



Simulations of ultralight axion dark matter halos

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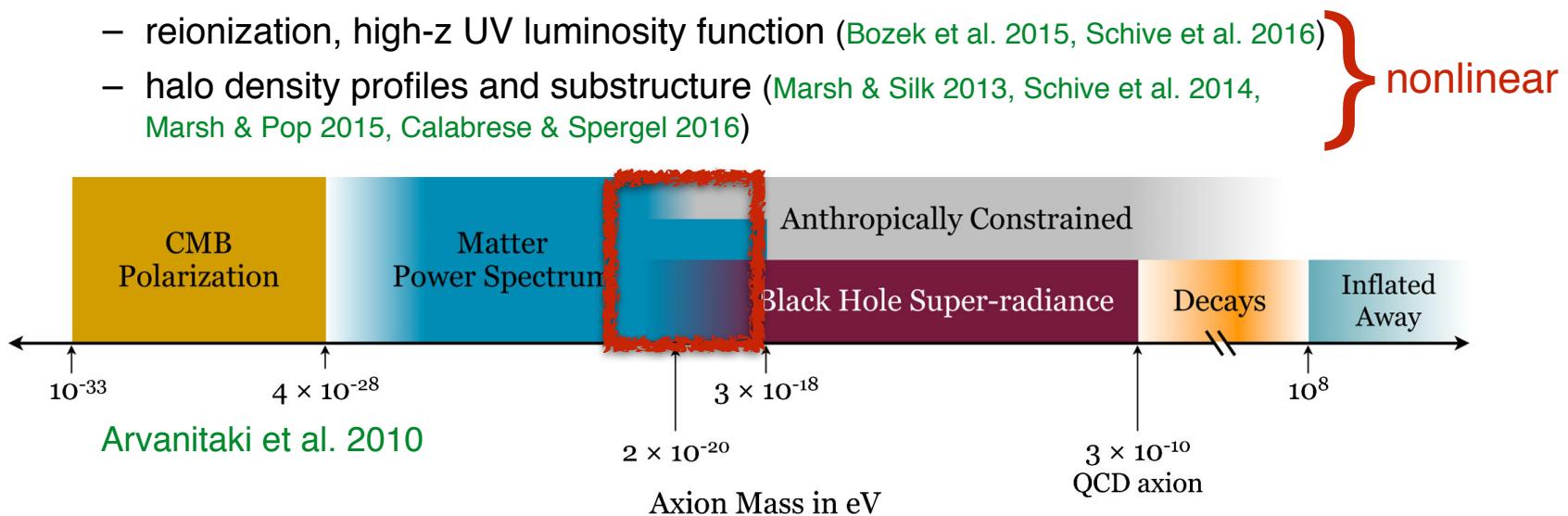
Overview

3 kinds of simulations, from small to large scales:

- Grid-based Schrödinger-Poisson simulations: **mergers of solitonic halo cores** ([arXiv:1606.05151](#))
- Particle-mesh Madelung-Poisson simulations:
cosmological simulations with and without „quantum pressure“ ([arXiv:160x.xxxxx](#))
- Stochastic merger trees and semi-analytic models for subhalo evolution: **subhalo and core mass function** ([arXiv:160x.xxxxx](#))

Ultralight Axion Dark Matter

- Conceptual overlap of „scalar field DM“, „BEC DM“ (Gross-Pitaevskii equ.), „ultralight axion DM“, and „fuzzy DM“ ([Hu et al. 2000](#)), albeit with different particle physics and/or cosmological motivations
- Production by *misalignment* (non-thermal) → **cold condensate**
- Small mass → large occupation numbers → **classical field equations**
- $H \ll m, k$ → **Newtonian dynamics**
- Change background expansion and growth of structure → constraints from:
 - CMB, LSS ([Hlozek et al. 2015](#))
 - reionization, high-z UV luminosity function ([Bozek et al. 2015, Schive et al. 2016](#))
 - halo density profiles and substructure ([Marsh & Silk 2013, Schive et al. 2014, Marsh & Pop 2015, Calabrese & Spergel 2016](#))



ULAs and small-scale structure

- „Quantum pressure“ prevents gravitational collapse of structures \sim below de Broglie wavelength (e.g., Hu et al. 2000):

$$v \sim (G\rho)^{1/2}r \quad \Rightarrow \quad \lambda \sim (mv)^{-1} \sim m^{-1}(G\rho)^{-1/2}r^{-1}$$

- This introduces a „Jeans length“ $r_J = \lambda = r$:

$$\begin{aligned} r_J &= 2\pi/k_J = \pi^{3/4}(G\rho)^{-1/4}m^{-1/2}, \\ &= 55m_{22}^{-1/2}(\rho/\rho_b)^{-1/4}(\Omega_m h^2)^{-1/4}\text{kpc} \qquad \qquad m_{22} = m/10^{-22}\text{eV} \end{aligned}$$

- This mass range may solve some of the small-scale problems (missing satellites, cusp-core, too-big-to-fail) (Marsh & Silk 2013) but is already under pressure from high-z UV sources (Bozek et al. 2014).

Cosmological simulations with ULA dark matter

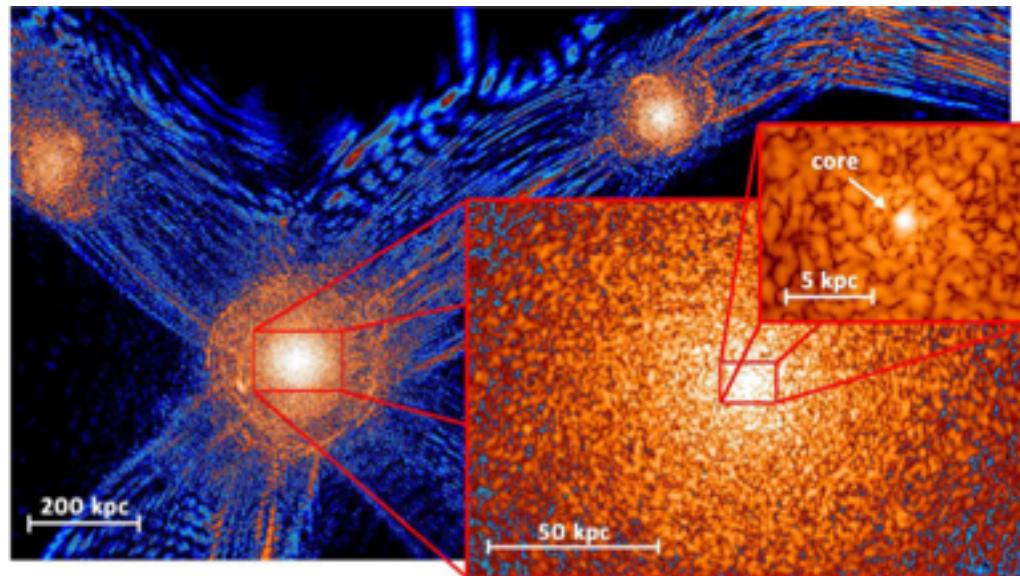
- In the Newtonian limit, ULAs obey the Schrödinger-Poisson (SP) equations:

$$i\hbar \frac{\partial \psi}{\partial t} = -\frac{\hbar^2}{2a^2m} \nabla^2 \psi + mV\psi$$

$$\nabla^2 V = 4\pi G a^2 \delta \rho = \frac{4\pi G}{a} \rho_0 (|\psi|^2 - 1)$$

(SP equations also proposed for numerical solution of coarse-grained Vlasov equation for CDM by [Widrow & Kaiser 1993](#))

- First $(2 \text{ Mpc})^3$ simulation resolving **solitonic halo cores** by [Schive et al. 2014](#):



Nyx

Almgren et al. 2013

- cosmology code developed at LBNL (Berkeley)
- C++ / fortran, MPI + OpenMP parallelized
- block-structured adaptive mesh refinement (AMR)
- unsplit PPM hydro scheme + particles + particle-mesh gravity
- star particles with feedback + multi-phase ISM model

additional physics:

- ULA dark matter (two alternative methods):
 1. Schrödinger solver (implicit or explicit)
 2. particle-mesh solver for Madelung equations:

$$\dot{\rho} + \nabla(\rho\mathbf{v}) = 0 \quad \dot{\mathbf{v}} + (\mathbf{v} \cdot \nabla)\mathbf{v} = -\nabla(Q + V)$$

$$\mathbf{v} = m^{-1} \nabla S$$

$$Q = -\frac{\hbar^2}{2m^2} \frac{\nabla^2 \sqrt{\rho}}{\sqrt{\rho}}$$

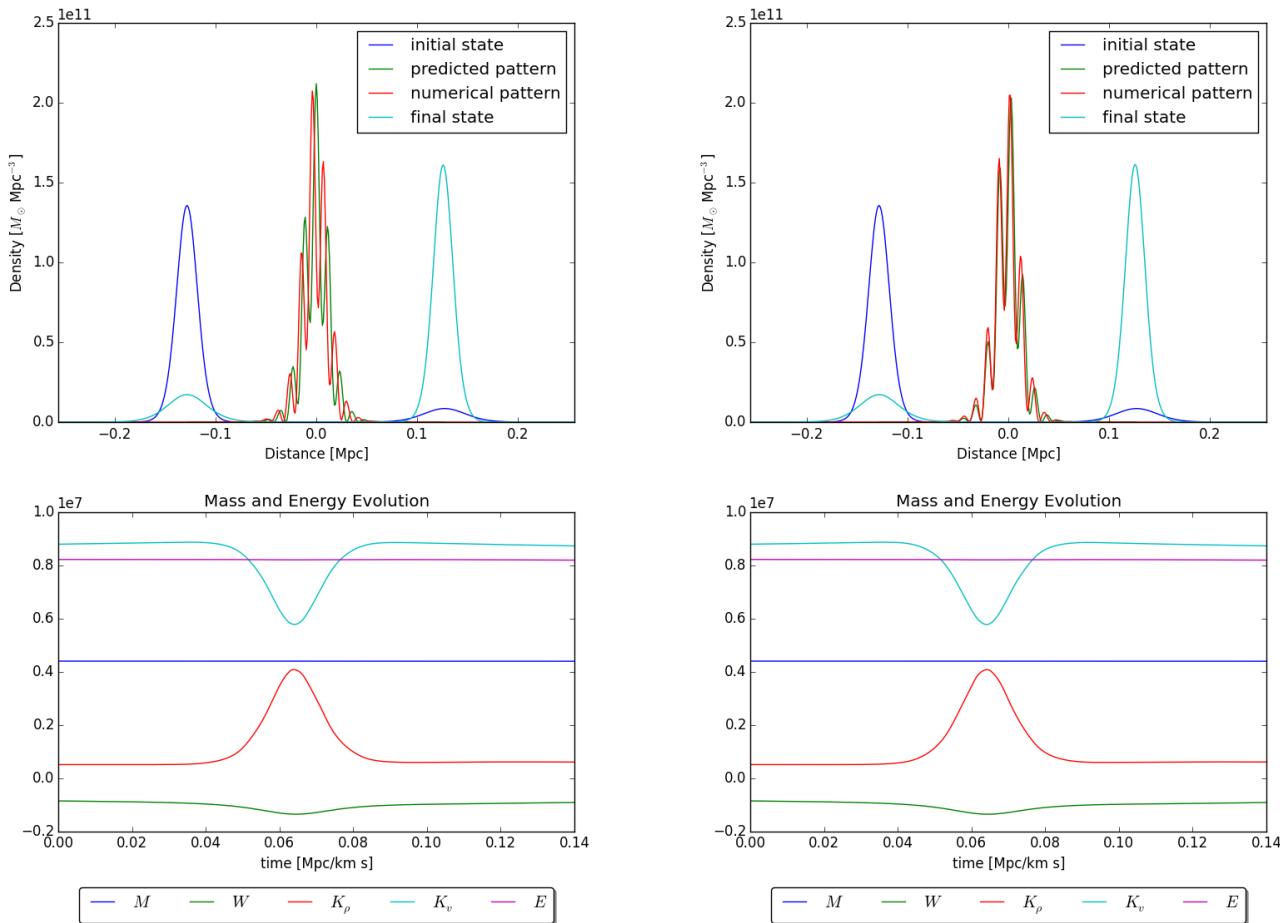
„quantum pressure“

Schrödinger-Poisson simulations of merging solitonic cores

(Schwabe,JN,Engels; arXiv:1606.05151)

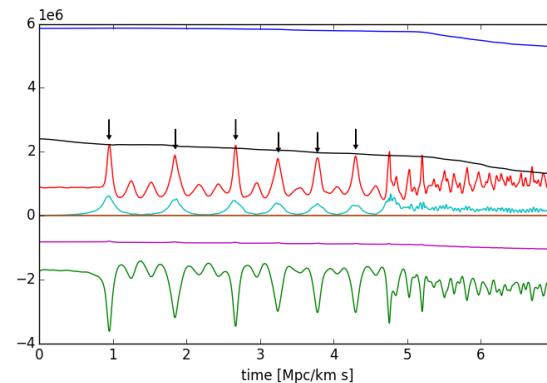
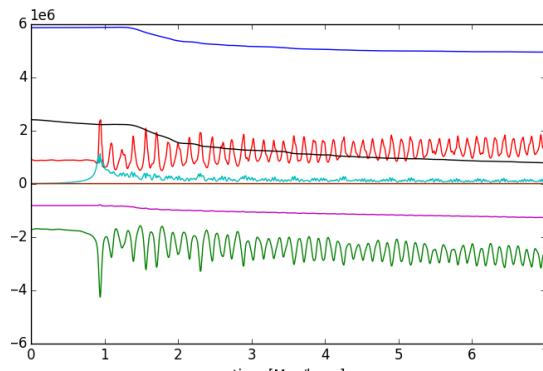
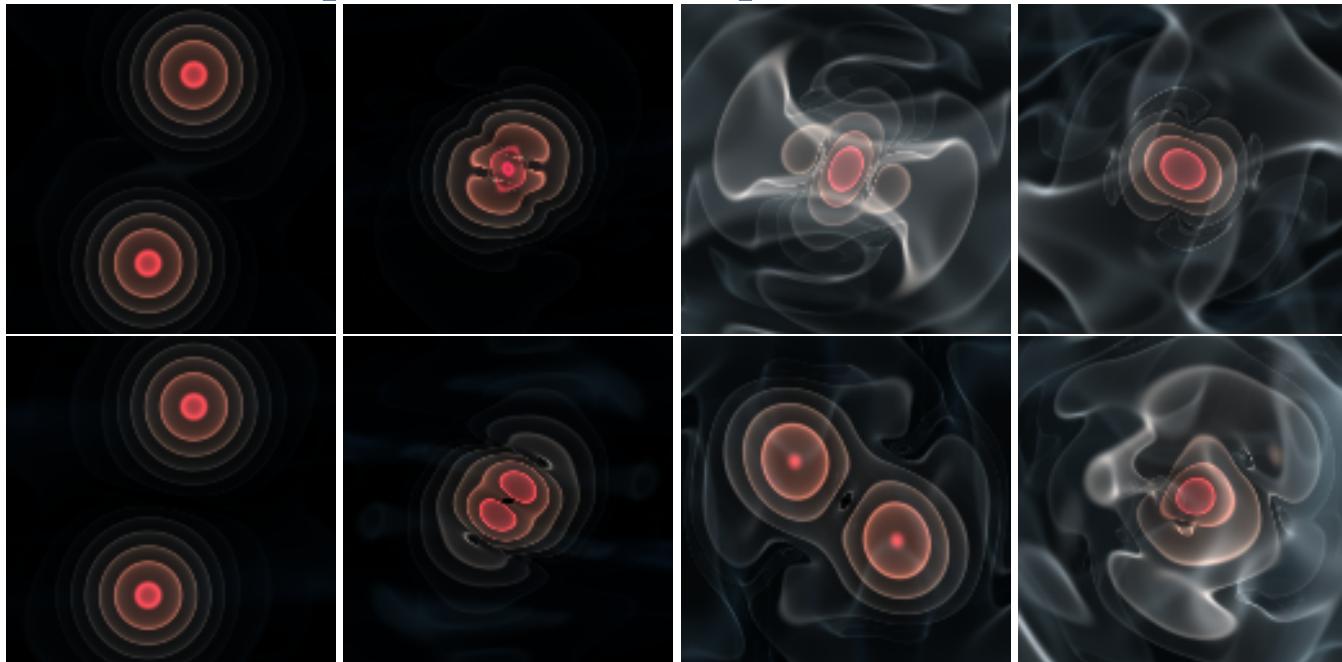
- Motivation: cosmological simulations (Schive et al. 2014) find formation of **solitonic halo cores**, i.e. Newtonian oscillaton solutions a.k.a. boson stars.
- Potential observable consequences:
 - dwarf galaxy cores (Marsh & Pop 2015, Calabrese & Spergel 2016)
 - offset between dark and visible matter in Abell 3827 from DM cores in phase opposition (Paredes & Michinel 2015)
 - halo substructure (e.g. from lensing power spectrum)
 - first stars / SMBH seeds
 - reionization
- Simulate core mergers to measure:
 - mass loss from **gravitational cooling**
 - dependence on mass ratio, angular momentum, total energy, relative phase
 - density profile of final core + halo

Unbound core collisions

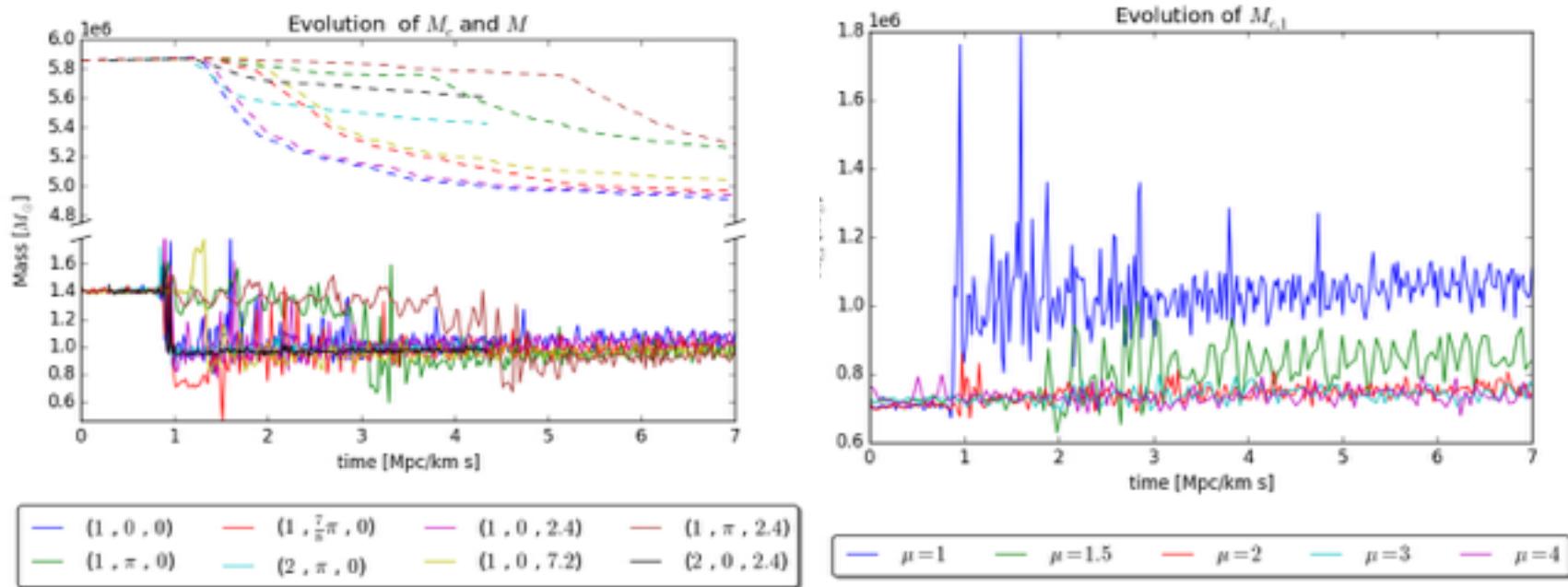


Structure formation with ultra-light axions

Bound binary mergers: phase dependence

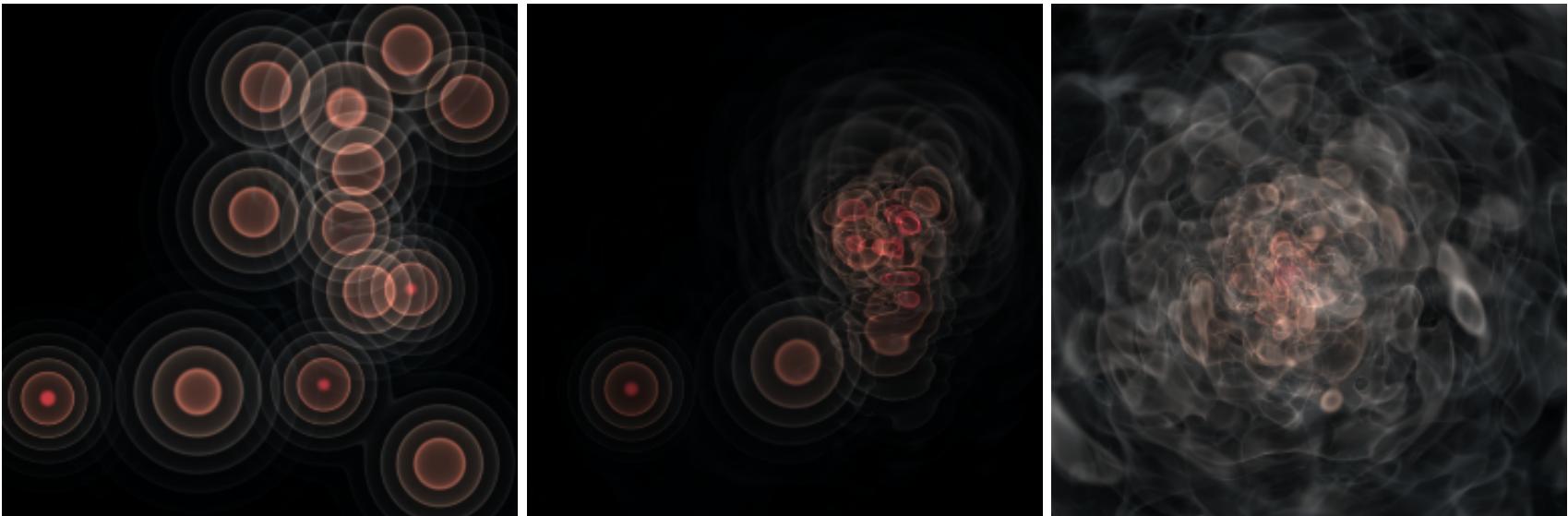


Bound binary mergers: summary

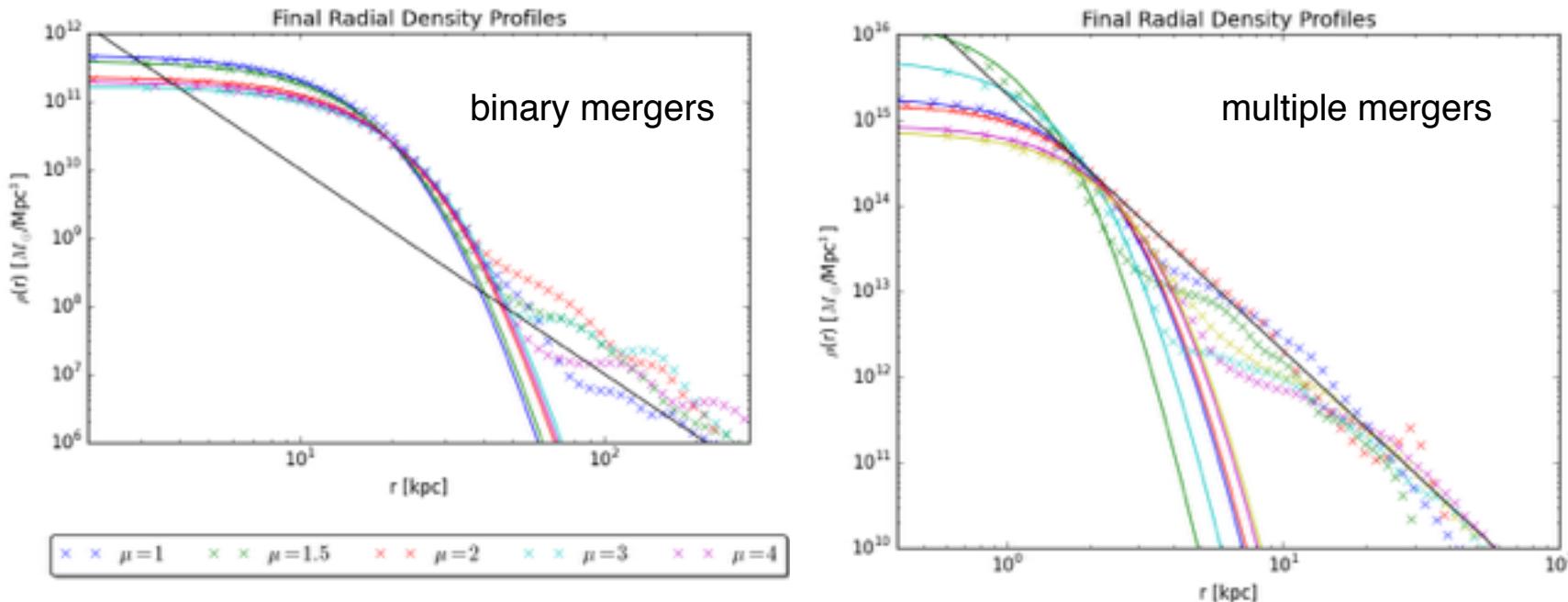


- final core mass practically independent of:
 - angular momentum
 - phase (bounces only for exact phase opposition)
- weak dependence on:
 - total energy
 - mass ratio (no growth of more massive core for $\mu > 2$)

Mergers of multiple cores (random phases and mass ratios)

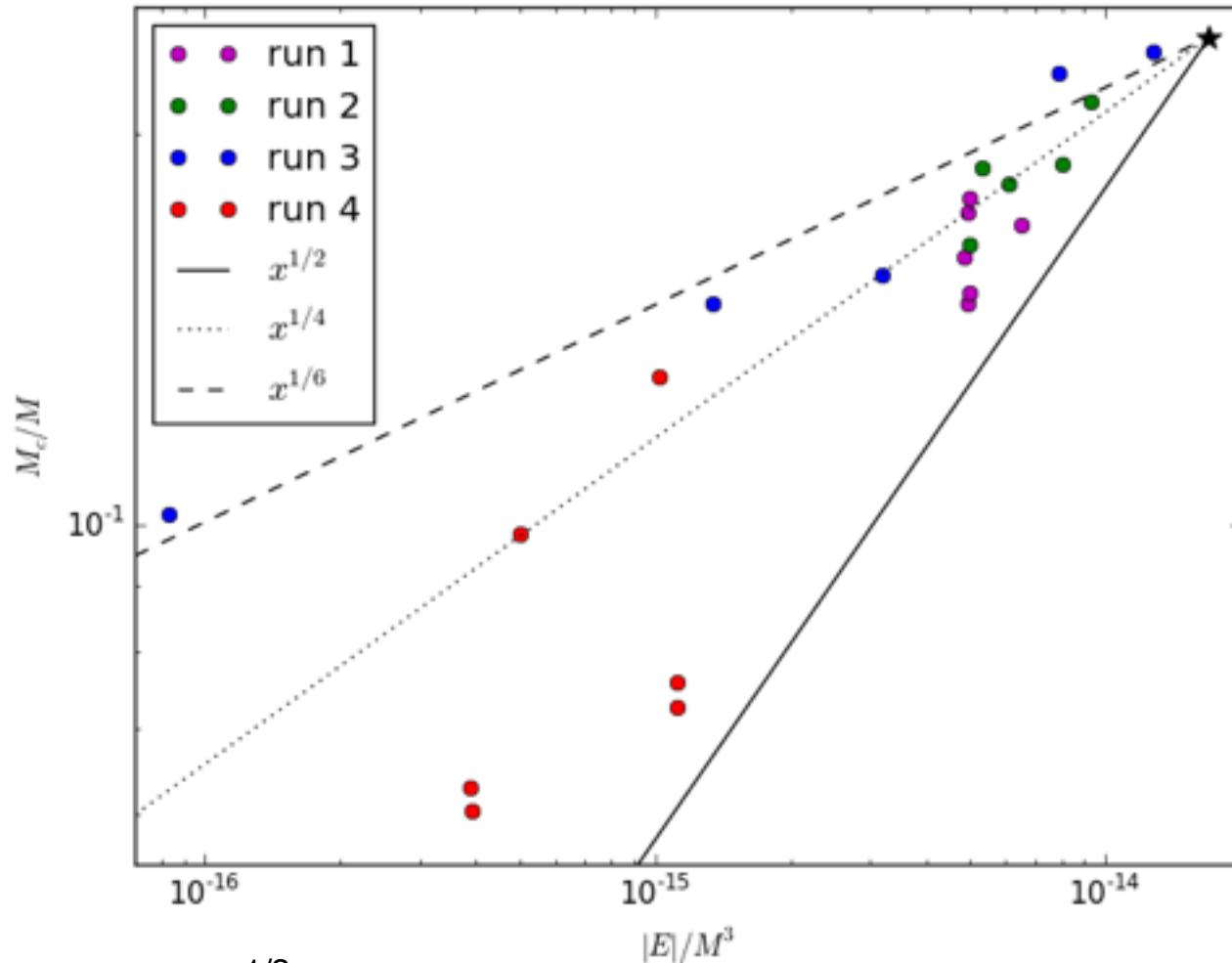


Density profiles for binary and multiple mergers



- **core** follows solitonic boson star profile
- **halo** has logarithmic slope of -3 like outer part of NFW profile
- agrees with cosmological simulation ([Schive et al. 2014](#))

Dependence on total energy



- $M_c \sim (|E|/M)^{1/2}$ found by Schive et al. 2014 not confirmed
- possible reason for spurious detection: residual scale invariance of SP equations (eliminated above by normalization to M)

Particle-Mesh Simulations of the Madelung-Poisson Equations

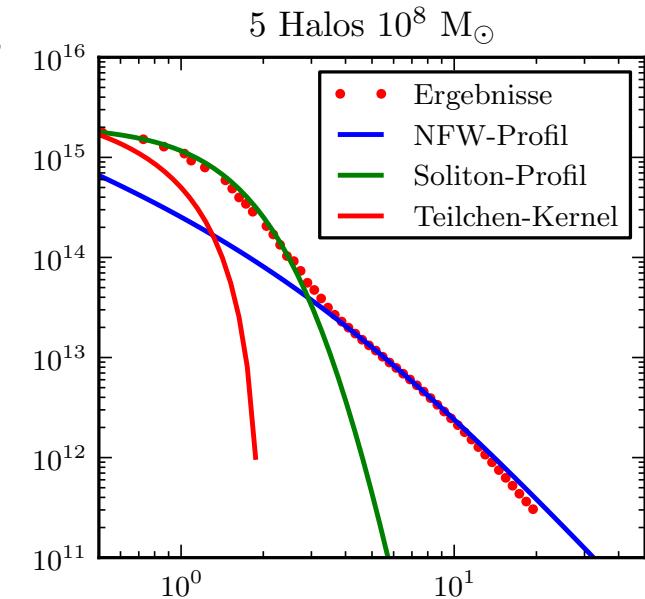
(Veltmaat & JN)

- Madelung transformation of Schrödinger-Poisson equations:

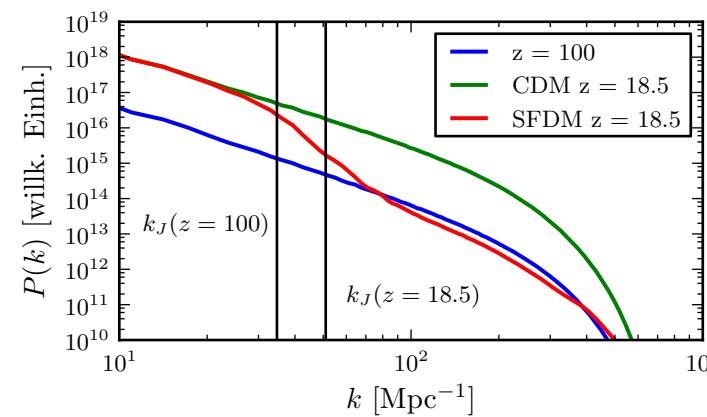
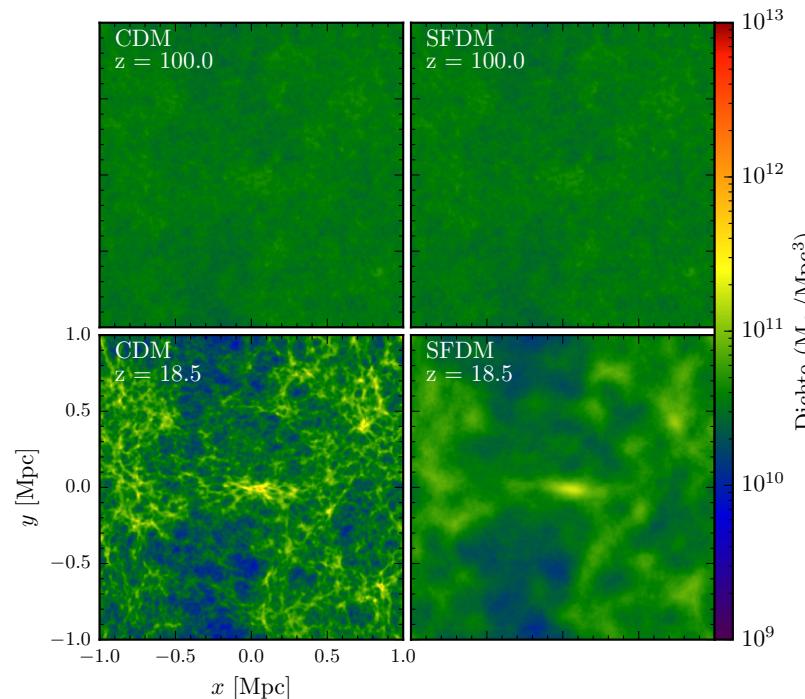
$$\Psi = \sqrt{\frac{\rho(\mathbf{x}, t)}{m}} \exp(iS(\mathbf{x}, t)/\hbar) \quad \mathbf{v} = m^{-1} \nabla S \quad Q = -\frac{\hbar^2}{2m^2} \frac{\nabla^2 \sqrt{\rho}}{\sqrt{\rho}}$$

$$\dot{\rho} + \nabla(\rho\mathbf{v}) = 0 \quad \dot{\mathbf{v}} + (\mathbf{v} \cdot \nabla)\mathbf{v} = -\nabla(Q + V)$$

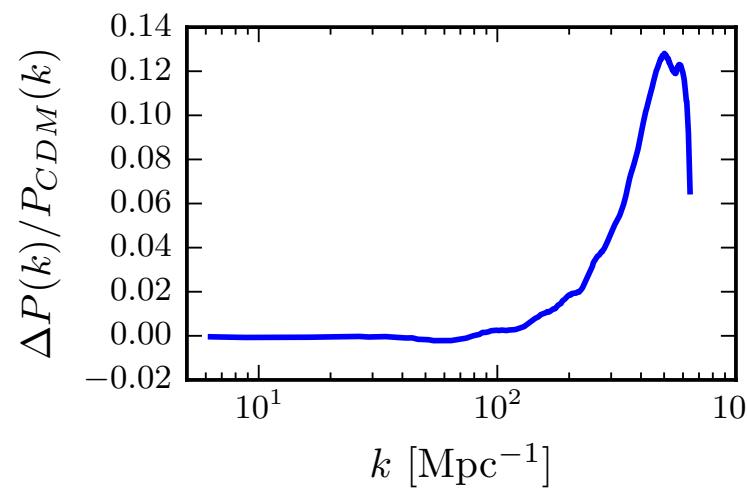
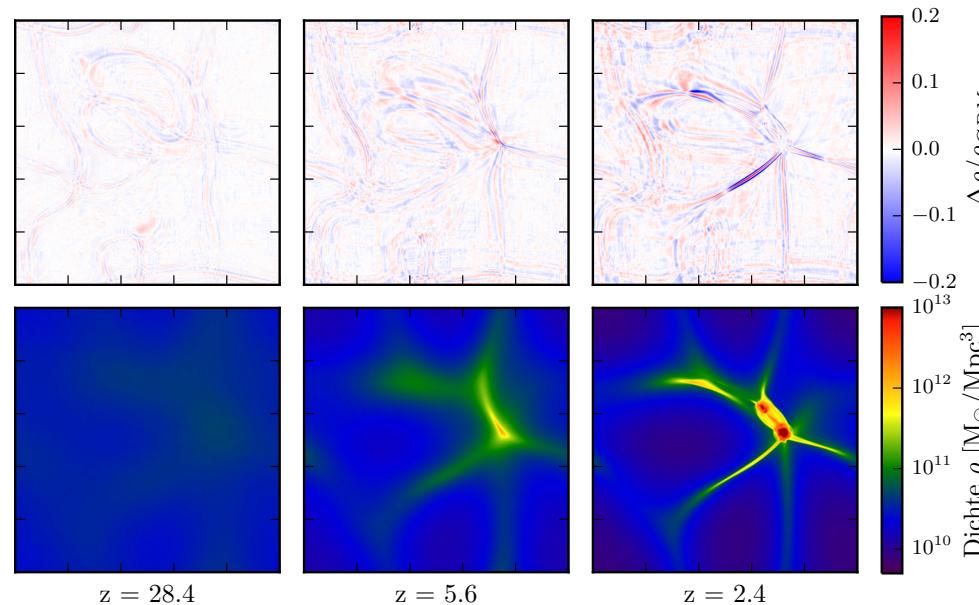
- SPH-like implementation of Q with energy conserving formalism
- tested with binary / multiple core mergers
- core collisions / mergers:
 - reproduces core-halo profile
 - interference patterns unresolved
 - superior velocity representation



CDM initial conditions: effect of quantum pressure



Axion DM initial conditions: effect of „quantum pressure“

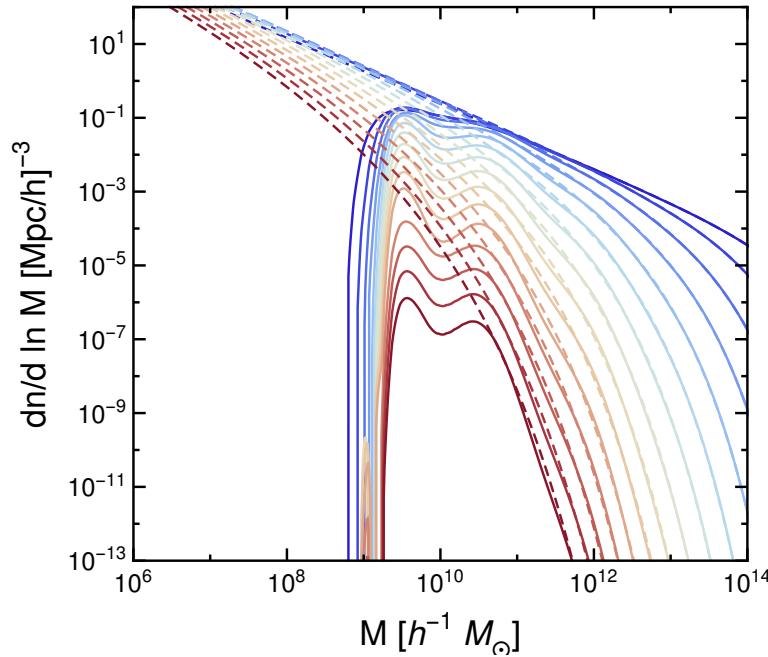
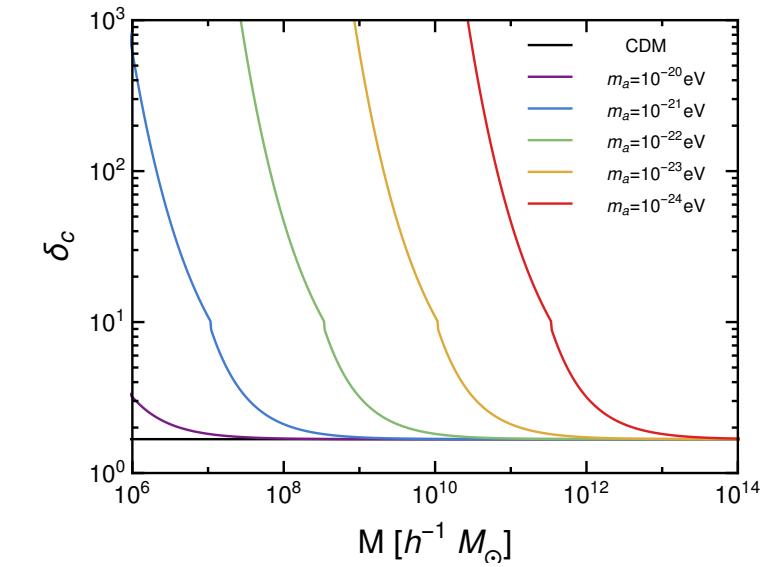


O(10%) difference
in power spectrum
compared to CDM

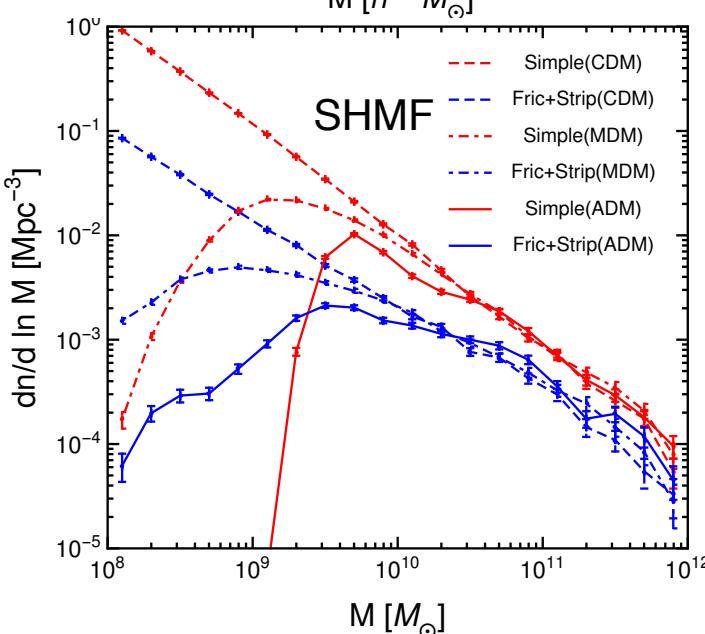
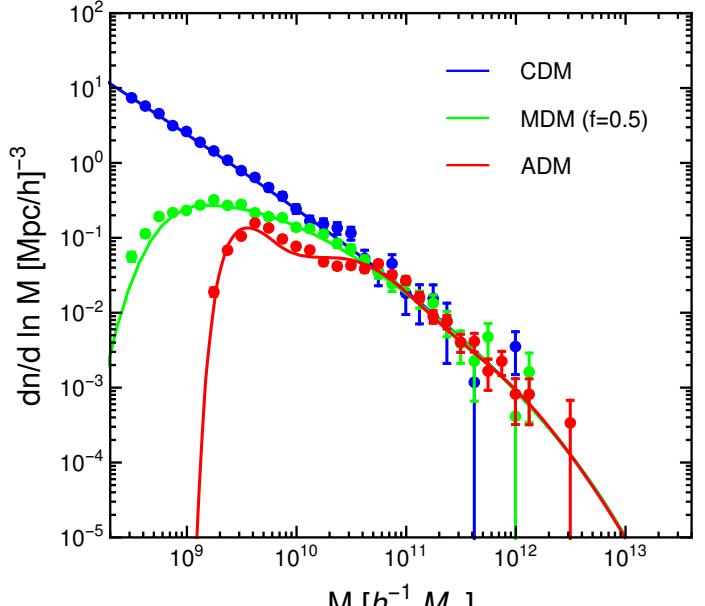
Stochastic merger trees for ULA halos

(Du,JN,Behrens)

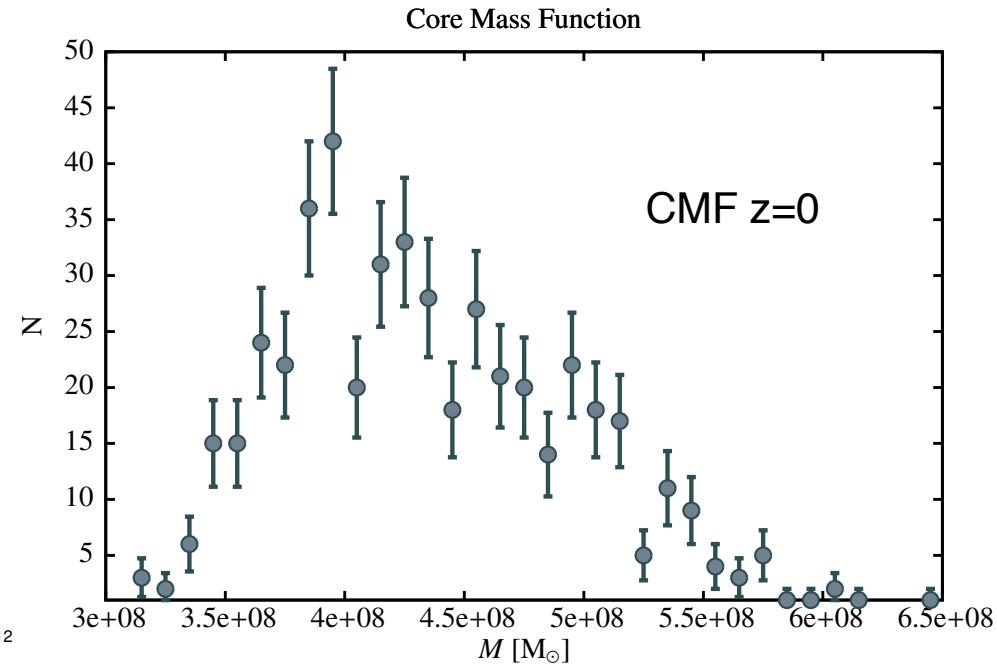
- quantum Jeans length → modifications w.r.t. CDM (Marsh & Silk 2013):
 - transfer function with small-scale cutoff
 - critical density for collapse higher near Jeans mass
 - scale dependent growth function
- use modified stochastic merger tree (Lacey & Cole 1993) including small-scale cutoff and solitonic core
- implemented into semi-analytic code for galaxy evolution *Galacticus* (Benson 2010)
- computational challenge: need to solve excursion set barrier distribution function numerically
- compute constraints from subhalo statistics



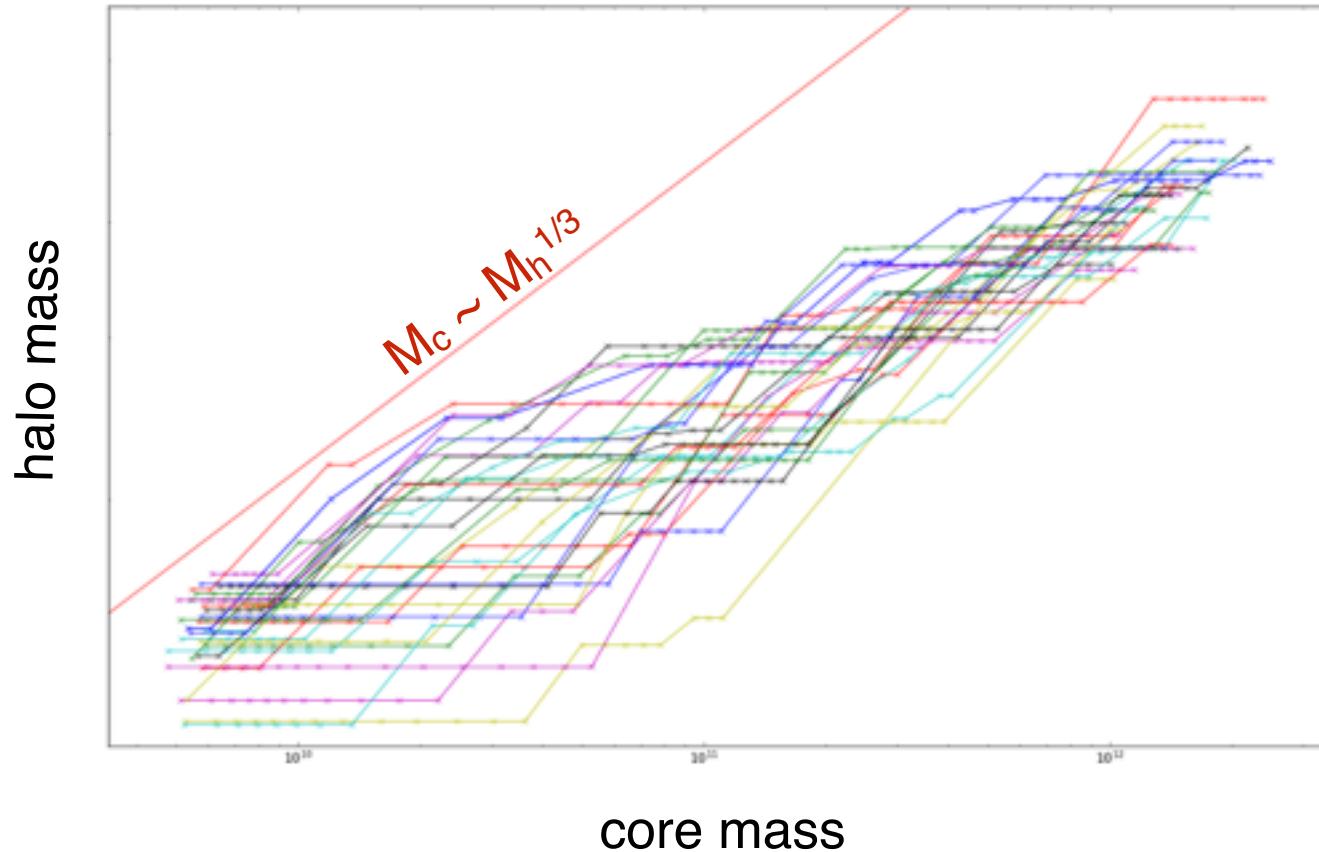
Stochastic merger trees for ULA halos: substructure



- Halo substructure models from parameter study of
 - different ULA/CDM fractions
 - tidal stripping stopped at solitonic core
- Core mass function using growth dynamics from merger simulations (**very preliminary**)



Core growth trajectories



Summary

- Ultra-light axions can be some or all of dark matter
- Interesting nonlinear phenomenology for LSS if de Broglie wavelength is of order several kpc (i.e. $m \sim 10^{-22}$ eV)
- Constraints from nonlinear clustering, degeneracies with neutrinos, etc. (e.g. from Lyman alpha forest) require simulations
- May or may not affect „CDM small scale crisis“ (missing satellites, cusp-core, too-big-to-fail); rich phenomenology from solitonic cores
- Grid-based simulations of Schrödinger-Poisson equations used for systematic investigation of **core mergers**
- Madelung (fluid) picture appears to be more efficient for cosmological simulations (no resolution constraints from velocity); **O(10%) effect on power spectrum on scales of $\sim 5\text{-}10$ kpc**
- Semi-analytic models with stochastic halo merger trees (constructed using the simulations above) for constraints from **subhalo statistics**, reionization,