

NLO+PS predictions for top-pair and Wt production and decay



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work in collaboration with:

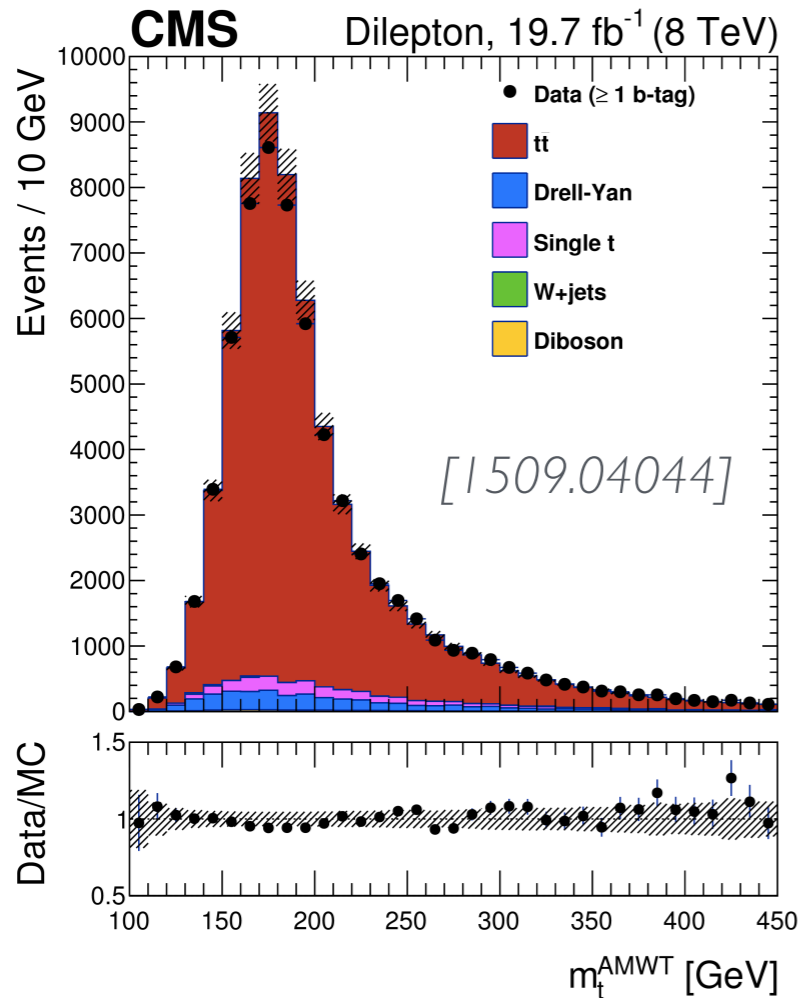
T. Ježo, P. Nason, C. Oleari, S. Pozzorini

based on [Ježo, Nason; '15] & [Ježo, JML, Nason, Oleari, Pozzorini; '16]

DESY Theory Workshop
DESY, Hamburg, 29th September 2016

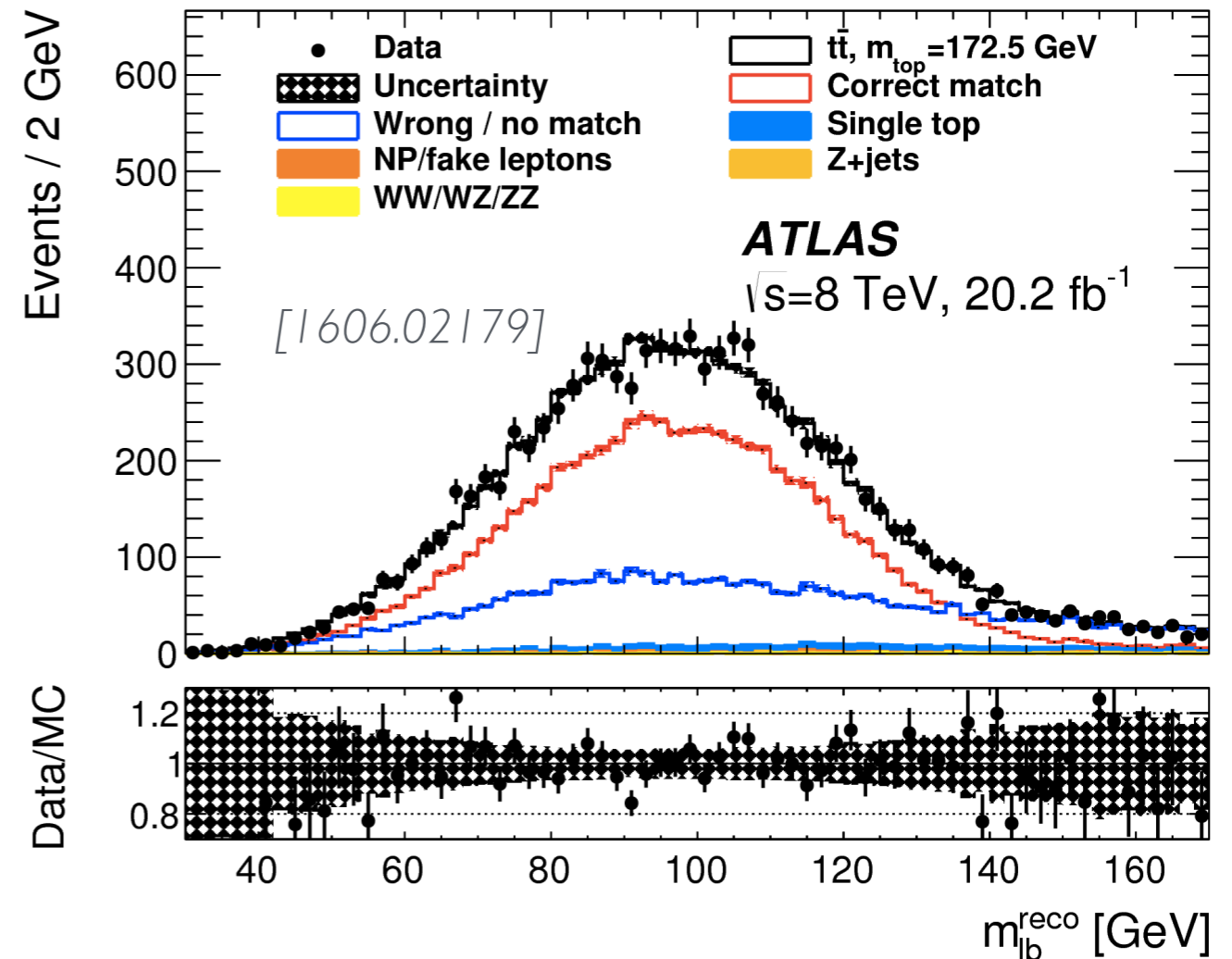
precision top-quark mass measurements rely on Monte Carlo modelling

via reconstruction using analytical distributions derived from simulated samples



$$m_{\text{top}} = 172.82 \pm 0.19 \text{ (stat)} \pm 1.22 \text{ (syst)} \text{ GeV}$$

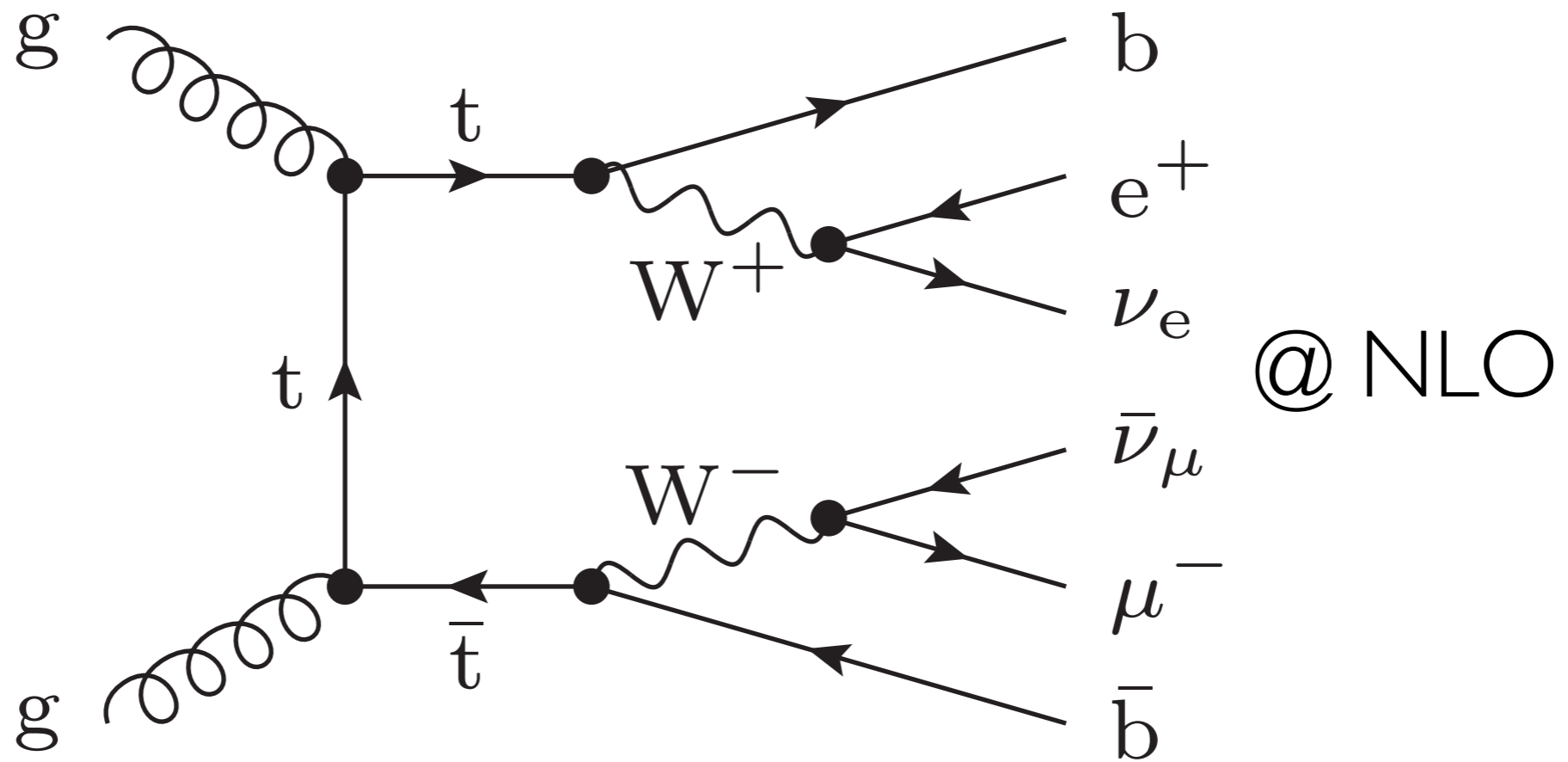
via template fit of lepton-b-jet invariant mass



$$m_{\text{top}} = 172.99 \pm 0.41 \text{ (stat)} \pm 0.74 \text{ (syst)} \text{ GeV}$$

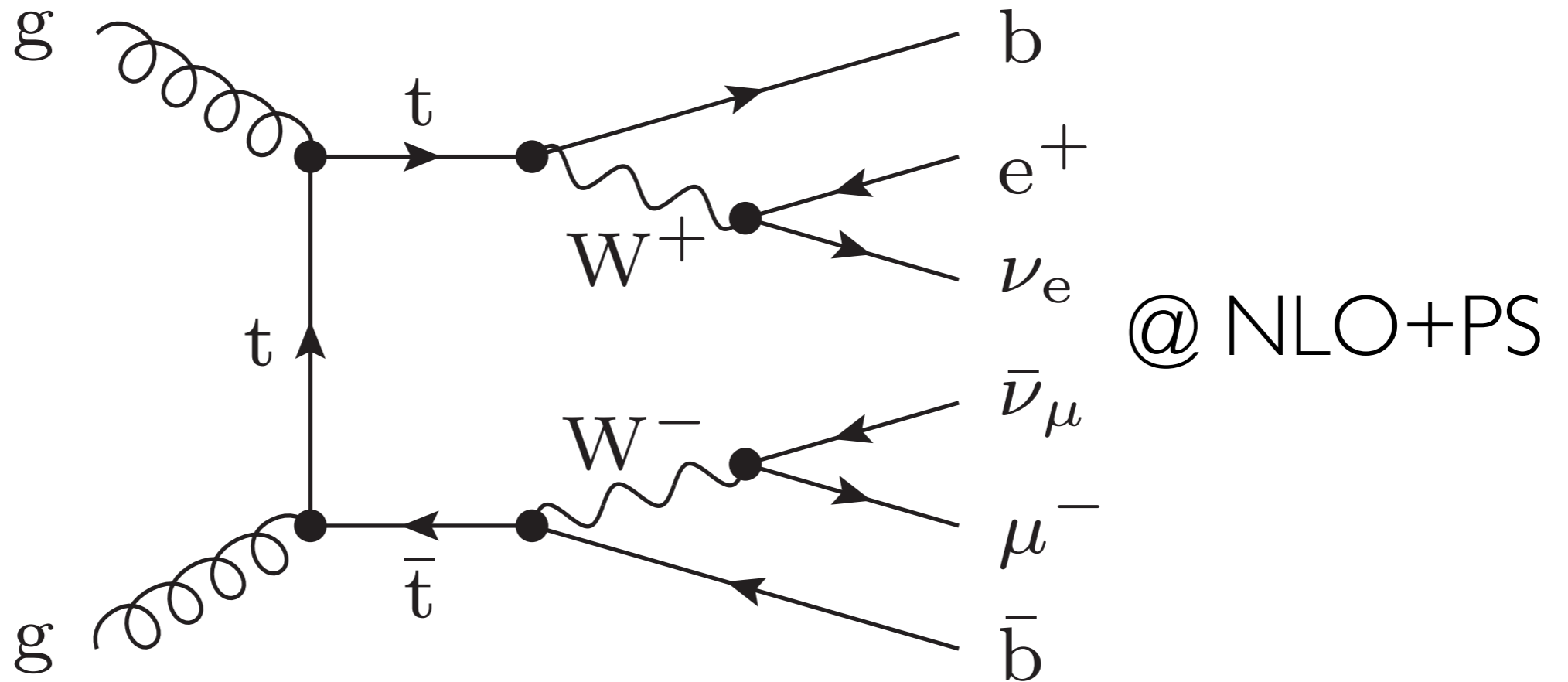
- these kinematic measurements strongly rely on MC modelling!

top-pair production and decay



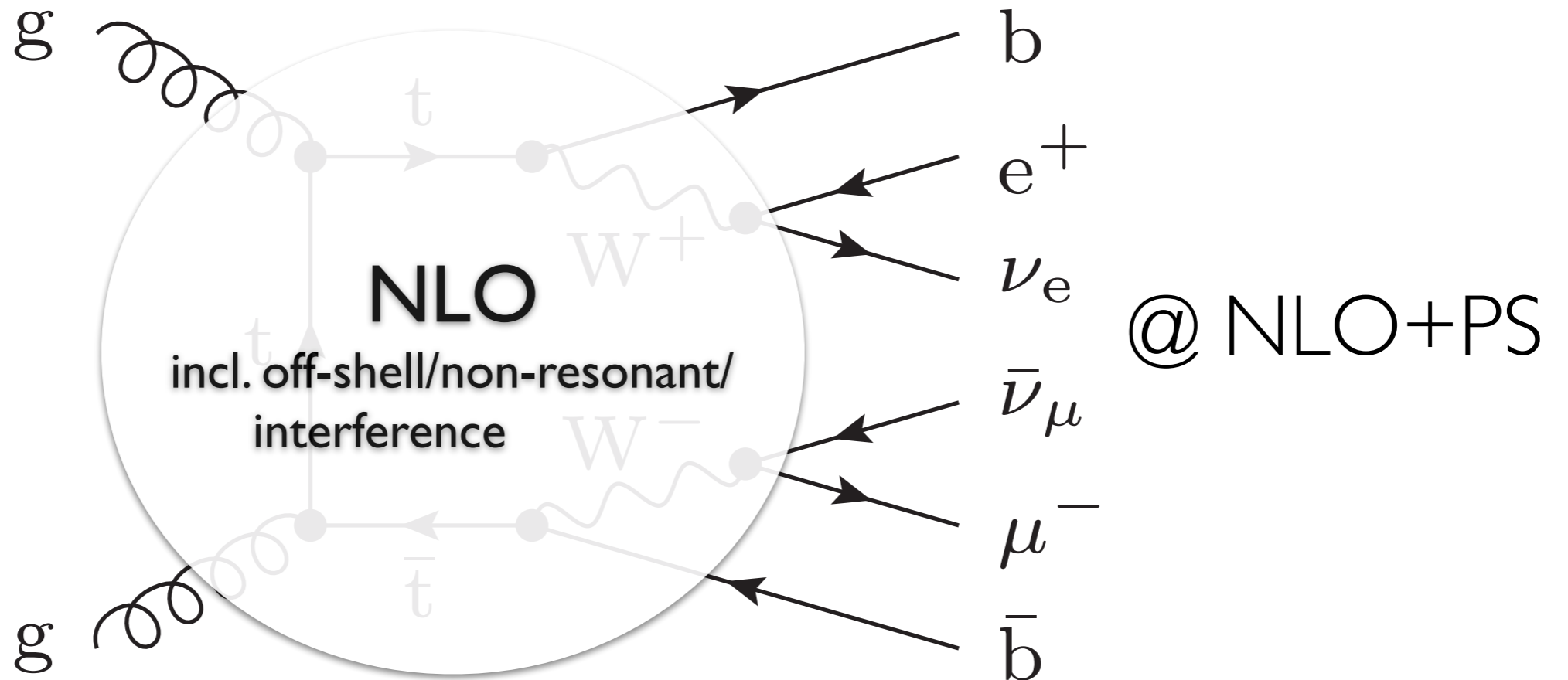
- NLO QCD 5FS:** [Bevilacqua, Czakon, van. Hameren, Papadopoulos, Worek; '11]
 [Denner, Dittmaier, Kallweit, Pozzorini; '11+'12] [Heinrich, Maier, Nisius, Schlenk, Winter; '14]
- 4FS:** [Frederix '14] [Cascioli, Kallweit, Maierhöfer, Pozzorini; '14]
- NLO EW 5FS:** [Denner, Pellen '16]

top-pair production and decay



- NLO QCD 5FS:** [Bevilacqua, Czakon, van. Hameren, Papadopoulos, Worek; '11]
[Denner, Dittmaier, Kallweit, Pozzorini; '11+'12] [Heinrich, Maier, Nisius, Schlenk, Winter; '14]
- 4FS:** [Frederix '14] [Cascioli, Kallweit, Maierhöfer, Pozzorini; '14]
- NLO EW 5FS:** [Denner, Pellen '16]
- NLO QCD+PS 5FS:** [Garzelli, Kardos, Trocsanyi; '14]

top-pair production and decay



- In a traditional off-shell NLO+PS calculation:
 - subtraction, matching and PS do not see/preserve intermediate resonances
 - ➔ **NLO**: efficiency problem
 - ➔ **NLO+PS**: distortion of important kinematic shapes!

Problem in POWHEG language

► Efficiency problem at NLO:

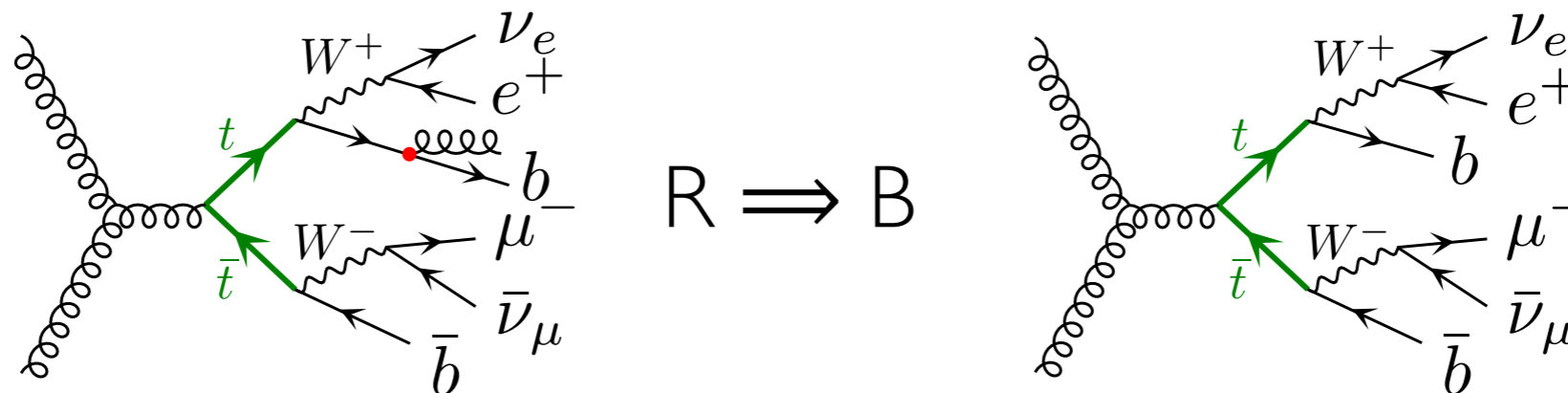
- FKS subtraction (and similar CS) does not preserve virtuality of intermediate resonances
- i.e. Real (R) and Subtraction-term (S~B) with different virtualities of intermediate resonances

$$(\Phi_B, \Phi_{\text{rad}}) \xleftrightarrow{\text{FKS}} \Phi_R$$

Φ_R = real phase-space

Φ_B = (underlying) Born phase-space

Φ_{rad} = radiation phase-space



- IR cancellation spoiled

⇒ severe efficiency problem for narrow resonances!

Problem in POWHEG language

► Fundamental problems at NLO+PS:

- **NLO+PS** matching according to POWHEG formula:

$$d\sigma = \bar{B}(\Phi_B) d\Phi_B \left\{ \Delta(q_{\text{cut}}) + \Delta(k_T) \frac{R(\Phi_R(\Phi_B, \Phi_{\text{rad}}))}{B(\Phi_B)} d\Phi_{\text{rad}} \right\}$$

$$\bar{B}(\Phi_B) = B(\Phi_B) + V(\Phi_B) + \int R(\Phi_R(\Phi_B, \Phi_{\text{rad}})) d\Phi_{\text{rad}}$$

$$\Delta(q) = \exp \left[- \int_{k_T > q} \frac{R(\Phi_R(\Phi_B, \Phi_{\text{rad}}))}{B(\Phi_B)} d\Phi_{\text{rad}} \right]$$

- ➔ FKS mappings $(\Phi_B, \Phi_{\text{rad}}) \xleftrightarrow{\text{FKS}} \Phi_R$ do not preserve intermediate resonances
 - ➔ **R/B** might become large by coincidence (e.g. R on-peak, B off-peak), but should be small (of the order of α_S) or approach Altarelli-Parisi splitting functions.
 - ➔ Radiation (incl. Sudakov form-factor) generated from uncontrollable **R/B** ratios
- also subsequent radiation by the **PS** itself reshuffles internal momenta and does in general not preserve the virtuality of intermediate resonances.

⇒ **expect uncontrollable distortion of important kinematic shapes!**

Resonance aware POWHEG

Rigorous solution to all these issues within POWHEG according to [Ježo, Nason; '15]

Idea: **preserve invariant mass of intermediate resonances at all stages!**

✓ NLO:

- Split phase-space integration into regions dominated by a single **resonance history**
- within a given resonance history **modify FKS mappings**, such that they *always* preserve intermediate resonances
$$\boxed{(\Phi_B, \Phi_{\text{rad}}) \xleftrightarrow{\text{RES FKS}} \Phi_R}$$
 - ⇒ R and S~B *by construction* with same virtuality of intermediate resonances
 - ⇒ **IR cancellation restored**

✓ NLO+PS:

- R and B related via resonance-aware FKS mappings
 - ⇒ **R/B** ratio with fixed virtuality of intermediate resonances
 - ⇒ **Sudakov form-factor preserves intermediate resonances**

✓ PS:

- pass information about resonance histories to the shower (via extension of LHE)
- tell **PS to respect intermediate resonances** (available in Pythia8)

Multiple-radiation scheme

- ▶ In traditional approach only hardest radiation is generated by POWHEG:

or or

$$\Leftrightarrow \quad d\sigma = \bar{B}(\Phi_B) d\Phi_B \left[\Delta(q_{\text{cut}}) + \sum_{\alpha} \Delta(k_T^{\alpha}) \frac{R_{\alpha}(\Phi_{\alpha}(\Phi_B, \Phi_{\text{rad}}))}{B(\Phi_B)} d\Phi_{\text{rad}} \right]$$

BUT: for top-pair (or single-top) production and decay, emission from production is almost always the hardest.

➔ emission off decays are mostly generated by the shower.

- ▶ **Multiple-radiation scheme:**

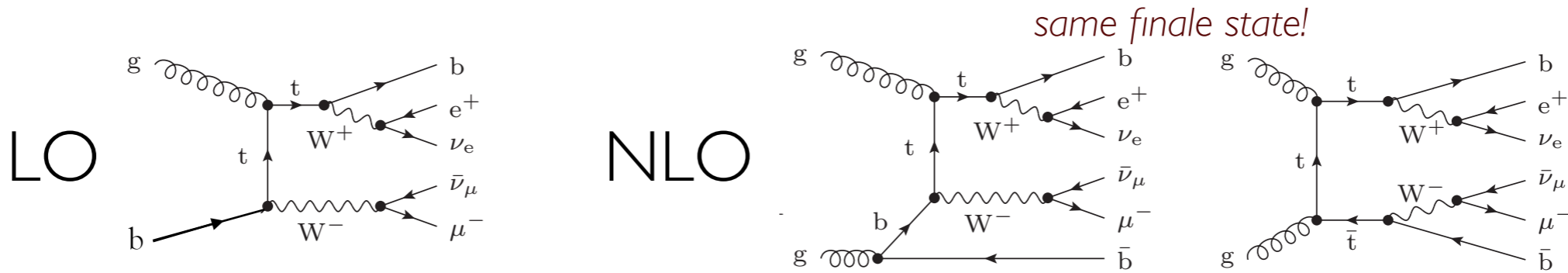
introduced in [Campbell, Ellis, Nason, Re; '15]

- keep hardest emission from all resonance histories.
- merge emissions into a single radiation event with several radiated partons

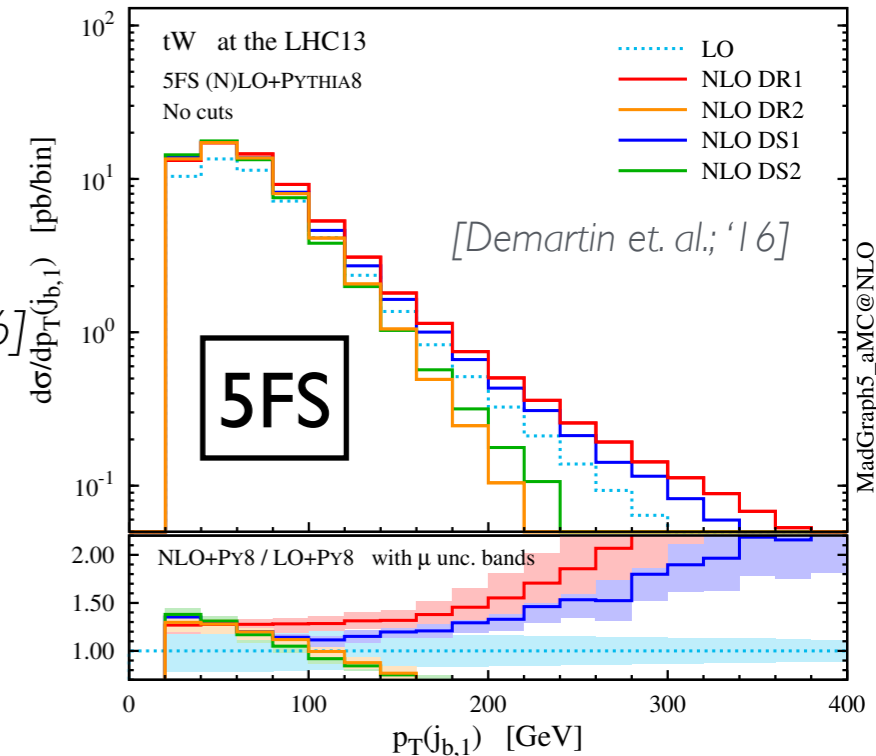
$$\Leftrightarrow \quad d\sigma = \bar{B}(\Phi_B) d\Phi_B \prod_{\alpha=\alpha_b, \alpha_{\bar{b}}, \alpha_{\text{ISR}}} \left[\Delta_{\alpha}(q_{\text{cut}}) + \Delta_{\alpha}(k_T^{\alpha}) \frac{R_{\alpha}(\Phi_{\alpha}(\Phi_B, \Phi_{\text{rad}}^{\alpha}))}{B(\Phi_B)} d\Phi_{\text{rad}}^{\alpha} \right]$$

Interplay between top-pair and Wt single-top production

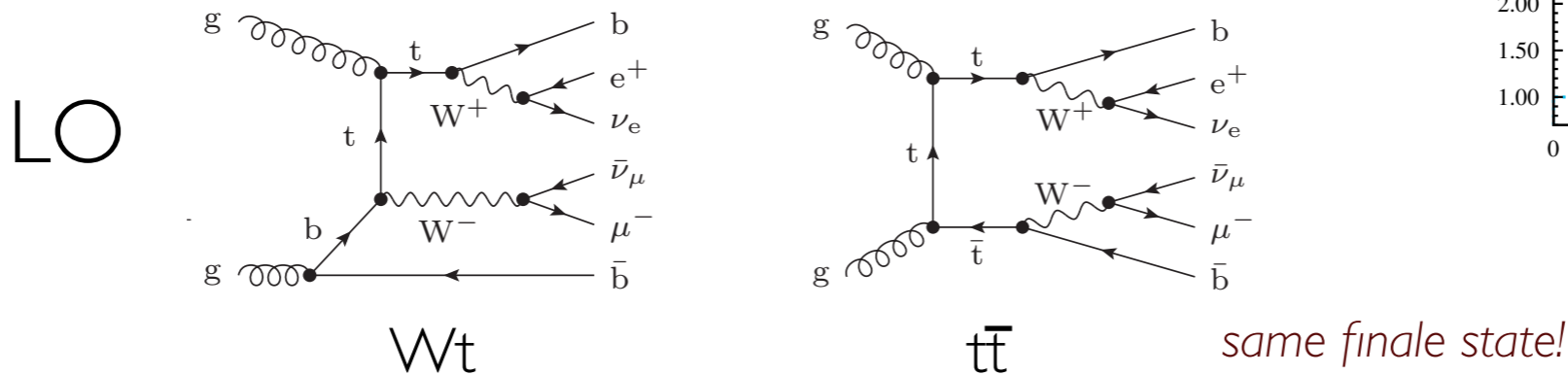
5FS



- NLO corrections to Wt swamped by LO $t\bar{t}$ +decay
- requires ad-hoc subtraction prescription: DRI, DRII, DSI, DSII
- NLO+PS for Wt available in MC@NLO [Frixione, et. al.; '08], POWHEG [Re; '11] and Madgraph_aMC@NLO [Demartin et. al.; '16]



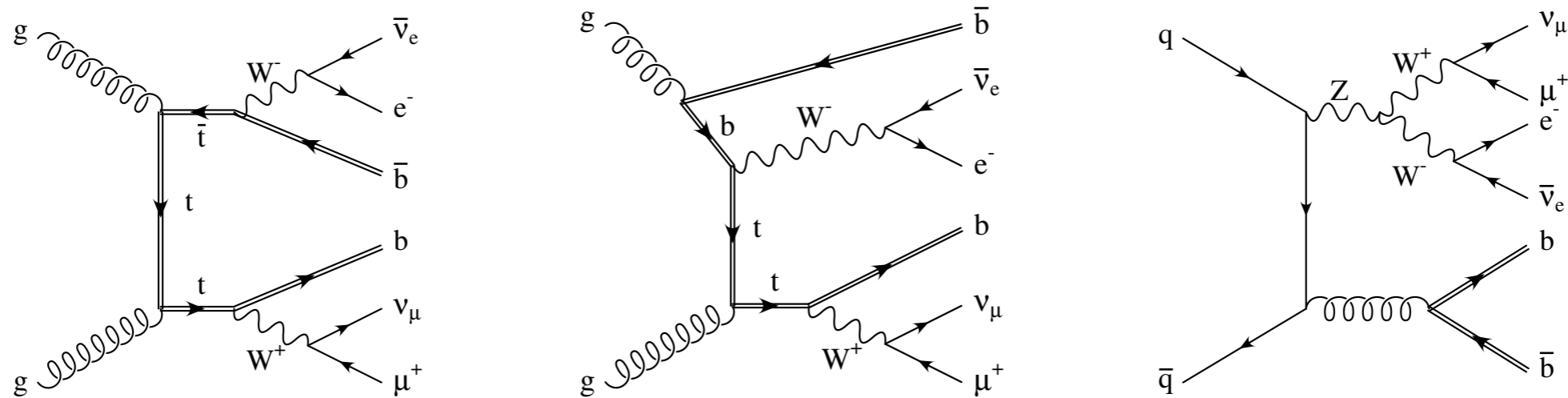
4FS



- **unified treatment of top-pair and Wt including interference**
- Wt enhanced in phase-space regions where one b becomes unresolved/vetoed
- requires off-shell WWbb calculation (with massive b's)

The new $b\bar{b}4l$ generator

- ▶ We consider the full process $pp \rightarrow b\bar{b}e^+\nu_e\mu^-\bar{\nu}_\mu$ with massive b's (**4FS scheme**)
- ▶ Implemented in the **POWHEG-BOX-RES** framework
- ▶ All matrix elements from **OpenLoops** [Cascioli, JML, Maierhöfer, Pozzorini]

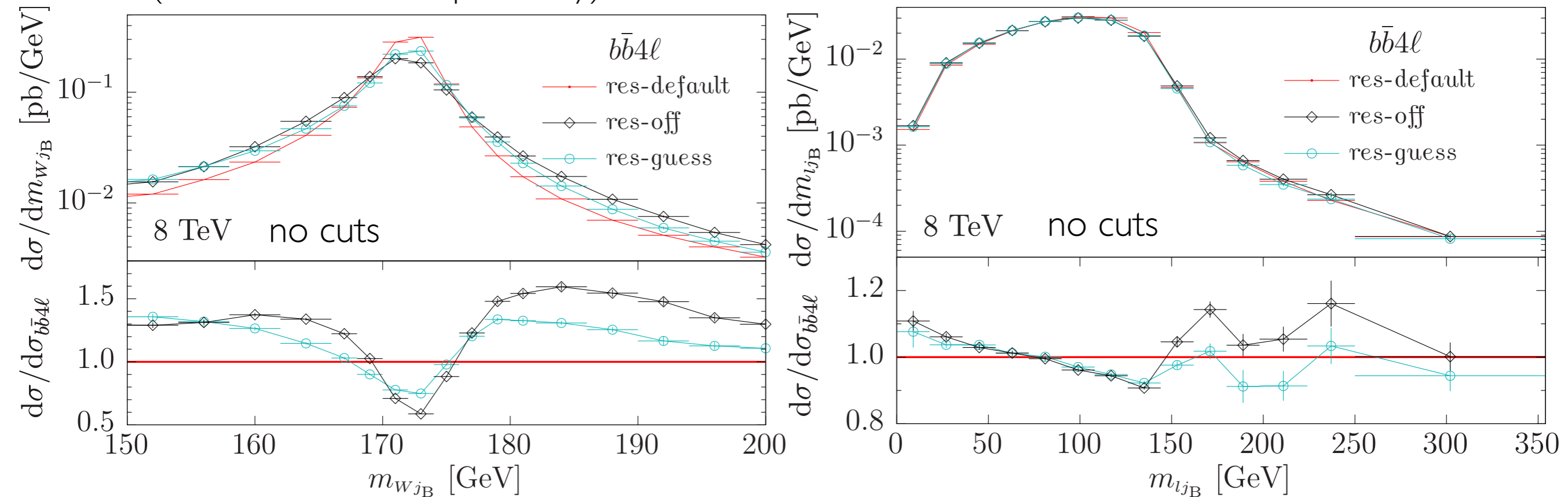


Physics features:

- exact **non-resonant / off-shell / interference / spin-correlation** effects at NLO
- unified treatment of **top-pair and Wt** production with interference at NLO
- access to phase-space regions with **unresolved b-quarks** and/or jet vetoes
- **consistent NLO+PS treatment of top resonances**, including quantum corrections to top propagators and off-shell top-decay chains

Results: top-resonance

- ▶ default: resonance aware matching & multiple-radiation scheme
- ▶ off: resonance unaware matching
- ▶ guess: resonance unaware matching but kinematic guess off resonance structure before PS (based on kinematic proximity)



⇒ resonance unaware matching yields distortions of important kinematic shapes

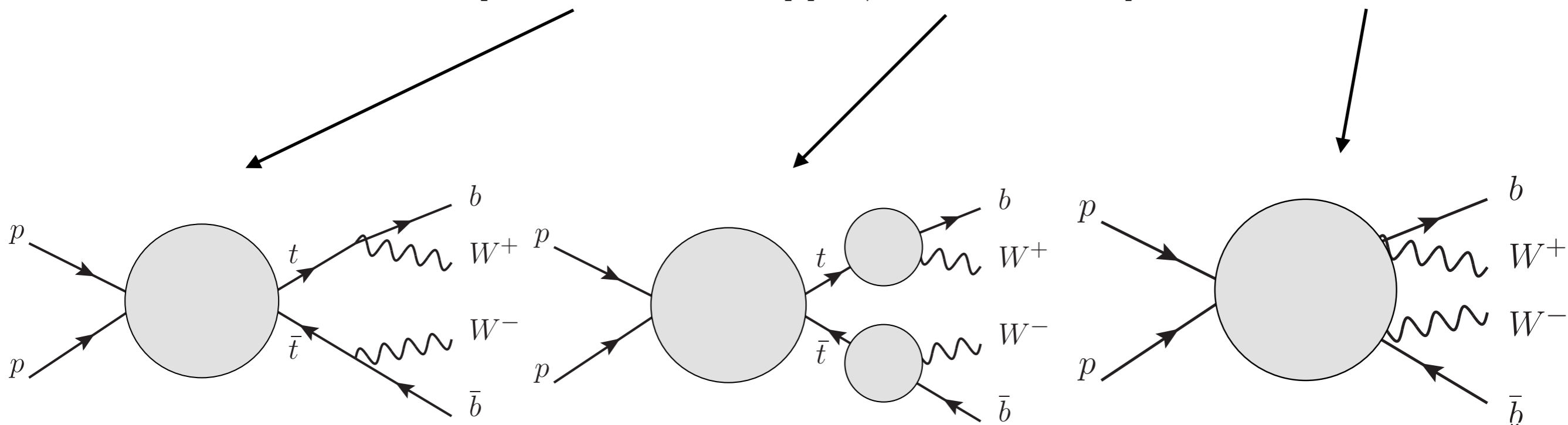
⇒ control of these shapes crucial for **precise top-mass measurements!**

⇒ resonance assignment based on kinematic proximity with standard matching not sufficient

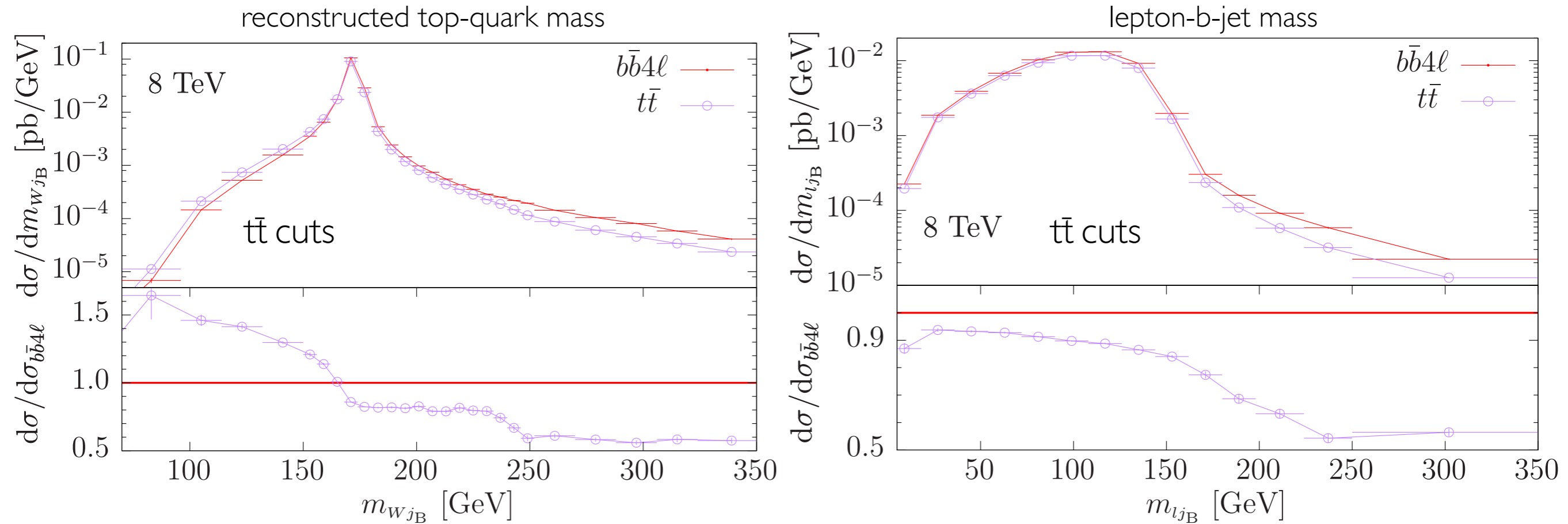
Top-pair production in POWHEG

label	$t\bar{t}$ NLOPS	$t\bar{t}$ +decay NLOPS	$b\bar{b}4\ell$ NLOPS-RES
NLO matrix elements	$t\bar{t}$	$t(\rightarrow e^+\nu_e b)\bar{t}(\rightarrow \mu^-\bar{\nu}_\mu \bar{b})$	$b\bar{b}e^+\nu_e\mu^-\bar{\nu}_\mu$
decay accuracy	LO+PS	NLO+PS	NLO+PS
NLO radiation	single	multiple	multiple
spin correlations	approx.	exact	exact
off-shell $t\bar{t}$ effects	BW smearing	LO $b\bar{b}4\ell$ reweighting	exact
Wt & non-resonant effects	no	LO $b\bar{b}4\ell$ reweighting	exact

[Frixione, Nason, Ridolfi; '07] [Campbell, Ellis, Nason, Re; '15] [Ježo, JML, Nason, Oleari, Pozzorini; '16]

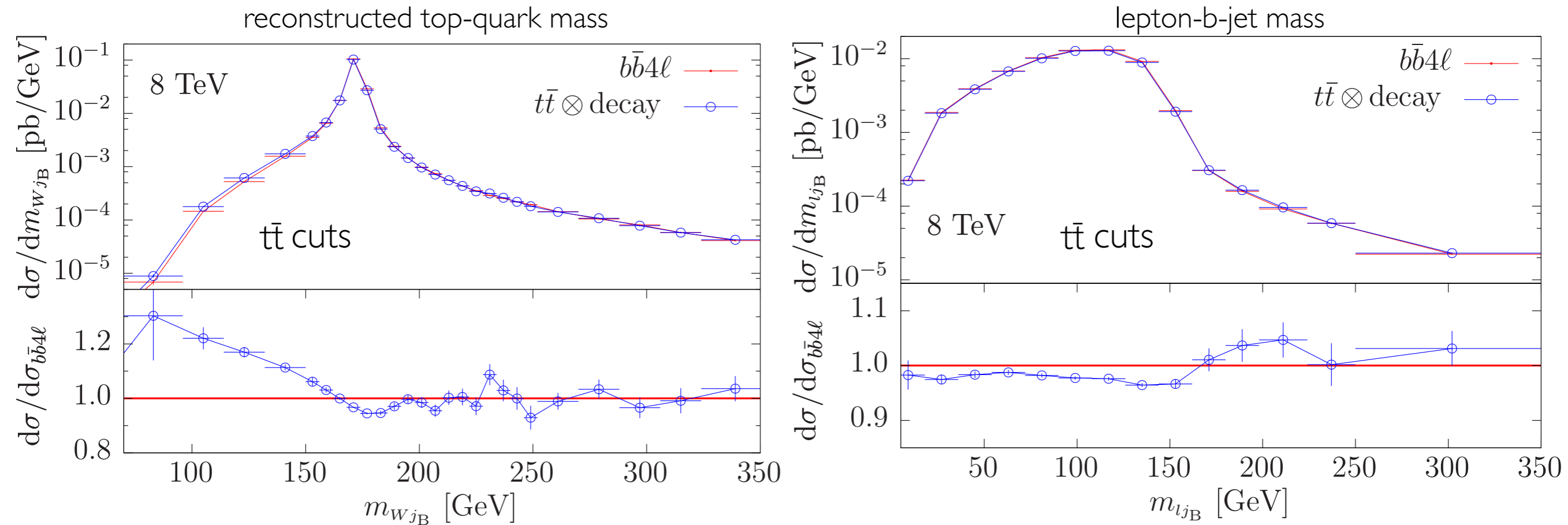


Results: on-shell $t\bar{t}$ vs. $bb4l$



- significant shape distortions around resonance with respect to on-shell calculation
- very relevant for top mass determination
- average m_{WjB} roughly 500 MeV smaller in on-shell $t\bar{t}$ (in ± 30 GeV around m_{top})
- ~ 20 - 30% effects around the b-jet-lepton invariant mass edge

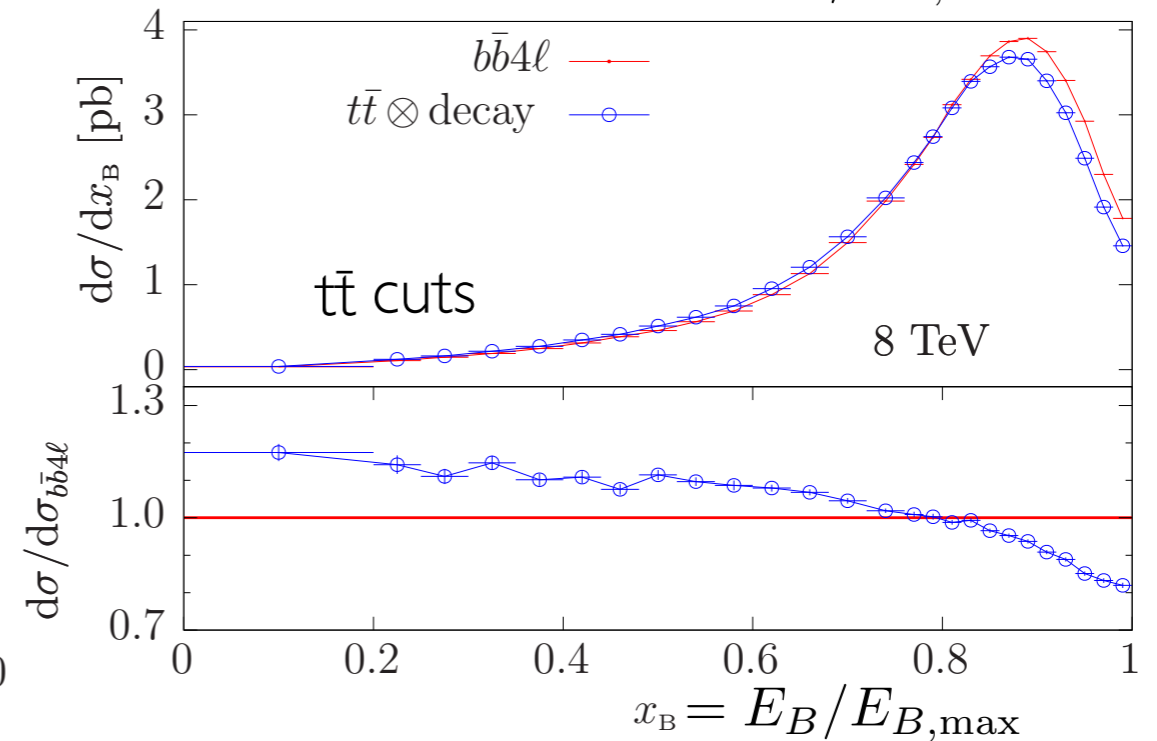
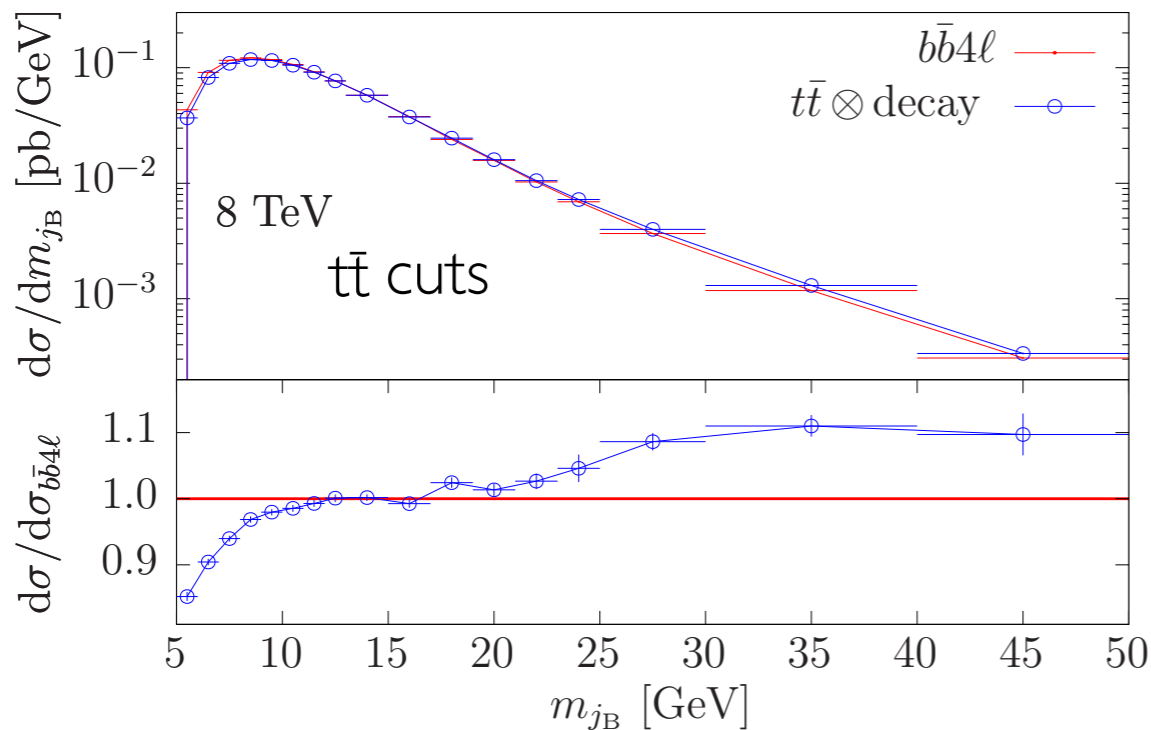
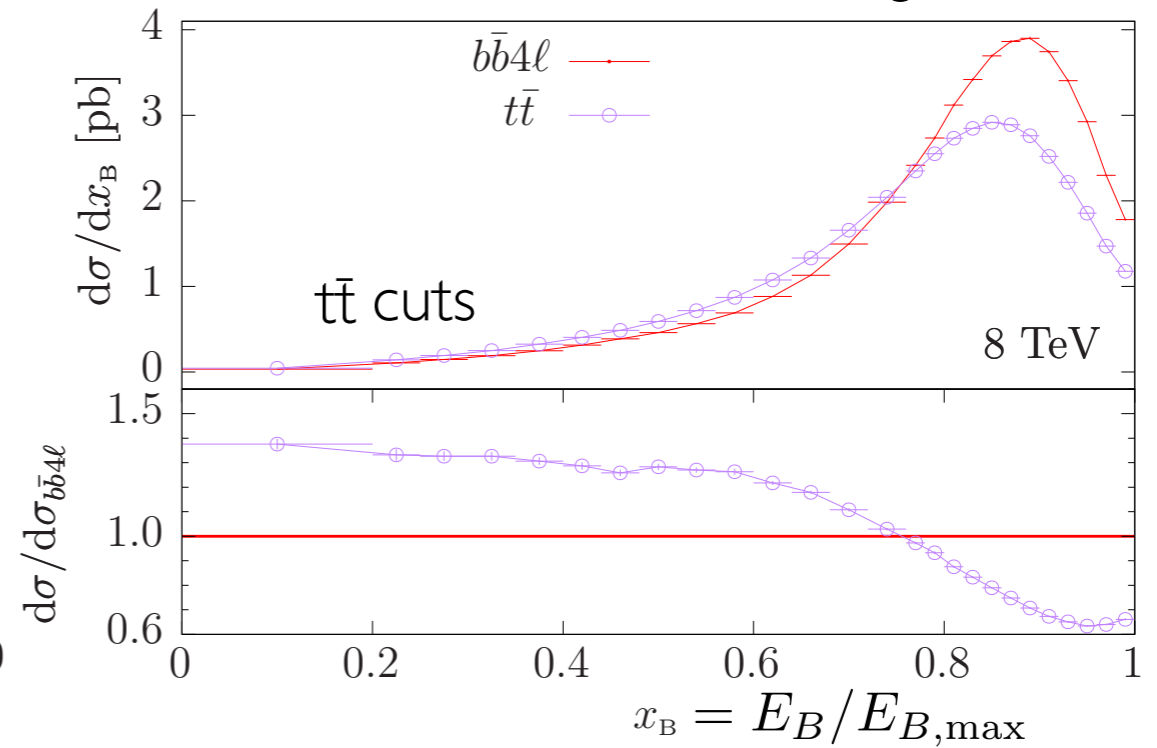
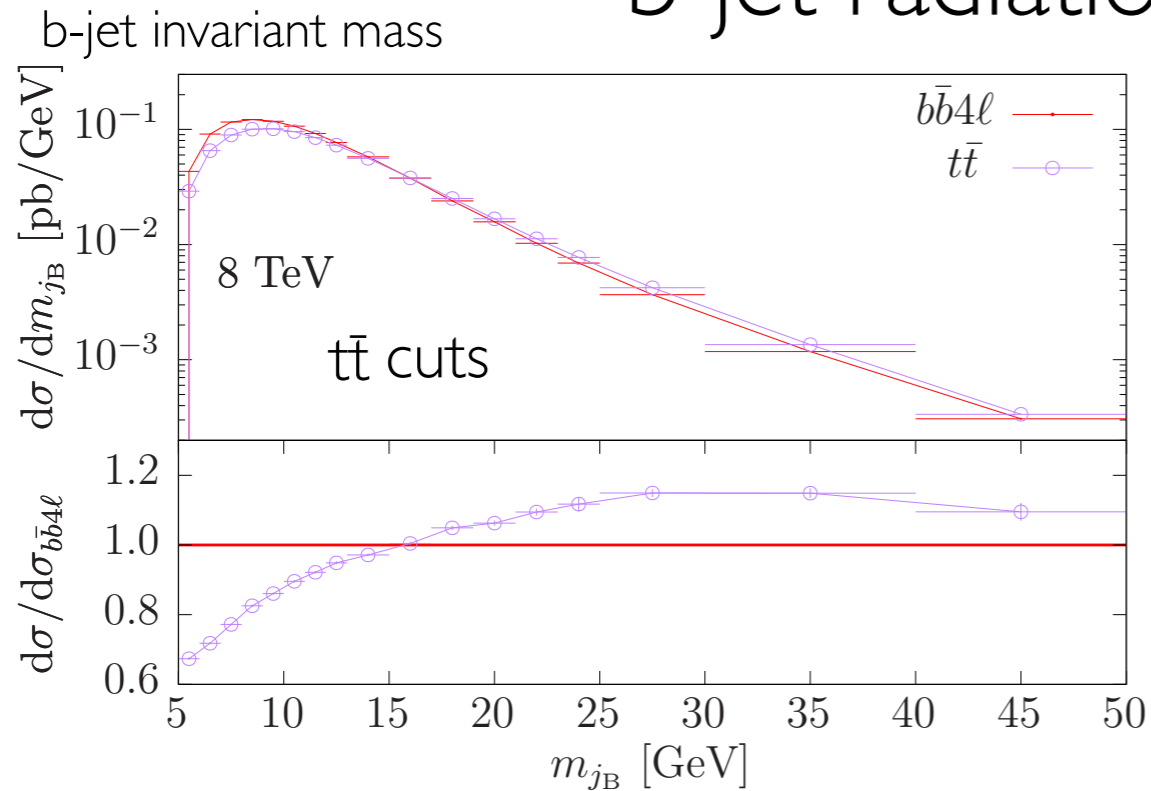
Results: $t\bar{t} \otimes$ decay vs. $b\bar{b}4\ell$



- very good agreement mostly $<5\%$ level between the two predictions
- the two calculations support each other (natural factorization of radiation between production and decay in $t\bar{t} \otimes$ decay)
- average m_{WjB} roughly 100 MeV smaller in $t\bar{t} \otimes$ decay (in ± 30 GeV around m_{top})

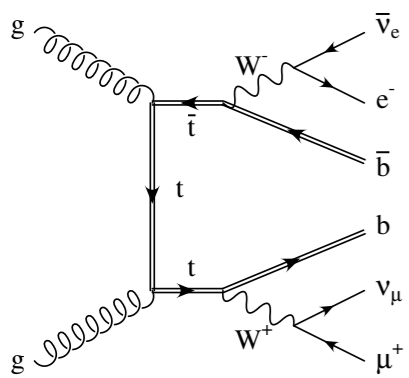
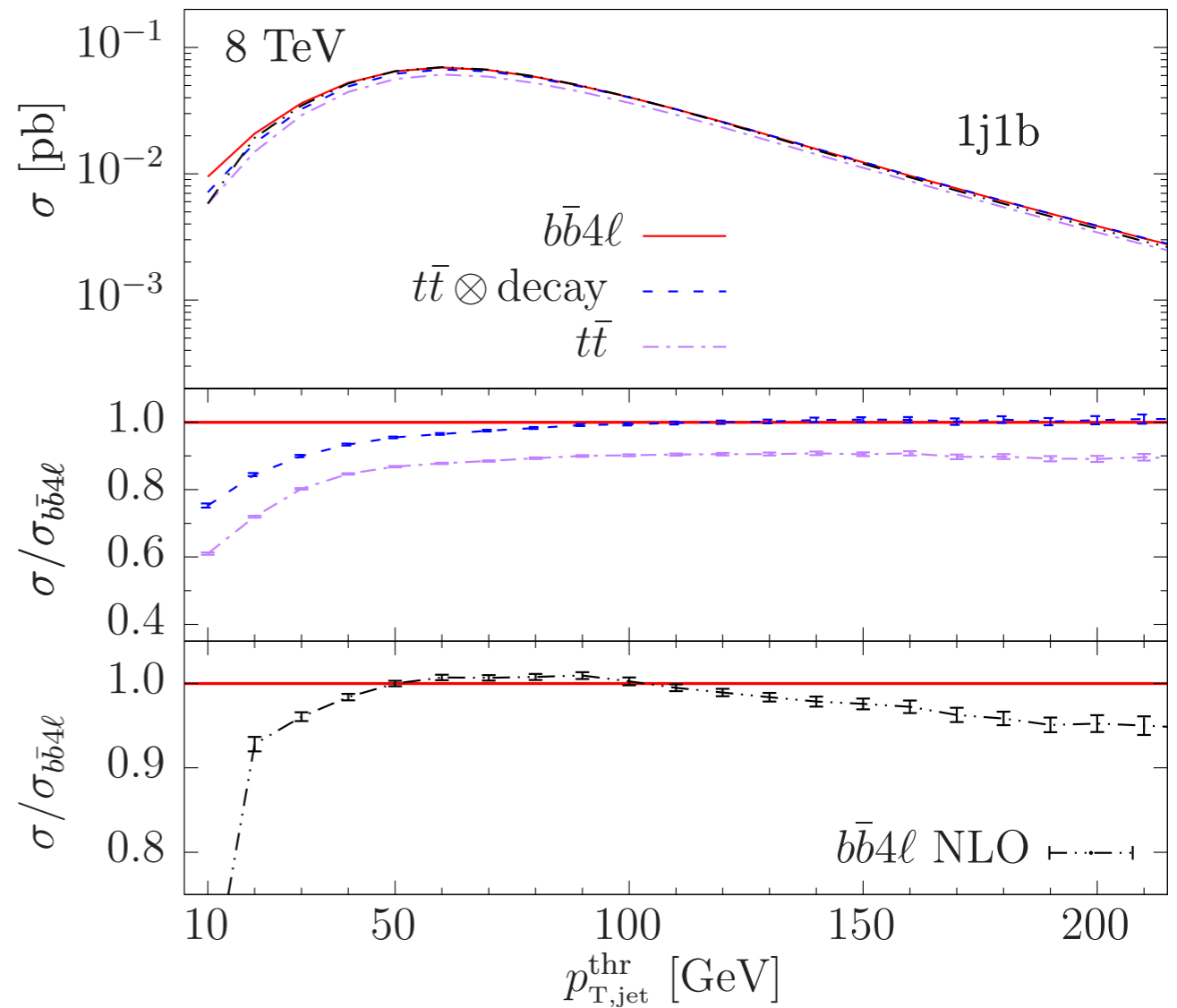
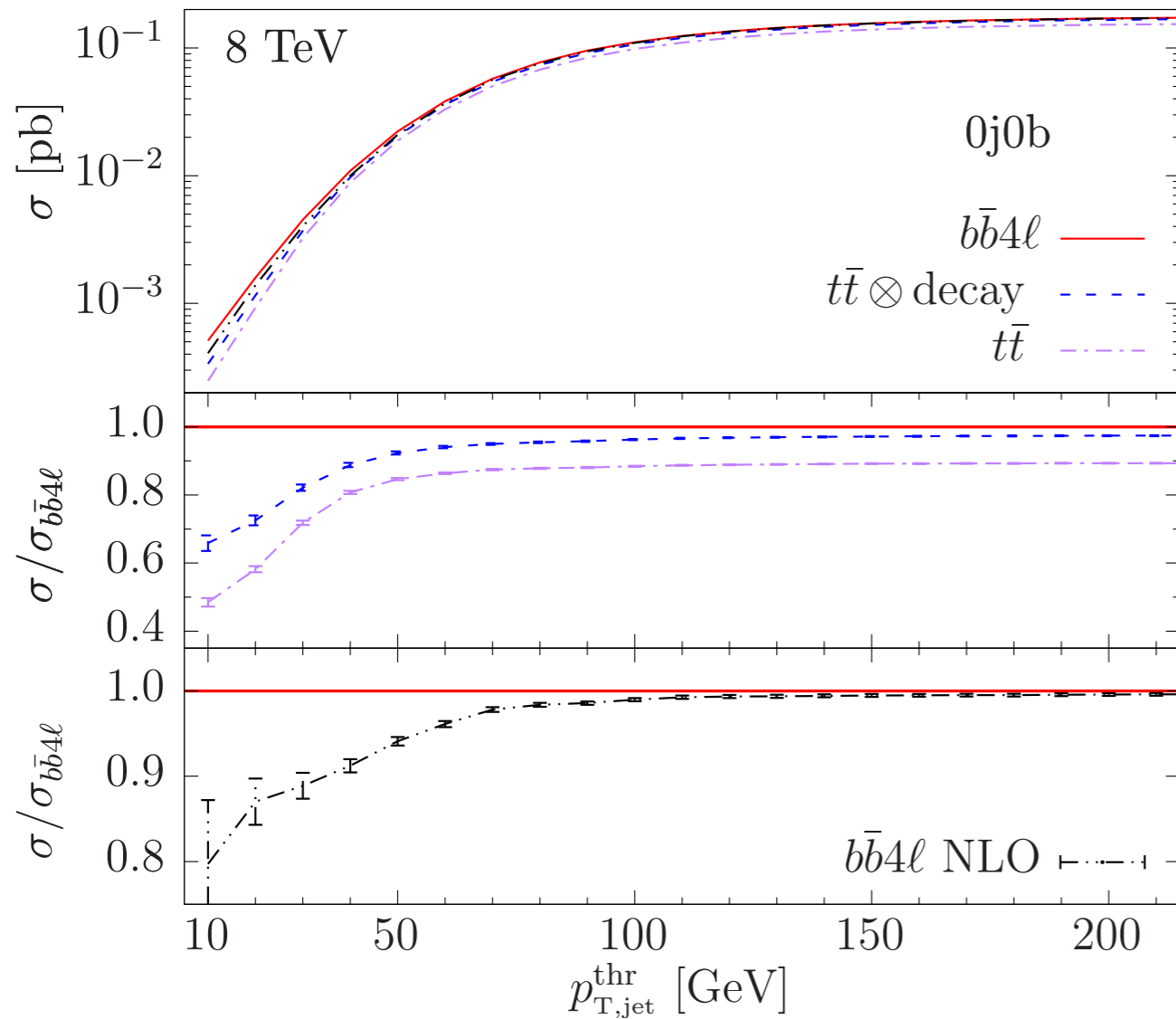
b-jet radiation properties

B-hadron fragmentation function

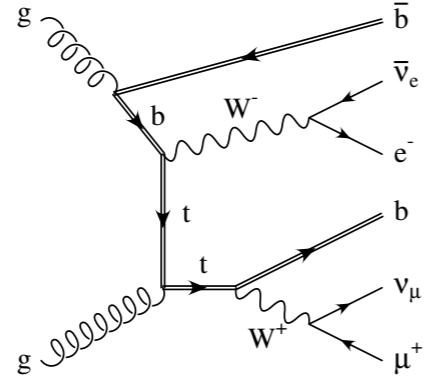


- narrower b-jets and harder B-fragmentation in $b\bar{b}4l$
- due to reduced radiation from b's in $b\bar{b}4l$

jet vetoes and single-top enriched observables



VS.



- for small jet thresholds Wt single-top reaches 40-50%
- $t\bar{t} \otimes \text{decay}$ includes Wt only at LO and treats tops on-shell at NLO \Rightarrow overestimates radiation in Wt region
- 10-20% jet veto resummation effects
- important for any $t\bar{t}$ background with jet vetoes (e.g. $H \rightarrow W^+W^-$)

Conclusions

Technology:

- ▶ Resonance-aware matching is pivotal for processes with intermediate resonances
 - ➔ (quite) Rigorous solution within POWHEG by [Ježo, Nason; '15]
- ▶ New POWHEG framework: **POWHEG-BOX-RES** (<http://powhegbox.mib.infn.it/>)
 - resonance-aware subtraction and matching for any process
 - automated generation of resonance histories and phase-space
 - process independent **POWHEG-BOX+OpenLoops** interface

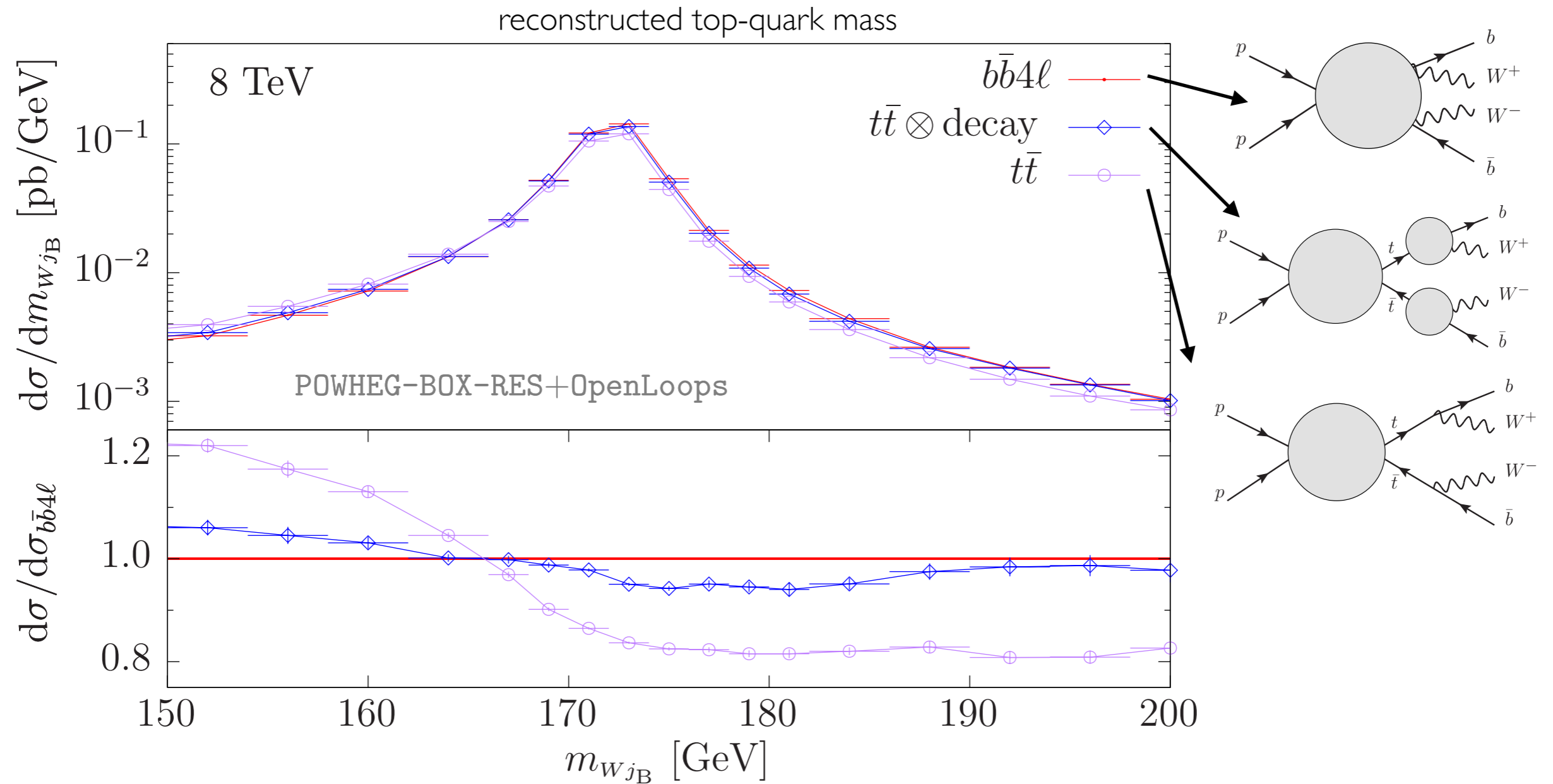
Phenomenology:

- ▶ resonance-aware matching crucial for kinematic precision top-mass measurements
- ▶ unified treatment of $t\bar{t}$ & $W\bar{t}$ important for precision single-top physics
- ▶and for modelling of $t\bar{t}$ backgrounds subject to jet vetoes.

Outlook:

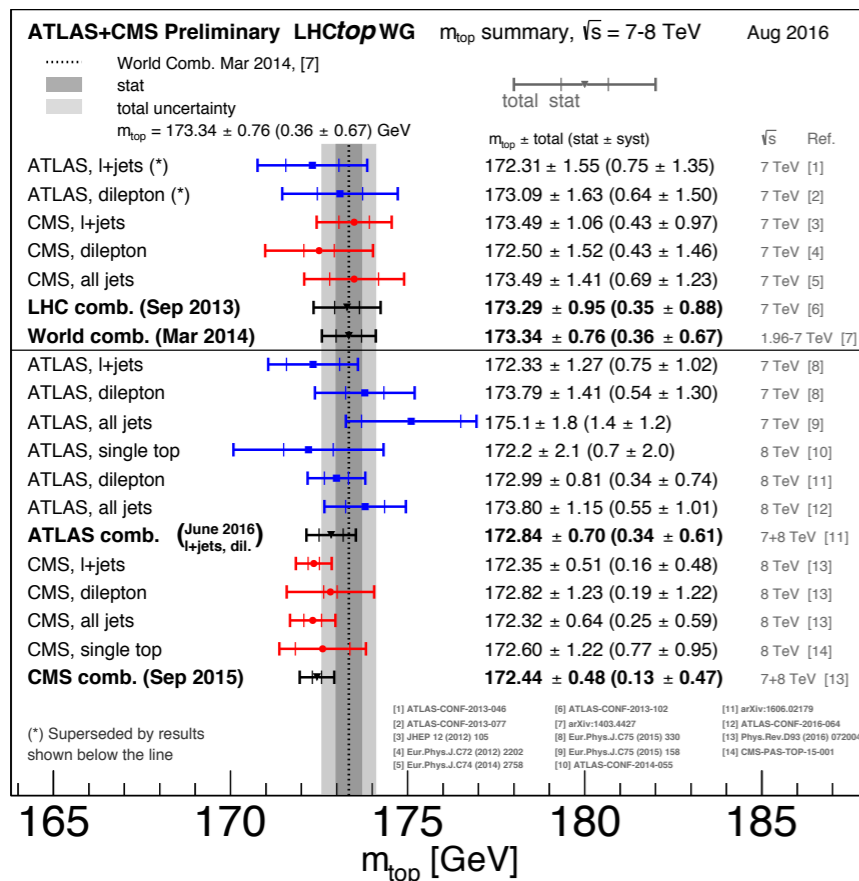
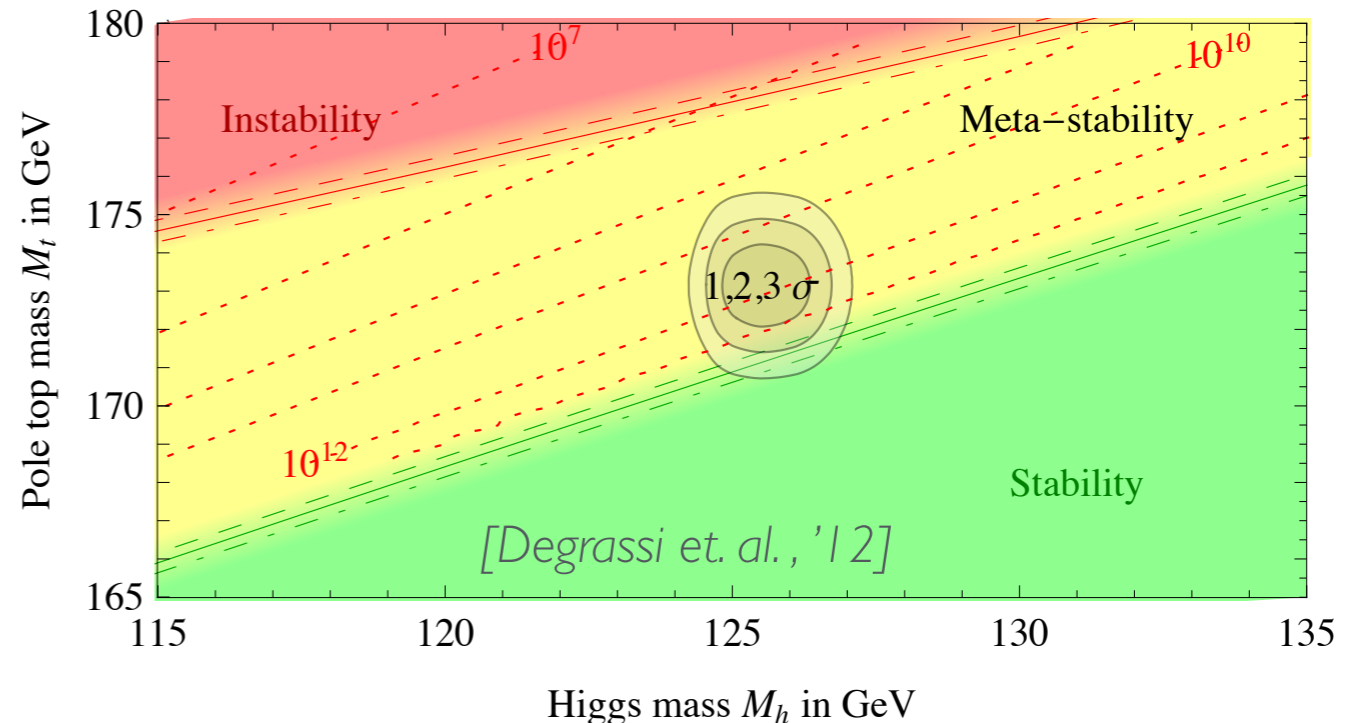
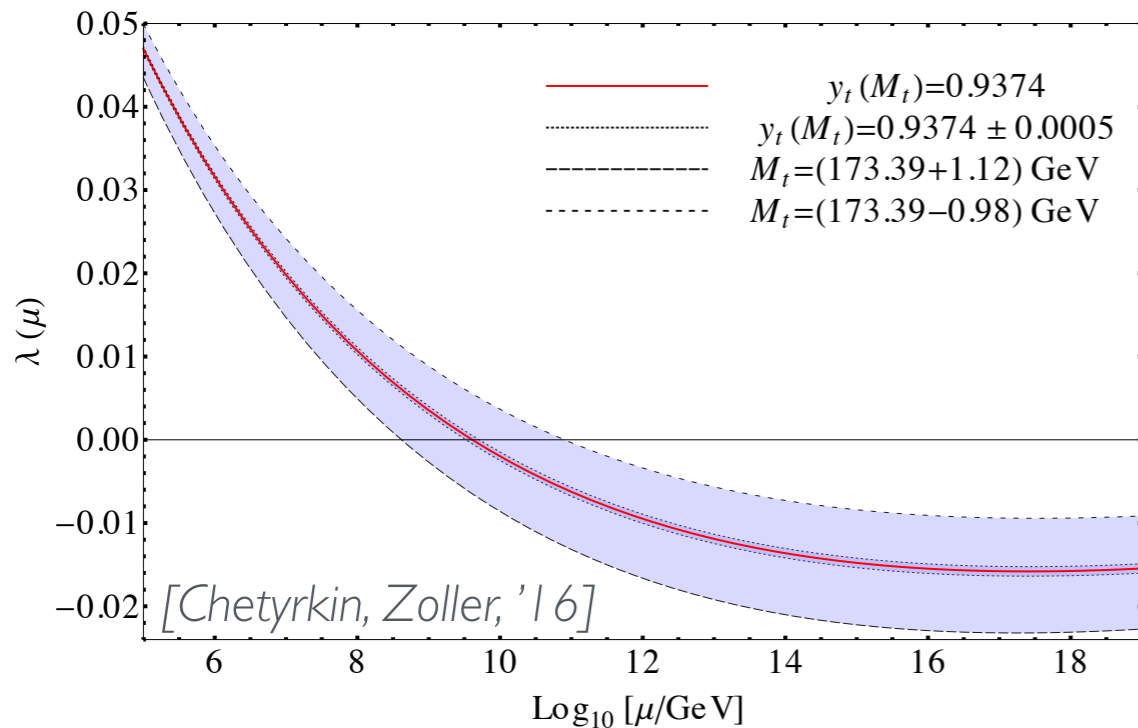
- Detailed investigation of effects on top mass measurements
- Hadronic top decays

Summary of the results



Backup slides

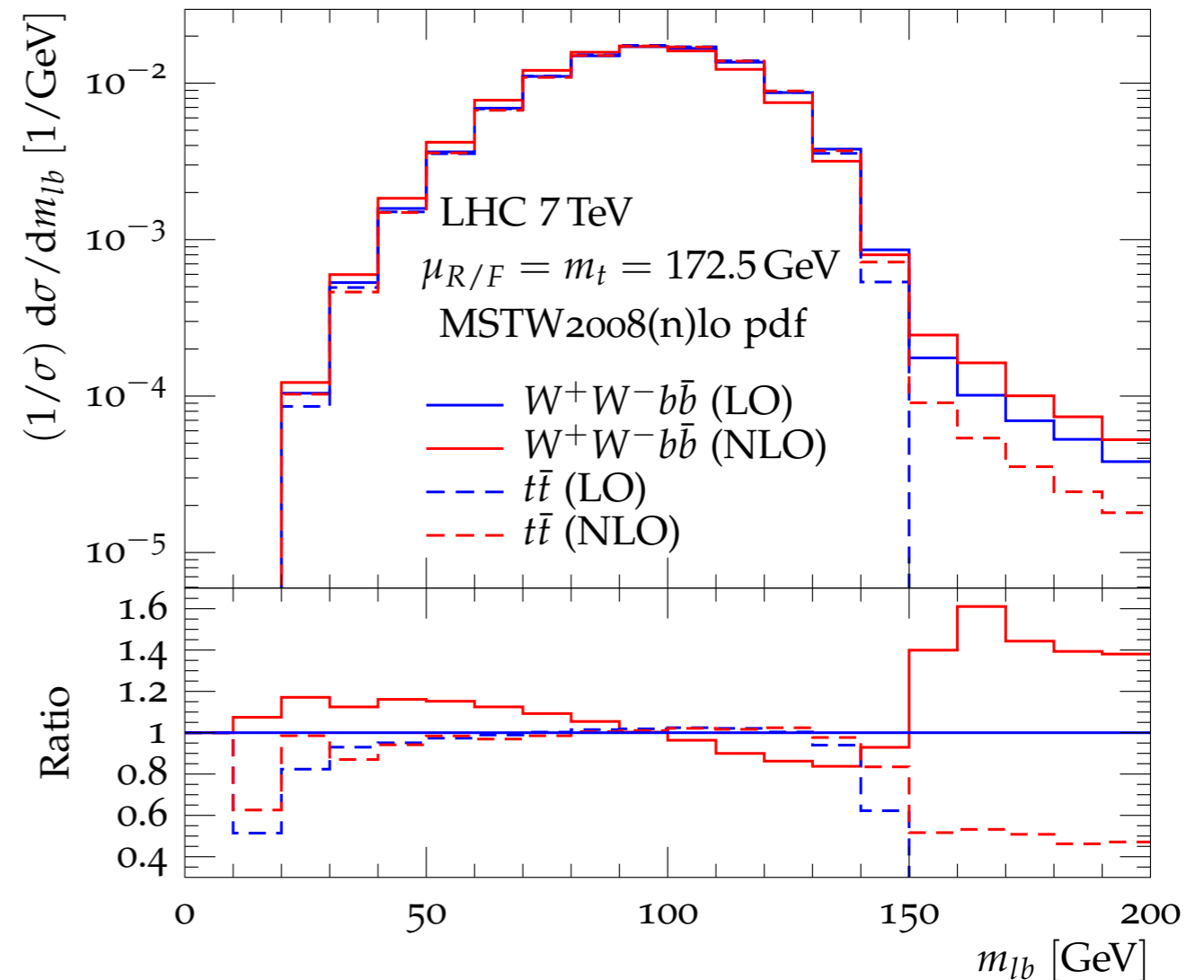
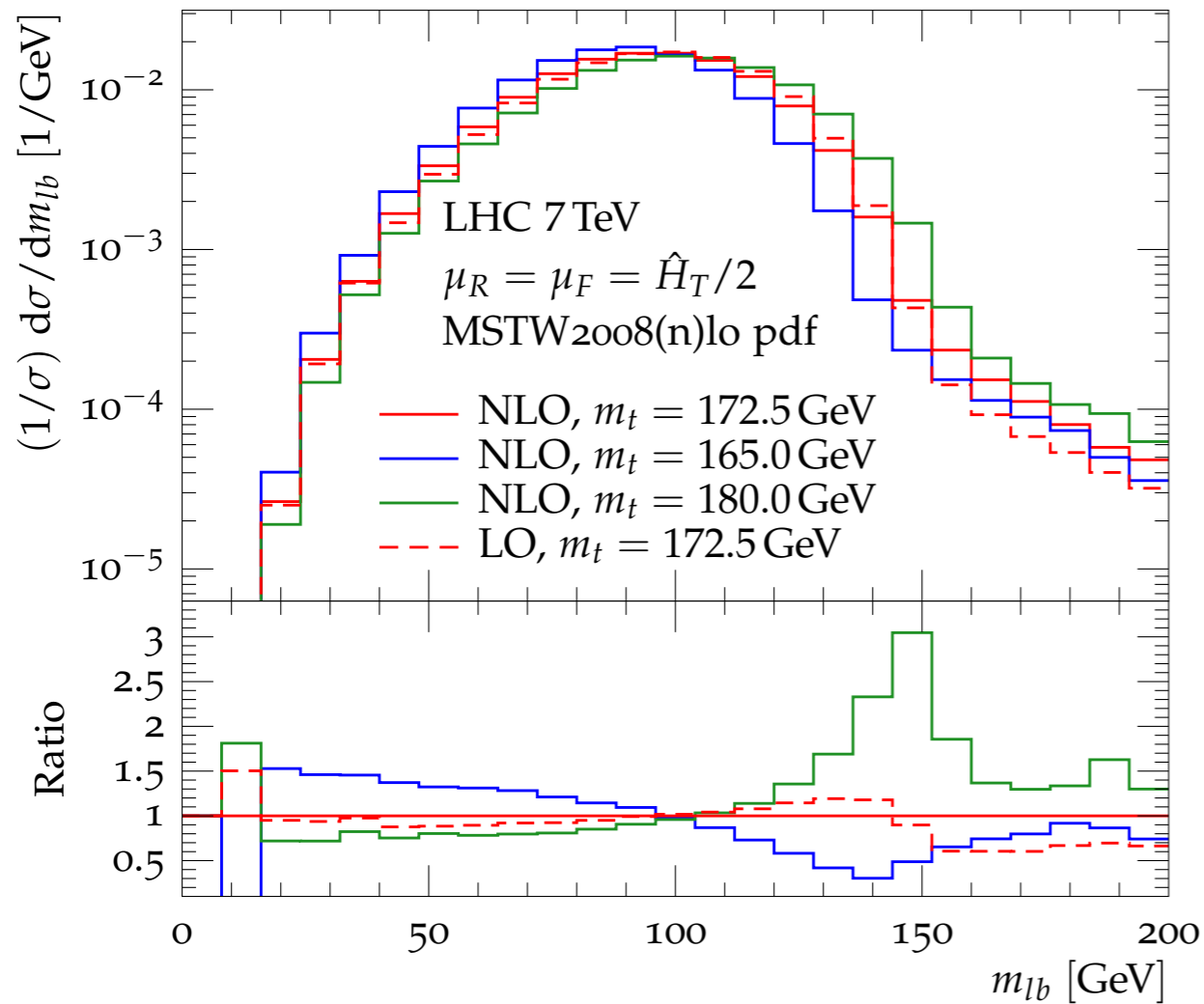
top-quark mass: crucial SM input parameter



- top-mass measurements at the LHC via combination of different strategies:
 - total x-section, $t\bar{t}$ +jet, kinematic reconstruction, kinematic edges,....
- many techniques rely on kinematic information of top decay products
 - ➔ need realistic MC modelling

kinematic top-quark mass measurements: theory

[Heinrich, Maier, Nisius, Schlenk, Winter; '14]



- m_{lb} is straightforward to measure and shows strong dependence on top mass
- off-shell and NLO effects crucial for precise modelling of shape at the edge

Setup

$$\begin{aligned}
 m_Z &= 91.188 \text{ GeV}, & \Gamma_Z &= 2.441 \text{ GeV}, & G_\mu &= 1.16585 \times 10^{-5} \text{ GeV}^{-2} \\
 m_W &= 80.419 \text{ GeV}, & \Gamma_W &= 2.048 \text{ GeV}, \\
 m_H &= 125 \text{ GeV}, & \Gamma_H &= 4.03 \times 10^{-3} \text{ GeV}, \\
 m_t &= 172.5 \text{ GeV}, & \Gamma_t &= 1.329 \text{ GeV}, \\
 m_b &= 4.75 \text{ GeV}.
 \end{aligned}$$

Complex-mass-scheme: $\mu_i^2 = M_i^2 - i\Gamma_i M_i$ for $i = W, Z, t, H$

$$\sin^2 \theta_W^2 = 1 - \cos^2 \theta_W^2 = 1 - \frac{\mu_W^2}{\mu_Z^2}$$

For $t\bar{t}$ resonance histories: $\mu_R = \mu_F = \left[(m_t^2 + p_{T,t}^2) (m_{\bar{t}}^2 + p_{T,\bar{t}}^2) \right]^{\frac{1}{4}}$

For Z resonance histories: $\mu_R = \mu_F = \frac{\sqrt{p_Z^2}}{2}$

PDFs: MSTW2008NLO

$t\bar{t}$ cuts: at least one b- and one \bar{b} -jet with $p_T^j > 30 \text{ GeV}$, $|\eta^j| < 2.5$

$$p_T^l > 20 \text{ GeV}, \quad |\eta^l| < 2.5, \quad p_T^{\text{miss}} > 20 \text{ GeV}$$

Resonance histories

This approach is rigorous up to the point that assignment of resonance histories requires a prescription.

Idea: **define resonance histories according to well defined NWA limit (valid to all orders)!**

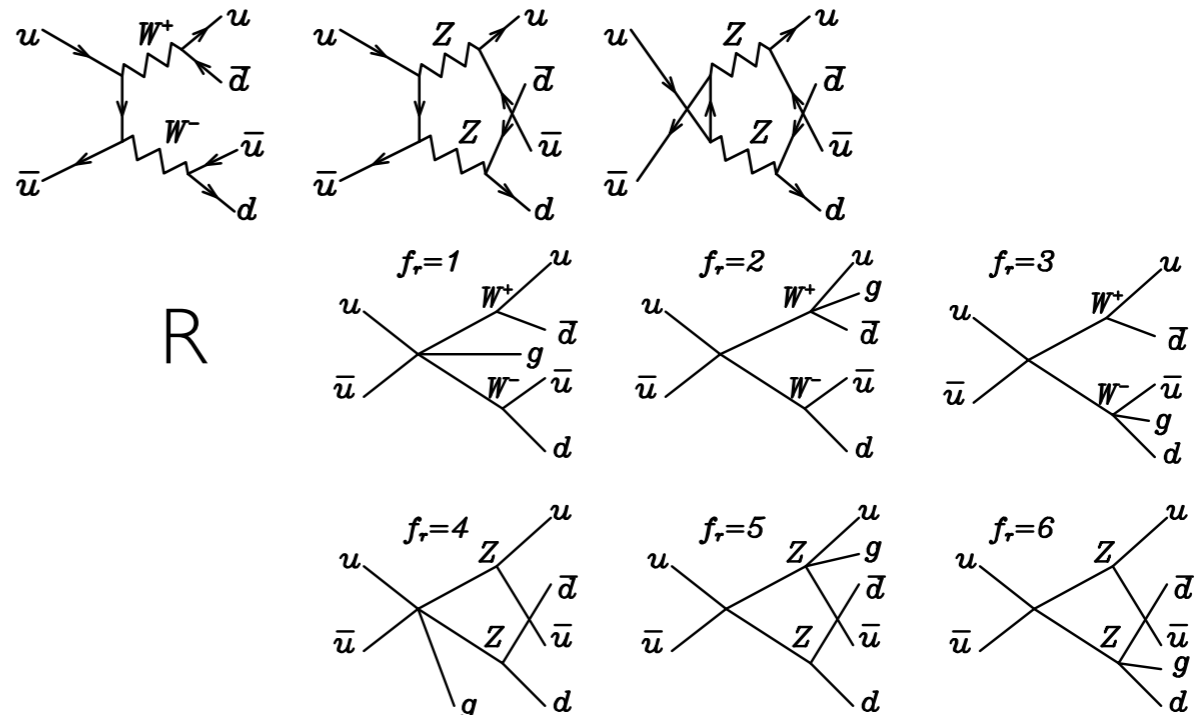
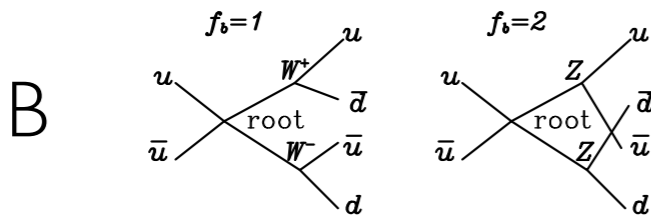
Project onto these resonance histories f_b and f_r based on kinematic proximity:

$$B_{F_b} = \sum_{f_b \in T(F_b)} B_{f_b}, \quad B_{f_b} = \Pi_{f_b} B_{F_b}$$

$$\Pi_{f_b} = \frac{P^{f_b}}{\sum_{f'_b \in T(F_b(f_b))} P^{f'_b}}, \quad P^{f_b} = \prod_{i \in \text{Nd}(f_b)} \frac{M_i^4}{(s_i - M_i^2)^2 + \Gamma_i^2 M_i^2}$$

(similar for R: separation into resonance structures and *compatible* FKS singular regions)

Example: $u\bar{u} \rightarrow u\bar{d}\bar{u}d$ @ $\mathcal{O}(\alpha^4)$



Efficiency study

		resonance aware	resonance unaware
NLO cross section	rel. accuracy (*)	0,11%	0,79%
efficiency of generation of radiation	vetos per event	750	15000
speed of event generation	events per hour	1500	200

⇒ factor of ~7 improvement in convergence/efficiency/speed!

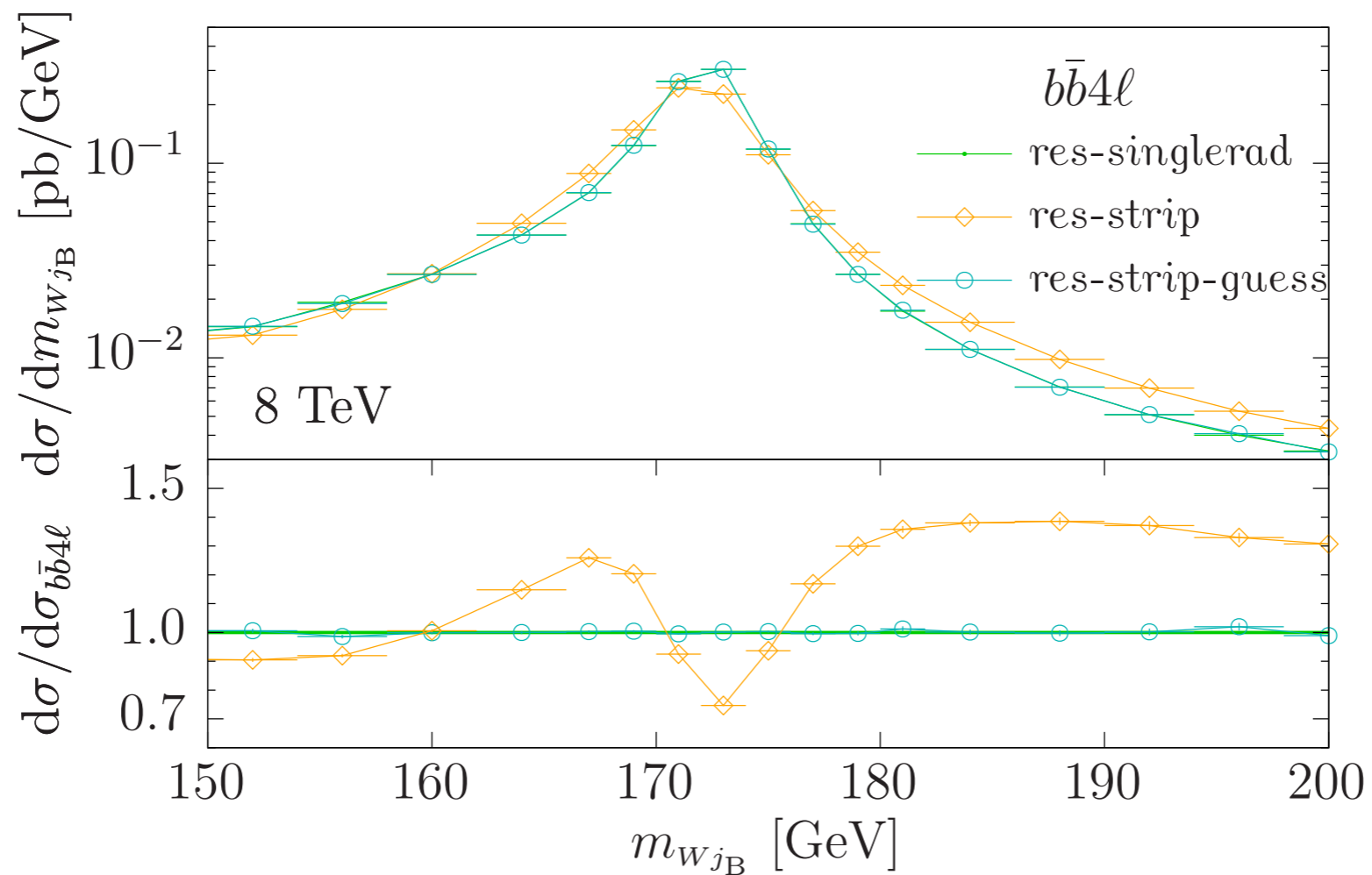
(*) NLO POWHEG setup

- stage 1: ncalls=80k, itmx=2
- stage 2: ncalls=100k, itmx=4
- nrun = 64

(typical setup for small cluster/blade)

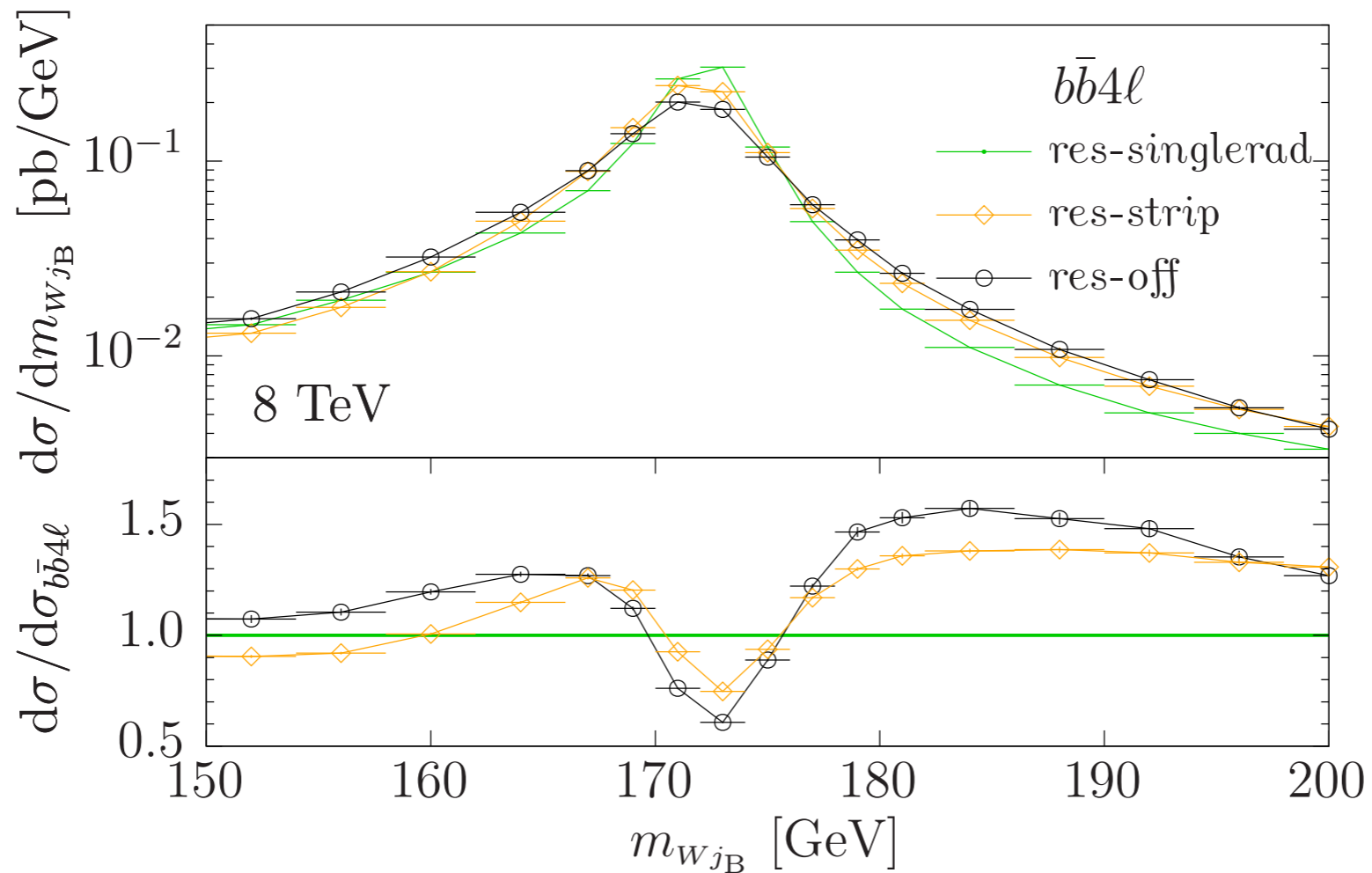
Kinematic guess

- ▶ res-singlerad: resonance aware matching & single-radiation scheme
- ▶ res-strip: resonance aware matching, but resonance information not passed to PS
- ▶ res-strip-guess: resonance aware matching, resonance information first stripped and then guessed (based on kinematic proximity) before passing to PS



Impact of PS momentum reshuffling

- ▶ res-singlerad: resonance aware matching & single-radiation scheme
- ▶ res-strip: resonance aware matching, but resonance information not passed to PS
- ▶ res-off: resonance unaware matching



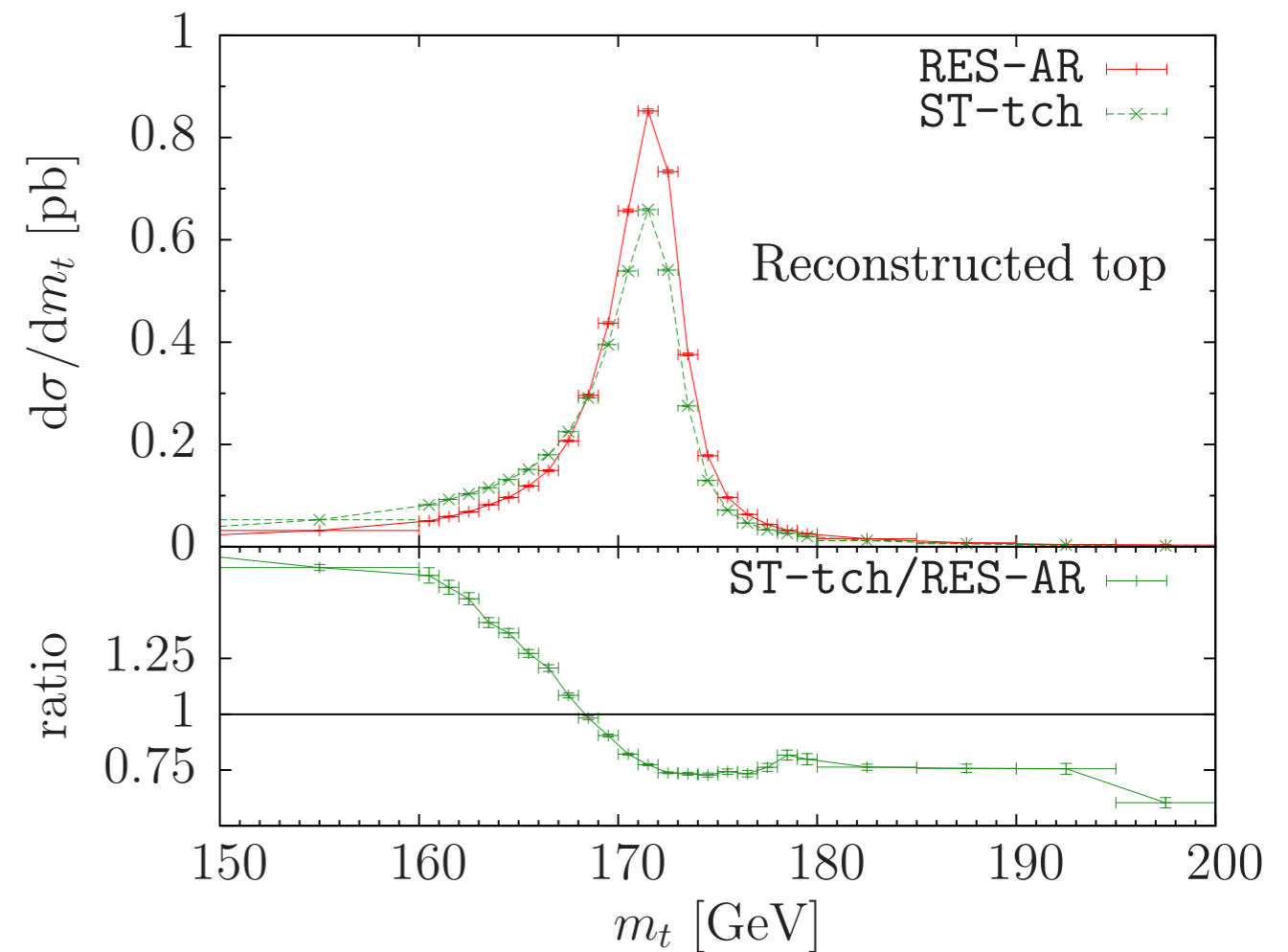
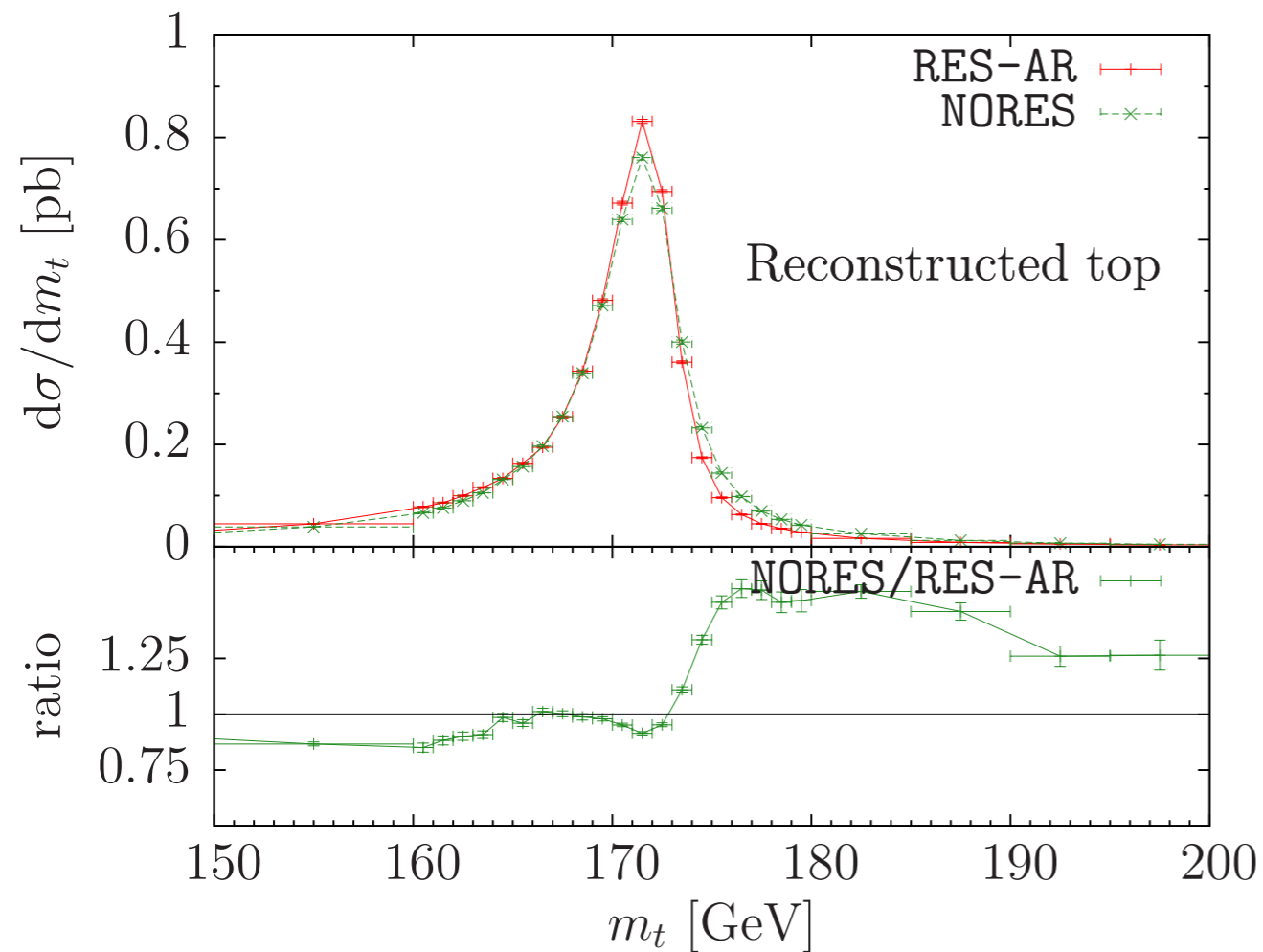
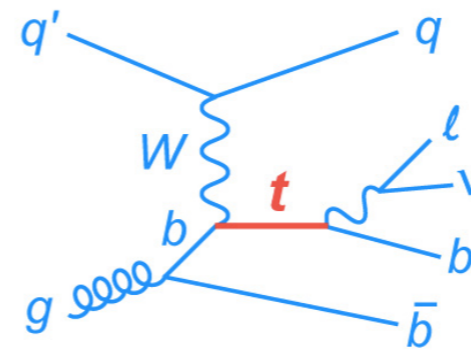
⇒ res-strip in-between res-singlerad and res-off

⇒ both effects important:

- I) first emission governed by resonance preserving R/B
- II) PS reshuffling preserves the resonance masses

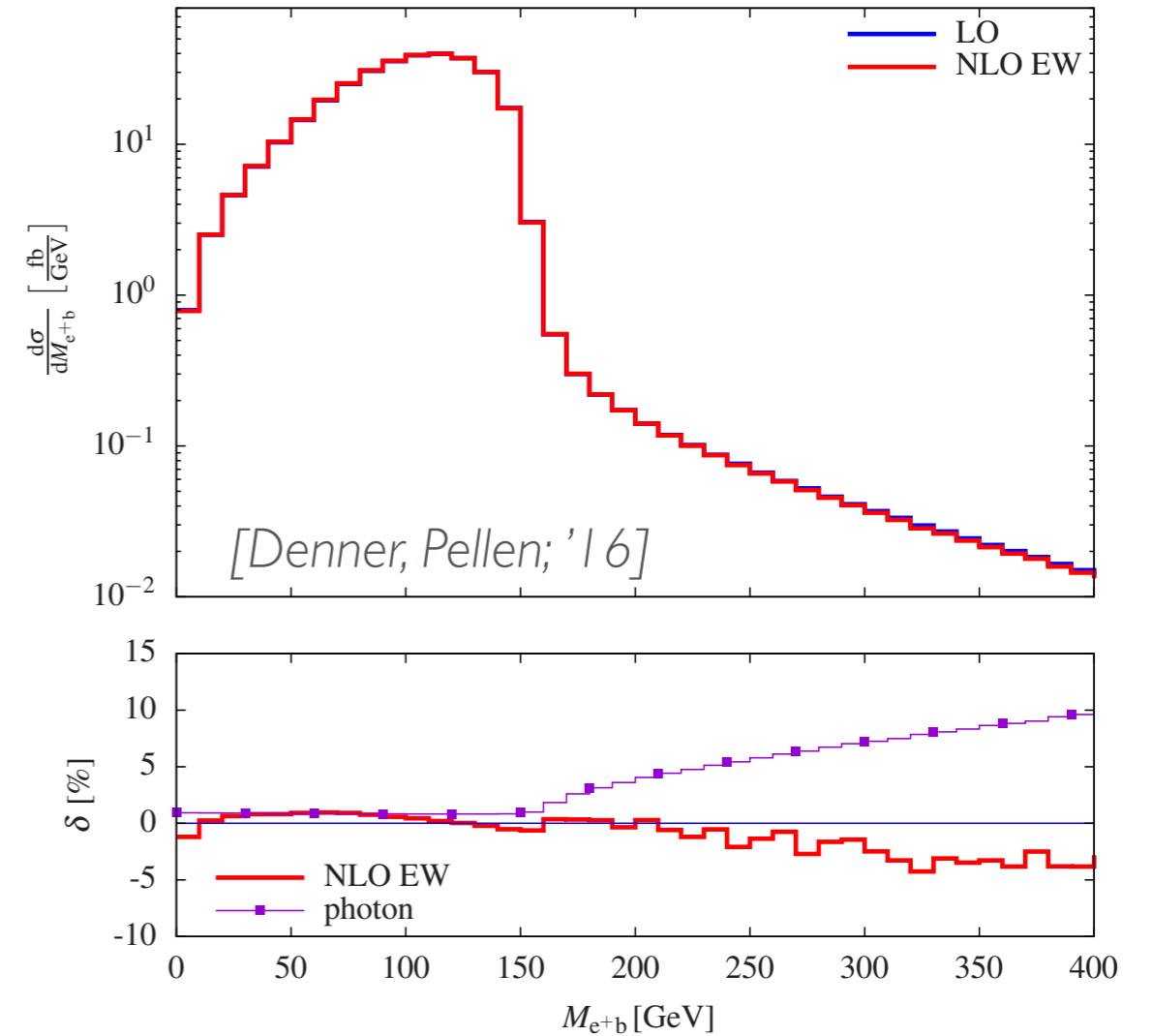
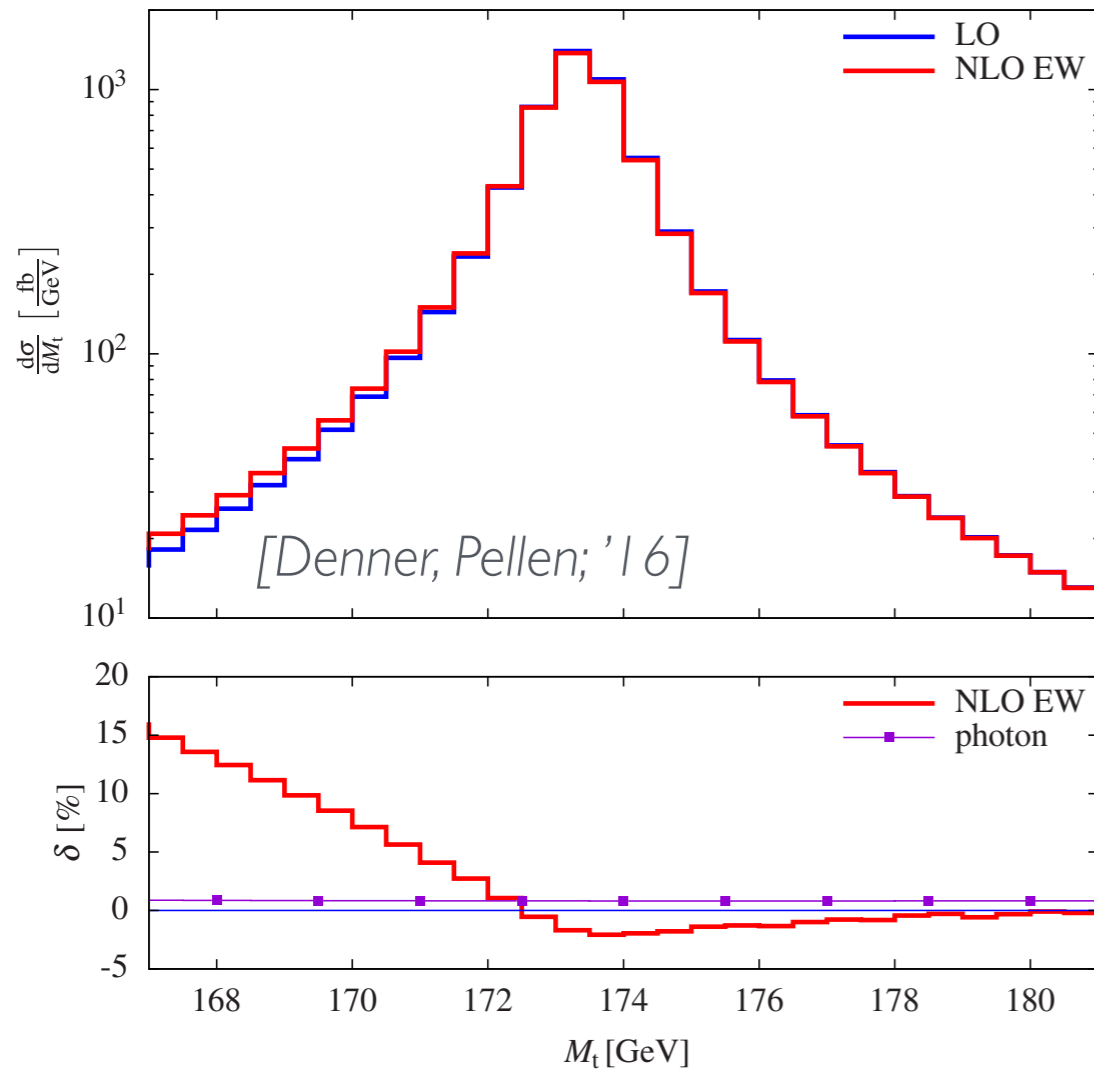
Single-top t-channel NLO+PS

[Ježo, Nason; '15]



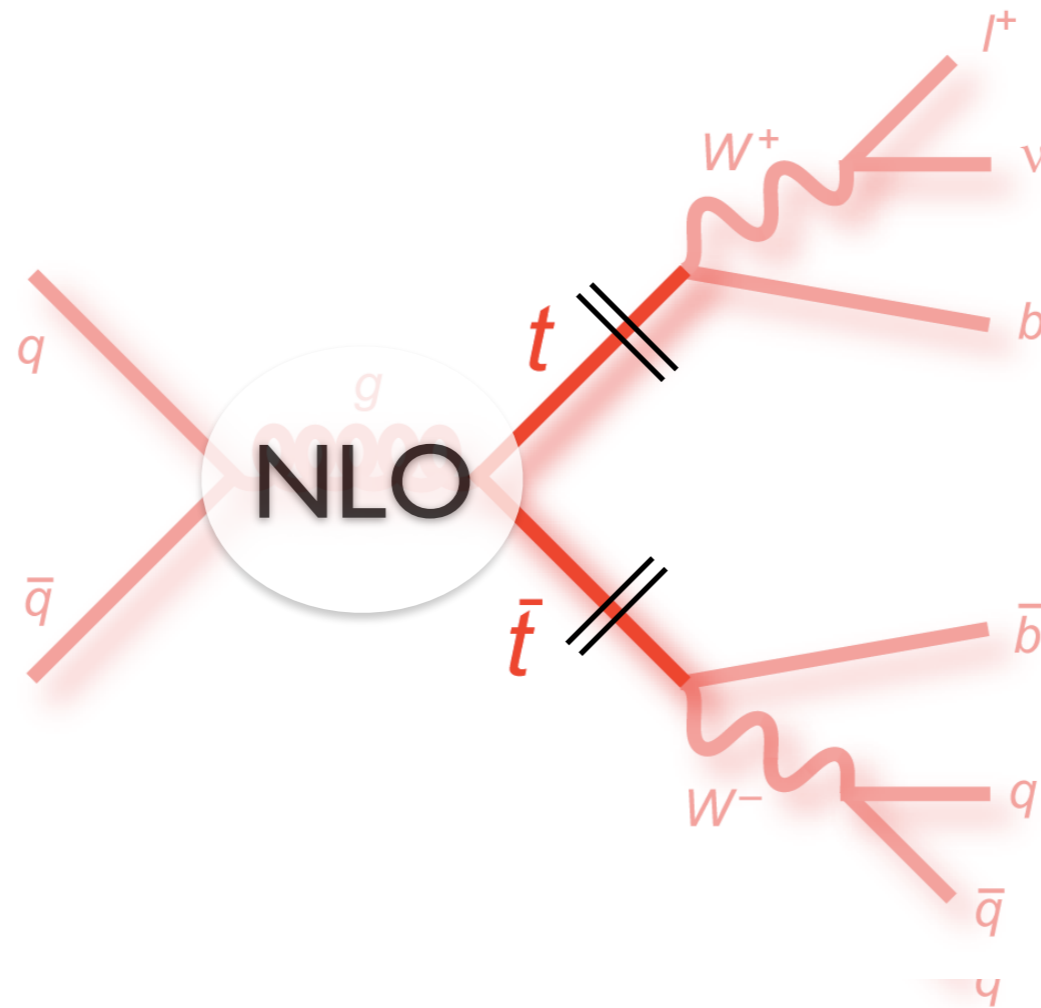
- significant shape distortions in resonance unaware calculation and with respect to on-shell top calculation [Alioli, Nason, Oleari, Re; '09]

NLO EW



- NLO EW $\sim 5\%$ around top peak, up to 15% below the peak
- sizeable photon-induced contributions in m_{lb} (using NNPDF2.3QED)

Top-pair production and decay



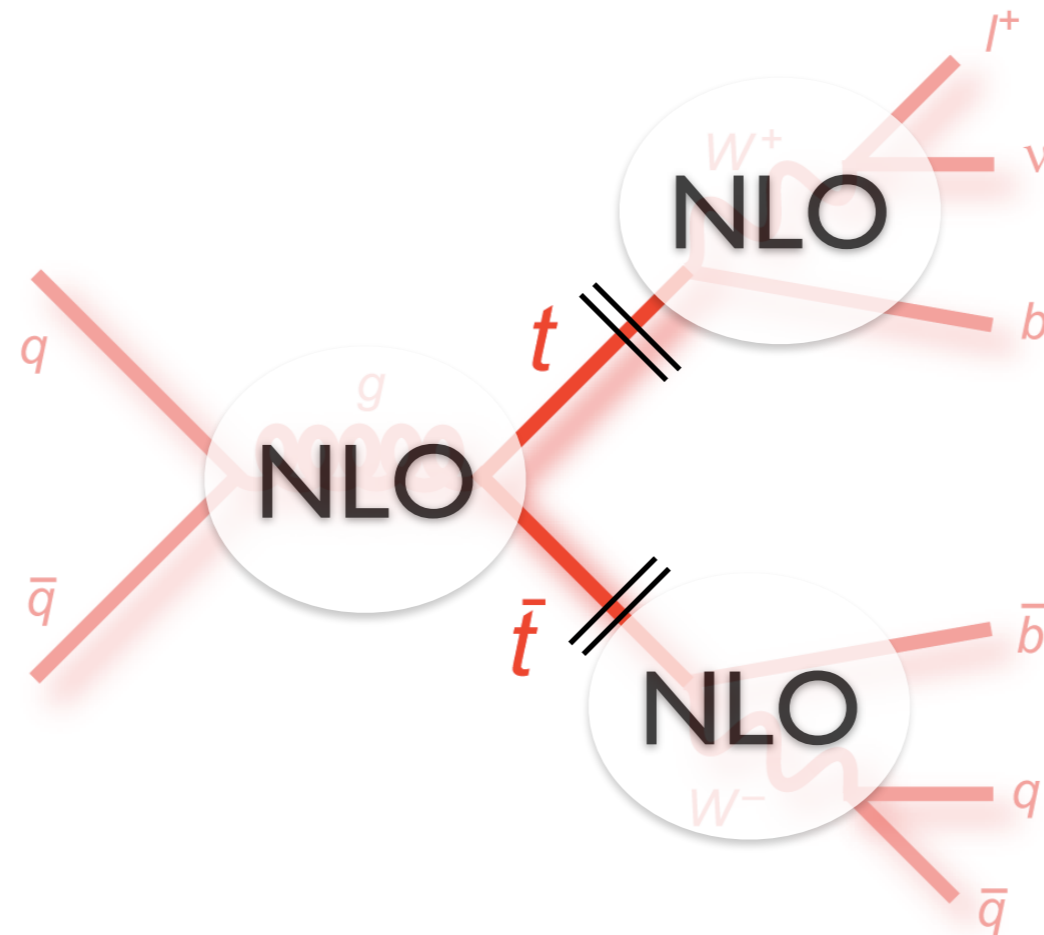
NLO QCD [Bernreuther, Brandenburg, Si; '04, Melnikov, Schulze; '09, Campbell, Ellis; '15] [Bevilacqua, Czakon, van. Hameren, Papadopoulos, Worek; '11, Denner, Dittmaier, Kallweit, Pozzorini; '11+'12, Heinrich, Maier, Nisius, Schlenk, Winter; '14, Frederix '14, Cascioli, Kallweit, Maierhofer, Pozzorini; '14]

NNLO [Czakon, Fiedler, Mitov; '13, Czakon, Heymes, Mitov; '16]

NLO EW [Beenakker, Denner, Hollik, Mertig, Sack, Wackerroth; '94, Bernreuther, Fuecker, Si; '06+'08, Kühn, Scharf, Uwer; '07,+'15, Hollik, Pagani; '07, Pagani, Tsinikos, Zaro; '16] [Bernreuther, Si; '10] [Denner, Pellen '16]

NLO QCD+PS [Frixione, Nason, Webber, '03, Frixione, Nason, Ridolfi; '07] [Campbell, Ellis, Nason, Re, '15] [Garzelli, Kardos, Trocsanyi; '14]

Top-pair production and decay



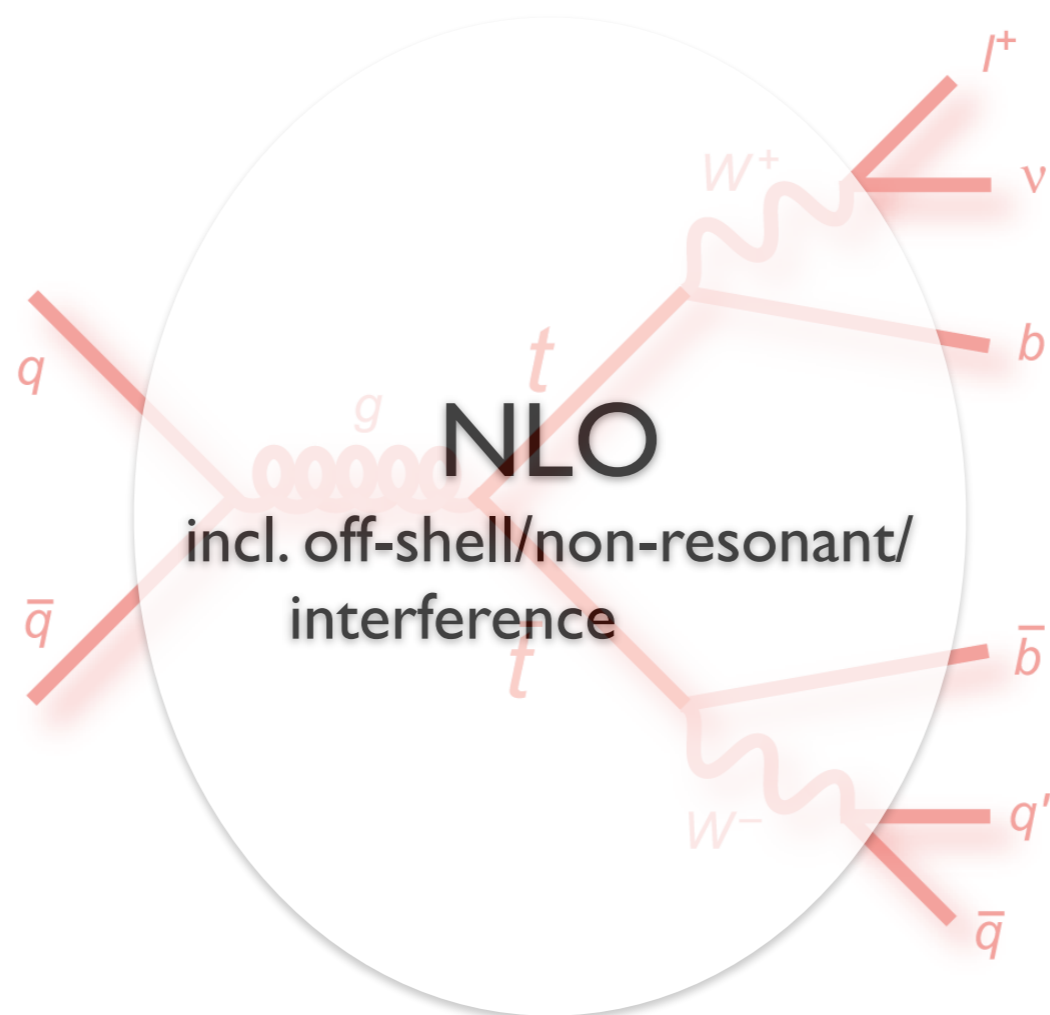
NLO QCD [Bernreuther, Brandenburg, Si; '04, Melnikov, Schulze; '09, Campbell, Ellis; '15] [Bevilacqua, Czakon, van. Hameren, Papadopoulos, Worek; '11, Denner, Dittmaier, Kallweit, Pozzorini; '11+'12, Heinrich, Maier, Nisius, Schlenk, Winter; '14, Frederix '14, Cascioli, Kallweit, Maierhofer, Pozzorini; '14]

NNLO [Czakon, Fiedler, Mitov; '13, Czakon, Heymes, Mitov; '16]

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NLO QCD+PS [Frixione, Nason, Webber, '03, Frixione, Nason, Ridolfi; '07] [Campbell, Ellis, Nason, Re, '15] [Garzelli, Kardos, Trocsanyi; '14]