

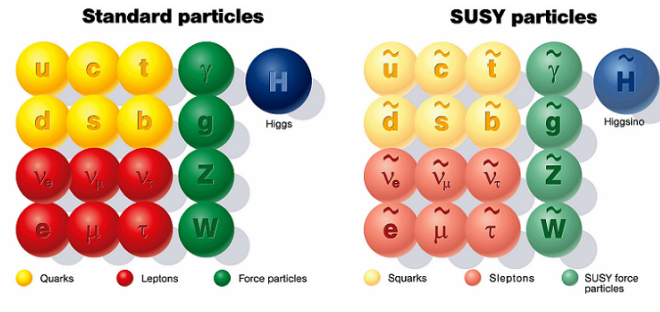
SUSY after Higgs

G.G.Ross, Bonn, May 2017

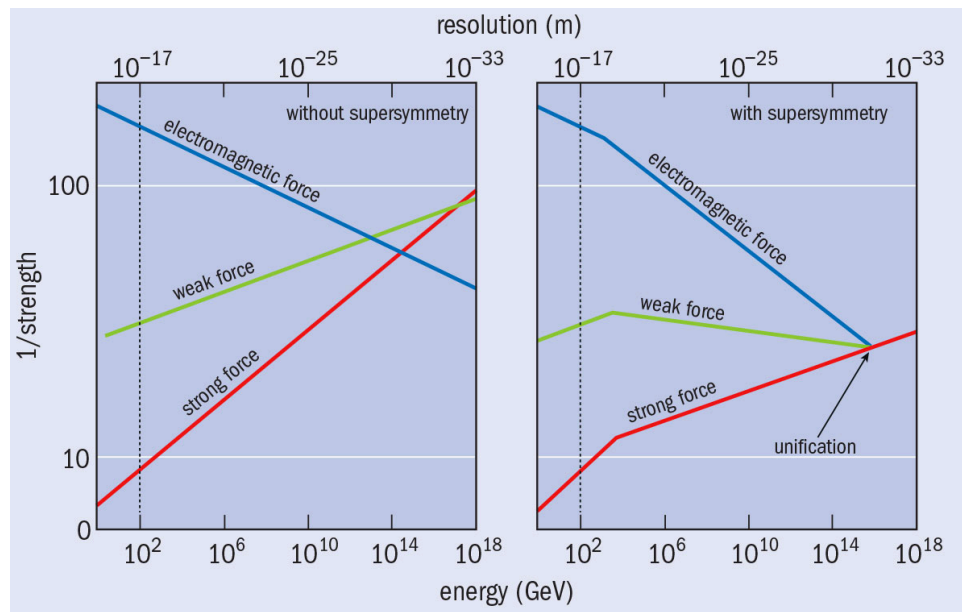
(Kai Schmidt-Hoberg, Florian Staub)



SUSY



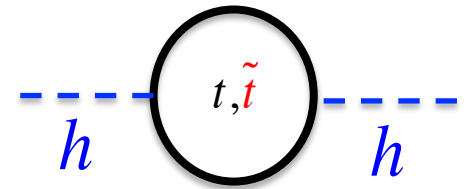
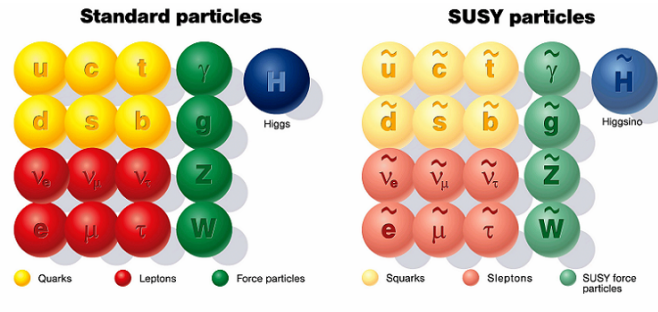
MSSM



GUTs

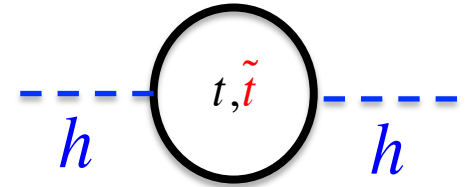
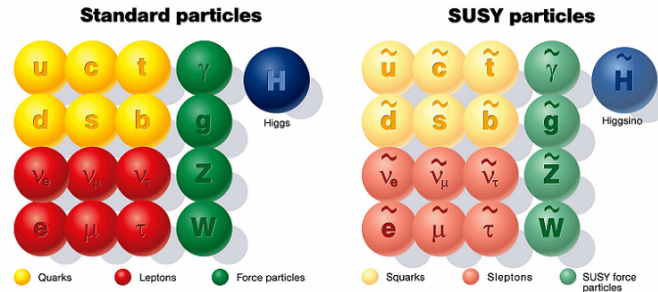
Georgi, Quinn, Weinberg
Ibanez, GGR
Dimopoulos, Raby, Wilczek

The Higgs mass and SUSY



$$m_h^2 = M_Z^2 + \frac{3m_t^2 h_t^2}{4\pi^2} \left(\ln \left(m_{stop}^2 / m_t^2 \right) + \delta_t \right) + \dots < \sim 140 \text{ GeV} \quad \checkmark$$

The Higgs mass and SUSY



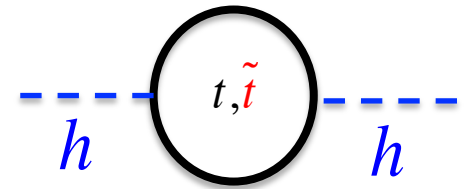
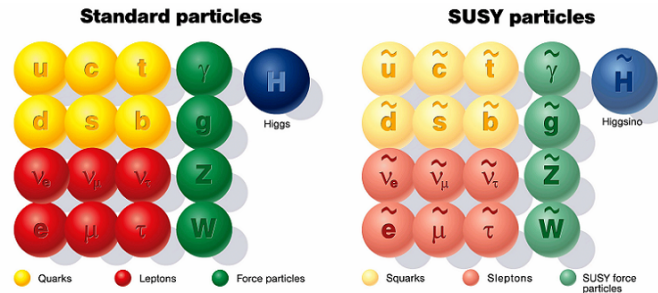
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Tension:

$$\Lambda \sim M_{GUT} ?$$

$$v^2 \sim \delta m_{H_u}^2 \simeq -\frac{3y_t^2}{4\pi^2} \left(m_{stop}^2 + \frac{g_s^2}{3\pi^2} m_{gluino}^2 \log \left(\frac{\Lambda}{m_{gluino}} \right) \right) \log \left(\frac{\Lambda}{m_{stop}} \right) < O \left(\langle H^2 \rangle \right)$$

The Higgs mass and SUSY



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$\Lambda \sim M_{GUT} ?$

... the "Hierarchy problem" - has SUSY been fully tested ?

MSSM: 105 +(19) Parameters

$$M_Z^2 = \sum_{\tilde{q}, \tilde{l}} a_i \tilde{m}_i^2 + \sum_{\tilde{g}, \tilde{W}, \tilde{B}} b_i \tilde{M}_i^2 + \dots$$

$$M_{\tilde{g}} > 1\text{TeV} \Rightarrow \Delta > b \frac{\tilde{M}^2}{M_Z^2} \sim 100$$

\Rightarrow Correlations between SUSY breaking parameters and/or additional low-scale states

Fine Tuning measure:

$$\Delta(a_i) = \left| \frac{\partial \ln M_Z^2}{\partial \ln \gamma_i} \right|, \quad \gamma_i = m_i, M_i \dots$$

$$\Delta_m = \text{Max}_{a_i} \Delta(\gamma_i), \quad \Delta_q = \left(\sum \Delta_{\gamma_i}^2 \right)^{1/2}$$

Ellis, Enquist, Nanopoulos, Zwirner
Barbieri, Giudice

Fine tuning from a likelihood fit:

SUSY parameters

If v included as a “Nuisance” variable

$$L(\text{data} \mid \gamma_i) \propto \int d v \delta(m_Z - m_Z^0) \delta\left(v - \left(-\frac{m^2}{\lambda}\right)^{1/2}\right) L(\text{data} \mid \gamma_i; v)$$

$$= \frac{1}{\Delta_q} \delta\left(n_q (\ln \gamma_i - \ln \gamma_i^S)\right) L(\text{data} \mid \gamma_i; v_0)$$

Fine tuning measure $\Delta_q = \left(\sum \Delta_{\gamma_i}^2\right)^{1/2}$

Ghilezea, GGR

Probabilistic interpretation:

$$\chi_{new}^2 = \chi_{old}^2 + 2 \ln \Delta_q$$

$$\Delta_q < 100, \quad \delta\left(\frac{\chi^2}{d.f.}\right) < 1$$

(should be averaged over #df)

Simplest case - the "Constrained" MSSM (CMSSM)

Soft SUSY breaking parameters:


$$\gamma_i(M_{GUT}) = \mu_0, m_0, m_{1/2}, A_0, B_0$$

- Parameters input at GUT scale (gauge coupling unification)
- SARAH/Spheno+FlavorKit Staub
(2-loop: RGE & Higgs mass)

Higgsino mass term μ_0

Radiative corrections can reduce sensitivity:

$$\gamma_i(M_{GUT}) = \mu_0, m_0, m_{1/2}, A_0, B_0$$

$$\frac{1}{2} M_Z^2 = -\mu^2 - m_{H_u}^2 \rightarrow -\mu^2 - m_{H_u}^2 - \frac{\partial \Delta V}{\partial v^2}$$


$$\Delta_{FT}^\mu = -\left. \frac{2\mu^2}{M_Z^2} \right|_{Tree} \rightarrow \geq \left. \frac{\mu^2}{M_Z^2} \right|_{\text{Radiative corrections}}$$

GGR, Schmidt-Hoberg, Staub
Cassell, Ghilencea, GGR

Scalar mass term m_0

Fine tuning also sensitive to *correlations* between SUSY breaking terms

e.g. $\gamma_i = \mu_0, m_0, m_{1/2}, A_0, B_0$ CMSSM

Focus point $Z_{h_u}^{m_0}(M_Z) \simeq 0$

$$m_{h_u}^2(Q) = z_{h_u}^{m_0}(Q)m_0^2 + z_{h_u}^{m_{1/2}}(Q)m_{1/2}^2 + z_{h_u}^{A_0}(Q)A_0^2 + 2z_{h_u}^{m_{1/2}A_0}(Q)m_{1/2}A_0$$

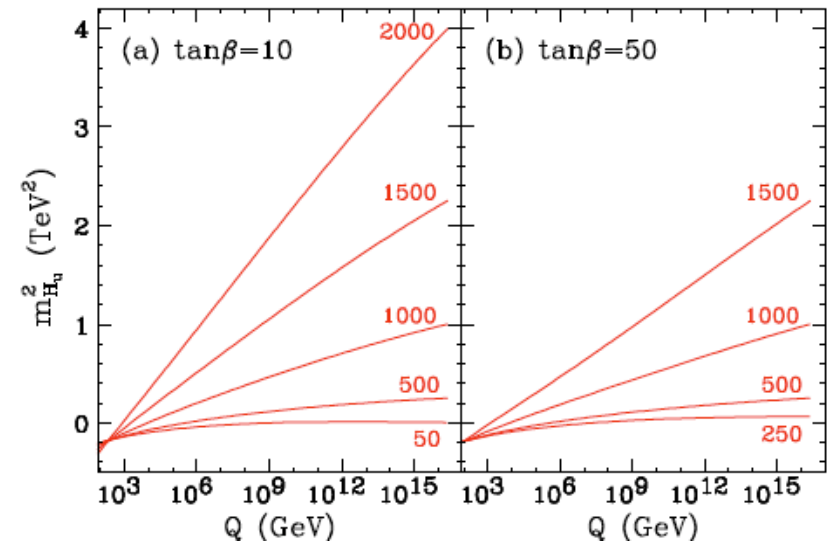
Focus Point

$$2|y_t|^2 (m_{H_u}^2 + m_{Q_3}^2 + m_{u_3}^2) + 2|a_t|^2$$

$$16\pi^2 \frac{d}{dt} m_{H_u}^2 = 3X_t - 6g_2^2 |M_2|^2 - \frac{6}{5}g_1^2 |M_1|^2$$

$$16\pi^2 \frac{d}{dt} m_{Q_3}^2 = X_t + X_b - \frac{32}{3}g_3^2 |M_3|^2 - 6g_2^2 |M_2|^2 - \frac{2}{15}g_1^2 |M_1|^2$$

$$16\pi^2 \frac{d}{dt} m_{u_3}^2 = 2X_t - \frac{32}{3}g_3^2 |M_3|^2 - \frac{32}{15}g_1^2 |M_1|^2$$



$$m_{H_u}^2(Q^2) = m_{H_u}^2(M_P^2) + \frac{1}{2} \left(m_{H_u}^2(M_P^2) + m_{Q_3}^2(M_P^2) + m_{u_3}^2(M_P^2) \right) \left[\left(\frac{Q^2}{M_P^2} \right)^{\frac{3y_t^2}{4\pi^2}} - 1 \right]$$

$$m_0^2$$

$$3m_0^2$$

$$\simeq -\frac{2}{3}, \quad Q^2 \simeq M_Z^2$$

“Focus point”: $m_{H_u}^2(0) = m_{Q_3}^2(0) = m_{u_3}^2(0) \equiv m^2$ $m_{H_u}^2(t_0) = a_0 m^2 + \dots, a_0 \leq 0.1$

i.e. $m_{Q_3}^2, m_{u_3}^2 \gg M_Z^2$ possible

Natural choice

Feng, Matchev, Moroi
Chan, Chattopadhyay, Nath
Barbieri, Giudice
Feng, Sanford

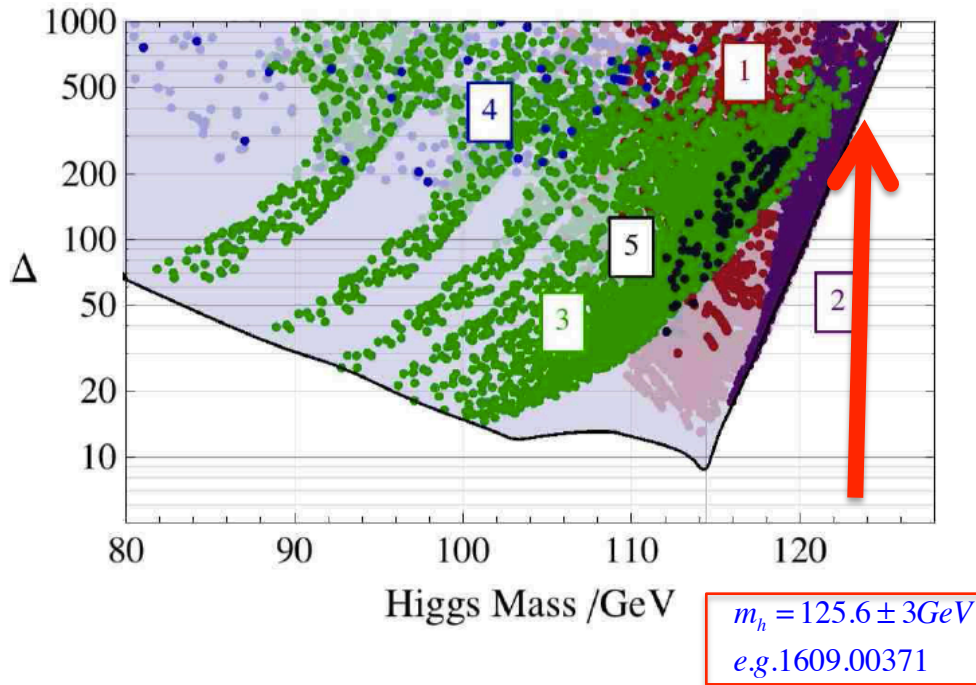
(sensitivity to y_t small)

Ciafaloni, Strumia

● The CMSSM - after Higgs discovery

$$\gamma_i = \mu_0, m_0, m_{1/2}, A_0, B_0$$

$$v^2 = -\frac{m_{eff}^2}{\lambda_{eff}}$$



Relic density restricted $\left\{ \begin{array}{l} 1, 3, 4, 5 : \tilde{B} \\ 2 : \tilde{H} / \tilde{B} \end{array} \right.$

- 1 h^0 resonant annihilation
- 2 \tilde{h} t-channel exchange
- 3 $\tilde{\tau}$ co-annihilation
- 4 \tilde{t} co-annihilation
- 5 A^0 / H^0 resonant annihilation

Model	LHC & Higgs	weak DM	strong DM
CMSSM	134	216	276

† (requiring gauge coupling unification $\Delta \propto \log(M_{GUT}^2 / Q^2)$)

Cassel, Ghilencea, GGR

GGR, Schmidt-Hoberg, Staub

Soft parameters?

further

Fine tuning sensitive to \wedge correlations between them

$$\gamma_i = \mu_0, m_0, m_{1/2}, A_0, B_0$$

CMSSM


Focus point

$$Z_{h_u}^{m_{1/2}}(M_Z) \simeq 0 ?$$

$$m_{h_u}^2(Q) = z_{h_u}^{m_0}(Q)m_0^2 + z_{h_u}^{m_{1/2}}(Q)m_{1/2}^2 + z_{h_u}^{A_0}(Q)A_0^2 + 2z_{h_u}^{m_{1/2}A_0}(Q)m_{1/2}A_0$$

● Correlation between SUSY breaking parameters

...non-universal gaugino masses

$$16\pi^2 \frac{d}{dt} m_{H_u}^2 = 3 \left(2 |y_t|^2 (m_{H_u}^2 + m_{Q_3}^2 + m_{u_3}^2) + 2 |a_t|^2 \right) - 6g_2^2 |M_2|^2 - \frac{6}{5} g_1^2 |M_1|^2$$


New focus point: cancellation between M_3 and M_2 contributions if $|M_2|^2 \simeq |M_3|^2$ at M_{SUSY}
Abe, Kobayashi, Omura
Horton, GGR

(Also improves precision of gauge coupling unification)

Shifman, Roszkowski
Krippendorf, Nilles, Ratz, Winkler

Reduced fine tuning (the MSSM-NUGM)


$$16\pi^2 \frac{d}{dt} m_{H_u}^2 = 3 \left(2 |y_t|^2 (m_{H_u}^2 + m_{Q_3}^2 + m_{u_3}^2) + 2 |a_t|^2 \right) - 6g_2^2 |M_2|^2 - \frac{6}{5} g_1^2 |M_1|^2$$

New focus point: cancellation between M_3 and M_2 contributions if $|M_2|^2 \simeq |M_3|^2$ at M_{SUSY}

Abe, Kobayashi, Omura
Horton, GGR

Natural ratios? e.g.:

GUT: $SU(5): \Phi^N \subset (24 \times 24)_{\text{symm}} = 1 + 24 + 75 + 200; \quad SO(10): (45 \times 45)_{\text{symm}} = 1 + 54 + 210 + 770$



Representation	$M_3 : M_2 : M_1$ at M_{GUT}	$M_3 : M_2 : M_1$ at M_{EWSB}
1	1:1:1	6:2:1
24	2:(-3):(-1)	12:(-6):(-1)
75	1:3:(-5)	6:6:(-5)
200	1:2:10	6:4:10

Younkin, Martin

STRING:

$(3 + \delta_{GS}) : (-1 + \delta_{GS}) : \left(-\frac{33}{5} + \delta_{GS} \right) \quad \delta_{GS} \text{ quantised} \quad (\text{OII orbifold})$

Brignole, Ibanez, Munoz

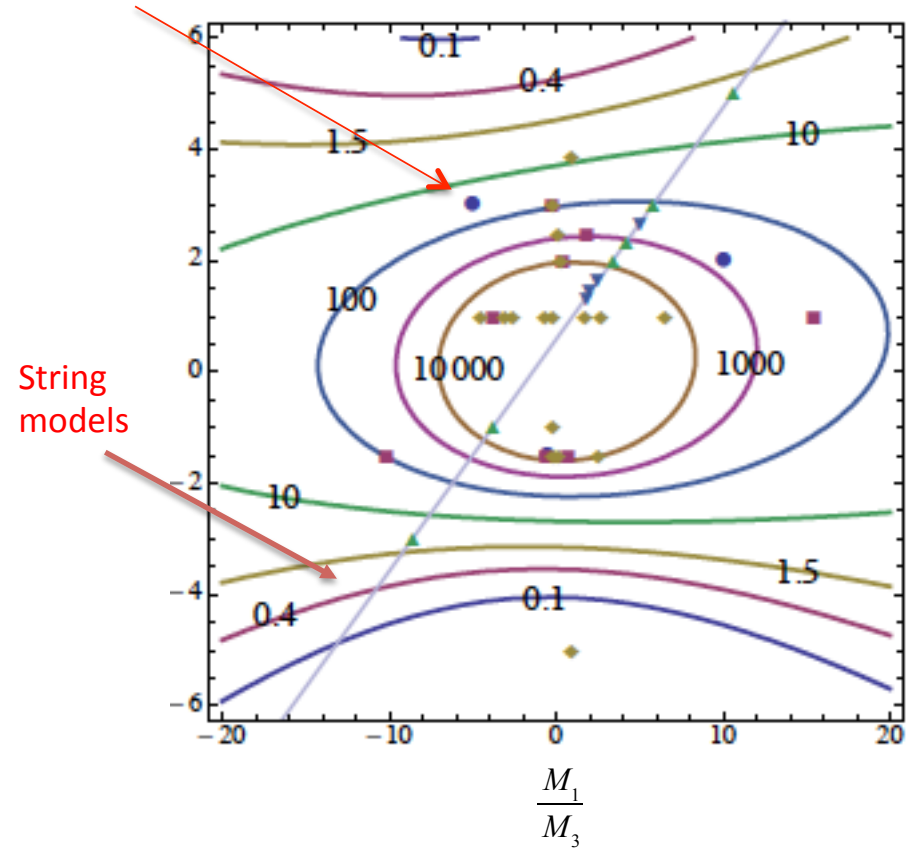
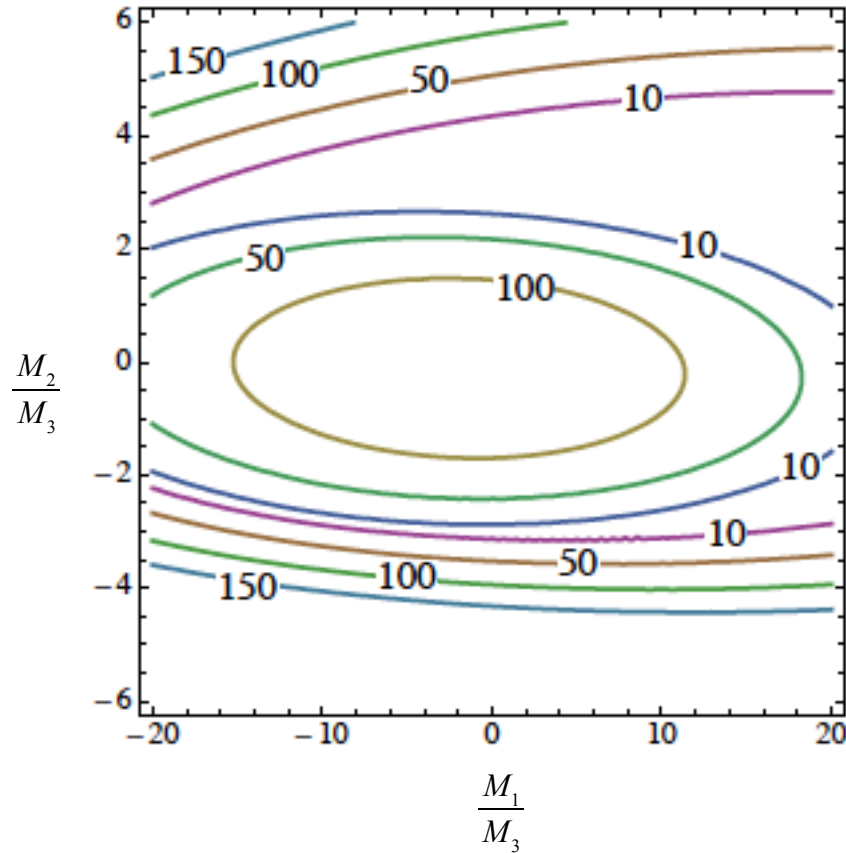
$M_a = m_{3/2} (\varrho + b_a g_a^2) \quad \rho \text{ quantised} \quad (\text{mixed moduli+anomaly..})$

Choi, Nilles
Badzick, Krippendorf,
Nilles, Winkler
Choi, Jeong, Okumura
...

..mirage, orbifold mini landscape, KKLT in IIB, hidden sector superpotentials)

Δ
 $SU(5):75$

Focus point (TeV)



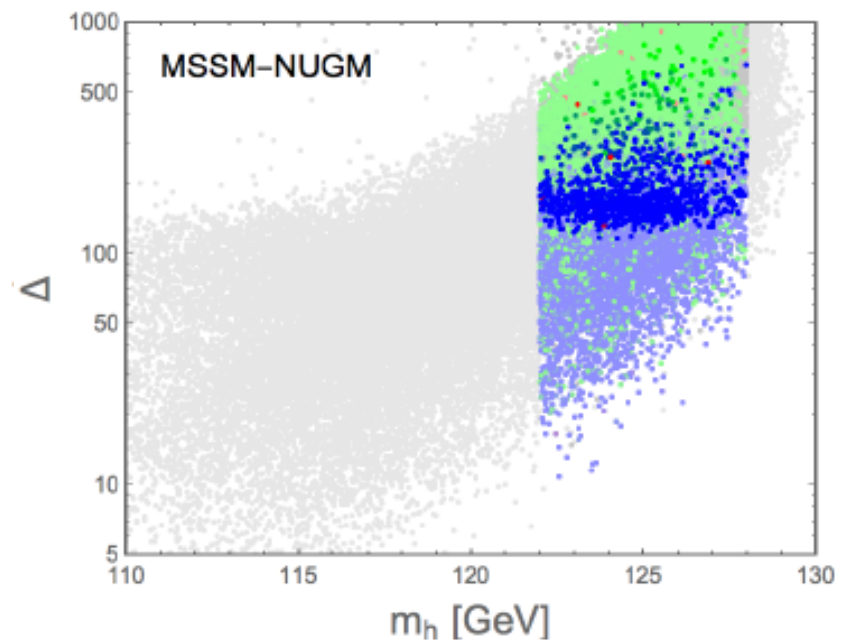
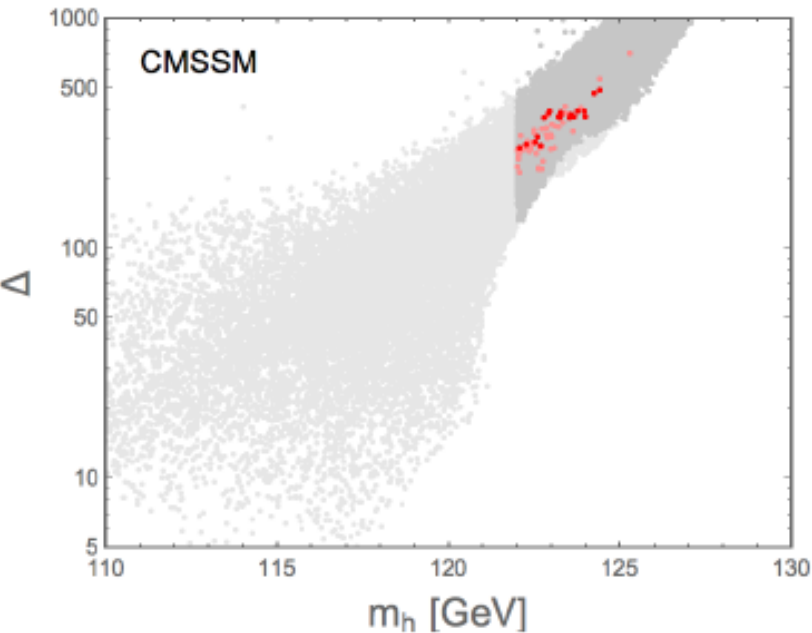
$$16\pi^2 \frac{d}{dt} m_{H_u}^2 = 3 \left(2 |y_t|^2 (m_{H_u}^2 + m_{Q_3}^2 + m_{u_3}^2) + 2 |a_t|^2 \right) - 6g_2^2 |M_2|^2 - \frac{6}{5} g_1^2 |M_1|^2$$

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Fine tuning -effect of gaugino focus point

LHC 13 TeV

$\delta m_h = \pm 3 \text{ GeV} \rightarrow \pm 1 \text{ GeV}$ at high scales $\Delta m_h = -2 \text{ GeV}$



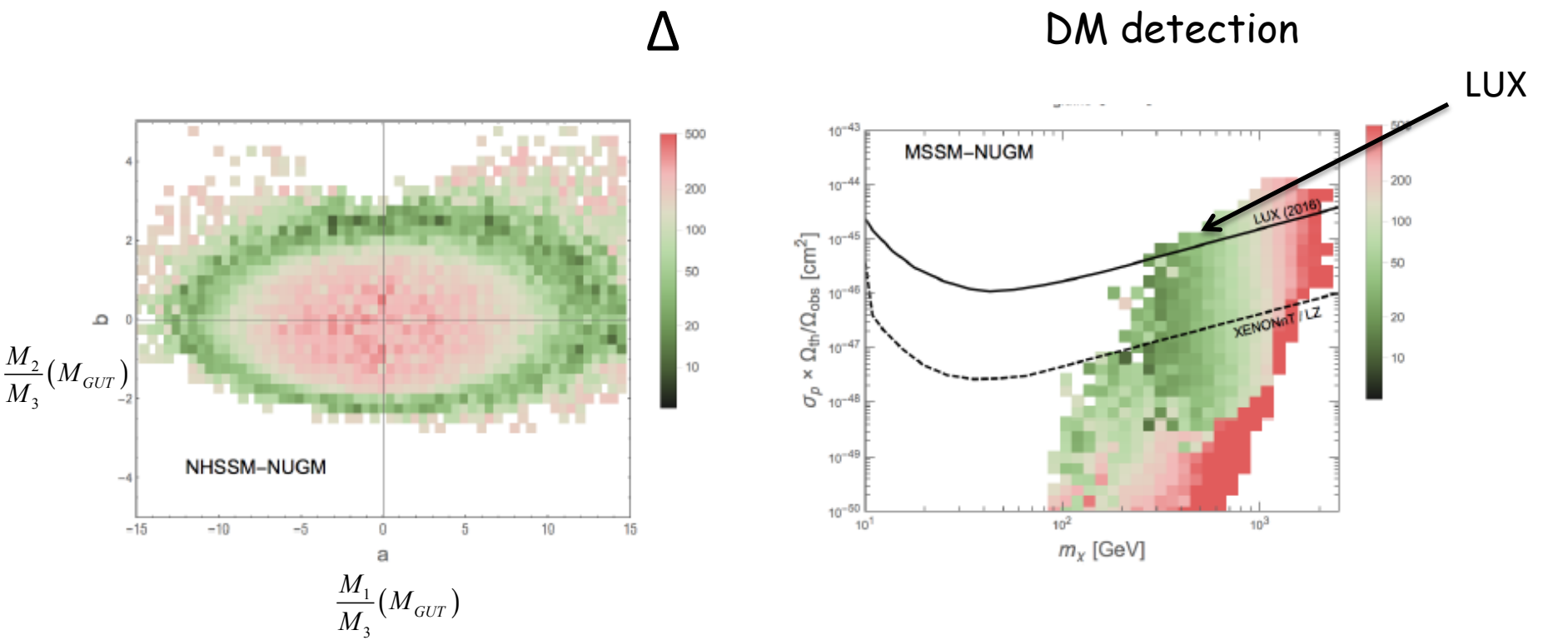
$\bullet \tilde{B}$
 $\bullet \tilde{H}$
 $\bullet \tilde{W}$

CMSSM

MSSM-NUGM

<i>Model</i>	<i>LHC & Higgs</i>	<i>weak DM</i>	<i>strong DM</i>
<i>CMSSM</i>	136	216	276
<i>MSSM – NUGM</i>	11	11	117

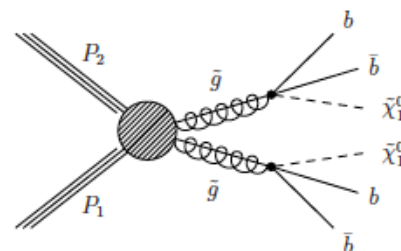
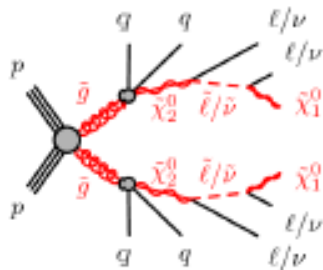
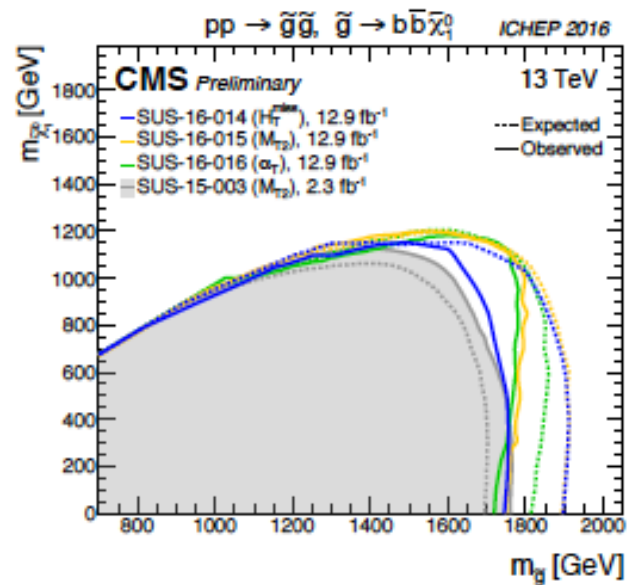
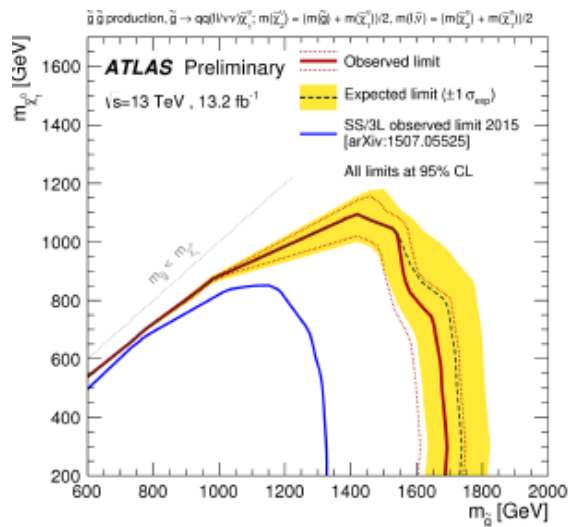
Fine tuning -effect of gaugino focus point LHC 13 TeV



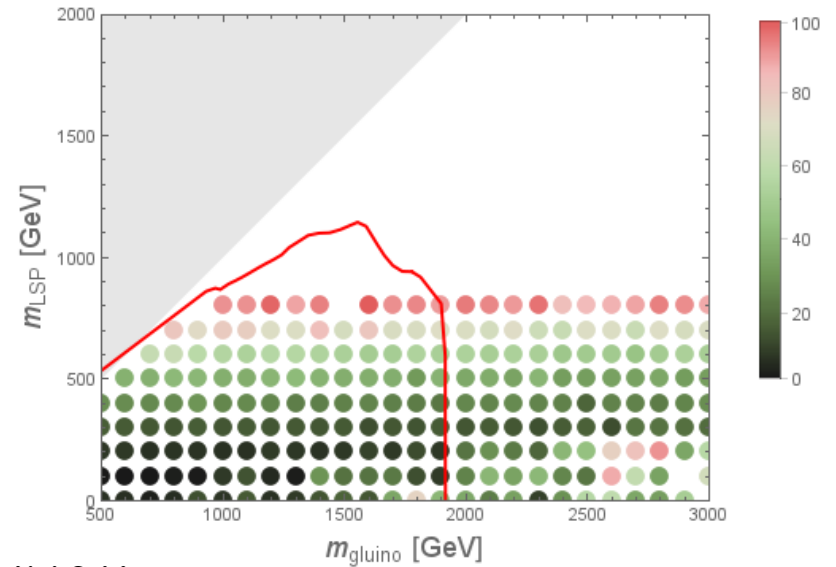
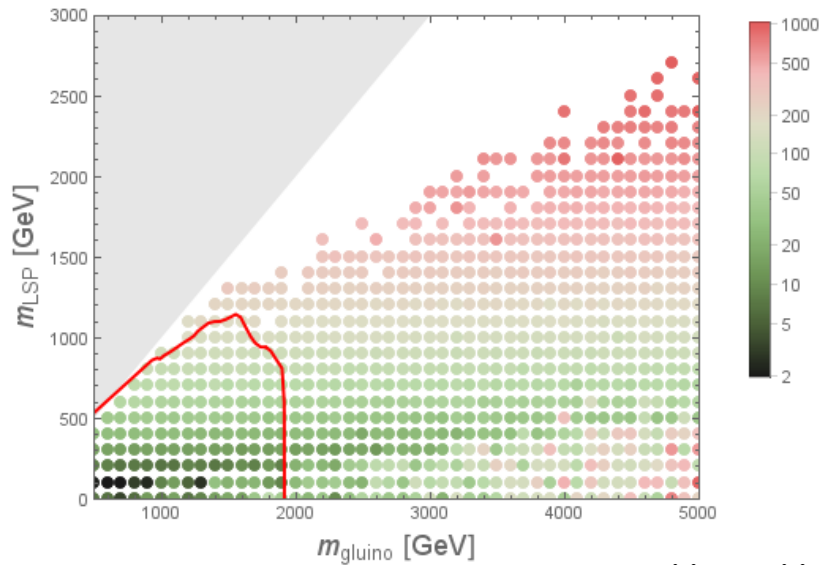
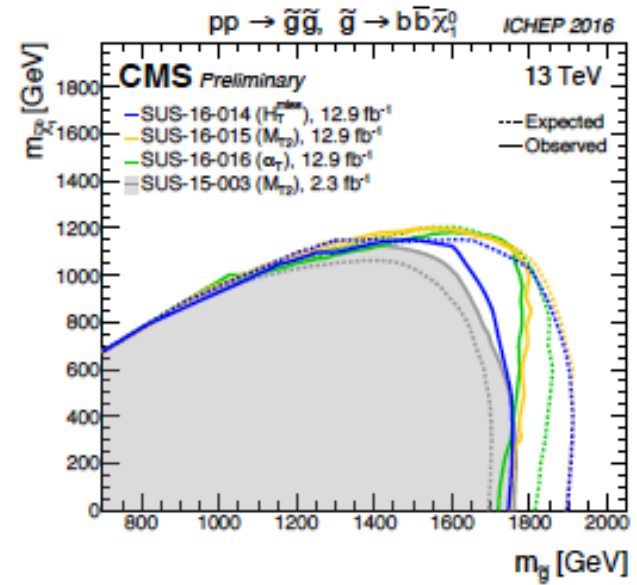
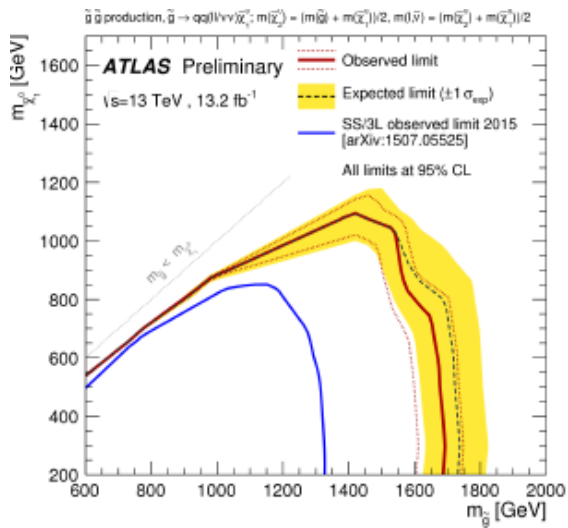
MSSM-NUGM

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LHC 13 TeV

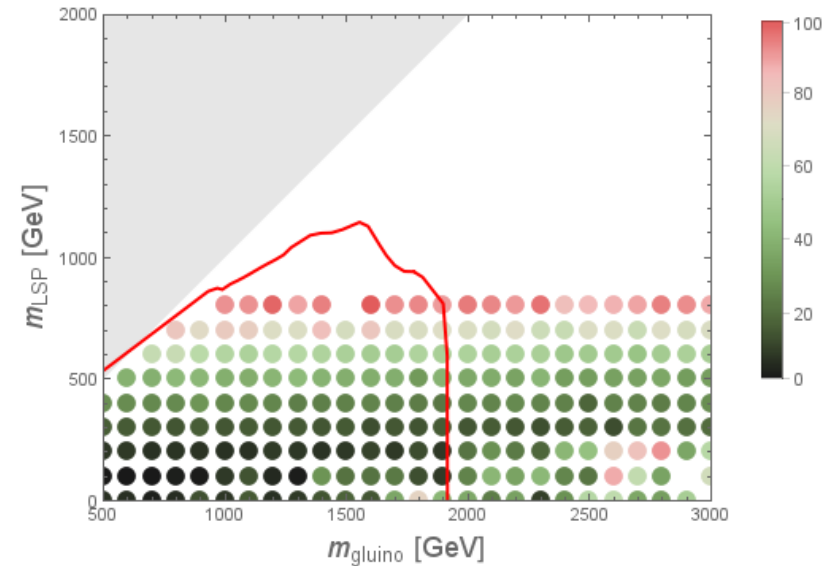
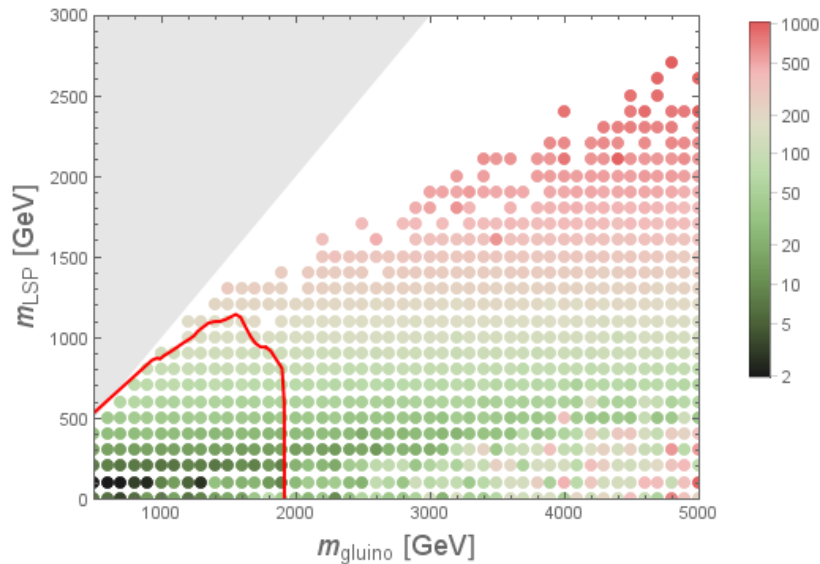
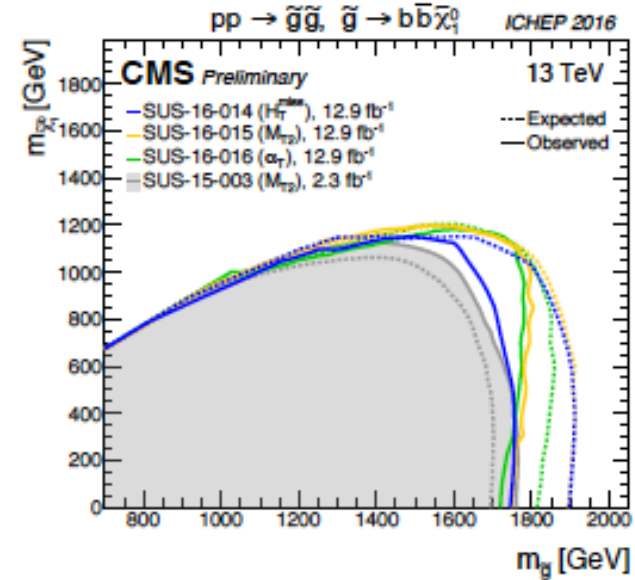
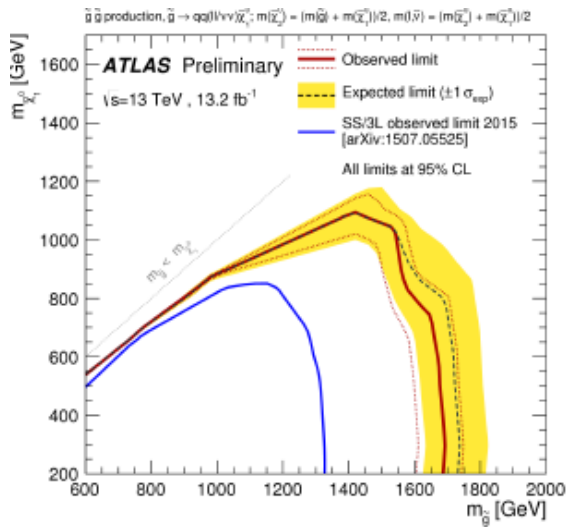


LHC 13 TeV



MSSM-NUGM

LHC 13 TeV

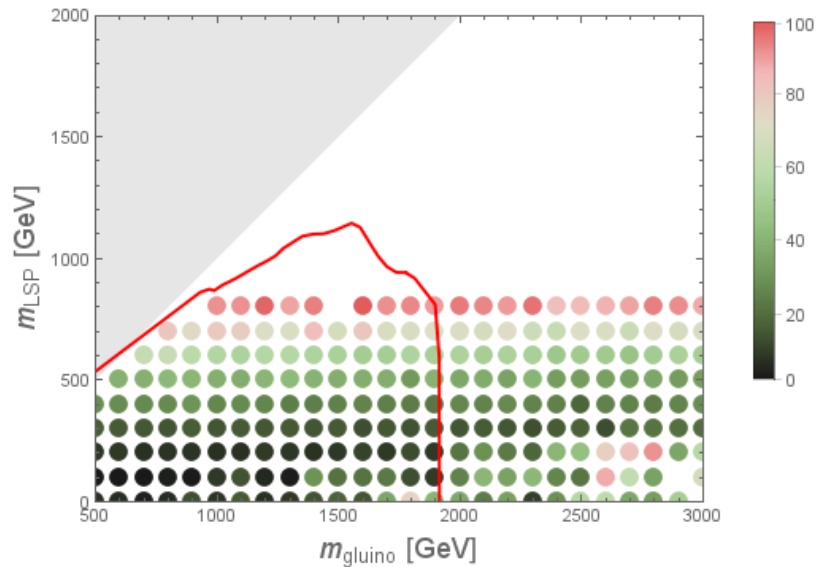
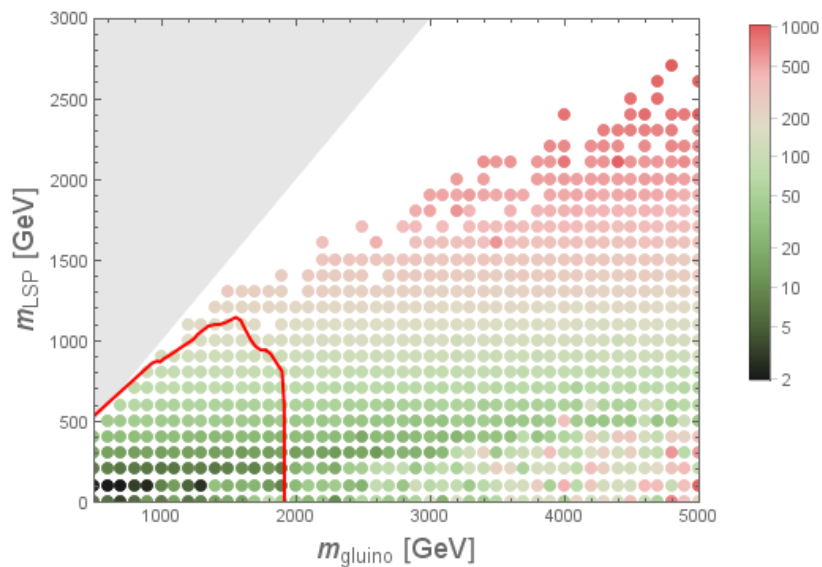
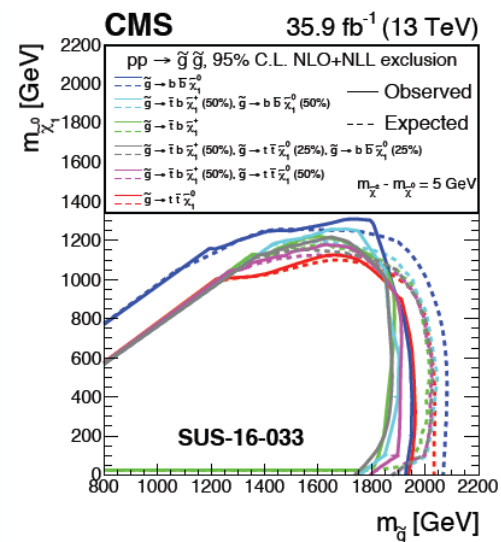
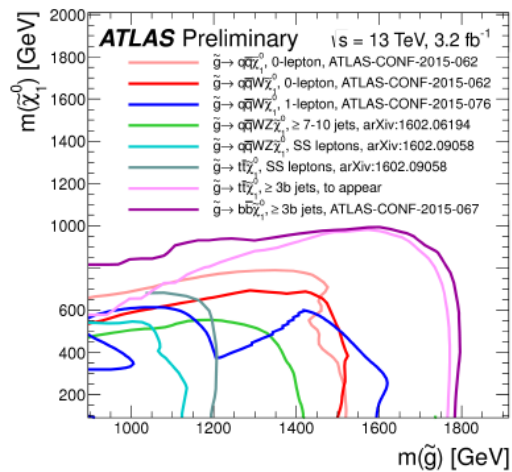


MSSM-NUGM

(Two-scale matching summing $\ln(M_{\text{SUSY}}/M_Z, M_h)$ can reduce Δ by further factor 2 and $\delta m_h = -2\text{ GeV}$)

Porod, Staub

LHC 13 TeV



MSSM-NUGM

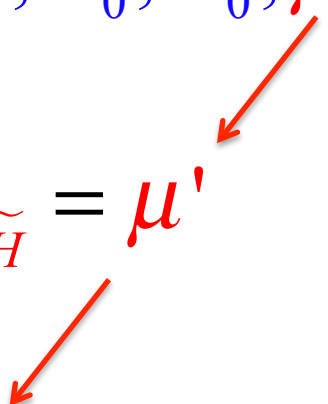
Soft parameters?

(No divergences introduced)

Fine tuning sensitive to correlations between them

$$\gamma_i = \mu, m_0, m_{1/2}, A_0, B_0, \mu'$$

Soft Higgsino mass?

$$m_H = 0, m_{\tilde{H}} = \mu'$$


Hard parameter - tadpole divergences

(Absent in MSSM)

Higgsino mass origin

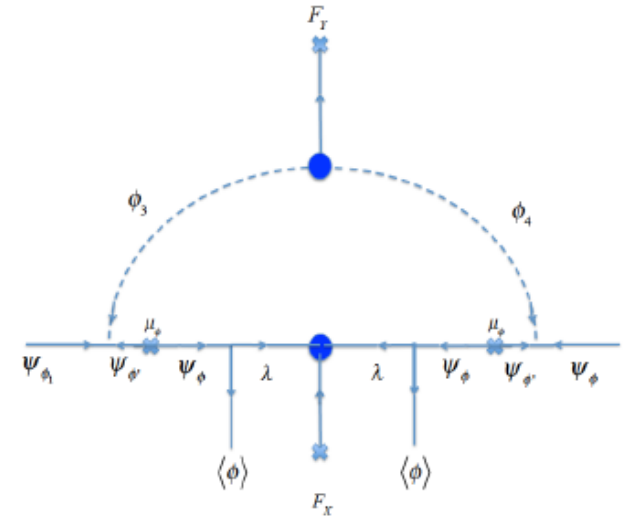
(c.f. Scherk-Schwarz ...low compactification scale)

Garcia-Garcia, Howe, March Russell
Delgado, Garcia-Pepin, Quiros
Dimopoulos, Howe, March-Russell

● Gaugino mediation

$$\int d^4\theta XX^\dagger \bar{D}_\alpha (\Phi_1^\dagger e^V) \bar{D}^\alpha e^{-V} \Phi_2^\dagger$$

$$m_{\psi_{\phi_1}\psi_{\phi_2}} \propto \frac{\mu_\phi^2 \langle \phi \rangle^2 F_Y F_X}{M^7}$$



Martin;
GGR, Schmidt-Hoberg, Staub

● Sequestering

Hidden sector running drives Higgs mass to zero leaving Higgsino mass unchanged

Perez, Roy, Schmaltz

$$\Rightarrow \mu_0 H_u H_d |_{\theta\theta} - \mu_0^2 \left(|H_u|^2 + |H_d|^2 \right)$$

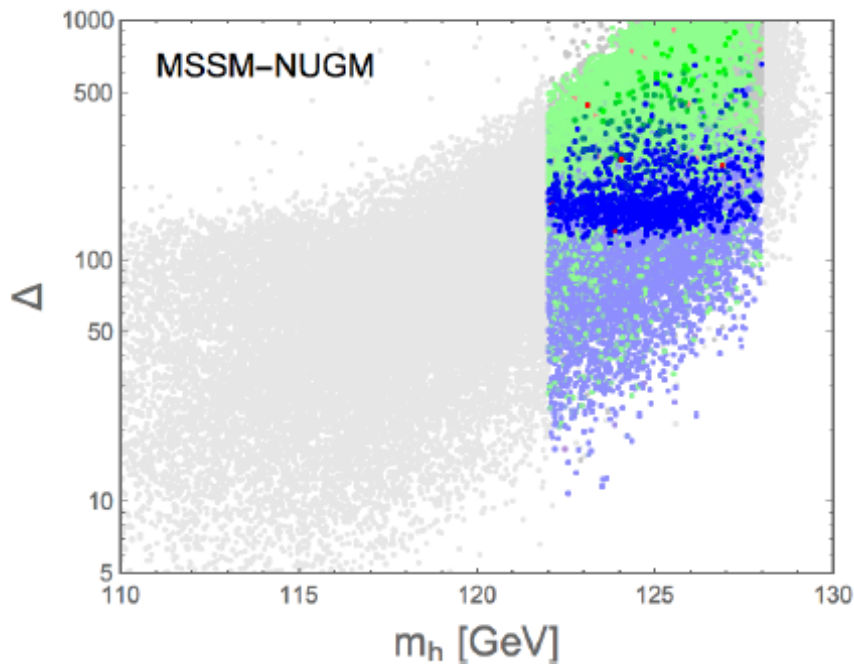
“Soft” even with singlets

• New SUSY breaking soft terms

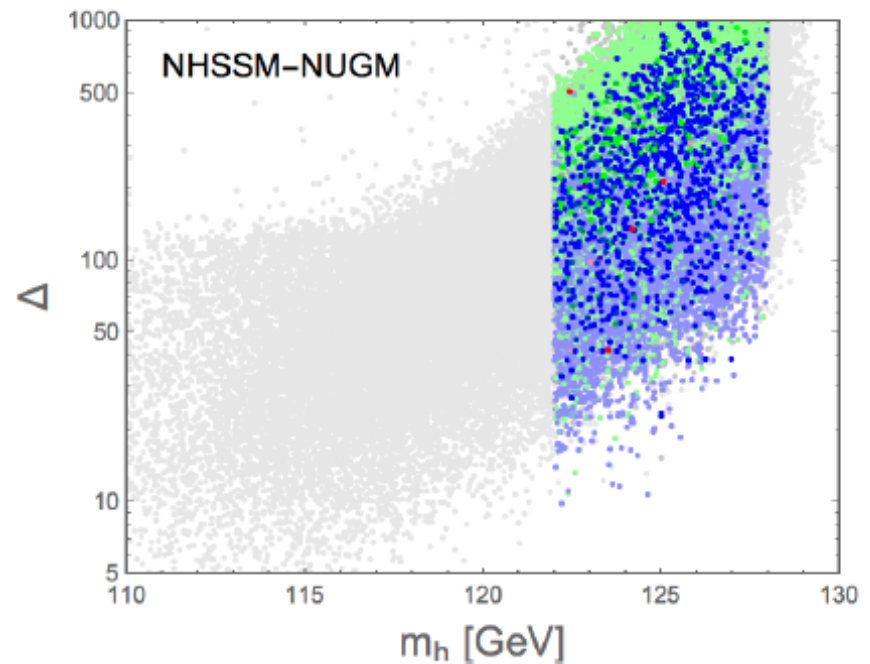
$m_0, m_{1/2}, A_0, \tan \beta, \mu, B\mu, \mu'$

$$\mathcal{L}_{NH} = T'_{u,ij} H_d^* \tilde{u}_{R,i}^* \tilde{q}_j + T'_{d,ij} H_u^* \tilde{d}_{R,i}^* \tilde{q}_j + T'_{e,ij} H_u^* \tilde{e}_{R,i}^* \tilde{l}_j + \underline{\mu' \tilde{H}_d \tilde{H}_u} + \text{h.c.}$$

$+\mu'$



MSSM-NUGM



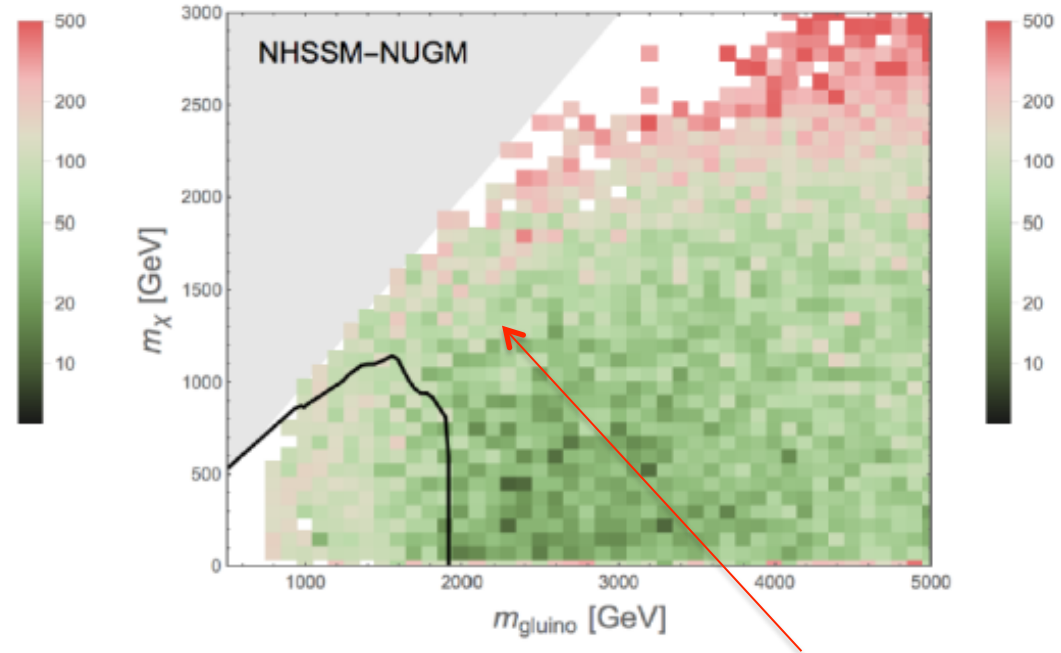
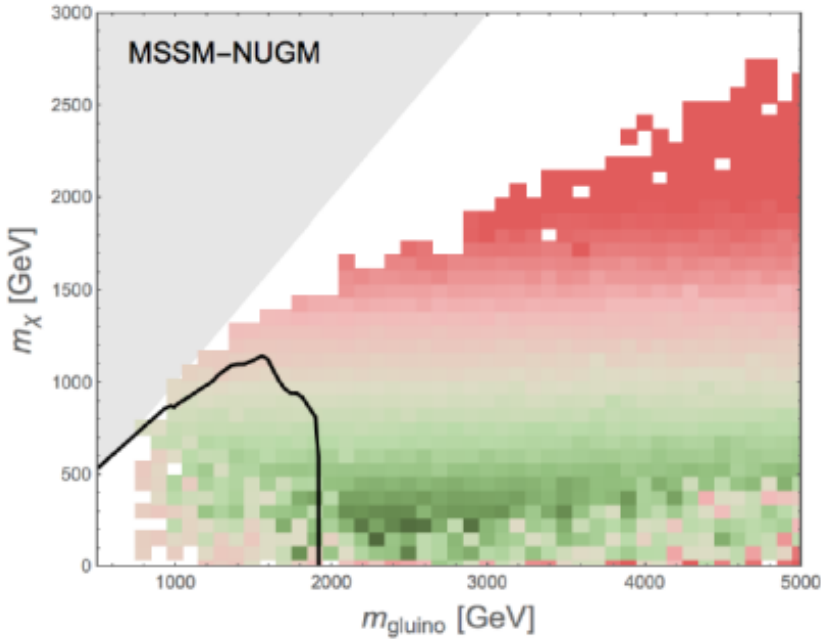
NHMSSM-NUGM

SUSY DM

$\bullet \tilde{B}$
 $\bullet \tilde{H}$
 $\bullet \tilde{W}$

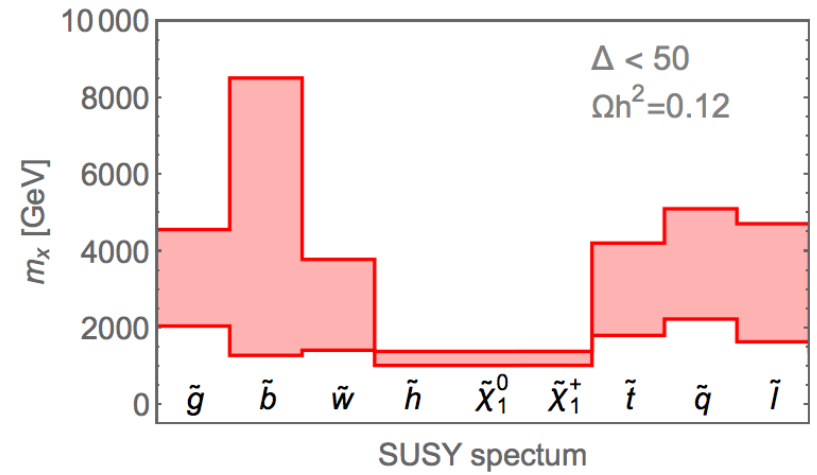
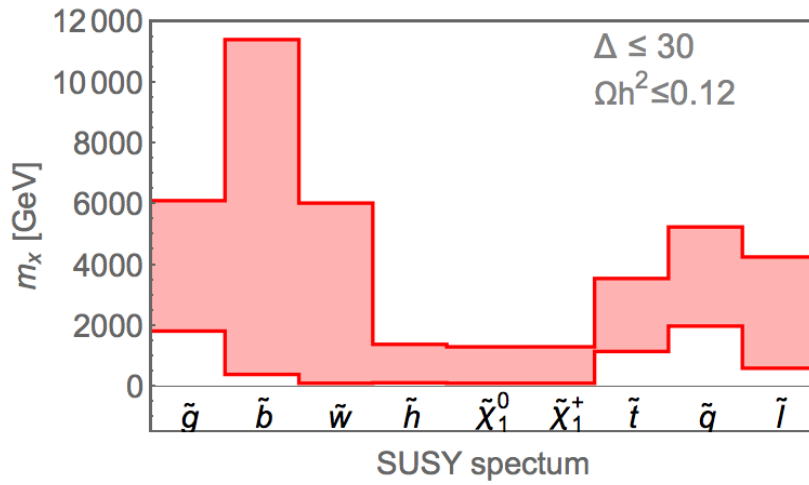
MSSM-NUGM

$+\mu'$



<i>Model</i>	<i>LHC & Higgs</i>	<i>weak DM</i>	<i>strong DM</i>
<i>MSSM – NUGM</i>	11	11	117
<i>NHSSM – NUGM</i>	10	10	23

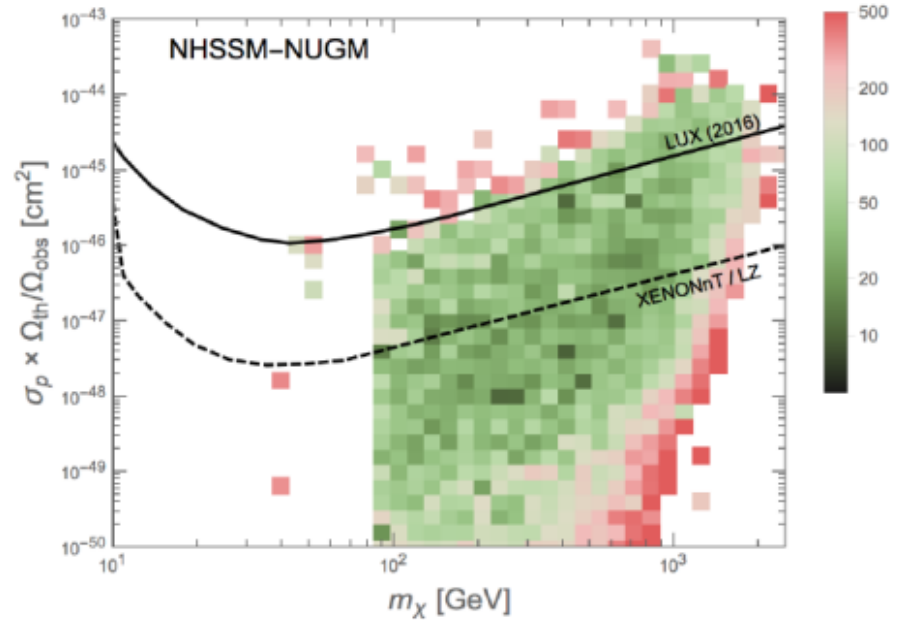
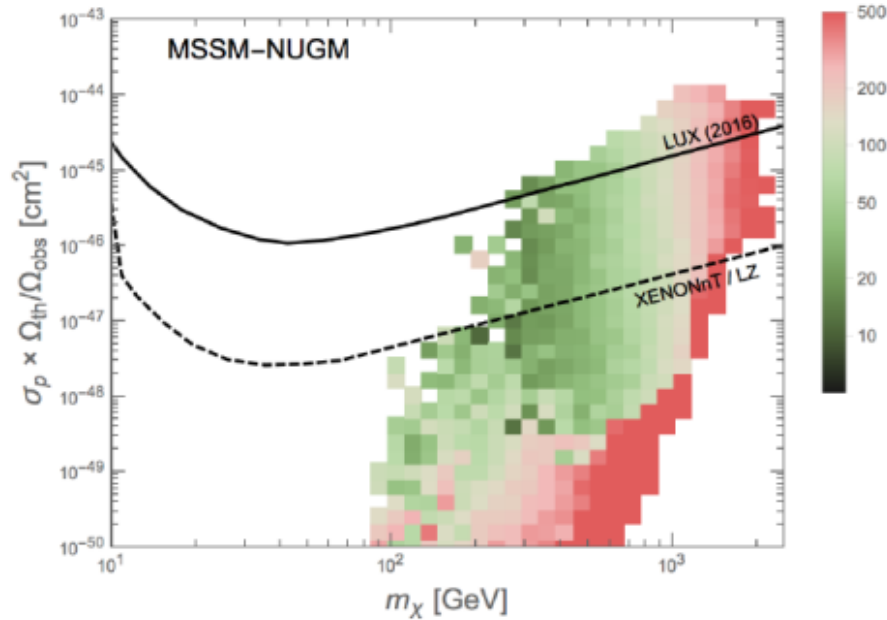
Spectrum



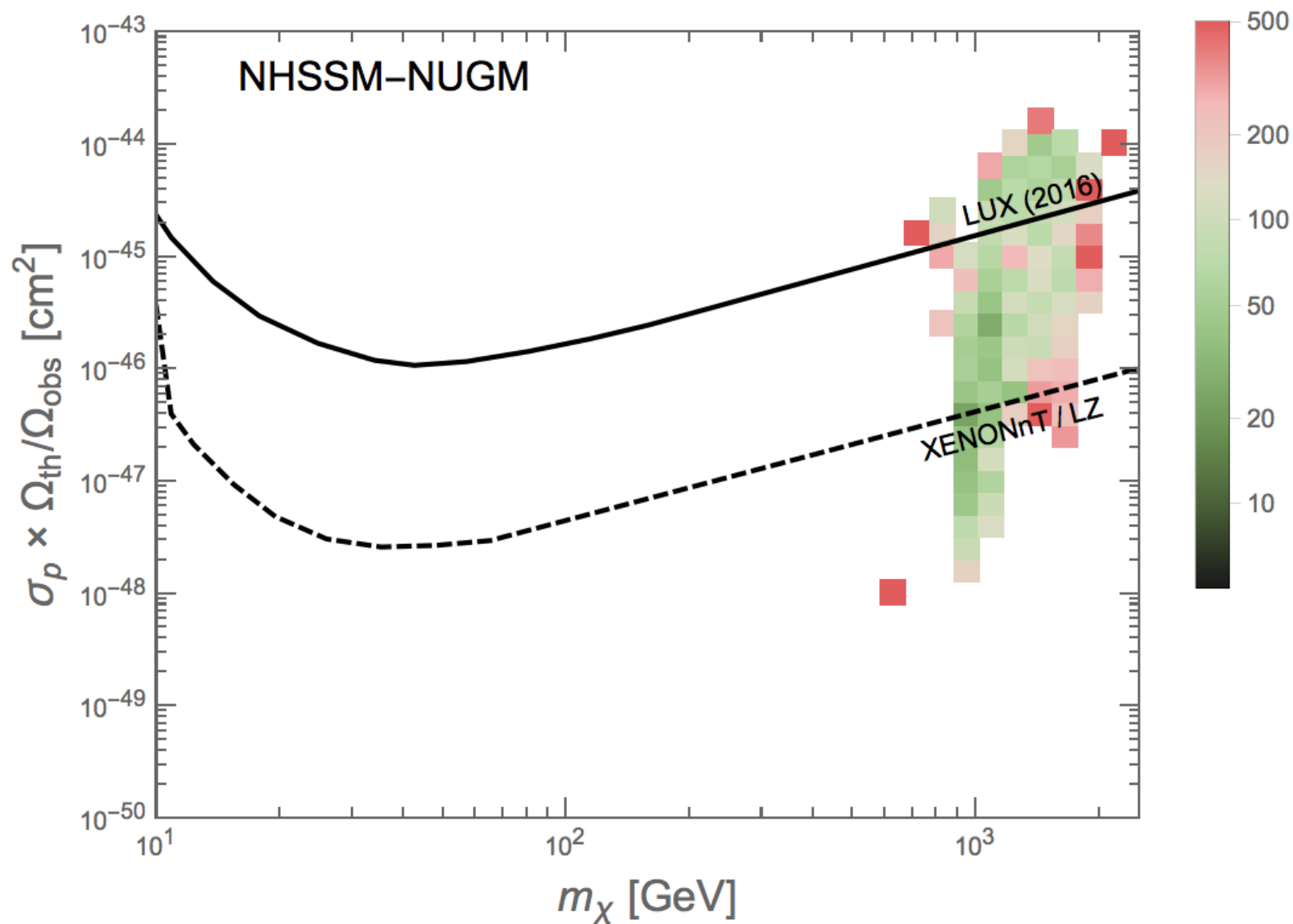
$m_{\tilde{H}} \sim 1\text{TeV}$

<i>Model</i>	<i>LHC & Higgs</i>	<i>weak DM</i>	<i>strong DM</i>
<i>MSSM – NUGM</i>	11	11	117
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Dark Matter



Thermal SUSY DM



SUMMARY

● GUTs \Rightarrow SUSY-GUTS (hierarchy problem)

SUMMARY

- GUTs \Rightarrow SUSY-GUTS (hierarchy problem)
- Fine tuning sensitive to SUSY spectrum
...scalar and gaugino focus points, Higgsino mass

<i>Model</i>	<i>LHC & Higgs</i>	<i>soft DM</i>	<i>strong DM</i>
<i>CMSSM</i>	134	216	276
<i>MSSM – NUGM</i>	11	11	117
<i>CNHSSM</i>	114	116	166
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... and non-minimal spectrum

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$$W = W_{Yukawa} + (\mu + \lambda S) H_u H_d + \frac{\mu_s}{2} S^2 + \frac{\kappa}{3} S^3 + \xi S \quad GNMSSM$$

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low energy

- Is \wedge SUSY alive ?

Yes (just) - Well motivated SUSY models remain to be tested

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low energy

- Is \wedge SUSY alive ?

Can LHC fully test it?

Prospects:

CMSSM							
	current			prospects			
Cut	LHC & Higgs	soft DM	strong DM	$m_{\tilde{g}} \geq 3 \text{ TeV}$	DD	$m_{\tilde{g}} \geq 5 \text{ TeV}$	DD
Δ_{\min}	134	216	276	231	271	686	-
CNHSSM							
	current			prospects			
Cut	LHC & Higgs	soft DM	strong DM	$m_{\tilde{g}} \geq 3 \text{ TeV}$	DD	$m_{\tilde{g}} \geq 5 \text{ TeV}$	DD
Δ_{\min}	114	116	166	227	264	665	677
MSSM-NUGM							
	current			prospects			
Cut	LHC & Higgs	soft DM	strong DM	$m_{\tilde{g}} \geq 3 \text{ TeV}$	DD	$m_{\tilde{g}} \geq 5 \text{ TeV}$	DD
Δ_{\min}	11	11	117	17	17	29	29
NHSSM-NUGM							
	current			prospects			
Cut	LHC & Higgs	soft DM	strong DM	$m_{\tilde{g}} \geq 3 \text{ TeV}$	DD	$m_{\tilde{g}} \geq 5 \text{ TeV}$	DD
Δ_{\min}	10	10	23	11	11	23	23

(DD: Direct detection DM)

Thermal SUSY DM

