Axion Models.

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Spring Block Course 2017 GRK1504/2 Rathen, D 13-16 March 2017





- > Add singlet complex scalar field σ featuring a global $U(1)_{PQ}$ symmetry to Standard Model (SM)
- Parameters in most general scalar potential such that symmetry spontaneously broken in vacuum:

$$V(H,\sigma) = \lambda_H \left(H^{\dagger}H - \frac{v^2}{2} \right)^2 + \lambda_\sigma \left(|\sigma|^2 - \frac{v_{\rm PQ}^2}{2} \right)^2 + 2\lambda_{H\sigma} \left(H^{\dagger}H - \frac{v^2}{2} \right) \left(|\sigma|^2 - \frac{v_{\rm PQ}^2}{2} \right)$$

> For $\lambda_H, \lambda_\sigma > 0$ and $\lambda_{H\sigma}^2 < \lambda_H \lambda_\sigma$, minimum of potential attained at:

$$\langle H^{\dagger}H\rangle = v^2/2, \qquad \langle |\sigma|^2\rangle = v_{\rm PQ}^2/2$$

Expansion about VEV:

$$\sigma(x) = \frac{1}{\sqrt{2}} \left(v_{\rm PQ} + \rho(x) \right) e^{iA(x)/v_{\rm PQ}}$$

Excitation of modulus:

- $m_{\rho} = \sqrt{2\,\lambda_{\sigma}}\,v_{\rm PQ} + \mathcal{O}\left(\frac{v}{v_{\rm PQ}}\right)$ Excitation of angle (Nambu-Goldstone Boson (NGB)): $m_{A} = 0$
- Low energy effective field theory: SM + massless non-interacting NGB



[Kim 79;Shifman,Vainshtein,Zakharov 80] Add color-triplet, electroweak singlet fermion $Q = (Q_L, Q_R)$

> PQ scalar and exotic quark are assumed to transform under $U(1)_{PQ}$ as

$$\sigma \to e^{i\alpha}\sigma$$
, $Q_L \to e^{i\alpha/2}Q_L$, $Q_R \to e^{-i\alpha/2}Q_R$

> Invariant Lagrangian:

$$\mathcal{L} \supset \frac{1}{2} \partial_{\mu} \sigma^* \partial^{\mu} \sigma - V(H, \sigma) + \frac{i}{2} \overline{Q} \partial_{\mu} \gamma^{\mu} Q - y \overline{Q}_L \sigma Q_R$$

> After PQ symmetry breaking, integrate out modulus: $\begin{bmatrix} \sigma(x) = \frac{v_{\mathrm{PQ}}}{\sqrt{2}}e^{iA(x)/v_{\mathrm{PQ}}} \end{bmatrix}$ $\mathcal{L} \supset \frac{1}{2}\partial_{\mu}A\partial^{\mu}A + \frac{i}{2}\overline{Q}\partial_{\mu}\gamma^{\mu}Q - y\frac{v_{\mathrm{PQ}}}{\sqrt{2}}e^{iA/v_{\mathrm{PQ}}}\overline{Q}_{L}Q_{R}$

Redefining fermion by local transformation,

$$Q_L \to e^{iA/2v_{\rm PQ}}Q_L; \quad Q_R \to e^{-iA/2v_{\rm PQ}}Q_R$$

we obtain:

$$\mathcal{L} \supset \frac{1}{2} \left(\partial_{\mu} A \right)^{2} + \frac{i}{2} \overline{Q} \partial_{\mu} \gamma^{\mu} Q - y \frac{v_{\mathrm{PQ}}}{\sqrt{2}} \overline{Q}_{L} Q_{R} + \frac{1}{2} \frac{\partial_{\mu} A}{v_{\mathrm{PQ}}} \overline{Q} \gamma^{\mu} \gamma_{5} Q$$



$$\mathcal{L} \supset \frac{1}{2} \left(\partial_{\mu} A\right)^{2} + \frac{i}{2} \overline{Q} \partial_{\mu} \gamma^{\mu} Q - y \frac{v_{\mathrm{PQ}}}{\sqrt{2}} \overline{Q}_{L} Q_{R} + \frac{1}{2} \frac{\partial_{\mu} A}{v_{\mathrm{PQ}}} \overline{Q} \gamma^{\mu} \gamma_{5} Q$$

Coupling of axion with exotic color-triplet gives rise to effective interaction with gluons via triangle anomaly:



> Integrating out heavy color-triplet, end up with effective theory at scales much below PQ scale v_{PQ} , but above QCD scale Λ_{QCD} :

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \frac{1}{2} \partial^{\mu} A \,\partial_{\mu} A - \frac{\alpha_s}{8\pi} \frac{A}{v_{\text{PQ}}} G^a_{\mu\nu} \tilde{G}^{a\,\mu\nu}$$



Indeed model with space-time dependent theta parameter:

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \frac{1}{2} (\partial_{\mu} A)^2 - \frac{\alpha_s}{8\pi} \frac{A}{f_A} G^a_{\mu\nu} \tilde{G}^{a\,\mu\nu}; \qquad f_A = v_{\text{PQ}}$$

> Anomalous coupling can be reshuffled by quark field redefinition,

$$q = \begin{pmatrix} u \\ d \end{pmatrix} \to e^{i\gamma_5 \frac{A}{f_A} \frac{Q_A}{2}} \begin{pmatrix} u \\ d \end{pmatrix}, \quad \text{tr} Q_A = 1$$

yielding, taking into account anomaly of chiral currents of light quarks,

$$\mathcal{L}_{\text{eff}} \supset \frac{1}{2} (\partial_{\mu} A)^{2} - \bar{q}_{L} M_{A} q_{R} + 6 \operatorname{tr} \left(Q_{A} Q^{2} \right) \frac{\alpha}{8\pi} \frac{A}{f_{A}} F_{\mu\nu} \tilde{F}^{\mu\nu} - \frac{1}{2} \frac{\partial_{\mu} A}{f_{A}} \bar{q} \gamma^{\mu} \gamma_{5} Q_{A} q$$
$$M_{A} = e^{i \frac{A}{2f_{A}} Q_{A}} M_{q} e^{i \frac{A}{2f_{A}} Q_{A}}, \qquad M_{q} = \begin{pmatrix} m_{u} & 0\\ 0 & m_{d} \end{pmatrix}, \qquad Q = \begin{pmatrix} \frac{2}{3} & 0\\ 0 & -\frac{1}{3} \end{pmatrix}$$

Anomalous coupling to QCD encoded in phase dependence of quark mass matrix of lightest quarks

[Di Vecchia, Veneziano `80; Georgi, Kaplan, Randall 86; di Cortona et al. 16]



> At leading order in chiral expansion all non-derivative dependence on axion contained in mass terms:

$$\mathcal{L}_{p^2} \supset 2B_0 \frac{f_\pi^2}{4} \operatorname{tr} \left(U M_A^{\dagger} + M_A U^{\dagger} \right) ; \quad U = e^{i\Pi/f_\pi} ; \quad \Pi = \left(\begin{array}{cc} \pi^0 & \sqrt{2}\pi^+ \\ \sqrt{2}\pi^- & -\pi^0 \end{array} \right)$$

> Choosing $Q_A = M_q^{-1}/\text{tr}(M_q^{-1})$ to avoid mass mixing between the axion and the neutral pion, one finds for axion potential and mass:

$$V(A) = -m_{\pi}^{2} f_{\pi}^{2} \sqrt{1 - \frac{4m_{u}m_{d}}{(m_{u} + m_{d})^{2}} \sin^{2}\left(\frac{A}{2f_{A}}\right)}$$

$$m_{A}^{2} = \frac{d^{2}V}{dA^{2}}|_{A=0} = \frac{m_{u}m_{d}}{(m_{u} + m_{d})^{2}} \frac{m_{\pi}^{2} f_{\pi}^{2}}{f_{A}^{2}}$$
Strong CP problem solved ($\langle A \rangle = 0$)
[di Cortona et al. `16]

Low energy interactions of KSVZ axion:

$$\mathcal{L}_{\text{eff}} \supset \frac{1}{2} (\partial_{\mu} A)^2 - V(A) - C_{A\gamma} \frac{\alpha}{8\pi} \frac{A}{f_A} F_{\mu\nu} \tilde{F}^{\mu\nu} + \frac{1}{2} \frac{\partial_{\mu} A}{f_A} \sum_{N} C_{AN} \bar{N} \gamma^{\mu} \gamma_5 N$$

Potential:

$$V(A) = -m_{\pi}^2 f_{\pi}^2 \sqrt{1 - \frac{4m_u m_d}{(m_u + m_d)^2} \sin^2\left(\frac{A}{2f_A}\right)}$$

Coupling to photon:

$$C_{A\gamma} = -\frac{2}{3} \frac{4m_d + m_u}{m_d + m_u} \simeq -1.92$$

[Kaplan 85;Srednicki `85]

- Coupling to nucleons:

$$C_{Ap} = -0.47(3), \qquad C_{An} = -0.02(3)$$

[di Cortona et al. `16]



> Unify PQ U(1) symmetry with lepton symmetry: add three right-handed SM-singlet neutrinos to KSVZ like model [Shin 87; Dias et al. `14] $\mathcal{L} \supset - \begin{bmatrix} Y_{uij}q_i\epsilon Hu_j + Y_{dij}q_iH^{\dagger}d_j + G_{ij}L_iH^{\dagger}E_j + F_{ij}L_i\epsilon HN_j + \frac{1}{2}Y_{ij}\sigma N_iN_j \end{bmatrix}$

$$+y\,\tilde{Q}\sigma Q + y_{Q_d\,i}\sigma Q d_i + h.c.$$

q	u	d	L	N	E	Q	$ ilde{Q}$	σ
$\boxed{1/2}$	-1/2	-1/2	1/2	-1/2	-1/2	-1/2	-1/2	1



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[di Bari 12]

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- > Unify PQ U(1) symmetry with lepton symmetry: add three right-handed SM-singlet neutrinos to KSVZ like model [Shin 87; Dias et al. `14] $\mathcal{L} \supset - \left[Y_{uij}q_i\epsilon Hu_j + Y_{dij}q_iH^{\dagger}d_j + G_{ij}L_iH^{\dagger}E_j + F_{ij}L_i\epsilon HN_j + \frac{1}{2}Y_{ij}\sigma N_iN_j + \frac{1}{2}Y_{ij}\sigma N_$
- 1. No strong CP problem
- 2. Axion dark matter
- 3. See-saw explanation of active neutrino masses

$$m_{\nu} = 0.04 \,\mathrm{eV}\left(\frac{10^{11} \,\mathrm{GeV}}{v_{\sigma}}\right) \left(\frac{-F \, Y^{-1} \, F^{T}}{10^{-4}}\right)$$

4. Explains matter-anti-matter asymmetry by thermal leptogenesis



[Buchmüller et al. 04]



- > Unify PQ U(1) symmetry with lepton symmetry: add three right-handed SM-singlet neutrinos to KSVZ like model [Shin 87; Dias et al. `14] $\mathcal{L} \supset - \left[Y_{uij}q_i\epsilon Hu_j + Y_{dij}q_iH^{\dagger}d_j + G_{ij}L_iH^{\dagger}E_j + F_{ij}L_i\epsilon HN_j + \frac{1}{2}Y_{ij}\sigma N_iN_j + y\tilde{Q}\sigma Q + y_{Q_di}\sigma Qd_i + h.c. \right]$ SM * Axion * See-saw * Higgs portal inflation
- 1. No strong CP problem
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$$m_{\nu} = 0.04 \,\mathrm{eV}\left(\frac{10^{11} \,\mathrm{GeV}}{v_{\sigma}}\right) \left(\frac{-F \, Y^{-1} \, F^{T}}{10^{-4}}\right)$$

- 4. Explains matter-anti-matter asymmetry by thermal leptogenesis
- 5. Higgs portal inflation

[Ballesteros, Redondo, AR, Tamarit, 1608.05414]



- > Allow for non-minimal coupling of Higgs and PQ scalar to gravity, $S \supset -\int d^4x \sqrt{-g} \left[\frac{M^2}{2} + \xi_H H^{\dagger} H + \xi_\sigma \sigma^* \sigma \right] R; \quad M_P^2 = M^2 + \xi_H v^2 + \xi_\sigma v_{PQ}^2$
 - Generated anyway radiatively even if set to zero at some scale
- Non-minimal couplings stretch scalar potential in Einstein frame; makes it convex and asymptotically flat at large field values

$$\tilde{V}(h,\rho) = \frac{1}{\Omega^4(h,\rho)} \left[\frac{\lambda_H}{4} \left(h^2 - v^2 \right)^2 + \frac{\lambda_\sigma}{4} \left(\rho^2 - v_\sigma^2 \right)^2 + \frac{\lambda_{H\sigma}}{2} \left(h^2 - v^2 \right) \left(\rho^2 - v_\sigma^2 \right) \right]$$
$$\tilde{g}_{\mu\nu} = \Omega^2(h,\rho) g_{\mu\nu} \qquad \qquad \Omega^2 = 1 + \frac{\xi_H(h^2 - v^2) + \xi_\sigma(\rho^2 - v_\sigma^2)}{M_P^2}$$



- > Allow for non-minimal coupling of Higgs and PQ scalar to gravity, $S \supset -\int d^4x \sqrt{-g} \left[\frac{M^2}{2} + \xi_H H^{\dagger} H + \xi_\sigma \sigma^* \sigma \right] R; \quad M_P^2 = M^2 + \xi_H v^2 + \xi_\sigma v_{PQ}^2$
 - Generated anyway radiatively even if set to zero at some scale
- Non-minimal couplings stretch scalar potential in Einstein frame; makes it convex and asymptotically flat at large field values
- > Potential has valleys = attractors for Higgs Inflation (HI), Hidden Scalar Inflation (HSI) or mixed Higgs Hidden Scalar Inflation (HHSI), depending on relative signs of $\kappa_H \equiv \lambda_{H\sigma}\xi_H - \lambda_H\xi_\sigma$, $\kappa_\sigma \equiv \lambda_{H\sigma}\xi_\sigma - \lambda_\sigma\xi_H$



sign(κ_H)sign(κ_σ)Inflation+-HI-+HSI--HHSI



CMB observables



$$\lambda \equiv \begin{cases} \lambda_H, & \text{for HI,} \\ \lambda_{\sigma}, & \text{for HSI,} \\ \lambda_{\sigma} \left(1 - \frac{\lambda_{H\sigma}^2}{\lambda_{\sigma}\lambda_H} \right), & \text{for HHSI} \end{cases}$$

[Ballesteros, Redondo, AR, Tamarit, 1610.01639]

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HI requires huge non-minimal coupling of the Higgs:

 $\xi_H \sim 2 \times 10^5 \sqrt{\lambda_H(\sim M_P)} \sim 2 \times 10^4$

- > Perturbative unitarity lost in HI $\Lambda_U \sim \frac{M_P}{\xi_H} \sim 10^{14} \, \text{GeV} \ll \tilde{V}^{1/4}(h_I) \sim 10^{16} \, \text{GeV} \checkmark$
- > No unitarity problem in HSI/HHSI, if $\lambda_{\sigma}, \tilde{\lambda}_{\sigma} \lesssim 10^{-10}$, since then $\xi_{\sigma} \lesssim 1$



[Ballesteros, Redondo, AR, Tamarit, 1610.01639]



> Fundamental questions:

- PQ symmetry restored after inflation?
- Reheating temperature large enough for successful thermal leptogenesis?
- SMASH complete model: evolution after inflation can be calculated



Fundamental questions:

- PQ symmetry restored after inflation?
- Reheating temperature large enough for successful thermal leptogenesis?
- SMASH complete model: evolution after inflation can be calculated
- > Both in HSI and HHSI with $\xi_{\sigma} \lesssim 1$, slow-roll inflation ends at a value of $\rho \sim \mathcal{O}(M_P)$
- Inflaton starts to undergo Hubbledamped oscillations in a quartic potential, with Universe expanding as in a radiation-dominated era

> Preheating:

- Fluctuations of hidden scalar grow fast due to parametric resonance while inflaton background oscillates in its quartic potential
- PQ symmetry restored after about 14 full oscillations

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> Perturbative reheating:

HSI: Large induced particle masses quench inflaton decays or annihilations into SM particles, resulting in low reheating temperature and too much cosmic axion background (CAB) radiation

$$T_R \sim 10^7 \,\text{GeV} v_{11} \lambda_{10}^{3/8} \delta_3^{-1/8}$$
$$\Delta N_{\nu}^{\text{eff}} \sim (\delta_3 v_{11} / \lambda_{10})^{-1/6}$$

HHSI: Higgs component of inflaton allows for production of SM gauge bosons, resulting in high reheating temperature (sufficient for thermal leptogenesis) and $\Delta N_{\mu}^{\rm eff} \simeq 0.03$

CAB in reach of future CMB polarization experiment

History of Universe in SMASH

> Universe expands as in a radiation-dominated era (w = 1/3) from the end of inflation until matter-radiation equality

History of Universe in SMASH

Can be probed decisively by next generation CMB experiments

Axion Dark Matter in SMASH

- SMASH predicts post-inflationary PQ breaking and thus one-to-one relation $m_A \Leftrightarrow \Omega_A$
- > Dark matter abundance fixes symmetry breaking scale $v_{\sigma} = f_A$
 - $3 \times 10^{10} \,\text{GeV} \lesssim f_A \lesssim 1.2 \times 10^{11} \,\text{GeV}$ and thus axion mass

 $50\,\mu\mathrm{eV} \lesssim m_A \lesssim 200\,\mu\mathrm{eV}$

 In reach of proposed axion dark matter experiments (MADMAX, ORPHEUS)

[Ballesteros, Redondo, AR, Tamarit, 1608.05414]

Dine-Fischler-Srednicki-Zhitnitskyi (DFSZ) Model

[Zhitnitsky 80;Dine,Fischler,Srednicki 81]

> Type II Higgs Doublet Model:

$$\mathcal{L}_Y = Y_{ij}\bar{q}_{iL}H_d d_{jR} + \Gamma_{ij}\bar{q}_{iL}\tilde{H}_u u_{jR} + h.c.$$

> Fields are supposed to transform under PQ symmetry as:

$$\sigma \to e^{i\alpha}\sigma ,$$

$$H_d \to e^{iX_d\alpha}H_d ,$$

$$H_u \to e^{-iX_u\alpha}H_u ,$$

$$d_{iR} \to e^{-iX_d\alpha}d_{iR} ,$$

$$u_{iR} \to e^{-iX_u\alpha}u_{iR}$$

> Yukawa interactions as well as most general scalar potential,

$$V(\sigma) = -\mu_{\sigma}^2 |\sigma|^2 + \lambda_{\sigma} |\sigma|^4 + \lambda_3 H_d^{\dagger} H_u \sigma^2$$

nt, if $X_u + X_d = 2$

> Anomalous divergence of PQ current:

invaria

$$\partial^{\mu}J^{\mathrm{PQ}}_{\mu} = -6\,\frac{\alpha_s}{8\pi}G^a_{\mu\nu}\tilde{G}^{a\,\mu\nu} - 16\frac{\alpha}{8\pi}F_{\mu\nu}\tilde{F}^{\mu\nu}$$

Dine-Fischler-Srednicki-Zhitnitskyi (DFSZ) Model

Low energy effective Lagrangian below EW, but above QCD scale:

$$\mathcal{L}_{\text{eff}} = \frac{1}{2} \partial_{\mu} A \partial^{\mu} A - \frac{\alpha_s}{8\pi} \frac{A}{f_A} G^c_{\mu\nu} \tilde{G}^{c,\mu\nu} - \frac{\alpha}{8\pi} \frac{8}{3} \frac{A}{f_A} F_{\mu\nu} \tilde{F}^{\mu\nu} + \frac{1}{2} \frac{\partial_{\mu} A}{f_A} \sum_f C_f \overline{f} \gamma^{\mu} \gamma_5 f$$
$$f_A = \frac{v_{\text{PQ}}}{6}; \quad C_{Ae} = C_{Ad} = \frac{\sin^2 \beta}{3}; \quad C_{Au} = \frac{\cos^2 \beta}{3}; \quad \tan \beta = \frac{v_u}{v_d}$$

Low energy effective Lagrangian below QCD scale: $\mathcal{L}_{eff} \supset \frac{1}{2} (\partial_{\mu} A)^{2} - V(A) - C_{A\gamma} \frac{\alpha}{8\pi} \frac{A}{f_{A}} F_{\mu\nu} \tilde{F}^{\mu\nu} + \frac{1}{2} \frac{\partial_{\mu} A}{f_{A}} \sum_{f} C_{Af} \bar{f} \gamma^{\mu} \gamma_{5} f$ Photon coupling

$$C_{A\gamma} = \frac{8}{3} - \frac{2}{3} \frac{4m_d + m_u}{m_d + m_u}$$
 [Kaplan 85;Srednicki `85]

Nucleon coupling

[di Cortona et al. `16]

 $C_{Ap} = -0.435 \sin^2 \beta + (-0.182 \pm 0.025); \quad C_{An} = 0.414 \sin^2 \beta + (-0.16 \pm 0.025)$

Modest hints for excessive energy losses of stars in various evolutionary stages

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Modest hints for excessive energy losses of stars in various evolutionary stages

DESY

Practically every stellar systems seems to be cooling faster than predicted by models:

[Giannotti, Irastorza, Redondo, AR (2015); Giannotti, Irastorza, Redondo, AR (in preparation)]

- Excessive energy losses of HBs, RG, WDs, NS can be explained at one stroke by production of axion with coupling to photons, electrons, quarks:
 - Primakoff production of axions in Helium Burning stars (HBs) and Red Giants (RG)

Bremsstrahlung off electrons in White Dwarfs (WD) and RGs

Bremsstrahlung off neutrons in Neutron Stars (NS)

Excessive energy losses of HBs, RG, WDs, NS can be explained at one stroke by production of axion with coupling to photons, electrons, nucleons, like in DFSZ axion model:

$$C_{A\gamma} = \frac{8}{3} - 1.92(4) ,$$

$$C_{Ae} = \frac{1}{3} \sin^2 \beta ,$$

$$C_{Ap} = -0.435 \sin^2 \beta + (-0.182 \pm 0.025) ,$$

$$C_{An} = 0.414 \sin^2 \beta + (-0.16 \pm 0.025)$$

$$\tan\beta = v_u/v_d$$

[Giannotti, Irastorza, Redondo, AR, Saikawa in preparation]

Excessive energy losses of HBs, RG, WDs, NS can be explained at one stroke by production of axion with coupling to photons, electrons, nucleons, and probed by next generation experiments:

[Giannotti, Irastorza, Redondo, AR, Saikawa in preparation]

Can be also dark matter:

[Giannotti,Irastorza,Redondo,AR,Saikawa in preparation]

[Borsanyi et al. `16]

Summary

- > Axion mass in units of decay constant very well determined
- Couplings to photons, nucleons, electrons model dependent
 - Photon and nucleon coupling in units of decay constant typically of order one
 - Coupling to electrons in units of decay constant may be suppressed
- PQ scalar may play the role of the inflaton: axion models may solve at one stroke strong CP problem, dark matter and inflation
- Axion in meV mass range may explain at the same time also hints of excessive stellar energy losses
- > Thursday: Axion/ALP Experiments

