

Loopedia – A Database for Loop Integrals

Thomas Hahn

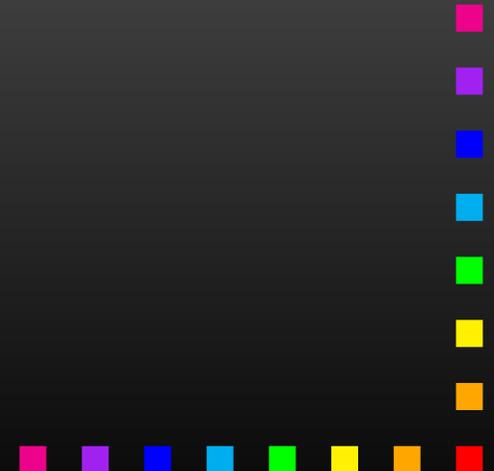
in collaboration with

C. Bogner, S. Borowka, G. Heinrich, S. Jones, M. Kerner,
A. von Manteuffel, M. Michel, E. Panzer, V. Papara



Introduction

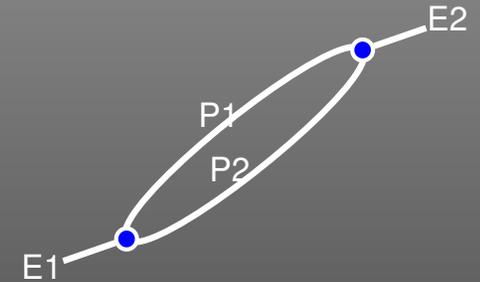
- Researchers in HEP enjoy **privileged bibliographic access** thanks to arXiv & SPIRES.
- But: **Indexing only by 'traditional' metrics:** author, title, year of publication, etc.
- Interesting for loop calculators: find all papers which **refer to graph X** , where X is specified in some graph-theoretical way.
- Ideally: store also available results.
- This new database is now available:
loopedia.org



Graph-Theory Inputs

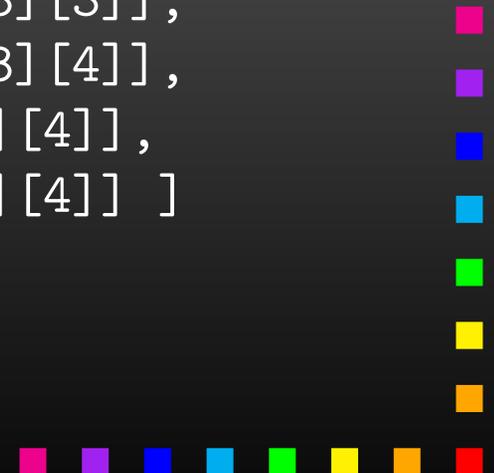
The **Topology** can be entered as

- an **Edge List**, e.g. $(e, 0) (0, 1) (0, 1) (e, 1)$
- an **Nickel Index**, e.g. $e11|e|$



Edge List has some latitude, can also put e.g.

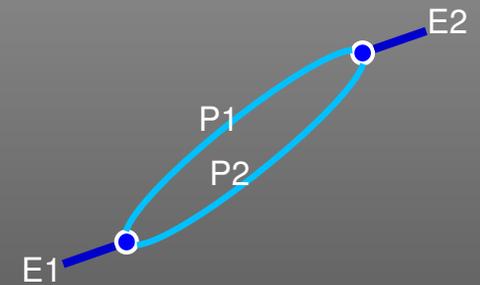
- $x a a b a b b y$
- `Topology[2] [`
 `Propagator[Incoming][Vertex[1][1], Vertex[3][3]],`
 `Propagator[Outgoing][Vertex[1][2], Vertex[3][4]],`
 `Propagator[Loop[1]][Vertex[3][3], Vertex[3][4]],`
 `Propagator[Loop[1]][Vertex[3][3], Vertex[3][4]]]`



Graph-Theory Inputs

The **Configuration** is appended to the topology as

- an **Extended Edge List**, e.g.
 $(e, 0|n) (0, 1|1) (0, 1|1) (e, 1|n)$
- a **Colored Nickel Index**, e.g. $e11|e|:n11|n|$
 - $z =$ any mass scale (including zero),
 - $n =$ non-zero mass scale,
 - $0 =$ zero,
 - $1\dots9 a\dots y =$ definite non-zero mass scale.

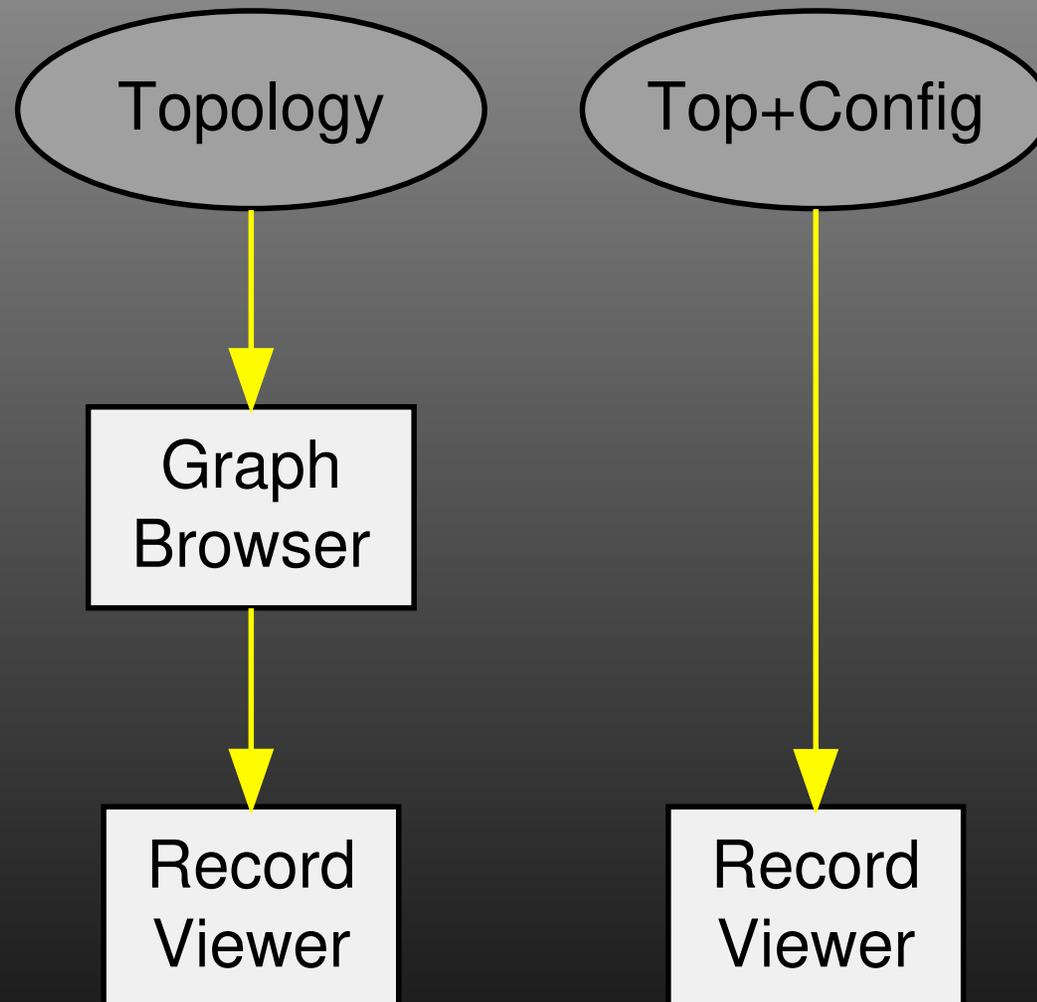


All graph-theory objects are handled by the **GraphState library** arXiv:1409.8227 (with some minor tweaks).

Graphs are drawn with the **'neato' component of graphviz.**



Flow Chart



Start Page

Multiple Upload (expert)

Loopedia

Ex.: Edge list [(1,2),(2,3),(2,3),(3,4)] or 1 2 2 3 2 3 3 4 — Nickel index e11|e|

Enter your graph by its edge list (adjacency list) or Nickel index

or browse:

Loops = any Legs = any Scales = any

Fulltext must contain: must not contain:

If you wish to add a new integral to the database, start by searching for its graph first.

The Loopedia Team is C. Bogner, S. Borowka, T. Hahn, G. Heinrich, S. Jones, M. Kerner, A. von Manteuffel, M. Michel, E. Panzer, V. Papara.

Software version of 06 Nov 2017 23:05 UTC. In case of technical difficulties with this site please contact [Thomas Hahn](#) or [Viktor Papara](#).

This Web site uses the [GraphState library \[arXiv:1409.8227\]](#) for all graph-theoretical operations
and the neato component of [Graphviz](#) for drawing graphs.

Loopedia is free and open to everyone. To acknowledge and support the work put into keeping Loopedia up to date, please cite [arXiv:1709.01266](#).



Graph Browser

Results for all loops, all legs, all scales — Row 11»

Prev

Next

Show 5 rows per page

Home



Configuration Editor

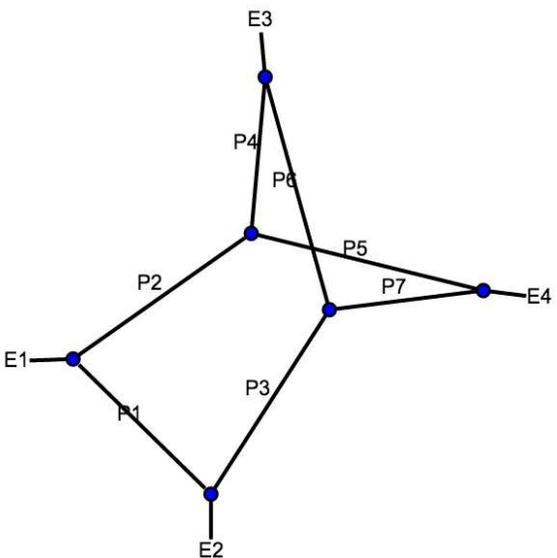
Graph **e12|e3|45|45|e|e|**

Edit **• : •** Edit **•** Browse **• : *** Home

Edge list: (e,0) (0,1) (0,2) (e,1) (1,3) (2,4) (2,5) (3,4) (3,5) (e,4) (e,5)

Nickel index: **e12|e3|45|45|e|e|**

Database path: 2/4/7/**e12|e3|45|45|e|e|**

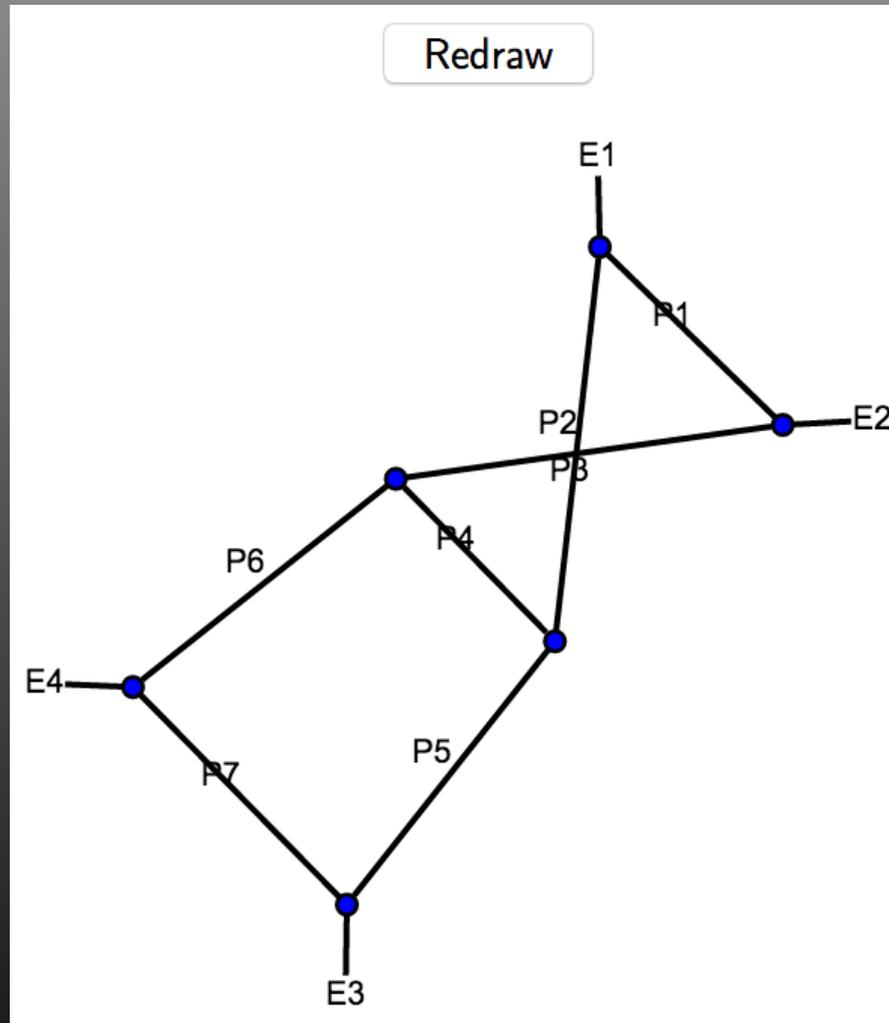


Propagator P1 any m
Propagator P2 any m
Propagator P3 any m
Propagator P4 any m
Propagator P5 any m
Propagator P6 any m
Propagator P7 any m
External Leg E1 any q^2
External Leg E2 any q^2
External Leg E3 any q^2
External Leg E4 any q^2

Choose Configuration



Redraw an 'Ugly' Graph



Record Viewer

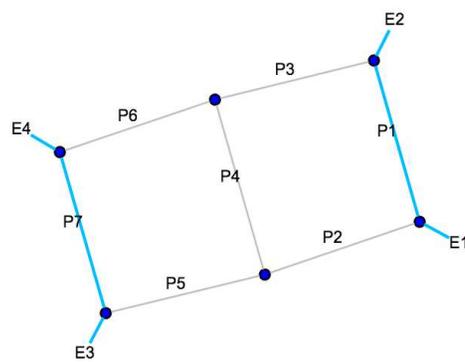
Graph **e12|e3|34|5|e5|e|** — Masses **110|10|00|0|11|1|**

Edit Edit Browse * Home

Edge list: (e,0|1) (0,1|1) (0,2|0) (e,1|1) (1,3|0) (2,3|0) (2,4|0) (3,5|0) (e,4|1) (4,5|1) (e,5|1)

Nickel index: **e12|e3|34|5|e5|e|**:**110|10|00|0|11|1|**

Database path: 2/4/7/**e12|e3|34|5|e5|e|**/1/**110|10|00|0|11|1|**



Propagator P1

Propagator P2

Propagator P3

Propagator P4

Propagator P5

Propagator P6

Propagator P7

External Leg E1

External Leg E2

External Leg E3

External Leg E4

Reference: [arXiv:1612.05609](https://arxiv.org/abs/1612.05609)

Description: The authors compute the planar 2-loop box master integrals involved in $QQ \rightarrow QQ$, where QQ are massive external quarks using the method of differential equations.

Submitter: sophia.borowka@cern.ch

Record 1482239373.Z1Fv

added 20 Dec 2016 13:09 UTC

last modified 23 May 2017 14:07 UTC



New Record Form

Integrand type: if *other*, please specify:

Propagator powers (the n in $(p^2 - m^2)^{-n}$ for which result is valid, separate by comma if necessary, leave empty if n/a):

P1 P2 P3 P4

Order(s) in ϵ (separate by comma, empty if n/a):

Reducible: **Number of master integrals:**

Reference (arXiv:*yymm.nnnnn* or hep-*xx/yymmnnn* preferred, empty if n/a):

Relevant equations in reference:

Authors:

Description (package URL, dimension computed in, type of functions, Euclidean/physical kinematics, weight, free text, etc.):

Submitter (e-mail):

Additional material (PDFs not on arXiv, Mathematica/Maple/FORM/Python/Fortran programs, etc.):

- No file selected.
- No file selected.
- No file selected.

Multiple Upload

Add record for multiple graphs

CNicksels and non-standard propagator powers

(One graph per line, format e.g. e12|e3|34|5|e5|e|:110|10|00|0|11|1| P2=1,2 P5=2, propagator powers not given default to 1, use `eps=...` and `nmasters=...` for per-line overrides):

```
e111|e|:n011|n| P2=2 P3=2
e111|e|:n011|n| P3=2 eps=-1,0,1,2
e12|23|3|e|:n00|11|1|n| eps=0,1
e112|e2|e|:0011|01|n| P2=3
```

Integrand type: if *other*, please specify:

Order(s) in ϵ (separate by comma, empty if n/a):

Reducible: **Number of master integrals:**

Reference (arXiv:yyymm.nnnnnn or hep-xx/yyymmnnn preferred, empty if n/a):

Relevant equations in reference:

Authors:

Description (package URL, dimension computed in, type of functions, Euclidean/physical kinematics, weight, free text, etc.):

The authors give the two-loop master integrals for Higgs production via a massive quark and a squark loop.

Submitter (e-mail):

Additional material (PDFs not on arXiv, Mathematica/Maple/FORM/Python/Fortran programs, etc.):

No file selected.

No file selected.

No file selected.



Multiple Submit

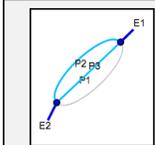
Submission overview

Reference: [hep-ph/0611236](https://arxiv.org/abs/hep-ph/0611236)

Authors: Charalampos Anastasiou, Stefan Beerli, Stefan Bucherer, Alejandro Daleo, Zoltan Kunszt

Description: The authors give the two-loop master integrals for Higgs production via a massive quark and a squark loop.

Submitter: michel.martin@uclouvain.be



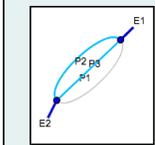
e111|e|:n011|n|

Non-standard propagator powers: P2=2 P3=2

Orders in ϵ : 0,1,2

Dry run — not in database yet

Record 1504335475.fuUH



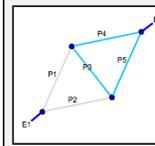
e111|e|:n011|n|

Non-standard propagator powers: P3=2

Orders in ϵ : -1,0,1,2

Dry run — not in database yet

Record 1504335476.3AVB

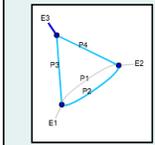


e12|23|3|e|:n00|11|1|n|

Orders in ϵ : 0,1

Dry run — not in database yet

Record 1504335476.CVSS



e112|e2|e|:0011|01|n|

Non-standard propagator powers: P2=3

Orders in ϵ : 0,1,2

Dry run — not in database yet

Record 1504335476.ZcWD

If this dry run was ok, press to actually add the records to the database.



Database Setup

Database realized as

- an `index.cgi` bash script in a CGI environment
- that uses the Unix filesystem as database (like iTunes),
- indexed by the `mlocate` utility.

Internal tools used:

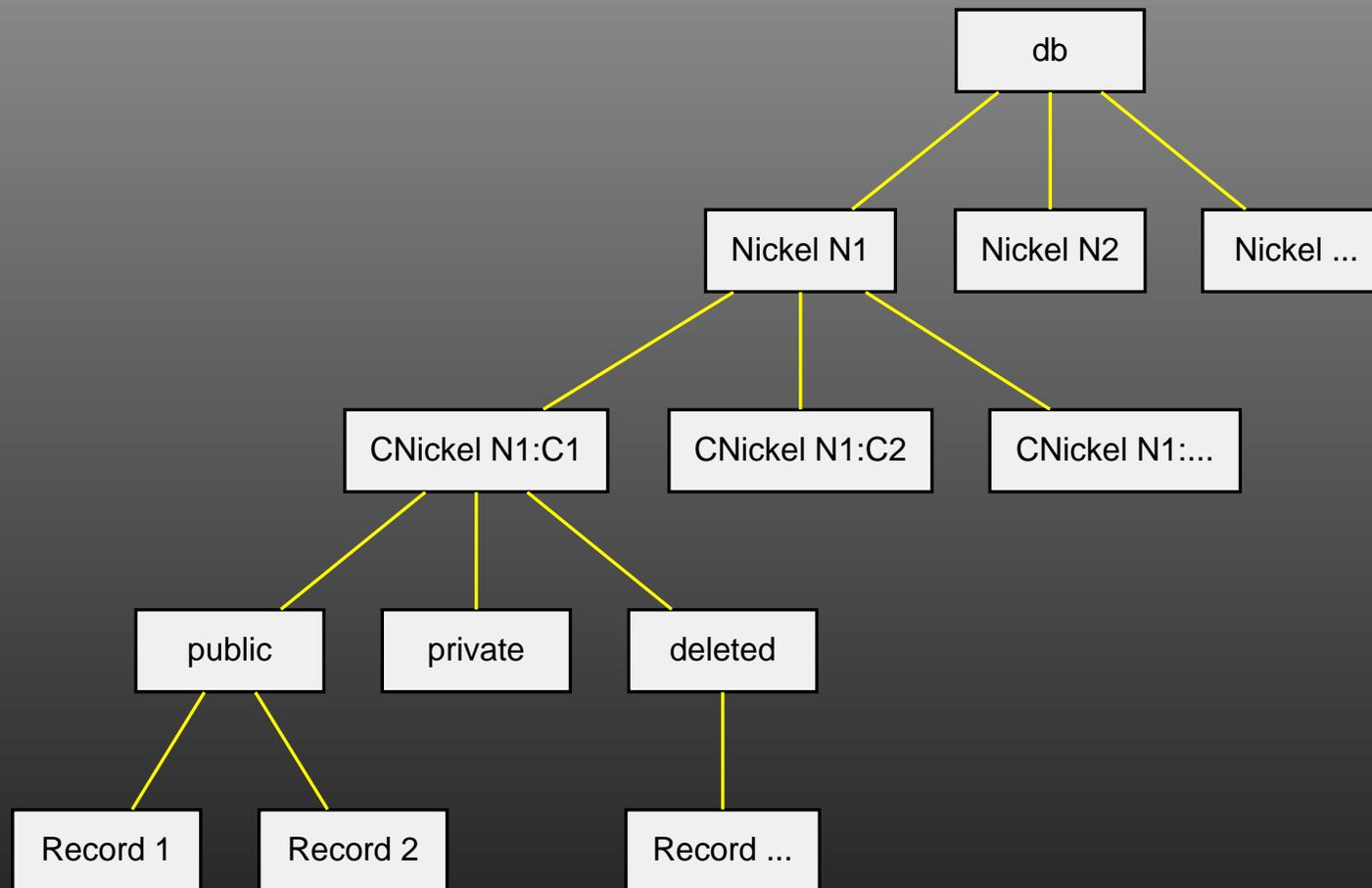
- `unescape.c`, `formdecode.c` - parsing CGI input
- `token.c`, `djb2hash.c`, `recfind.c` - token generation, hashing, finding
- `loopedia.py` - interfacing with GraphState

External tools used:

- GraphState [mod] (<https://pypi.python.org/pypi/GraphState>)
- mlocate [mod] (<https://github.com/msekletar/mlocate>)
- graphviz (<http://graphviz.org>)



Database Structure



Full DB path: $db/L/\ell/p/\mathbf{Nickel}/s/\mathbf{Config}/\mathbf{Visibility}/\mathbf{Record}$



Summary

Loopedia is a new database for loop integrals

- indexed by **graph-theoretical properties**,
- can hold **bibliographic but also other information**, e.g. results in some machine-readable format,
- slim CGI design, **Unix filesystem doubles as database**,
- filling database **task for researchers**,
- still pretty much **work in progress**.

Please try it out and give us feedback!



Part II: MathLink



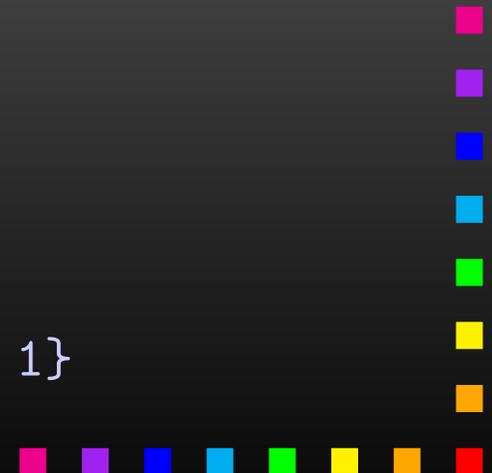
MathLink programming

MathLink is Mathematica's API to interface with C and C++. J/Link offers similar functionality for Java. (There's more.)

A MathLink program consists of three parts:

a) Declaration Section

```
:Begin:  
:Function: a0  
:Pattern: A0[m_, opt___Rule]  
:Arguments: {N[m], N[Delta /. {opt} /. Options[A0]],  
            N[Mudim /. {opt} /. Options[A0]]}  
:ArgumentTypes: {Real, Real, Real}  
:ReturnType: Real  
:End:  
  
:Evaluate: Options[A0] = {Delta -> 0, Mudim -> 1}
```



MathLink programming

b) C code implementing the exported functions

```
#include "mathlink.h"

static double a0(const double m,
                const double delta, const double mudim) {
    return m*(1 - log(m/mudim) + delta);
}
```



MathLink programming

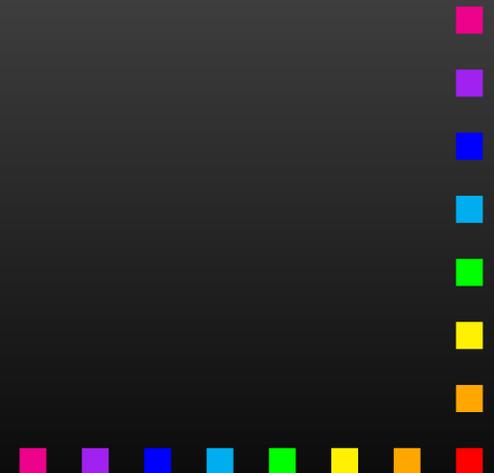
c) Boilerplate main function

```
int main(int argc, char **argv) {  
    return MLMain(argc, argv);  
}
```

Compile with `mcc` instead of `cc`.

Load in Mathematica with `Install["program"]`.

For even more details see [arXiv:1107.4379](https://arxiv.org/abs/1107.4379).



Recent Problems

arXiv:1107.4379 gives details on how to set up **thread to listen on stdout and send output back to Mathematica.**

No error/warning messages reported on Cygwin + gfortran.

Careful analysis:

- Mathematica **closes stdin, stdout, stderr** before launching MathLink executable.
- libgfortran startup considers closed descriptors useless and **refuses to allocate workable Fortran units 5, 6, 0.**
- Workarounds using e.g. FIFO pipes not desirable/straightforward (Windows FIFO API not fully POSIX).



Solution

- **First Try: open stdout, then exec self:**

```
stdoutorig = dup(1);
if( stdoutorig == -1 && getenv("LTRESPAWN") == NULL ) {
    openstdout();
    putenv("LTRESPAWN=1");
    execv(argv[0], argv);
    exit(1);
}
```

Downside: Spurious terminal window opens (why?).

- **'Squeeze in' before libgfortran constructor runs:**

```
static void __attribute__((constructor(4711)))
    make_sure_stdout_is_open() {
    if( fcntl(1, F_GETFD) == -1 ) openstdout();
}
```



Summary

- MathLink is Wolfram Research's API for **interfacing Mathematica to C/C++** (and everything that links to C/C++).
- Generally straightforward but **many caveats** beyond pure C/C++ (mixed languages, Cygwin).
- Copy-&-paste "**Cookbook recipes**" for most issues. Standard Unix build on Linux, MacOS, Windows.
- Details in arXiv:1107.4379.
- But: API very **stable over time**, statically linked executables work 'forever'.
- Recently solved two issues with Cygwin + gfortran.

