

Hunting the Flavon

Martin Bauer

Based on

[MB, Gemmler, Carena, JHEP 1511, 016 (2015)]

[MB, Gemmler, Carena, 1512.03458]

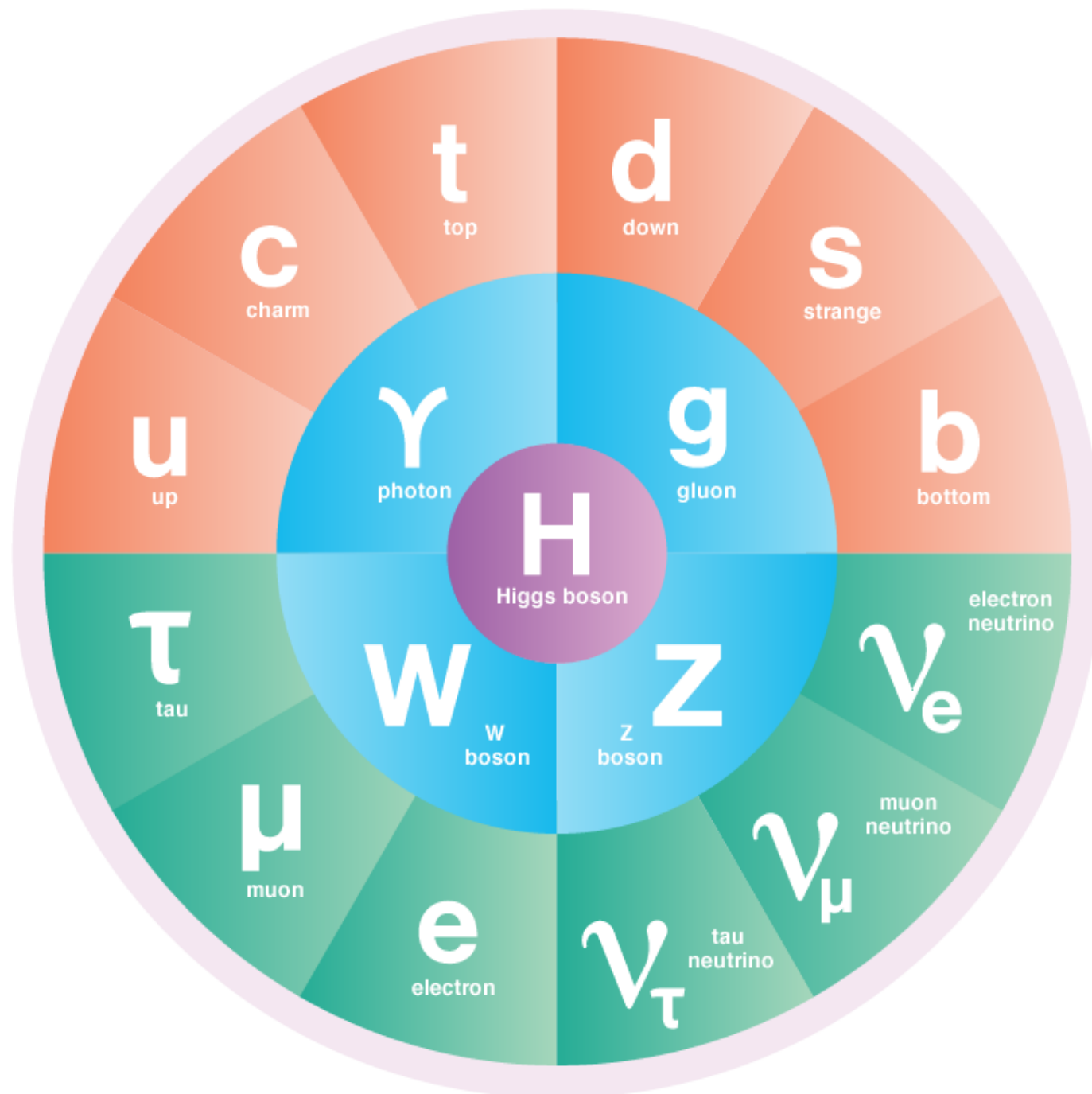
[MB, Schell, Plehn, 1603.06950]



DESY, July 19th, 2016



The Standard Model of Particle Physics



Quarks

Spin $1/2$

Charge $2/3$: Up type

Charge $-1/3$: Down type

Leptons

Spin $1/2$

Charge -1 : e , μ , τ

Charge 0 : Neutrinos

Gauge Bosons

Spin 1

Charge 0 : g , γ , Z

Charge ± 1 : W

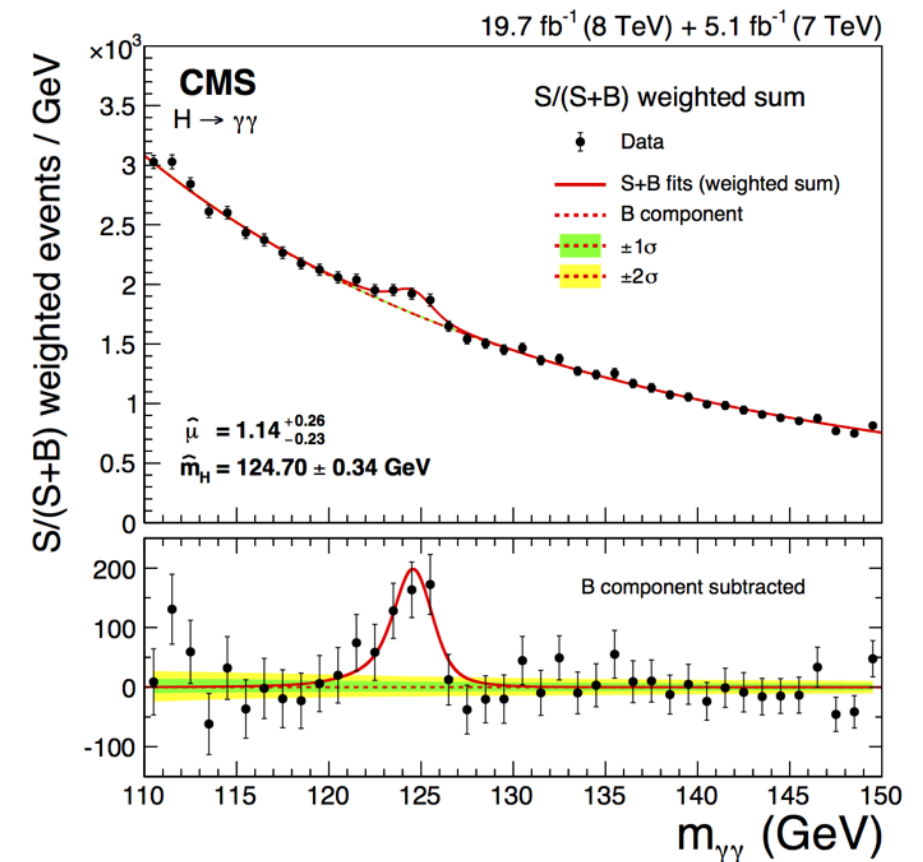
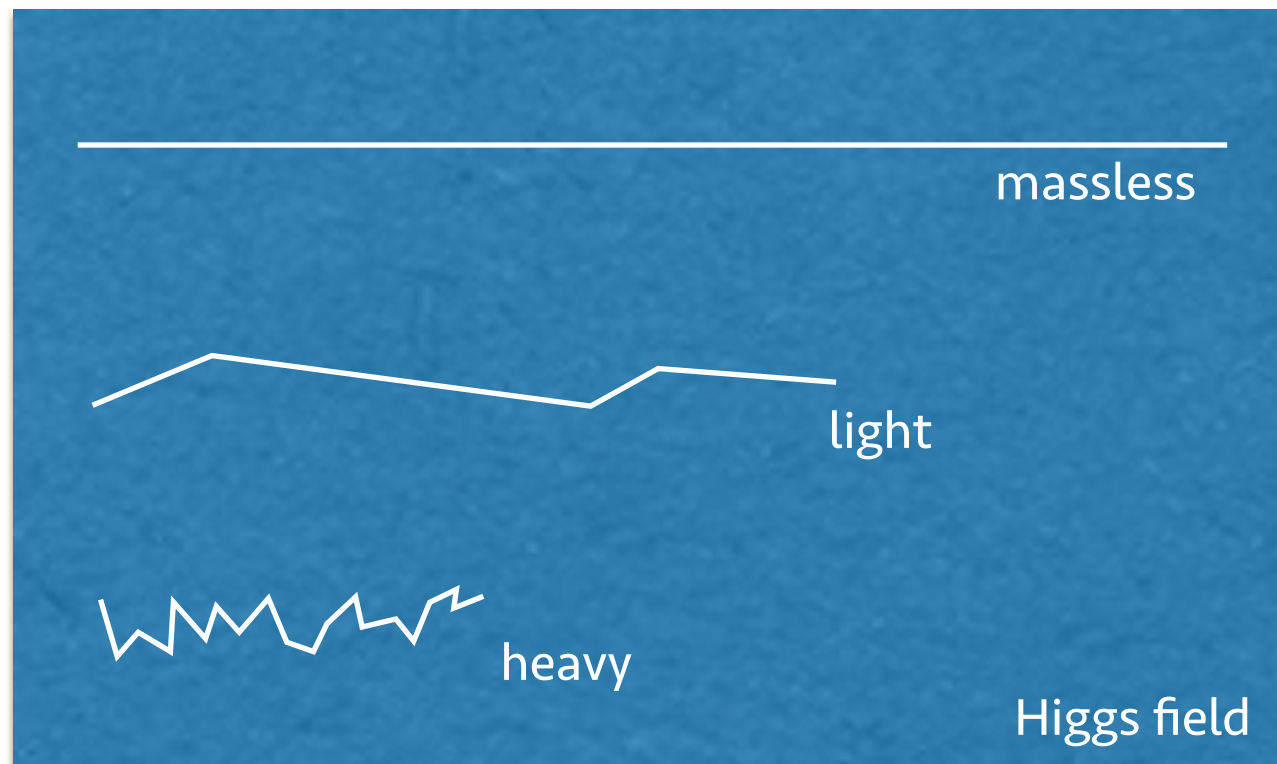
Higgs Boson

Spin 0

Charge 0

Why are elementary particles massive?

The Higgs mechanism explains why fundamental particles are massive.

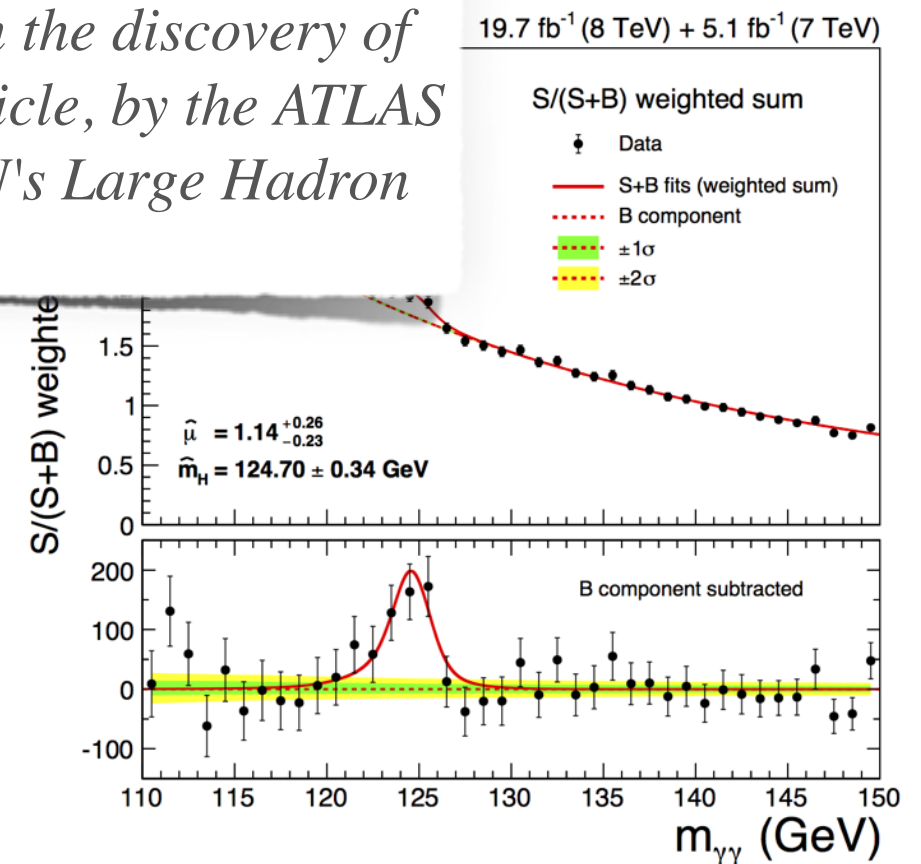
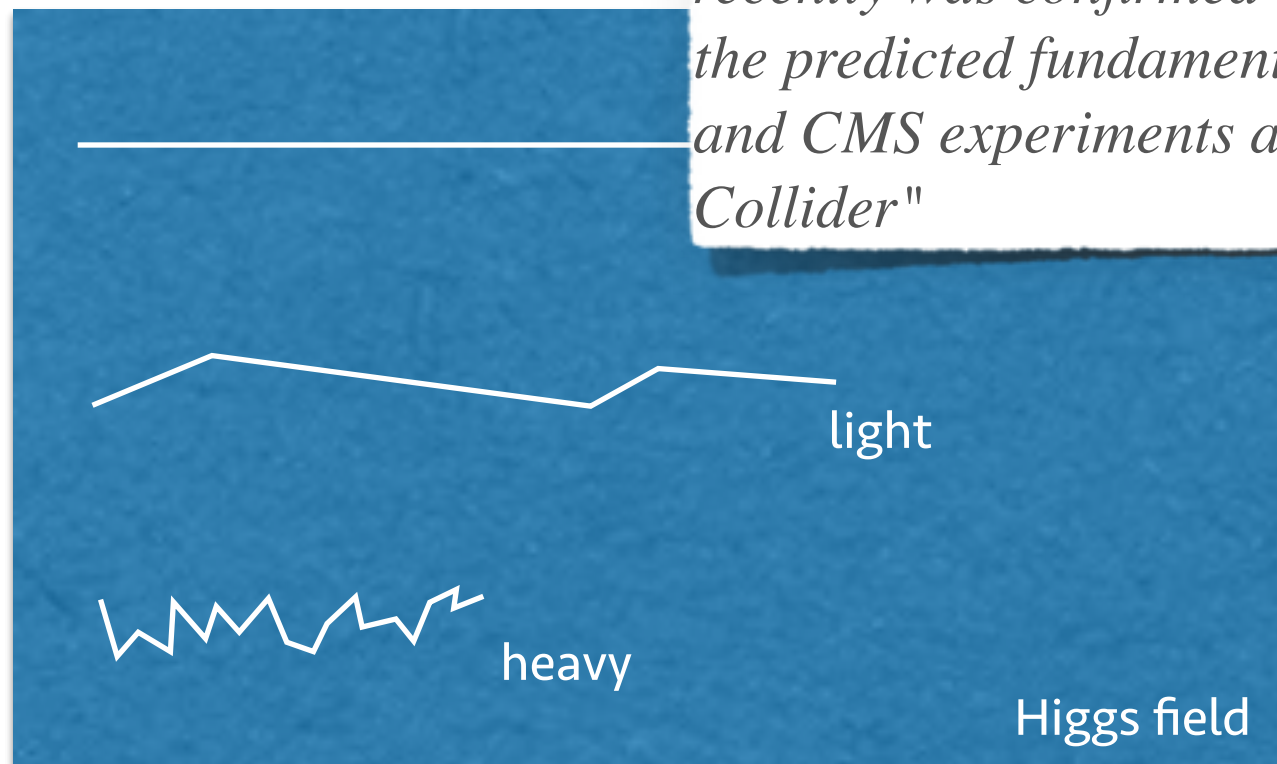


Why are elementary particles massive?

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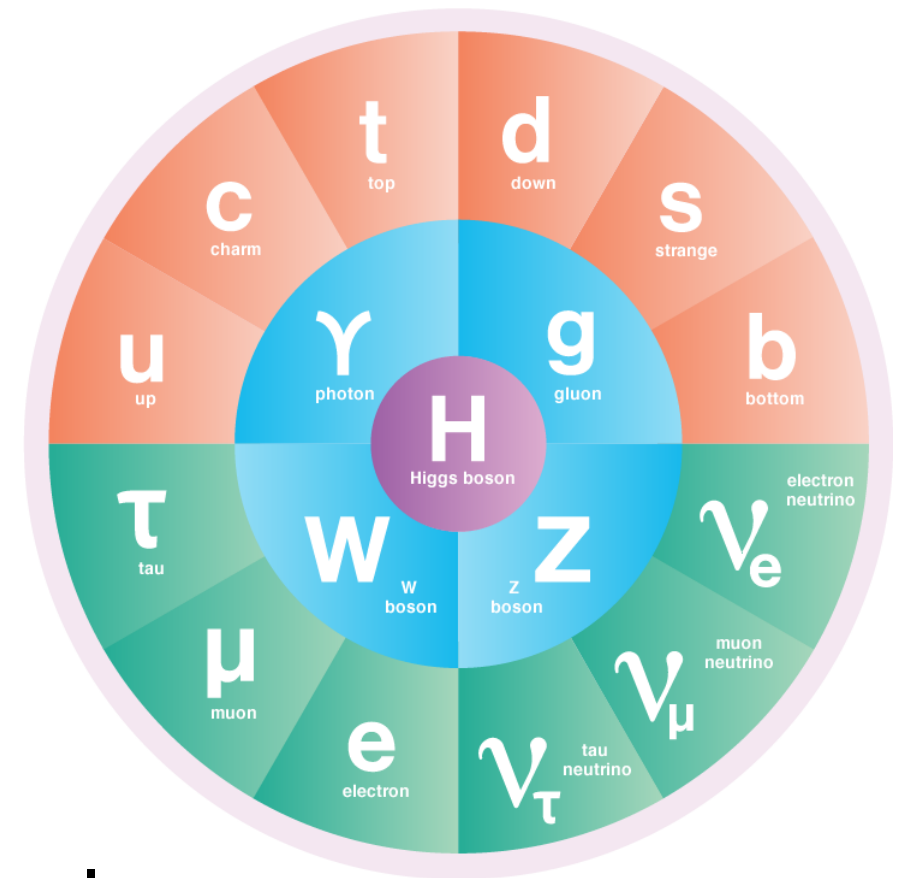
The Nobel Prize in Physics 2013 was awarded jointly to François Englert and Peter W. Higgs "for the theoretical discovery of *a mechanism that contributes to our understanding of the origin of mass of subatomic particles*, and which recently was confirmed through the discovery of the predicted fundamental particle, by the ATLAS and CMS experiments at CERN's Large Hadron Collider"



Why are fermion masses so different?

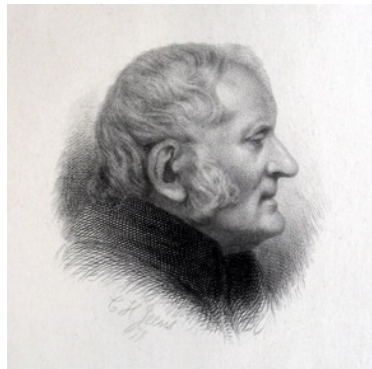
Fermion mass hierarchy:
At least 6 orders of magnitude

top mass = 170.000 x up mass



Take a lesson from history

Hierarchies \longrightarrow Fundamental Structure



John
Dalton,
1808



A historical table titled 'ELEMENTS' showing chemical symbols and atomic weights. Each element is represented by a unique symbol in a circle, a name, a weight, and a numerical value. The symbols are arranged in two columns. The first column includes Hydrogen, Carbon, Oxygen, Phosphorus, Sulphur, Magnesia, Lime, Soda, and Potash. The second column includes Strontian, Barytes, Iron, Zinc, Copper, Lead, Silver, Gold, Platina, and Mercury.

ELEMENTS			
Hydrogen	1	Strontian	46
Carbon	5	Barytes	68
Oxygen	7	Iron	50
Phosphorus	9	Zinc	56
Sulphur	13	Copper	56
Magnesia	20	Lead	90
Lime	24	Silver	190
Soda	28	Gold	190
Potash	42	Platina	190
		Mercury	167

Take a lesson from history

Hierarchies \longrightarrow Fundamental Structure

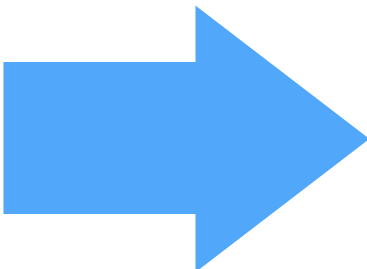
John Dalton, 1808

A black and white engraving of John Dalton, showing him from the chest up in profile, facing right. He has a full, curly beard and hair, and is wearing a dark coat with a high collar. The background is plain.

John
Dalton,
1808

ELEMENTS				
	Hydrogen	1	⊕	Strontian 46
	Carbon	5	⊗	Barytes 68
	Oxygen	7	⊙	Iron 50
	Phosphorus	9	⊕	Zinc 56
	Sulphur	13	⊗	Copper 56
	Sulphur	13	⊕	Lead 90
	Magnesia	20	⊗	Silver 190
	Lime	24	⊕	Gold 190
	Soda	28	⊗	Platina 190
	Potash	42	⊕	Mercury 167

Dmitri Mendeleev, 1869

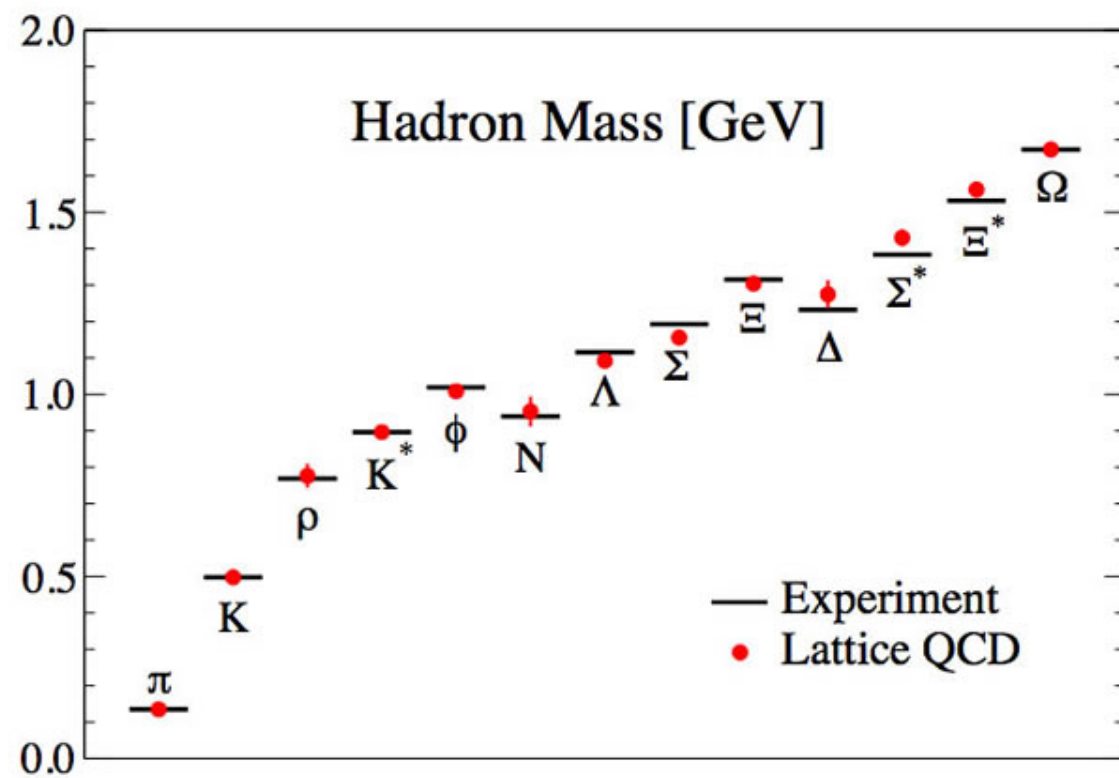


Dmitri Mendeleev, 1869

Periodic Table of Elements																													
1 IA 1A		2 IIA 2A												13 IIIA 3A		14 IVA 4A		15 VA 5A		16 VIA 6A		17 VIIA 7A		18 VIIIA 8A					
H		He												B		C		N		O		F		Ne					
Li		Be												Al		Si		P		S		Cl		Ar					
Na		Mg												Ga		Ge		As		Se		Br		Kr					
K		Ca												In		Sn		Sb		Te		I		Xe					
Rb		Sr												Tl		Pb		Bi		Po		At		Rn					
Cs		Ba												Fr		Ra													
Fr		Ra												Uut		Uuq		Uup		Uuh		Uus		Uuo					
Lanthanide Series		Ce		Pr		Nd		Pm		Sm		Eu		Gd		Tb		Dy		Ho		Er		Tm		Yb		Lu	
Actinide Series		Th		Pa		U		Np		Pu		Am		Cm		Bk		Cf		Es		Fm		Md		No		Lr	
		Alkali Metal		Alkaline Earth		Transition Metal		Basic Metal		Semimetal		Nonmetal		Halogen		Noble Gas		Lanthanide		Actinide									

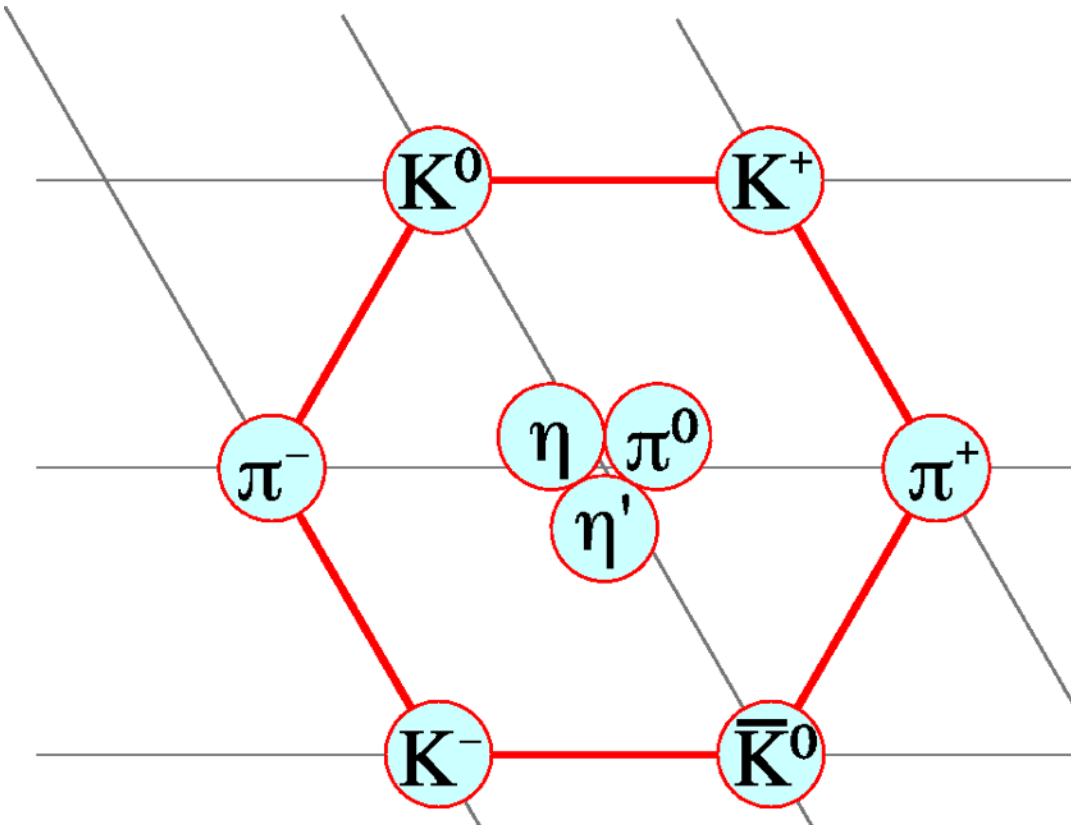
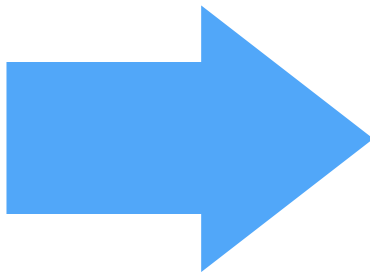
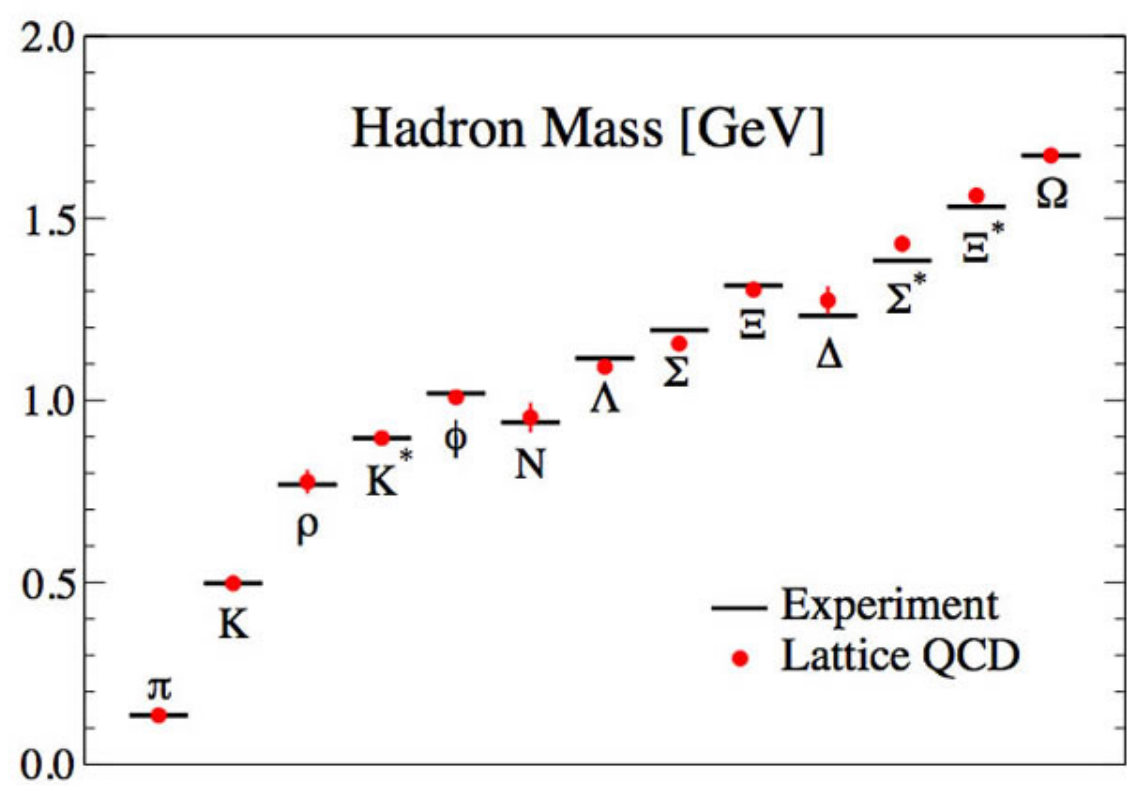
Take a lesson from history

Hierarchies \longrightarrow Fundamental Structure



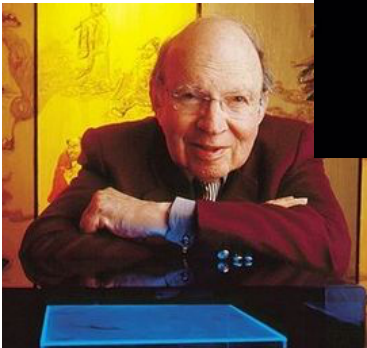
Take a lesson from history

Hierarchies \longrightarrow Fundamental Structure



The eightfold way

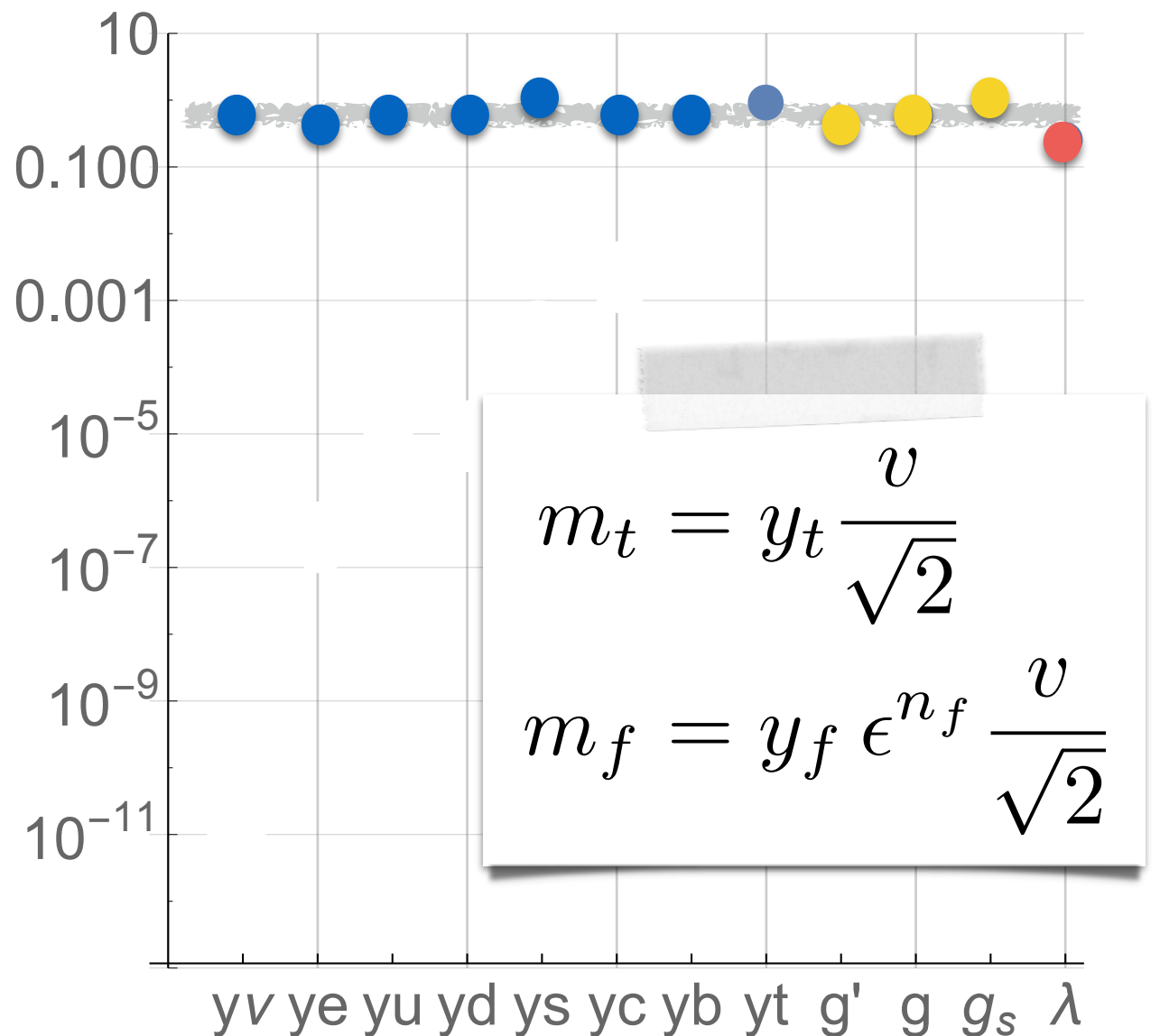
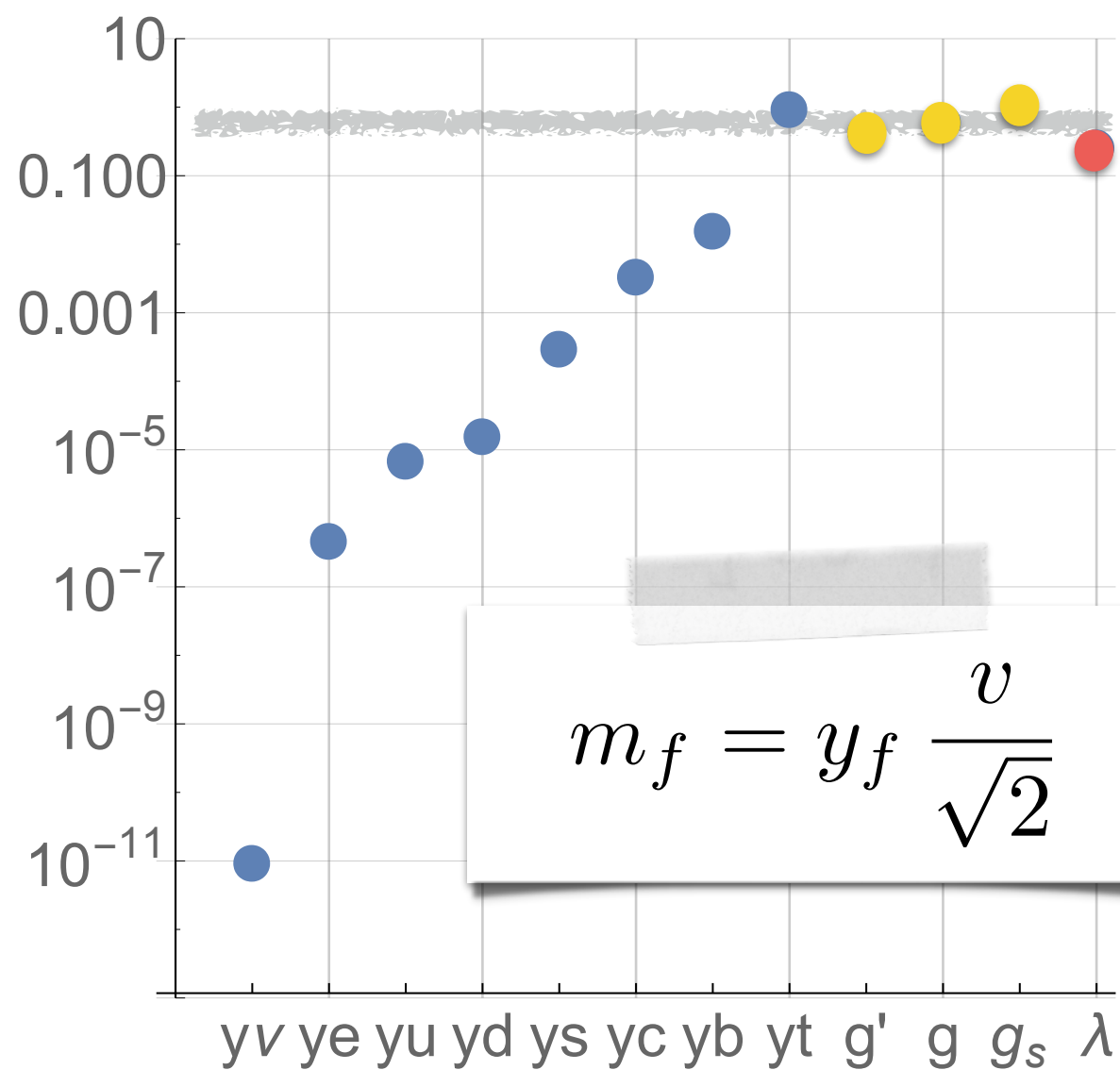
Ne'eman



Fritzsch, Gell-Mann

Why are elementary particles so different?

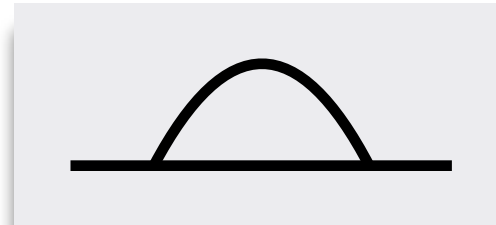
$$\mathcal{L} = \mu_h^2 H^\dagger H + \lambda(H^\dagger H)^2 + \mathcal{L}_{\text{gauge}} + \mathcal{L}_{\text{Yukawa}} + \frac{\mathcal{L}_5}{\Lambda} + \frac{\mathcal{L}_6}{\Lambda^2} + \dots$$



Theories of Flavor

1. Loop Induced

[Georgi, Glashow '72]

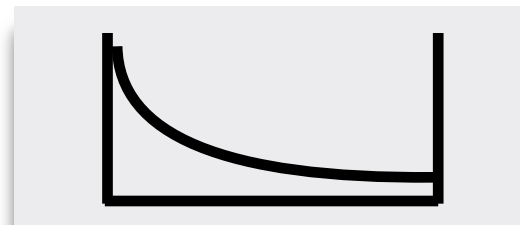


$$\epsilon \approx \frac{1}{16\pi^2} \ln \left(\frac{m_s^2}{\Lambda^2} \right)$$

2. Extra Dimensions

[Grossmann, Neubert 9912408]

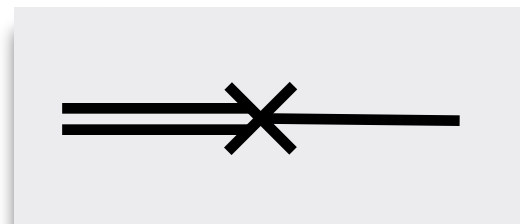
[Gherghetta, Pomarol 0003129]



$$\epsilon^n \approx e^{(c_L - c_R) \ln \frac{\Lambda_{\text{IR}}}{\Lambda_{\text{UV}}}}$$

3. Partial Compositeness

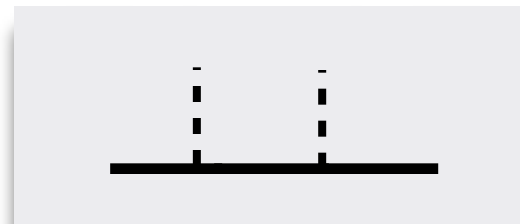
[Kaplan '91]



$$\epsilon^\gamma = \left(\frac{m}{M_B} \right)^\gamma$$

4. Froggatt Nielsen

[Froggatt, Nielsen '79]



$$\epsilon \approx \frac{f}{\Lambda}$$

Can we discover this mechanism?

Illustration: $y_t \bar{t} H t + y_f \left(\frac{S}{\Lambda} \right)^1 \bar{b} H b + \dots$

$$\langle S \rangle = f \quad \Rightarrow \quad y_b = \epsilon y_f$$

and $\epsilon = \frac{f}{\Lambda} = 0.23$

In general, the flavor scale can be arbitrarily high!

Planck Scale

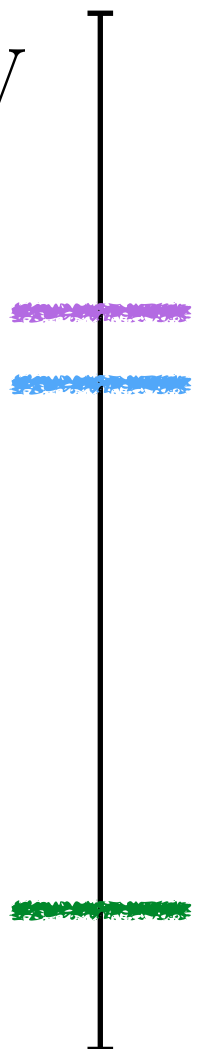
$$M_{\text{Pl}} = 10^{19} \text{ GeV}$$

Λ

f

Electroweak
Scale

$$v = 246 \text{ GeV}$$



Why should the flavor scale be low?

- Why not?
- A link to Baryogenesis?
- A link to Dark Matter?
- It could be related to the electroweak scale

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Flavon Potential

Scalar potential leads to a flavor breaking minimum

$$-\mathcal{L}_{\text{potential}} = -\mu_S^2 S^\dagger S + \lambda_S (S^\dagger S)^2 + b (S^2 + S^{\dagger 2}) + \lambda_{HS} (S^\dagger S) (H^\dagger H) + V(H) .$$

Breaks the flavor symmetry

Two degrees of freedom

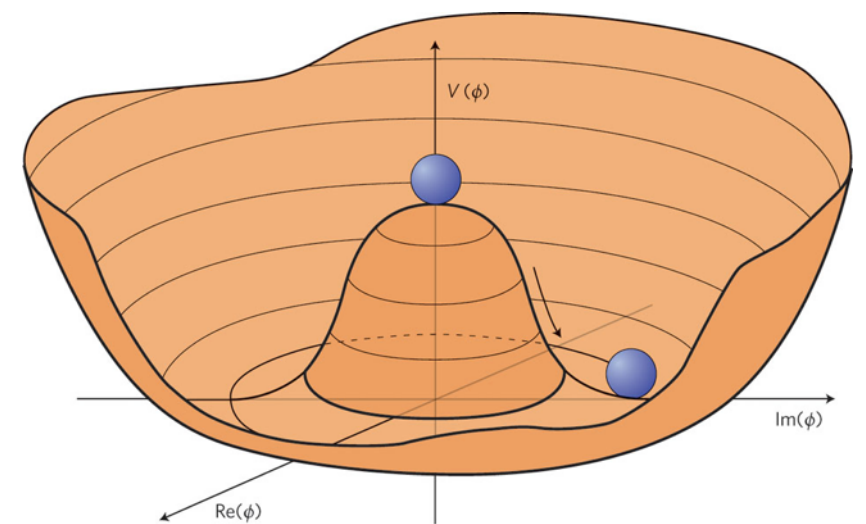
$$S(x) = \frac{f + s(x) + i a(x)}{\sqrt{2}}$$

With masses

$$m_s = \sqrt{2\lambda_S} f$$

$$m_a = 2\sqrt{b}$$

$$m_a < m_s \approx f < \Lambda$$



Yukawa Couplings

Yukawa couplings for quarks and leptons

$$\begin{aligned}\mathcal{L}_{\text{Yukawa}} = & y_{ij}^d \left(\frac{S}{\Lambda} \right)^{n_{ij}^d} \bar{Q}_i H d_{Rj} + y_{ij}^u \left(\frac{S}{\Lambda} \right)^{n_{ij}^u} \bar{Q}_i \tilde{H} u_{Rj} \\ & + y_{ij}^\ell \left(\frac{S}{\Lambda} \right)^{n_{ij}^\ell} \bar{L}_i H \ell_{Rj} + y_{ij}^\nu \left(\frac{S}{\Lambda} \right)^{n_{ij}^\nu} \bar{L}_i \tilde{H} \nu_{Rj} + \text{h.c.}\end{aligned}$$

Exponents are fixed by U(1)
flavor charges.

$$n_{ij}^d = a_{Q_i} - a_{d_j} - a_H$$

$$n_{ij}^u = a_{Q_i} - a_{u_j} + a_H$$

Masses and Mixings

$$\epsilon = \frac{f}{\Lambda} \equiv \frac{\langle S \rangle}{\Lambda} \equiv (V_{\text{CKM}})_{12} \approx 0.23$$

Quark and Lepton Masses

$$\begin{array}{cccccc} m_t \approx \frac{v}{\sqrt{2}} & \frac{m_b}{m_t} \approx \epsilon^3 & \frac{m_c}{m_t} \approx \epsilon^4 & \frac{m_s}{m_t} \approx \epsilon^5 & \frac{m_d}{m_t} \approx \epsilon^7 & \frac{m_u}{m_t} \approx \epsilon^8 \\ \frac{m_\tau}{m_t} \approx \epsilon^3 & \frac{m_\mu}{m_t} \approx \epsilon^5 & \frac{m_e}{m_t} \approx \epsilon^8 & \frac{m_{\nu_1}}{m_t} \approx \epsilon^{24} & \frac{m_{\nu_2}}{m_t} \approx \epsilon^{21} & \frac{m_{\nu_3}}{m_t} \approx \epsilon^{20} \end{array}$$

and Mixings

$$V_{\text{CKM}} \approx \begin{pmatrix} 1 & \epsilon & \epsilon^3 \\ \epsilon & 1 & \epsilon^2 \\ \epsilon^3 & \epsilon^2 & 1 \end{pmatrix}$$

$$U_{\text{PMNS}} \approx \begin{pmatrix} 1 & \epsilon & \epsilon \\ \epsilon & 1 & 1 \\ \epsilon & 1 & 1 \end{pmatrix}$$

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and Mixings

After fixing the ratio of scales there are 2 free parameters:

$$m_a \quad \text{and} \quad f$$

Flavon couplings

Flavon Couplings are dictated by this structure

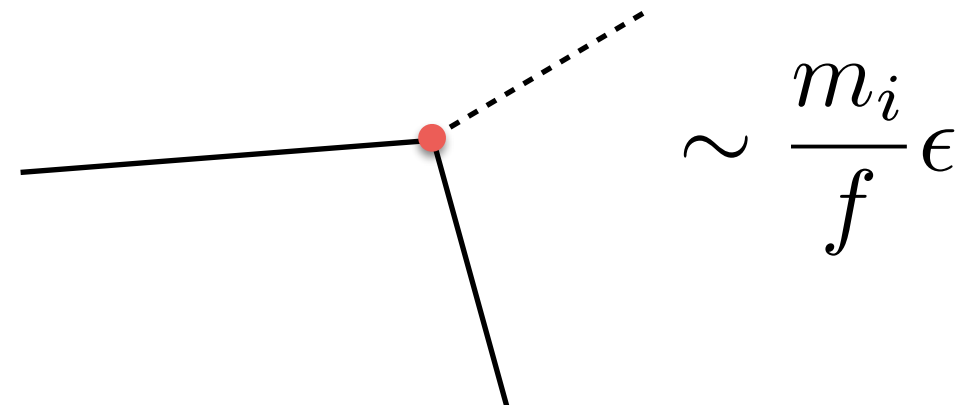
$$S(x) = \frac{f + s(x) + i a(x)}{\sqrt{2}}$$

$$g_{aij}^u = \frac{1}{f} \begin{pmatrix} 8m_u & \epsilon m_c & \epsilon^3 m_t \\ \epsilon^3 m_c & 4m_c & \epsilon^2 m_t \\ \epsilon^5 m_t & \epsilon^2 m_t & 0 \end{pmatrix}$$

$$g_{aij}^d = \frac{1}{f} \begin{pmatrix} 7m_d & \epsilon m_s & \epsilon^3 m_b \\ \epsilon m_s & 5m_s & \epsilon^2 m_b \\ \epsilon m_b & \epsilon^2 m_b & 3m_b \end{pmatrix}$$

$$g_{aij}^\ell = \frac{1}{f} \begin{pmatrix} 9m_e & \epsilon m_\mu & \epsilon m_\tau \\ \epsilon^3 m_\mu & 5m_\mu & \epsilon^2 m_\tau \\ \epsilon^5 m_\tau & \epsilon^2 m_\tau & 3m_\tau \end{pmatrix}$$

small....potentially very small!


$$\sim \frac{m_i}{f} \epsilon$$

Flavon couplings

Flavon Couplings are dictated by this structure

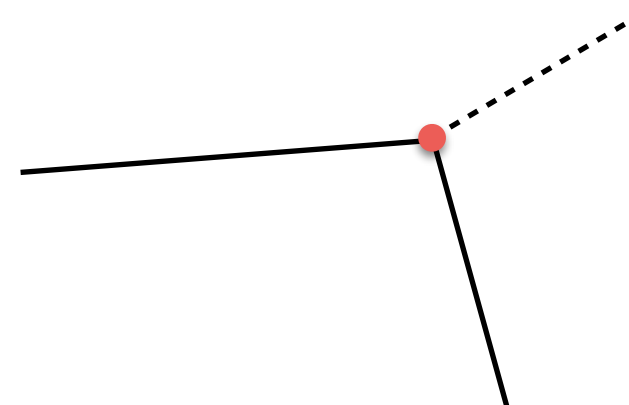
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$$g_{aij}^\ell = \frac{1}{f} \begin{pmatrix} 9m_e & \epsilon m_\mu & \epsilon m_\tau \\ \epsilon^3 m_\mu^3 & 5m_\mu & \epsilon^2 m_\tau \\ \epsilon^5 m_\tau & \epsilon^2 m_\tau & 3m_\tau \end{pmatrix}$$

$$g_{act} = \frac{1}{3\epsilon} g_{abb}$$



$$\sim \frac{m_i}{f} \epsilon$$

Flavon couplings

Effects from flavon interactions lead to

- Quark Flavor Constraints
- Lepton Flavor Constraints
- Future Collider Constraints

Flavon couplings

Generate fundamental Yukawa couplings at the high scale and reproduce fermion masses and mixings in agreement with the SM.

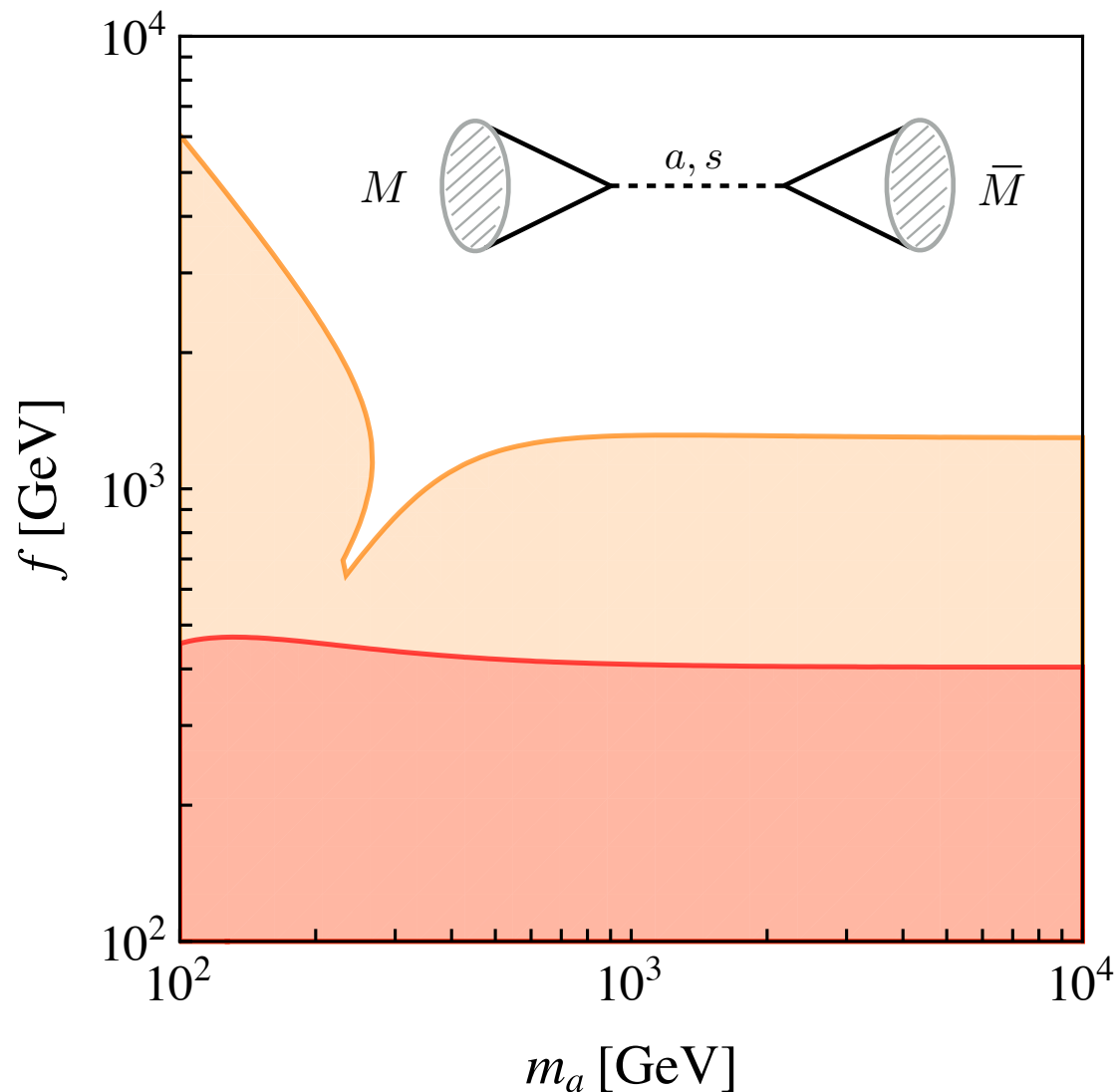
$$\begin{aligned} m_{u_i} &= (0.00138, 0.563, 150.1) \text{ GeV} \\ m_{d_i} &= (0.00342, 0.054, 2.29) \text{ GeV} \end{aligned} \quad |V_{\text{ckm}}| = \begin{pmatrix} 0.974 & 0.226 & 0.0035 \\ 0.226 & 0.974 & 0.0388 \\ 0.011 & 0.037 & 0.999 \end{pmatrix}$$

Demand $|y_{ij}| \in [0.5, 1.5]$ with arbitrary phase.

$$\begin{aligned} Y_u &= \begin{pmatrix} 0.34 + 0.82i & -0.23 + 0.69i & 0.41 - 0.43i \\ -0.84 + 0.26i & -0.64 + 0.32i & 1.35 - 0.24i \\ 0.98 - 0.90i & -0.84 - 1.20i & 0.75 + 0.65i \end{pmatrix} \\ Y_d &= \begin{pmatrix} 0.53 + 0.72i & 0.50 - 0.34i & 0.65 - 0.10i \\ 1.12 - 0.14i & 0.93 - 0.54i & -0.31 - 0.65i \\ -0.16 + 0.6i & -0.73 + 0.34i & 0.84 + 0.61i \end{pmatrix} \end{aligned}$$

Quark Flavor constraints

$$\epsilon_K, \Delta m_K \quad \mathcal{H}_{\text{NP}}^{\Delta F=2} = C_1^{ij} (\bar{q}_L^i \gamma_\mu q_L^j)^2 + \tilde{C}_1^{ij} (\bar{q}_R^i \gamma_\mu q_R^j)^2 + C_2^{ij} (\bar{q}_R^i q_L^j)^2 + \tilde{C}_2^{ij} (\bar{q}_L^i q_R^j)^2 \\ + C_4^{ij} (\bar{q}_R^i q_L^j) (\bar{q}_L^i q_R^j) + C_5^{ij} (\bar{q}_L^i \gamma_\mu q_L^j) (\bar{q}_R^i \gamma^\mu q_R^j) + \text{h.c.}$$



$$C_2^{sd} = -(g_{ds}^*)^2 \left(\frac{1}{m_s^2} - \frac{1}{m_a^2} \right),$$

$$\tilde{C}_2^{sd} = -g_{sd}^2 \left(\frac{1}{m_s^2} - \frac{1}{m_a^2} \right),$$

$$C_4^{sd} = -\frac{g_{sd}g_{ds}}{2} \left(\frac{1}{m_s^2} + \frac{1}{m_a^2} \right).$$

Run down and match

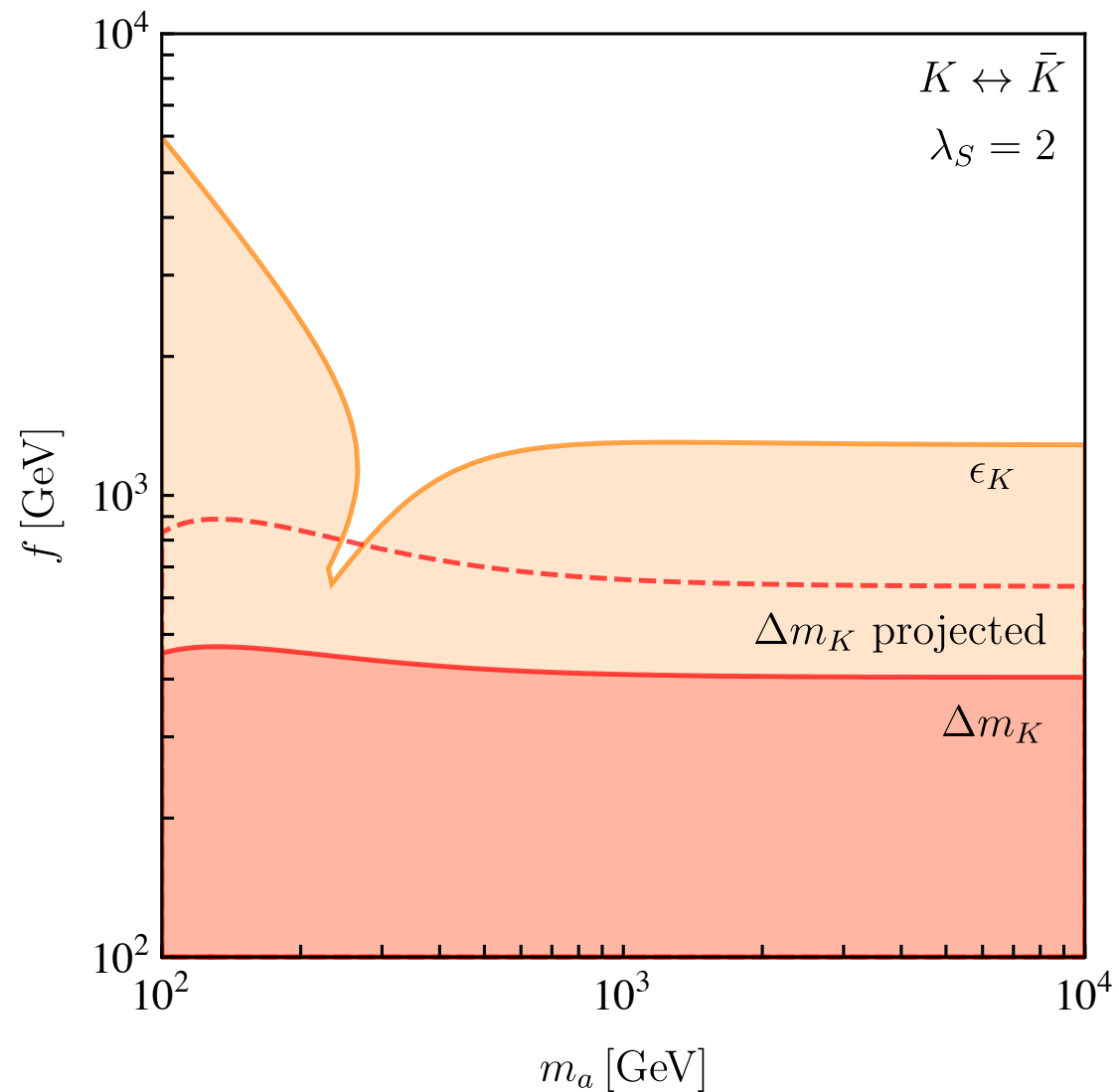
$$C_{\epsilon_K} = \frac{\text{Im} \langle K^0 | \mathcal{H}^{\Delta F=2} | \bar{K}^0 \rangle}{\text{Im} \langle K^0 | \mathcal{H}_{\text{SM}}^{\Delta F=2} | \bar{K}^0 \rangle}$$

UTFIT

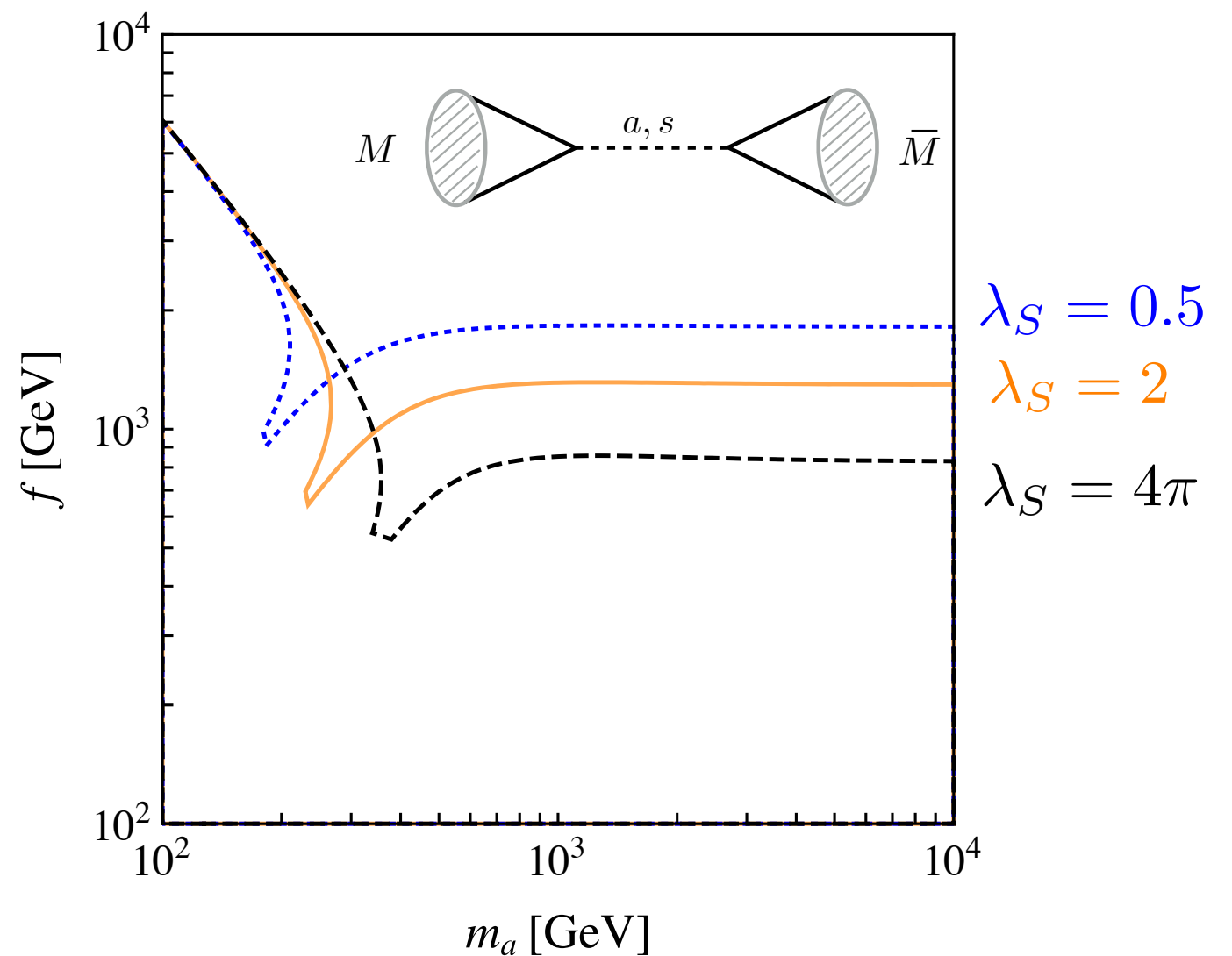
$$C_{\epsilon_K} = 1.05_{-0.28}^{+0.36} \quad @ 95\% \text{ CL}, \quad C_{\Delta m_K} = 0.93_{-0.42}^{+1.14} \quad @ 95\% \text{ CL}$$

Quark Flavor constraints

$$\epsilon_K, \Delta m_K$$

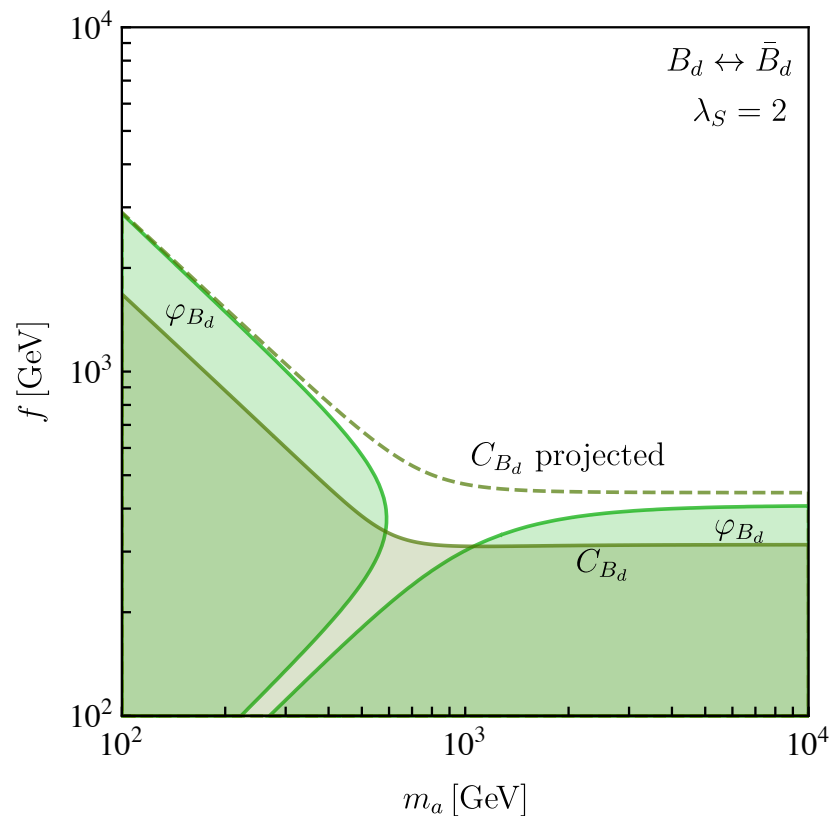


Varying the scalar quartic

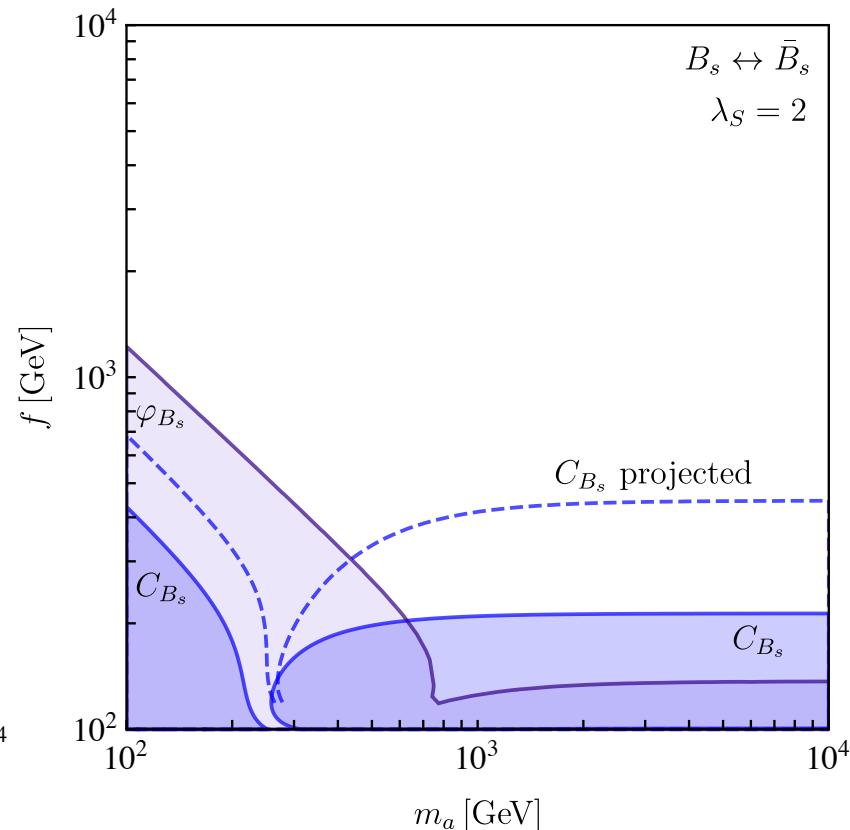


Quark Flavor constraints

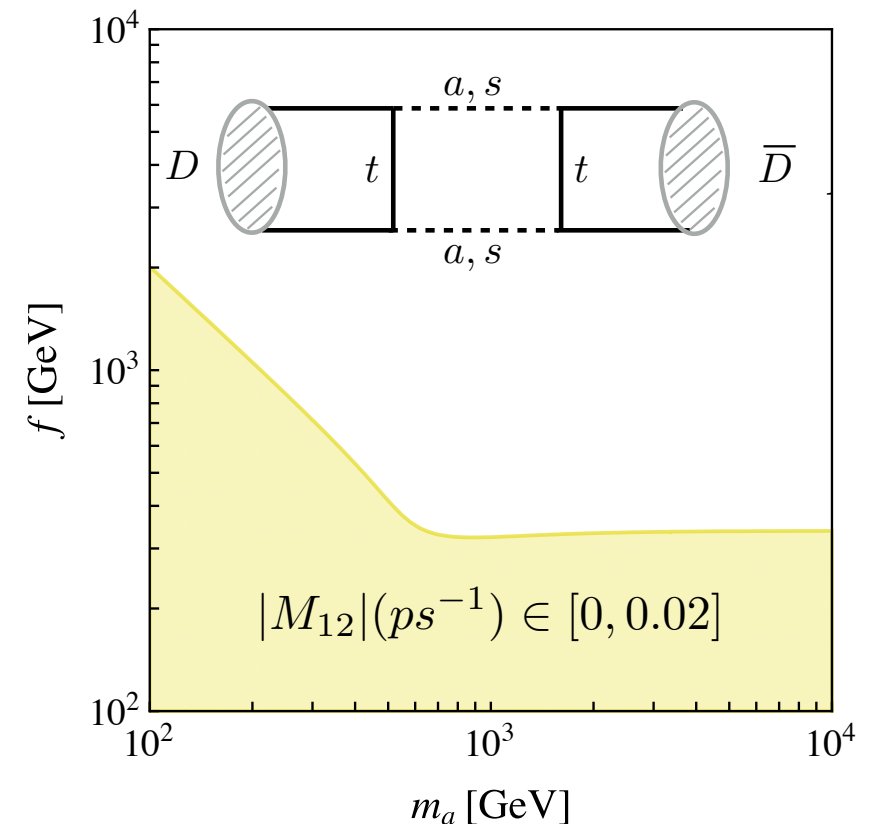
$B_d - \bar{B}_d$



$B_s - \bar{B}_s$



$D - \bar{D}$



$$C_{B_q} e^{2i\varphi_{B_q}} = \frac{\langle B_q | \mathcal{H}^{\Delta F=2} | \bar{B}_q \rangle}{\langle B_q | \mathcal{H}_{\text{SM}}^{\Delta F=2} | \bar{B}_q \rangle}$$

$$C_{B_d} = 1.07^{+0.36}_{-0.31} \quad @ 95\% \text{CL},$$

$$C_{B_s} = 1.052^{+0.178}_{-0.152} \quad @ 95\% \text{CL},$$

$$\varphi_{B_d} = -2.0^{+6.4}_{-6.0} \quad @ 95\% \text{CL},$$

$$\varphi_{B_s} = 0.72^{+3.98}_{-2.28} \quad @ 95\% \text{CL},$$

Using recent Lattice results

1602.03560 MILC & Fermilab Lattice

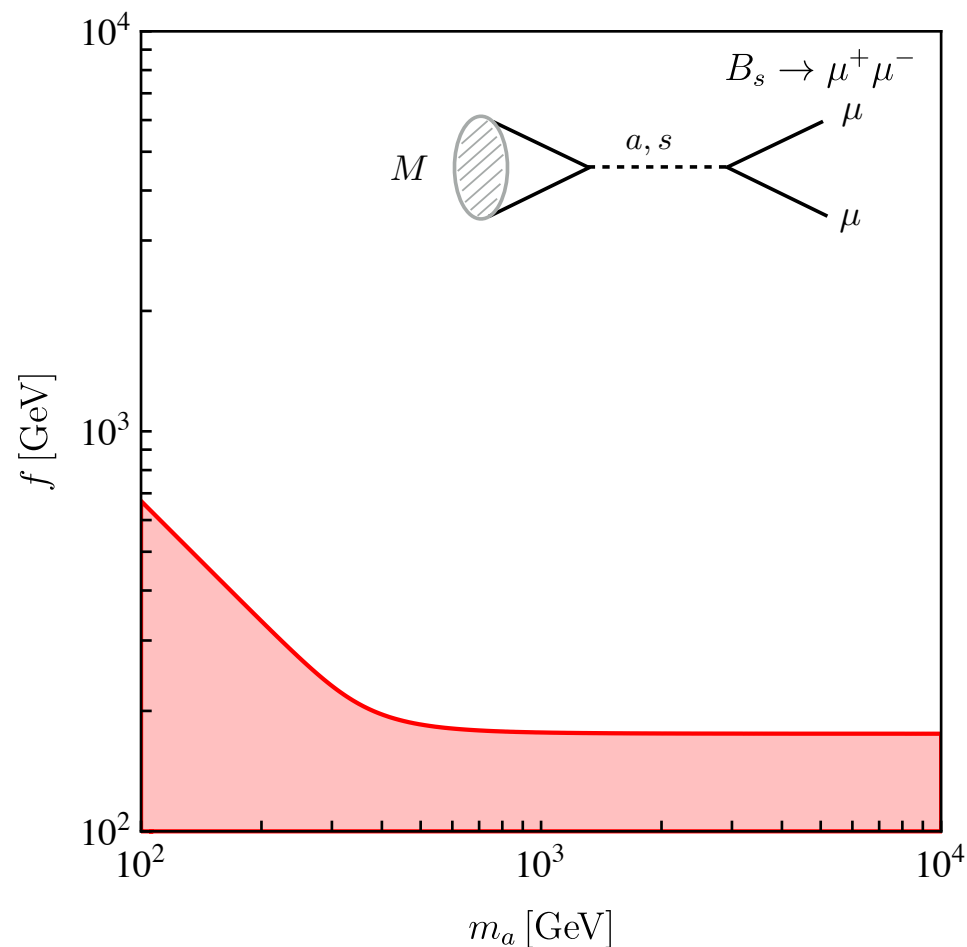
Quark Flavor constraints

$$\text{BR}(M \rightarrow \ell\ell) = \frac{G_F^4 M_W^4}{8\pi^5} \beta \left(\frac{m_\ell}{M_M} \right) M_M f_M^2 m_\ell^2 \tau_M \left\{ \left| \frac{M_M^2 (C_P^{ij} - \tilde{C}_P^{ij})}{2m_\ell(m_i + m_j)} - C_A^{\text{SM}} \right|^2 + \left| \frac{M_M^2 (C_S^{ij} - \tilde{C}_S^{ij})}{2m_\ell(m_i + m_j)} \right|^2 \beta^2 \left(\frac{m_\ell}{M_M} \right) \right\}$$

LHCb&CMS

$$\text{BR}(B_s \rightarrow \mu^+ \mu^-) = 2.8_{-0.6}^{+0.7} \times 10^{-9}$$

$$\text{BR}(B_d \rightarrow \mu^+ \mu^-) = 3.6 \pm 1.6 \times 10^{-10}$$



$$C_S^{ij} = \frac{\pi^2}{2G_F^2 M_W^2} \frac{2g_{\ell\ell}g_{ji}}{m_s^2}, \quad \tilde{C}_S^{ij} = \frac{\pi^2}{2G_F^2 M_W^2} \frac{2g_{\ell\ell}g_{ij}}{m_s^2},$$

$$C_P^{ij} = \frac{\pi^2}{2G_F^2 M_W^2} \frac{2g_{\ell\ell}g_{ji}}{m_a^2}, \quad \tilde{C}_P^{ij} = \frac{\pi^2}{2G_F^2 M_W^2} \frac{2g_{\ell\ell}g_{ij}}{m_a^2}.$$

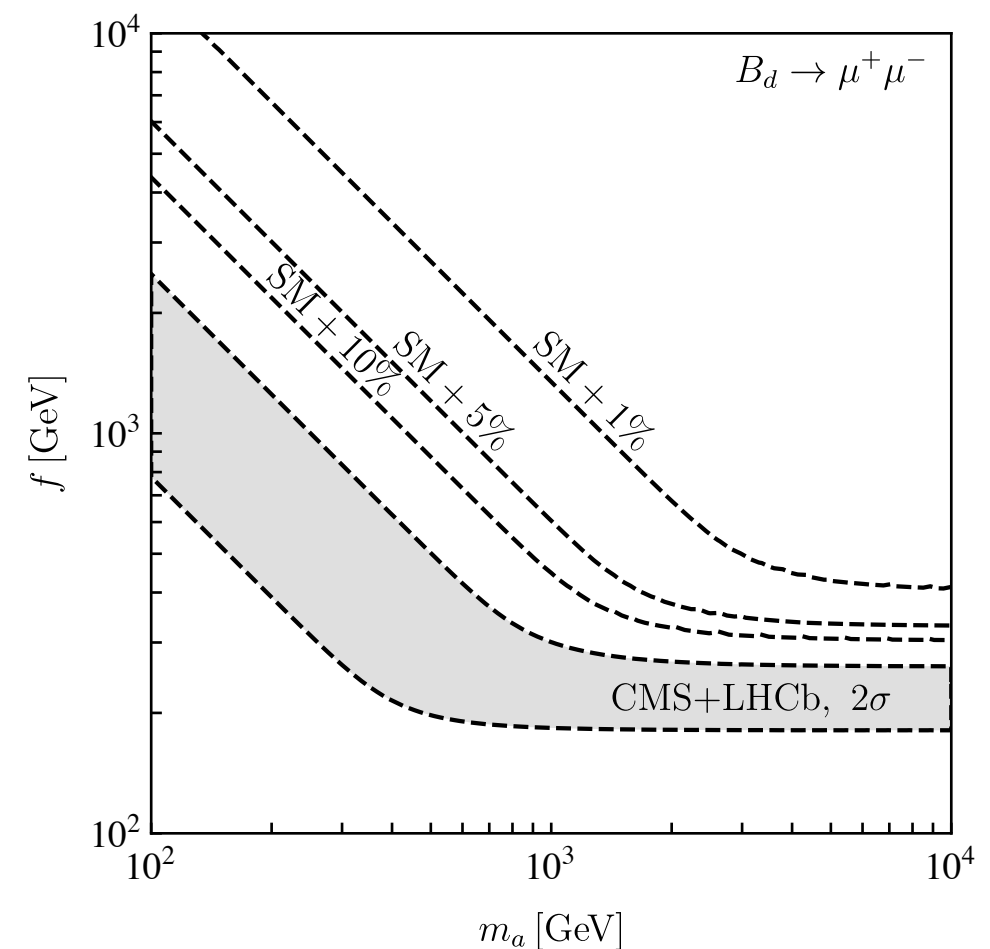
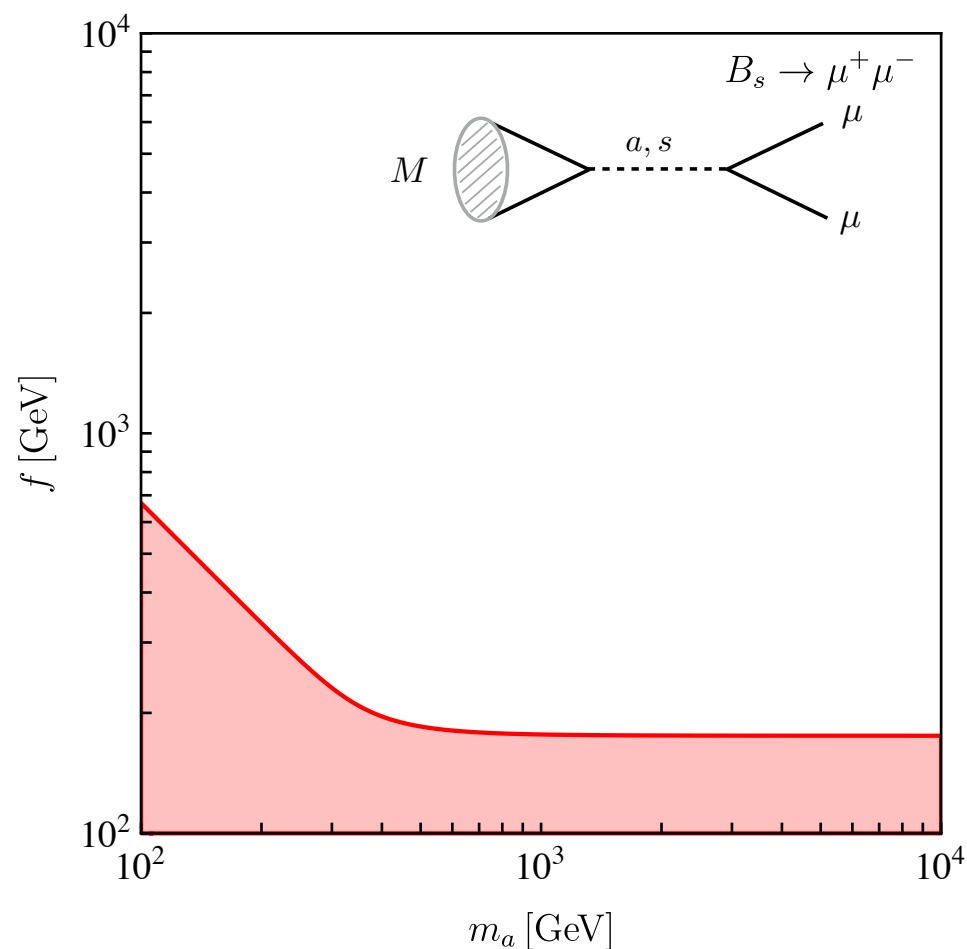
Quark Flavor constraints

$$\text{BR}(M \rightarrow \ell\ell) = \frac{G_F^4 M_W^4}{8\pi^5} \beta \left(\frac{m_\ell}{M_M} \right) M_M f_M^2 m_\ell^2 \tau_M \left\{ \left| \frac{M_M^2 (C_P^{ij} - \tilde{C}_P^{ij})}{2m_\ell(m_i + m_j)} - C_A^{\text{SM}} \right|^2 + \left| \frac{M_M^2 (C_S^{ij} - \tilde{C}_S^{ij})}{2m_\ell(m_i + m_j)} \right|^2 \beta^2 \left(\frac{m_\ell}{M_M} \right) \right\}$$

LHCb&CMS

$$\text{BR}(B_s \rightarrow \mu^+ \mu^-) = 2.8_{-0.6}^{+0.7} \times 10^{-9}$$

$$\text{BR}(B_d \rightarrow \mu^+ \mu^-) = 3.6 \pm 1.6 \times 10^{-10}$$

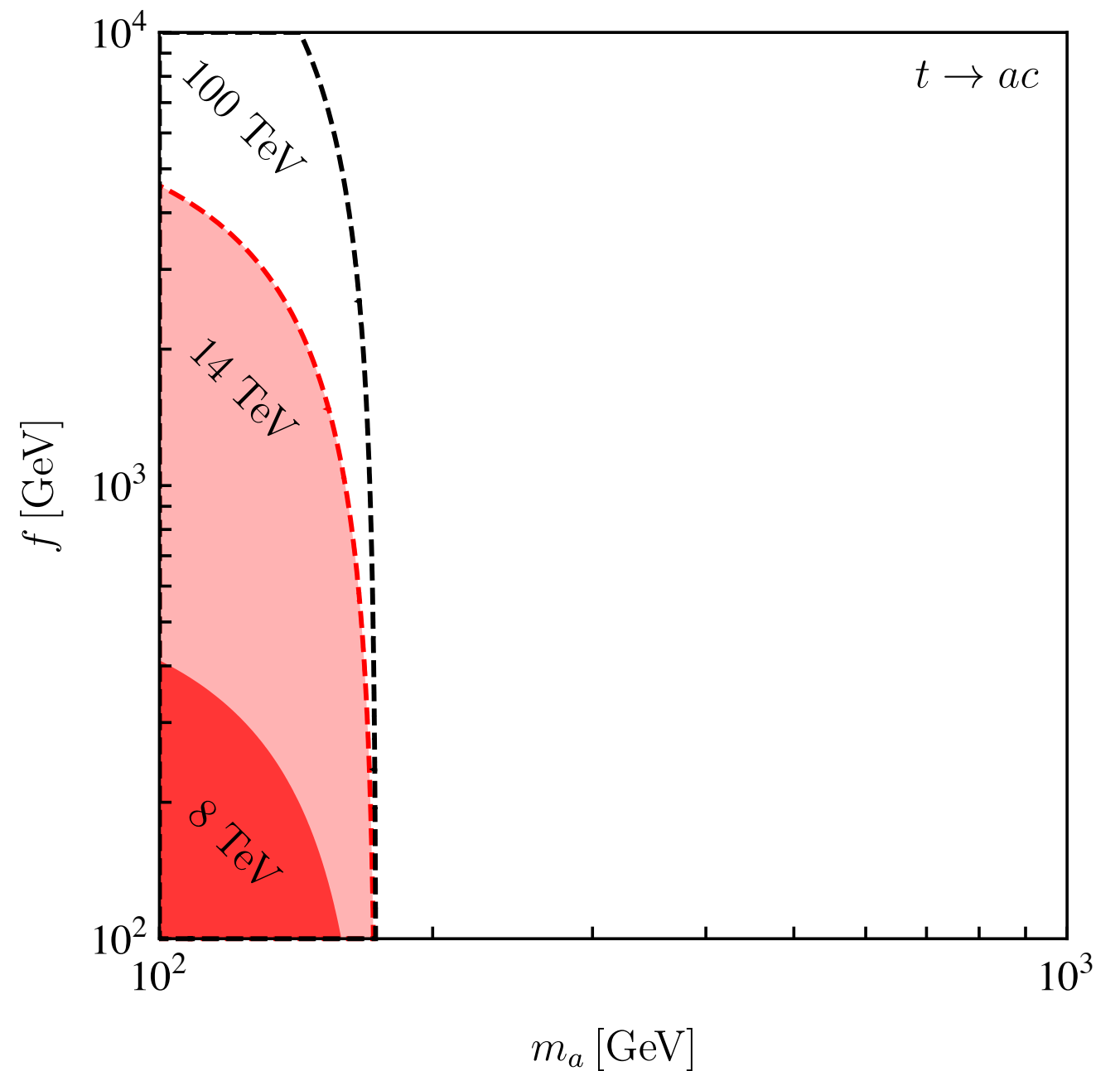


Top decays

LHC 8 $\text{BR}(t \rightarrow ac) < 5.6 \times 10^{-3}$

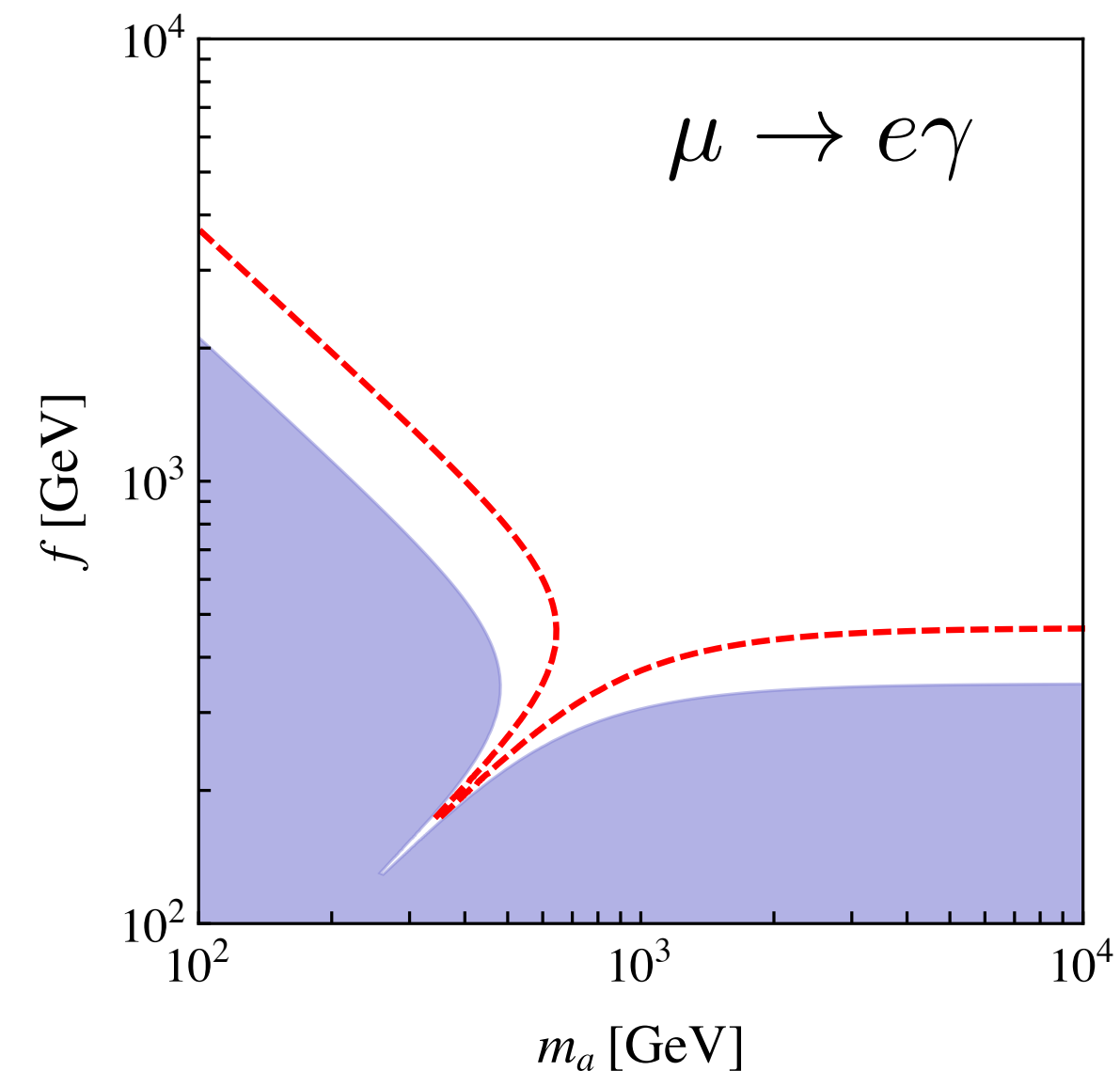
LHC 14 $\text{BR}(t \rightarrow ac) < 4.5 \times 10^{-5}$

100TeV $\text{BR}(t \rightarrow ac) < 1.5 \times 10^{-6}$



Lepton Flavor constraints

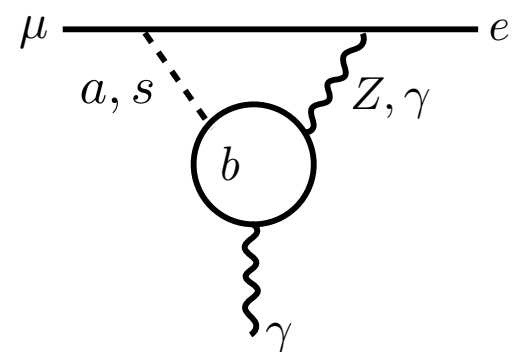
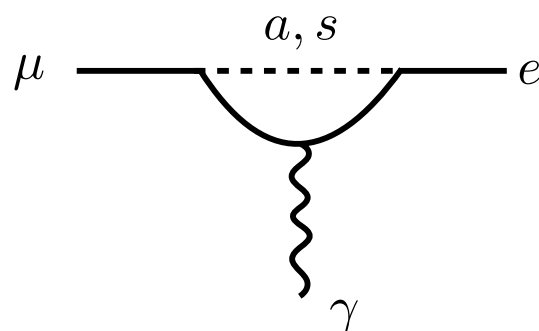
$$\mathcal{L}_{\text{eff}} = m_{\ell'} C_T^L \bar{\ell} \sigma^{\rho\lambda} P_L \ell' F_{\rho\lambda} + m_{\ell'} C_T^R \bar{\ell} \sigma^{\rho\lambda} P_R \ell' F_{\rho\lambda}$$



$$C_T^L = \frac{g}{32\pi^2} \sum_{k=e,\mu,\tau} \left[\frac{1}{6} \left(g_{\ell k}^* g_{\ell' k} + \frac{m_{\ell}}{m_k} g_{k\ell}^* g_{k\ell'} \right) \left(\frac{1}{m_s^2} - \frac{1}{m_a^2} \right) - g_{\ell k} g_{k\ell'} \frac{m_k}{m_{\ell'}} \left\{ \frac{1}{m_s^2} \left(\frac{3}{2} + \log \frac{m_{\ell'}^2}{m_s^2} \right) - \frac{1}{m_a^2} \left(\frac{3}{2} + \log \frac{m_{\ell'}^2}{m_a^2} \right) \right\} \right]$$

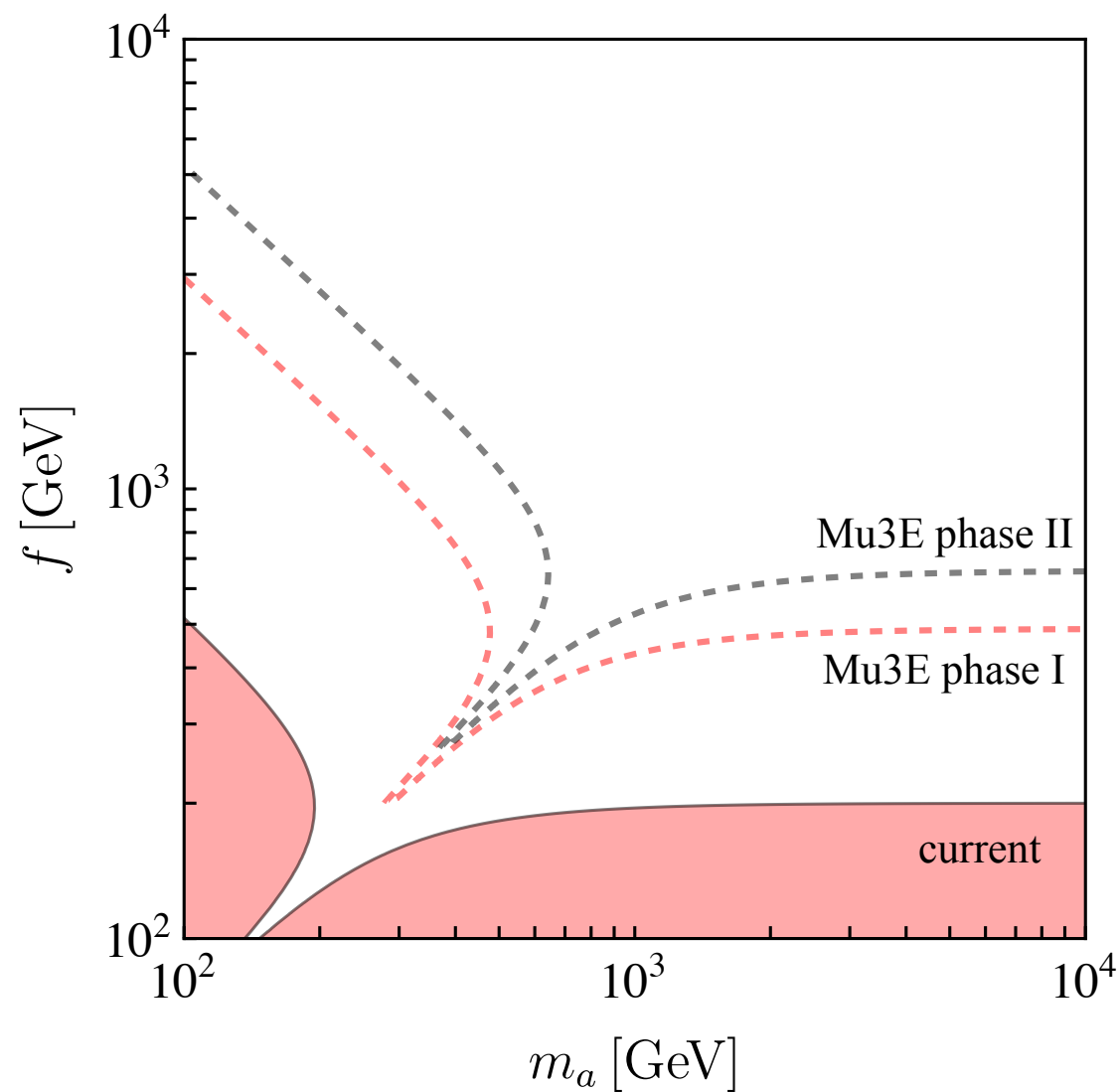
MEG I $\text{BR}(\mu \rightarrow e\gamma) < 5.7 \times 10^{-13}$

MEG II $\text{BR}(\mu \rightarrow e\gamma) < 6 \times 10^{-14}$



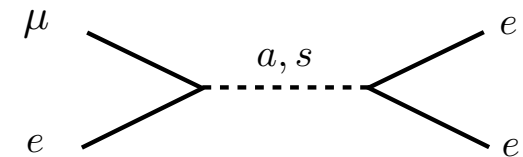
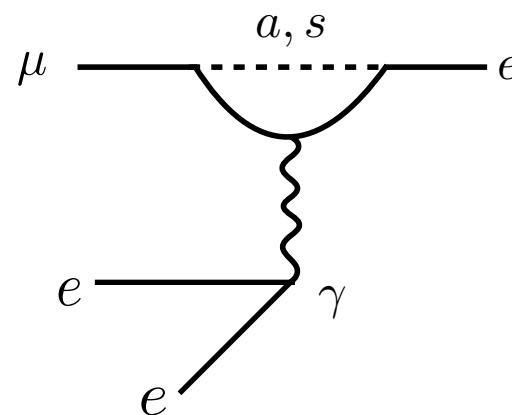
Lepton Flavor constraints

$$\mathcal{L}_{\text{eff}} = m_{\ell'} C_T^L \bar{\ell} \sigma^{\rho\lambda} P_L \ell' F_{\rho\lambda} + m_{\ell'} C_T^R \bar{\ell} \sigma^{\rho\lambda} P_R \ell' F_{\rho\lambda}.$$



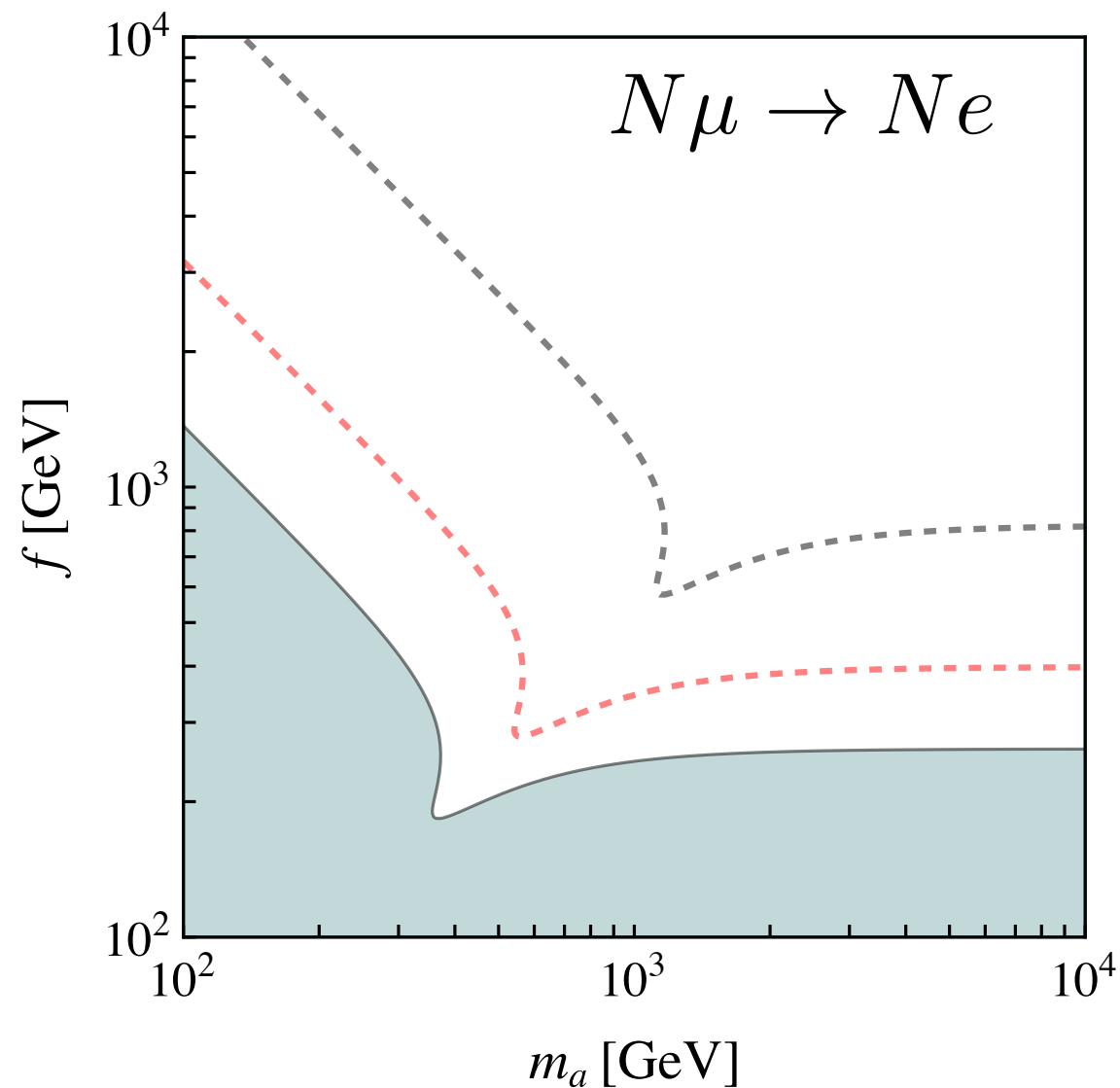
$$\begin{aligned} \text{BR}(\tau \rightarrow 3\mu) &< 2.1 \cdot 10^{-8}, \\ \text{BR}(\tau \rightarrow 3e) &< 2.7 \cdot 10^{-8}, \\ \text{BR}(\mu \rightarrow 3e) &< 1.0 \cdot 10^{-12}. \end{aligned}$$

Mu3E will improve this by 3-4 orders of magnitude!



Lepton Flavor constraints

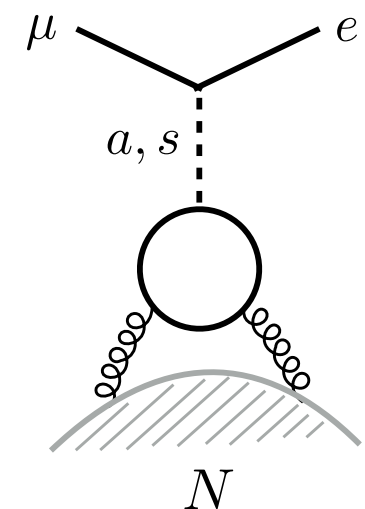
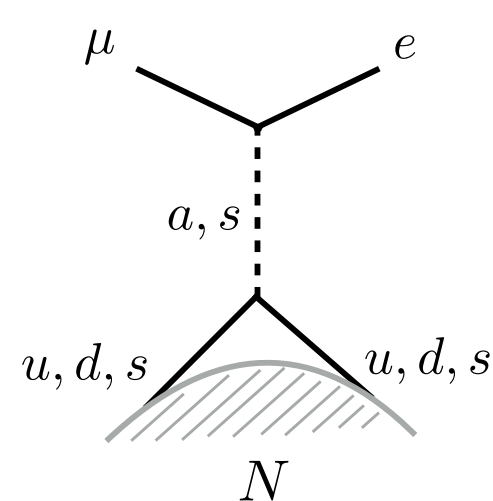
$$\mathcal{L}_{\text{eff}} = C_{qq}^{VL} \bar{e} \gamma^\nu P_L \mu \bar{q} \gamma_\nu q + m_\mu m_q C_{qq}^{SL} \bar{e} P_R \mu \bar{q} q + m_\mu \alpha_s C_{gg}^L \bar{e} P_R \mu G_{\rho\nu} G^{\rho\nu} + R \leftrightarrow L,$$



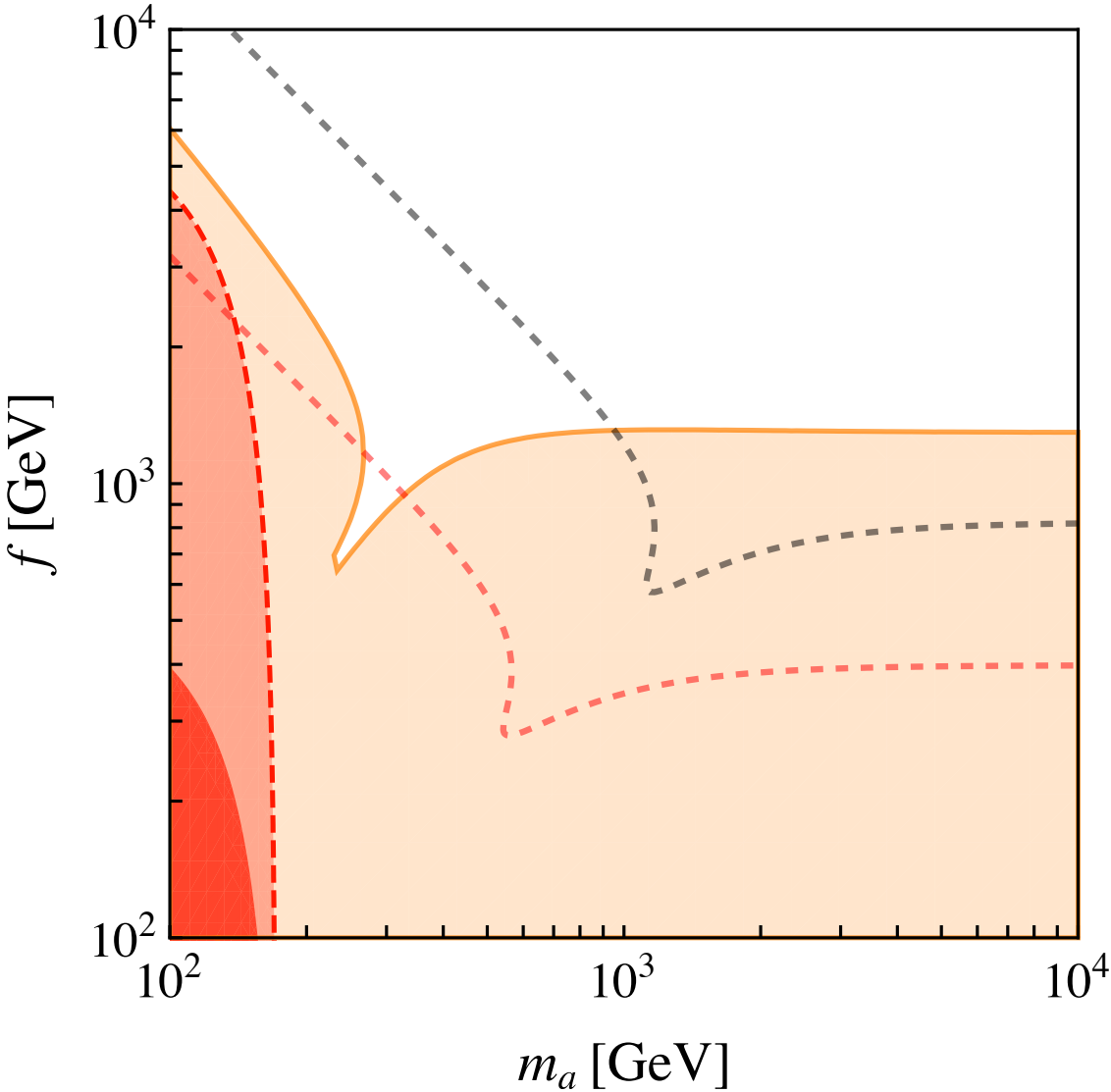
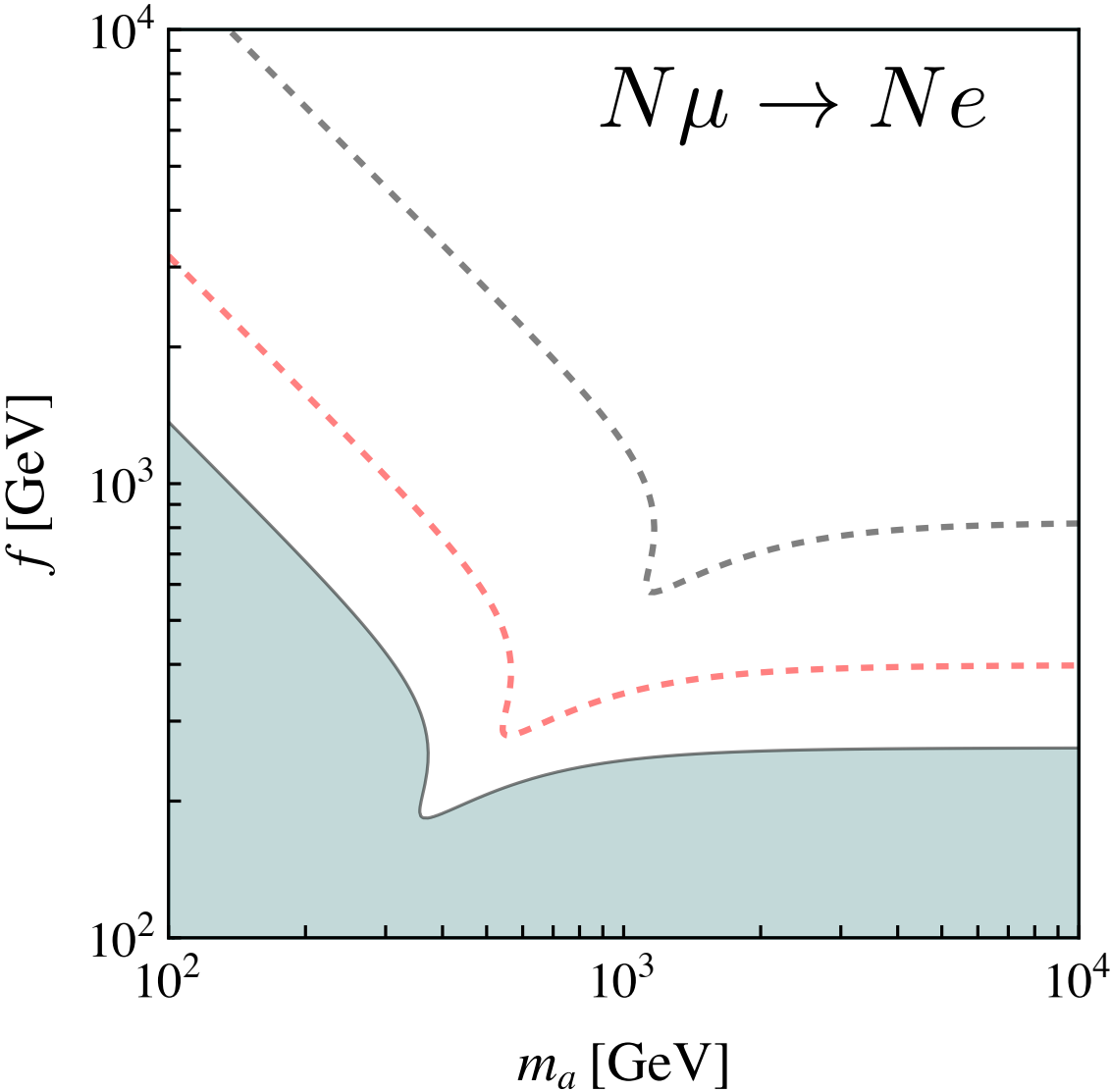
Sindrum II $\text{BR}(\mu \rightarrow e)^{\text{Au}} < 7 \times 10^{-13}$

DeeMe $\text{BR}(\mu \rightarrow e)^{\text{Si}} < 2 \times 10^{-14}$

COMET $\text{BR}(\mu \rightarrow e)^{\text{Al}} < 6 \times 10^{-17}$

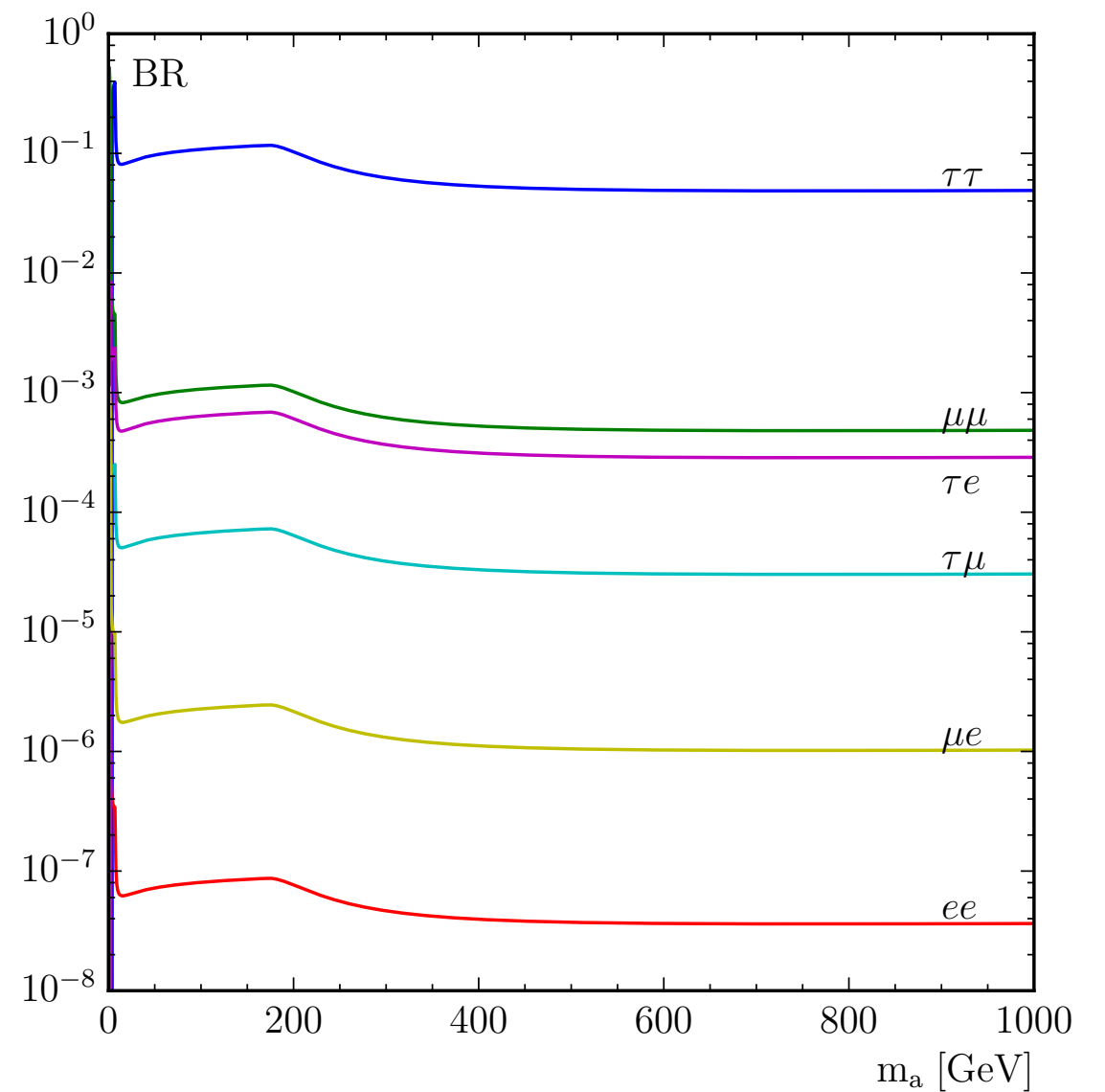
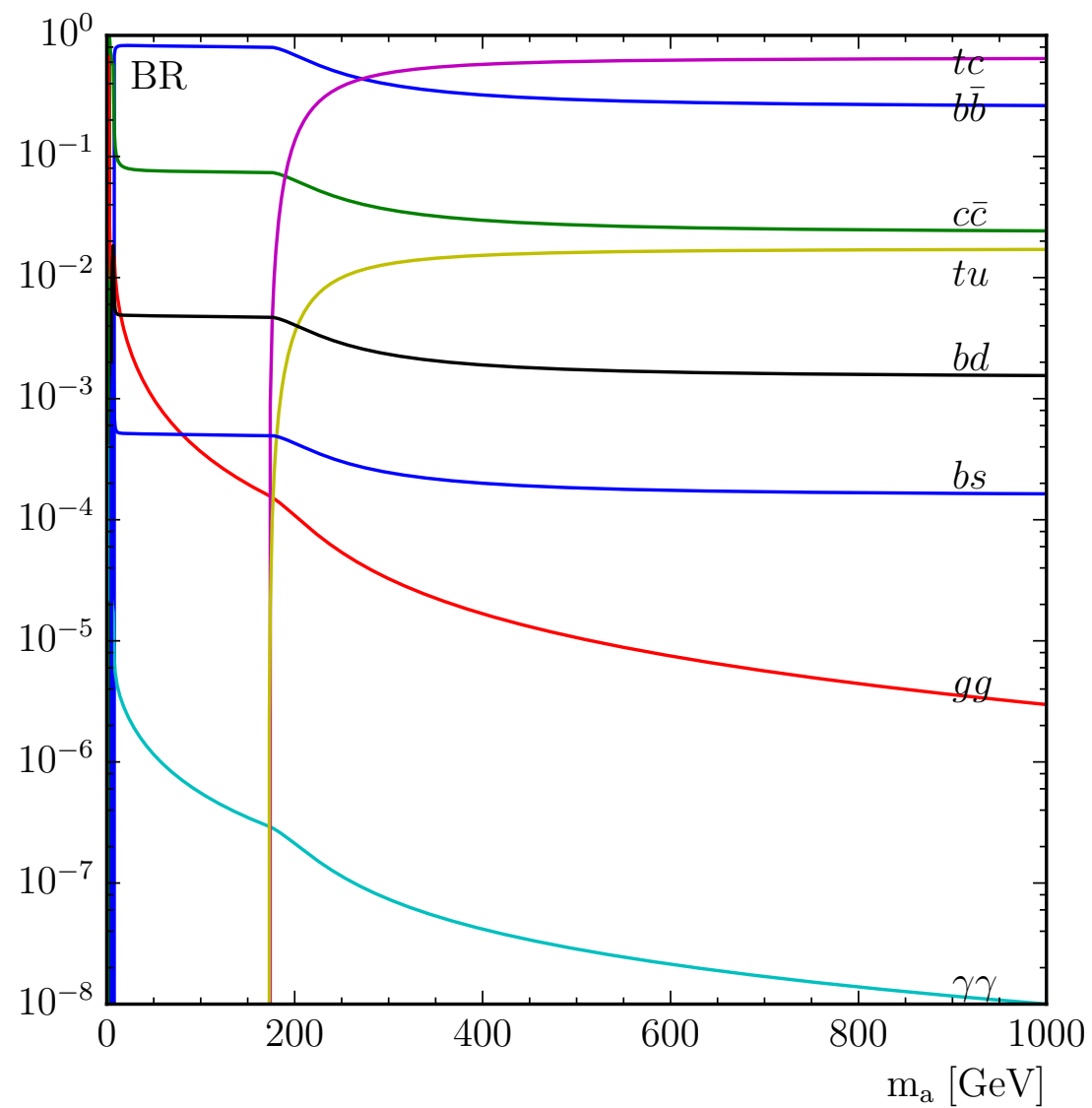


Lepton Flavor constraints



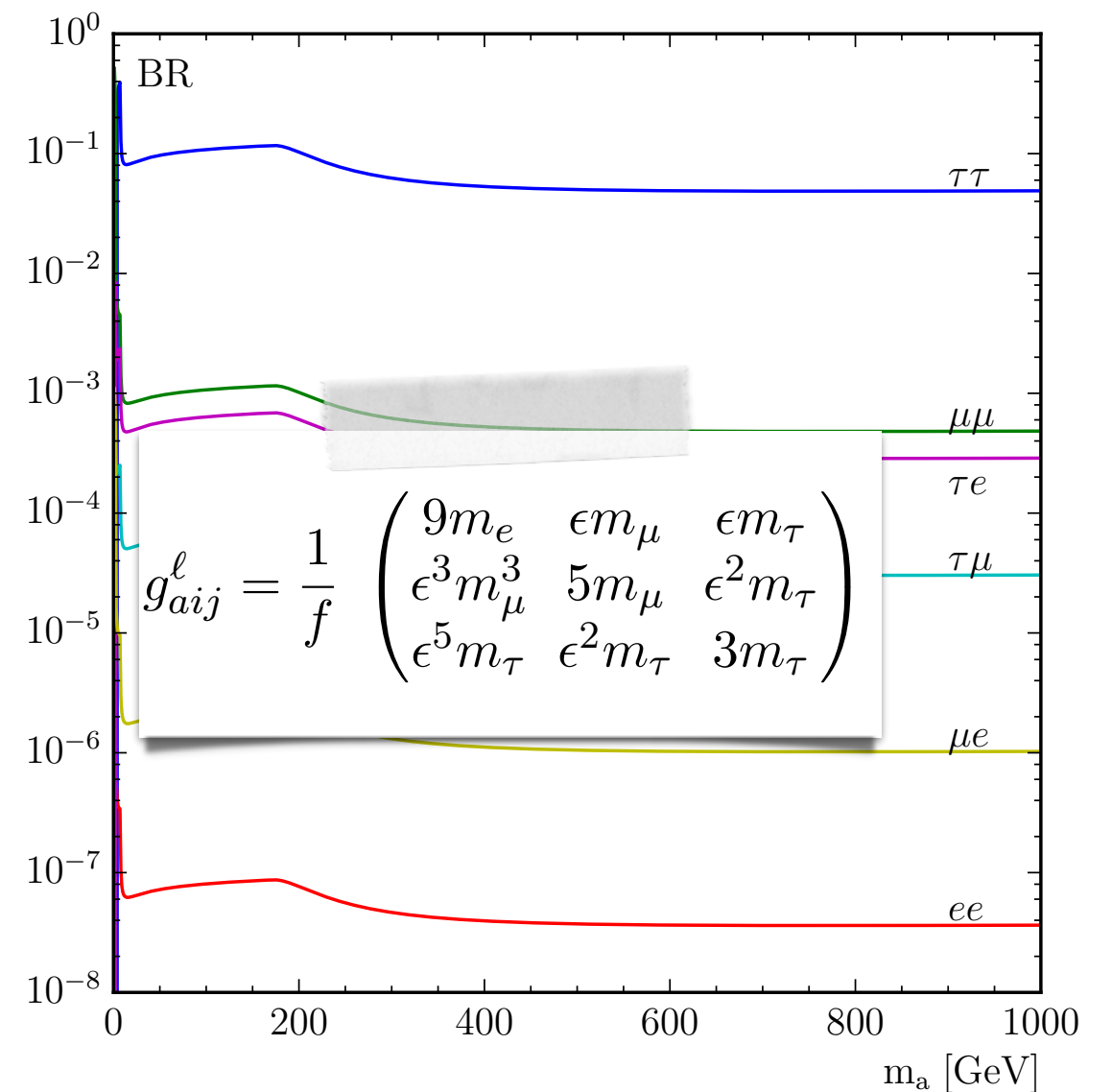
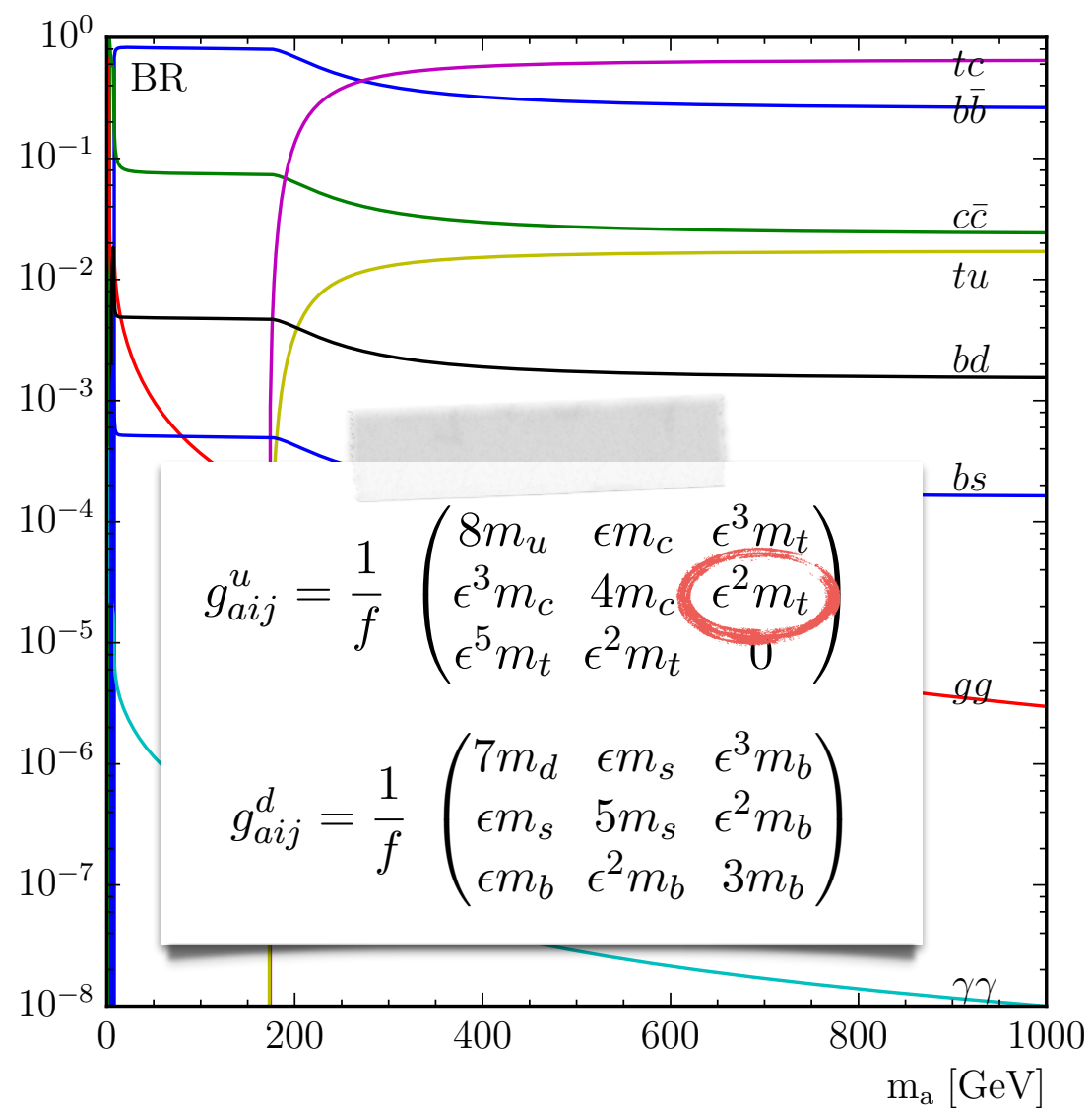
Future Collider Searches

Branching Ratios



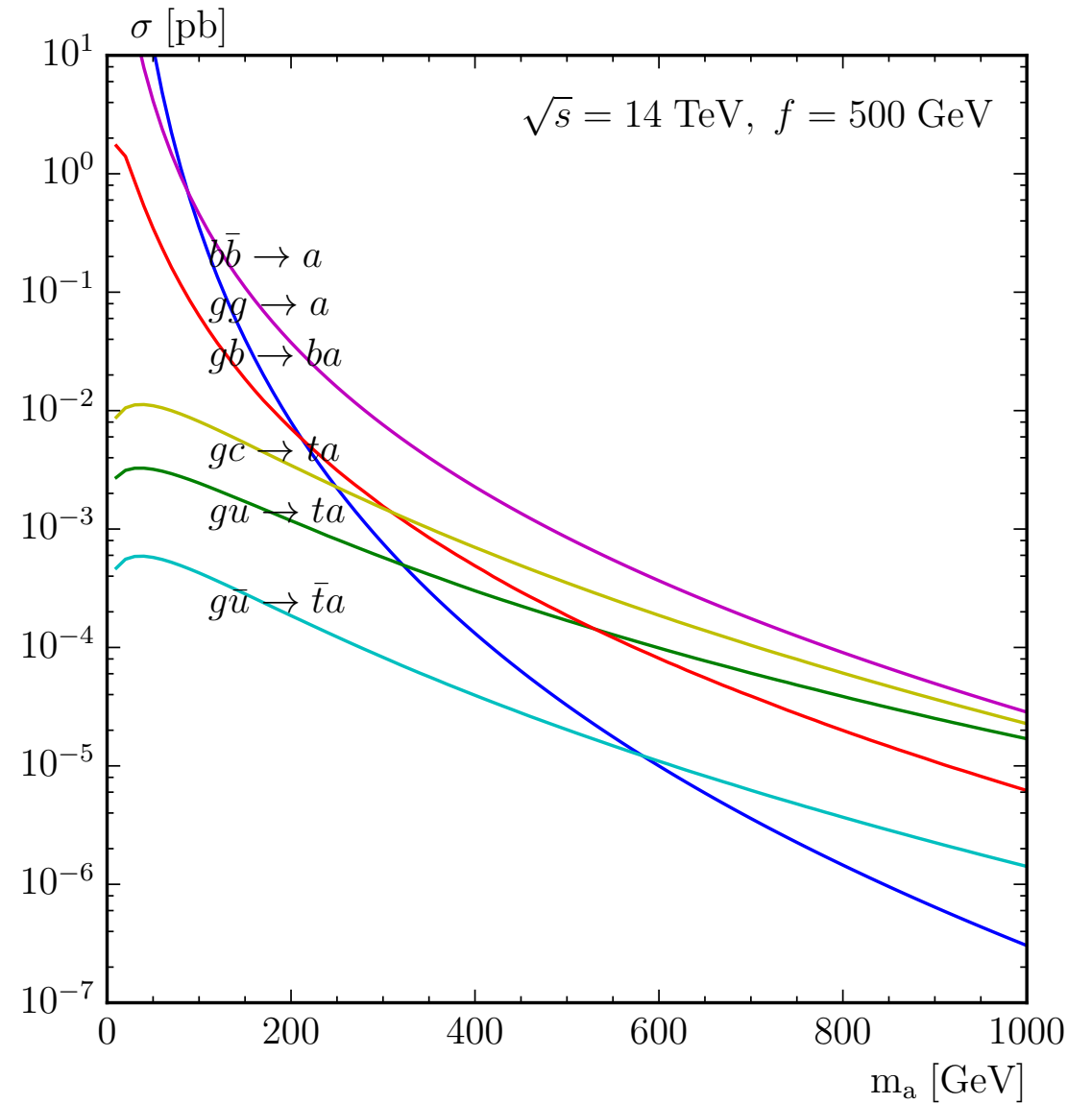
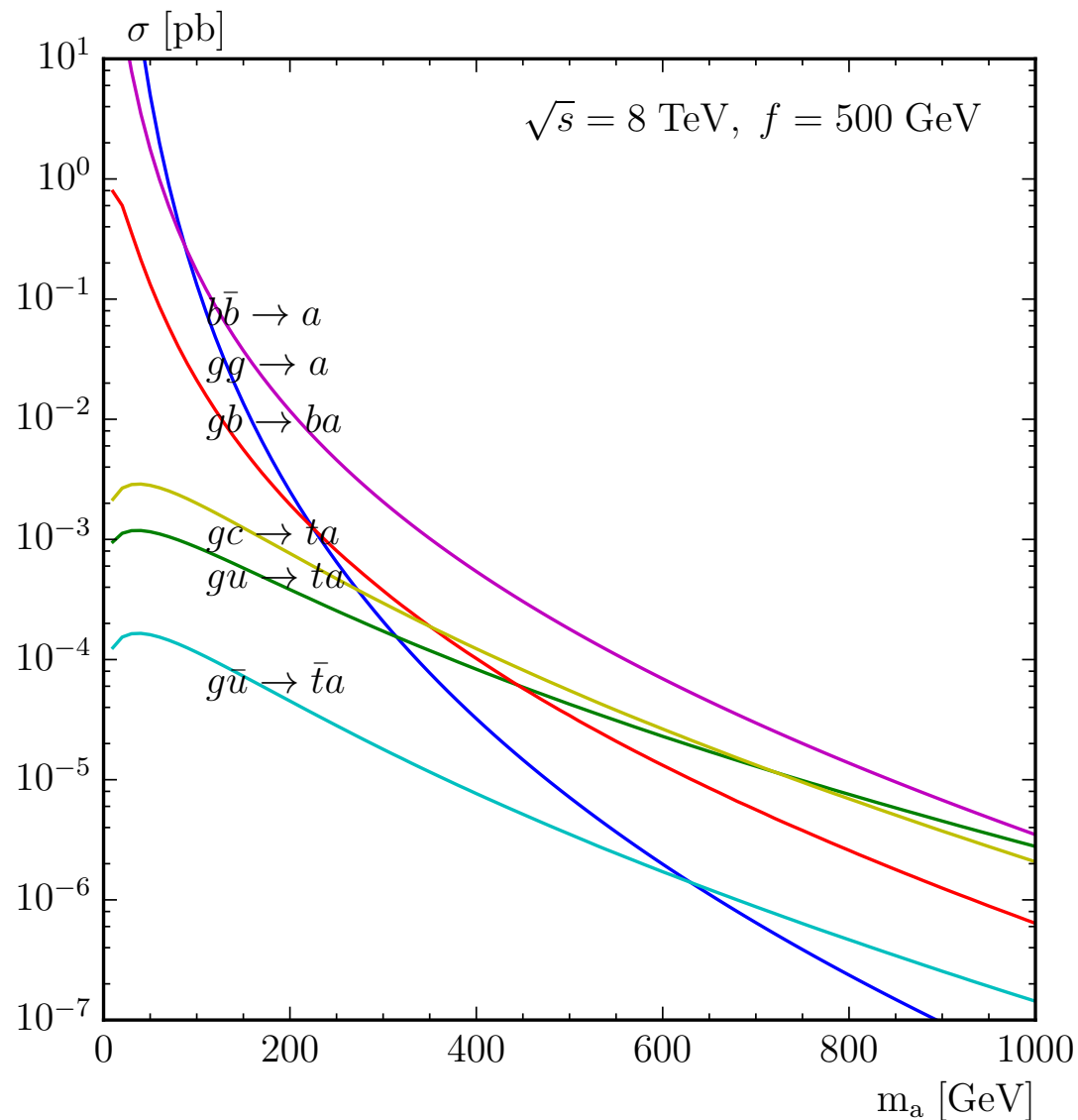
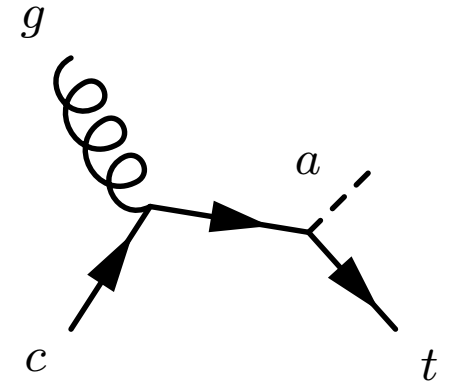
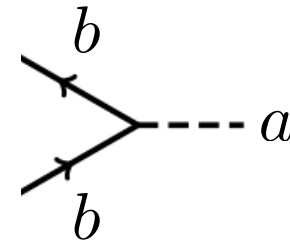
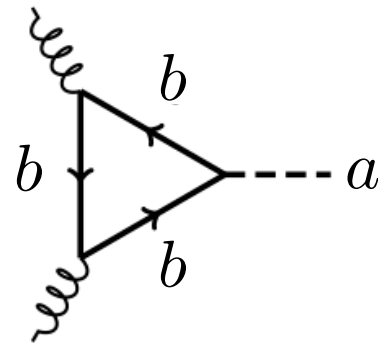
Future Collider Searches

Branching Ratios



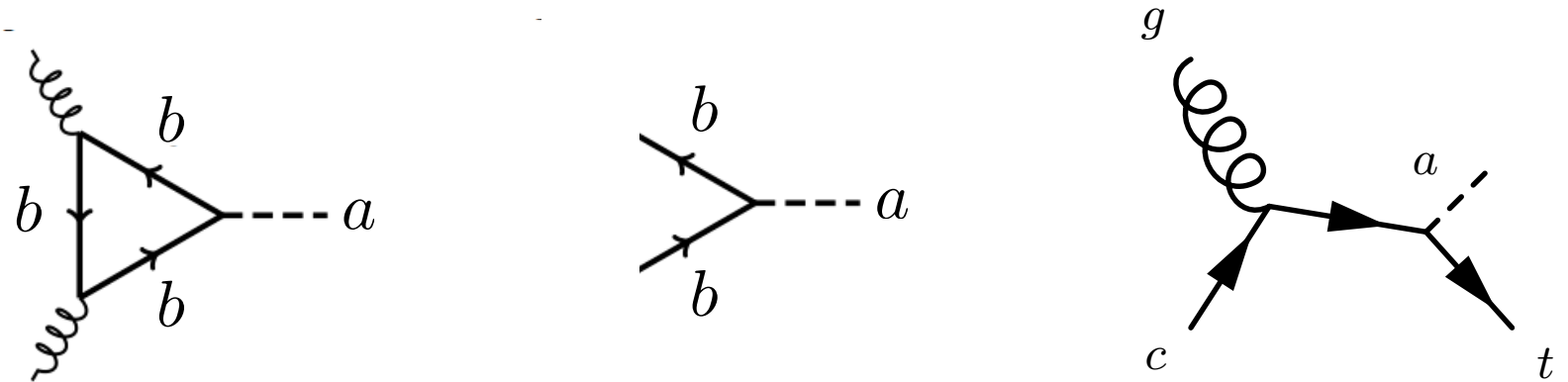
(Future) Collider Searches

Production Cross Sections at LHC

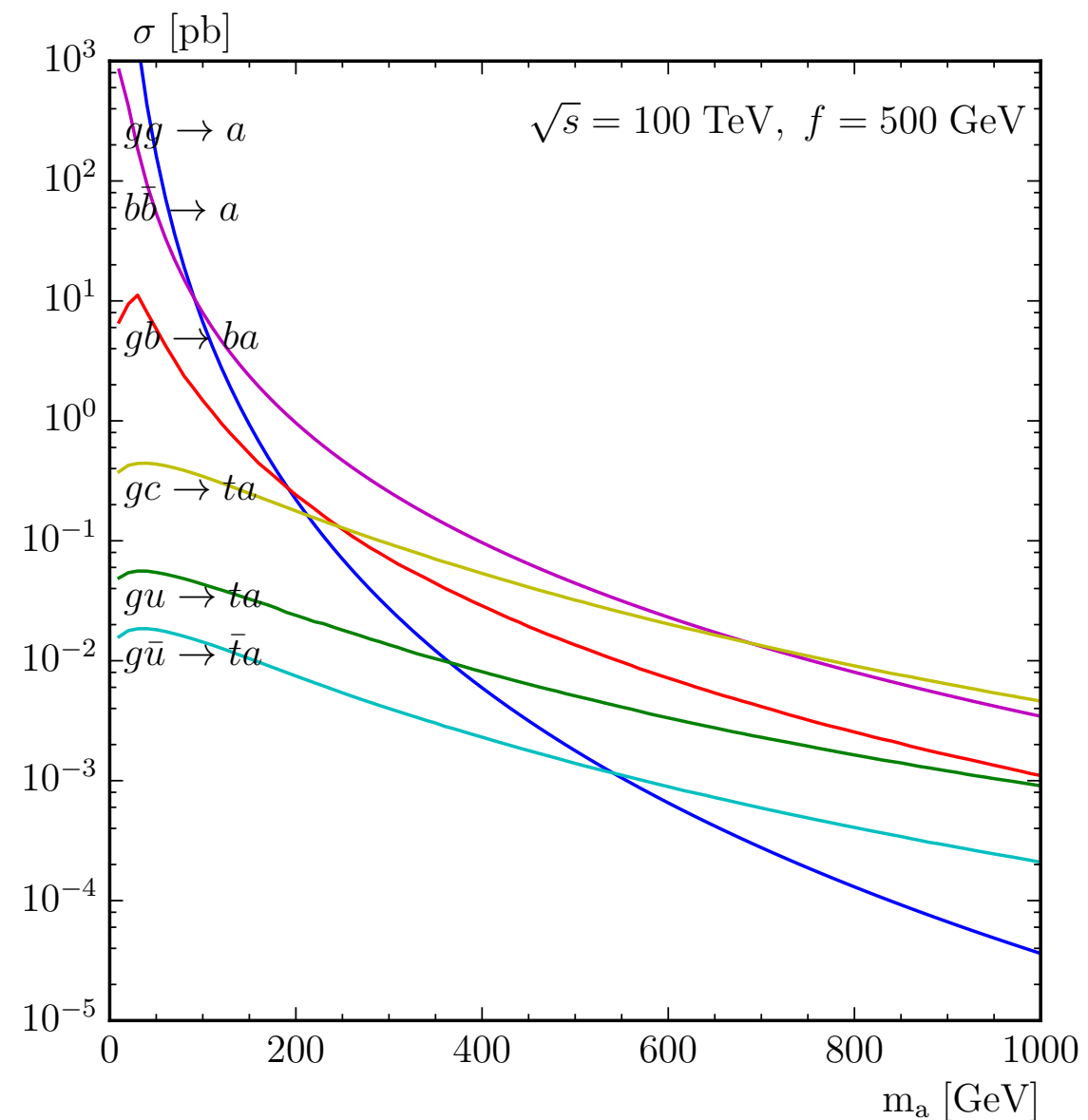


Future Collider Searches

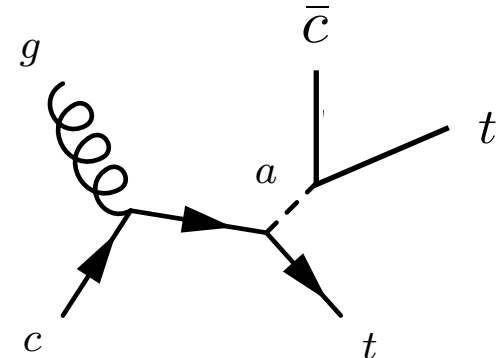
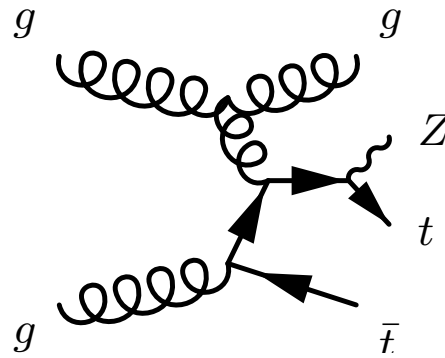
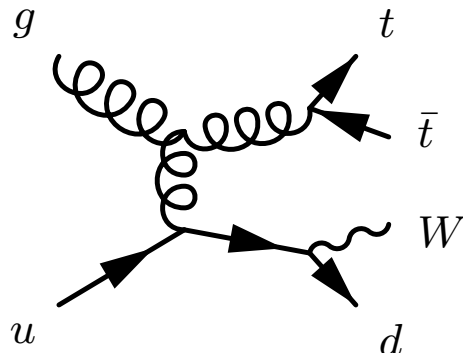
Production Cross
Sections at 100 TeV



The huge
background and
the BRs make
decays into taus
and bs hopeless!



Future Collider Searches



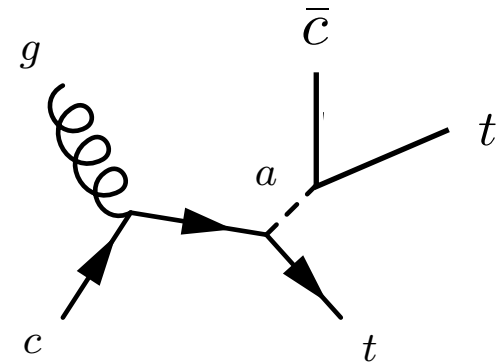
- 2 same-sign leptons(+) (2 hardest ones) with $p_T > 10$ GeV, $|\eta| < 2.5$ $R_{\text{iso}} = 0.2$
- if there is a 3rd lepton of different sign, veto events with $|m_{\ell_i^{(\text{ss})}\ell^{(\text{ds})}} - m_Z| < 15$ GeV
- require for hardest jet $p_T > 100$ GeV
- b -tagging: partonlevel b within $R < 0.3$, assumed efficiency 50 %
- require for the remaining jets $N_b \geq 2$
- $\cancel{p}_T > 50$ GeV
- minimize $R_{\ell_1 b_i} + R_{\ell_2 b_j}$ to define $(\ell b)_1$ and $(\ell b)_2$
- minimize $\Delta y((\ell b)_i, j)$ to define $(\ell b j)$ and (ℓb)
- calculate m_{T2}

Future Collider Searches

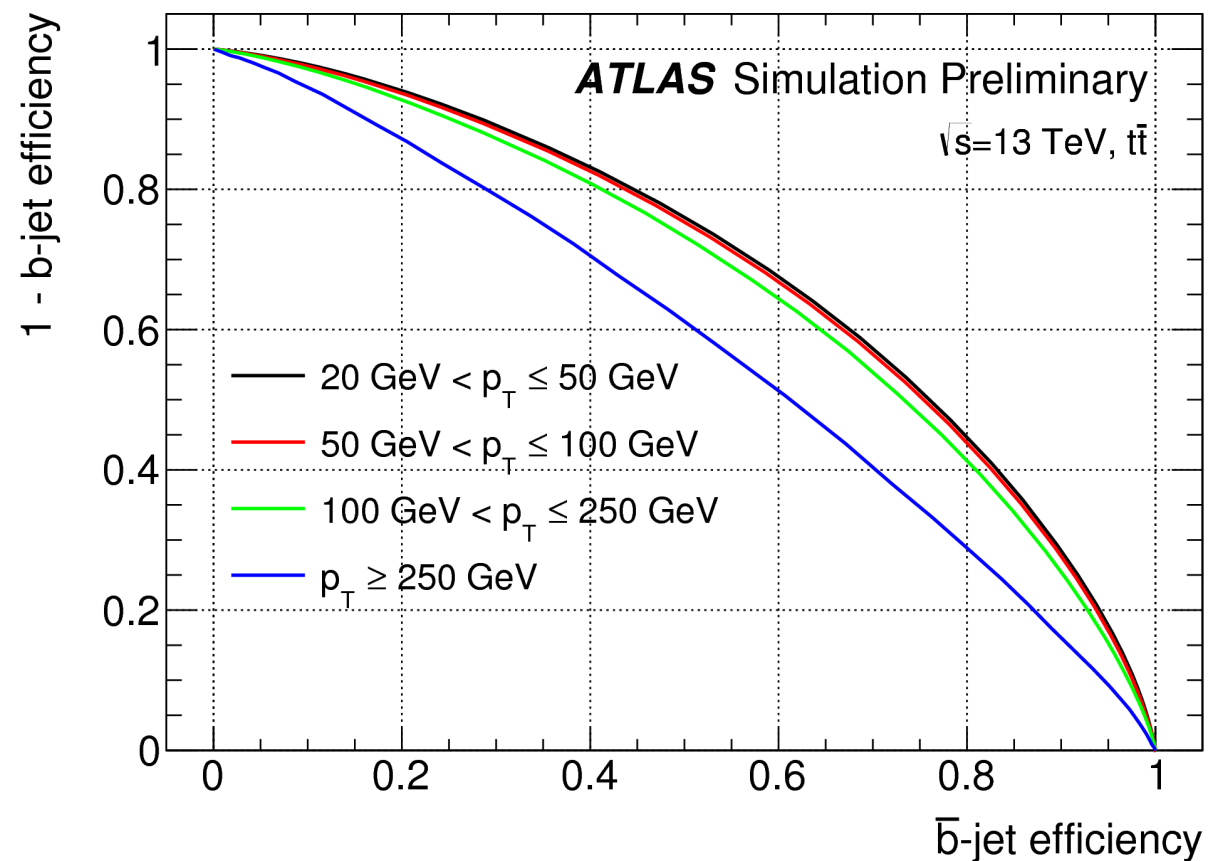
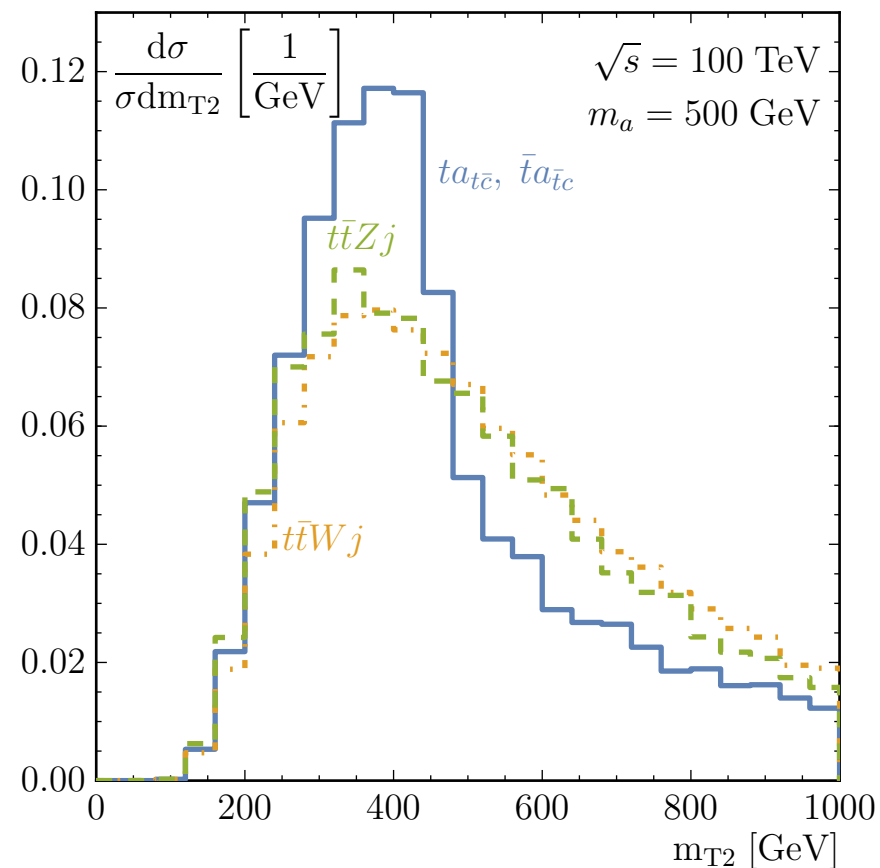
- b - \bar{b} distinction

conservative $\epsilon_b = 0.2, \epsilon_{\bar{b}} = 0.06$

optimistic $\epsilon_b = 0.2, \epsilon_{\bar{b}} = 0.01$



ATL-PHYS-PUB-2015-040

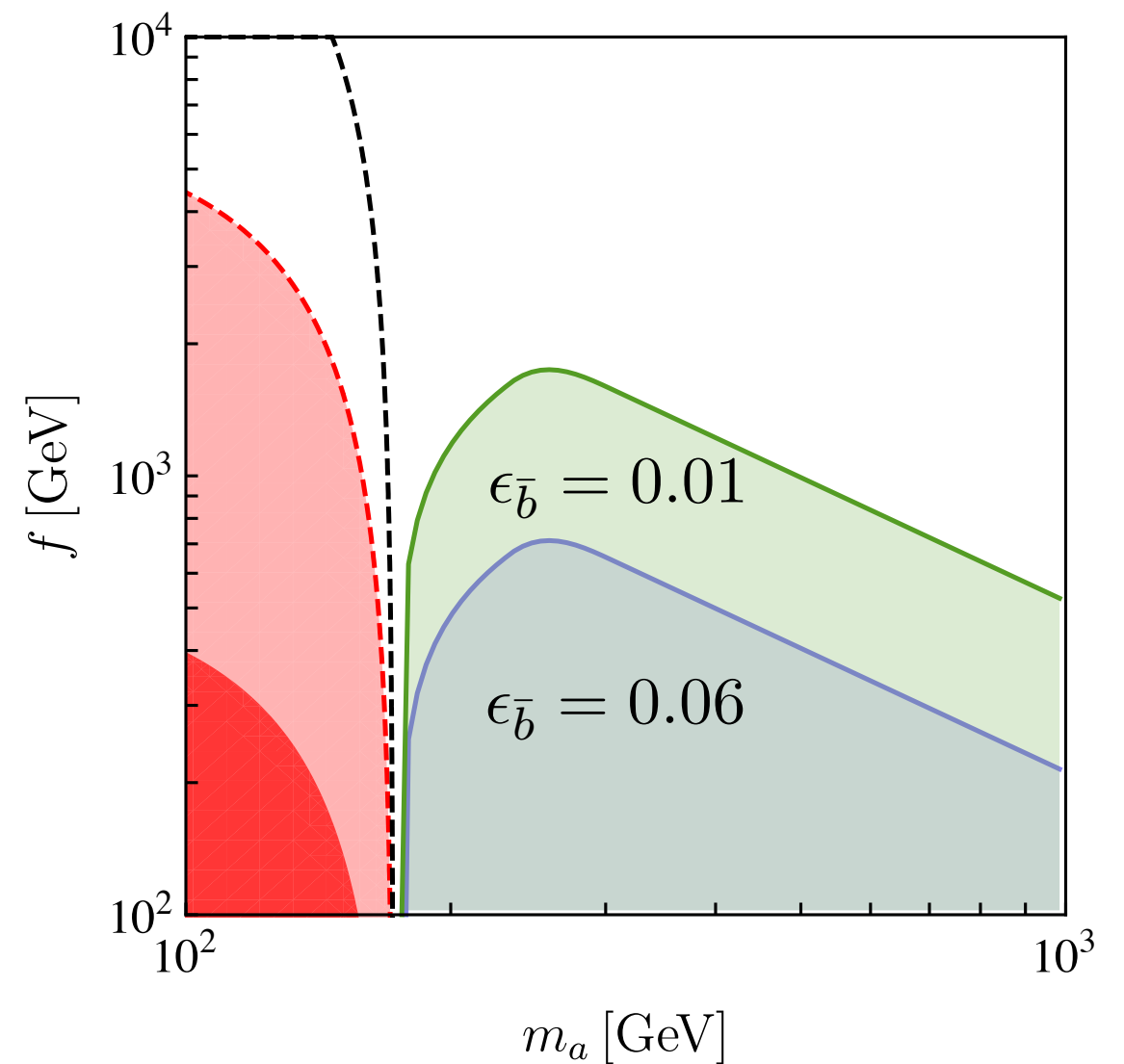
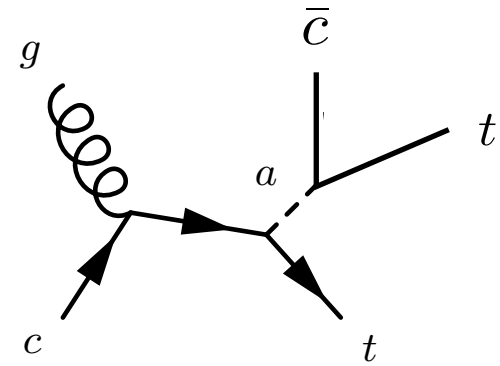


Future Collider Searches

- $b\text{-}\bar{b}$ distinction

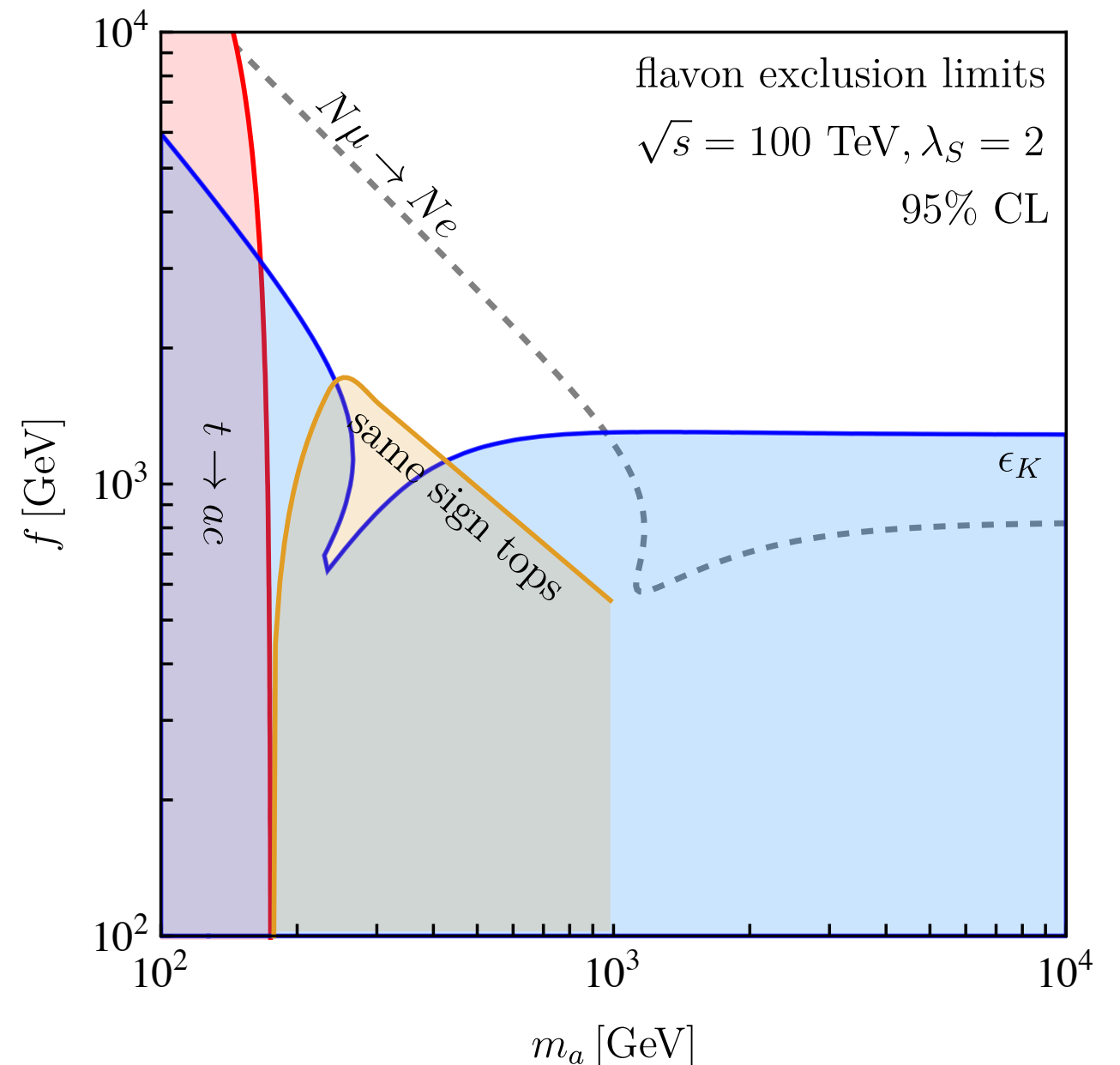
conservative $\epsilon_b = 0.2, \epsilon_{\bar{b}} = 0.06$

optimistic $\epsilon_b = 0.2, \epsilon_{\bar{b}} = 0.01$



Future Collider Searches

- Next generation lepton flavor experiments will cut deep into the parameter space
- A 100 TeV collider is our first semi-realistic shot at discovering a flavon



Why should the flavor scale be low?

- Why not?
- A link to Baryogenesis?
- A link to Dark Matter?
- It could be related to the electroweak scale

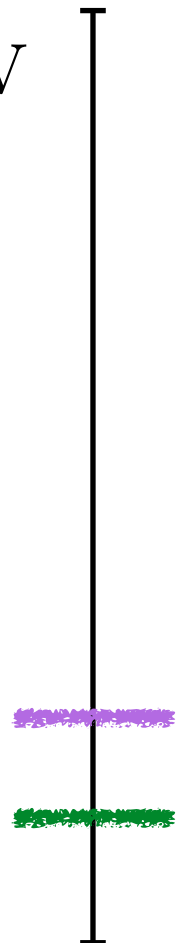
Why should the flavor scale be low?

- Why not?
- A link to Baryogenesis?
- A link to Dark Matter?
- It could be related to the electroweak scale

Planck Scale

$$M_{\text{Pl}} = 10^{19} \text{ GeV}$$

EW Scale $f \approx v$



Flavor from the Electroweak Scale?

$$y_b \left(\frac{S}{\Lambda} \right)^{n_b} \bar{Q}_L H b_R \rightarrow y_b \left(\frac{H^\dagger H}{\Lambda^2} \right)^{n_b} \bar{Q}_L H b_R$$

with $\epsilon = \frac{v^2}{2\Lambda^2} = \frac{m_b}{m_t} \Rightarrow \Lambda \approx (5 - 6) v$

Two drawbacks:

- The flavon is a flavor singlet
- The coupling to b quarks is

[Babu 033002]

[Giudice, Lebedev 0804.1753]

$$g_{hbb} \propto 3 \frac{m_b}{v} \quad \Gamma(h \rightarrow b\bar{b}) \approx 9 \times \Gamma(h \rightarrow b\bar{b})_{\text{SM}}$$

Flavor from the Electroweak Scale

$$y_b \left(\frac{S}{\Lambda} \right)^{n_b} \bar{Q}_L H b_R \rightarrow y_b \left(\frac{H_u H_d}{\Lambda^2} \right)^{n_b} \bar{Q}_L H_d b_R$$

$$\text{with } \epsilon = \frac{v_u v_d}{\Lambda^2} = \frac{m_b}{m_t} \Rightarrow \Lambda \approx (5 - 6) v \sqrt{\frac{\tan \beta}{1 + \tan^2 \beta}}$$

$$\tan \beta = \mathcal{O}(1), \quad \Lambda \approx 1 \text{TeV}$$

Flavor from the Electroweak Scale

$$\mathcal{L}_{\text{Yuk}} = y_{ij}^u \left(\frac{H_u H_d}{\Lambda^2} \right)^{a_i - a_{uj} - a_{H_u}} \bar{Q}_i H_u u_{Rj} + y_{ij}^d \left(\frac{H_u H_d}{\Lambda^2} \right)^{a_i - a_{dj} - a_{H_d}} \bar{Q}_i H_d d_{Rj} + h.c.$$

11 Flavour charges, 8 + 2 conditions

$$m_t \approx \frac{v_u}{\sqrt{2}}, \quad \frac{m_b}{m_t} \approx \frac{m_c}{m_t} \approx \varepsilon^1, \quad \frac{m_s}{m_t} \approx \varepsilon^2, \quad \frac{m_d}{m_t} \approx \frac{m_u}{m_t} \approx \varepsilon^3.$$

$$V_{\text{CKM}} \approx \begin{pmatrix} 1 & 1 & \epsilon \\ 1 & 1 & \epsilon \\ \epsilon & \epsilon & 1 \end{pmatrix}$$

A rescaling freedom remains

$$\begin{aligned} a_{H_u} &= 1, & a_1 &= 2, & a_u &= -2, & a_d &= -1, \\ a_{H_d} &= 0, & a_2 &= 2, & a_c &= 0, & a_s &= 0, \\ & & a_3 &= 1, & a_t &= 0, & a_b &= 0. \end{aligned}$$

$$m_t = 172 \text{ GeV}$$

$$m_b \approx m_c \approx 2.9 \text{ GeV}$$

$$m_s = 50 \text{ MeV}$$

$$m_u = m_d \approx 1 \text{ MeV}$$

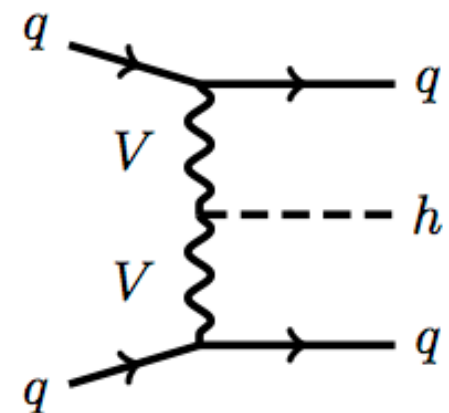
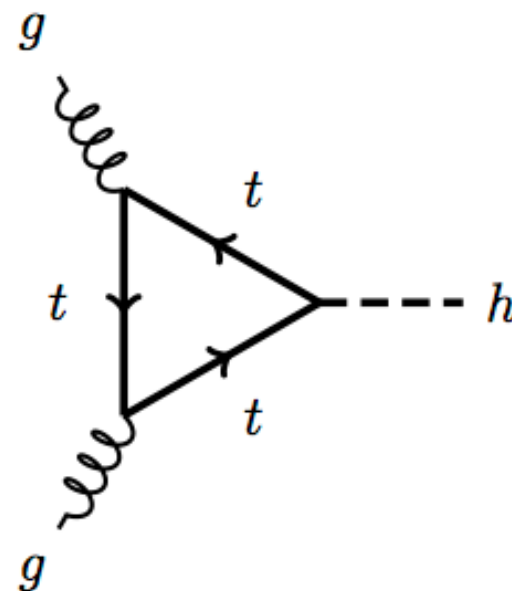
Higgs Couplings

- Couplings are rescaled $g_{hVV} = \kappa_V g_{hVV}^{\text{SM}}$ $g_{hff} = \kappa_f g_{hff}^{\text{SM}}$
- To W^\pm, Z fixed by gauge symmetry:

$$\kappa_V = \sin(\beta - \alpha)$$

- To the top: $\kappa_t = \kappa_t^{\text{II HDM}} = \frac{\cos \alpha}{\sin \beta}$

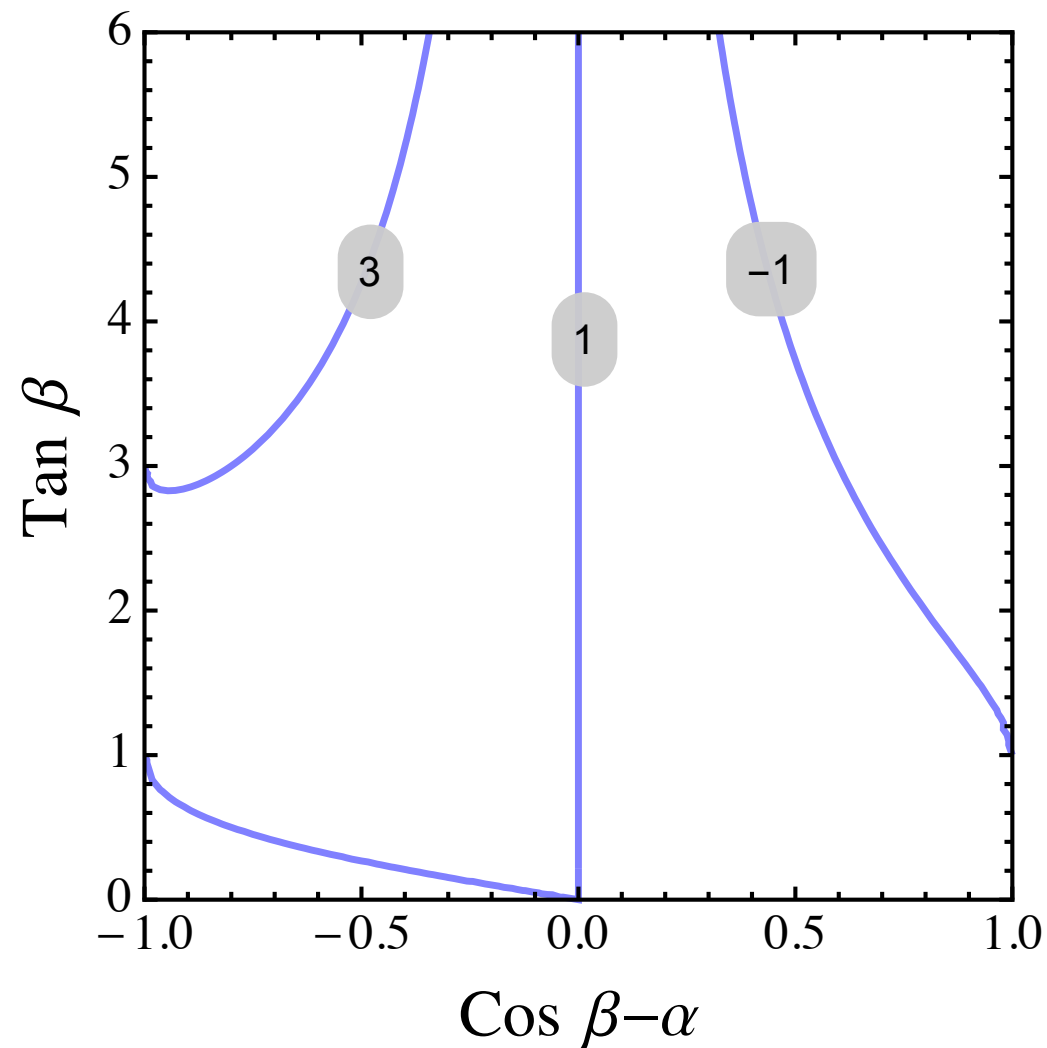
Higgs Production like
in a 2HDM of type II



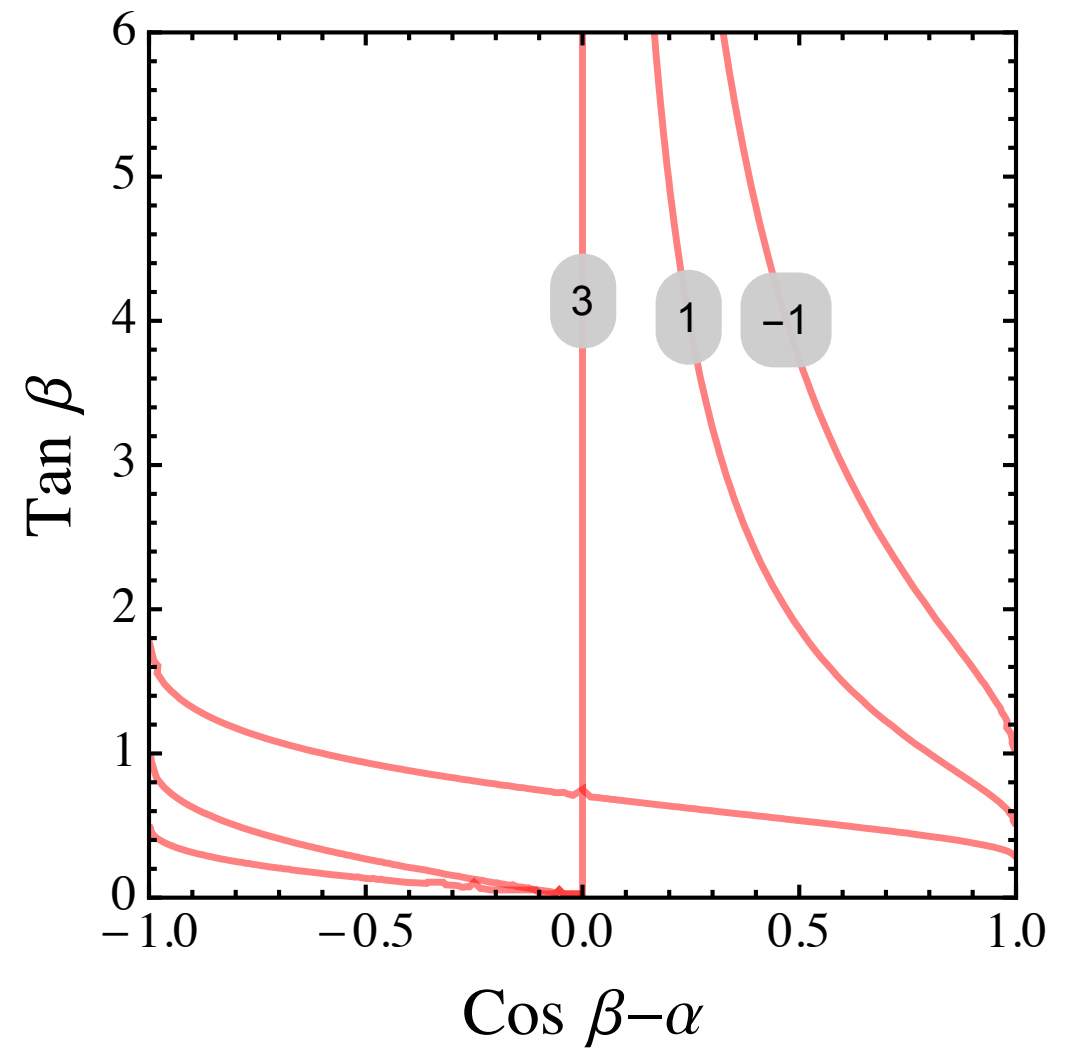
Higgs Couplings

- To the bottom:

$$\kappa_b^{\text{II HDM}} = -\frac{\sin \alpha}{\cos \beta}$$



$$\kappa_b = -2\frac{\sin \alpha}{\cos \beta} + \frac{\cos \alpha}{\sin \beta}$$



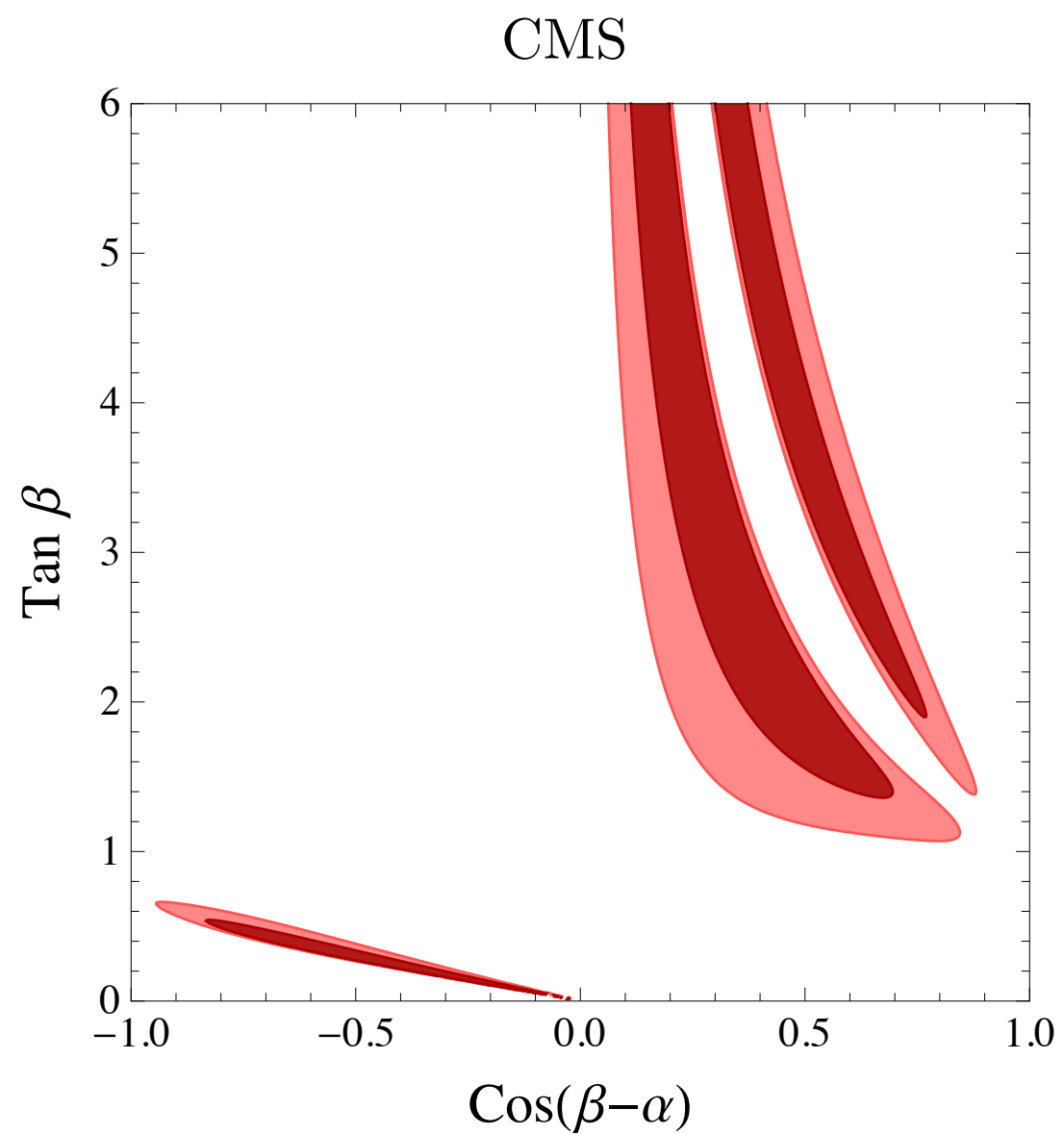
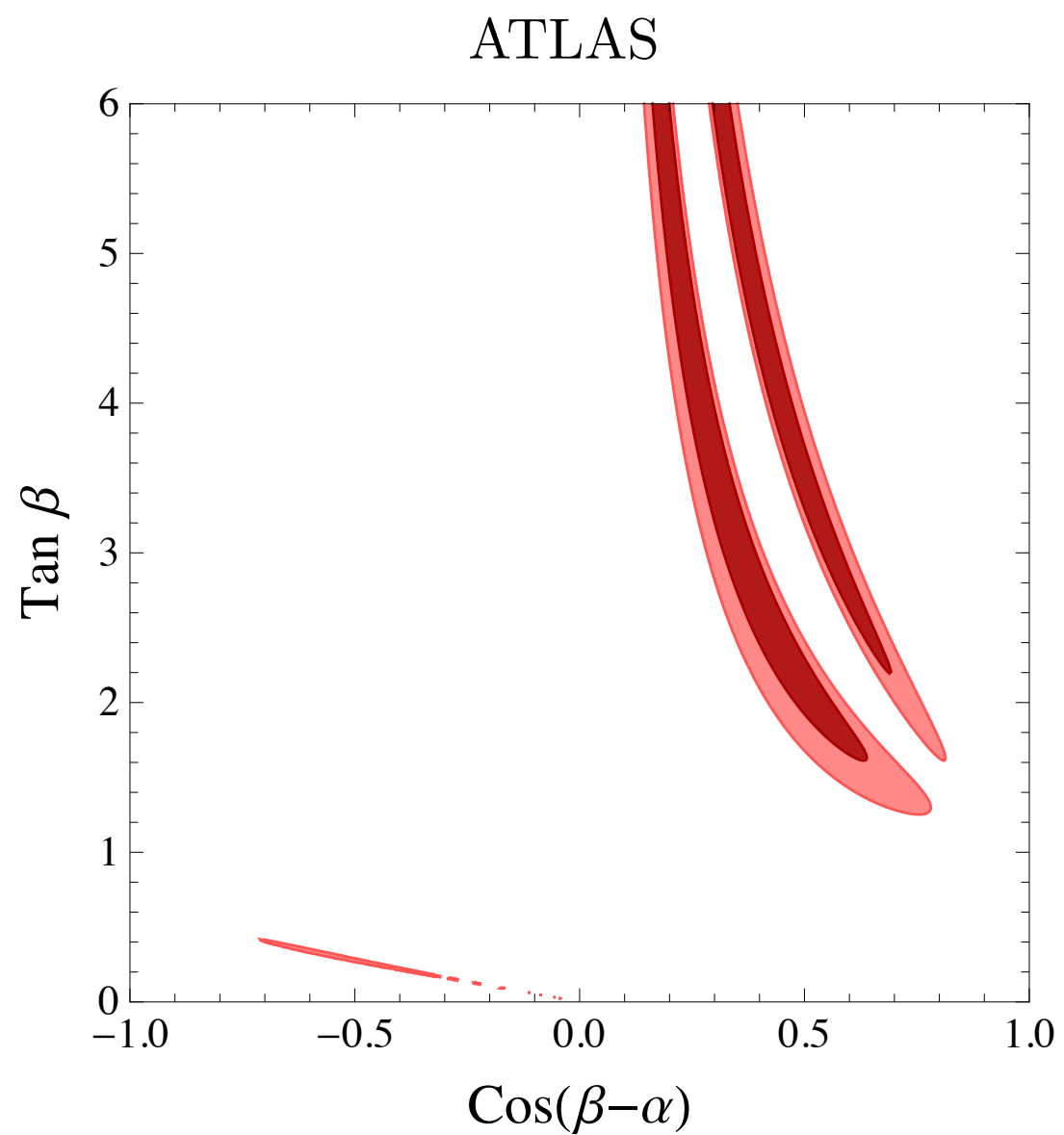
Global Higgs Fit

We performed a global Higgs fit to 8 different channels at ATLAS & CMS

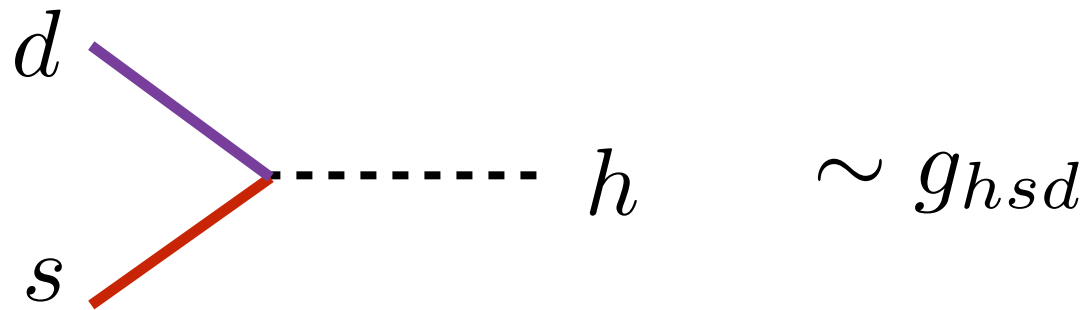
$$\mu_X = \frac{\sigma_{\text{prod}}}{\sigma_{\text{prod}}^{\text{SM}}} \frac{\Gamma_{h \rightarrow X}}{\Gamma_{h \rightarrow X}^{\text{SM}}} \frac{\Gamma_{h, \text{tot}}^{\text{SM}}}{\Gamma_h}$$

Decay Mode	Production Channels $\sigma_{gg \rightarrow h}, \sigma_{t\bar{t} \rightarrow h}$	Production Channels $\sigma_{VBF}, \sigma_{VH}$	Experiment
$h \rightarrow WW^*$	$\mu_W = 1.02^{+0.29}_{-0.26}$ [17] $\mu_W \simeq 0.75 \pm 0.35$ [18]	$\mu_W = 1.27^{+0.53}_{-0.45}$ [17] $\mu_W \simeq 0.7 \pm 0.85$ [18]	ATLAS CMS
$h \rightarrow ZZ^*$	$\mu_Z = 1.7^{+0.5}_{-0.4}$ [19] $\mu_Z = 0.8^{+0.46}_{-0.36}$ [20]	$\mu_Z = 0.3^{+1.6}_{-0.9}$ [19] $\mu_Z = 1.7^{+2.2}_{-2.1}$ [20]	ATLAS CMS
$h \rightarrow \gamma\gamma$	$\mu_\gamma = 1.32 \pm 0.38$ [21] $\mu_\gamma = 1.13^{+0.37}_{-0.31}$ [22]	$\mu_\gamma = 0.8 \pm 0.7$ [21] $\mu_\gamma = 1.16^{+0.63}_{-0.58}$ [22]	ATLAS CMS
$h \rightarrow \bar{b}b$	$\mu_b = 1.5 \pm 1.1$ [23] $\mu_b = 0.67^{+1.35}_{-1.33}$ [25]	$\mu_b = 0.52 \pm 0.32 \pm 0.24$ [24] $\mu_b = 1.0 \pm 0.5$ [26]	ATLAS CMS
$h \rightarrow \tau\tau$	$\mu_\tau = 2.0 \pm 0.8^{+1.2}_{-0.8} \pm 0.3$ [27] $\mu_\tau \simeq 0.5^{+0.8}_{-0.7}$ [28]	$\mu_\tau = 1.24^{+0.49}_{-0.45} {}^{+0.31}_{-0.29} \pm 0.08$ [27] $\mu_\tau \simeq 1.1^{+0.7}_{-0.5}$ [28]	ATLAS CMS

Global Higgs Fit



Flavor from the Electroweak Scale



Universal function

$$f^h(\alpha, \beta) = \frac{c_\alpha}{s_\beta} - \frac{s_\alpha}{c_\beta}$$

$$g_{h d_i d_i} = \left(\frac{c_\alpha}{s_\alpha} + n_{d_i} f^h(\alpha, \beta) \right) \frac{m_{d_i}}{v}$$

$$g_{h d_i d_j} = \left(Q_{ij} \frac{m_{d_j}}{v} - \frac{m_{d_i}}{v} \mathcal{D}_{ij} \right) f^h(\alpha, \beta)$$

$$Q^u \sim Q^d \sim \begin{pmatrix} 2 & \varepsilon^2 & \varepsilon \\ \varepsilon^2 & 2 & \varepsilon \\ \varepsilon & \varepsilon & 1 \end{pmatrix}, \quad \mathcal{U} \sim \begin{pmatrix} -2 & \varepsilon^2 & \varepsilon^2 \\ \varepsilon^2 & \varepsilon^2 & \varepsilon^4 \\ \varepsilon^2 & \varepsilon^4 & \varepsilon^4 \end{pmatrix}, \quad \mathcal{D} \sim \begin{pmatrix} -1 & \varepsilon & \varepsilon \\ \varepsilon & \varepsilon^2 & \varepsilon^2 \\ \varepsilon & \varepsilon^2 & \varepsilon^2 \end{pmatrix}$$

Flavor from the Electroweak Scale

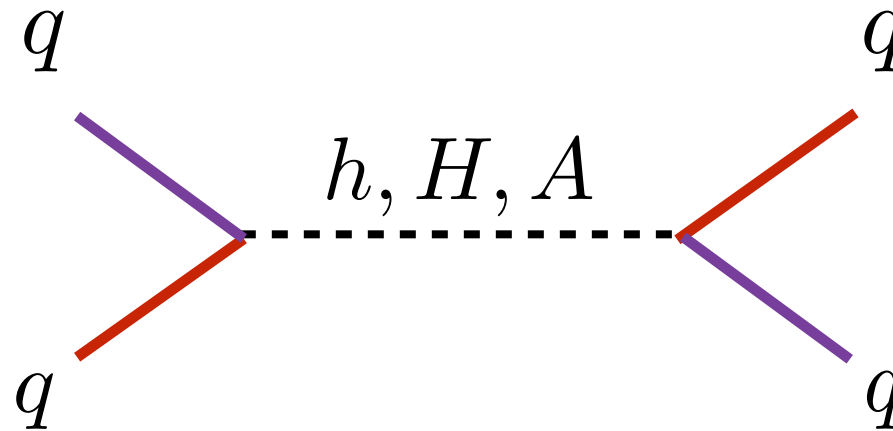
$$\begin{array}{c} d \\ \diagdown \\ \text{---} \\ \diagup \\ s \end{array} \text{---} h \quad \sim \quad \frac{m_s}{v} \epsilon f^h(\alpha, \beta) \approx 3 \times 10^{-6} \times f^h(\alpha, \beta)$$

$$g_{hd_i d_i} = \left(\frac{c_\alpha}{s_\alpha} + n_{d_i} f^h(\alpha, \beta) \right) \frac{m_{d_i}}{v}$$

$$g_{hd_i d_j} = \left(Q_{ij} \frac{m_{d_j}}{v} - \frac{m_{d_i}}{v} \mathcal{D}_{ij} \right) f^h(\alpha, \beta)$$

$$Q^u \sim Q^d \sim \begin{pmatrix} 2 & \epsilon^2 & \epsilon \\ \epsilon^2 & 2 & \epsilon \\ \epsilon & \epsilon & 1 \end{pmatrix}, \quad \mathcal{U} \sim \begin{pmatrix} -2 & \epsilon^2 & \epsilon^2 \\ \epsilon^2 & \epsilon^2 & \epsilon^4 \\ \epsilon^2 & \epsilon^4 & \epsilon^4 \end{pmatrix}, \quad \mathcal{D} \sim \begin{pmatrix} -1 & \epsilon & \epsilon \\ \epsilon & \epsilon^2 & \epsilon^2 \\ \epsilon & \epsilon^2 & \epsilon^2 \end{pmatrix}$$

Flavor from the Electroweak Scale

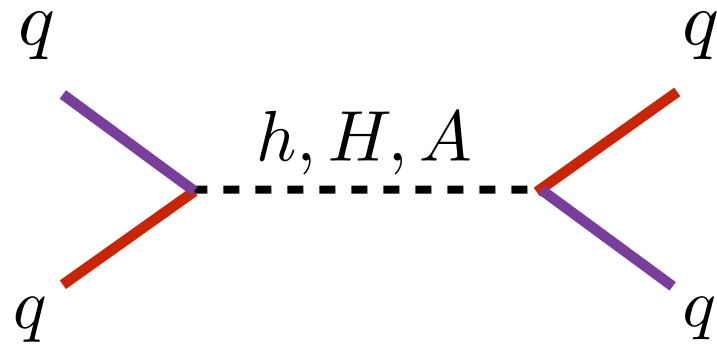


$$g_{hd_i d_j} = g^h(\alpha, \beta) \left(\frac{m_d}{v} \right)_{ij} + f^h(\alpha, \beta) \left[\mathcal{Q}_{ij}^d \left(\frac{m_d}{v} \right)_{jj} - \left(\frac{m_d}{v} \right)_{ii} \mathcal{D}_{ij} \right]$$

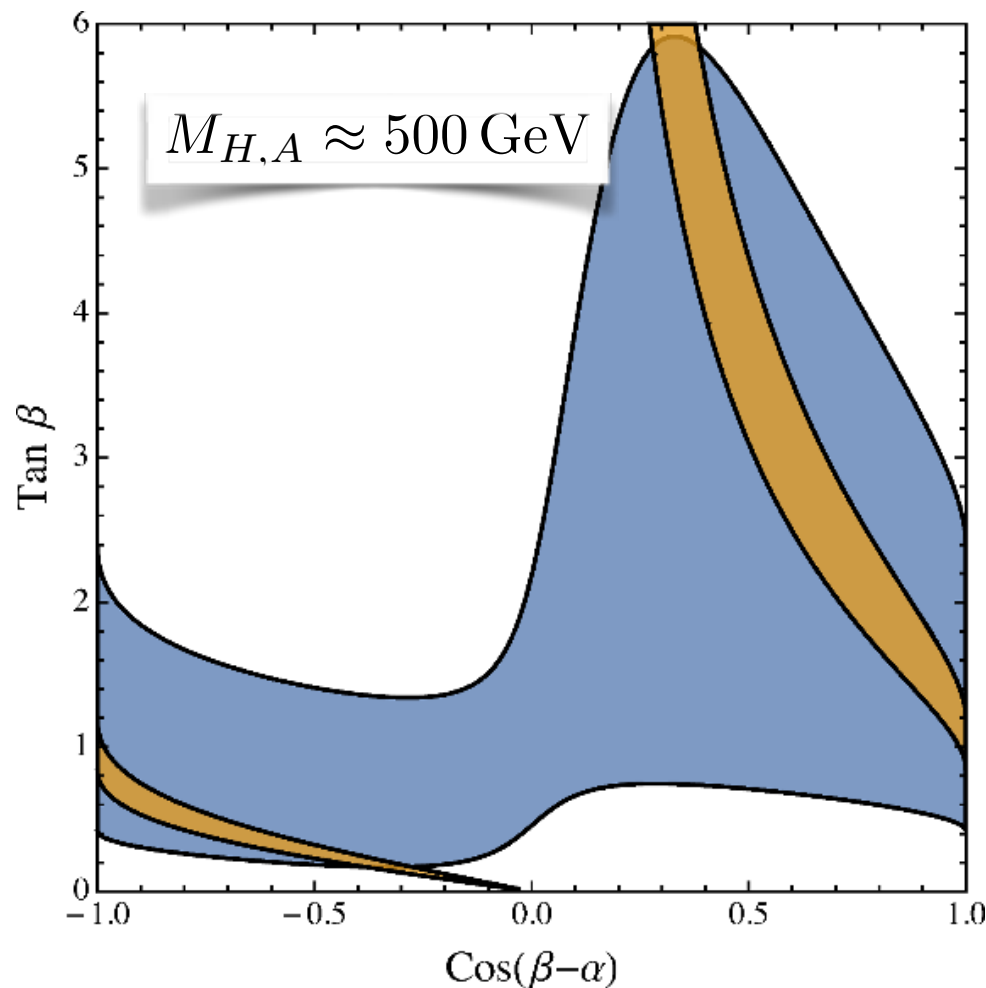
$$g_{Hd_i d_j} = G^H(\alpha, \beta) \left(\frac{m_d}{v} \right)_{ij} + F^H(\alpha, \beta) \left[\mathcal{Q}_{ij}^d \left(\frac{m_d}{v} \right)_{jj} - \left(\frac{m_d}{v} \right)_{ii} \mathcal{D}_{ij}^d \right]$$

$$g_{Ad_i d_j} = G^A(\alpha, \beta) \left(\frac{m_d}{v} \right)_{ij} + F^A(\alpha, \beta) \left[\mathcal{Q}_{ij}^d \left(\frac{m_d}{v} \right)_{jj} - \left(\frac{m_d}{v} \right)_{ii} \mathcal{D}_{ij}^d \right]$$

Constraints from Meson Mixing

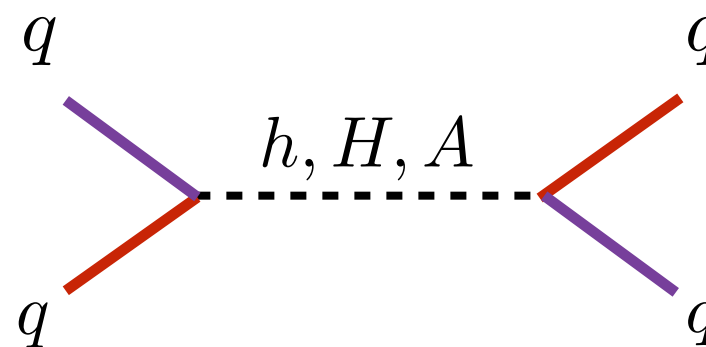


$$\approx \varepsilon^X \frac{m_q^2}{v^2} \left\{ \frac{f^h(\alpha, \beta)^2}{m_h^2} + \frac{F^H(\alpha, \beta)^2}{M_H^2} \pm \frac{F^A(\alpha, \beta)^2}{M_A^2} \right\}$$



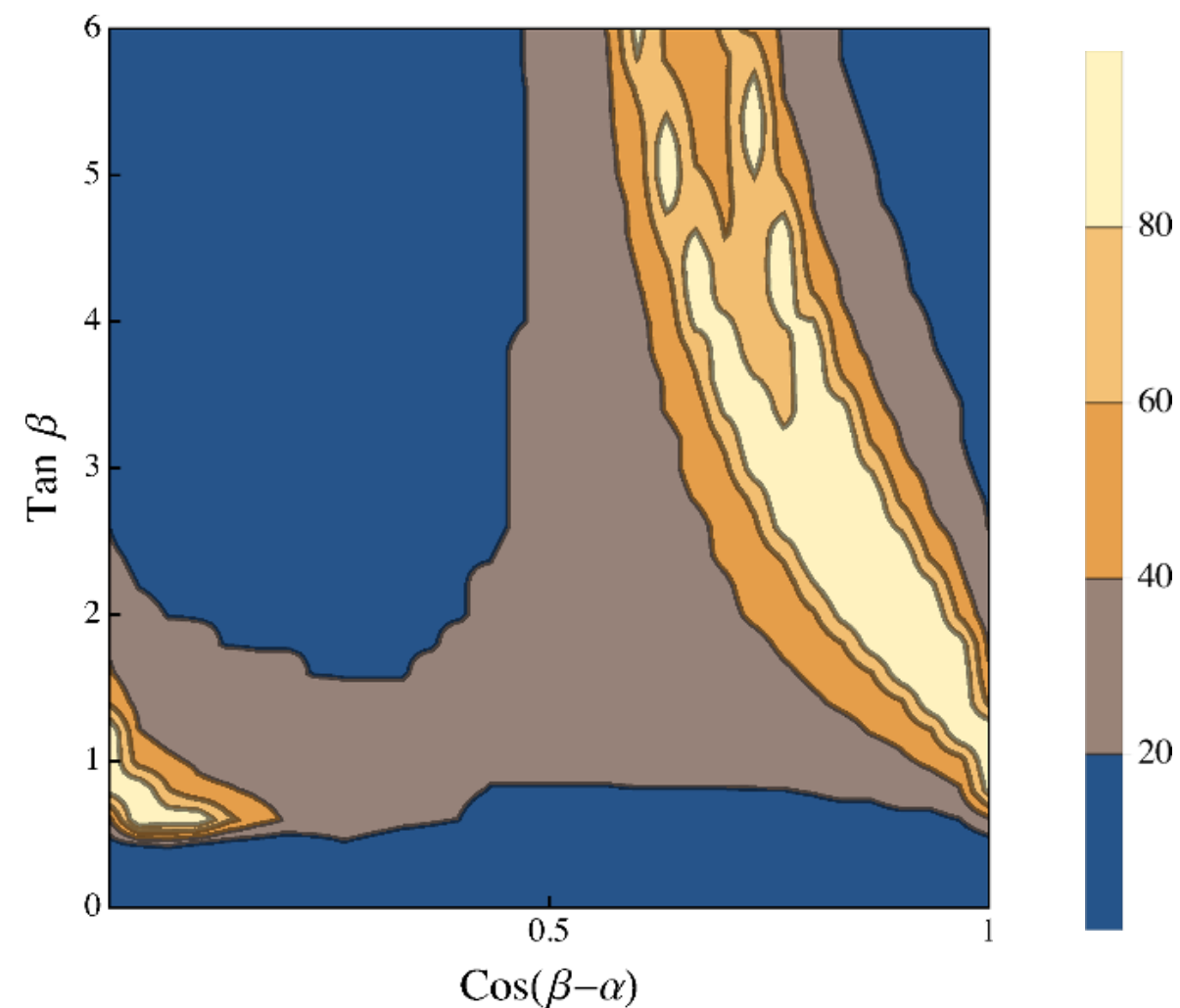
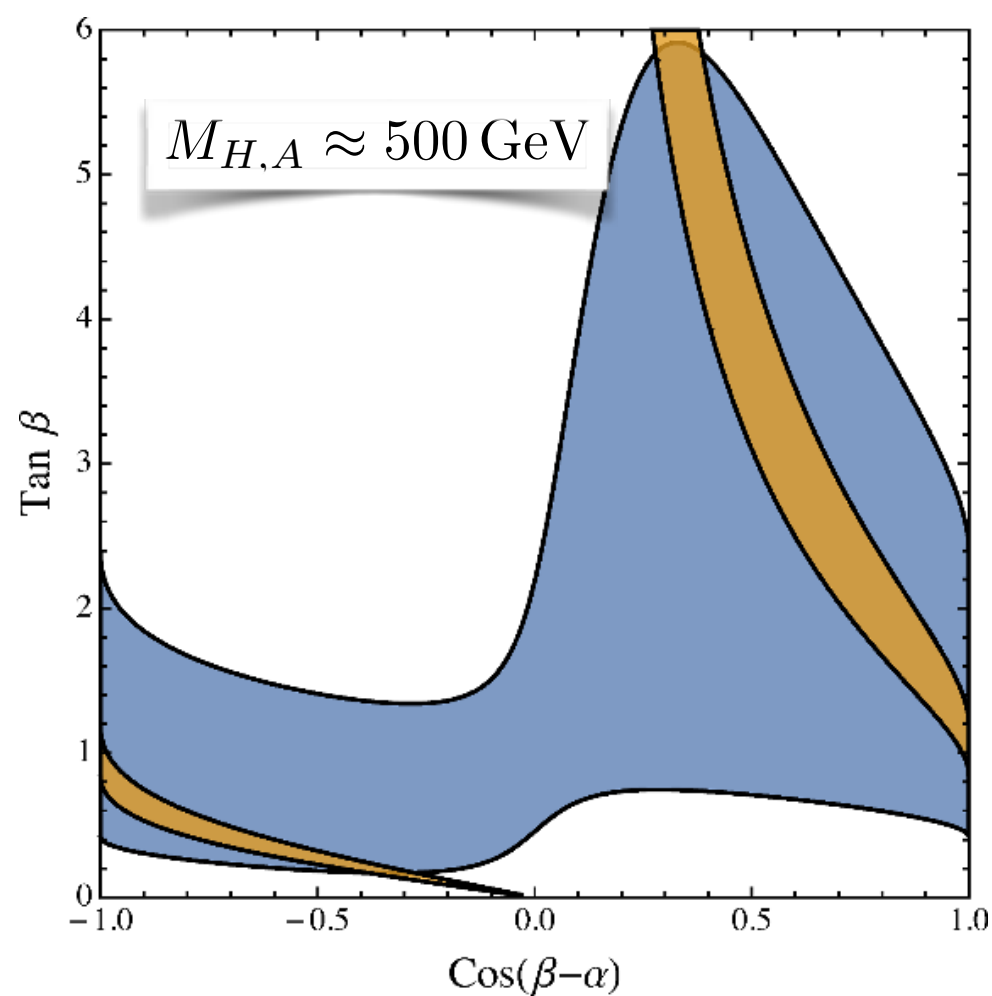
$$\begin{aligned} \mathcal{H}_{\text{eff}}^{\Delta S=2} = & C_1^{sd} (\bar{s}_L \gamma_\mu d_L)^2 + \tilde{C}_1^{sd} (\bar{s}_R \gamma_\mu d_R)^2 \\ & + C_2^{sd} (\bar{s}_R d_L)^2 + \tilde{C}_2^{sd} (\bar{s}_L d_R)^2 \\ & + C_4^{sd} (\bar{s}_R d_L) (\bar{s}_L d_R) \\ & + C_5^{sd} (\bar{s}_L \gamma_\mu d_L) (\bar{s}_R \gamma^\mu d_R) + h.c. \end{aligned}$$

$K^0 - \bar{K}^0$ Mixing



A Feynman diagram showing the exchange of a scalar particle (dashed line) between two quark pairs. The incoming quarks on the left are labeled q (purple line) and q (red line). The outgoing quarks on the right are labeled q (red line) and q (purple line). The dashed line is labeled h, H, A .

$$\approx \varepsilon_X \frac{m_q^2}{v^2} \left\{ \frac{f^h(\alpha, \beta)^2}{m_h^2} + \frac{F^H(\alpha, \beta)^2}{M_H^2} \pm \frac{F^A(\alpha, \beta)^2}{M_A^2} \right\}$$



$K^0 - \bar{K}^0$ Mixing

$$\begin{array}{c} \diagup \\ \diagdown \end{array} \begin{array}{c} \text{purple} \\ \text{red} \end{array} \xrightarrow{h, H, A} \begin{array}{c} \diagdown \\ \diagup \end{array} \begin{array}{c} \text{red} \\ \text{purple} \end{array} \approx \frac{c_i}{v^2} \left\{ \frac{f^h(\alpha, \beta)^2}{m_h^2} + \frac{F^H(\alpha, \beta)^2}{M_h^2} \pm \frac{F^A(\alpha, \beta)^2}{M_A^2} \right\}$$

Flavor dependent Wilson Coefficient

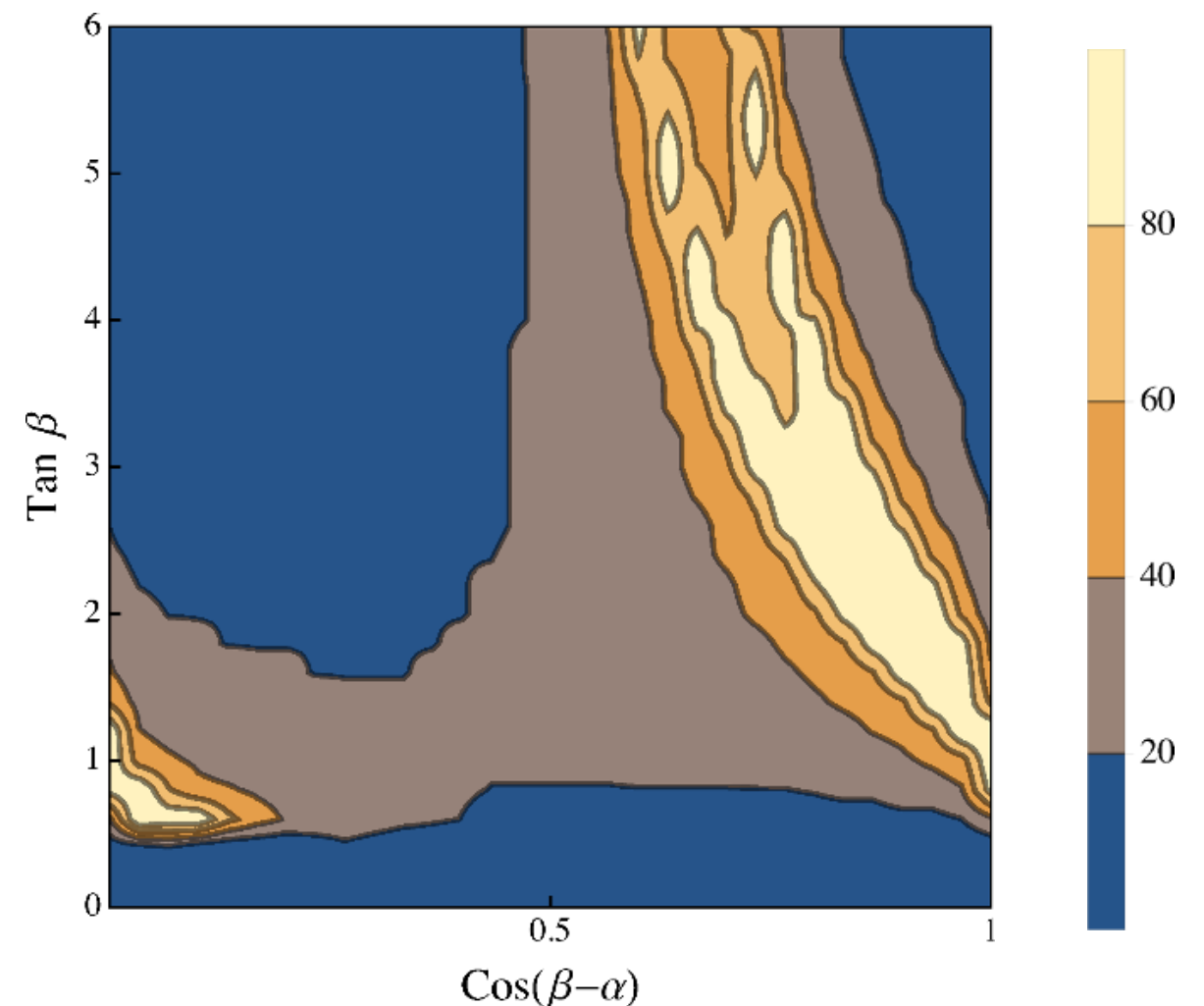
$$Q^d \sim \begin{pmatrix} 2 & \boxed{\varepsilon^2} & \varepsilon \\ \varepsilon^2 & 2 & \varepsilon \\ \varepsilon & \varepsilon & 1 \end{pmatrix} \quad \mathcal{D} \sim \begin{pmatrix} -1 & \boxed{\varepsilon} & \varepsilon \\ \varepsilon & \varepsilon^2 & \varepsilon^2 \\ \varepsilon & \varepsilon^2 & \varepsilon^2 \end{pmatrix}$$

$$c_2^{sd} = \varepsilon^4 m_s^2$$

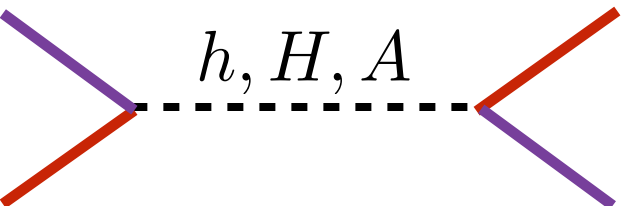
$$\tilde{c}_2^{sd} = \varepsilon^2 m_s^2$$

$$c_4^{sd} = \varepsilon^3 m_s^2$$

$$M_{H,A} \approx 500 \text{ GeV}$$



$B_s^0 - \bar{B}_s^0$ Mixing



$$\approx \frac{c_i}{v^2} \left\{ \frac{f^h(\alpha, \beta)^2}{m_h^2} + \frac{F^H(\alpha, \beta)^2}{M_h^2} \pm \frac{F^A(\alpha, \beta)^2}{M_A^2} \right\}$$

Flavor dependent Wilson Coefficient

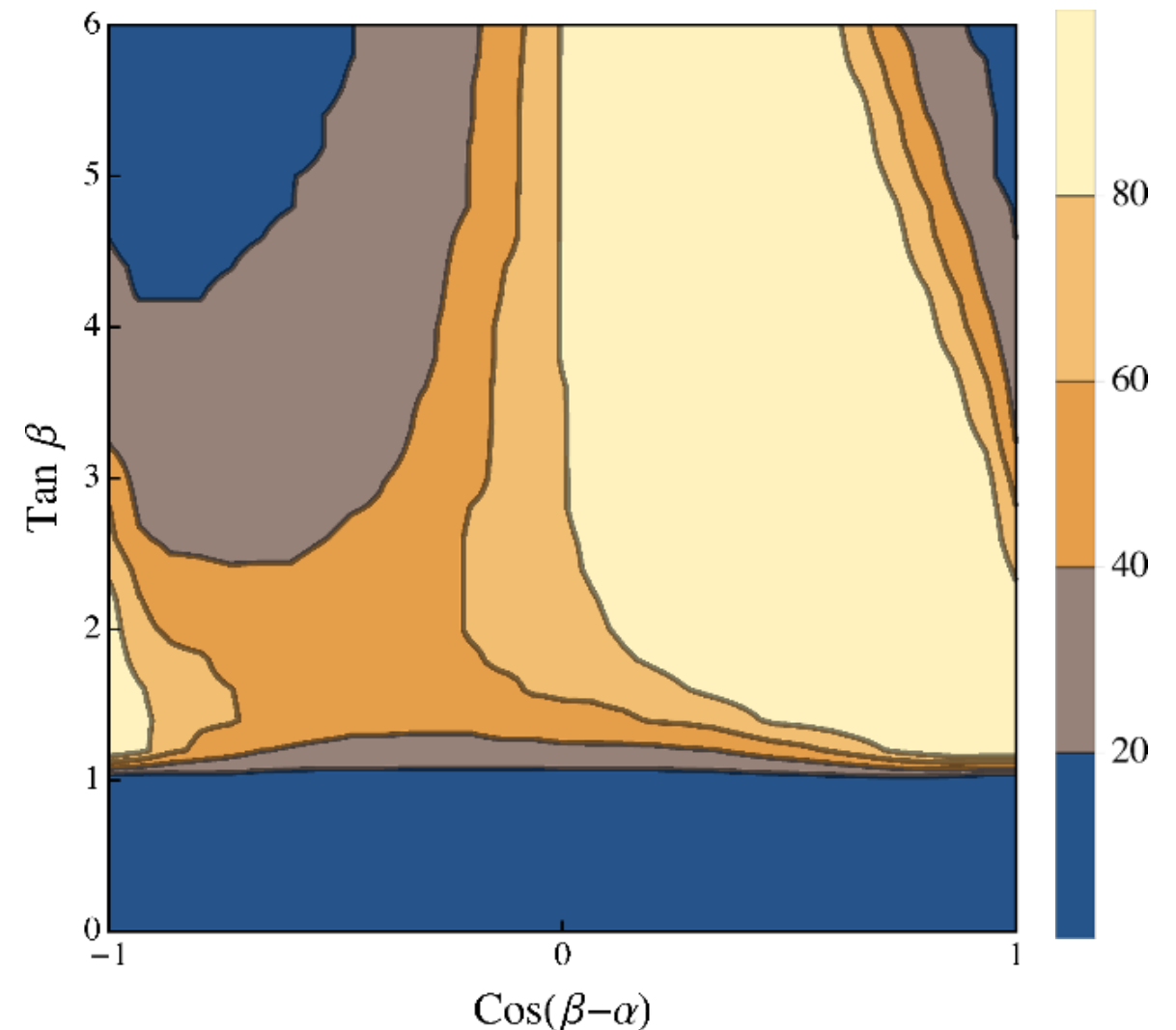
$$Q^d \sim \begin{pmatrix} 2 & \varepsilon^2 & \varepsilon \\ \varepsilon^2 & 2 & \varepsilon \\ \varepsilon & \varepsilon & 1 \end{pmatrix} \quad \mathcal{D} \sim \begin{pmatrix} -1 & \varepsilon & \varepsilon \\ \varepsilon & \varepsilon^2 & \varepsilon^2 \\ \varepsilon & \varepsilon^2 & \varepsilon^2 \end{pmatrix}$$

$$c_2^{bs} = \varepsilon^2 m_b^2$$

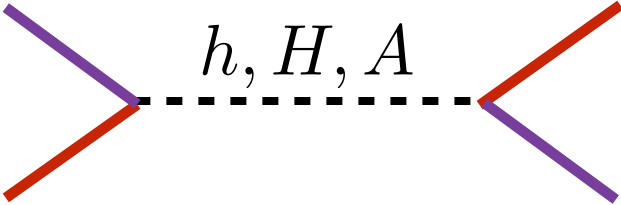
$$\tilde{c}_2^{bs} = \varepsilon^4 m_b^2$$

$$c_4^{bs} = \varepsilon^3 m_b^2$$

$$M_{H,A} \approx 500 \text{ GeV}$$



$B_d^0 - \bar{B}_d^0$ Mixing



$$\approx \frac{c_i}{v^2} \left\{ \frac{f^h(\alpha, \beta)^2}{m_h^2} + \frac{F^H(\alpha, \beta)^2}{M_h^2} \pm \frac{F^A(\alpha, \beta)^2}{M_A^2} \right\}$$

Flavor dependent Wilson Coefficient

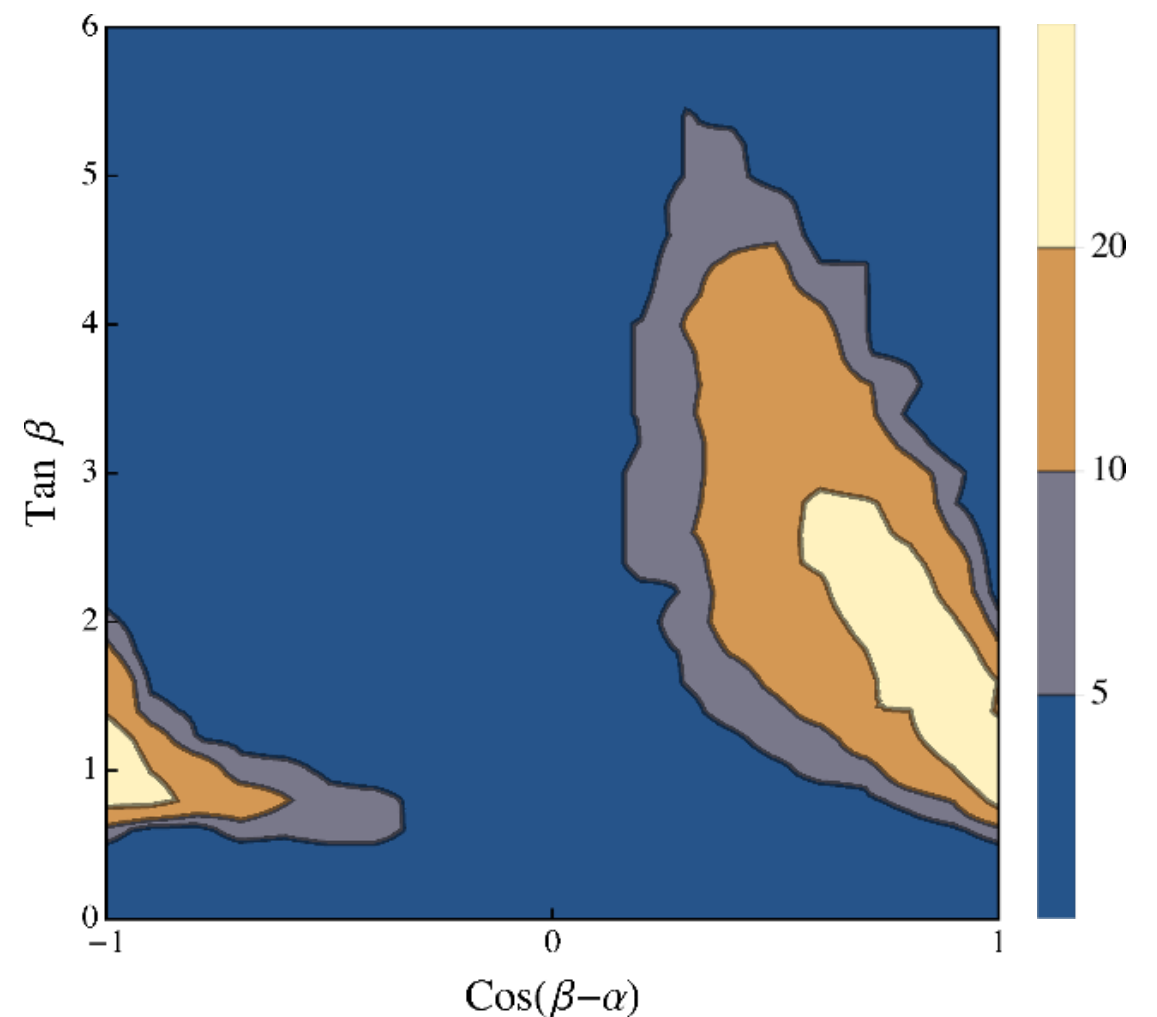
$$Q^d \sim \begin{pmatrix} 2 & \varepsilon^2 & \varepsilon \\ \varepsilon^2 & 2 & \varepsilon \\ \varepsilon & \varepsilon & 1 \end{pmatrix} \quad \mathcal{D} \sim \begin{pmatrix} -1 & \varepsilon & \varepsilon \\ \varepsilon & \varepsilon^2 & \varepsilon^2 \\ \varepsilon & \varepsilon^2 & \varepsilon^2 \end{pmatrix}$$

$$c_2^{bd} = \varepsilon^2 m_b^2$$

$$\tilde{c}_2^{bd} = \varepsilon^2 m_b^2$$

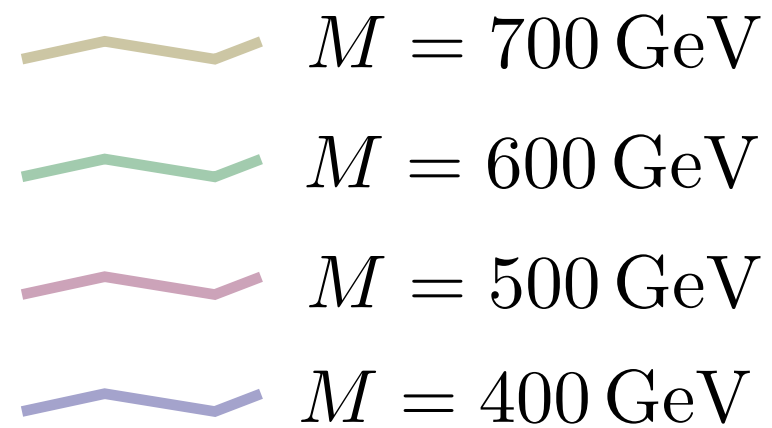
$$c_4^{bd} = \varepsilon^2 m_b^2$$

$$M_{H,A} \approx 500 \text{ GeV}$$

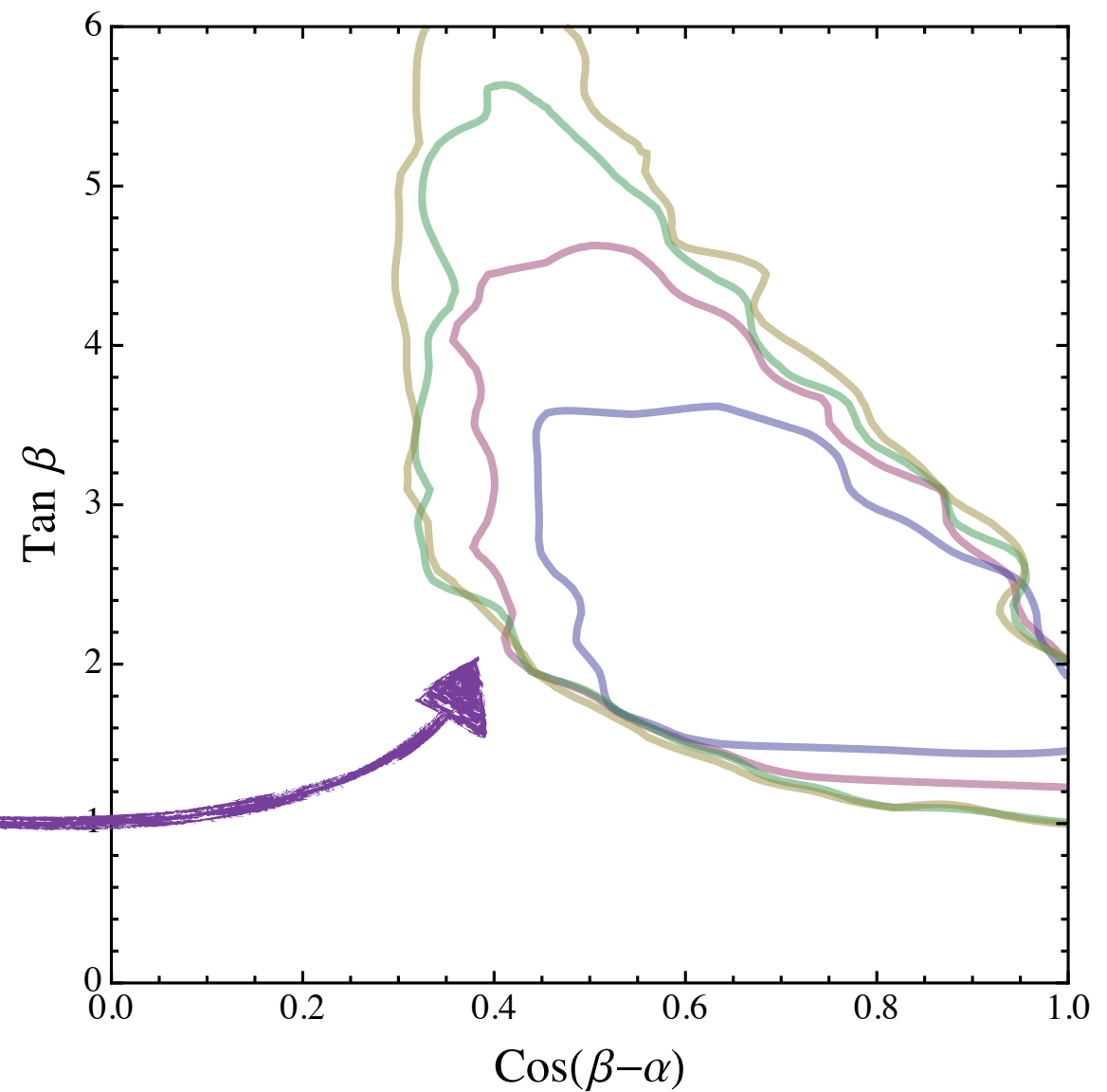


Flavor Bounds

$$M \equiv M_H = M_A = M_{H^\pm}$$



10% Contours

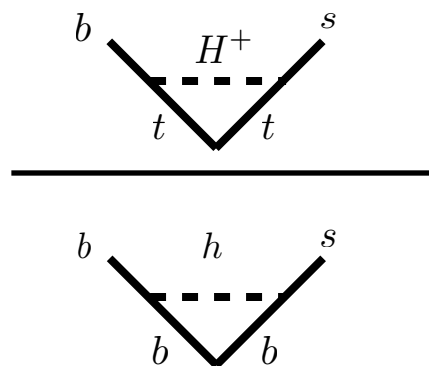


Flavor Bounds

- Contributions to rare leptonic decays depend on the lepton flavor sector
- Bounds from Loop induced processes like $b \rightarrow s\gamma$ put constraints on the mass of the charged scalar

$$M_{H^\pm} \gtrsim 358 \text{ (480) GeV} \quad @ 99\%(95\%) \text{ CL} \quad [\text{Misiak et al. 1503.01789}]$$

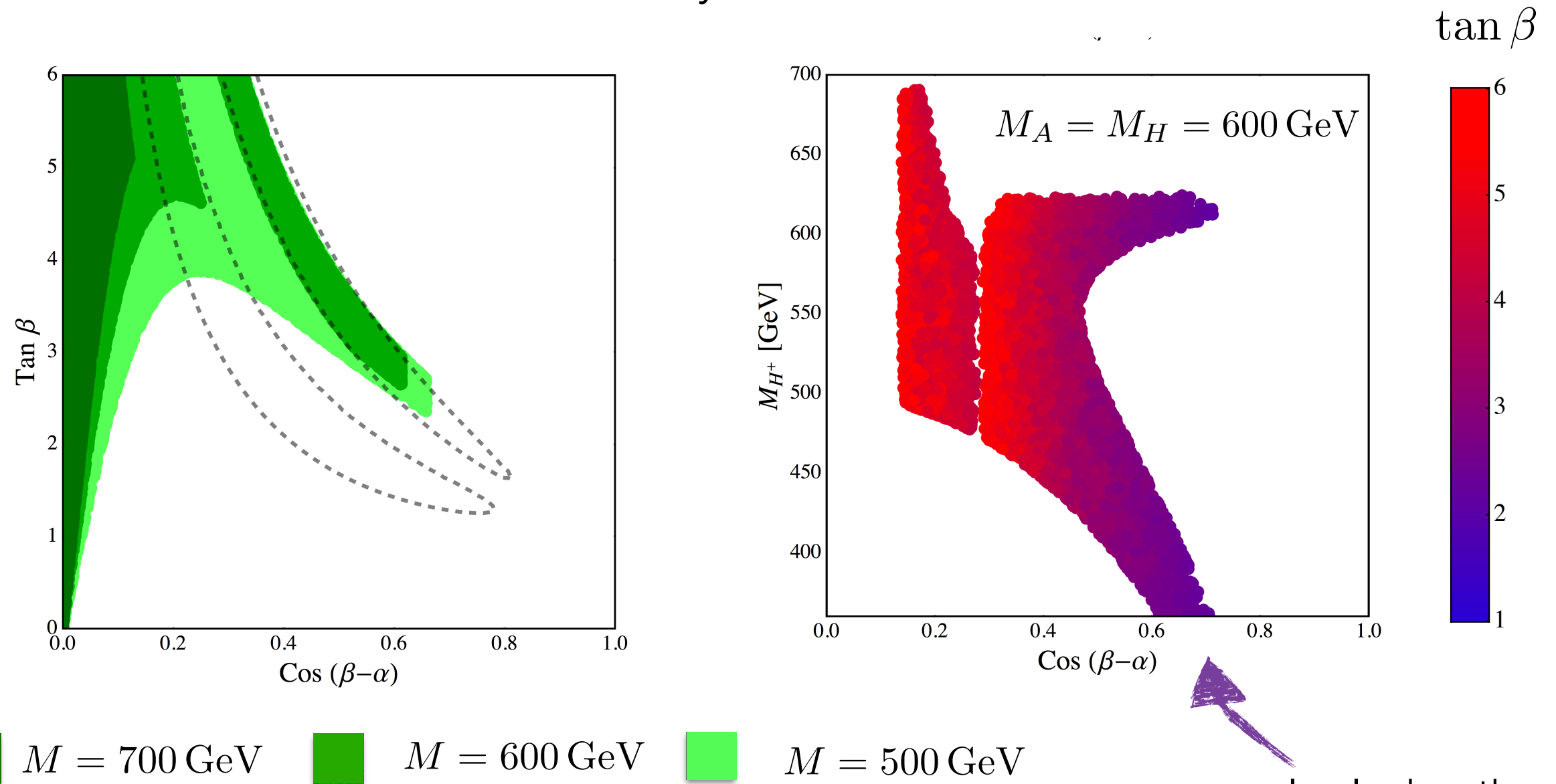
- Neutral Scalar contributions are typically much smaller



$$\frac{m_t V_{tb} V_{ts}^*}{m_b f(\alpha, \beta) \varepsilon} \approx \mathcal{O}(10^2 - 10^3)$$

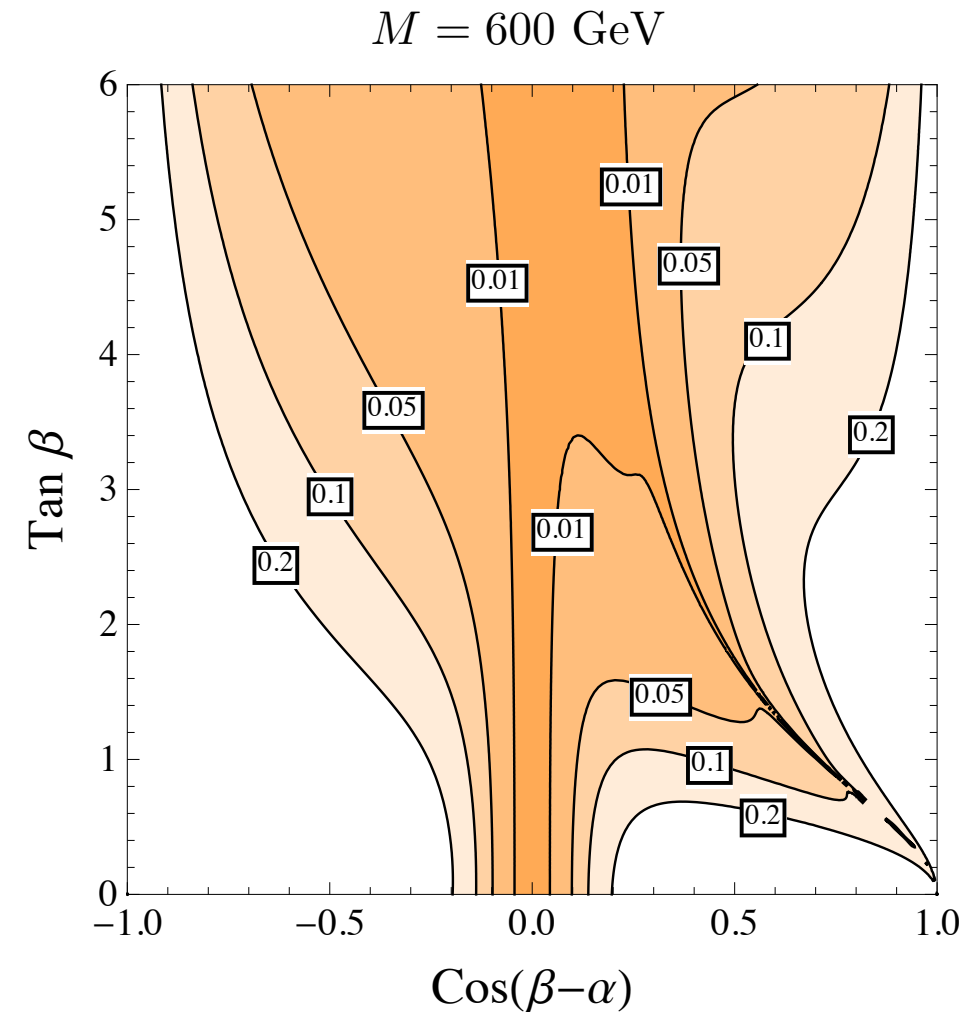
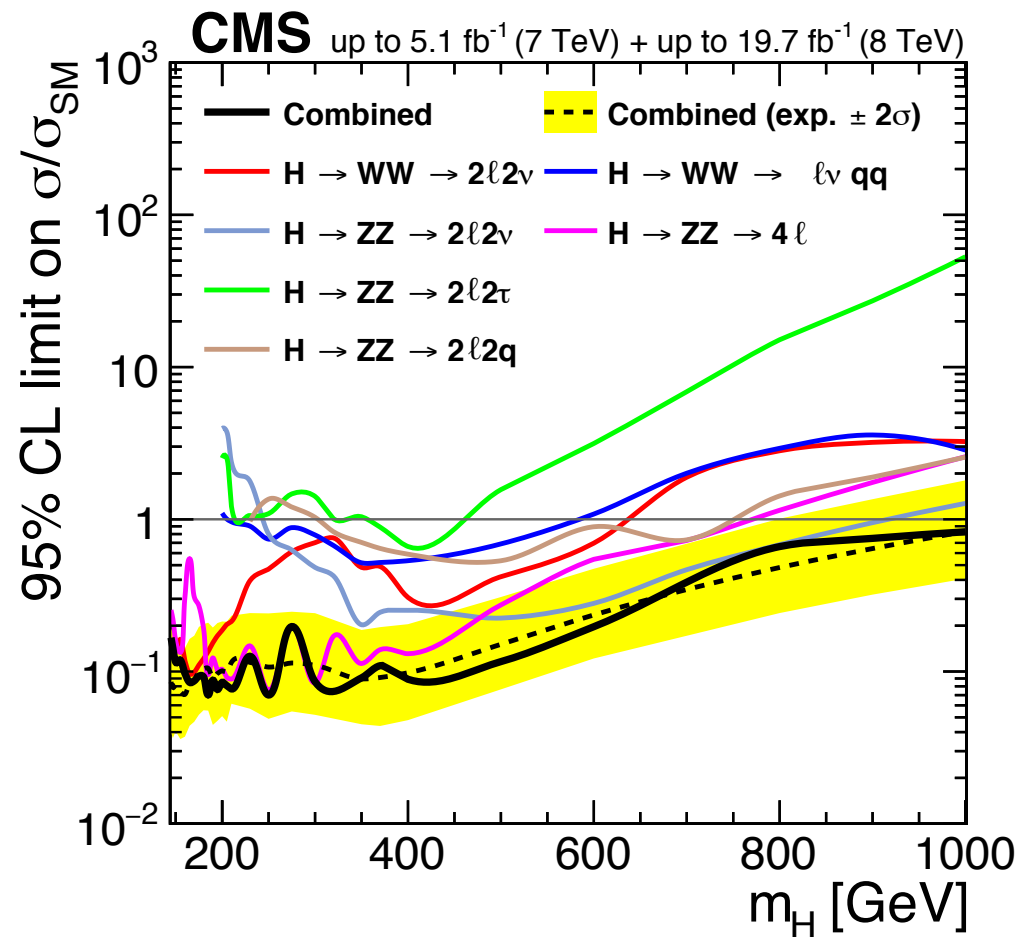
Decoupling and EWPM

- The global Higgs fit (and Flavor bounds) demand sizable $\cos(\beta - \alpha)$
- Flavor bounds demand heavy extra scalars



Includes the
Higgs fit

Collider Searches for Heavy Higgses

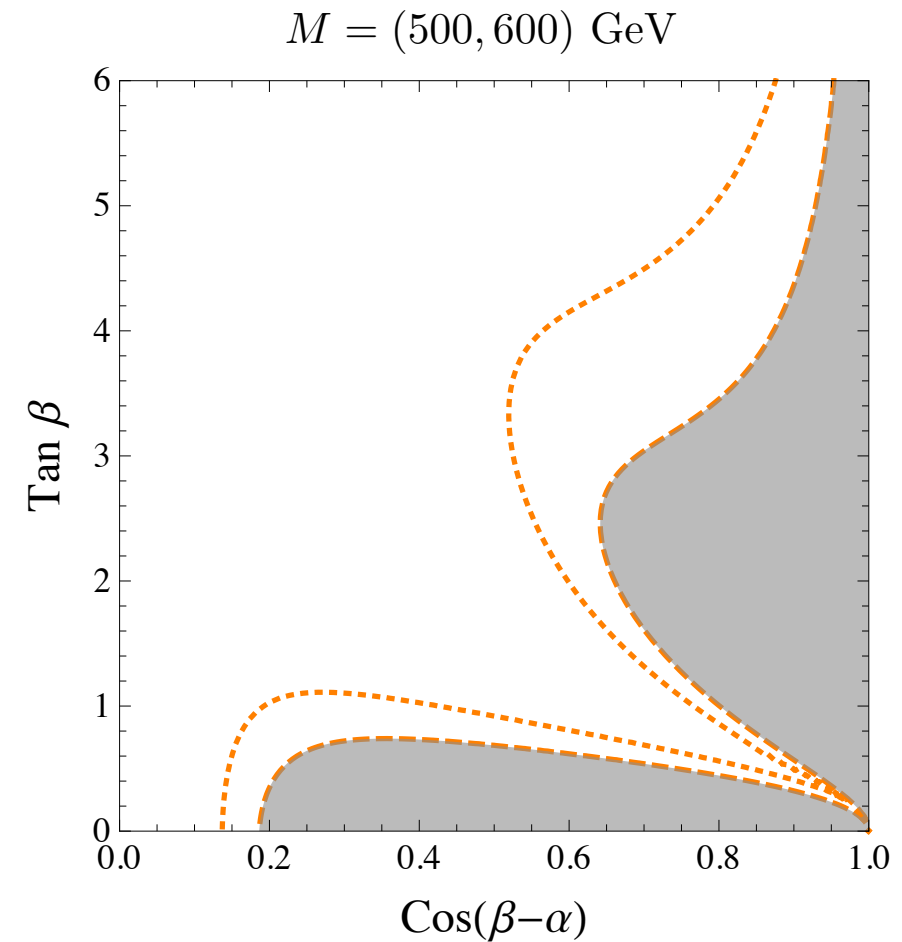
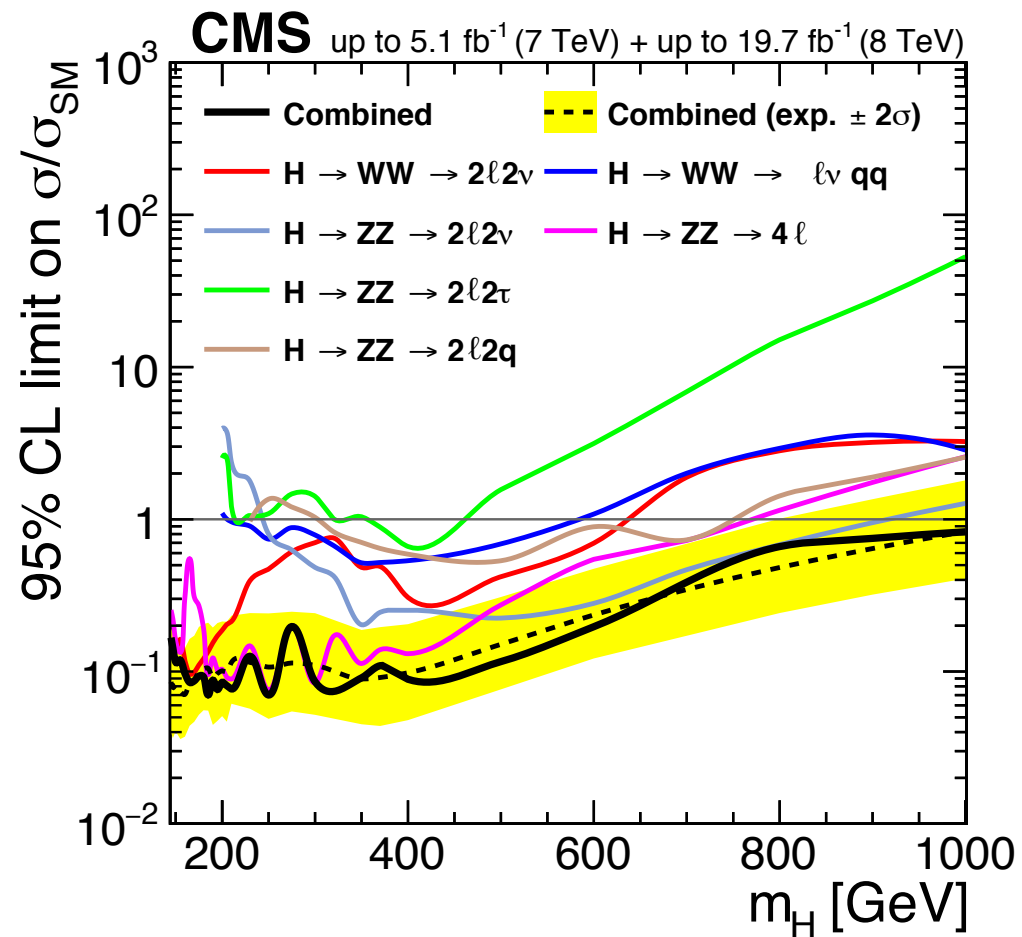


$$\frac{\sigma(gg \rightarrow H) \times \text{Br}(H \rightarrow VV)}{(\sigma(gg \rightarrow H) \times \text{Br}(H \rightarrow VV))_{\text{SM}}} = (\kappa_t^H)^2 \left(1 + \xi_b^H \frac{\kappa_b^H}{\kappa_t^H} \right)^2 (\kappa_V^H)^2 \frac{\Gamma_H^{\text{SM}}}{\Gamma_H},$$

$$\frac{\sigma(pp \rightarrow qqH) \times \text{Br}(H \rightarrow VV)}{(\sigma(pp \rightarrow qqH) \times \text{Br}(H \rightarrow VV))_{\text{SM}}} = (\kappa_V^H)^4 \frac{\Gamma_H^{\text{SM}}}{\Gamma_H},$$

[CMS 1504.00936]

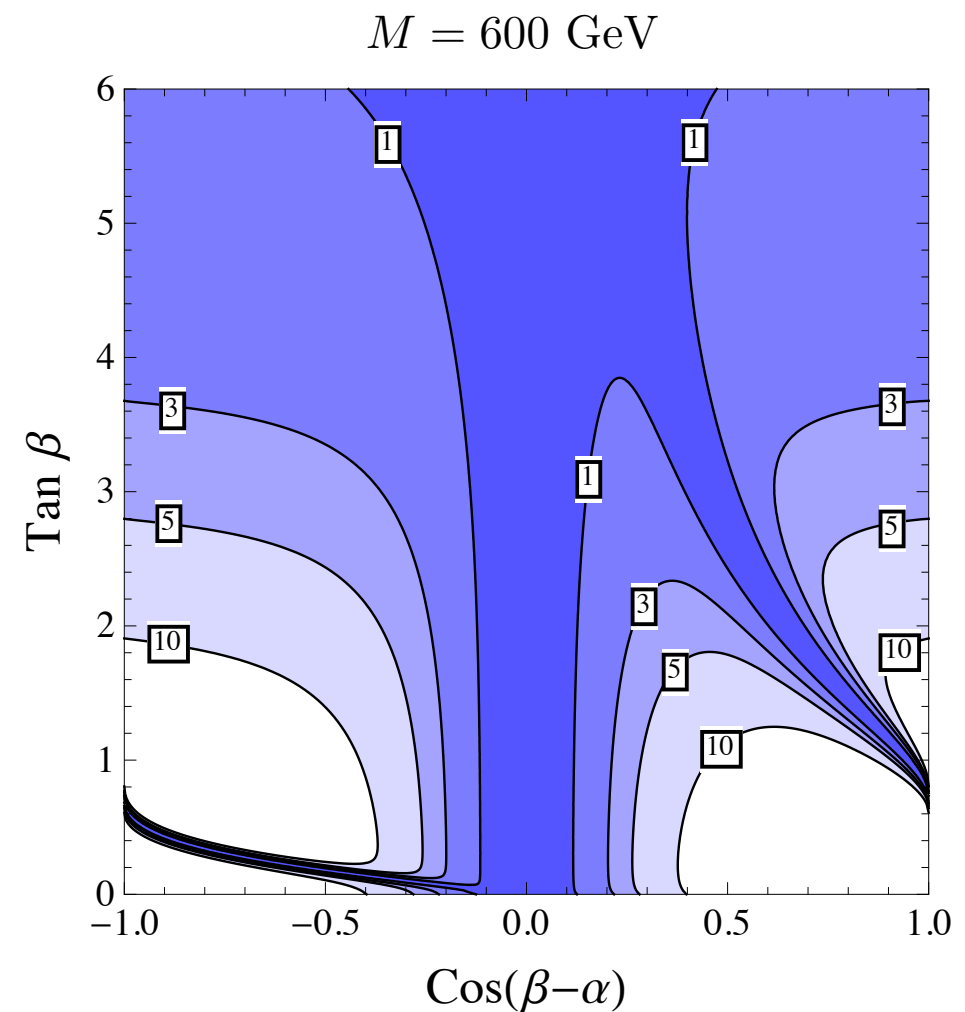
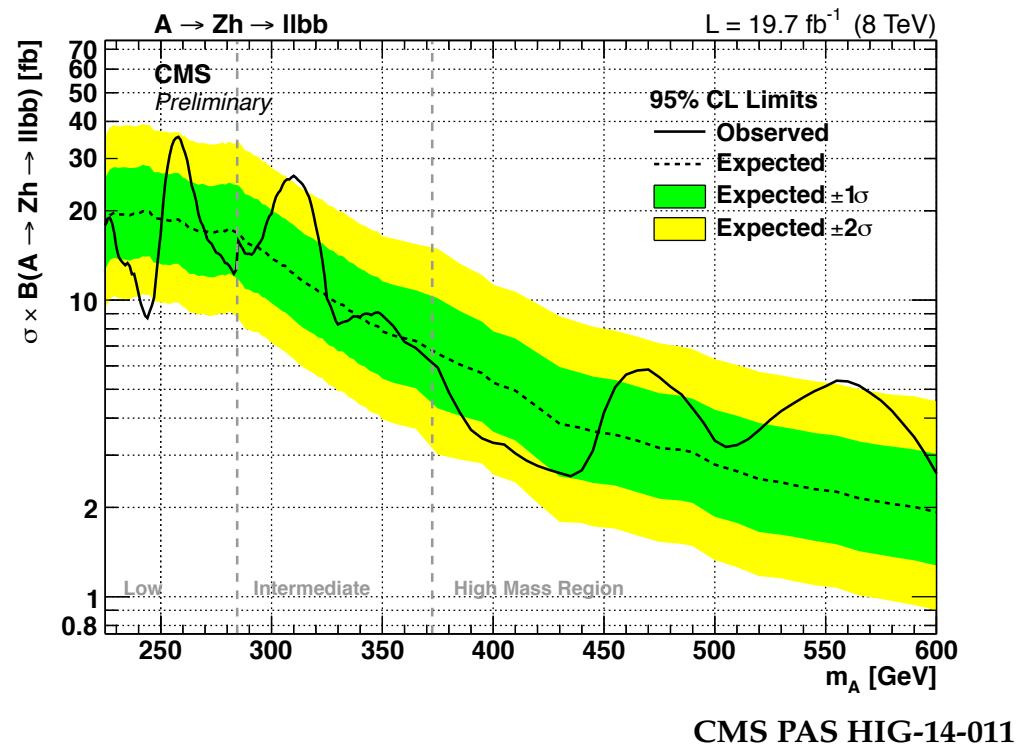
Collider Searches for Heavy Higgses



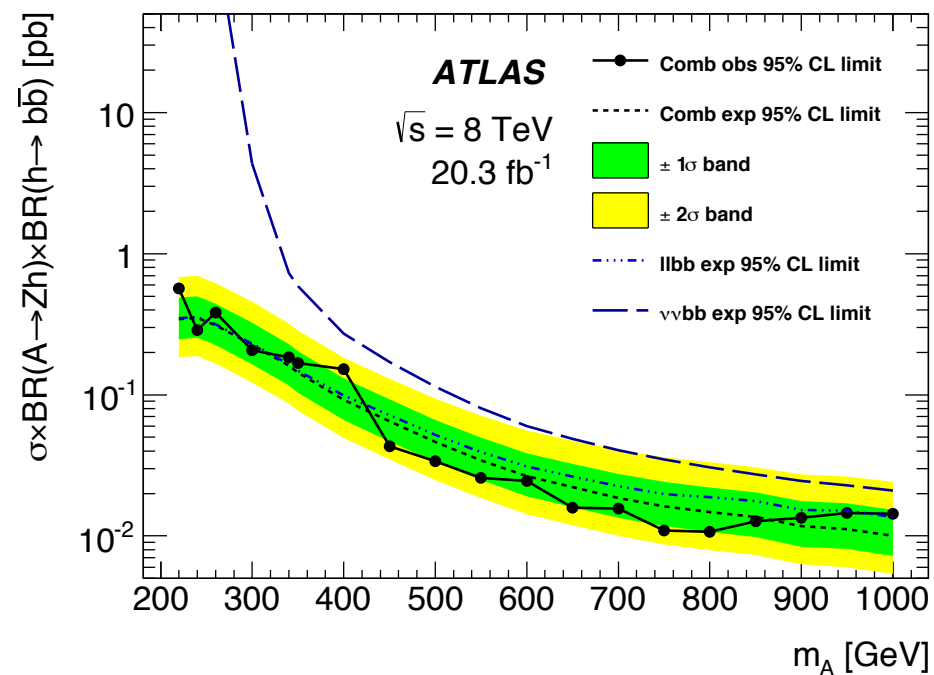
$$\frac{\sigma(gg \rightarrow H) \times \text{Br}(H \rightarrow VV)}{(\sigma(gg \rightarrow H) \times \text{Br}(H \rightarrow VV))_{\text{SM}}} = (\kappa_t^H)^2 \left(1 + \xi_b^H \frac{\kappa_b^H}{\kappa_t^H} \right)^2 (\kappa_V^H)^2 \frac{\Gamma_H^{\text{SM}}}{\Gamma_H},$$

$$\frac{\sigma(pp \rightarrow qqH) \times \text{Br}(H \rightarrow VV)}{(\sigma(pp \rightarrow qqH) \times \text{Br}(H \rightarrow VV))_{\text{SM}}} = (\kappa_V^H)^4 \frac{\Gamma_H^{\text{SM}}}{\Gamma_H},$$

Collider Searches for Heavy Higgses

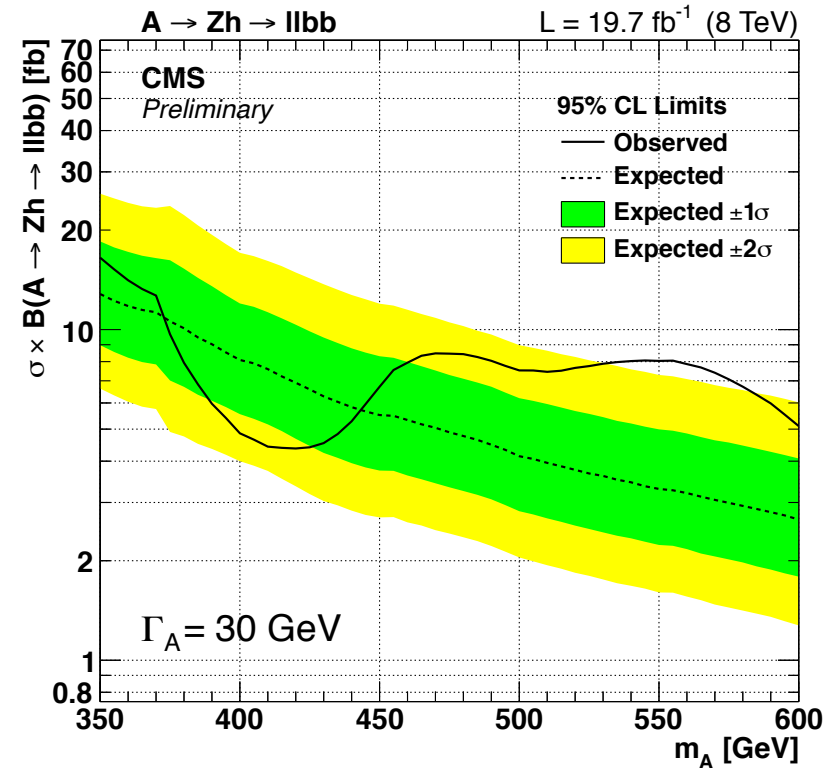


$$\sigma(gg \rightarrow A) \times \text{Br}(A \rightarrow hZ \rightarrow \ell^+ \ell^- b\bar{b})$$

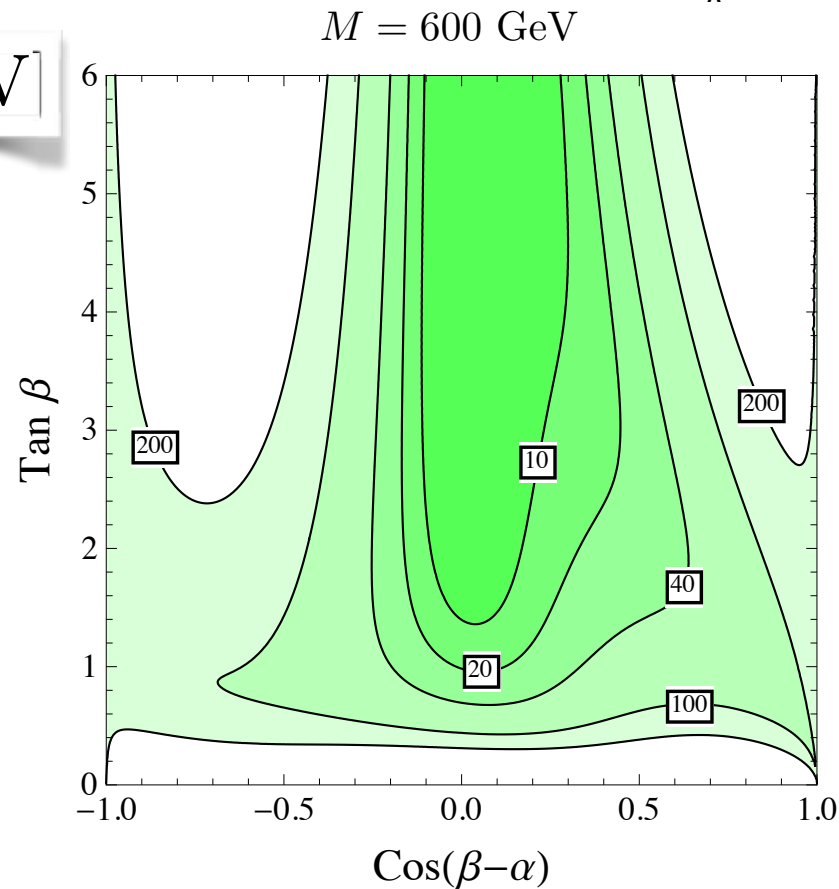
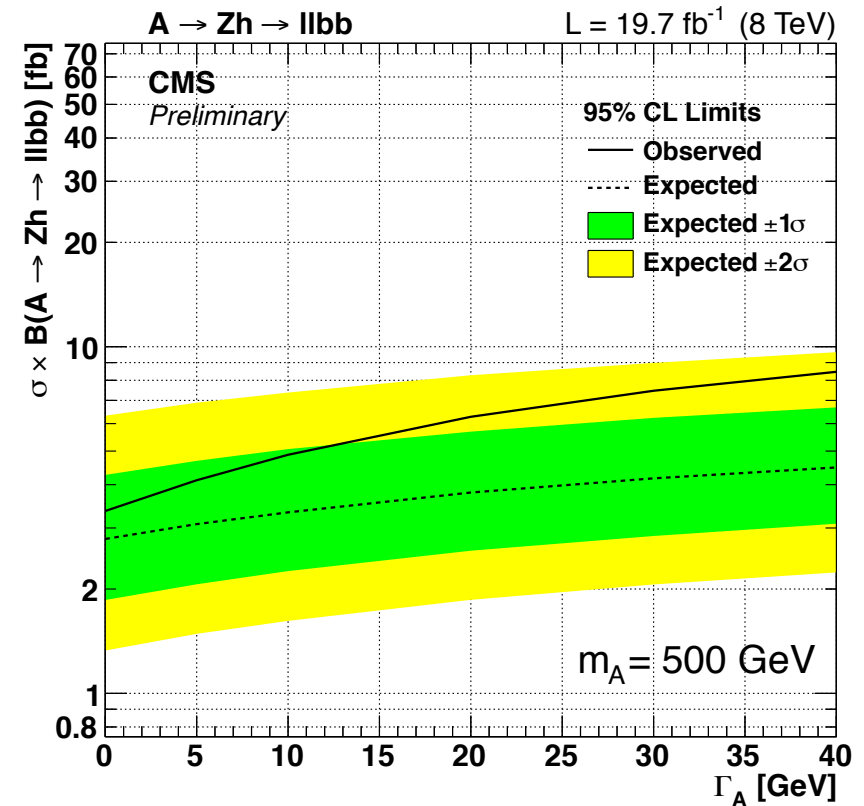


[ATLAS 1502.04478]

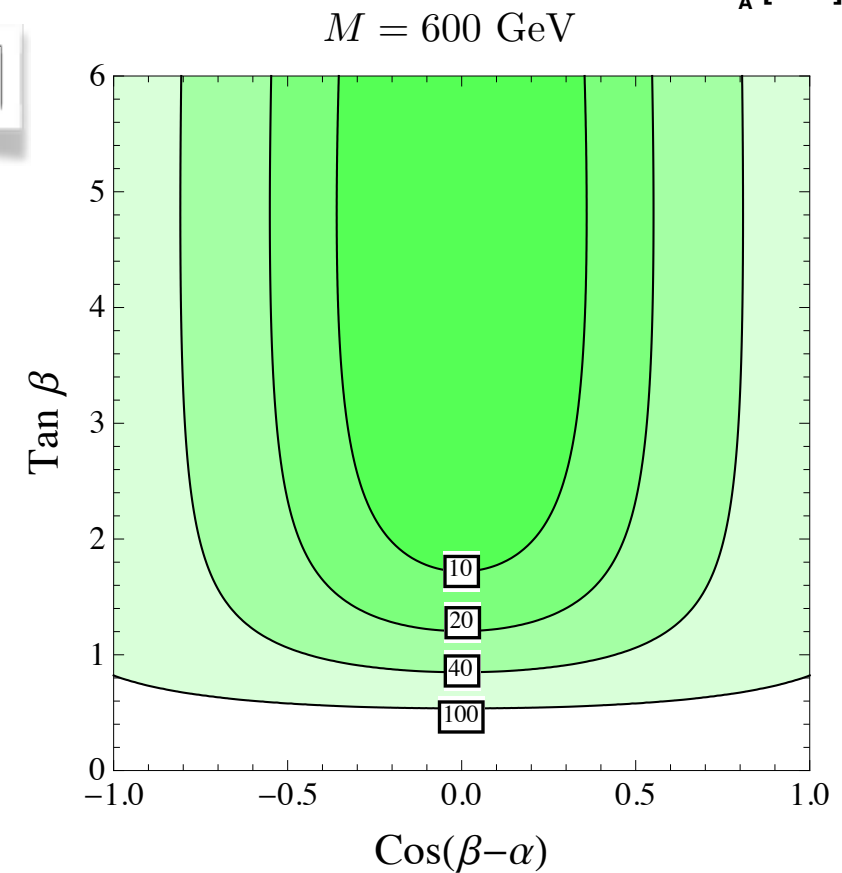
Finite Width Effects



CMS PAS HIG-14-011



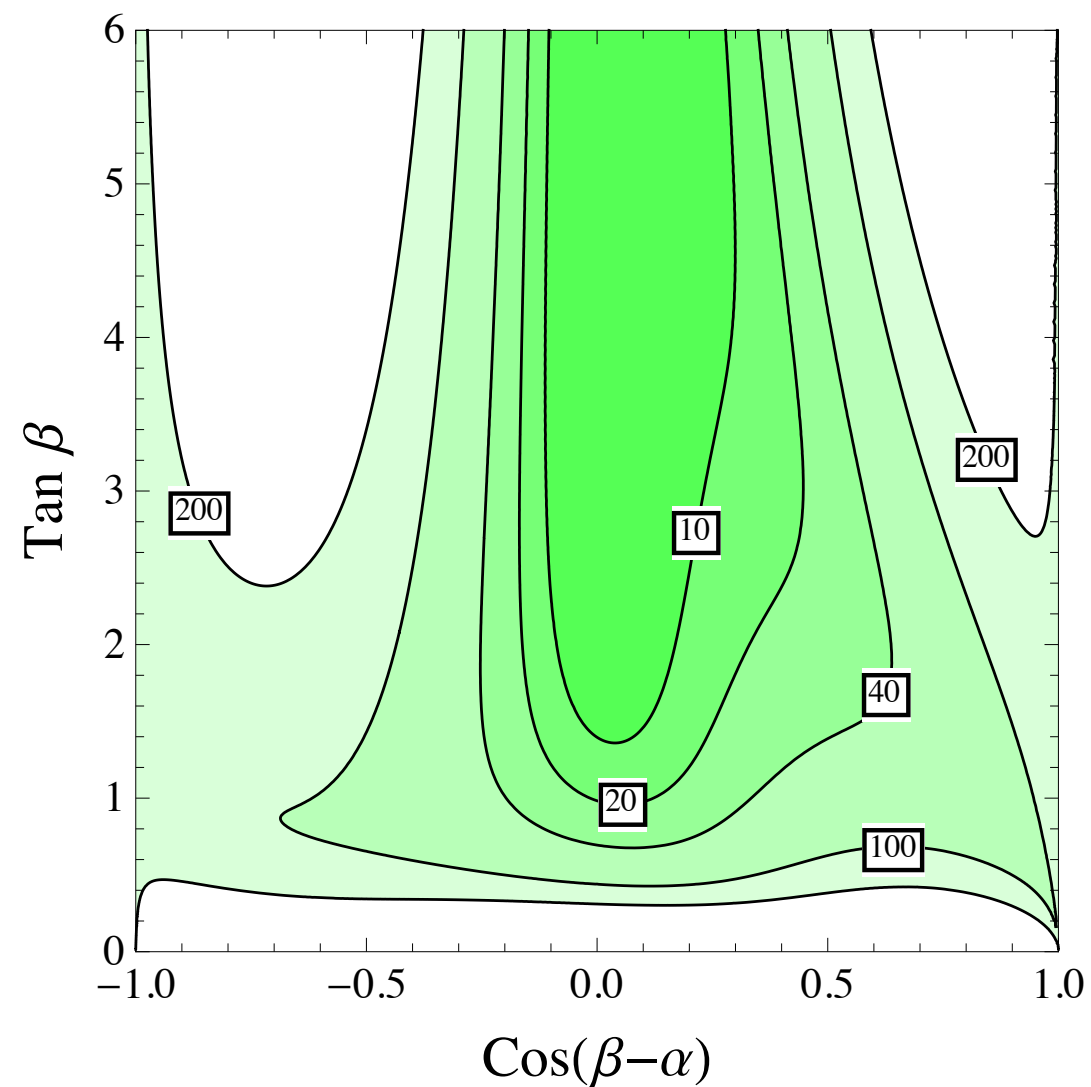
$\Gamma_H [\text{GeV}]$



Finite Width Effects

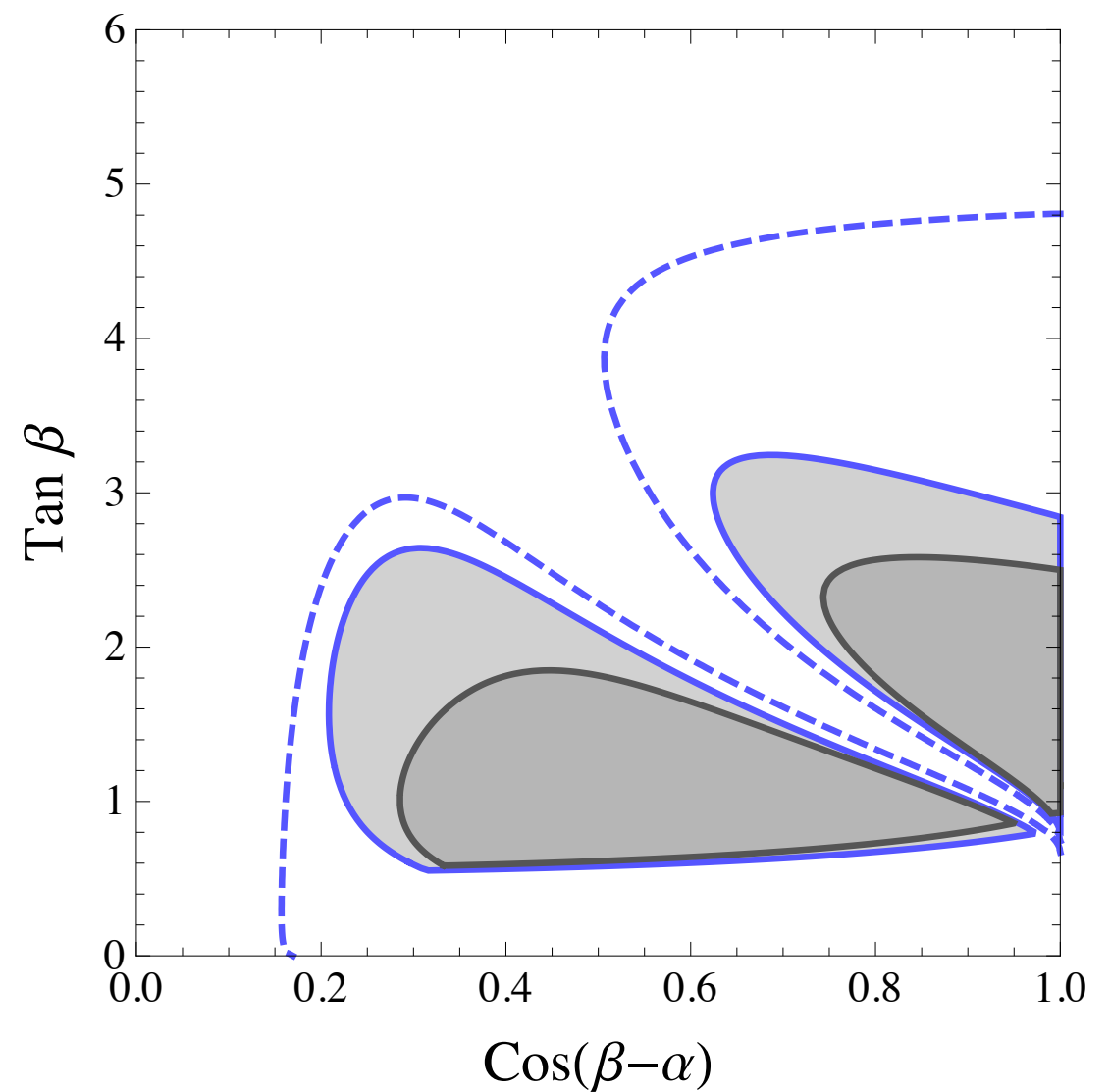
$$\Gamma_A [\text{GeV}]$$

$$M = 600 \text{ GeV}$$

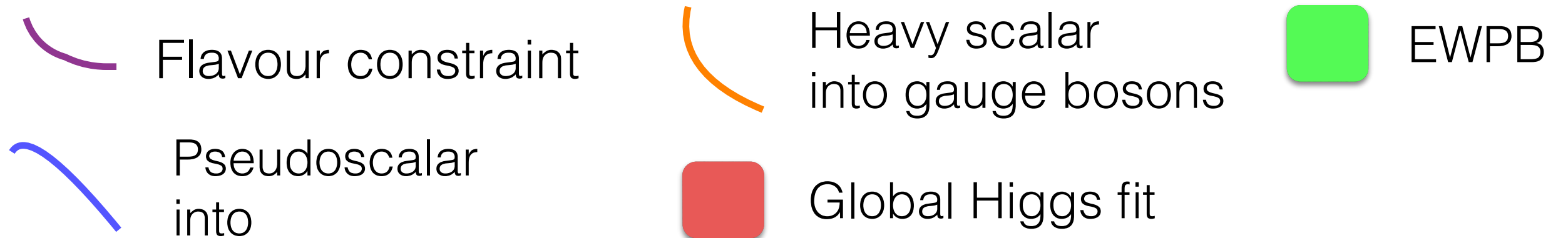
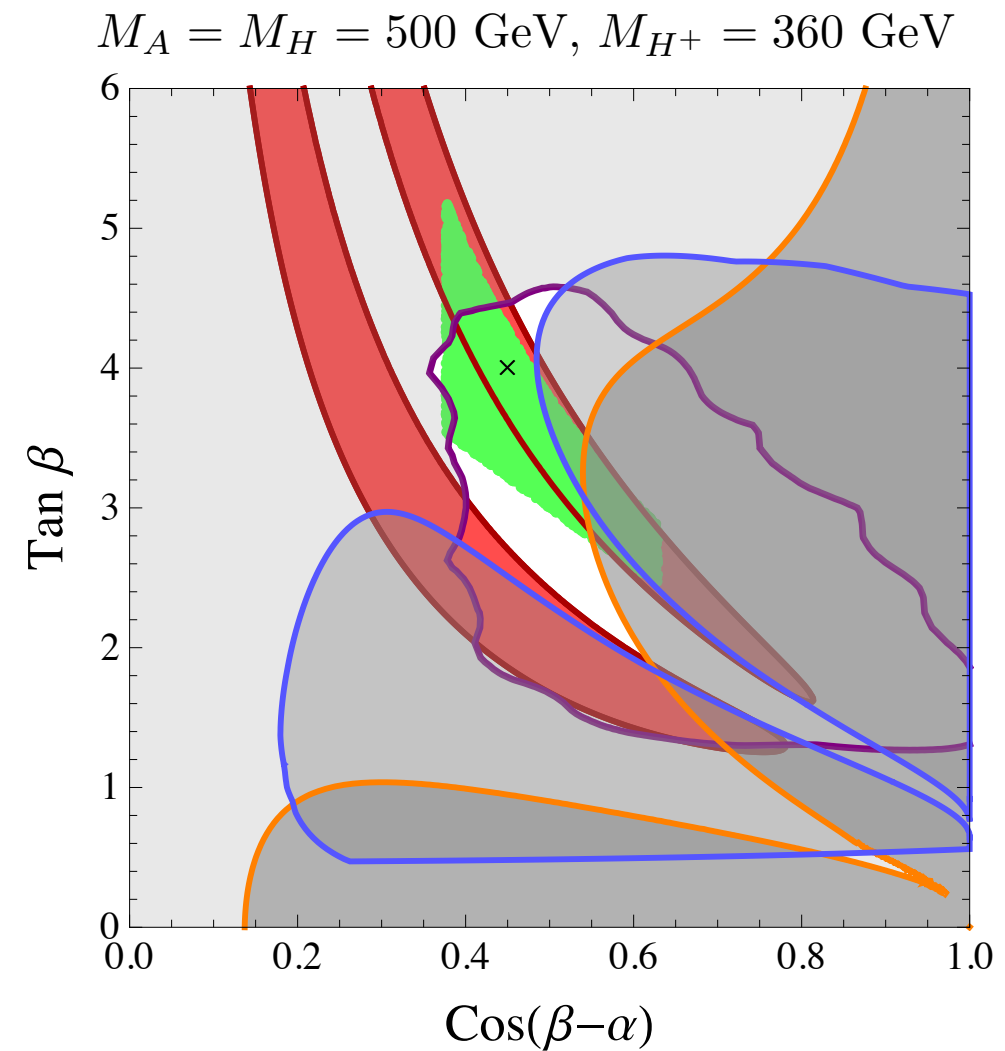
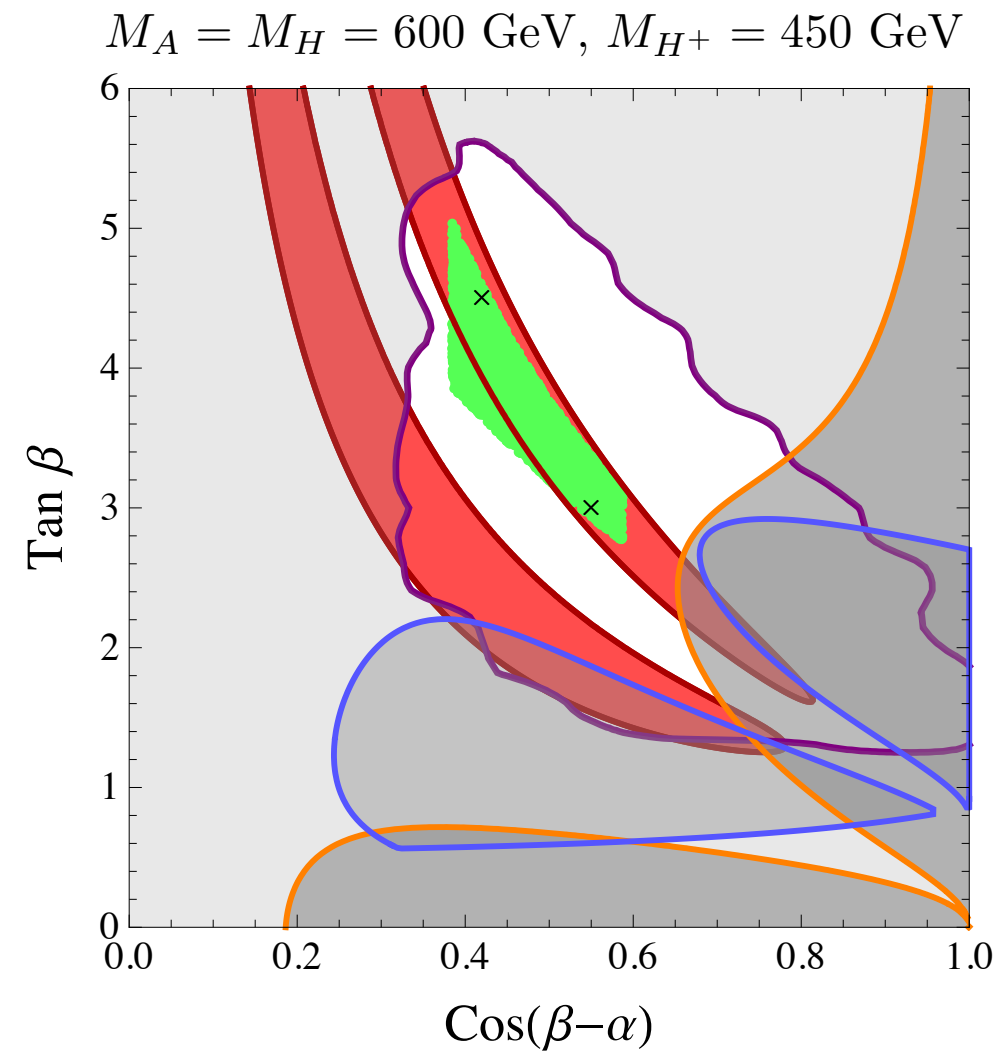


$$\sigma(gg \rightarrow A) \times \text{Br}(A \rightarrow hZ \rightarrow \ell^+ \ell^- b \bar{b})$$

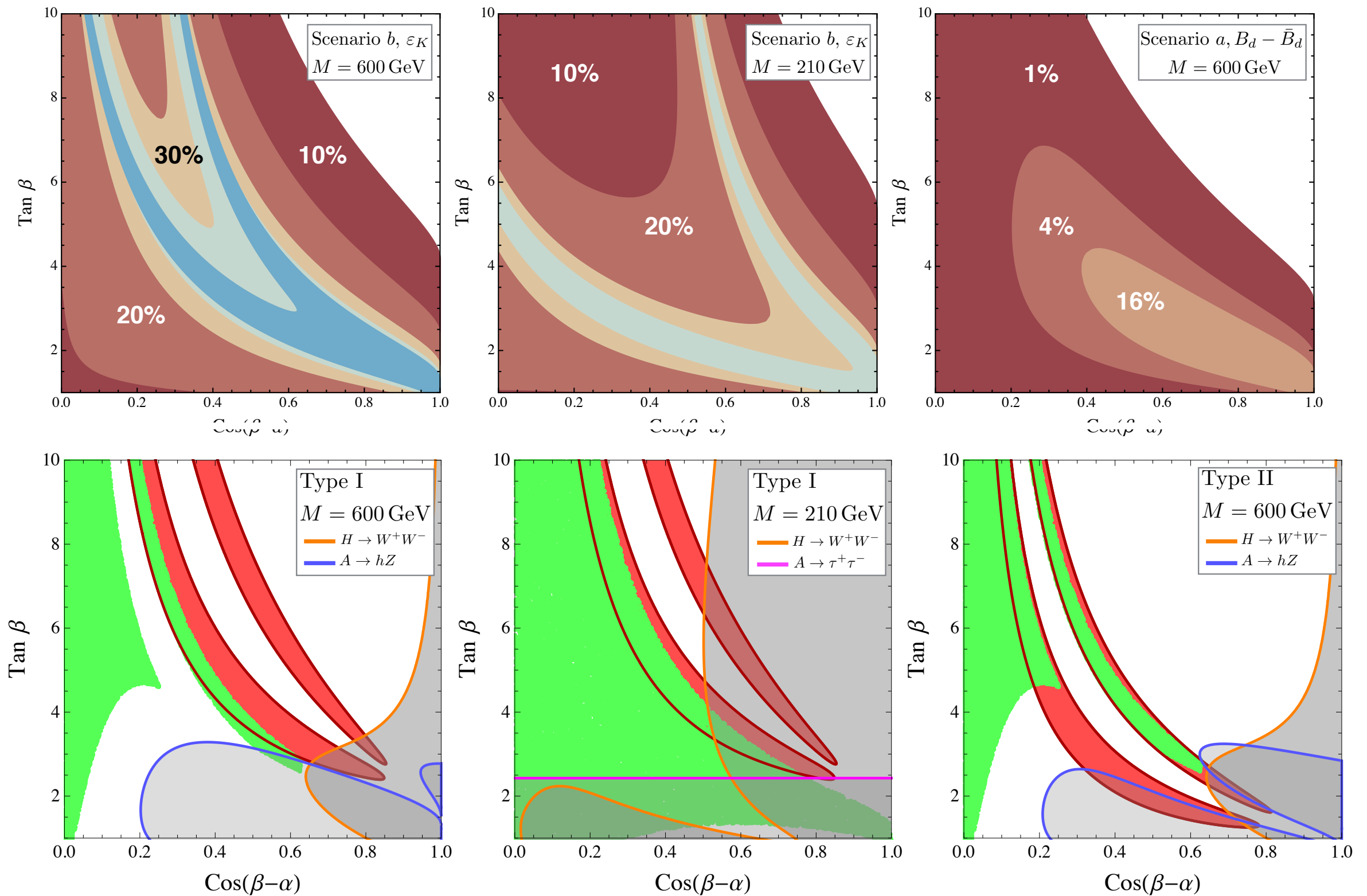
$$M_A = M_H = 600 \text{ GeV}, M_{H^\pm} = (400, 600) \text{ GeV}$$



Final Plots



Type I vs Type II



Conclusions

- Electroweak scale flavor symmetries will be discovered or excluded by the LHC.
- A generic flavon is very hard to discover. A 100 TeV collider would be the first machine in history with a realistic shot.
- The upcoming golden age of Lepton flavor will test the flavor structure in the lepton sector and improve on the bounds in the quark sector