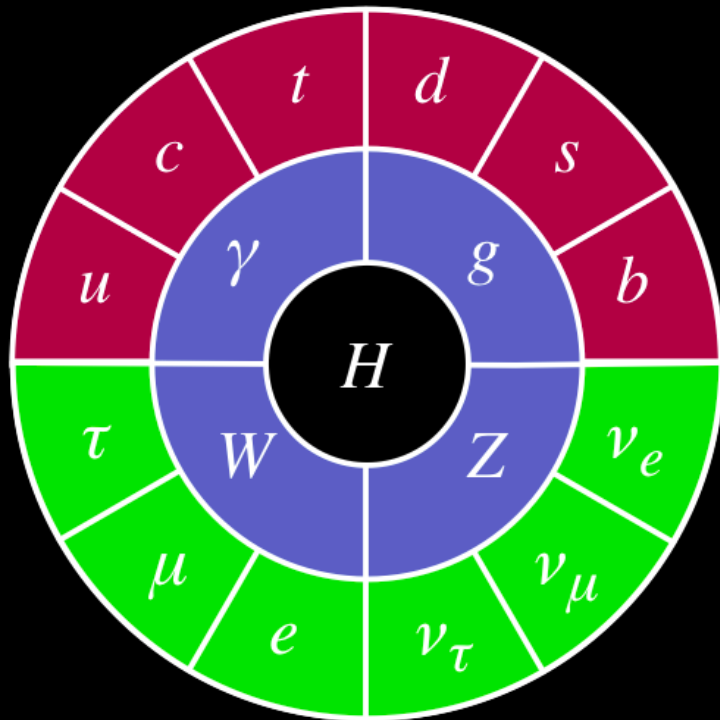


in collaboration with:

Javier Pardo Vega

JHEP 1507 (2015) 159 – [1504.05200] **SusyHD**

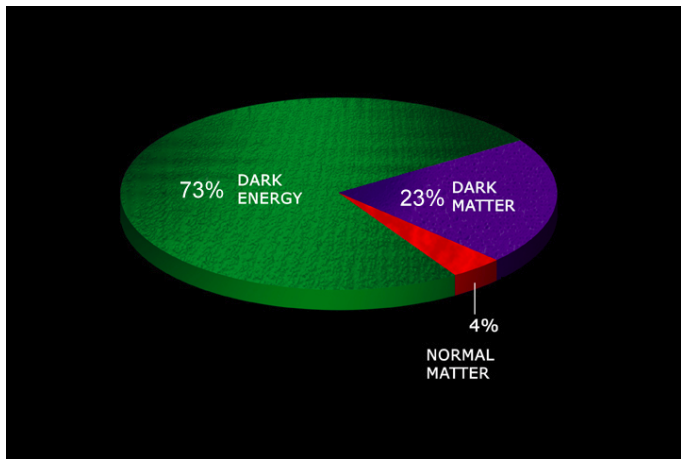




$$\mathcal{L}_{\text{SM}} = -\frac{1}{4}F^2 + i\bar{\psi}\not{D}\psi + H\bar{\psi}Y\psi + h.c. + |D_\mu H|^2 + m^2|H|^2 - \lambda|H|^4 - \Lambda$$

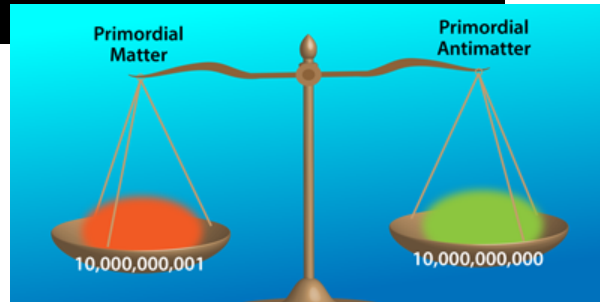
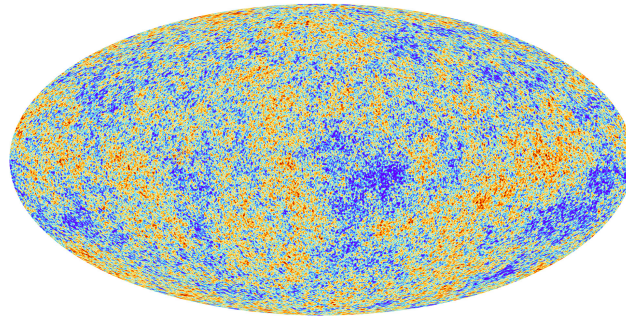
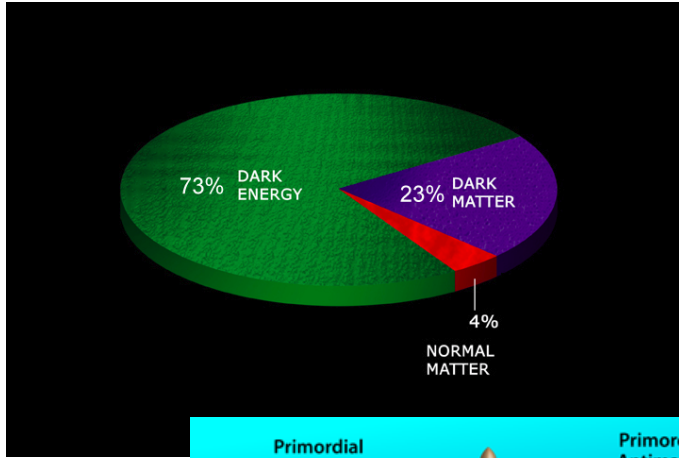
the Standard ~~Model~~ EFT

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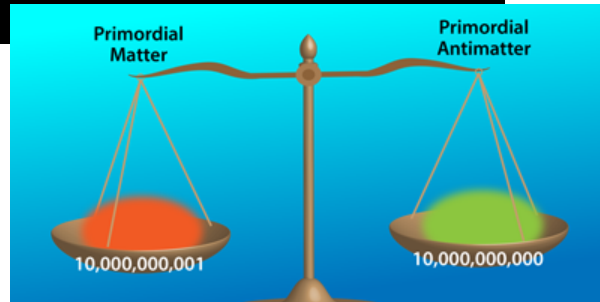
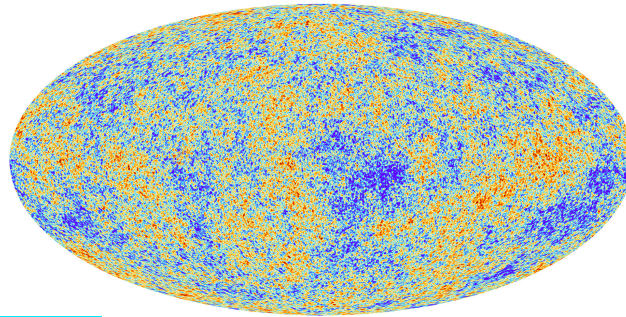
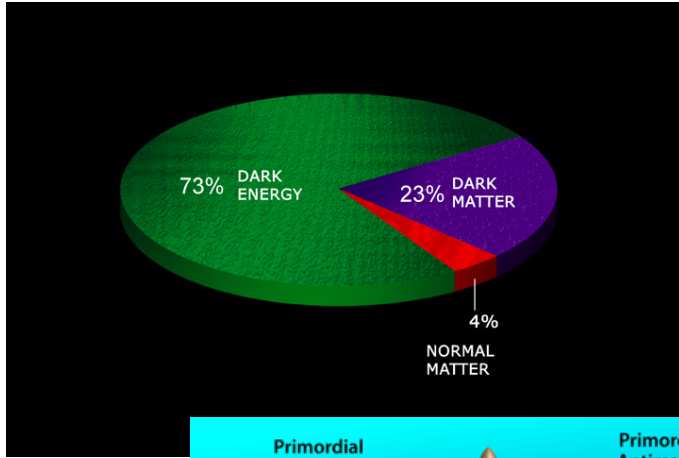
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naturally:

small FCNC:

$$\frac{\psi g \not{F} \psi}{M_{\text{NP}}} + \dots$$

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$$\frac{(LH)^2}{M_{\text{NP}}}$$

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large
 M_{NP}

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$$\boxed{\arg \det Y \lesssim 10^{-10}}$$

axion?

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tiny vacuum energy:

$$\Lambda = M_{\text{NP}}^4$$

light EW scale:

$$m^2 = M_{\text{NP}}^2$$

$$10^{-47} \text{ GeV}^4$$



$$10^{-3} \text{ GeV}^4$$



$$10^8 \text{ GeV}^4$$



The CC problem:

$$\Lambda = -m_K^2 f_K^2 - \frac{1}{2}m_h^2 v^2 + \cdots + M_{\text{NP}}^4$$

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Λ prefers m_{SUSY} as low as possible!

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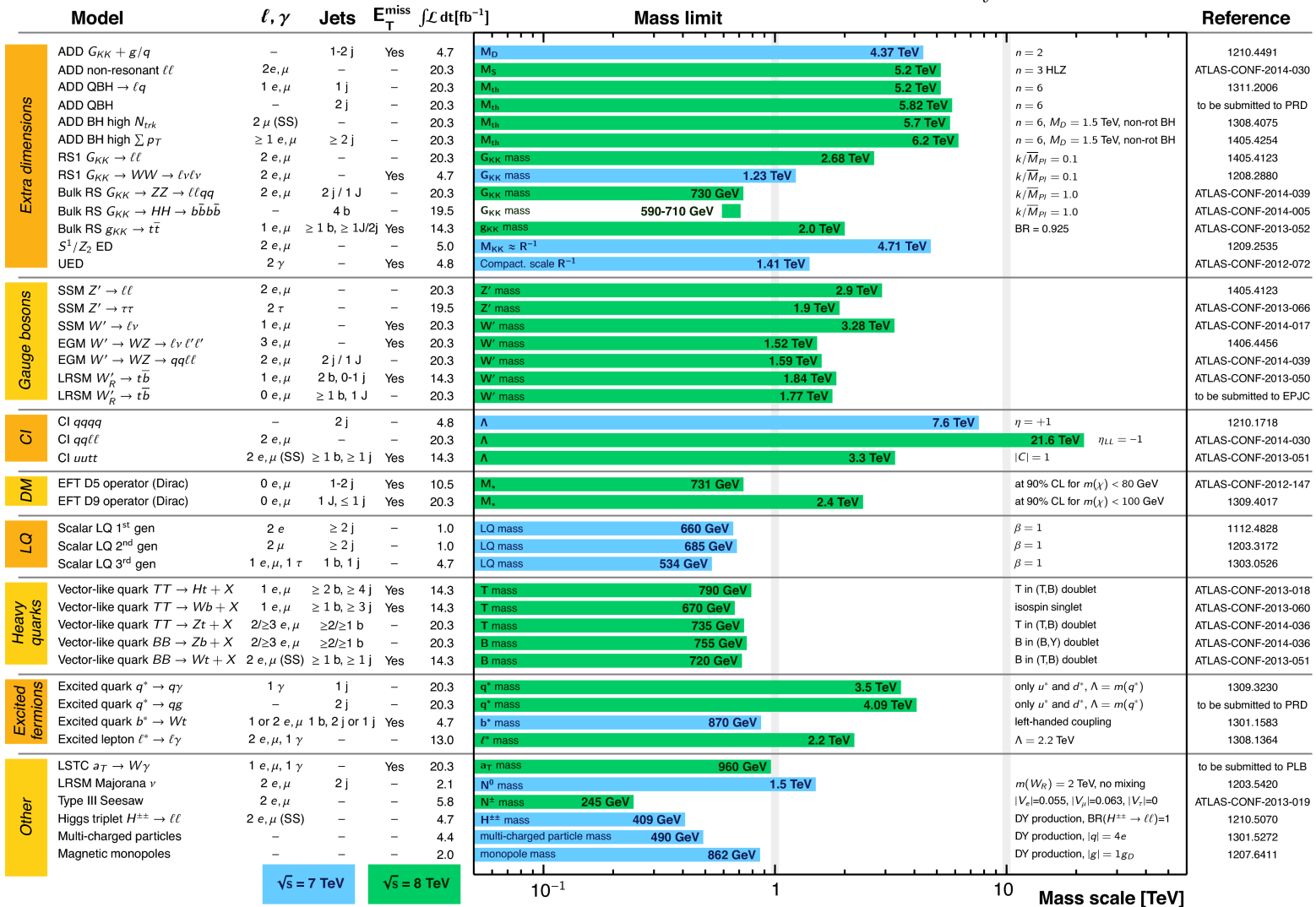
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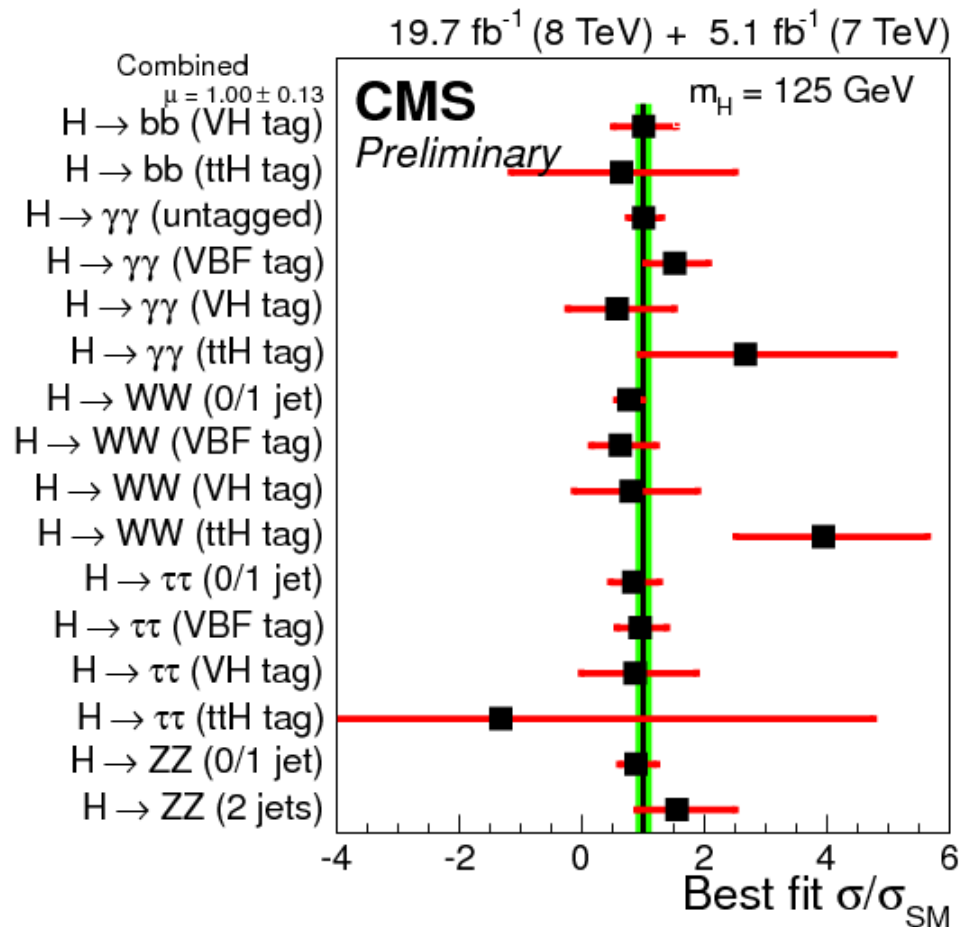
The EW hierarchy problem: $m^2 = M_{\text{NP}}^2$

possible solutions: SUSY, composite models, extra-dimensions...

$$\int \mathcal{L} dt = (1.0 - 20.3) \text{ fb}^{-1} \quad \sqrt{s} = 7, 8 \text{ TeV}$$



the “SM” Higgs:



Compatible/Expected from indirect searches:

Flavor: $\gtrsim 10^5 \text{ TeV}$

EDMs: $\gtrsim 100 \text{ TeV}$

LEP2: $\gtrsim 20 \text{ TeV}$

EWPT: $\gtrsim \text{few TeV}$

(assuming $O(1)$ couplings)

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What about SUSY?

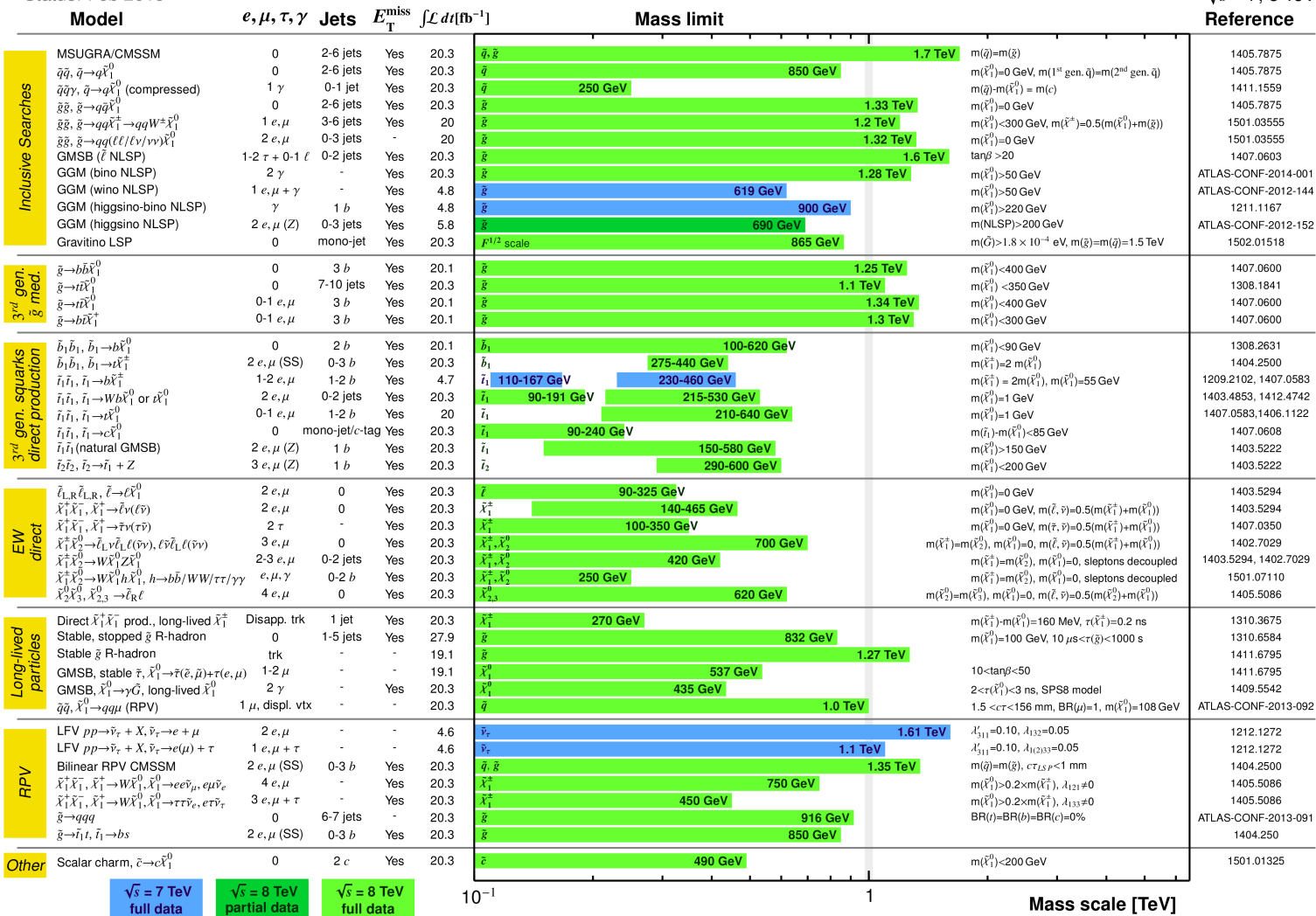
WANTED

~~DEAD~~ OR ALIVE

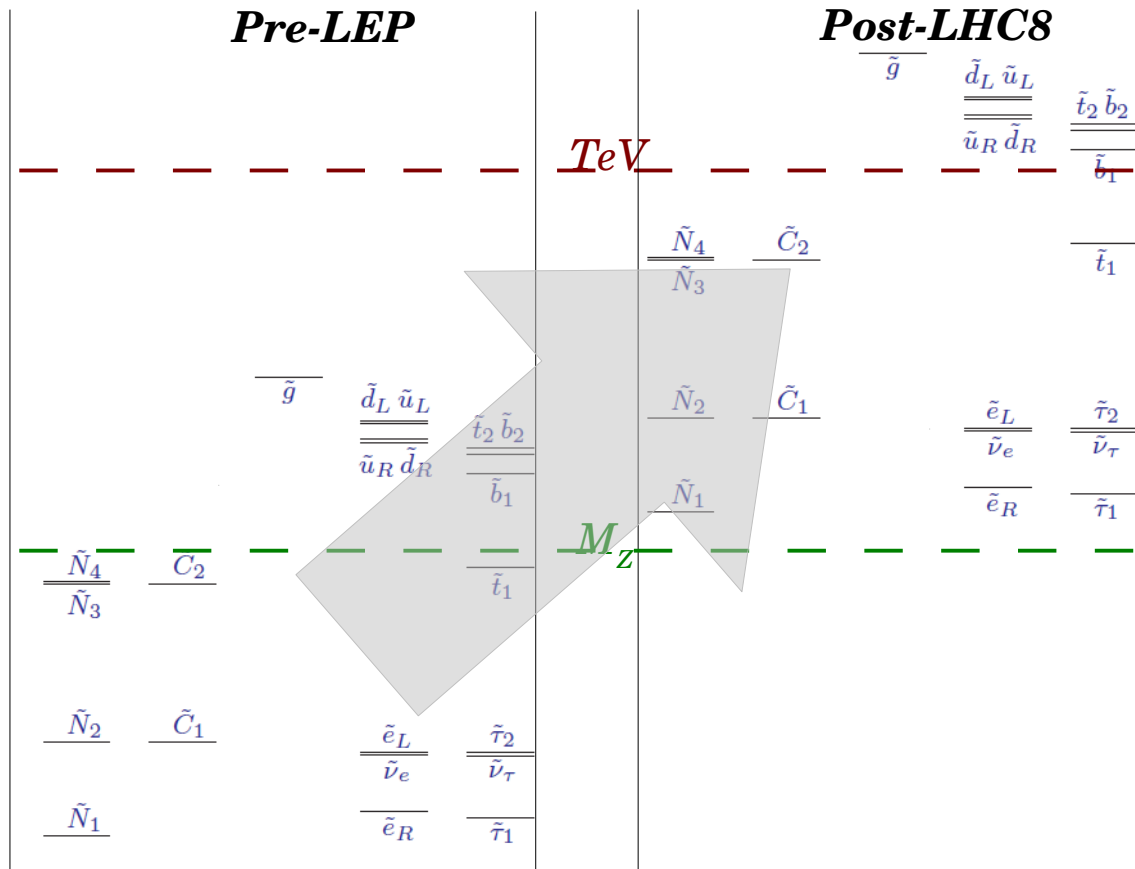


SUSY

REWARD \$ 1,000,000

*Only a selection of the available mass limits on new states or phenomena is shown. All limits quoted are observed minus 1 σ theoretical signal cross section uncertainty.

SUSY is tuned!



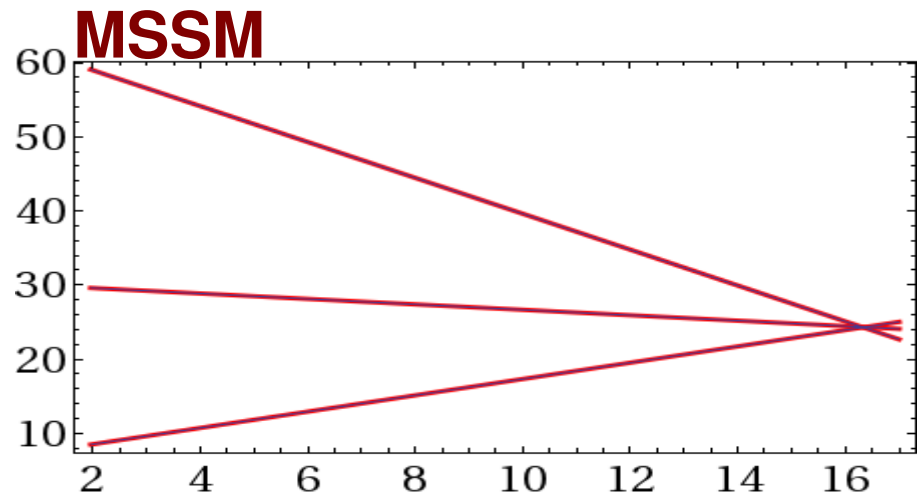
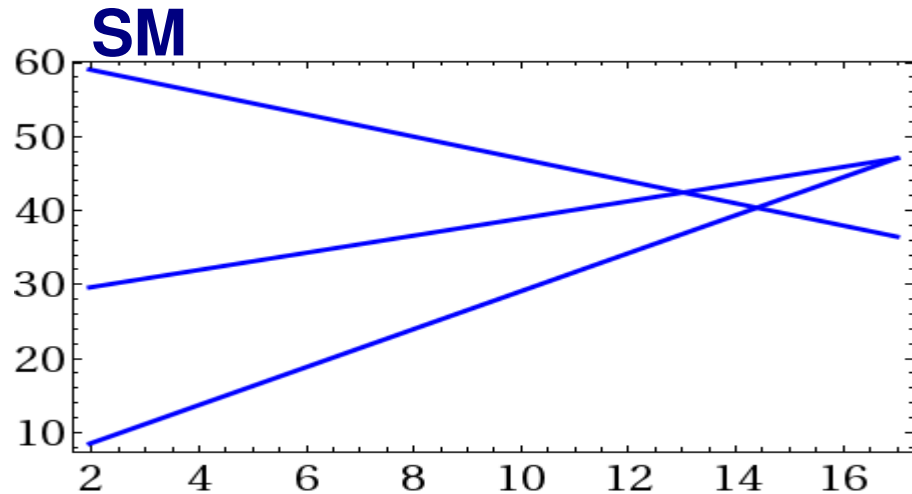
Keep trying with
“clever” model
building



Accept that naturalness
is not a good criterion
for BSM

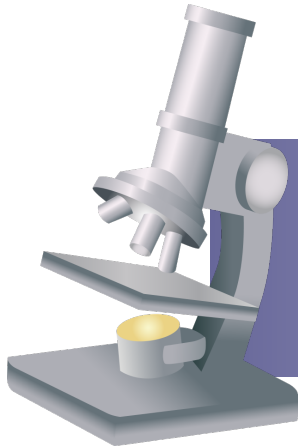
Weaker hint:

Gauge Coupling Unification



$$m_{\text{SUSY}} \lesssim \text{few} \cdot 10 \text{ TeV}$$

SUSY breaking scale?



Back to Experiments
Use Precision Data

In SUSY the Higgs mass is calculable:

ATLAS + CMS $m_h^{\text{exp}} = 125.09 \pm 0.24 \text{ GeV}$

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$$m_h^2 \simeq m_Z^2 \cos^2 2\beta + \frac{3}{\pi^2} \frac{m_t^4 \sin^4 \beta}{v^2} \left[\log \frac{m_{\tilde{t}}^2}{m_t^2} + \tilde{X}_t^2 \left(1 - \frac{\tilde{X}_t^2}{12} \right) \right] + \dots$$

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only *log*-dependence on new physics scale

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only *log*-dependence on new physics scale

⇒ high precision to get reliable constraints

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$$125^2 \approx \underbrace{90^2} + \underbrace{90^2}$$

$$\Rightarrow \delta m_h \sim \delta m_t$$

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$$125^2 \approx \underbrace{90^2}_{\text{tree}} + \underbrace{90^2}_{\text{1-loop}} + \dots$$

$$\Rightarrow \delta m_h \sim \delta m_t$$

$$m_t^{\overline{\text{MS}}}(M_t) = 173.34 - 8.00 - 1.90 - 0.59 - 0.21 \text{ GeV}$$

1 loop 2 loop 3 loop 4 loop

Exploiting the Hierarchy Problem:

the EFT technique

SUSY

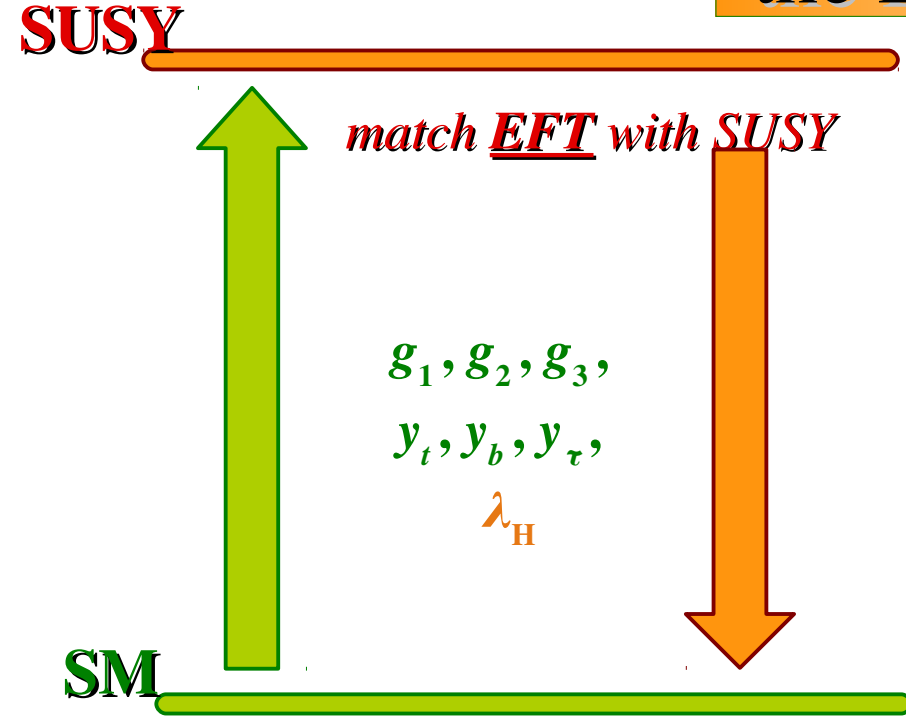
A thick, horizontal orange bar with rounded ends, positioned below the 'SUSY' text.

SM

A thick, horizontal green bar with rounded ends, positioned below the 'SM' text.

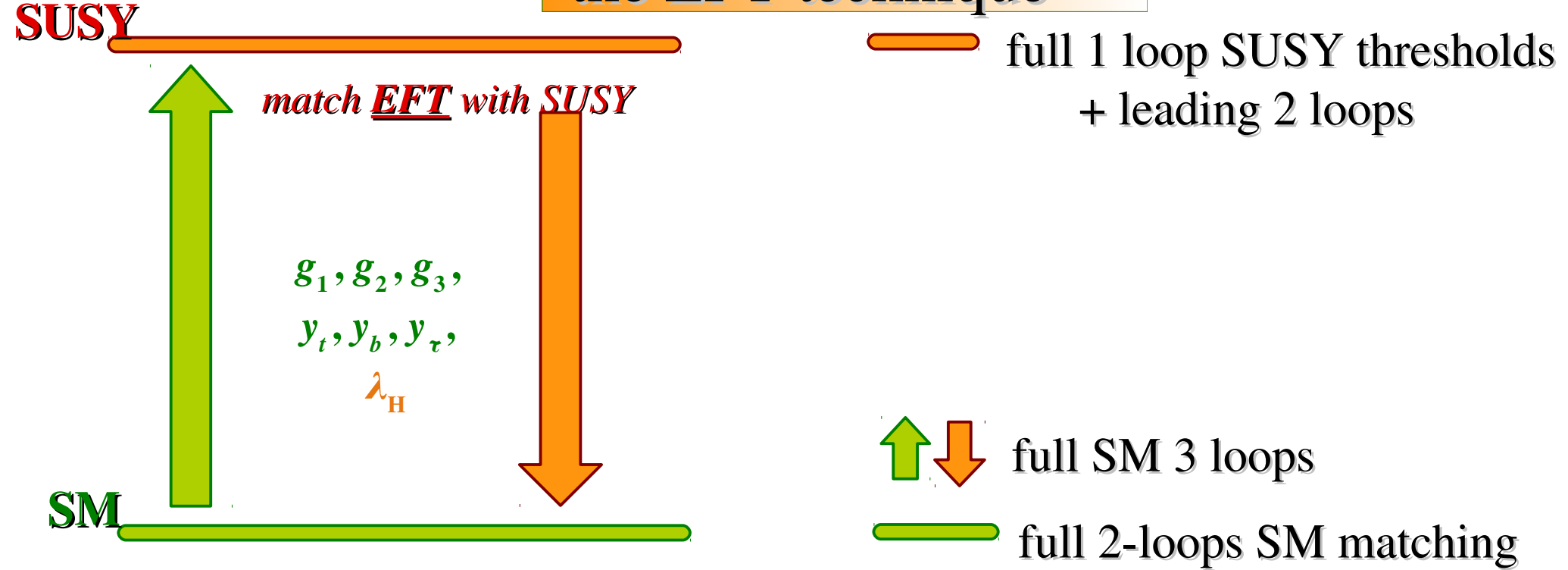
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Exploiting the Hierarchy Problem:

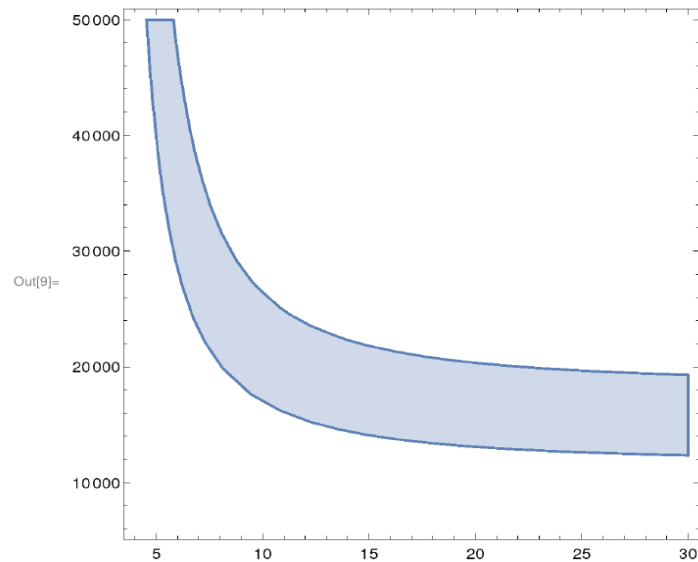
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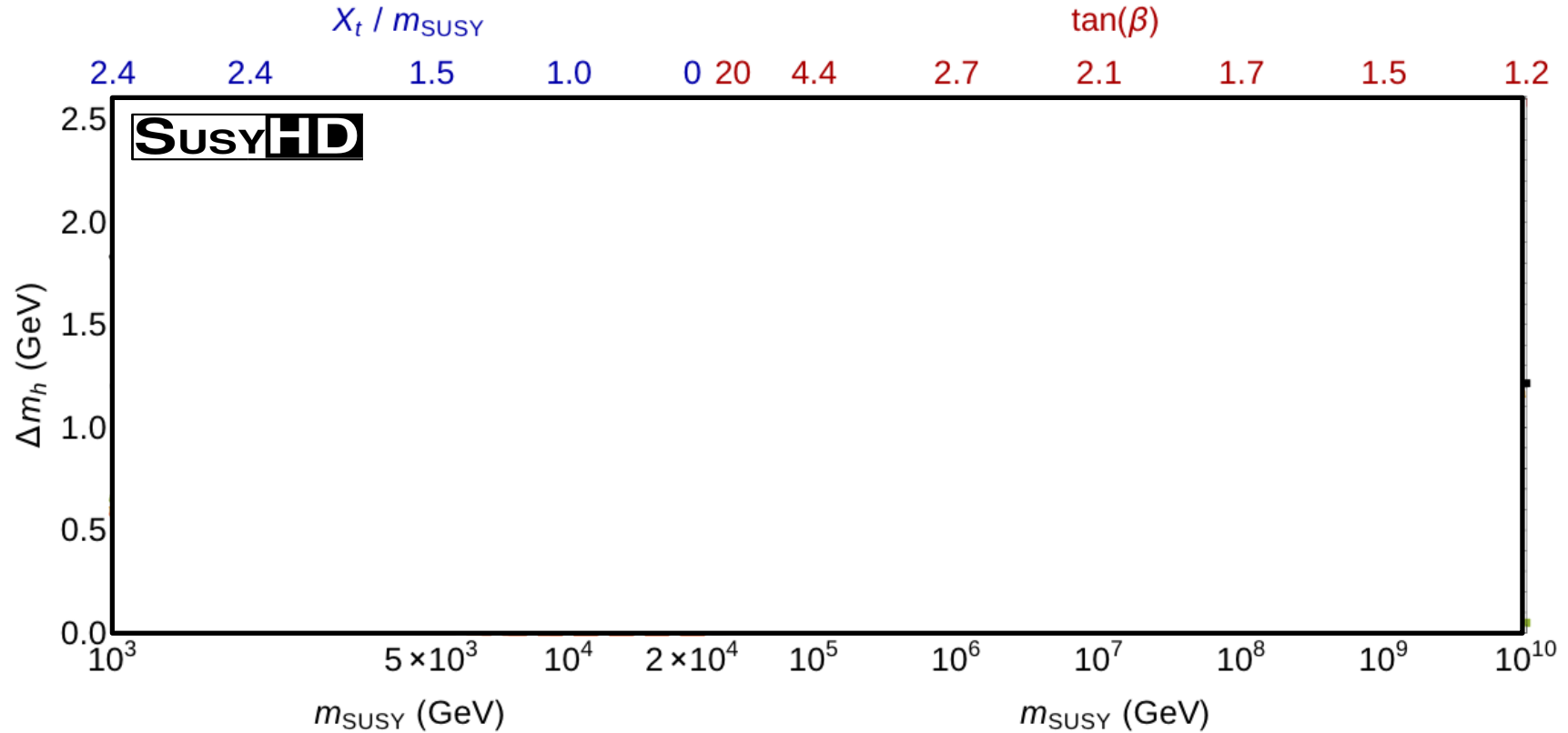


www.ictp.it/~susyhd

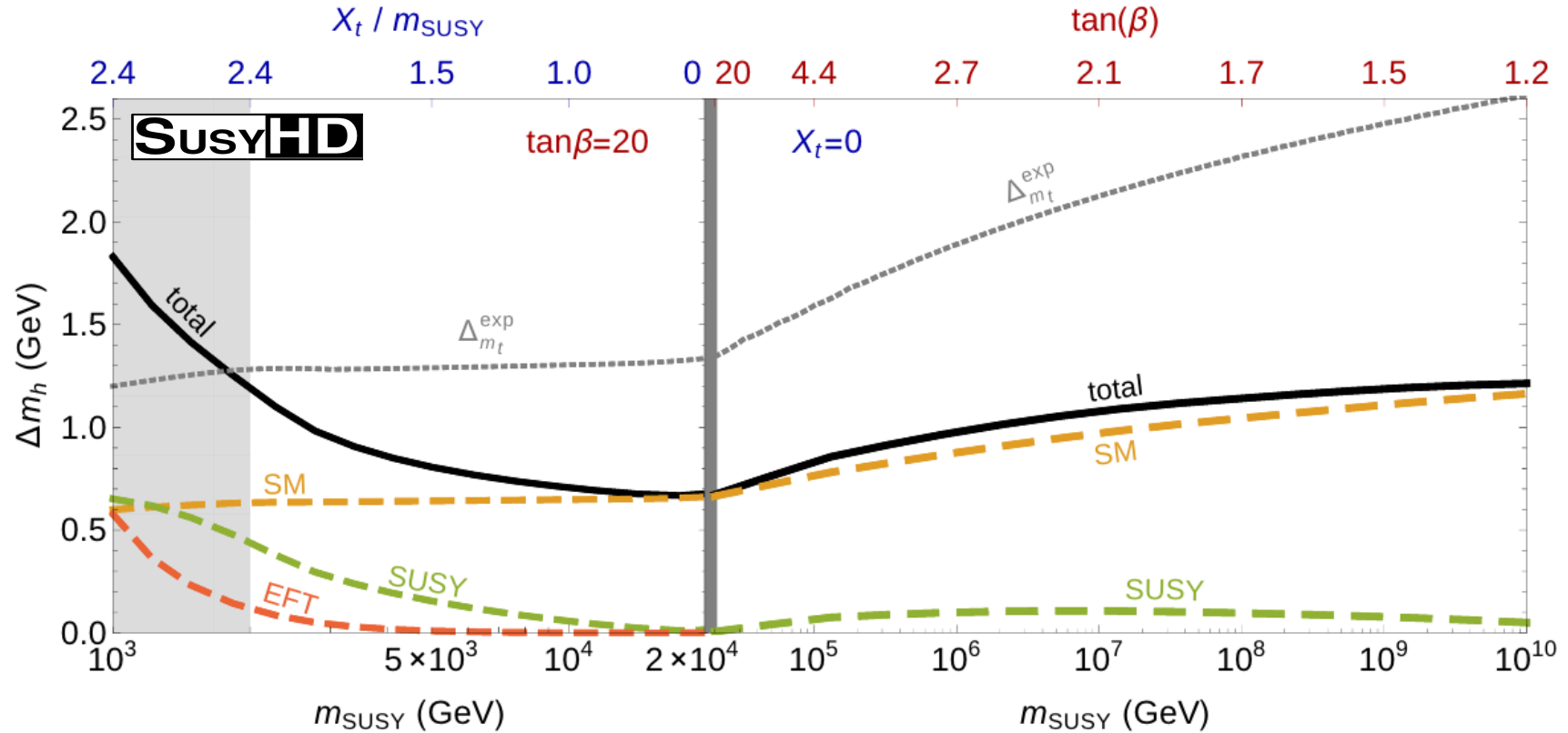
```
In[1]:= << SUSYHD`  
  
In[2]:= mh := MHiggs[{tb, m0, At}]  
        Δmh := ΔMHiggs[{tb, m0, At}]  
  
In[4]:= tb := 20;  
        m0 := 2000;  
        At := 5000;  
        mh // Timing  
        Δmh // Timing  
Out[7]= {0.006999, 125.033}  
Out[8]= {0.039994, 1.30843}  
  
In[9]:= RegionPlot[125 - Δmh < mh < 125 + Δmh, {tb, 4, 30}, {m0, 6000, 50000}]
```



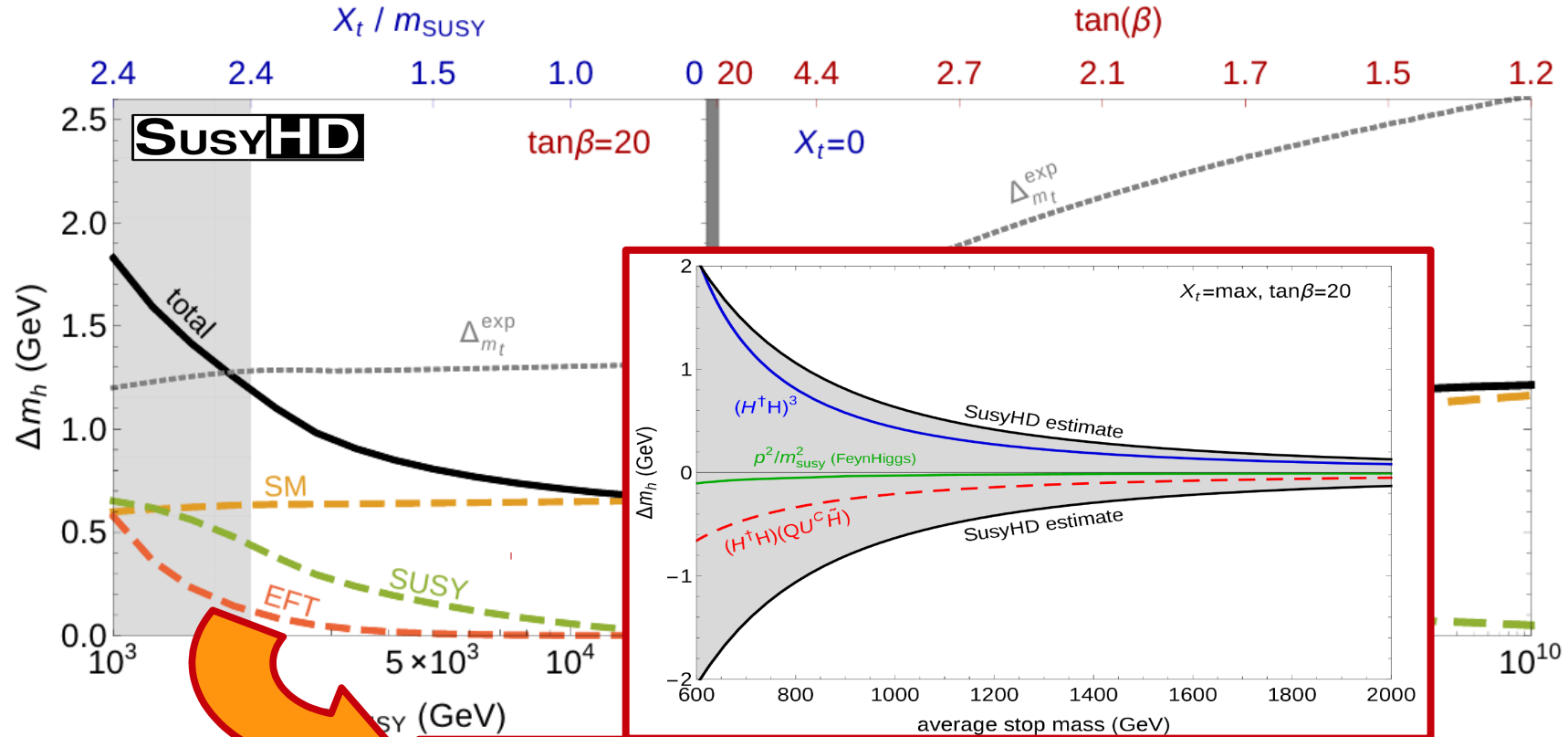
Estimate of the Uncertainties:



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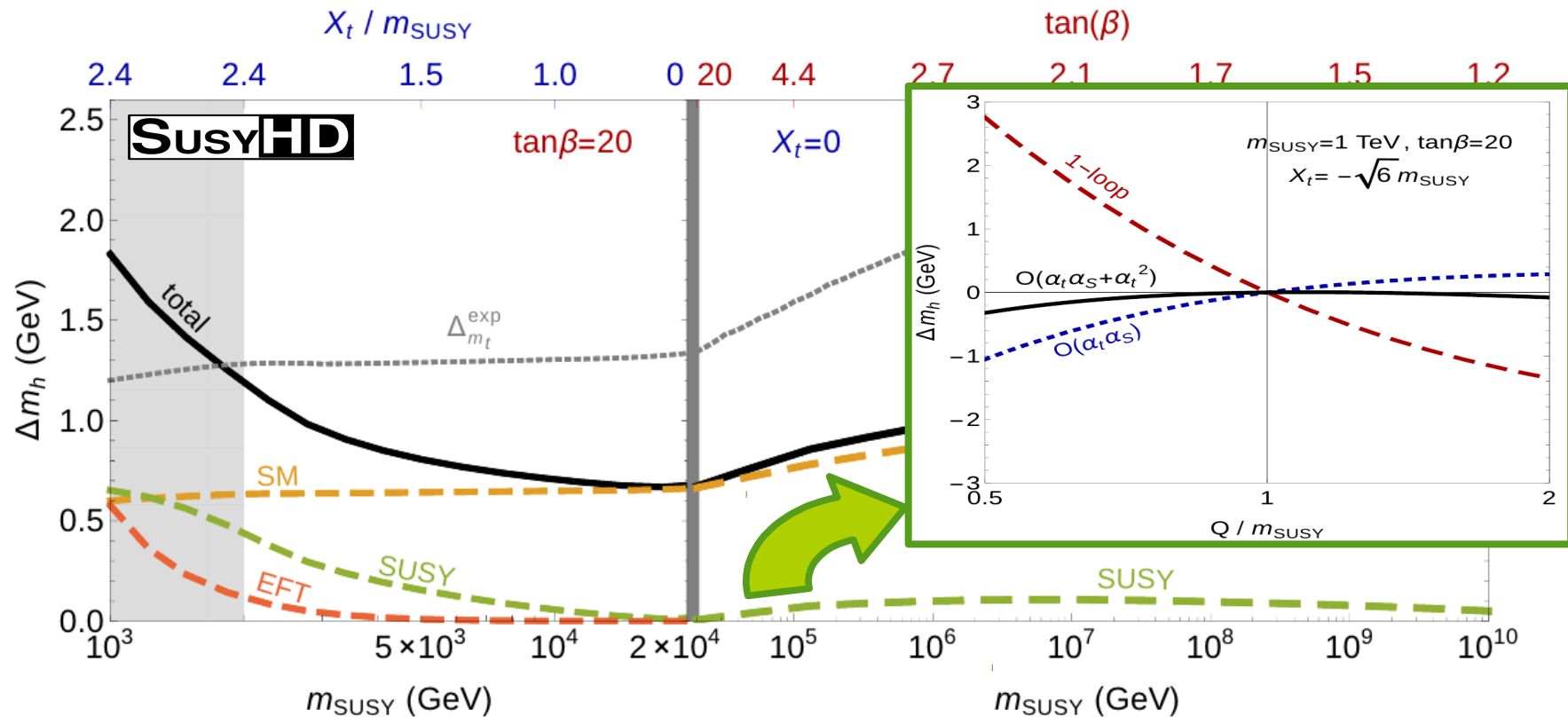


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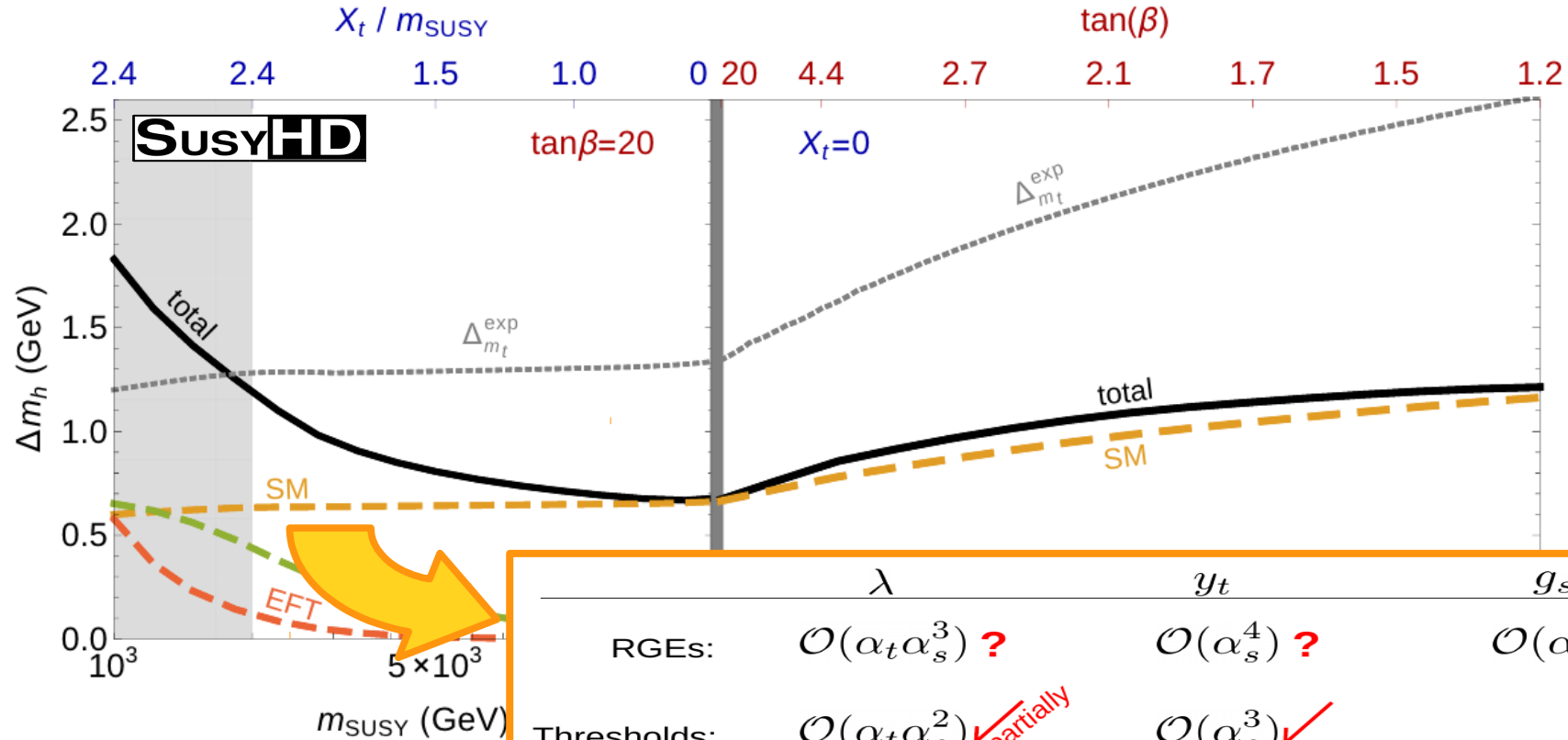


$$c_6 \frac{(H^\dagger H)^3}{m_{\text{SUSY}}^2} + c_t \frac{H^\dagger H}{m_{\text{SUSY}}^2} H Q U^c + \dots$$

Estimate of the Uncertainties:



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Estimate of the Uncertainties:

PRL **114**, 142002 (2015)

PHYSICAL REVIEW LETTERS

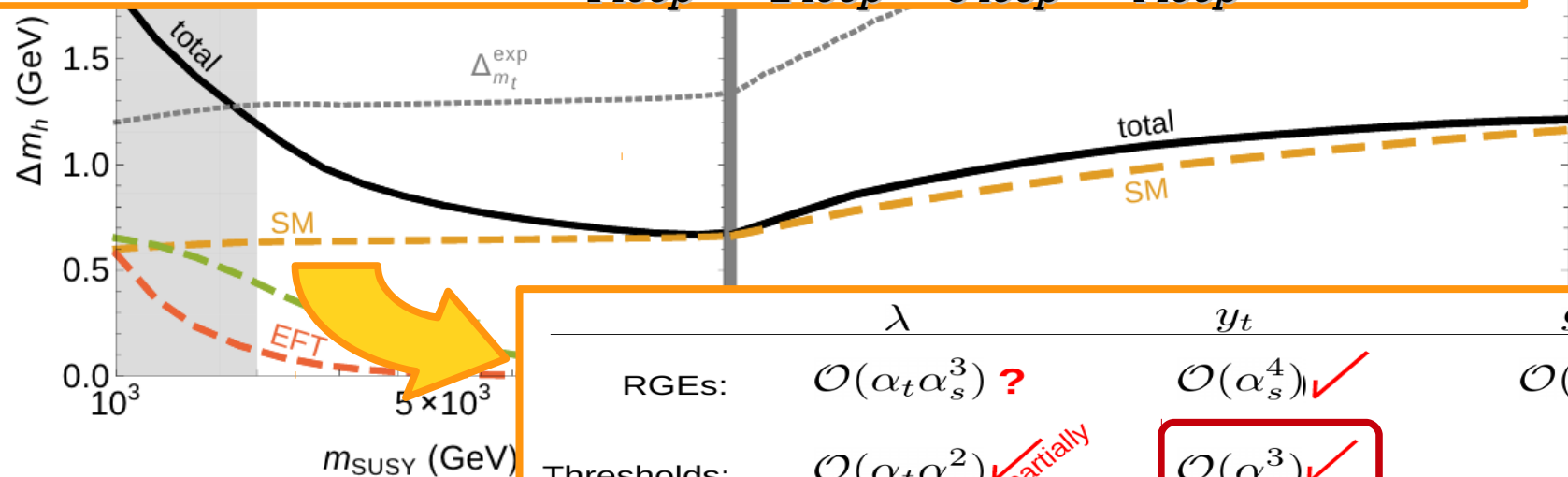
week ending
10 APRIL 2015

Quark Mass Relations to Four-Loop Order in Perturbative QCD

Peter Marquard,¹ Alexander V. Smirnov,² Vladimir A. Smirnov,³ and Matthias Steinhauser⁴

$$m_t^{\overline{\text{MS}}}(M_t) = 173.34 - 8.00 - 1.90 - \boxed{0.59} - 0.21 \text{ GeV}$$

1 loop 2 loop 3 loop 4 loop



	λ	y_t	g_s
RGEs:	$\mathcal{O}(\alpha_t \alpha_s^3) ?$	$\mathcal{O}(\alpha_s^4) \checkmark$	$\mathcal{O}(\alpha_s^4) \checkmark$
Thresholds:	$\mathcal{O}(\alpha_t \alpha_s^2) \checkmark_{\text{partially}}$	$\boxed{\mathcal{O}(\alpha_s^3) \checkmark}$	

Estimate of the Uncertainties

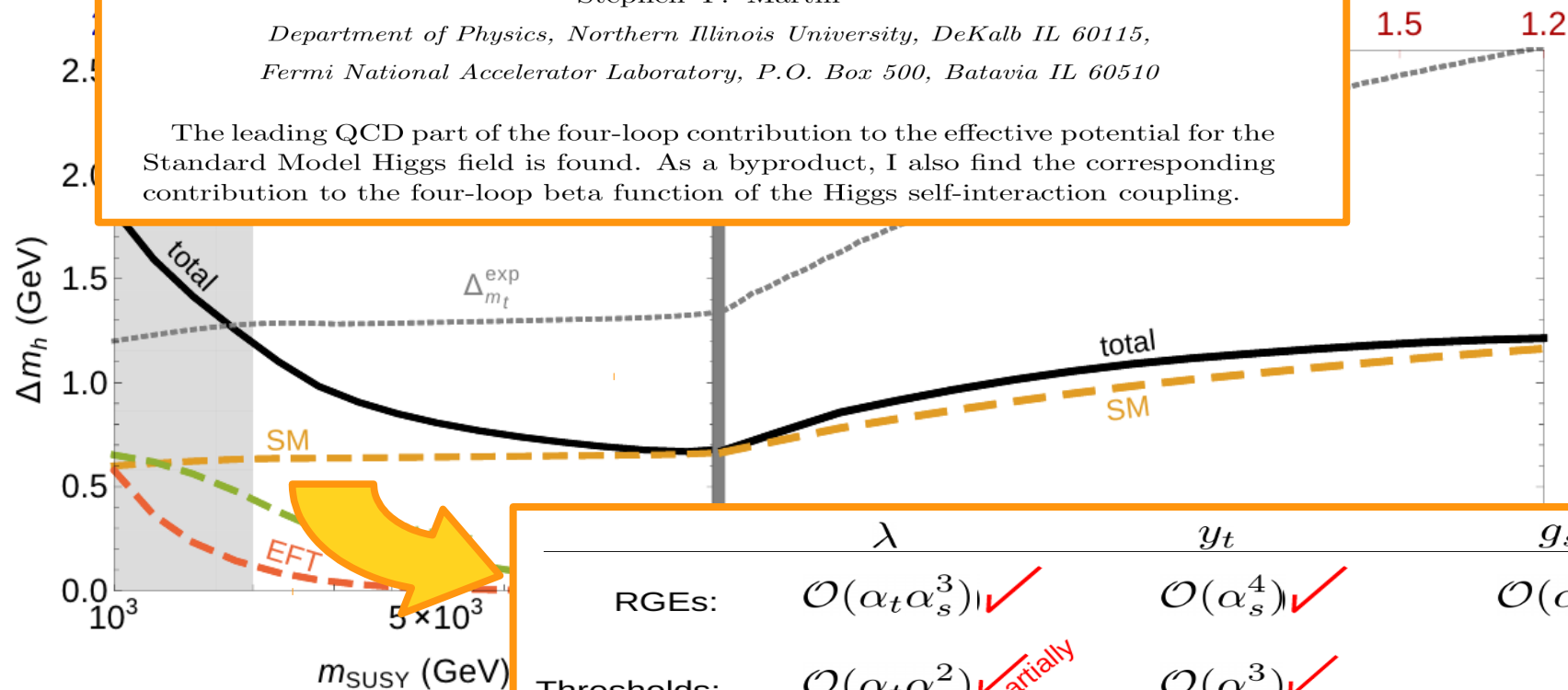
Four-loop Standard Model effective potential at leading order in QCD

Stephen P. Martin

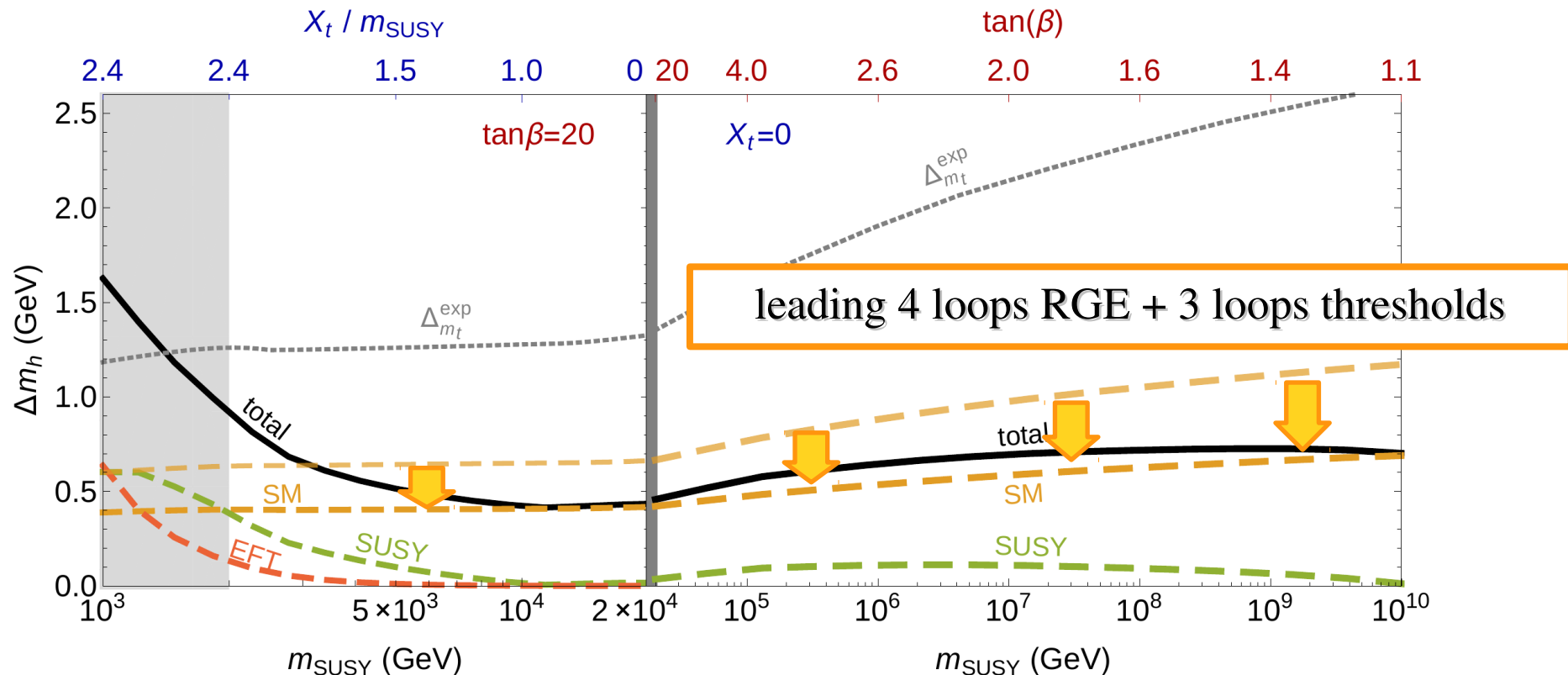
Department of Physics, Northern Illinois University, DeKalb IL 60115,

Fermi National Accelerator Laboratory, P.O. Box 500, Batavia IL 60510

The leading QCD part of the four-loop contribution to the effective potential for the Standard Model Higgs field is found. As a byproduct, I also find the corresponding contribution to the four-loop beta function of the Higgs self-interaction coupling.

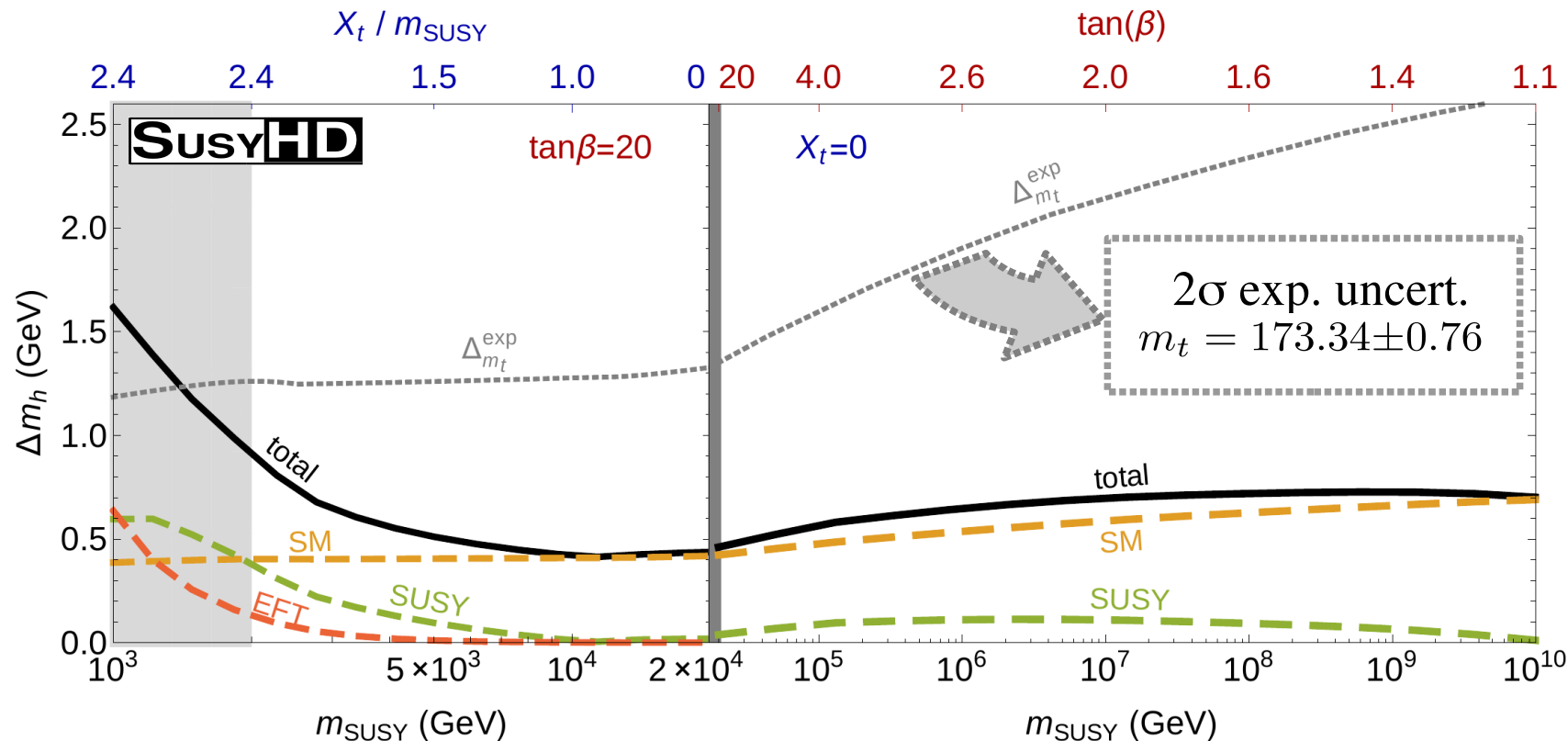


Estimate of the Uncertainties:



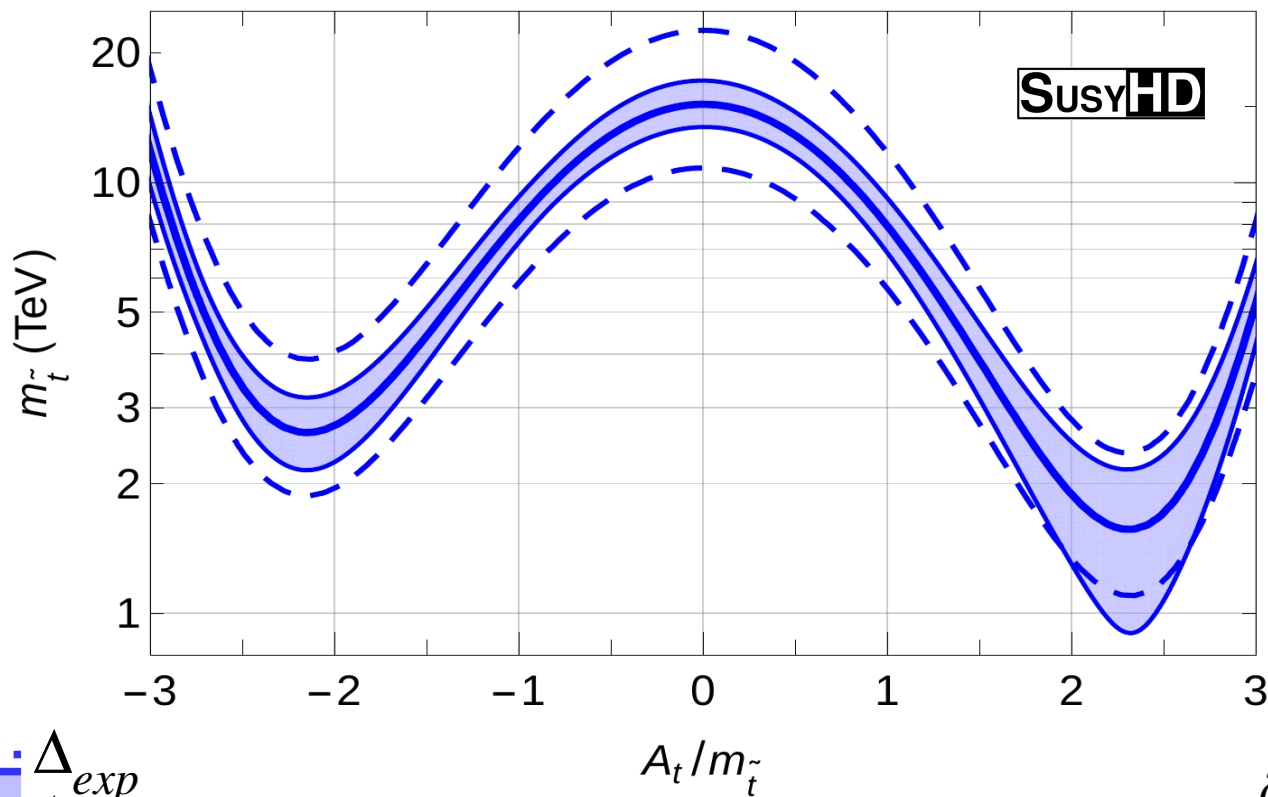
soon in SusyHD v1.1

Estimate of the Uncertainties:



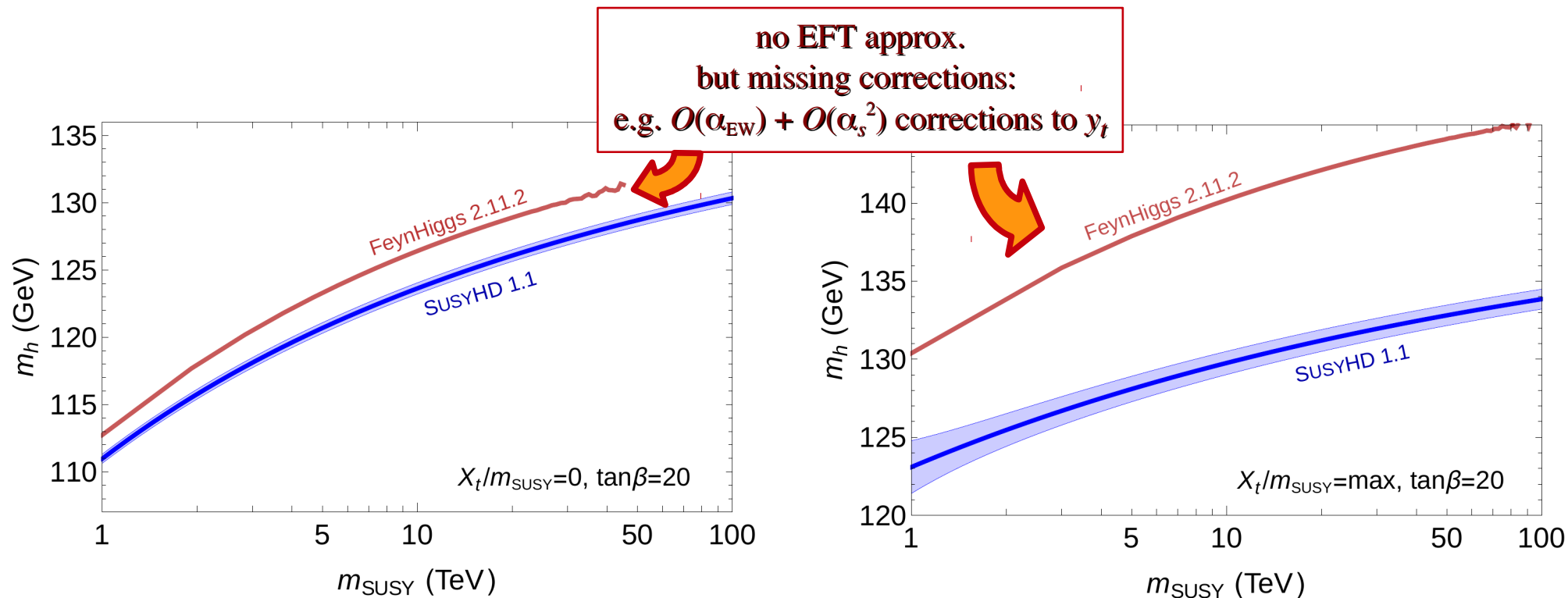
Where is SUSY ?

@ $\tan\beta = 20$, w/ degenerate spectrum $m_{\text{SUSY}} = m_{\text{stop}}$



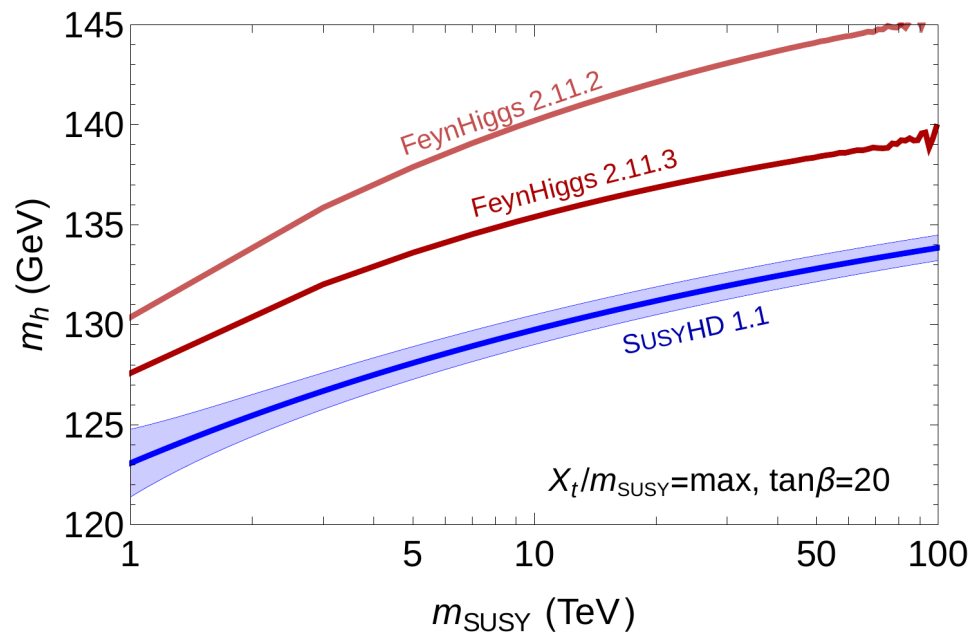
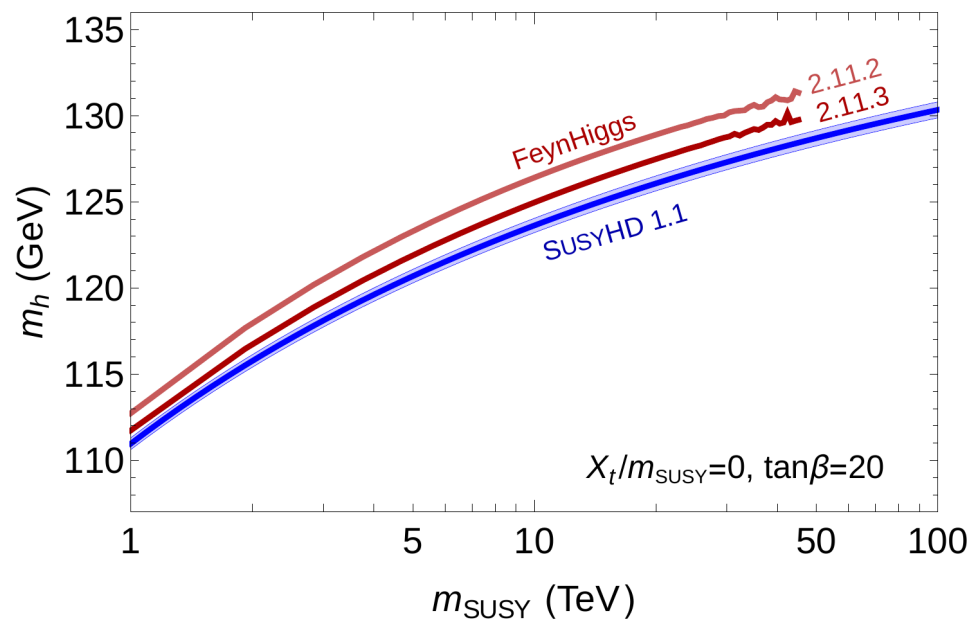
$$\partial A_t / \partial \mu > 0$$

Comparison with fixed order comp.: FeynHiggs



Comparison with fixed order comp.: FeynHiggs

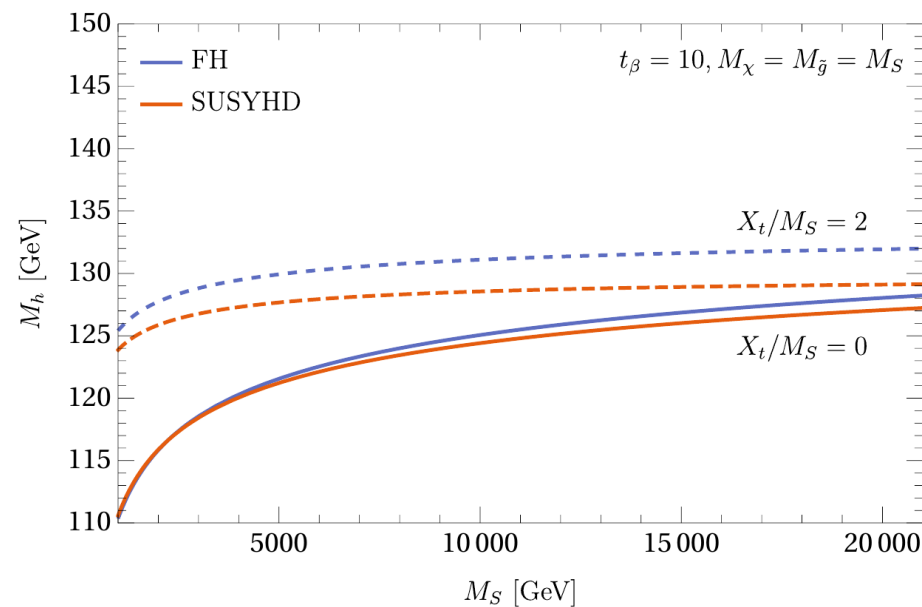
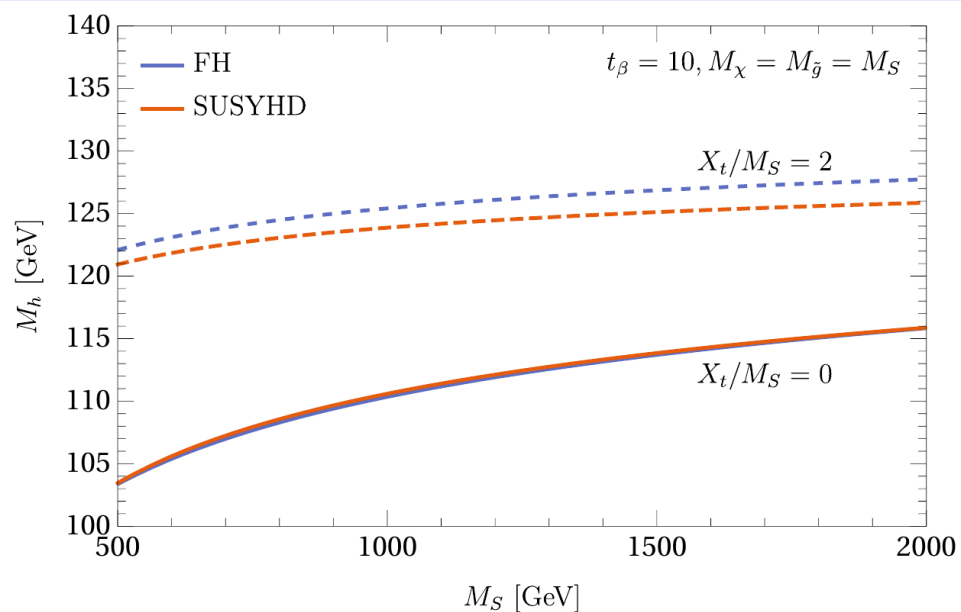
FH 2.11.3 now includes
 $O(\alpha_s^2)$ corrections to y_t



Comparison with fixed order comp.: FeynHiggs

towards implementing all higher order corrections in FH...

from **Henning Bahl** talk @ KUTS'16 - 21/01/2016



Where is the Simplest SUSY?

The Simplest SUSY

(m_h, λ)
SM

The Simplest SUSY

$$\begin{array}{c} (m_h, \lambda) \\ \text{SM} + \text{SUSY} \\ \underbrace{\hspace{10em}} \\ \text{MSSM } (\mu) \end{array}$$

The Simplest SUSY

$$\begin{array}{c} (m_h, \lambda) \\ \underbrace{\text{SM} + \text{SUSY}}_{\text{MSSM } (\mu)} + \cancel{\text{SUSY}} \\ (F) \end{array}$$

The Simplest SUSY

$$\begin{array}{ccccccc}
 (m_h, \lambda) & & & & & & \\
 \text{SM} & + & \text{SUSY} & + & \cancel{\text{SUSY}} & + & \text{Mess.} \\
 \underbrace{\hspace{10em}} & & & & & & \\
 \text{MSSM } (\mu) & & (F) & & (M) & &
 \end{array}$$

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 & & (F) & & (M) & &
 \end{array}$$

$\mu, \Lambda = F/M$ fixed by m_Z, m_h

weak dependence on $\log(M)$

Minimal Gauge Mediation

Dine, Nir, Shirman
Rattazzi, Sarid '96

spectrum mostly fixed by usual GM relations

gauginos $M_j = N \frac{\alpha_j}{4\pi} \Lambda$ **scalars** $m_i = 2\sqrt{N} C_{ij} \frac{\alpha_j}{4\pi} \Lambda$ **higgsinos** μ

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$$A_t \leq m_0 \quad \rightarrow \quad \text{no maximal mixing}$$

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$$B_\mu \ll m_0^2 \quad \rightarrow \quad \tan(\beta) \sim 30 - 60$$

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spectrum mostly fixed by usual GM relations

gauginos $M_j = N \frac{\alpha_j}{4\pi} \Lambda$ **scalars** $m_i = 2\sqrt{N} C_{ij} \frac{\alpha_j}{4\pi} \Lambda$ **higgsinos** μ



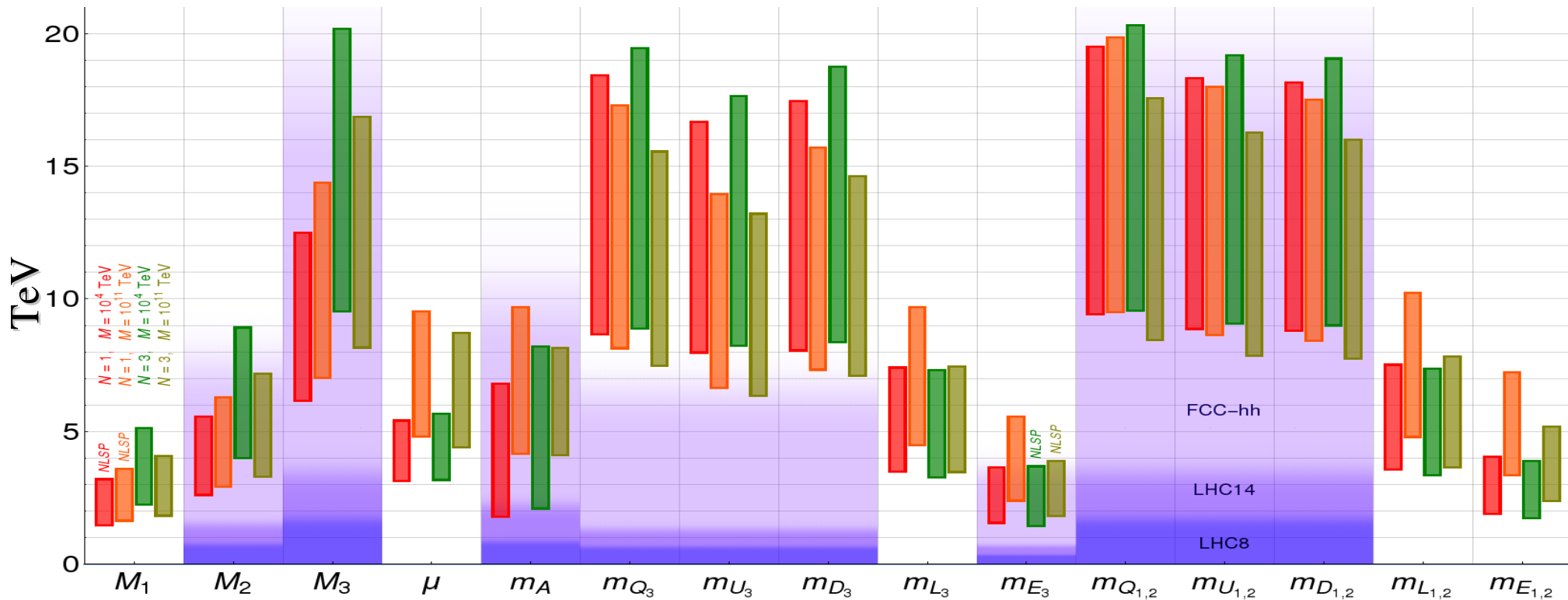
no flavor problems (MFV)

$$A_t \leq m_0 \rightarrow \text{no maximal mixing}$$

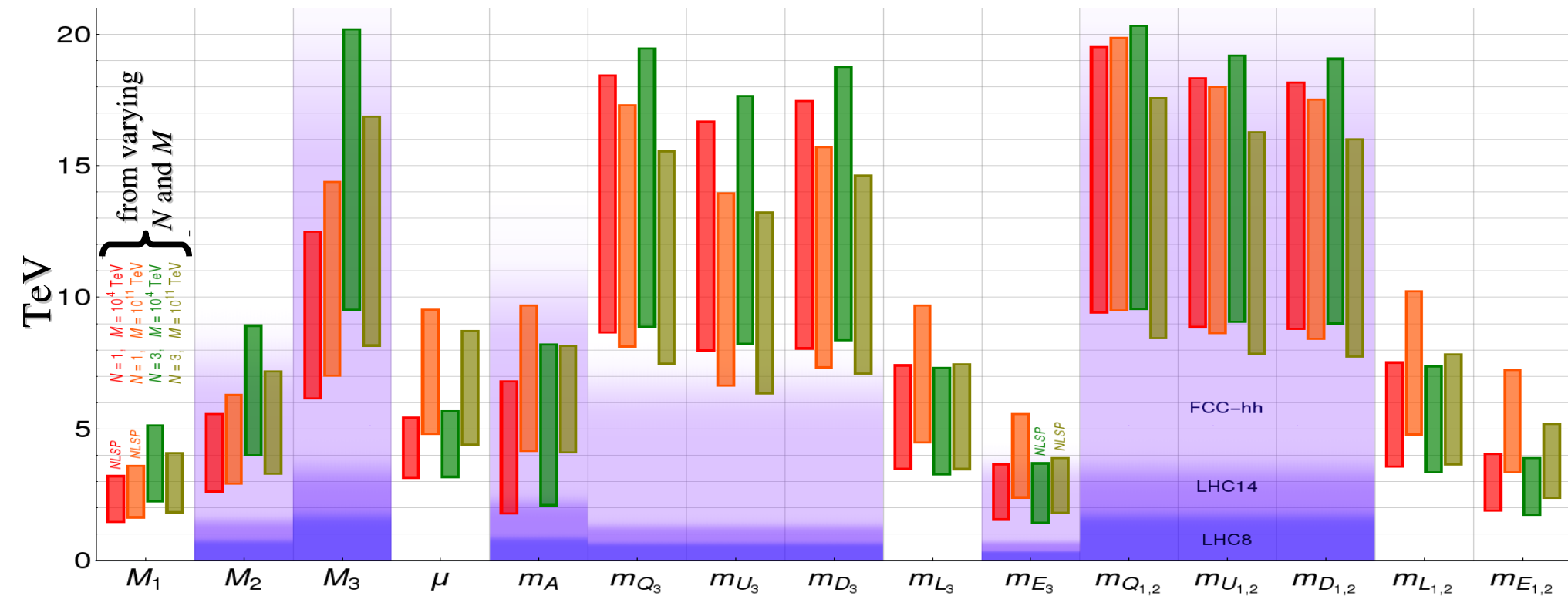
$$B_\mu \ll m_0^2 \rightarrow \tan(\beta) \sim 30 - 60$$

no CP phases $\rightarrow$ no EDMs

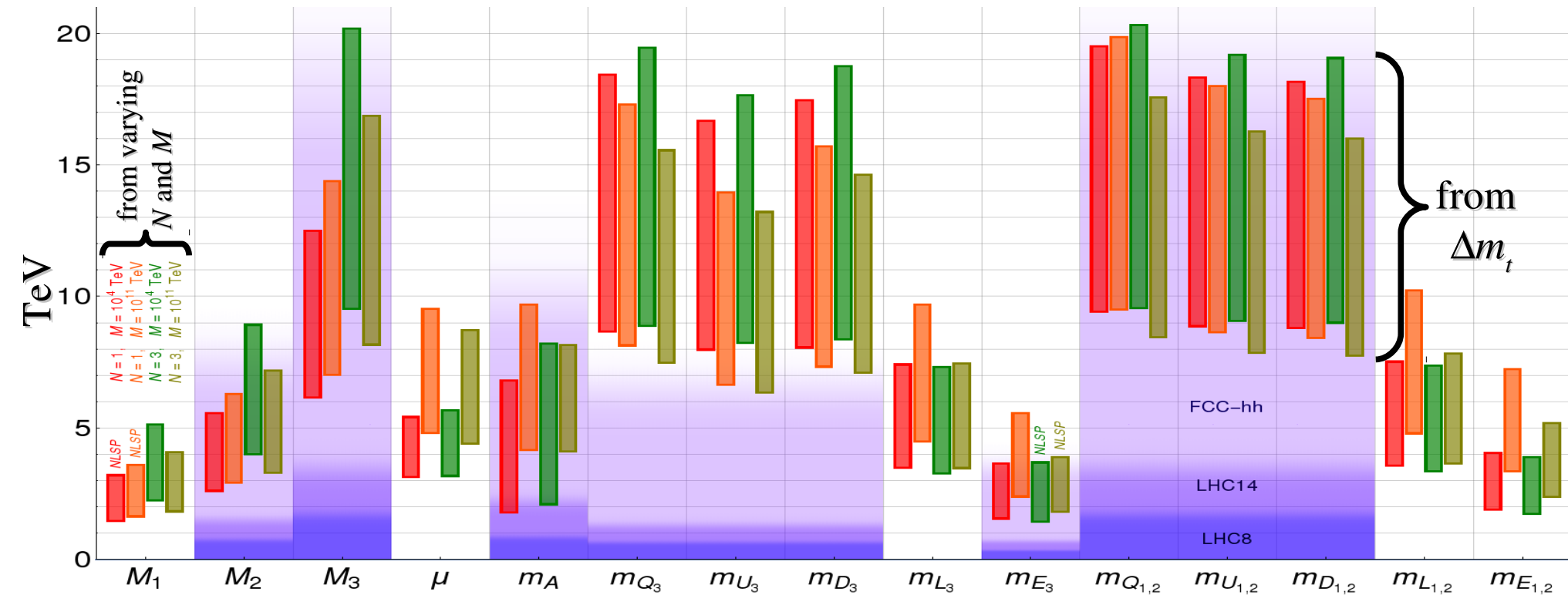
Predicting the MGM spectrum



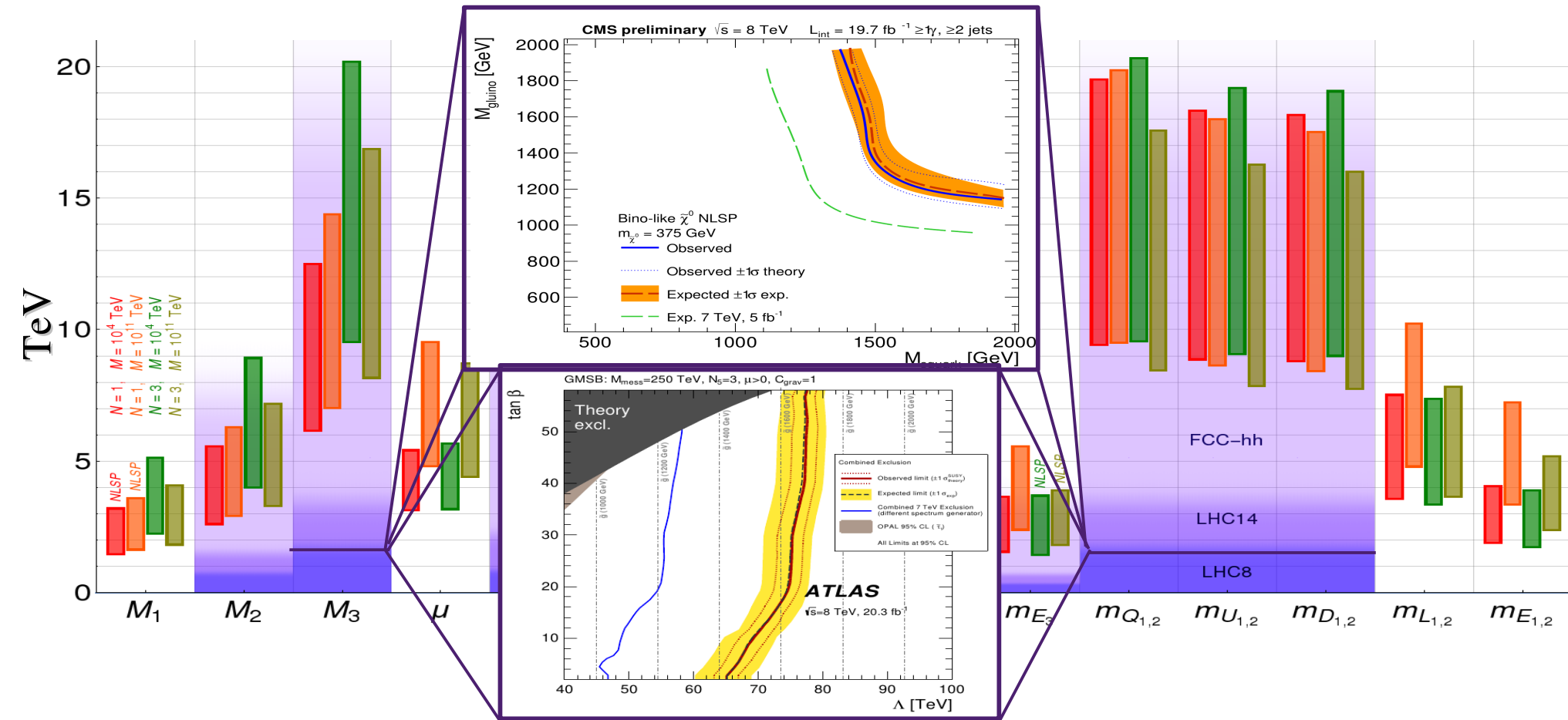
Predicting the MGM spectrum



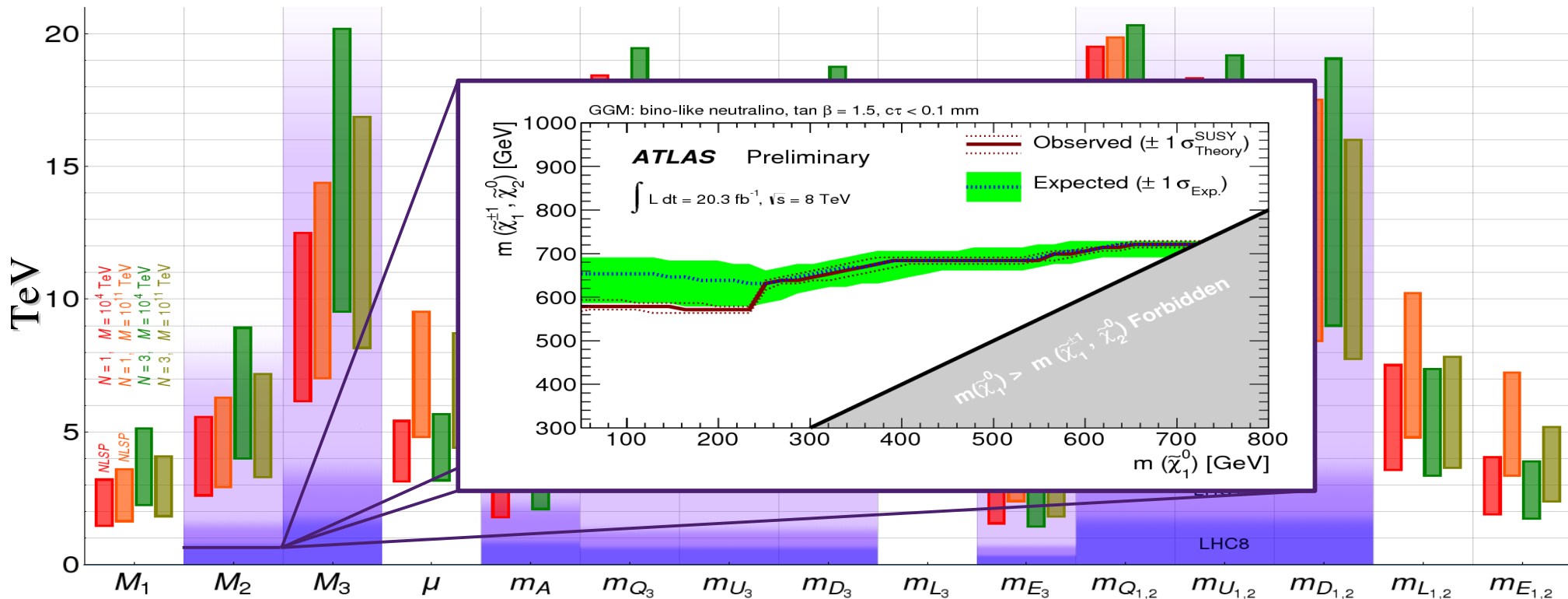
Predicting the MGM spectrum



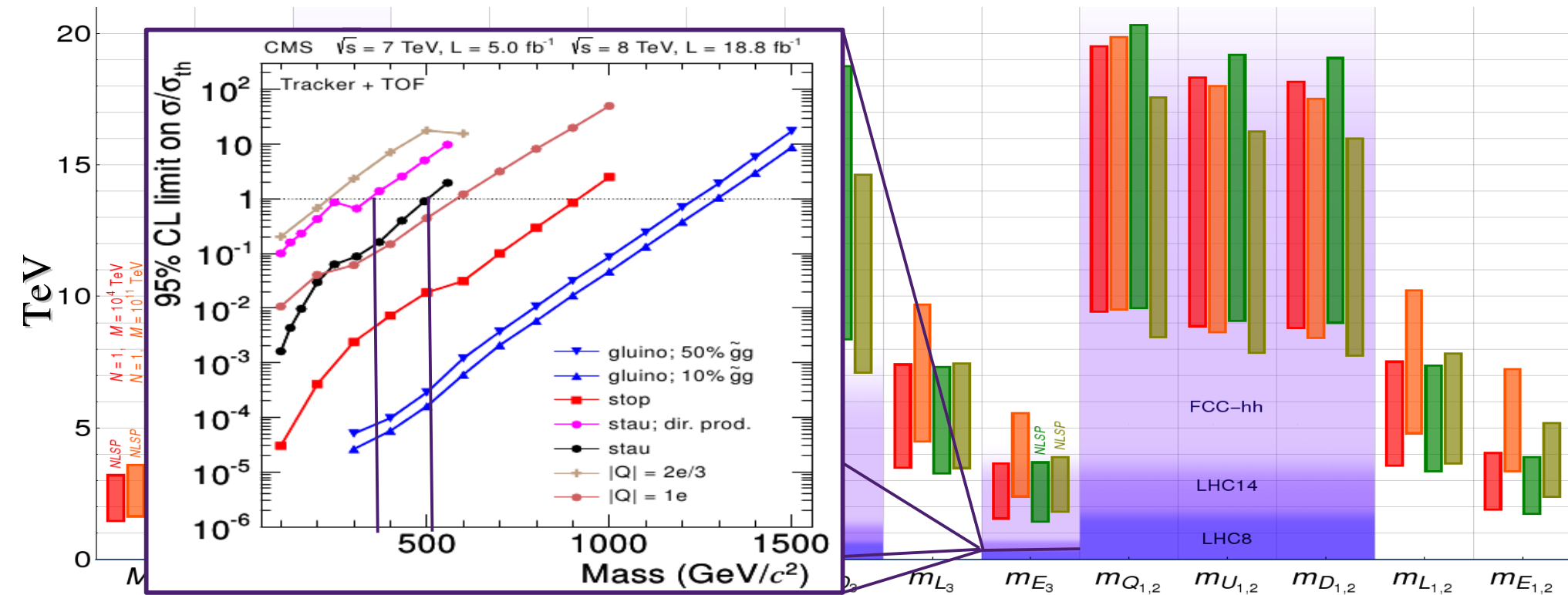
Predicting the MGM spectrum



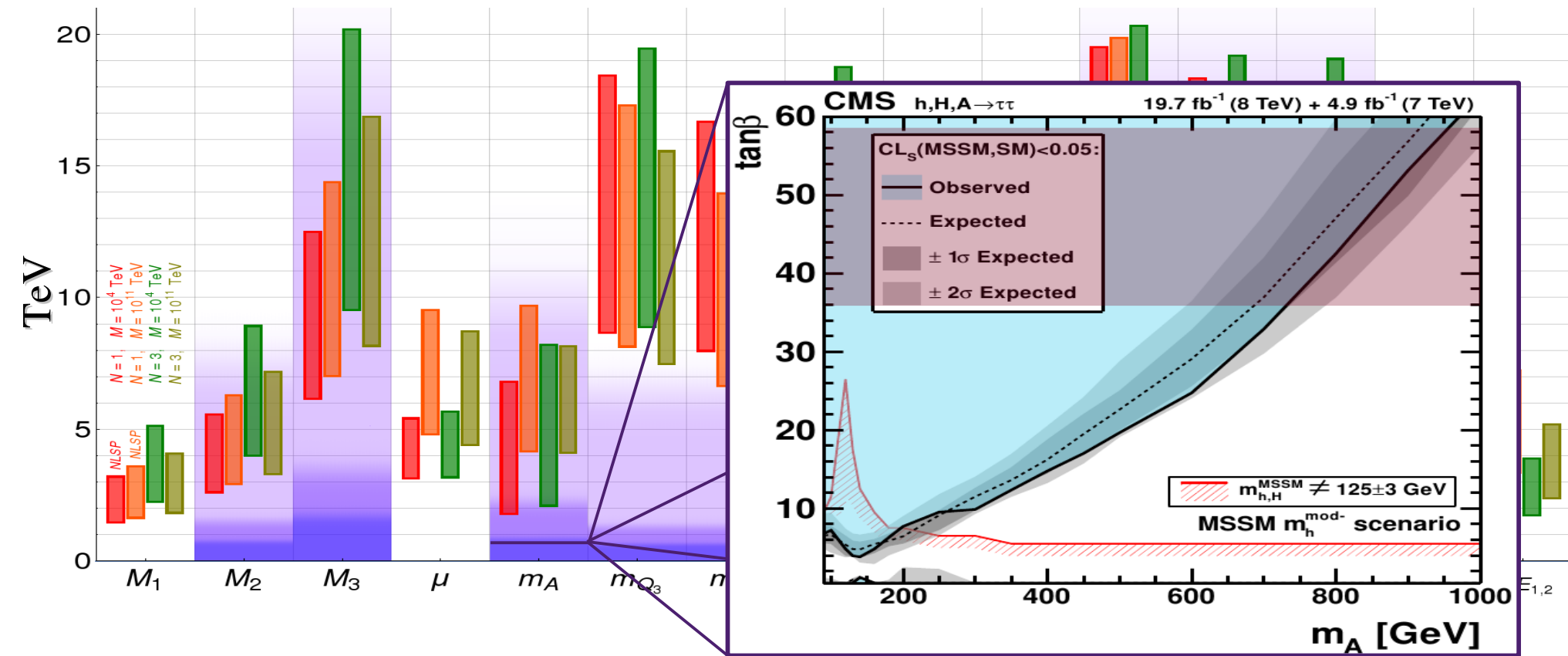
Predicting the MGM spectrum



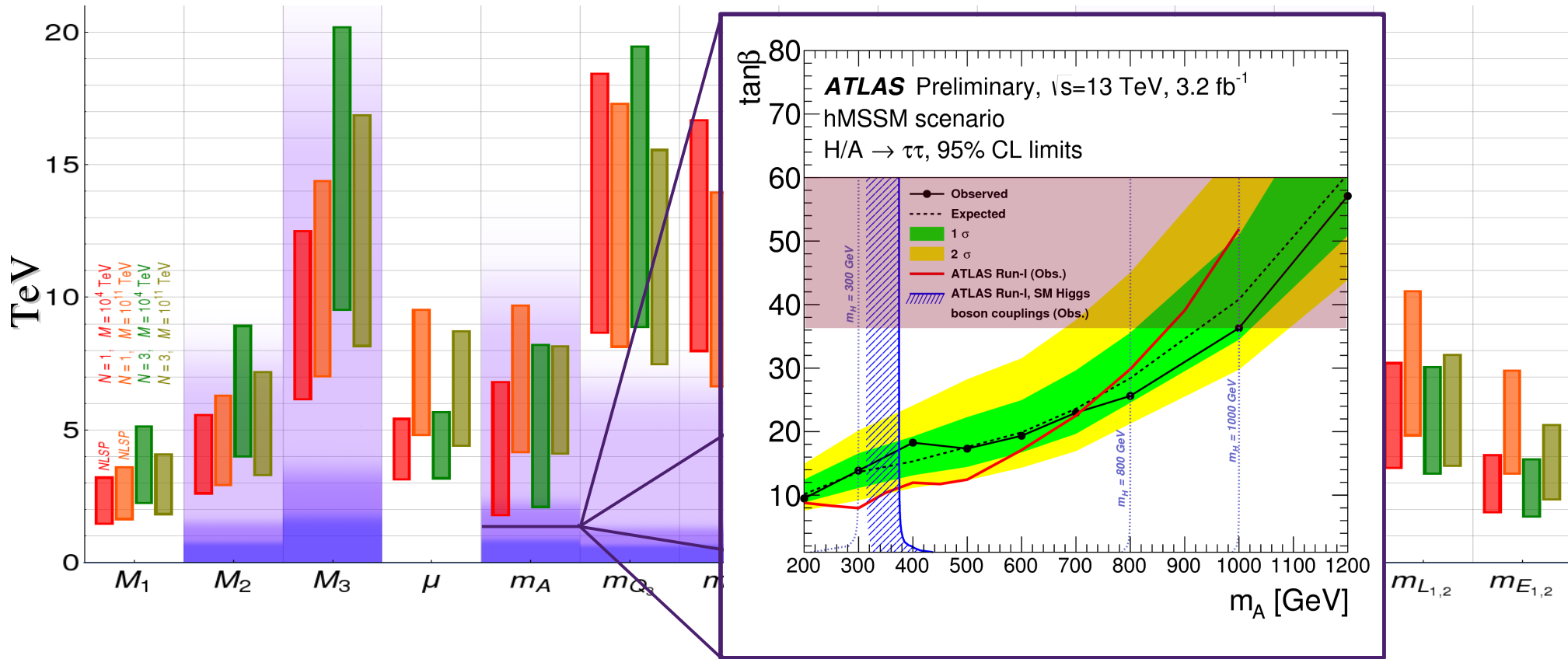
Predicting the MGM spectrum



Predicting the MGM spectrum



Predicting the MGM spectrum



MGM:

minimal and most predictive implementation of SUSY

it explains:

- absence of deviation in flavor
- absence of EDMs
- absence of DM in WIMP searches
- gauge coupling unification
- absence of sparticles at the LHC!

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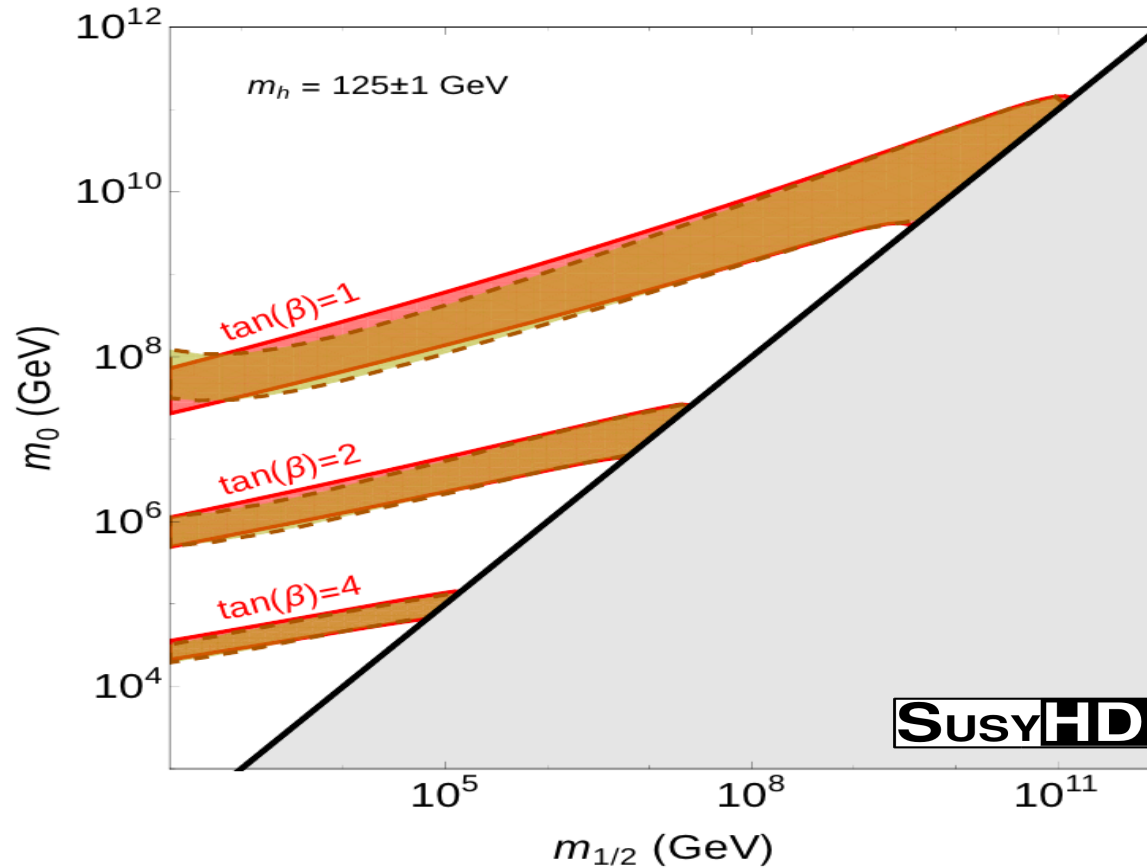
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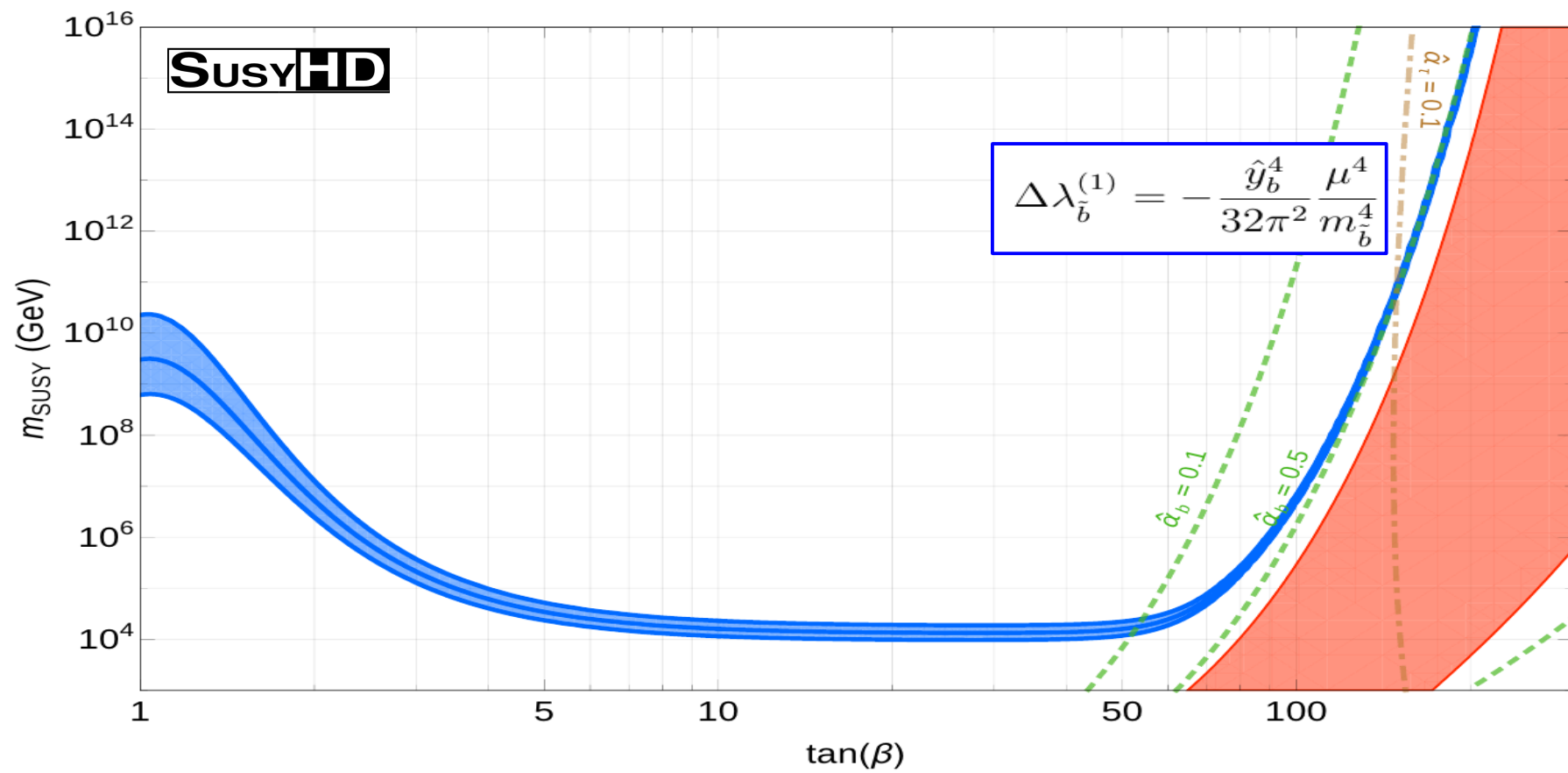
Perfect target for an 100 TeV collider?

Improvement on *top* mass **required!**

Backup

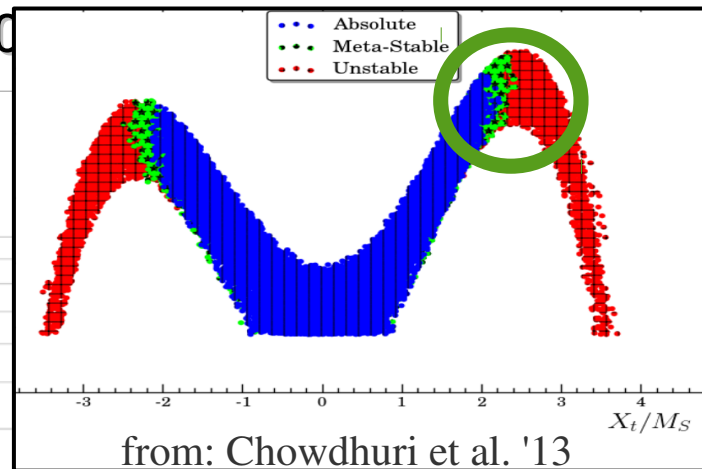
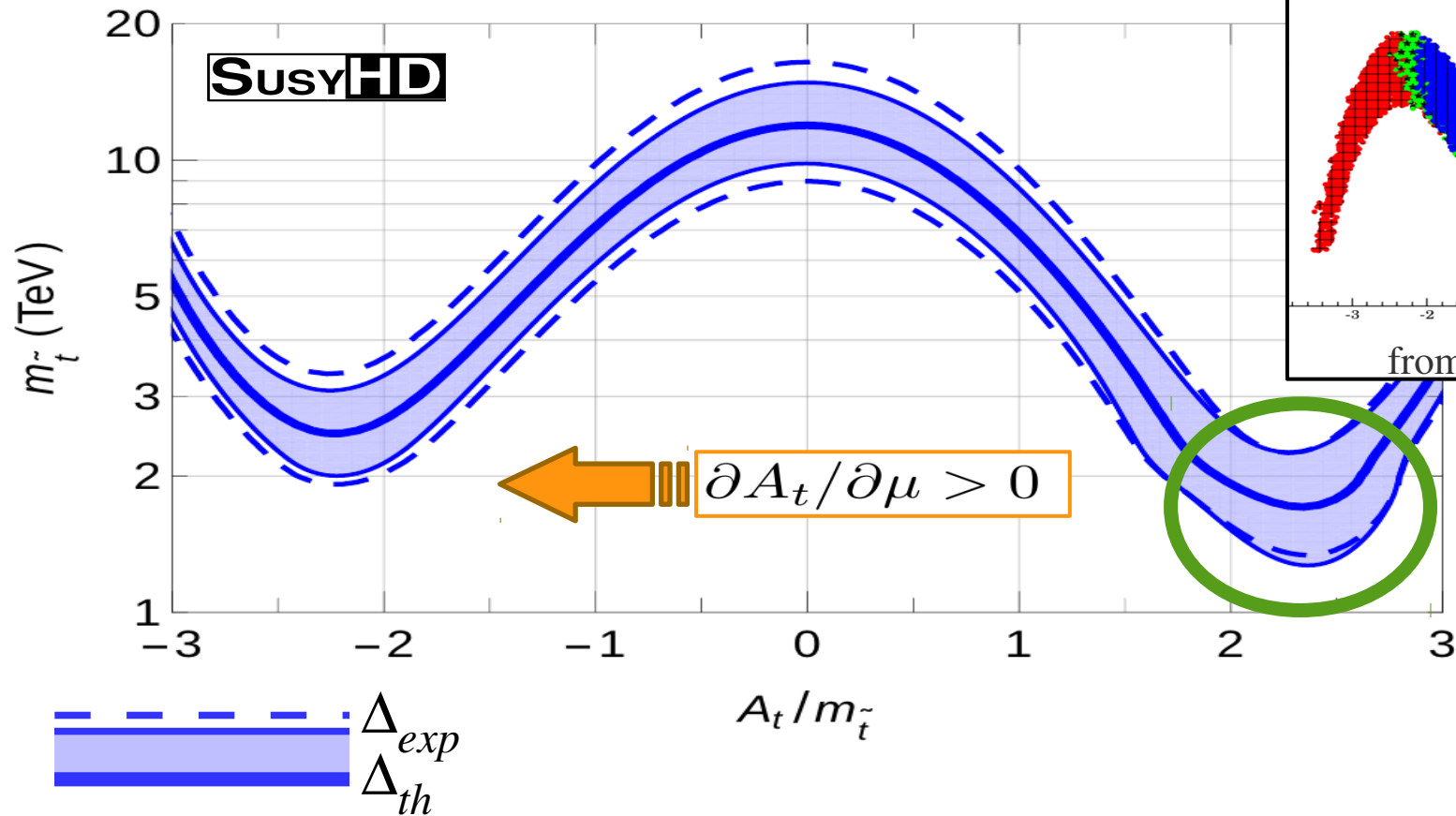
Effects from splitting fermions





A “natural” SUSY-like spectrum:

$\tan\beta = 20$, $\mu = 300$



No naturalness $\rightarrow$ no μ problem:

SUSY term

μ



No naturalness $\rightarrow$ no μ problem:

μ 

no EWSB

 $m_0, M_{1/2}$

No naturalness $\rightarrow$ no μ problem:

m_Z $m_0, M_{1/2}$ EWSB $\sim m_0$

μ

No naturalness $\rightarrow$ no μ problem:

μ 



$m_0, M_{1/2}$

$$|\mu|^2 \simeq -m_{H_u}^2 + \dots$$



m_Z

$$\text{EWSB} \ll m_0$$

No naturalness $\rightarrow$ no μ problem:

μ   $m_0, M_{1/2}$ $|\mu|^2 \simeq -m_{H_u}^2 + \dots$

 m_Z EWSB $\ll m_0$

$B_\mu, A = 0$ at the scale
 M

generated radiatively

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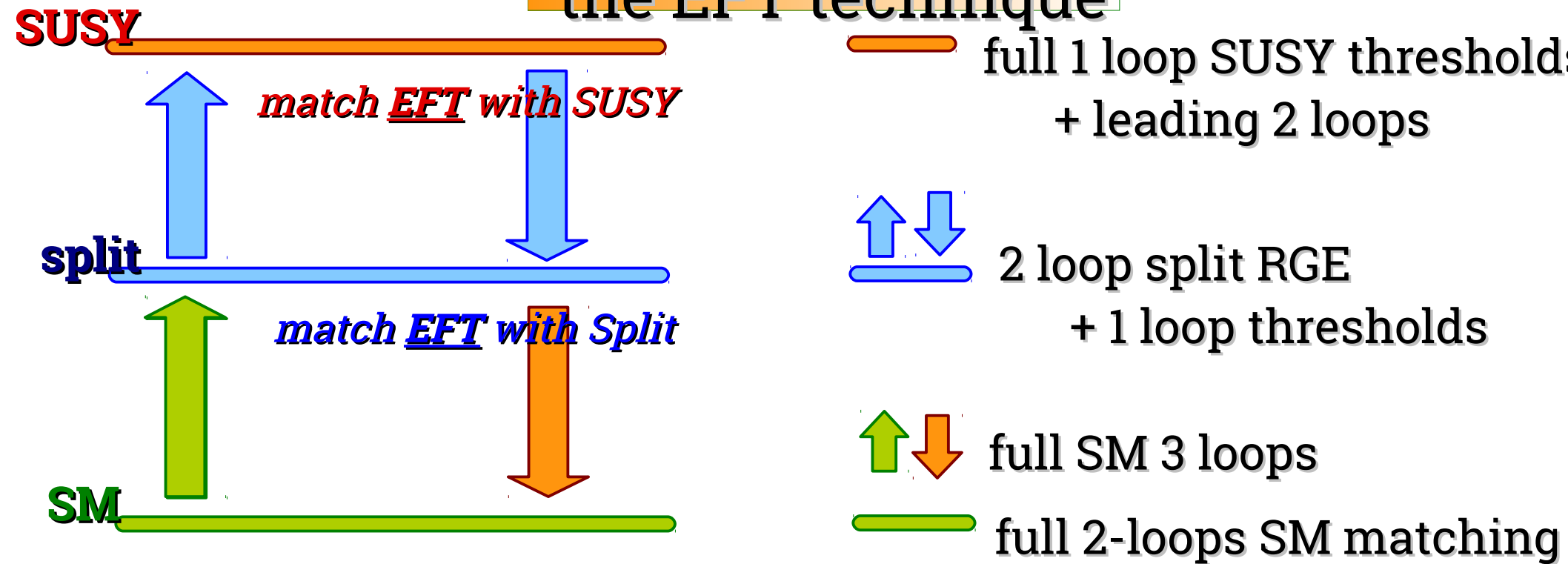
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no CP phases $\rightarrow$ no EDMs

Exploiting the Hierarchy Problem:

the EFT technique



Small improvement w.r.t. to a longstanding effort

Pokorski, Rosiek, Dabelstein, Zhang, Espinosa, Quiros,
Hempfling, Hoang, Heinemeyer, Hollik, Weiglein,
Brignole, Slavich, Zwirner, Deggrasi, Martin,
Giudice, Strumia, Wagner ... many many others

apologies to the missing ones

Our contribution: (mostly w.r.t. Bagnaschi *et al.* '14)

- Recomputation of $O(\alpha_s \alpha_t)$ corrections
- Computation of $O(\alpha_t^2)$ with scale dependence
- Inclusion bottom/tau corrections (w/ resummation of $\tan\beta$ enhanced corr.)
- Computation both in $\overline{\text{DR}}$ and OS schemes
- Study of the uncertainties and comparison with existing computations
- A “fast” Mathematica[®] package: **SusyHD**

