

# Precision calculations in BSM theories

—  
 $M_h$  and  $g - 2$

Dominik Stöckinger (TU Dresden)

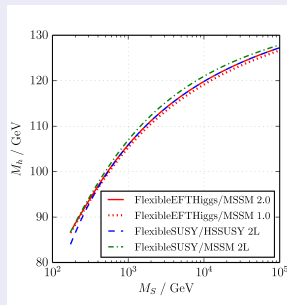
Loops & Legs, May 2018, St. Goar

# Outline

- 1 Higgs mass in MSSM and dimensional reduction [DS, Unger '18]
- 2 Muon  $g - 2$  in the THDM [Cherchiglia, DS, Stöckinger-Kim '17]

# Motivation: Higgs mass and dimensional reduction

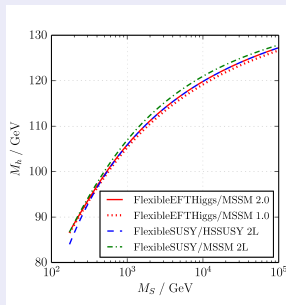
$$m_h^{\text{Exp}} = 125 \text{ GeV} \quad \text{compatible with } m_h^{\text{SUSY}}$$
$$\Delta m_h^{\text{Exp}} = 0.2 \text{ GeV} \quad \ll \Delta m_h^{\text{SUSY}}$$



⇒ should increase theory precision of  $m_h^{\text{SUSY}}$  !

# Motivation: Higgs mass and dimensional reduction

$$m_h^{\text{Exp}} = 125 \text{ GeV} \quad \text{compatible with } m_h^{\text{SUSY}}$$
$$\Delta m_h^{\text{Exp}} = 0.2 \text{ GeV} \quad \ll \Delta m_h^{\text{SUSY}}$$



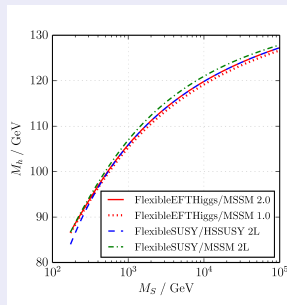
⇒ should increase theory precision of  $m_h^{\text{SUSY}}$  !

● current  $\Delta m_h^{\text{SUSY}}$  from FlexibleSUSY implementations:

- ▶ fixed-order (2L), pure EFT, hybrid [Athron, Park, Steudtner, DS, Voigt '16]
- ▶ fixed-order (3L), pure EFT [Allanach, Voigt '18]
- ▶ scale variation not sufficient, dominant:  $\propto m_t, \alpha_s$

# Motivation: Higgs mass and dimensional reduction

$$m_h^{\text{Exp}} = 125 \text{ GeV} \quad \text{compatible with } m_h^{\text{SUSY}}$$
$$\Delta m_h^{\text{Exp}} = 0.2 \text{ GeV} \quad \ll \Delta m_h^{\text{SUSY}}$$



⇒ should increase theory precision of  $m_h^{\text{SUSY}}$  !

- existing 3-loop calculation  $\mathcal{O}(\alpha_t \alpha_S^2)$ : [Harlander, Kant, Mihaila, Steinhauser 08 + 10]  
further developments: [Kunz, Mihaila, Zerf '14; Harlander, Klappert, Voigt '17]
- **future**: full 3-loop calculation  $\mathcal{O}(\alpha_t \alpha_S^2, \alpha_t^2 \alpha_S, \alpha_t^3)$ : “gaugeless limit”
- **But subtlety: regularization scheme!**

# Motivation: Regularization by dimensional reduction

## Subtlety in such calculations: is DRED consistent with SUSY?

- E.g. in DREG:  $m_e^{1L} \neq m_{\bar{e}}^{1L}$   $\longleftrightarrow$   $\sim \langle (\delta_{\text{SUSY}} \mathcal{L}^{(D)}) \phi \psi \rangle \neq 0$



- in DRED: better but no all-order proof

Question: Is DRED consistent with SUSY for 3-loop Higgs mass calculations in the gaugeless limit in the MSSM?

## Previous related results:

- 2-loop SUSY-QCD:  $\tilde{q}q\tilde{g}$ ,  $qq\epsilon$ , . . . [Harlander, Jones, Kant, Mihaila, Steinhauser 06 + 09]
  - ▶ using higher-order  $\beta$  functions
- 2-loop 2-point functions,  $\delta m_h$  [DS 05][Hollik, DS 05]
  - ▶ using Slavnov-Taylor identities

# Technical details

Tree-level:

$$m_h^2 = m_Z^2 \cos^2(2\beta) + \mathcal{O}(1/m_A^2)$$

after SUSY renormalization transformation:

$$\delta m_h^2 = \delta(m_Z^2 \cos^2(2\beta)) + \dots$$

However, if SUSY is broken by DRED, we need:

$$\delta m_h^2 = \delta(m_Z^2 \cos^2(2\beta)) + \dots + \delta m_h^2|_{\text{SUSY-restore}}$$

# Technical details

Tree-level:

$$\mathcal{L}_{y_u} = y_u \left( H_2 \bar{u} q_L + \tilde{u}_R^\dagger \overline{\tilde{H}_2^C} q_L + \dots \right)$$

after SUSY renormalization transformation:

$$\mathcal{L}_{y_u} \rightarrow y_u \left( Z_{y_u} \sqrt{Z_{H_2} Z_{q_L} Z_{u_R}} H_2 \bar{u} q_L + Z_{y_u} \sqrt{Z_{\tilde{H}_2} Z_{q_L} Z_{\tilde{u}_R}} \tilde{u}_R^\dagger \overline{\tilde{H}_2^C} q_L + \dots \right) .$$

However, if SUSY is broken by DRED, we need:

$$\mathcal{L}_{y_u} \rightarrow y_u \left( Z_{H_2 q u} H_2 \bar{u} q_L + Z_{\tilde{H}_2 q \tilde{u}} \tilde{u}_R^\dagger \overline{\tilde{H}_2^C} q_L + \dots \right) .$$



# Technical details

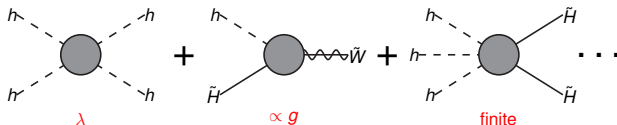
Technical goal: verify that/whether at 3-loop (2-loop)

$$\delta m_h^2|_{\text{SUSY-restore}} = 0, \quad (\text{and } Z_{y_u} \text{ etc sufficient})$$

Method:

- 1 find (set of) SUSY Slavnov-Taylor identities which determines CTs
- 2 verify that/whether STI is valid in DRED

# Step 1: STI for Higgs mass/quartic Higgs coupling



$$0 = \frac{\delta^5 S(\Gamma)}{\delta\phi_a \delta\phi_b \delta\phi_c \delta\tilde{H} \delta\tilde{\epsilon}} = \Gamma_{\tilde{H} Y_{\phi_i} \tilde{\epsilon}} \Gamma_{\phi_a \phi_b \phi_c \phi_i} + \Gamma_{\phi_a \phi_b Y_{\lambda} \tilde{\epsilon}} \Gamma_{\phi_c \tilde{H} \lambda} + \dots$$

Determines directly  $\delta m_h$

## Step 1: STIs for Yukawa couplings

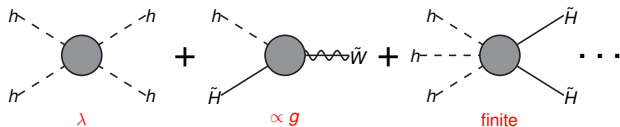
$$0 = -\Gamma_{\tilde{u}_R^\dagger \bar{\epsilon} y_{u_R}} \Gamma_{q_L^j H_2^j \bar{u}_R} - \Gamma_{H_2^j \bar{\epsilon} y_{\tilde{H}_1^m} c} \Gamma_{q_L^j \tilde{u}_R^\dagger \overline{\tilde{H}_1^m} c} + \dots \Rightarrow \text{Yukawa couplings}$$

$$0 = \Gamma_{\tilde{u}_R^\dagger \bar{\epsilon} y_{u_R}} \Gamma_{u_R \bar{\epsilon} Y_{\tilde{u}_R^\dagger}} + \text{known} \Rightarrow \text{SUSY transf.}$$

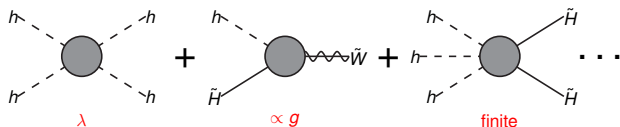
$$0 = -\Gamma_{\tilde{u}_R^\dagger \bar{\epsilon} y_{u_R}} \Gamma_{u_R \bar{u}_R} - \Gamma_{u_R \bar{\epsilon} Y_{\tilde{u}_R^\dagger}} \Gamma_{\tilde{u}_R \tilde{u}_R^\dagger} \Rightarrow \text{self energies}$$

Combination determines Yukawa counterterms  
(up to field renormalization)

## Step 2: Verify that STIs are valid in DRED



## Step 2: Verify that STIs are valid in DRED



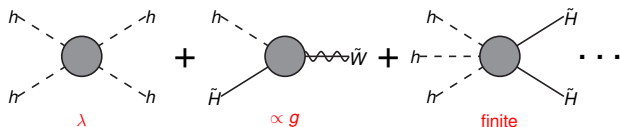
### Strategy:

- Use quantum action principle in DRED [Breitenlohner, Maison '77][DS '05]

$$\text{violation of this STI in DRED} = \langle \Delta h h h \tilde{H} \rangle$$

$$\text{where } \Delta = \delta_{\text{SUSY}} \int d^D x \mathcal{L}_{\text{bare}}$$

## Step 2: Verify that STIs are valid in DRED



### Strategy:

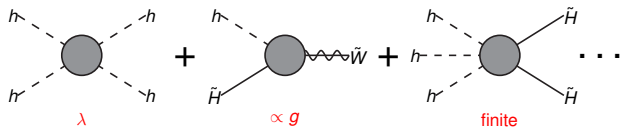
- Use quantum action principle in DRED [Breitenlohner, Maison '77][DS '05]

$$\text{violation of this STI in DRED} = \langle \Delta h h h \tilde{H} \rangle$$

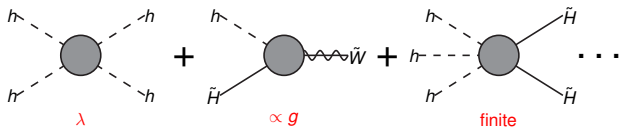
$$\text{where } \Delta = \delta_{\text{SUSY}} \int d^D x \mathcal{L}_{\text{bare}}$$

- determine  $\Delta$  from  $\mathcal{L}_{\text{bare}}^{\leq 2L}$ : [DS '05]-result sufficient
- evaluate all diagrams for  $\langle \Delta h h h \tilde{H} \rangle \Rightarrow$  they all vanish!

## Step 2: Verify that STIs are valid in DRED

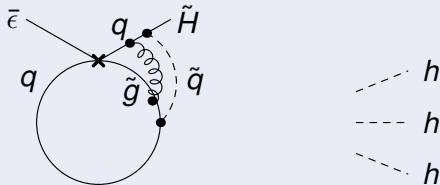


## Step 2: Verify that STIs are valid in DRED



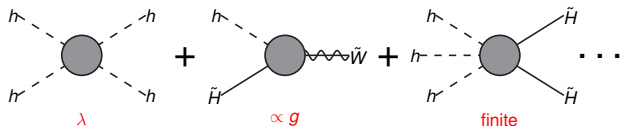
3-loop STI: sample diagrams at  $\mathcal{O}(\alpha_t \alpha_s^2, \alpha_t^2 \alpha_s, \alpha_t^3)$

$\langle \Delta h h h \tilde{H} \rangle = 0 ?$



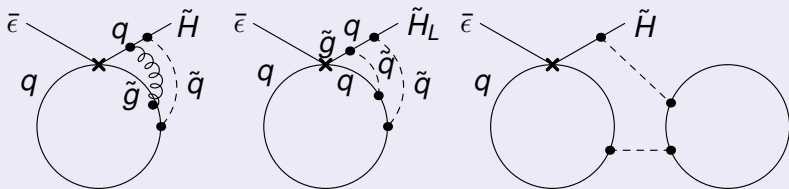


## Step 2: Verify that STIs are valid in DRED



3-loop STI: sample diagrams at  $\mathcal{O}(\alpha_t \alpha_s^2, \alpha_t^2 \alpha_s, \alpha_t^3)$

$\langle \Delta h h h \tilde{H} \rangle = 0 ?$



# Is DRED consistent with SUSY for 3-loop Higgs mass calculations in the gaugeless limit in the MSSM?

Answer: Yes!

- all such diagrams vanish, for all relevant STIs
- no SUSY-restoring CTs needed at 3-loop or subrenormalization level
- concrete cases (all in gaugeless limit):
  - ▶ quartic Higgs coupling 3-loop
  - ▶ Yukawa interactions Higgs/Higgsino quark/squark 2-loop
  - ▶ quartic interactions Higgs–squarks 2-loop
  - ▶ quartic interactions Higgs– $\epsilon$ -scalars 2-loop
  - ▶ triple interactions gluon/gluino quark/squark [Harlander et al 06 + 09]

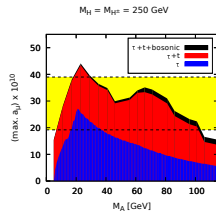
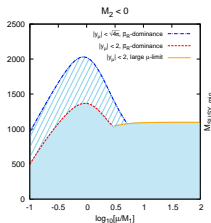
# Outline

- 1 Higgs mass in MSSM and dimensional reduction [DS, Unger '18]
- 2 Muon  $g - 2$  in the THDM [Cherchiglia, DS, Stöckinger-Kim '17]

# Motivation: Muon $g - 2$ in the THDM

$$a_{\mu}^{\text{exp}} - a_{\mu}^{\text{SM}} = (28.1 \pm (6.3^{\text{Exp}} \rightarrow 1.6^{\text{FUTURE}})) \pm 3.6^{\text{Th(KNT)}}) \times 10^{-10}$$

Keshavarzi, Nomura, Teubner'17; Jegerlehner'17:  $\pm 4.4^{\text{Th}}$



⇒ should compare BSM scenarios

New experiment (Fermilab)

Largest SUSY

[Bach, Park, DS, Stöckinger-Kim '15]

Largest THDM

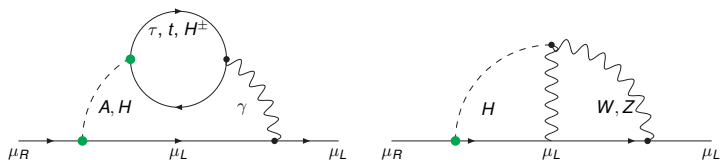
[Cherchiglia, DS, Stöckinger-Kim '17]

# Motivation: Muon $g - 2$ in the THDM

Extra Higgs bosons negligible at 1-loop  $\rightsquigarrow$  2-loop = leading

LHC constraints on extra Higgs bosons  $\rightsquigarrow$  can 2HDM explain  $a_\mu$ ?

Recent calculations: all Barr-Zee [Ilisie '15], full 2-loop [Cherchiglia, Kneschke, DS, Stöckinger-Kim, 16]



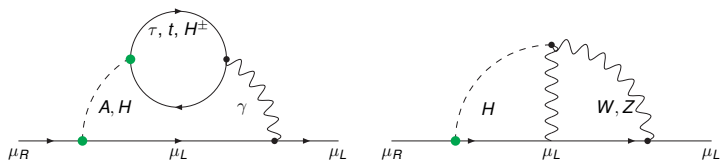
Question: What is the largest  $a_\mu$  possible in the THDM?

# Motivation: Muon $g - 2$ in the THDM

Extra Higgs bosons negligible at 1-loop  $\rightsquigarrow$  2-loop = leading

LHC constraints on extra Higgs bosons  $\rightsquigarrow$  can 2HDM explain  $a_\mu$ ?

Recent calculations: all Barr-Zee [Ilisie '15], full 2-loop [Cherchiglia, Kneschke, DS, Stöckinger-Kim, 16]

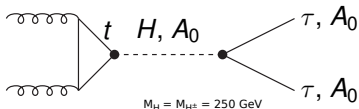
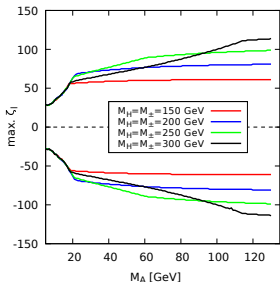
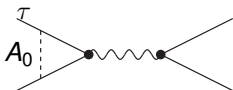


Question: What is the largest  $a_\mu$  possible in the THDM?

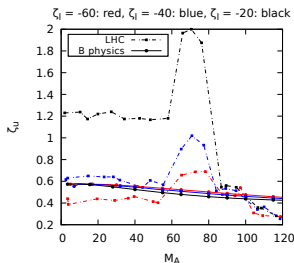
- Need to study first: experimental constraints on parameters
  - ▶ non-Barr-Zee: small couplings to gauge bosons,  $\Delta\rho$
  - ▶ Barr-Zee:  $\propto$  new Yukawa couplings/triple Higgs couplings

# What are the constraints on the 2HDM parameters ?

Most important:  $M_A$ , Yukawa parameters  $\zeta_I$  and  $\zeta_U$

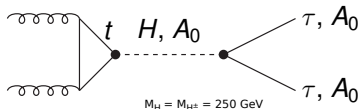
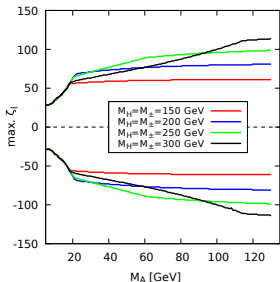
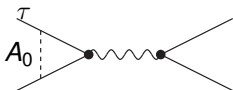


$$M_H = M_{H^\pm} = 250 \text{ GeV}$$

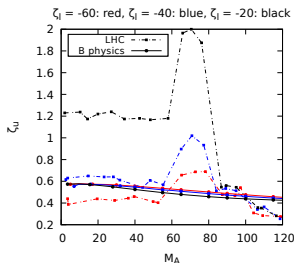


# What are the constraints on the 2HDM parameters ?

Most important:  $M_A$ , Yukawa parameters  $\zeta_l$  and  $\zeta_U$



$$M_H = M_{H^\pm} = 250 \text{ GeV}$$



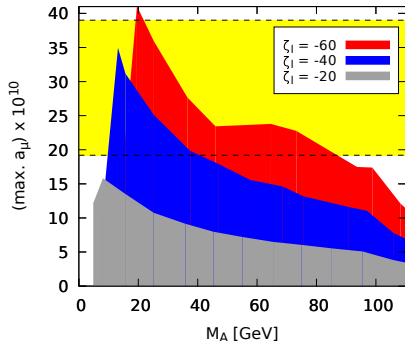
- lepton Yukawa  $< \sim 100$  for  $M_A > 20$  GeV
- quark Yukawas  $< \sim 0.5$  for  $M_A < 100$  GeV



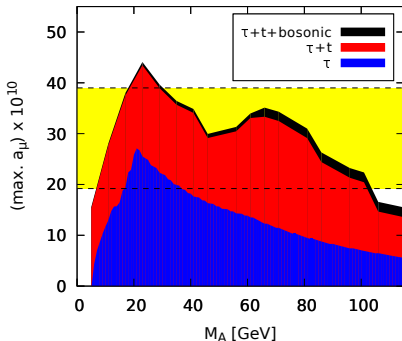
# What is the maximum possible $a_{\mu}$ in the 2HDM?

Answer:

$$M_H = M_{H^\pm} = 300 \text{ GeV}$$



$$M_H = M_{H^\pm} = 250 \text{ GeV}$$



Small  $M_A$  and large  $\zeta_l$  needed  $\rightsquigarrow$  not in Type I or Type II (correlations!)

Type X ( $\zeta_l \approx 0$ ): barely explains current deviation

Beyond Type I, II, X: top-loop, bosonic less suppressed for higher  $M_A$ ;  $1\sigma$  explanation possible between  $M_A = 20 \dots 100$ .

# Conclusions

- $m_h$  in MSSM: DRED consistent with SUSY at 3-loop (gaugeless)?

- ▶ Yes
- ▶ SUSY renormalization transformation correct
- ▶ holds for genuine 3-loop and sub-CTs
- ▶ method: STI and quantum action principle



- Muon  $g - 2$ : Largest  $a_\mu$  in aligned Two-Higgs doublet model?

- ▶ need light  $A_0$  and large  $\tau$  Yukawa
- ▶ Type I, II excluded
- ▶ also prefers large  $t$  Yukawa couplings
- ▶ constraints:  $|\zeta_I| < \sim 50$ ,  $\zeta_U < \sim 0.5$
- ▶ should be tested at LHC

