

# New constraints on the 3-3-1 model with right-handed neutrinos

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# Outline

- 1 The Model
  - Gauge group
  - Matter Content
  - Lagrangian
- 2 The Model with  $\mathbb{Z}_2$  symmetry
- 3 The Model with soft  $\mathbb{Z}_2$  breaking terms
  - $\mu_4^2 \chi^\dagger \eta$  term
  - $\frac{f}{\sqrt{2}} \epsilon_{ijk} \eta_i \rho_j \chi_k$  term
- 4 Summary and Conclusions

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# Gauge Group

$$\text{3-3-1 : } \text{SU}(3)_L \otimes \text{U}(1)_N$$

$$\downarrow \langle \chi \rangle$$

$$\text{SM : } \text{SU}(2)_L \otimes \text{U}(1)_Y$$

$$\downarrow \langle \rho \rangle, \langle \eta \rangle$$

$$\text{U}(1)_Q$$

## Why 3-3-1?

- Dark matter;
- Neutrino masses;
- Chiral anomaly free.

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# Matter Content

## Scalar triplets

$$\eta = \begin{pmatrix} \eta_1^0 \\ \eta_2^- \\ \eta_3^0 \end{pmatrix}, \quad \rho = \begin{pmatrix} \rho_1^+ \\ \rho_2^0 \\ \rho_3^+ \end{pmatrix}, \quad \chi = \begin{pmatrix} \chi_1^0 \\ \chi_2^- \\ \chi_3^0 \end{pmatrix}$$

## Left-handed fermions

$$f_{aL} = \begin{pmatrix} \nu_a \\ e_a \\ N_a^c \end{pmatrix}_L, \quad Q_L = \begin{pmatrix} u_1 \\ d_1 \\ u_4 \end{pmatrix}_L, \quad Q_{bL} = \begin{pmatrix} d_b \\ u_b \\ d_{b+2} \end{pmatrix}_L,$$

where  $a = 1, 2, 3$  and  $b = 2, 3$ .

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# Matter content

## Right-handed fermions

$e_{aR}$ ,  $u_{sR}$ ,  $d_{tR}$  are singlets with respect to  $SU(3)_L$

where  $s = 1, \dots, 4$  and  $t = 1, \dots, 5$ .

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# Yukawa Lagrangian

 $\mathcal{L}_{\text{Yuk}}$ 

$$\mathcal{L}_{\text{Yuk}} = \mathcal{L}_{\text{Yuk}}^{\rho} + \mathcal{L}_{\text{Yuk}}^{\eta} + \mathcal{L}_{\text{Yuk}}^{\chi} \quad ,$$

$$\mathcal{L}_{\text{Yuk}}^{\rho} = \alpha_t \bar{Q}_L d_{tR} \rho + \alpha_{bs} \bar{Q}_{bL} u_{sR} \rho^* + \\ Y_{aa'} \epsilon_{ijk} (\bar{f}_{aL})_i (f_{a'L})_j^c (\rho^*)_k + Y'_{aa'} \bar{f}_{aL} e_{a'R} \rho + \text{H.c.},$$

where  $a, a', i, j, k = 1, 2, 3$ ;  $b = 2, 3$ ;  $s = 1, \dots, 5$ ;  $t = 1, \dots, 4$ .

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# Yukawa Lagrangian

$$\mathcal{L}_{\text{Yuk}}^\eta = \beta_s \bar{Q}_L u_{sR} \eta + \beta_{bt} \bar{Q}_{bL} d_{tR} \eta^* + \text{H.c.},$$

$$\mathcal{L}_{\text{Yuk}}^\chi = \gamma_s \bar{Q}_L u_{sR} \chi + \gamma_{bt} \bar{Q}_{bL} d_{tR} \chi^* + \text{H.c.}$$

where  $b = 2, 3$ ;  $s = 1, \dots, 5$ ;  $t = 1, \dots, 4$ .

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# Spontaneous Symmetry breaking

## Minimally general vacuum structure

$$\langle \eta \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} v_{\eta_1} \\ 0 \\ 0 \end{pmatrix}, \quad \langle \rho \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_{\rho_2} \\ 0 \end{pmatrix}, \quad \langle \chi \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ 0 \\ v_{\chi_3} \end{pmatrix}$$

- $\langle \chi \rangle$  : mass to the exotic quarks:  $d_4, d_5$  and  $u_4$ ;
- $\langle \rho \rangle$  : mass to  $e, \mu, \tau$ ;  $d_1, u_2, u_3$  quarks; 2 neutrinos;
- $\langle \eta \rangle$  : mass to  $u_1, d_2, d_3$  quarks.

# Scalar Potential

$$V(\eta, \rho, \chi) = V_{\mathbb{Z}_2}(\eta, \rho, \chi) + V_{\not{\mathbb{Z}_2}}(\eta, \rho, \chi);$$

$$\begin{aligned} V_{\mathbb{Z}_2}(\eta, \rho, \chi) = & -\mu_1^2 \eta^\dagger \eta - \mu_2^2 \rho^\dagger \rho - \mu_3^2 \chi^\dagger \chi \\ & + \lambda_1 (\eta^\dagger \eta)^2 + \lambda_2 (\rho^\dagger \rho)^2 + \lambda_3 (\chi^\dagger \chi)^2 \\ & + \lambda_4 (\chi^\dagger \chi) (\eta^\dagger \eta) + \lambda_5 (\chi^\dagger \chi) (\rho^\dagger \rho) \\ & + \lambda_6 (\eta^\dagger \eta) (\rho^\dagger \rho) + \lambda_7 (\chi^\dagger \eta) (\eta^\dagger \chi) \\ & + \lambda_8 (\chi^\dagger \rho) (\rho^\dagger \chi) + \lambda_9 (\eta^\dagger \rho) (\rho^\dagger \eta) \\ & + [\lambda_{10} (\chi^\dagger \eta)^2 + \text{H.c.}]; \end{aligned}$$

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# Scalar Potential

$$\begin{aligned}
 V_{\cancel{\mathbb{Z}_2}}(\eta, \rho, \chi) = & -\mu_4^2 \chi^\dagger \eta + \lambda_{11} (\chi^\dagger \eta) (\eta^\dagger \eta) \\
 & + \lambda_{12} (\chi^\dagger \eta) (\chi^\dagger \chi) + \lambda_{13} (\chi^\dagger \eta) (\rho^\dagger \rho) \\
 & + \lambda_{14} (\chi^\dagger \rho) (\rho^\dagger \eta) + \frac{f}{\sqrt{2}} \epsilon_{ijk} \eta_i \rho_j \chi_k + \text{H.c.}
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# The Model with $\mathbb{Z}_2$ symmetry

## Transformation

$$\mathbb{Z}_2: \chi \rightarrow -\chi, u_{4R} \rightarrow -u_{4R}, d_{(4,5)R} \rightarrow -d_{(4,5)R}$$

Most studied 3-3-1 scenario.

## Consequences of $\mathbb{Z}_2$

- It brings simplicity to the model;
- Possibility of DM through the  $\chi$  transformation;
- It alleviates FCNC processes, since the  $u_{4R}$  and  $d_{(4,5)R}$  quarks only interact with one of the triplets,  $\chi$ .

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# The Model with $\mathbb{Z}_2$ symmetry

## U(1) symmetries

	$Q_L$	$Q_{iL}$	$(u_{aR}, u_{4R})$	$(d_{aR}, d_{(4,5)R})$	$f_{aL}$	$e_{aR}$	$\eta$	$\rho$	$\chi$
$U(1)_N$	1/3	0	2/3	-1/3	-1/3	-1	-1/3	2/3	-1/3
$U(1)_B$	1/3	1/3	1/3	1/3	0	0	0	0	0
$U(1)_{PQ}$	1	-1	0	0	-1/2	-3/2	1	1	1

## Constraining the 3 VEVs case

### NG boson

$$J = \frac{1}{N_J} \left( \frac{v_{\eta_1} v_{\chi_3}}{v_{\rho_2}} \text{Im } \rho_2^0 + v_{\chi_3} \text{Im } \eta_1^0 + v_{\eta_1} \text{Im } \chi_3^0 \right)$$

### $g_{eeJ}$ coupling

- This coupling implies an energy loss channel through the process  $\gamma + e^- \rightarrow e^- + J$  ;
- Evolution of red-giant stars:  $|g_{eeJ}| \lesssim g_{\text{max}} \equiv 10^{-13}$  ;
- Our model:  $g_{eeJ} = \frac{\sqrt{2} m_e v_{\eta_1} v_{\chi_3}}{N_J v_{\rho_2}^2}$  because

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## Constraining the 3 VEVs case

Together with  $M_{W^\pm}^2 = \frac{g_L^2}{4} (v_{\eta_1}^2 + v_{\rho_2}^2) = \frac{g_L^2}{4} v_{\text{SM}}^2$ , one finds

$$v_{\chi_3} = v_{\chi_3}(v_{\rho_2})$$

$$v_{\chi_3} \leq v_{\chi_{\text{max}}}(v_{\rho_2}) \equiv v_{\rho_2} \left[ 2g_{\text{max}}^{-2} m_e^2 / v_{\rho_2}^2 - 1 / (1 - v_{\rho_2}^2 / v_{\text{SM}}^2) \right]^{-1/2}.$$

$$v_{\chi_{\text{max}}}(v_{\rho_2} \rightarrow v_{\text{SM}}^-) \simeq 11.5 \text{ keV}.$$

which contradicts  $\langle \chi \rangle > \langle \rho \rangle$ ,  $\langle \eta \rangle$ , which is assumed at the SSB.

**BAD!**

## 4 and 5 VEVs cases

- 2 NG bosons:  $J_I$  and  $J_R$ ;
- $Z \rightarrow J_R J_I$ , therefore these scenarios are **ruled out!**

### Making the $\mathbb{Z}_2$ -symmetric model safe

- Add terms which break explicitly the additional U(1) symmetries;
- We explore two soft terms from the  $\mathbb{Z}_2$ -breaking potential:  
 $\mu_4^2 \chi^\dagger \eta$  and  $\frac{f}{\sqrt{2}} \epsilon_{ijk} \eta_i \rho_j \chi_k$ .



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$$\mu_4^2 \chi^\dagger \eta$$

- 1 NG boson with imaginary components;
- The case  $(v_{\eta 1}, v_{\rho 2}, v_{\chi 3})$  is ruled out, because the NG boson has the same form as the earlier case;
- 4 VEVs:  $v_{\chi 3} \lesssim 355$  GeV.
- 5 VEVs:  $v_{\chi 3} \lesssim 355$  GeV if  $v_{\rho 2} \simeq v_{\text{SM}}$ .

We have used as constraints the  $W^\pm$ ,  $Z$  masses, the  $g_{eeJ}$  coupling and the positivity of the VEVs.

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There appear no physical NG bosons, therefore the model is safe regarding the appearance of massless scalars.

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# Summary and conclusions

- This approach had not yet been considered in 3-3-1 models;
- Physical NG bosons play an important role at constraining parameters
  - Can interact with matter;
  - Example:  $\gamma + e^- \rightarrow e^- + J \implies g_{eeJ}$  coupling.
- $\mathbb{Z}_2$ -symmetric potential
  - 3 VEVs: bad!  $v_{\chi_3} \lesssim 11.5$  keV.
  - 4 and 5 VEVs: bad!  $Z \rightarrow J_L + J_R$  allowed.
- Softly broken  $\mathbb{Z}_2$ 
  - $\mu_4^2 \chi^\dagger \eta$ :  $v_{\chi_3} \lesssim 355$  GeV for 4 VEVs. The 5 VEVs case has more freedom;
  - $\frac{f}{\sqrt{2}} \epsilon_{ijk} \eta_i \rho_j \chi_k$ : NO massless scalars!

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