

Leptonic Structure Functions Measured with the L3 Detector

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May 12, 2009

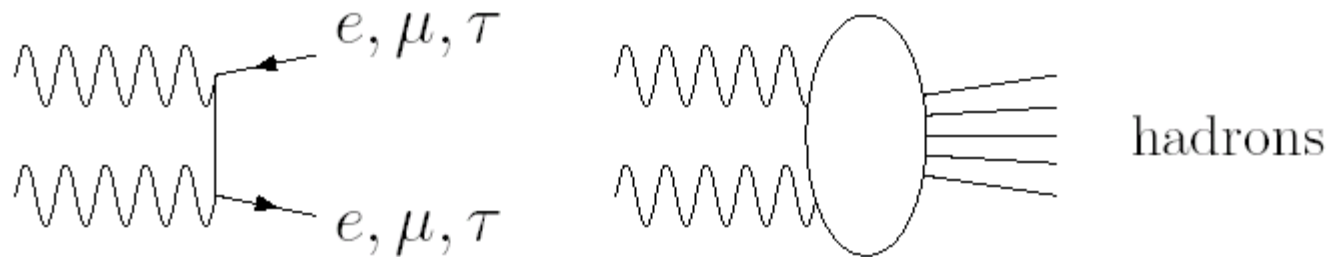


Photon 2009

11-15 May 2009
DESY, Hamburg

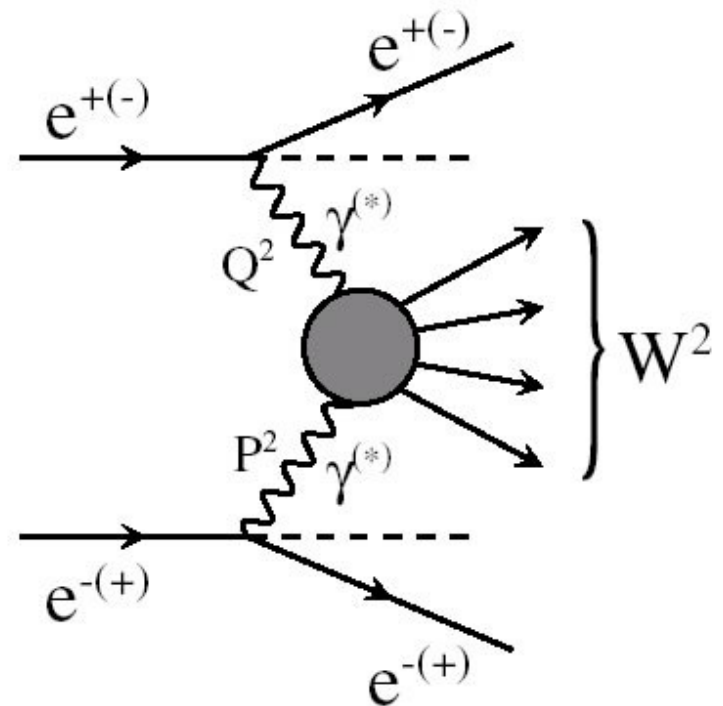
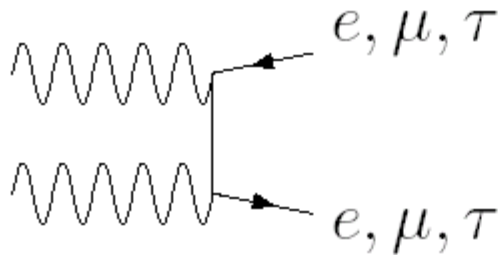
“Structure of the Photon”

- Dual nature of photons: uncertainty principle allows photon to fluctuate into various states (leptons, quarks, ...)
- Photon is ideal tool for probing structure of objects



Dilepton Formalism

$$e^+e^- \rightarrow e^+e^-\gamma^*\gamma^* \rightarrow e^+e^-\mu^+\mu^-$$



Dilepton Formalism

$$d\sigma = K(4\rho_1^{++}\rho_2^{++}\sigma_{TT} + 2\rho_1^{00}\rho_2^{++}\sigma_{LT} + 2\rho_1^{++}\rho_2^{00}\sigma_{TL} + \rho_1^{00}\rho_2^{00}\sigma_{LL} \\ + 2|\rho_1^{+-}\rho_2^{+-}|\tau_{TT}\cos 2\tilde{\phi} - 8|\rho_1^{+0}\rho_2^{+0}|\tau_{TL}\cos \tilde{\phi}) \frac{d^3p'_1 d^3p'_2}{E_1 E_2}$$

$$\left| \begin{array}{c} \Rightarrow \\ \leftarrow \end{array} \right| + \left| \begin{array}{c} \Rightarrow \\ \Rightarrow \end{array} \right| + \left| \begin{array}{c} \text{L} \quad \text{T} \\ \bigcirc \leftarrow \end{array} \right| : A_1$$

$$2\text{Re}\left\{ \begin{array}{c} \bigcirc \leftarrow \\ \leftarrow \end{array} \right\} \otimes \left(\begin{array}{c} \Rightarrow \\ \leftarrow \end{array} \right) \\ 2\text{Re}\left\{ \begin{array}{c} \bigcirc \leftarrow \\ \leftarrow \end{array} \right\}^+ \otimes \left(\begin{array}{c} \Rightarrow \\ \Rightarrow \end{array} \right) : A_2$$

$$2\text{Re}\left\{ \begin{array}{c} \Rightarrow \\ \leftarrow \end{array} \right\} \otimes \left(\begin{array}{c} \Rightarrow \\ \Rightarrow \end{array} \right) : A_3$$

$$K = \frac{\alpha^2}{16\pi^4 q_1^2 q_2^2} \sqrt{\frac{\nu^2 - q_1^2 q_2^2}{(p_1 p_2)^2 - m^4}}$$

ρ_i^{MN} : density matrix

σ_{PQ}, τ_{PQ} : cross-sections

for different helicity
states of the photon

Dilepton Formalism

$$F_1 = \frac{\sqrt{\nu^2 - q_1^2 q_2^2}}{4\pi^2 \alpha} \left(\sigma_{TT} - \frac{1}{2} \sigma_{TL} \right)$$

$$F_2 = \frac{\nu |q_1^2|}{4\pi^2 \alpha \sqrt{\nu^2 - q_1^2 q_2^2}} \left(\sigma_{TT} + \sigma_{LT} - \frac{1}{2} (\sigma_{LL} + \sigma_{TL}) \right)$$

$$\left| \begin{array}{c} \Rightarrow \\ \text{---} \end{array} \right|^2 + \left| \begin{array}{c} \Rightarrow \\ \text{---} \end{array} \right|^2 + \left| \begin{array}{c} \ominus \\ \text{---} \end{array} \right|^2 : A_1$$

$$2\text{Re} \left\{ \left(\begin{array}{c} \ominus \\ \text{---} \end{array} \right) \otimes \left(\begin{array}{c} \Rightarrow \\ \text{---} \end{array} \right) \right\}$$

$$2\text{Re} \left\{ \left(\begin{array}{c} \ominus \\ \text{---} \end{array} \right) \otimes \left(\begin{array}{c} \Rightarrow \\ \text{---} \end{array} \right) \right\} : A_2$$

$$2\text{Re} \left\{ \left(\begin{array}{c} \Rightarrow \\ \text{---} \end{array} \right) \otimes \left(\begin{array}{c} \Rightarrow \\ \text{---} \end{array} \right) \right\} : A_3$$

ρ_i^{MN} : density matrix

σ_{PQ}, τ_{PQ} : cross-sections

for different helicity
states of the photon

Single Tag Formalism

→ One electron detected

→ One electron escapes undetected

⇒

$$q_2^2 \rightarrow 0$$

→ Photon with $-q_1^2 = Q^2$: probe photon

→ Photon with $-q_2^2 = P^2$: target photon

Structure Function

Extraction of $F_{2,QED}'$

Express $d\sigma$ in terms of Structure Functions

$$\begin{aligned} d\sigma = & K \left(2|\rho_1^{+-}\rho_2^{+-}|\tau_{TT} \cos 2\tilde{\phi} - 8|\rho_1^{+0}\rho_2^{+0}|\tau_{TL} \cos \tilde{\phi} \right. \\ & + 2\rho_1^{++}\rho_2^{00} \{ F_2(W, q_1^2, q_2^2)/D - F_1(W, q_1^2, q_2^2)/C \} \\ & \left. + 4\rho_1^{++}\rho_2^{++} F_1(W, q_1^2, q_2^2)/C \right) \frac{d^3p'_1 d^3p'_2}{E_1 E_2} \end{aligned}$$

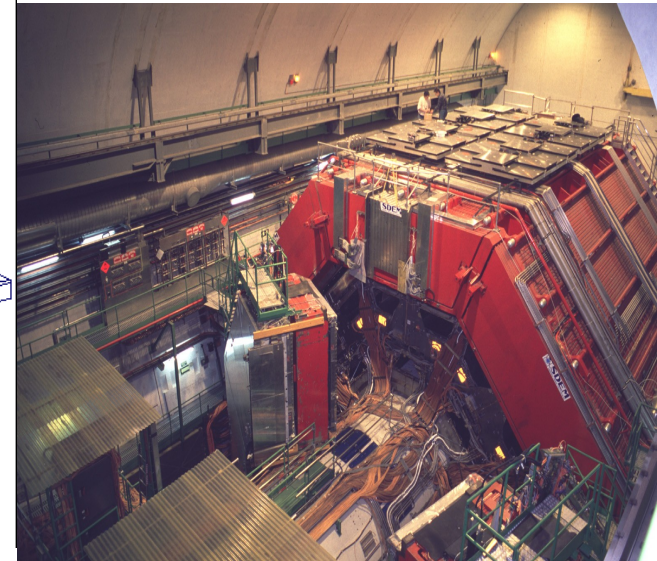
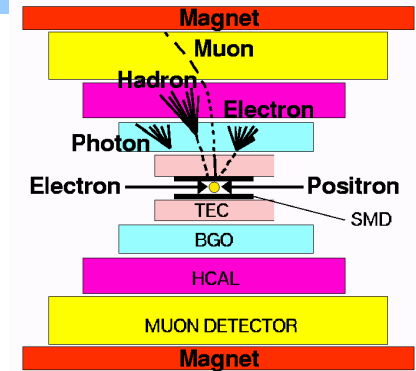
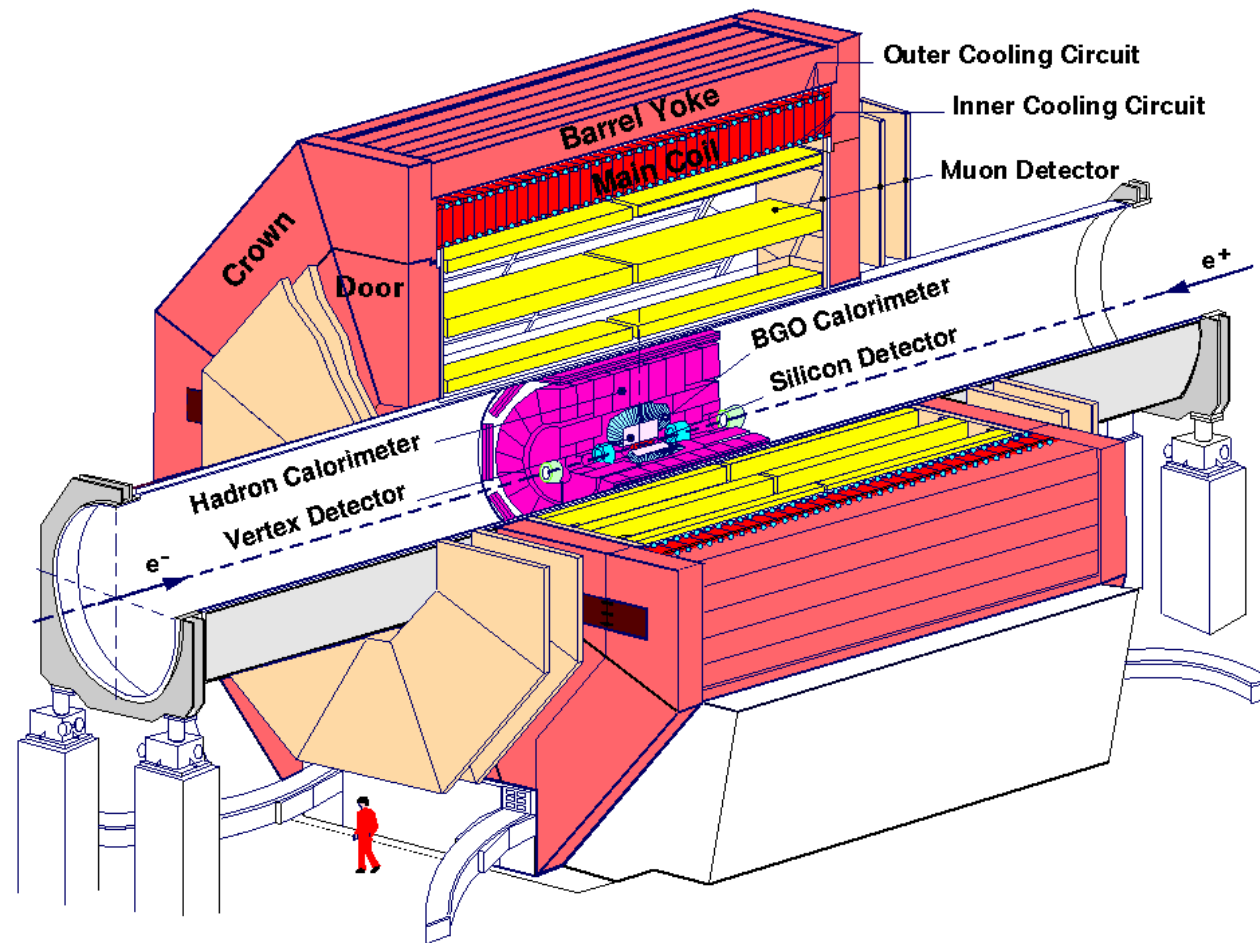
Structure Function

Extraction of $F_{2,QED}^\gamma$
Normalize the portion of $F_{2,QED}^\gamma$

$$F_2(W, q_1^2, q_2^2) \equiv 1$$

$$F_2^\gamma / \alpha = \frac{d\sigma_{measured}}{d\sigma_{Galuga, F_2=1}}$$

L3 – The Detector



L3 Tagging Detectors

Very Small Angle Tagger – VSAT

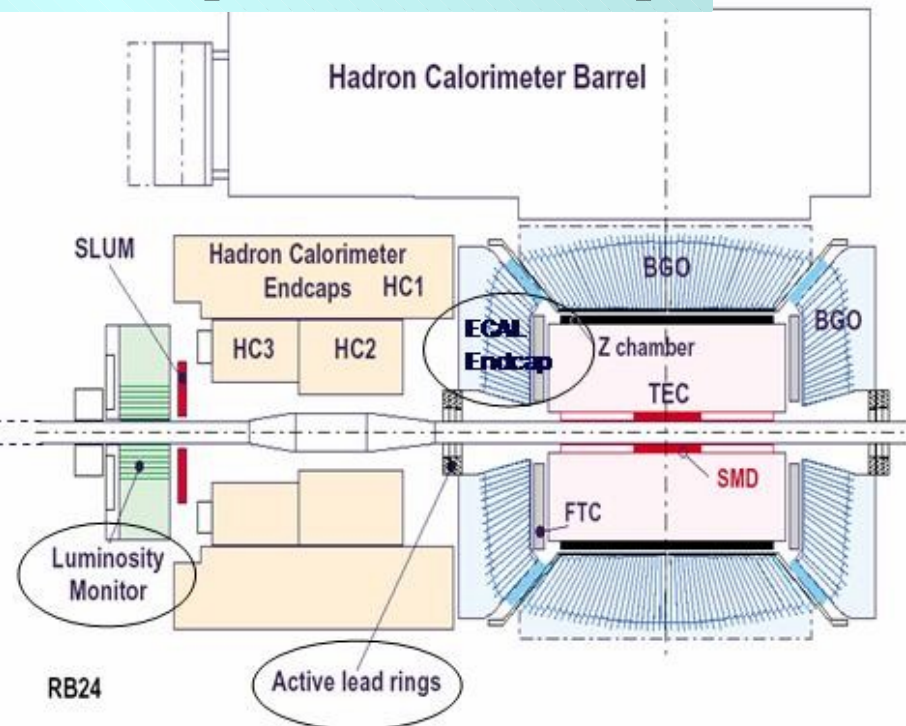
Luminosity Monitor – LUMI

Active Lead Ring – ALR

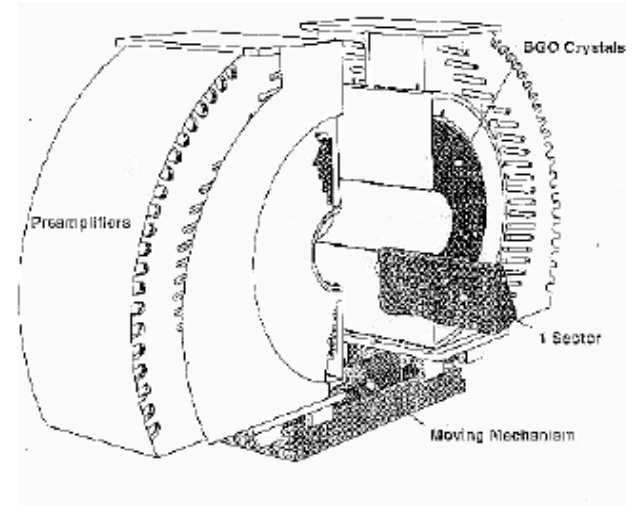
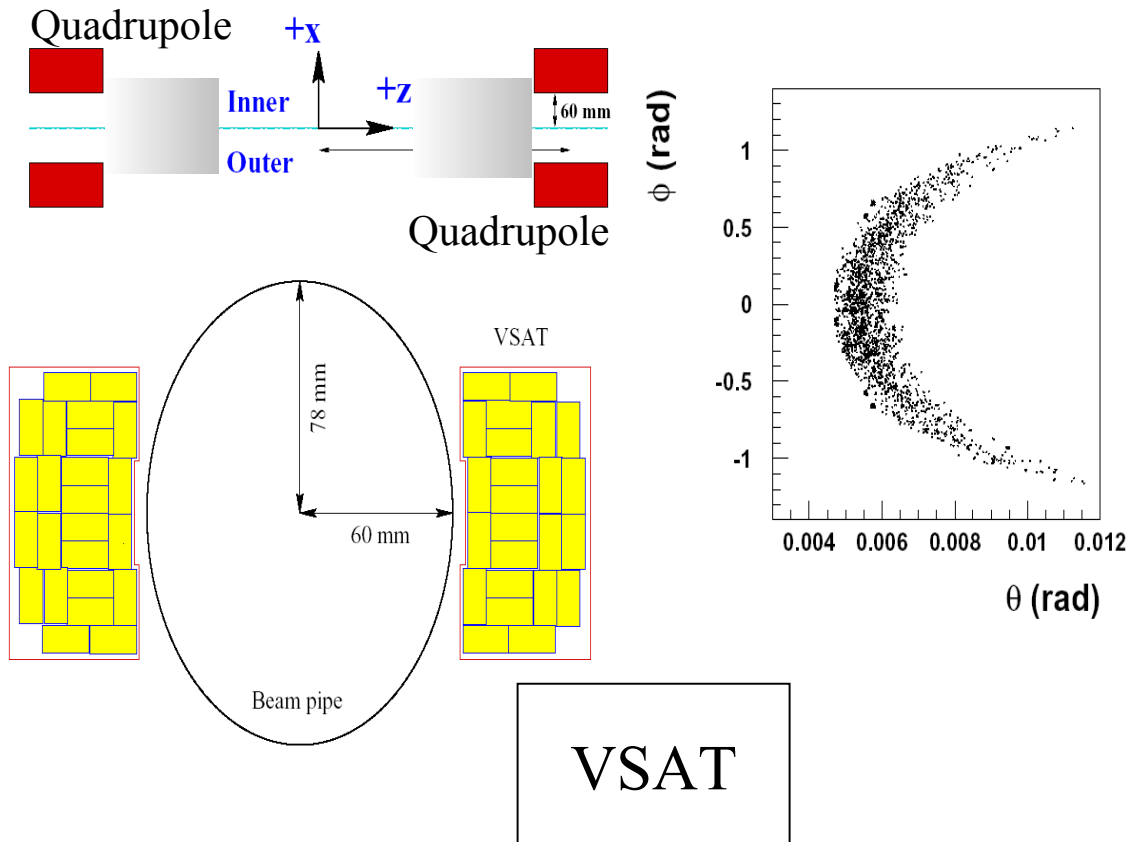
Electromagnetic Calorimeter Endcaps – BGO Endcaps

Tagging detectors used to identify scattered electron

VSAT: background due to proximity to beam pipe



L3 Tagging Detectors: VSAT / LUMI



LUMI

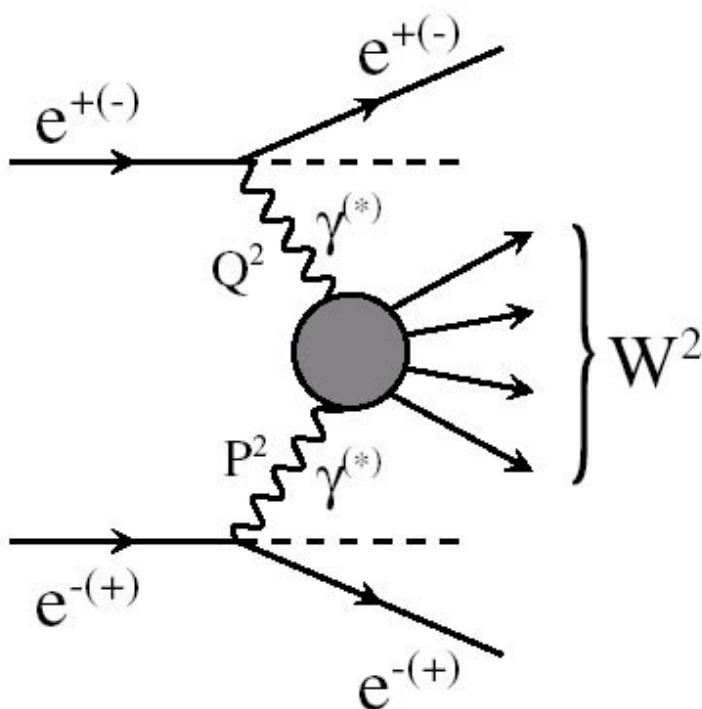
Two-Photon Interactions with Dimuon Events

$$e^+e^- \rightarrow e^+e^- \gamma^* \gamma^* \rightarrow e^+e^- \mu^+ \mu^-$$

Data sample:

$$E_{cms} = 189 \dots 206 \text{ GeV}$$

$$\mathcal{L}_{int} = 600 \text{ pb}^{-1}$$



- Single Tagged Electron, High Energy Deposition in Electromagnetic Calorimeters
- Two tracks, at least one to be identified as a lepton (μ^\pm)
- VERMASEREN Monte Carlo generator for large statistics

Selection Criteria VSAT

- Single tag: $0.5 \times E_{\text{beam}} \leq E_{\text{VSAT}}$

and only one

- Two well-measured tracks with $\Sigma Q_i = 0$

- At least one track to be identified as μ

- Squared four-momentum transfer:

$$0.2 \text{ GeV}^2 \leq Q^2 \leq 0.85 \text{ GeV}^2$$

with track information: $Q^2 = (\vec{p}_{T,1} + \vec{p}_{T,2})^2$

Selection Criteria LUMI

- Single tag: $0.7 \times E_{\text{beam}} \leq E_{\text{LUMI}}$

and only one

- Two well-measured tracks with $\Sigma Q_i = 0$

- At least one track to be identified as μ

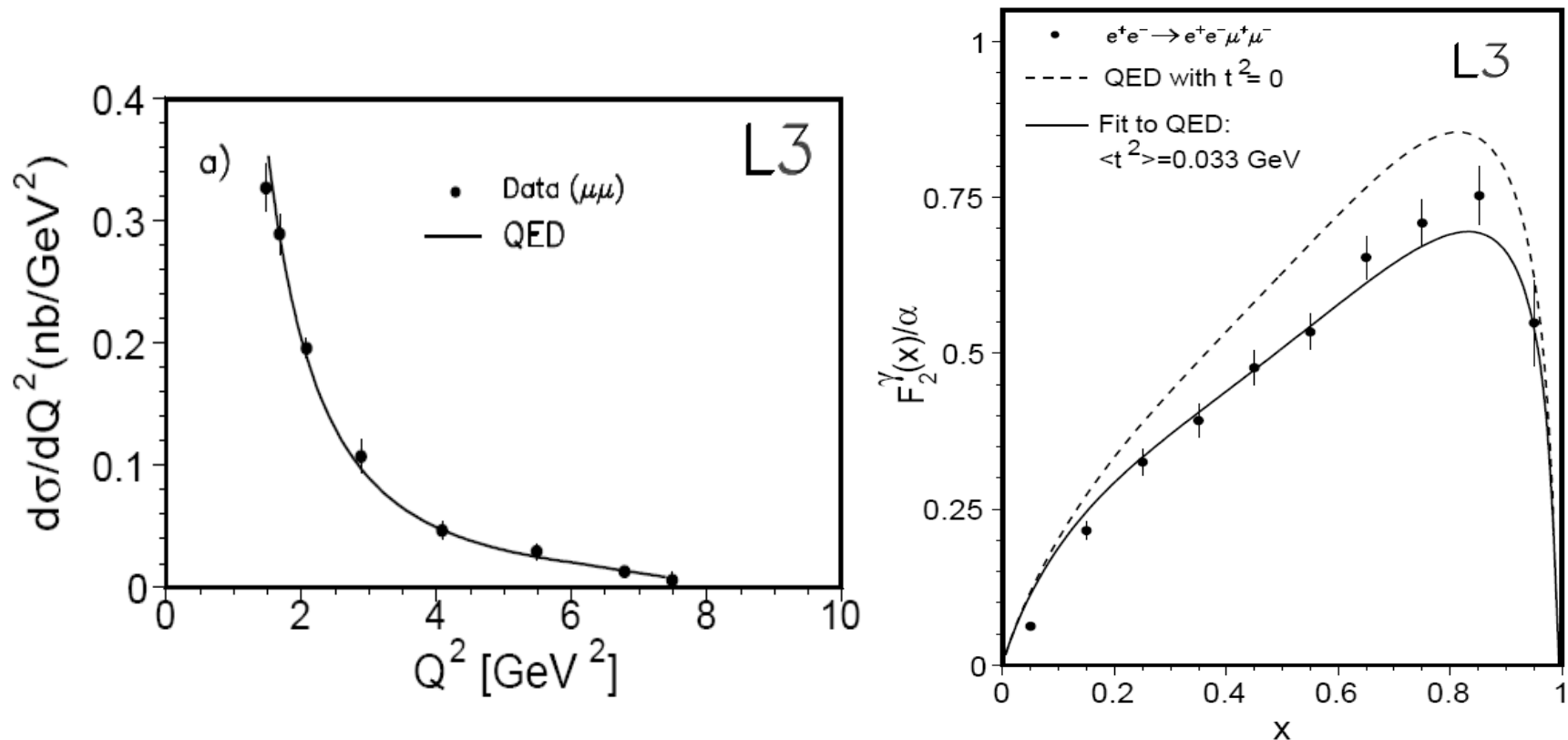
- Squared four-momentum transfer:

$$11 \text{ eV}^2 \leq Q^2 \leq 34 \text{ GeV}^2$$

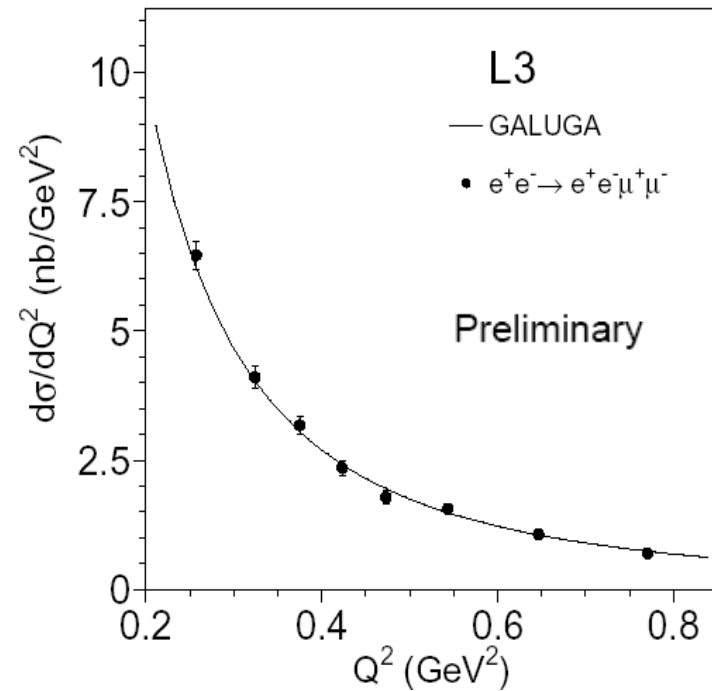
with track information: $Q^2 = (\vec{p}_{T,1} + \vec{p}_{T,2})^2$

Cross-Section & Structure-Function

Physics Letters B 438 (1998) 363–378

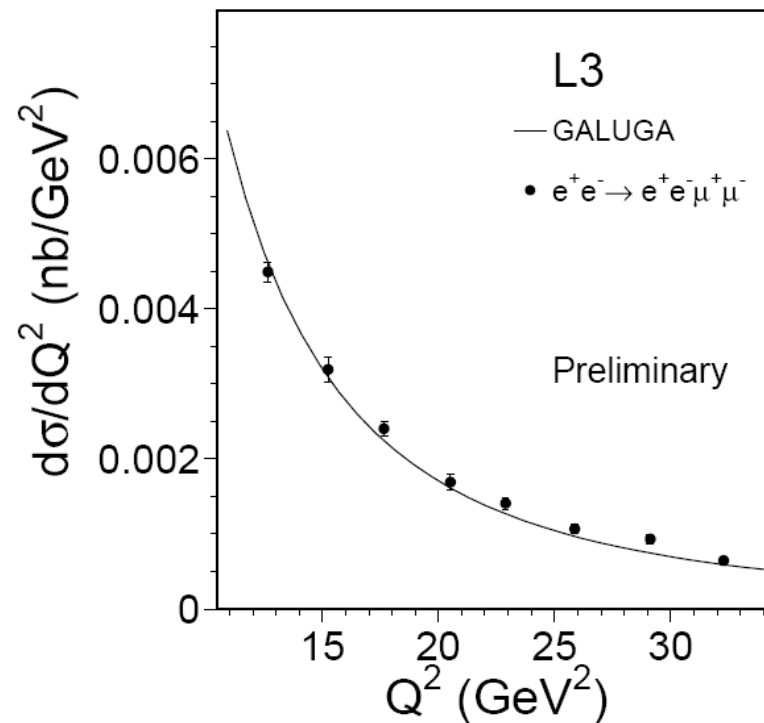


Cross-Section & Structure-Function



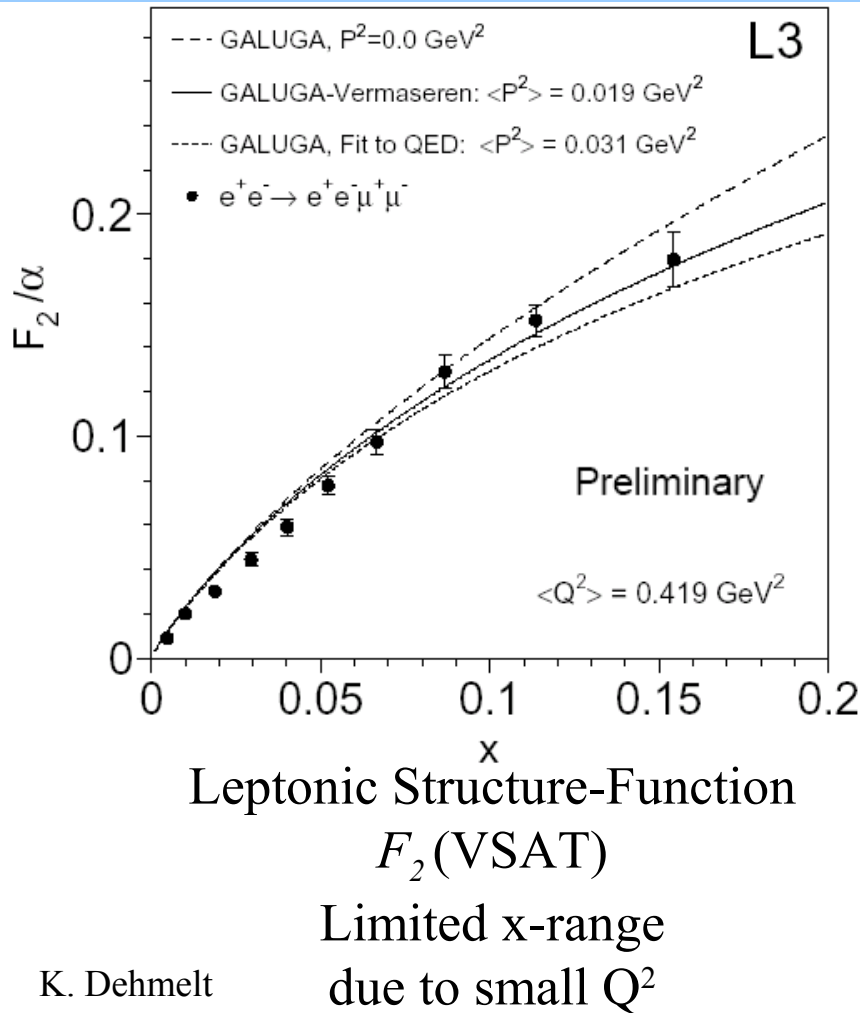
VSAT

$$\frac{d\sigma}{dQ^2} = \frac{N_{data}}{\Delta Q^2 \cdot \mathcal{A} \cdot \varepsilon \cdot \mathcal{L}}$$

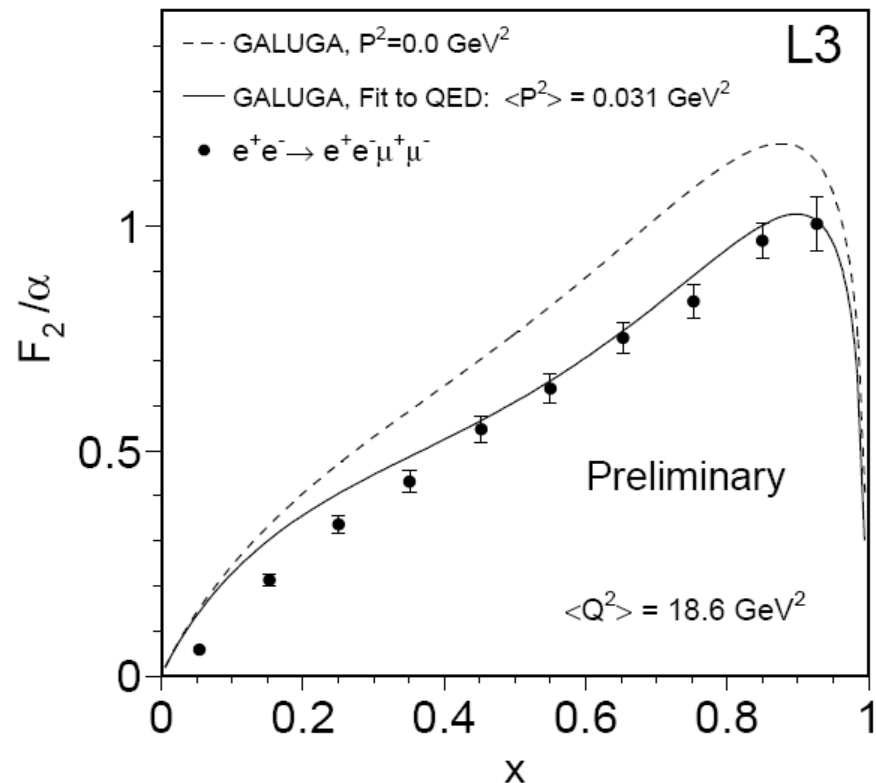


LUMI

Cross-Section & Structure-Function



Leptonic Structure-Function $F_2(\text{LUMI})$



Summary

✓ Measurement of

- differential cross-section

$$\boxed{\frac{d\sigma}{dQ^2}}$$

- structure-function

$$\boxed{F_{2,QED}^{\gamma}}$$

in the kinematical range

$$\mathbf{0.2 \text{ GeV}^2 \leq Q^2 \leq 0.85 \text{ GeV}^2}$$

$$\mathbf{11 \text{ GeV}^2 \leq Q^2 \leq 34 \text{ GeV}^2}$$

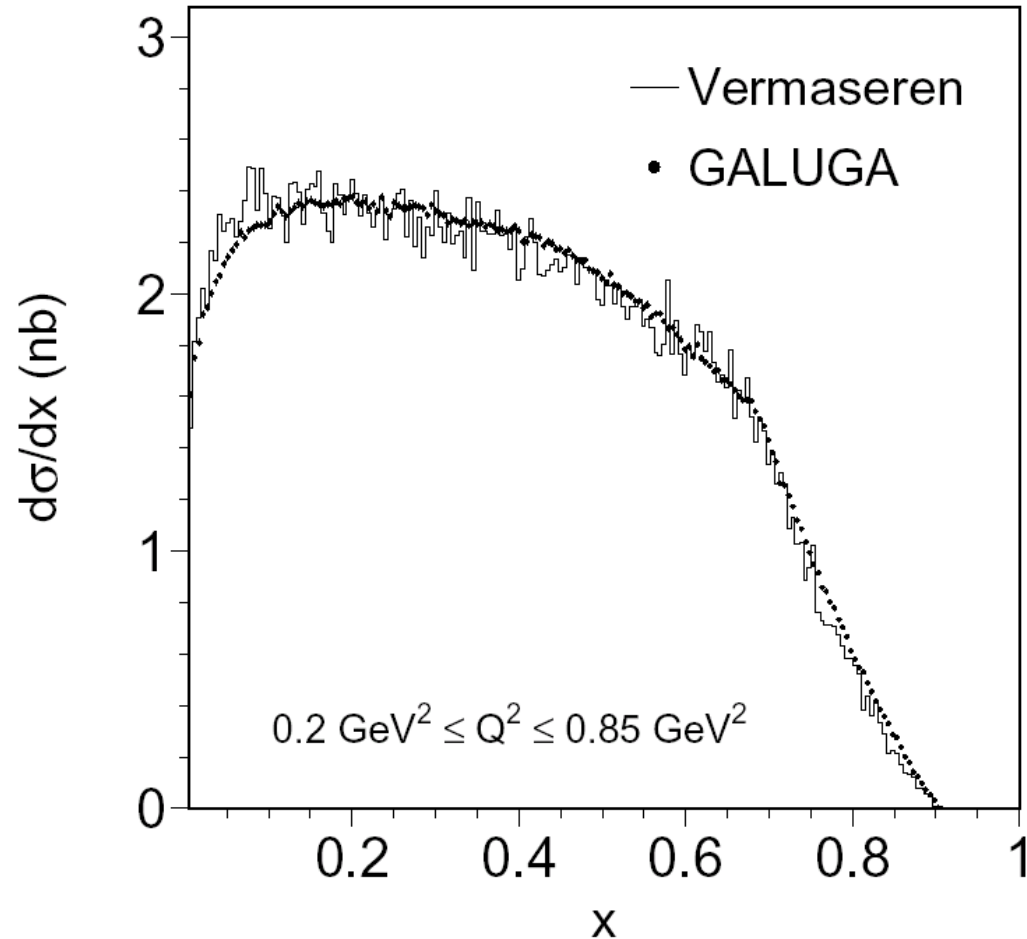
$$\mathbf{189 \text{ GeV} \leq \sqrt{s} \leq 206 \text{ GeV}}$$

✓ Data suggest $P^2 > 0$

Backup Slides

Cross-Section & Structure-Function VERMASEREN - GALUGA

Adaptation of parameters
GALUGA - VERMASEREN



Systematic Error Estimation

Error source	Error contribution (in %)
Luminosity Data	0.06
Luminosity MC	0.90
Background	0.09
Radiative events	0.60
Trigger efficiency	0.12
Selection criteria	2.36
GALUGA	2.16
Total	3.38

Background sources

$$e^-e^+ \rightarrow e^-e^+l^-l^+ \quad (l = e, \mu) \rightarrow \text{Non Multiperipheral}$$

