

# ***CEPC Partial Double Ring Lattice Design and SPPC Lattice Design***

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**CERN-BINP workshop for young scientists in e+e- colliders, August 24, 2016**

# Outline

## **I. CEPC Partial Double Ring Lattice Design**

- 1. CEPC PDR Parameter and Lattice Layout**
- 2. CEPC PDR ARC Length Consideration and Redesign**
- 3. CEPC PDR DA Study ( NSGAI & DA Optimization)**
- 4. CEPC APDR Scheme**
- 5. CEPC Double Ring Scheme**
- 6. Summary**

## **II. SPPC Parameter Choice and Lattice Design**

- 1. SPPC Parameter Choice and Optimize**
- 2. SPPC Lattice Layout and Design:**
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  - b. Dispersion Suppressor Section**
  - c. Long Straight Section**
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- 3. SPPC Dynamic Aperture Study**
- 4. Summary**

## **I. CEPC Partial Double Ring Lattice Design**

- 1. CEPC PDR Parameter and Lattice Layout**
- 2. CEPC PDR ARC Length Consideration and Redesign**
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# ***I. CEPC***

## **1. CEPC PDR Parameter and Lattice Layout**

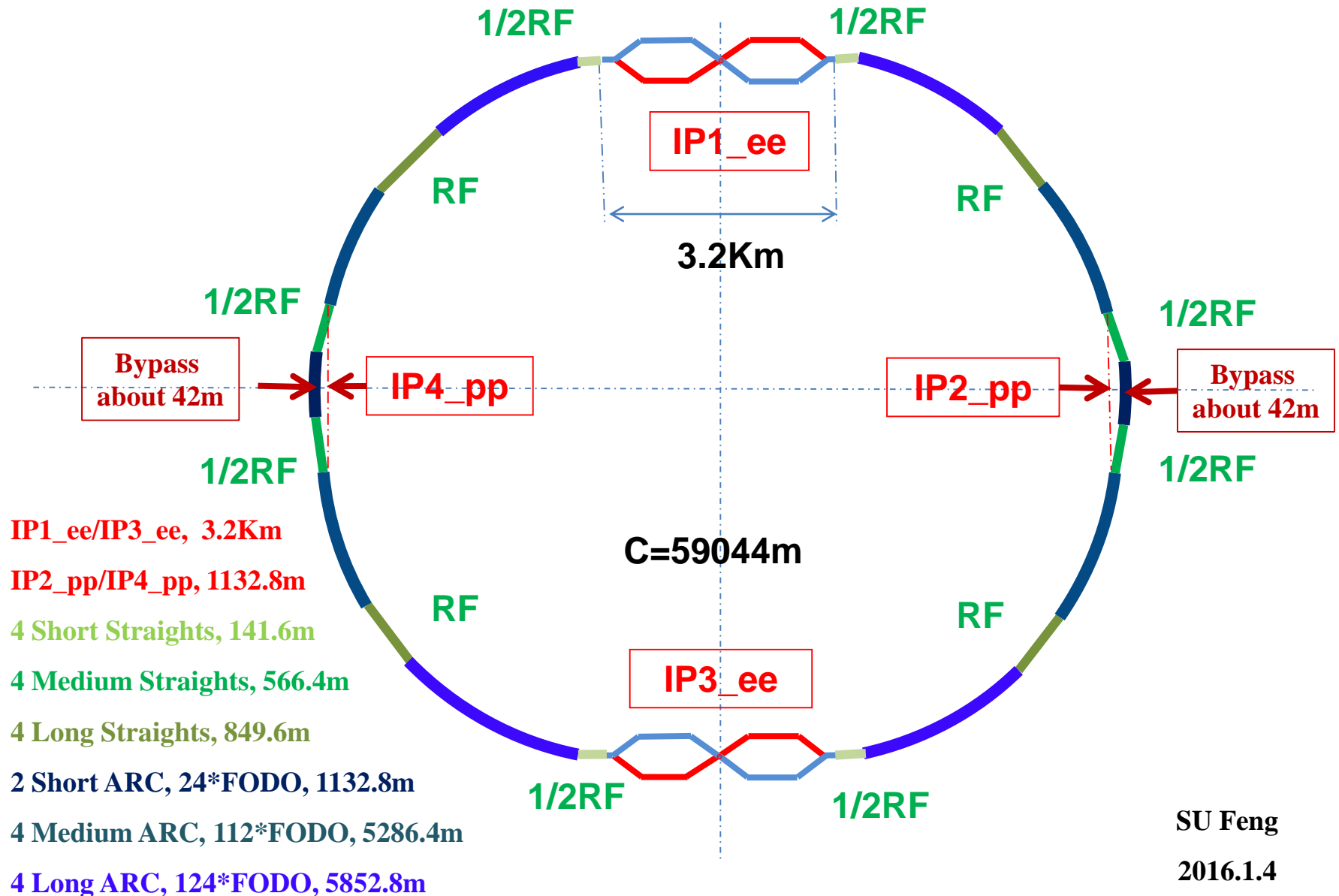


# CEPC PDR Parameter

(wangdou20160325)

	<i>Pre-CDR</i>	<i>H-high lumi.</i>	<i>H-low power</i>	<i>W</i>	<i>Z</i>
Number of IPs	2	2	2	2	2
Energy (GeV)	120	120	120	80	45.5
Circumference (km)	54	54	54	54	54
SR loss/turn (GeV)	3.1	2.96	2.96	0.59	0.062
Half crossing angle (mrad)	0	15	15	15	15
Piwinski angle	0	2.5	2.6	5	7.6
$N_e$ /bunch ( $10^{11}$ )	3.79	2.85	2.67	0.74	0.46
Bunch number	50	67	44	400	1100
Beam current (mA)	16.6	16.9	10.5	26.2	45.4
SR power /beam (MW)	51.7	50	31.2	15.6	2.8
Bending radius (km)	6.1	6.2	6.2	6.1	6.1
Momentum compaction ( $10^{-5}$ )	3.4	2.5	2.2	2.4	3.5
$\beta_{IP}$ x/y (m)	0.8/0.0012	0.25/0.00136	0.268 /0.00124	0.1/0.001	0.1/0.001
Emittance x/y (nm)	6.12/0.018	2.45/0.0074	2.06 /0.0062	1.02/0.003	0.62/0.0028
Transverse $\sigma_{IP}$ (um)	69.97/0.15	24.8/0.1	23.5/0.088	10.1/0.056	7.9/0.053
$\xi_x$ /IP	0.118	0.03	0.032	0.008	0.006
$\xi_y$ /IP	0.083	0.11	0.11	0.074	0.073
$V_{RF}$ (GV)	6.87	3.62	3.53	0.81	0.12
$f_{RF}$ (MHz)	650	650	650	650	650
Nature $\sigma_z$ (mm)	2.14	3.1	3.0	3.25	3.9
Total $\sigma_z$ (mm)	2.65	4.1	4.0	3.35	4.0
HOM power/cavity (kw)	3.6	2.2	1.3	0.99	0.99
Energy spread (%)	0.13	0.13	0.13	0.09	0.05
Energy acceptance (%)	2	2	2		
Energy acceptance by RF (%)	6	2.2	2.1	1.7	1.1
$n_\gamma$	0.23	0.47	0.47	0.3	0.24
Life time due to beamstrahlung_cal (minute)	47	36	32		
$F$ (hour glass)	0.68	0.82	0.81	0.92	0.95
$L_{max}$ /IP ( $10^{34}\text{cm}^{-2}\text{s}^{-1}$ )	2.04	2.96	2.01	3.09	3.09

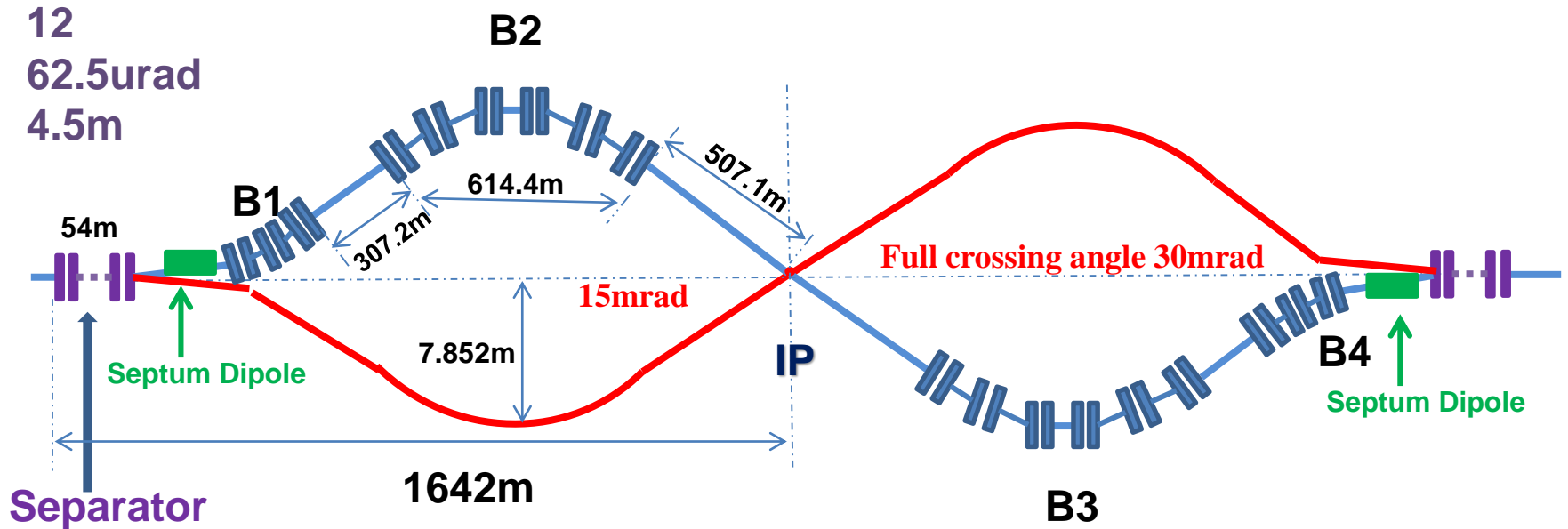
# CEPC Partial Double Ring Layout



SU Feng

2016.1.4

# CEPC Partial Double Ring Layout



For CEPC 120GeV beam:

➤ Max. deflection per separator is **66urad**.

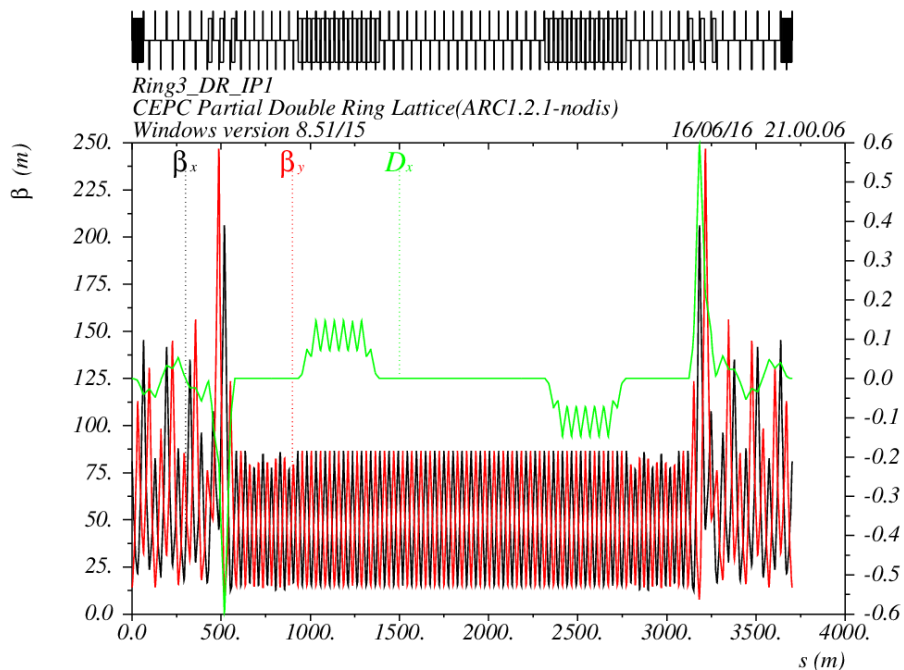
Using **Septum Dipole** after separator to acquire 15 mrad

Version 1.0

sufeng

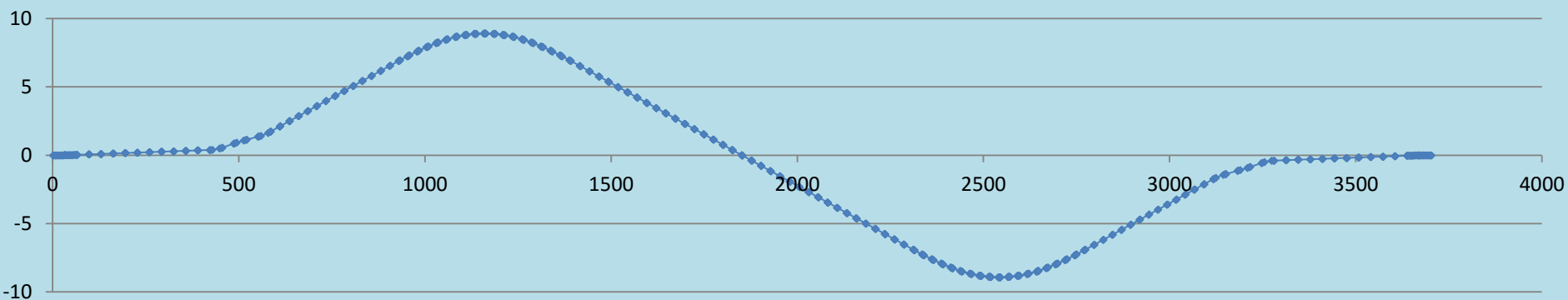
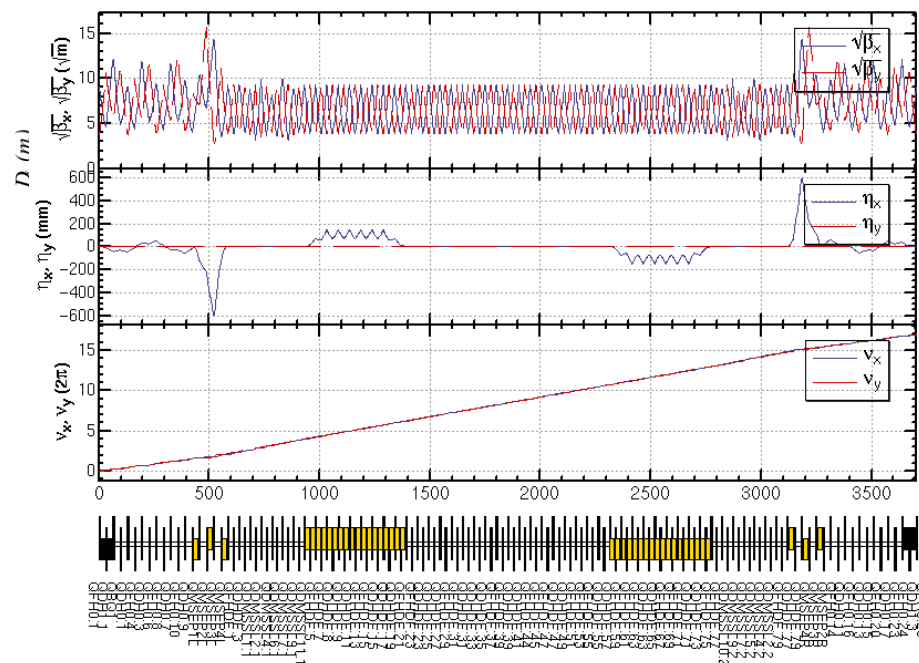
2015.12.20

# CEPC PDR1.0.3 noFFS



$$\delta_E / p_{oc} = 0.00000$$

Table name = TWISS





# ***I. CEPC***

## **2. CEPC PDR ARC Length Consideration and Redesign**



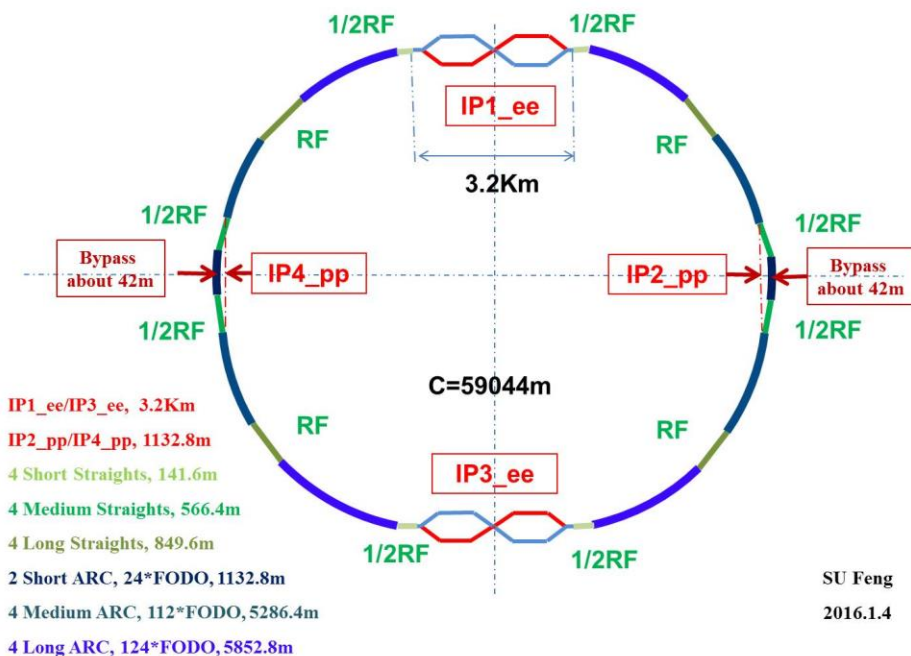
# CEPC PDR ARC Length Consideration

The circumference should be also considered of SPPC requirement...

1. ARC+Straight ( $\geq 53$  Km)
2. ARC+Straight+PDR
3. ARC+Straight+PDR+FFS

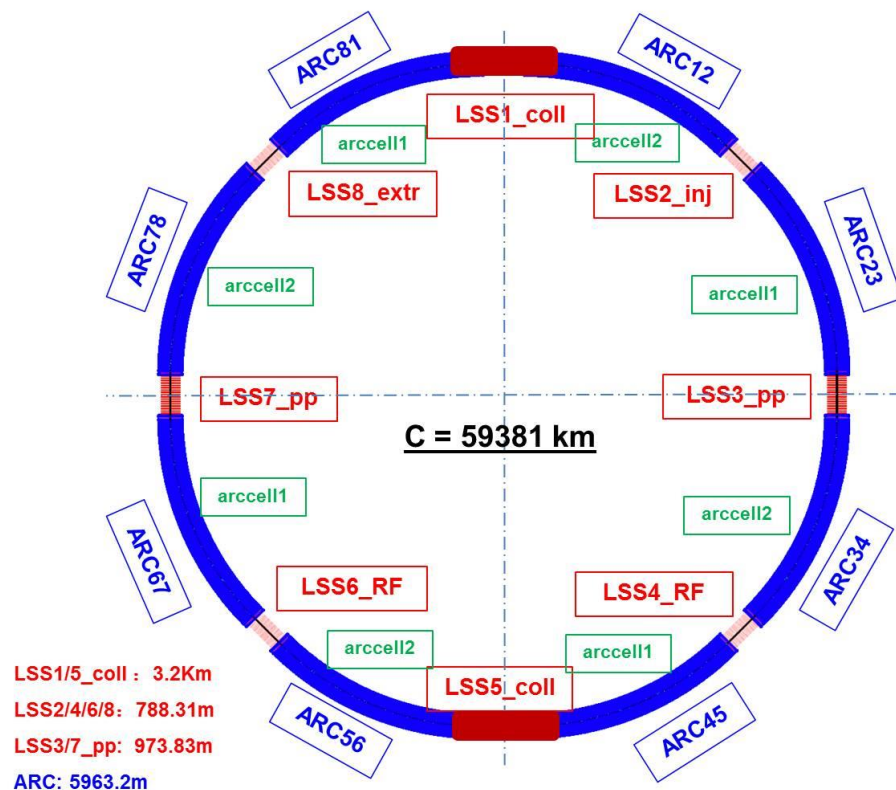
# CEPC & SPPC Layout

## CEPC Partial Double Ring Layout



SU Feng  
2016.1.4

## SPPC Layout (Su Feng Jan. 10, 2016)



# CEPC ARC Length According to SPPC

## Theory:

$$E_0 = 70 - 100 \text{ TeV}$$

$$\gamma = \frac{35 \text{ TeV}}{938.27 \text{ MeV}} = 37313.4$$

$$\beta = 1$$

$$B\rho = \frac{E_0}{c} = 3.1267 \text{ Tm} \quad \beta\gamma = 116635.29 \text{ Tm}$$

$$B_0 = 20 \text{ T}$$

$$\rho = \frac{B\rho}{B_0} = \frac{116635.29}{20} = 5831.7645 \text{ m}$$

$$L_{\text{Dipole}} = 2\pi\rho = 36642.05 \text{ m}$$

$$\text{ARC filling factor } f_1 = 0.8$$

$$L_{\text{ARC}} = \frac{L_{\text{Dipole}}}{f_1} = \frac{36642.05}{0.8} = 45802.56 \text{ m}$$

$$L_{\text{ss3pp}} = L_{\text{ss7pp}} = 973.83 \text{ m}$$

$$L_{\text{ss2}} = L_{\text{ss4}} = L_{\text{ss6}} = L_{\text{ss8}} = 788.31 \text{ m}$$

$$L_1 = 50903.46 \text{ m}$$

$$L_{\text{ss1}} = L_{\text{ss5}} = 3.3 \text{ km}$$

$$C_0 = 57503.46 \text{ m}$$

## In Practice:

### ARC CELL

	LQ	DQS	LS	DSB	LB	DBB
SPPC	4m	1m	0.5m	1m	14.8m	1m
FCC-hh	6.3137m	1m	0.5m	2.184m	14.3m	1.36m

B max [T]	G max [T/m]	k1	k2
19.61	582.156	4.9899E-3	0

### Pre-CDR:

Dipole: L=15m B=20T

Quadrupole:

D = 45 mm  $B_{\text{pole}} = 16 \text{ T}$   
G = 711.1 T/m  $K_1 = 6.097 \times 10^{-3}$

Betax: 244.878/42.57  
Betay: 42.569/244.869 ( $\epsilon_n = 4.1 \mu\text{m}$ )

E (Collision: 35TeV)  
(Injection: 2.1TeV)

$$\epsilon = \frac{\epsilon_n}{\gamma}$$

$\epsilon$  (Collision:  $1.099 \times 10^{-10} \text{ m} = 0.1099 \text{ nm}$ )  
(Injection:  $1.83 \times 10^{-9} \text{ m} = 1.83 \text{ nm}$ )

$\sigma$  (Collision:  $1.66 \times 10^{-4} \text{ m} = 166 \mu\text{m}$ )  
(Injection:  $6.76 \times 10^{-4} \text{ m} = 676 \mu\text{m}$ )

$R = 20 \times \sigma_{\text{inj}} = 13.52 \text{ mm}$

D = 27.04

$$L_B = 14.8 \text{ m}$$

$$\text{FODO : } f_1 = \frac{14.8 \times 8}{144.4} = 0.8199$$

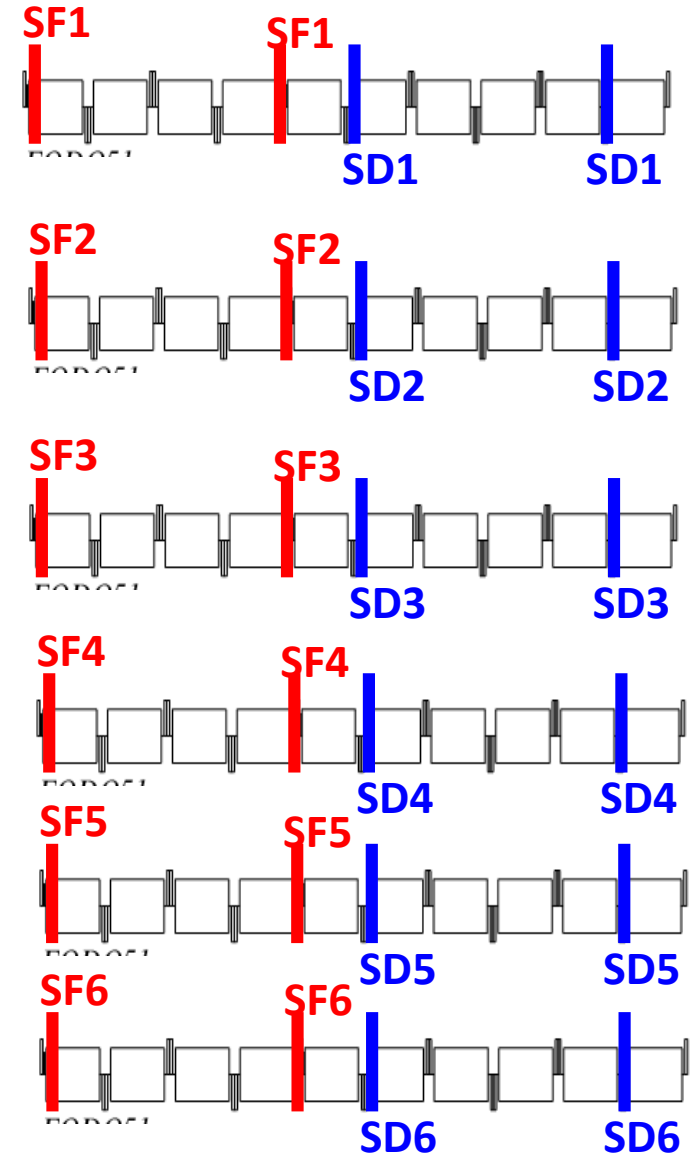
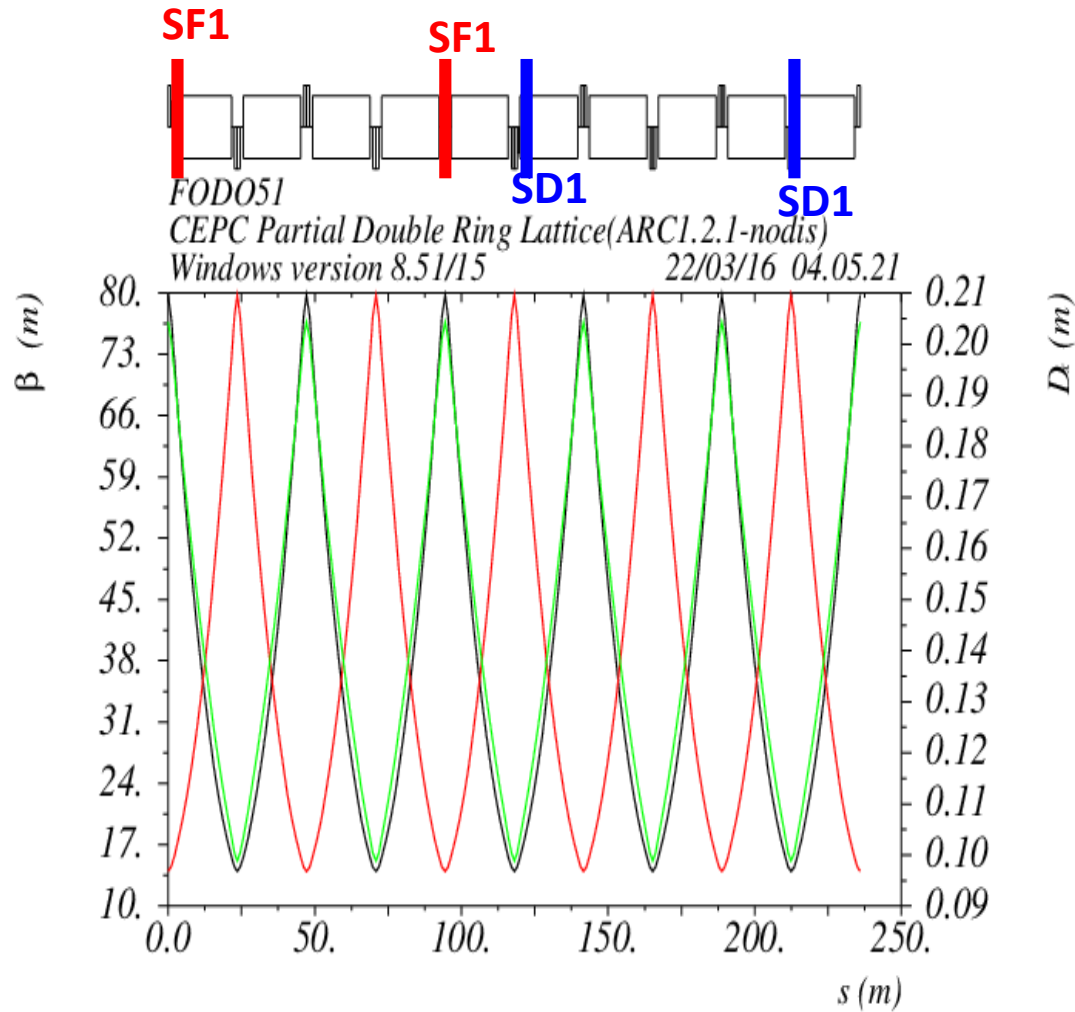
$$\text{ARC : } f_1 = \frac{14.8 \times 8 \times 38 + 14.8 \times 8 \times 2}{(38 + 2 + 2) \times 144.4} = 0.7809$$

$$L_{\text{ARC}} = \frac{37389.85}{0.7809} = 47880.46$$

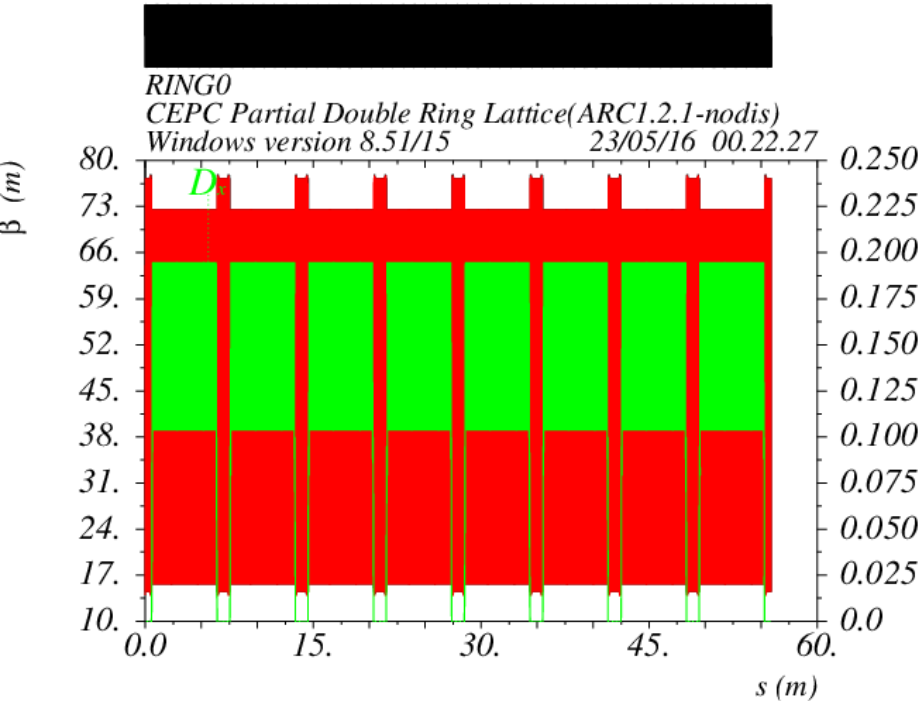
$$L_1 = 52981.42$$

$$C_0 = 59581.42$$

# New ARC FODO 90/90 non-interleave

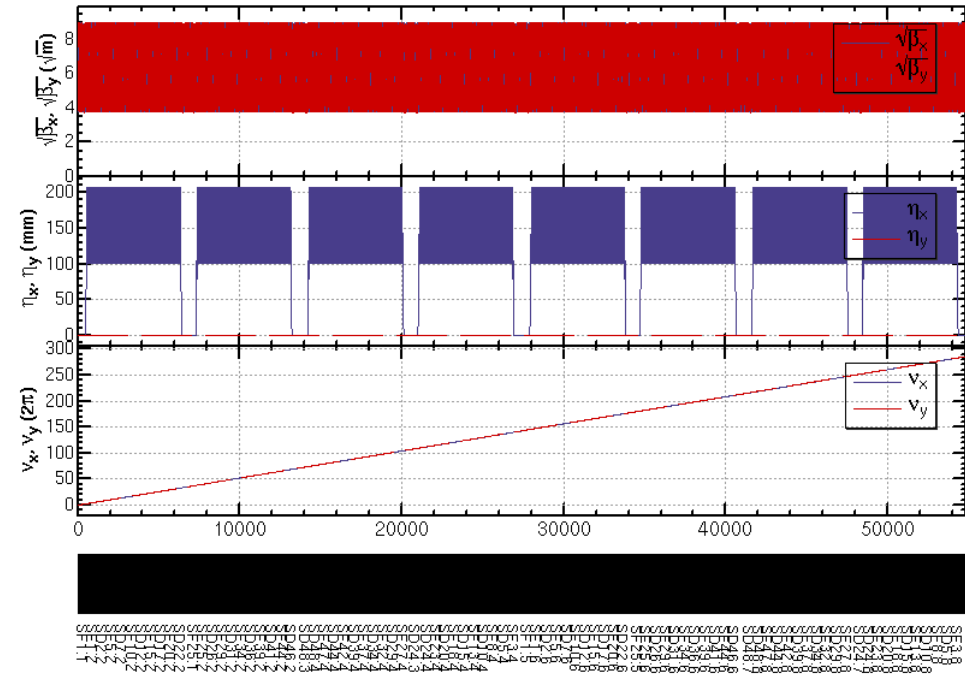


# CEPC ARC



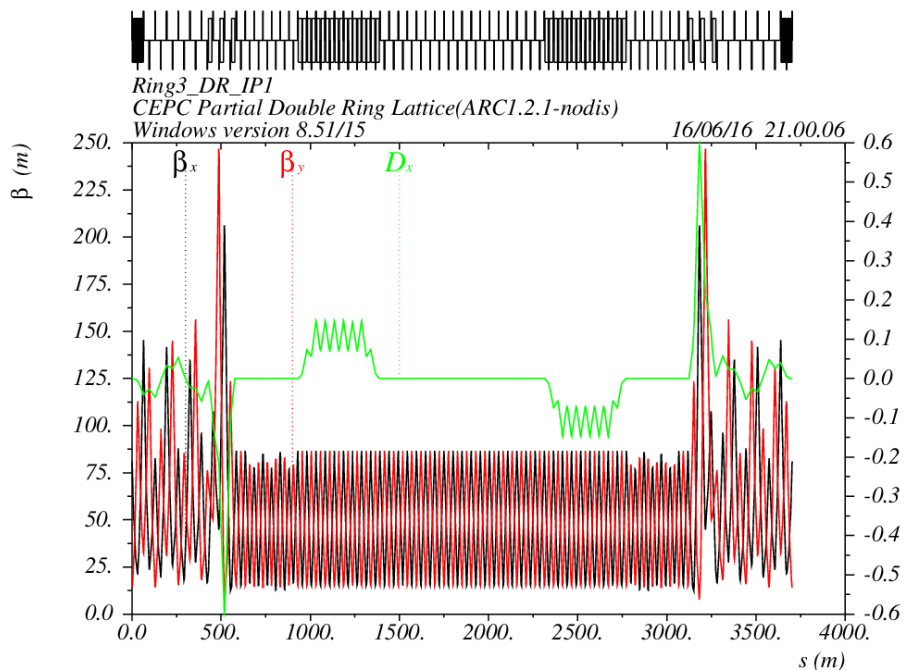
$$\delta_E / p_{0c} = 0.00000$$

Table name = TWISS



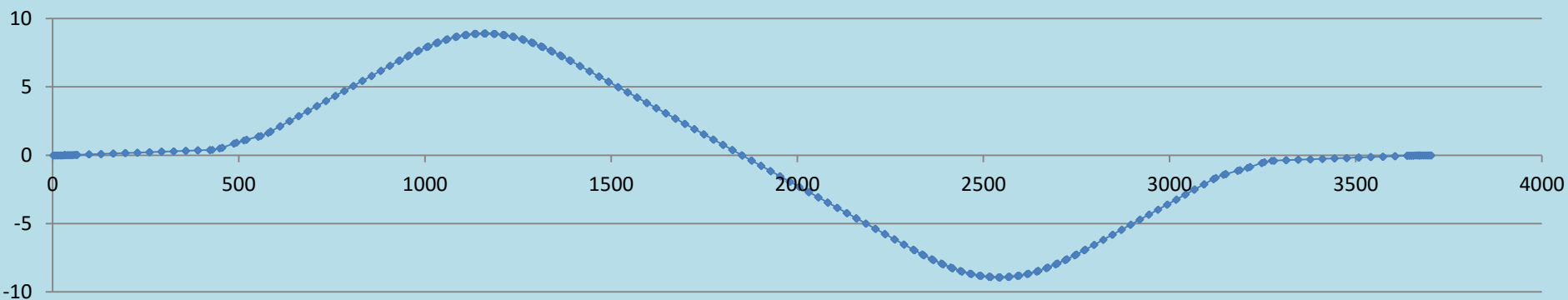
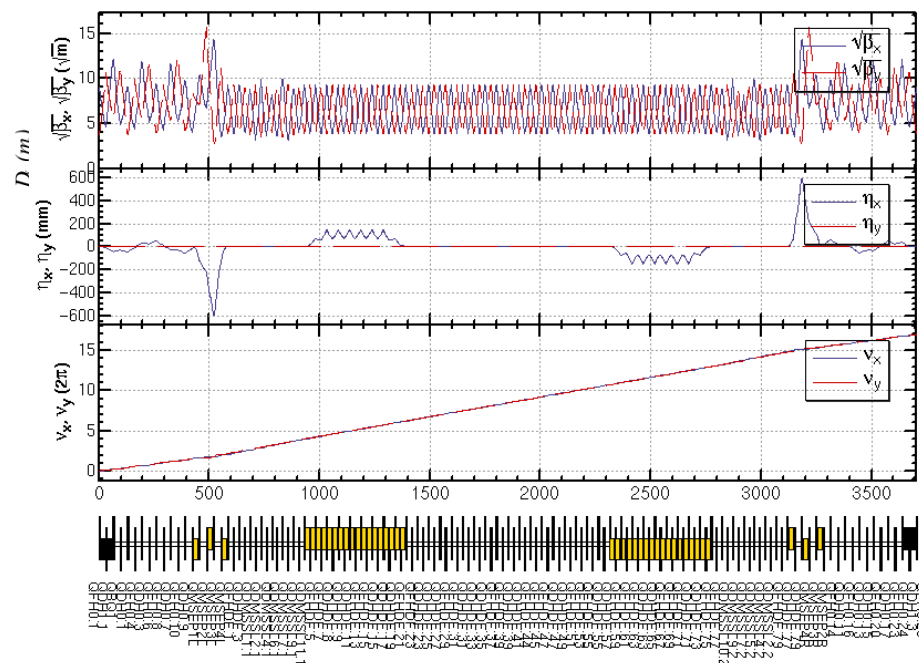


# CEPC PDR1.0.3 noFFS



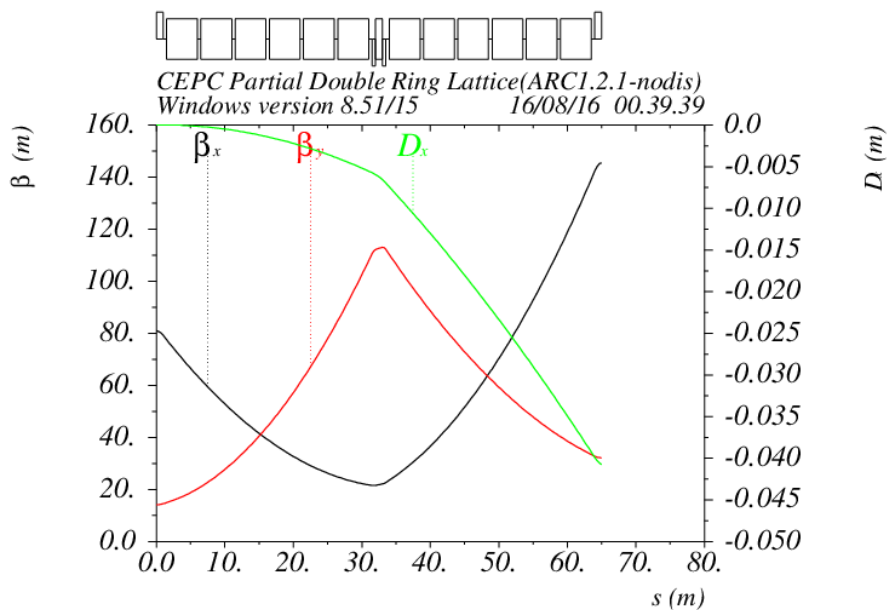
$$\delta_E / p_{oc} = 0.00000$$

Table name = TWISS

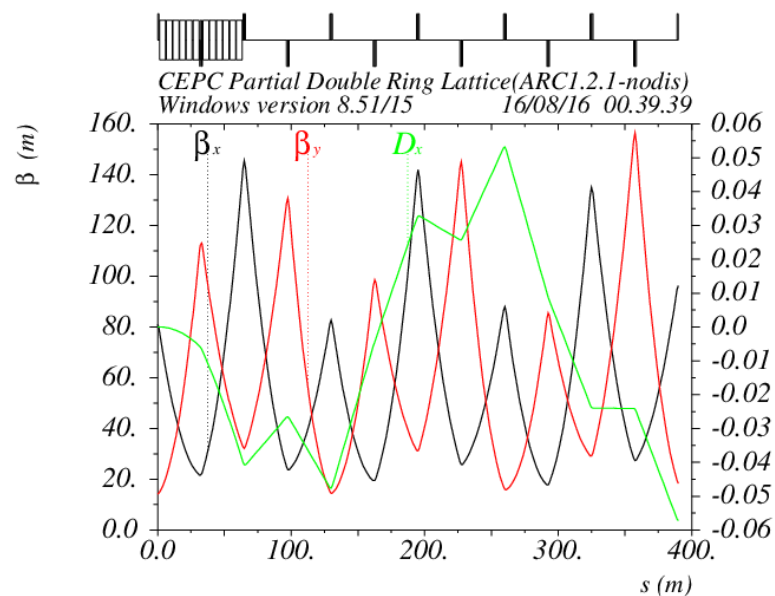




# CEPC PDR1.0.3 noFFS

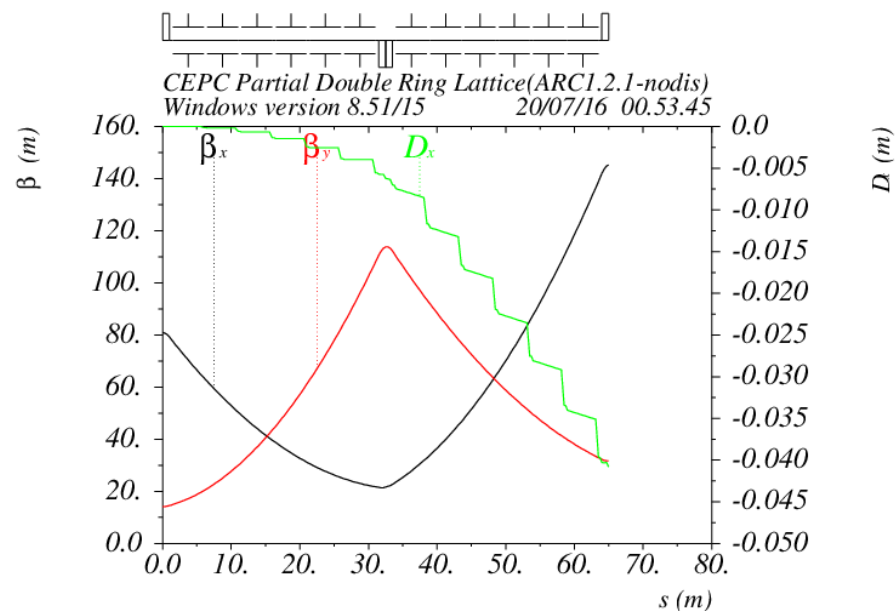


$$\delta_E / p_{oc} = 0.00000$$

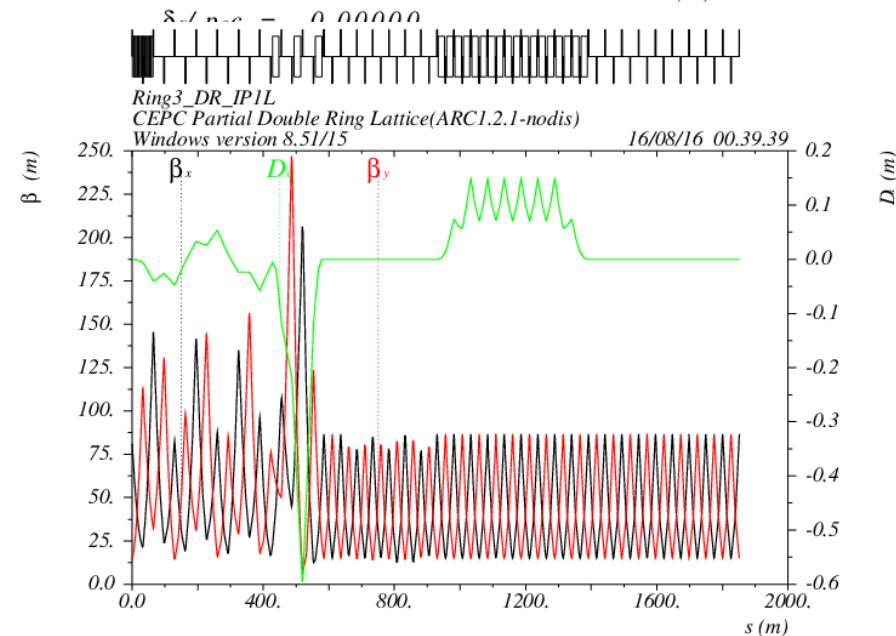


$$\delta_E / p_{oc} = 0.00000$$

Table name = TWISS



$$\delta_E / p_{oc} = 0.00000$$



$$\delta_E / p_{oc} = 0.00000$$

Table name = TWISS

## Electrostatic Separator in LEP

Separator length	4.5 m
Inner diameter of separator tank	540 mm
Electrode length	4.0 m
Electrode width	260 mm
Nominal gap	110 mm
Maximum operating field strength	20 kV/cm
Maximum operating voltage	+110 kV
Max. deflection per separator at 55 GeV	145 $\mu$ rad
Conditioning voltage on the test bench	$\pm 200$ kV
Conditioning voltage after installation	$\pm 160$ kV
Maximum voltage for vernier adjustment	$\pm 35$ kV
Range of vernier adjustment at 55 GeV	76 $\mu$ m
Horizontal good field region (1% limit)	$\pm 80$ mm
Maximum tilt per electrode	$\pm 5$ mrad
Pumping speed of sputter ion pumps	800 l/s
Pumping speed of sublimation pumps	1300 l/s
Nominal vacuum pressure in the low-beta insertions	$2.7 \cdot 10^{-8}$ Pa
Number of separators per collision point	4
Total number of separators	32
Total number of high voltage circuits	32

$L=4.5\text{m}$

$L_{\text{electrode}}=4.0\text{m}$

$E_{\text{field}}=2\text{MV/m}$

$E=55\text{GeV}$

$\text{Angle}=145\mu\text{rad}$

$E=120\text{GeV}$

$\text{Angle}=66\mu\text{rad}$

## Defocusing Quadrupole

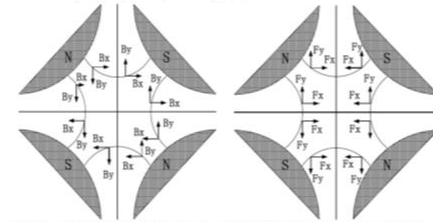
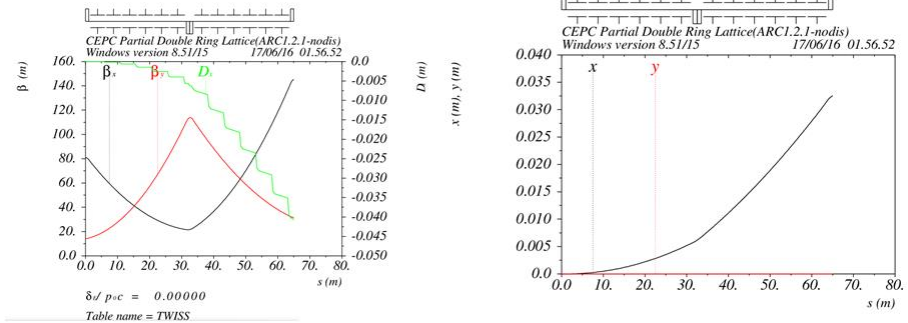


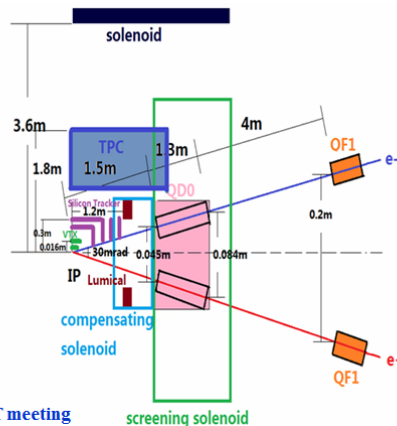
图 2.2 四极磁铁中磁场及粒子受力 (带负电荷的粒子垂直于纸面向里运动)



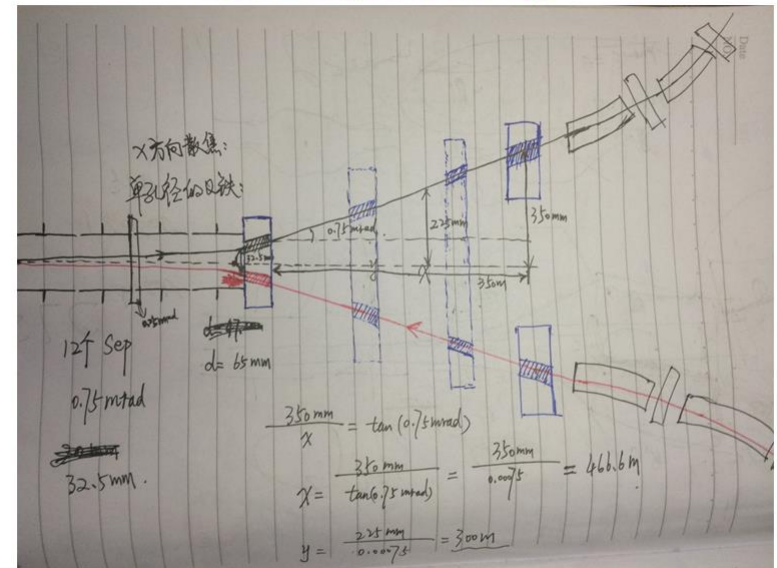
## Design Progress of QD0 in partial double ring

- ❖ Compact high gradient QD0 quadrupole magnets are needed in interaction region of the CEPC partial double ring.

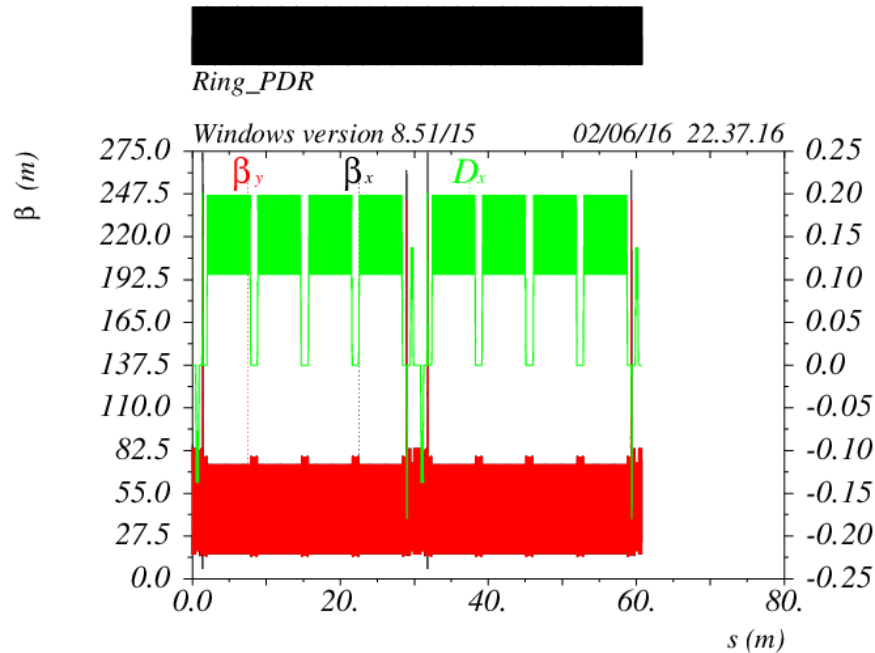
Name	Magnetic length (m)	Field gradient (T/m)	Coil inner radius (mm)
QD0	1.3	200	12.5



## Dual Aperture Q

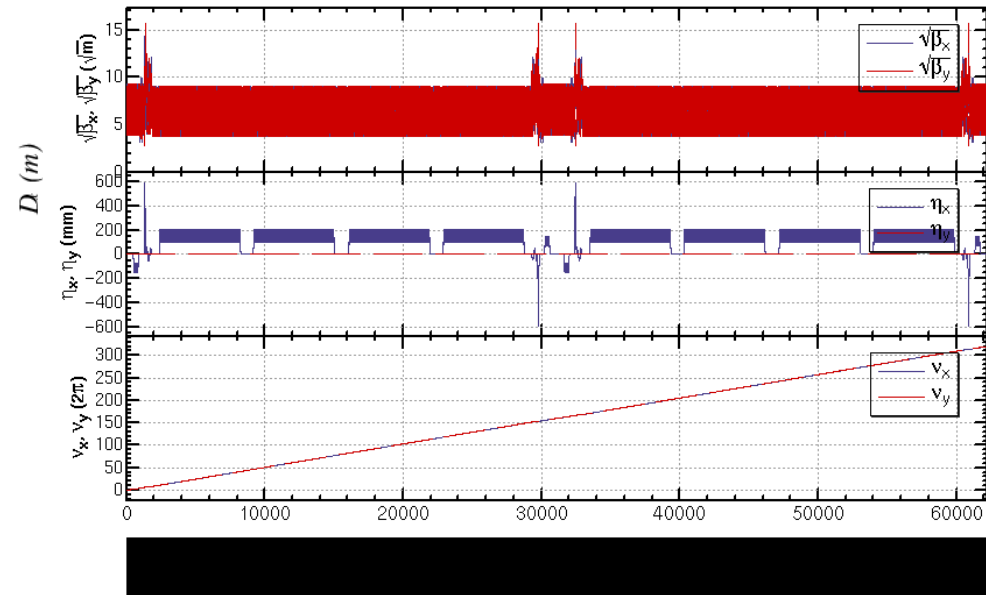


# CEPC ARC+PDR

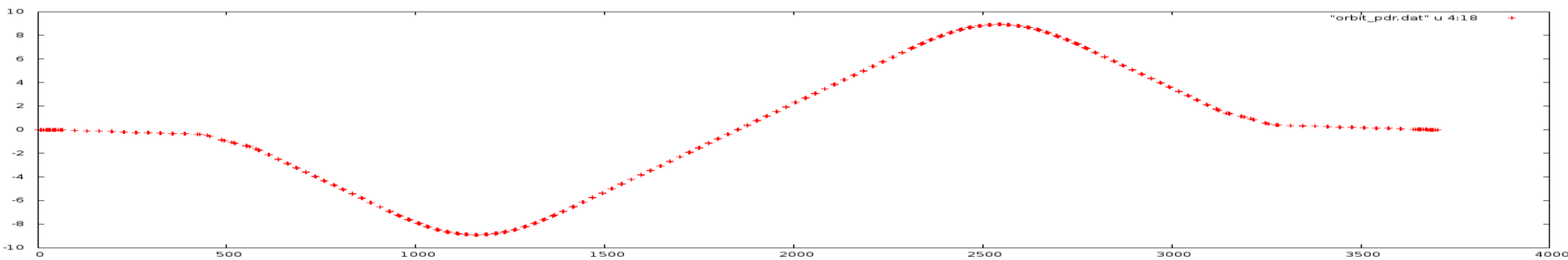
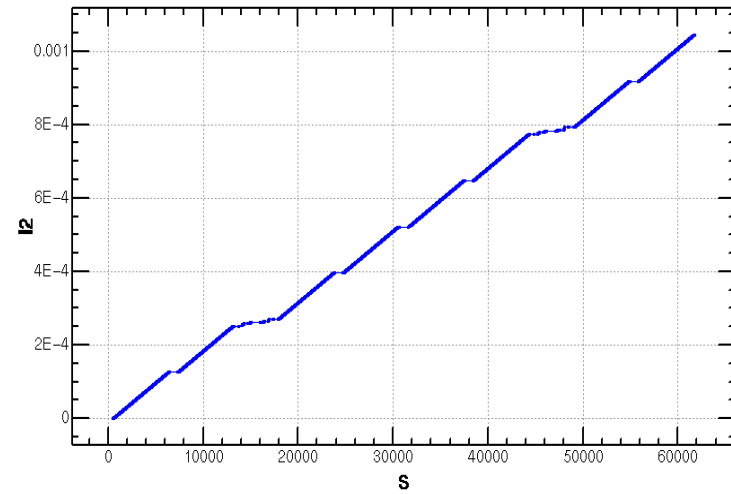
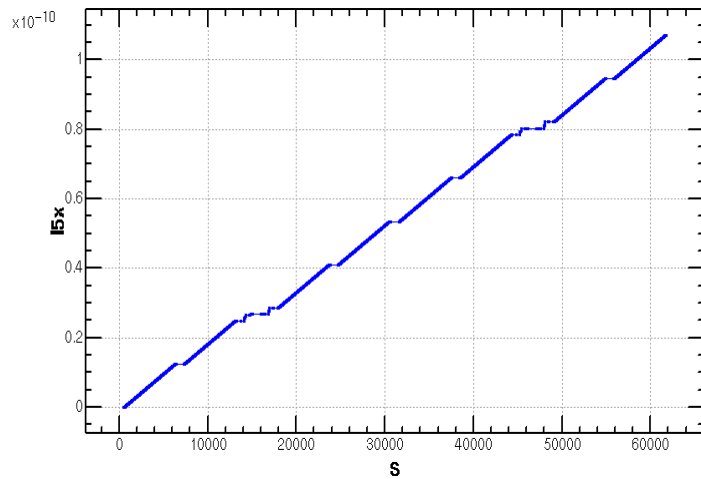
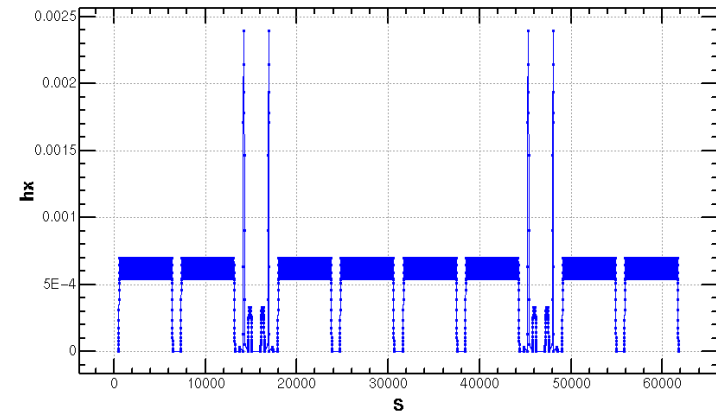
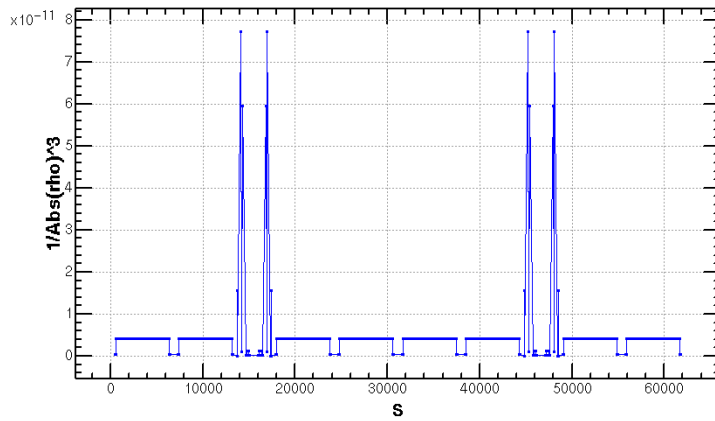


$\delta_E / p_{oc} = 0.00000$

Table name = TWISS



# Emittance Increase (2.06nm->2.1668nm)





# According to CEPC Pre-CDR Magnet Parameter

Dipole magnets	
Quantity	1984
Maximum field strength(T)	0.07
Magnetic gap (mm)	80
Bending angle (mrad)	3.17
Magnetic Length (m)	18
Bending radius (m)	6094
Good field region (mm)	100
Core cross section (W*H) (mm)	450*400

Super Conducting Q in CEPC IR	QF	QD
Field Gradient (T/m)	304	309
Magnetic Length (m)	1.25	0.72
Peak field in coil (T)	7.2	7.1
Coil inner diameter (mm)	40	40
Coil out diameter (mm)	74	74
Cryostat diameter (mm)	400	400
Coil mechanical length (mm)	1500	950

CEPC MQ	
Quantity	2304
Bore diameter (mm)	100
Field Gradient (T/m)	10
Magnetic Length (m)	2.0
Core width and height (mm)	700*700
Core length (mm)	1960

CEPC MS	SD	SF
Quantity	992	992
Aperture diameter (mm)	120	120
Good field region (mm)	100	100
Strength of sextupole field (T/m^2)	180	180
Magnetic Length (m)	700	400
Core width and height (mm)	520	520
Length of iron core (mm)	670	370

# Dipole Strength PDR1.0.3 without FFS

	Angle(mrad)	L(m)	Rho(m)	Brho(E0/c)(T/m)	B(T)	Ek(KeV)	KeV/m
B0	3.205	19.6	6115.44	400	0.06541	626.349	31.956
BSepL	-0.0625	4.5	-72000	400	-0.00556	53.2	11.822
BMatch1L	-8.344	19.6	-2348.99	400	-0.1702	1630.66	83.1967
BMatch2L	1.997	19.6	9814.72	400	0.0407	390.271	19.9118
BMatch3L	-7.653	19.6	-2561.09	400	-0.1562	1495.61	76.3069
B2	2.1428	19.6	9146.91	400	0.04373	418.764	21.3655
B3	-2.1428	19.6	-9146.91	400	-0.04373	418.764	21.3655
BMatch3R	7.653	19.6	2561.09	400	0.1562	1495.61	76.3069
BMatch2R	-1.997	19.6	-9814.72	400	-0.0407	390.271	19.9118
BMatch1R	8.344	19.6	2348.99	400	0.1702	1630.66	83.1967
BSepR	0.0625	4.5	72000	400	0.00556	53.2	11.822



# ***I. CEPC***

## **3. CEPC PDR DA Study ( NSGAI & DA Optimization)**

# NSGA-II & DA Optimization

## Objective

'npop': 500,  
'ngen': 100,  
'nobj': 30,  
'nvar': 12,

200CPU  
T1=40min  
T2=70h

## Variable

SF1.K2  
SF2.K2  
SF3.K2  
SF4.K2  
SF5.K2  
SF6.K2

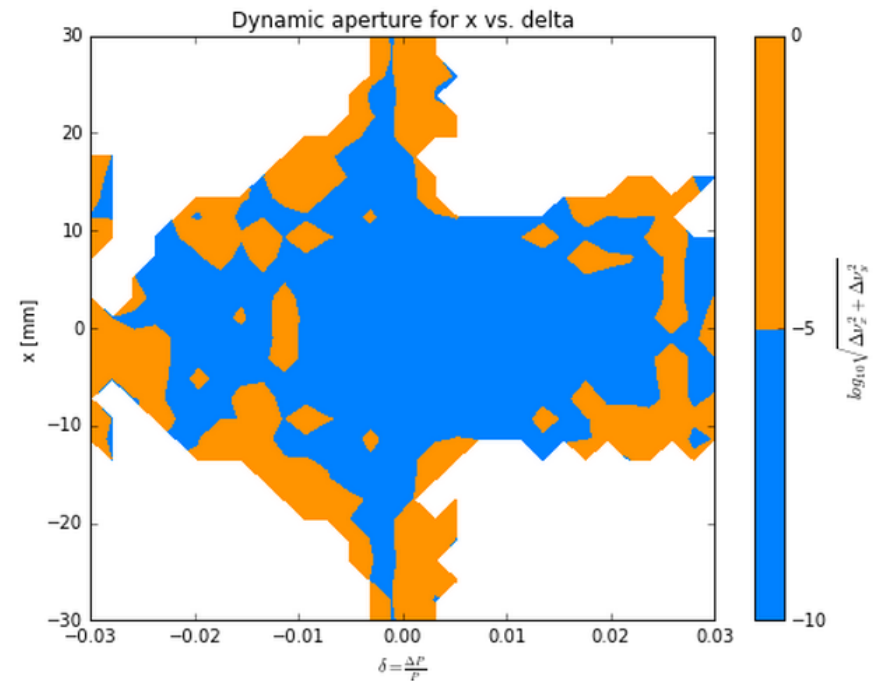
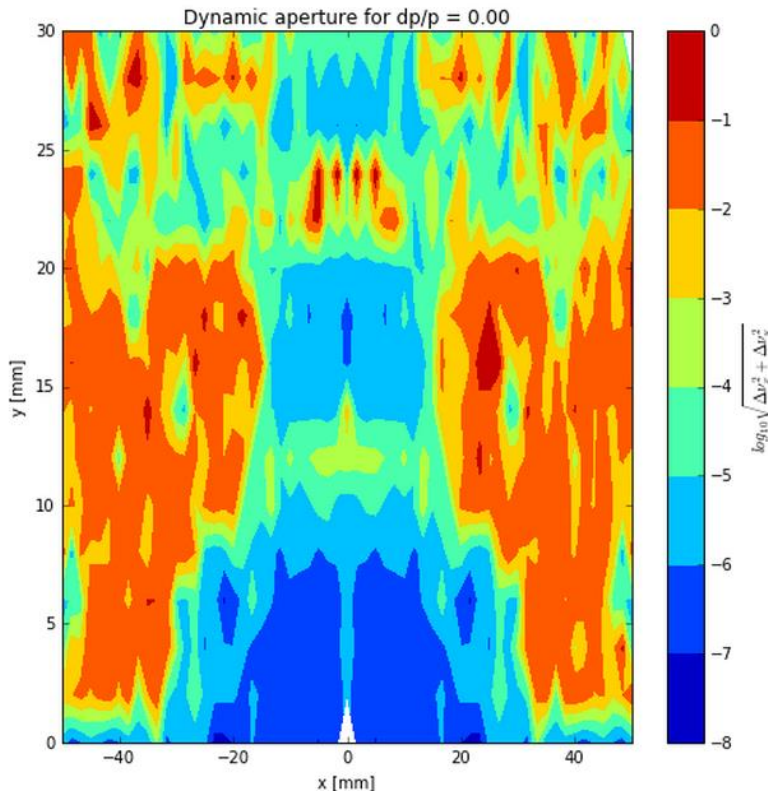
SD1.K2  
SD2.K2  
SD3.K2  
SD4.K2  
SD5.K2  
SD6.K2

cepc\_ndr\_0099.txt

```
p[nvar+0] = abs(nsls2.ring.h1['h30000'])  
p[nvar+1] = abs(nsls2.ring.h1['h21000'])  
p[nvar+2] = abs(nsls2.ring.h1['h10110'])  
p[nvar+3] = abs(nsls2.ring.h1['h10200'])  
p[nvar+4] = abs(nsls2.ring.h1['h10020'])  
p[nvar+5] = abs(nsls2.ring.h1['h20001'])  
p[nvar+6] = abs(nsls2.ring.h1['h10002'])  
p[nvar+7] = abs(nsls2.ring.h1['h00201'])
```

```
p[nvar+8] = abs(nsls2.ring.h2['h00310'])  
p[nvar+9] = abs(nsls2.ring.h2['h11200'])  
p[nvar+10] = abs(nsls2.ring.h2['h10111'])  
p[nvar+11] = abs(nsls2.ring.h2['h00112'])  
p[nvar+12] = abs(nsls2.ring.h2['h30001'])  
p[nvar+13] = abs(nsls2.ring.h2['h11110'])  
p[nvar+14] = abs(nsls2.ring.h2['h22000'])  
p[nvar+15] = abs(nsls2.ring.h2['h00004'])  
p[nvar+16] = abs(nsls2.ring.h2['h00400'])  
p[nvar+17] = abs(nsls2.ring.h2['h10201'])  
p[nvar+18] = abs(nsls2.ring.h2['h20020'])  
p[nvar+19] = abs(nsls2.ring.h2['h10021'])  
p[nvar+20] = abs(nsls2.ring.h2['h10003'])  
p[nvar+21] = abs(nsls2.ring.h2['h21001'])  
p[nvar+22] = abs(nsls2.ring.h2['h31000'])  
p[nvar+23] = abs(nsls2.ring.h2['h40000'])  
p[nvar+24] = abs(nsls2.ring.h2['h20002'])  
p[nvar+25] = abs(nsls2.ring.h2['h00220'])  
p[nvar+26] = abs(nsls2.ring.h2['h20200'])  
p[nvar+27] = abs(nsls2.ring.h2['h20110'])  
p[nvar+28] = abs(nsls2.ring.h2['h11002'])  
p[nvar+29] = abs(nsls2.ring.h2['h00202'])
```

# Nonlinear Driving Term (ARC)



Betx: 80.992367

bety: 14.172123

2nm

Sizmax: 402.47um

Sigmay: 9.22um

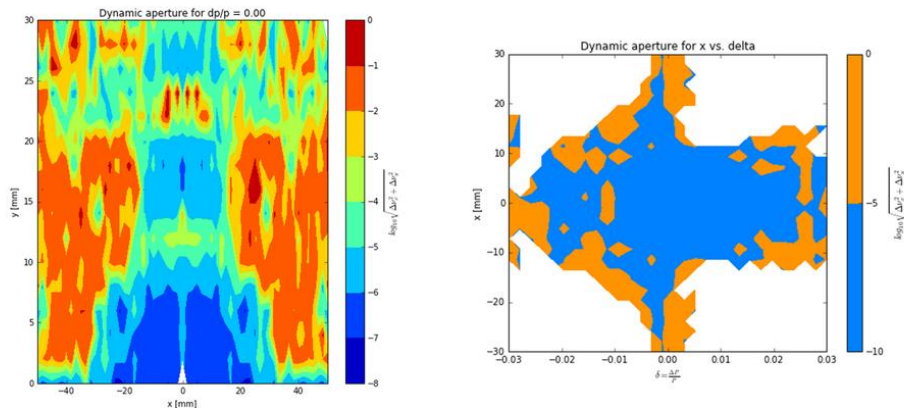
X: 60 Sigma

Y: 813 Sigma

2 groups



## Nonlinear Driving Term (ARC)

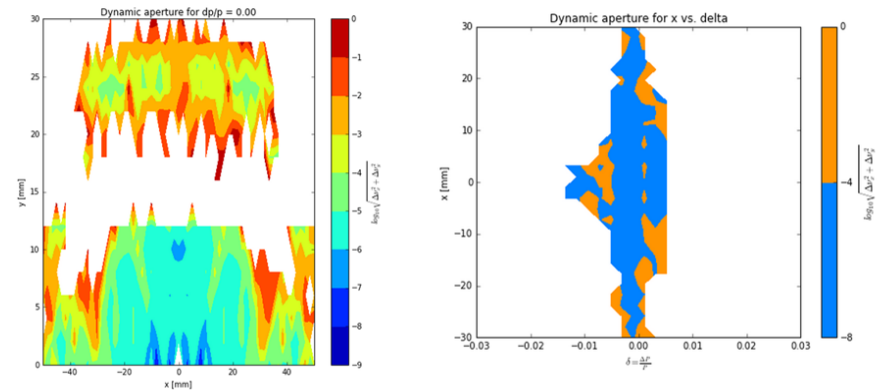


Betx: 80.992367  
 bety: 14.172123  
 2nm  
 Sizmax: 402.47um  
 Sigmay: 9.22um

X: 60 Sigma  
 Y: 813 Sigma

2 groups

## Nonlinear Driving Term (ARC-20160630)

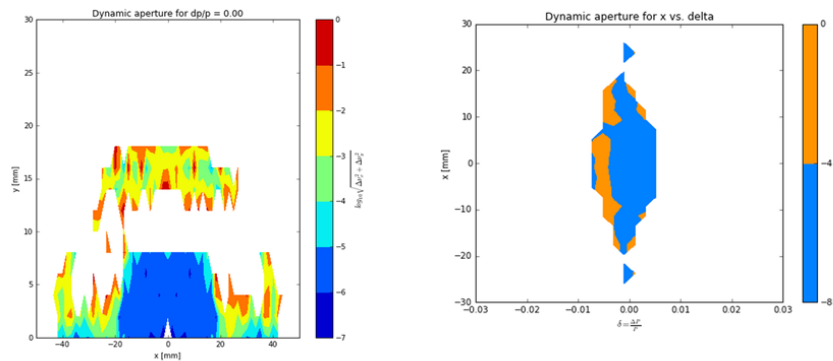


Betx: 80.992367  
 bety: 14.172123  
 2nm  
 Sizmax: 402.47um  
 Sigmay: 9.22um

X: 60 Sigma  
 Y: 813 Sigma

96 groups

## Nonlinear Driving Term (ARC-20160707)

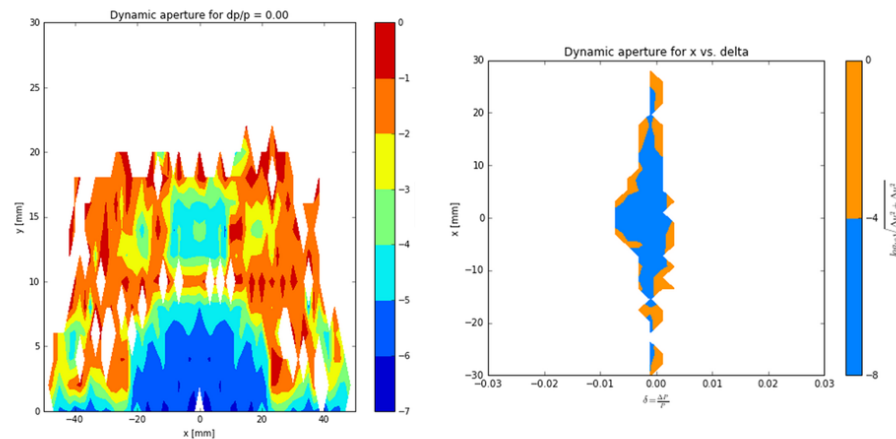


Betx: 80.992367  
 bety: 14.172123  
 2nm  
 Sizmax: 402.47um  
 Sigmay: 9.22um

X: 60 Sigma  
 Y: 700 Sigma

96 groups

## Nonlinear Driving Term (ARC-20160722)



Betx: 80.992367  
 bety: 14.172123  
 2nm  
 Sizmax: 402.47um  
 Sigmay: 9.22um

X: 65 Sigma  
 Y: 813 Sigma

96 groups

# Nonlinear Driving Term (ARC)

```
In [7]: cepec.ring.geth1()
cepec.ring.h1
```

```
Out[7]: {'h00111': (4.906054441305847+0j), 'h11001': (4.883077561376199+0j)}
```

```
In [8]: cepec.ring.geth2()
cepec.ring.h2
```

```
Out[8]: {'h00112': (-6713.2390326540426-2.4327666617307564e-12j),
'h00220': (-6.7117007239114013e-06+2.4007420051930239e-08j),
'h11002': (-5459.1975174445843+3.0300657816173526e-12j),
'h11110': (7.6489916699494385e-06+4.3427621676528361e-07j),
'h22000': (-8.6121626494394287e-06-9.276845958083868e-11j)}
```



Out[7]:

	s	betax	alfax	mux	etax	etaxp	betay	alfay	muy	etay	etayp
0.000e+00	8.099e+01	-1.141e-14	0.000e+00	2.912e-08	-6.628e-18	1.417e+01	-1.144e-15	0.000e+00	-0.000e+00	-0.000e+00	
5.482e+04	8.099e+01	-1.199e-14	2.861e+02	2.912e-08	3.373e-17	1.417e+01	1.018e-13	2.862e+02	-0.000e+00	0.000e+00	

Tune: nux = 286.080, nuy = 286.220

uncorrected chromaticity: chx0 = -3.643e+02, chy0 = -3.645e+02

corrected chromaticity: chx = 3.444e-01, chy = 4.578e-01

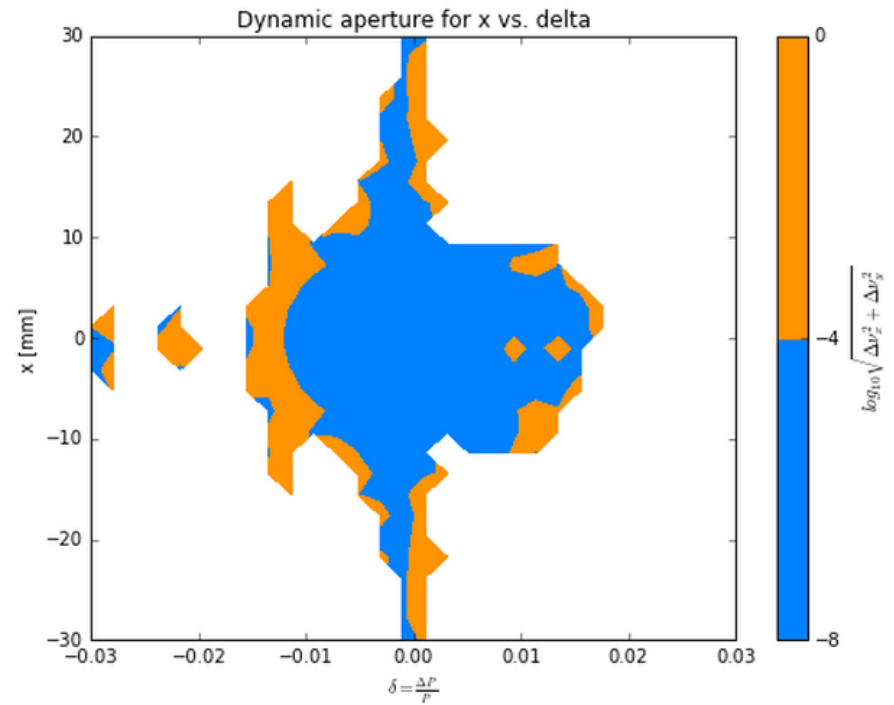
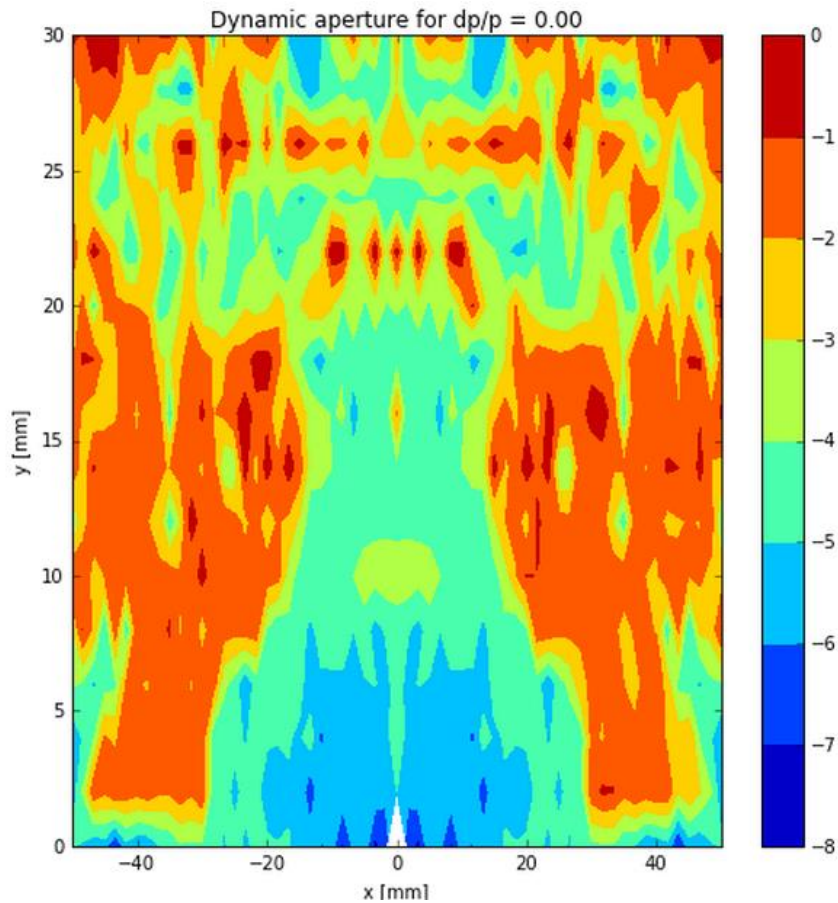
== First order driving terms ==

```
h11001 = 3.791759e+00 +0.000000e+00j
h00111 = 3.466382e+00 +0.000000e+00j
```

== Second order driving terms ==

```
h00112 = 4.271577e+00 -1.784912e-11j
h11110 = -2.187326e-04 -2.742092e-07j
h00220 = 2.154167e-04 -3.058040e-08j
h11002 = 9.935156e+01 -3.127386e-10j
h22000 = 3.593634e-04 +2.928573e-10j
```

# Nonlinear Driving Term (ARC\_PDR\_20160630)



Betx: 80.992367

bety: 14.172123

2nm

Sizmax: 402.47um

Sigmay: 9.22um

X: 45 Sigma

Y: 780 Sigma

2 groups



# ***I. CEPC***

## **4. CEPC APDR Scheme**

# New idea: Advanced PDR (APDR)



IHEP-AC-LC-Note2016-002

ILC-物理-2016-02

May 20<sup>th</sup>, 2016

The advanced partial double ring scheme for CEPC

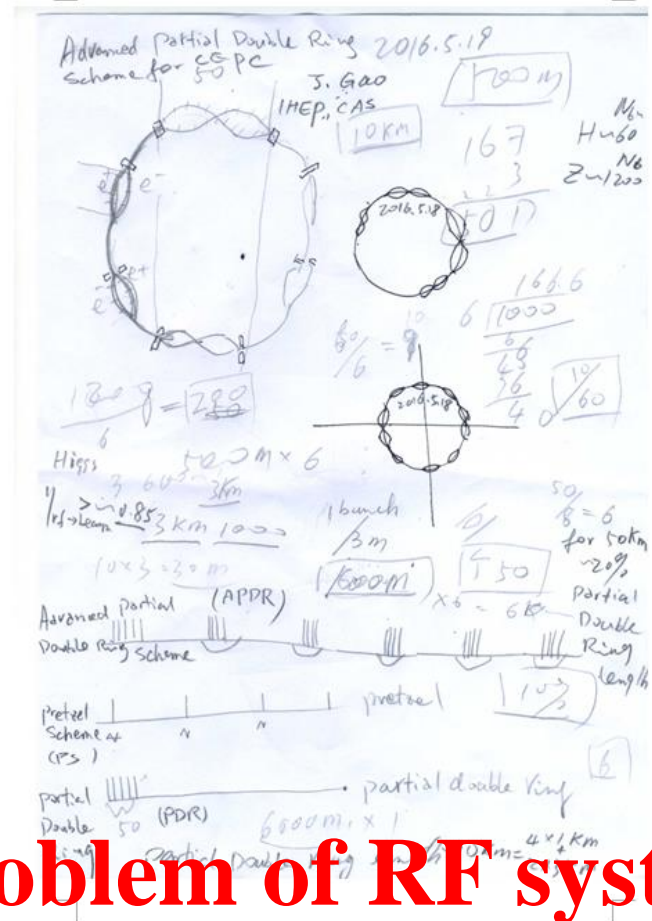
GAO Jie (高杰)

ILC Group, Accelerator Center

Institute of High Energy Physics (IHEP), Beijing

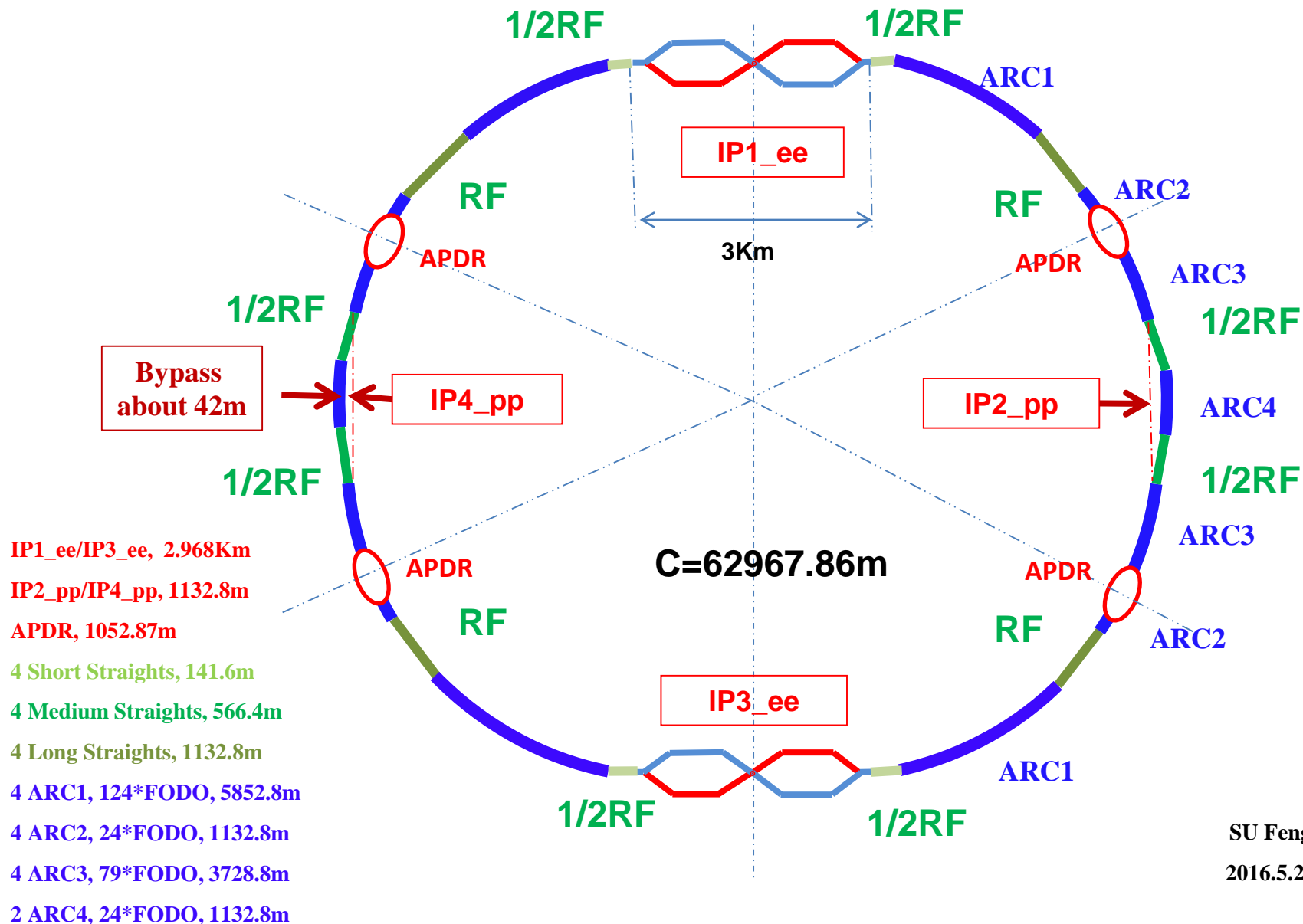
中国科学院高能物理研究所

Institute of High Energy Physics



To solve the big problem of RF system

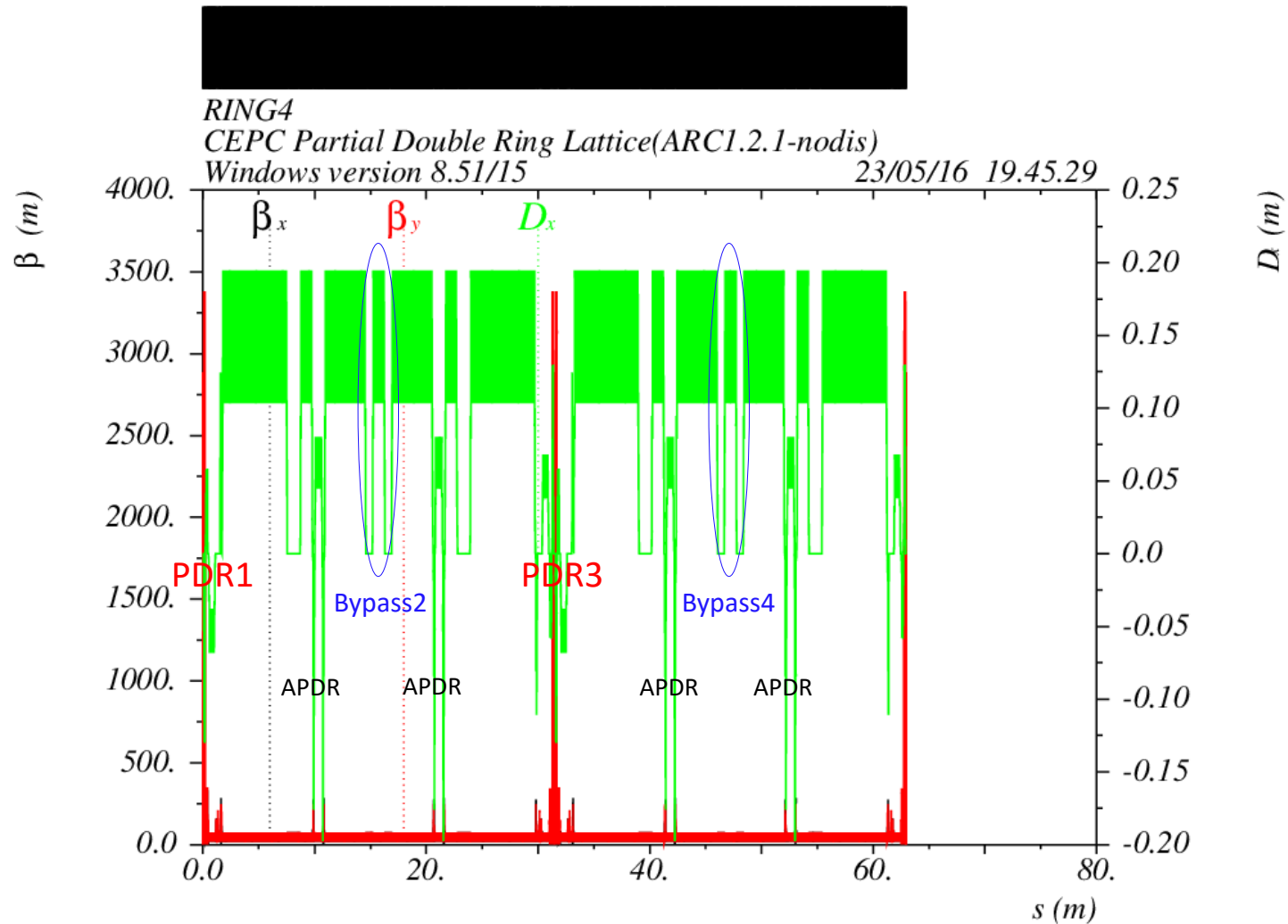
# CEPC Advanced Partial Double Ring Layout I



SU Feng

2016.5.23

# CEPC Advanced Partial Double Ring Optics I

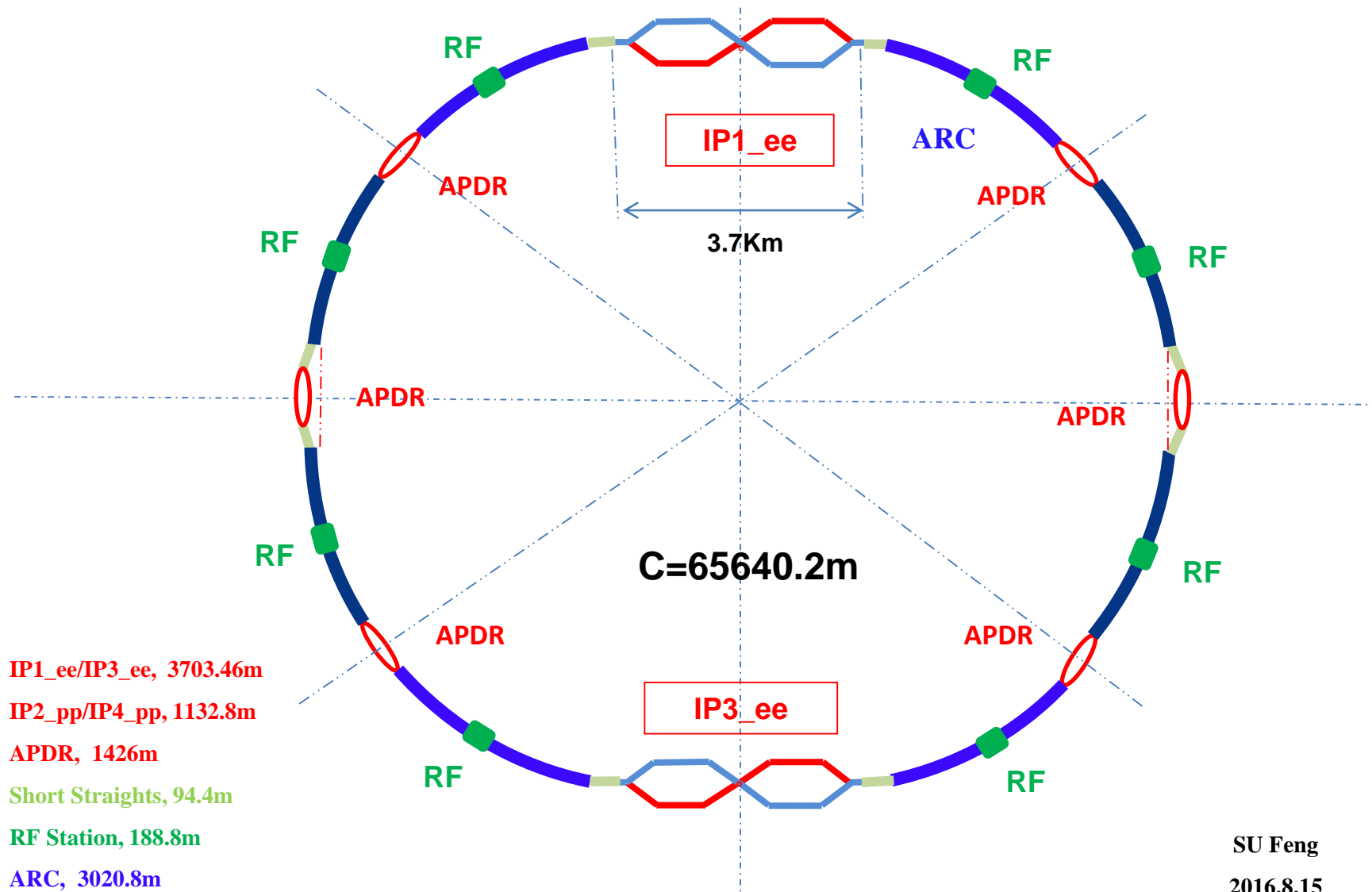


$$\delta_E / p_{0c} = 0.00000$$

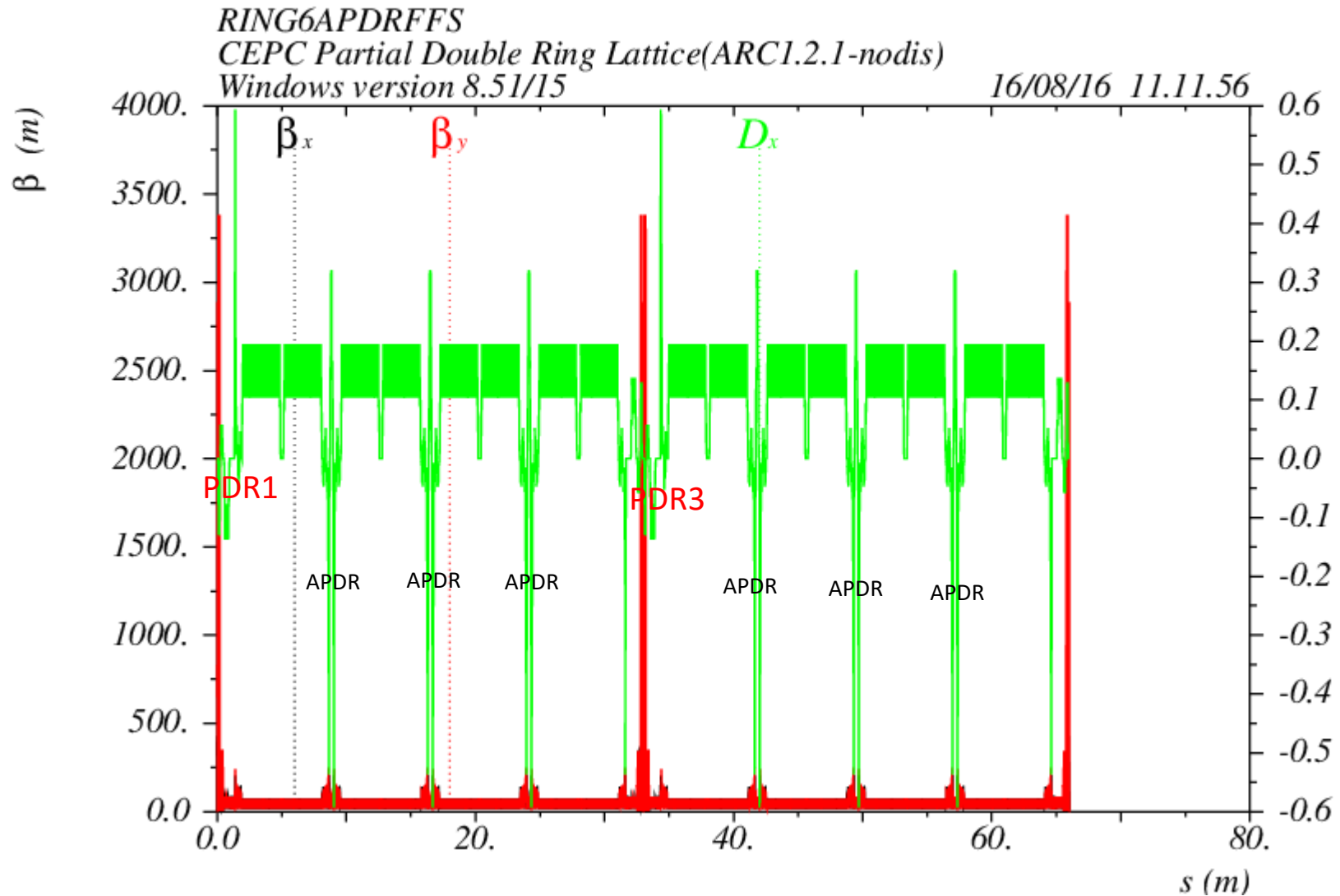
Table name = TWISS



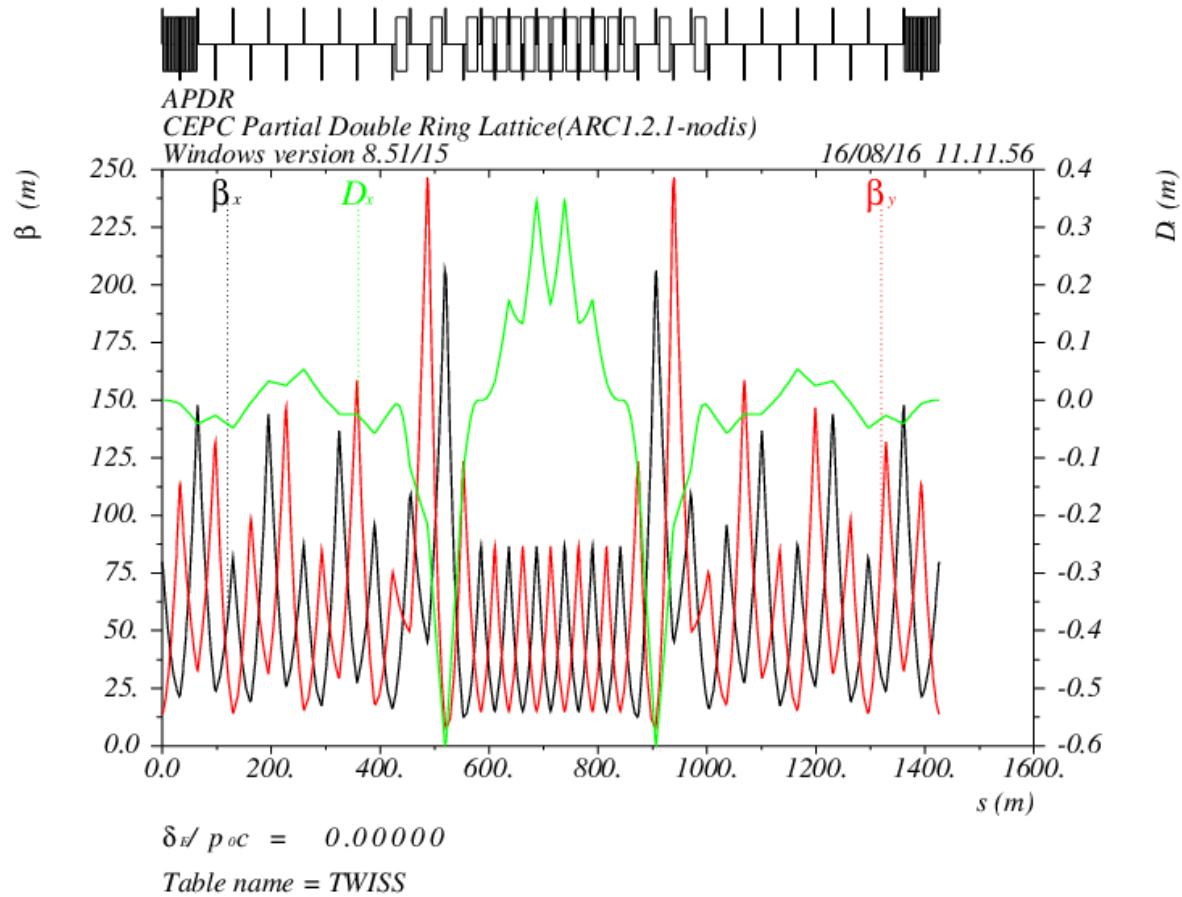
# CEPC Advanced Partial Double Ring Layout II



# CEPC Advanced Partial Double Ring Optics II

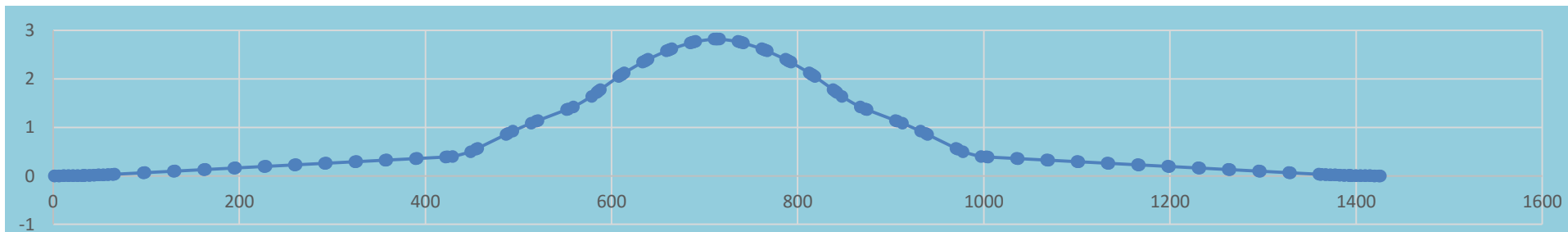


# APDR Part

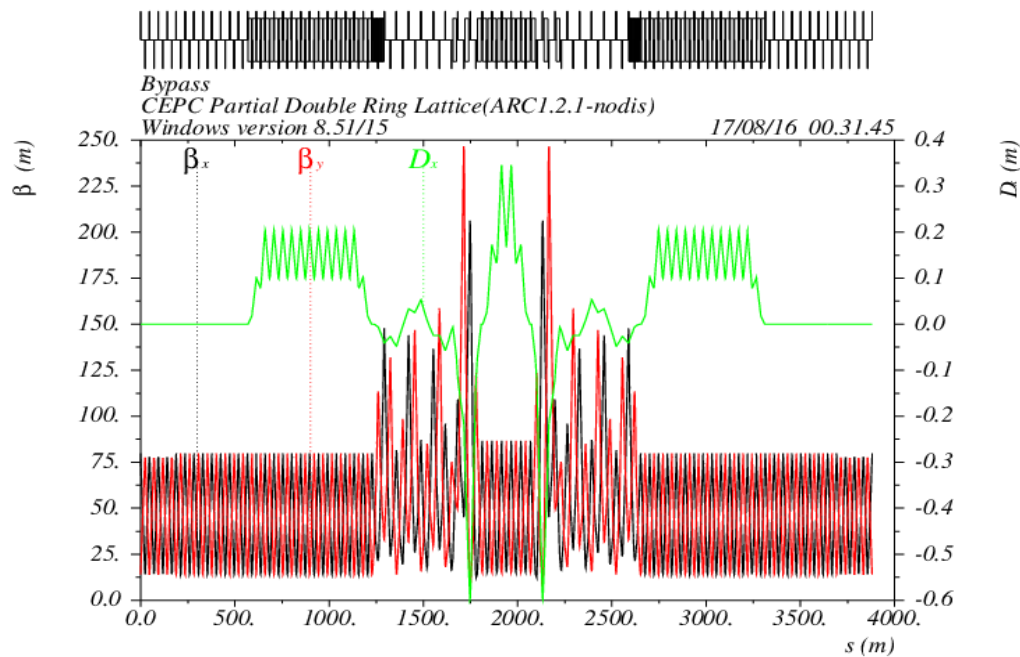
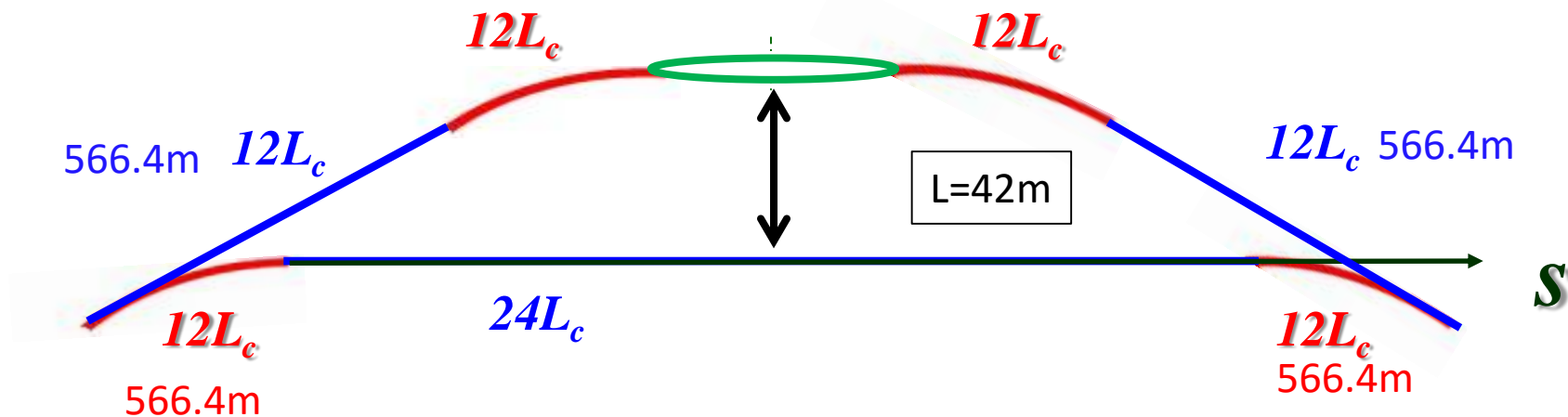


Need update

1426m



# Bypass Part at IP2/4

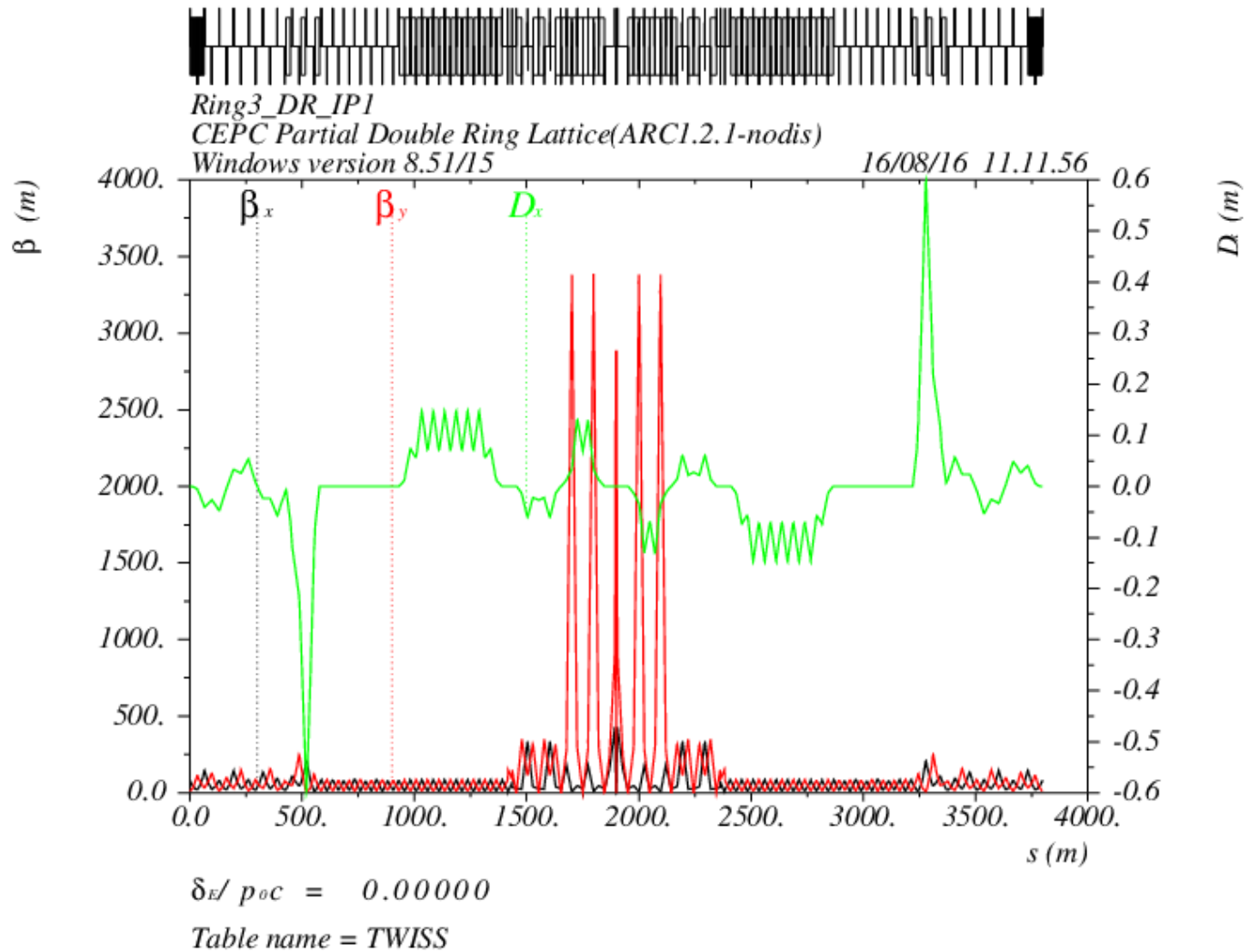


$\delta s / p_{oc} = 0.00000$

Table name = TWISS

Cell length=47.2m

# PDR Part

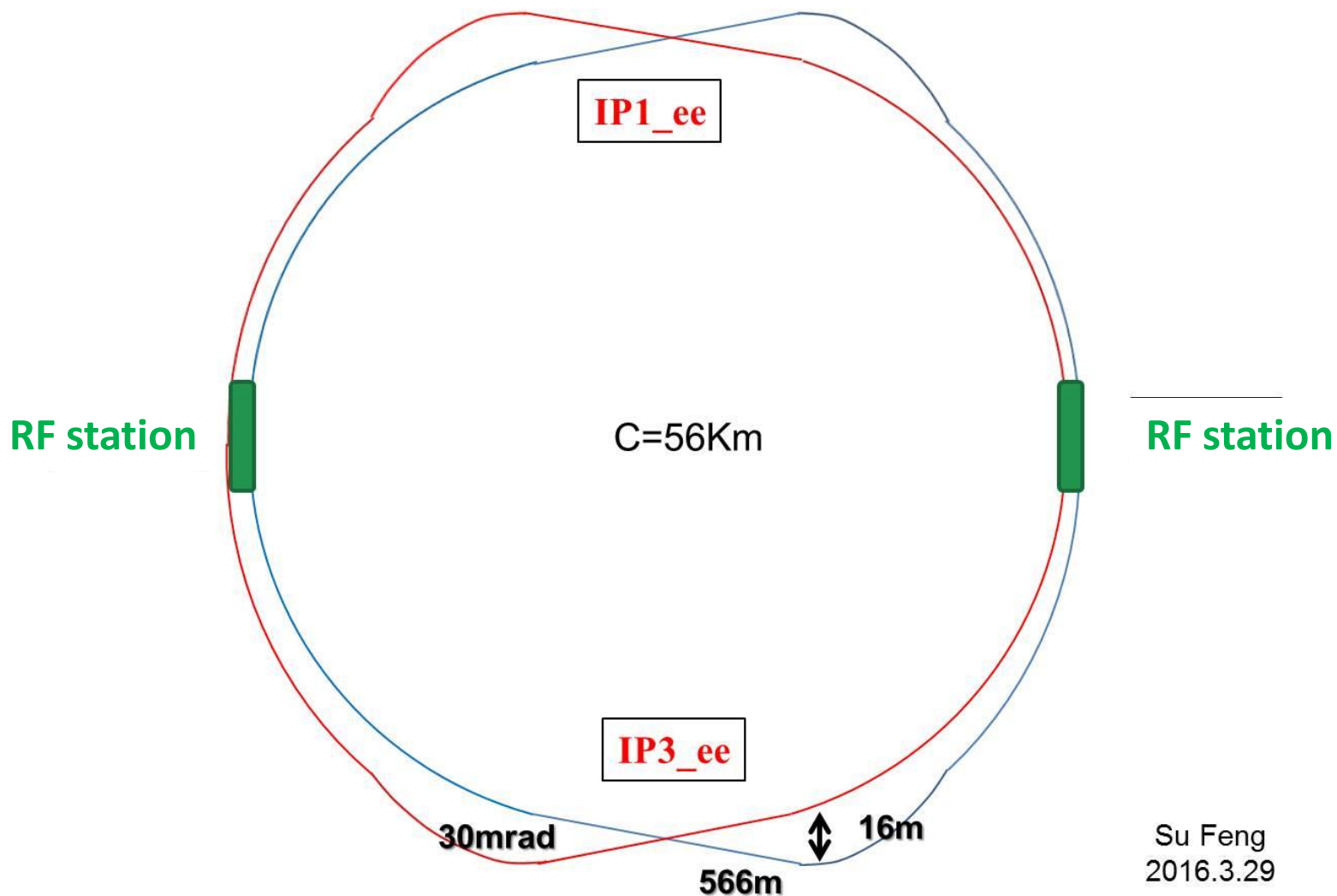




# ***I. CEPC***

## **5. CEPC Double Ring Scheme**

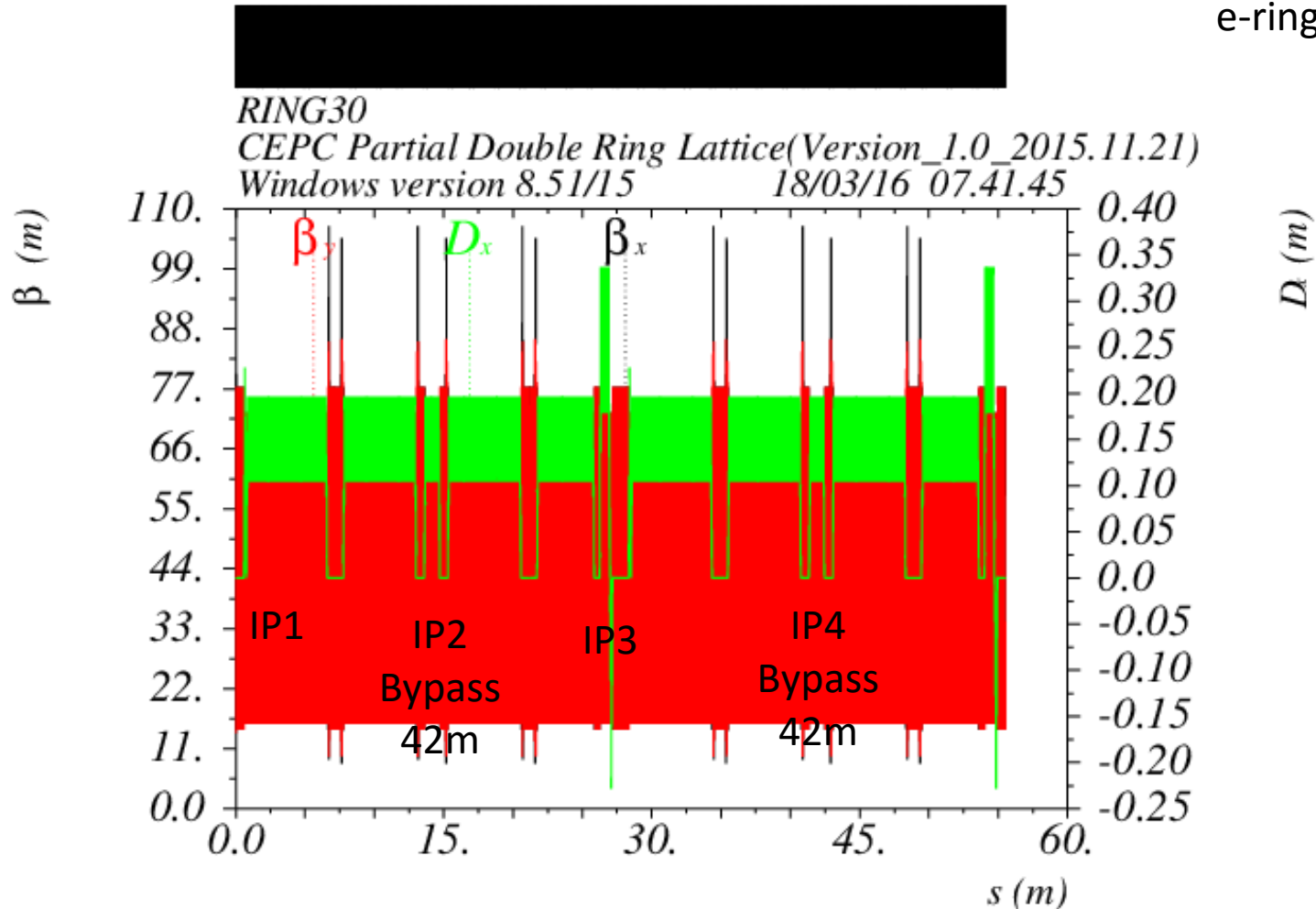
# CEPC Double Ring Scheme Layout





# Double Ring Scheme

e-ring



$$\delta_E / p_0 c = 0.00000$$

Table name = TWISS

## **6. Summary**

- ◆ The first version of CEPC Partial Double Ring Lattice was designed (Version 1.0). The whole length of CEPC PDR is 3781.27m, full crossing angle is 30mrad, maximum distance between two ring is 14.913m.
- ◆ The Dynamic Aperture need to be optimized. Now the DA of CEPC with PDR and Bypass(at IP2/4) and without FFS is better than before, but the DA with FFS is not good enough.
- ◆ The linear lattice of PDR may also be optimized.

## **II. SPPC Parameter Choice and Lattice Design**

- 1. SPPC Parameter Choice and Optimize**
- 2. SPPC Lattice Layout and Design:**
  - a. FODO Cell and ARC**
  - b. Dispersion Suppressor Section**
  - c. Long Straight Section**
  - d. IR**
- 3. SPPC Dynamic Aperture Study**
- 4. Summary**

## ***II. SPPC***

### **1. SPPC Parameter Choice and Optimize**

# SPPC ARC Parameter Choice

## Theory:

$$E_0 = 70 - 100 \text{ TeV}$$

$$\gamma = \frac{35 \text{ TeV}}{938.27 \text{ MeV}} = 37313.4$$

$$\beta = 1$$

$$B\rho = \frac{E_0}{c} = 3.1267 \beta\gamma = 116635.29 \text{ Tm}$$

$$B_0 = 20 \text{ T}$$

$$\rho = \frac{B\rho}{B_0} = \frac{116635.29}{20} = 5831.7645$$

$$L_{\text{Dipole}} = 2\pi\rho = 36642.05 \text{ m}$$

$$\text{ARC filling factor } f_1 = 0.8$$

$$L_{\text{ARC}} = \frac{L_{\text{Dipole}}}{f_1} = \frac{36642.05}{0.8} = 45802.56 \text{ m}$$

$$L_{\text{ss3pp}} = L_{\text{ss7pp}} = 973.83 \text{ m}$$

$$L_{\text{ss2}} = L_{\text{ss4}} = L_{\text{ss6}} = L_{\text{ss8}} = 788.31 \text{ m}$$

$$L_1 = 50903.46$$

$$L_{\text{ss1}} = L_{\text{ss5}} = 3.3 \text{ km}$$

$$C_0 = 57503.46 \text{ m}$$

## In Practice:

### ARC CELL

	LQ	DQS	LS	DSB	LB	DBB
SPPC	4m	1m	0.5m	1m	14.8m	1m
FCC-hh	6.3137m	1m	0.5m	2.184m	14.3m	1.36m

B max [T]	G max [T/m]	k1	k2
19.61	582.156	4.9899E-3	0

#### Pre-CDR:

Dipole: L=15m B=20T

Quadrupole:

D = 45 mm  $B_{\text{pole}} = 16 \text{ T}$   
G = 711.1 T/m  $K_1 = 6.097 \times 10^{-3}$

Betax: 244.878/42.57  
Betay: 42.569/244.869 ( $\epsilon_n = 4.1 \mu\text{m}$ )

E (Collision: 35TeV)  
(Injection: 2.1TeV)

$$\epsilon = \frac{\epsilon_n}{\gamma}$$

$\epsilon$  (Collision:  $1.099 \times 10^{-10} \text{ m} = 0.1099 \text{ nm}$ )  
(Injection:  $1.83 \times 10^{-9} \text{ m} = 1.83 \text{ nm}$ )

$\sigma$  (Collision:  $1.66 \times 10^{-4} \text{ m} = 166 \mu\text{m}$ )  
(Injection:  $6.76 \times 10^{-4} \text{ m} = 676 \mu\text{m}$ )

$R = 20 \times \sigma_{\text{inj}} = 13.52 \text{ mm}$

D = 27.04

$$L_B = 14.8 \text{ m}$$

$$\text{FODO: } f_1 = \frac{14.8 \times 8}{144.4} = 0.8199$$

$$\text{ARC: } f_1 = \frac{14.8 \times 8 \times 38 + 14.8 \times 8 \times 2}{(38 + 2 + 2) \times 144.4} = 0.7809$$

$$L_{\text{ARC}} = \frac{37389.85}{0.7809} = 47880.46$$

$$L_1 = 52981.42$$

$$C_0 = 59581.42$$

# SPPC Parameter Choice and Optimize

Table 1: SPPC Parameter List.

**Version 201503**

	SPPC(Pre-CDR)	SPPC-54.7Km	SPPC-100Km	SPPC-100Km	SPPC-78Km
<b>Main parameters and geometrical aspects</b>					
Beam energy[ $E_0$ ]/TeV	35.6	35.0	50.0	68.0	50.0
Circumference[ $C_0$ ]/km	54.7	54.7	100.0	100.0	78.0
Dipole field[B]/T	20	19.69	14.73	20.03	19.49
Dipole curvature radius[ $\rho$ ]/m	5928	5922.6	11315.9	11315.9	8549.8
Bunch filling factor[ $f_2$ ]	0.8	0.8	0.8	0.8	0.8
Arc filling factor[ $f_1$ ]	0.79	0.79	0.79	0.79	0.79
Total dipole length [ $L_{Dipole}$ ]/m	37246	37213	71100	71100	53720
Arc length[ $L_{ARC}$ ]/m	47146	47105	90000	90000	68000
Straight section length[ $L_{ss}$ ]/m	7554	7595	10000	10000	10000
<b>Physics performance and beam parameters</b>					
Peak luminosity per IP[ $L$ ]/ $cm^{-2}s^{-1}$	$1.1 \times 10^{35}$	$1.2 \times 10^{35}$	$1.52 \times 10^{35}$	$1.02 \times 10^{36}$	$1.52 \times 10^{35}$
Beta function at collision[ $\beta^*$ ]/m	0.75	0.85	0.97	0.24	1.06
Max beam-beam tune shift per IP[ $\xi_y$ ]	0.006	0.0065	0.0067	0.008	0.0073
Number of IPs contribut to $\Delta Q$	2	2	2	2	2
Max total beam-beam tune shift	0.012	0.013	0.0134	0.016	0.0146
Circulating beam current[ $I_b$ ]/A	1.0	1.024	1.024	1.024	1.024
Bunch separation[ $\Delta t$ ]/ns	25	25	25	25	25
Number of bunches[ $n_b$ ]	5835	5835	10667	10667	8320
Bunch population[ $N_p$ ] ( $10^{11}$ )	2.0	2.0	2.0	2.0	2.0
Normalized RMS transverse emittance[ $\varepsilon$ ]/ $\mu m$	4.10	3.72	3.65	3.05	3.36
RMS IP spot size[ $\sigma^*$ ]/ $\mu m$	9.0	8.85	7.85	3.04	7.86
Beta at the 1st parasitic encounter[ $\beta_1$ ]/m	19.5	18.70	16.51	64.1	15.36
RMS spot size at the 1st parasitic encounter[ $\sigma_1$ ]/ $\mu m$	45.9	43.2	33.6	51.9	31.14
RMS bunch length[ $\sigma_z$ ]/mm	75.5	56.5	65	15.8	70.6
Full crossing angle[ $\theta_c$ ]/ $\mu rad$	146	138	108	166	99
Reduction factor according to cross angle[ $F_{ca}$ ]	0.8514	0.9257	0.9248	0.9283	0.9248
Reduction factor according to hour glass effect[ $F_h$ ]	0.9975	0.9989	0.9989	0.9989	0.9989
Energy loss per turn[ $U_0$ ]/MeV	2.10	1.97	4.30	14.7	5.69
Critical photon energy[ $E_c$ ]/keV	2.73	2.60	3.97	9.96	5.25
SR power per ring[ $P_0$ ]/MW	2.1	2.0	4.4	15.1	5.82
Transverse damping time [ $\tau_x$ ]/h	1.71	1.80	2.15	0.86	1.27
Longitudinal damping time [ $\tau_\varepsilon$ ]/h	0.85	0.90	1.08	0.43	0.635

# SPPC Parameter Choice and Optimize

Table 1: SPPC Parameter List.

**Version 201607**

	SPPC(Pre-CDR)	SPPC-59.2Km	SPPC-100Km	SPPC-100Km	SPPC-80Km
<b>Main parameters and geometrical aspects</b>					
Beam energy[ $E_0$ ]/TeV	35.6	35.0	50.0	65.0	50.0
Circumference[ $C_0$ ]/km	54.7	59.2	100.0	100.0	80.0
Dipole field[B]/T	20	19.70	15.52	19.83	19.74
Dipole curvature radius[ $\rho$ ]/m	5928	5921.5	10924.4	10924.4	8441.6
Bunch filling factor[ $f_2$ ]	0.8	0.8	0.8	0.8	0.8
Arc filling factor[ $f_1$ ]	0.79	0.78	0.78	0.78	0.78
Total dipole length [ $L_{Dipole}$ ]/m	37246	37206	68640	68640	53040
Arc length[ $L_{ARC}$ ]/m	47146	47700	88000	88000	68000
Straight section length[ $L_{ss}$ ]/m	7554	11500	12000	12000	12000
<b>Physics performance and beam parameters</b>					
Peak luminosity per IP[ $L$ ]/ $cm^{-2}s^{-1}$	$1.1 \times 10^{35}$	$1.20 \times 10^{35}$	$1.52 \times 10^{35}$	$1.02 \times 10^{36}$	$1.52 \times 10^{35}$
Beta function at collision[ $\beta^*$ ]/m	0.75	0.85	0.99	0.22	1.06
Max beam-beam tune shift per IP[ $\xi_y$ ]	0.006	0.0065	0.0068	0.0079	0.0073
Number of IPs contribut to $\Delta Q$	2	2	2	2	2
Max total beam-beam tune shift	0.012	0.0130	0.0136	0.0158	0.0146
Circulating beam current[ $I_b$ ]/A	1.0	1.024	1.024	1.024	1.024
Bunch separation[ $\Delta t$ ]/ns	25	25	25	25	25
Number of bunches[ $n_b$ ]	5835	6315	10667	10667	8533
Bunch population[ $N_p$ ]( $10^{11}$ )	2.0	2.0	2.0	2.0	2.0
Normalized RMS transverse emittance[ $\varepsilon$ ]/ $\mu m$	4.10	3.72	3.62	3.10	3.35
RMS IP spot size[ $\sigma^*$ ]/ $\mu m$	9.0	8.85	7.86	3.04	7.86
Beta at the 1st parasitic encounter[ $\beta_1$ ]/m	19.5	18.70	16.36	68.13	15.31
RMS spot size at the 1st parasitic encounter[ $\sigma_1$ ]/ $\mu m$	45.9	43.20	33.31	55.20	31.03
RMS bunch length[ $\sigma_z$ ]/mm	75.5	56.60	65.68	14.88	70.89
Full crossing angle[ $\theta_c$ ]/ $\mu rad$	146	138.23	106.60	176.66	99.28
Reduction factor according to cross angle[ $F_{ca}$ ]	0.8514	0.9257	0.9247	0.9283	0.9241
Reduction factor according to hour glass effect[ $F_h$ ]	0.9975	0.9989	0.9989	0.9989	0.9989
Energy loss per turn[ $U_0$ ]/MeV	2.10	1.97	4.45	12.71	5.76
Critical photon energy[ $E_c$ ]/keV	2.73	2.60	4.11	9.02	5.32
SR power per ring[ $P_0$ ]/MW	2.1	2.01	4.56	13.01	5.89
Transverse damping time [ $\tau_x$ ]/h	1.71	1.946	2.08	0.946	1.28
Longitudinal damping time [ $\tau_\varepsilon$ ]/h	0.85	0.973	1.04	0.473	0.64



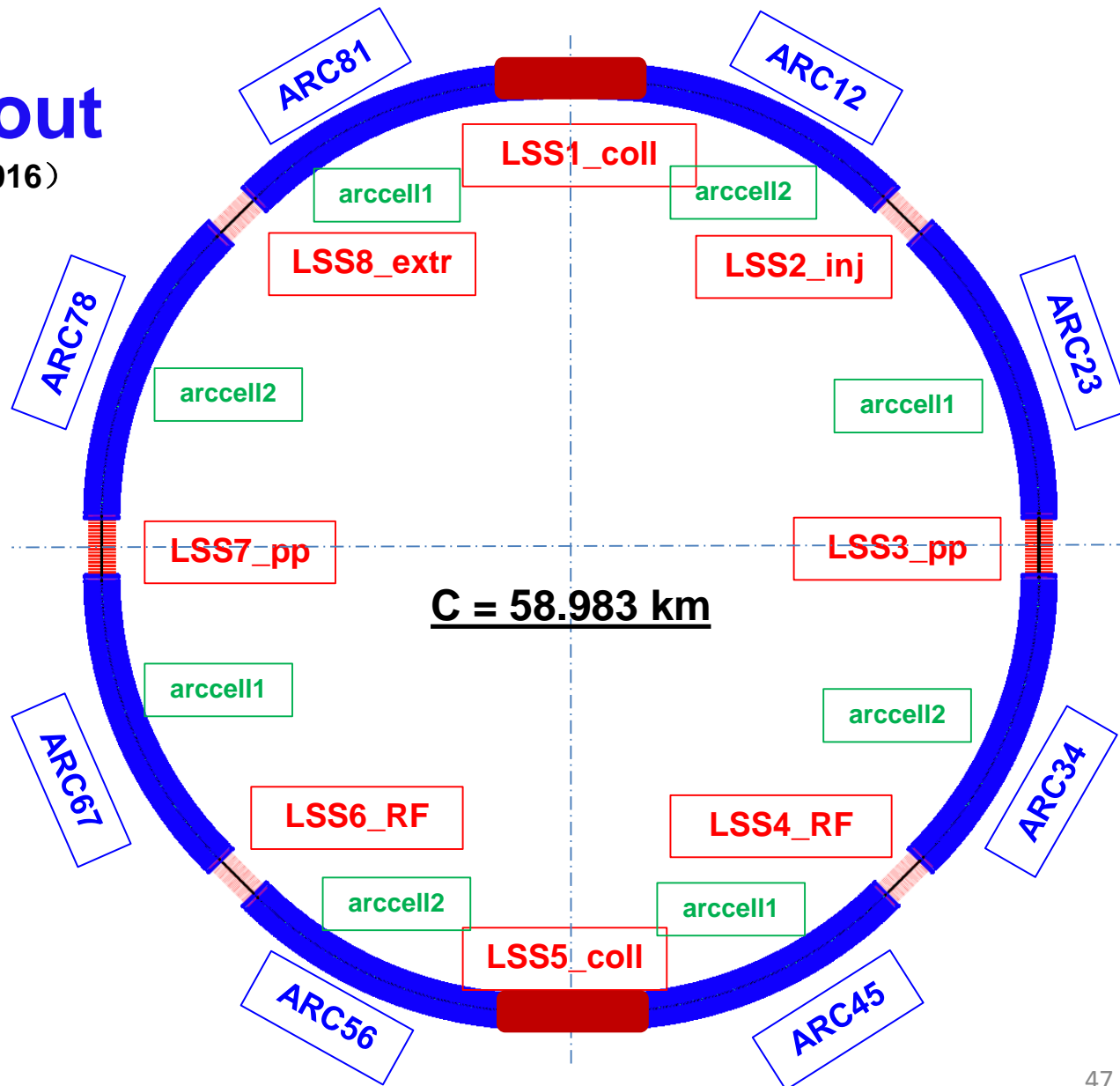
## ***II. SPPC***

### **2. SPPC Lattice Layout and Design:**

- a. FODO Cell and ARC**
- b. Dispersion Suppressor Section**
- c. Long Straight Section**
- d. IR**

# SPPC Layout

(Su Feng Jan. 10, 2016)



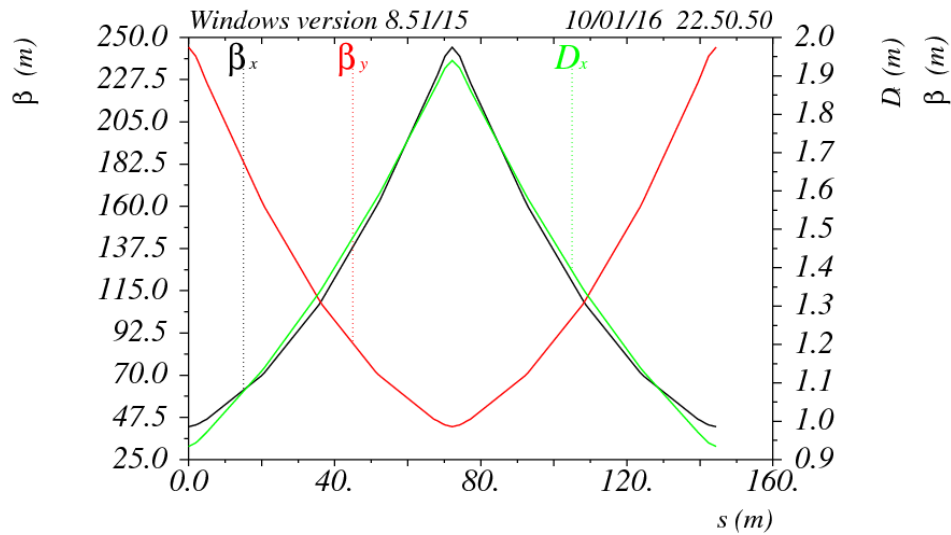
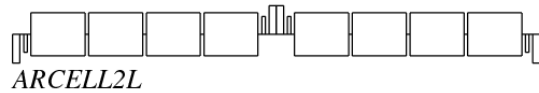
LSS1/5\_coll : 3.2Km

LSS2/4/6/8: 788.31m

LSS3/7\_pp: 973.83m

ARC: 5963.2m

# FODO Cell in ARC



$\delta_E / p_{oc} = 0.00000$

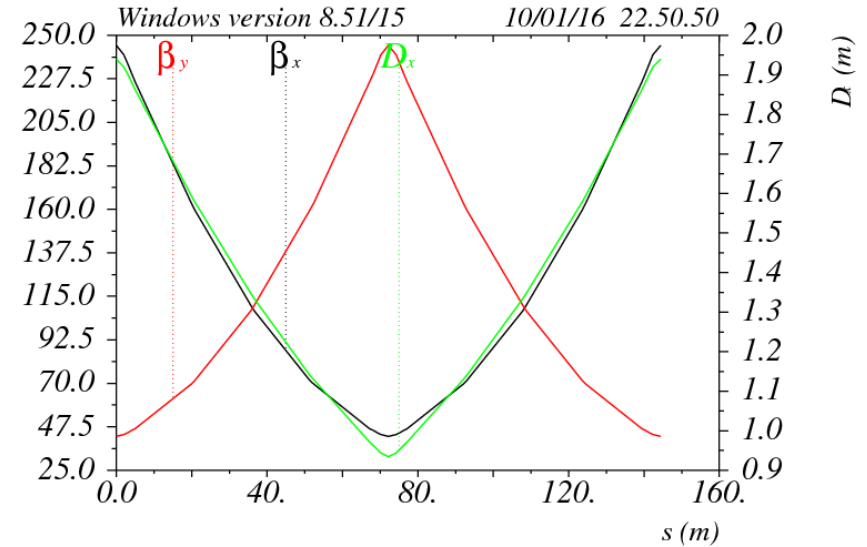
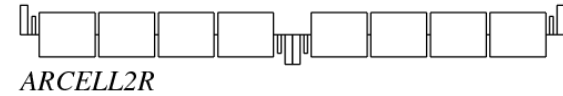
Table name = TWISS

arccell1

L=144.4m

Betax: 244.878/42.57

Betay: 42.569/244.869

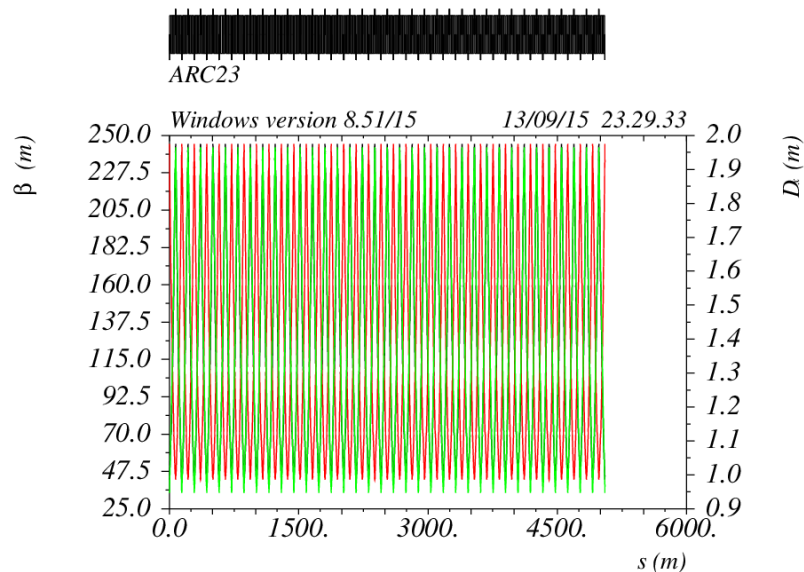


$\delta_E / p_{oc} = 0.00000$

Table name = TWISS

arccell2

# ARC (ARCDSP, 36 CELL, ARCDSPR)

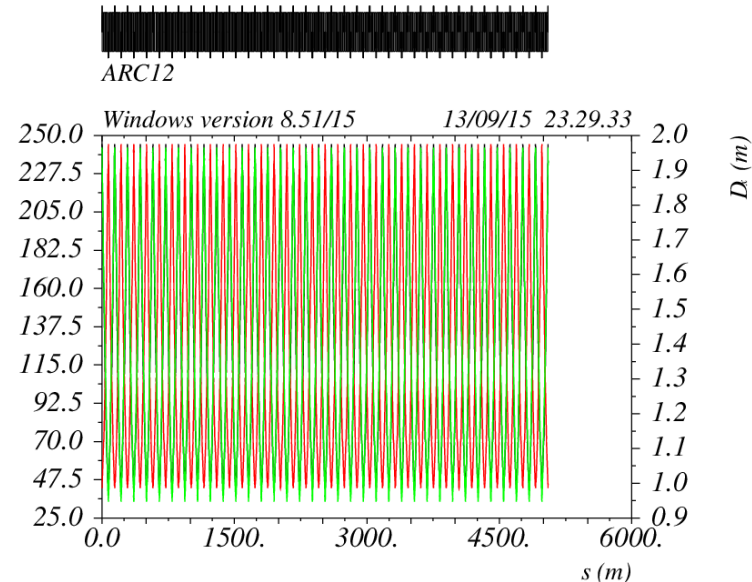


$\delta E / p_0 c = 0.00000$

Table name = TWISS

ARC23  
ARC45  
ARC67  
ARC81

L=5963.2m

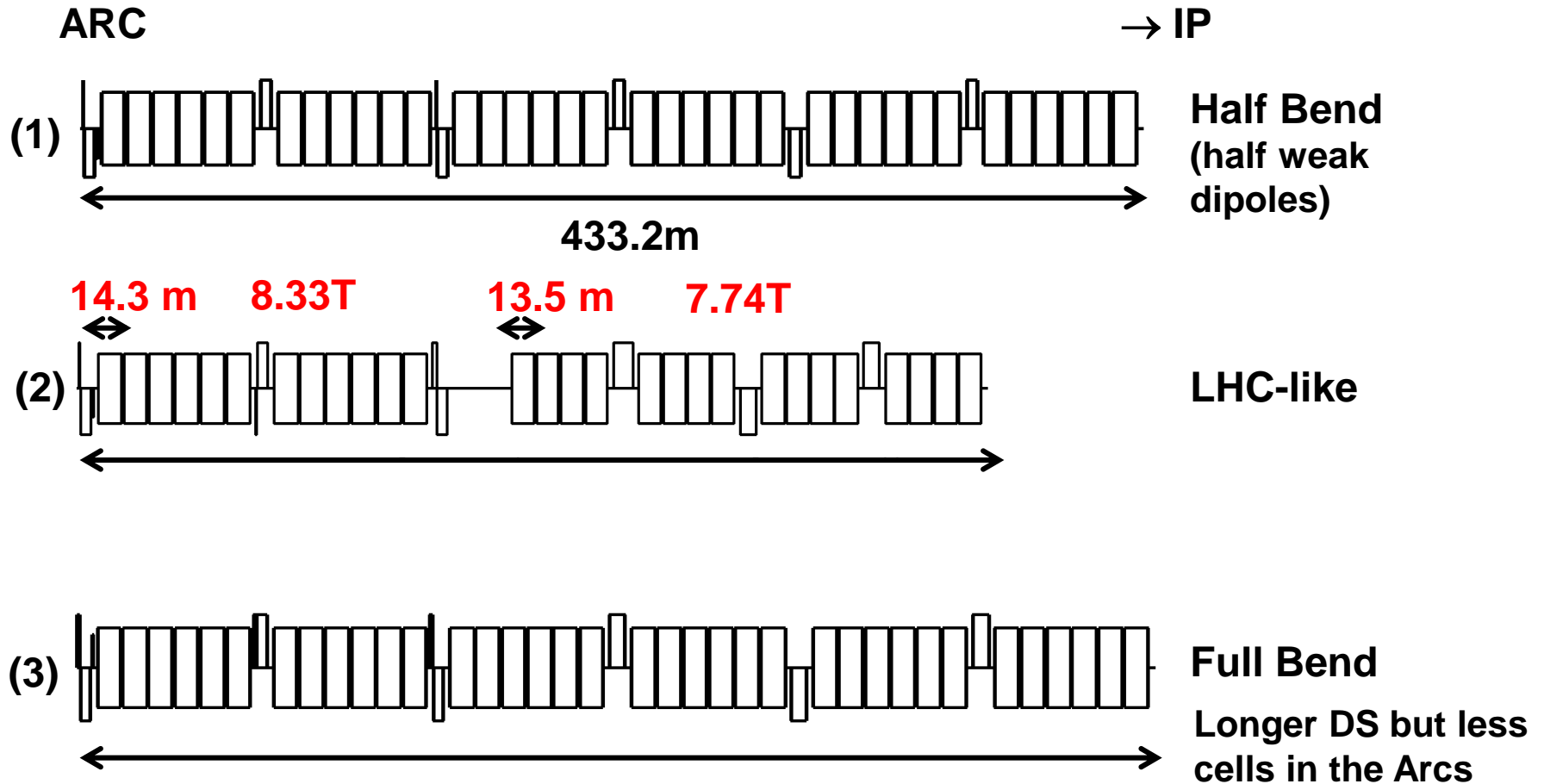


$\delta E / p_0 c = 0.00000$

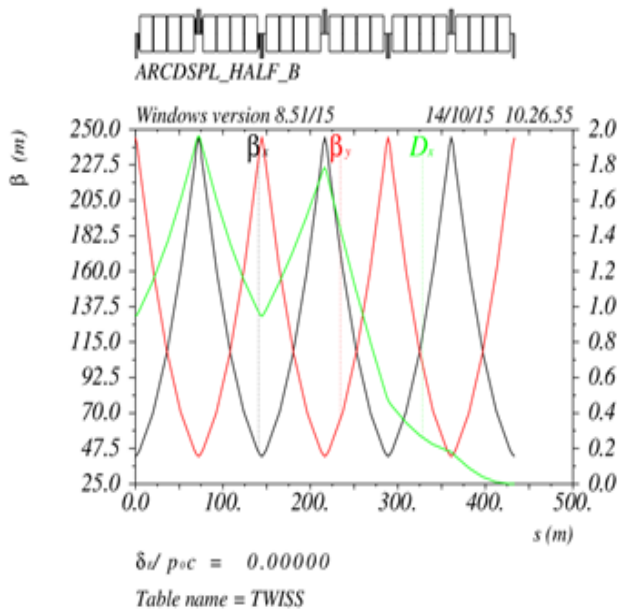
Table name = TWISS

ARC12  
ARC34  
ARC56  
ARC78

# Dispersion Suppressor (DS) types

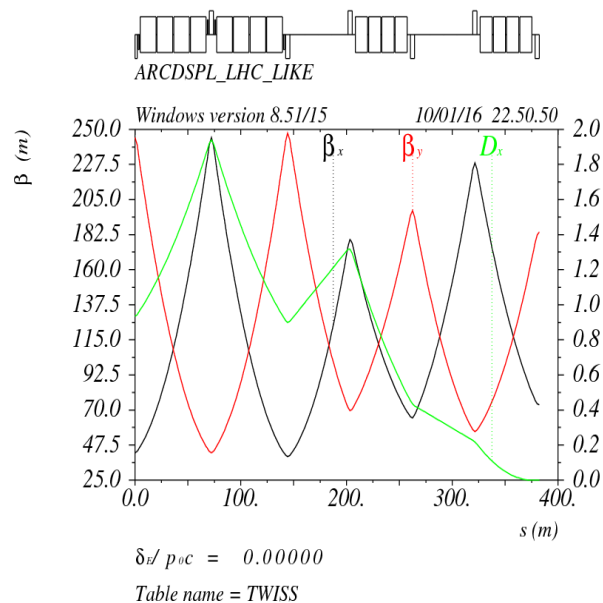


## (1) Half Bend



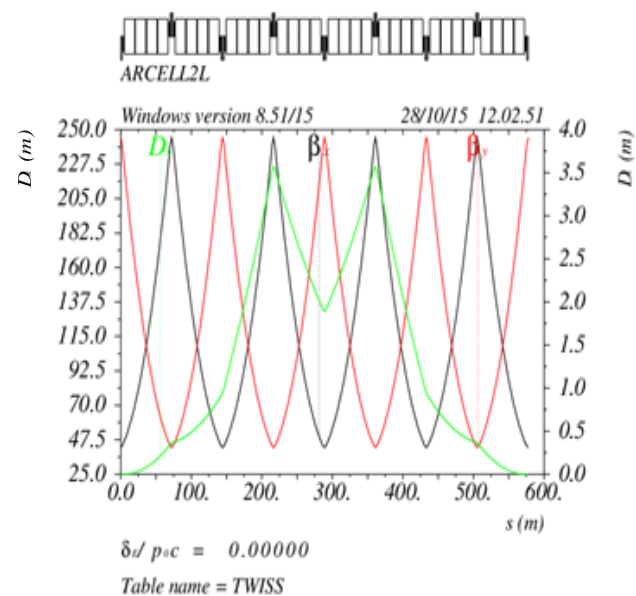
**L=433.2m**

## (2) LHC Like



**L=382.4m**

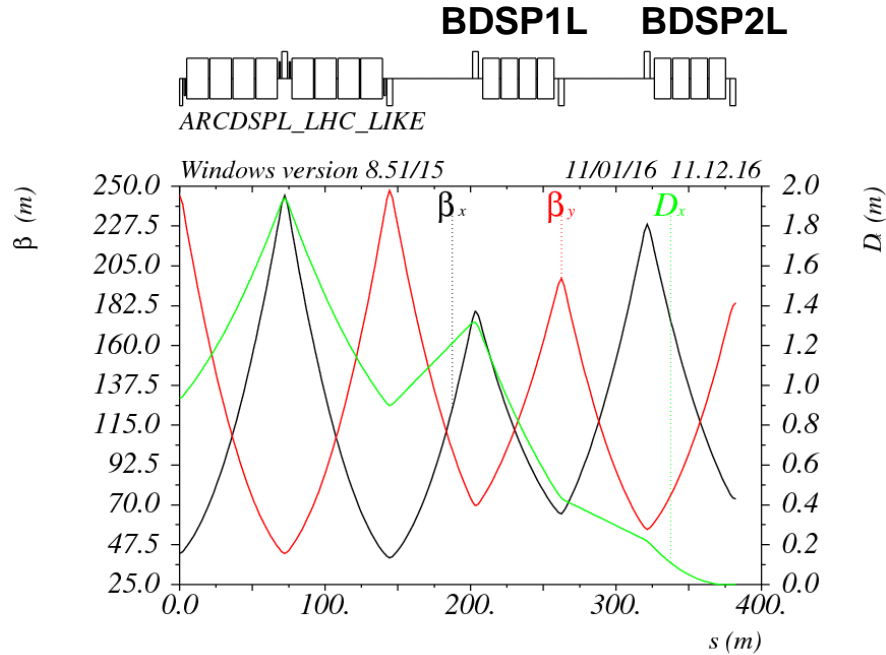
## (3) Full Bend



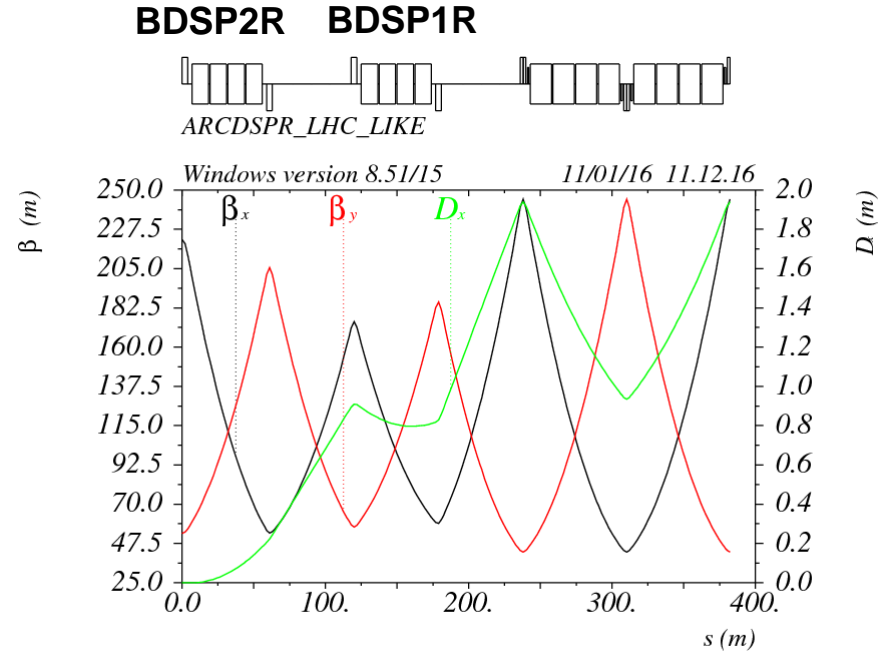
**L=577.6m**

	BDSP1L	BDSP2L	BDSP1R	BDSP2R	B0	
(1)	9.805	9.805	9.805	9.805	19.61	(T)
(2)	18.93	18.93	18.93	18.93	19.61	(T)
(3)	19.61	19.61	19.61	19.61	19.61	(T)

# Dispersion Suppressor (DS)



**382.4m**



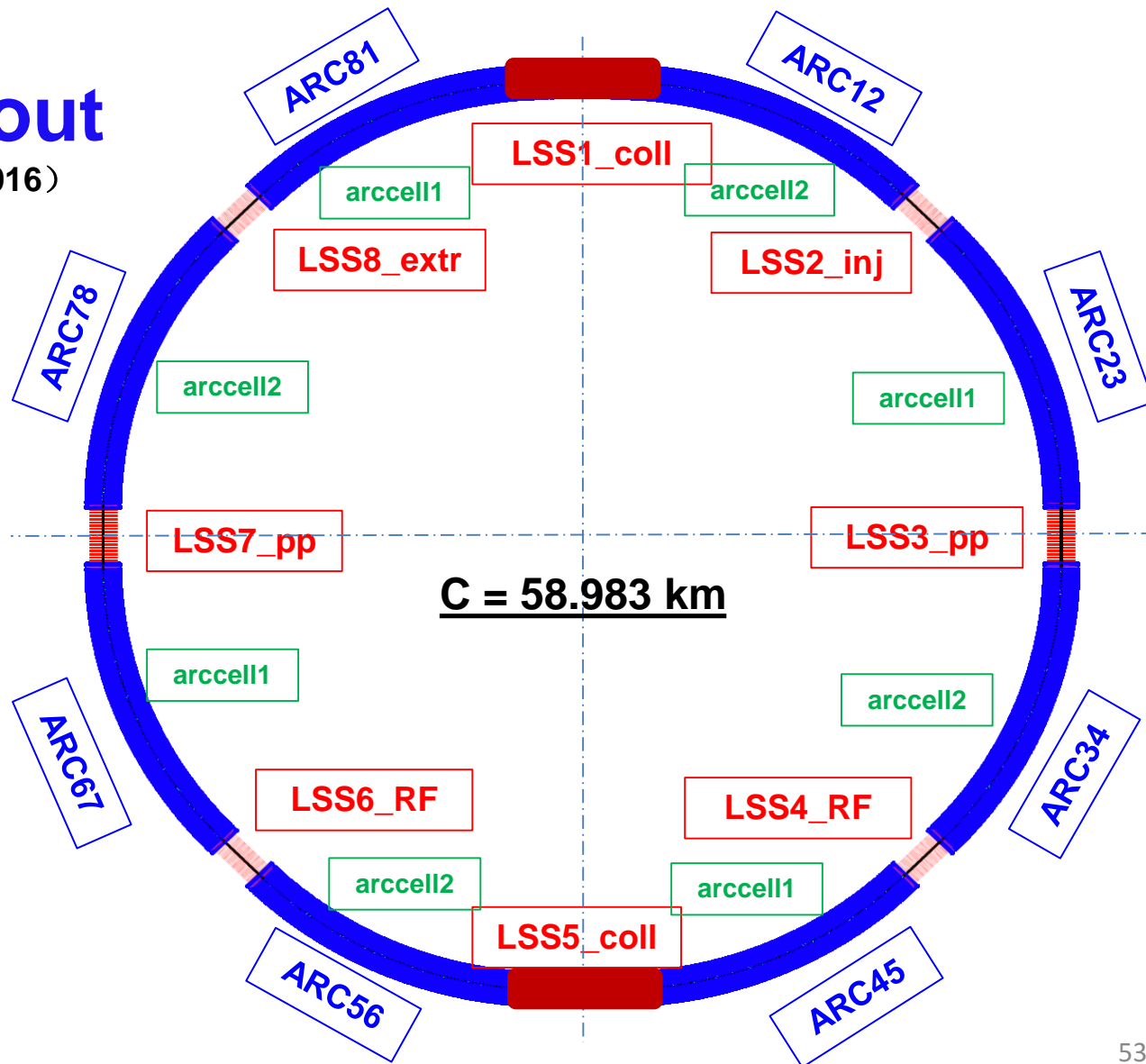
	BDSP1L	BDSP2L	BDSP1R	BDSP2R	B0	
B	18.93	18.93	18.93	18.93	19.61	T
L	11.5	11.5	11.5	11.5	14.8	m



# Long Straight Section

## SPPC Layout

(Su Feng Jan. 10, 2016)



LSS1/5\_coll : 3.2Km

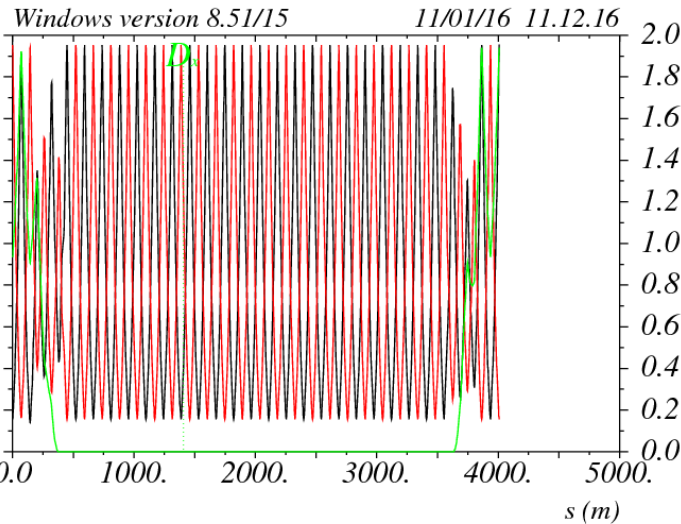
LSS2/4/6/8: 788.31m

LSS3/7\_pp: 973.83m

ARC: 5963.2m

# LSS1/5\_coll

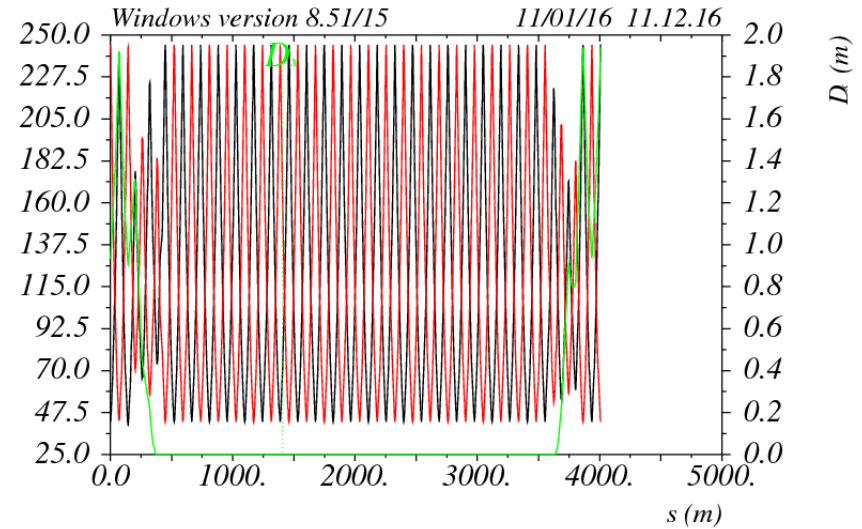
LSS1\_COLL



$\delta_E / p_{oc} = 0.00000$

Table name = TWISS

LSS5\_COLL



$\delta_E / p_{oc} = 0.00000$

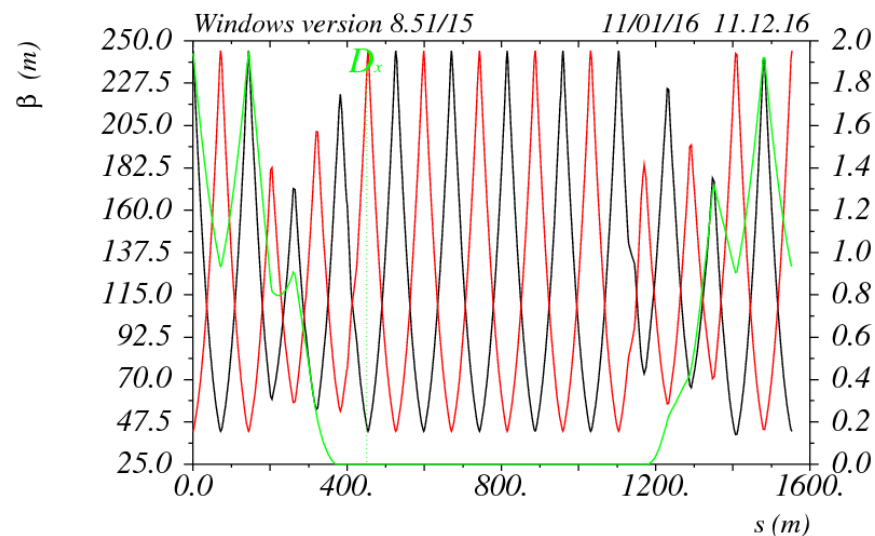
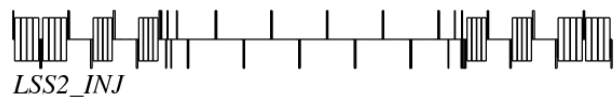
Table name = TWISS

**L=3243.106m**

**ARCDSPL, ARC\_to\_STR, 21.5\*STRCELL, STR\_to\_ARC, ARCDSPL**

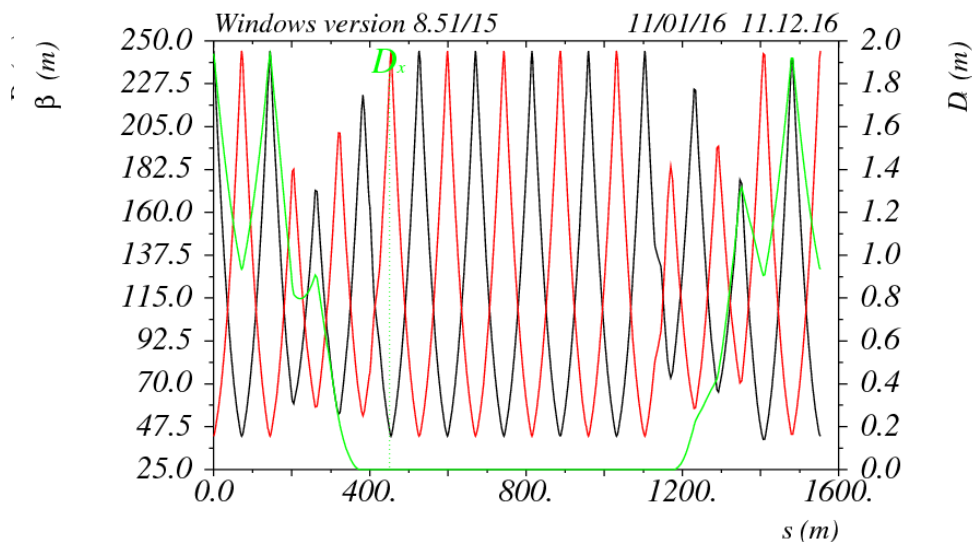
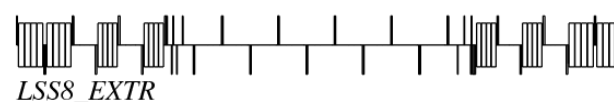
**382.4m, 71.719m, 3104.6m, 66.789m, 382.4m**

# LSS2\_inj/LSS8\_extr



$\delta_E / p_{oc} = 0.00000$

Table name = TWISS



$\delta_E / p_{oc} = 0.00000$

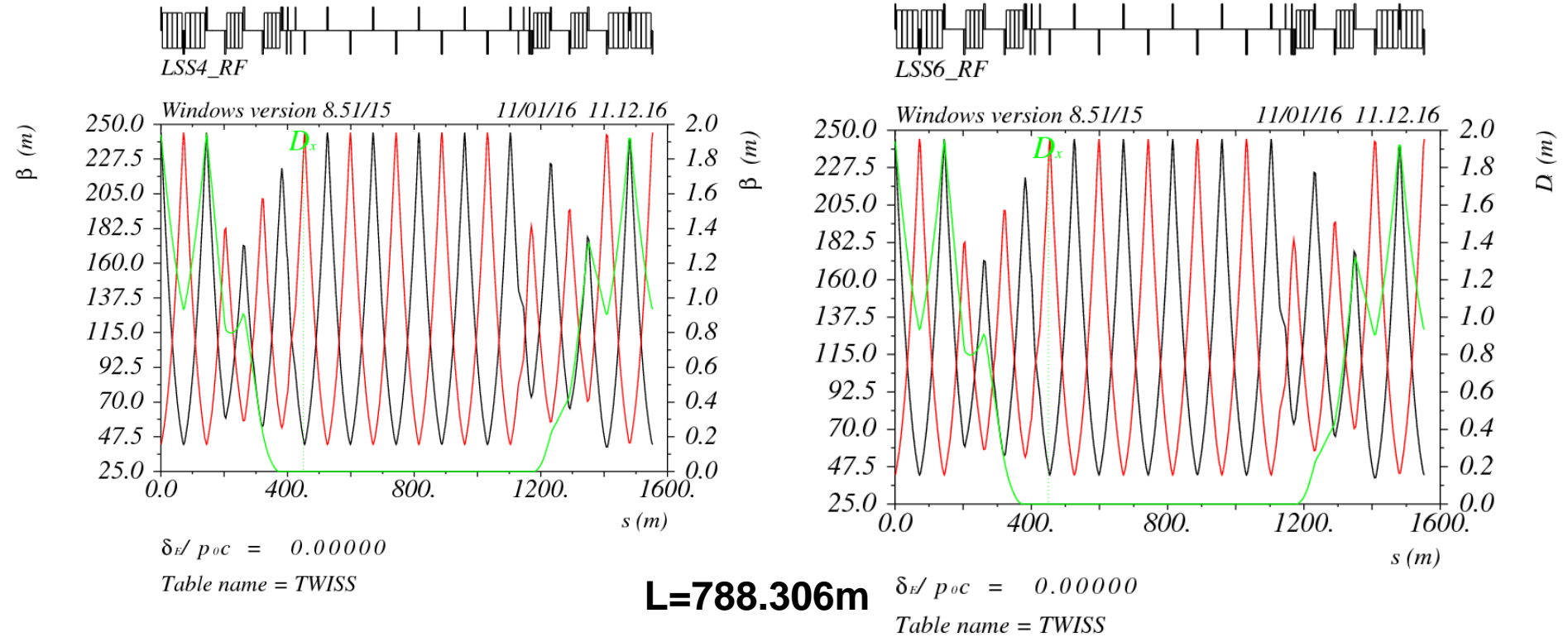
Table name = TWISS

**L=788.306m**

**-ARCDSPR, ARC\_to\_STR, 4.5\*STRCELL, STR\_to\_ARC, -ARCDSPR**

**382.4m, 71.719m, 649.8m, 66.787m, 382.4m**

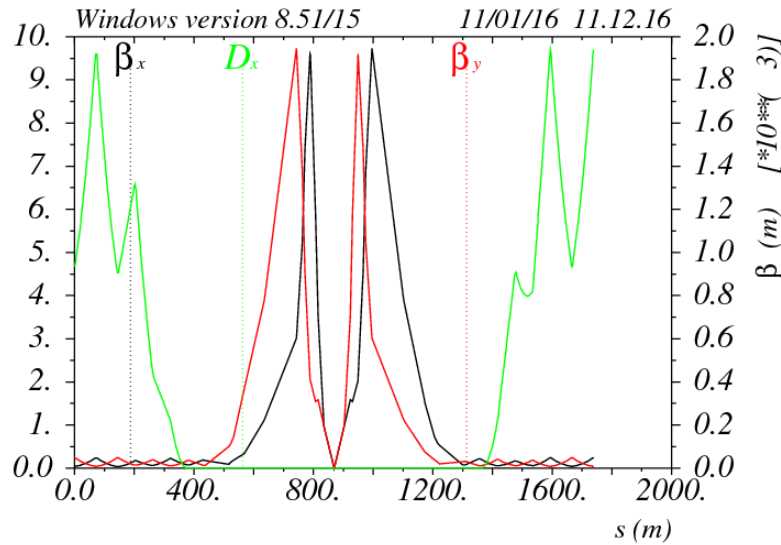
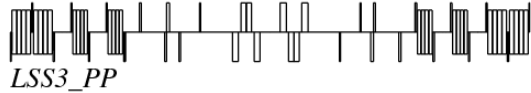
# LSS4/6\_rf



-ARCDSR, ARC\_to\_STR, 4.5\*STRCELL, STR\_to\_ARC, -ARCDSPL

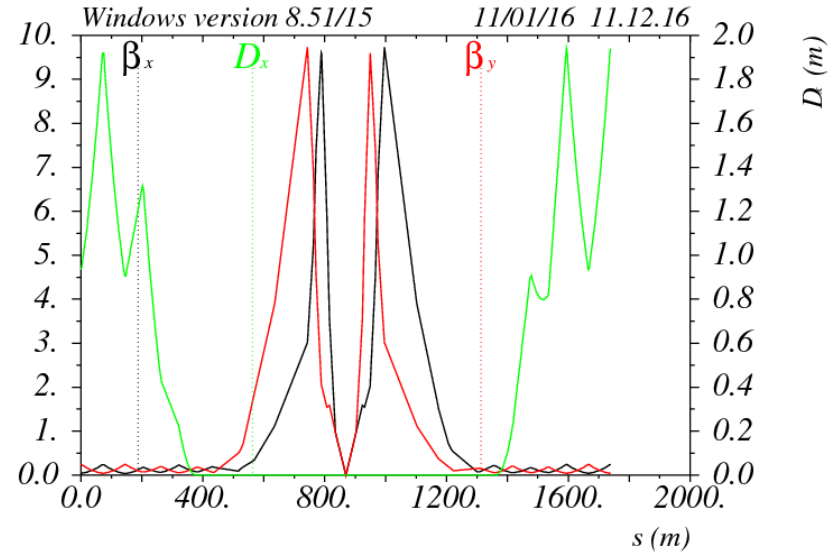
382.4m, 71.719m, 649.8m, 66.787m, 382.4m

# LSS3\_pp/LSS7\_pp



$\delta_E / p_{oc} = 0.00000$

Table name = TWISS



$\delta_E / p_{oc} = 0.00000$

Table name = TWISS

**L=973.829m**

**Beta: 0.75m**

**Crossing angle: 146urad**

ARCDSP, ARC\_to\_STR, 21.5\*STRCELL, STR\_to\_ARC, ARCDSPR

382.4m, 71.719m, 973.829m, 66.789m, 382.4m

	K1(m <sup>-2</sup> )	G (T/M)	L(M)	β <sub>max</sub>
K1.QT.1R	4.9751e-03	580.428	6	3543.69
K1.QT.A2R	-5.2595e-03	-613.668	9	9601.686
K1.QT.B2R	-5.2595e-03	-613.668	9	9601.686
K1.QT.3R	5.3434e-03	623.369	8	9731.53
K1.QM.4R	-2.2804E-04	-266.04	4	3798.29
K1.QM.5R	8.8592E-04	103.36	4	1506.53
K1.QM.6R	-1.2144E-03	-141.68	4	587.87
K1.QM.7R	1.0640E-04	124.133	4	531.25
K1.QM.8R	-4.2431E-03	-495.028	4	162.20
K1.QT.1L	-4.9751e-03	-580.428	6	3543.69
K1.QT.A2L	5.2595e-03	613.668	9	9601.686
K1.QT.B2L	5.2595e-03	613.668	9	9601.686
K1.QT.3L	-5.3434e-03	-623.369	8	9731.53
K1.QM.4L	2.2804E-04	266.04	4	3798.29
K1.QM.5L	-8.8592E-04	-103.36	4	1506.53
K1.QM.6L	1.2144E-03	141.68	4	587.87
K1.QM.7L	-1.0640E-04	-124.133	4	531.25
K1.QM.8L	4.2431E-03	495.028	4	162.20

# Q Strength

Pre-CDR:

IR:

**D = 60 mm**     **B<sub>pole</sub> = 20 T**

**G=666.7T/m**     **K1=5.716\*10<sup>-3</sup>**

**R=30mm**

**20mm=20σ**

**σ=1mm**

**β=σ<sup>2</sup>/ε=10.03km**

**Matching section:**

**D = 60 mm**     **B<sub>pole</sub> = 16 T**

**G=533.3T/m**     **K1=4.572\*10<sup>-3</sup>**



## ***II. SPPC***

### **3. SPPC Dynamic Aperture Study**

# Definition of Dynamic Aperture

## 1. Real World Dynamic Aperture (RW-DA) Definition → W. Fischer:

**Largest Amplitude** at which particles **remain** in the accelerator over a **time range of interest**.

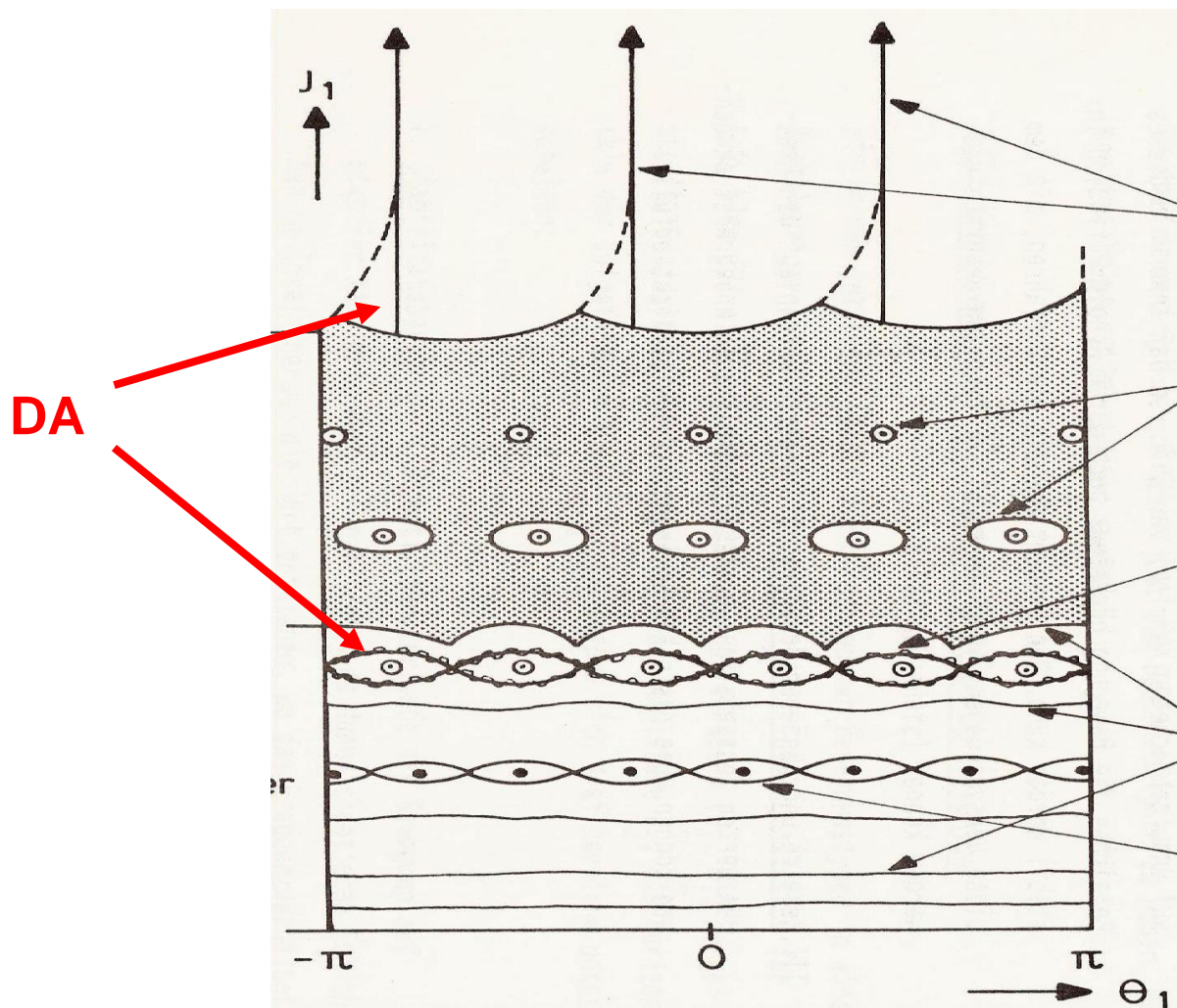
## 2. Potential Dynamic Aperture (PO-DA) = Onset of global Chaos

- **Largest Amplitude** with **mainly regular motion**.
- **Insignificant chaotic layers** within the regular regime will be **ignored**.
- However **considerable wide “chaotic spikes”** have to be **taken into account**

→ It turns out that the PO-DA is typically too small as RW-DA estimate



# Dynamic Aperture Scheme



**Rapid amplitude growth and loss**

**Stable Islands in chaotic sea**

**Fine chaotic layers in stable regime**

**Mostly stable particle motion**

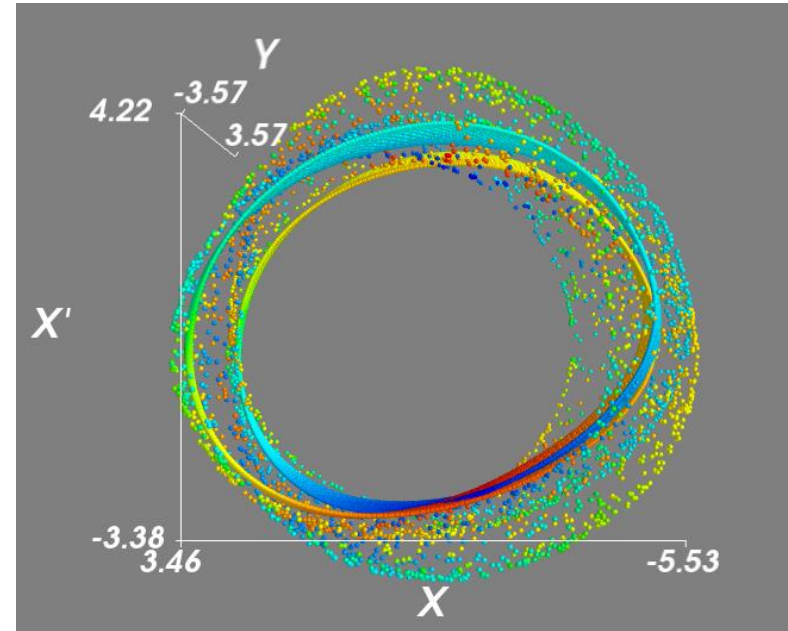
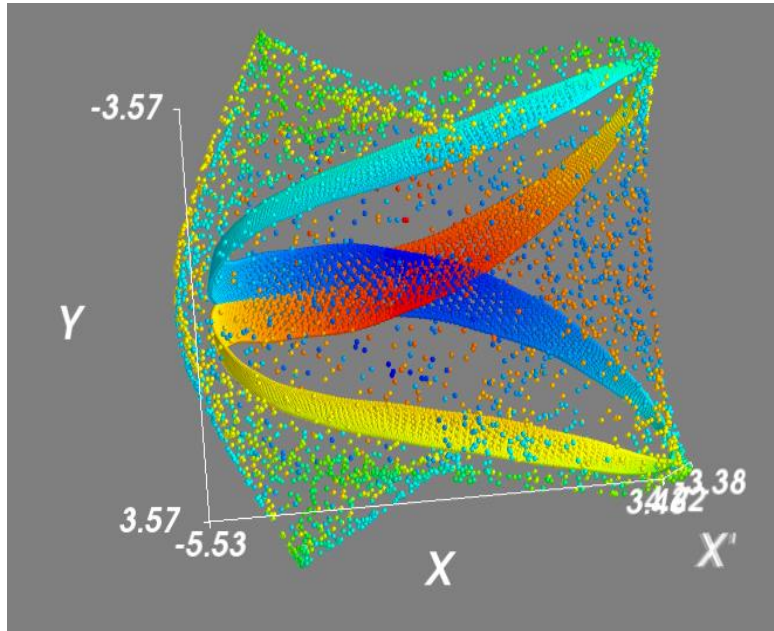
# SPPC Main Ring DA *without* low beta pp IR(1/7)

At first, we studied the dynamic aperture of SPPC main ring without interaction region. There are 8 arcs in the main ring and 8 long straight sections. Now we use simple FODO in the long straight section, latter we should optimize the long straight section design for difference use like RF part, injection, extraction and collimation.

Following is the dynamic aperture from Sixtrack.

We can get from the figures that the dynamic aperture is about 22.58 mm ( $346 \sigma_x$ ) in horizontal and 49.16 mm ( $315 \sigma_y$ ) in vertical.

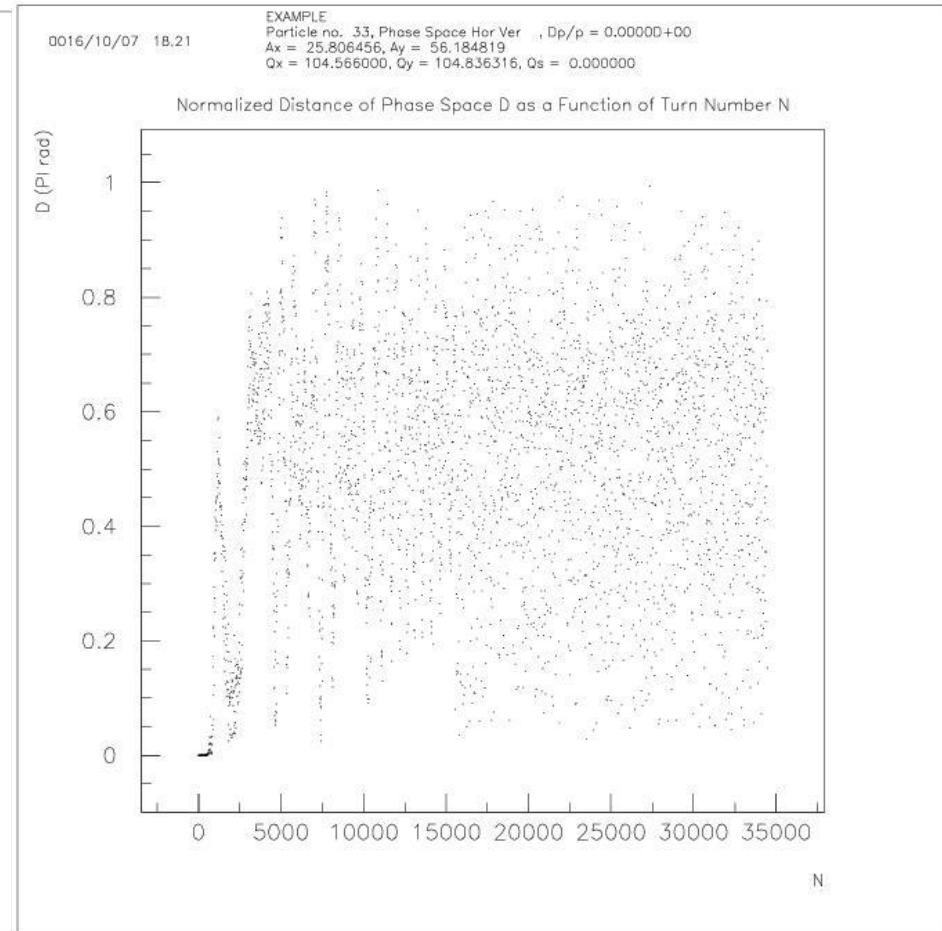
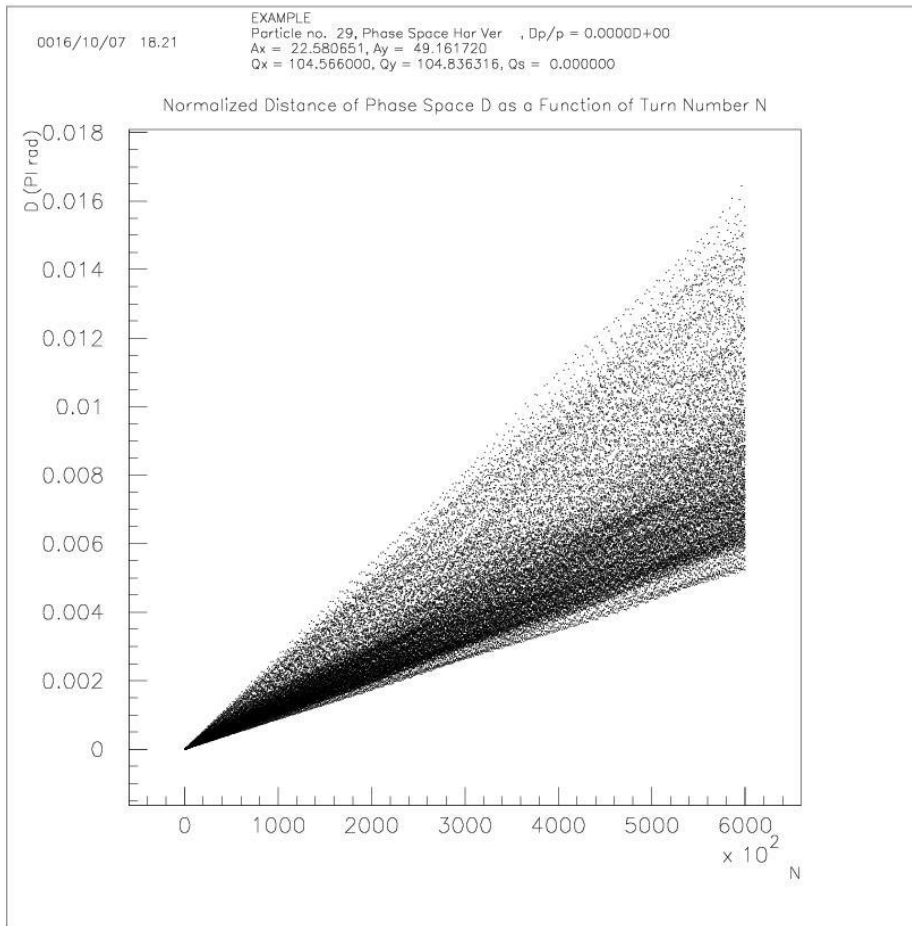
# SPPC Main Ring DA *without* low beta pp IR(2/7)



## 4-Dimension phase space for regular and chaotic motion (cm).

(The solid tie shape shows the regular particles motion which has the largest amplitude, if the amplitude becomes a little larger, the motion will become chaotic, the diffusion points around the solid tie show the chaotic motion. This largest amplitude is the dynamic aperture we want to study.)

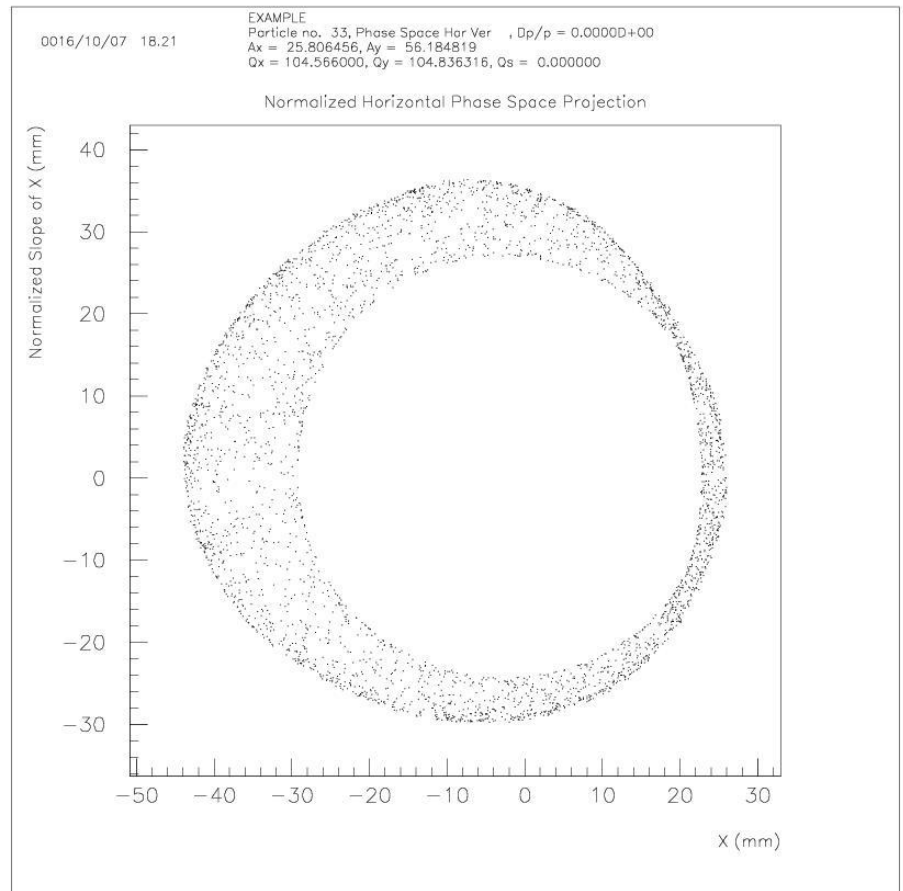
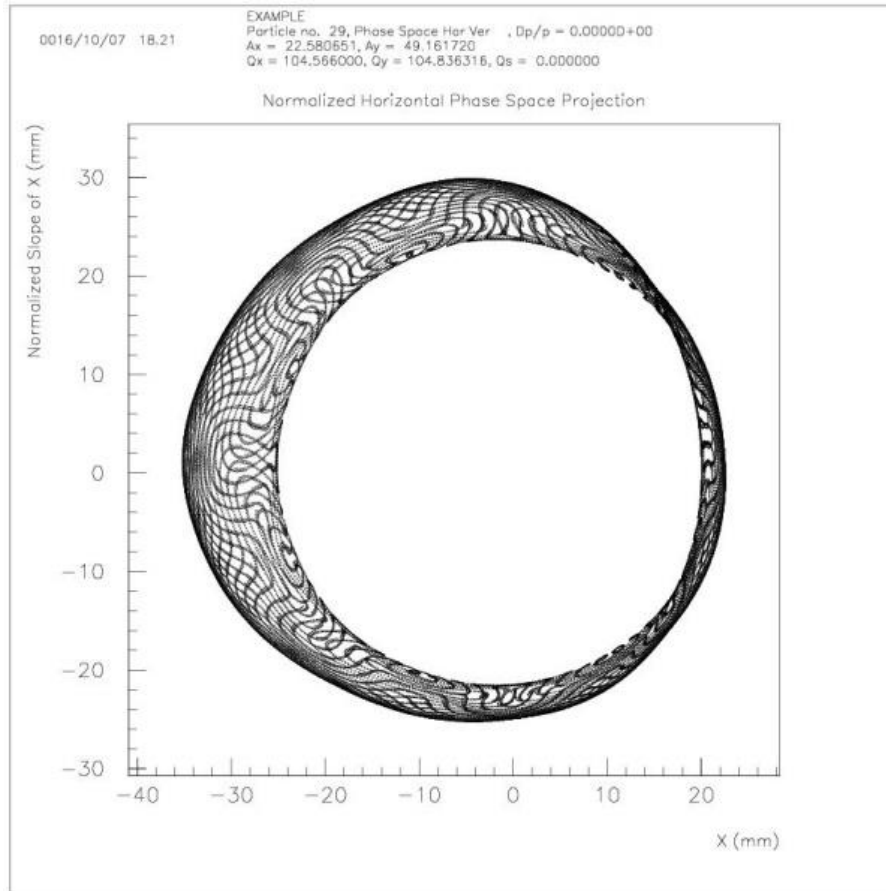
# SPPC Main Ring DA *without* low beta pp IR(3/7)



Evolution of the distance of phase space for regular (left) and chaotic (right) motion.

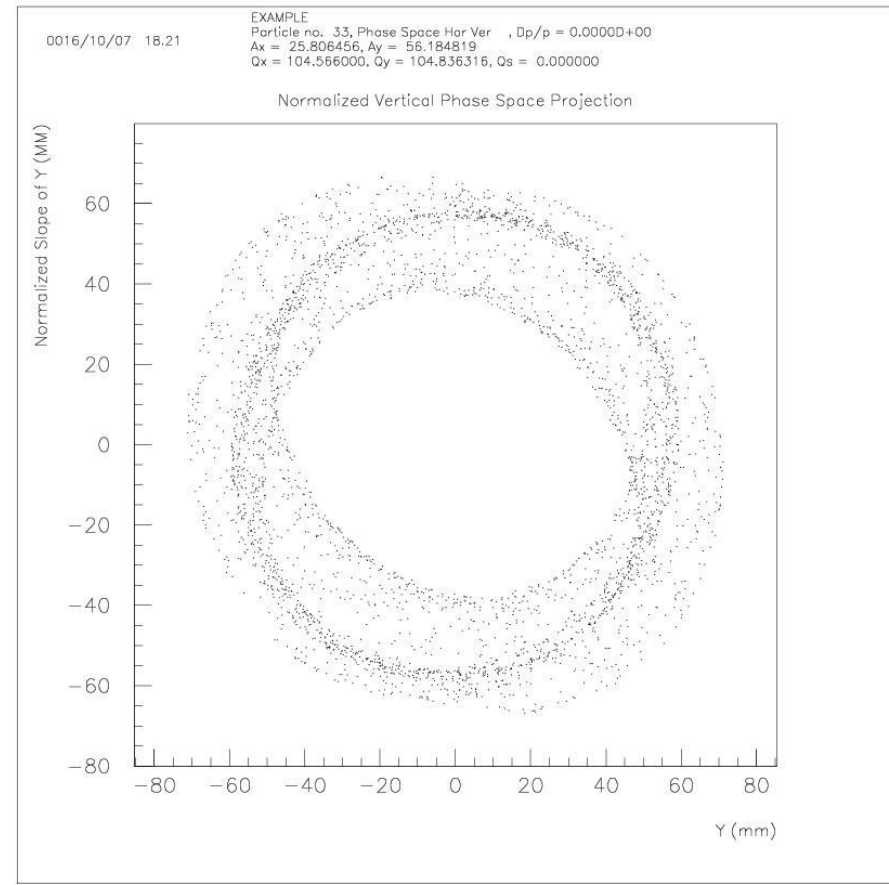
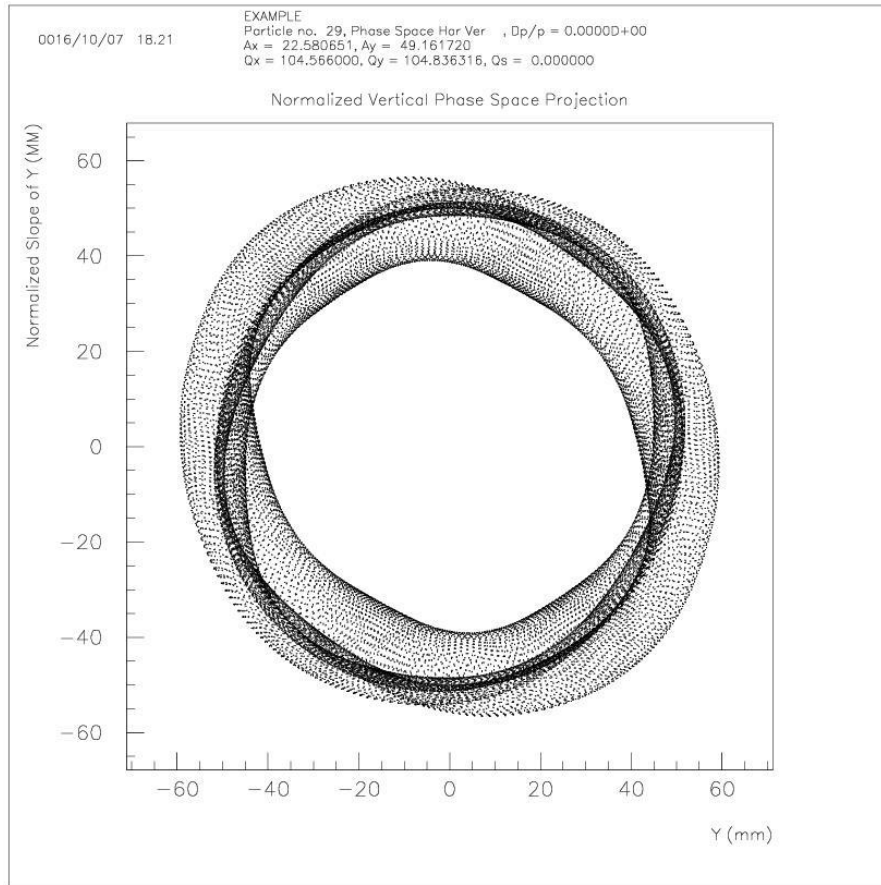


# SPPC Main Ring DA *without* low beta pp IR(4/7)



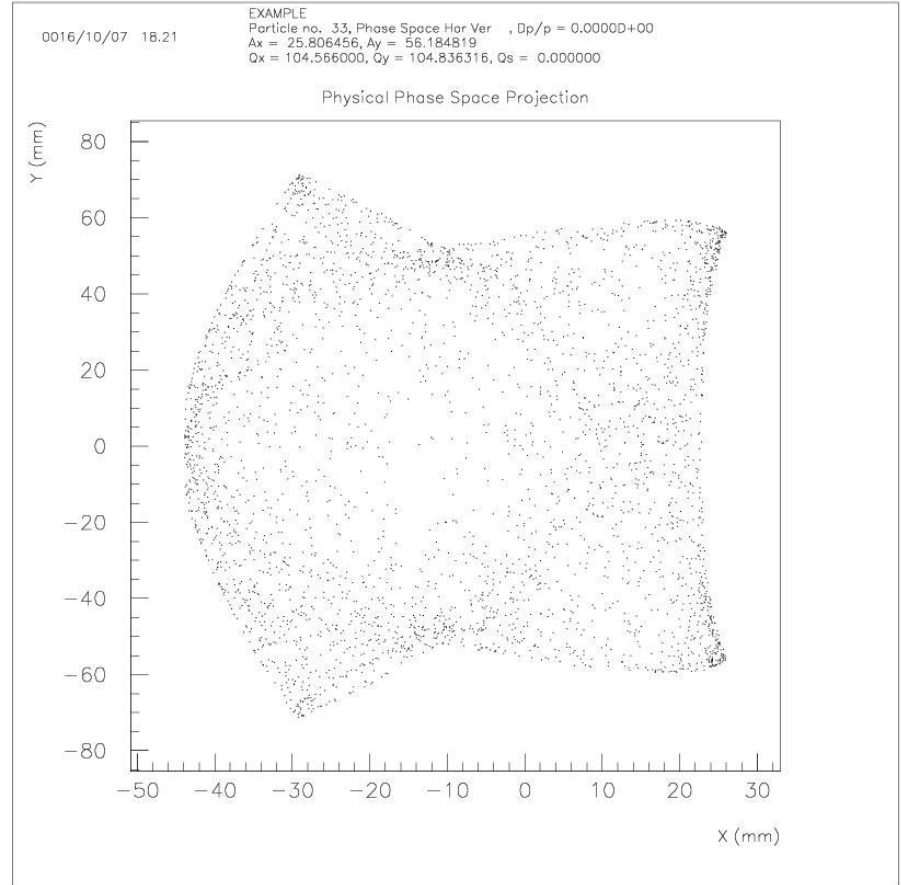
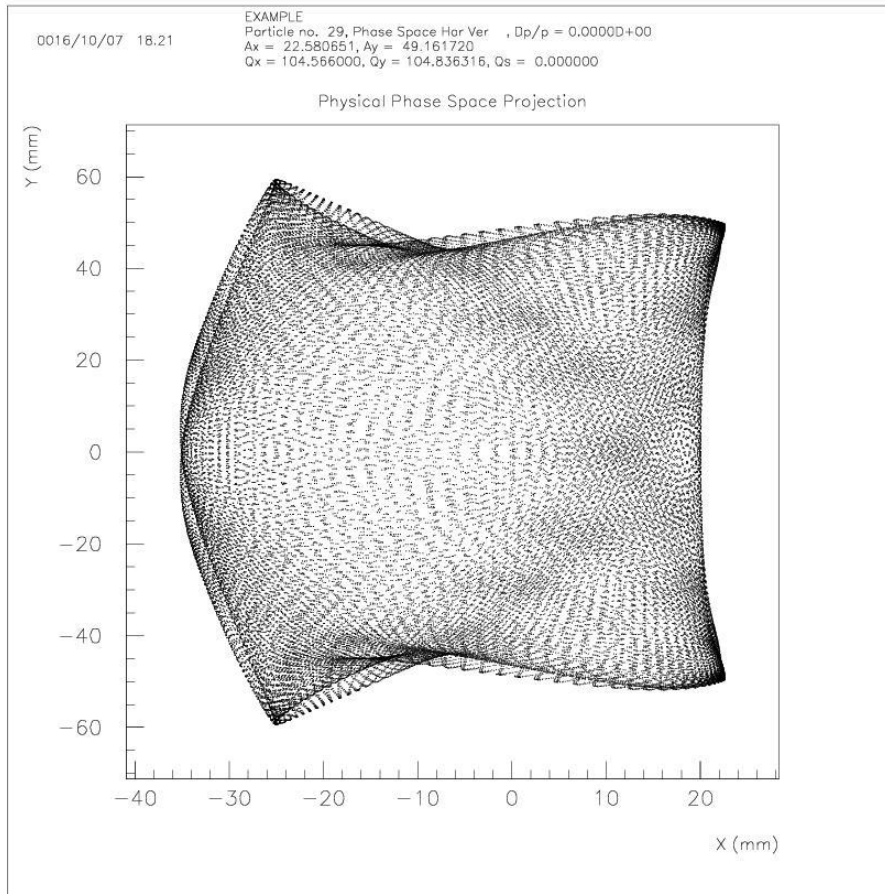
Horizontal phase space projections for regular (left) and chaotic (right) cases.

# SPPC Main Ring DA *without* low beta pp IR(5/7)



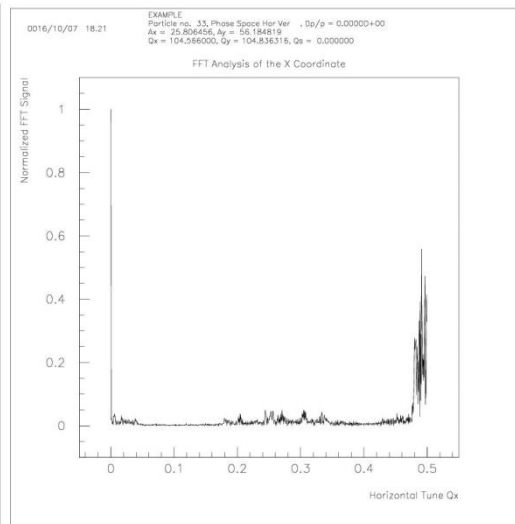
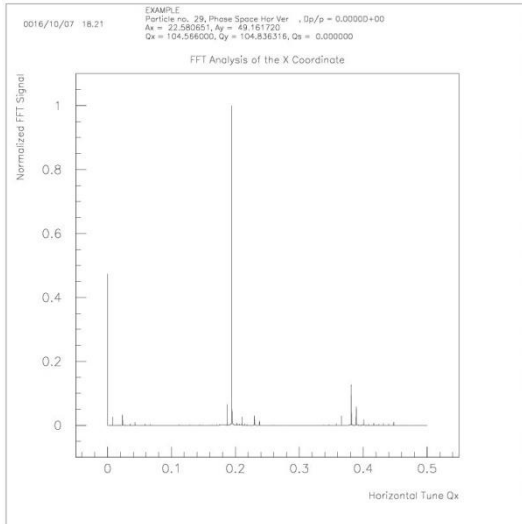
Vertical phase space projections for regular (left) and chaotic (right) cases.

# SPPC Main Ring DA *without* low beta pp IR(6/7)

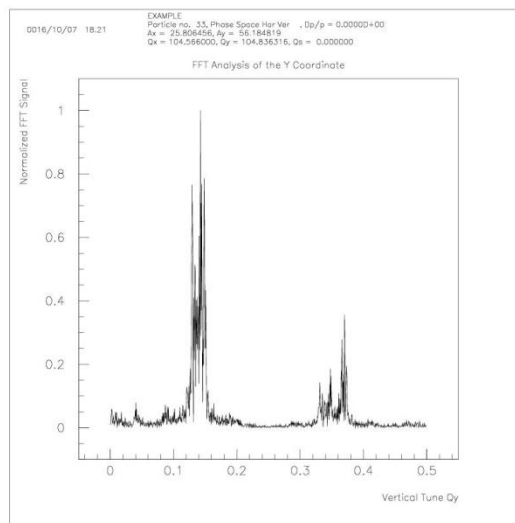
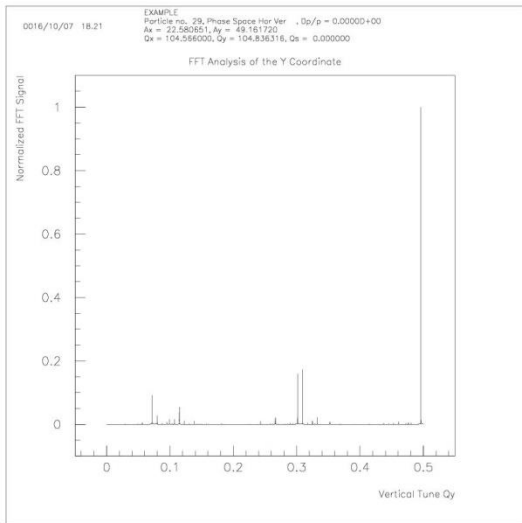


Physical phase space projections for regular (left) and chaotic (right) cases.

# SPPC Main Ring DA *without* low beta pp IR(7/7)



Horizontal FFT-analysis for the regular (left) and the chaotic (right) cases.



Vertical FFT-analysis for the regular (left) and the chaotic (right) cases.



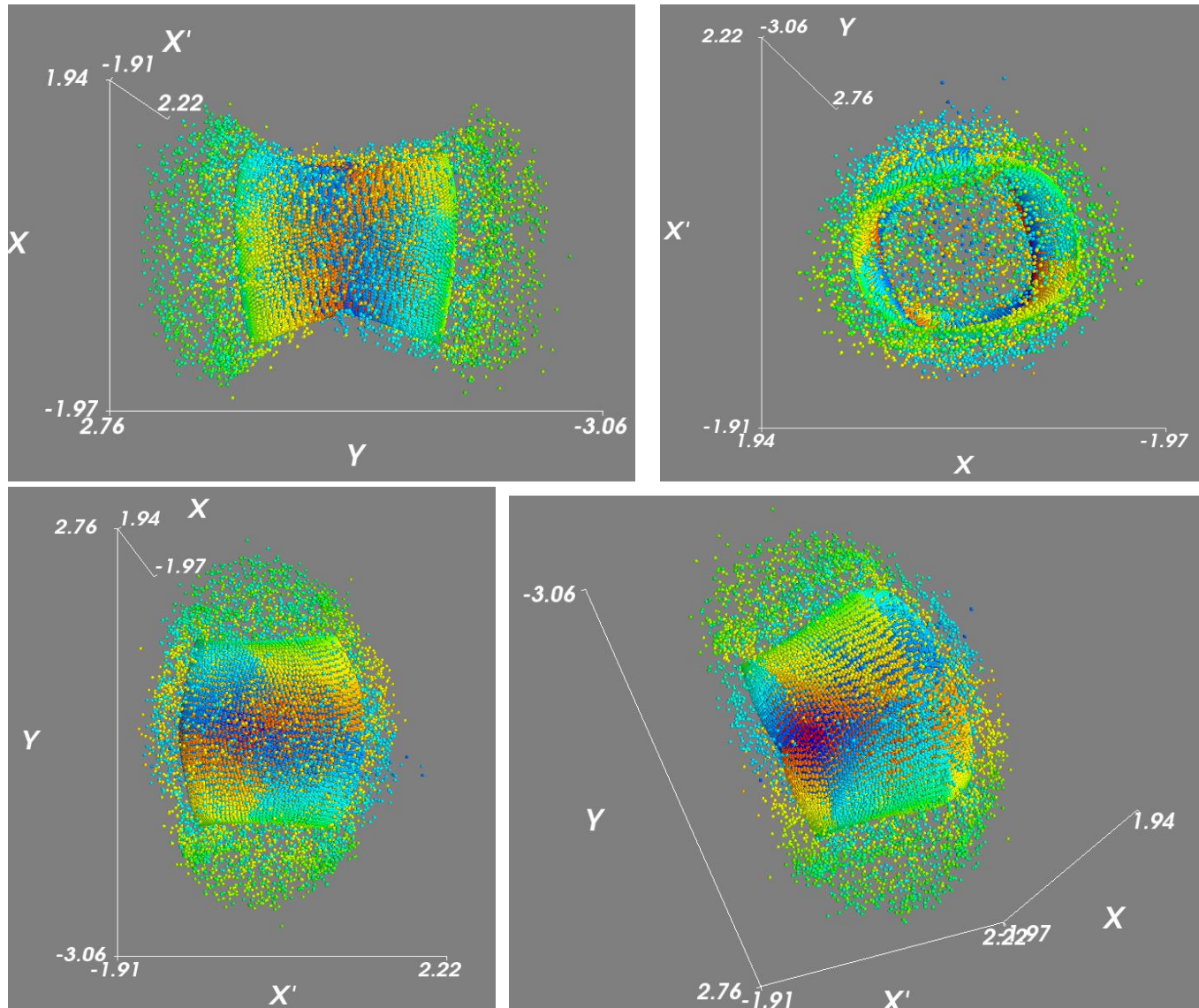
# SPPC Main Ring DA *with* low beta pp IR(1/5)

Following is the dynamic aperture with low beta pp interaction region.

The beta function at IP is 0.75m. The maximum beta function in this region is about 9.6 km. The dynamic aperture becomes smaller, 8.22 mm ( $126 \sigma_x$ ) in horizontal and 19.73 mm ( $126 \sigma_y$ ) in vertical (we keep the same observation point for comparison with the DA without low beta pp IR). At the low beta pp IR point, the dynamic aperture is only 1.089mm ( $126 \sigma$ ) in both horizontal and vertical because the beam size is very small (8.647 $\mu$ m).

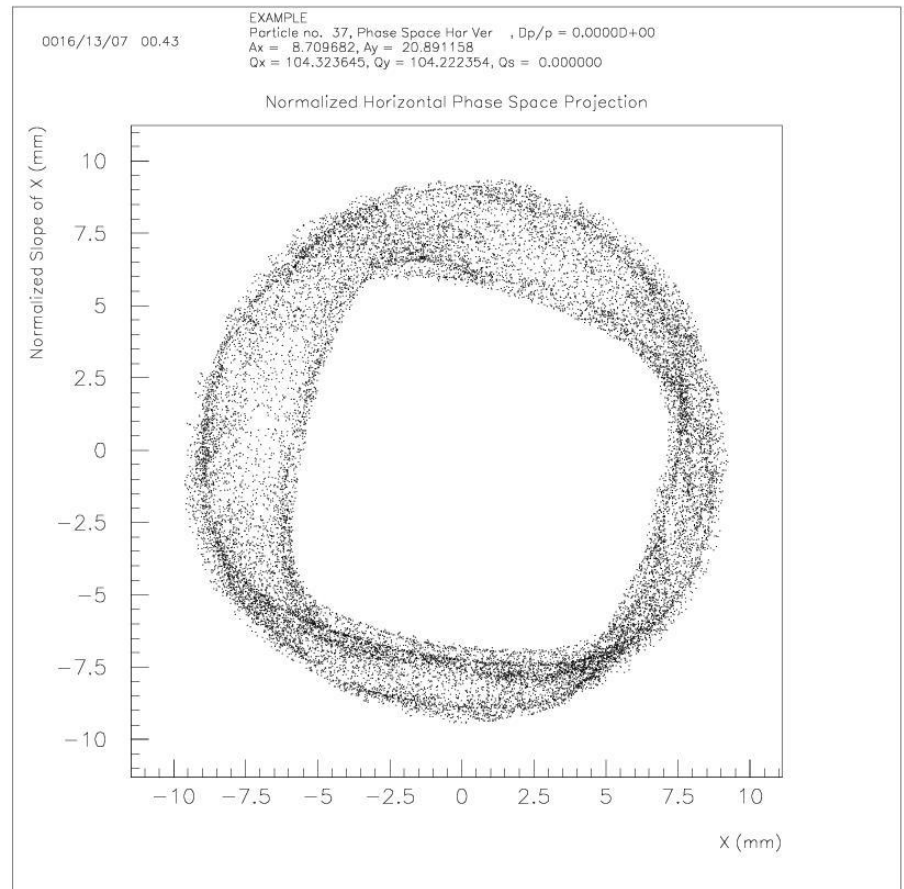
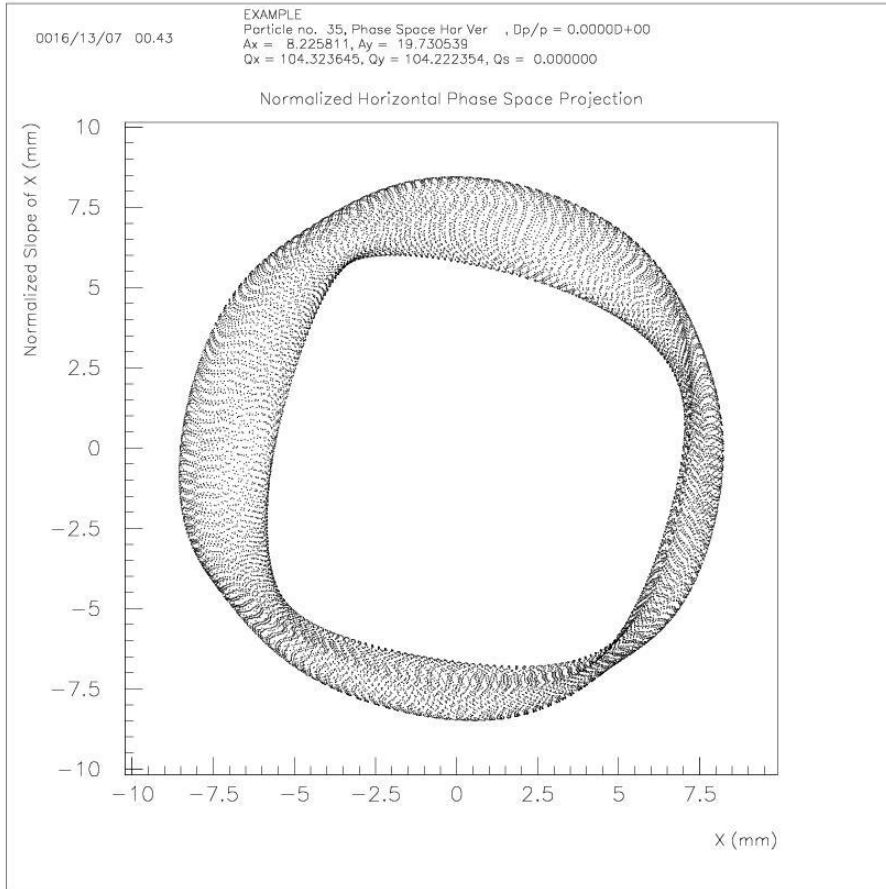
Following figures show the details.

# SPPC Main Ring DA *with* low beta pp IR(2/5)



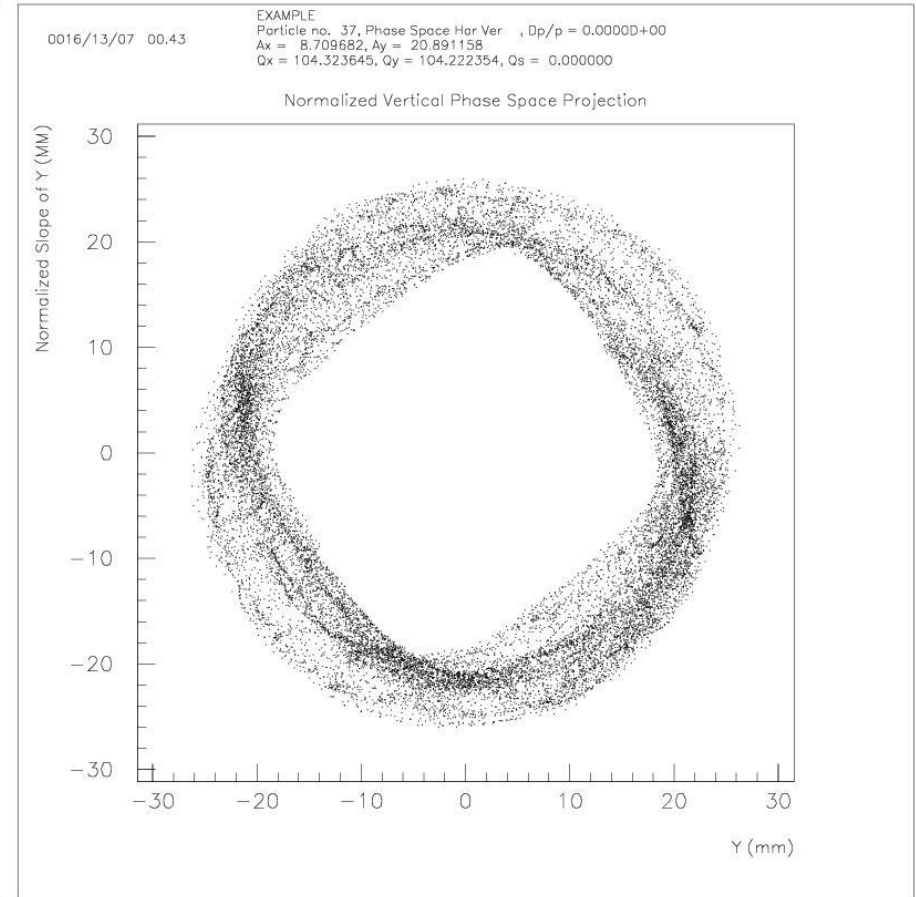
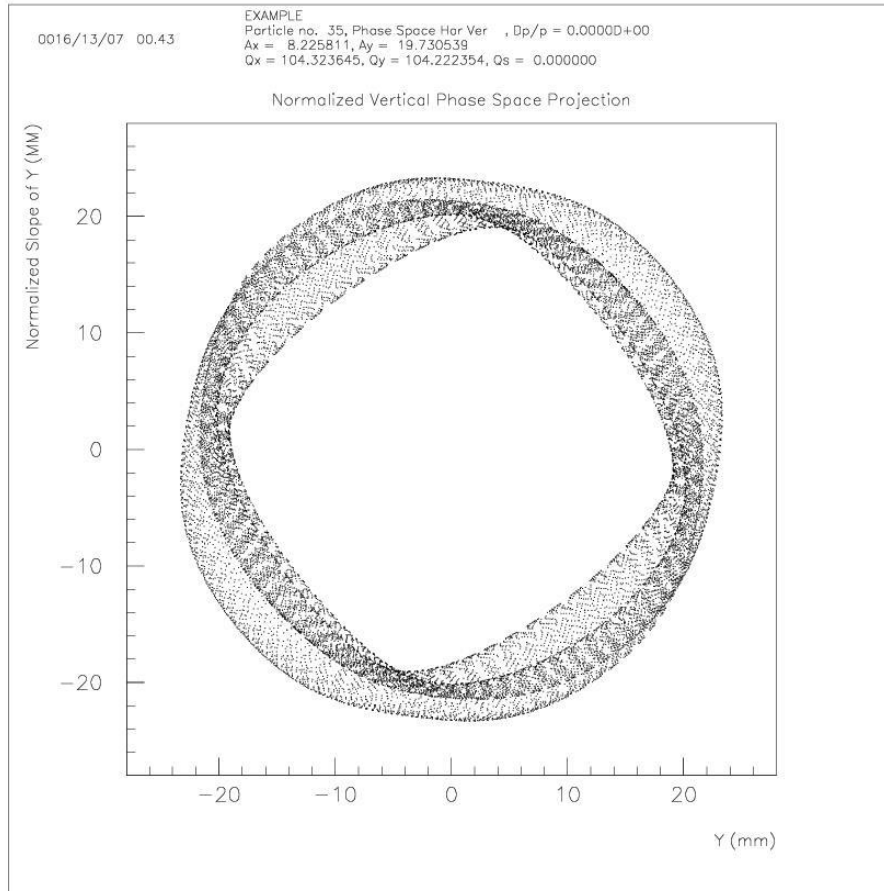
4-Dimension phase space for regular and chaotic motion (cm).

# SPPC Main Ring DA *with* low beta pp IR(3/5)



Horizontal phase space projections for regular (left) and chaotic (right) cases.

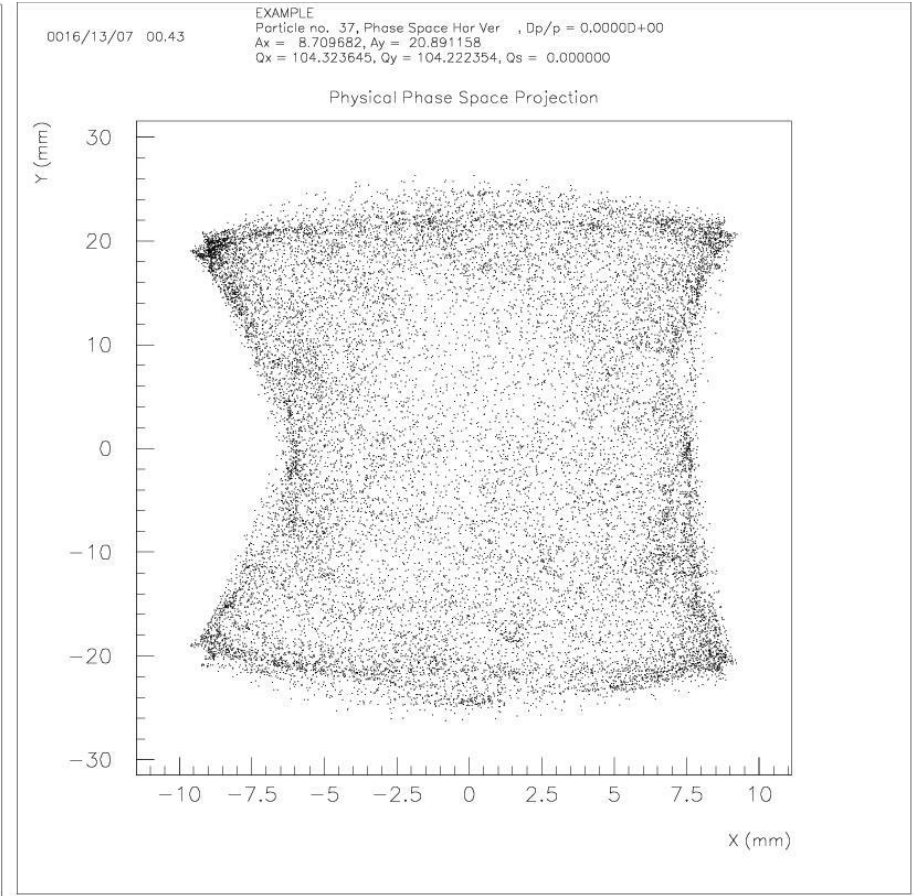
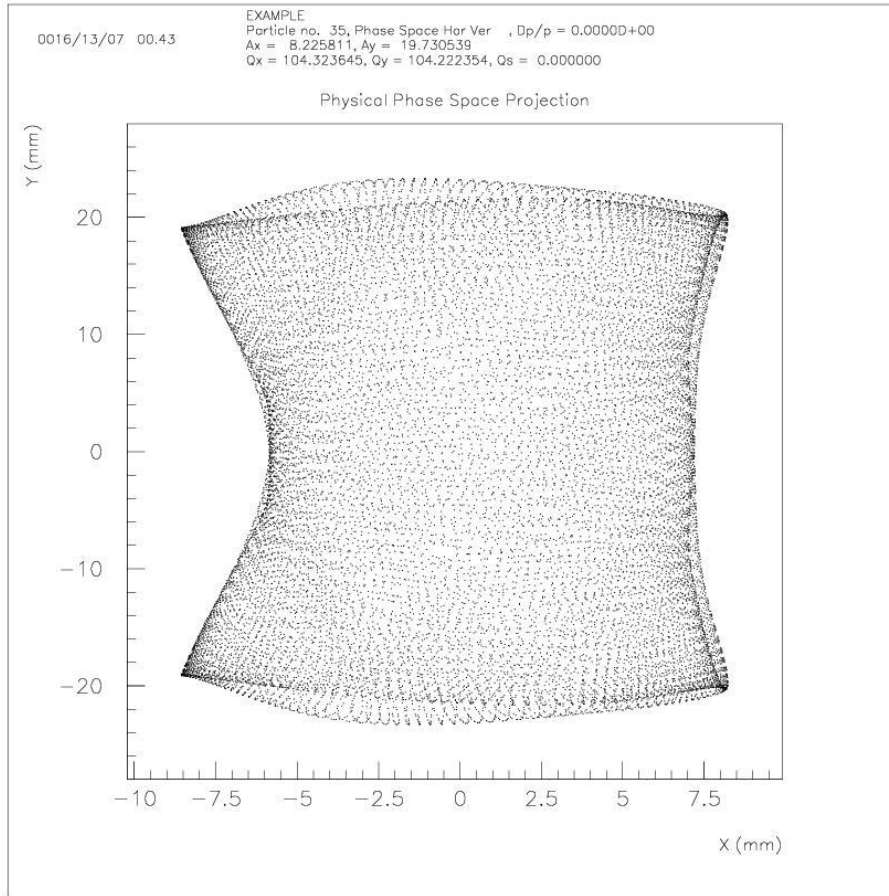
# SPPC Main Ring DA *with* low beta pp IR(4/5)



Vertical phase space projections for regular (left) and chaotic (right) cases.



# SPPC Main Ring DA *with* low beta pp IR(5/5)



Physical phase space projections for regular (left) and chaotic (right) cases.

### **4. Summary**

- ◆ We optimized the parameter list version201503, we considered the new lattice layout of CEPC PDR and the combination of CEPC and SPPC. The beam energy and length of long straight sections so as the circumference have a little change. We get the newest parameter list version201607.
- ◆ The first version of SPPC Lattice was designed . Full crossing angle is 146urad. Beta at IP is 0.75um.
- ◆ A first Dynamic Aperture study and the preliminary DA is showed and it seems not too small. 126 sigma at IR.
- ◆ The deep beam dynamics study is needed.



# Thank You !

# Acknowledge

- The authors would thank Frank Schmidt very much for the help in SixTrack and Dynamic Aperture Study.
- Thanks for Gang Xu, Qing Qin, Yuan Zhang, Yuemei Peng, Qingjin Xu, Xiaohao Cui, Zhe Duan and Yudong Liu's kind help and beneficial discussion!



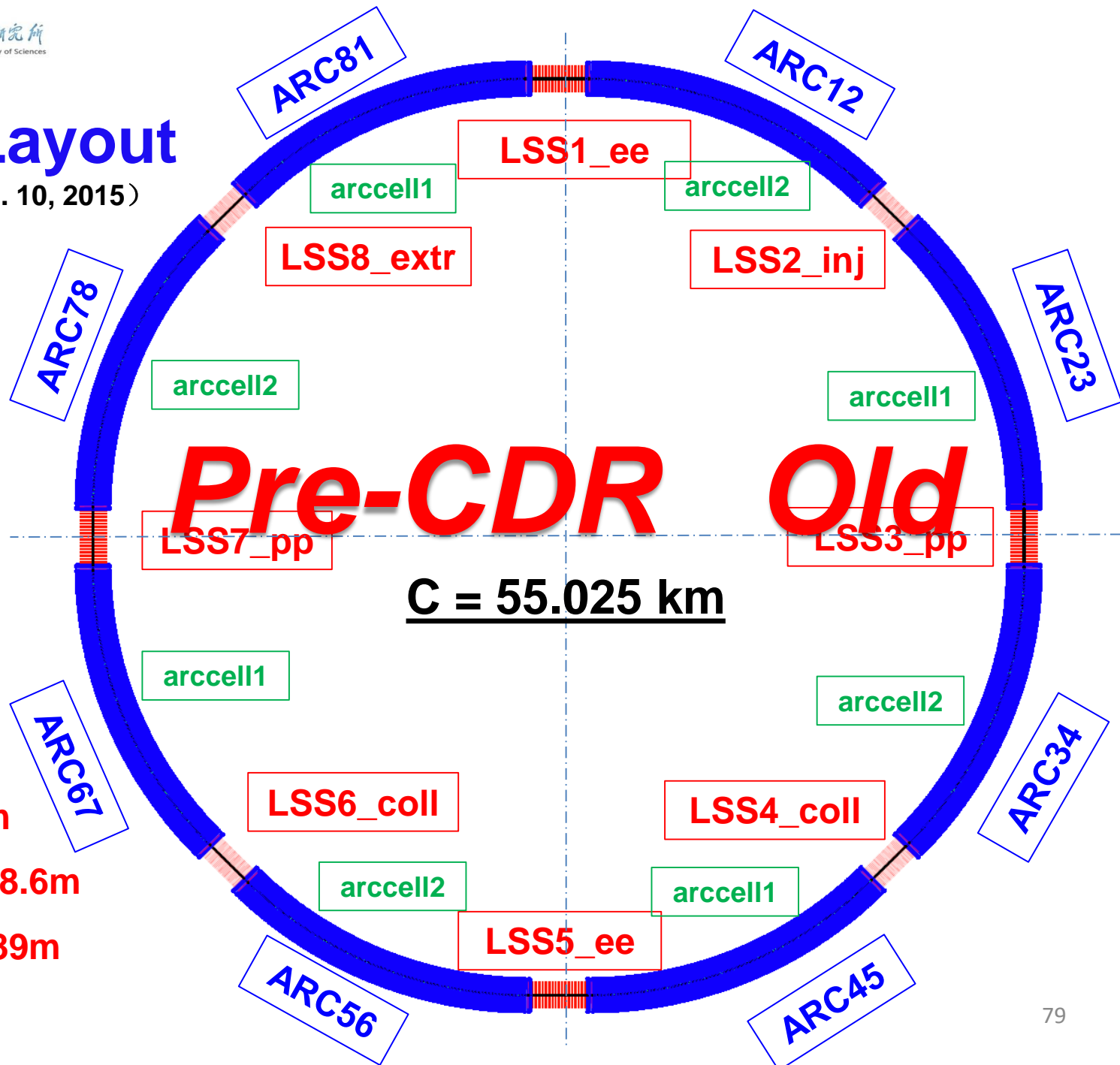
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# Backup

# SPPC Layout

(Su Feng, Jul. 10, 2015)



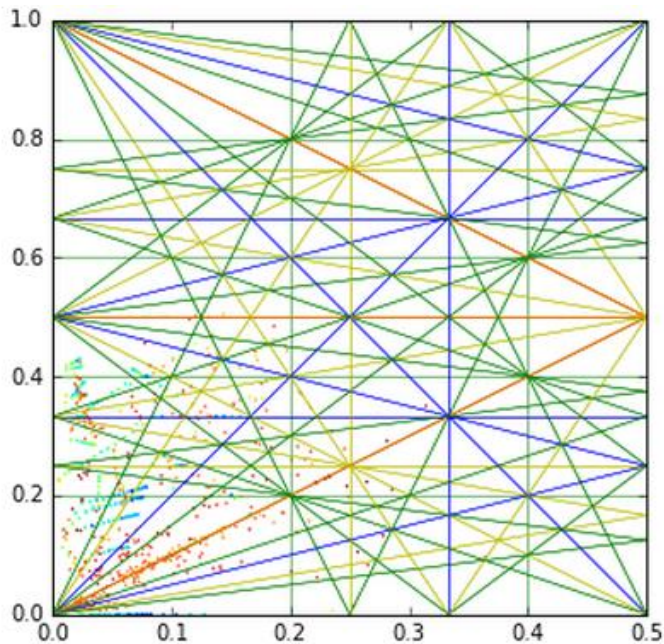
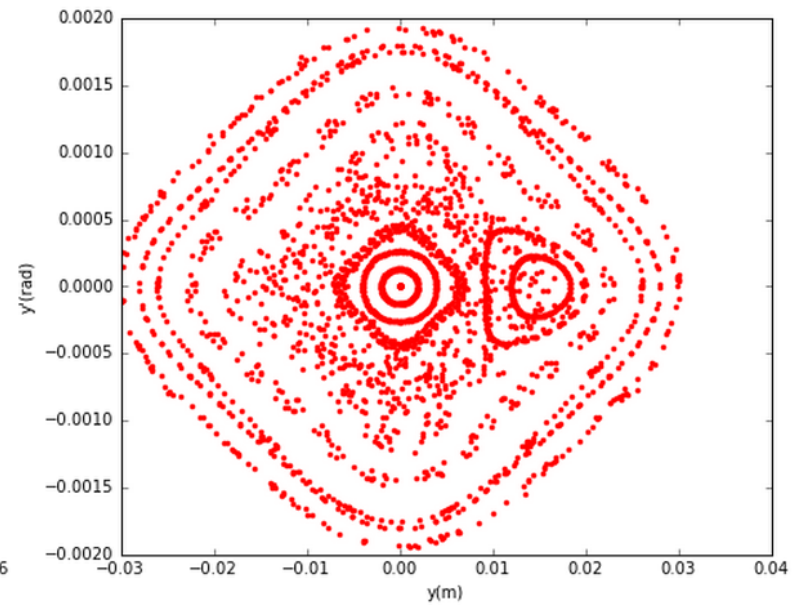
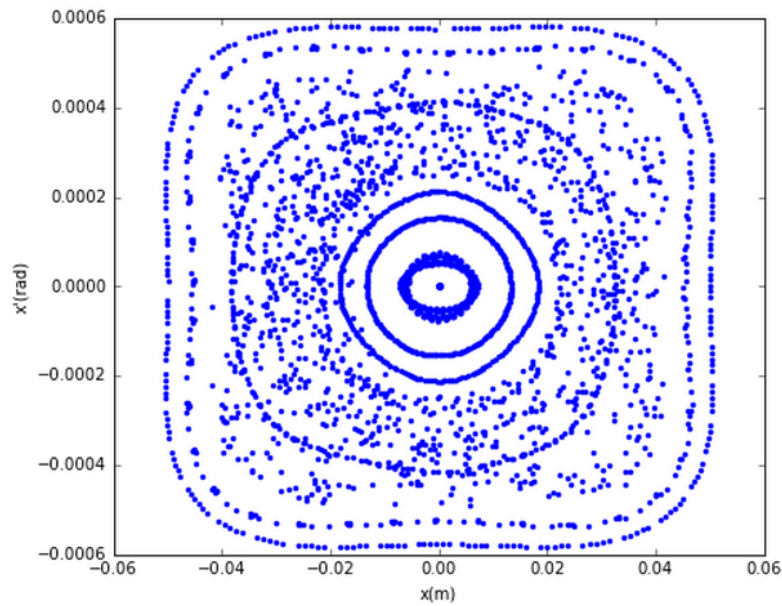
LSS1/5 : 1083m

LSS2/4/6/8 : 938.6m

LSS3/7 : 1070.89m

ARC 5920.4m





```
In [3]: cepe.ring.geth1()
        cepe.ring.h1
```

```
Out[3]: {'h00111': (5.742221251626866+0j), 'h11001': (5.6703595956706225+0j)}
```

```
In [4]: cepe.ring.geth2()
        cepe.ring.h2
```

```
Out[4]: {'h00112': (-8001.8844135165946+2.0997153668544932e-12j),
          'h00220': (0.00021258305237598912-1.5197626779261952e-07j),
          'h11002': (-6646.5151814247183-7.2161998598829769e-12j),
          'h11110': (-0.00019662996670510063+7.9286005150169814e-08j),
          'h22000': (0.00027491287281040234+1.7103984981808873e-10j)}
```

# Chaos Criteria

PO-DA Detection → find amplitude with non-zero **Lyapunov Exponent**:

$$\lambda = \lim_{N \rightarrow \infty} \lim_{d(0) \rightarrow 0} \frac{1}{N} \log \frac{d(N)}{d(0)}$$

In **practice**, the **Lyapunov exponent** is rarely evaluated **directly**.

Instead, one follows the **evolution of the distance in phase space**. Most effectively by using the **angular distance** that is **extremely sensitive** to find even **weakly chaotic motion**.