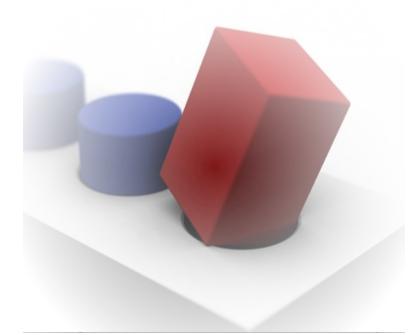




Combined QCD and EW analysis of HERA data



I. Abt, A. Cooper-Sarkar, C. Gwenlan, K. Klimek, <u>V. Myronenko</u>

ZEUS analysis forum 18.11.2015, Hamburg

Analysis setup

- Data used in the analysis (separate datasets, correlations as in HERAPDF2.0):
 - HERAI: H1 + ZEUS;
 - HERAII: H1 unpol. + ZEUS pol.;
 - Reduced E_p runs: H1 + ZEUS;



- HF scheme: GM VFNS NLO (RT OPT).
- $ightharpoonup Q_{min}^2 = 3.5 \text{ GeV}^2.$
- ightharpoonup PDFs parametrised with 13p (HERAPDF2.0 $D\overline{U}$) at $Q_0^2 = 1.9 \text{ GeV}^2$

$$xf(x) = Ax^{B}(1-x)^{C}(1+Dx+Ex^{2})$$

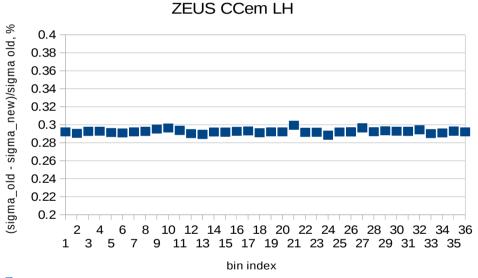
$$xg(x)$$
, $xu_v(x)$, $xd_v(x)$, $x\bar{U}(x)$, $x\bar{D}(x)$

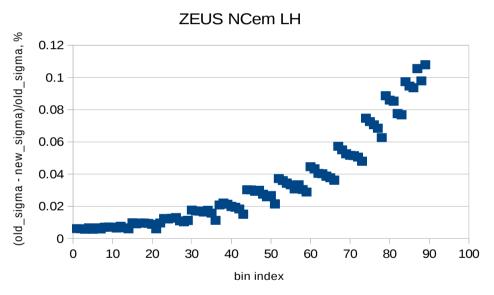
- \clubsuit Free parameters: PDF parameters + couplings of Z^0 to quarks (a_u, a_d, v_u, v_d) or M_w .
- ightharpoonup Optimal M_c and M_b and α_s inherited from HERAPDF2.0.
- \clubsuit Model and parametrisation uncertainty estimation \to HERAPDF2.0 strategy.
- \clubsuit Correction calculated using EPRC code: Δr^{QCD} order α_s . No QED corrections.

Polarisation update

◆ Correction from QCD predictions (PDF → HERAPDF2.0)

$$\sigma_{pol}^{\pm NEW} = \frac{\sigma_{NEWP_e}^{pred}}{\sigma_{OLDP_e}^{pred}} \sigma_{pol}^{\pm OLD}$$





- Very tiny effect on the cross sections.
- Uncertainties due to polarisation were also estimated (treated as correlated in the analysis).

More details in dedicated talk on 07.10.2015

Couplings were determined simultaneously with PDFs (ZEUS-EW-Z)

<u>SM</u>

0.5

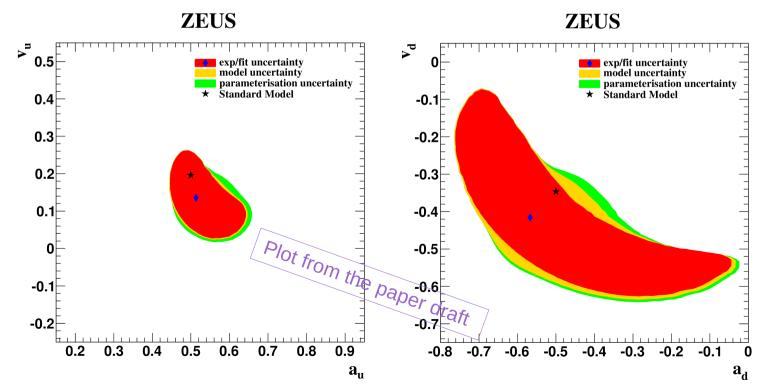
$$a_u = +0.514 + 0.088 + 0.036 + 0.036 + 0.061 + 0.061 + 0.061 + 0.006$$

-0.5

0.196

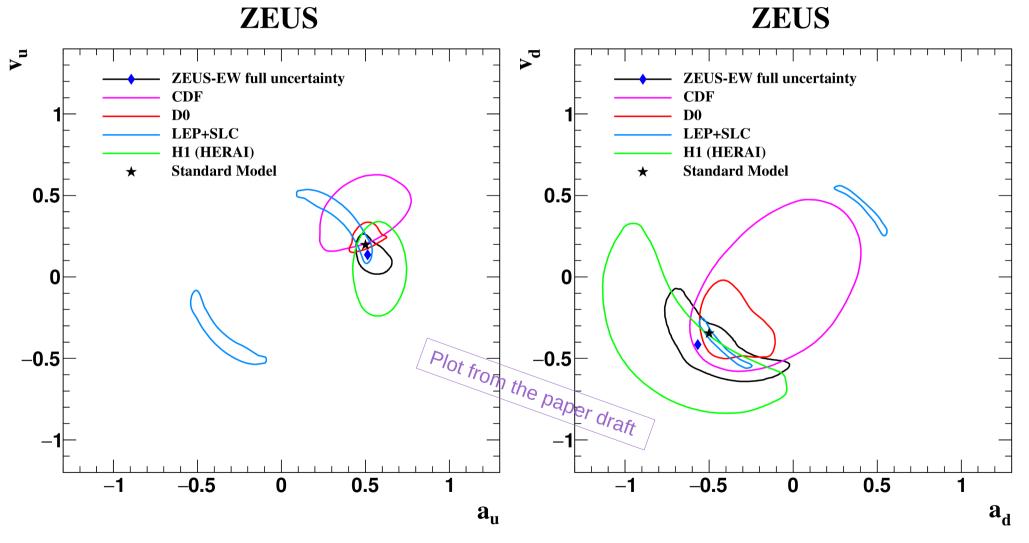
-0.346

2D uncertainties were also evaluated.



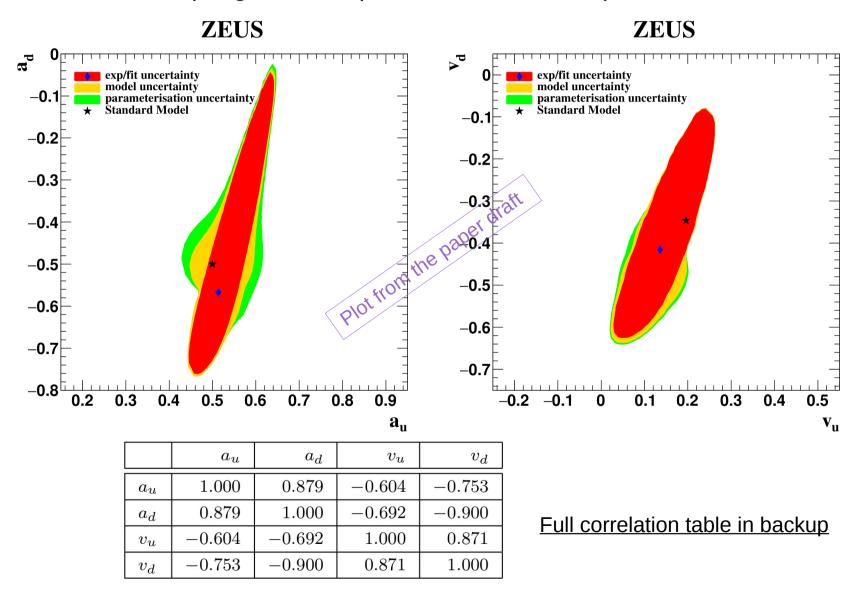
<u>Mod/par variations in backup</u>

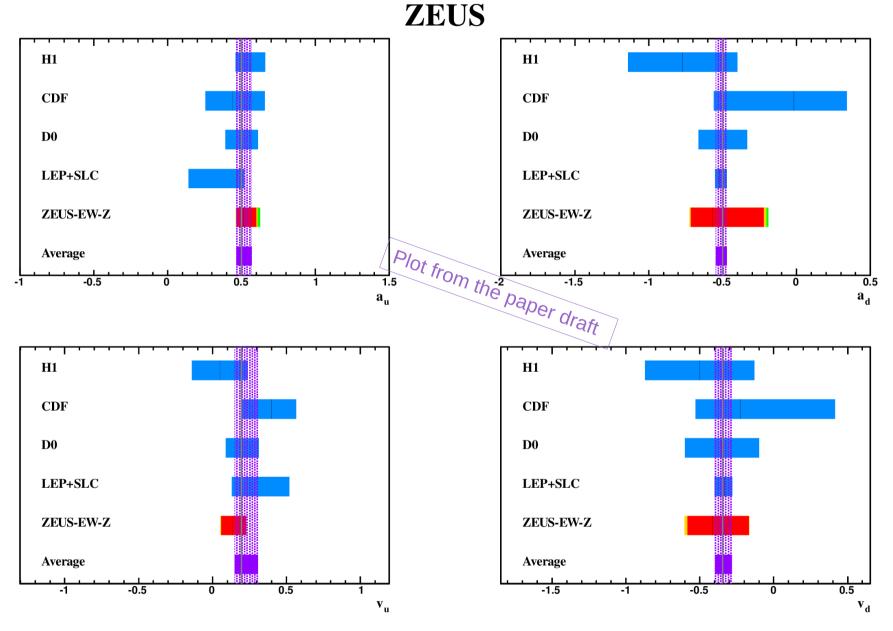
ZEUS-EW-Z results are compatible with previous measurements



Comparison of numerical values in backup

- Couplings in the fit show pretty high correlation
- Correlation of couplings to PDF parameters is weak (see also slides 9 and 10)

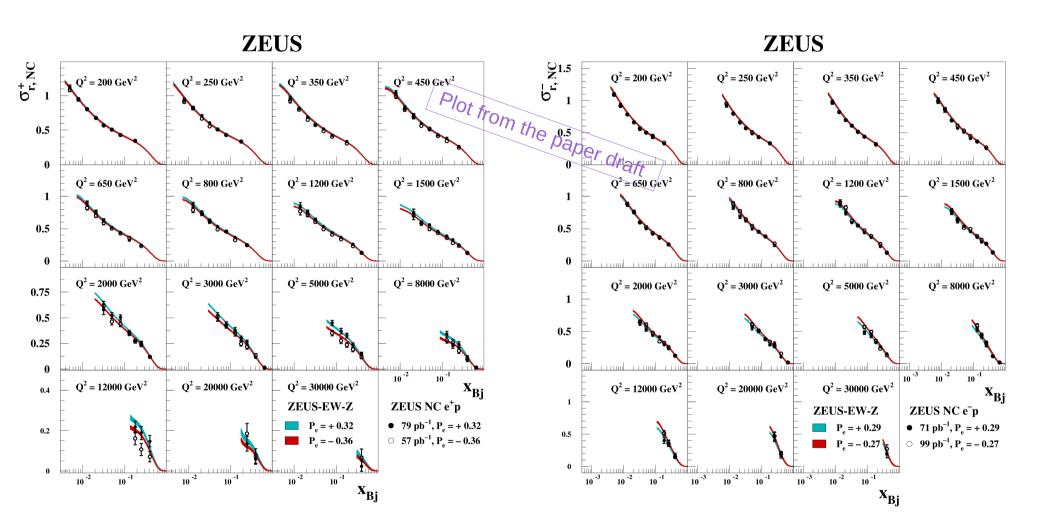




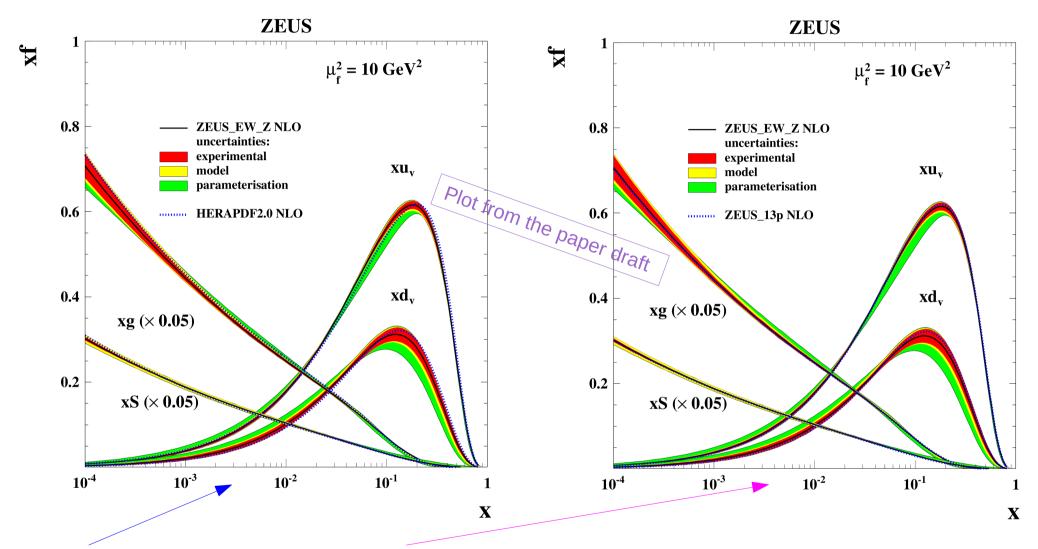


Data description (ZEUS-EW-Z)

Fitted predictions describe data very well.



Effect of coupling determination on PDFs



[♦] HERAPDF2.0 and ZEUS-13p PDFs with couplings set to SM agree with ZEUS-EW-Z PDFs.

PDFs do not absorb any non-SM effects which could show up in EW couplings.

Effect of PDFs determination on couplings

Couplings, fitted at fixed PDFs are well compatible with those from ZEUS-EW-Z fit.

	a_u	exp	tot	a_d	exp	tot	v_u	exp	tot	v_d	exp	tot
EW-Z	+.514	$+.088 \\049$	$+.113 \\052$	567	$+.345 \\148$	$+.379 \\157$	+.136	$+.093 \\078$	$+.094 \\091$	416	$+.249 \\168$	$+.252 \\193$
13p+Z	+.497	$+.075 \\034$		582	+.303 110		+.138	$+.081 \\078$		407	$+.221 \\176$	
HPDF+Z	+.486	$^{+.061}_{034}$		634	$^{+.239}_{110}$		+.149	$^{+.078}_{078}$		357	$^{+.220}_{194}$	
SM	+.500			500			+.196			346		

Differences in the experimental uncertainties can give a rough estimate of PDF uncertainties in the measurement.

Cross-checks: HERAFitter vs ZEUSFitter

Parameter	HF Volodymyr	HF Katarzyna	ZF Amanda
'Bg'	-0.068 ± 0.074	-0.068 ± 0.085	-0.07 ± 0.13
'Cg'	8.50 ± 0.84	8.50 ± 0.84	8.5 ± 1.1
'Aprig'	1.41 ± 0.60	1.41 ± 0.62	1.35 ± 0.53
'Bprig'	-0.158 ± 0.058	-0.158 ± 0.064	-0.16 ± 0.12
'Cprig'	25.00	25.00	25.00
'Buv'	0.742 ± 0.026	0.742 ± 0.026	0.737 ± 0.026
'Cuv'	4.698 ± 0.089	4.698 ± 0.089	4.675 ± 0.088
'Euv'	9.2 ± 1.3	9.2 ± 1.3	9.2 ± 1.2
'Bdv'	0.763 ± 0.077	0.763 ± 0.077	0.741 ± 0.076
'Cdv'	4.38 ± 0.33	4.38 ± 0.33	4.34 ± 0.35
'CUbar'	3.56 ± 0.48	3.56 ± 0.48	3.61 ± 0.50
'ADbar'	0.1976 ± 0.0088	0.1976 ± 0.0088	0.1959 ± 0.0091
'BDbar'	-0.1583 ± 0.0054	-0.1583 ± 0.0054	-0.1586 ± 0.0055
'CDbar'	4.1 ± 1.1	4.1 ± 1.1	3.6 ± 1.1
'alphas'	0.1180	0.1180	0.1180
'fs'	0.4000	0.4000	0.4000
'auEW'	0.514 ± 0.057	0.514 ± 0.057	0.520 ± 0.064
'adEW'	-0.57 ± 0.21	-0.57 ± 0.21	-0.55 ± 0.23
'vuEW'	0.136 ± 0.084	0.136 ± 0.084	0.136 ± 0.087
'vdEW'	-0.42 ± 0.21	-0.42 ± 0.21	-0.41 ± 0.23
Fit status	converged	converged	undefined
Uncertainties	migrad-hesse	migrad-hesse	migrad-hesse
Total χ^2 / dof	3270 / 2925	3270 / 2925	3269 / 2925

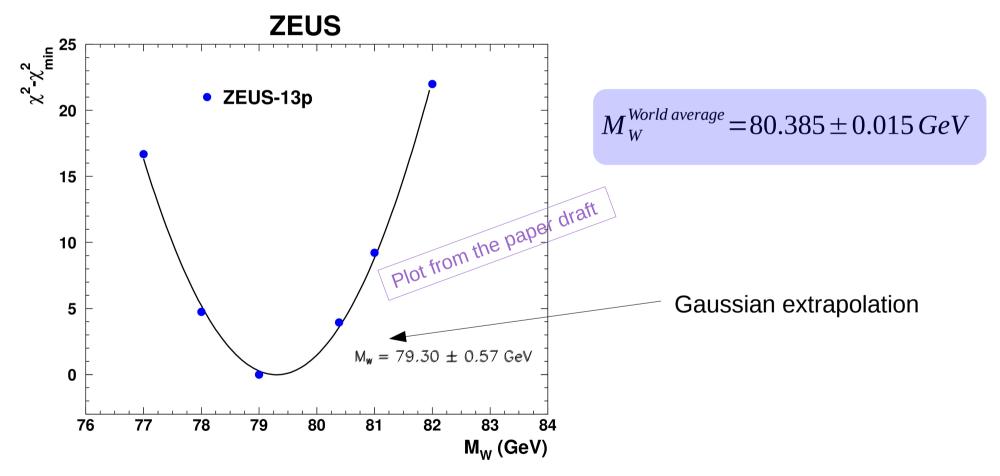


PDF comparison @ 1.9GeV² in backup

Mass of W boson

Mass of W boson was determined simultaneously with PDFs (ZEUS-EW-W)

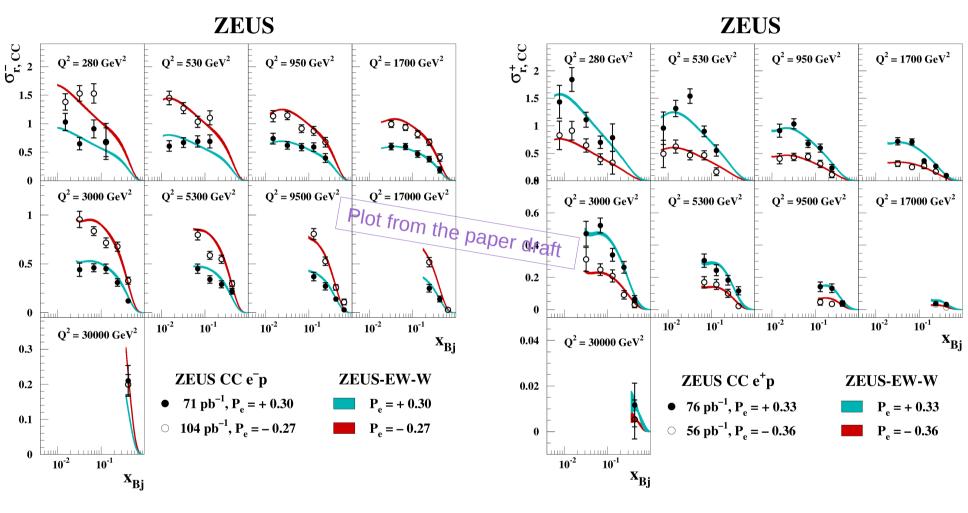
$$M_W = 79.20 \pm 0.56 \text{(exp)}^{+0.06}_{-0.18} \text{(model)}^{+0.02}_{-0.60} \text{(param) GeV}$$



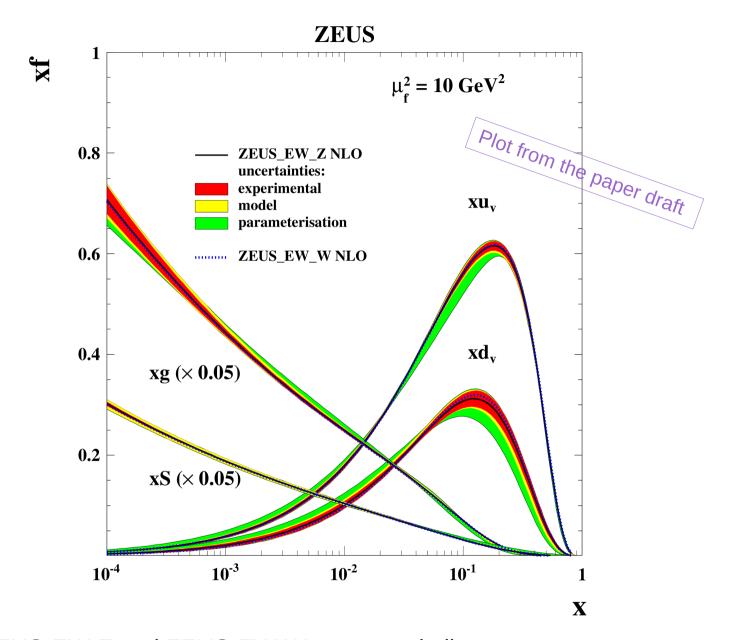
 $ightharpoonup M_{
m w}$ form ZEUS-EW-W is consistent with current world average.

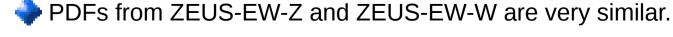
Data description (ZEUS-EW-W)

Fitted predictions describe data very well.



ZEUS-EW-Z vs ZEUS-EW-W

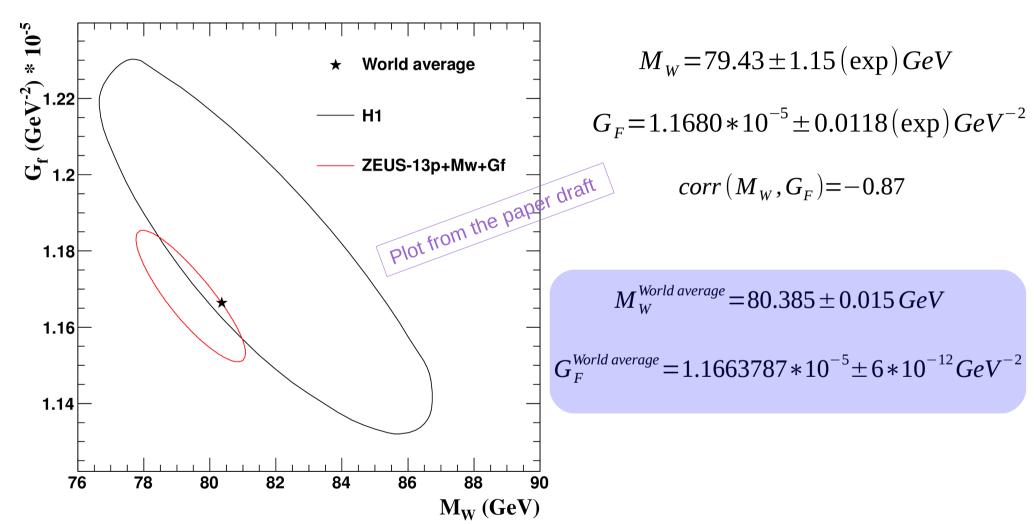




G_E and mass of W boson

 \rightarrow G_F and mass of W boson were also determined simultaneously with PDFs

ZEUS



 \rightarrow Fitter G_F and M_W are consistent with current world average values.

Summary

- QCD and EW analysis of HERA data was performed.
- Couplings of light quarks to Z boson were determined (ZEUS-EW-Z).
 - Fitted couplings are consistent with SM predictions;
 - Results are compatible with those frome other measurements;
 - Couplings of u-quark are constrained significantly better than those of d-quarks.
- Mass of W boson was determined (ZEUS-EW-W).
 - Fitted value of M_w is consistent with current world average;
- \clubsuit Mass of W boson and Fermi constant G_F were determined.
 - Fitted value of M_w and G_E are consistent with current world average values;

Paper draft of the analysis can be found at:

http://www.desy.de/~myronv/ZEUSEW/

Questions / answers

Misha

0) I. 67-75 Do I understand correctly, that in fact we measure a_U, v_U and a_D, v_D, as we do to distinguish between flavours in the see?

Yes, we can separate flavours (not in the sea though).

1) why don't we consider NNLO fit? This would be interesting at least as a cross check.

	a_u	a_b	V_{u}	V_{d}	chi2
ZEUS-EW-Z (NNLO)	0.454	-0.609	0.128	-0.452	3283
ZEUS-EW-Z	$0.514^{+0.113}_{-0.052}$	$-0.567.^{+0.379}_{-0.157}$	$0.136^{+0.094}_{-0.091}$	$-0.416_{-0.193}^{+0.252}$	3269
SM	0.5	-0.5	0.196	-0.346	

NNLO fits are very unstable. In the current cross-check HESSE did not converge.

2) I'm confused about the data sample used in the analysis. From the description it is unclear to me how the polarised ZEUS data samples were usedtogether with the HERAI+II combined data.

Data used: ZEUS and H1 HERAI data + H1 HERAII unpolarised data + ZEUS HERAII polarised data + H1 and ZEUS data from runs with reduced proton energy.

All the correlations are preserved as in the HERAPDF2.0 combination.

Misha

3) I.189: how the 68% CL is defined? Does it cover 68% of the 2D pdf? does it correspond to deltaChi2=1 criteria of the 2D chi2 (what are the values of other 2 couplings? are they frozen?)

This is basically a MINOS approach: you shift two of your parameters away from the optimal values, fix them and refit all the other parameters in the fit. In such a way one can probe the contour, alone which you have (chi2 - chi2_min) = 2.3 (CL = 68% for 2D case).

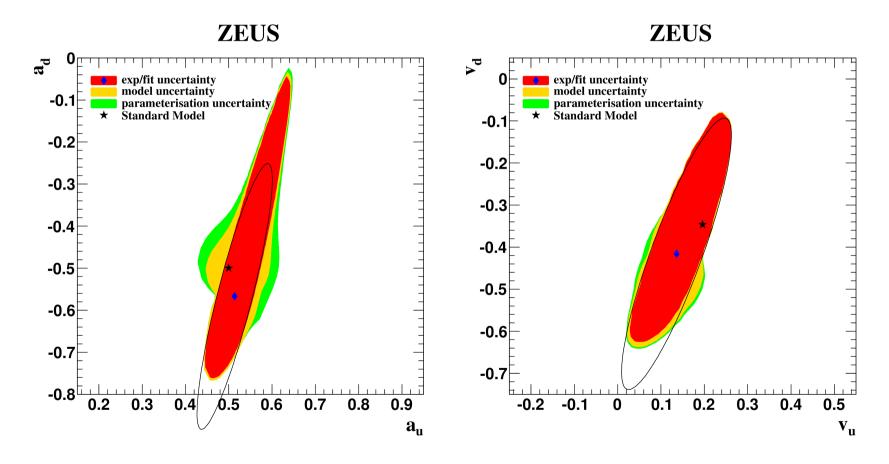
4) Fig. 7: I think we should remove the average. We know the values are correlated with each other within each other and very significantly (for us and LEP at least) and we neglect this significant correlation. We also see that some values have very asymmetric uncertainties (e.g. LEP a_u and v_u) and we had to make some symmetrisation assumptions to use some simple average most likely.

I symmetrised measurements before averaging. however, for the u-quarks our result, as one can see is not that asummetric, and it strongly dominates the average value. in the d-quark case it is LEP who dominates in the average and there it is also not that asymmetric. So symmetrisation here is not so significant, I guess. In addition, neglecting possible correlations between the experiments means overestimating the uncertainty of average result. This plot has just an illustrative purpose

Misha

5) Fig. 8: please check these plots as the correlation seems to be not very significant on this plots (tilt is far from ~pi/4), whereas the correlation table quotes coefficients ~0.9. Is it due to funny model + param. uncertainties? Can we get stat-only correlation coefficient for a visual check (not to include in the draft)?

Checked. All fine.



Quark couplings to Z

Now consider fits to electroweak NC couplings as well as PDF parameters

The total cross-section : $\sigma = \sigma^0 + P \sigma^P$

The unpolarised cross-section is given by $\sigma^0 = Y_+ F_2^0 + Y_- xF_3^0$

$$F_2^0 = \Sigma_i A_i^0(Q^2) \left[xq_i(x,Q^2) + xq_i(x,Q^2) \right]$$

$$xF_3^0 = \Sigma_i B_i^0(Q^2) [xq_i(x,Q^2) - xq_i(x,Q^2)]$$

$$A_i^0(Q^2) = e_i^2 - 2 e_i v_i v_e P_Z + (v_e^2 + a_e^2)(v_i^2 + a_i^2) P_Z^2$$

$$A_i^0(Q^2) = e_i^2 - 2 e_i \mathbf{v_i} \mathbf{v_e} P_Z + (\mathbf{v_e}^2 + \mathbf{a_e}^2)(\mathbf{v_i}^2 + \mathbf{a_i}^2) P_Z^2$$

$$B_i^0(Q^2) = -2 e_i \mathbf{a_i} a_e P_Z + 4 \mathbf{a_i} a_e \mathbf{v_i} v_e P_Z^2$$

$$P_Z = \frac{1}{\sin^2 2\theta} \frac{Q^2}{(M_Z^2 + Q^2)}$$

$$P_{Z} = \frac{1}{\sin^{2} 2\theta} \frac{Q^{2}}{(M_{Z}^{2} + Q^{2})}$$

The polarised cross-section is given by $\sigma^P = Y_+ F_2^P + Y_- x F_3^P$

$$F_2^P = \Sigma_i A_i^P(Q^2) [xq_i(x,Q^2) + xq_i(x,Q^2)]$$

$$xF_3^P = \sum_i B_i^P(Q^2) [xq_i(x,Q^2) - xq_i(x,Q^2)]$$

$$A_i^P(Q2) = 2 e_i v_i a_e P_Z - 2 v_e a_e (v_i^2 + a_i^2) P_Z^2$$

$$B_i^P(Q2) = 2 e_i a_i v_e P_Z - 2 a_i v_i (v_e^2 + a_e^2) P_Z^2$$

 $P_Z >> P_Z^2$ (yZ interference is dominant) unpolarized $xF_3 \rightarrow a_i$, polarized $F_2 \rightarrow v_i$

Ewald

1) I have a problem with the statement that we improve the precision of a_u and v_u by our results. Of course, as shown in fig. 7, we improve these parameters with respect to other collider experiments. However, having lookedinto the PDG tables I saw that the uncertainties quoted for the world averages of a_uand v_u are by a factor 2 smaller than shown in fig.7. This I would like to understand. I wonder what neutrino experiments contribute.

	a_u	a_b	V_{u}	V_{d}
PDG (average)	0.5 +0.04 -0.06	-0.523 ^{+0.050} -0.029	0.25 ^{+0.07} -0.06	-0.33 ^{+0.05} -0.06
ZEUS-EW-Z	$0.514^{+0.113}_{-0.052}$	$-0.567^{+0.379}_{-0.157}$	$0.136^{+0.094}_{-0.091}$	$-0.416^{+0.252}_{-0.193}$
SM	0.5	-0.5	0.196	-0.346

Checked. No neutrino results on this.

PDG does its own FIT using separate measurements. Meaning our current precision CAN contribute significantly to the PDG average.

2) The electroweak coupling constants of u and d on one side and the W mass with the Fermi constant on the other have been fitted on different data sets

Both couplings of light quarks to Z-boson and mass of W-boson were fitted on the same data collection. It was ZEUS and H1 HERAI data + H1 HERAII unpolarised data + ZEUS HERAII polarised data + H1 and ZEUS data from runs with reduced proton energy.

Erich

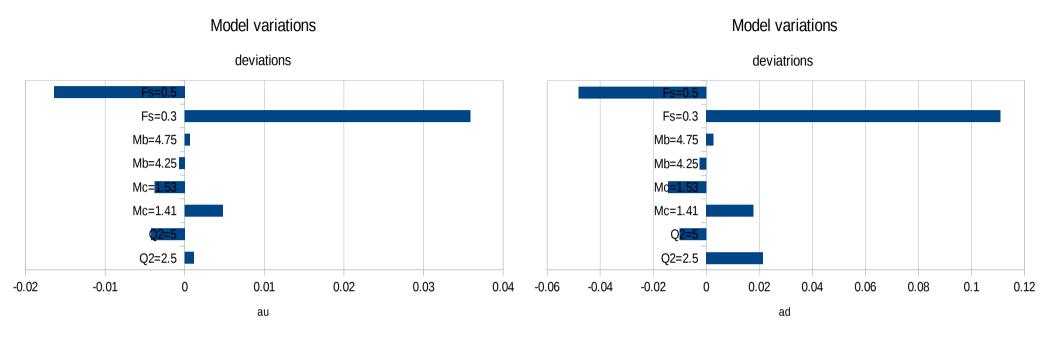
1)Whereas we contribute something new to the quark ew couplings, this is not the case for the W mass and G. Here our accuracy is far worse than the PDG values and our measurements have more the meaning of a consistency check. I therefore suggest to shorten this chapter fittingly.

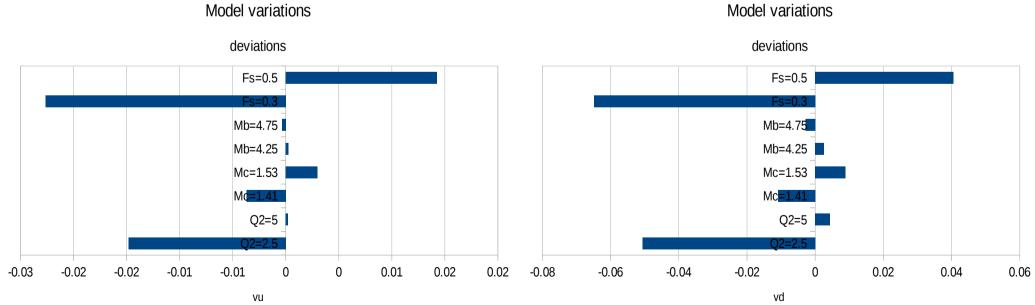
Backup

World results (full uncertainties)

	\mathbf{a}_{u}	a_b	V_{u}	V_d
LEP	$0.47^{+0.05}_{-0.33}$	$-0.52^{+0.05}_{-0.03}$	$0.24^{+0.28}_{-0.11}$	-0.33 ^{+0.05} -0.07
D0	0.50±0.11	-0.50±0.17	0.20±0.11	0.35±0.25
CDF	$0.44^{+0.22}_{-0.19}$	$-0.02^{+0.36}_{-0.54}$	$0.40^{+0.17}_{-0.20}$	$-0.23^{+0.64}_{-0.30}$
H1: HERA1 (publ.)	0.56±0.10	-0.77±-0.37	0.05±0.19	-0.50±0.37
ZEUS: HERA1+2 (prel.)	0.51±0.20	-0.54±0.37	0.05±0.10	-0.64±0.24
ZEUS-EW-Z	$0.514_{-0.052}^{+0.113}$	$-0.567{-0.157}^{+0.379}$	$0.136.^{+0.094}_{-0.091}$	$-0.416{-0.193}^{+0.252}$
SM	0.5	-0.5	0.196	-0.346

Model variations

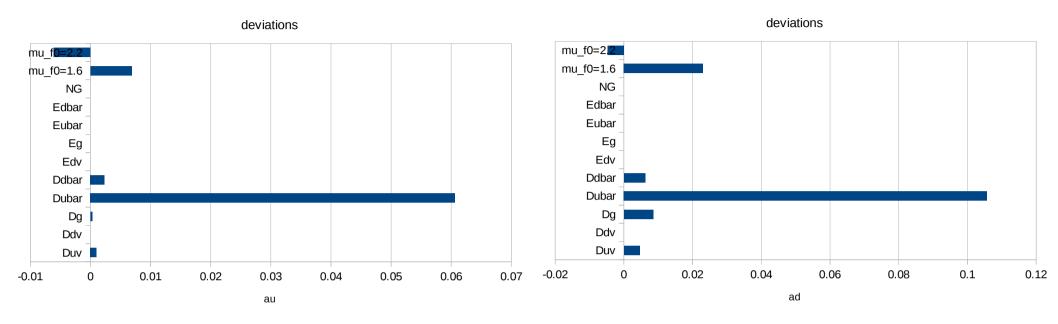




Parametrisation variations variations

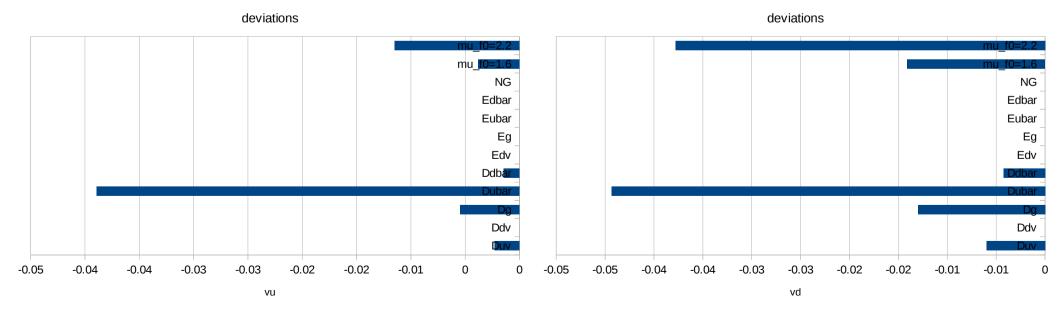


Parameterisation variations

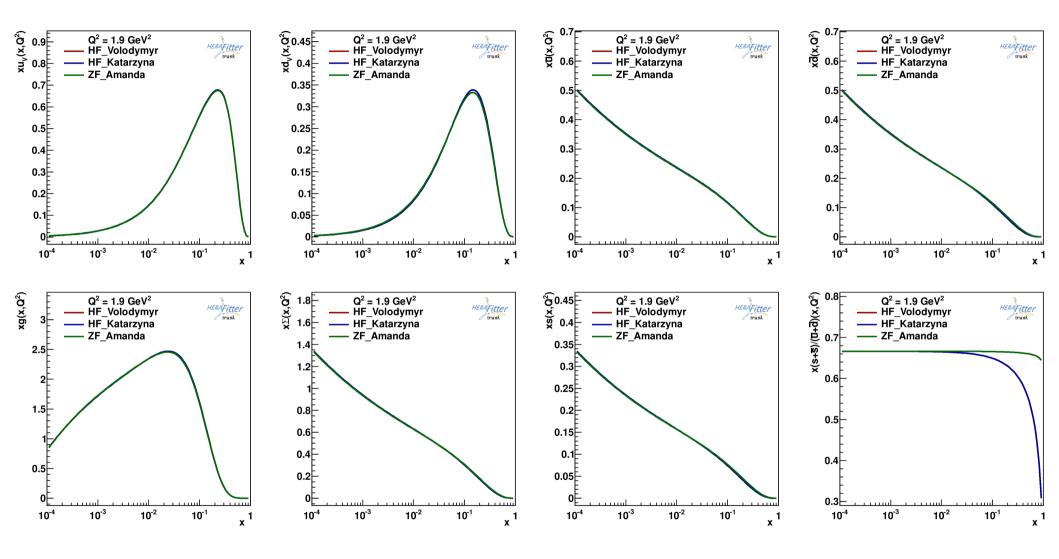


Parameterisation variations

Parameterisation variations



Cross-checks: HERAFitter vs ZEUSFitter



Correlation matrix for the fit parameters

NO. Ba Cg Aprig Bprig Buv Cuv Euv Bdv Cdv CUbar ADbar BDbar CDbar auEW adEW vuEW vdEW 1.000-0.017-0.451 0.823-0.217 0.173 0.251-0.084-0.085-0.098-0.107-0.136 0.047 0.025 0.003 0.015 0.018 Ba $-0.017\ 1.000\ 0.831\ 0.456\ 0.338 - 0.372 - 0.549\ 0.007\ 0.297 - 0.020 - 0.084 - 0.104 - 0.437\ 0.108\ 0.097 - 0.099 - 0.112$ Ca Aprig -0.451 0.831 1.000 0.119 0.547-0.404-0.629 0.231 0.275 0.159 0.080 0.071-0.150-0.051 0.001-0.044-0.054 Bprig 0.823 0.456 0.119 1.000 0.106-0.037-0.082 0.074 0.047 0.043 0.011-0.014 0.012-0.029-0.011-0.001-0.002 -0.217 0.338 0.547 0.106 1.000-0.408-0.774 0.466-0.087 0.690 0.477 0.396 0.440-0.361-0.179 0.079 0.071 0.173-0.372-0.404-0.037-0.408 1.000 0.828-0.296-0.235-0.187-0.095-0.069-0.039 0.109 0.029 0.040 0.028 0.251-0.549-0.629-0.082-0.774 0.828 1.000-0.296-0.066-0.363-0.170-0.117-0.091 0.192 0.087-0.023-0.017 -0.084 0.007 0.231 0.074 0.466-0.296-0.296 1.000 0.516 0.406 0.352 0.293 0.675-0.336-0.135 0.038 0.022 -0.085 0.297 0.275 0.047-0.087-0.235-0.066 0.516 1.000-0.137-0.187-0.194-0.140 0.111 0.129-0.101-0.128 CUbar -0.098-0.020 0.159 0.043 0.690-0.187-0.363 0.406-0.137 1.000 0.674 0.636 0.329-0.321-0.138 0.055 0.052 ADbar -0.107-0.084 0.080 0.011 0.477-0.095-0.170 0.352-0.187 0.674 1.000 0.959 0.478-0.273-0.138 0.057 0.060 BDbar -0.136-0.104 0.071-0.014 0.396-0.069-0.117 0.293-0.194 0.636 0.959 1.000 0.416-0.240-0.120 0.048 0.053 CDbar 0.047-0.437-0.150 0.012 0.440-0.039-0.091 0.675-0.140 0.329 0.478 0.416 1.000-0.450-0.272 0.149 0.154 0.025 0.108-0.051-0.029-0.361 0.109 0.192-0.336 0.111-0.321-0.273-0.240-0.450 1.000 0.879-0.604-0.753 0.003 0.097 0.001-0.011-0.179 0.029 0.087-0.135 0.129-0.138-0.138-0.120-0.272 0.879 1.000-0.692-0.900 0.015-0.099-0.044-0.001 0.079 0.040-0.023 0.038-0.101 0.055 0.057 0.048 0.149-0.604-0.692 1.000 0.871 vdEW 0.018-0.112-0.054-0.002 0.071 0.028-0.017 0.022-0.128 0.052 0.060 0.053 0.154-0.753-0.900 0.871 1.000

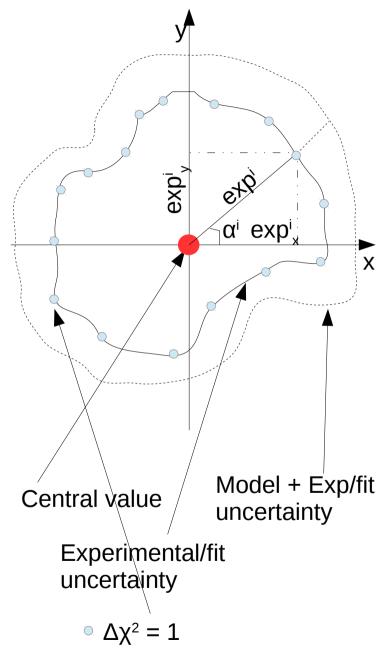
Trying various Q^2_{min} and calc. orders.

	13p+4EW						14p+4EW				Number
	a _u	a _d	V _u	V _d	χ²	a _u	a _d	V _u	V _d	χ²	of data points
NLO 3.5 GeV ²	0.516 ±0.062	-0.523 ±0.227	0.148 ±0.071	-0.442 ±0.187	3589	0.601 ±0.061	-0.303 ±0.253	0.102 ±0.049	-0.533 ±0.085	3571	3248
NLO 10 GeV ²	0.499 ±0.054	-0.559 ±0.184	0.149 ±0.065	-0.432 ±0.172	3161	0.619 ±0.055	-0.266 ±0.240	0.114 ±0.048	-0.509 ±0.084	3145	3006
NNLO 3.5 GeV ²	-	-	-	-	-	-	-	-	-	-	3248
NNLO 10 GeV ²	0.501 ±0.051	-0.554 ±0.175	0.146 ±0.061	-0.441 ±0.158	3154	-/	-	-	-	-	3006
SM	0.5	-0.5	0.196	-0.346		0.5	-0.5	0.196	-0.346		
Both MIGRAD and HESSE failed											

only MIGRAD has converged

- 14p+EW is VERY unstable.
- $ightharpoonup Q^2_{min} = 3.5 \text{ GeV}^2 \rightarrow Q^2_{min} = 10 \text{ GeV}^2$: reduction of uncertainty (but not too stable).

Contours with exp + other uncertainty



$$\exp^{i} = \sqrt{\exp_{x}^{i2} + \exp_{y}^{i2}}$$

$$mod^{i} = \sqrt{(\cos\alpha \, mod_{x})^{2} + (\sin\alpha \, mod_{y})^{2}}$$

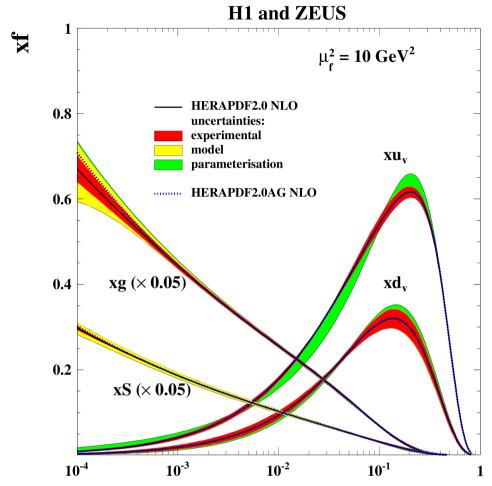
$$\cos \alpha \frac{\exp_x^i}{\exp i} \qquad \sin \alpha \frac{\exp_y^i}{\exp i}$$

$$total^{i} = \sqrt{\exp^{i2} + mod^{i2}}$$

$$total_x^i = \cos \alpha total^i$$

$$total_y^i = \sin \alpha total_i^i$$

HERAPDF2.0: errors estimation



- Parametrisation uncertainties:
- The largest deviation taken.

- Full systematic correlation treatment.
- Experimental uncertainties:
 - Hessian method used: full second-derivative matrix calculated
 - Conventional $\Delta \chi^2 = 1 => 68\%$ CL

Model uncertainties:

- All variations are added in quadratures, separately positive and negative.

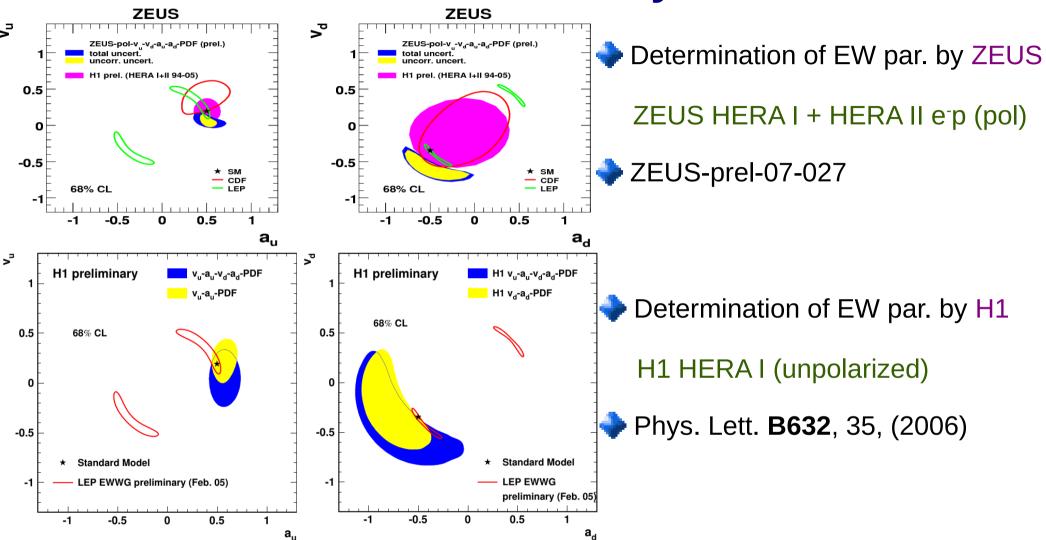
Variation	Standard Value	Lower Limit	Upper Limit
Q_{\min}^2 [GeV ²]	3.5	2.5	5.0
Q_{\min}^2 [GeV ²] HiQ2	10.0	7.5	12.5
$M_c(NLO)$ [GeV]	1.47	1.41	1.53
M_c (NNLO) [GeV]	1.43	1.37	1.49
M_b [GeV]	4.5	4.25	4.75
f_s	0.4	0.3	0.5
μ_{f_0} [GeV]	1.9	1.6	2.2

Adding D and E parameters to each PDF

$$\bar{x} = \frac{\sum_{i}^{X_{i}} \frac{X_{i}}{\sigma_{i}^{2}}}{\sum_{i}^{X_{i}} \frac{1}{\sigma_{i}^{2}}}$$

$$\sigma_{\bar{x}} = \frac{1}{\sqrt{\sum_{i} \frac{1}{\sigma_{i}^{2}}}}$$

Previous analysis

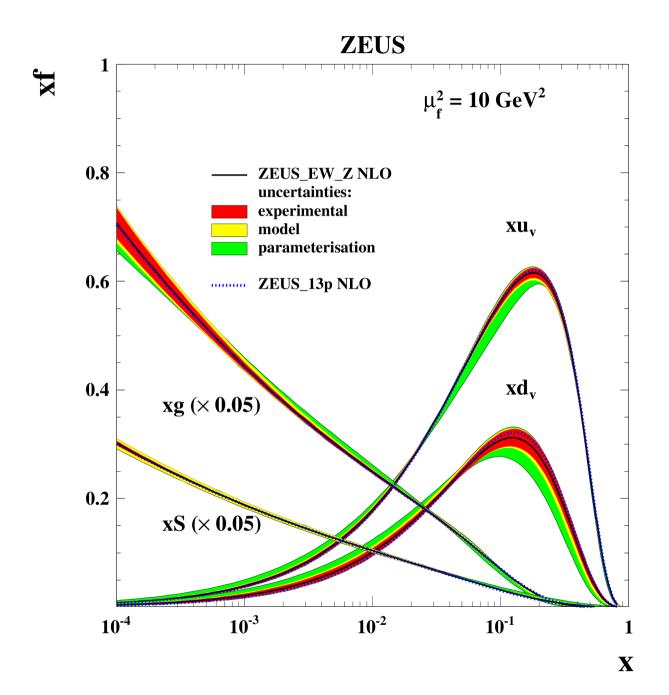


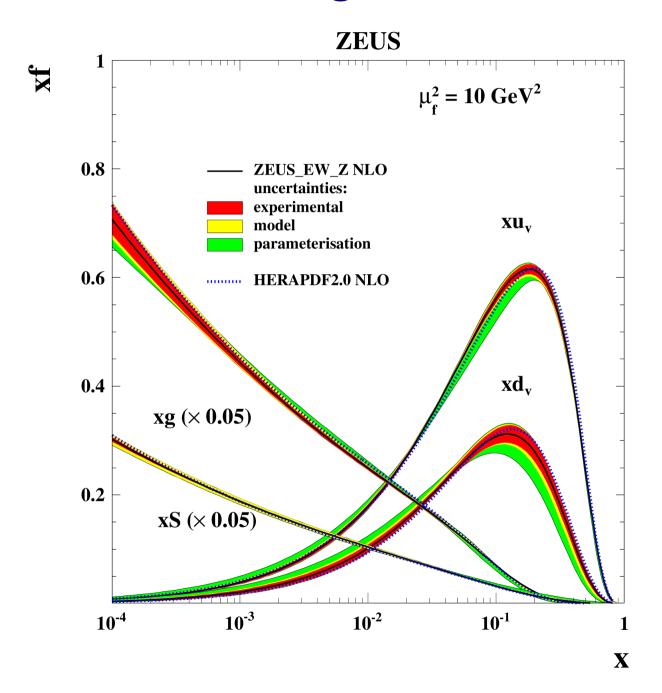
All H1 and ZEUS HERA I unpolarized and HERA II polarized data are now available

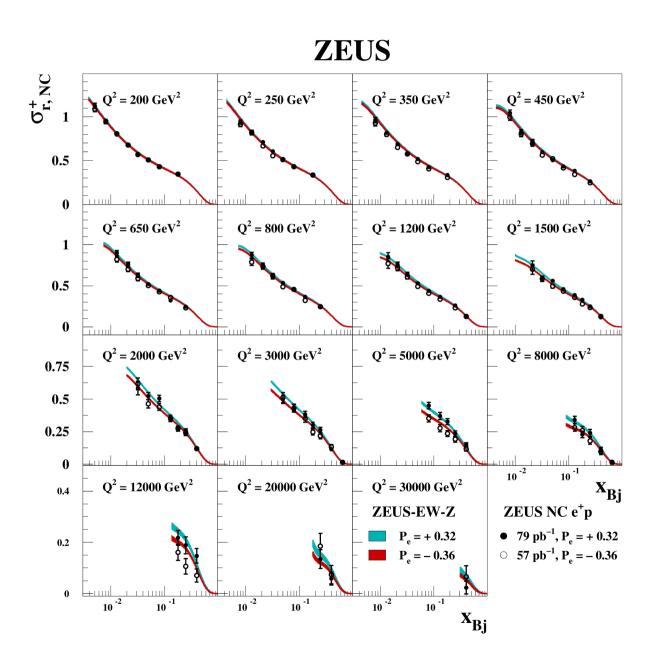
$$\tilde{F}_{2}^{\pm} = F_{2} + k_{Z}(-v_{e} \mp Pa_{e}) \cdot F_{2}^{\gamma Z} + k_{Z}^{2}(v_{e}^{2} + a_{e}^{2} \pm 2Pv_{e}a_{e}) \cdot F_{2}^{Z}
x\tilde{F}_{3}^{\pm} = k_{Z}(\pm a_{e} + Pv_{e}) \cdot xF_{3}^{\gamma Z} + k_{Z}^{2}(\mp 2v_{e}a_{e} - P(v_{e}^{2} + a_{e}^{2})) \cdot xF_{3}^{Z}
(F_{2}, F_{2}^{\gamma Z}, F_{2}^{Z}) = x \sum (e_{q}^{2}, 2e_{q}v_{q}, v_{q}^{2} + a_{q}^{2})(q + \overline{q}) \qquad (xF_{3}^{\gamma Z}, xF_{3}^{Z}) = 2x \sum (e_{q}a_{q}, v_{q}a_{q})(q - \overline{q})$$

Plots from paper draft

Fig. 1







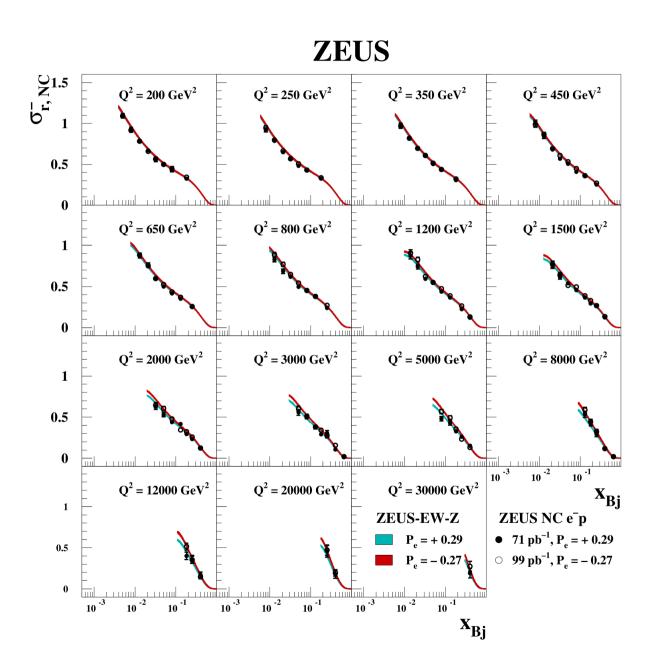


Fig. 5

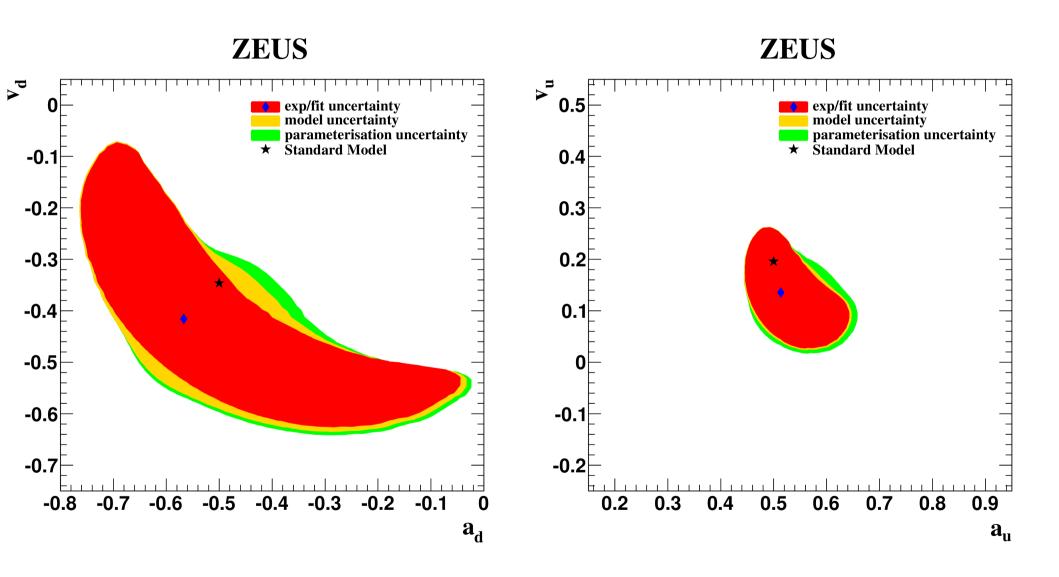
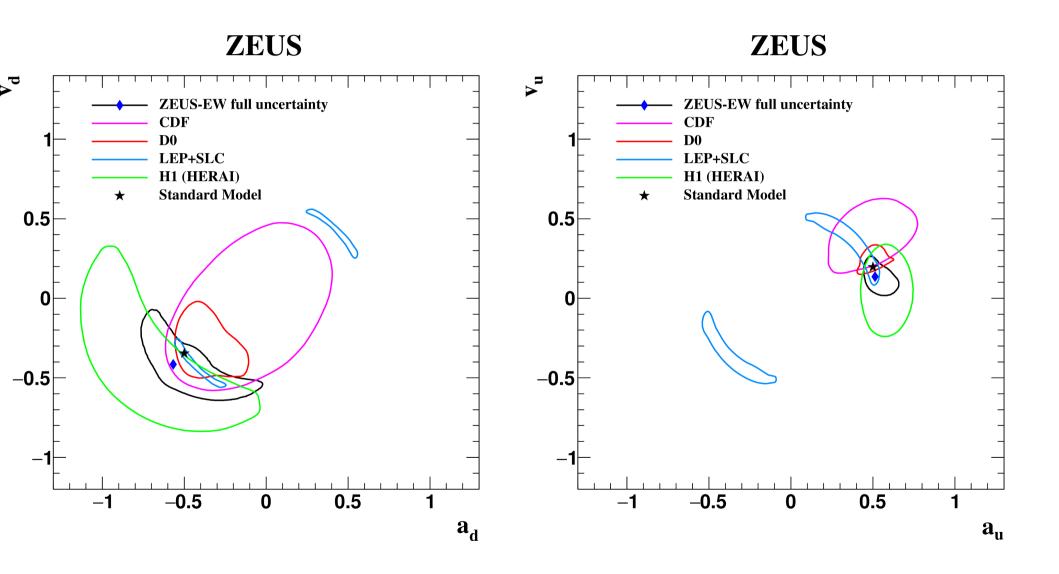


Fig. 6



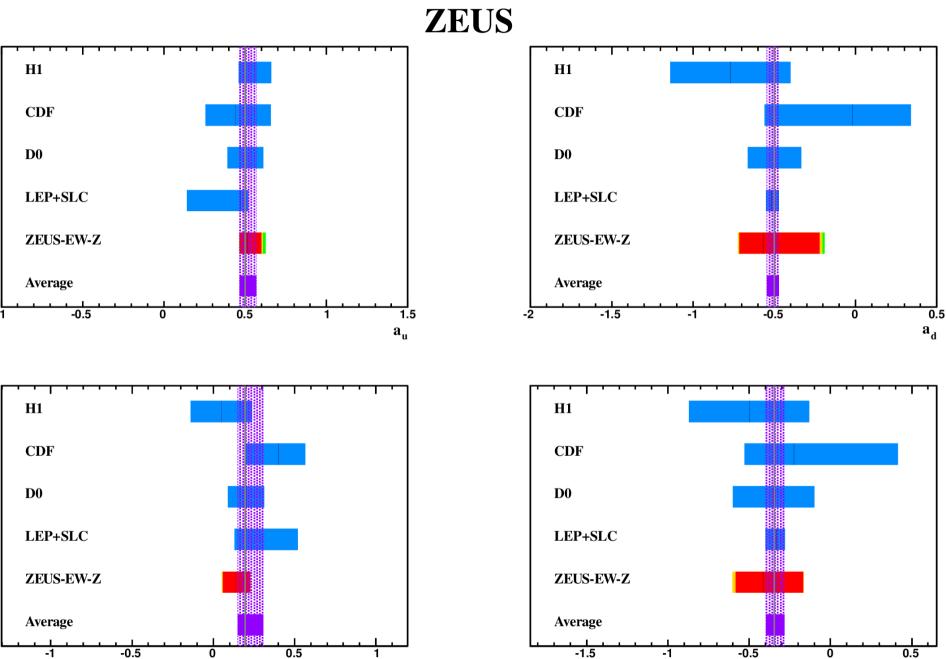
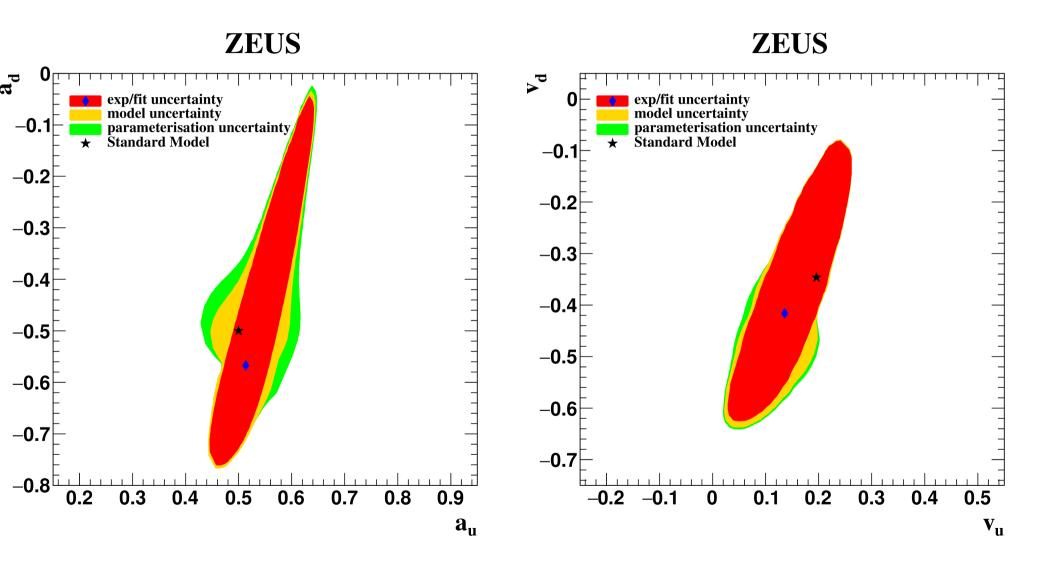
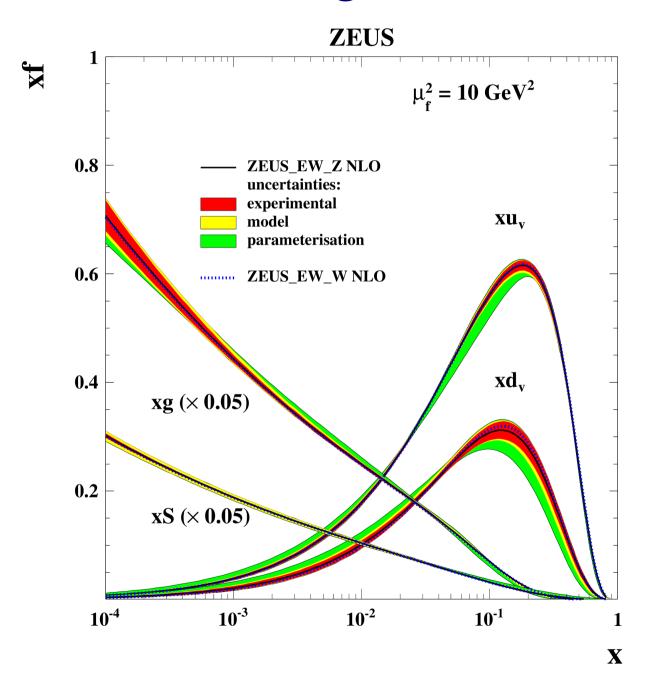
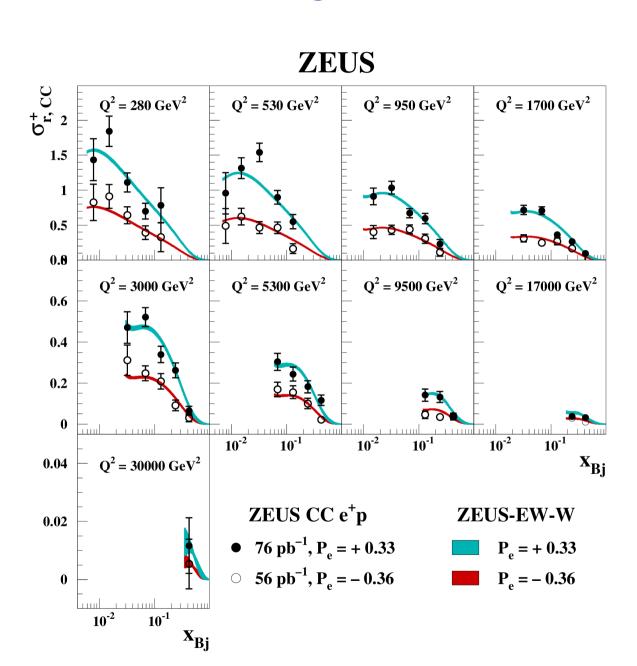
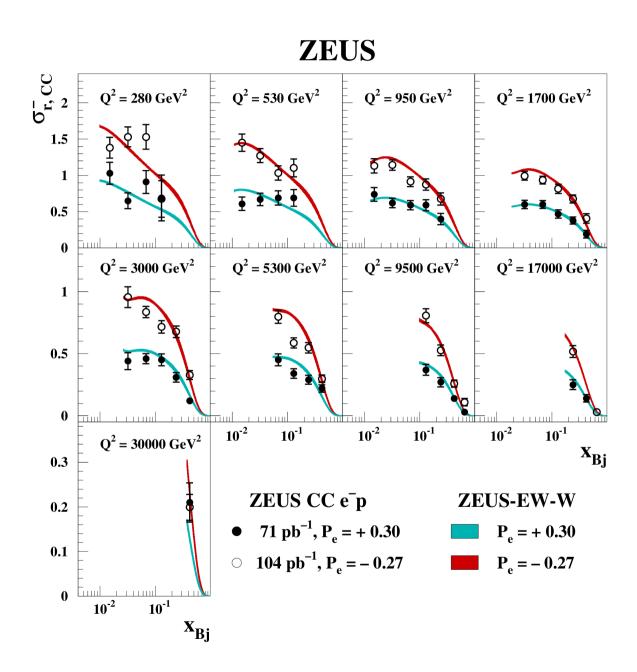


Fig. 8









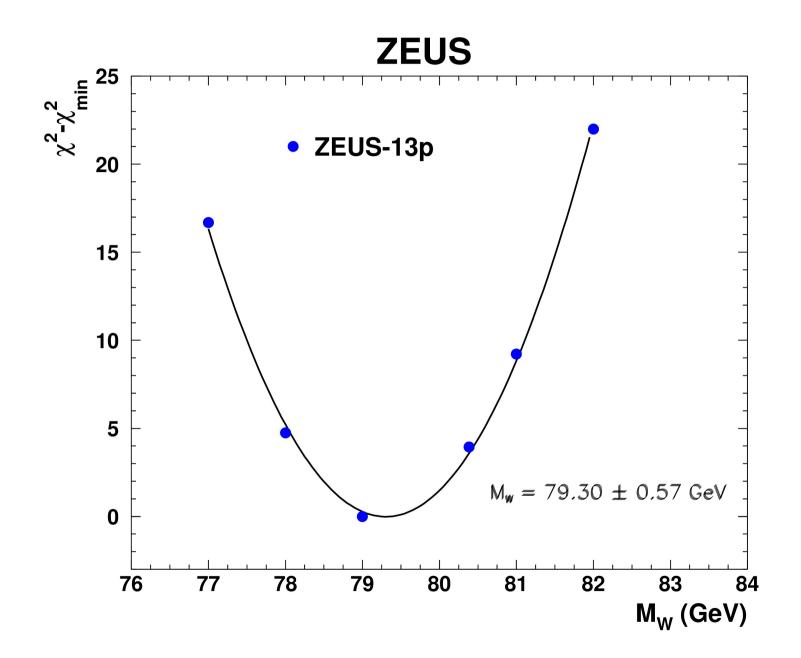


Fig. 13

ZEUS

