

# Open charm production at high energies and the quark Reggeization hypothesis

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## Plan

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2. Effective vertices in the QMRK approach
3. Fragmentation model
4.  $D$ -meson photoproduction at DESY HERA
5.  $D$ -meson production at the Fermilab Tevatron
6. Conclusions

## QMRK approach and the particle Reggeization hypothesis

Regge limit of QCD:  $\Lambda_{QCD} \ll \mu \ll \sqrt{S} \Rightarrow x = \mu/S \ll 1 \Rightarrow$

$\Rightarrow$  large contributions of the type  $[\alpha_s \ln(1/x)]^n$ ,  
described by BFKL(-like) evolution equations  
for unintegrated PDFs  $\Phi_{g(q)}^p(x, |\mathbf{q}_T|^2, \mu^2)$ .

### Numerical calculations:

- the Kimber-Martin-Ryskin (KMR) prescription for UPDFs;
- input: collinear densities by Martin-Roberts-Stirling-Thorne (MRST).

## QMRK approach and the particle Reggeization hypothesis

### 1. Electron Reggeization in QED:

M. Gellmann, M. L. Goldberger, F. E. Low, E. Marx, and F. Zachariasen, 1964.

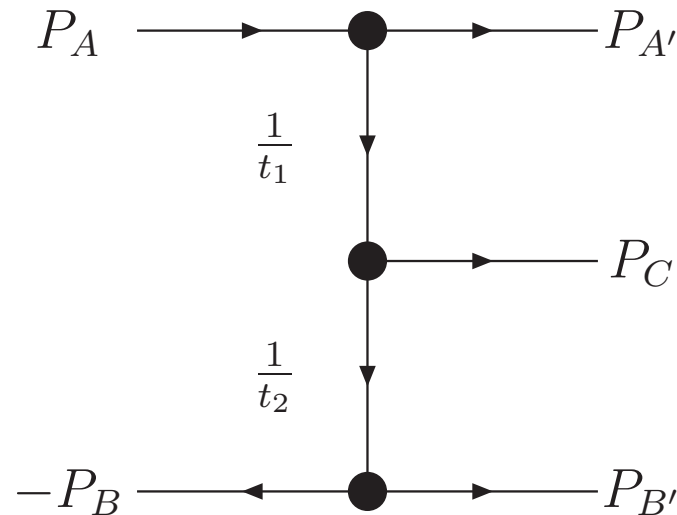
### 2. Gluon Reggeization in QCD:

E. A. Kuraev, L. N. Lipatov, and V. S. Fadin, 1976;  
I. I. Balitsky and L. N. Lipatov, 1978.

### 3. Quark Reggeization in QCD:

V. S. Fadin and V. E. Sherman, 1976.

# QMRK approach and the particle Reggeization hypothesis



$$S_{AB} = (P_A + P_B)^2, \quad S_{A'C} = (P_{A'} + P_C)^2, \quad S_{B'C} = (P_{B'} + P_C)^2$$

$$S_{A'C}, S_{B'C}, P_C^2, P_{C_T}^2 \ll S_{AB}, \quad (P_A \cdot P_{A'}) \ll (P_A \cdot P_C) \ll (P_A \cdot P_{B'})$$

$$y_{A'} \gg y_C \gg y_{B'}$$

## QMRK approach and the particle Reggeization hypothesis

$$P_1 = E_1(1, 0, 0, 1), \quad P_2 = E_2(1, 0, 0, -1), \quad S = 4E_1E_2$$

$$(n^+)^\mu = \frac{P_1^\mu}{E_1}, \quad (n^-)^\mu = \frac{P_2^\mu}{E_2}, \quad k^\pm = k \cdot n^\pm = k^\mu n_\mu^\pm$$

$$k_1 = x_1 P_1 + k_{1T}, \quad k_2 = x_2 P_2 + k_{2T}$$

$$t_1 = -k_1^2 = -k_{1T}^2, \quad t_2 = -k_2^2 = -k_{2T}^2$$

$$x_1 \ll 1, \quad x_2 \ll 1$$

## Effective vertices in the QMRK approach

The QMRK approach is based on the effective quantum field theory implemented with the non-abelian gauge-invariant action:

Reggeized gluons (R), L. N. Lipatov, 1995,

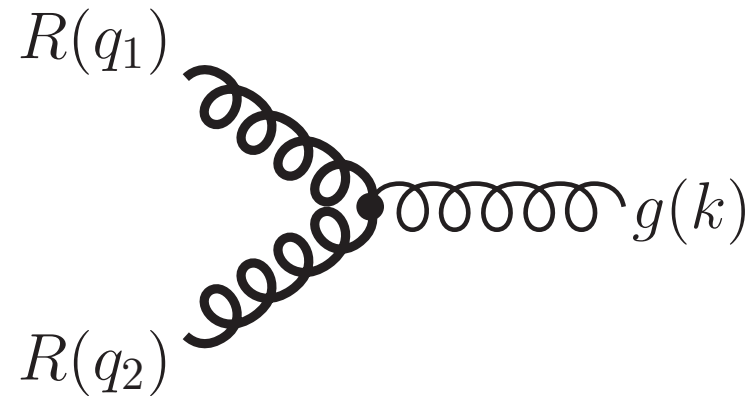
Reggeized quarks (Q), L. N. Lipatov and M. I. Vyazovsky, 2001

Feynman rules for the effective theory:

E. N. Antonov, L. N. Lipatov, E. A. Kuraev, and I. O. Cherednikov, 2005

L. N. Lipatov and M. I. Vyazovsky, 2001

## Effective vertices in the QMRK approach

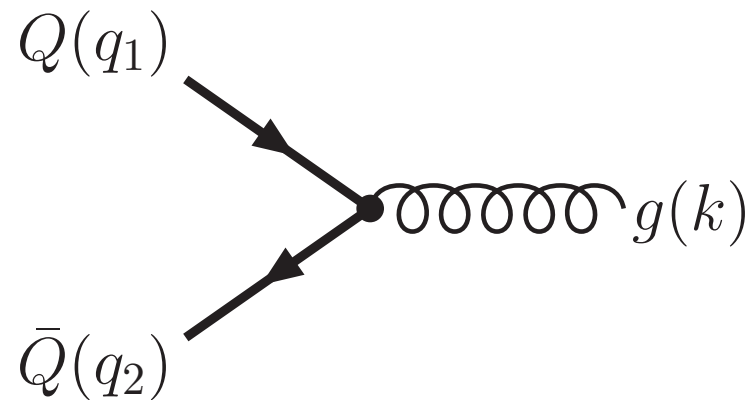


$$C_{\mu}^{RR \rightarrow g}(q_1, q_2) = 2g_s f^{abc} \left( (q_1 - q_2)_{\mu} - (n^+)_{\mu} \left( q_1^- + \frac{q_1^2}{q_2^+} \right) + (n^-)_{\mu} \left( q_2^- + \frac{q_2^2}{q_1^-} \right) \right) \times \frac{x_1 x_2 E_1 E_2}{\sqrt{t_1 t_2}}$$

$$k = q_1 + q_2$$



## Effective vertices in the QMRK approach

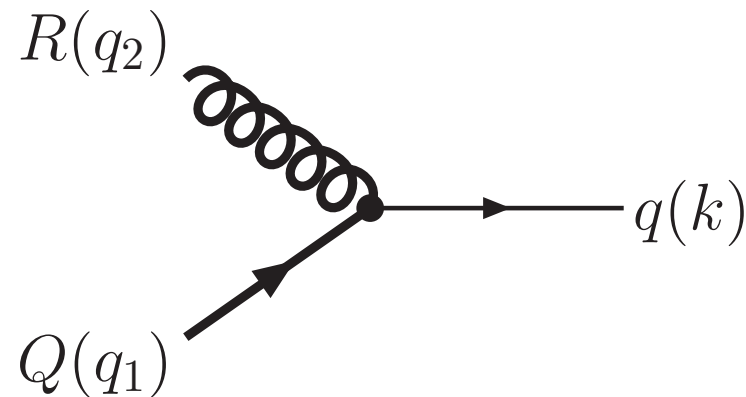


$$C_\mu^{Q\bar{Q} \rightarrow g}(q_1, q_2) = -ig_s T^a \gamma_\mu^{(+ -)}(q_1, -q_2)$$

$$\gamma_\mu^{(+ -)}(q_1, q_2) = \gamma_\mu - \hat{q}_1 \frac{(n^-)_\mu}{k^-} + \hat{q}_2 \frac{(n^+)_\mu}{k^+}$$

$$k = q_1 + q_2$$

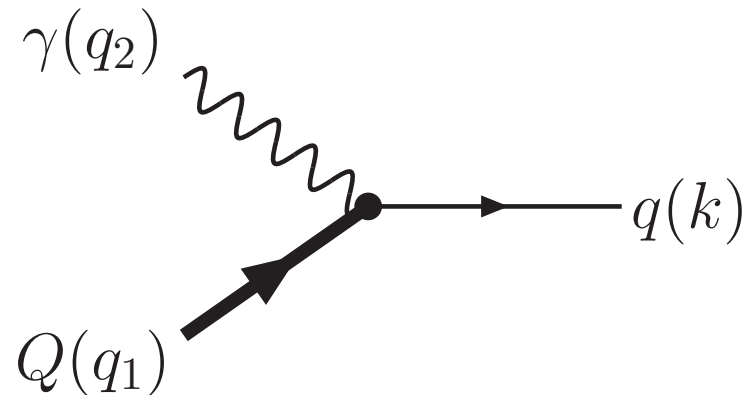
## Effective vertices in the QMRK approach



$$C^{RQ \rightarrow q}(q_1, q_2) = -ig_s T^a \gamma_\mu^{(-)}(q_1, q_2) \Pi_T^{(+)\mu}(q_2)$$

$$\Pi_T^{(+)\mu}(q_2) = \frac{q_{2T}^\mu}{|\vec{q}_{2T}|}, \quad \Pi_T^{(+)\mu}(q_2) = -\frac{x_2 E_2 (n^+)^{\mu}}{|\vec{q}_{2T}|}$$

## Effective vertices in the QMRK approach



$$C^{\gamma Q \rightarrow q}(q_1, q_2) = -ie e_q \gamma_\mu^{(-)}(q_1, q_2)$$

$$\gamma_\mu^{(+)}(q, k) = \gamma_\mu + \hat{q} \frac{n_\mu^+}{k^+} = \gamma_\mu + \hat{q} \frac{P_{2\mu}}{P_2 \cdot k}, \quad \gamma_\mu^{(-)}(q, k) = \gamma_\mu + \hat{q} \frac{n_\mu^-}{k^-} = \gamma_\mu + \hat{q} \frac{P_{1\mu}}{P_1 \cdot k}$$

## Fragmentation model

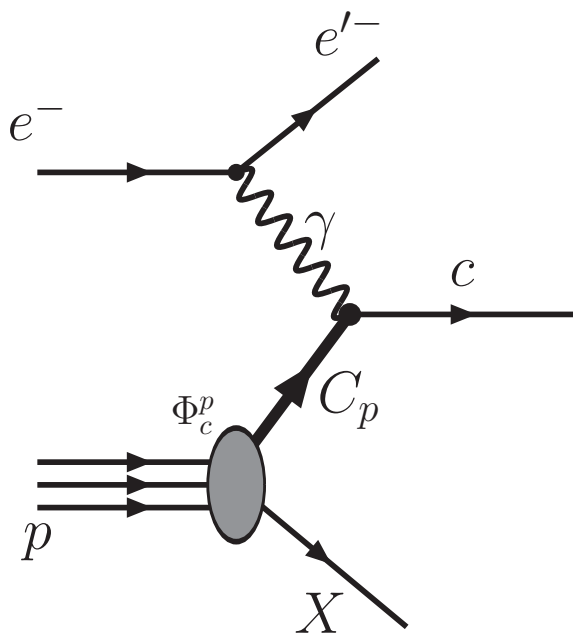
- Fragmentation approach:  $p_T \gg M_D$ .
- D-meson production cross section:

$$d\sigma(p\bar{p}(e) \rightarrow DX) = \int d\sigma(p\bar{p}(e) \rightarrow cX) D_{c \rightarrow D}(z, \mu^2) dz$$

$$\mu = \sqrt{p_T^2 + M_D^2}.$$

- B. A. Kniehl, G. Kramer, Phys. Rev. D **74**, 037502 (2006): universal non-perturbative fragmentation functions, obtained by fitting the OPAL Collaboration  $e^+e^-$ -annihilation data at CERN LEP1.

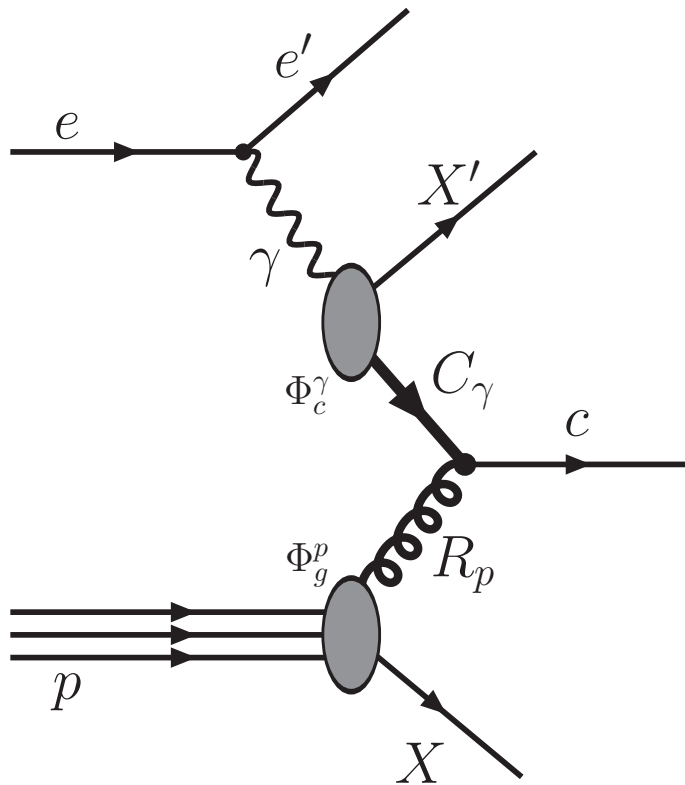
## *D*-meson photoproduction at HERA: QMRK subprocesses



Direct:  $\gamma + C \rightarrow c$

$$\overline{|M(\gamma C \rightarrow c)|^2} = 4\pi\alpha e_c^2 \vec{k}_T^2.$$

## QMRK subprocesses



Resolved:  $R_p + C_\gamma \rightarrow c$  and  
 $R_\gamma + C_p \rightarrow c$

$$\begin{aligned} & \overline{|M(C_{p(\gamma)} R_{\gamma(p)} \rightarrow c)|^2} = \\ & = \frac{2}{3} \pi \alpha_s(\mu^2) \vec{k}_T^2 \end{aligned}$$

## *D*-meson photoproduction at HERA

The master formula for the direct production:

$$p_T^3 \frac{d\sigma}{dp_T} = 2\pi \int d\eta \int dz D_{c \rightarrow D}(z, \mu^2) z^2 y f_{\gamma/e}(y) \Phi_c^p(x_1, t_1, \mu^2) \overline{|M(\gamma C_p \rightarrow c)|^2},$$

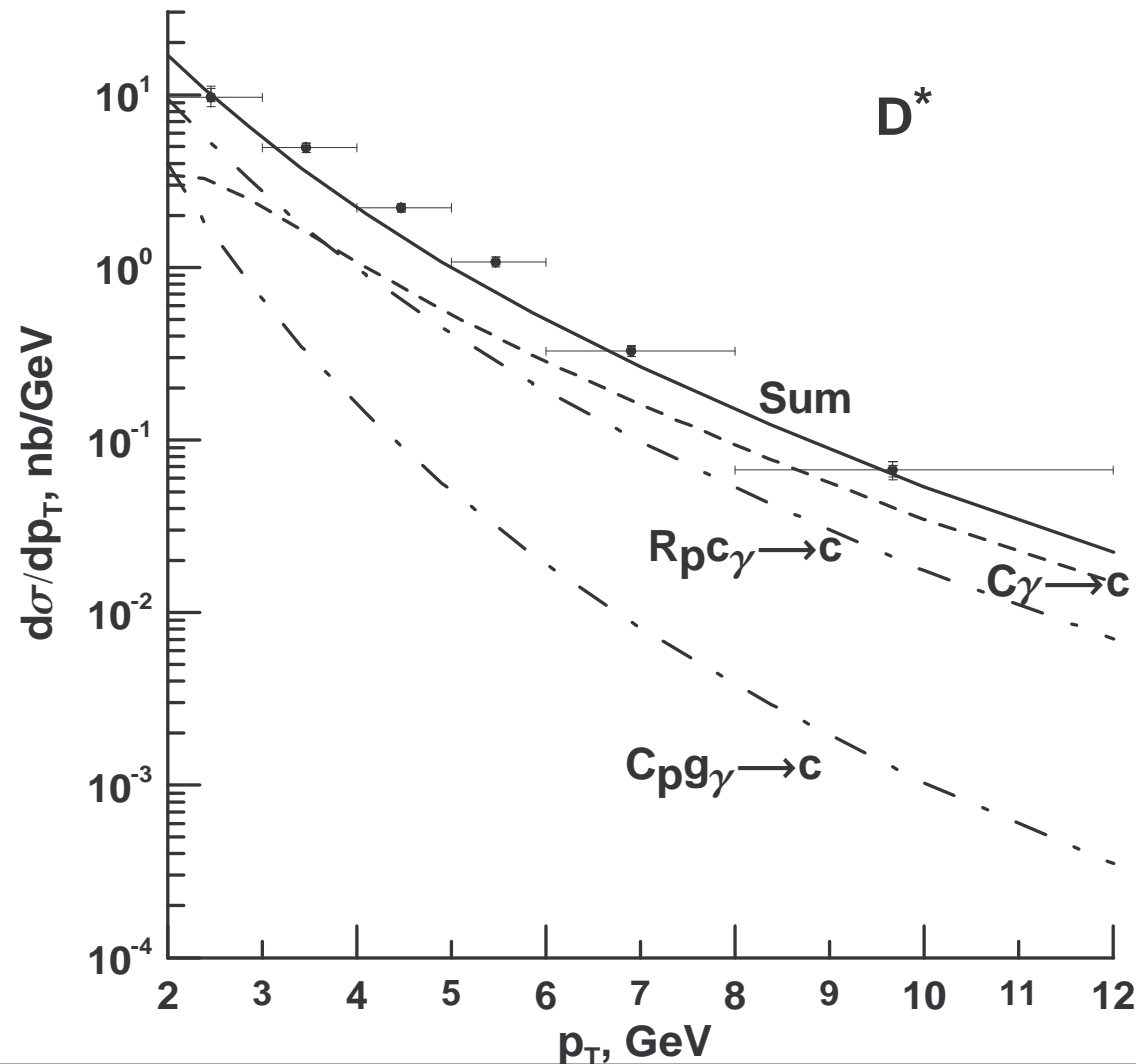
$$x_1 = \frac{p_T e^\eta}{2z E_p}, \quad y = \frac{p_T e^{-\eta}}{2z E_e}, \quad k_T = \frac{p_T}{z}, \quad t_1 = \vec{k}_T^2.$$

The master formula for the resolved production:

$$p_T^3 \frac{d\sigma}{dp_T} = \int d\eta \int dz \int dy \int dt_2 \int d\phi_2 D_{c \rightarrow D}(z, \mu^2) z^2 f_{\gamma/e}(y) \times \\ \times \Phi_c^p(x_1, t_1, \mu^2) \Phi_g^\gamma(x_2, t_2, \mu^2) \overline{|M(C_p R_\gamma \rightarrow c)|^2},$$

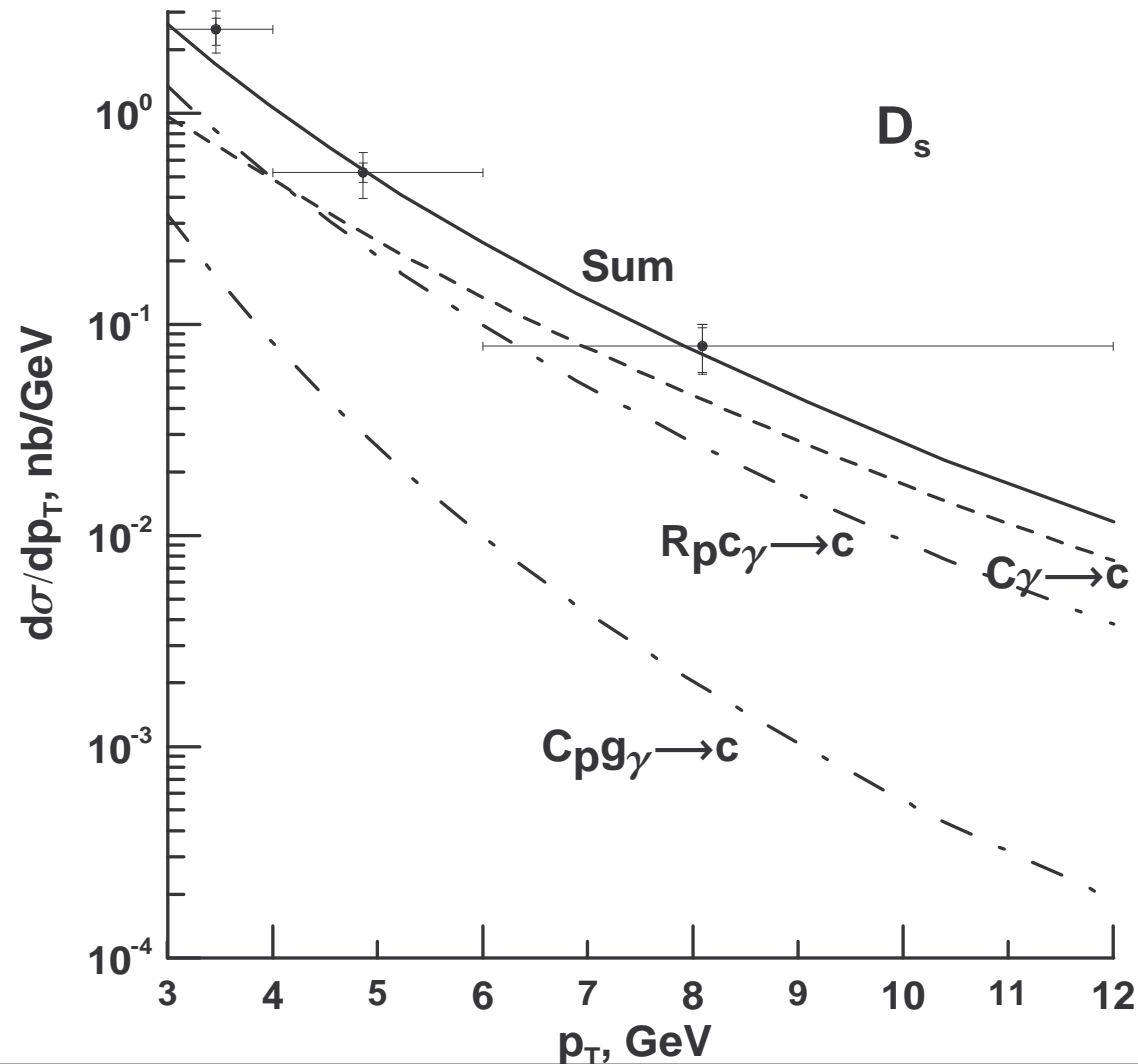
$$x_1 = \frac{p_T e^\eta}{2z E_p}, \quad x_2 = \frac{p_T e^{-\eta}}{2zy E_e}, \quad t_1 = t_2 - 2|\vec{k}_T| \sqrt{t_2} \cos \phi_2 + \vec{k}_T^2, \quad k_T = \frac{p_T}{z}.$$

# $D^*$ -meson photoproduction at HERA





# $D_s$ -meson photoproduction at HERA



## $D$ -meson production at the Fermilab Tevatron

### CDF Collaboration:

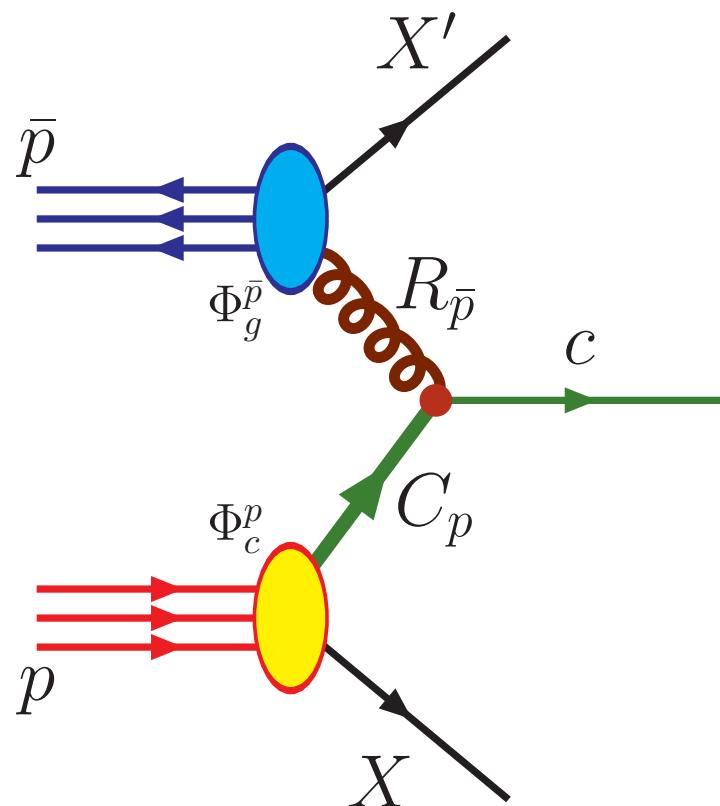
$d\sigma/dp_T$  for prompt  $D$ -meson production  
in  $p\bar{p}$  collisions at  $\sqrt{S} = 1.96$  TeV  
in the central rapidity region  $|y| < 1$ .

### QMRK subprocesses

1.  $R + C \rightarrow c$
2.  $R + R \rightarrow c + \bar{c}$
3.  $Q + \bar{Q} \rightarrow c + \bar{c}$ , where  $Q = U, D$  and  $S$ .

# $D$ -meson production at the Fermilab Tevatron

QMRK subprocess  $R + C \rightarrow c$

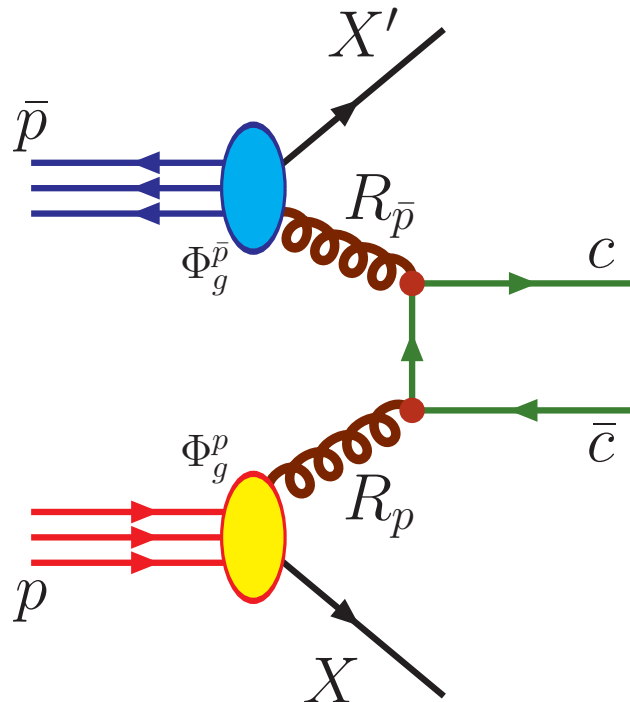


$$C_p + R_{\bar{p}} \rightarrow c$$

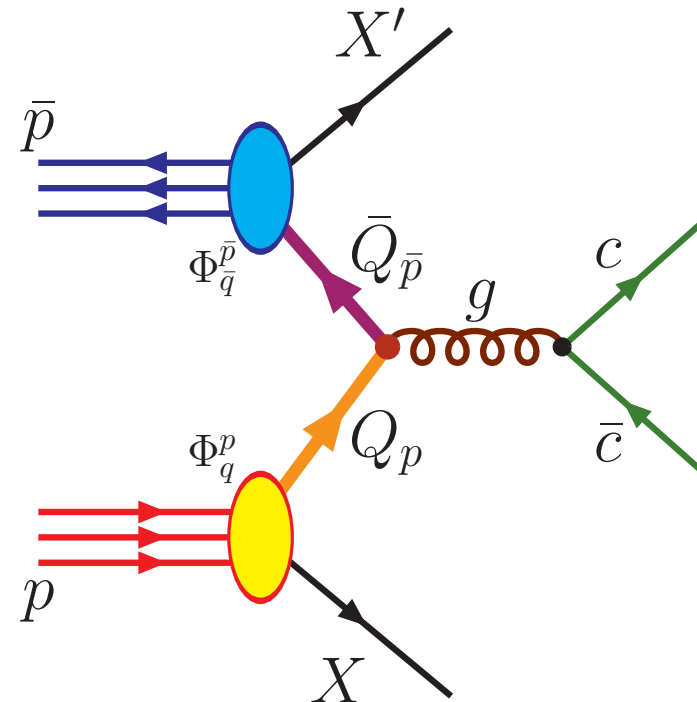
$$\overline{|M(C_p R_{\bar{p}} \rightarrow c)|^2} = \frac{2}{3} \pi \alpha_s(\mu^2) \vec{k}_T^2$$

# *D*-meson production at the Fermilab Tevatron QMRK subprocesses $R + R \rightarrow c + \bar{c}$ and $Q + \bar{Q} \rightarrow c + \bar{c}$

$$R_p + R_{\bar{p}} \rightarrow c + \bar{c}$$



$$Q_p + \bar{Q}_{\bar{p}} \rightarrow c + \bar{c}$$



## *D*-meson production at the Fermilab Tevatron

### QMRK subprocess $R + R \rightarrow c + \bar{c}$

$$\overline{|M(R + R \rightarrow c + \bar{c})|^2} = \frac{1}{8} \cdot \frac{1}{8} \cdot \frac{k_1^- k_2^+}{16 t_1 t_2} \left[ 12 M_{11} + \frac{16}{3} (M_{22} + M_{33}) + 2 \left( 6 (M_{12} + M_{13}) - \frac{2}{3} M_{23} \right) \right]$$

$$k_{1T} = |\vec{k}_{1T}|, \quad k_{2T} = |\vec{k}_{2T}|, \quad T = t - m^2, \quad U = u - m^2$$

$$\begin{aligned} M_{11} = & \frac{8g_s^4}{s^2} \left\{ - \left[ k_{1T}^2 - k_{2T}^2 + T - U - 2 \left( \left( \frac{k_{1T}^2}{k_2^+} - k_1^- \right) k_3^+ - \left( \frac{k_{2T}^2}{k_1^-} - k_2^+ \right) k_3^- \right) \right]^2 + \right. \\ & \left. + s^2 + 4s \frac{k_{1T}^2 k_{2T}^2}{k_1^- k_2^+} \right\} \end{aligned}$$

$$M_{22} = \frac{32g_s^4}{T^2} k_3^+ (k_3^- - k_1^-) (T - k_3^+ (k_3^- - k_1^-))$$

$$M_{33} = \frac{32g_s^4}{U^2} k_3^- (k_3^+ - k_2^+) (U - k_3^- (k_3^+ - k_2^+))$$

## *D*-meson production at the Fermilab Tevatron

QMRK subprocess  $R + R \rightarrow c + \bar{c}$

$$\begin{aligned}
 M_{12} &= \frac{16g_s^4}{sT} \left\{ k_3^+ \frac{k_{1T}^2}{k_2^+} (T + k_{2T}^2) - k_3^- \frac{k_{2T}^2}{k_1^-} (T + k_{1T}^2) + T(k_3^- k_2^+ - k_3^+ k_1^- + U + k_{2T}^2) + \right. \\
 &\quad \left. + k_3^+ (k_3^- - k_1^-) \left[ k_{1T}^2 - k_{2T}^2 + T - U - 2 \left( \left( \frac{k_{1T}^2}{k_2^+} - k_1^- \right) k_3^+ - \left( \frac{k_{2T}^2}{k_1^-} - k_2^+ \right) k_3^- \right) \right] \right\} \\
 M_{13} &= \frac{16g_s^4}{sU} \left\{ k_3^- \frac{k_{2T}^2}{k_1^-} (U + k_{1T}^2) - k_3^+ \frac{k_{1T}^2}{k_2^+} (U + k_{2T}^2) + U(k_3^+ k_1^- - k_3^- k_2^+ + T + k_{1T}^2) - \right. \\
 &\quad \left. - k_3^- (k_3^+ - k_2^+) \left[ k_{1T}^2 - k_{2T}^2 + T - U - 2 \left( \left( \frac{k_{1T}^2}{k_2^+} - k_1^- \right) k_3^+ - \left( \frac{k_{2T}^2}{k_1^-} - k_2^+ \right) k_3^- \right) \right] \right\} \\
 M_{23} &= \frac{16g_s^4}{TU} \left\{ k_{1T}^2 k_{2T}^2 - TU - T k_2^+ k_3^- - U k_3^+ k_1^- + \right. \\
 &\quad \left. + k_3^+ k_3^- (T + U - 2(k_3^- - k_1^-)(k_3^+ - k_2^+)) \right\}
 \end{aligned}$$

*D*-meson production at the Fermilab Tevatron  
 QMRK subprocess  $Q + \bar{Q} \rightarrow c + \bar{c}$

$$\begin{aligned} \overline{|M(Q + \bar{Q} \rightarrow c + \bar{c})|^2} &= \frac{1}{4} \cdot \frac{1}{9} \cdot 2 \cdot \frac{8g_s^4}{s^2} \left[ 8(a_{13} - a_{23})^2 - s(T + U) + \right. \\ &\quad + 4a_{13}(T + k_{1T}^2) + 4a_{23}(U + k_{2T}^2) + 4a_{12}m^2 - \\ &\quad \left. - \frac{4}{a_{12}}(a_{13}^2 k_{1T}^2 + a_{23}^2 k_{2T}^2 + a_{13}a_{23}(T + U)) \right] \\ a_{ij} &= k_{i||} k_{j||} \end{aligned}$$

## *D*-meson production at Tevatron

QMRK subprocess:  $R + C \rightarrow c$

The master formula:

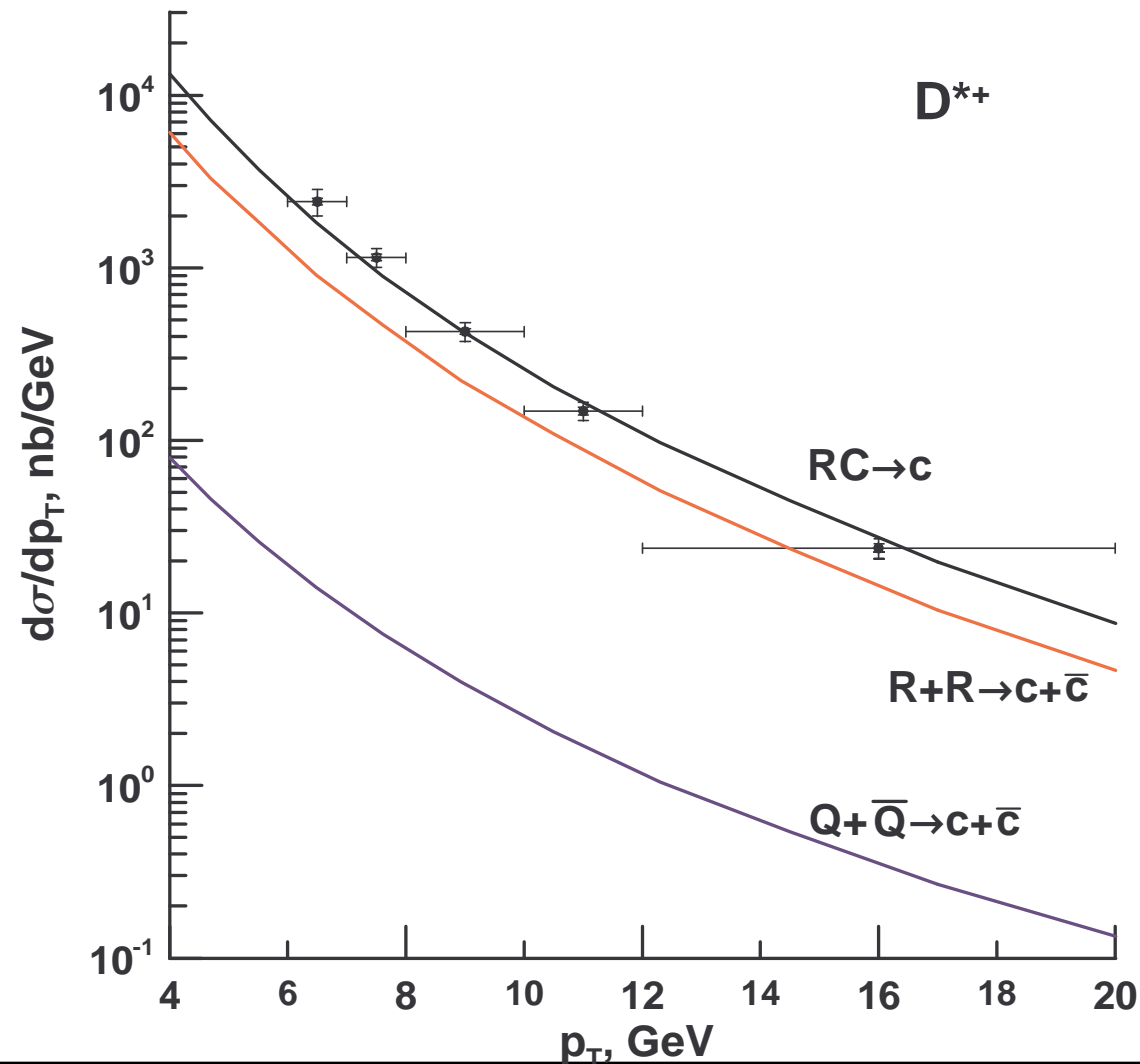
$$p_T^3 \frac{d\sigma}{dp_T} = \int dy \int dz \int dt_1 \int d\phi_1 D_{c \rightarrow D}(z, \mu^2) z^2 \times$$

$$\times \Phi_c^p(x_1, t_1, \mu^2) \Phi_g^{\bar{p}}(x_2, t_2, \mu^2) \overline{|M(C_p R_{\bar{p}} \rightarrow c)|^2},$$

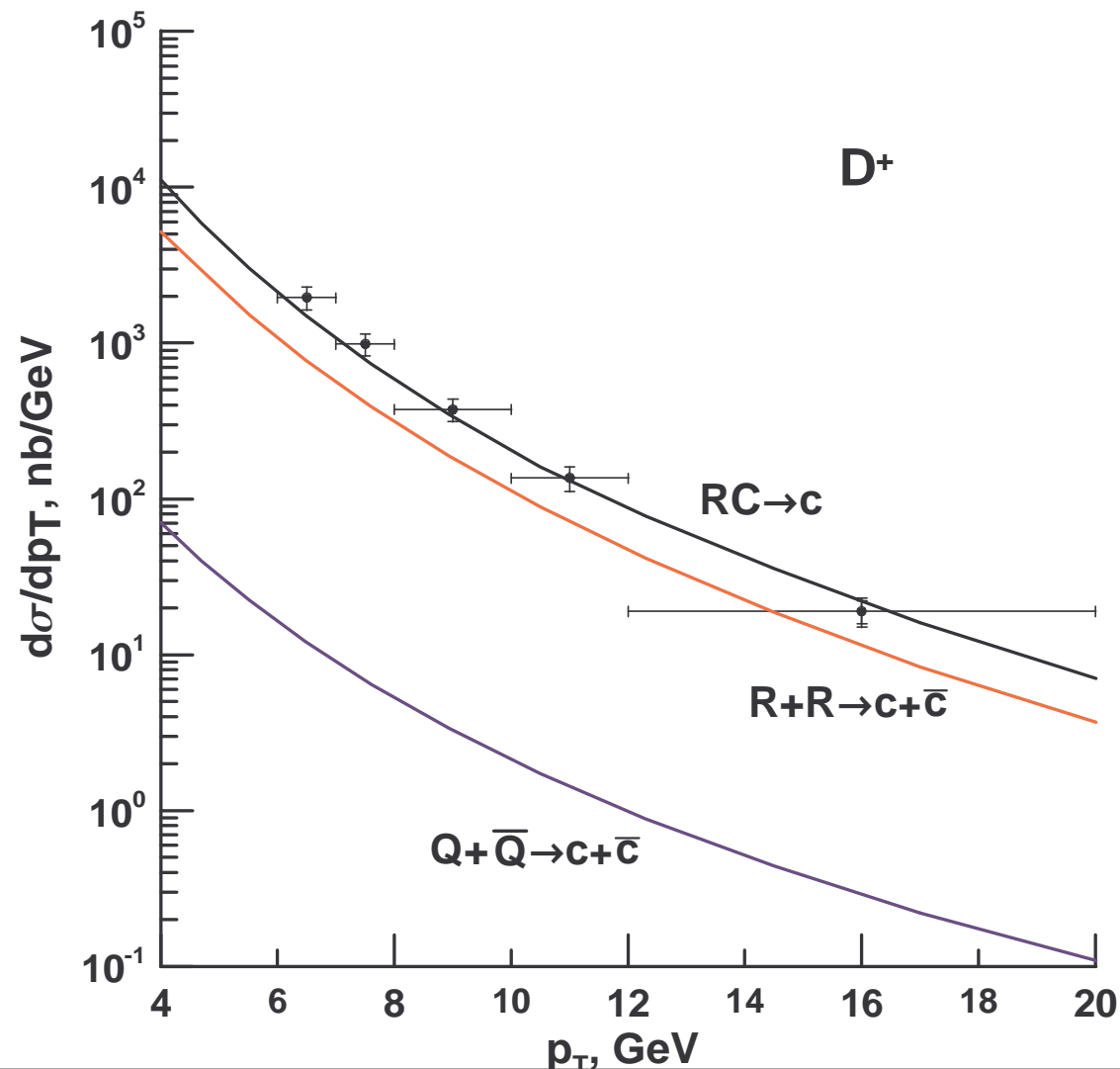
$$x_1 = \frac{p_T e^y}{z\sqrt{S}}, \quad x_2 = \frac{p_T e^{-y}}{z\sqrt{S}}, \quad t_2 = t_1 - 2\frac{p_T}{z}\sqrt{t_1} \cos \phi_2 + \frac{p_T^2}{z^2}.$$



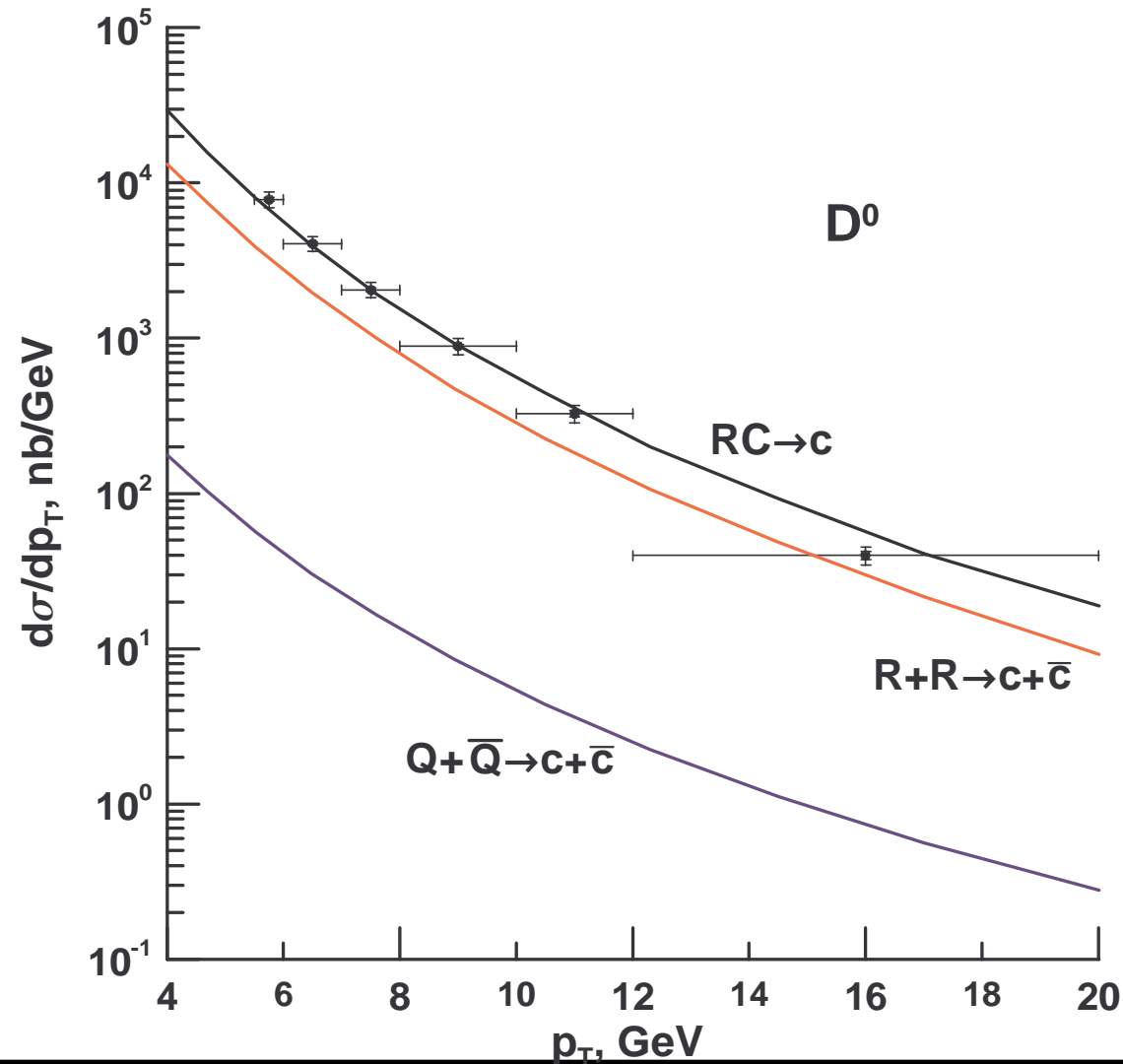
## $D^{*+}$ -meson production at Tevatron



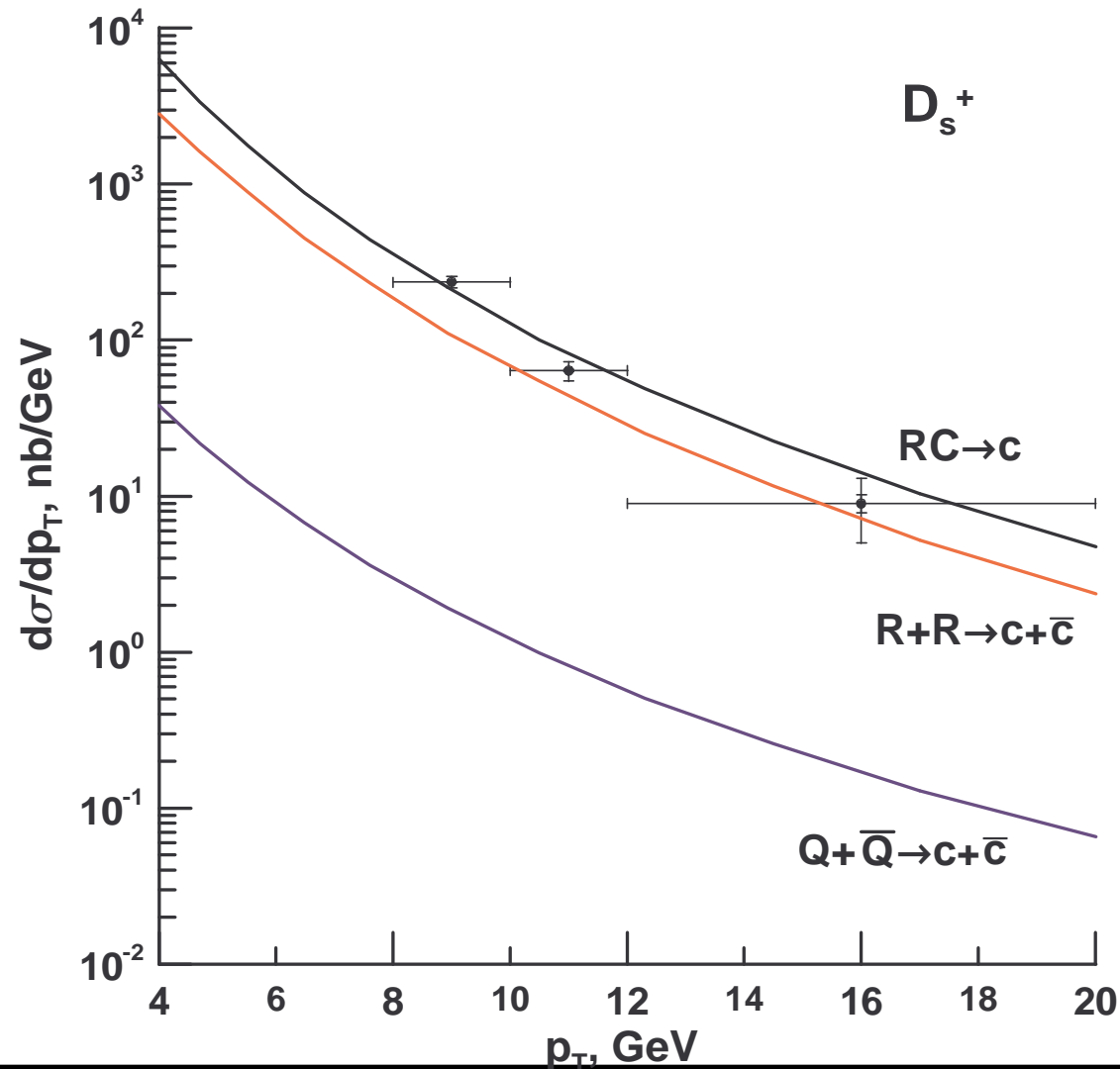
## $D^+$ -meson production at Tevatron



# $D^0$ -meson production at Tevatron



# $D_s^+$ -meson production at Tevatron



## Conclusion

1. Working in the above mentioned approach and fragmentation model we calculated the  $p_T$ -spectra of  $D^{*-}$ ,  $D_s$ -meson photoproduction at HERA Collider and obtained a satisfactory agreement at high  $p_T$  between the our results for the production via LO QMRK subprocess  $\gamma C \rightarrow c$  and the experimental data.
2. We also calculated in this approach the  $p_T$ -spectra of  $D$ -meson production at Tevatron and obtained a good coincidence between our results and the experimental data.

## Conclusion

Taking into consideration pointed out coincidences between analytical calculations and experimental data, we conclude:

1. The quark Reggeization hypothesis justify itself when one admits it because of correct describing the experimental data for cross sections of  $D$ -meson production in different reactions even at LO.
2. The Kimber-Martin-Ryskin-Watt unintegrated  $c$ -quark and gluon distribution functions in a proton seem to be correct because of successful using them for calculations of  $D$ -meson production in different reactions.
3. The details of the calculations are published in the work B. A. Kniehl, A. V. Shipilova, V. A. Saleev arXiv:0812.3376.

Thank you for attention.