

# OFF-SHELL TOP QUARKS WITH A JET: A COMPREHENSIVE STUDY AT NLO QCD

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in collaboration with G. Bevilacqua, H. B. Hartanto, M. Worek  
DESY Hamburg, 29 September 2016



based on

[*PRL* 116 (2016) 052003]  
[*arXiv:1609.01659*]

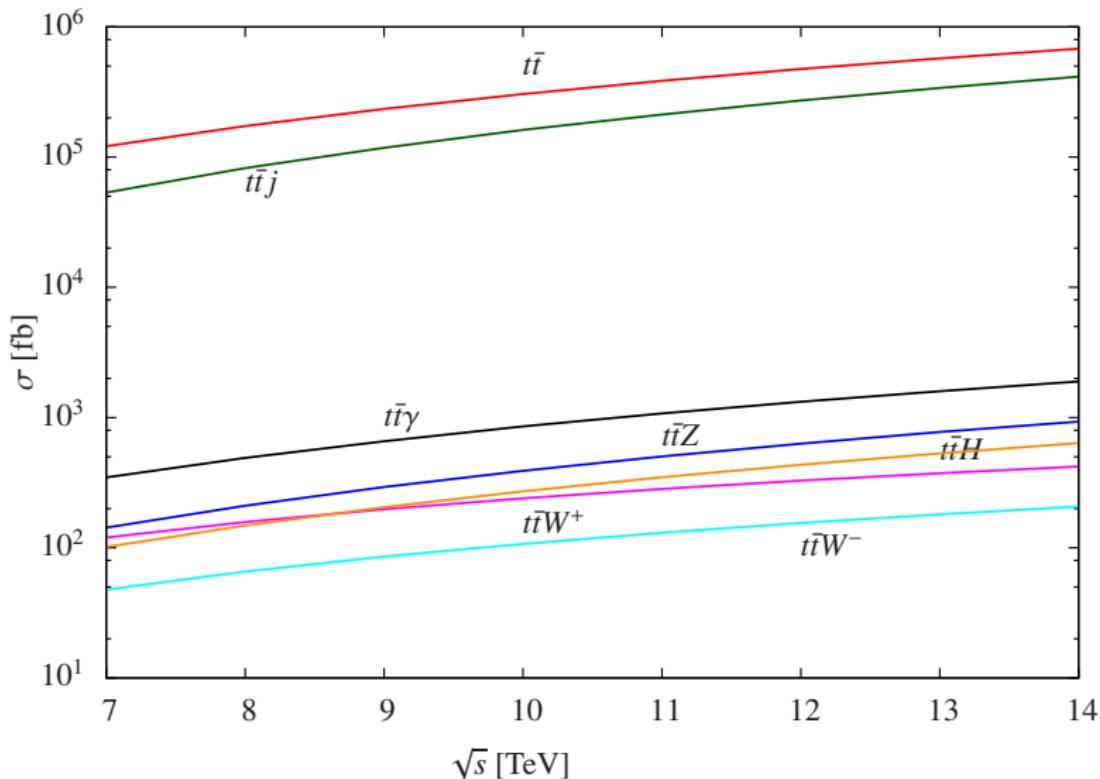
# OUTLINE

Next-to-Leading Order QCD predictions for

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} j + X$$

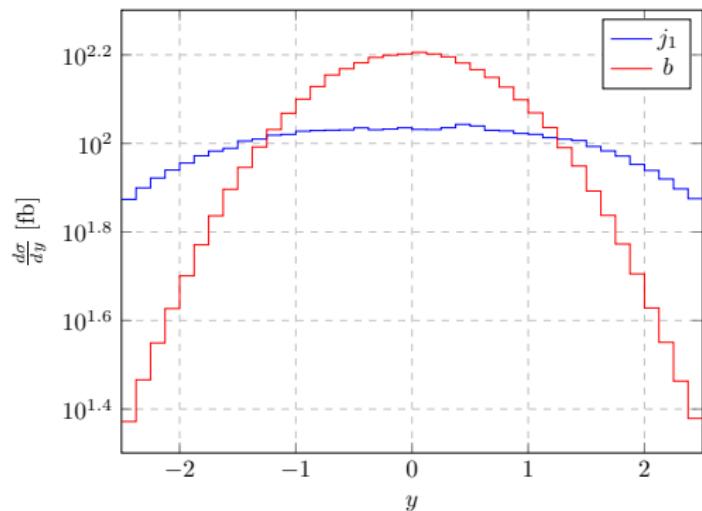
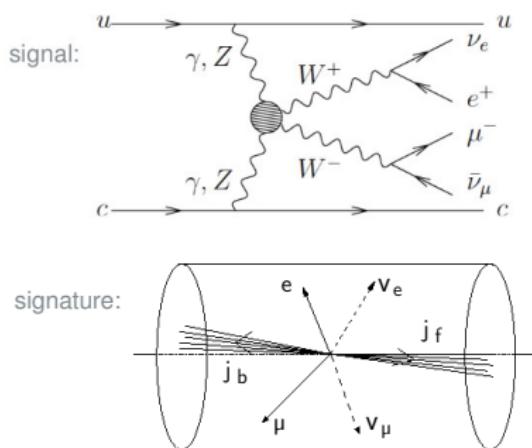
1. Motivation for  $t\bar{t}j$  process
2. Off-shell effects in top-quark pair production
3. Complete off-shell effects with HELAC-NLO for  $t\bar{t}j$
4. Conclusions

# ASSOCIATED $t\bar{t}$ PRODUCTION



# $t\bar{t}j$ AS A BACKGROUND

- Background for SM Higgs production in VBF:  $qq \rightarrow Hqq \rightarrow W^+W^-qq$
- VBF requires two tagged jets:  $\Delta y_{ij} = |y_i - y_j| > 4$  and  $y_i \times y_j < 0$



also background for BSM searches with  $\ell_1^+\ell_2^- + MET + jets$  signature

# $t\bar{t}j$ AS A SIGNAL

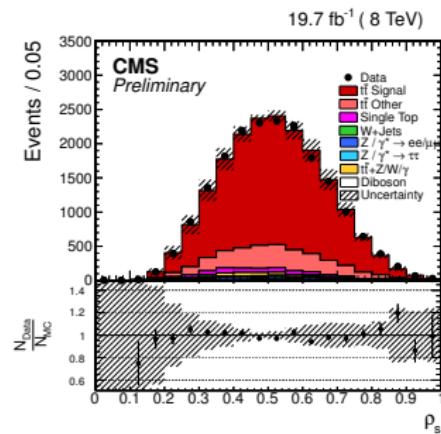
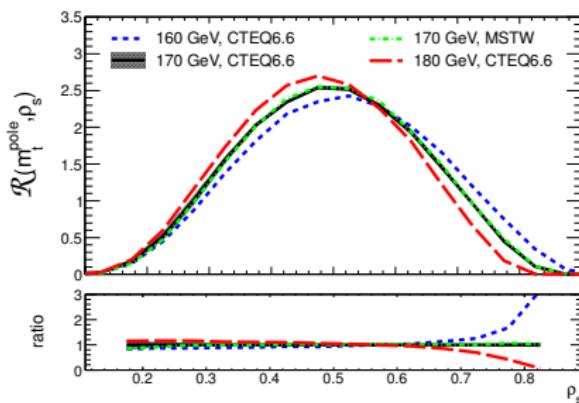
An alternative method for the top-quark mass extraction

[Alioli et al '13]

$$\mathcal{R}(m_t, \rho_s) = \frac{1}{\sigma_{t\bar{t}j}} \frac{d\sigma_{t\bar{t}j}}{d\rho_s(m_t, \rho_s)}$$

$$\rho_s = \frac{2m_0}{\sqrt{s_{t\bar{t}j}}}$$

- $\mathcal{R}(m_t, \rho_s)$  shape is sensitive to  $m_t$
- $t\bar{t}j$  has higher sensitivity than  $t\bar{t}$
- 7 TeV:  $m_t = (173.7 \pm 2.2)$  GeV [ATLAS '15]
- 8 TeV:  $m_t = (169.9 \pm 3.9)$  GeV [CMS '16]

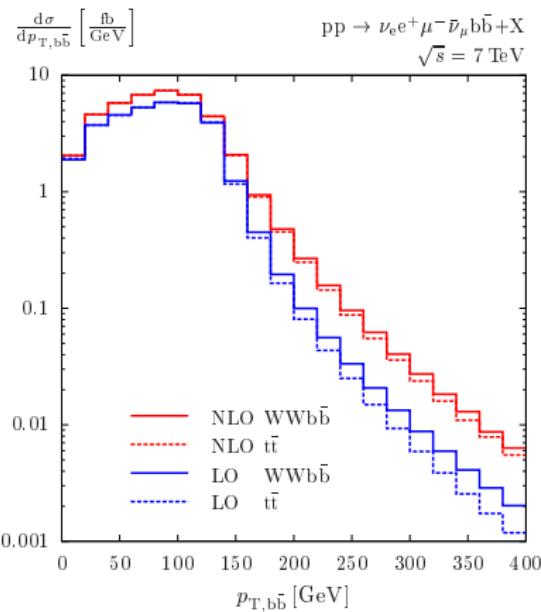


Theoretical and PDF uncertainties affect the  $m_t$  extraction

# TOP-QUARK OFF-SHELL EFFECTS - I

Contributions dropped in the NWA are suppressed by  $\Gamma_t/m_t \sim 1\%$ .

- True for sufficiently inclusive observables
- Larger impact on differential distributions



For  $\sigma_{\text{tot}}$  at the % level ( $t\bar{t}, t\bar{t}j, t\bar{t}H$ )

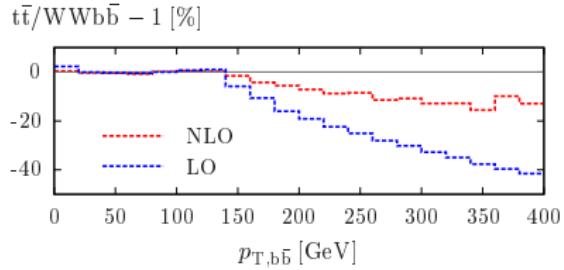
[A. Denner et al '11, '12, '15]

[G. Bevilacqua et al '11, '16]

[R. Frederix '14]

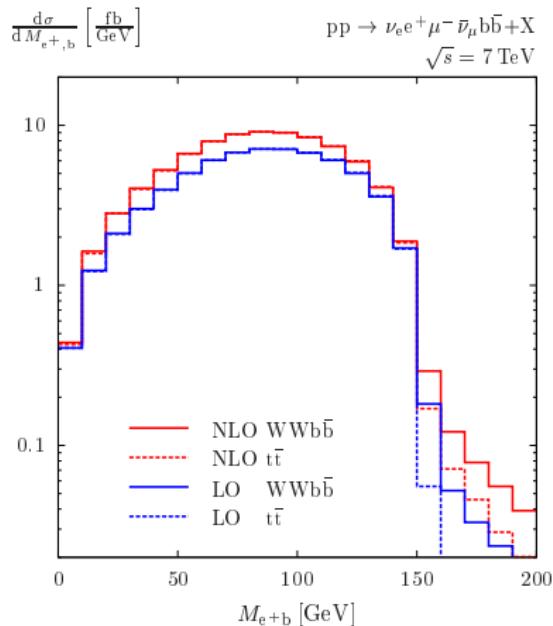
[F. Cascioli et al '14]

[G. Heinrich et al '14]



[A. Denner, S. Dittmaier, S. Kallweit, S. Pozzorini, M. Schulze '12]

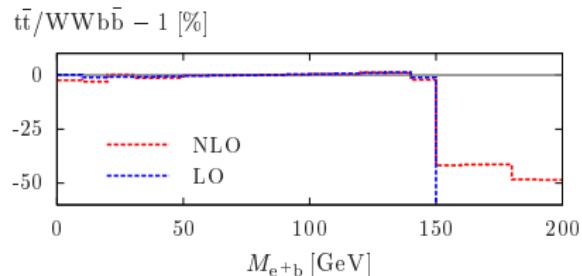
# TOP-QUARK OFF-SHELL EFFECTS - II



- If both top and W decay on-shell  
 $\rightarrow$  end-point given by sharp cut

$$M_{\ell b} = \sqrt{m_t^2 - m_W^2} \approx 152 \text{ GeV}$$

- Additional radiation & off-shell effects introduce smearing



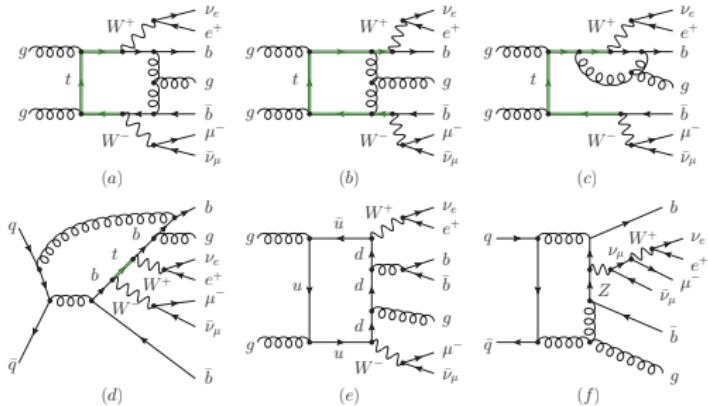
[A. Denner, S. Dittmaier, S. Kallweit, S. Pozzorini, M. Schulze '12]

$m_t$  measurement based on  $M_{\ell b} \rightarrow m_t$  extraction is very sensitive to template (LO/NLO and Full/NWA). [Heinrich, Maier, Nisius, Schlenk, Winter '14]

# TOP-QUARK OFF-SHELL EFFECTS IN $t\bar{t}j$

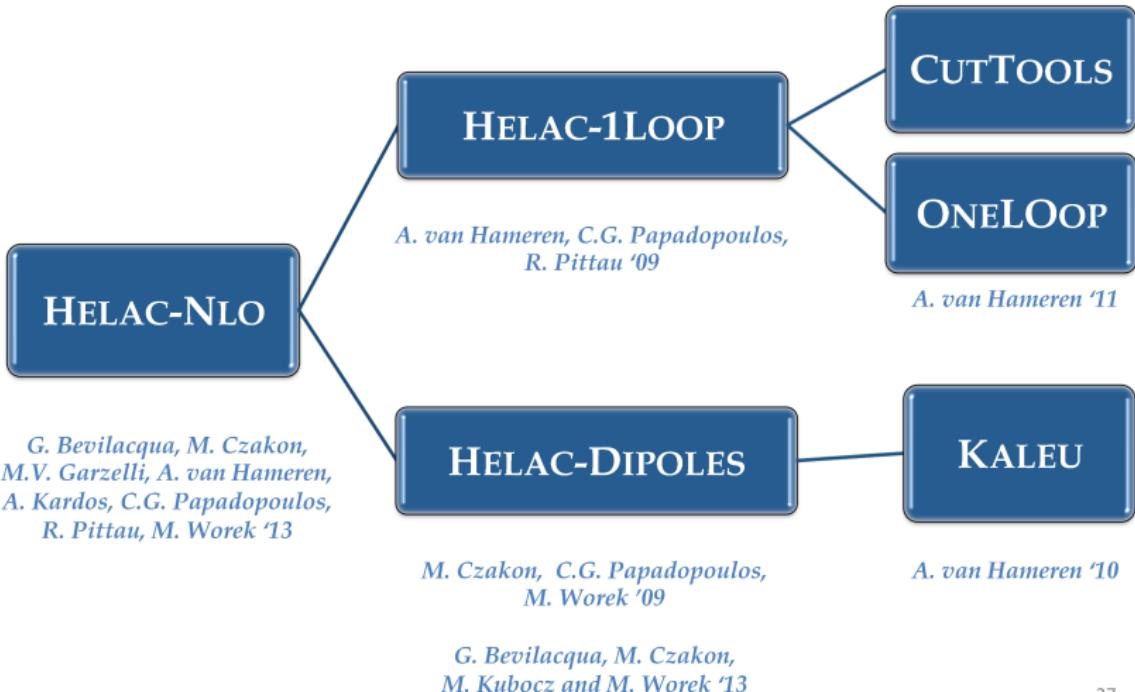
$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} j + X$$

- $t\bar{t}j$  production at  $\mathcal{O}(\alpha_s^4 \alpha^4)$  in the di-lepton decay channel
- $2 \rightarrow 5$  QCD process ( $W^+ W^- b\bar{b} j$ )
- **$gg$  initial state** is the most complicated production channel
  - LO: 508
  - Real: 4447
  - Virtual: 39180  $\rightarrow$  1155 hexagons and 120 heptagons



# HELAC-NLO

*G. Ossola, C.G. Papadopoulos,  
R. Pittau '08*



# SETUP FOR LHC 13 TeV - I

A comprehensive study for off-shell  $pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}j + X$  production:

- fixed vs. dynamical scale, independent  $\mu_R$  and  $\mu_F$  variations
- PDF uncertainties (different PDFs, internal PDF uncertainty)  
⇒ very time consuming and CPU intensive
- ⇒ Extend HELAC-NLO functionality to produce NTuple

Fixed scale:  $\mu_0 = m_t$

Dynamical scale:  $\mu_0 = E_T/2$  and  $\mu_0 = H_T/2$ , with

$$E_T = \sqrt{p_T^2(t) + m_t^2} + \sqrt{p_T^2(\bar{t}) + m_t^2}$$

$$H_T = \sum_i p_T(i) + \not{p}_T, \quad i = \{e^+, \mu^-, J_b, J_{\bar{b}}, j_1\}$$

PDF sets: CT14nlo, MMHT14, NNPDF3.0

Scale uncertainty from envelopes obtained from the following grid

$$\left( \frac{\mu_R}{\mu_0}, \frac{\mu_F}{\mu_0} \right) = \{(0.5, 0.5), (0.5, 1), (1, 0.5), (1, 1), (1, 2), (2, 1), (2, 2)\}$$

# SETUP FOR LHC 13 TeV - II

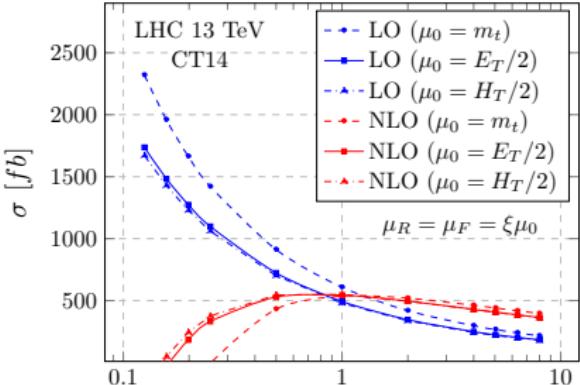
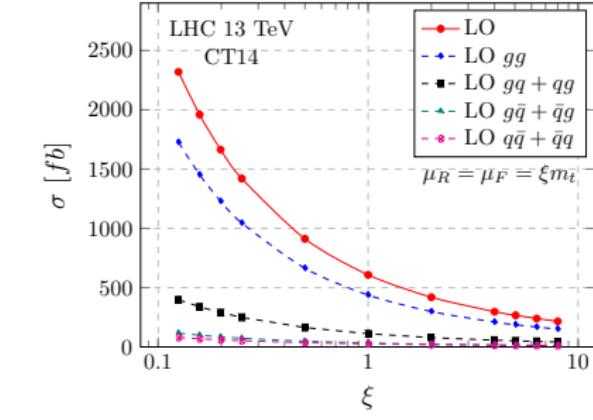
- SM parameters:

$$\begin{aligned} G_F &= 1.16637 \cdot 10^{-5} \text{ GeV}^{-2}, & m_t &= 173.2 \text{ GeV}, \\ m_W &= 80.399 \text{ GeV}, & \Gamma_W &= 2.09875 \text{ GeV}, \\ m_Z &= 91.1876 \text{ GeV}, & \Gamma_Z &= 2.50848 \text{ GeV}, \\ \Gamma_t^{LO} &= 1.47834 \text{ GeV}, & \Gamma_t^{NLO} &= 1.35146 \text{ GeV}, \end{aligned}$$

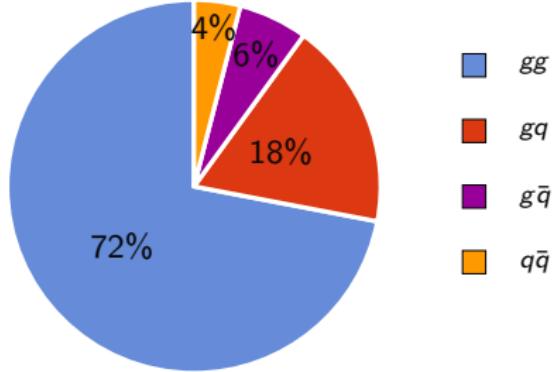
- Light quarks (also bottom) and leptons are massless
- Bottom induced channels are neglected (0.1% at LO)
- Final state: exactly 2 b-jets, at least 1 light jet,  
2 charged leptons, missing  $p_T$
- Jets: partons with  $|\eta| < 5$ , anti- $k_T$ ,  $\Delta R = 0.5$
- Cuts:

$$\begin{aligned} p_{T,I} &> 30 \text{ GeV}, & p_{T,j} &> 40 \text{ GeV}, & \not{p}_T &> 40 \text{ GeV}, \\ \Delta R_{jj} &> 0.5, & \Delta R_{II} &> 0.4, & \Delta R_{lj} &> 0.4, \\ |y_I| &< 2.5, & |y_j| &< 2.5, \end{aligned}$$

# SCALE DEPENDENCE



## LO contributions




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$\mu_0 = m_t$	$K = 0.88$	$-12\%$
$\mu_0 = E_T/2$	$K = 1.10$	$+10\%$
$\mu_0 = H_T/2$	$K = 1.15$	$+15\%$

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# THEORETICAL UNCERTAINTIES

- Same PDF, different scales

$$\sigma^{NLO}(CT14, \mu_0 = m_t) = 537.24_{-190.35}^{+10.12} (+2\%) \quad [scales] \text{ fb}$$

$$\sigma^{NLO}(CT14, \mu_0 = E_T/2) = 544.64_{-117.47}^{+2.95} (+1\%) \quad [scales] \text{ fb}$$

$$\sigma^{NLO}(CT14, \mu_0 = H_T/2) = 549.65_{-53.42}^{+10.25} (+2\%) \quad [scales] \text{ fb}$$

$\Rightarrow \mu_0 = H_T/2$  yields smallest uncertainty  $\sim 6\%$  (sym)

- Same scale, different PDFs

$$\sigma^{NLO}(CT14, \mu_0 = H_T/2) = 549.65_{-53.42}^{+10.25} (+2\%) \quad [scales]_{-19.15}^{+18.00} (+3\%) \quad [PDF] \text{ fb}$$

$$\sigma^{NLO}(MMHT14, \mu_0 = H_T/2) = 554.61_{-54.51}^{+10.85} (+2\%) \quad [scales]_{-12.22}^{+12.06} (+2\%) \quad [PDF] \text{ fb}$$

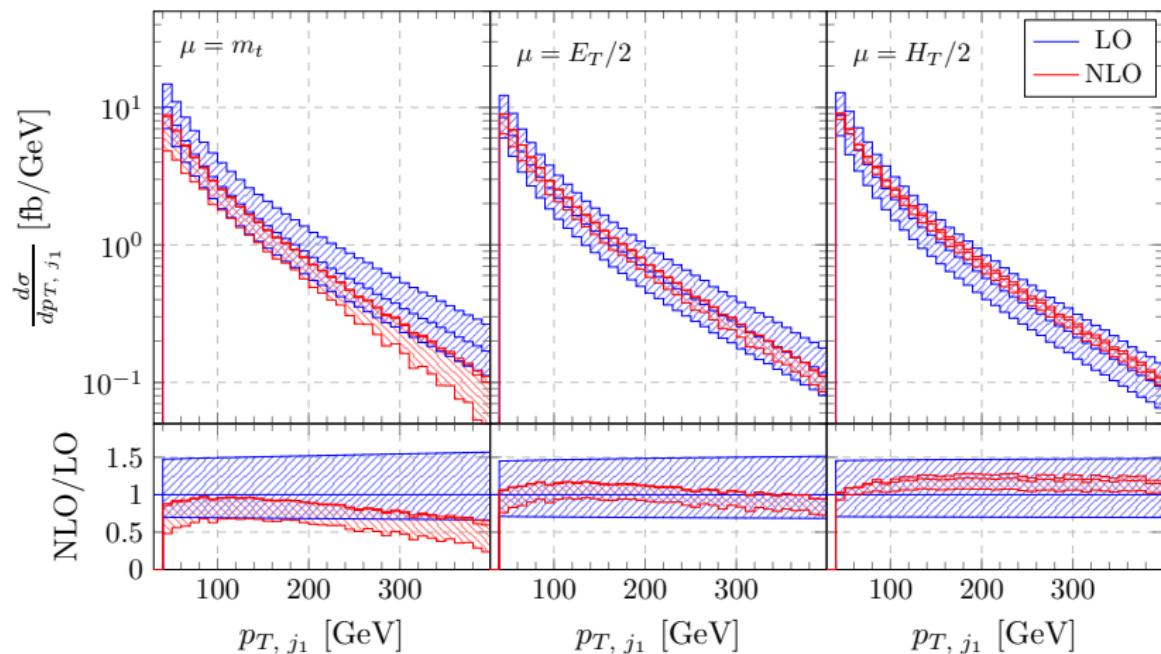
$$\sigma^{NLO}(NNPDF3.0, \mu_0 = H_T/2) = 572.18_{-56.23}^{+11.14} (+2\%) \quad [scales]_{-11.31}^{+11.31} (+2\%) \quad [PDF] \text{ fb}$$

$\Rightarrow$  Scale uncertainty unaffected by PDFs

$\Rightarrow$  PDF uncertainty small  $\sim 2 - 3\%$

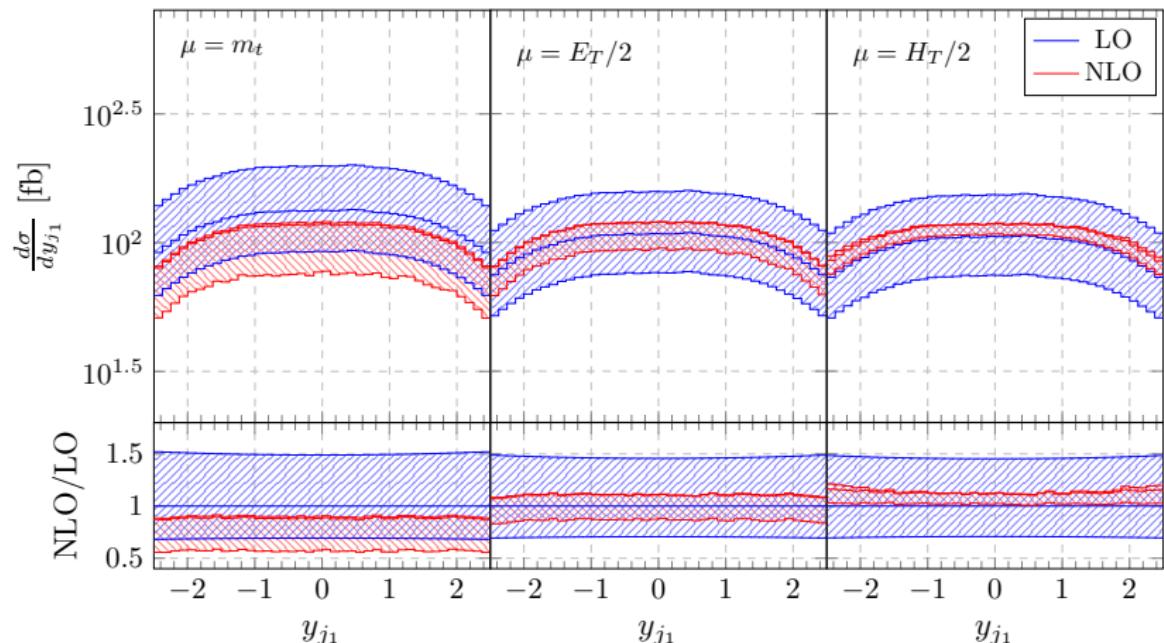
# FIXED VS DYNAMICAL SCALE - I

Transverse momentum of hardest light jet

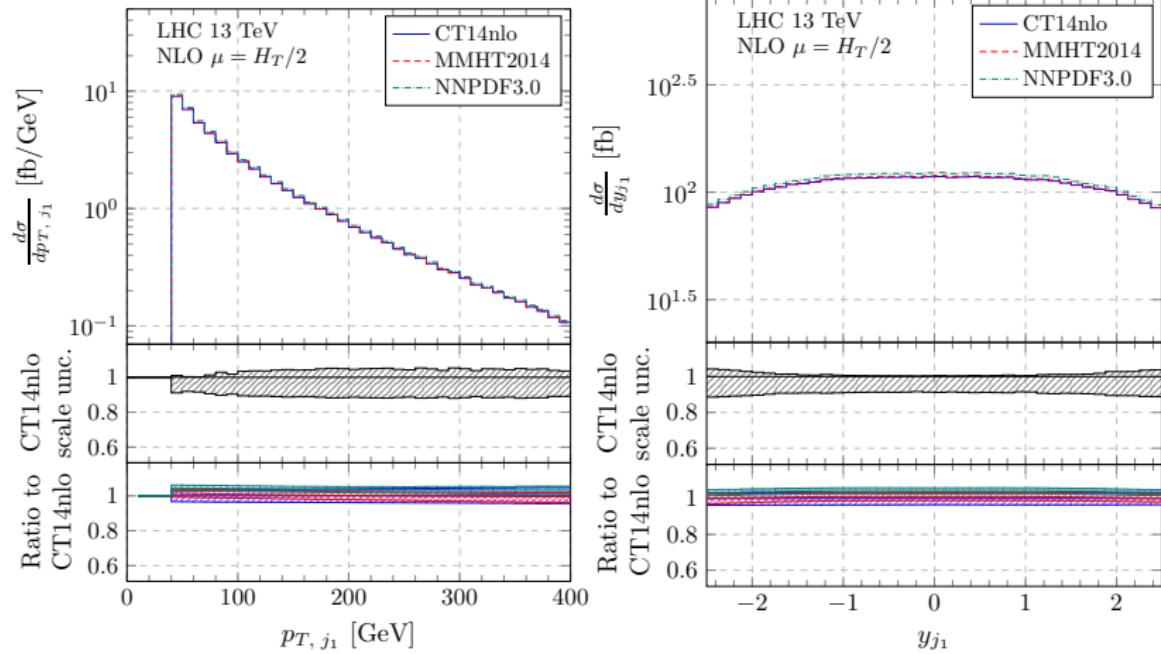


# FIXED VS DYNAMICAL SCALE - II

Rapidity of hardest light jet



# PDF UNCERTAINTIES



Scales  $\sim 10\%$ , PDF CT14  $\sim 5\%$

# CONCLUSIONS

## Summary:

- ✓ First description of  $t\bar{t}j$  with all resonant and non-resonant contributions
- ✓ Comparison of fixed and dynamic scales:  $m_t$ ,  $E_T/2$ ,  $H_T/2$   
⇒  $H_T/2$  gives smaller uncertainty than  $E_T/2$
- ✓ Scale and PDF uncertainties for  $\sigma$  and various  $d\sigma/dX$

## Work in Progress:

- Comparison of NWA vs full off-shell calculation
- Off-shell effects on the top mass extraction ( $m_t$  extraction from  $M_{be^+}$ ,  $\rho$ )

## Future studies:

- ✗ Impact of bottom-quark masses – 4 FS vs. 5 FS

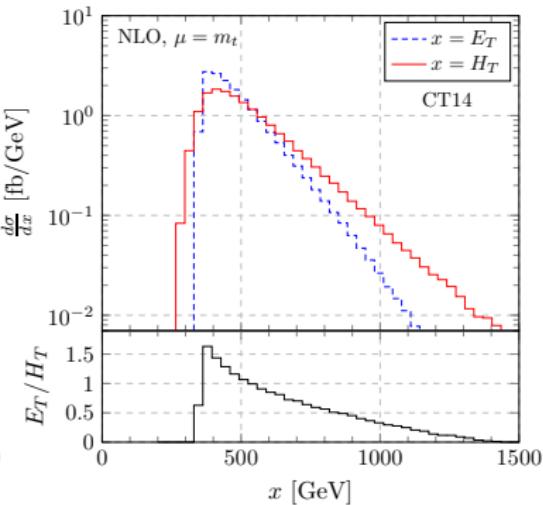
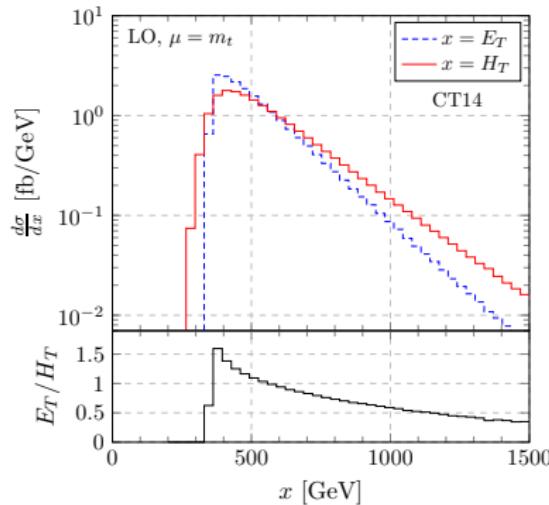
# BACKUP

# HELACNLO - NTUPLES

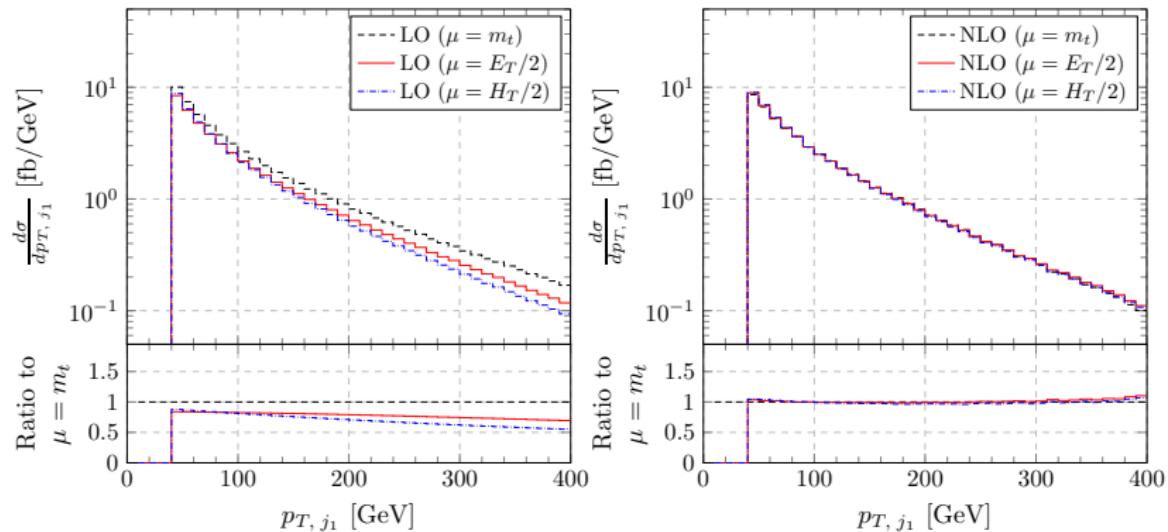
Generated Event samples for  $pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}j + X$  used for reweighting

CONTRIBUTION	NR. OF EVENTS	NR. OF FILES	(AVG) EVENTS/FILE	SIZE
Born	$21 \cdot 10^6$	60	$350 \cdot 10^3$	38 GB
Born + Virtual	$33 \cdot 10^6$	380	$87 \cdot 10^3$	72 GB
Int. dipoles	$80 \cdot 10^6$	450	$178 \cdot 10^3$	160 GB
Real subtracted	$626 \cdot 10^6$	18000	$35 \cdot 10^3$	1250 GB
Total:	$760 \cdot 10^6$	18890	$40 \cdot 10^3$	1520 GB

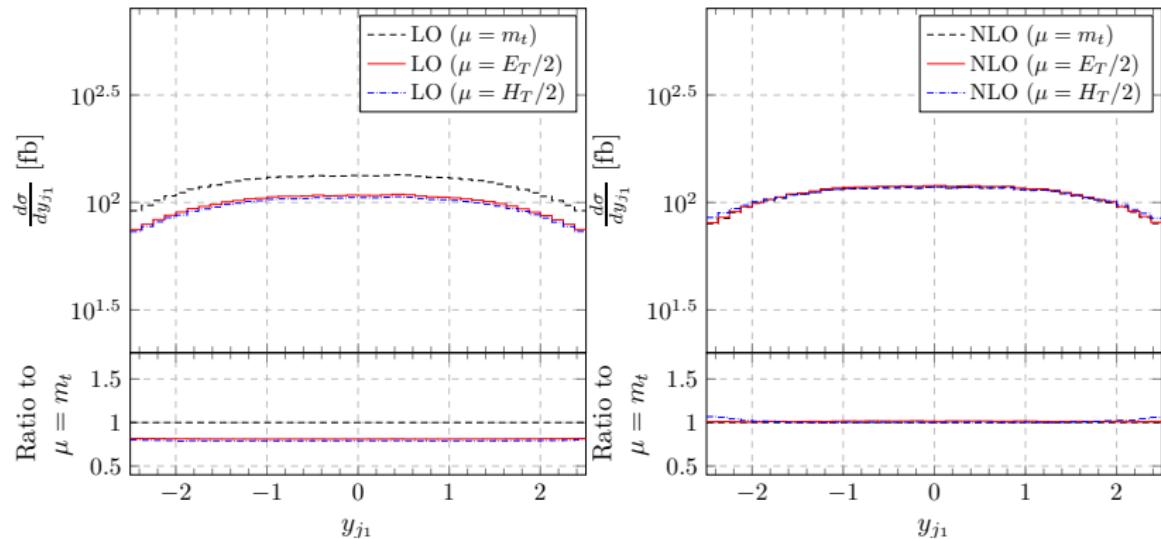
# COMPARISON OF THE DYNAMICAL SCALES



# TRANSVERSE MOMENTUM OF HARDEST LIGHT JET



# RAPIDITY OF HARDEST LIGHT JET



# SCALE DEPENDENCE

