







# Neural Network Fits of Parton Distributions

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# (unpolarized) Parton Distributions

The distribution of energy that **quarks and gluons carry inside the proton** is quantified by the **Parton Distribution Functions (PDFs)** 



**PDFs are** determined by **non-perturbative QCD dynamics:** cannot be computed from first principles, and need to be **extracted from experimental data** with a **global analysis** 

Energy conservation

$$\int_0^1 dx \left( g(x,Q) + \sum_q q(x,Q) \right) = 1$$

Dependence with quark/gluon collision energy Q determined in perturbation theory

$$\frac{\partial g(x,Q)}{\partial \ln Q} = P_g(\alpha_s) \otimes g(x,Q) + P_q(\alpha_s) \otimes q(x,Q)$$

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### The Factorization Theorem

The **QCD Factorization Theorem** guarantees **PDF universality: extract them from a subset of process** and use them to provide pure predictions for **new processes** 

$$\sigma_{lp}\simeq\widetilde{\sigma}_{lq}\left(lpha_{s},lpha
ight)\otimes q(x,Q)$$

 $\sigma_{pp} \simeq \widetilde{\sigma}_{q\bar{q}}\left(\alpha_s, \alpha\right) \otimes q(x_1, Q) \otimes \bar{q}(x_2, Q)$ 



# The NNPDF approach

A **novel approach to PDF determination**, improving the limitations of the traditional PDF fitting methods with the use of **advanced statistical techniques** such as **machine learning** and **multivariate analysis** 

#### Non-perturbative PDF parametrization

- **Traditional approach**: based on **restrictive functional forms** leading to strong theoretical bias
- Solution: use Artificial Neural Networks as universal unbiased interpolants

PDF uncertainties and propagation to LHC calculations

- **Fraditional approach**: limited to Gaussian/linear approximation
- NNPDF solution: based on the Monte Carlo replica method to create a probability distribution in the space of PDFs. Specially critical in extrapolation regions (i.e. high-*x*) for New Physics searches

Fitting technique

- **Fraditional approach**: deterministic minimization of  $\chi^2$ , flat directions problem
- NNPDF solution: Genetic Algorithms to explore efficiently the vast parameter space, with crossvalidation to avoid fitting stat fluctuations

# ANN as universal interpolators

- ANNs are routinely exploited in **high-energy physics**, in most cases as **classifiers** to separate between interesting and more mundane events
- ANNs also provide universal unbiased interpolants to parametrize the non-perturbative dynamics that determines the size and shape of the PDFs from experimental data



$$(x, Q_0) = A_g (1-x)^{a_g} x^{-b_g} \left( 1 + c_g \sqrt{s} + d_g x + \dots \right)$$

$$g(x, Q_0) = A_g \text{ANN}_g(x)$$

$$ANN_{g}(x) = \xi^{(L)} = \mathcal{F}\left[\xi^{(1)}, \{\omega_{ij}^{(l)}\}, \{\theta_{i}^{(l)}\}\right]$$
$$\xi_{i}^{(l)} = g\left(\sum_{j=1}^{n_{l-1}} \omega_{ij}^{(l-1)} \xi_{j}^{(l-1)} - \theta_{i}^{(l)}\right)$$

- ANNs eliminate **theory bias** introduced in PDF fits from choice of *ad-hoc* functional forms
- NNPDF fits used O(400) free parameters, to be compared with O(10-20) in traditional PDFs. Results stable if O(4000) parameters used!
- Faithful extrapolation: PDF uncertainties blow up in regions with scarce experimental data

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### Artificial Neural Networks vs Polynomials

Geometric Compare a **benchmark PDF analysis** where **the same dataset** is fitted with **Artificial Neural Networks** and with **standard polynomials**, other settings identical)

ANNs avoid biasing the PDFs, faithful extrapolation at small-x (very few data, thus error blow up)



# The Monte Carlo replica method

Two main approaches to estimate PDF uncertainties: the Hessian method and the Monte Carlo method

 $\Im$  In the **Hessian method**, the  $\chi^2$  is expanded quadratically in the **fit parameters** {**a**<sub>n</sub>} around the best fit

$$H_{lm}^{n} \equiv \frac{1}{2} \frac{\partial \chi_{n}^{2}}{\partial a_{l} \partial a_{m}} = \sum_{i=1}^{N_{\text{pts.}}} \frac{1}{(\sigma_{n,i}^{\text{uncorr.}})^{2} + \sum_{k} (\sigma_{n,k,i}^{\text{corr.}})^{2}} \frac{\partial T_{n,i}(\{a\})/\mathcal{N}_{n}}{\partial a_{l}} \frac{\partial T_{n,i}(\{a\})}{\partial a_{m}}$$

Final The Hessian matrix is diagonalized, and PDF errors on cross sections F from linear error propagation

$$\Delta \chi_{\text{global}}^2 \equiv \chi_{\text{global}}^2 - \chi_{\text{min}}^2 = \sum_{i,j=1}^n H_{ij}(a_i - a_i^0)(a_j - a_j^0) \qquad \Delta F = \frac{1}{2}\sqrt{\sum_{k=1}^n \left[F(S_k^+) - F(S_k^-)\right]^2},$$

- In the **Monte Carlo replica method**, pseudo-data replicas with same fluctuations as real data are generated, and then a PDF fit is performed **in each individual replica**
- Leads to probability distribution in the space of PDFs, without linear/Gaussian approximations

$$D_{m,i} \rightarrow \left( D_{m,i} + R_{m,i}^{\text{uncorr.}} \sigma_{m,i}^{\text{uncorr.}} + \sum_{k=1}^{N_{\text{corr.}}} R_{m,k}^{\text{corr.}} \sigma_{m,k,i}^{\text{corr.}} \right) \cdot \left( 1 + R_m^{\mathcal{N}} \sigma_m^{\mathcal{N}} \right)$$

$$\Delta F = \sqrt{\frac{N_{\text{rep}}}{N_{\text{rep}} - 1}} \left( \langle F^2 \rangle - \langle F \rangle^2 \right).$$

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#### Closure Testing of Parton Distributions

PDF uncertainties have been often criticised by a potential lack of statistical interpretation

NNPDF performed a systematic closure tests analysis based on pseudo-data, and verified that PDF uncertainties exhibit a statistically robust behaviour



#### Closure Testing of Parton Distributions

For instance, if the **pseudo-data is generated without statistical fluctuations** (that is, identical to the input theory) then the agreement with theory by construction should become **arbitrarily good** 

 $\frac{1}{2}$  And indeed it does: as the minimization advances, the  $\chi^2$  decreases monotonically, and the PDF uncertainties as well are reduced, as the fitted theory collapses to the underlying law



 $\varphi_{\chi^2} \equiv \sqrt{\langle \chi^2[\mathcal{T}[f_{\text{fit}}], \mathcal{D}_0] \rangle - \chi^2[\langle \mathcal{T}[f_{\text{fit}}] \rangle, \mathcal{D}_0]}$ 

Measure of PDF uncertainties in units of data uncertainties



# Recent Results with Unpolarized NNPDFs

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#### PDF constrains from LHC data

Exploitation of PDF-sensitive information from LHC data: essential component of global PDF fit program



#### Parton Distributions with QED corrections

At the LHC, **electroweak corrections** can become comparable or larger than **QCD effects** Precision physics thus requires **PDFs with QCD+QED evolution**, and a determination of the **photon PDF** 

Drell-Yan process: high-mass lepton pair production

QCD-only, leading order



#### Parton Distributions with QED corrections

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For many processes, accurate determination of the photon PDF as important as that of quark and gluon PDFs

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#### The charm content of the proton

- From the motivation to fit a charm PDF in a global analysis is two-fold:
  - **Stabilise the dependence of LHC calculations** with respect to **value of the charm mass**
  - **Or and Compare With Methods and Compare With Models**



#### A 30-years old conundrum of QCD!

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### Global QCD analysis with Intrinsic Charm



Ball, Bertone, Bonvini, Carrazza, Forte, Guffanti, Hartland, Rojo and Rottoli 16

At low scales, evidence for a **non-perturbative charm component**, but PDF errors still large At LHC scales, **fitted and dynamical charm in good agreement** for x < 0.01

Charm can account up to 1% of the total proton momentum at low scales

PDF set	Q	Charm momentum fraction
NNPDF3 dynamical charm		$(0.239 \pm 0.003)\%$
NNPDF3 fitted charm	$1.65~{ m GeV}$	$(0.7\pm0.3)\%$
NNPDF3 fitted charm (no EMC)		$(1.6\pm1.2)\%$

#### The charm PDF: implications for the LHC

- A number of LHC processes are sensitive to the **charm content of the proton**
- **Typically to probe large-x charm** we need either **large pT** or **forward rapidities** production
- **Within the reach of the LHC** at Run II



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#### PDFs usage in ATLAS and CMS



Parton Distributions are an essential component of many LHC analyses



# **Recent Results with Polarized NNPDFs**

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NNPDF, arXiv:1303.7236 NNPDF, arXiv:1406.5539

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#### Polarised Parton Distributions

- **Polarised PDFs** provide a unique windows on the **spin structure of the proton**.
- How the proton spin is distributed among its constituents is a crucial issue for our understanding of non-perturbative QCD and confinement

How do quarks (including sea quarks) and gluons carry the proton spin

$$\mathcal{S}(\mu) = \frac{1}{2} = \sum_{f} \left\langle P; S | \hat{J}_{f}^{z}(\mu) | P; S \right\rangle = \frac{1}{2} \int_{0}^{1} dx \Delta \Sigma(x, \mu) + \int_{0}^{1} dx \Delta g(x, \mu) + L_{z}$$

Quarks?

Gluons?

Angular Mom?

e.g. DIS 
$$d\Delta\sigma = \sum_{q,\bar{q},g} \Delta f(x,Q^2) \otimes d\Delta\hat{\sigma}_{\gamma^*f}(xP,\alpha_s(Q^2)) \quad d\Delta\hat{\sigma}_{\gamma^*f} = \sum_{n=0}^{\infty} \left(\frac{\alpha_s}{4\pi}\right)^n d\Delta\hat{\sigma}_{\gamma^*f}^{(n)}$$

	Reaction	Partonic subprocess	PDF probed	x	$Q^2 \; [\text{GeV}^2]$
	$\ell^{\pm}\{p,d,n\} \to \ell^{\pm}X$	$\gamma^* q  o q$	$\Delta q + \Delta ar q \ \Delta g$	$0.003 \lesssim x \lesssim 0.8$	$1 \lesssim Q^2 \lesssim 70$
*,K, SIDIS	$\ell^{\pm}\{p,d\} \to \ell^{\pm}hX$ $\ell^{\pm}\{p,d\} \to \ell^{\pm}DX$	$\gamma^* q  o q$ $\gamma^* g  o c \bar{c}$	$\Delta u \ \Delta ar u \ \Delta ar u \ \Delta ar d \ \Delta ar d \ \Delta ar d \ \Delta ar g \ \Delta g \ \Delta g \ \Delta g \ \Delta ar g \ A \ A \ A \ A \ A \ A \ A \ A \ A \$	$0.005 \lesssim x \lesssim 0.5$ $0.06 \lesssim x \lesssim 0.2$	$1 \lesssim Q^2 \lesssim 60$ $\sim 10$
Pp	$\vec{p} \vec{p} \to jet(s)X$ $\vec{p} p \to W^{\pm}X$ $\vec{p} \vec{p} \to \pi X$	$\begin{array}{c} gg \rightarrow qg \\ qg \rightarrow qg \\ u_L \bar{d}_R \rightarrow W^+ \\ d_L \bar{u}_R \rightarrow W^- \\ gg \rightarrow qg \\ qg \rightarrow qg \end{array}$	$\Delta g$ $\Delta u \ \Delta ar u$ $\Delta d \ \Delta ar d$ $\Delta g$	$0.05 \lesssim x \lesssim 0.2$ $0.05 \lesssim x \lesssim 0.4$ $0.05 \lesssim x \lesssim 0.4$	$30 \lesssim p_T^2 \lesssim 800$ $\sim M_W^2$ $1 \lesssim p_T^2 \lesssim 200$

- First measurements with polarised DIS (80s) showed that quark contribution much smaller than expected (proton spin crisis)
- With the availability of polarised hadronic and semi-inclusive data, global polarised
   PDF fits possible
- The NNPDF framework has also been applied to the polarized case, with NNPDFpol1.1 is the most updated set

## Unraveling the gluon polarisation

- Contribution of **gluon polarisation to the proton spin** has been of the **big unknowns** in the last 30 years
- The analysis of RHIC polarised jet data in the NNPDFpol1.1 and DSSV frameworks provides first ever evidence for positive (non-zero) polarisation of the gluon in the proton
- Importance of this important result recognised also in media outlets





# **Proton Spin Mystery Gains a New Clue**

Physicists long assumed a proton's spin came from its three constituent quarks. New measurements suggest particles called gluons make a significant contribution July 21, 2014 | By Clara Moskowitz

Protons have a constant spin that is an intrinsic particle property like mass or charge. Yet where this spin comes from is such a mystery it's dubbed the "proton spin crisis." Initially physicists thought a proton's spin was the sum of the spins of its three constituent quarks. But a 1987 experiment showed that quarks can account



Total contribution of gluons to proton spin still unknown since large uncertainties at small-x from lack of data: need an Electron-Ion Collider

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#### The polarised quark sea

Just Inclusive DIS data does not allow to separate polarised quarks from antiquarks

- Recent data on polarised **semi-inclusive DIS** and **hadronic** *W* **production** allow this separation
- Stringent constraints on **non-perturbative models of the polarized proton**



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# The Way Ahead

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#### Neural Network Fragmentation Functions

- Fragmentation functions (FFs) parametrize the non-perturbative dynamics responsible for the hadronization process (*Rodolfo's talk*)
- As opposed to MC hadronization models, FFs can be used to compute hadron production to much higher formal accuracy: NNLO in e+e-, NLO in DIS and pp
- Crucial for our understanding of non-perturbative QCD, to obtain information on the nucleon structure from semi-inclusive processes, and for LHC phenomenology, *i.e.* inclusive hadron production as probe of the quark-gluon plasma
- Solution Not the Second Second



NNFF1.0: Bertone, Carrazza, Nocera and JR, in preparation

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#### Neural Network Nuclear PDFs

- The PDFs of nucleons in bound nuclei are modified as compared to the free nucleon PDFs
- Solution Nuclear PDFs parametrize a rich variety of nuclear effects: shadowing, the EMC effect, Fermi motion ....
- High-precision nuclear PDFs are a crucial ingredient of the pPb and PbPb heavy ion program at the LHC, providing the cold-nuclear matter benchmark for quark-gluon plasma characterisation
- Solution North Nor of nuclear PDFs using the NNPDF methodology



Unpolarized present: NNPDF3.0 future: NNPDF3.1/4.0 LHC Run II data, theory errors, NNLO QCD+NLO EW ....



Unpolarized present: NNPDF3.0 future: NNPDF3.1/4.0 LHC Run II data, theory errors, NNLO QCD+NLO EW ....

**Polarized** present: NNPDFpol1.2 future: NNPDFpol2.0 (?) Semi-inclusive data using NNFFs

Nucleon Structure





