

NLO electroweak corrections to Higgs production through gluon-gluon fusion

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in collaboration with [G. Passarino](#), [C. Sturm](#) and [S. Uccirati](#)

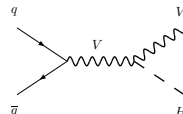
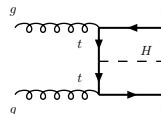
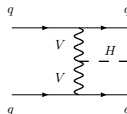
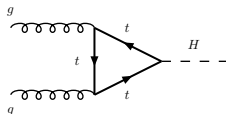
25 Mar 2009 – SFB/TR9 – DESY, Zeuthen

Outline

- 1 EW corrections to $\sigma(gg \rightarrow H)$ below WW threshold
- 2 Crossing of double vector-boson thresholds
- 3 Numerical results

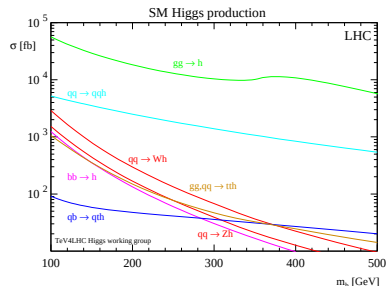
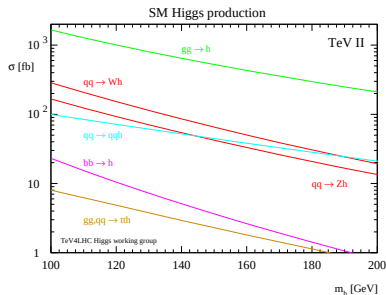
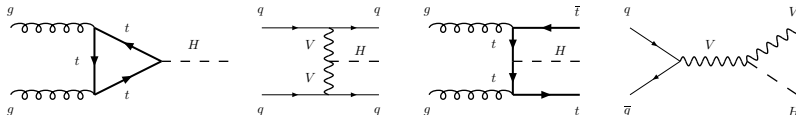
Hadronic SM Higgs production

Main production channels for the **Standard Model** Higgs in **hadron collisions**



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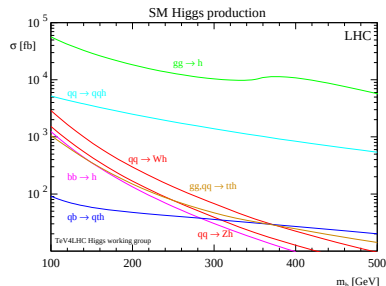
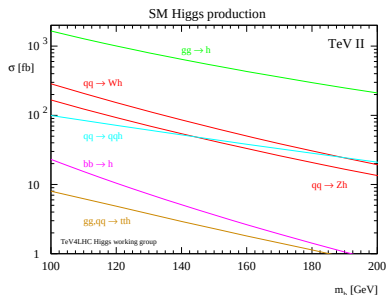
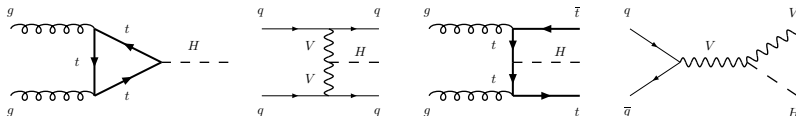
Main production channels for the **Standard Model** Higgs in **hadron collisions**



Hahn, Heinemeyer, Maltoni, Weiglein, Willenbrock [hep-ph/0607308]

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Main production channels for the **Standard Model** Higgs in **hadron collisions**



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Gluon-fusion production channel does **not** lead to the **cleanest signal**, but it has by far the **largest cross section** both at the TEVATRON and the LHC

QCD corrections

NLO and **NNLO** QCD corrections to the cross section **extremely large**

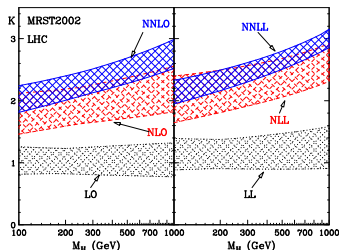
Dawson'91, Djouadi, Spira, Zerwas'91, Spira, Djouadi, Graudenz, Zerwas'95

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Harlander'00, Catani, de Florian, Grazzini'01, Harlander, Kilgore'01,

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Catani, de Florian, Grazzini, Nason

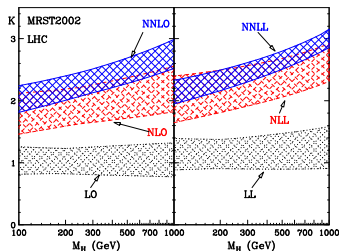
[hep-ph/0306211]

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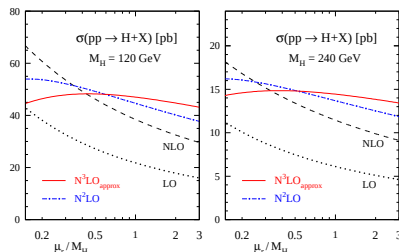
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Catani, de Florian, Grazzini, Nason
[hep-ph/0306211]



Moch, Vogt [hep-ph/0508265]

$N^3\text{LO}$ soft limit $\Rightarrow$ 5% uncertainty

EW corrections

NLO EW corrections needed for matching the precision of QCD predictions, but not very well known

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- "Dominant" contributions enhanced by M_t^2 Djouadi, Gambino'94

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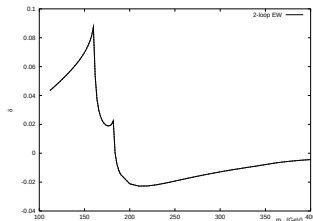
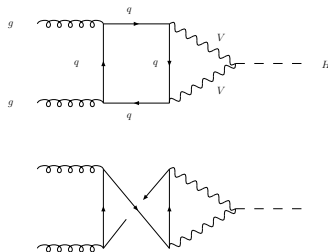
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- Top diagrams by a **Taylor expansion** in q_H Degrassi, Maltoni'04
- Light-quark analytically Aglietti, Bonciani, Degrassi, Vicini'04



Aglietti, Bonciani, Degrassi, Vicini
[hep-ph/0404071]

Outline of the computation

NLO EW corrections not complete $\Rightarrow$ extend the results above the WW threshold (after checking below)

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- 4 M_j **divergent** for $m_f \rightarrow 0$; $\mathcal{A}^{\text{NLO}}$ **finite** for $m_f \rightarrow 0$

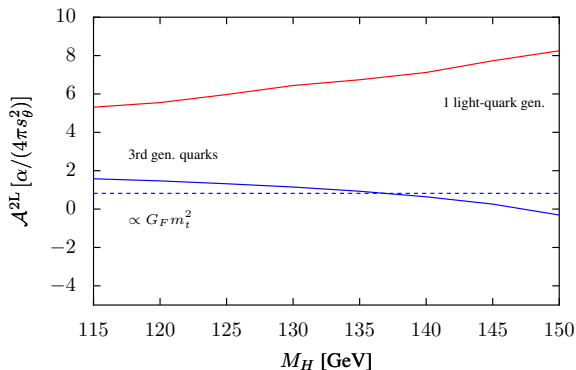
$$\Rightarrow \boxed{M_j = \underbrace{c_j \ln(m_f^2/s)}_{\text{analytically}} + M_j^{\text{reg}} \Rightarrow \underbrace{\sum c_j \ln(m_f^2/s)}_{\text{amplitude}} = 0 \Rightarrow m_f = 0}$$

- 5 Renormalized $\mathcal{A}^{\text{NLO}} = \sum a_j M_j^{\text{reg}}$ **evaluated numerically**

* No details about numerical part; focus on the **threshold behaviour**

EW corrections to $gg \rightarrow H$ below 150 GeV

Anatomy of EW corrections to $gg \rightarrow H$ for $115 \text{ GeV} < M_H < 150 \text{ GeV}$



$M_H [\text{GeV}]$	$\delta^{EW} [\%]$
115	+4.73
120	+4.92
125	+5.12
130	+5.31
135	+5.49
140	+5.66
145	+5.80
150	+5.90

$$\sigma = \frac{G_F \alpha_S^2}{512 \sqrt{2} \pi} |\mathcal{A}^{1L} + \mathcal{A}^{2L} + \dots|^2 = \sigma^{\text{LO}} (1 + \delta^{\text{EW}}) \quad \mathcal{A}^{2L} = \mathcal{A}_{\text{1q}}^{2L} + \mathcal{A}_{\text{3gen}}^{2L}$$

- Agreement with **light quarks** Aglietti, Bonciani, Degrassi, Vicini '04 and corrected (1PR) **3rd gen. quarks** Degrassi, Maltoni '04
- **Light quarks** dominate respect to $\propto G_F m_t^2$ Djouadi, Gambino '94

Around the VV thresholds: square-root divergencies

Problem with the crossing of both WW and ZZ : square-root divergencies

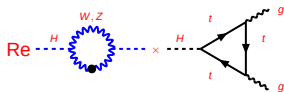
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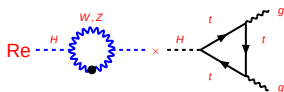
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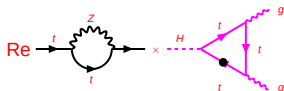
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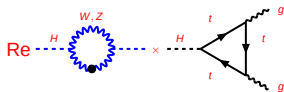
der. finite
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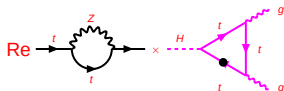
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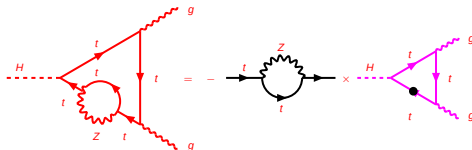
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der. finite
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3) (irreducible 2-loop diagrams with a bubble insertion in an internal t line)



fin. part
for $M_H = 2M_t$

$\Rightarrow$ would-be **divergency** for $M_H = 2M_t$ as 1-loop $\otimes$ 1-loop, finite as in class 2)

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Cure problems with crossing of thresholds implementing the complex-mass scheme at 1 loop Denner, Dittmaier, Roth, Wieders'05

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Introduce the CMS in both threshold factors β_V and coefficients $A_{\text{div}}^{1,2}$

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2) Complete introduction of the complex-mass scheme

Introduce the CMS in all divergent and finite terms of the amplitude

Practical implementation of the CMS

Practical implementation of the complex-mass scheme through two steps:

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- ⇒ Replace the **conventional on-shell mass renormalization** equations with the associated expressions for the **complex poles** of the W and Z bosons

$$m_i^2 = M_i^2 \left[1 + \frac{G_F M_W^2}{2\sqrt{2}\pi^2} \text{Re}\Sigma_i^{(1)}(M_i^2) \right] \quad \Rightarrow \quad m_i^2 = s_i \left[1 + \frac{G_F s_W}{2\sqrt{2}\pi^2} \Sigma_i^{(1)}(s_i) \right]$$

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- ⇒ Insert the **full self-energy for the W boson** in the renormalization equation for the Fermi-coupling constant, expressed through the **complex mass of the W** , s_W

$$g = 2 \left(\sqrt{2} G_F s_W \right)^{1/2} \left[1 - \frac{G_F s_W}{4\sqrt{2} \pi^2} \Delta \right], \Delta = \Sigma_W^{(1)}(0) - \Sigma_W^{(1)}(s_W) + 6 + \frac{7 - 4s_\theta^2}{2s_\theta^2} \ln c_\theta^2$$

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CMS → replacements done also at the level of the couplings ⇒ $s_\theta^2 = 1 - s_W/s_Z$

Introduction of complex masses in loop integrals

Loop integrals have to be evaluated with complex masses

- Internal masses complexified $\rightarrow$ no problems; the replacement $M^2 - i0 \Rightarrow s = \mu^2 - i\mu\gamma$ does not clash with the $-i0$ prescription

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$$B_0(p^2; 0, 0) \Rightarrow \int_0^1 dx \ln \chi(x), \quad \chi(x) = p^2 x(1-x) - i0$$

$$\text{real } M_W^2 \Rightarrow \text{Re}\chi(x) = -M_W^2 x(1-x) < 0, \quad \text{Im}\chi(x) = -0 < 0$$

$$\text{complex } s_W \Rightarrow \text{Re}\chi(x) = -\mu_W^2 x(1-x) < 0, \quad \text{Im}\chi(x) = +\mu_W \gamma_W x(1-x) > 0$$

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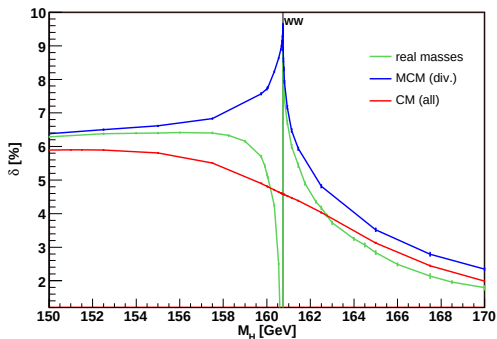
$\rightarrow$ 0-width limit of the complex-mass case doesn't reproduce the real-mass one

$\rightarrow$ define an analytic continuation of $\ln$ such that the value for a stable gauge boson is smoothly approached when the coupling tends to zero

$$\ln(z_R + iz_I) \Rightarrow \ln(z_R + iz_I) - 2i\pi\theta(-z_R), \quad \lim_{z_I \rightarrow 0} = \underbrace{\ln(z_R - i0)}_{\text{real mass}}$$

Threshold behaviour for $gg \rightarrow H$

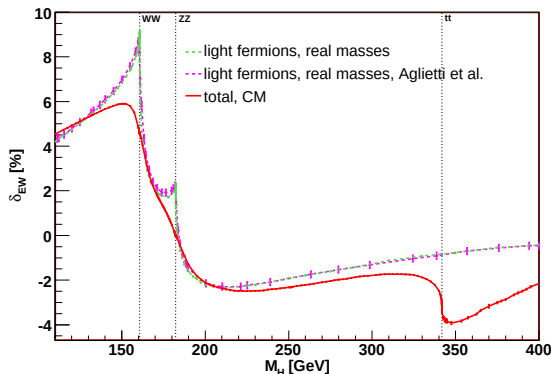
Comparison of EW corrections to $gg \rightarrow H$ around the WW threshold, obtained using different schemes for treating unstable particles



- Result obtained with real masses divergent at WW ; good approx. below/above
- MCM setup gives finite result at WW ; large effect 9.6 % associated with cusp
- CM setup smoothens singular behaviour; effects at threshold reduced to 4.6 %

EW corrections to $gg \rightarrow H$ (I)

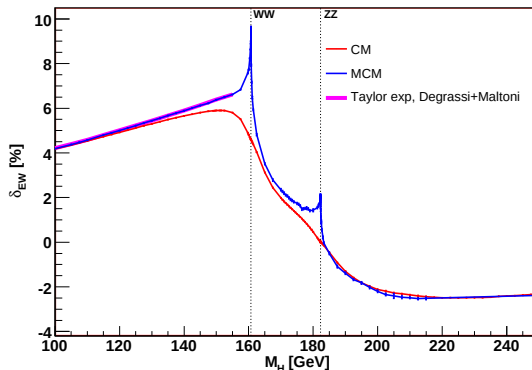
Summary of EW corrections to $gg \rightarrow H$ for $100 \text{ GeV} < M_H < 400 \text{ GeV}$



- Full agreement with Aglietti, Bonciani, Degrassi, Vicini'04 using RMs as input data; light fermions dominate up to 300 GeV (max +9%)
- CMs change the result around WW and ZZ thresholds, where cusps disappear
- Top-quark diagrams relevant at $t\bar{t}$ threshold, with relative correction $\delta_{ew} \sim -4\%$

EW corrections to $gg \rightarrow H$ (II)

Summary of EW corrections to $gg \rightarrow H$ for $100 \text{ GeV} < M_H < 250 \text{ GeV}$



- Full agreement below WW with Taylor expansion Degrassi, Maltoni'04 using CMs as input data in divergent terms only
- Implementation of CMs everywhere smoothens the result around WW and ZZ thresholds and leads to a -4% shift respect to MCM at 140 GeV

Inclusion of NLO EW effects

Partonic result convoluted with the **PDFs**:

$$\begin{aligned} \sigma(h_1 h_2 \rightarrow H) = & \sum_{i,j} \int_0^1 dx_1 dx_2 f_{i,h_1}(x_1, \mu_F^2) f_{j,h_2}(x_2, \mu_F^2) \times \\ & \times \int_0^1 dz \delta\left(z - \frac{M_H^2}{s x_1 x_2}\right) z \sigma^0 G_{ij}(z, \mu_R^2, \mu_F^2) \end{aligned}$$

I) **Complete factorization** $G_{ij} \rightarrow (1 + \delta_{EW}) G_{ij}$

analogous to Aglietti, Bonciani, Degraffi, Vicini '06 light Higgs

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II) **Partial factorization** $G_{ij} \rightarrow G_{ij} + \alpha_S^2 \delta_{EW} G_{ij}^{(0)}$

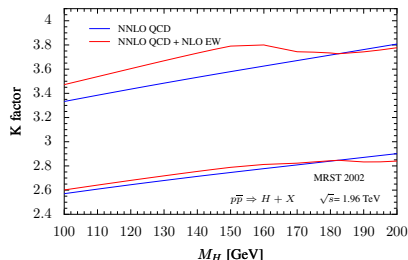
- Vary $\mu_{R,F}$ for $M_H/2 < \mu_{R,F} < 2M_H$ with $\mu_R/2 < \mu_F < 2\mu_R$

$\Rightarrow$ For each $M_H \rightarrow \sigma_{ref}, \sigma_{max}, \sigma_{min}$, uncertainty band $\sigma_{max} - \sigma_{min}$

- Very conservative estimate, since in PF option the scale dependence is controlled by the LO QCD result (multiplied by δ_{EW})

NLO EW corrections at the Tevatron

Impact of NLO EW effects at Tevatron II, $\sqrt{s} = 1.96$ TeV,
 $100 \text{ GeV} < M_H < 200 \text{ GeV}$ (using HIGGSNNLO, by M.Grazzini)

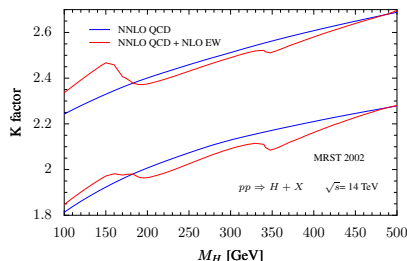


M_H [GeV]	δ_{CF} [%]	δ_{PF} [%]
120	+4.9	+1.6
140	+5.7	+1.8
160	+4.8	+1.5
180	+0.5	+0.1
200	-2.1	-0.6

- Uncertainty band shows stronger sensitivity on the Higgs mass, once NLO EW effects are included
- Impact of NLO EW corrections smaller respect to NNLL resummation Catani, de Florian, Grazzini, Nason'03 (+12 % for $M_H = 120$ GeV)
- Effective-theory computation of mixed three-loop EW and QCD effects by Anastasiou, Boughezal, Petriello'08 supports the hypothesis of a complete factorization

NLO EW corrections at the LHC

Impact of NLO EW effects at LHC, $\sqrt{s} = 14$ TeV,
 $100 \text{ GeV} < M_H < 500 \text{ GeV}$ (using HIGGSNNLO, by M.Grazzini)



M_H [GeV]	δ_{CF} [%]	δ_{PF} [%]
120	+4.9	+2.4
150	+5.9	+2.8
200	-2.1	-1.0
310	-1.7	-0.9
410	-0.8	-0.8

- Uncertainty band shows stronger sensitivity on the Higgs mass, once NLO EW effects are included
- WW and $t\bar{t}$ thresholds visible, but smooth having introduced everywhere CMs
- Impact of NLO EW corrections comparable to that of NNLL resummation Catani, de Florian, Grazzini, Nason'03 (+6 % for $M_H = 120$ GeV); for large M_H NLO EW corrections turn negative, screening effect with NNLL resummation

Conclusions

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- Corrections range between +6% for $M_H = 150$ GeV (light fermions) and -4% for $M_H \sim 2 M_t$ (top-quark diagrams)
- Full implementation of the complex-mass scheme needed to avoid large effects at two-particle thresholds; for $M_H = 2 M_W$, corrections reduced from +10% (almost naive introduction of finite-width effects) to +5% (CMS in all terms)