

# Freiburg Lectures 2016

Graduiertenkolleg "Mass and Symmetries after the  
Discovery of the Higgs Particle at the LHC"

## Tracking and Tracking Detectors

Norbert Wermes  
University of Bonn



## Lecture 1

### Tracking

- momentum measurement
- vertex measurement
- influence of multiple scattering
- errors and what to do ...

## Lectures 2 & 3 & 4

### Tracking Detectors

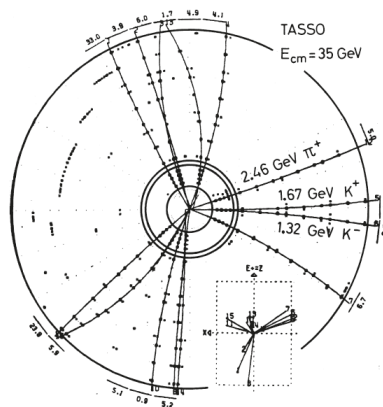
- the signal and the noise
- spatial resolution with structured electrodes
- gaseous detectors
- semiconductor detectors
- pixel detectors ... status and future

# Freiburg Lectures 2016

Graduiertenkolleg "Mass and Symmetries after the  
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## Lecture 2

### Tracking Detectors (Gas)



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universität**bonn**

**SI** **LAB**  
Silizium Labor Bonn

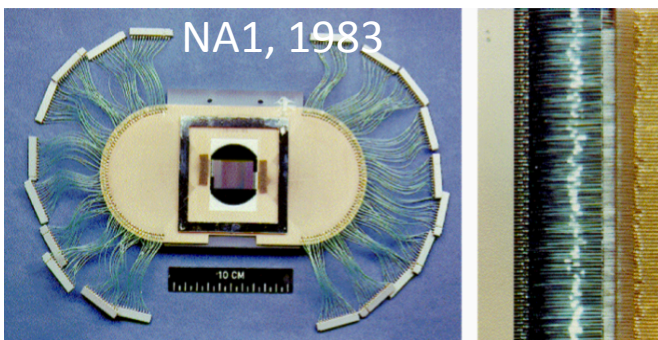
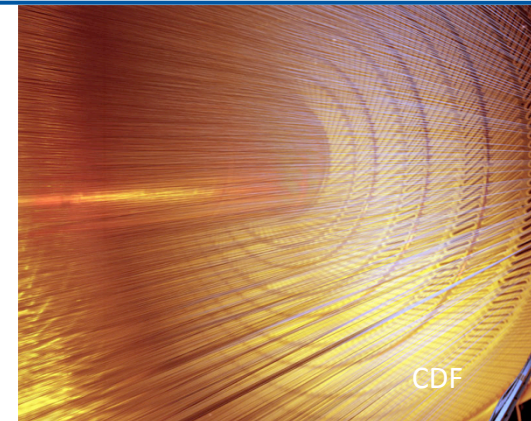
- ❑ Main used trackers: gas-filled or Si
  - commonalities and differences
- ❑ How the signal develops
  - Shockley-Ramo theorem
  - **Weighting fields in**
    - parallel (w/o and w/ space charge)
    - cylindrical
    - patterned
  - electrode configurations
- ❑ Gas amplification in gaseous detectors
- ❑ Diffusion and drift (short)
- ❑ Motion in E and B (short)
- ❑ **Space resolution** w/ patterned electrodes
  - binary
  - centroid
  - eta - method
- ❑ gas-filled detector types
  - operation modes
  - **avalanche – streamer – spark**
  - the magic of gases
  - ageing of gas filled wire chambers
  - cathode readout
  - stereo readout
- ❑ drift chambers
  - drift cells
  - stereo R/O
- ❑ Time Projection Chambers
- ❑ **New developments for LHC**
  - MPGDs
    - MSGC
    - GEM
    - Micromegas
  - RPCs





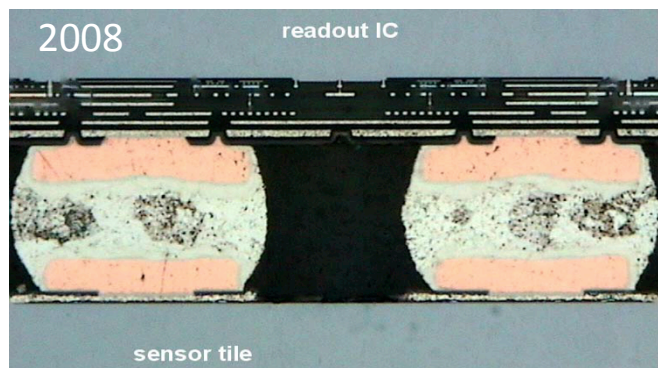
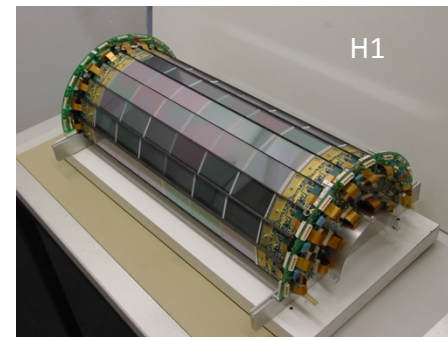
## Wire chambers

- electronic recording of particle tracks
- electronic recording of tracks
- $\sigma = \text{mm} \rightarrow 50 \mu\text{m}$ ,  
0.05 channels /  $\text{cm}^2$



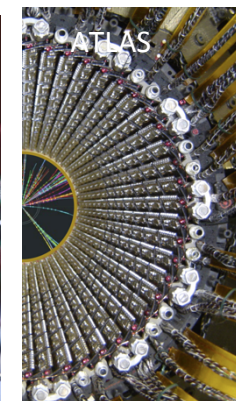
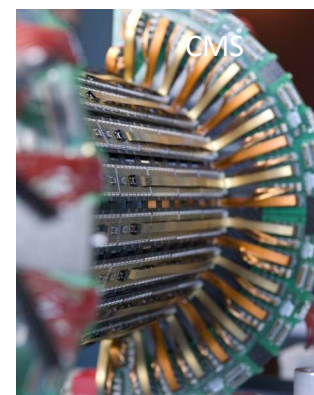
## Silicon strip detectors

- measurement of ps – lifetimes and heavy quark “tagging”
- $\sigma < 5 \mu\text{m}$ , 50 channels /  $\text{cm}^2$

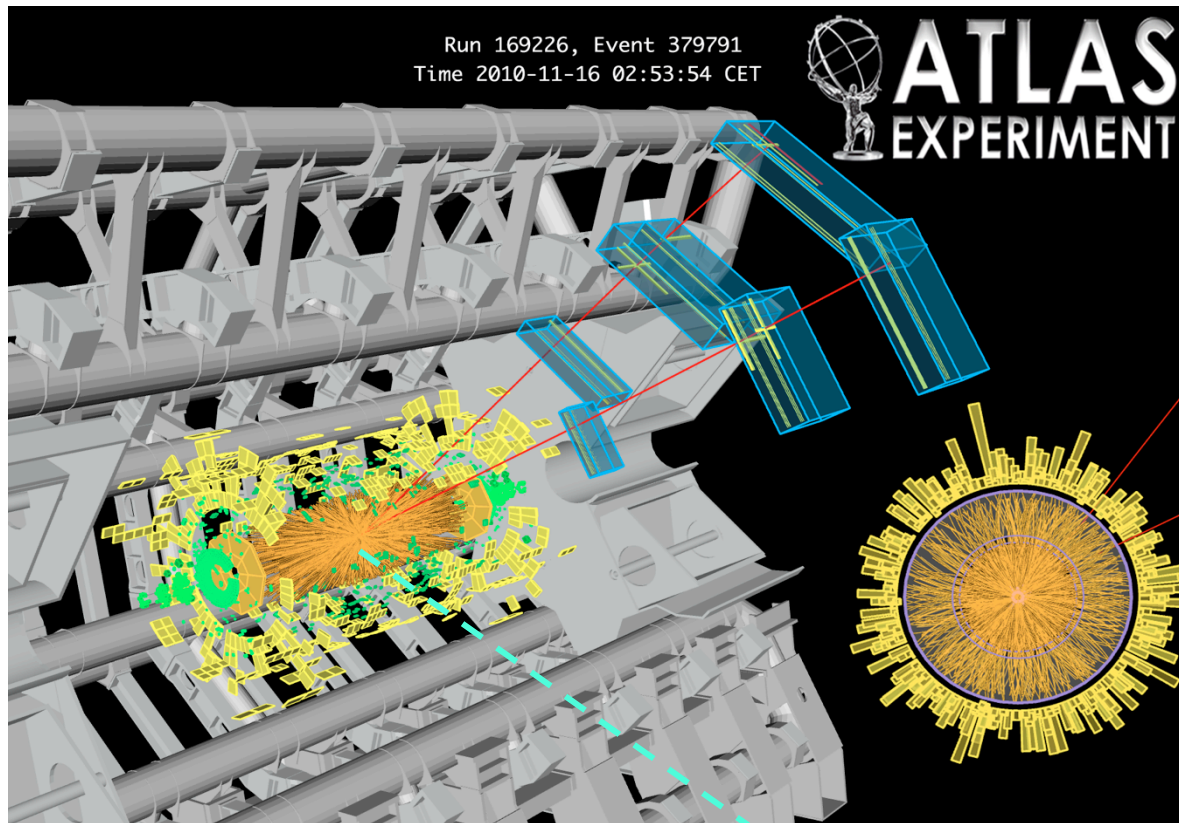


## Pixel detectors

- 3-dim point measurement in **high rate** environments like LHC
- $\sigma \sim 10 \mu\text{m} \rightarrow 2 \mu\text{m}$ ,
- 10 000 channels /  $\text{cm}^2$



# Tracking in pp collisions at 13 TeV (LHC)



$\sim 1200$  tracks every 25 ns  
or  $\sim 10^{11}$  per second

$\Rightarrow$  high radiation dose

$10^{15} n_{eq} / \text{cm}^2 / 10 \text{ yrs @ LHC}$

or

600 kGy (60 Mrad)  
through ionisation of particles

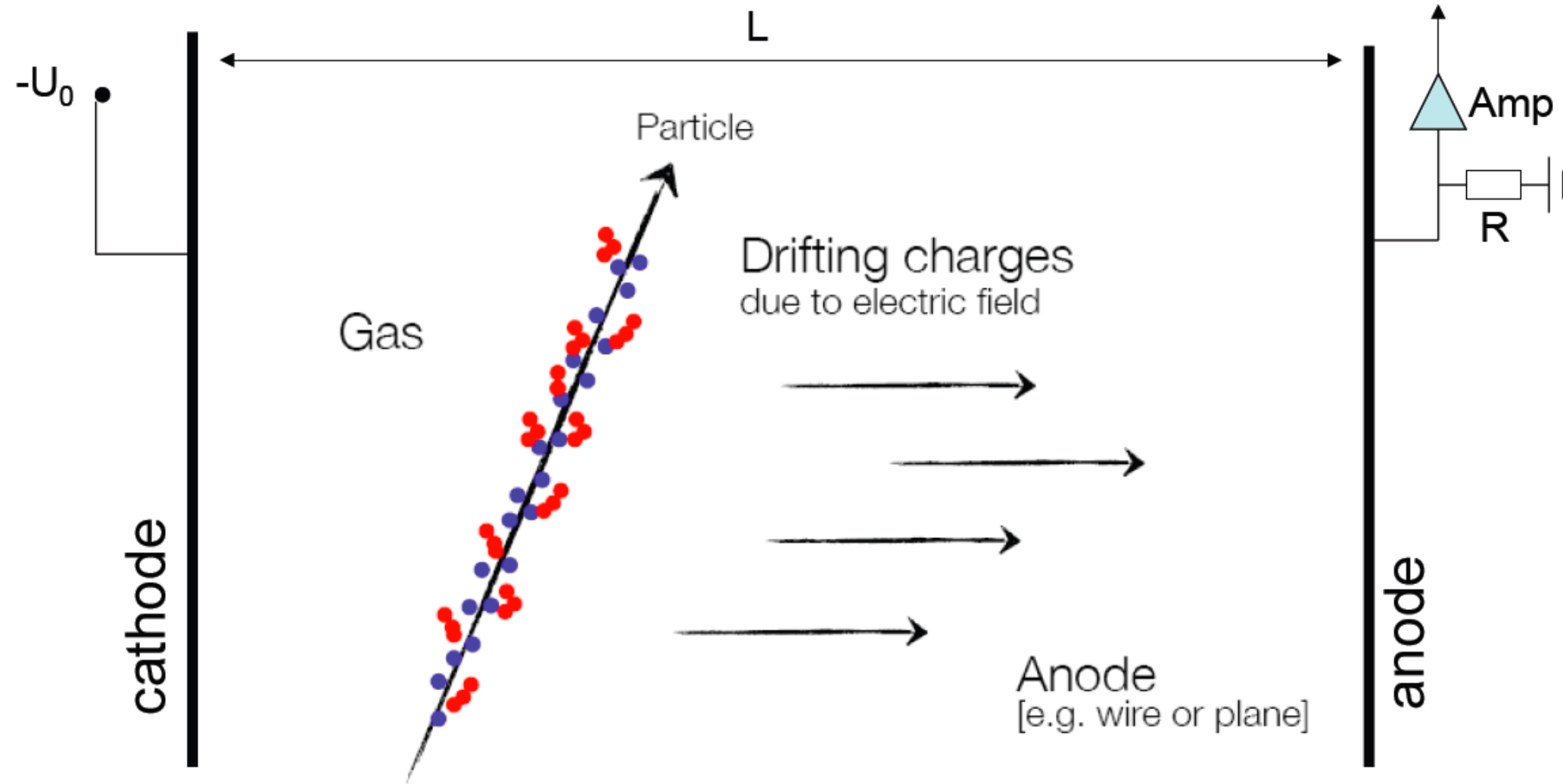
position of  
tracking detector (pixels, strips, straw tubes)

## DEMANDS

$\text{LHC} \cong 10^6 \times \text{LEP}$  in track rate !

Note: LHC Upgrade (2026): HL-LHC  $\approx$  LHC  $\times 10$  !

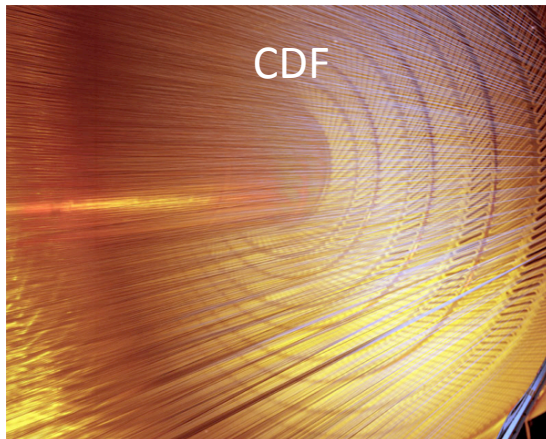
# Most tracking detectors are **ionization** detectors



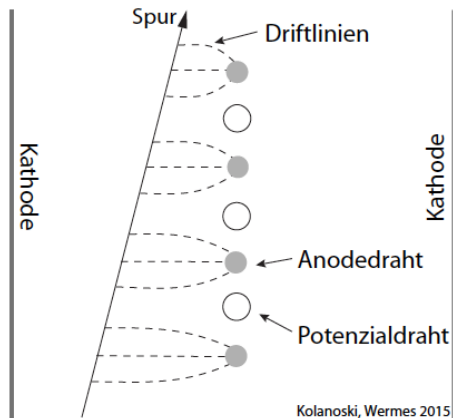
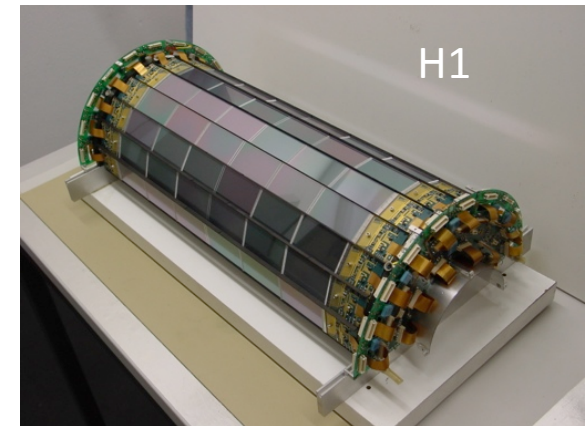
- Primary Ionization
- Secondary Ionization (due to  $\delta$ -electrons)



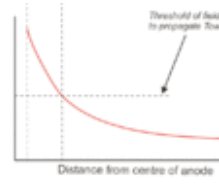
# For trackers: gas-filled and semiconductor detectors



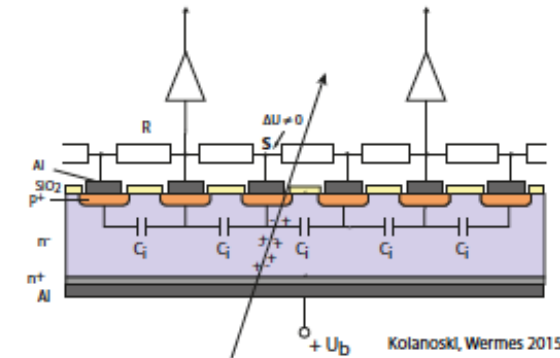
++	material	-
+	$N_{\text{meas}}$	--
low	cost	high
--	rate/speed	++
100 $\mu\text{m}$	resolution	10 $\mu\text{m}$



field near wire  
 $E(r) \sim 1/r$



$\Rightarrow$  gas amplification

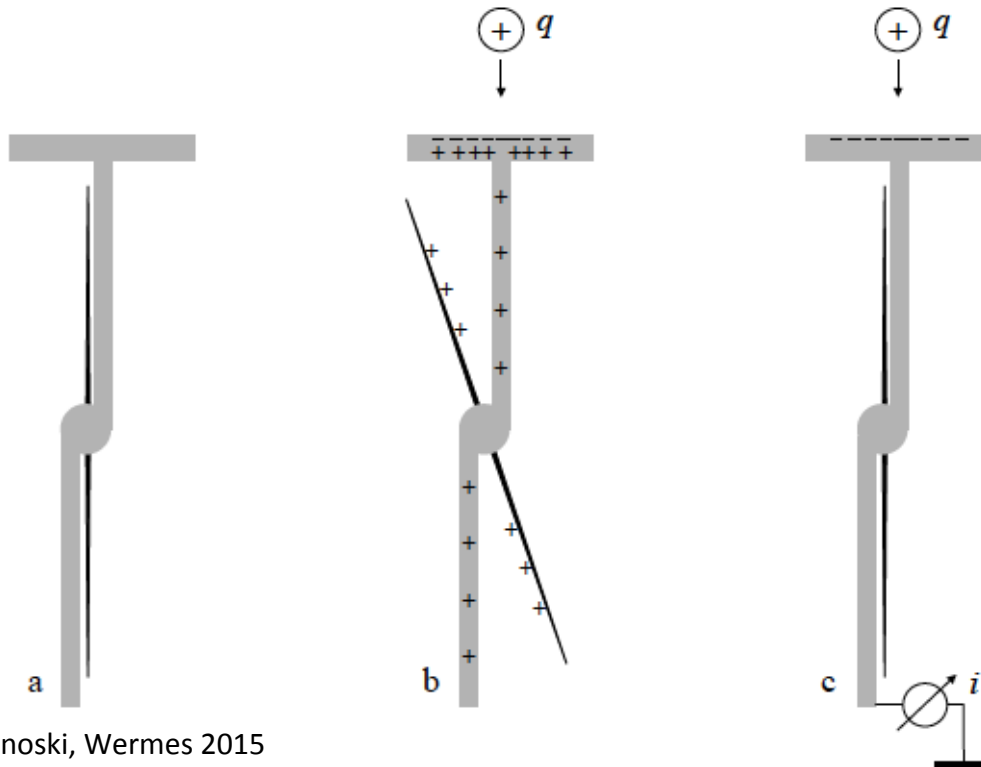


linear  $E$

**26 eV needed (Ar)** per e/ion pair  
**94 e/ion pairs per cm**  
intrinsic amplification **typ.  $10^5$**   
typ. noise: > 3000 e- (ENC)

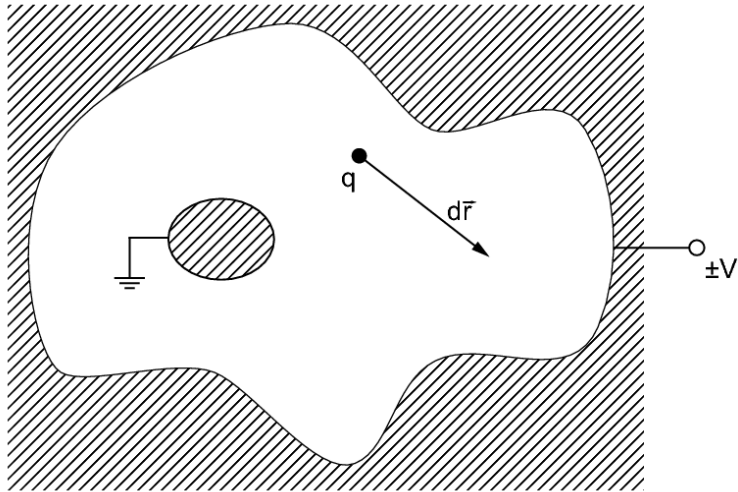
**3.65 eV (Si)** needed per e/h pair  
 **$\sim 10^6$  e/h** pairs per cm (20 000/250 $\mu\text{m}$ )  
no intrinsic amplification  
typ. noise: 100 e- (pix) to 1000 e- (strip)

by “electrostatic induction” (influence electrique, elektrische Influenz)



Kolanoski, Wermes 2015

a current is  
generated



how does a moving charge couple to an electrode ?

- respect Gauss' law and find

## Shockley- Ramo theorem

(Shockley J Appl.Phys 1938, Ramo 1939)

**weighting field**

determines how charge movement couples to a specific electrode

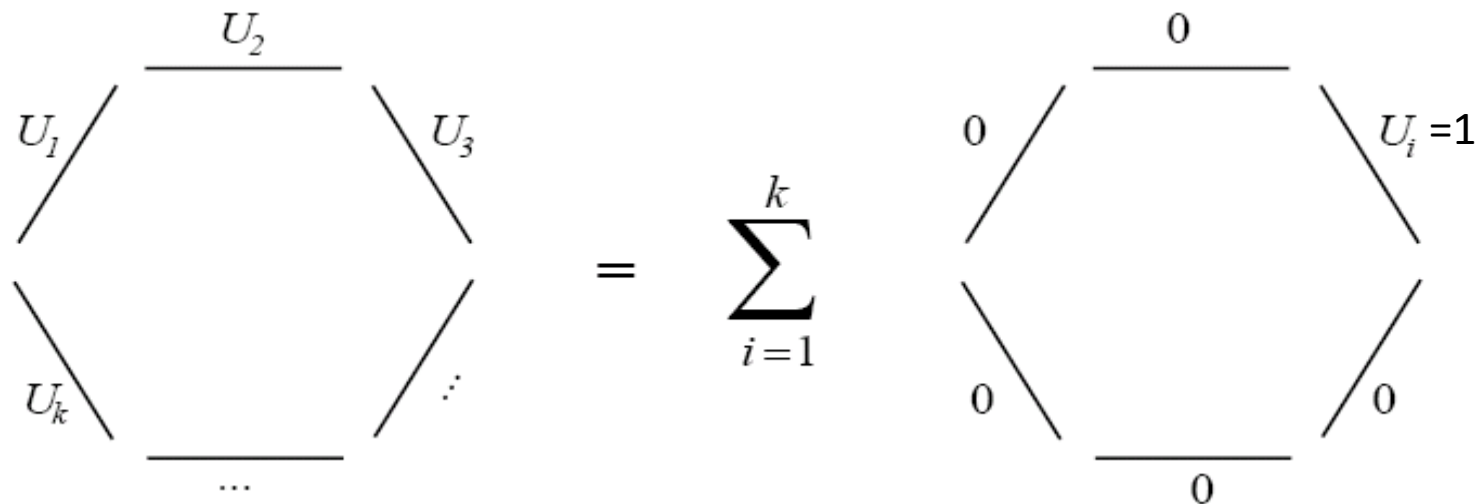
$$i_S = -\frac{dQ}{dt} = q \vec{E}_w \vec{v}$$

$$dQ = q \vec{\nabla} \Phi_W d\vec{r}$$

**induction (weighting) potential**

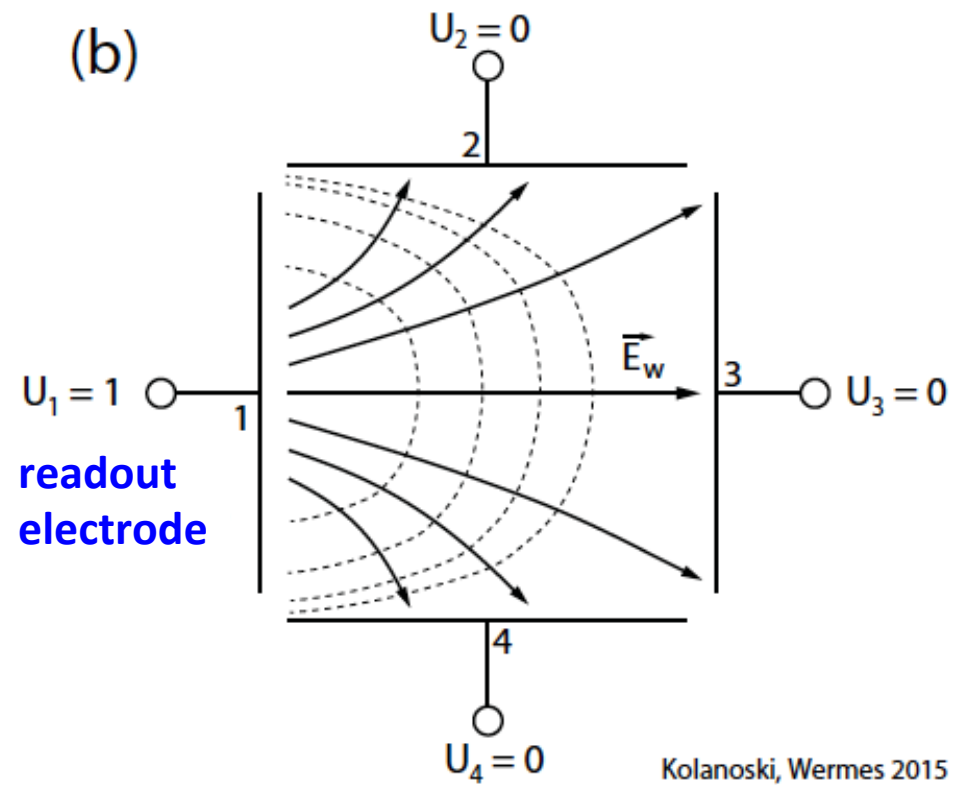
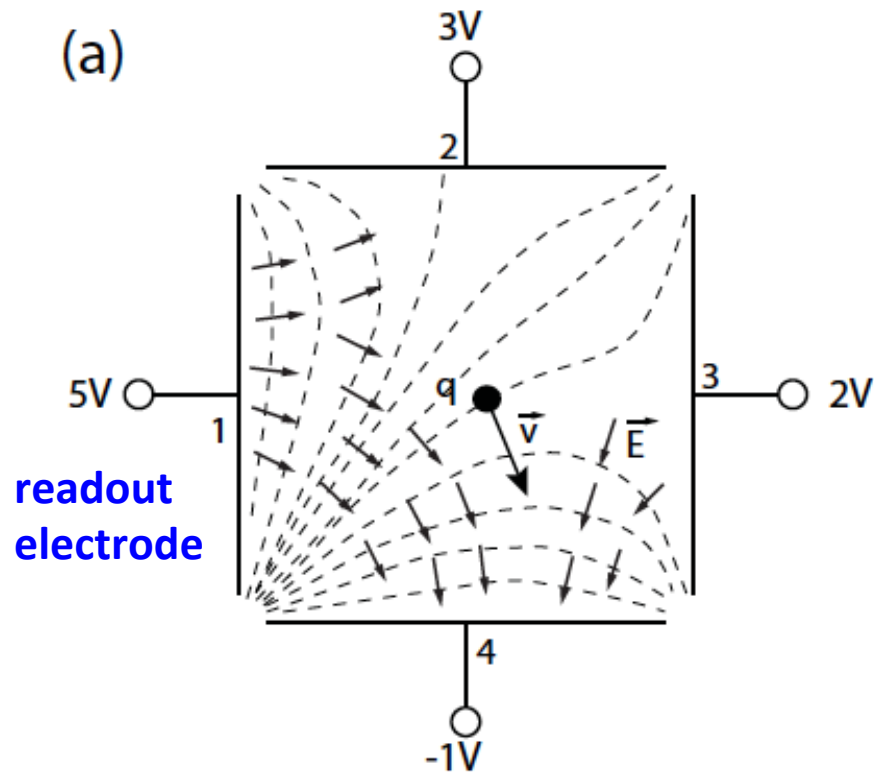
determines how charge movement couples to a specific electrode

# Ramo Theorem in a many electrode configuration



$$dQ_i = -q \vec{E}_{w,i} d\vec{r}$$

**Recipe:** To compute the weighting field of a readout electrode  $i$ , set voltage of electrode  $i$  to 1 and all other electrodes to 0.



Kolanoski, Wermes 2015

$$i_S = -\frac{dQ}{dt} = q \vec{E}_w \vec{v}$$

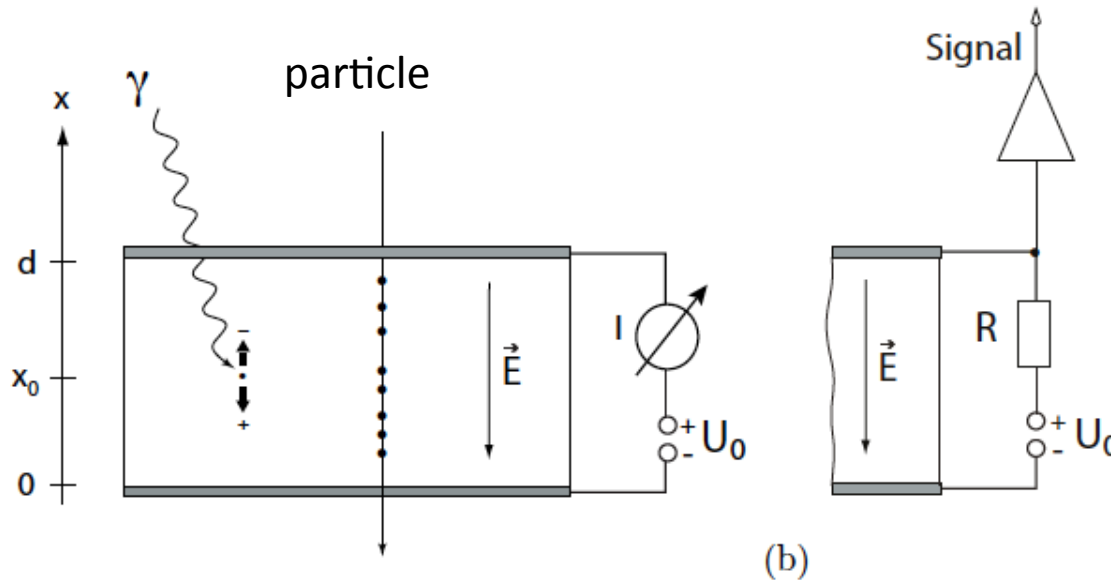


# A detector is a **current source**

delivers a current pulse  
independent of the load

one can convert current into  
charge (integral) or voltage (via R or C)

# A parallel plate detector (capacitor)

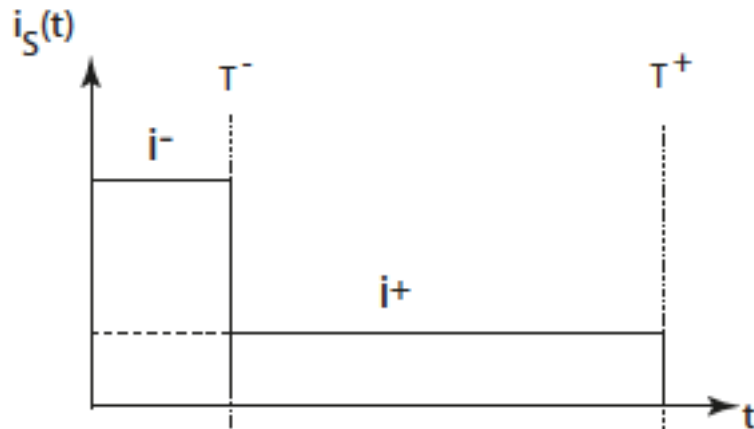


$$\vec{E} = -\frac{U_0}{d} \vec{e}_x ; \quad C = \frac{\epsilon \epsilon_0 A}{d}$$

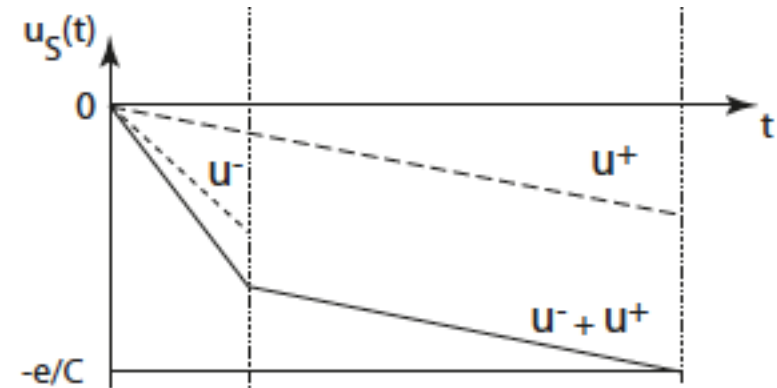
- constant E-field
- almost constant velocity ( $v = \mu E$ )
- weighting field simple

$$dQ = -q \frac{\vec{E}_0}{U} d\vec{r}. \quad \vec{E}_w = -\frac{1}{d} \vec{e}_x$$

Kolanoski, Wermes 2015

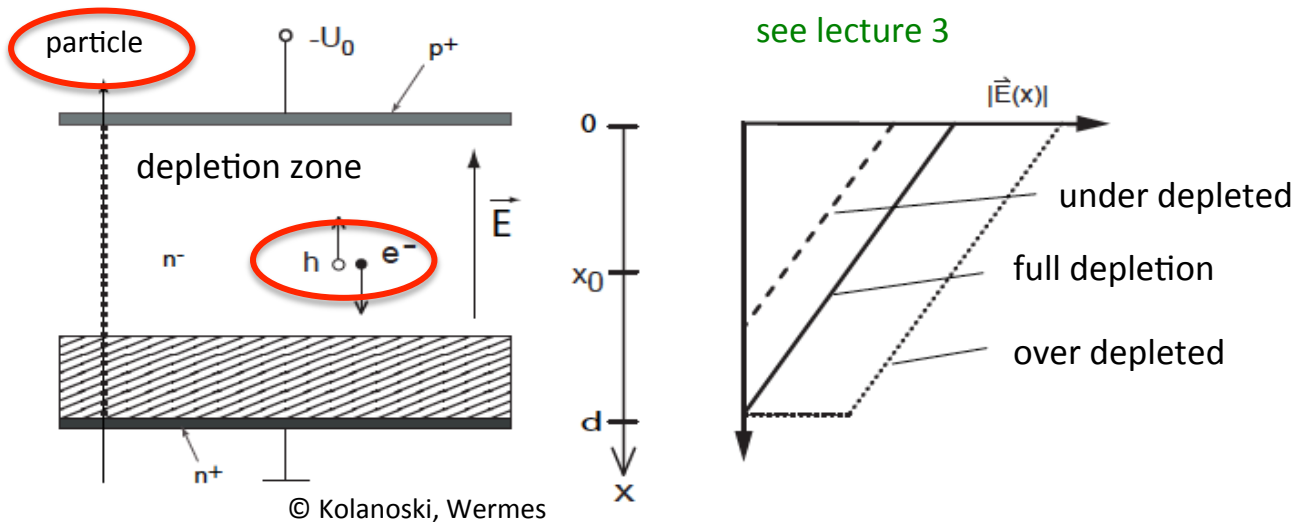


$$i_S^\pm = q^\pm \vec{E}_w \vec{v}^\pm = -\frac{q^\pm}{d} \vec{e}_x \vec{v}^\pm = \frac{e}{d} v^\pm$$



$$Q_S^{tot} = Q_S^- + Q_S^+ = -\frac{e}{d} \left( \int_0^{T^-} v^- dt + \int_0^{T^+} v^+ dt \right) = -\frac{e}{d} v^- \left( \frac{d - x_0}{v^-} \right) - \frac{e}{d} v^+ \left( \frac{x_0}{v^+} \right) = -e.$$

# Signal in a Silicon detector (= parallel plate w/ space charge)



- E-field not constant
- velocity not constant
- weighting field still the same

$$\vec{E}_w = -\frac{1}{d}\vec{e}_x$$

$$E(x) = -\left[\frac{2U_{dep}}{d^2}(d-x) + \frac{U - U_{dep}}{d}\right] = -\left[\frac{U + U_{dep}}{d} - \frac{2U_{dep}}{d^2}x\right] = -(a - bx)$$

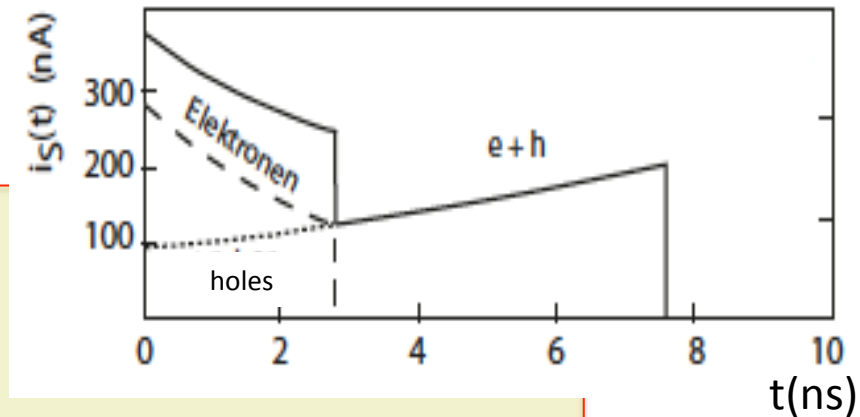
$$v_e = -\mu_e E(x) = +\mu_e (a - bx) = \dot{x}_e$$

$$v_h = +\mu_h E(x) = -\mu_h (a - bx) = \dot{x}_h$$

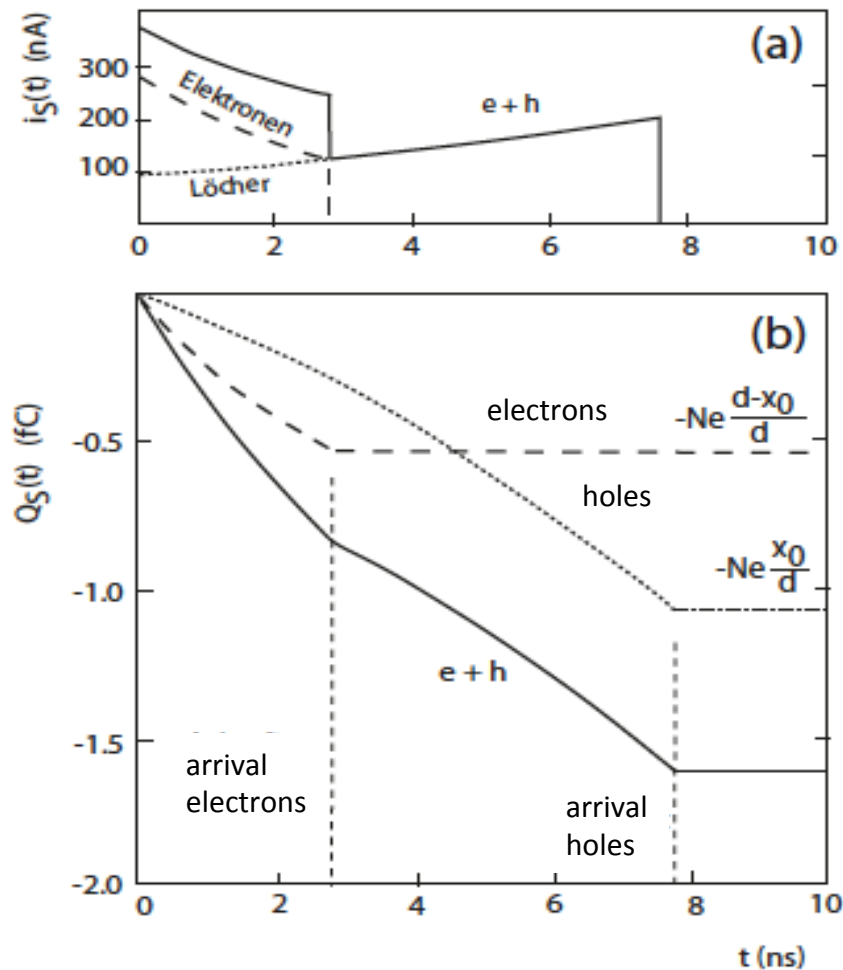
$$i_S(t) = i_S^e(t) + i_S^h(t)$$

$$= -\frac{e}{d} \left( \frac{2U_{dep}}{d^2} x_0 - \frac{U + U_{dep}}{d} \right)$$

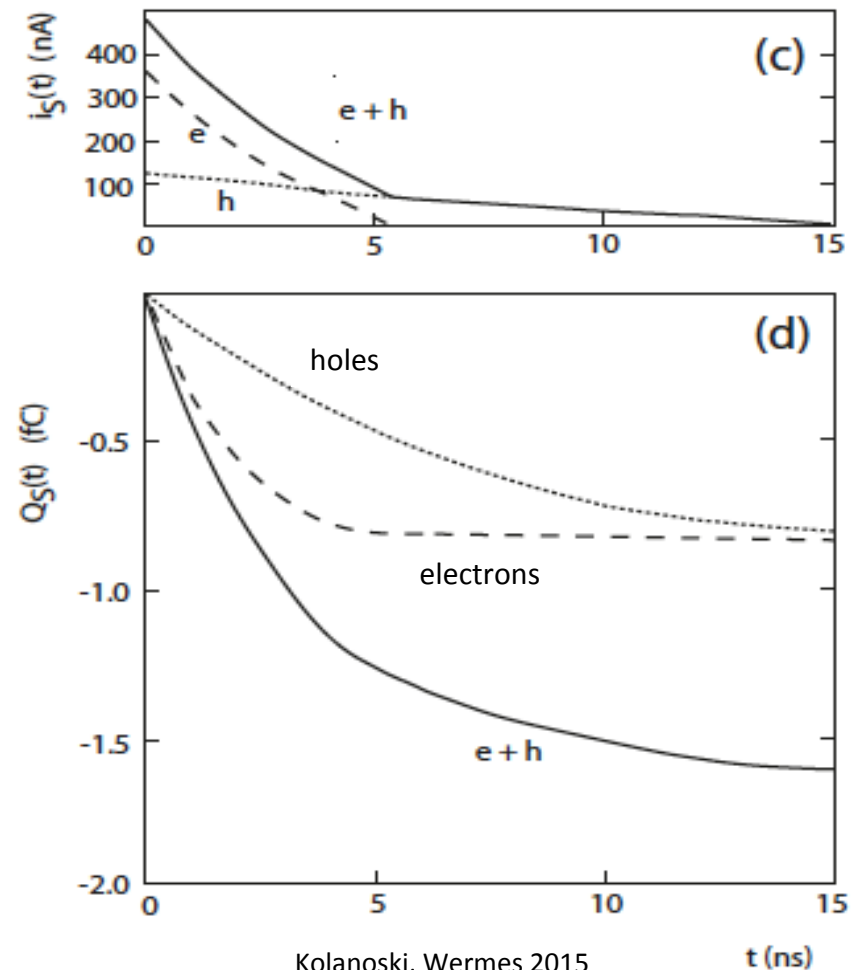
$$\times \left\{ \mu_e \exp\left(-2\mu_e \frac{U_{dep}}{d^2} t\right) \Theta(T^- - t) - \mu_h \exp\left(+2\mu_h \frac{U_{dep}}{d^2} t\right) \Theta(T^+ - t) \right\}$$



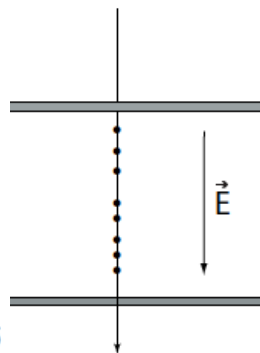
point charge



charged particle track



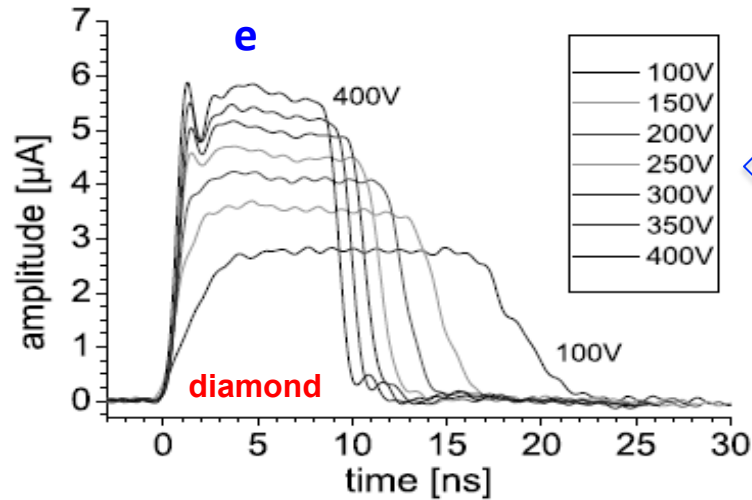
particle



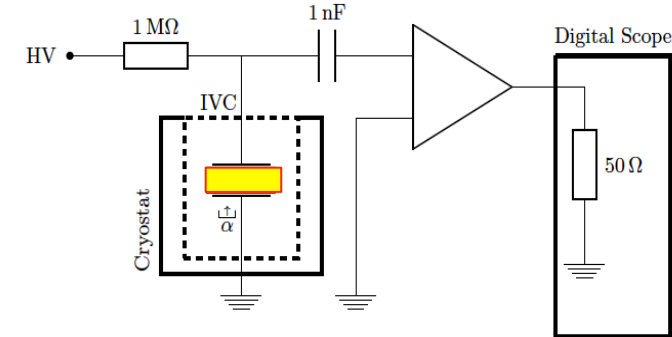
Kolanoski, Wermes 2015

$t$  (ns)

# Current pulse measurements: TCT technique

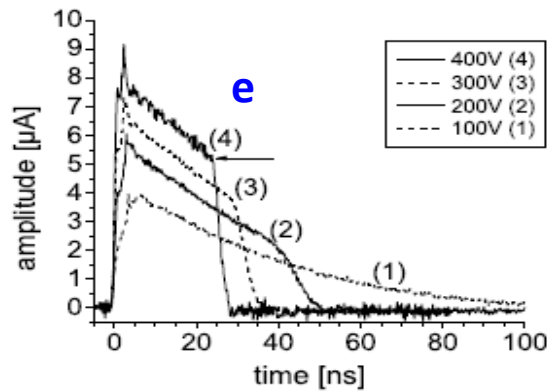


single crystal **diamond** is like a parallel plate detector filled with a dielectric w/o space charge

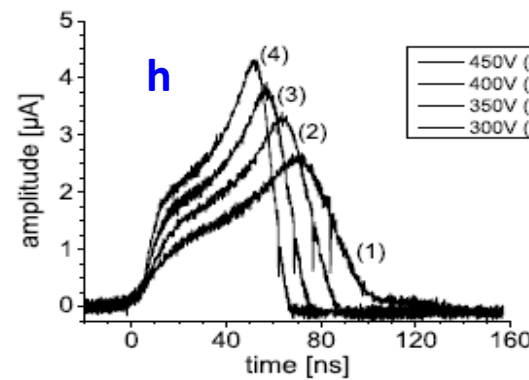


1mm pn – Diode **silicon**

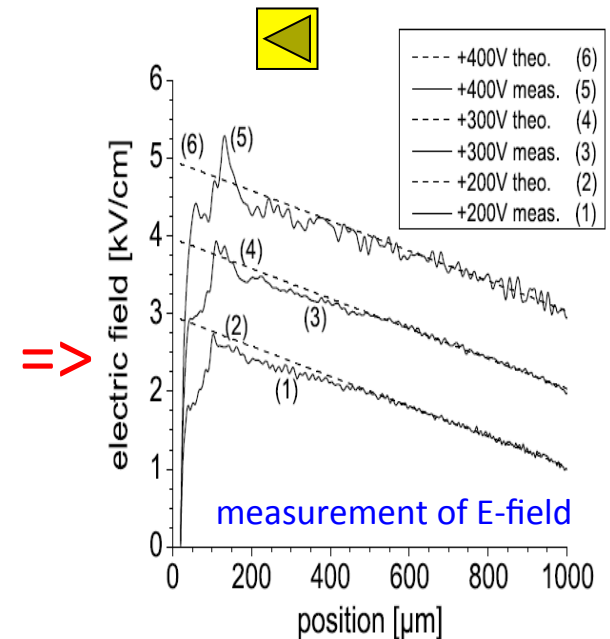
- same weighting field
- different electric field

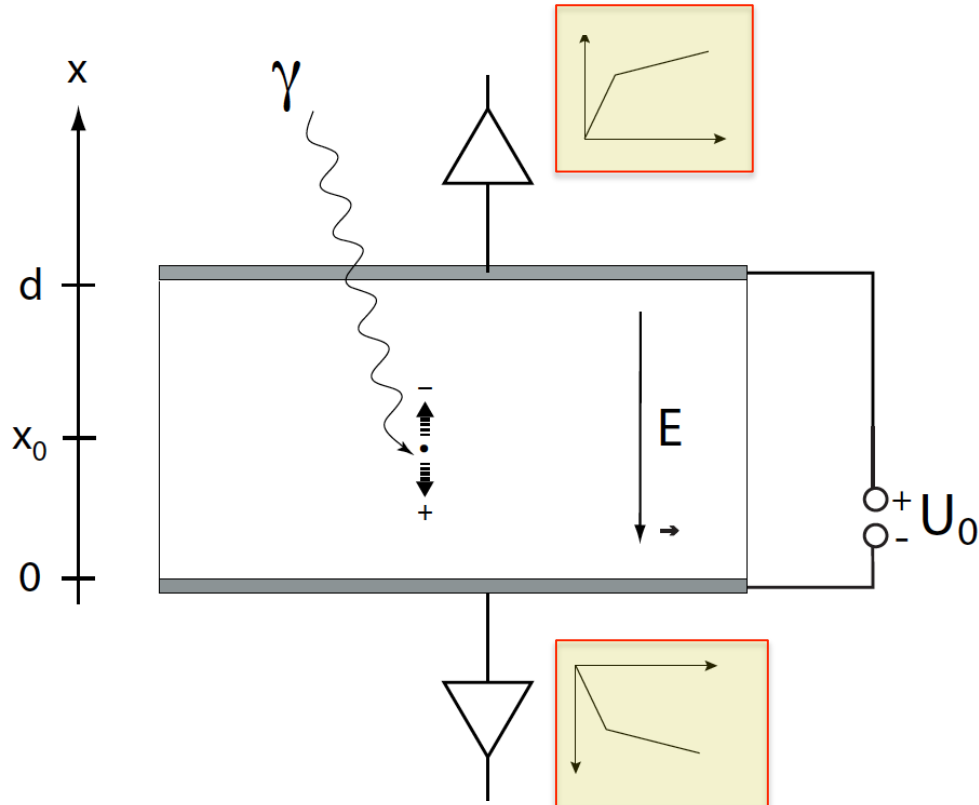


(a) Electron signals from  $\alpha$ -particles impinging on the cathode.



(b) Hole signals from  $\alpha$ -particles impinging on the anode.



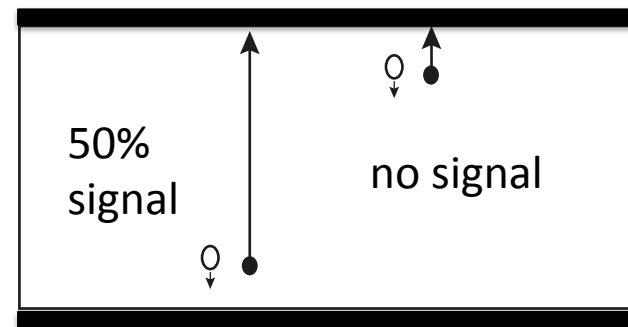


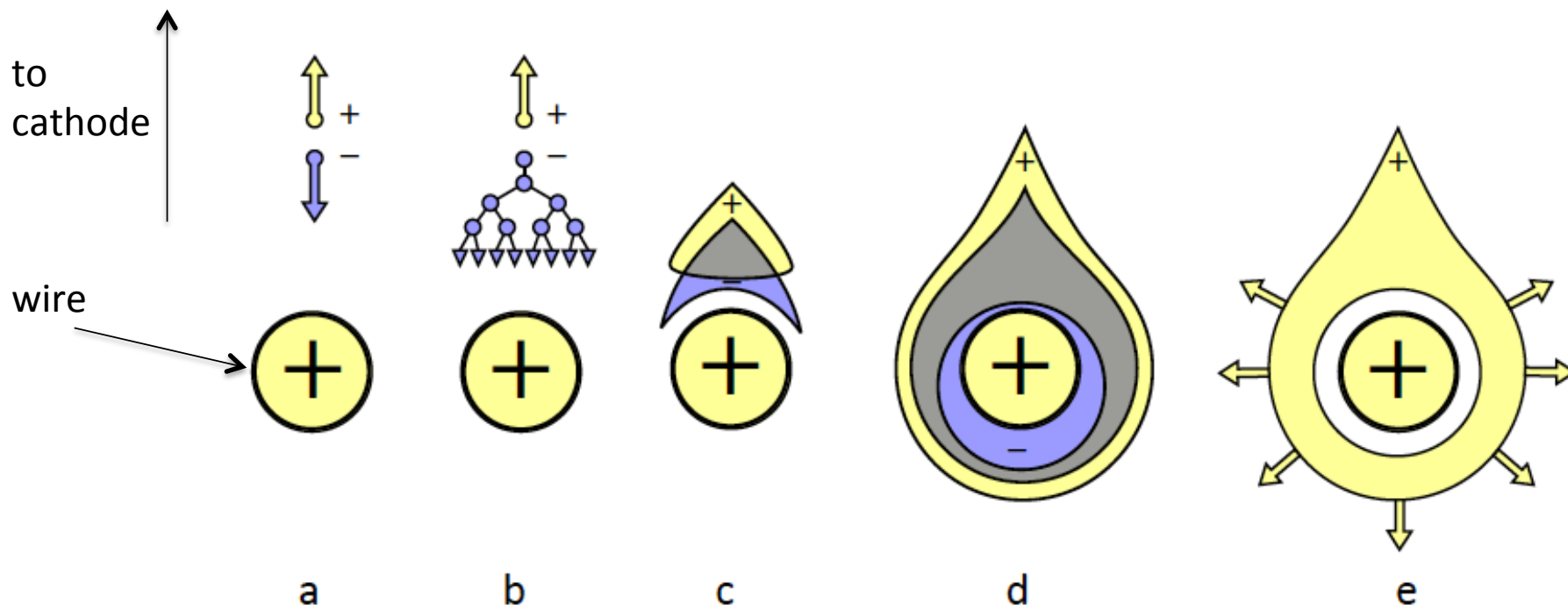
- movement of **both charges** create signals on **both electrodes**.
- on every electrode a **total charge** of

$$Q_S^{tot} = Q_S^- + Q_S^+ = -Ne$$

is induced.

- if a material the produced charges have very different mobilities (like **CdTe**) e.g. with  $\mu_h \approx 0$ , then part of the signal is lost and the signal becomes dependent on where the charge was deposited.





**big difference:**

- ❑ electrode (wire) does not “see” (too small) the charge before gas amplification
- ❑ signal (on wire) shape is governed by the (large) ion cloud moving away from the wire to cathode

**Avalanche process:**

$$dN = \alpha(E) N ds$$

with

$$N(x) = N_0 e^{\alpha x}$$

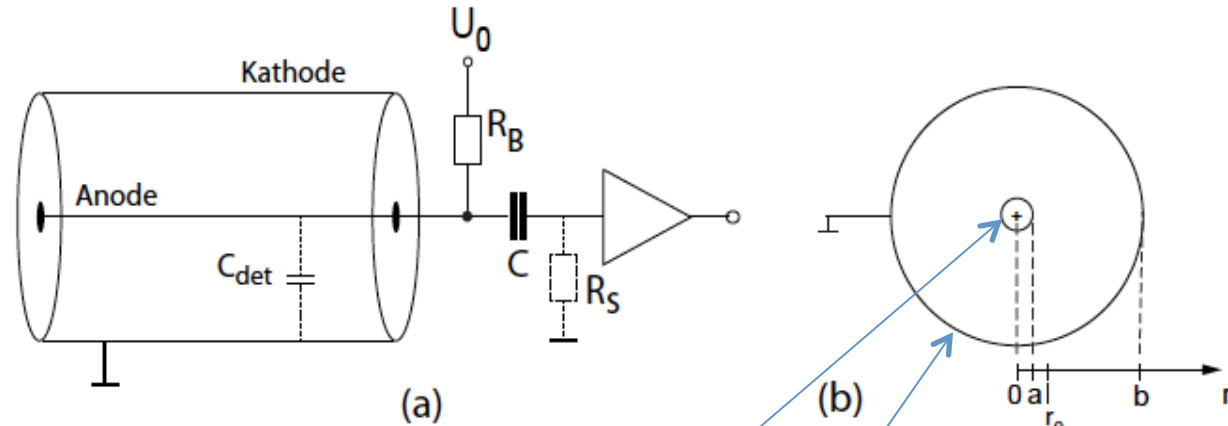
**gas gain**

$$\frac{N}{N_0} = G = e^{\alpha x}$$

$$\alpha = \sigma_{ion} n = \frac{1}{\lambda_{ion}}$$

**1<sup>st</sup> Townsend coefficient**

configuration



$$\vec{E}(r) = \frac{1}{r} \frac{U_0}{\ln b/a} \frac{\vec{r}}{r}, \quad \phi(r) = -U_0 \frac{\ln r/b}{\ln b/a}, \quad C_l = \frac{2\pi\epsilon_0}{\ln b/a}.$$

- we follow our Shockley-Ramo-recipe: find the weighting field  $E_w$  or the weighting potential  $\Phi_w$  by setting

$$\phi_w(a) = 1, \quad \phi_w(b) = 0. \quad (*)$$

- we know already the shape of  $\Phi_w \sim \ln r$ , since  $E(r) \sim 1/r$
- hence

$$\vec{E}_w(r) = \frac{1}{r} \frac{1}{\ln b/a} \frac{\vec{r}}{r}, \quad \phi_w(r) = -\frac{\ln r/b}{\ln b/a}$$

which fulfils (\*)



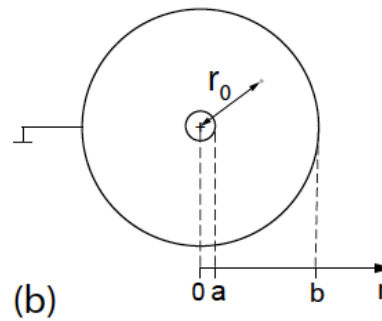
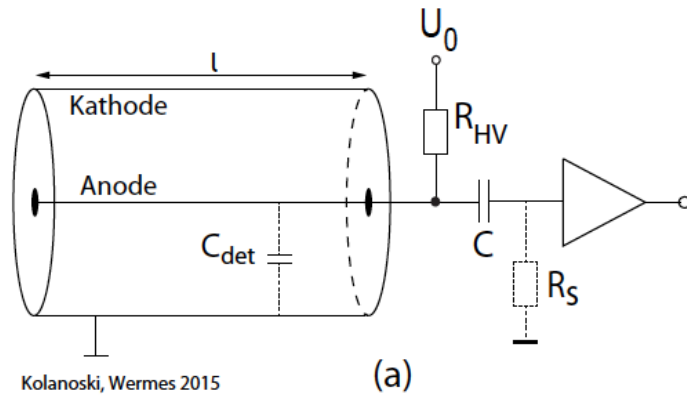
- now use Shockley-Ramo  $dQ_S = -q\vec{E}_w d\vec{r}$
- we assume that  $N$  e/ion-pairs are produced at  $r = r_0$ . Note that, **if there is avalanche amplification** (starting only in the high field region) the vast majority of charges is produced very close to the wire ( $r_0 < 10 \mu\text{m}$ , see previous page)

- then we get immediately

$$\begin{aligned} Q_S^- &= -(-Ne) \frac{1}{\ln b/a} \int_{r_0}^a \frac{1}{r} dr = -Ne \frac{\ln r_0/a}{\ln b/a} \\ Q_S^+ &= -(+Ne) \frac{1}{\ln b/a} \int_{r_0}^b \frac{1}{r} dr = -Ne \frac{\ln b/r_0}{\ln b/a} \end{aligned} \quad (**)$$

- and the total charge is  $Q_S^{\text{tot}} = Q_S^- + Q_S^+ = -Ne$  ✓  
**however**, due to the  $1/r$  dependence of the weighting field the situation is **much different** from that of a parallel plate detector: the contribution from electrons and ions is not necessarily the same but depends on  $r_0$  (i.e where the avalanche is created, because only there  $N$  becomes large enough that the signal is “felt” by the electrode (wire).

# Signal development in a wire configuration (3)



ratio depends on  $r_0$

$$\left( \frac{Q_S^-}{Q_S^+} \right)_{r_0} = \frac{\ln r_0 / a}{\ln b / r_0}$$

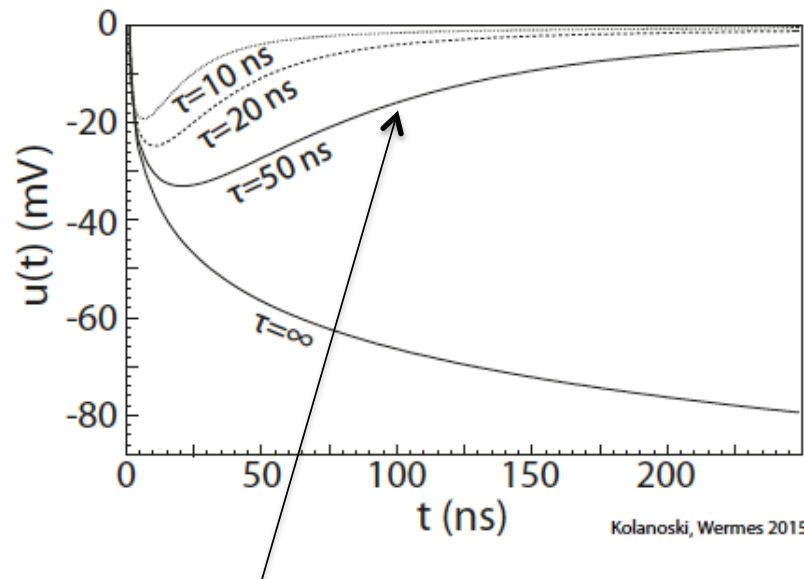
for a typical ( $a=10 \mu\text{m}$ ,  $b=10 \text{ mm}$ )

far away  
from wire

near wire

$$\left( \frac{Q_S^-}{Q_S^+} \right)_{r_0=b/2} \approx 9$$

$$\left( \frac{Q_S^-}{Q_S^+} \right)_{r_0=a+\epsilon} \approx 0.01 - 0.02$$



in wire chambers the (integrated) **signal is dominated by the ion contribution**. Reason: specific form of the weighting field

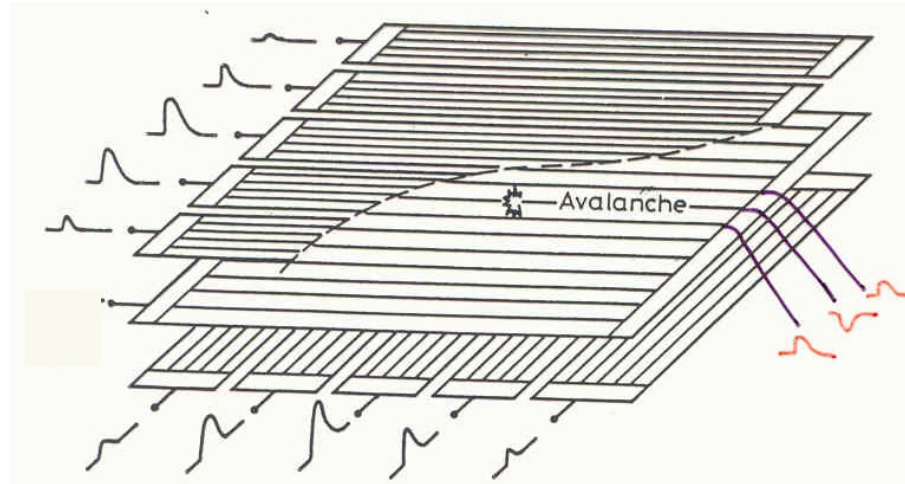
using Ramo and  $r(t)$  from the  $1/r$  - E-field, we get ...

$$i_S^+(t) = \frac{Ne}{2 \ln b/a} \frac{1}{t + t_0^+} \quad \text{ions only}$$

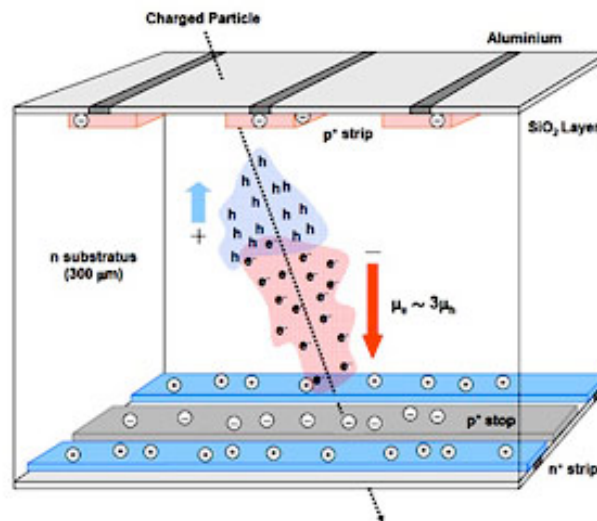
$$u_s(t) = \frac{Q_S(t)}{C_l l} = -\frac{Ne}{2\pi\epsilon_0 l} \ln \left( 1 + \frac{t}{t_0^+} \right)$$

- ❑ electric field is large close to the wire @  $r \approx r_{\text{wire}}$ 
  - => **secondary ionisation** has a much **larger** effect on signal than **primary ionisation**
  - => **avalanche near wire**:  $q \rightarrow q \times 10^{4-7}$
- ❑ from there ( $\mu\text{m}$ 's away from wire) the electrons reach the wire fast
  - => very **small and fast  $e^-$**  component of  $Q_{\text{tot}}$
- ❑ **ions** move slowly away from wire => **main component of  $Q_{\text{tot}}(t)$**
- ❑ signal only relevant after avalanche ionization  $\cong$  **quasi only  $Q^+(t)$**
- ❑ the term '**charge collection**' is more justified in wire chambers than in other ionisation detectors (e.g. parallel plate detectors) since most of the signal is created only very close to the wire

signals are induced on **BOTH (ALL)** electrodes => exploit for second coordinate readout



wire chamber  
with cathode readout

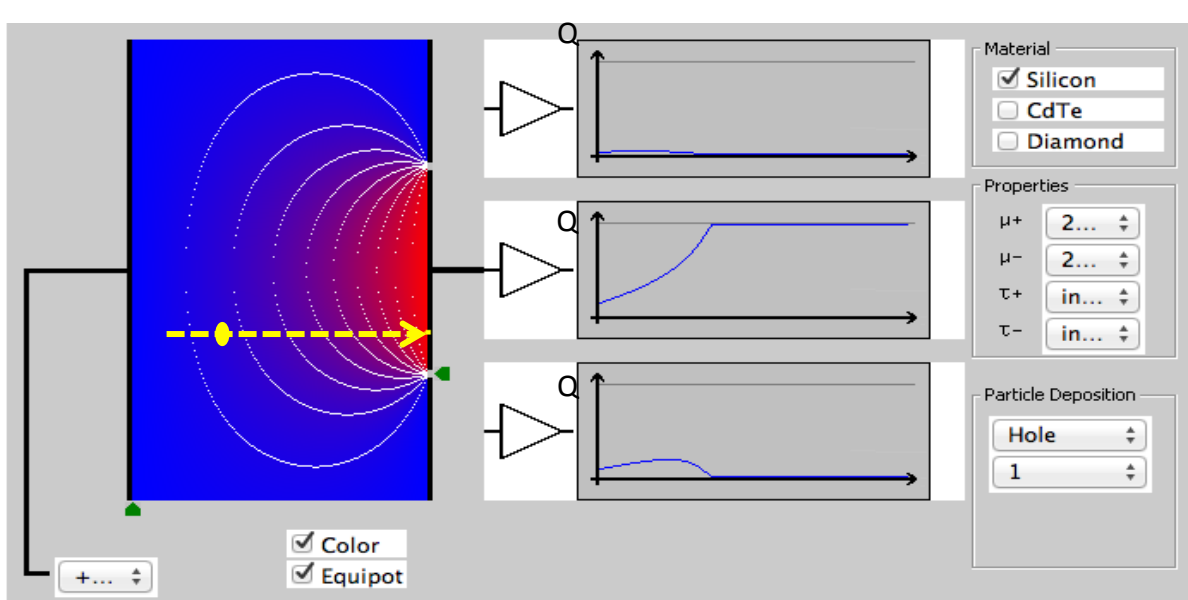
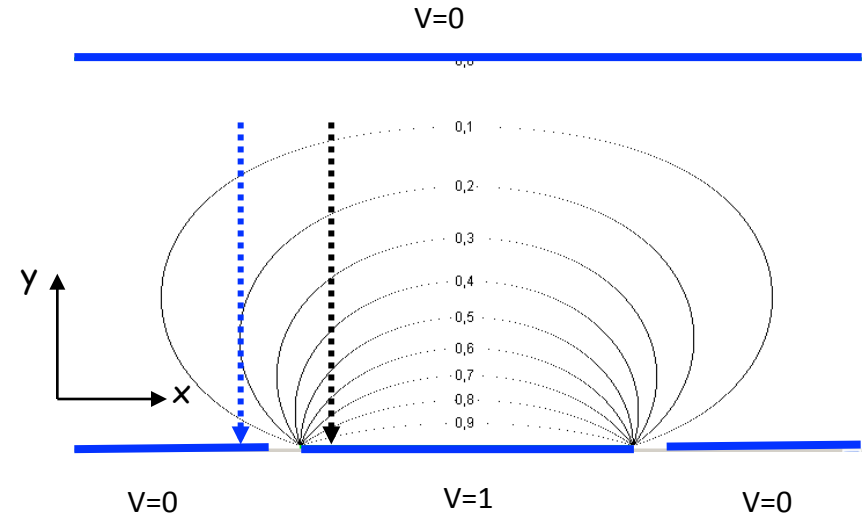


double sided  
silicon strip detector

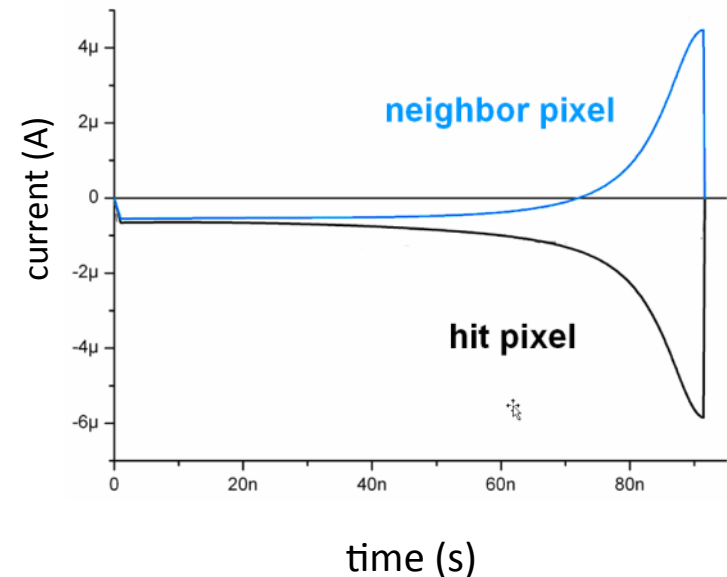
$\Phi_w$  for a strip/pixel geometry

$$\Phi(x, y) = \frac{1}{\pi} \arctan \frac{\sin(\pi y) \cdot \sinh(\pi \frac{a}{2})}{\cosh(\pi x) - \cos(\pi y) \cosh(\pi \frac{a}{2})}$$

(can be calculated e.g. by using “conformal mapping”)



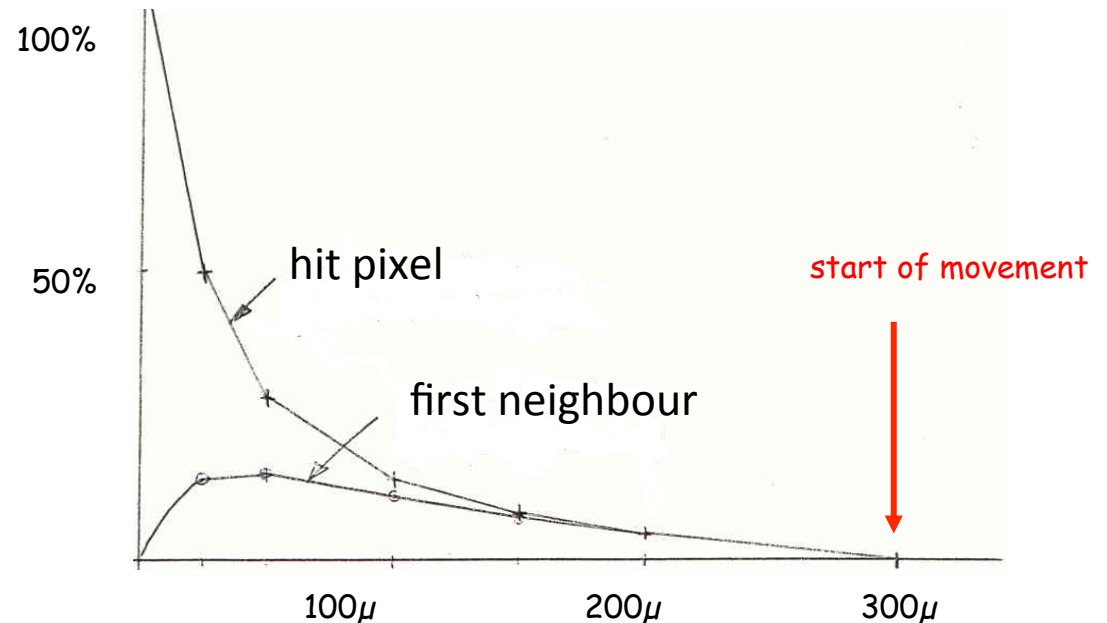
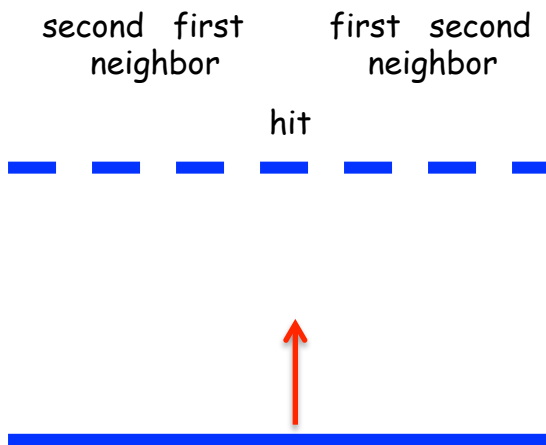
“small pixel effect” !



# Concluding ... consequences ...

- ❑ The weighting field reaches also into regions of neighbor pixels → induced signals there as well
- ❑ At the beginning of the charge movement, neighbor pixels “see” almost as much signal as the “hit” pixel → no difference when electronics is (too) fast
- ❑ consequences for small electrodes is, that most of the charge is induced, when  $q$  is near the hit pixel → small pixel effect
- ❑ when charges drift only a short distance due to
  - $\mu_h \ll \mu_e$  (e.g. for CdTe)
  - trapping (e.g. for pCVD diamond)

peculiar signal patterns may arise (worst case: holes do not move and electrons are trapped after  $50\text{ }\mu\text{m}$  → several pixels “fire”)



# Transport of charges to the R/O electrode

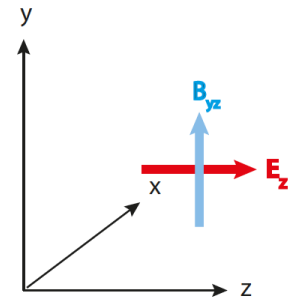
generally described by the Boltzmann Transport Equation

$$\frac{df}{dt} = \frac{\partial f}{\partial t} + \frac{d\vec{r}}{dt} \vec{\nabla}_{\vec{r}} f + \frac{d\vec{v}}{dt} \vec{\nabla}_{\vec{v}} f = \frac{\partial f}{\partial t} |_{coll}$$

with  $f(r, v, t)$  describing the probability distribution in phase space

$$dp(\vec{r}, \vec{v}, t) = f(\vec{r}, \vec{v}, t) d^3\vec{r} d^3\vec{v}$$

Which can treat arbitrary E and B-fields ... (E in z-direction, B in z-y-direction)



$$v_{D,1}^B = -\frac{4\pi}{3} \frac{qE}{m} \int_0^\infty \tau \frac{\omega_2 \tau}{1 + \omega^2 \tau^2} \left( \frac{2\epsilon}{m} \right)^{3/2} \frac{\partial f_0}{\partial \epsilon} d\epsilon = \frac{qE}{m} \left\langle \tau \frac{\omega_2 \tau}{1 + \omega^2 \tau^2} \right\rangle_\epsilon \quad \text{with}$$

$$v_{D,2}^B = \frac{4\pi}{3} \frac{qE}{m} \int_0^\infty \tau \frac{\omega_2 \omega_3 \tau^2}{1 + \omega^2 \tau^2} \left( \frac{2\epsilon}{m} \right)^{3/2} \frac{\partial f_0}{\partial \epsilon} d\epsilon = \frac{qE}{m} \left\langle \tau \frac{\omega_2 \omega_3 \tau^2}{1 + \omega^2 \tau^2} \right\rangle_\epsilon \quad \omega_i = qB_i/m = \text{cyclotron frequencies}$$

$$v_{D,3}^B = \frac{4\pi}{3} \frac{qE}{m} \int_0^\infty \tau \frac{1 + \omega_3^2 \tau^2}{1 + \omega^2 \tau^2} \left( \frac{2\epsilon}{m} \right)^{3/2} \frac{\partial f_0}{\partial \epsilon} d\epsilon = \frac{qE}{m} \left\langle \tau \frac{1 + \omega_3^2 \tau^2}{1 + \omega^2 \tau^2} \right\rangle_\epsilon \quad \begin{array}{l} \tau = \text{mean collision time} \\ \epsilon = \text{kin. energy} \end{array}$$

In detectors: usually either

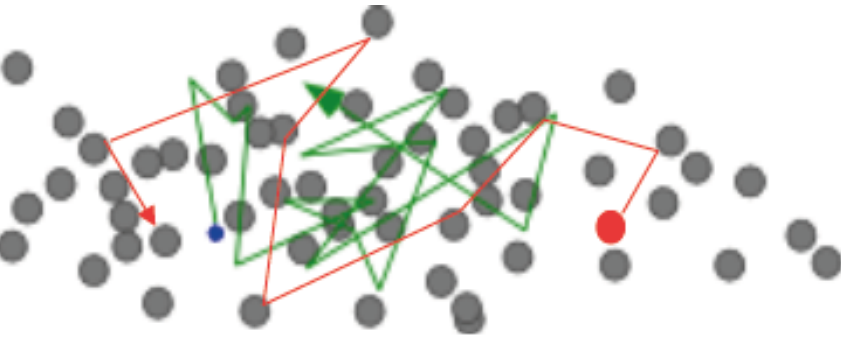
$$\vec{E} \perp \vec{B}$$

or

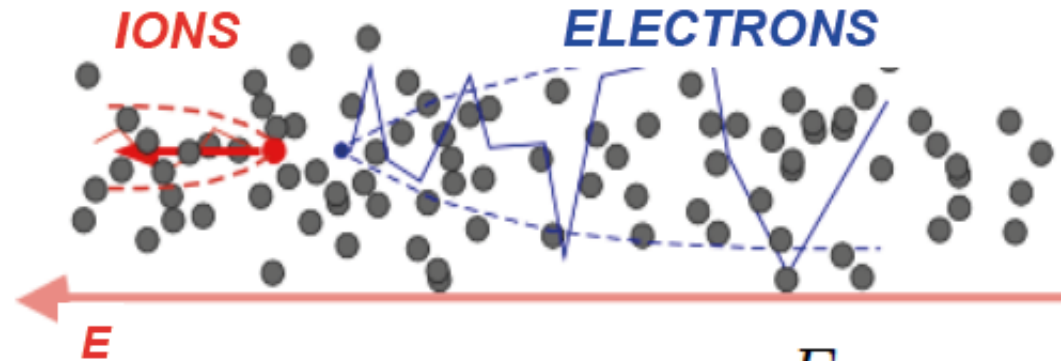
$$\vec{E} \parallel \vec{B}$$

# Diffusion and drift of charge cloud on way to electrode

$E = 0, T > 0$ : diffusion

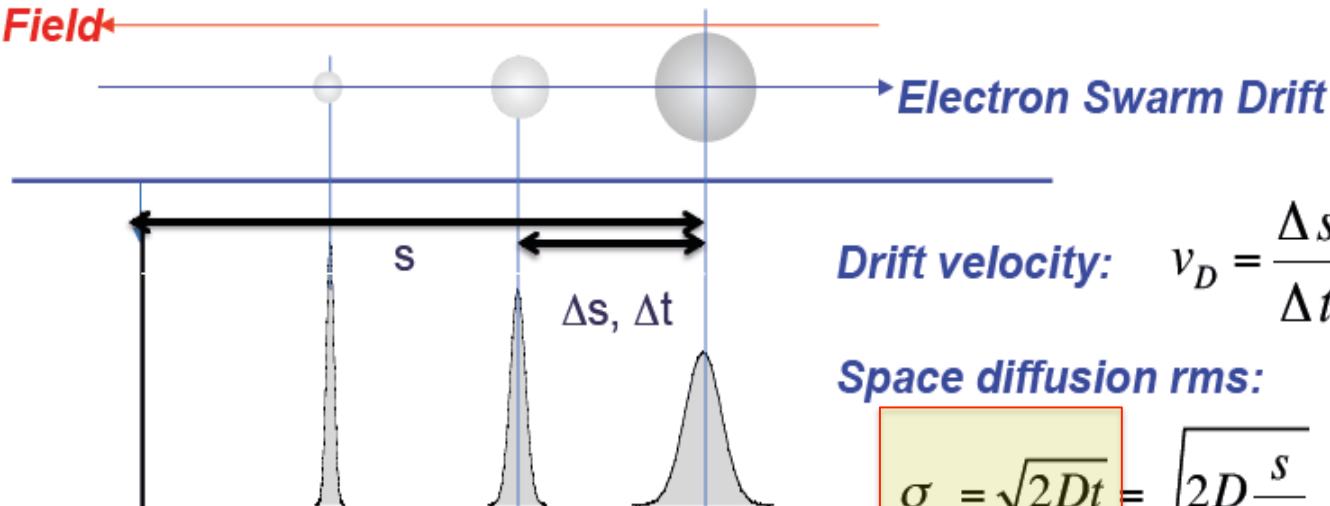


$E > 0, T > 0$ : diffusion + drift



$$D = \frac{\langle \lambda v \rangle}{3} = \frac{1}{3\sigma p} \sqrt{\frac{8(kT)^3}{\pi m}}$$

**Electric Field** ←



**Drift velocity:**  $v_D = \frac{\Delta s}{\Delta t}$

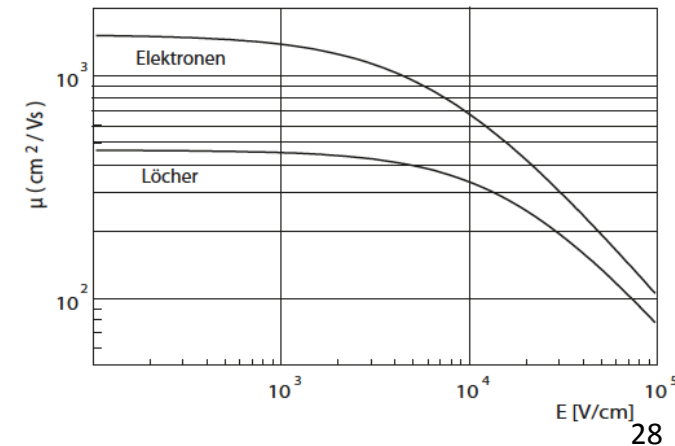
**Space diffusion rms:**

$$\sigma_x = \sqrt{2Dt} = \sqrt{2D \frac{s}{v_D}}$$

$$v_D = \mu(E) E = \frac{\mu_0 E}{\left[ 1 + \left( \frac{\mu_0 E}{v_{\text{sat}}} \right)^\beta \right]^{1/\beta}}$$

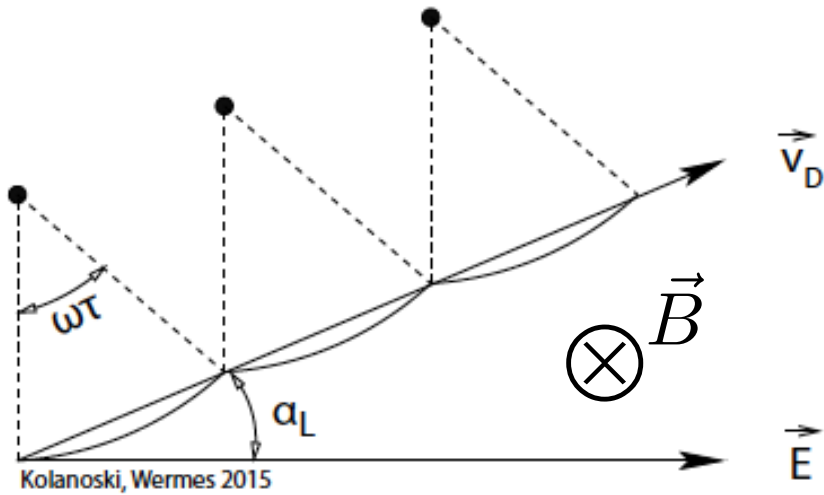
Drude Ansatz (emp.)  
(especially semicond.)

$\beta \sim 1-2$





# Movement in the presence of a magnetic field



- if the electric field  $E$  is perpendicular to a magnetic field  $B$  then the **charges drift on circle segments** until they stop in a collision
- on **average** this results in a **deflection of the drift path by an angle** called

**Lorentz angle**

$$\tan \alpha_L = \frac{v_{D,\perp}}{v_{D,\parallel}} = \omega \tau$$

perp. to  $E$

parallel to  $E$

with

$\omega = qB/m$  = cyclotron frequency

$\tau$  = mean collision time

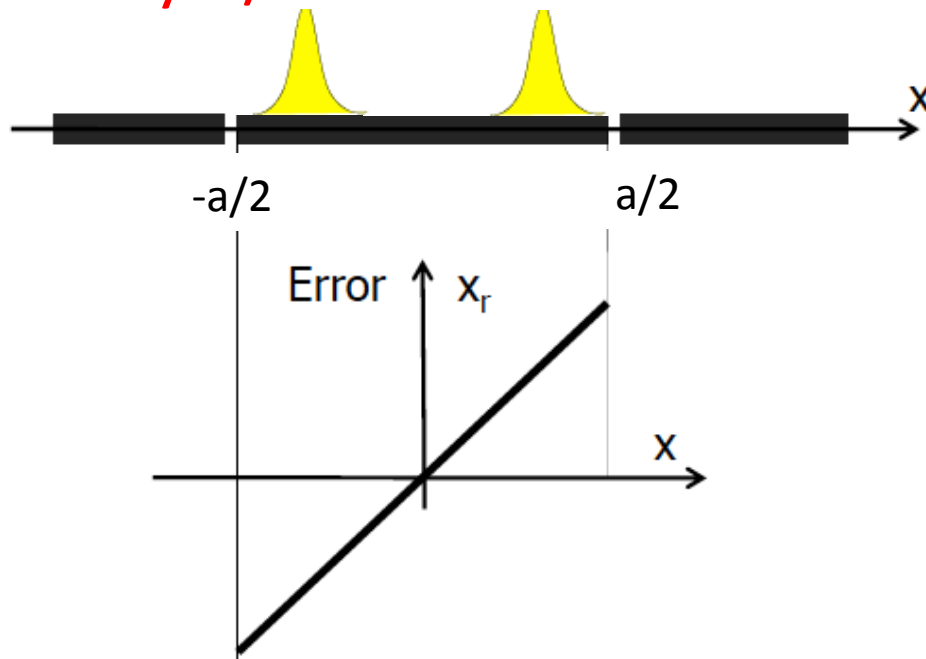
remember **Gluckstern formula**

$$\left( \frac{\sigma_{pT}}{pT} \right)_{\text{mess}} = \frac{pT}{0.3|z|} \frac{\sigma_{\text{mess}}}{L^2 B} \sqrt{\frac{720}{N+4}}$$

$$[pT] = \text{GeV}/c, [L] = \text{m}, [B] = \text{T}$$

- binary readout (hit/no hit)
- analog readout (pulse height information)
- signal (charge) distributed on more than one electrode

**binary R/O**



$$v = \int_{x_1}^{x_2} x^2 f(x) dx$$

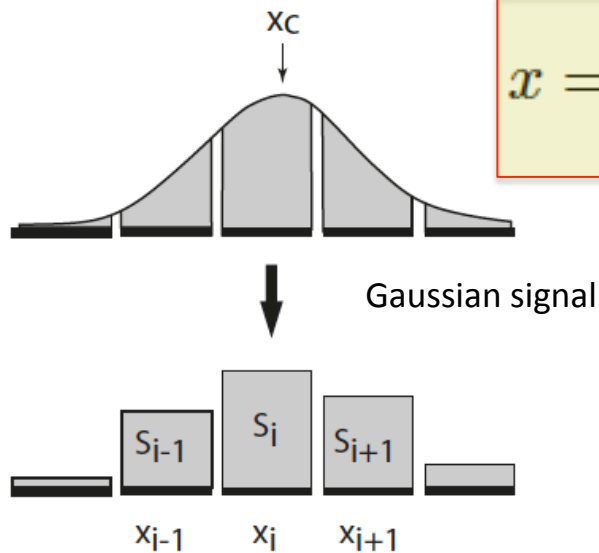
$$\sigma_x^2 = \frac{1}{a} \int_{-a/2}^{a/2} \Delta_x^2 d(\Delta_x) = \frac{a^2}{12}$$

$$\sigma_x = \frac{a}{\sqrt{12}}$$

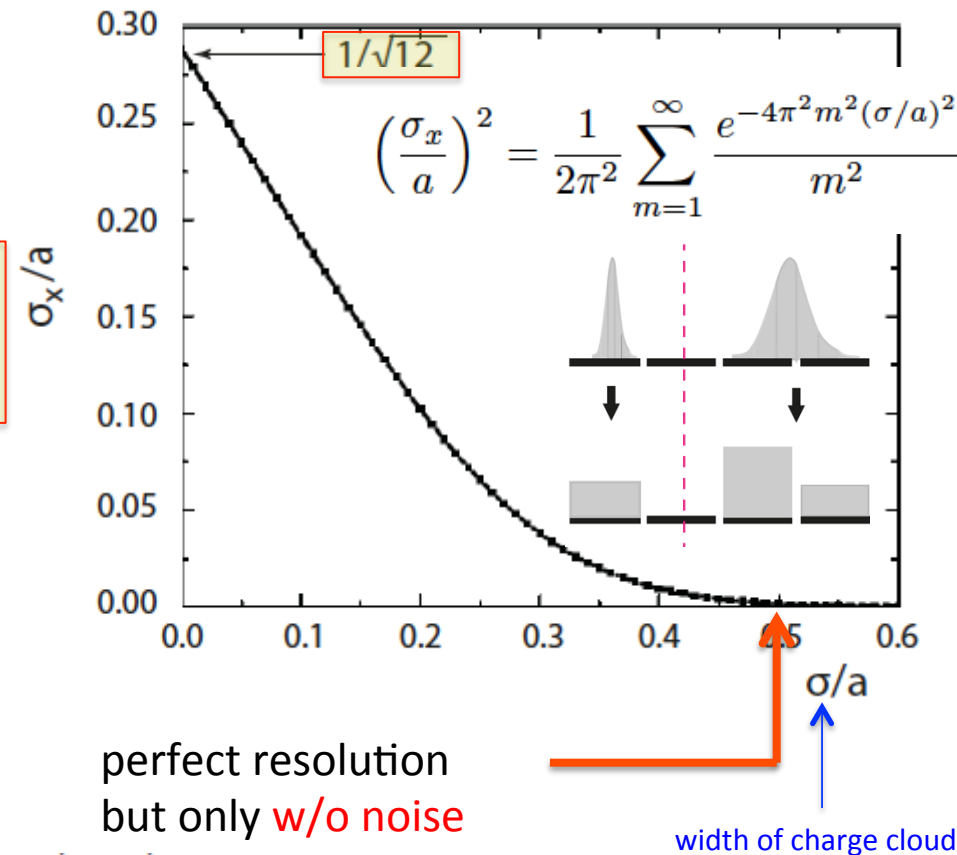
# Spatial Resolution in segmented electrode configurations

with **analog information**  
and spread over more  
than one electrode

center of gravity



$$x = x_c = \frac{\sum S_i x_i}{\sum S_i}$$



$$x_{rec} = \frac{\sum (S_i + n_i) x_i}{\sum (S_i + n_i)} = \frac{x + \sum n_i x_i}{1 + \sum n_i} = \left(x + \sum n_i x_i\right) \left(1 - \sum n_i + \mathcal{O}(n_i^2)\right)$$

with uncorrelated noise  
(normalized to signal and with  $S=1$ )

$$\langle n_i^2 \rangle = \sigma_n^2$$

$$\Rightarrow \sigma_x^2 = \sigma_n^2 \left[ \left( \sum_{i=1}^N x_i^2 \right) + N \langle x^2 \rangle \right] + \mathcal{O}(\sigma_n^3)$$

P. Fischer  
publ. in prep.  
also in KW2016



formalism can be extended accordingly to 2D

$$\sigma_x^2 = \sigma_n^2 \left[ \left( \sum_{i=1}^N x_i^2 \right) + N \langle x^2 \rangle \right] + \mathcal{O}(\sigma_n^3)$$

small number of electrodes good (because of noise)

good, if charge confined in small area -> circle like

## Geometry

## factor for (a = A = 1)

strips	0.816
pixel (square)	1.155
pixel (hexagonal)	0.491

hexagons least sensitive to noise contributions on electrodes

## Example:

- ❑ two strips at  $x_1 = -a/2$  and  $x_2 = +a/2$  ( $N = 2$ )
- ❑ Signals for a hit at  $x$  are  $S_1(x) = (x_2 - x)/a$  and  $S_2(x) = (x + x_2)/a$
- ❑  $S_1 + S_2 = 1$ ;  $x_1 S_1 + x_2 S_2 = x$ ;  $x_1 + x_2 = 0$  ✓

$$\left( \frac{\sigma_x}{\sigma_n} \right)^2 \approx x_1^2 + x_2^2 + \frac{2}{a} \int_{x_1}^{x_2} x^2 dx = \frac{2}{3} a^2$$

$$\sigma_x = 0.816 a \sigma_n$$

- ❑ Thus the resolution for  $S/N = 10$  ( $\sigma_n = 0.1$ ) is

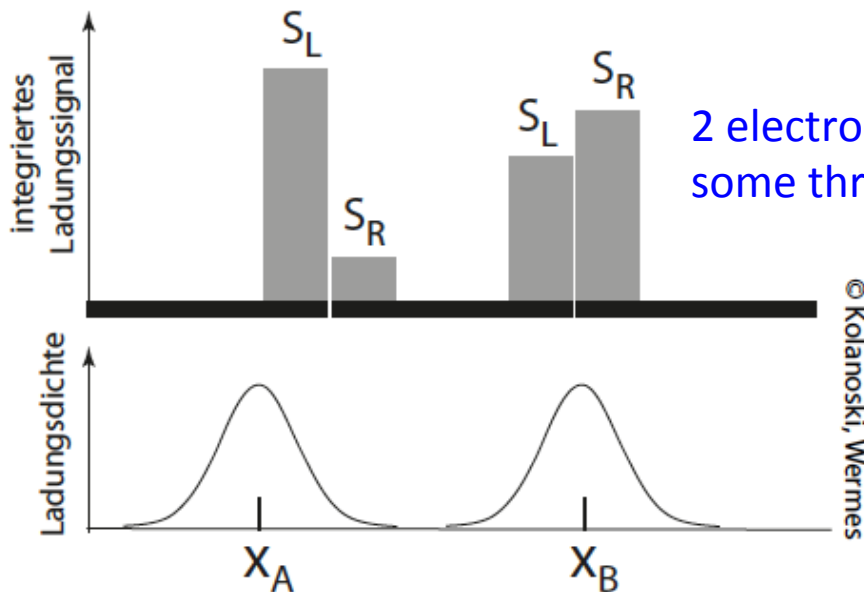
$$\sigma_x = 0.08a$$

It is better than binary ( $a/\sqrt{12}$ ) as long as  $S/N > 2.8$ .

# Arbitrary detector response (“data driven method”)

typical for semiconductor detectors  
and patterned gaseous detectors  
channels have different gains

$$N_{\text{electrodes}} = 2-3, S/N \sim 10$$



2 electrodes have signal over  
some threshold

$$S_L(x) = Q \eta(x)$$

$$S_R(x) = Q - S_L(x) = Q (1 - \eta(x))$$

$\eta$  = response function, indep. of  $Q$

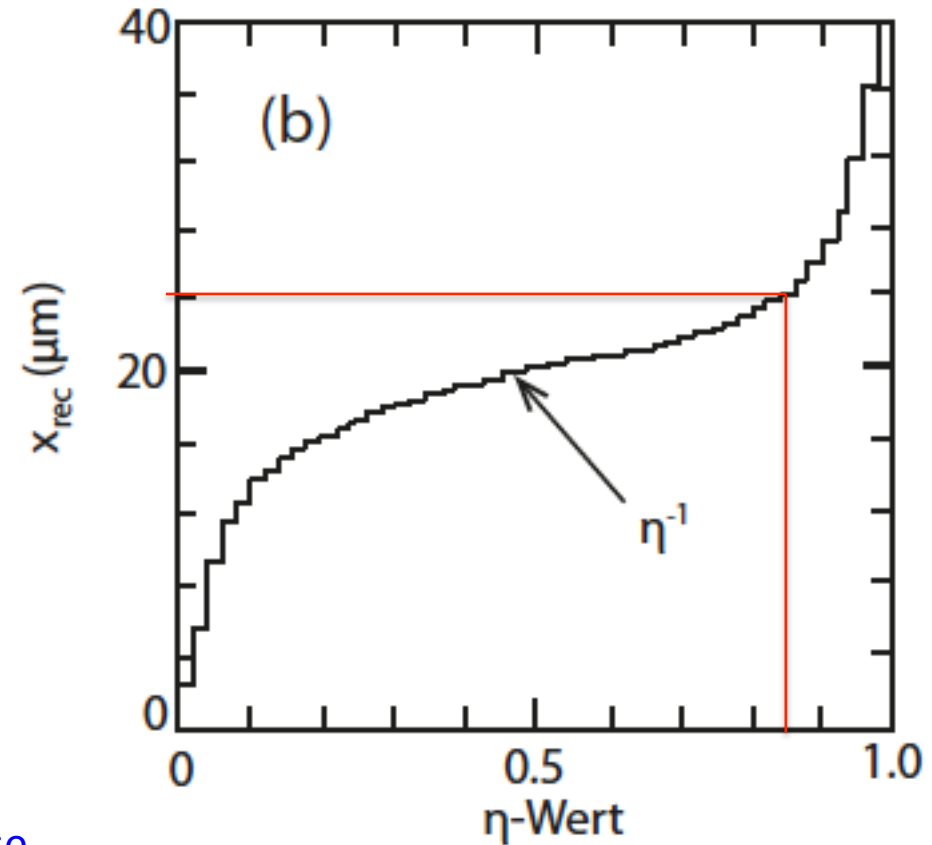
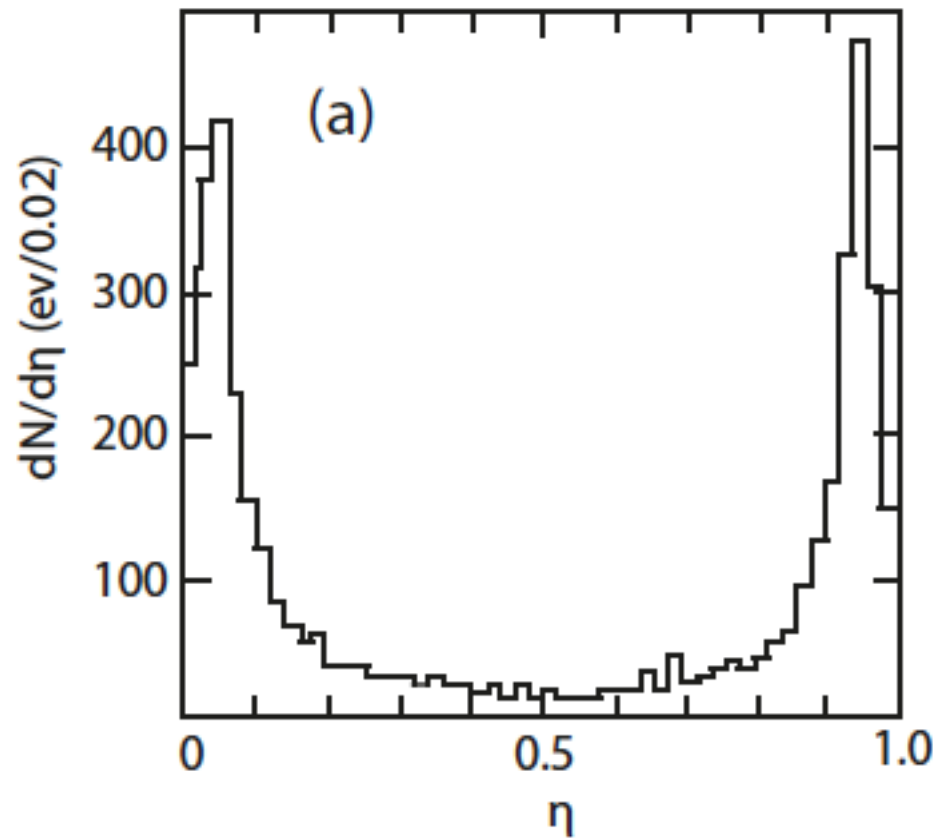
can be determined from signals themselves

$$\eta = \frac{S_L}{S_L + S_R}$$

- assume a constant hit probability density
- => can build inverse of  $\eta$ -function ( $\eta \rightarrow x$ )
- pick best estimate of position from measured distribution
- algorithm can also be extended to three – electrode situations

$$x_{\text{rec}} = \eta^{-1} \left( \frac{S_L}{S_L + S_R} \right) = \frac{a}{N} \int_0^\eta \frac{dN}{d\eta'} d\eta'$$

Belau, E. et al.: NIM 214 (1983) 253–260

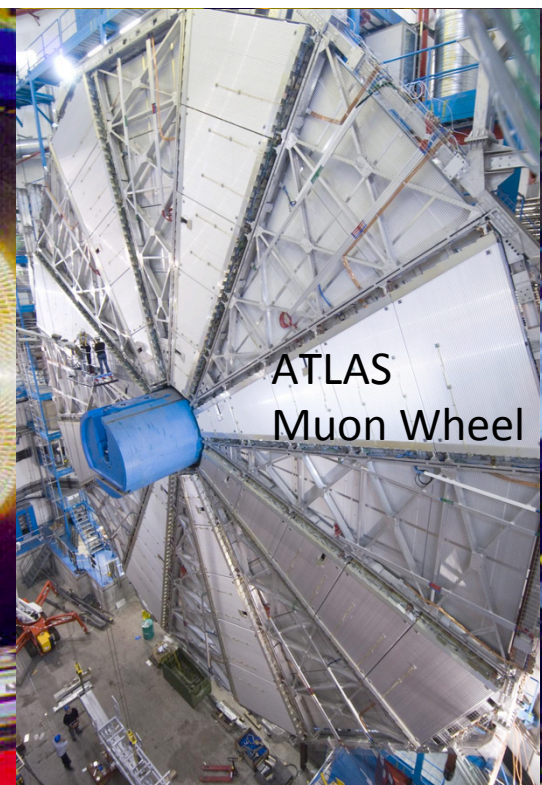
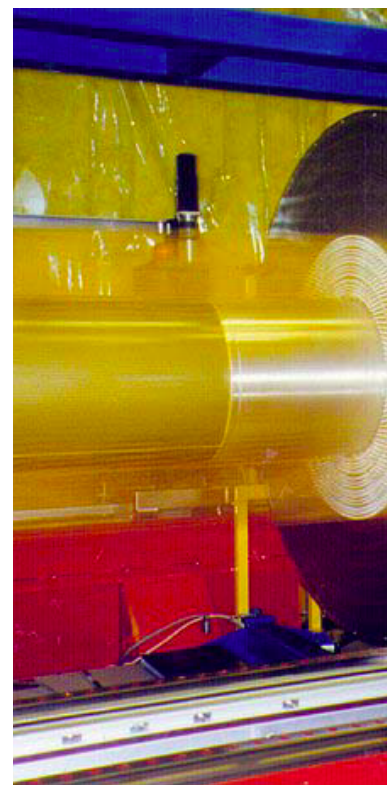
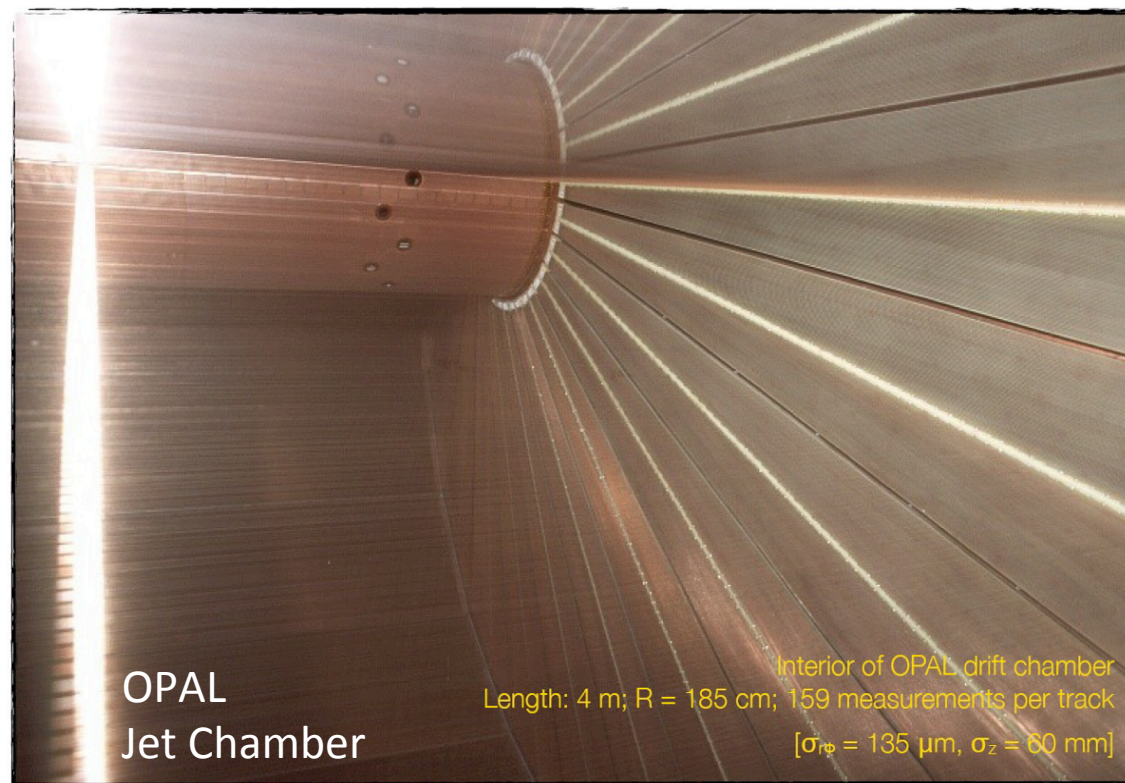


reconstruction  
with noise

$$x_{rec_{noise}} \approx x_{rec} = \frac{1}{\eta'} \left( n_L (1 - \eta(x)) - n_R \eta(x) \right)$$

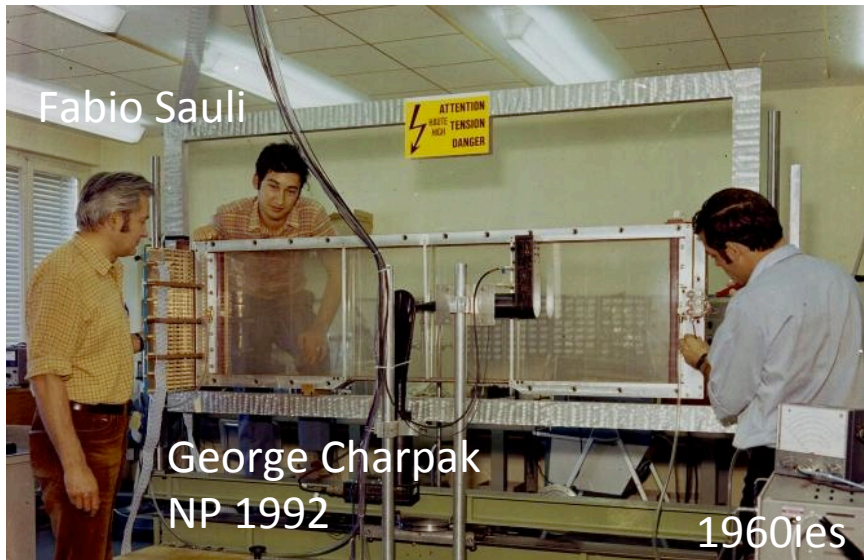
noise



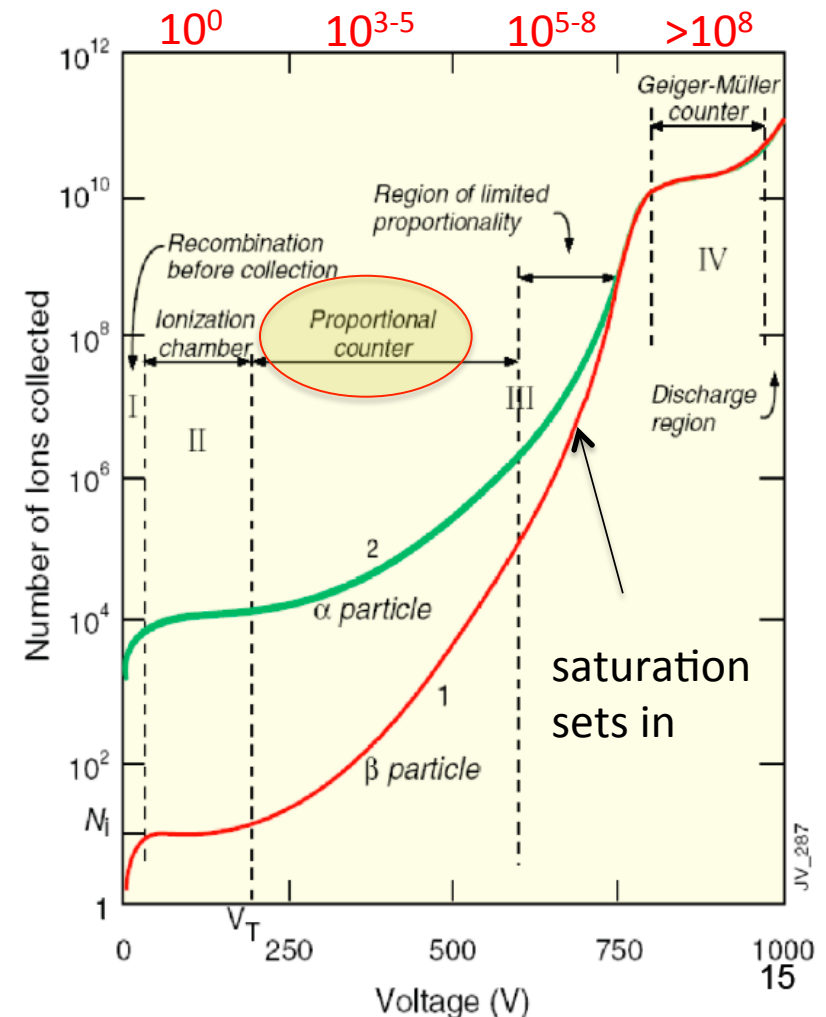




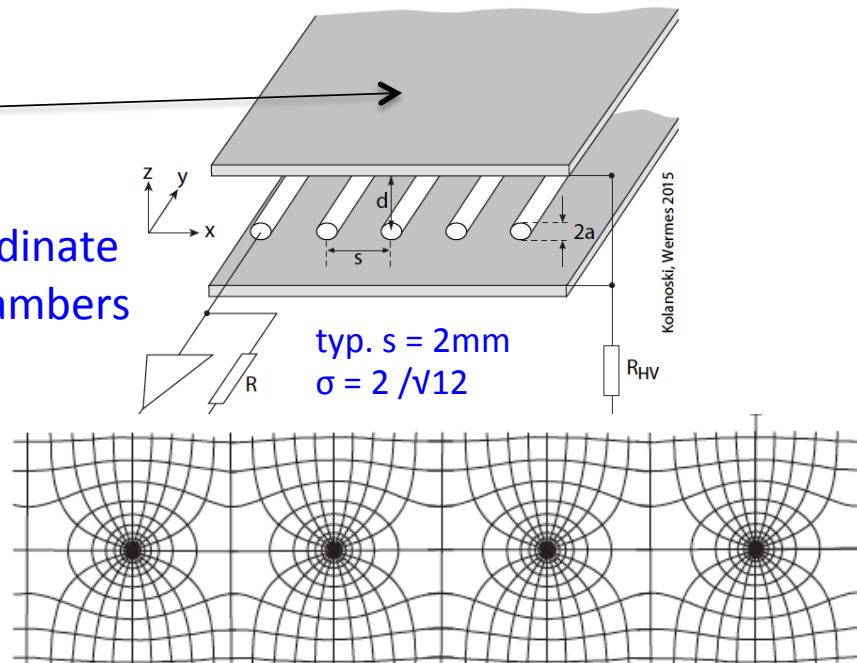
# Multi Wire Proportional Chamber



- mother of all wire chambers (1960ies)
- **break through in tracking**, because tracks became electronically recordable
- Nobel Prize 1992



cathodes  
often  
patterned  
for 2<sup>nd</sup> coordinate  
or more chambers

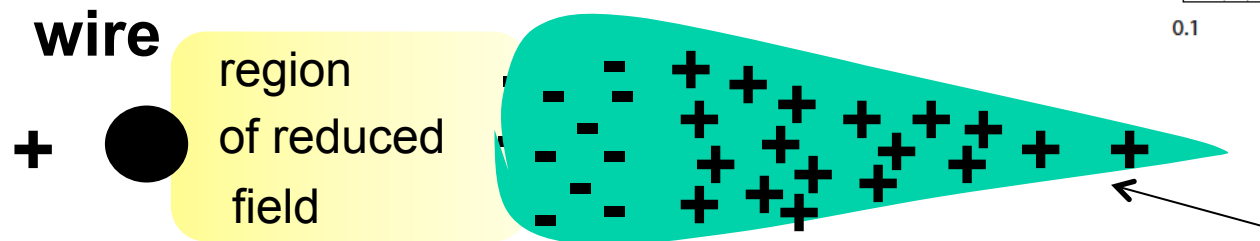
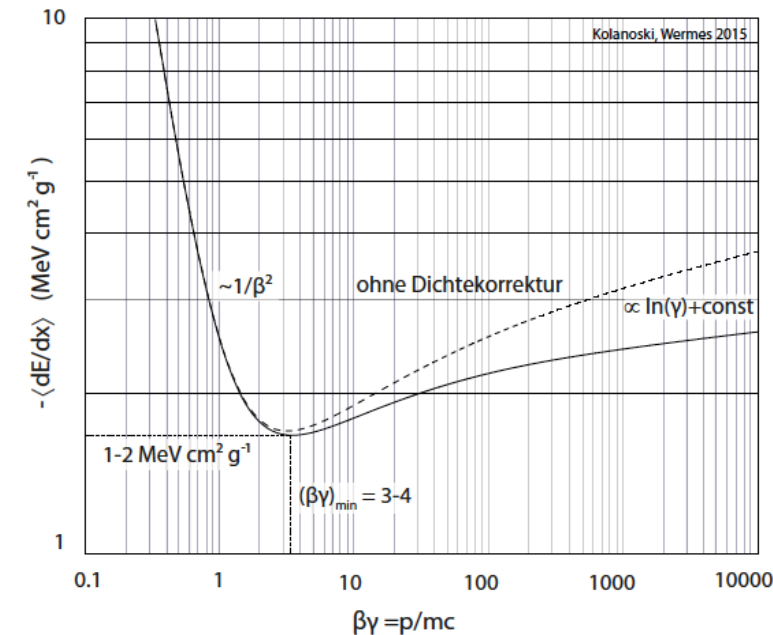




## region of limited proportionality → multi wire chamber operation in saturation region ( $G \sim 10^5 - 10^7$ )

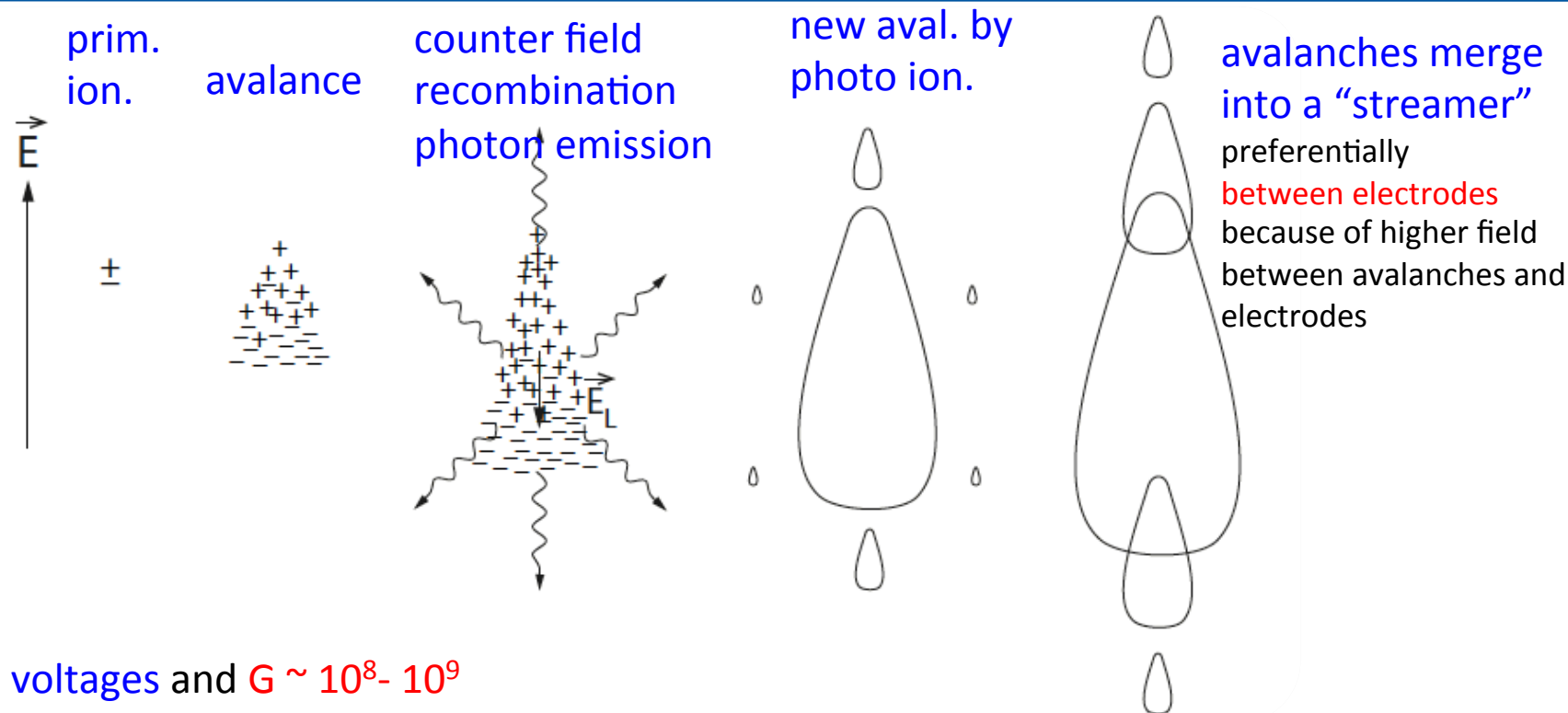
- operation point: gain  $> 10^6 \rightarrow$  strong secondary ionization
- space charge effects (stationary ion cloud decreases the electric field at the anode)  
destroy  $1/r$  shape near wire

- saturation of signal sets in  
this is sometimes wanted, when the number of particles is to be determined by the total signal height; e.g. when slow ( $1/\beta^2$ !) protons shall give the same signal height as m.i.p.s



**ion cloud  
is ~ stationary  
acts like a  
space charge**

# Saturation → Avalanche → Streamer → Spark



- ❑ at **very high voltages** and  $G \sim 10^8 - 10^9$
- ❑ **discharges** either spontaneous or initiated by ionisation
- ❑  $\Rightarrow$  **saturated avalanche**  $\rightarrow$  **streamer**  $\rightarrow$  **discharge** (= glow  $\rightarrow$  corona  $\rightarrow$  spark) occur
- ❑ streamer/discharge accompanied by **photon emission** (can be visible) and need to be **quenched** (by space charge screening, HV-lowering, pulsed HV, etc. ) when used as detectors rather than demonstration objects (spark ch.)
- ❑ **very fast** ( $10^6$  m/s) governed by photon emission, 10x faster than avalanche dev. (governed by  $v_{\text{drift}}$ )
- ❑ when streamer reaches electrode  $\Rightarrow$  spark/discharge  $\Rightarrow$  avoid in detectors (**limited streamer mode**)
- ❑ streamer operation in: **straw tube** geometries or **RPCs**

# The magic of the choice of the gas / gas-mixture

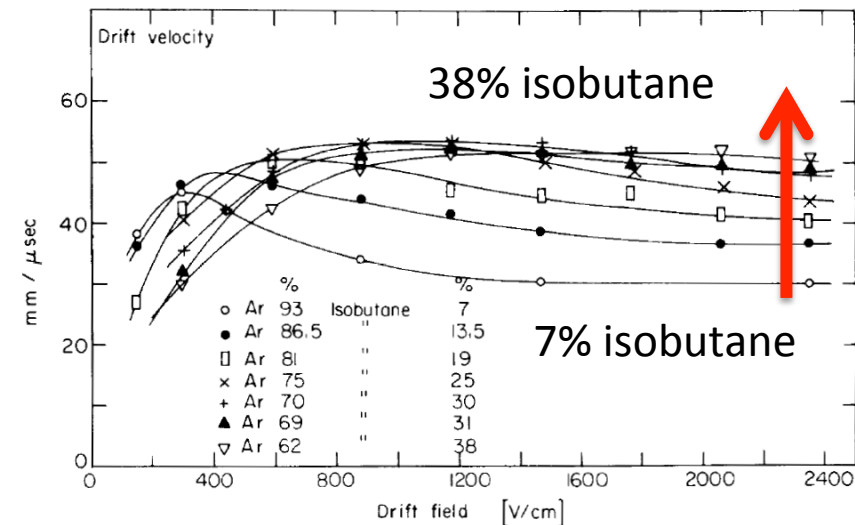
- ❑ high ionisation density => best are heavy **nobel gases** (Ar, Kr, Xe) or  $\text{CO}_2$ ,  $\text{C}_x\text{H}_y$ ,  $\text{CF}_4$
- ❑ little charge loss => **no  $\text{O}_2$**  or electronegative gases
- ❑ high gain at low voltage => nobel gases best => **Ar** (cheapest)
- ❑ proportionality between prim. ionisation and signal
- ❑ spark robustness => need photon **quencher** (Ar no good) => **hydrocarbons or  $\text{CO}_2$**

examples:

Ar – $\text{C}_2\text{H}_6$	50:50
Ar – $\text{CH}_4$	90:10
Ar – $\text{C}_4\text{H}_{10}$	75:25
Ar – $\text{CO}_2$ – $\text{CH}_4$	90:9:1

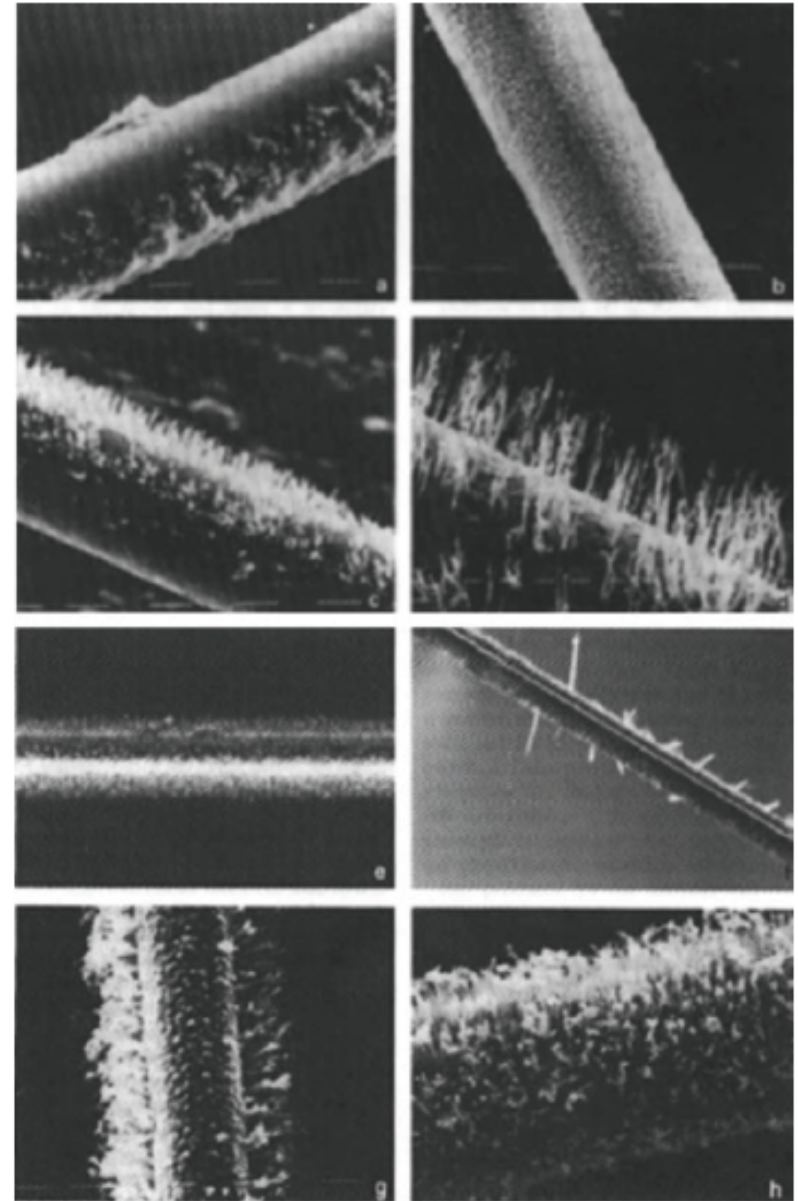
- ❑ small diffusion and constant  $v_{\text{drift}}$   
=> also **provided by quench gas** => tune mixture
- ❑ **no polymerisation** (ageing) => ions from organic gases tend to polymerize => add propanol, methylal

- ❑ rate tolerance w/o space charge
- ❑ radiation resistance
- ❑ non flammable

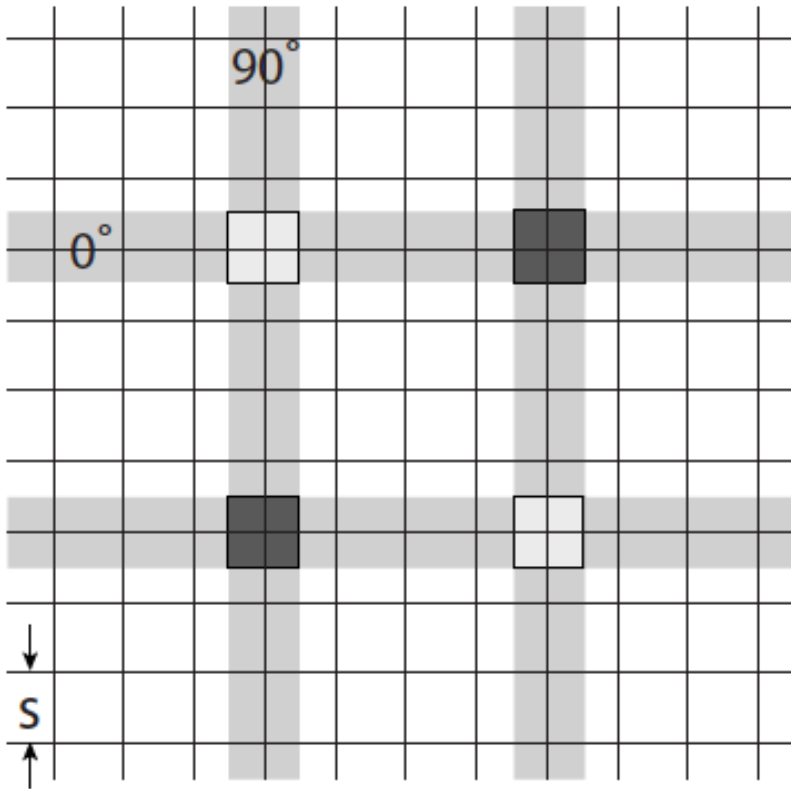


Drift velocity in several argon-isobutane ( $\text{C}_4\text{H}_{10}$ ) mixtures

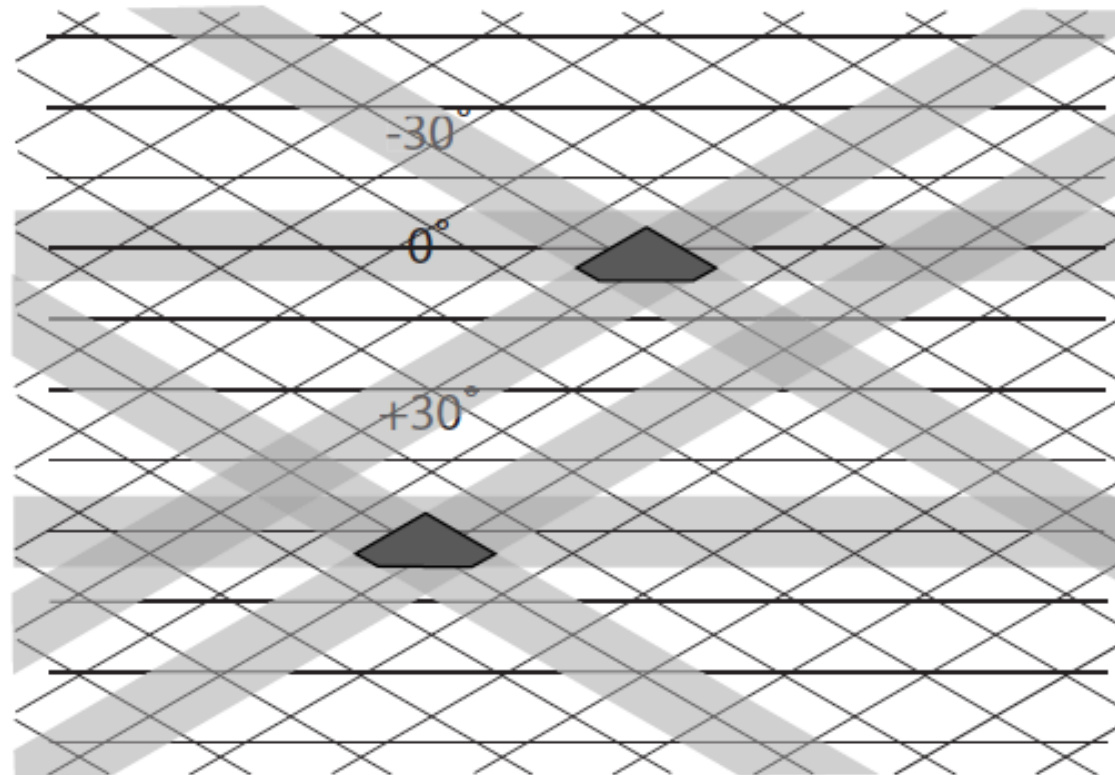
- **cause:** avalanche process + radiation
- polymerisation on wires -> **wisker** growth
- **result**
  - gain reduction
  - dark currents
  - corrosion
  - mechanical damage
- chemical disintegration of complex gas molecules, i.e. by **hydrocarbons** (quencher) or by **gas impurities**
- long chains of molecules become attached to the electrodes



cathode readout (see page 24) or **crossed wire planes** 

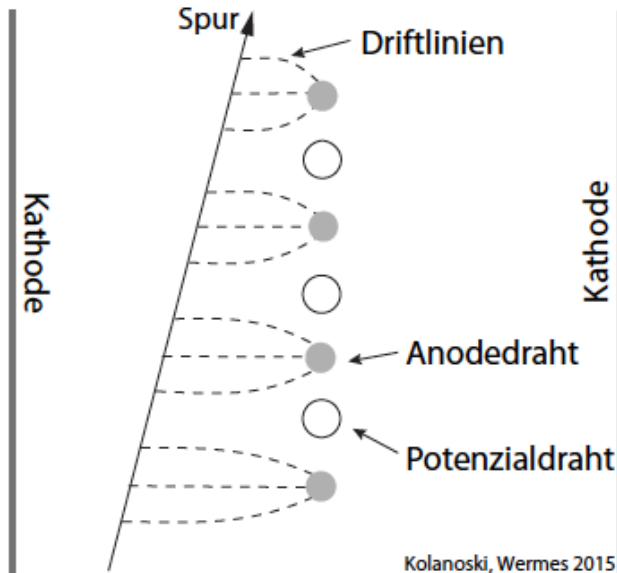


$90^\circ$  “stereo” arrangement  
best for resolution  
but  $n^2$  “ghost” hits

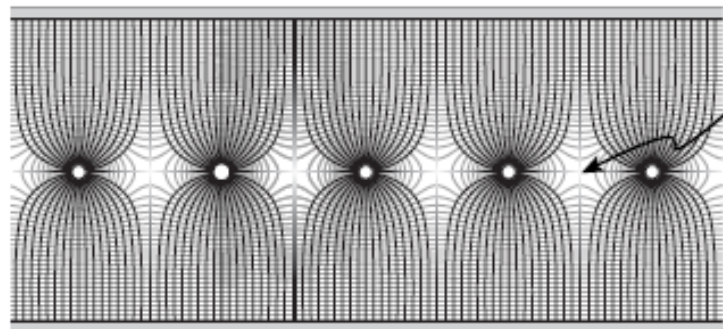


Kolanoski, Wermes 2015

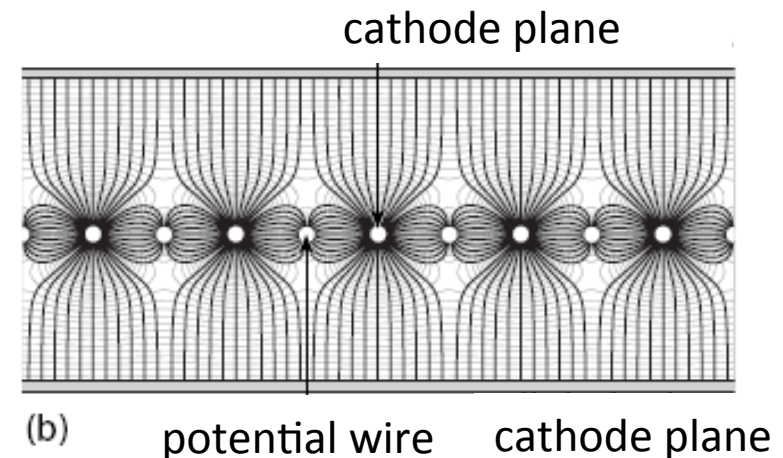
$\pm 30^\circ$  “stereo” arrangement  
(3 layers)  
small angles often easier due to wire fixations or R/O  
no ghosts in this example



- ❑ MWPC limited for very narrow wire spacing due to electrostatic repulsion: typ.:  $s > 1\text{mm}$  for  $\varnothing 10\text{ }\mu\text{m}$ ,  $l = 25\text{ cm}$
- ❑ better resolution obtained by **measurement of arrival time** of the electron cloud (measured by **TDC** or similar)
- ❑ need additional "**potential wire**" to avoid low field regions
- ❑ track **space point to drift-time relation** usually field dependent and thus **non linear** (-> calibration)

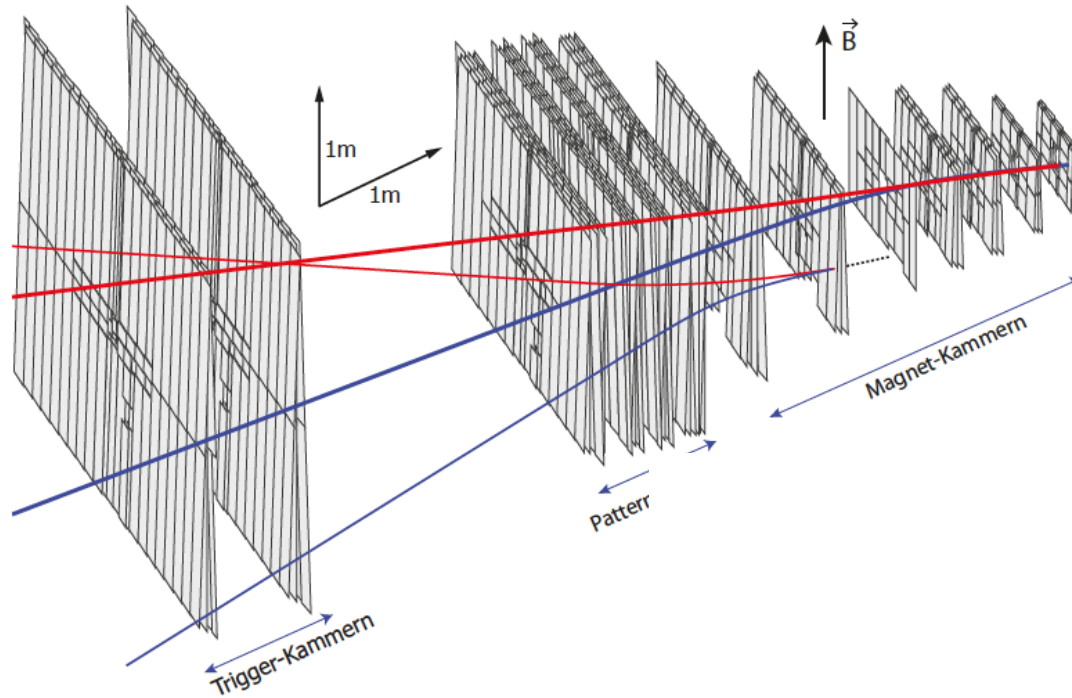


(a)

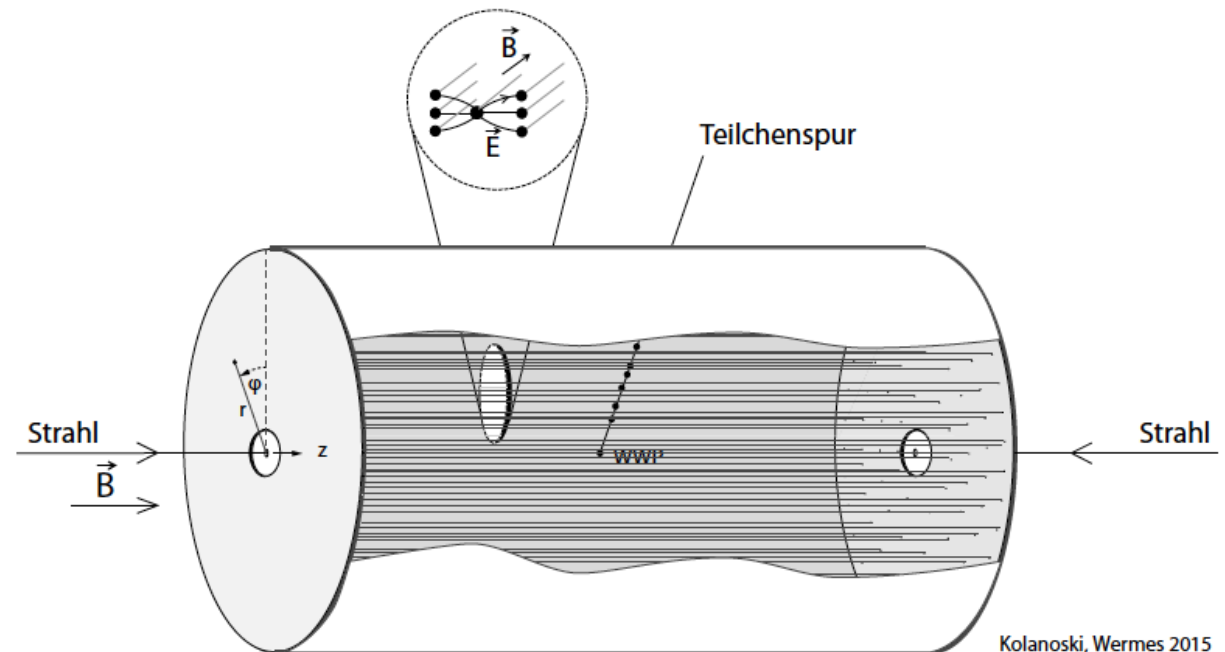


(b)



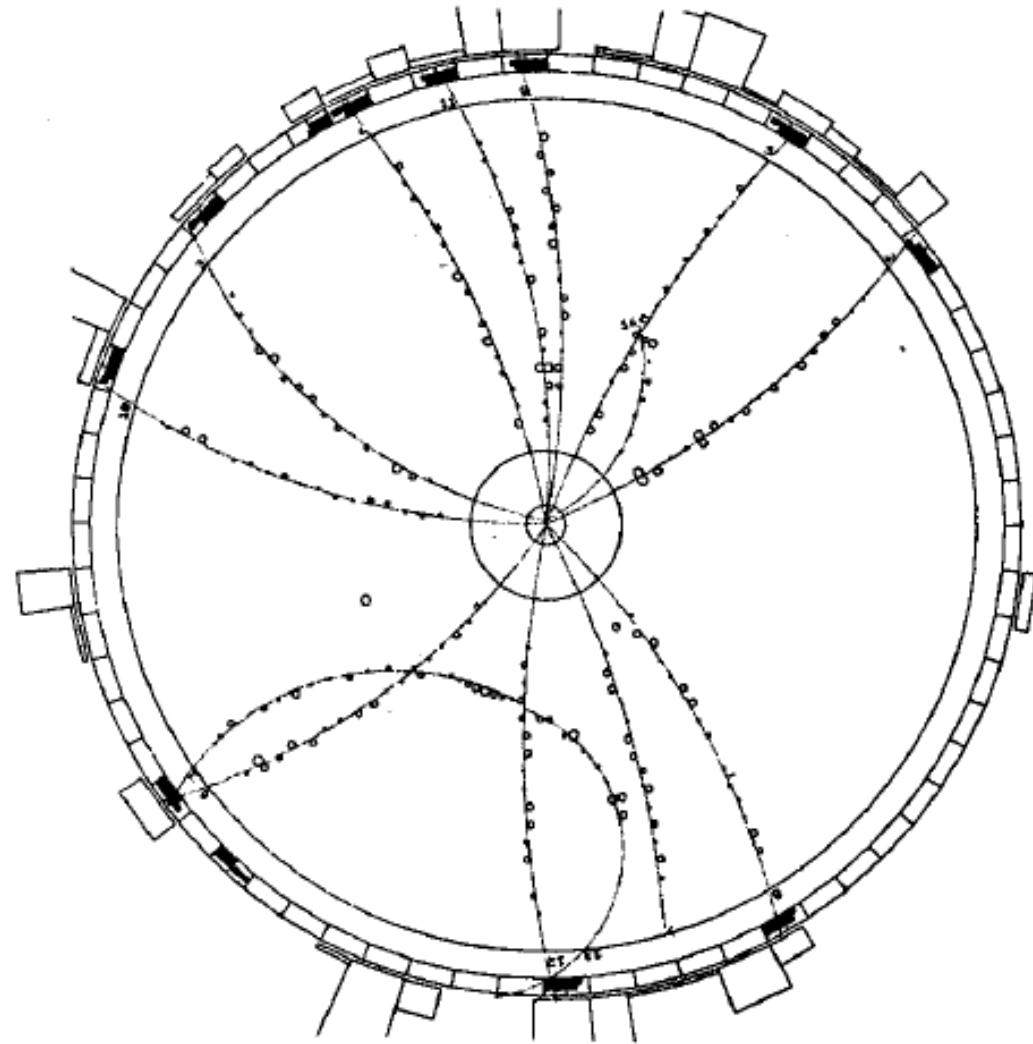
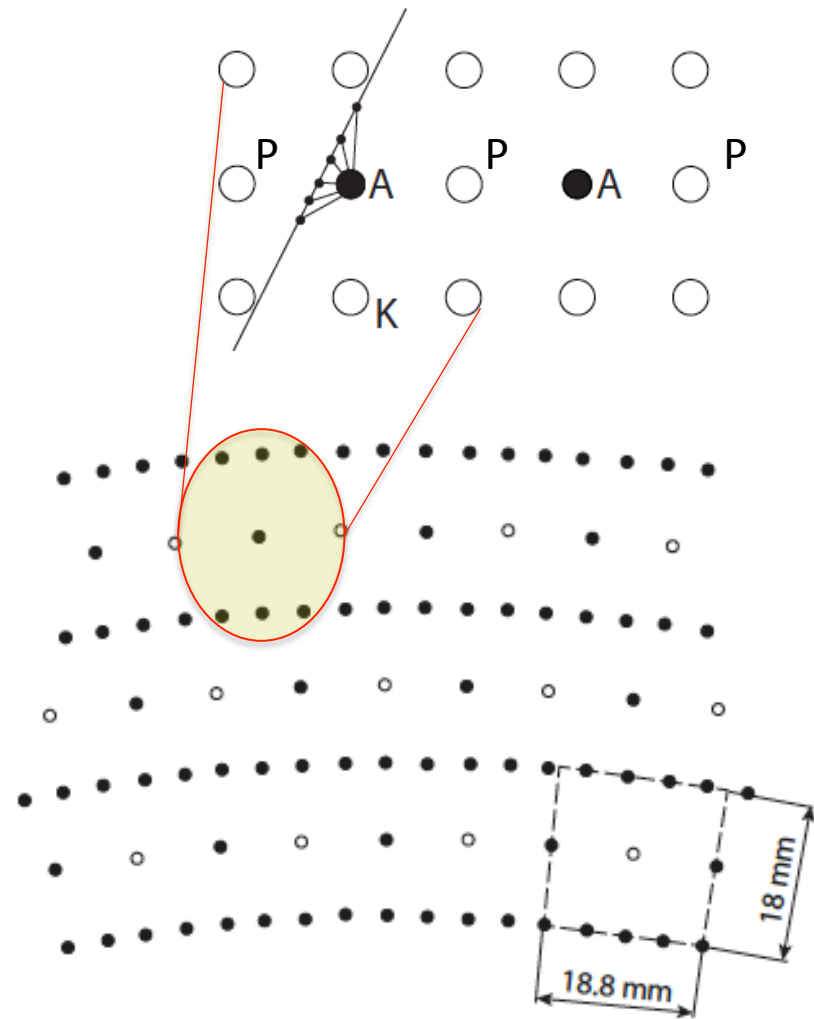


planar chambers  
in fixed target experiments



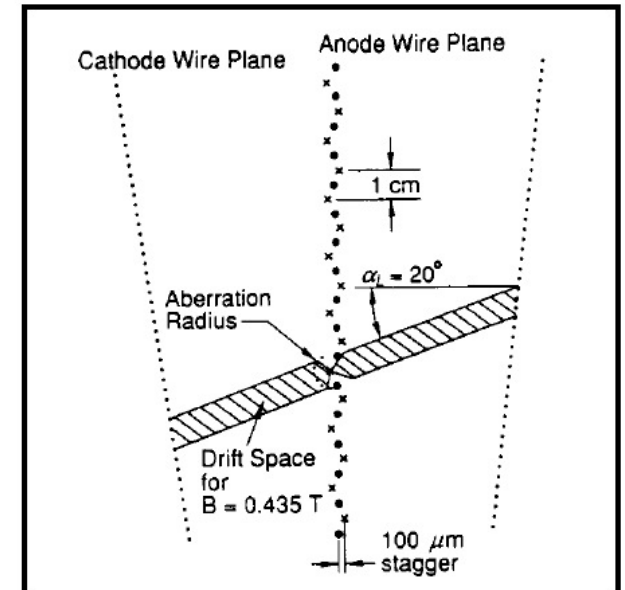
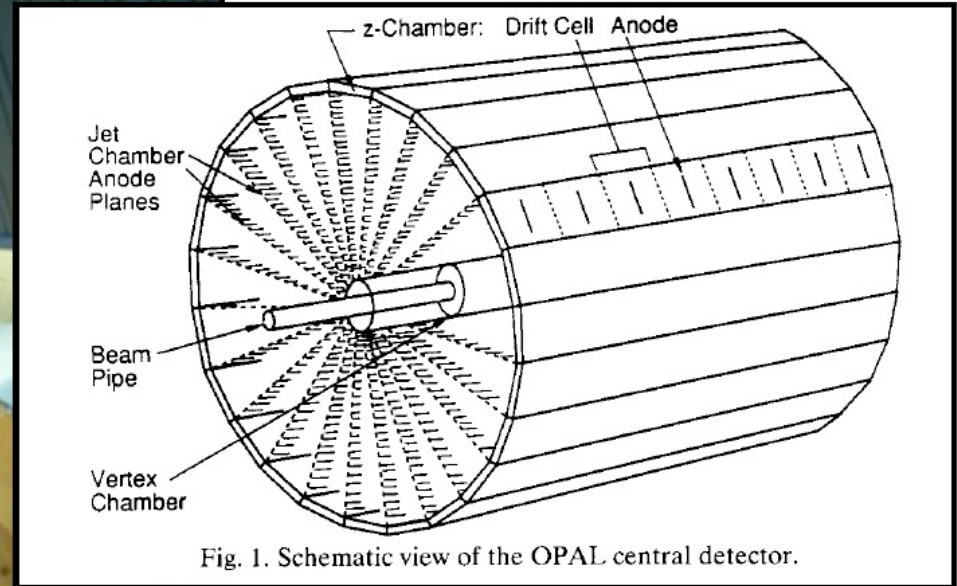
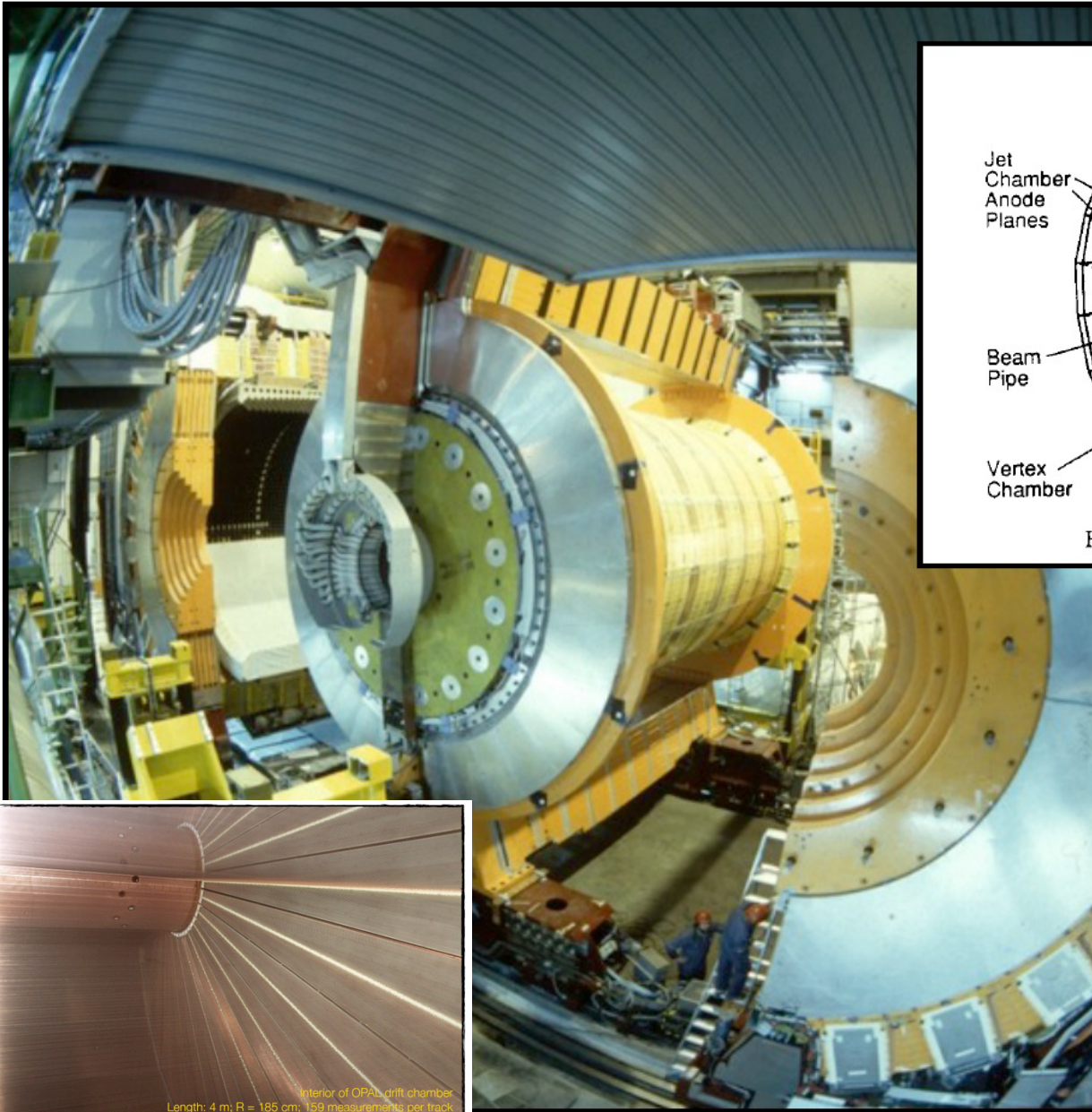
cylindrical chambers  
in collider experiments





used for example in ARGUS and TASSO experiments at DESY in the 1980ies.

# Drift cells: OPAL Jet Chamber

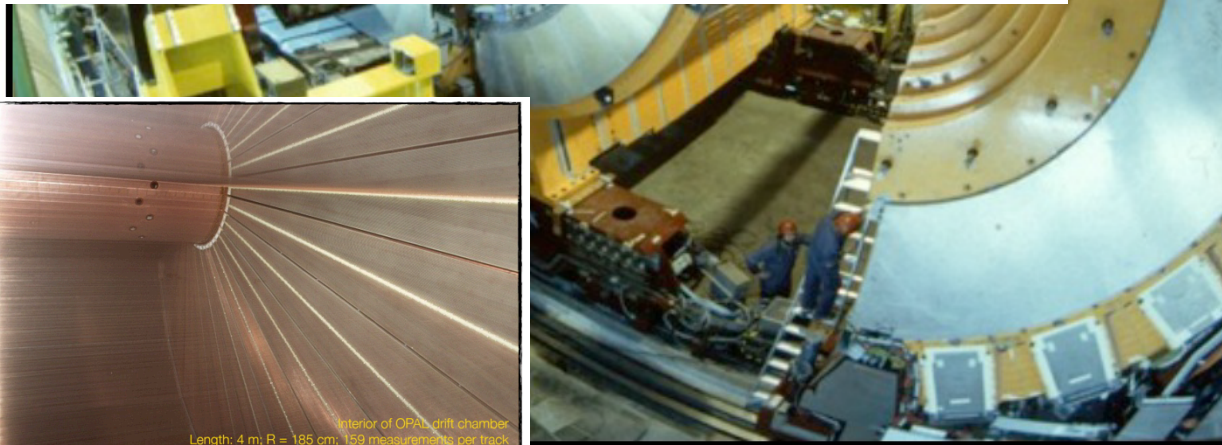
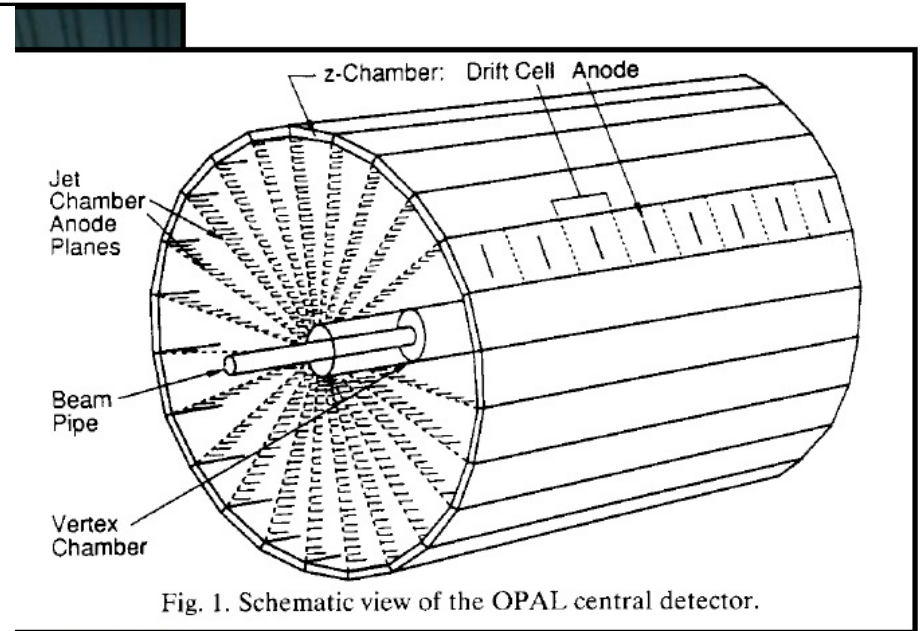


Interior of OPAL drift chamber.  
Length: 4 m; R = 185 cm; 159 measurements per track  
[ $\sigma_r = 135 \mu\text{m}$ ,  $\sigma_z = 60 \text{ mm}$ ]

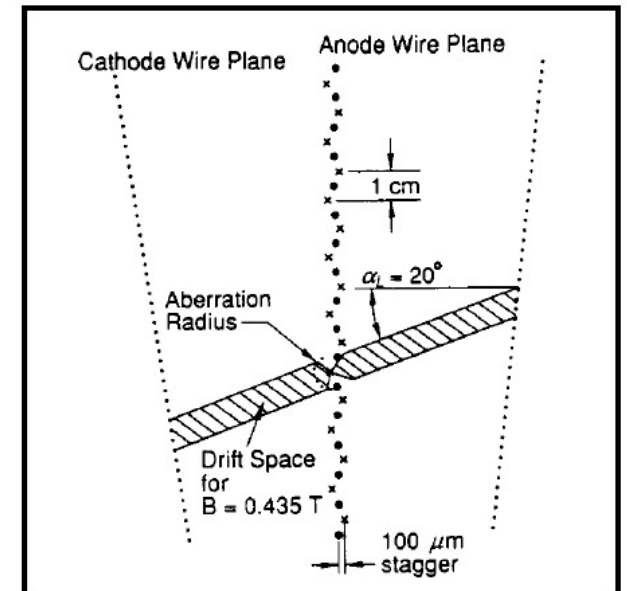


# Drift cells: OPAL Jet Chamber

- + many hits per particle track
- + but still only modest number of wires needed in total
- + homogeneous E-field → easy space point to drift-time relation
- + large drift distances
- get 3D space point by charge division on wire
- multi-hit electronics → good 2-track resolution
- “staggering” of anode wires to resolve the left-right ambiguity

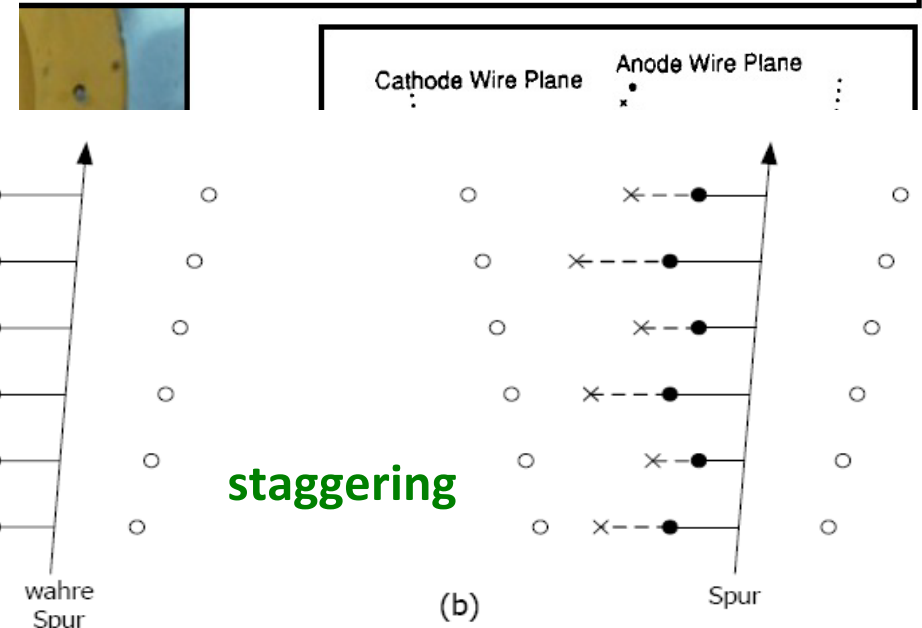
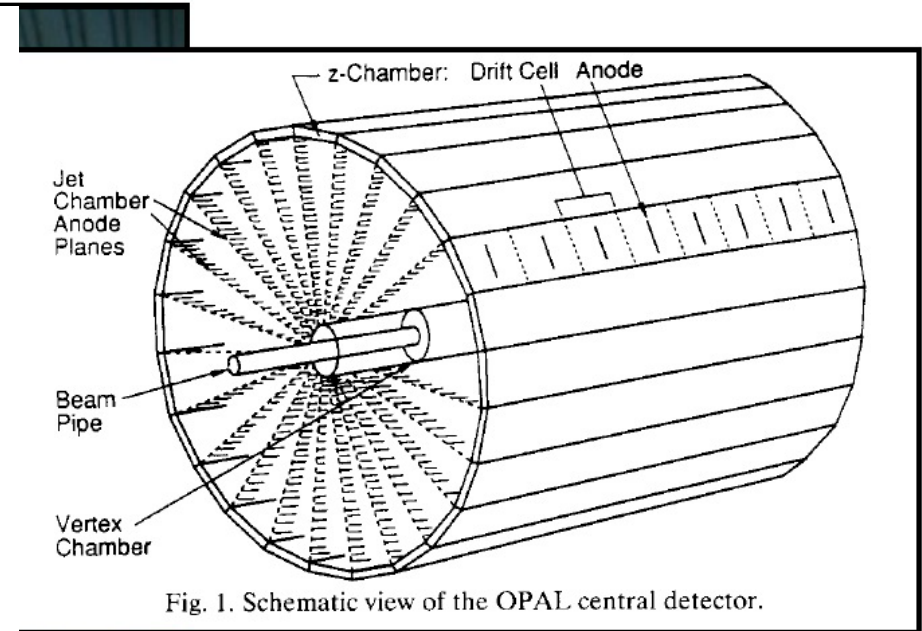


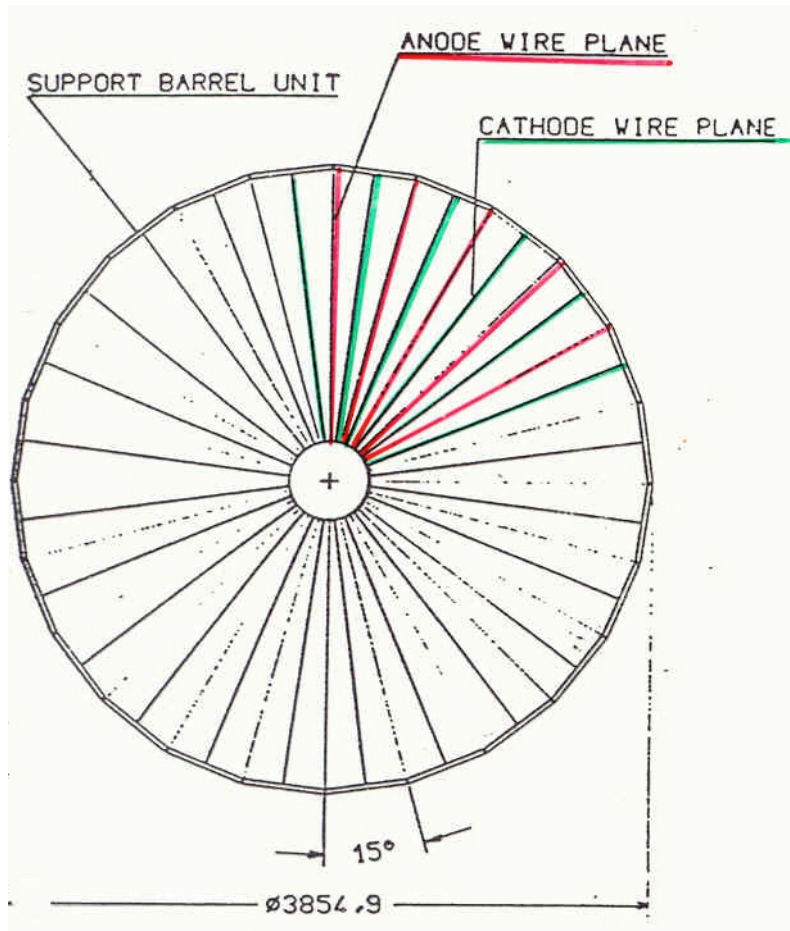
Interior of OPAL drift chamber.  
Length: 4 m;  $R = 185$  cm; 159 measurements per track  
[ $\sigma_r = 135$   $\mu$ m,  $\sigma_z = 60$  mm]



# Drift cells: OPAL Jet Chamber

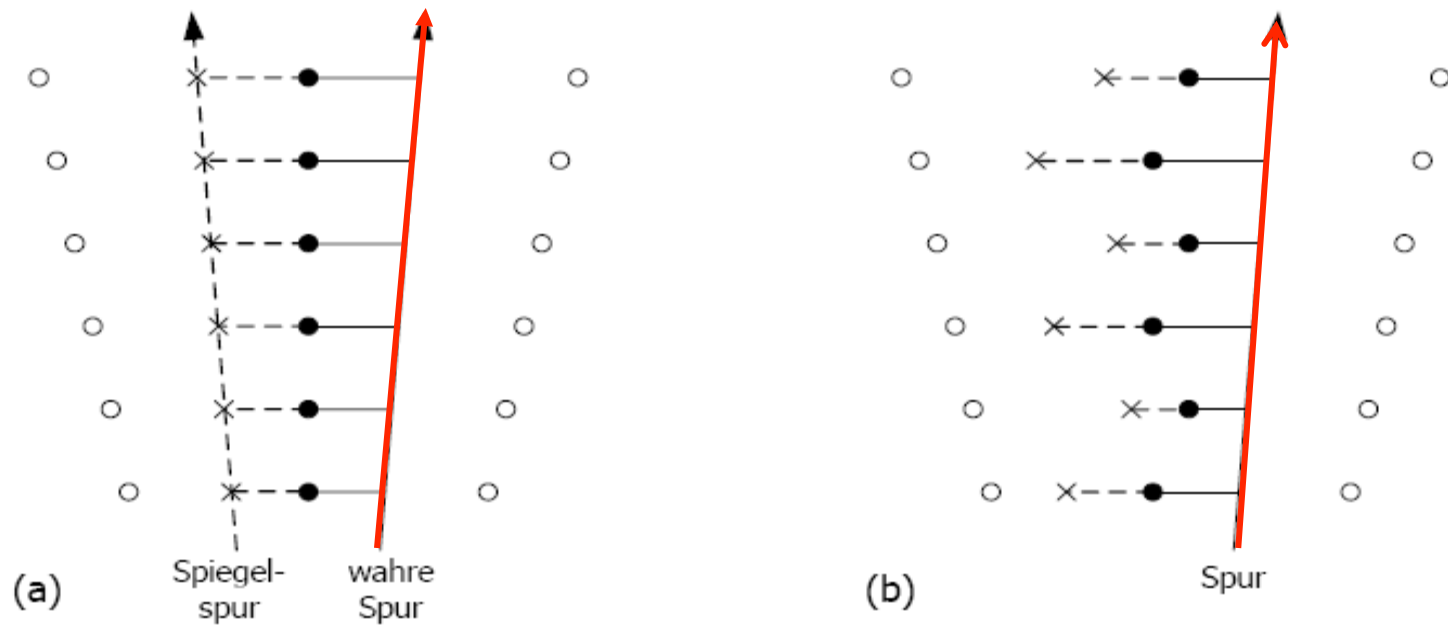
- + many hits per particle track
- + but still only modest number of wires needed in total
- + homogeneous E-field → easy space point to drift-time relation
- ± large drift distances
- get 3D space point by charge division on wire
- multi-hit electronics → good 2-track resolution
- “staggering” of anode wires to resolve the left-right ambiguity





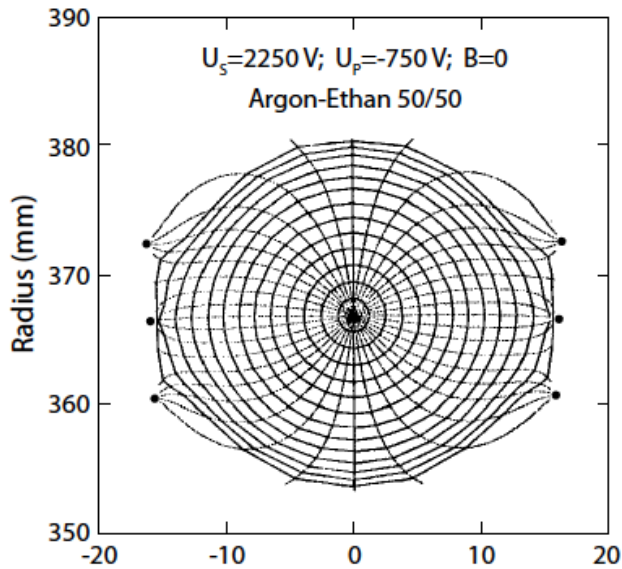
- + many hits per particle track
- + but still only modest number of wires needed in total
- + homogenous E-field → easy space point to drift-time relation
- ± large drift distances
- get 3D space point by charge division on wire
- multi-hit electronics → good 2-track resolution
- “staggering” of anode wires to resolve the left-right ambiguity

## staggering



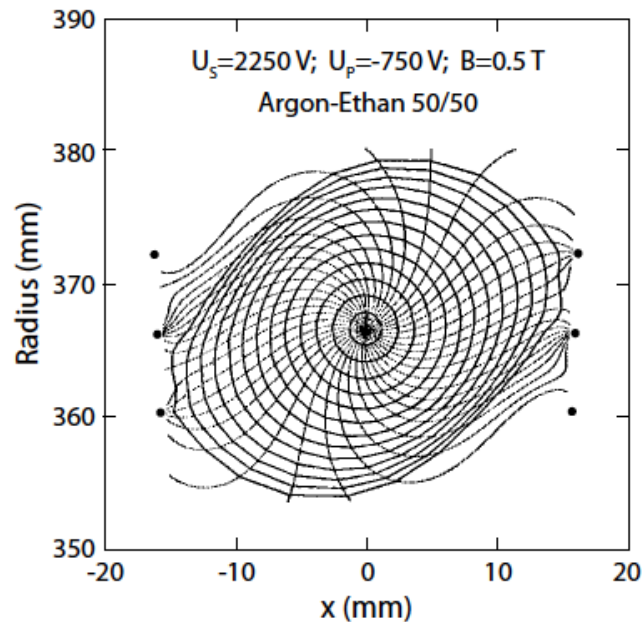


# Effect of B-field



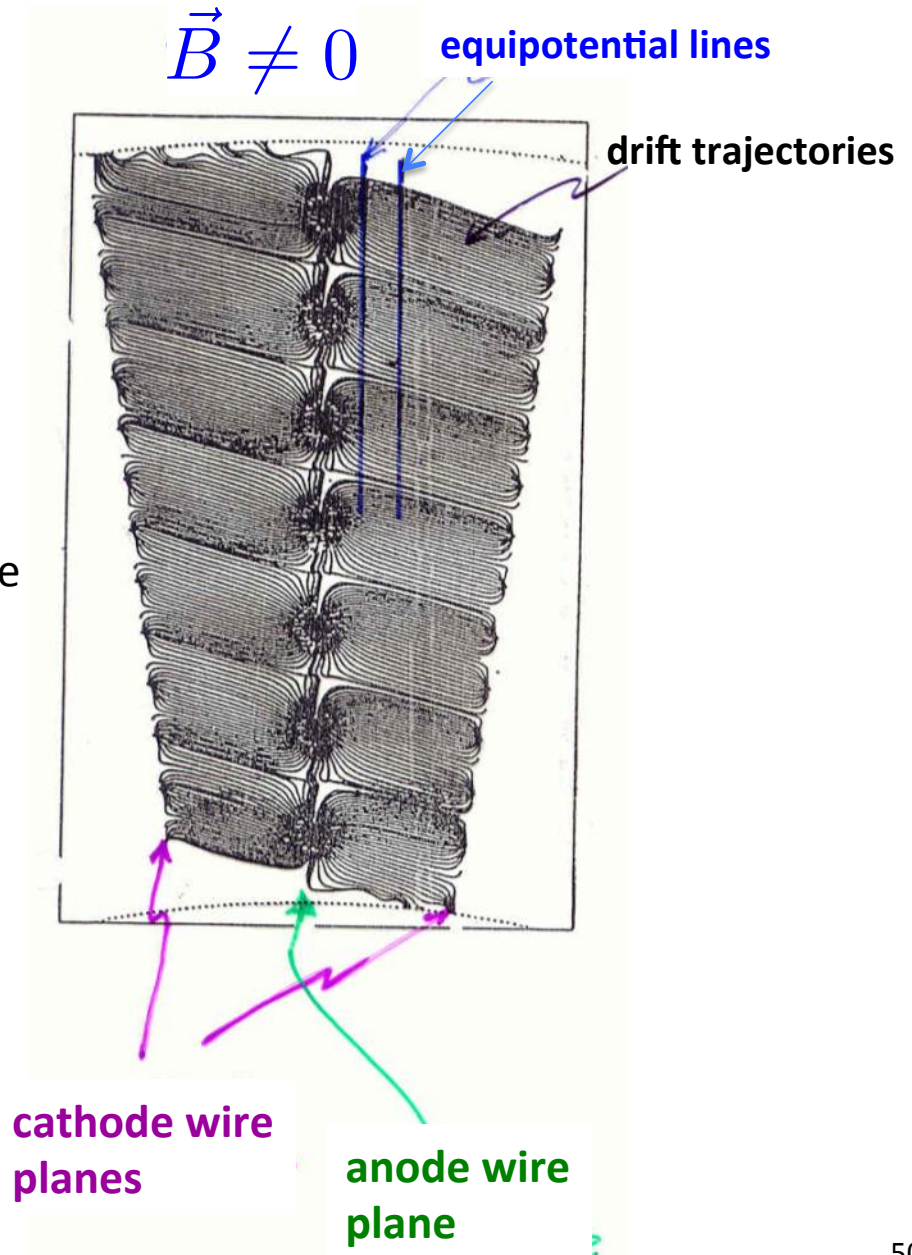
$B = 0$

isochrone-curves  
with  
same drift time to wire



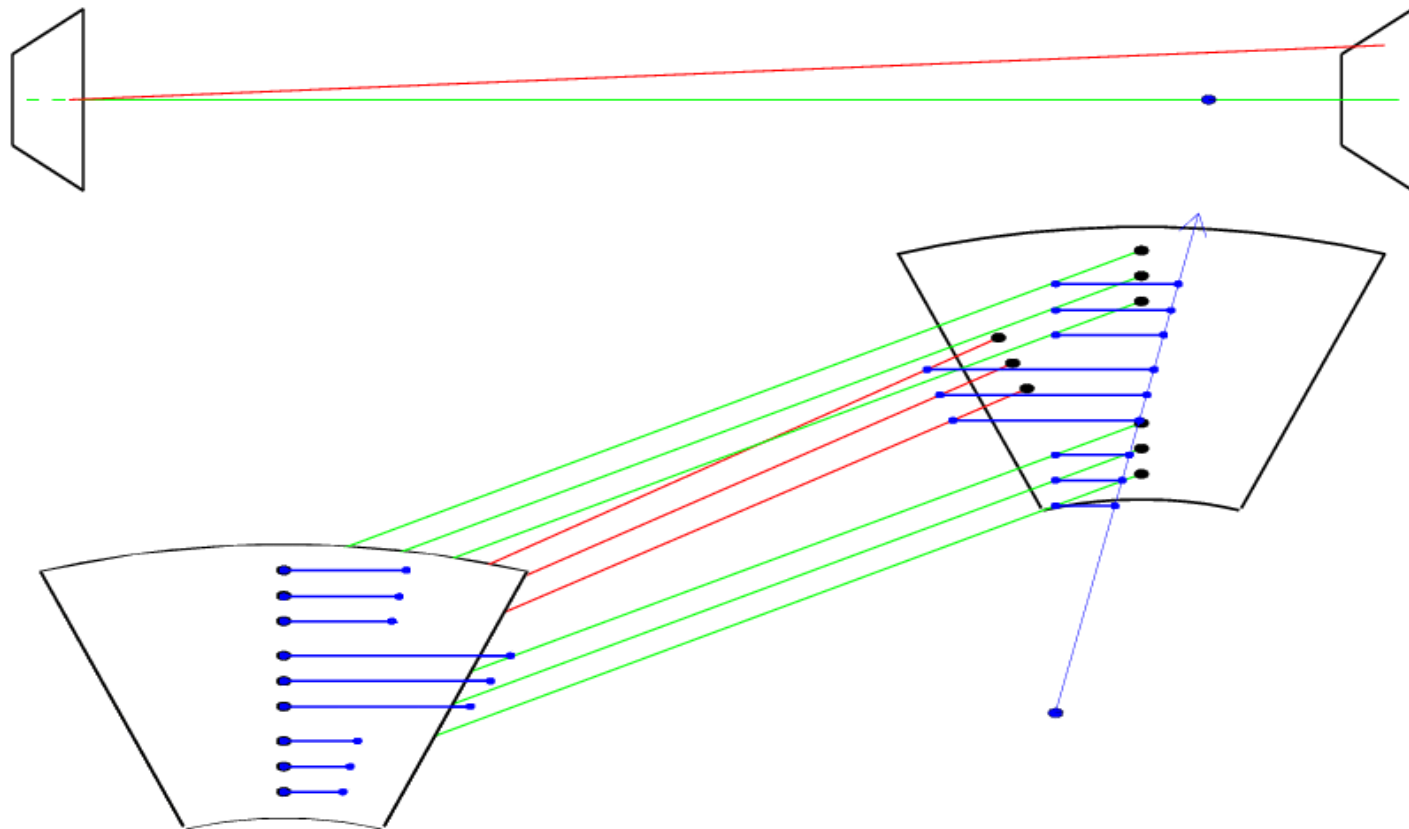
$B = 0.5 \text{ T}$

$B \perp E$



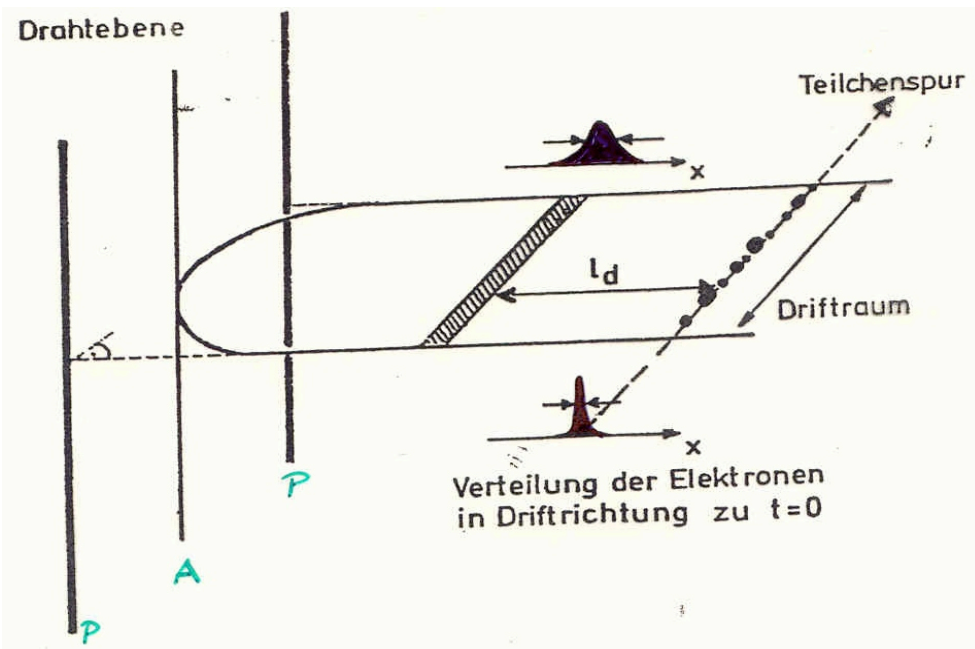


“stereo” wires in a cylindrical geometry



$$\sigma_z = \sigma_{r\phi} \cdot \frac{1}{\sin \alpha_{\text{stereo}}}$$

- + (still) relatively good spatial resolution
- one loses wires for other tasks ( $r\phi$ )
- not practical in high track density



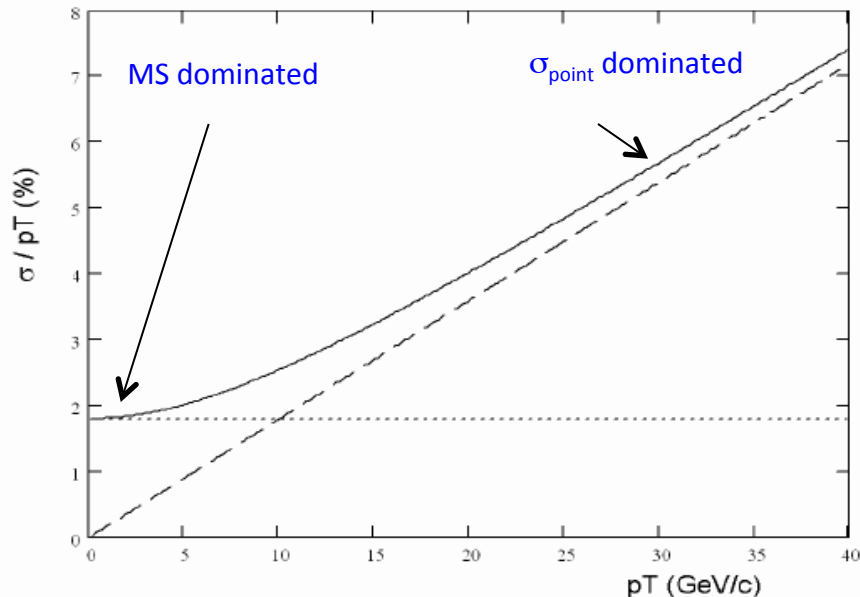
$$\sigma^2_{\text{tot}} = \sigma^2_{\text{point}} + \sigma^2_{\text{multiple scattering}} + \sigma^2_{\text{sys}}$$

- $\sigma_{\text{point}} \rightarrow$
- longitudinal diffusion (  $\sim 1/\text{pressure} \times \sqrt{\text{drift distance}}$  )
  - ionisation statistics  $\sim (\text{distance from wire})^{-1}$
  - time resolution for e-cloud  $\rightarrow$  leading edge discrimination  
Flash ADC timing
- $\sigma_{\text{MS}} \rightarrow$
- $\propto \frac{1}{p} \sqrt{\frac{L}{X_0}}$
- $\sigma_{\text{sys}} \rightarrow$
- wire sagging, electrostatic wire attraction  
torsion of chamber flanges, electric cross-talk

$$\left( \frac{\sigma_{p_T}}{p_T} \right)_{\text{point}} = \frac{p_T}{0.3} \cdot \frac{\sigma_{\text{point}}}{L'^2 B} \sqrt{\frac{720}{N+4}} \quad L' = L \sin \theta$$

$[p_T] = \text{GeV}/c, [L'] = \text{m}, [B] = \text{T}$

$$\left( \frac{\sigma_{p_T}}{p_T} \right)_{\text{MS}} = \frac{0.054}{L' B \beta} \sqrt{\frac{L}{X_0}} \quad [p_T] = \text{GeV}/c, [L, L'] = \text{m}, [B] = \text{T}$$

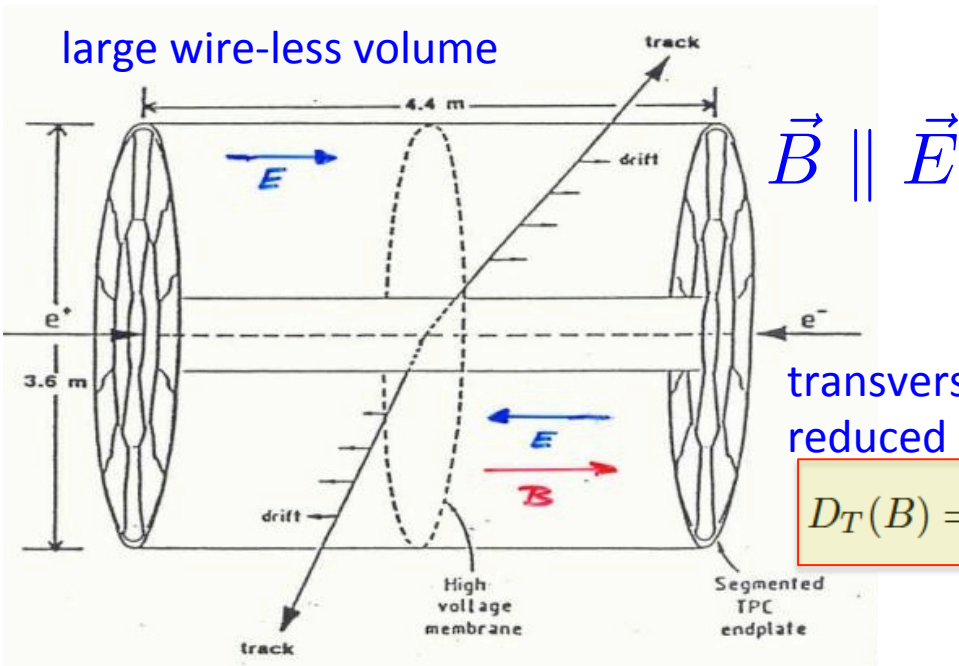


$$L = 2\text{m}, N = 159, \sigma_{\text{point}} = 120 \mu\text{m}$$

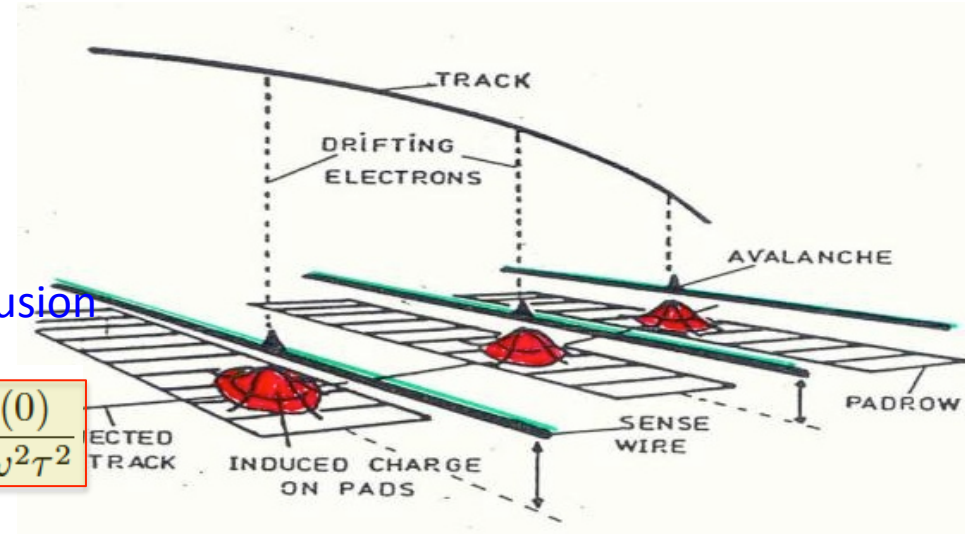
$$\frac{\sigma_{p_T}}{p_T} = \sqrt{(0.15 \% p_T)^2 + (2\%)^2}$$

$$= \begin{cases} 2\% @ 1 \text{ GeV} \\ 7.5\% @ 50 \text{ GeV} \end{cases}$$

large wire-less volume



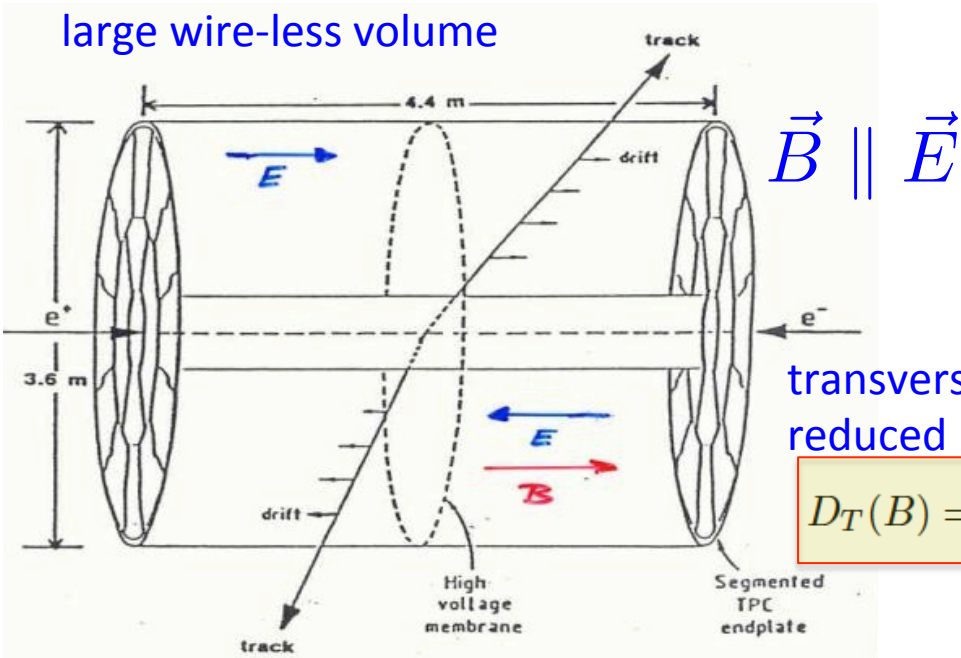
long drift along , amplification at end of long drift



$$D_T(B) = \frac{D_T(0)}{1 + \omega^2 \tau^2}$$

- ☐ full 3-D reconstruction (voxels):  $xy$  from wire/pad geometry at the end flanges;  $z$  from drift time
- ☐ 3D track information recorded -> good momentum resolution
- ☐ also  $dE/dx$  measurement easy -> particle ID (not topic of this lecture)
- ☐ large field cage necessary
- ☐ typical resolutions: in  $z$  and  $y \approx \text{mm}$ , in  $x = 150\text{-}300 \mu\text{m}$
- ☐ challenges
  - long drift time -> limited rate capability
  - large volume -> geometrical precision
  - large voltages (discharges)

large wire-less volume

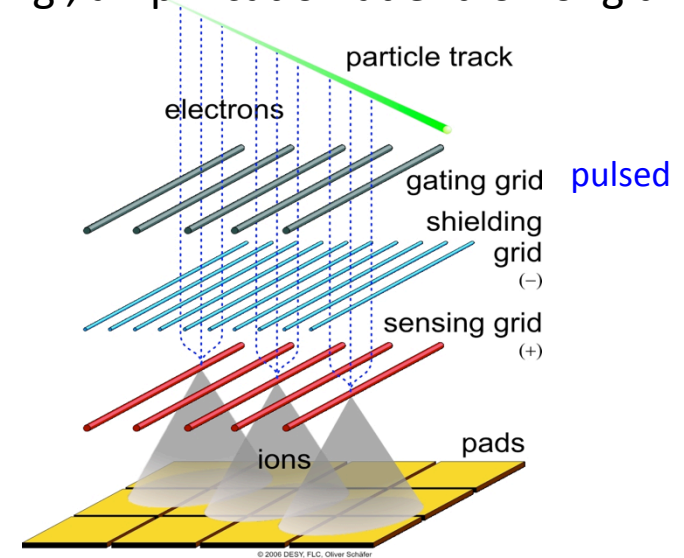


$$\vec{B} \parallel \vec{E}$$

transverse diffusion reduced

$$D_T(B) = \frac{D_T(0)}{1 + \omega^2 \tau^2}$$

long drift along , amplification at end of long drift



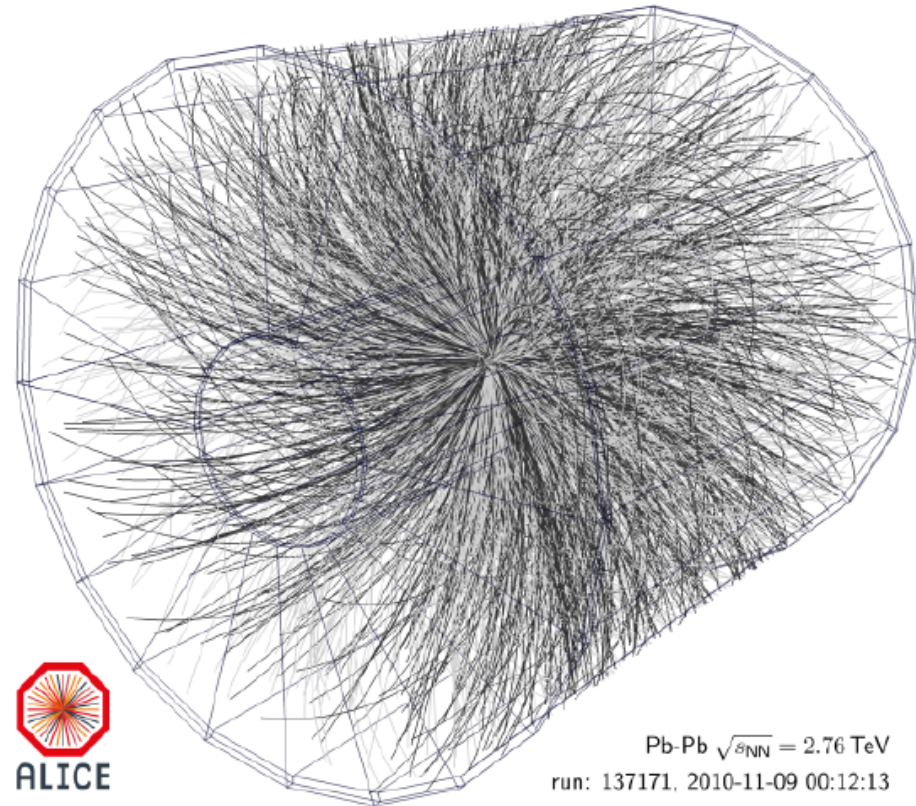
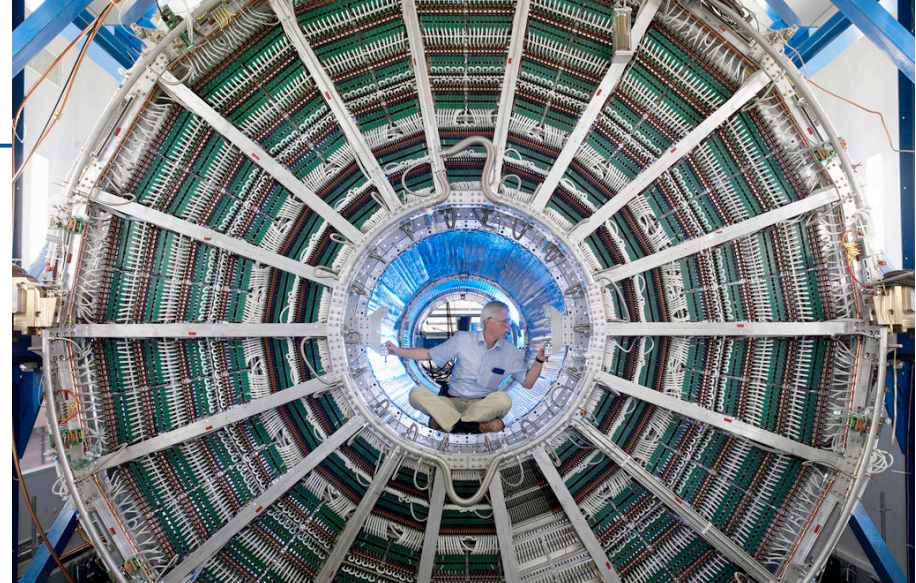
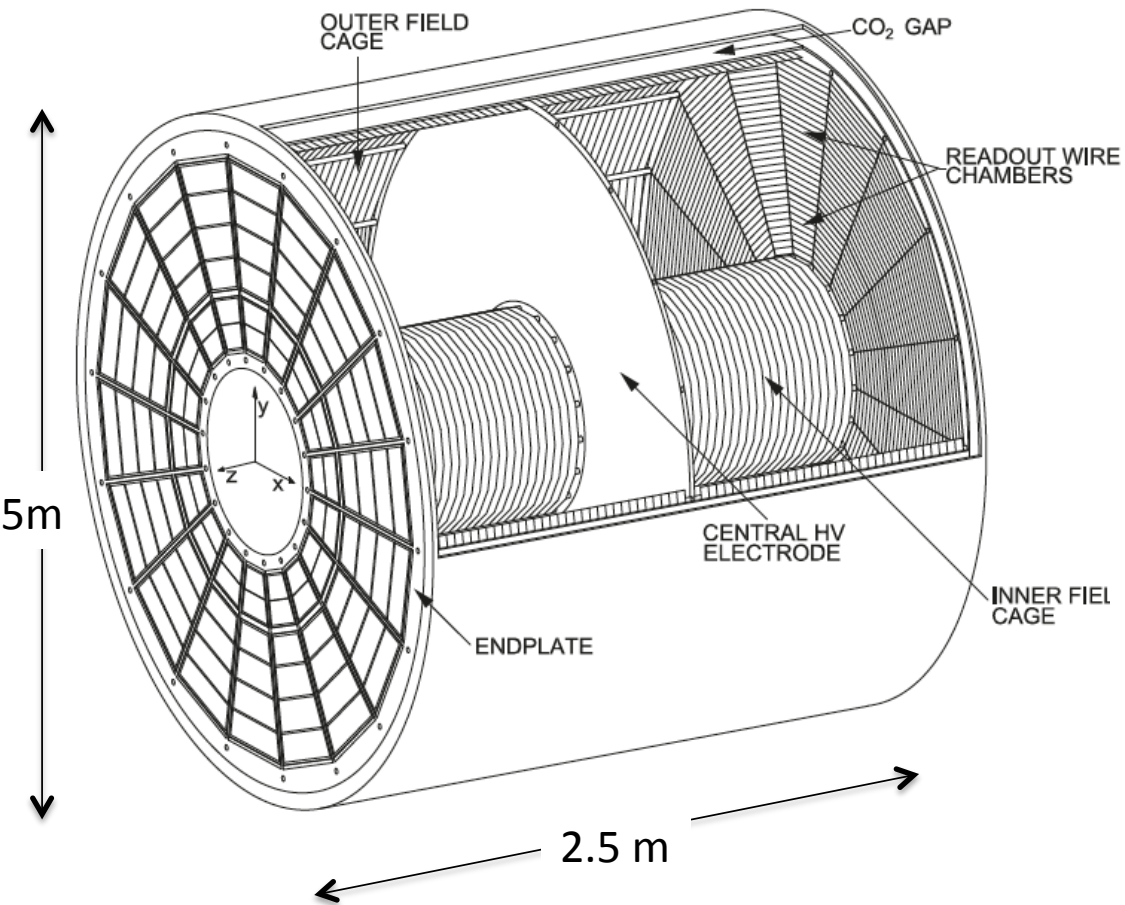
prevent ion-feedback by gating grid

- ☐ full 3-D reconstruction (voxels): **xy** from wire/pad geometry at the end flanges; **z** from drift time
- ☐ 3D track information recorded -> **good momentum resolution**
- ☐ also **dE/dx** measurement easy -> particle ID (not topic of this lecture)
- ☐ large **field cage** necessary
- ☐ typical resolutions: in z and y  $\approx$  **mm**, in x = **150-300  $\mu$ m**
- ☐ **challenges**
  - long drift time -> limited rate capability
  - large volume -> geometrical precision
  - large voltages -> potential discharges

Parameter/Experiment	PEP4 [612]	ALEPH [100]	ALICE [72]
Volume (m <sup>3</sup> )	5	20	26
$\sigma_{r\phi}$ (μm)	130–200	170–450	800–1100
$\sigma_z$ (μm)	160–260	500–1700	1100–1250
Zweispurtrennung (mm), T/L	20	15	13/30
$\sigma_p/p^2$ (GeV <sup>-1</sup> ) ( $p$ groß)	0.0065	0.0012	0.022

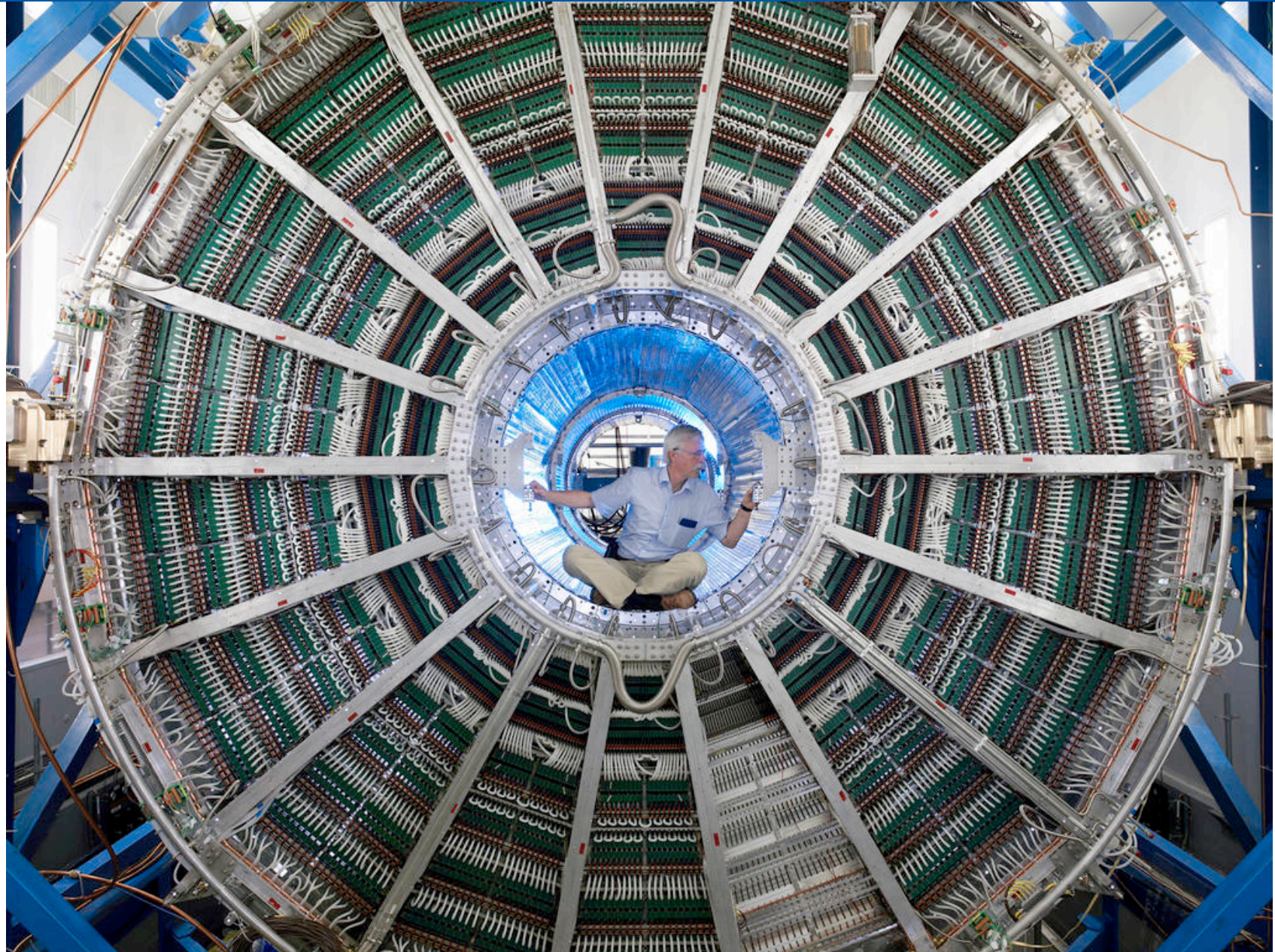


# ALICE TPC



Pb-Pb  $\sqrt{s_{NN}} = 2.76$  TeV  
run: 137171, 2010-11-09 00:12:13







# New developments in the context of high rate applications (i.e. LHC)

# What is different at the LHC (pp experiments)?

□ particle rates ( $\mathcal{L} = 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ )

note: heavy ions:  $\mathcal{L} = 10^{27} \text{ cm}^{-2} \text{ s}^{-1}$

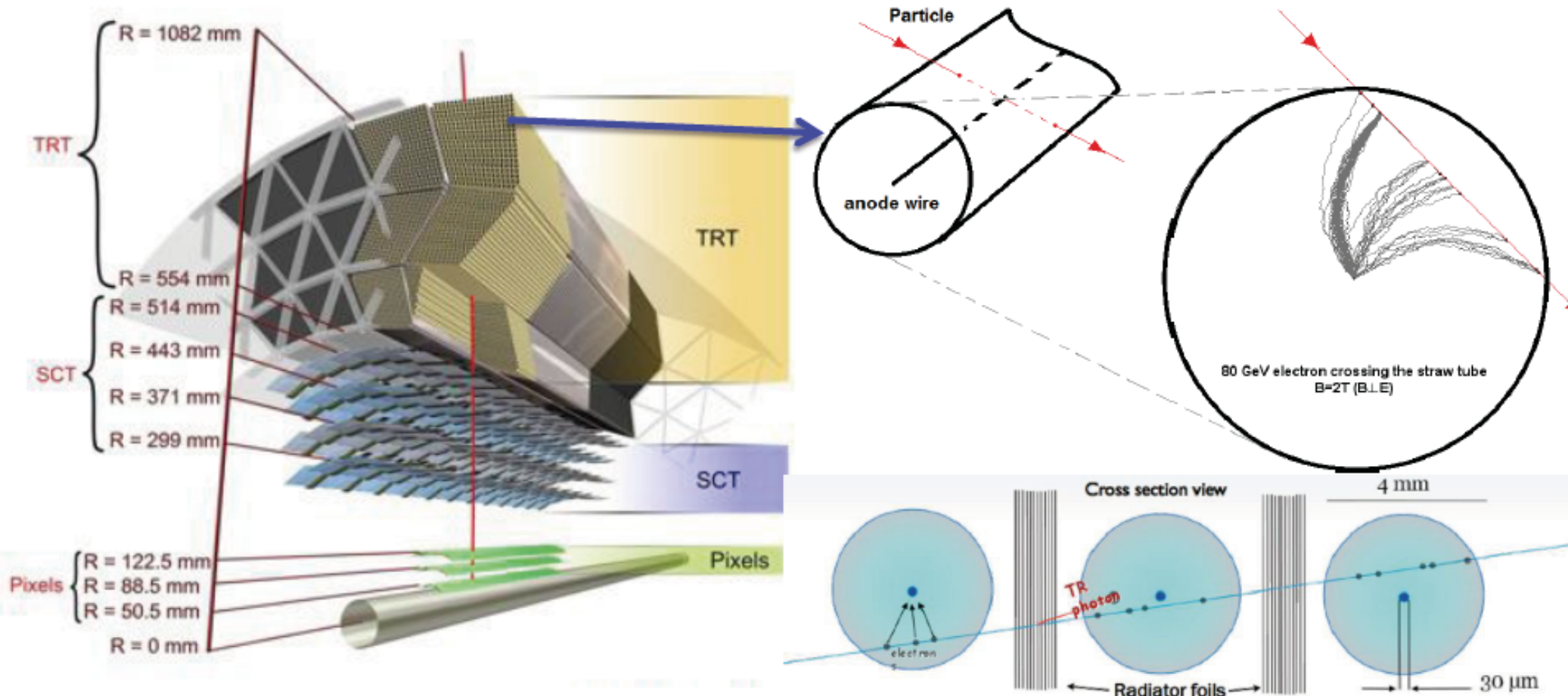
- bunch crossing every 25 ns
- $N_{\text{trk}} = \sigma \mathcal{L} = 100 \text{ mb} \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1} \times 120 \approx 10^{11} \text{ tracks/s in } 4\pi$   
this is **10<sup>6</sup> times** the track rate at **LEP**
- @  $r = 5 \text{ cm} \Rightarrow 9.5 \text{ tracks/cm}^2/25 \text{ ns}$  but only  $10^{-4}$  per pixel ( $100 \times 100 \text{ } \mu\text{m}^2$ )

□ radiation level (@  $r = 5 \text{ cm}$ , per detector lifetime)

- ionizing dose = energy/mass (J/kg) = 100 Mrad
- non ionizing fluence (breaks the lattice) =  $10^{15}$  particles per  $\text{cm}^2$
- affects ageing on wires, electronics, ...

□ way out

- **high granularity**, small cells
- high **timing precision**  $\ll 25 \text{ ns}$
- **solid state detectors** ( $\rightarrow$  lecture 3)
  - micro structuring  $\Rightarrow$  highest granularity
  - but: sensitive to radiation (different to gaseous detectors at moderate gas gains)



**ATLAS ID Barrel**

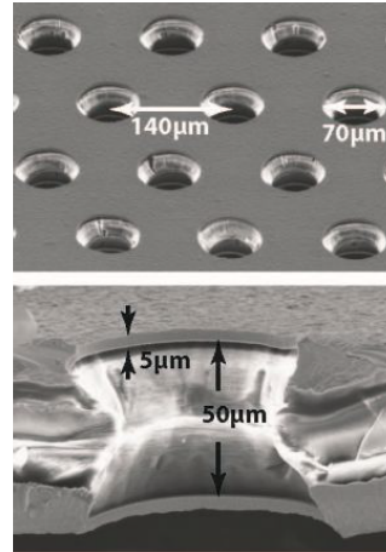
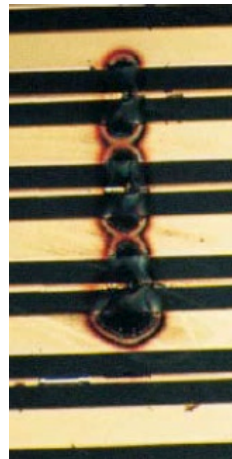
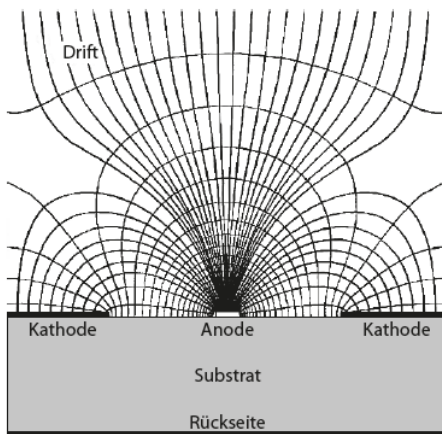
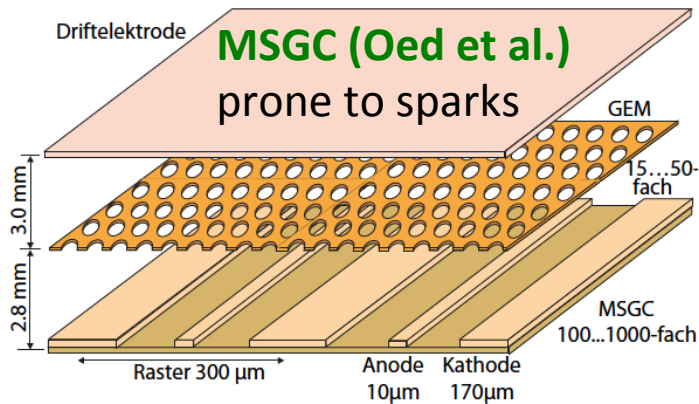
- diameter = 4 mm
- $\sim 36$  hits along a barrel track
- can better cope with high rates due to individual units and short drift distances
- gas: Xe - CO<sub>2</sub> - O<sub>2</sub> (70%:27%:3%)
- serves as tracker and e- ID at the same time

# MPGCs (Micro Pattern Gas Detectors)

❑ advances in micro structuring also entered clever chamber designs

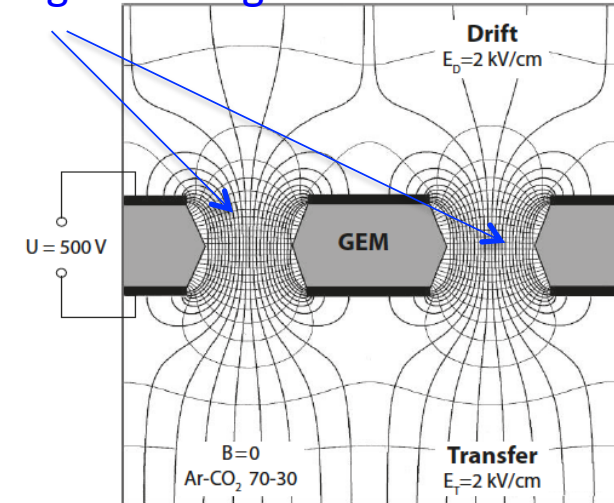
❑ goals:

- thin gap
- high rate capability (100 x MWPC)
- high resolution

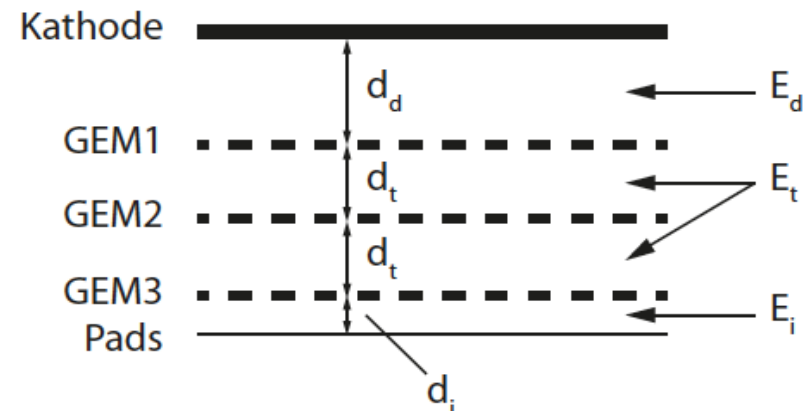


**GEM**  
(Sauli et al.)

high field regions

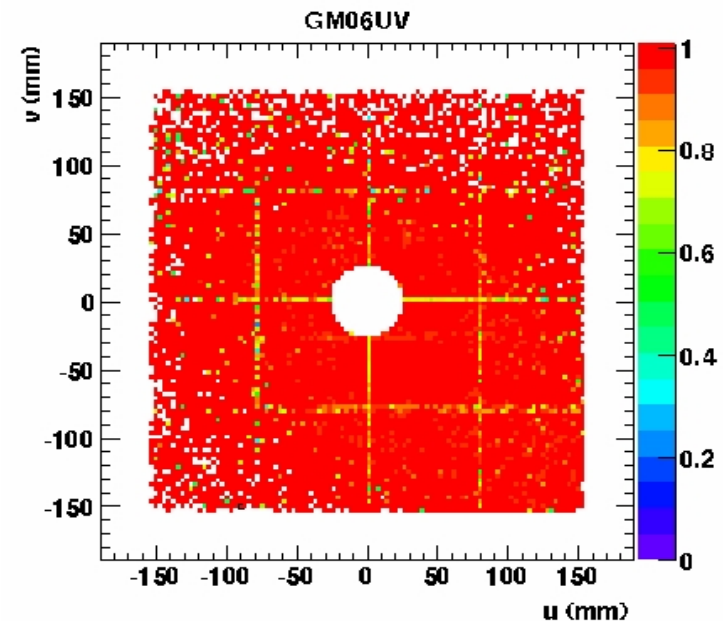
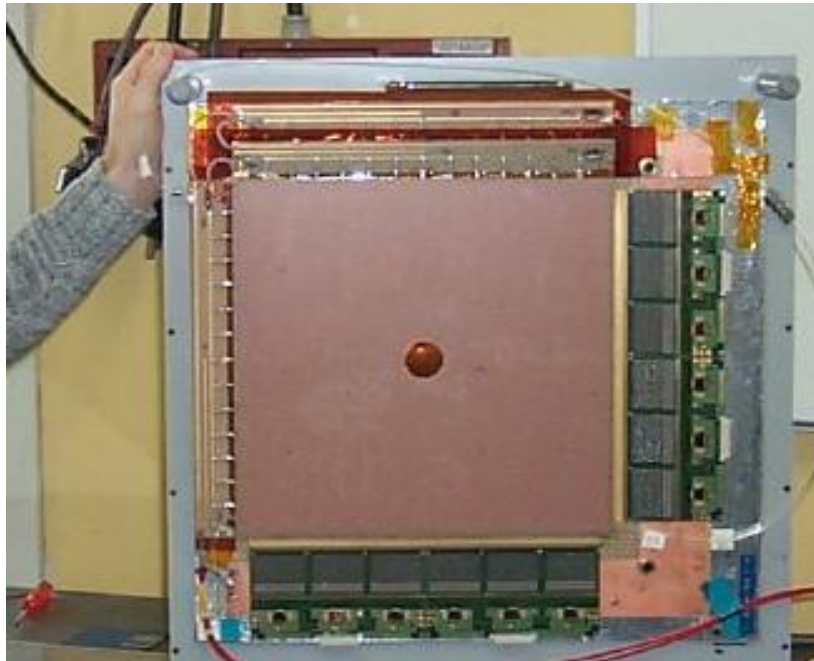
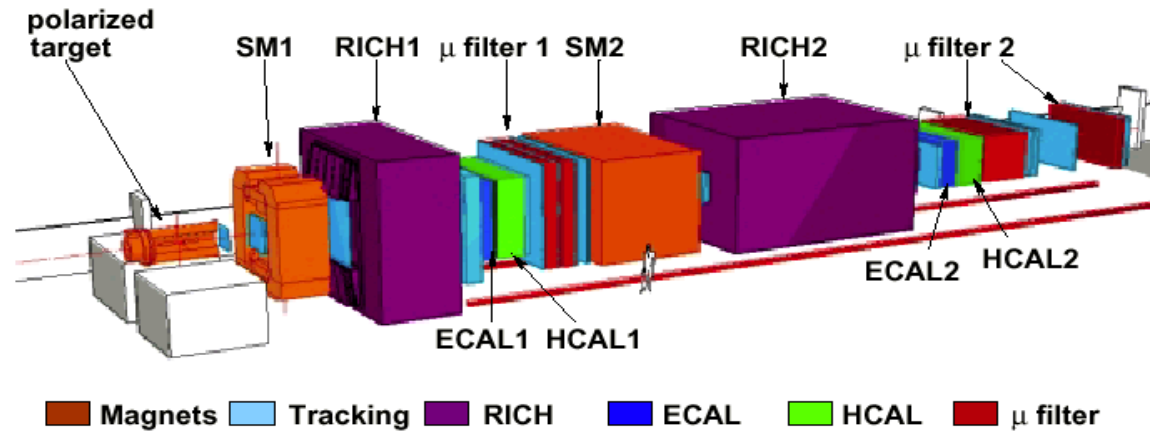


**today's standard: Triple GEMs (stand alone detectors)**



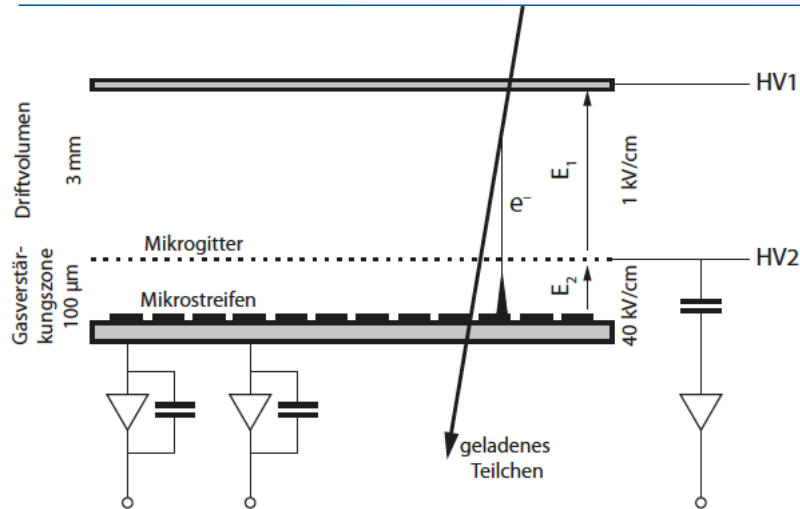
# Example: GEM tracker in COMPASS

COMPASS Magnetic Spectrometer  
22 TRIPLE GEMs

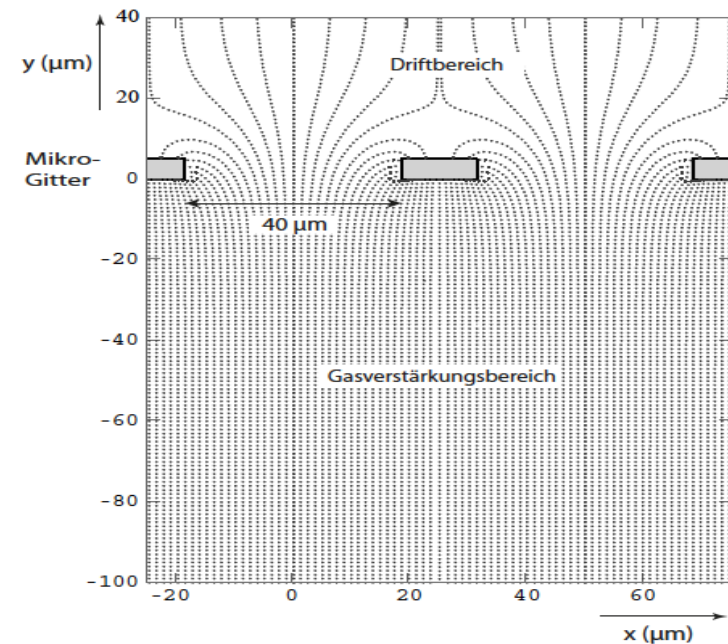


UNIFORMITY OF TRACKING EFFICIENCY

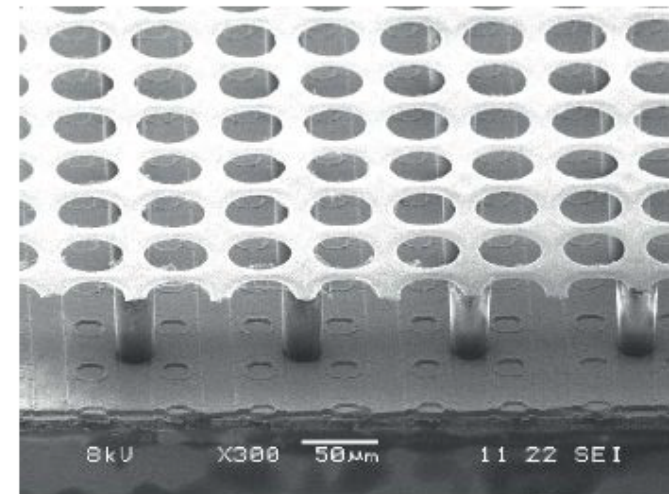




- separation of drift region and (short) amplification region by a **micro grid**
- R/O of induced charges by **patterned electrode**
- fast induced signals
- need precise grid alignment
- new development: **INGRID** structure obtained by “post processing” of grid directly on R/O chip

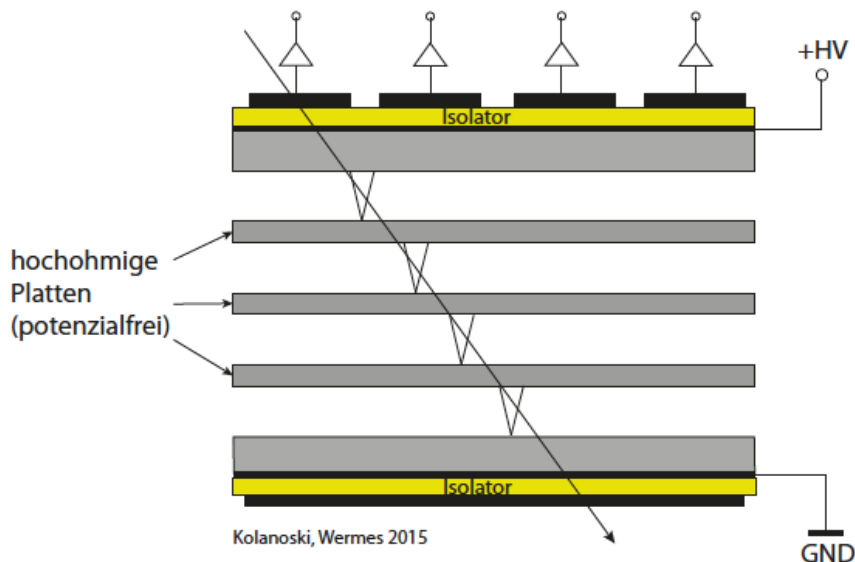
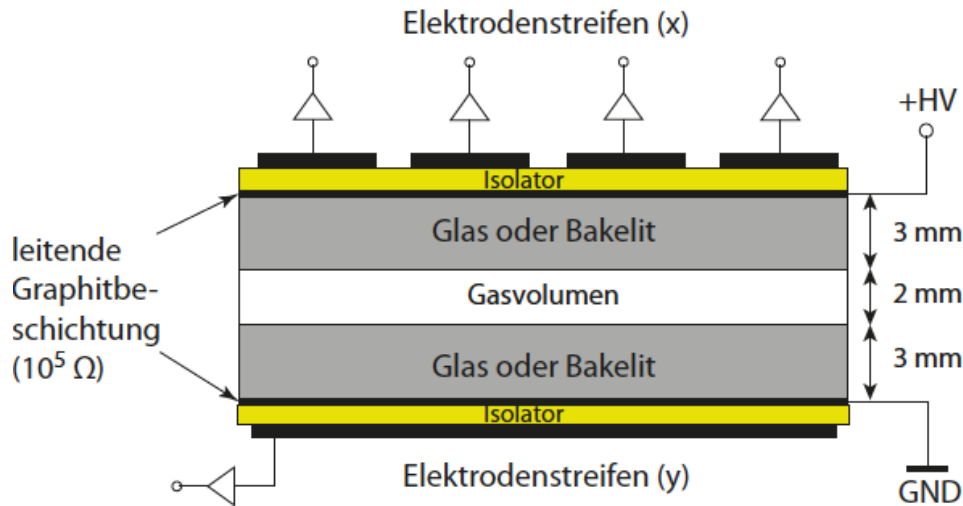


**INGRID** structure



# RPCs (resistive plate chambers)

- target **high timing precision** (trigger and timing chambers, e.g. ATLAS Muon Spectrometer)



Kolanoski, Wermes 2015

- use **high ohmic** ( $10^8$ - $10^{12} \Omega \text{ cm}$ ) plates (glass, bakelit) with **small gap** (2mm)
- operation ( $\sim 10 \text{ kV}$ ) in **avalanche** (shorter quench times) or **streamer** mode (larger and faster signals)
- induced signals **reach through** to patterned electrodes
- large signals**:  $< 100 \text{ pC}$  streamer,  $< 10 \text{ pC}$  avalanche
- gas with **high ionisation density** and **high quenching efficiency** needed:  
e.g. 94.7%  $\text{C}_2\text{H}_2\text{F}_4$ , 5% i -  $\text{C}_4\text{H}_{10}$ , 0.3%  $\text{SF}_6$

Trigger-RPC	avalanche mode	Timing-RPC	streamer mode
$E = 50 \text{ kV/cm}$		$E = 100 \text{ kV/cm}$	
$\alpha = 13.3/\text{mm}$	$\eta = 3.5/\text{mm}$	$\alpha = 123/\text{mm}$	$\eta = 10.5/\text{mm}$
$v_D = 140 \mu\text{m/ns}$	$d = 2 \text{ mm}$	$v_D = 210 \mu\text{m/ns}$	$d = 0.3 \text{ mm}$
$\sigma_t = 1 \text{ ns}$		$\sigma_t = 50 \text{ ps}$	
$\epsilon = 98\%$		$\epsilon = 75\%$	

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# End of Lecture 2