

# Higgs characterisation

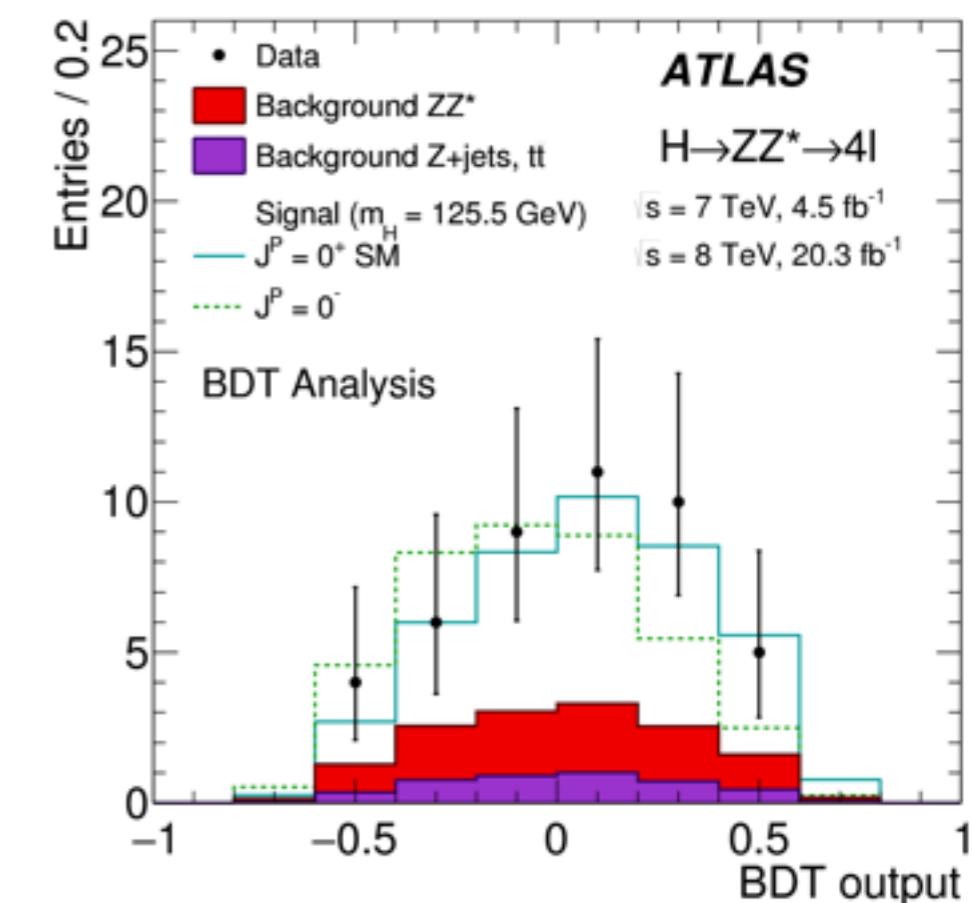
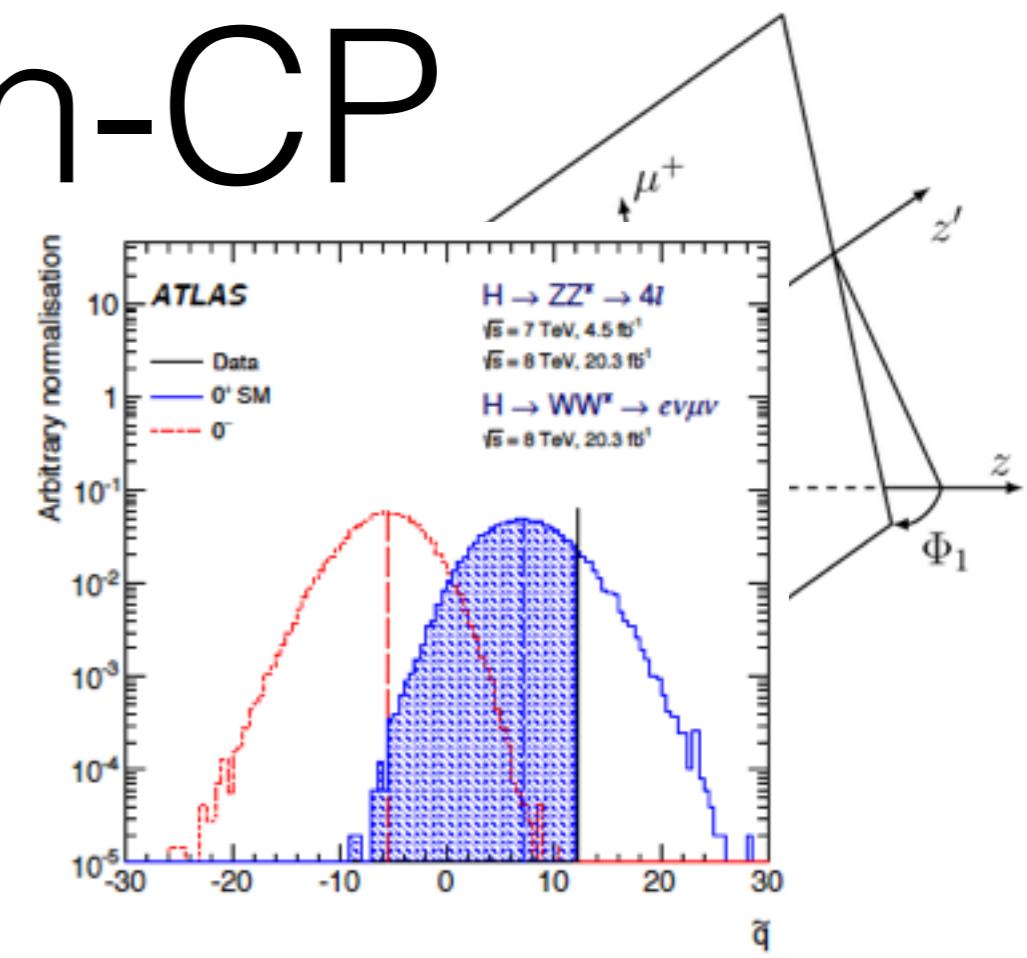
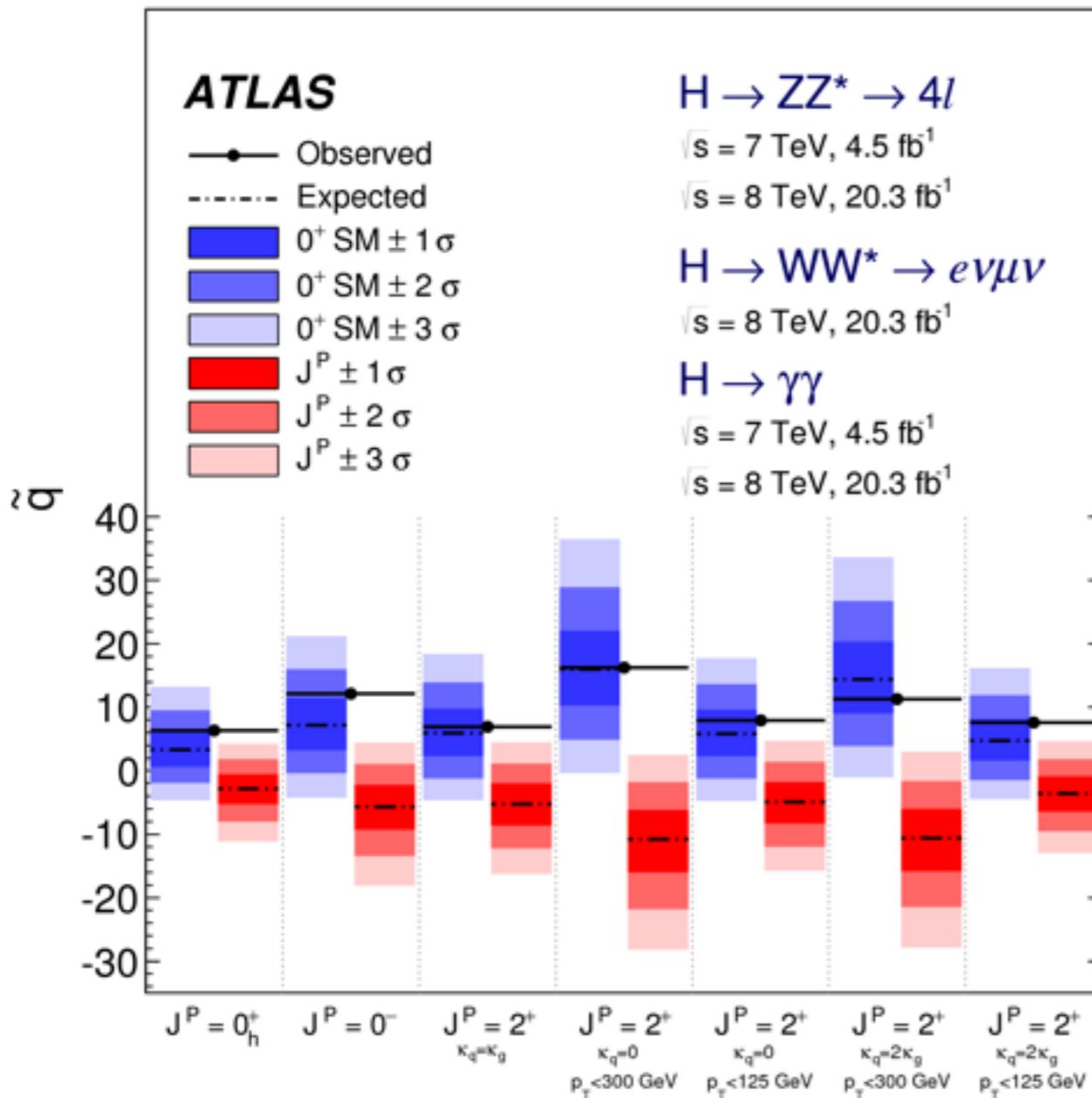
Kentarou Mawatari



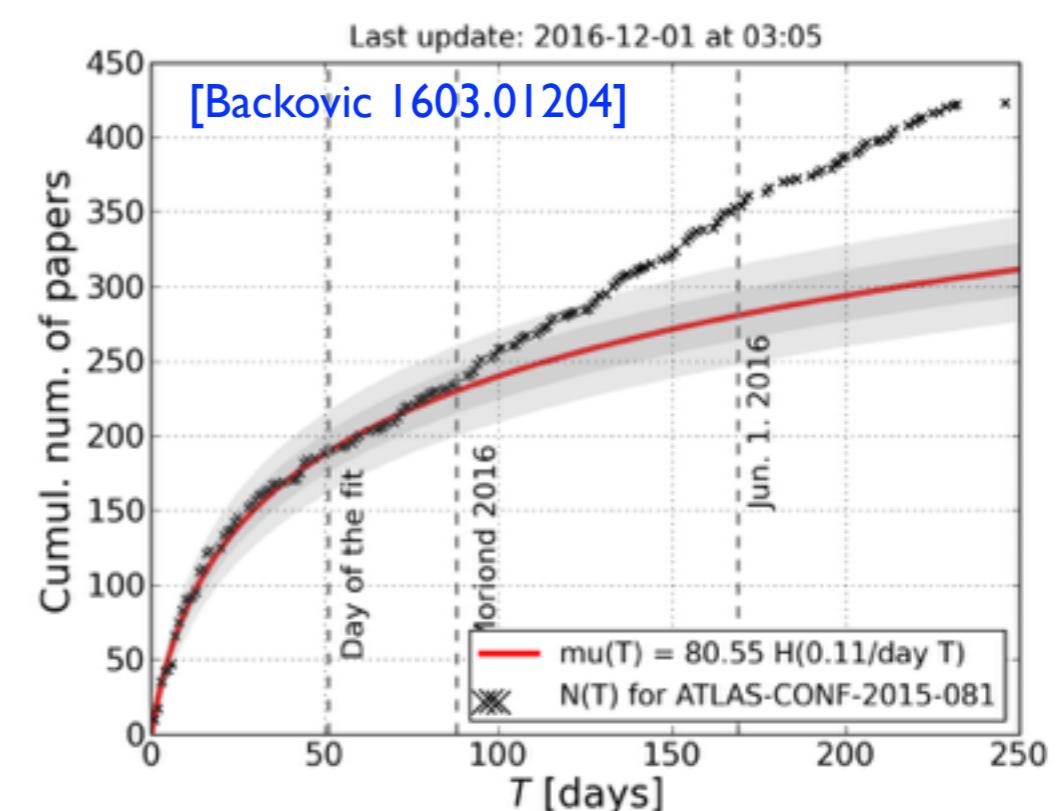
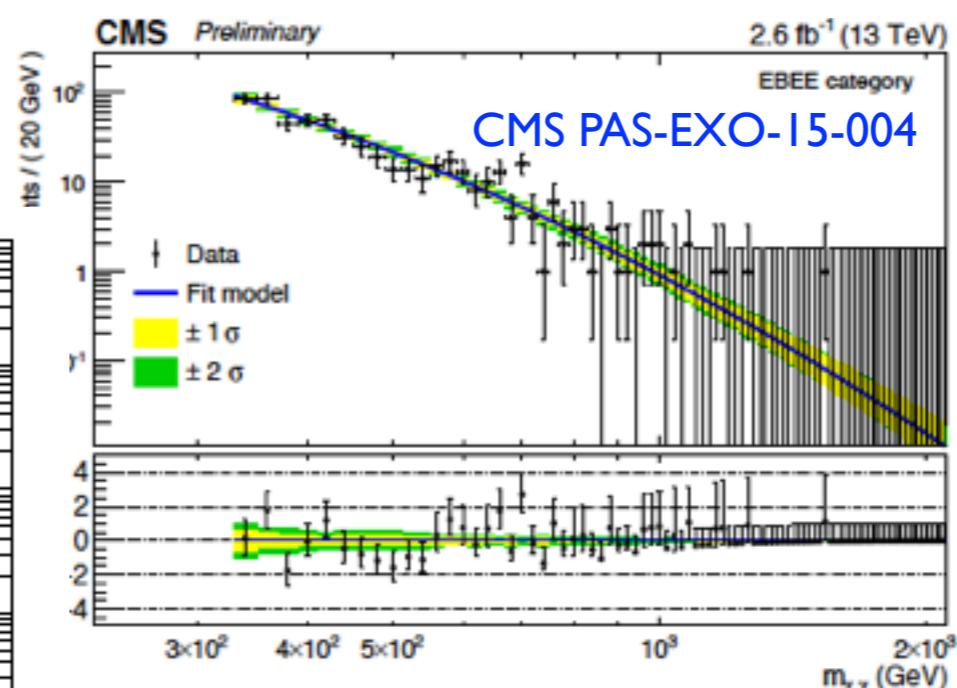
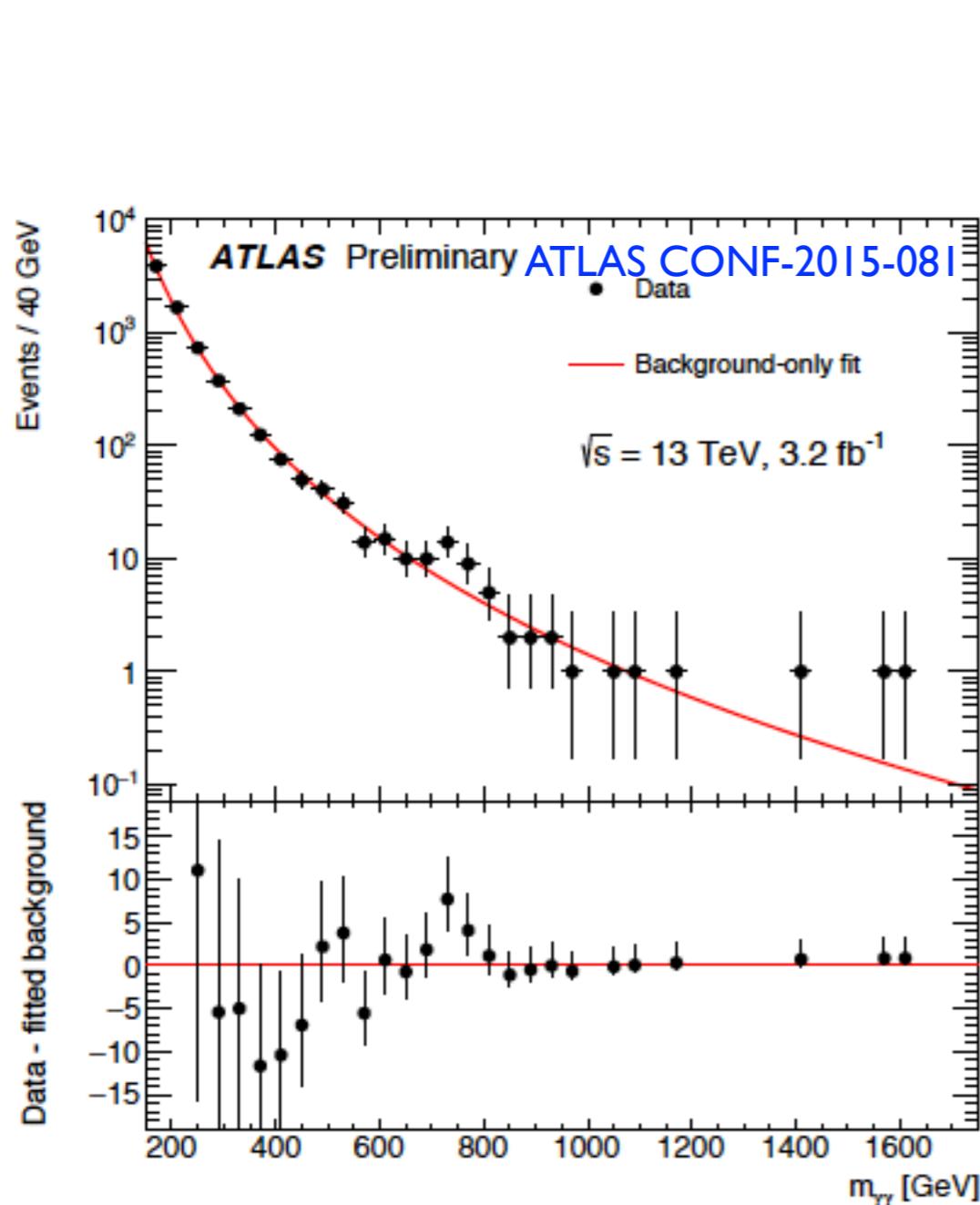
We would like to thank the organisers:  
Sabine, Hans Peter, Tilman, and Veronica!

# $h(125)$ spin-CP

$J^P = 0^+$  strongly favoured



# A year ago...

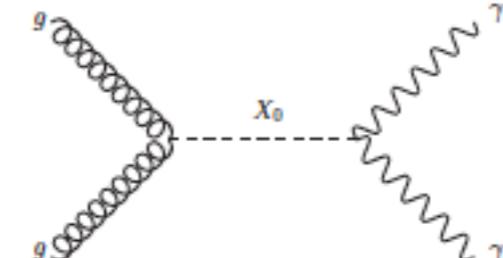


# BSM resonance characterisation

Martini, KM, Sengupta [1601.05729, PRD]

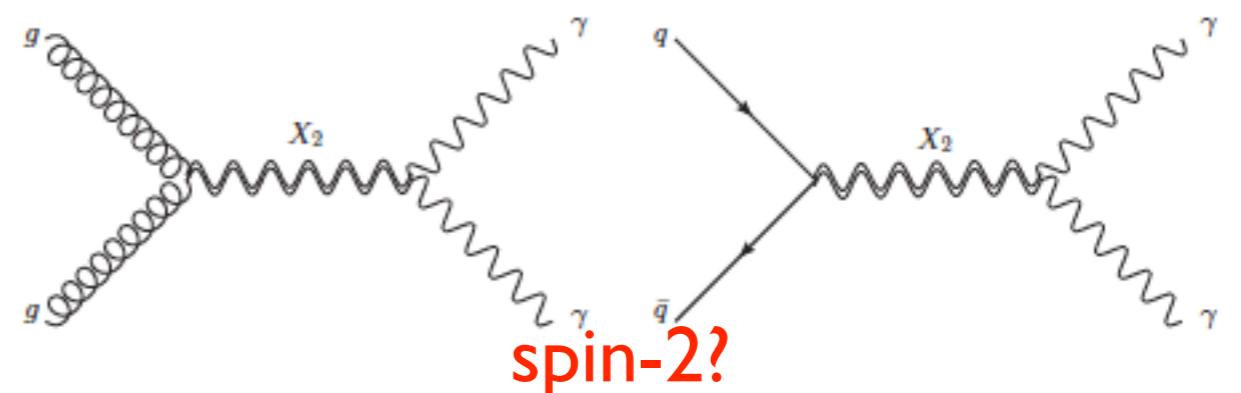
Bernon, Goudelis, Kraml, KM, Sengupta [1603.03421, JHEP]

$$\mathcal{L}_0^g = \frac{1}{4\Lambda} \left[ \overset{\sim}{\kappa_g} G_{\mu\nu}^a \overset{\sim}{G}^{a,\mu\nu} + \overset{\sim}{\kappa_\gamma} A_{\mu\nu} \overset{\sim}{A}^{\mu\nu} \right] X_0 ,$$

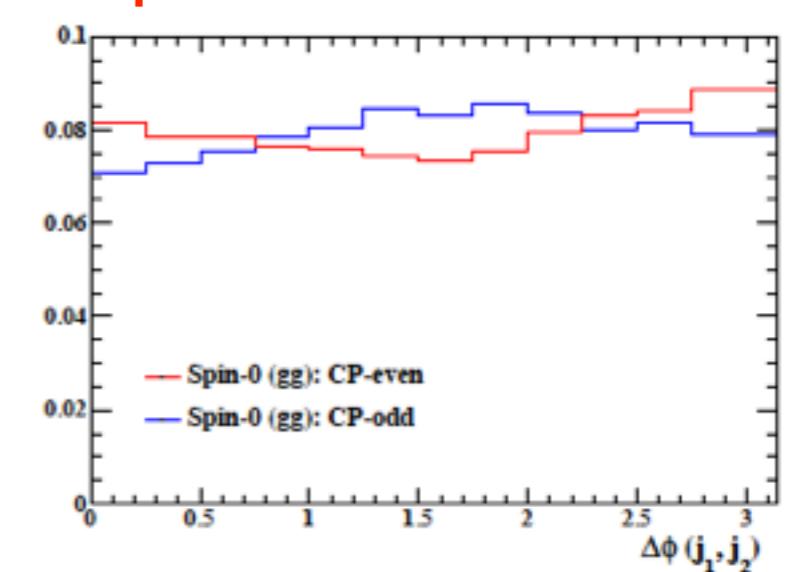
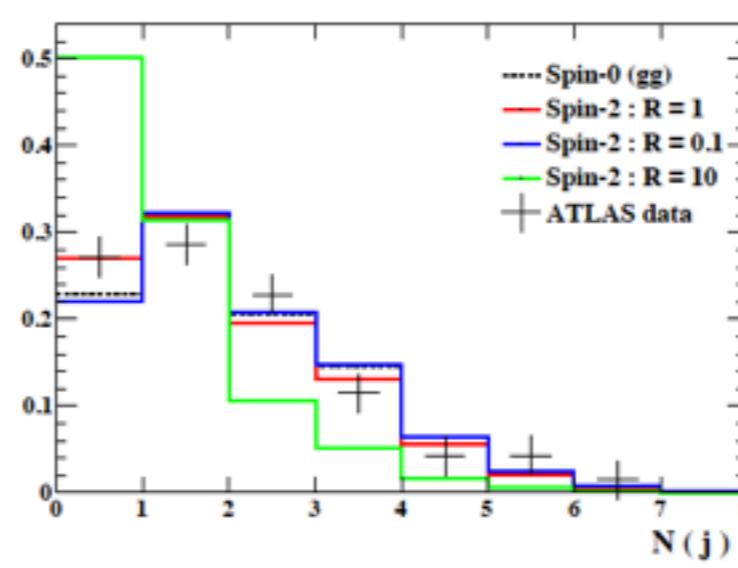
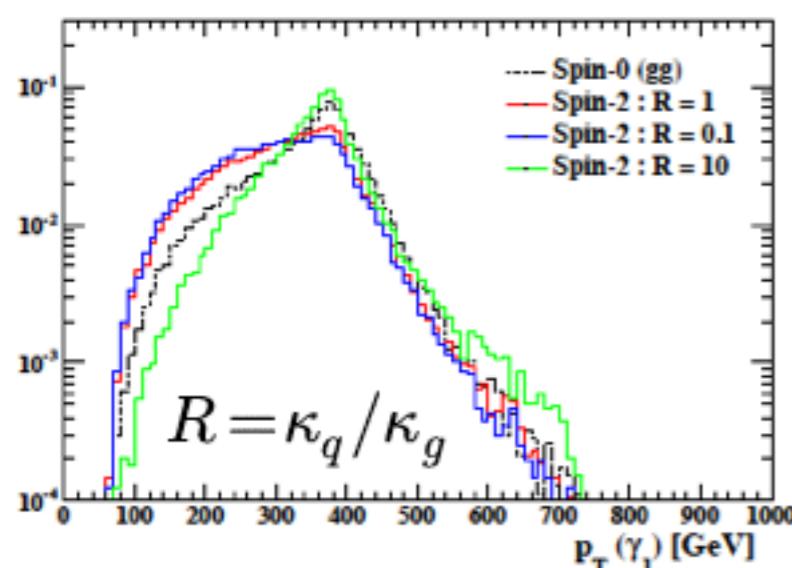


spin-0?

$$\mathcal{L}_2 = -\frac{1}{\Lambda} \left[ \kappa_g T_{\mu\nu}^g + \kappa_q T_{\mu\nu}^q + \kappa_\gamma T_{\mu\nu}^\gamma \right] X_2^{\mu\nu} ,$$



spin-2?



# BSM workflow at the LHC

- take a BSM model (symmetry, particle contents,...), i.e. Lagrangian

- derive the Feynman rules [FeynRules](#)

- draw Feynman diagrams for our interesting any processes

- compute the amplitude (squared)

- generate events

[Grace](#), [MadGraph](#),  
[Whizard](#), [CompHEP](#),  
[CalcHEP](#), [FDC](#), [Gosam](#)

- parton-shower/hadronisation [Herwig](#), [Pythia](#), [Sherpa](#)

- detector simulation [Fastjet](#), [Delphes](#)

- analysis [GAMBIT](#), [Checkmate](#), [FastLim](#), [MadAnalysis](#)



[micrOMEGAs](#)  
[MadDM](#)

# H-boson observation, evidence, precision, ...

## • 2012 July

- ▶ Observation of a new particle in the search for the Standard Model Higgs boson with the ATLAS detector at the LHC
- ▶ Observation of a new boson at a mass of 125 GeV with the CMS experiment at the LHC

## • 2013 July

- ▶ Evidence for the spin-0 nature of the Higgs boson

## • 2013 October

- ▶ Physics Nobel Prize [F. Englert (Brussels) and P. Higgs (Edinburgh)]

## • 2015 Spring

- ▶ LHC Run-II

looking for deviations from the SM  $\Leftrightarrow$  Higgs precision



# Higgs quantum numbers in weak boson fusion

---

Christoph Englert,<sup>a</sup> Dorival Gonçalves-Netto,<sup>b</sup> Kentarou Mawatari<sup>c</sup> and Tilman Plehn<sup>b</sup>

<sup>a</sup>*Institute for Particle Physics Phenomenology, Department of Physics, Durham University,  
DH1 3LE, U.K.*

<sup>b</sup>*Institut für Theoretische Physik, Universität Heidelberg,  
Philosophenweg 16, 69120 Heidelberg, Germany*

<sup>c</sup>*Theoretische Natuurkunde and IIHE/ELEM, Vrije Universiteit Brussel,  
and International Solvay Institutes, Pleinlaan 2, B-1050 Brussels, Belgium*

*E-mail:* [christoph.englert@durham.ac.uk](mailto:christoph.englert@durham.ac.uk),

[d.goncalves@thphys.uni-heidelberg.de](mailto:d.goncalves@thphys.uni-heidelberg.de), [kentarou.mawatari@vub.ac.be](mailto:kentarou.mawatari@vub.ac.be),  
[plehn@uni-heidelberg.de](mailto:plehn@uni-heidelberg.de)

**ABSTRACT:** Recently, the ATLAS and CMS experiments have reported the discovery of a Higgs like resonance at the LHC. The next analysis step will include the determination of its spin and CP quantum numbers or the form of its interaction Lagrangian channel-by-channel. We show how weak-boson-fusion Higgs production and associated  $ZH$  production can be used to separate different spin and CP states.

# Higgs Characterisation (HC)

via the FeynRules and MadGraph5\_aMC@NLO frameworks

- HC provides an automated NLO(QCD)+PS accurate tool and predictions to accomplish the most general and accurate characterisation of Higgs interactions in the main production and decay modes at the LHC.
- The code is publicly available at the FeynRules repository:  
<https://feynrules.irmp.ucl.ac.be/wiki/HiggsCharacterisation>

- ▶ **HC1:** “A framework for Higgs characterisation” JHEP11(2013)043 [[1306.6464](#)]  
Artoisenet, de Aquino, Demartin, Frederix, Frixione, Maltoni, Mandal, Mathews, Mawatari, Ravindran, Seth, Torrielli, Zaro
  - ➡ **HC framework based on the effective filed theory (EFT) approach**
- ▶ **HC2:** “Higgs characterisation via VBF/VH: NLO and parton-shower effects” EPJC74(2014)2710 [[1311.1829](#)]  
Maltoni, Mawatari, Zaro
  - ➡ **VBF and VH @ automated NLO+PS**
- ▶ **HC3:** “Higgs characterisation at NLO in QCD: CP properties of the top Yukawa” EPJC74(2014)3065 [[1407.5089](#)]  
Demartin, Maltoni, Mawatari, Page, Zaro
  - ➡ **GF (H+jets) and ttH @ automated NLO+PS**
- ▶ **HC4:** “Higgs production in association with a single top quark at the LHC” EPJC75(2015)267 [[1504.00611](#)]  
Demartin, Maltoni, Mawatari, Zaro
  - ➡ **tH @ automated NLO+PS**
- ▶ **HC5:** “tWH associated production at the LHC” EPJCxx(2016)xxx [[1607.05862](#)]  
Demartin, Maier, Maltoni, Mawatari, Zaro
  - ➡ **tWH @ automated NLO+PS**

# Tools for Higgs Physics

## Cross Section

### ggF

- [HIGLU](#) (NNLO QCD+NLO EW)
- [iHixs](#) (NNLO QCD+NLO EW)
- [FeHiPro](#) (NNLO QCD+NLO EW)
- [HNNLO, HRes](#) (NNLO+NNLL QCD)
- [SusHi](#) (NNLO QCD)
- [RGHiggs](#) (NNLO+NNNLL QCD)
- [ggHiggs](#) (approx. NNNLO QCD)

### VBF

- [VV2H](#) (NLO QCD)
- [VBFNLO](#) (NLO QCD)
- [HAWK](#) (NLO QCD+EW)
- [VBF@NNLO](#) (NNLO QCD)

### WH/ZH

- [V2HV](#) (NLO QCD)
- [HAWK](#) (NLO QCD+EW)
- [VH@NNLO](#) (NNLO)

### ttH

- [HQQ](#) (LO QCD)

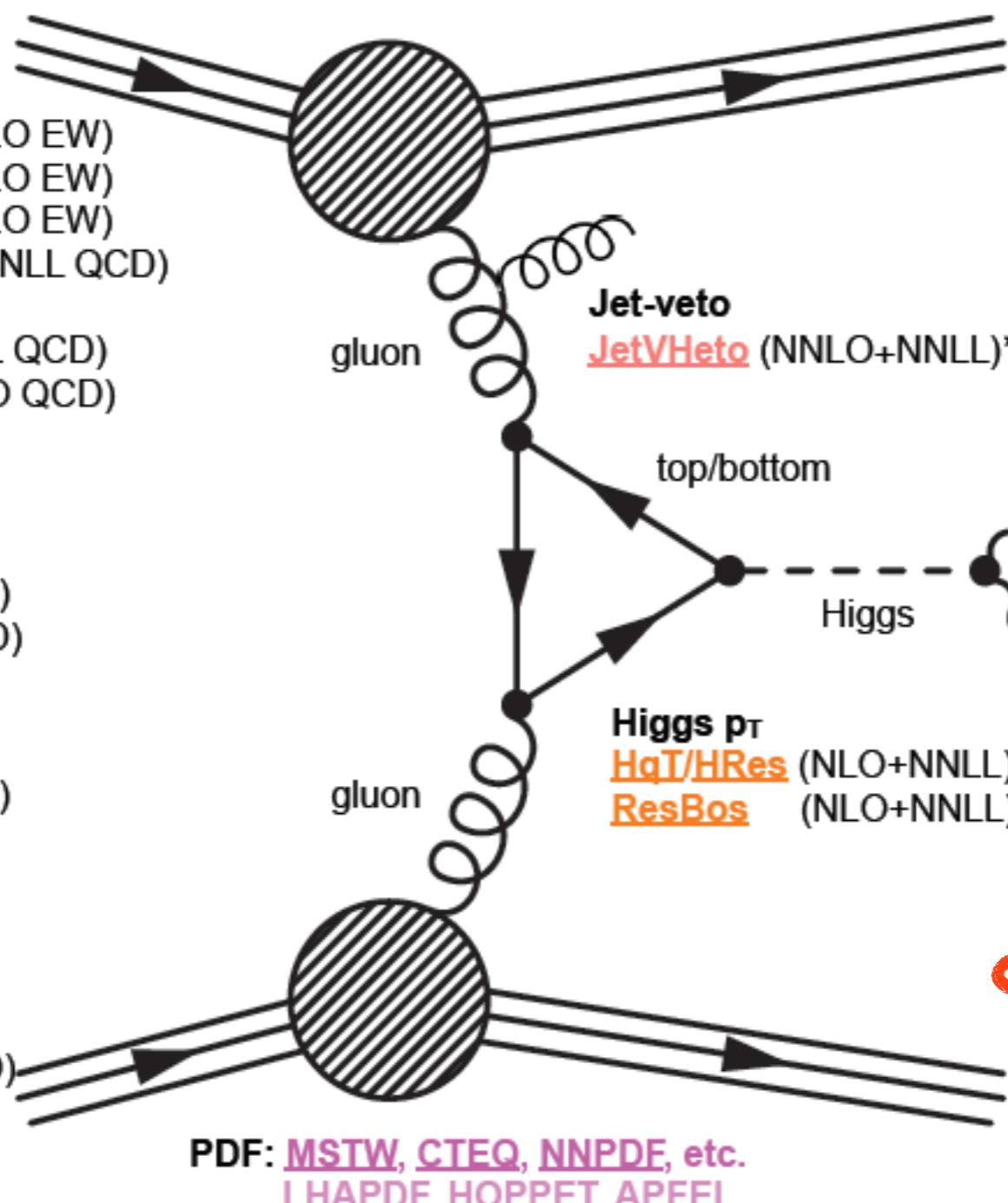
### bbH

- [bbh@NNLO](#) (NNLO QCD)

### HH

- [HPAIR](#) (NLO QCD)

+ private codes.



## NLO MC

- [POWHEG](#) [MiNLO](#)
- [MadGraph5](#) [aMC@NLO](#)
- [SHERPA](#) [MEPS@NLO](#)

## LO MC

- [gg2VV](#)

## NLO ME

- [MCFM](#), [MG5\\_aMC@NLO](#)

## W/Z

- Higgs Decay**
- [HDECAY](#) (NLO++)
- [Prophecy4f](#) (NLO)

## W/Z

## Higgs Properties

- [MELA/HHU](#), [MEKD](#)
- [MG5\\_aMC@NLO](#) (HC)

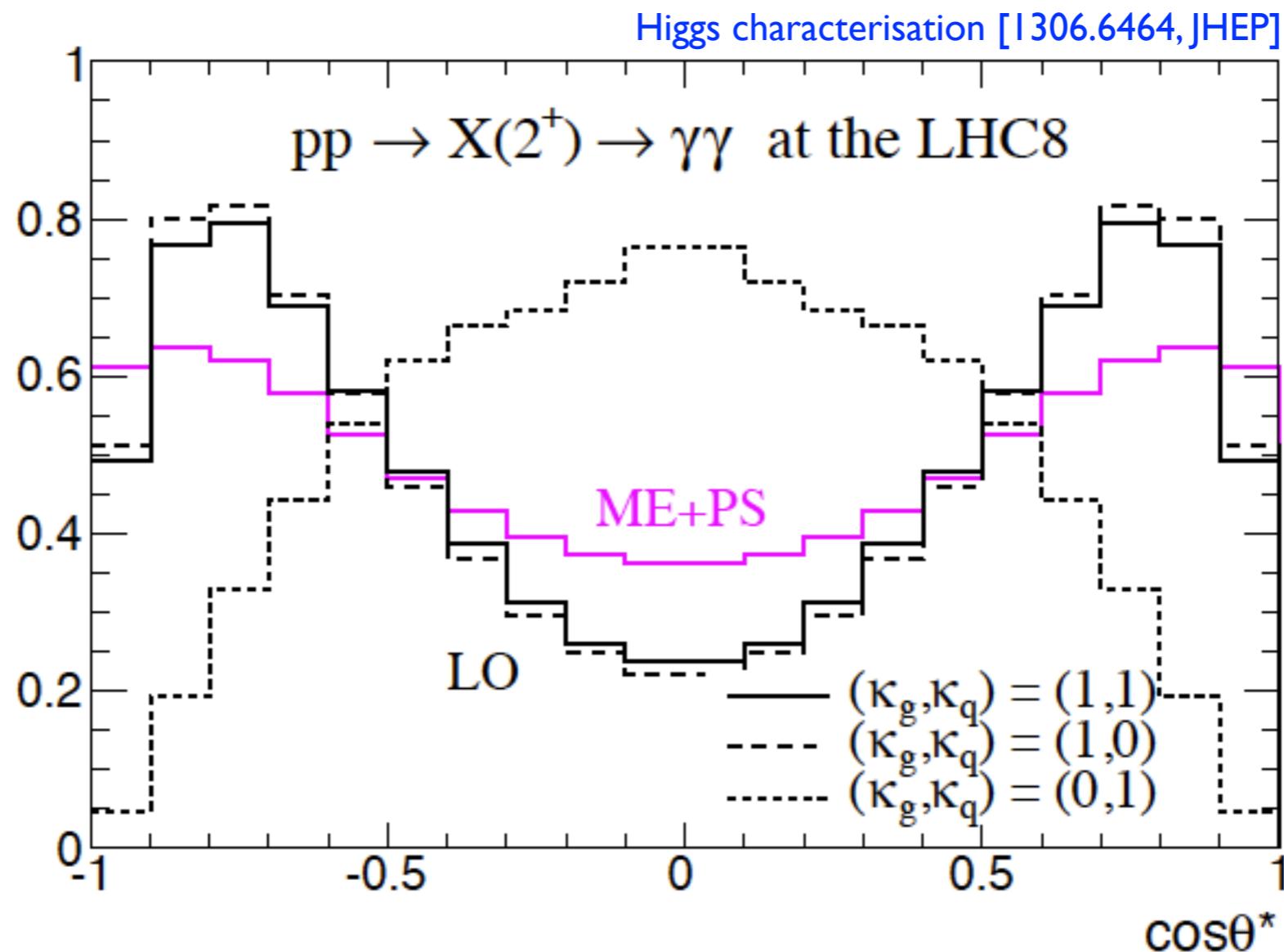
## MSSM/2HDM

- [FeynHiggs](#), [CPSuperH](#)
- [SusHi+2HDMC](#)
- [HIGLU+HDECAY](#)

\* NLO+NNLL in differential

Compiled by R. Tanaka, Jan. 2014

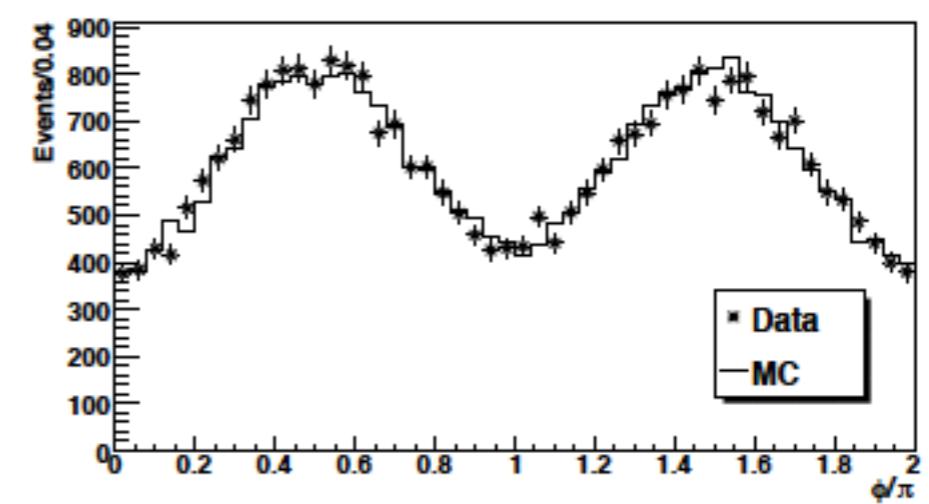
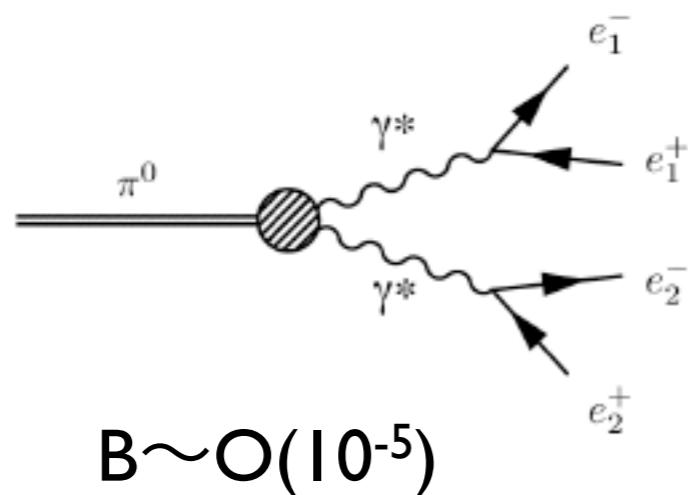
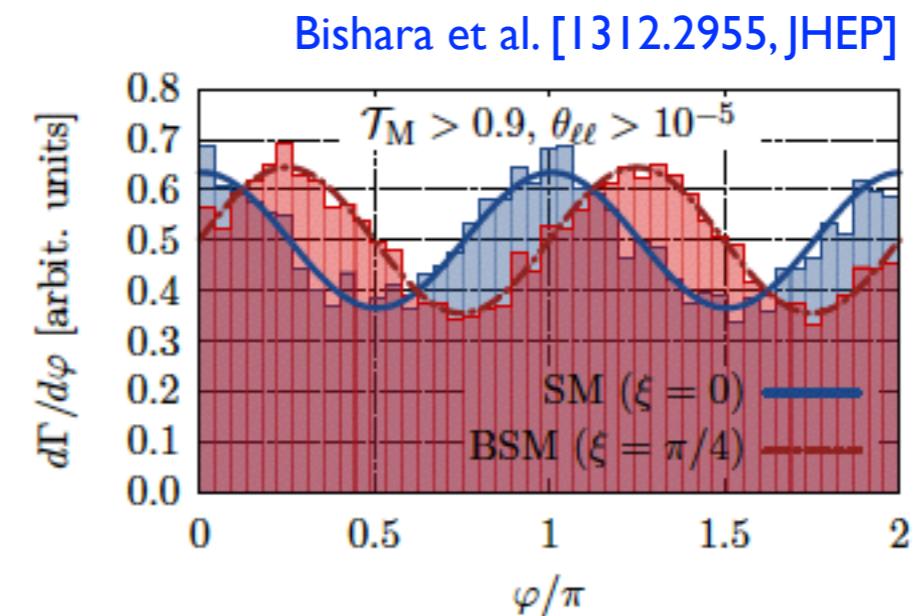
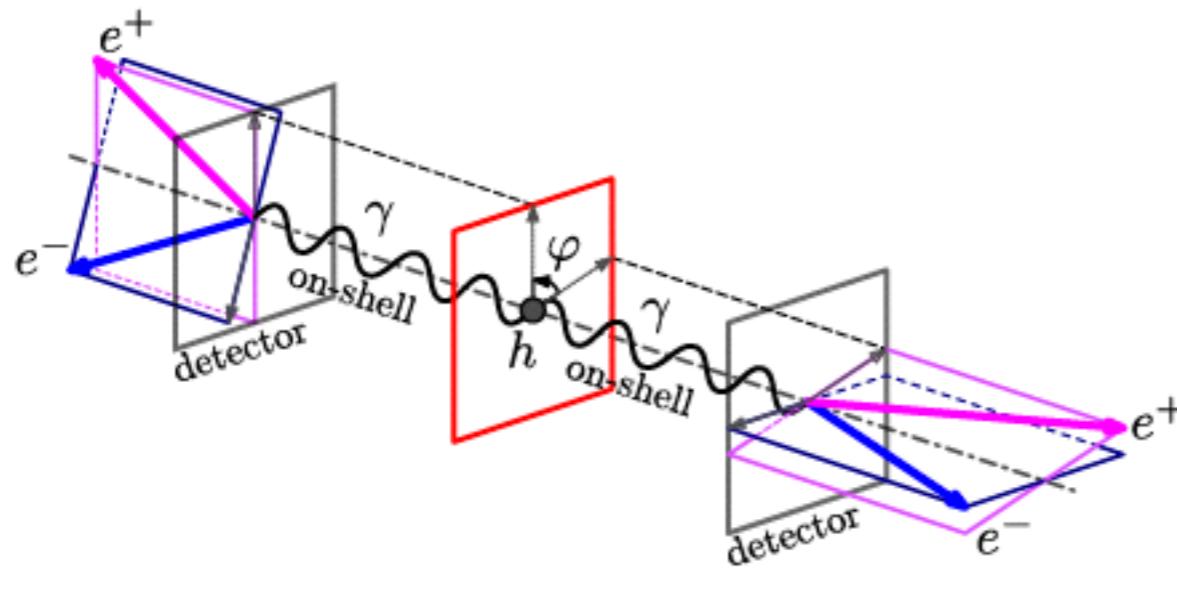
# pp>X> $\gamma\gamma$



$$\frac{d\sigma(gg)}{d\cos\theta^*} \propto |d_{22}^2(\theta^*)|^2 + |d_{2-2}^2(\theta^*)|^2 = \frac{1}{8}(1 + 6\cos^2\theta^* + \cos^4\theta^*) ,$$

$$\frac{d\sigma(q\bar{q})}{d\cos\theta^*} \propto |d_{12}^2(\theta^*)|^2 + |d_{1-2}^2(\theta^*)|^2 = \frac{1}{2}(1 - \cos^4\theta^*) .$$

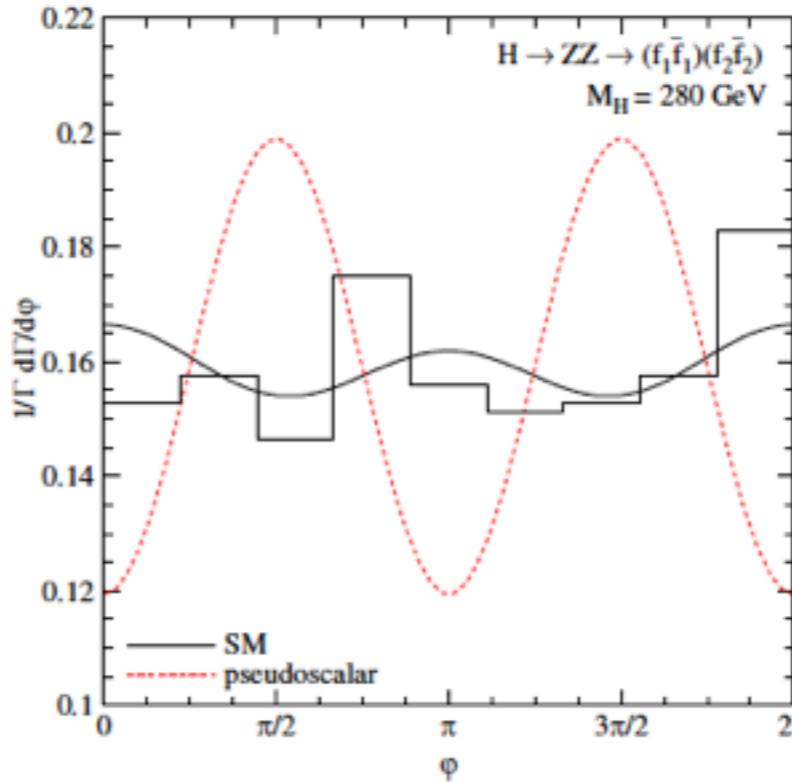
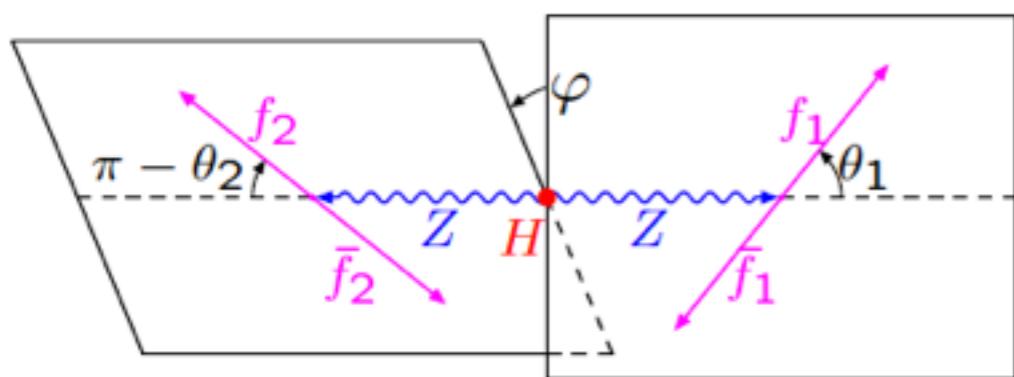
$\text{pp} > X > \gamma\gamma > 4e$



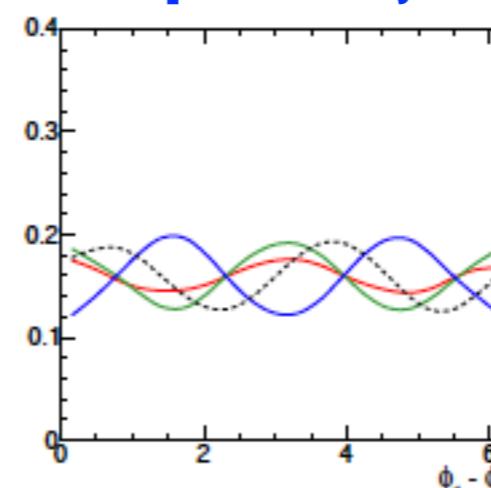
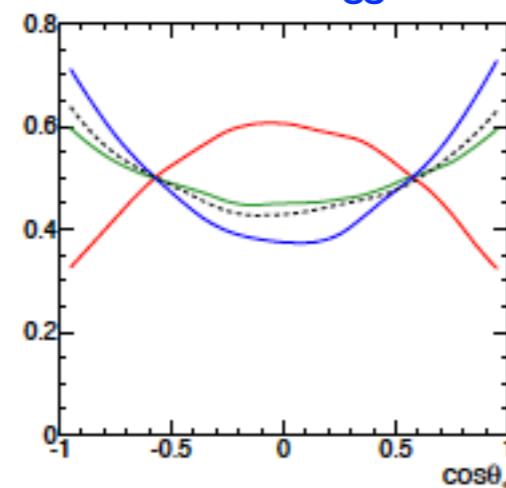
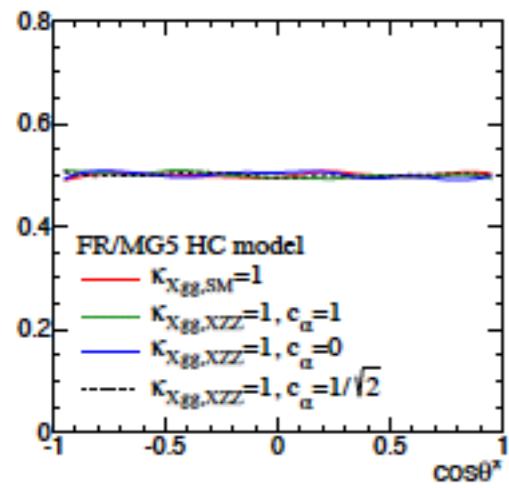
$$d\sigma/d\Delta\phi \sim 1 \pm A \cos 2\Delta\phi$$

# X>ZZ>4leptons

Choi, Miller, Muhlleitner, Zerwas [hep-ph/0210077, PLB]



Higgs characterisation [1306.6464, JHEP]



$$\mathcal{L}_{0_{SM}^+} = g_{0_{SM}^+} V_\mu V^\mu X_0$$

$$\mathcal{L}_{0_{D5}^+} = g_{0_{D5}^+} V_{\mu\nu} V^{\mu\nu} X_0$$

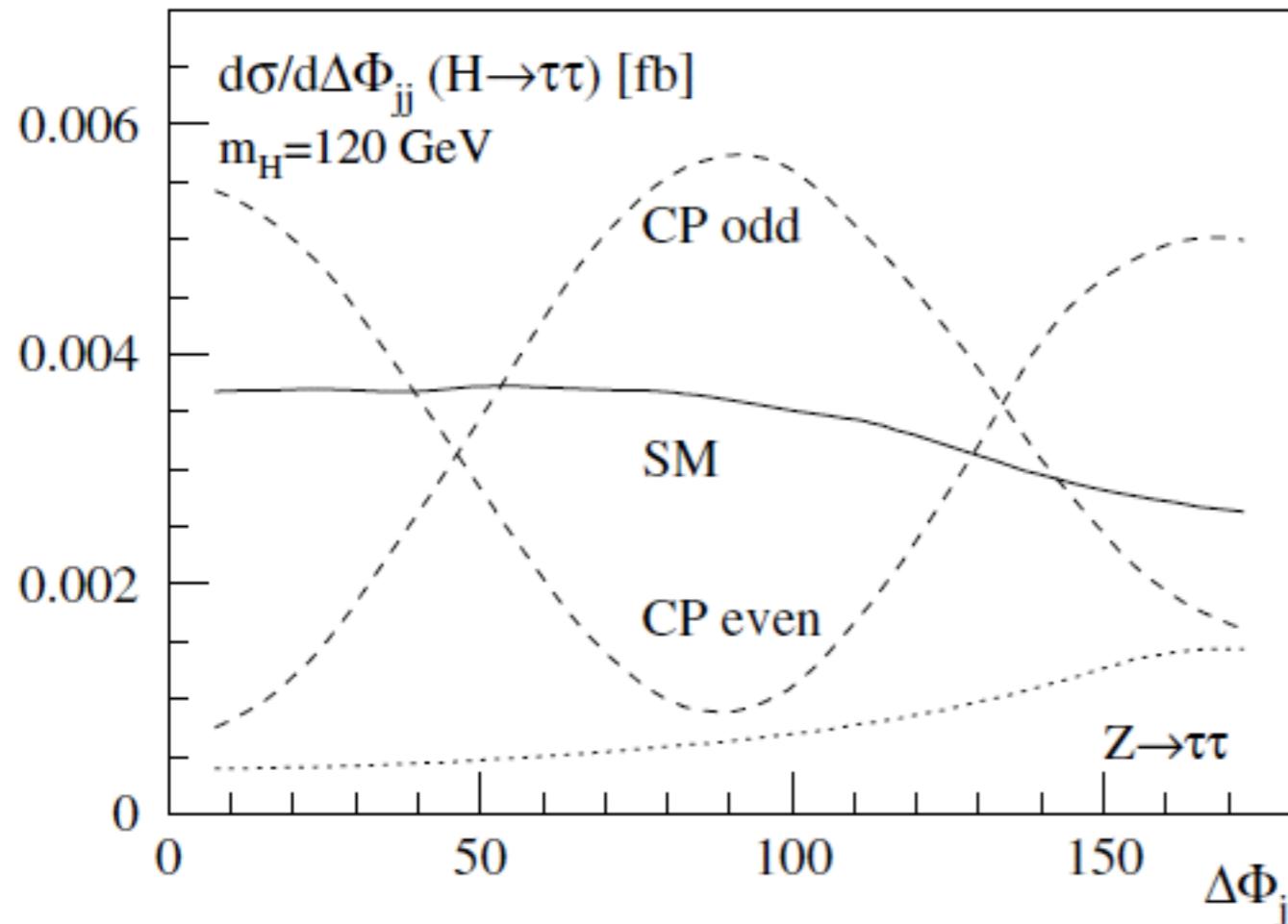
$$\mathcal{L}_{0_{D5}^-} = g_{0_{D5}^-} V_{\mu\nu} \tilde{V}^{\mu\nu} X_0$$

$d\sigma/d\Delta\phi \sim \text{const.}$  for  $0_{SM}^+$

$d\sigma/d\Delta\phi \sim 1 \pm A \cos 2\Delta\phi$  for  $0_{D5}^\pm$

# pp $\rightarrow X_{jj}$ (VBF: vector boson fusion)

Plehn, Rainwater, Zeppenfeld [hep-ph/0105325, PRL]

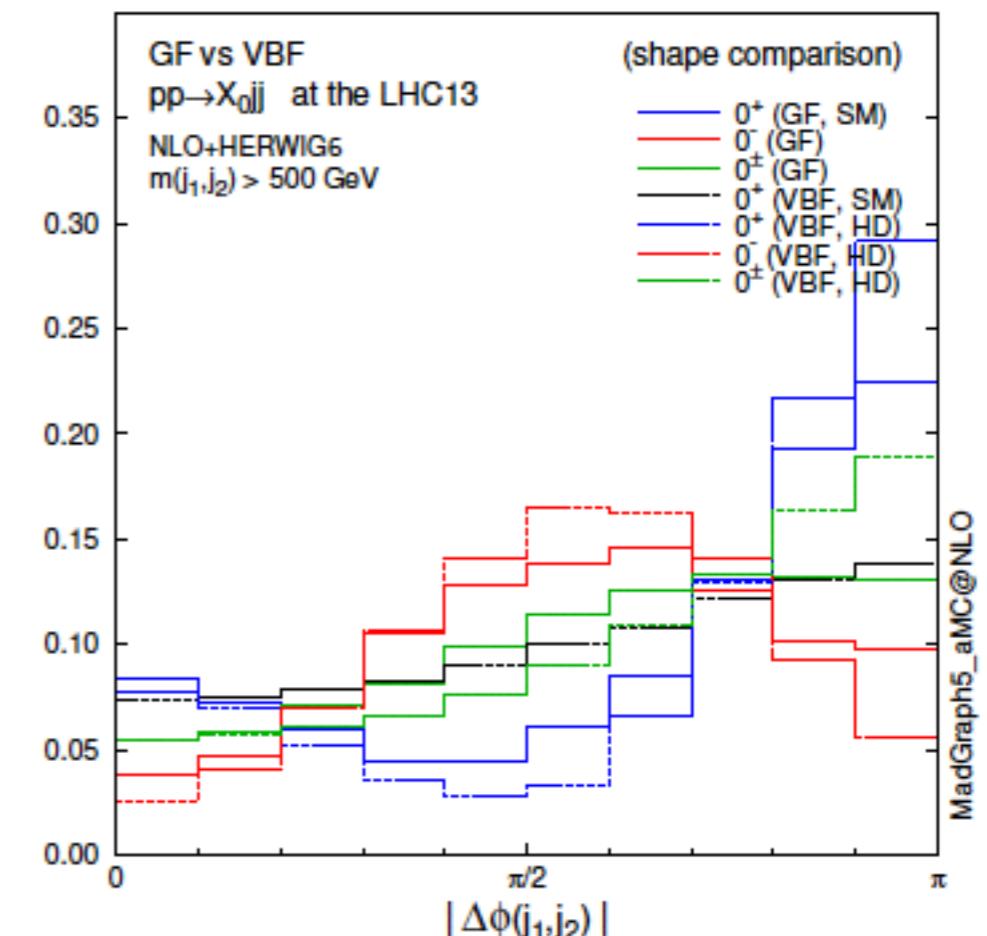


$$\mathcal{L}_{0_{SM}^+} = g_{0_{SM}^+} V_\mu V^\mu X_0$$

$$\mathcal{L}_{0_{D5}^+} = g_{0_{D5}^+} V_{\mu\nu} V^{\mu\nu} X_0$$

$$\mathcal{L}_{0_{D5}^-} = g_{0_{D5}^-} V_{\mu\nu} \tilde{V}^{\mu\nu} X_0$$

Demartin, Maltoni, KM, Page, Zaro [1407.5089, EPJC]

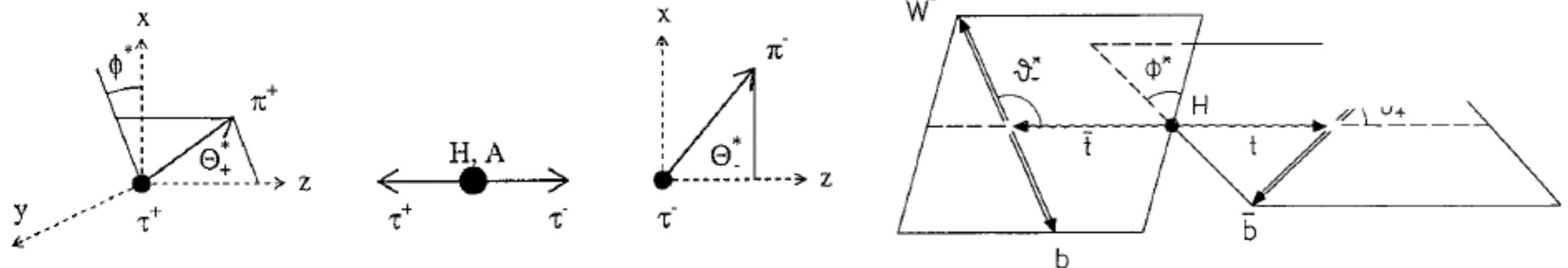


$$d\sigma/d\Delta\phi \sim \text{const. for } 0_{SM}^+$$

$$d\sigma/d\Delta\phi \sim 1 \pm A \cos 2\Delta\phi \text{ for } 0_{D5}^\pm$$

# X>TT

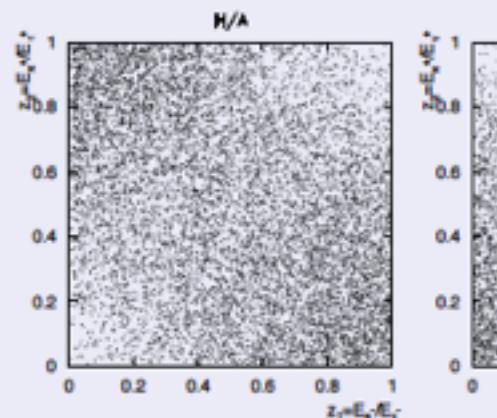
Kramer, Kuhn, Stong, Zerwas [hep-ph/9404280, ZPC]



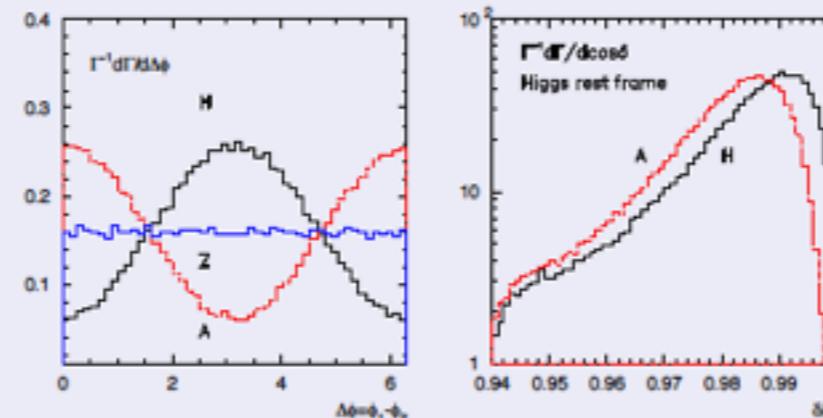
Hagiwara, Li, KM, Nakamura [1212.6247, EPJC]

Hagiwara, Ma, Mori [1609.00943]

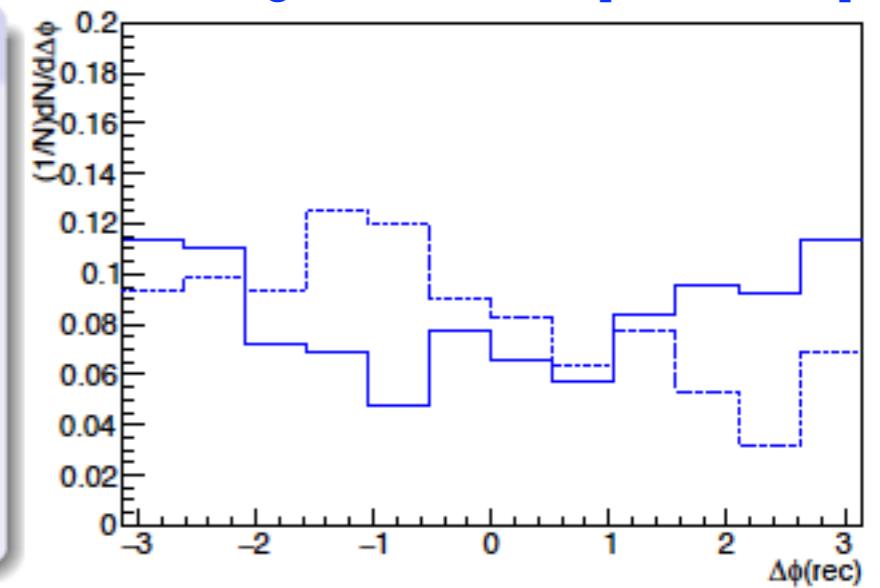
## Longitudinal spin (helicity) effect



## Transverse spin effect

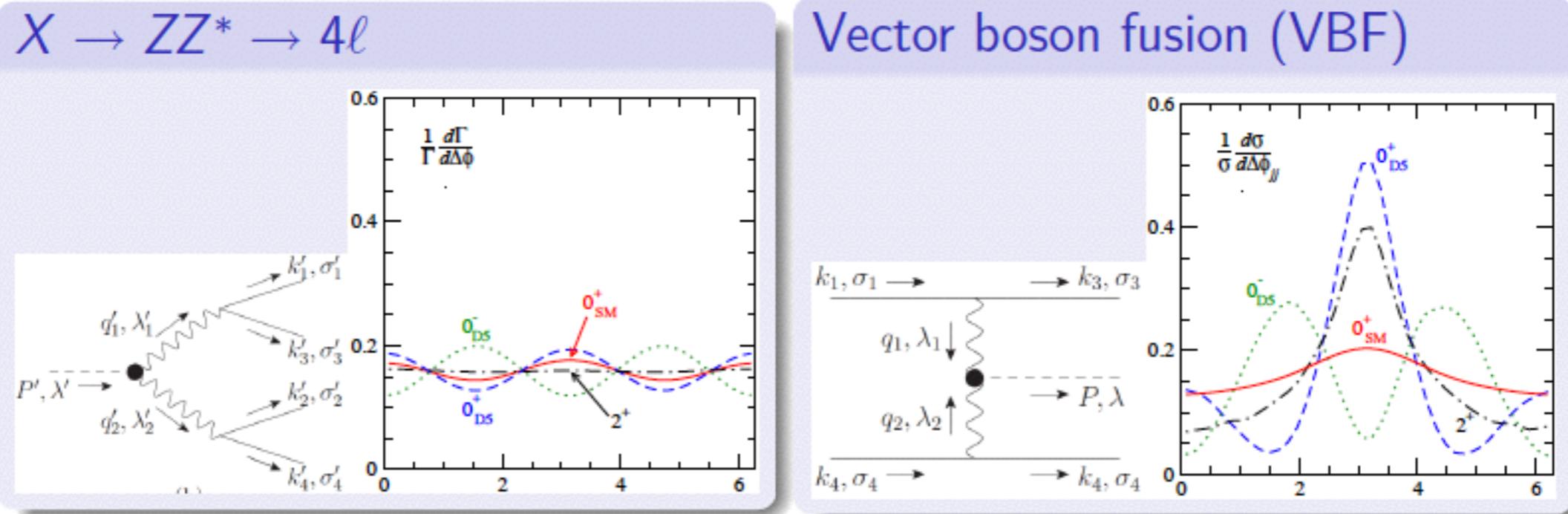


$$d^2\Gamma/dz_1 dz_2 \sim 1 \mp z_1 z_2 \text{ for spin-0/1}, \quad d\Gamma/d\Delta\phi \sim 1 \mp A \cos \Delta\phi \text{ for } 0^\pm$$



# Spin/parity determination with gauge bosons

Hagiwara, Li, KM [0905.4314, JHEP]  
Englert, Goncalves-Netto, KM, Plehn [1212.0843, JHEP]



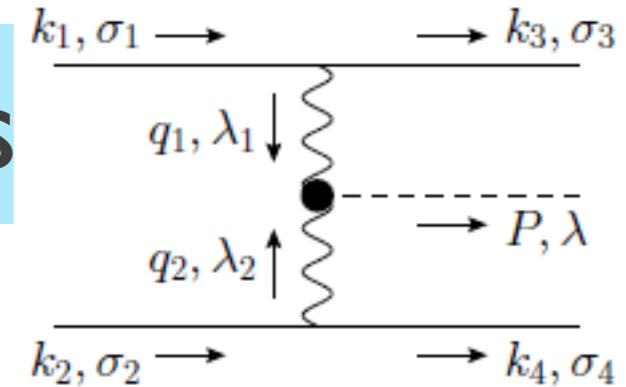
$$d\sigma/d\Delta\phi \sim \text{const. for } 0_{SM}^+, \quad d\sigma/d\Delta\phi \sim 1 \pm A \cos 2\Delta\phi \text{ for } 0_{D5}^\pm.$$

Nontrivial azimuthal angle correlations of the decay planes ( $X \rightarrow ZZ$ ) and the jets (VBF) can be explained as the quantum interference among different helicity states of the intermediate vector-bosons.

# Contents

1. Introduction Hagiwara, Li, KM [0905.4314, JHEP]
2. Helicity formalism and kinematics
3. Helicity amplitudes for VBF processes
4. Azimuthal correlations between the two jets
  - Higgs boson ( $J=0$ ) productions
  - (Massive graviton ( $J=2$ ) productions)
5. Summary

# The VBF helicity amplitudes



The helicity amplitudes for VBF processes

$$\mathcal{M}_{\sigma_1\sigma_3,\sigma_2\sigma_4}^{\lambda} = J^{\mu'_1}(k_1, k_3; \sigma_1, \sigma_3) \frac{-g_{\mu'_1\mu_1} + \frac{q_{1\mu'_1}q_{1\mu_1}}{m_V^2}}{q_1^2 - m_V^2} J^{\mu'_2}(k_2, k_4; \sigma_2, \sigma_4) \frac{-g_{\mu'_2\mu_2} + \frac{q_{2\mu'_2}q_{2\mu_2}}{m_V^2}}{q_2^2 - m_V^2} \Gamma_{XVV}^{\mu_1\mu_2}(q_1, q_2; \lambda)^*$$

can be expressed by using

completeness relation

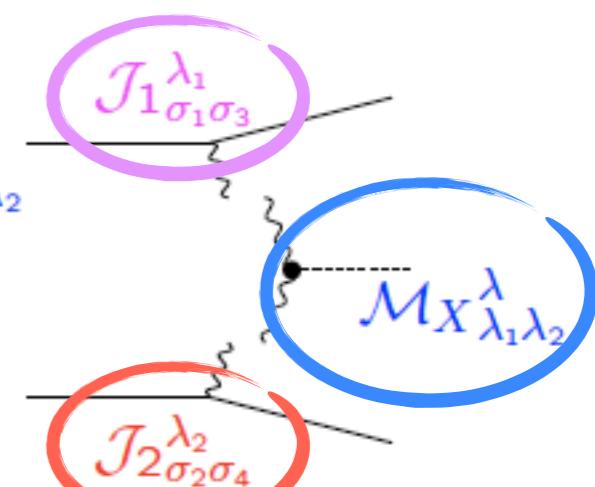
$$-g_{\mu'\mu} + \frac{q_i\mu'q_i\mu}{q_i^2} = \sum_{\lambda_i=\pm,0} (-1)^{\lambda_i+1} \epsilon_{\mu'}(q_i, \lambda_i)^* \epsilon_{\mu}(q_i, \lambda_i)$$

current conservation

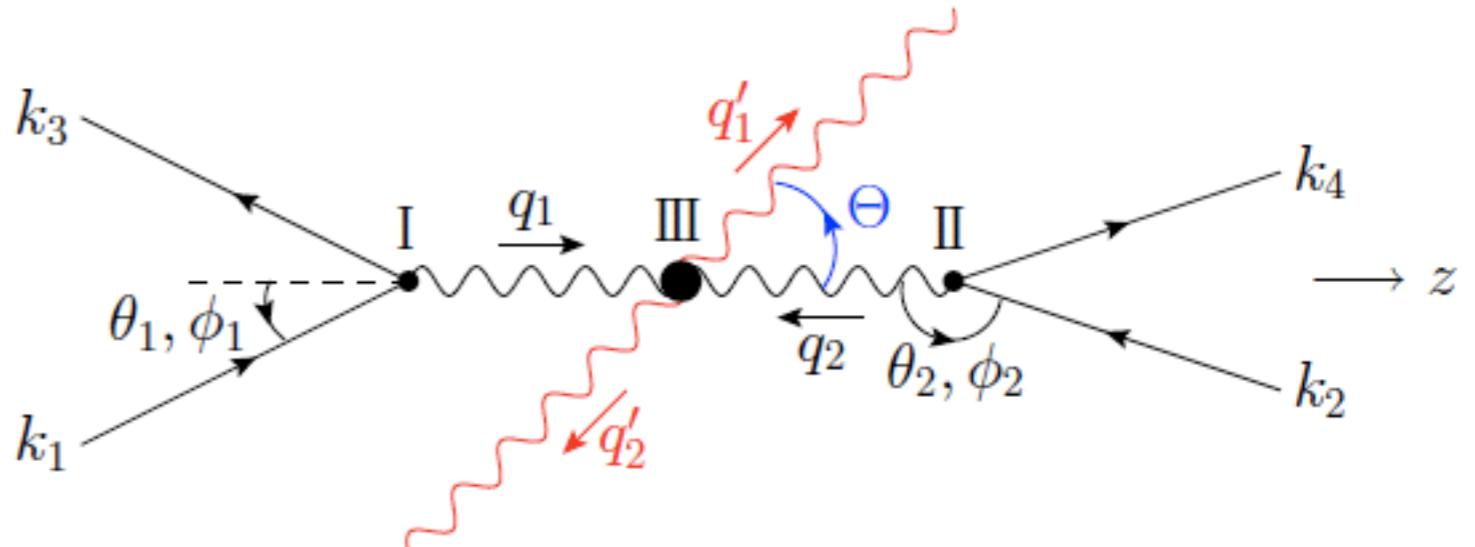
$$q_i\mu J^{\mu}(k_i, k_{i+2}; \sigma_i, \sigma_{i+2}) = 0$$

as the product of the three helicity amplitudes summed over the polarization of the intermediate vector-bosons:

$$\begin{aligned} \mathcal{M}_{\sigma_1\sigma_3,\sigma_2\sigma_4}^{\lambda} &= \frac{1}{q_1^2 - m_V^2} J^{\mu'_1}(k_1, k_3; \sigma_1, \sigma_3) \sum_{\lambda_1=\pm,0} (-1)^{\lambda_1+1} \epsilon_{\mu'_1}(q_1, \lambda_1)^* \epsilon_{\mu_1}(q_1, \lambda_1) \\ &\quad \times \frac{1}{q_2^2 - m_V^2} J^{\mu'_2}(k_2, k_4; \sigma_2, \sigma_4) \sum_{\lambda_2=\pm,0} (-1)^{\lambda_2+1} \epsilon_{\mu'_2}(q_2, \lambda_2)^* \epsilon_{\mu_2}(q_2, \lambda_2) \\ &\quad \times \Gamma_{XVV}^{\mu_1\mu_2}(q_1, q_2; \lambda)^* \\ &= \frac{1}{(q_1^2 - m_V^2)(q_2^2 - m_V^2)} \sum_{\lambda_1=\pm,0} \sum_{\lambda_2=\pm,0} \mathcal{J}_{1\sigma_1\sigma_3}^{\lambda_1} \mathcal{J}_{2\sigma_2\sigma_4}^{\lambda_2} \mathcal{M}_{X\lambda_1\lambda_2}^{\lambda} \end{aligned}$$



# Kinematics



I)  $q_1$  Breit frame ( $Q_1 = \sqrt{-q_1^2}$ ,  $0 < \theta_1 < \pi/2$ ):

$$q_1^\mu = k_1^\mu - k_3^\mu = (0, 0, 0, Q_1)$$

$$k_1^\mu = \frac{Q_1}{2 \cos \theta_1} (1, \sin \theta_1 \cos \phi_1, \sin \theta_1 \sin \phi_1, \cos \theta_1)$$

$$k_3^\mu = \frac{Q_1}{2 \cos \theta_1} (1, \sin \theta_1 \cos \phi_1, \sin \theta_1 \sin \phi_1, -\cos \theta_1)$$

II)  $q_2$  Breit frame ( $Q_2 = \sqrt{-q_2^2}$ ,  $\pi/2 < \theta_2 < \pi$ ):

$$q_2^\mu = k_2^\mu - k_4^\mu = (0, 0, 0, -Q_2)$$

$$k_2^\mu = -\frac{Q_2}{2 \cos \theta_2} (1, \sin \theta_2 \cos \phi_2, \sin \theta_2 \sin \phi_2, \cos \theta_2)$$

$$k_4^\mu = -\frac{Q_2}{2 \cos \theta_2} (1, \sin \theta_2 \cos \phi_2, \sin \theta_2 \sin \phi_2, -\cos \theta_2)$$

III) VBF frame ( $X$  rest frame):

$$q_1^\mu + q_2^\mu = P^\mu = q_1'^\mu + q_2'^\mu = (M, 0, 0, 0)$$

$$q_1^\mu = \frac{M}{2} \left( 1 - \frac{Q_1^2 - Q_2^2}{M^2}, 0, 0, \beta \right);$$

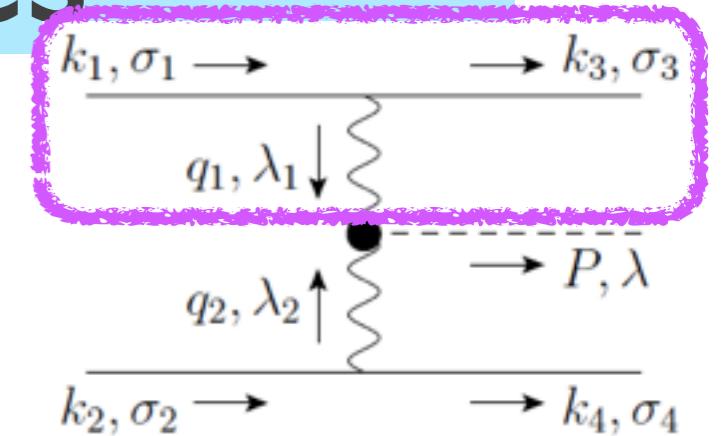
$$q_2^\mu = \frac{M}{2} \left( 1 - \frac{Q_2^2 - Q_1^2}{M^2}, 0, 0, -\beta \right);$$

$$q_1'^\mu = \frac{M}{2} \left( 1 + \frac{Q_1'^2 - Q_2'^2}{M^2}, \beta' \sin \Theta, 0, \beta' \cos \Theta \right)$$

$$q_2'^\mu = \frac{M}{2} \left( 1 + \frac{Q_2'^2 - Q_1'^2}{M^2}, -\beta' \sin \Theta, 0, -\beta' \cos \Theta \right)$$

# Current amplitudes

$$\mathcal{J}_{i\sigma_i\sigma_{i+2}}^{\lambda_i} = (-1)^{\lambda_i+1} \mathcal{J}^\mu(k_i, k_{i+2}; \sigma_i, \sigma_{i+2}) \epsilon_\mu(q_i, \lambda_i)^*$$



- Quark current vectors

$$J_{Vff'}^\mu(k_i, k_{i+2}; \sigma_i, \sigma_{i+2}) = g_{\sigma_i}^{Vff'} \bar{u}_{f'}(k_{i+2}, \sigma_{i+2}) \gamma^\mu u_f(k_i, \sigma_i)$$

- Wavefunctions for the quarks

$$u(k_1, +) = \sqrt{2E_1} \begin{pmatrix} 0 \\ 0 \\ \cos(\theta_1/2) \\ \sin(\theta_1/2) e^{i\phi_1} \end{pmatrix}; \quad u(k_1, -) = \sqrt{2E_1} \begin{pmatrix} -\sin(\theta_1/2) e^{-i\phi_1} \\ \cos(\theta_1/2) \\ 0 \\ 0 \end{pmatrix}$$

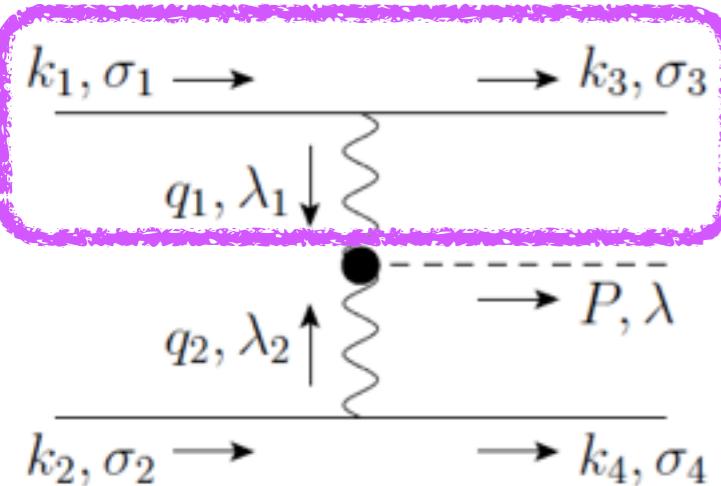
$$u(k_3, +) = \sqrt{2E_1} \begin{pmatrix} 0 \\ 0 \\ \sin(\theta_1/2) \\ \cos(\theta_1/2) e^{i\phi_1} \end{pmatrix}; \quad u(k_3, -) = \sqrt{2E_1} \begin{pmatrix} -\cos(\theta_1/2) e^{-i\phi_1} \\ \sin(\theta_1/2) \\ 0 \\ 0 \end{pmatrix}$$

- Wavefunctions for the  $t$ -channel vector-bosons

$$\epsilon^\mu(q_1, \pm) = \frac{1}{\sqrt{2}}(0, \mp 1, -i, 0)$$

$$\epsilon^\mu(q_1, 0) = (1, 0, 0, 0)$$

# Current helicity amplitudes



---

$\mathcal{J}_1^{\lambda_1}_{\sigma_1\sigma_3}$  (quark)

---

$$\begin{aligned}\mathcal{J}_1^{++}_{++} &= -(\mathcal{J}_1^{--}_{--})^* \frac{1}{2 \cos \theta_1} (1 + \cos \theta_1) e^{-i\phi_1} \\ \mathcal{J}_1^0_{++} &= \mathcal{J}_1^0_{--} \quad -\frac{1}{\sqrt{2} \cos \theta_1} \sin \theta_1 \\ \mathcal{J}_1^{--}_{++} &= -(\mathcal{J}_1^{+-}_{--})^* \frac{1}{2 \cos \theta_1} (1 - \cos \theta_1) e^{i\phi_1} \\ \mathcal{J}_1^{\lambda_1}_{+-} &= \mathcal{J}_1^{\lambda_1}_{-+} \quad 0\end{aligned}$$

---

- The amplitudes with a transversely (longitudinally) polarized VB do (not) have a phase.
- The phases are opposite between those with transverse polarization.

# XVV vertex

- $VV \rightarrow X$  fusion amplitudes:

$$\mathcal{M}_{X\lambda_1\lambda_2} = \epsilon_\mu(q_1, \lambda_1) \epsilon_\nu(q_2, \lambda_2) \Gamma_{XVV}^{\mu\nu}(q_1, q_2; \lambda)^*$$

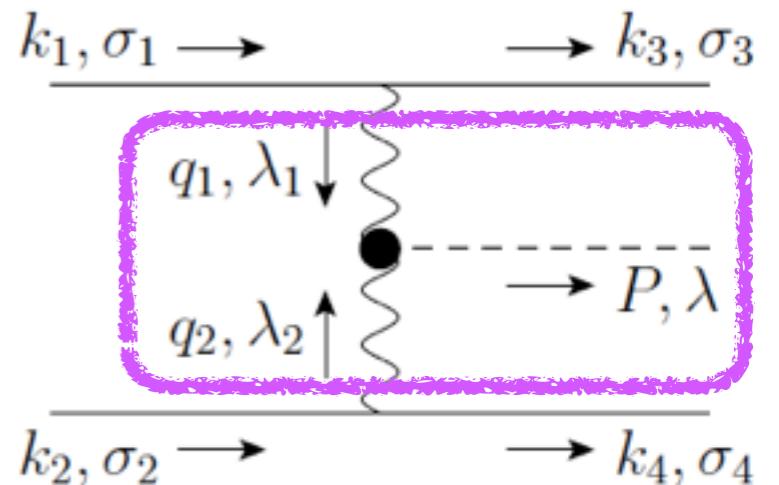
- Effective Lagrangian:

$$\mathcal{L}_{H,A} = -\frac{1}{4}g_{Hgg}HF_{\mu\nu}^a F^{a,\mu\nu} - \frac{1}{4}g_{Agg}AF_{\mu\nu}^a \tilde{F}^{a,\mu\nu}$$

$$\mathcal{L}_G = -\frac{1}{\Lambda}T^{\mu\nu}G_{\mu\nu}$$

- XVV vertex:

$X$	$(\lambda)$	$V$	$\Gamma_{XVV}^{\mu\nu}/g_{XVV}$
$H$	(0)	$W, Z$	$g^{\mu\nu}$
$H$	(0)	$\gamma, Z/\gamma, g$	$q_1 \cdot q_2 g^{\mu\nu} - q_2^\mu q_1^\nu$
$A$	(0)	$\gamma, Z/\gamma, g$	$\epsilon^{\mu\nu\alpha\beta} q_{1\alpha} q_{2\beta}$
$G$	$(\pm 2, \pm 1, 0)$	$W, Z, \gamma, g$	$\epsilon_{\alpha\beta} \hat{\Gamma}_{GVV}^{\alpha\beta\mu\nu}$



\*  $\epsilon^{\alpha\beta}(P, \lambda)$ : the polarization tensor;  $\hat{\Gamma}_{GVV}^{\alpha\beta\mu\nu}(q_1, q_2)$ : the GVV vertex

# $VW \rightarrow H/A$ amplitudes



$\lambda$	$(\lambda_1 \lambda_2)$	CP-even		CP-odd
		$H$ (WBF)	$H$ (loop-induced)	$A$
0	( $\pm\pm$ )	-1	$-\frac{1}{2}(M^2 + Q_1^2 + Q_2^2)$	$\mp\frac{i}{2}\sqrt{(M^2 + Q_1^2 + Q_2^2)^2 - 4Q_1^2Q_2^2}$
0	(00)	$\frac{M^2 + Q_1^2 + Q_2^2}{2Q_1Q_2}$	$Q_1Q_2$	0

The helicity amplitudes for the CP-even/odd Higgs boson productions via off-shell vector-bosons,  $\hat{\mathcal{M}}_{X\lambda_1\lambda_2}$ , in the VBF frame.  $M$  is the Higgs boson mass, and  $Q_1$  and  $Q_2$  are magnitudes of the four-momentum squared of the vector bosons.

For  $Q_1, Q_2 \ll M$ , where the VBF contributions dominant,

- WBF  $H$ : produced by the longitudinally polarized vector-bosons.
- GF  $H/A$ : produced by the transversely polarized vector-bosons.

# $VV \rightarrow G$ amplitudes

$\lambda$	$(\lambda_1 \lambda_2)$	$G$
$\pm 2$	$(\pm \mp)$	$-(M^2 + Q_1^2 + Q_2^2)$
$\pm 1$	$(\pm 0)$	$\frac{1}{\sqrt{2}M} Q_2 (M^2 - Q_1^2 + Q_2^2)$
$\pm 1$	$(0 \mp)$	$\frac{1}{\sqrt{2}M} Q_1 (M^2 + Q_1^2 - Q_2^2)$
0	$(\pm \pm)$	$\frac{1}{\sqrt{6}M^2} [(Q_1^2 - Q_2^2)^2 + M^2(Q_1^2 + Q_2^2)]$
0	$(00)$	$-\frac{4}{\sqrt{6}} Q_1 Q_2$

For  $Q_1, Q_2 \ll M$ , the  $\lambda = \pm 2$  states are dominantly produced through the collisions of the vector-bosons which have the opposite-sign transverse polarization.

# Azimuthal correlations for Higgs bosons

The  $J = 0$  VBF amplitudes are the sum of the three amplitudes:

$$\begin{aligned} \mathcal{M}_{\sigma_1\sigma_3,\sigma_2\sigma_4}^{\lambda=0} &= \frac{1}{(Q_1^2 + m_V^2)(Q_2^2 + m_V^2)} \sum_{\lambda_1=\pm,0} \sum_{\lambda_2=\pm,0} \mathcal{J}_1^{\lambda_1}_{\sigma_1\sigma_3} \mathcal{J}_2^{\lambda_2}_{\sigma_2\sigma_4} \mathcal{M}_X^{\lambda=0}_{\lambda_1\lambda_2} \\ &\sim \mathcal{J}_1^+_{\sigma_1\sigma_3} \mathcal{J}_2^+_{\sigma_2\sigma_4} \mathcal{M}_X^0_{++} e^{-i(\phi_1-\phi_2)} + \mathcal{J}_1^0_{\sigma_1\sigma_3} \mathcal{J}_2^0_{\sigma_2\sigma_4} \mathcal{M}_X^0_{00} \\ &\quad + \mathcal{J}_1^-_{\sigma_1\sigma_3} \mathcal{J}_2^-_{\sigma_2\sigma_4} \mathcal{M}_X^0_{--} e^{i(\phi_1-\phi_2)} \end{aligned}$$

The squared amplitudes are

$$\sum_{\sigma_1,\dots,\sigma_4} |\mathcal{M}_{\sigma_1\sigma_3,\sigma_2\sigma_4}^{\lambda=0}|^2 = \Sigma_0 + \Sigma_1 \cos \Delta\phi + \Sigma_2 \cos 2\Delta\phi \quad (\Delta\phi \equiv \phi_1 - \phi_2)$$

The azimuthal correlation is manifestly expressed by the interference among different helicity states of the intermediate vector-bosons.

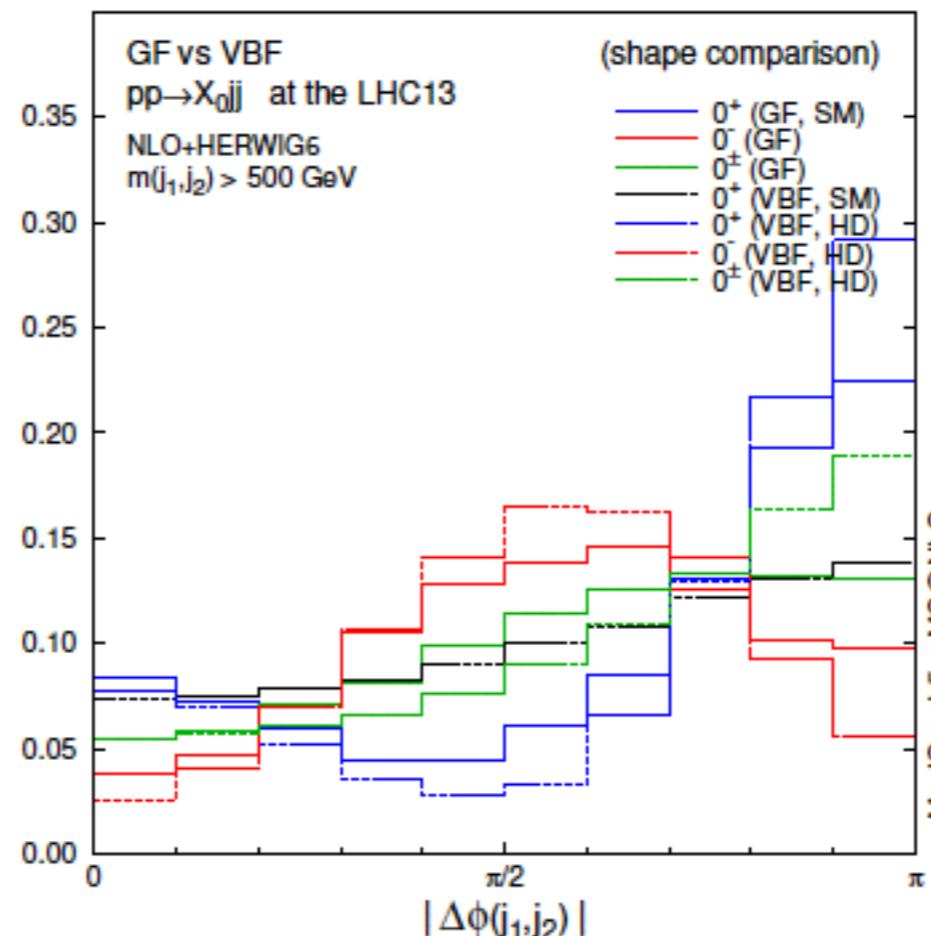
The different tensor structures of the  $XVV$  couplings give rise to the different azimuthal angle dependences:

$$H(\text{WBF}) : \mathcal{M}_{00} \gg \mathcal{M}_{++} = \mathcal{M}_{--} \Rightarrow d\hat{\sigma}/d\Delta\phi \sim \text{constant}$$

$$H(\text{GF}) : \mathcal{M}_{00} \ll \mathcal{M}_{++} = \mathcal{M}_{--} \Rightarrow d\hat{\sigma}/d\Delta\phi \sim \Sigma_0 + |\Sigma_2| \cos 2\Delta\phi$$

$$A : \mathcal{M}_{00} = 0, \mathcal{M}_{++} = -\mathcal{M}_{--} \Rightarrow d\hat{\sigma}/d\Delta\phi \sim \Sigma_0 - |\Sigma_2| \cos 2\Delta\phi$$

# $\Delta\phi$ distributions for Higgs bosons

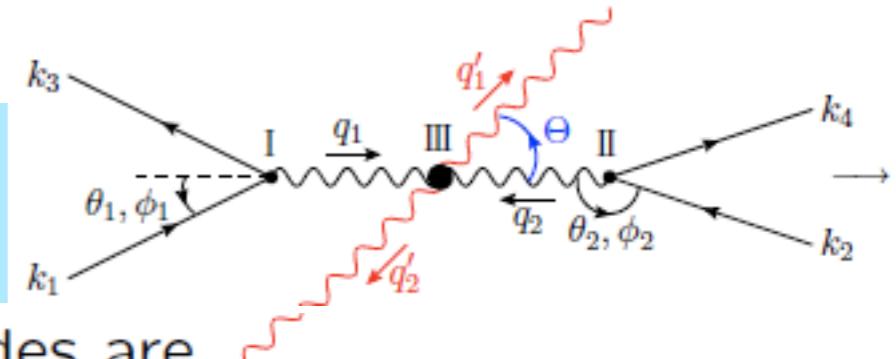


$H(\text{WBF}) \Rightarrow d\sigma/d\Delta\phi \sim \text{constant}$

$H(\text{GF}) \Rightarrow d\sigma/d\Delta\phi \sim \Sigma_0 + |\Sigma_2| \cos 2\Delta\phi$

$A \Rightarrow d\sigma/d\Delta\phi \sim \Sigma_0 - |\Sigma_2| \cos 2\Delta\phi$

# Azimuthal correlations for gravitons



The VBF  $G$  production plus its 2-body decay amplitudes are

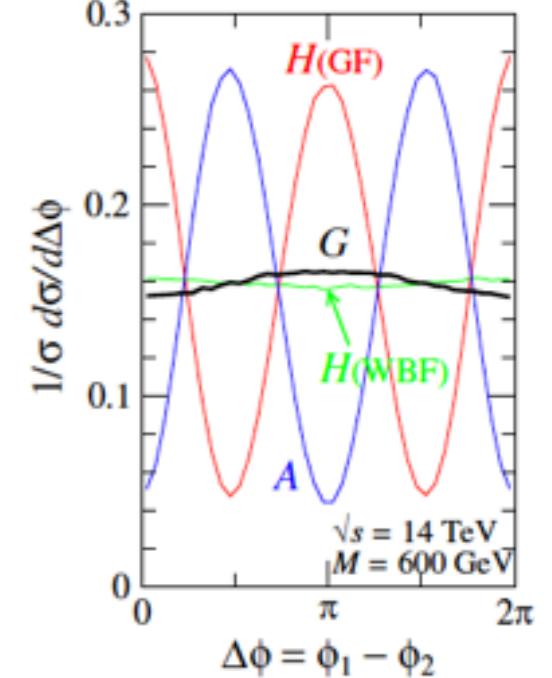
$$\begin{aligned} \mathcal{M}_{\sigma_1, \dots, 4; \sigma_5, 6} &= \frac{1}{Q_1^2 Q_2^2} \sum_{\lambda_1} \sum_{\lambda_2} \mathcal{J}_1^{\lambda_1}{}_{\sigma_1 \sigma_3} \mathcal{J}_2^{\lambda_2}{}_{\sigma_2 \sigma_4} \mathcal{M}_{G \lambda_1 \lambda_2}^{\lambda = \lambda_1 - \lambda_2} \frac{d_{\lambda, \lambda'}^2(\Theta)}{P^2 - M^2 + iM\Gamma} \mathcal{M}'_{G \sigma_5 \sigma_6}^{\lambda' = \sigma_5 - \sigma_6} \\ &\sim \mathcal{J}_1^+{}_{\sigma_1 \sigma_3} \mathcal{J}_2^-{}_{\sigma_2 \sigma_4} \mathcal{M}_{G+-}^{+2} e^{-i(\phi_1 + \phi_2)} d_{+2, \lambda'}^2(\Theta) \\ &\quad + \mathcal{J}_1^-{}_{\sigma_1 \sigma_3} \mathcal{J}_2^+{}_{\sigma_2 \sigma_4} \mathcal{M}_{G-+}^{-2} e^{i(\phi_1 + \phi_2)} d_{-2, \lambda'}^2(\Theta) \end{aligned}$$

The squared amplitudes are

$$\sum_{\sigma_1, \dots, 4} |\mathcal{M}_{\sigma_1, \dots, 4; \sigma_5, 6}|^2 = \Sigma_0 + \Sigma_1 \cos 2\Phi \quad (\Phi \equiv \phi_1 + \phi_2)$$

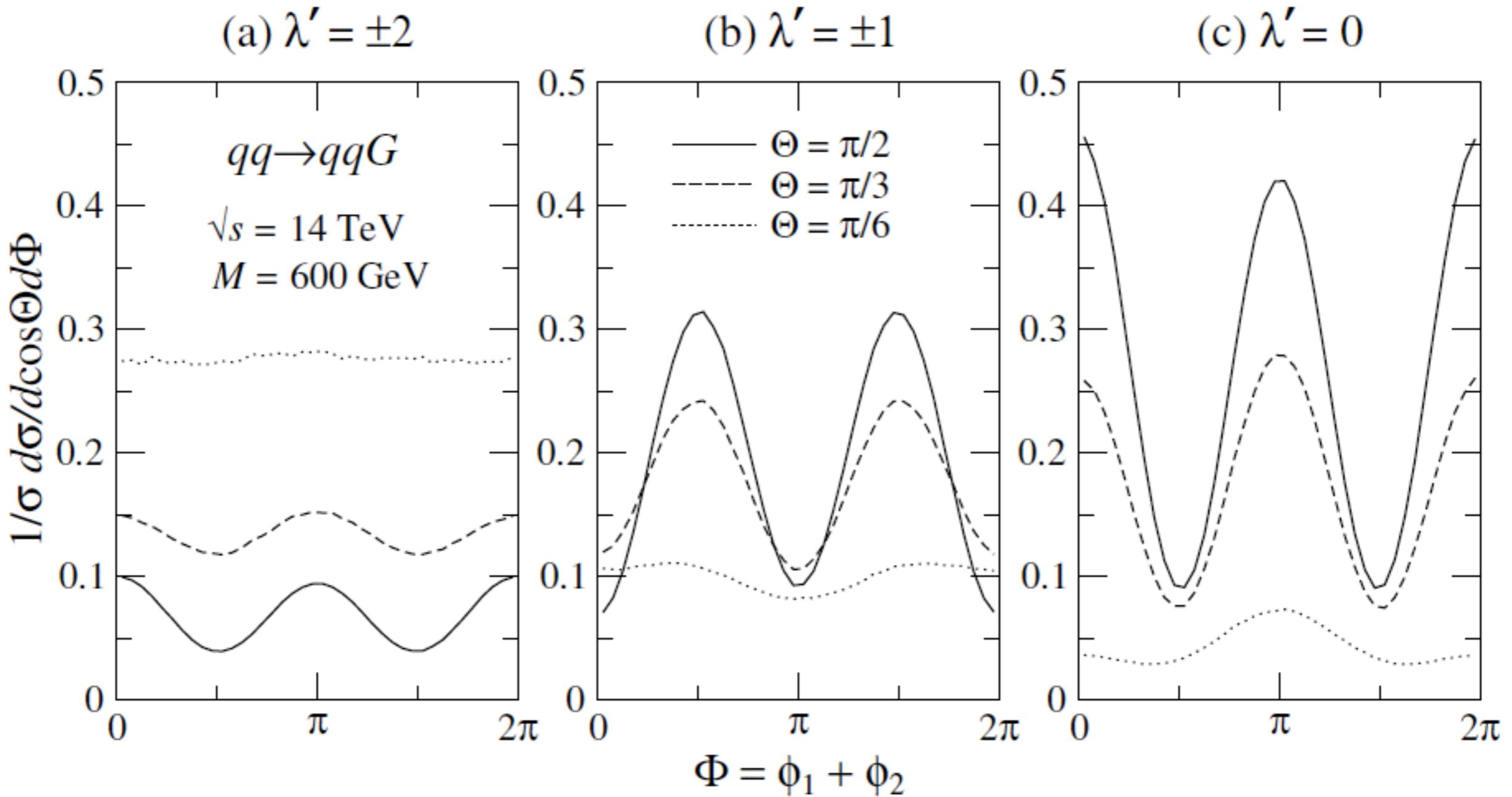
where

$$\begin{aligned} \Sigma_0 &\propto (d_{+2, \lambda'}^2(\Theta))^2 + (d_{-2, \lambda'}^2(\Theta))^2 = \begin{cases} \frac{1}{8}(1 + 6 \cos^2 \Theta + \cos^4 \Theta) & \text{for } \lambda' = \pm 2 \\ \frac{1}{2}(1 - \cos^4 \Theta) & \text{for } \lambda' = \pm 1 \\ \frac{3}{4}\sin^4 \Theta & \text{for } \lambda' = 0 \end{cases} \\ \Sigma_1 &\propto 2 d_{+2, \lambda'}^2(\Theta) d_{-2, \lambda'}^2(\Theta) = \begin{cases} +\frac{1}{8}\sin^4 \Theta & \text{for } \lambda' = \pm 2 \\ -\frac{1}{2}\sin^4 \Theta & \text{for } \lambda' = \pm 1 \\ +\frac{3}{4}\sin^4 \Theta & \text{for } \lambda' = 0 \end{cases} \end{aligned}$$



⇒ The azimuthal  $\Phi$  correlations depend on  $\Theta$  and  $\lambda'$ .

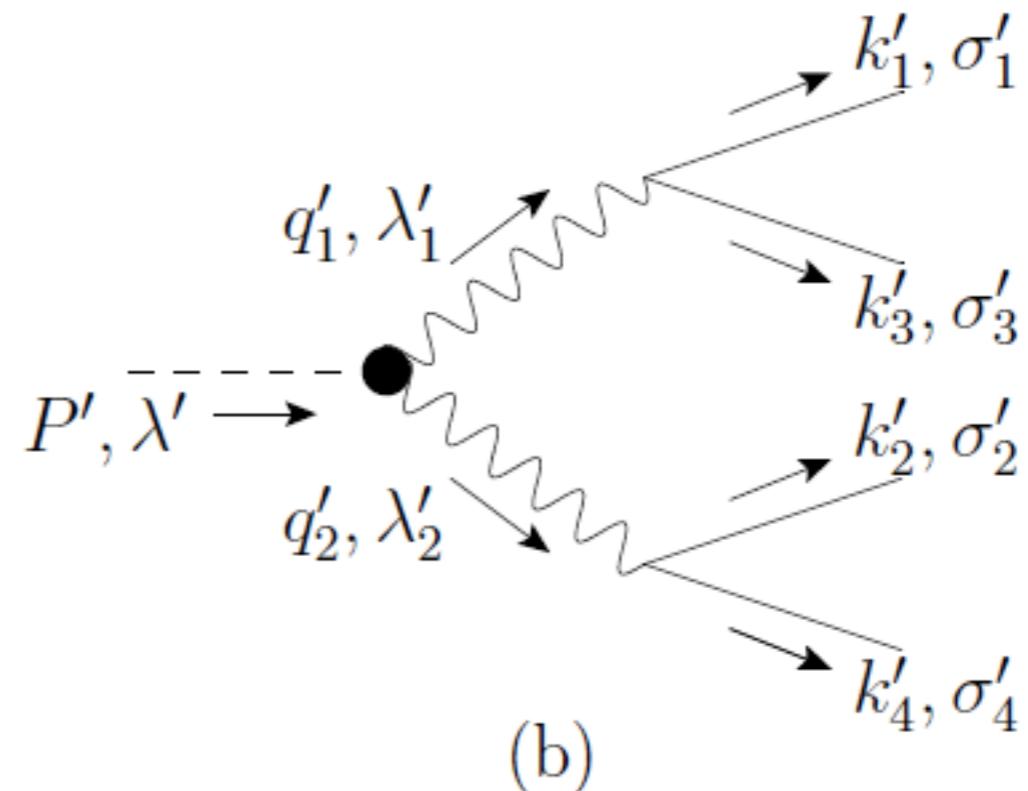
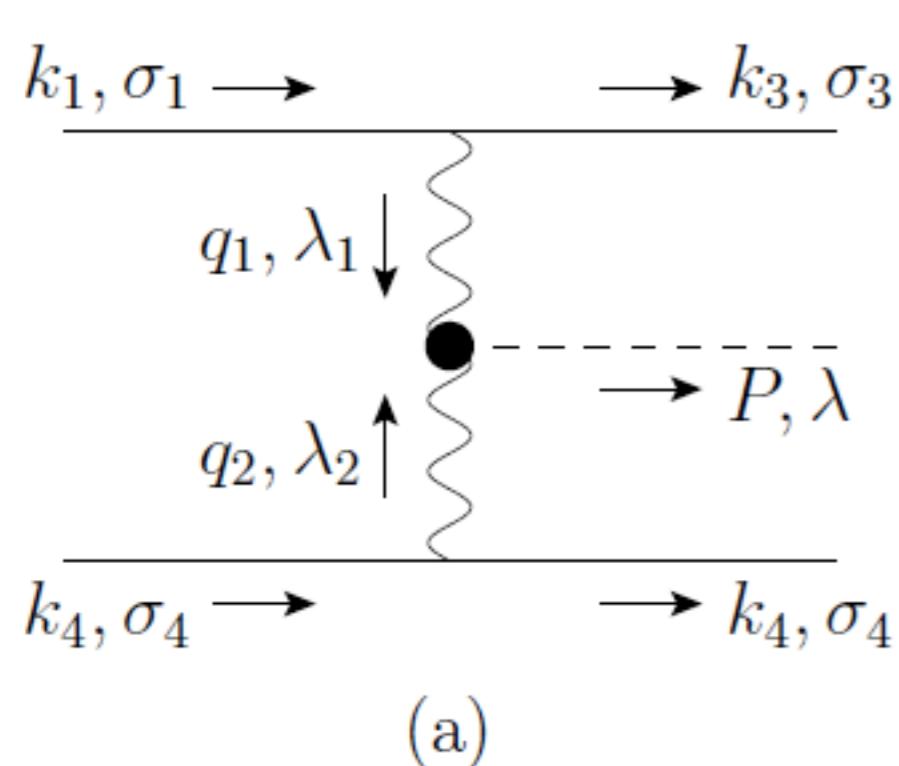
# $\Phi$ distributions for gravitons



$$d\sigma/d \cos \Theta d\Phi \sim \Sigma_0 + \Sigma_1 \cos 2\Phi; \quad \Sigma_1 \propto \begin{cases} +\frac{1}{8} \sin^4 \Theta & \text{for } \lambda' = \pm 2 \\ -\frac{1}{2} \sin^4 \Theta & \text{for } \lambda' = \pm 1 \\ +\frac{3}{4} \sin^4 \Theta & \text{for } \lambda' = 0 \end{cases}$$

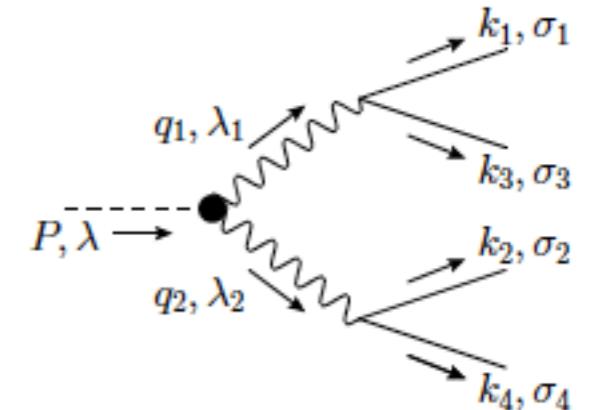
The  $\Theta$  and  $\lambda'$  dependent azimuthal  $\Phi$  correlations !

# $X$ decay to a vector-boson pair



Angular correlations in heavy-particle decays are also promising tools to determine their properties.

The process of  $X$  decays into 4 jets/leptons via a vector-boson pair is related by crossing symmetry to the VBF process.



## The helicity amplitude formalism

The helicity amplitudes for  $X \rightarrow VV \rightarrow 4f$

$$\mathcal{M}_{\sigma_1\sigma_3,\sigma_2\sigma_4}^{\lambda} = \Gamma_{XVV}^{\mu_1\mu_2}(q_1, q_2; \lambda) \frac{-g_{\mu'_1\mu_1} + \frac{q_{1\mu'} q_{1\mu_1}}{m_V^2}}{q_1^2 - m_V^2} J^{\mu'_1}(k_1, k_3; \sigma_1, \sigma_3) \frac{-g_{\mu'_2\mu_2} + \frac{q_{2\mu'} q_{2\mu_2}}{m_V^2}}{q_2^2 - m_V^2} J^{\mu'_2}(k_2, k_4; \sigma_2, \sigma_4)$$

can be expressed by using

completeness relation       $-g_{\mu'\mu} + \frac{q_{i\mu'} q_{i\mu}}{q_i^2} = \sum_{\lambda_i=\pm,0} \epsilon_{\mu'}(q_i, \lambda_i)^* \epsilon_{\mu}(q_i, \lambda_i)$

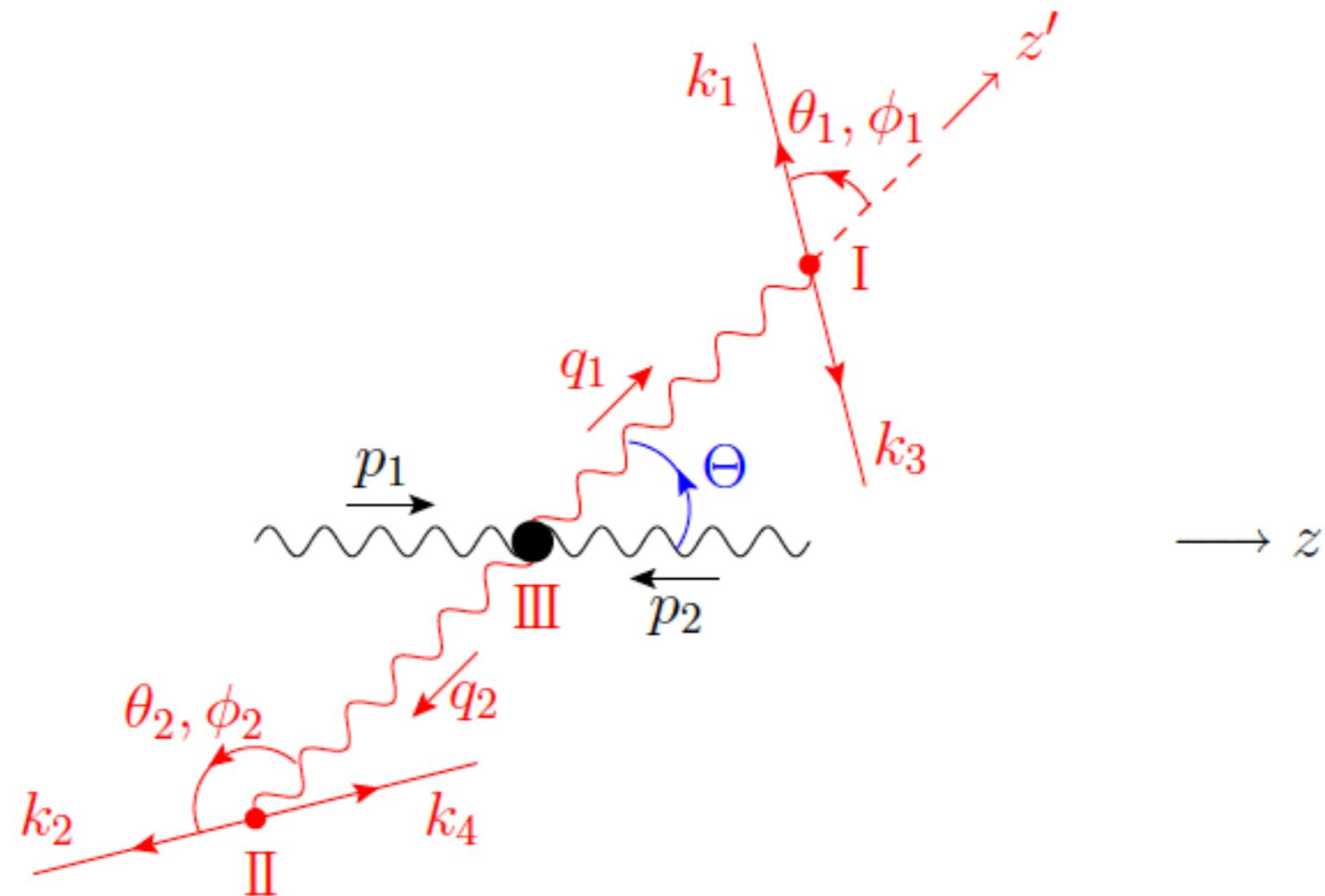
current conservation       $q_{i\mu} J^{\mu}(k_i, k_{i+2}; \sigma_i, \sigma_{i+2}) = 0$

as the product of the three helicity amplitudes summed over the polarization of the intermediate vector-bosons:

$$\begin{aligned} \mathcal{M}_{\sigma_1\sigma_3,\sigma_2\sigma_4}^{\lambda} &= \Gamma_{XVV}^{\mu_1\mu_2}(q_1, q_2; \lambda) \\ &\times \frac{1}{q_1^2 - m_V^2} J^{\mu'_1}(k_1, k_3; \sigma_1, \sigma_3) \sum_{\lambda_1=\pm,0} \epsilon_{\mu'_1}(q_1, \lambda_1) \epsilon_{\mu_1}(q_1, \lambda_1)^* \\ &\times \frac{1}{q_2^2 - m_V^2} J^{\mu'_2}(k_2, k_4; \sigma_2, \sigma_4) \sum_{\lambda_2=\pm,0} \epsilon_{\mu'_2}(q_2, \lambda_2) \epsilon_{\mu_2}(q_2, \lambda_2)^* \\ &= \frac{1}{(q_1^2 - m_V^2)(q_2^2 - m_V^2)} \sum_{\lambda_1=\pm,0} \sum_{\lambda_2=\pm,0} \mathcal{M}_{X\lambda_1\lambda_2}^{\lambda} \mathcal{J}_1^{\lambda_1}_{\sigma_1\sigma_3} \mathcal{J}_2^{\lambda_2}_{\sigma_2\sigma_4} \end{aligned}$$

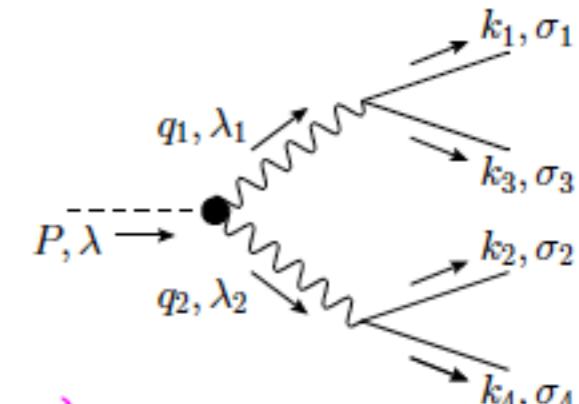
Note: The total amplitudes are generally the coherent sum of the 9 amplitudes which have the different helicity combinations of the decaying vector-bosons.

## Kinematics for $gg/q\bar{q} \rightarrow X \rightarrow VV \rightarrow (f\bar{f})(f\bar{f})$



Note: The azimuthal angles ( $\phi_1$  and  $\phi_2$ ) are measured individually from the  $X$  production-decay ( $gg/q\bar{q} \rightarrow X \rightarrow VV$ ) plane.

## Current amplitudes

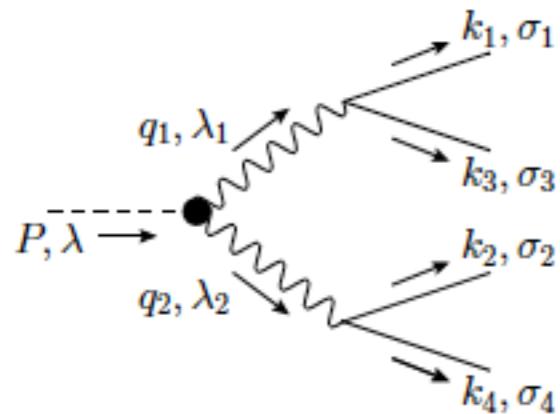


$$\begin{aligned}\mathcal{J}_{i\sigma_i\sigma_{i+2}}^{\lambda_i} &= \epsilon_\mu(q_i, \lambda_i) J_{Vff'}^\mu(k_i, k_{i+2}; \sigma_i, \sigma_{i+2}) \\ &= \epsilon_\mu(q_i, \lambda_i) g_{\sigma_i}^{Vff'} \bar{u}_{f'}(k_{i+2}, \sigma_{i+2}) \gamma^\mu u_f(k_i, \sigma_i)\end{aligned}$$

$$\mathcal{J}_{1\sigma_1\sigma_3}^{\lambda_1}$$

- $\mathcal{J}_{1+-}^+ = -(\mathcal{J}_{1-+}^-)^* \quad \frac{1}{2}(1 + \cos \theta_1) e^{i\phi_1}$
- $\mathcal{J}_{1+-}^0 = \mathcal{J}_{1-+}^0 \quad \frac{1}{\sqrt{2}} \sin \theta_1$
- $\mathcal{J}_{1+-}^- = -(\mathcal{J}_{1-+}^+)^* \quad \frac{1}{2}(1 - \cos \theta_1) e^{-i\phi_1}$
- $\mathcal{J}_{1++}^{\lambda_1} = \mathcal{J}_{1--}^{\lambda_1} \quad 0$

Note: The amplitudes for **transversely** polarized vector-bosons have a phase,  $e^{+i\phi_1}$  or  $e^{-i\phi_1}$ , while those for **longitudinal** ones do not.



$X \rightarrow VV$  decay amplitudes

in the  $q_{1,2}^2 \rightarrow m_V^2$  limit ( $\beta = \sqrt{1 - 4m_V^2/M^2}$ )

$\lambda$	$(\lambda_1\lambda_2)$	$H$	$A$	$G$
$\pm 2$	$(\pm\mp)$	.	.	$-M^2$
$\pm 1$	$(\pm 0), (0\mp)$	.	.	$\sqrt{\frac{1}{2}(1-\beta^2)}M^2$
0	$(\pm\pm)$	$-1$	$\mp\frac{i}{2}\beta M^2$	$-\frac{1}{\sqrt{6}}(1-\beta^2)M^2$
0	$(00)$	$(1+\beta^2)/(1-\beta^2)$	0	$-\frac{1}{\sqrt{6}}(2-\beta^2)M^2$

- light  $H (\beta \rightarrow 0; M \sim 2m_V)$ : decay into both longitudinally- and transversely-polarized VBs.
- heavy  $H (\beta \rightarrow 1; M \gg m_V)$ : decay into the longitudinally-polarized VBs.
- $A$ : decay only into transversely-polarized VBs.
- $G (\beta \rightarrow 1)$ : decay into both longitudinally- and  $(\lambda_1\lambda_2) = (\pm\mp)$  transversely-polarized VBs.

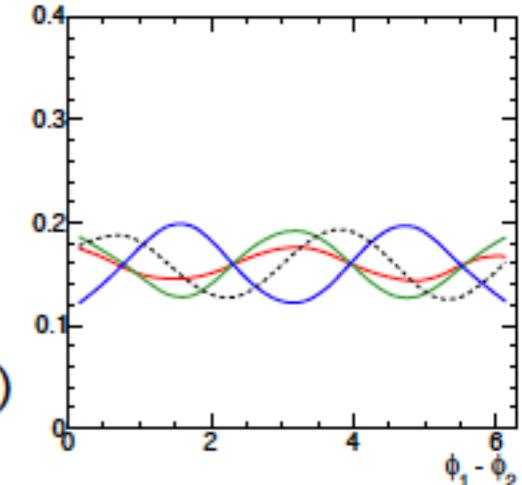
## Azimuthal correlations for Higgs bosons

The  $J = 0$  total amplitudes are the sum of the three amplitudes:

$$\begin{aligned}\mathcal{M}_{\sigma_1\sigma_3,\sigma_2\sigma_4}^{\lambda=0} &= \frac{1}{(q_1^2 - m_V^2)(q_2^2 - m_V^2)} \sum_{\lambda_1=\pm,0} \sum_{\lambda_2=\pm,0} \mathcal{M}_{X\lambda_1\lambda_2}^{\lambda=0} \mathcal{J}_{1\sigma_1\sigma_3}^{\lambda_1} \mathcal{J}_{2\sigma_2\sigma_4}^{\lambda_2} \\ &\sim \mathcal{M}_{X++}^0 \mathcal{J}_{1\sigma_1\sigma_3}^+ \mathcal{J}_{2\sigma_2\sigma_4}^+ e^{-i(\phi_1-\phi_2)} + \mathcal{M}_{X00}^0 \mathcal{J}_{1\sigma_1\sigma_3}^0 \mathcal{J}_{2\sigma_2\sigma_4}^0 \\ &\quad + \mathcal{M}_{X--}^0 \mathcal{J}_{1\sigma_1\sigma_3}^- \mathcal{J}_{2\sigma_2\sigma_4}^- e^{i(\phi_1-\phi_2)}\end{aligned}$$

Therefore, the squared amplitudes are generally given by

$$\sum_{\sigma_1,\dots,\sigma_4} |\mathcal{M}_{\sigma_1\sigma_3,\sigma_2\sigma_4}^{\lambda=0}|^2 = \Sigma_0 + \Sigma_1 \cos \Delta\phi + \Sigma_2 \cos 2\Delta\phi \quad (\Delta\phi \equiv \phi_1 - \phi_2)$$



The azimuthal correlation is manifestly expressed by the interference among different helicity states of the intermediate vector-bosons.

The different tensor structures of the  $H/A$  coupling to a  $Z$ -pair give rise to the different azimuthal angle dependences:

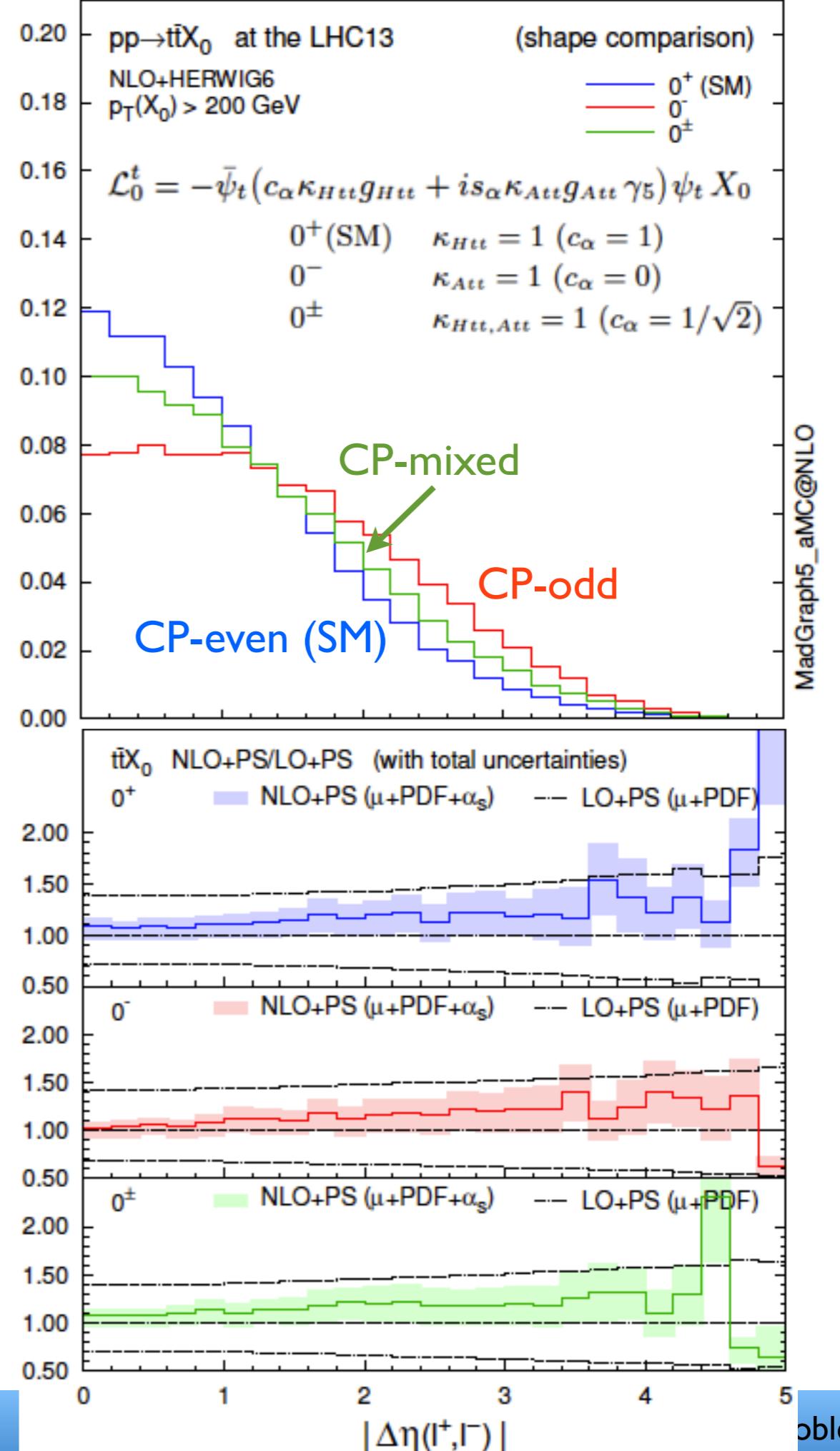
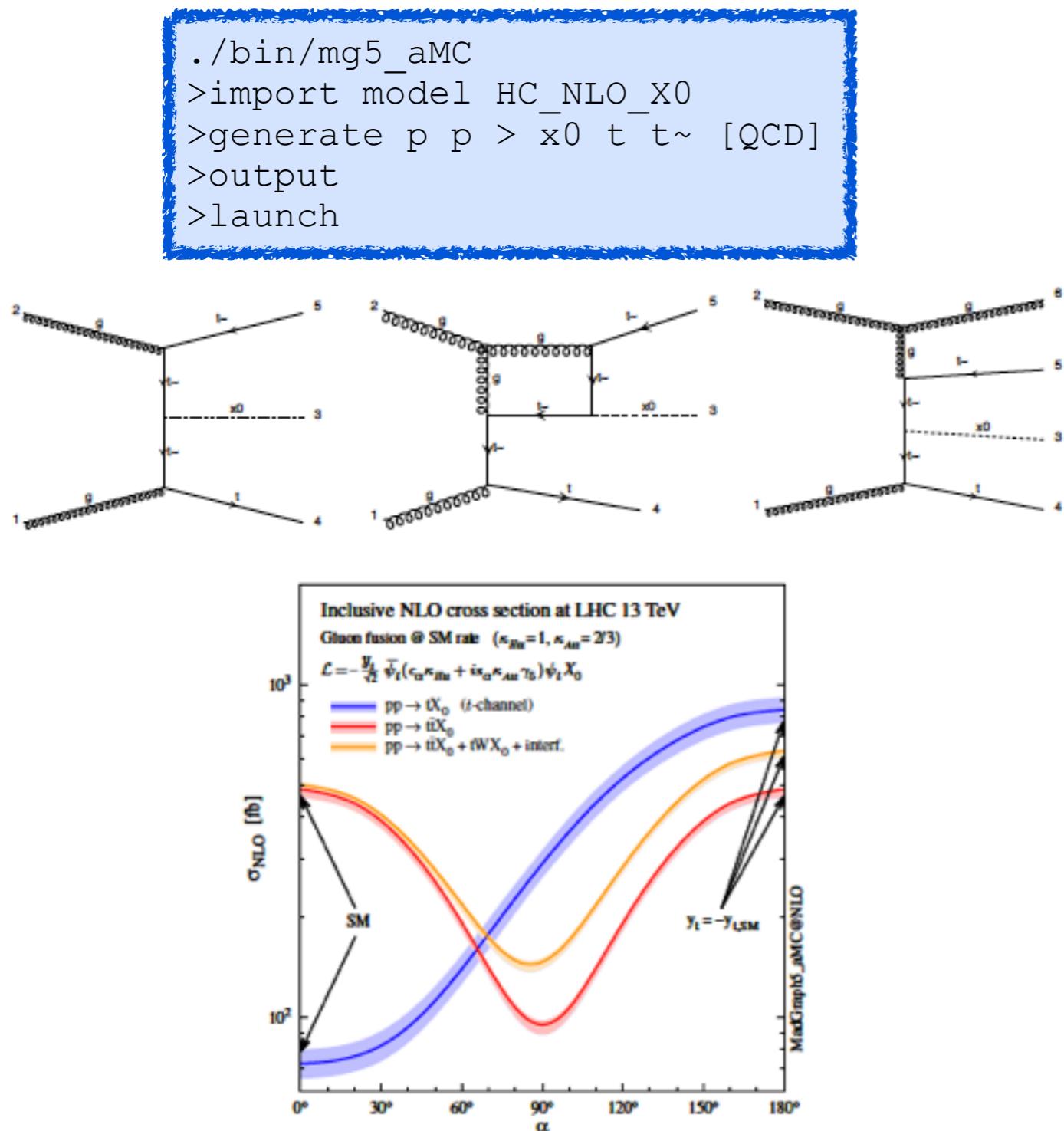
$$H_{(\text{heavy})} : \mathcal{M}_{00} \gg \mathcal{M}_{++} = \mathcal{M}_{--} \Rightarrow d\Gamma/d\Delta\phi \sim \text{constant}$$

$$H_{(\text{light})} : \mathcal{M}_{00} \sim \mathcal{M}_{++} = \mathcal{M}_{--} \quad (\Sigma_1 \ll 1) \Rightarrow d\Gamma/d\Delta\phi \sim \Sigma_0 + |\Sigma_2| \cos 2\Delta\phi$$

$$A : \quad \mathcal{M}_{00} = 0, \quad \mathcal{M}_{++} = -\mathcal{M}_{--} \Rightarrow d\Gamma/d\Delta\phi \sim \Sigma_0 - |\Sigma_2| \cos 2\Delta\phi$$

# Higgs CP in ttH/tH

Demartin, Maltoni, KM, Page, Zaro [1407.5089, EPJC]



# Summary

- I discussed
  - how we can determine the Higgs spin/parity at the LHC.
  - azimuthal correlations in the various processes are sensitive to the Higgs CP property.
  - the correlations can be explained as the quantum interference among different helicity states of the intermediate particles.