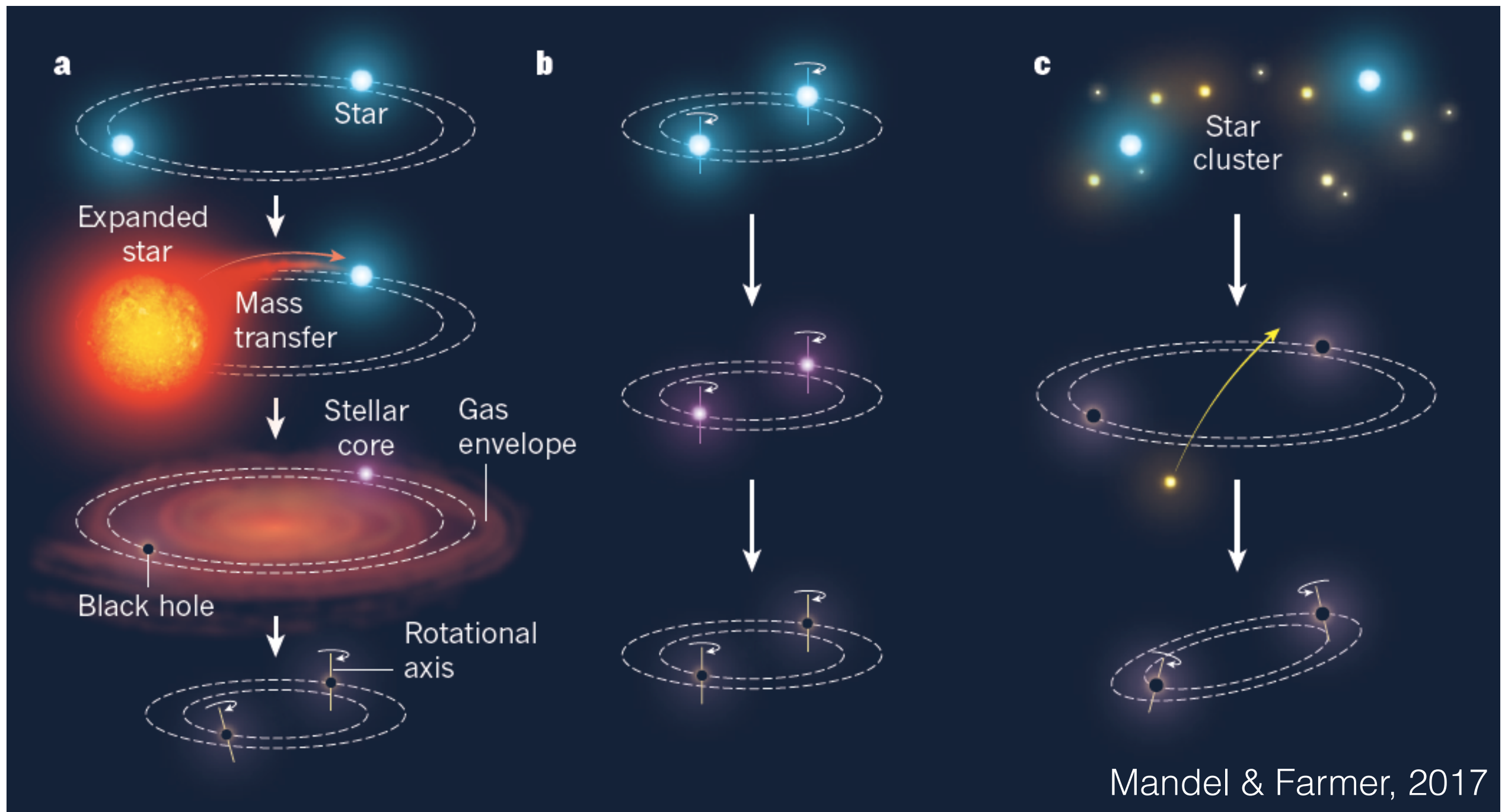
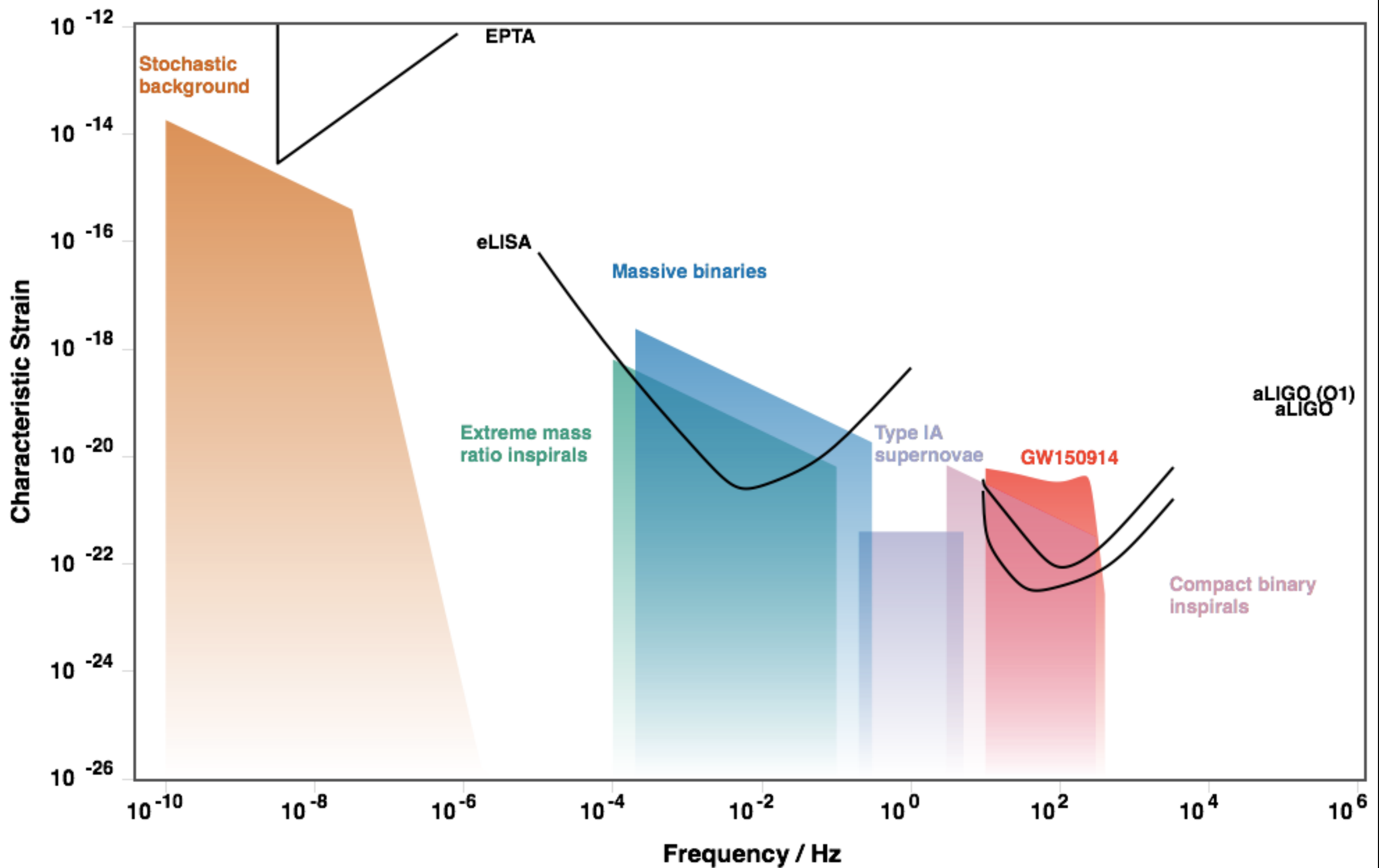


Astrophysical sources of GWs and future prospects for their detection

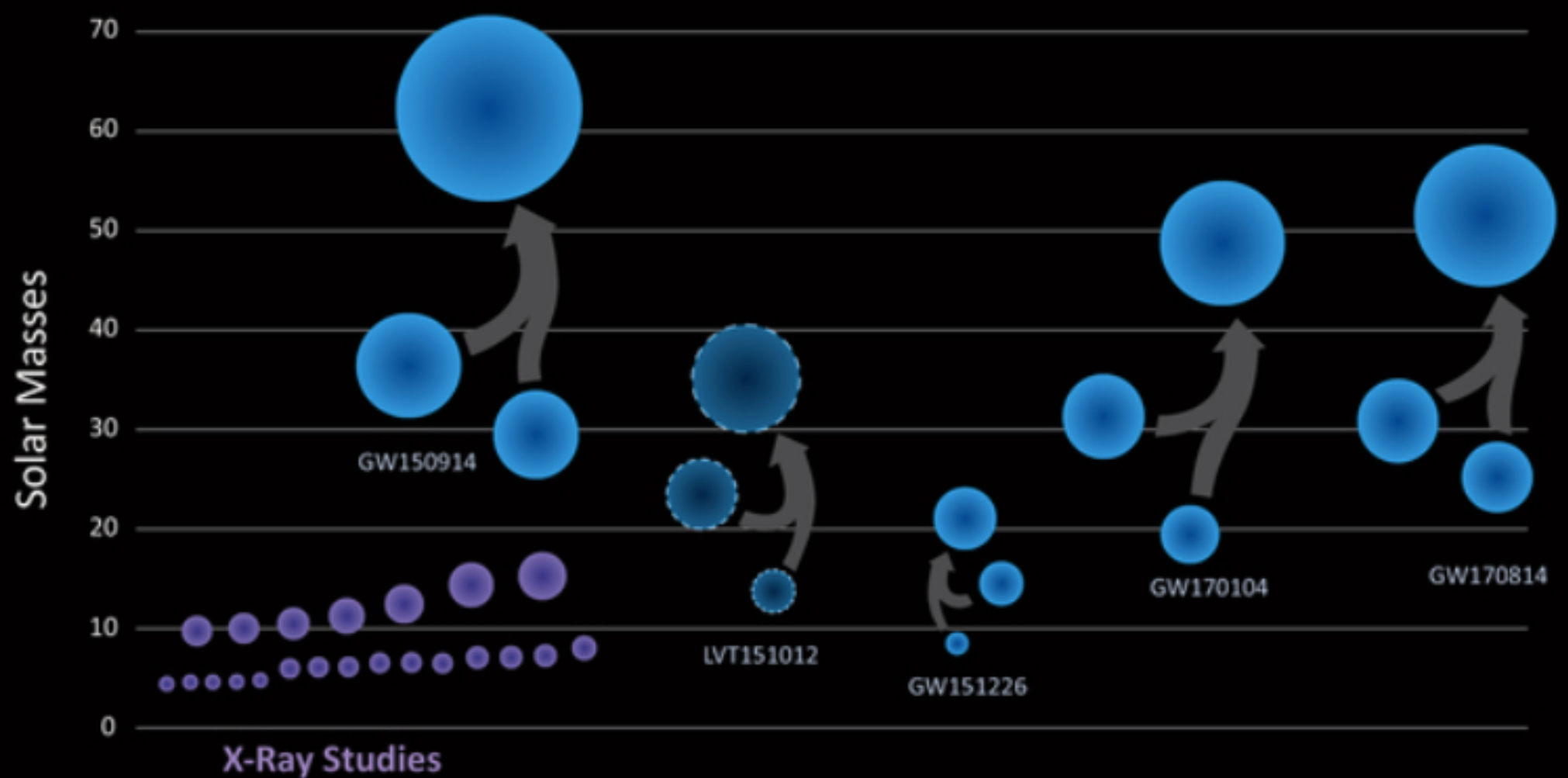


Ilya Mandel
University of Birmingham



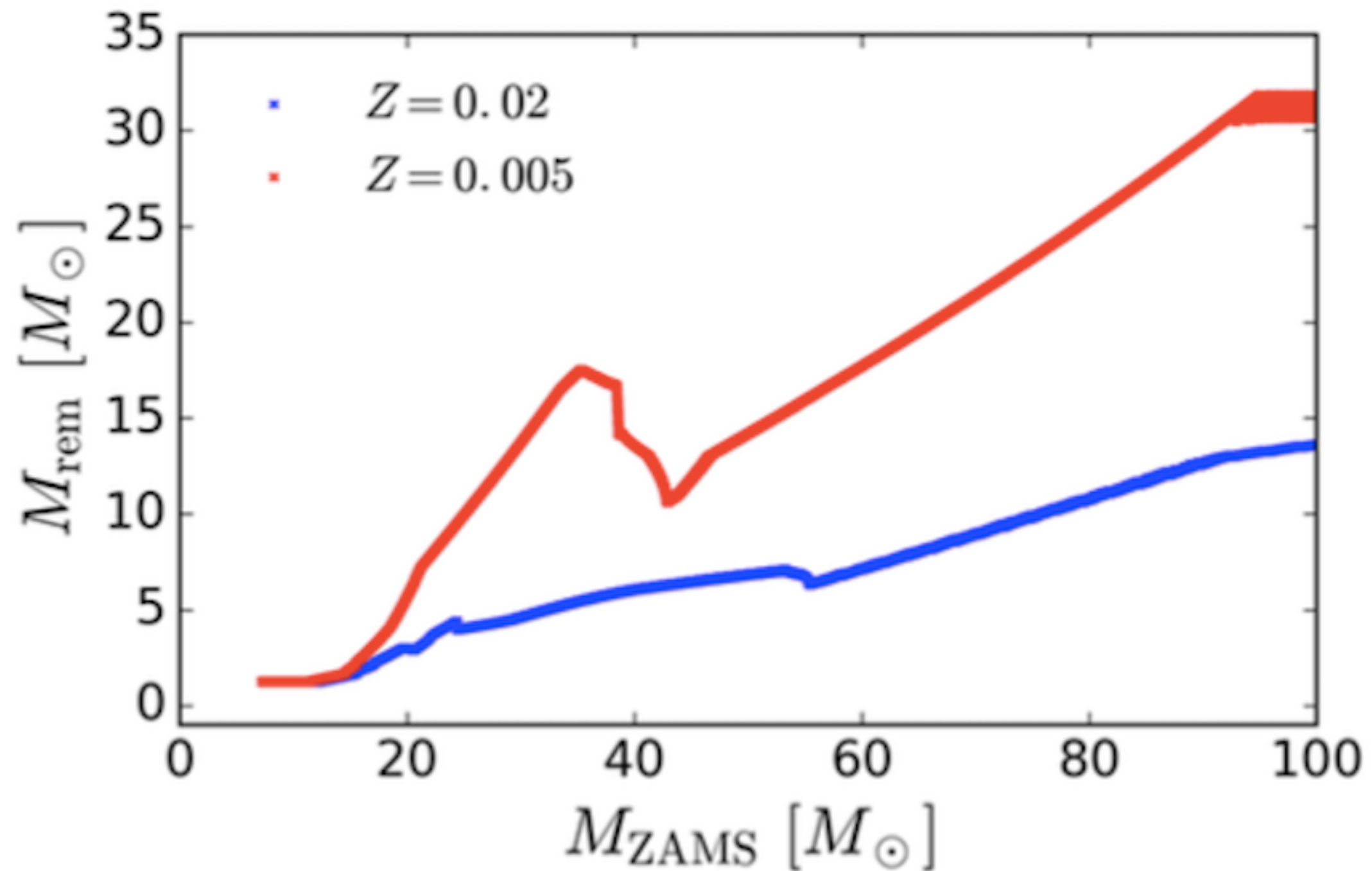
The mass problem

Black Holes of Known Mass

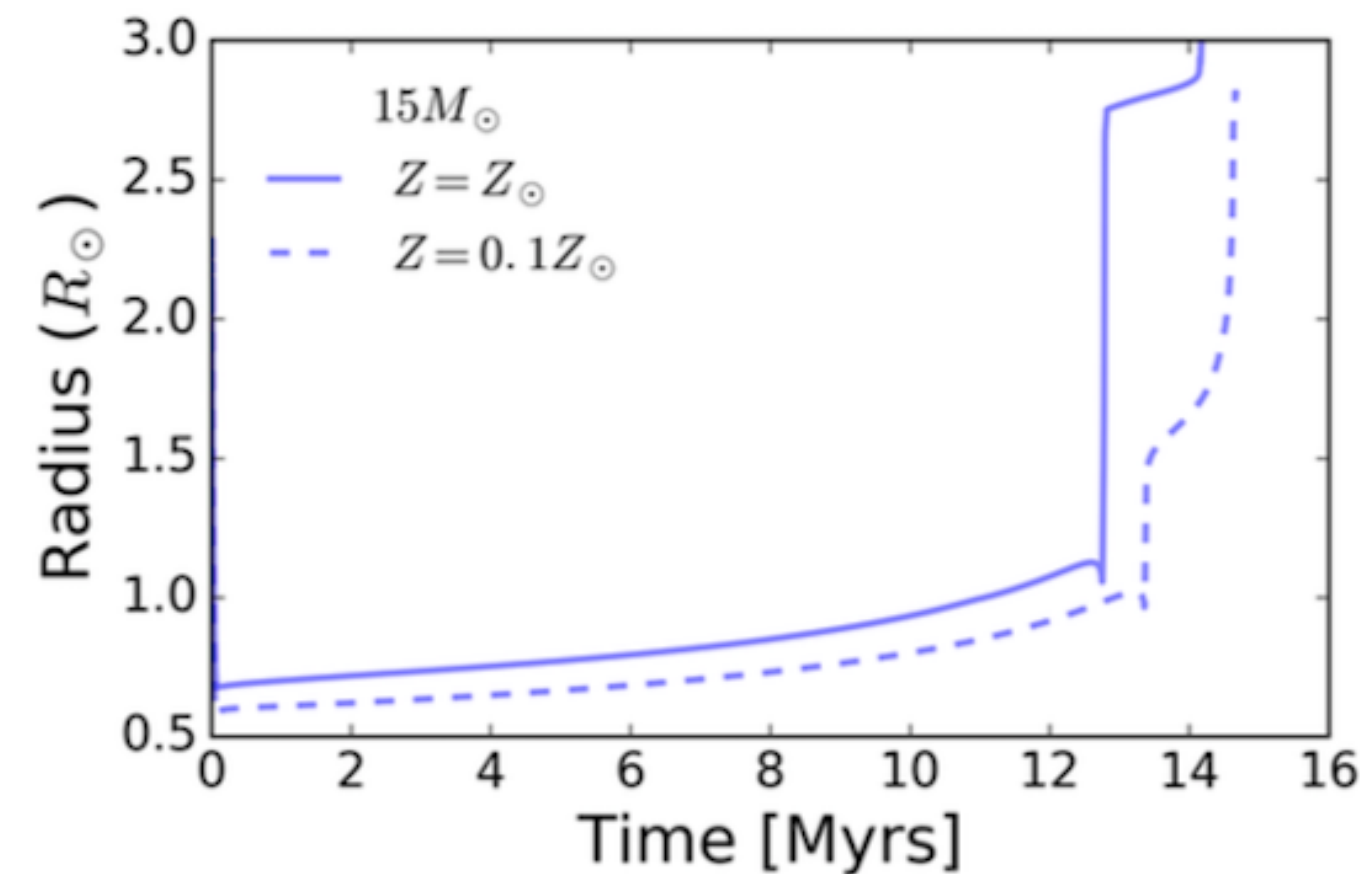


LIGO/VIRGO

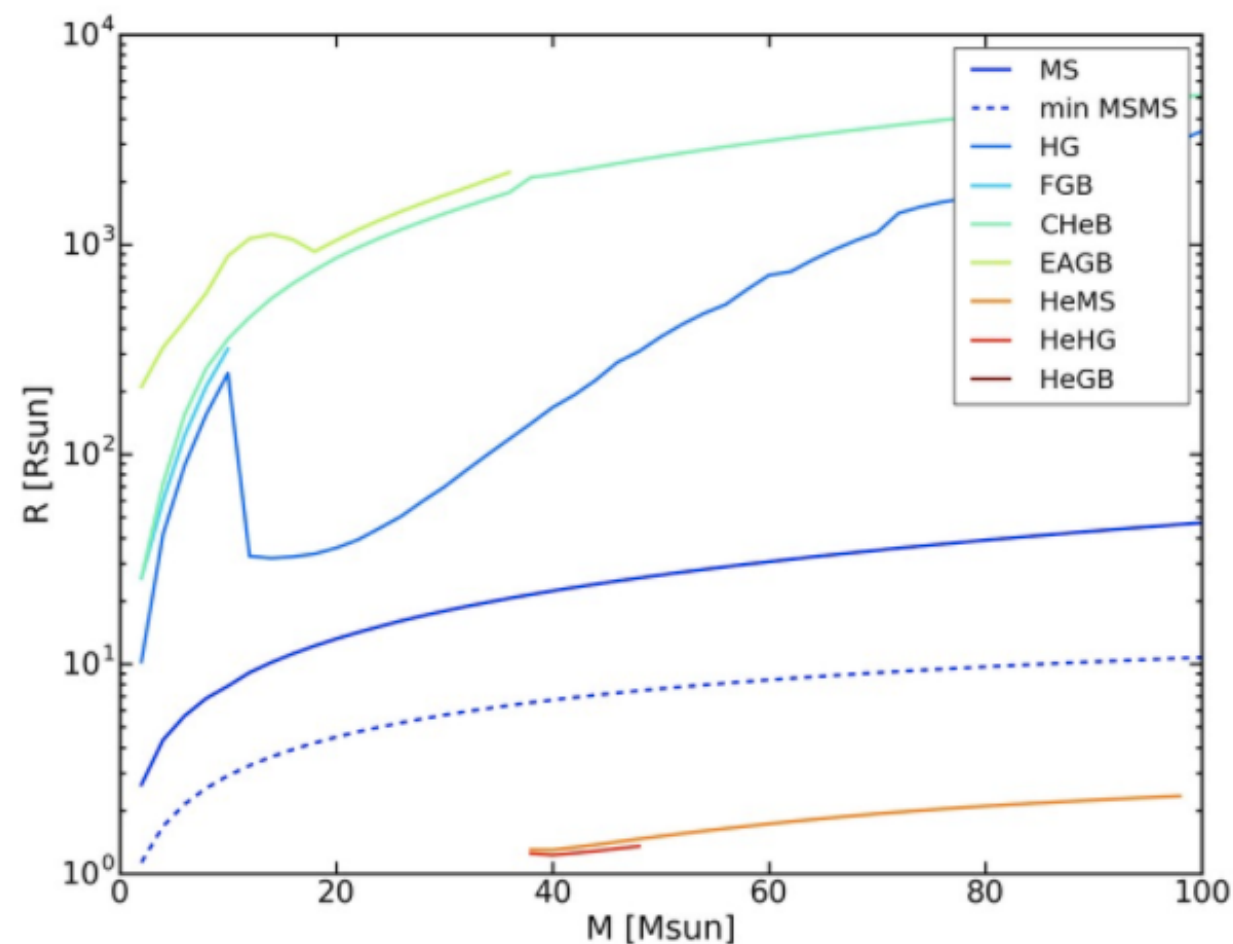
The mass problem



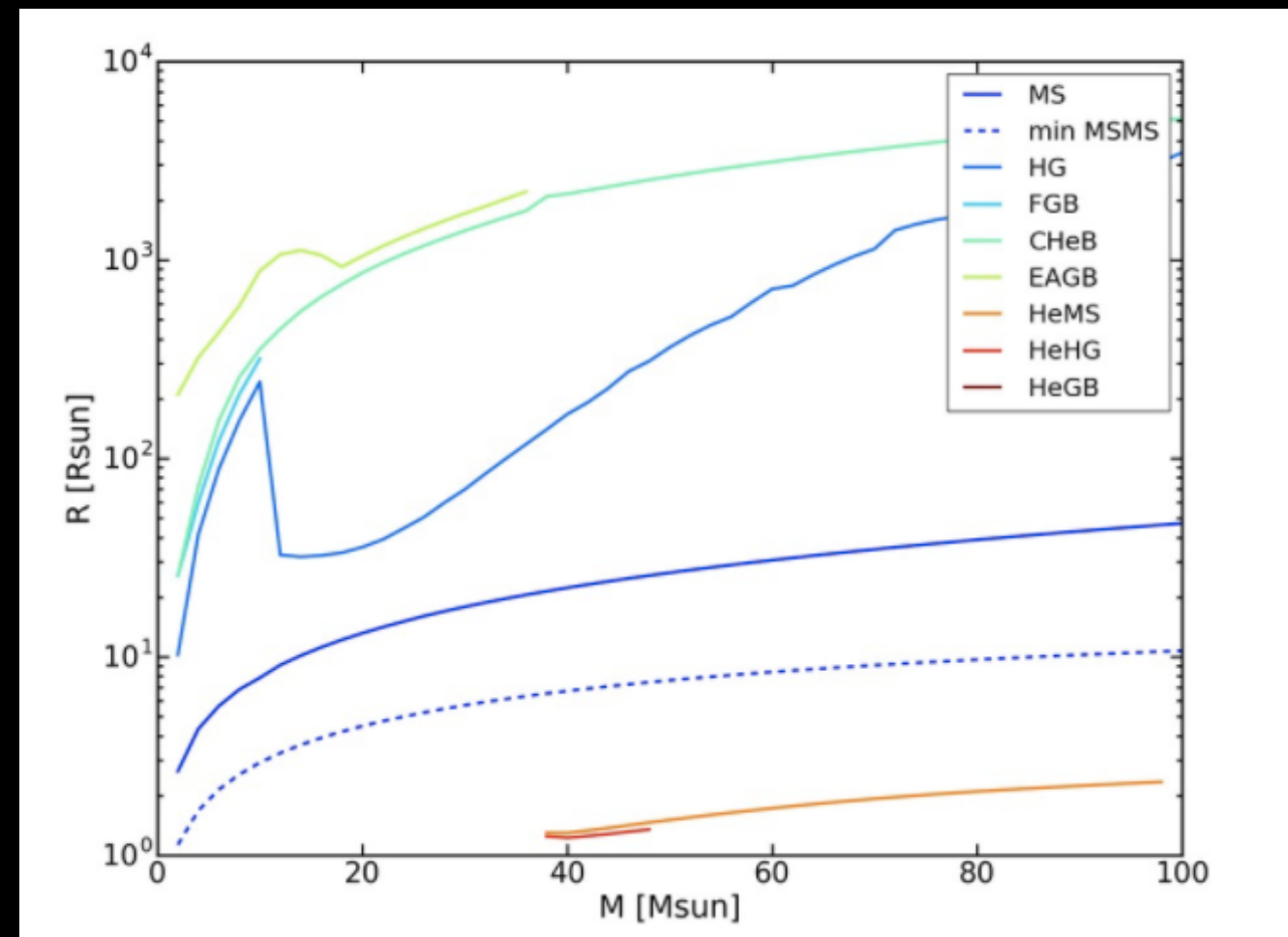
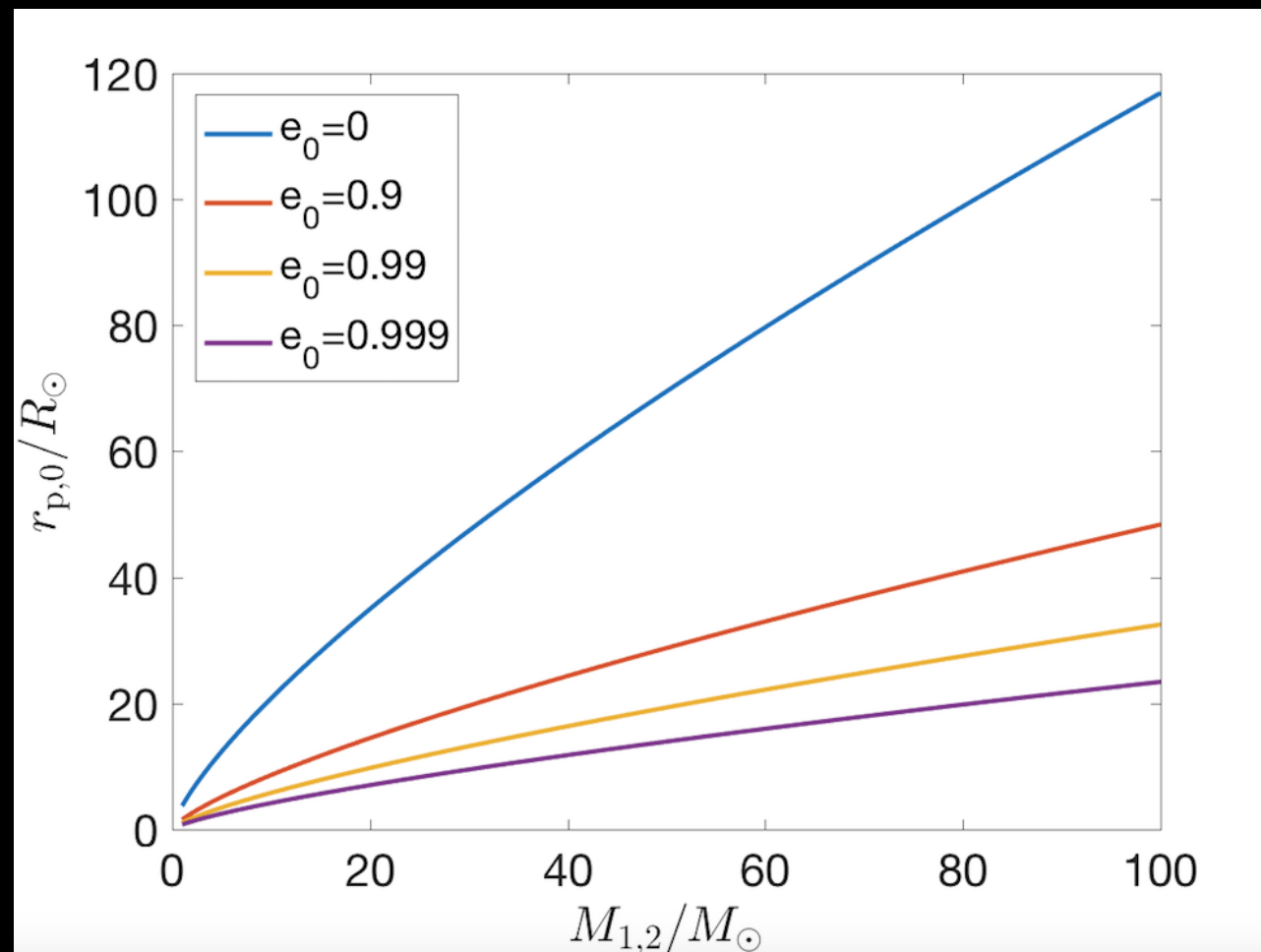
The separation problem



based on Hurley+, 2000

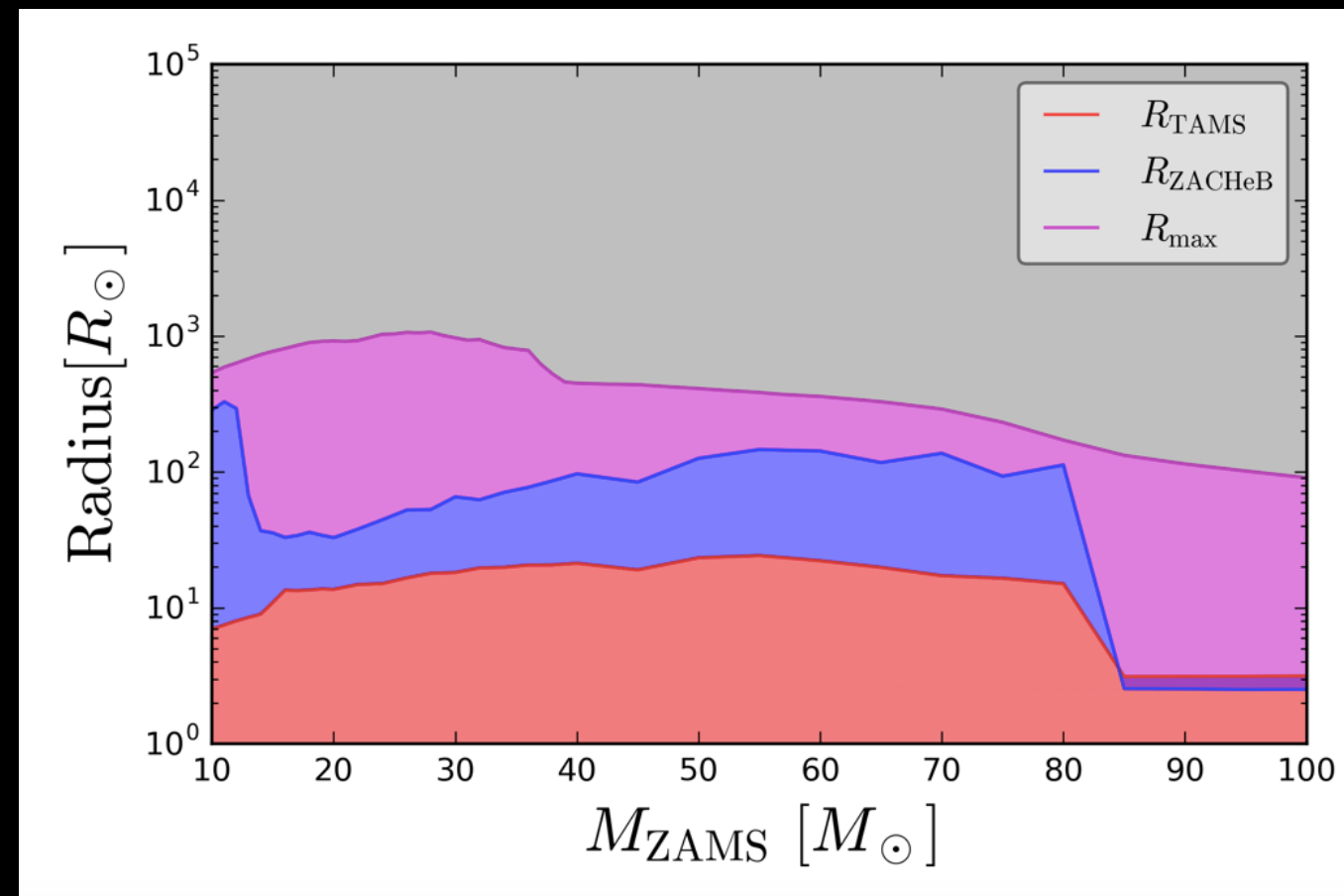
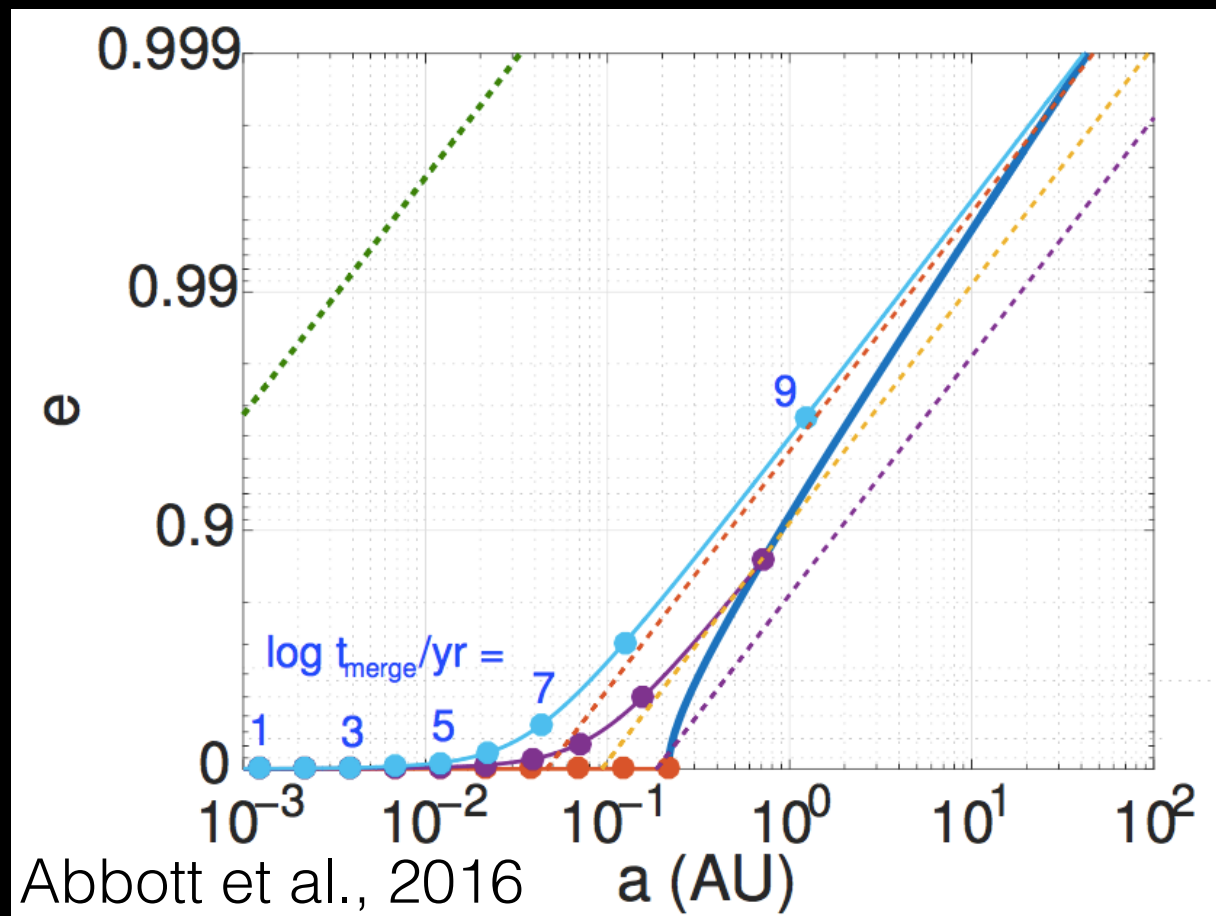


The separation problem



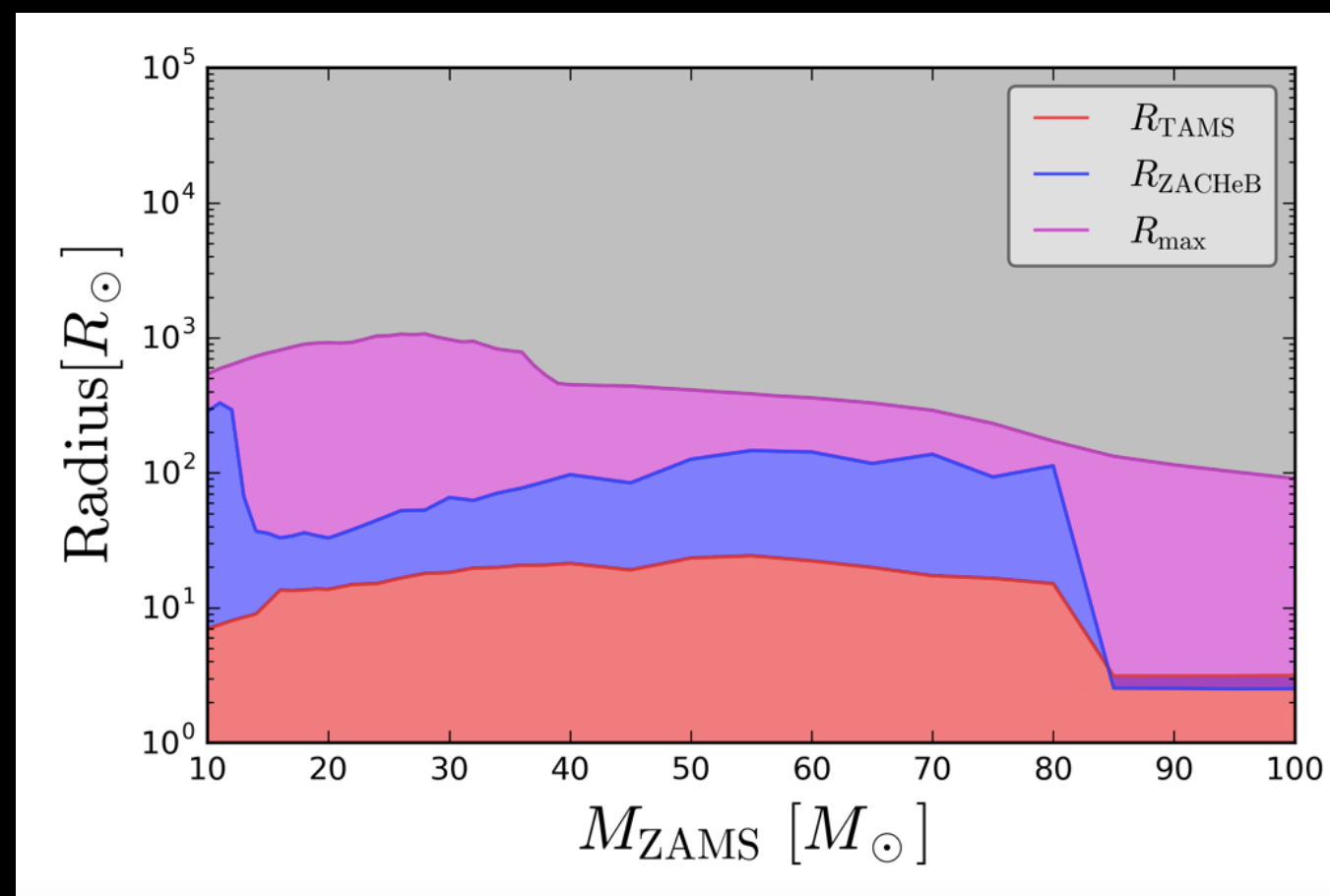
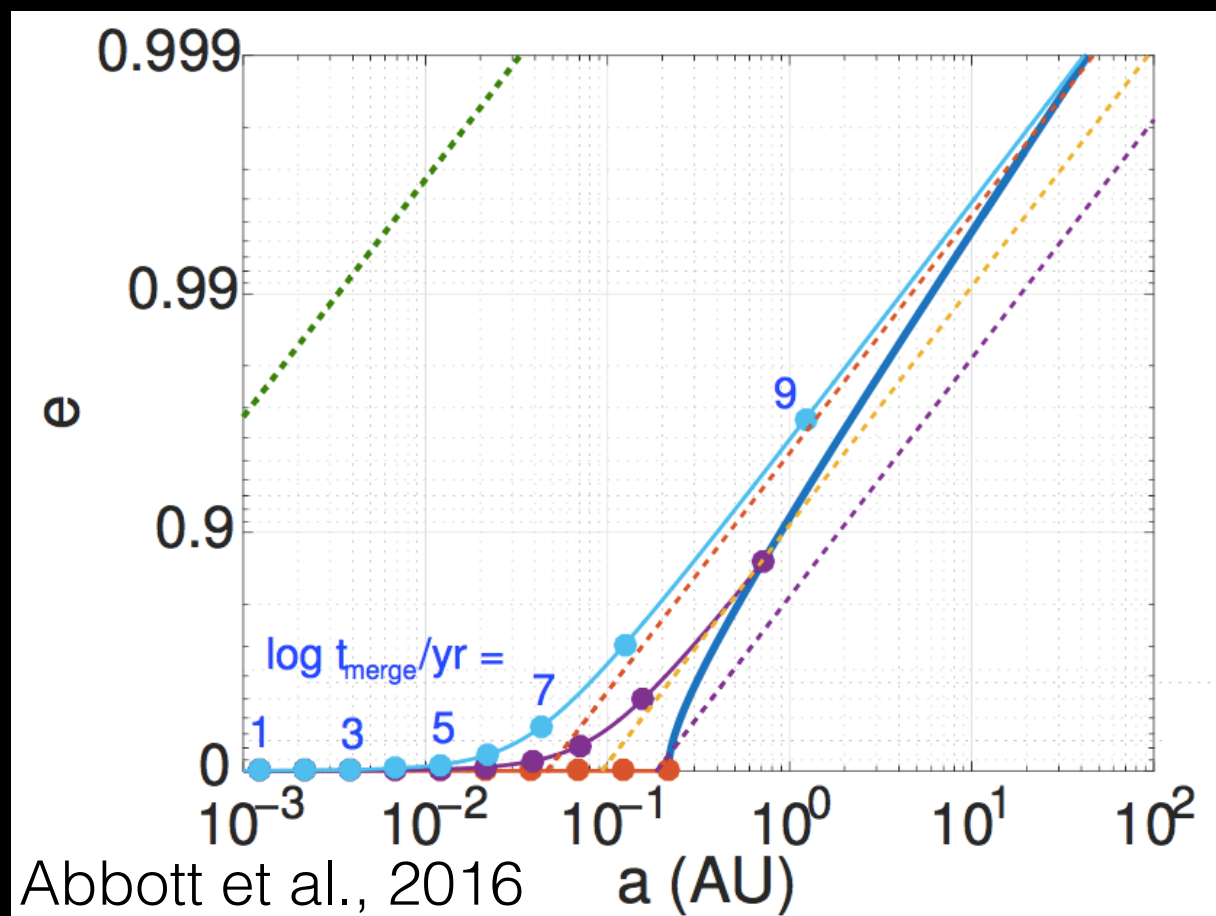
Mandel, in prep.

The separation problem



- Harden the binary after stars evolved
- Don't let stars expand
- Let stars evolve before they make a binary

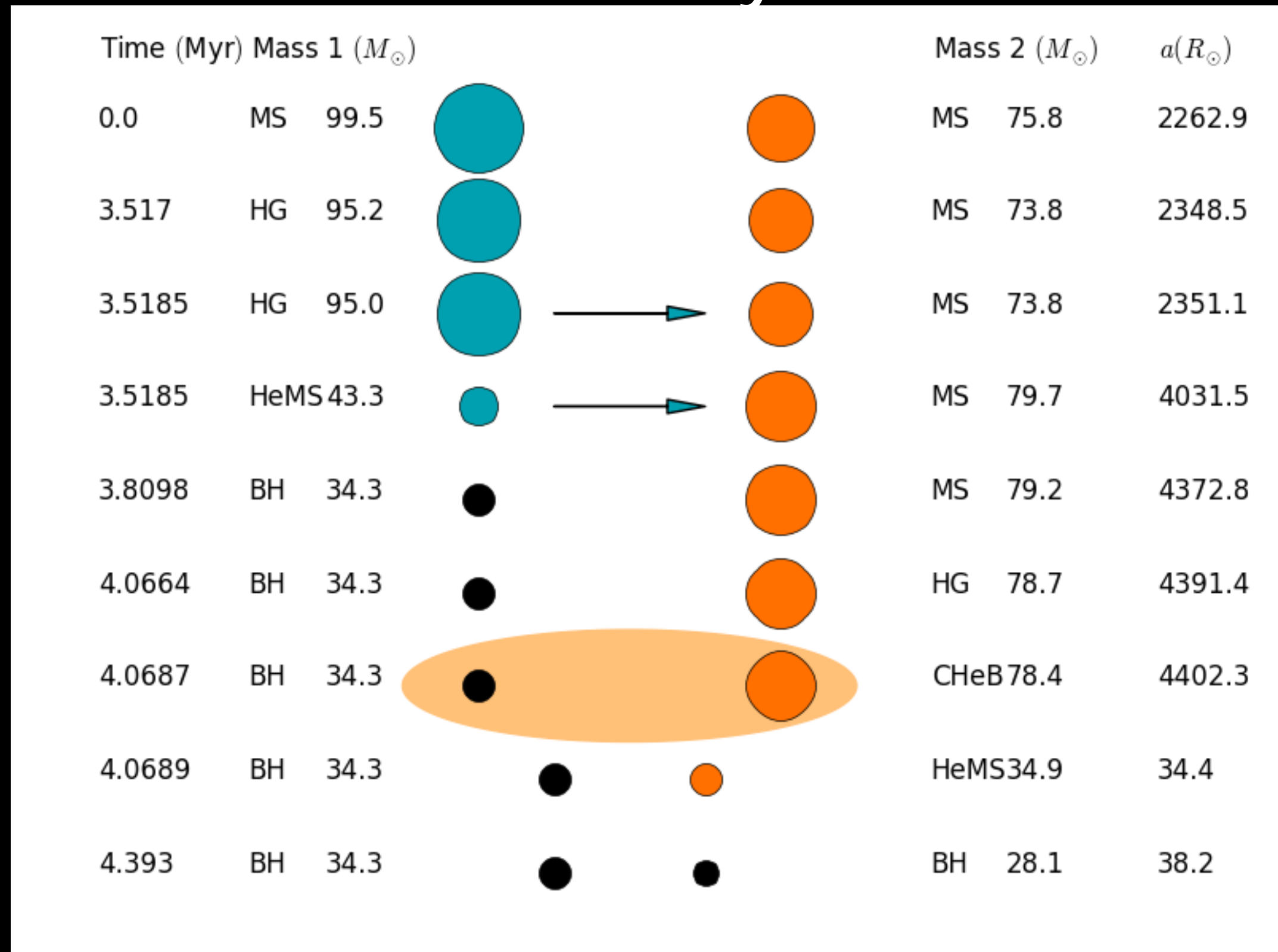
The separation problem



- Harden the binary after stars evolved: classical binary evolution via a common envelope

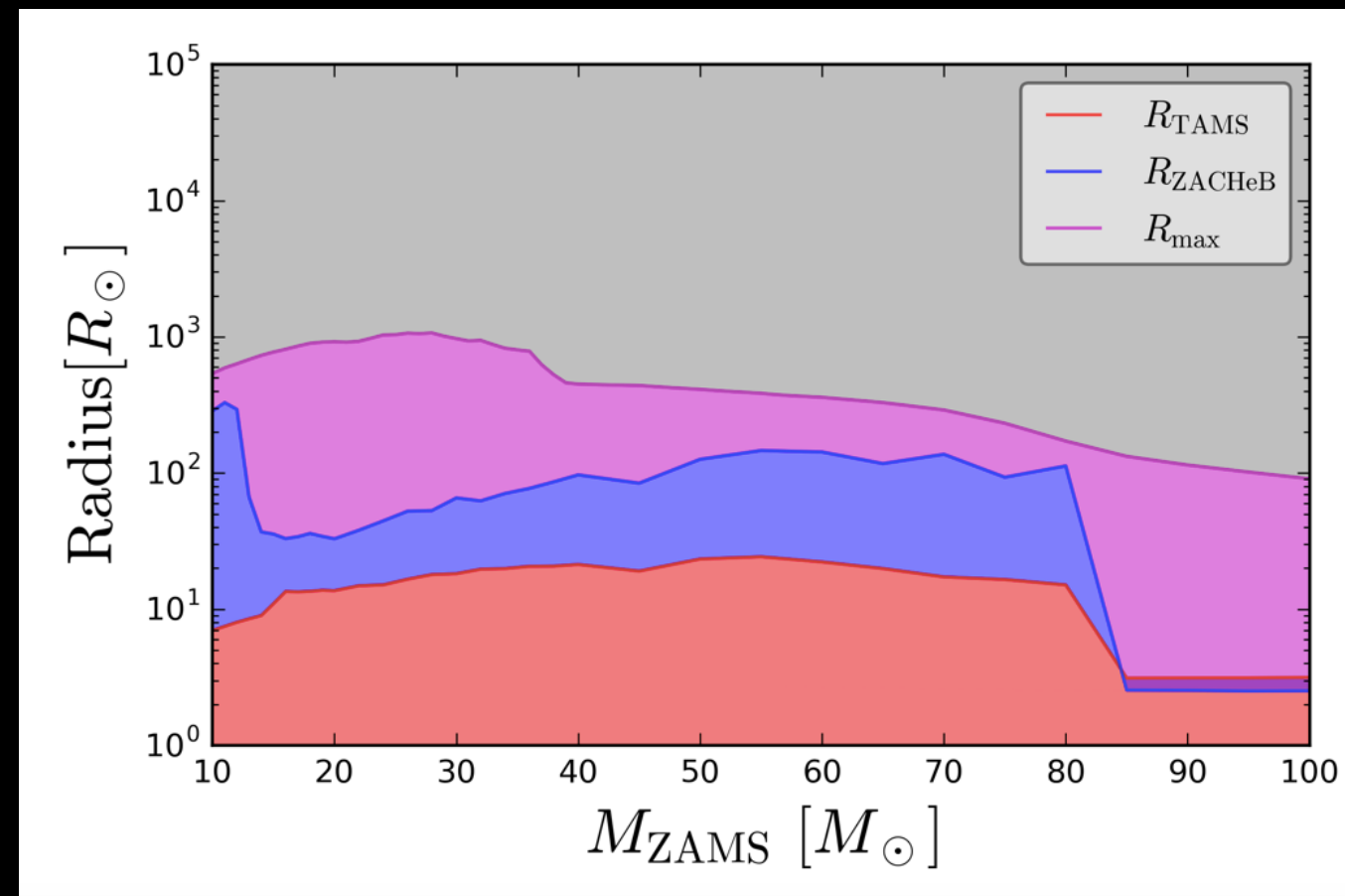
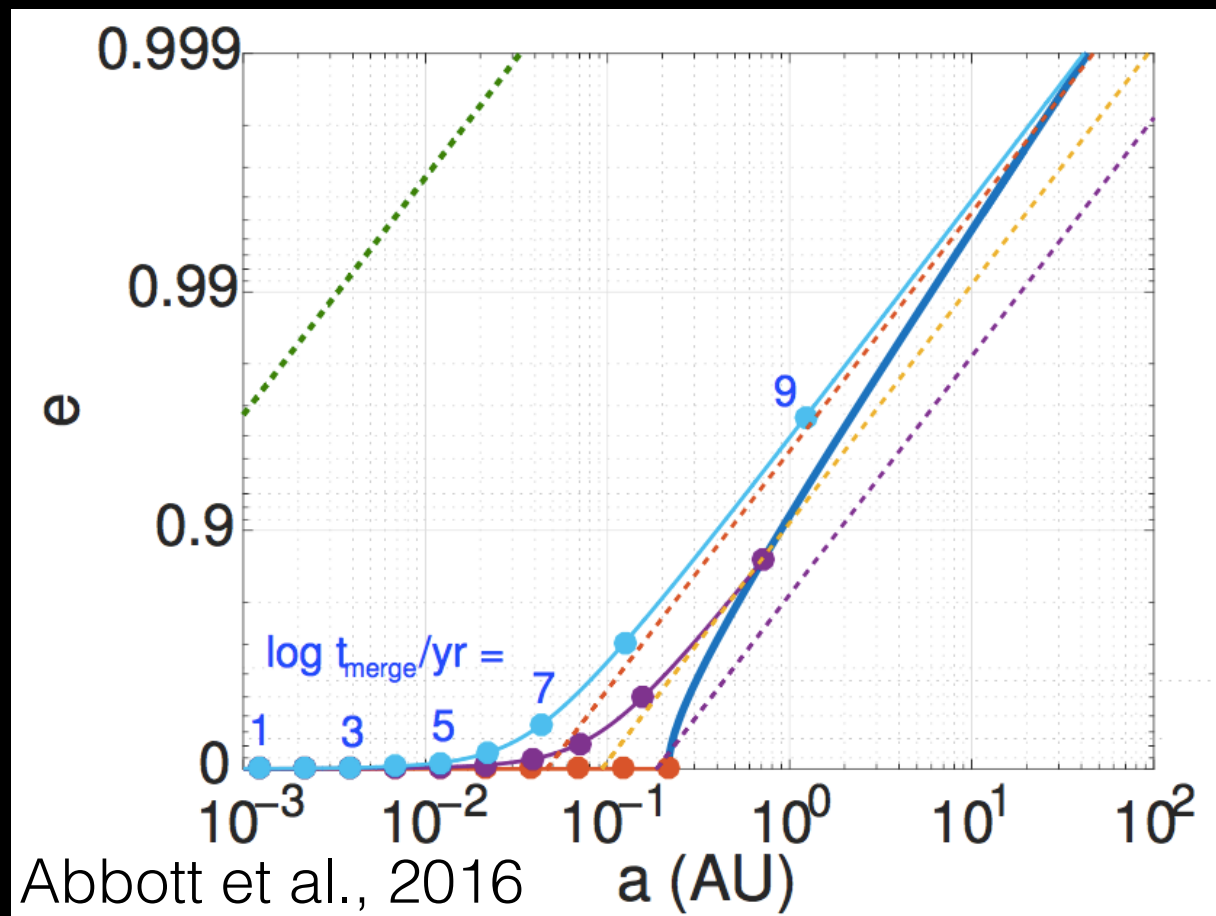
- Tutukov & Yungelson 1973, 1993; Lipunov, Postnov & Prokhorov (1997), Bethe & Brown (1998), Bloom, Sigurdsson & Pols (1999), De Donder & Vanbeveren (2004), Grishchuk et al. (2001), Nelemans (2003), Voss & Tauris (2003), Pfahl, Podsiadlowski & Rappaport (2005), Dewi, Podsiadlowski & Sena (2006), Kalogera et al. 2007; O'Shaughnessy et al. (2008), Mennekens & Vanbeveren (2014), Dominik et al. (2012, 2013, 2015), Belczynski et al. 2016, Eldridge & Stanway (2016), Lipunov+ (2016), ...

Isolated binary evolution

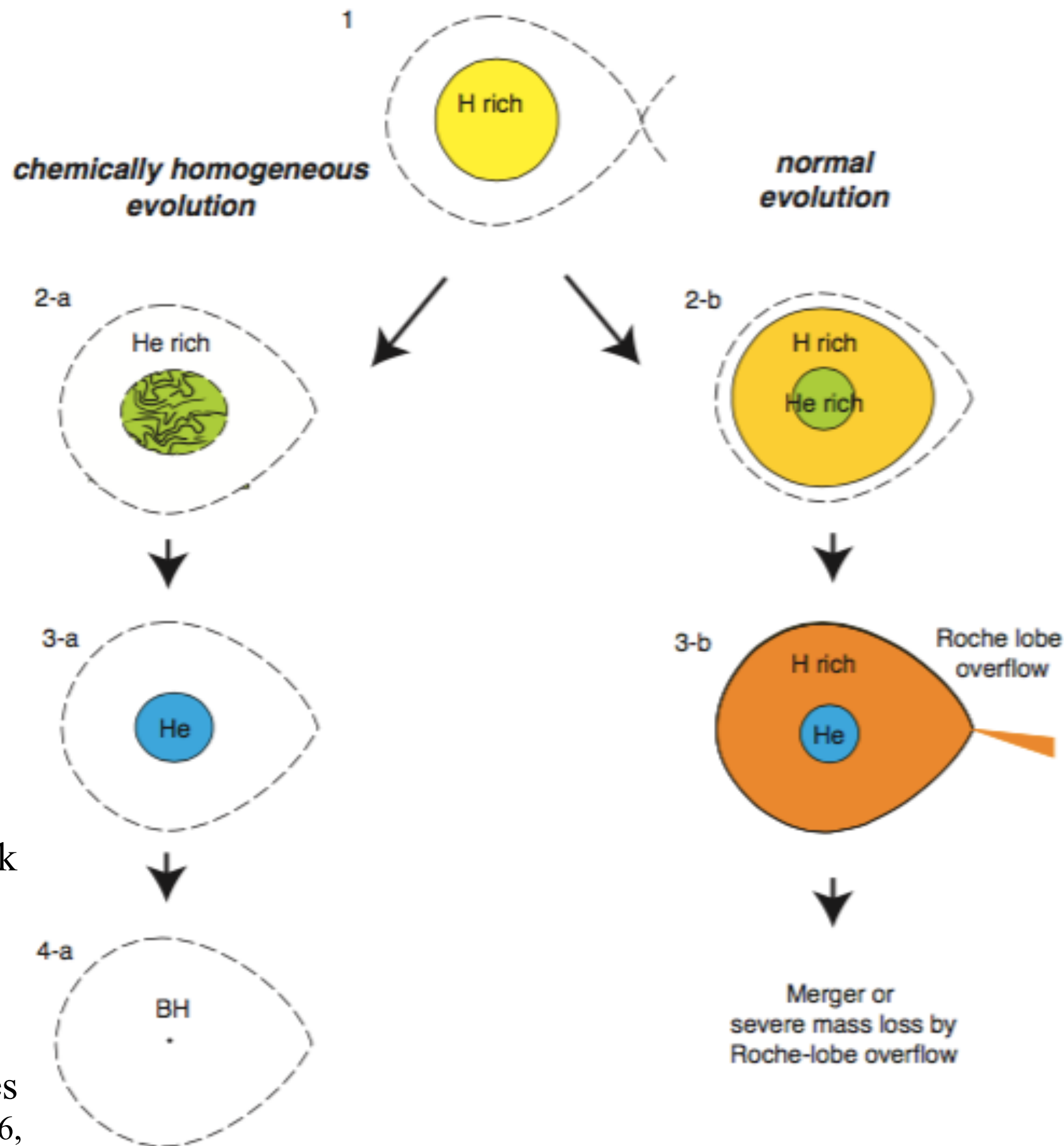


Stevenson, Vigna Gomez, Mandel+, Nat Comm, 2017

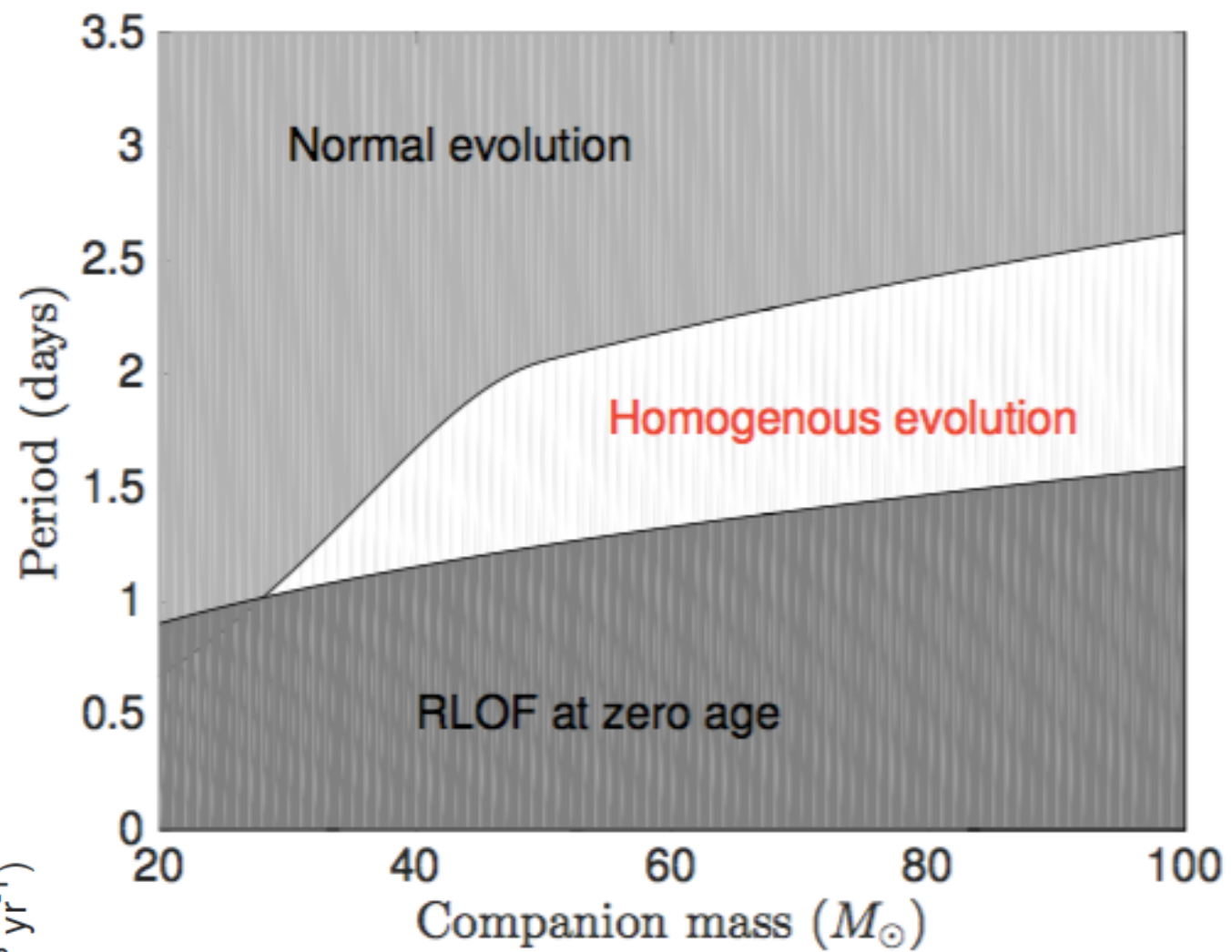
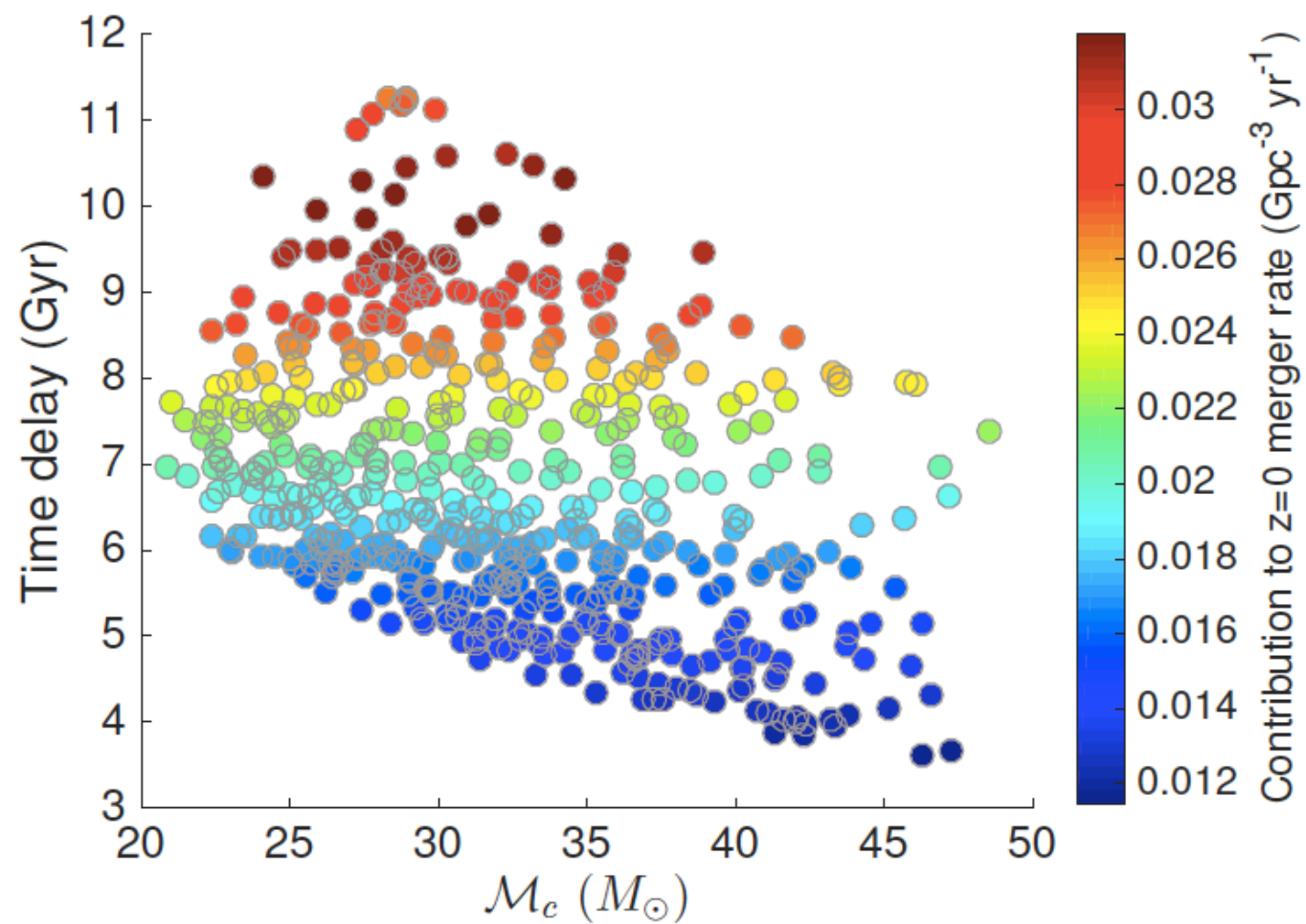
The separation problem



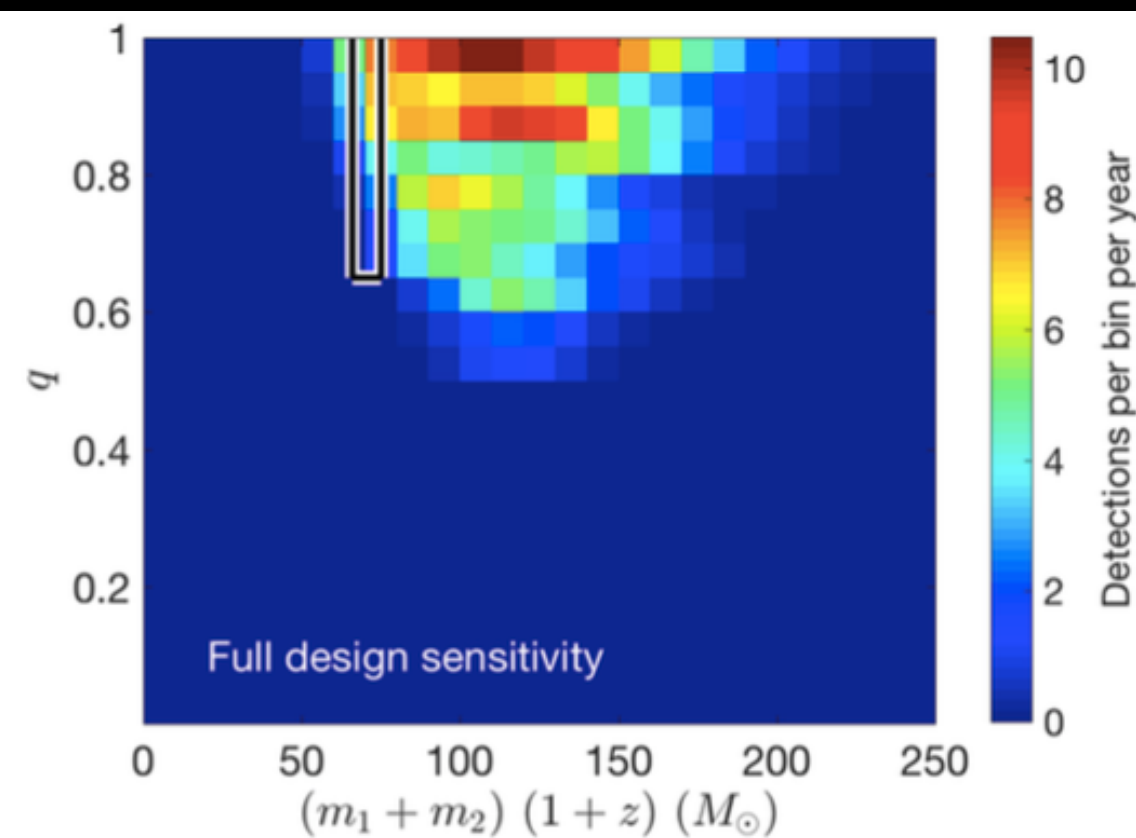
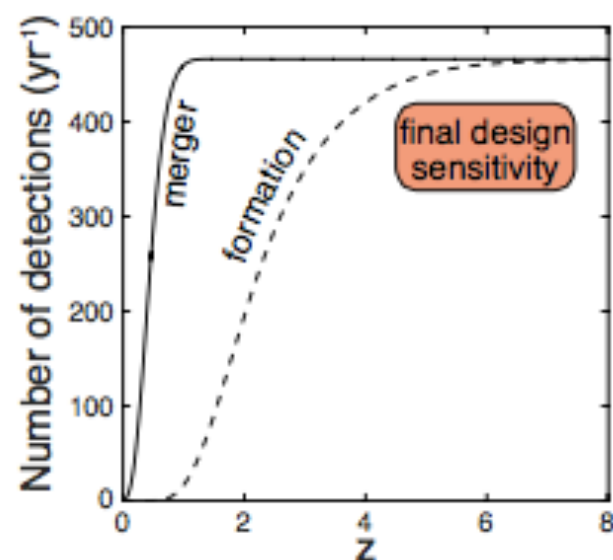
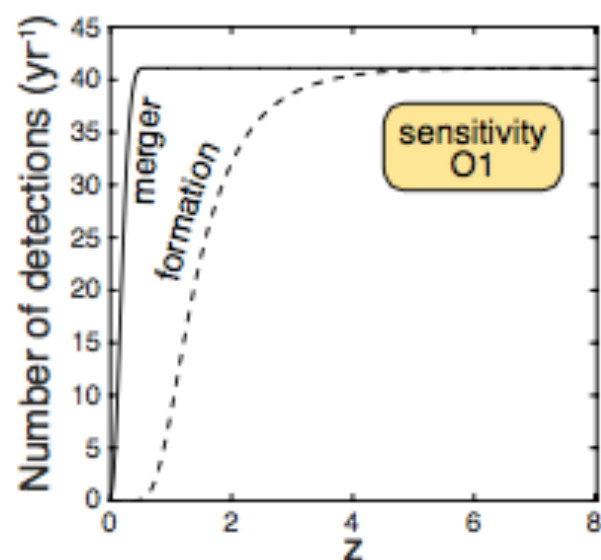
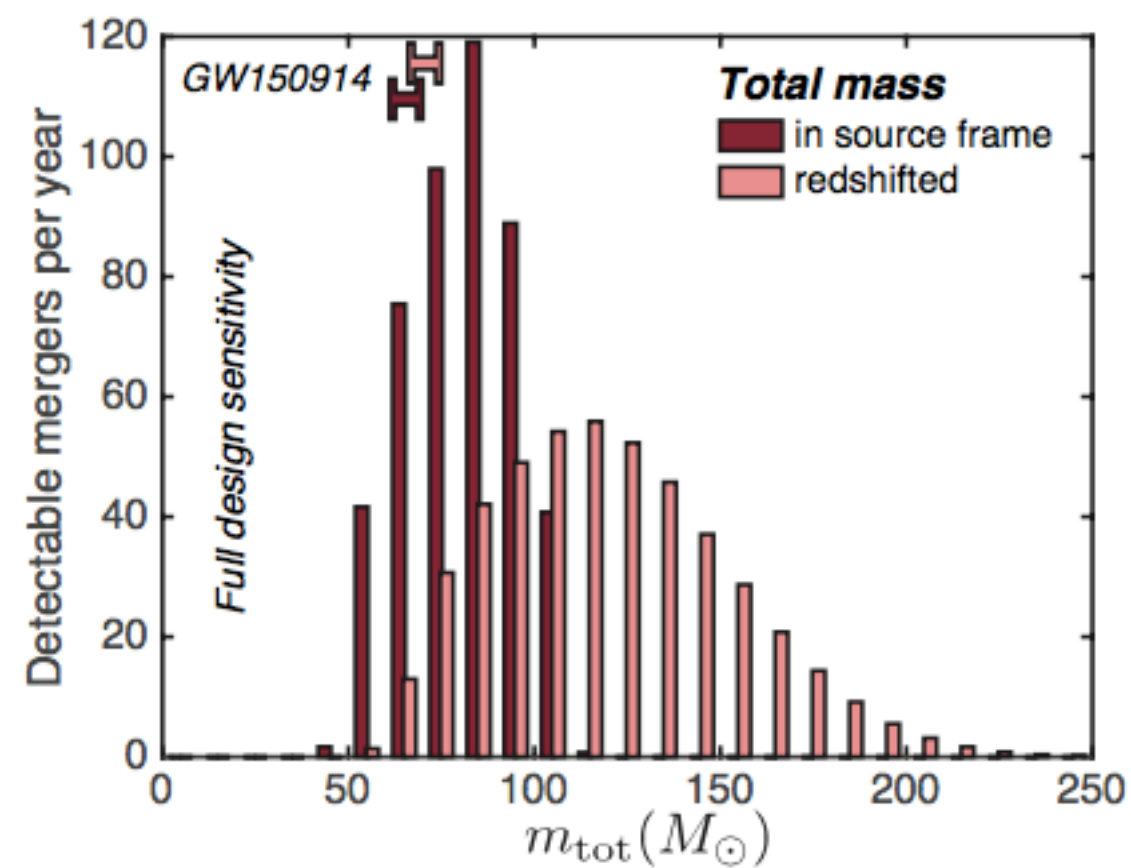
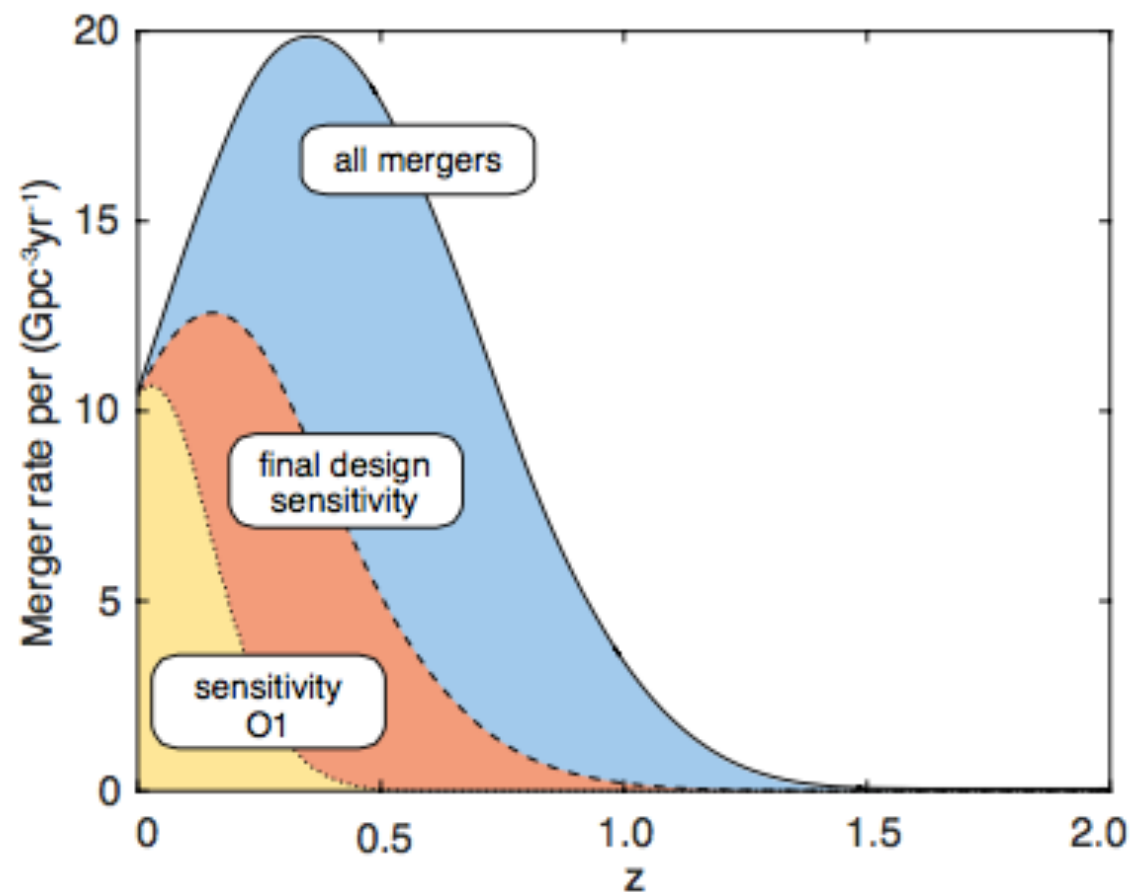
- Harden the binary after stars evolved
- Don't let stars expand: chemically homogeneous evolution
 - Mandel & de Mink, 2016; Marchant+, 2016; de Mink & Mandel, 2016
- Let stars evolve before they make a binary



Merging binary black
holes formed
through chemically
homogeneous
evolution in short-
period stellar binaries
[Mandel & de Mink, 2016,
after de Mink+, 2009]

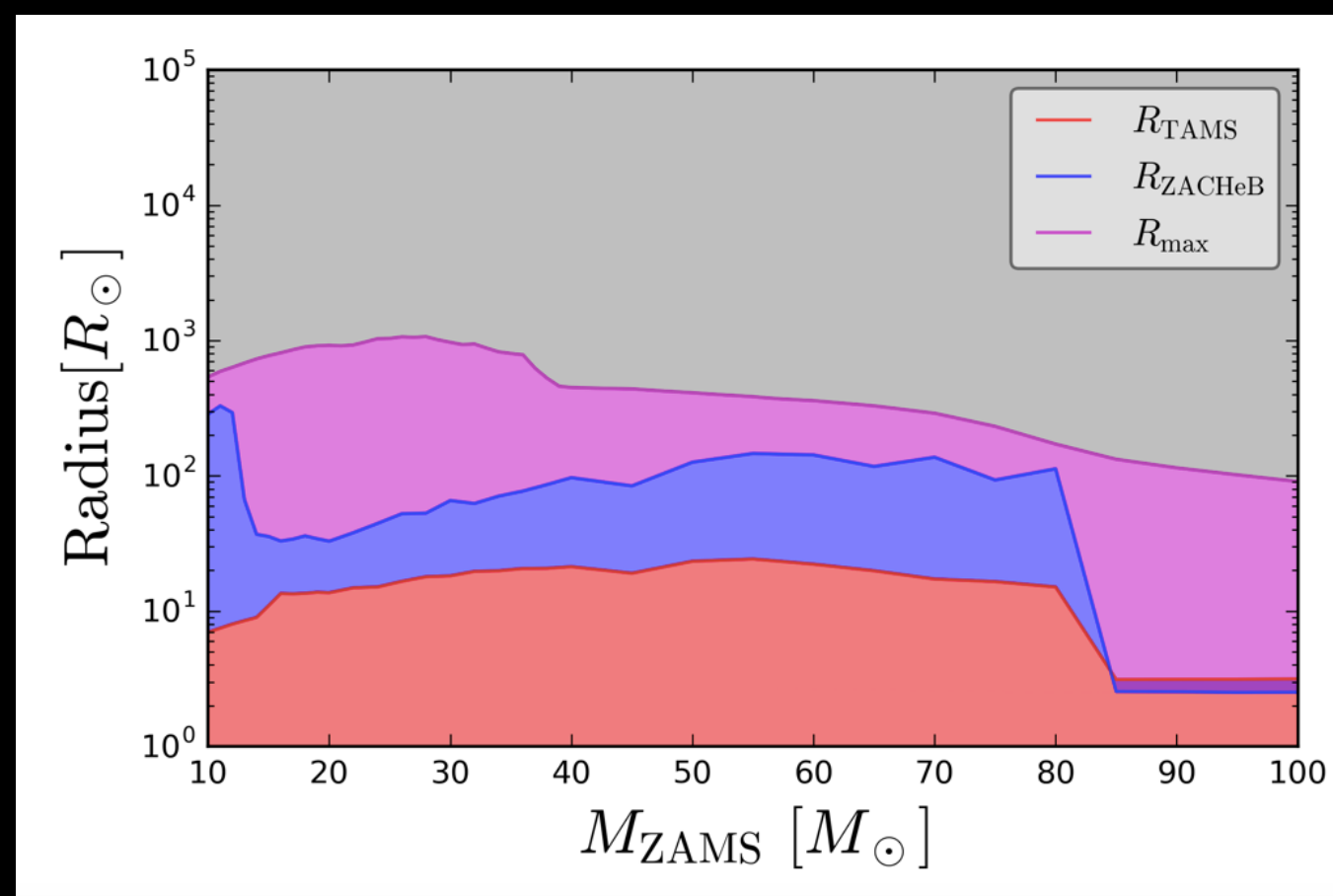
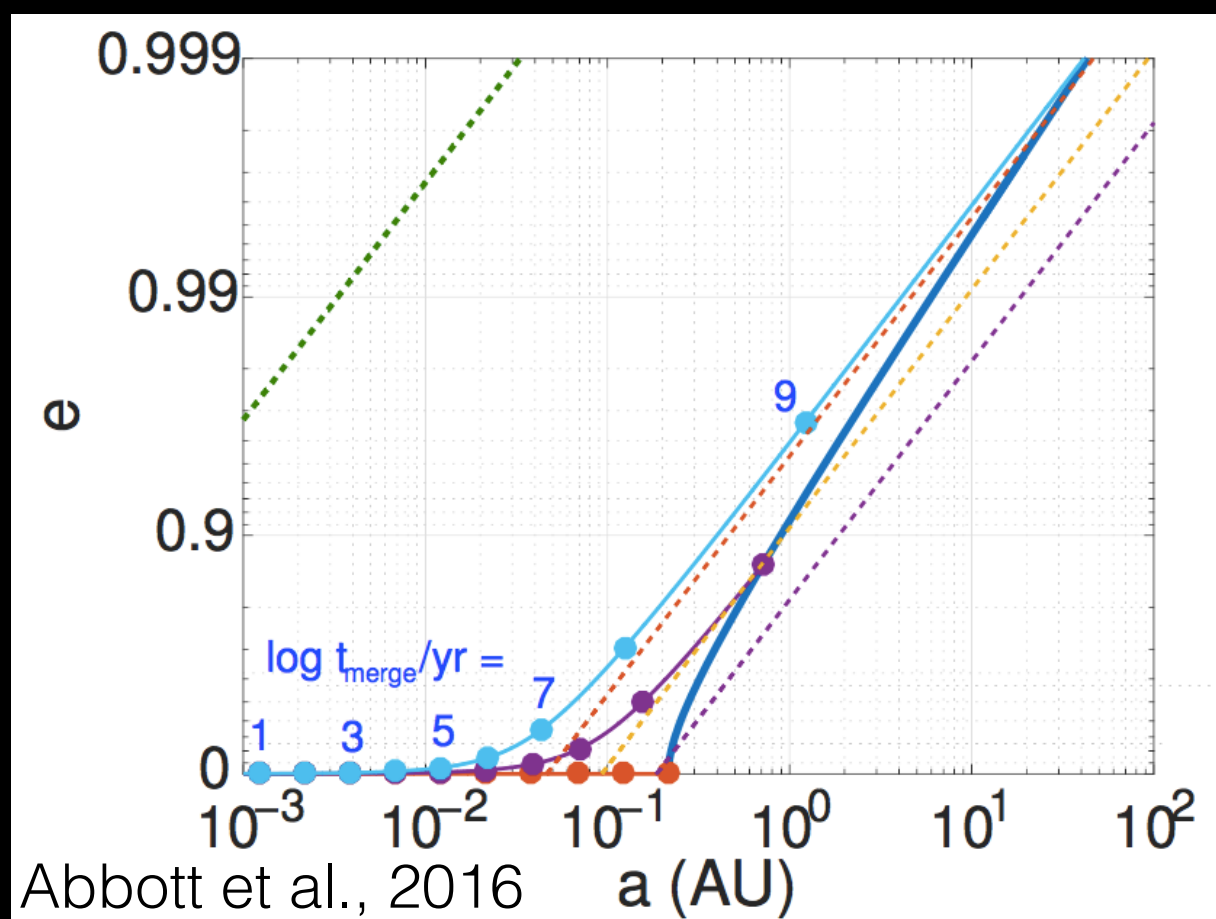


Mandel & de Mink, 2016

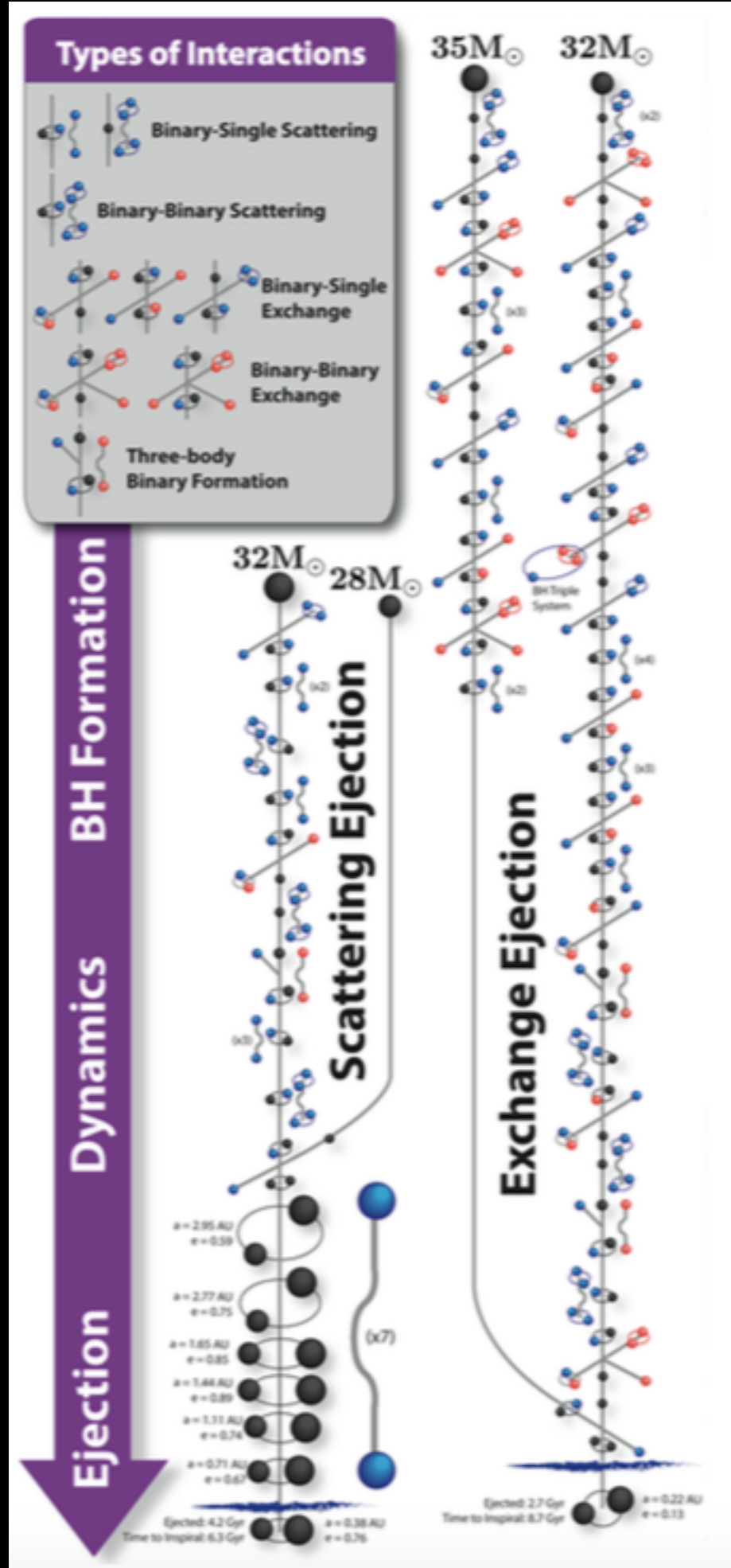


de Mink & Mandel, 2016

The separation problem



- Let stars evolve before they make a binary: dynamical formation in clusters
 - Stellar and globular clusters: Sigurdsson & Hernquist (1993); Kulkarni+ (1993); Portegies Zwart & McMillan (2000); Gultekin+ (2004, 2006); Kocsis+ (2006); O'Leary+ (2006, 2007, 2016); Sadowski+ (2008); Banerjee+ (2010); Downing+ (2010, 2011); Morscher+ (2013, 2015); Mapelli+ (2016); Rodriguez+ (2015, 2016)
 - Galactic nuclear clusters: Miller & Lauburg (2009); O'Leary+ (2009); Kocsis & Levin (2012); Tsang (2013); Bae+ (2014); Bartos+ (2016); Stone+ (2016)



Rodriguez, Haster+,
(2016)

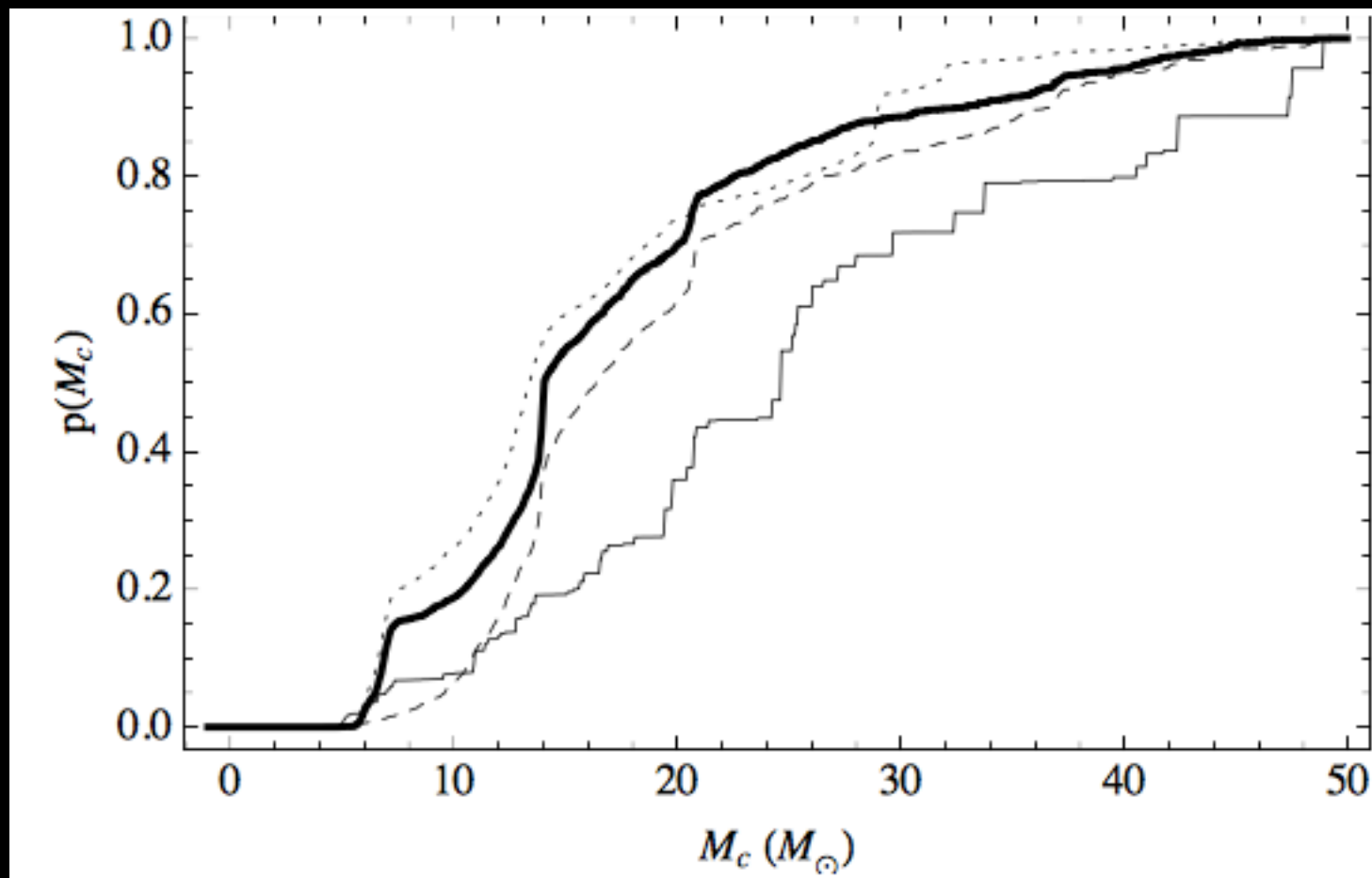
Are predictions borne out?

TABLE IV: Compact binary coalescence rates per Mpc^3 per Myr.^a

Source	R_{low}	R_{re}	R_{high}	R_{max}
NS-NS ($\text{Mpc}^{-3} \text{ Myr}^{-1}$)	0.01 [1]	1 [1]	10 [1]	50 [16]
NS-BH ($\text{Mpc}^{-3} \text{ Myr}^{-1}$)	6×10^{-4} [18]	0.03 [18]	1 [18]	
BH-BH ($\text{Mpc}^{-3} \text{ Myr}^{-1}$)	1×10^{-4} [14]	0.005 [14]	0.3 [14]	

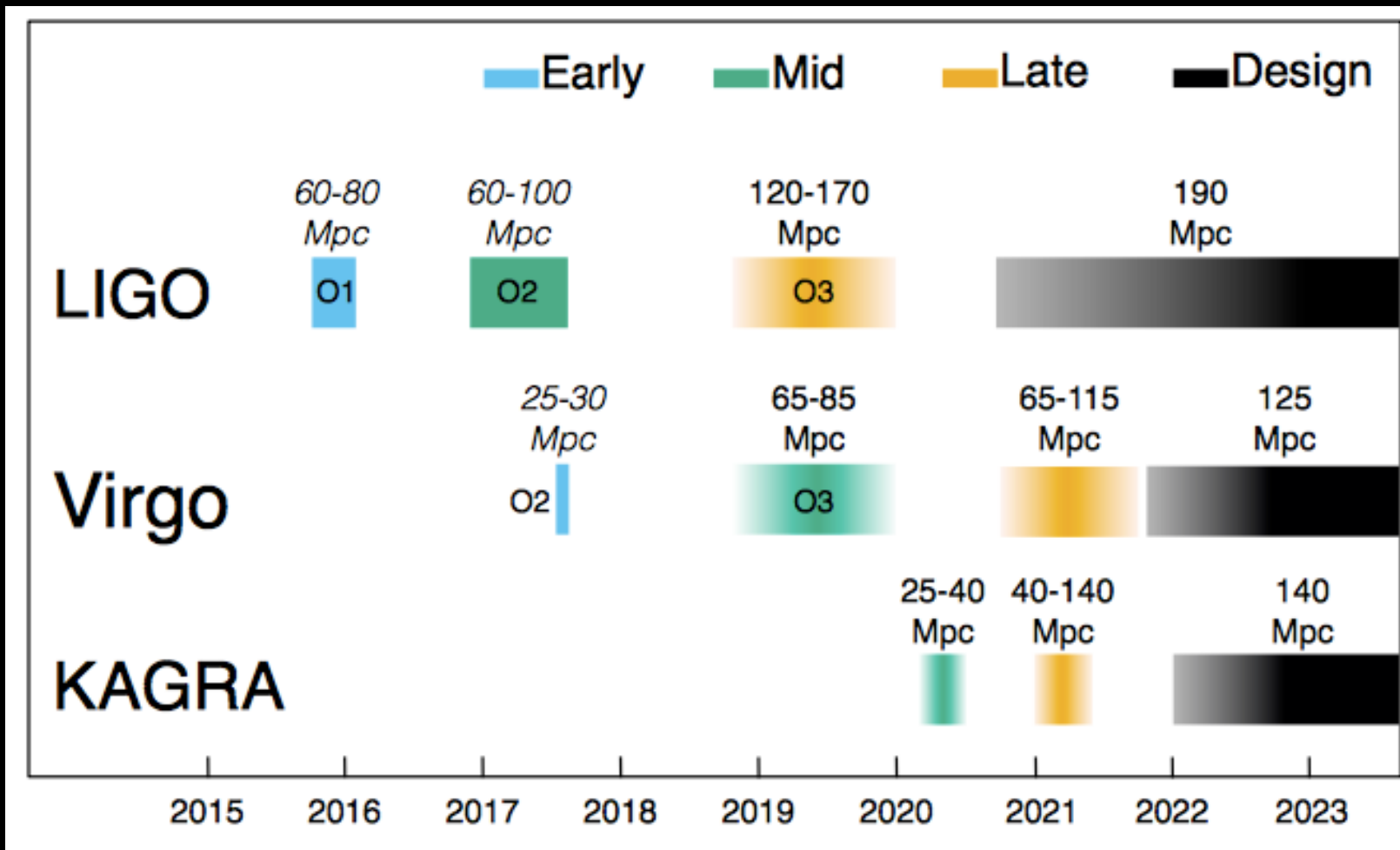
Advanced	NS-NS	0.4	40	400	1000
	NS-BH	0.2	10	300	
	BH-BH	0.4	20	1000	

Abadie+ (2010)

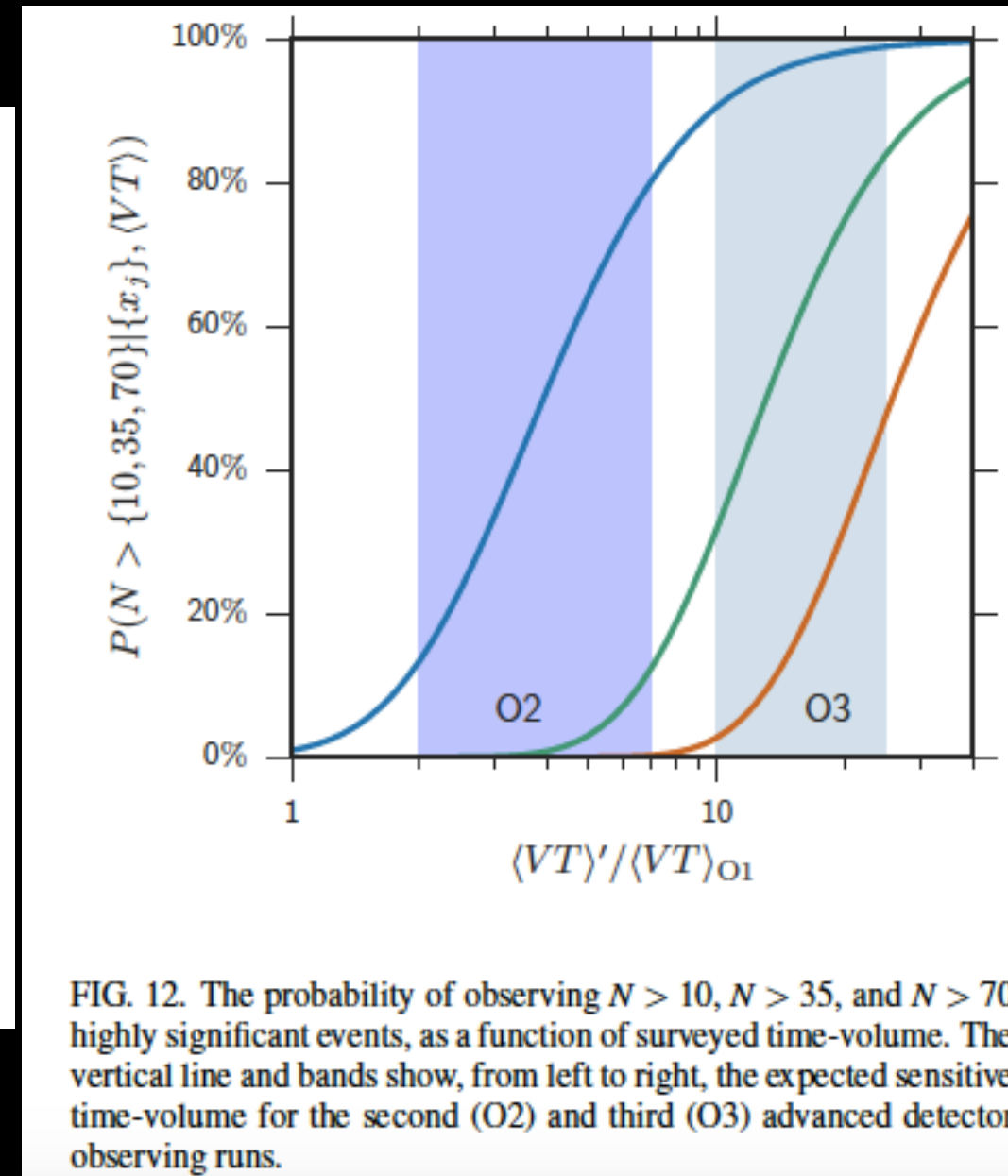


Dominik+, 2015

Prospects



Abbott+, 2017,
Living Reviews



Abbott+, 2016

COMPAS

The inverse problem of gravitational-wave astrophysics:
how to go from a population of observed sources to
understanding key uncertainties about binary evolution?



CMPAS



Simon Stevenson



Alejandro Vigna Gómez



Jim Barrett

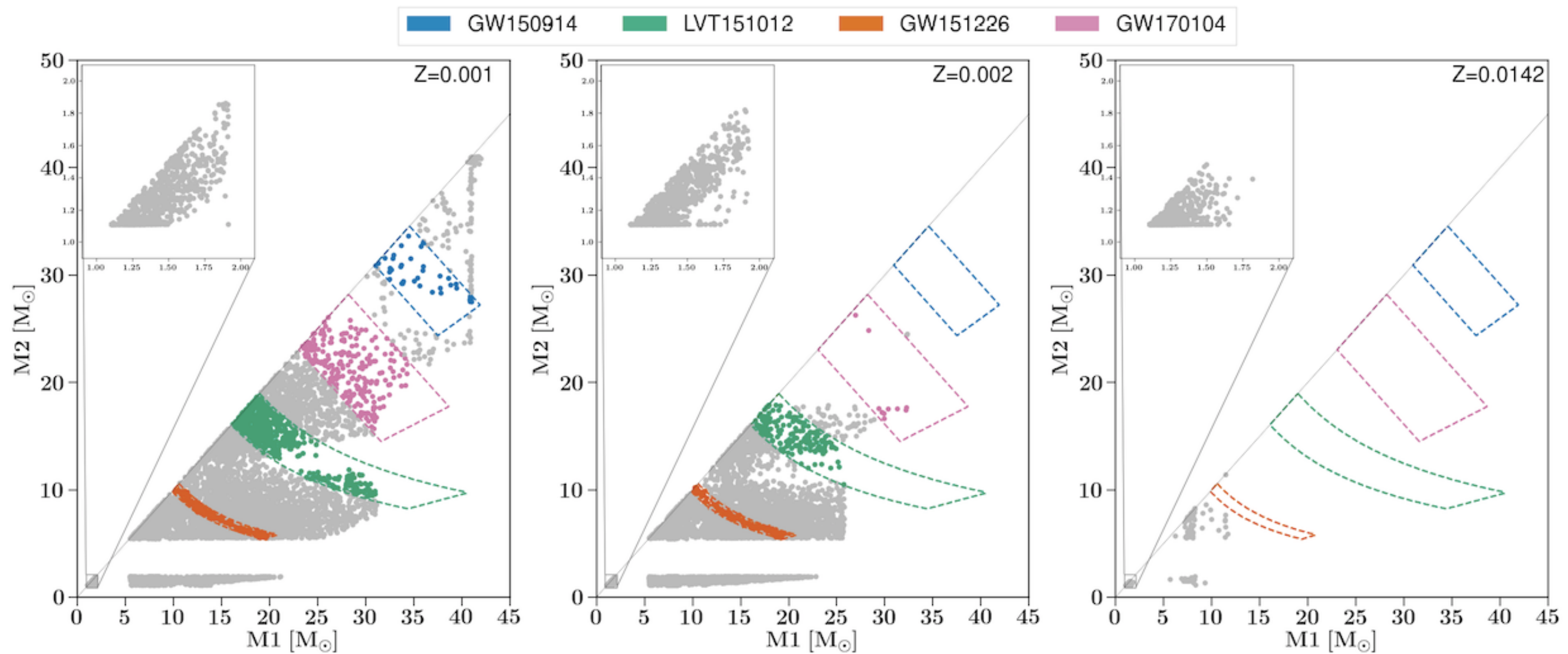


Coenraad Neijssel

Key collaborators / consultants: Christopher Berry, Will Farr, Sebastian Gaebel, Selma de Mink, Stephen Justham, Natasha Ivanova, Vicky Kalogera, Chris Belczynski, Gijs Nelemans, Philipp Podsiadlowski...

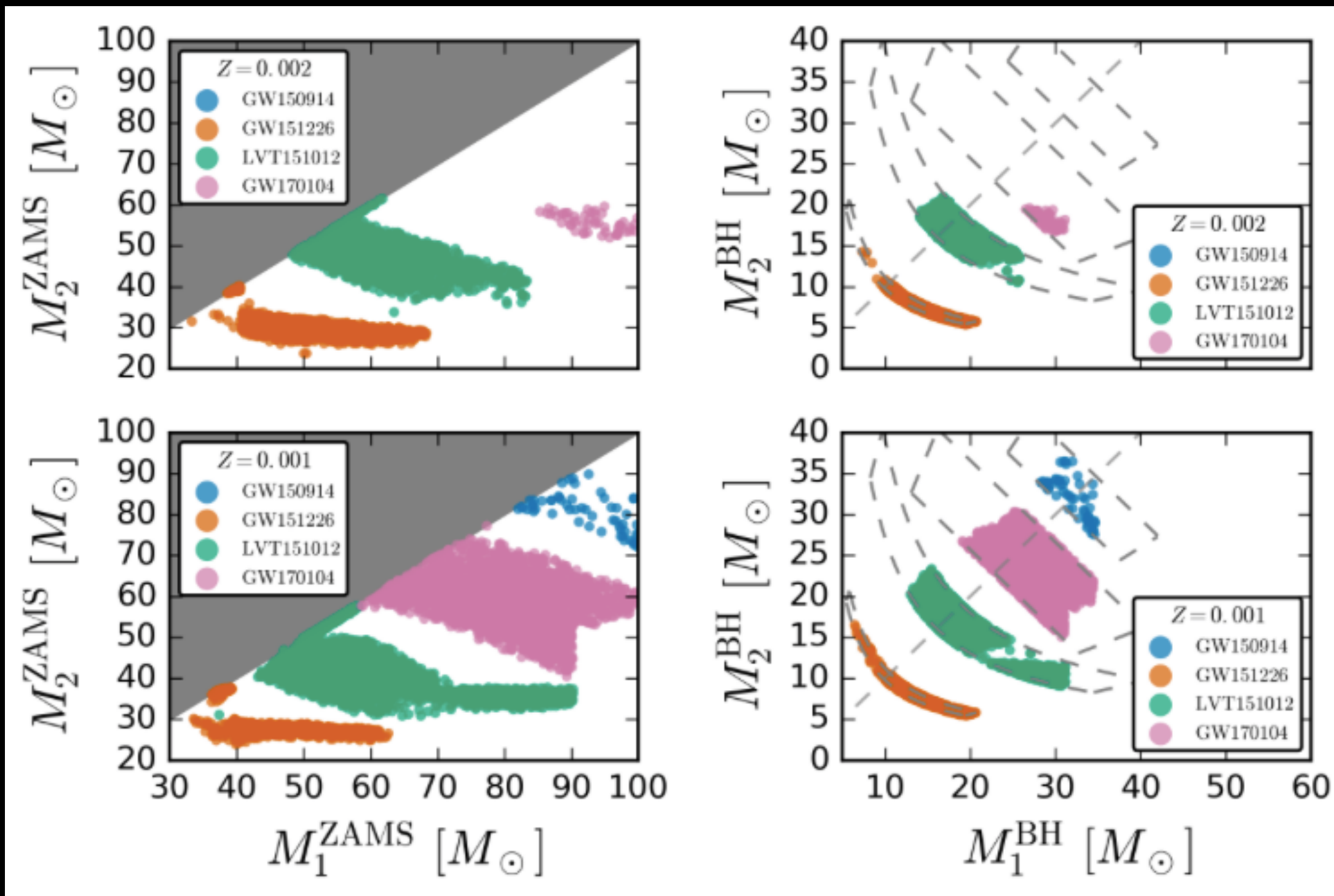
YOUR NAME COULD BE HERE!

Population Synthesis

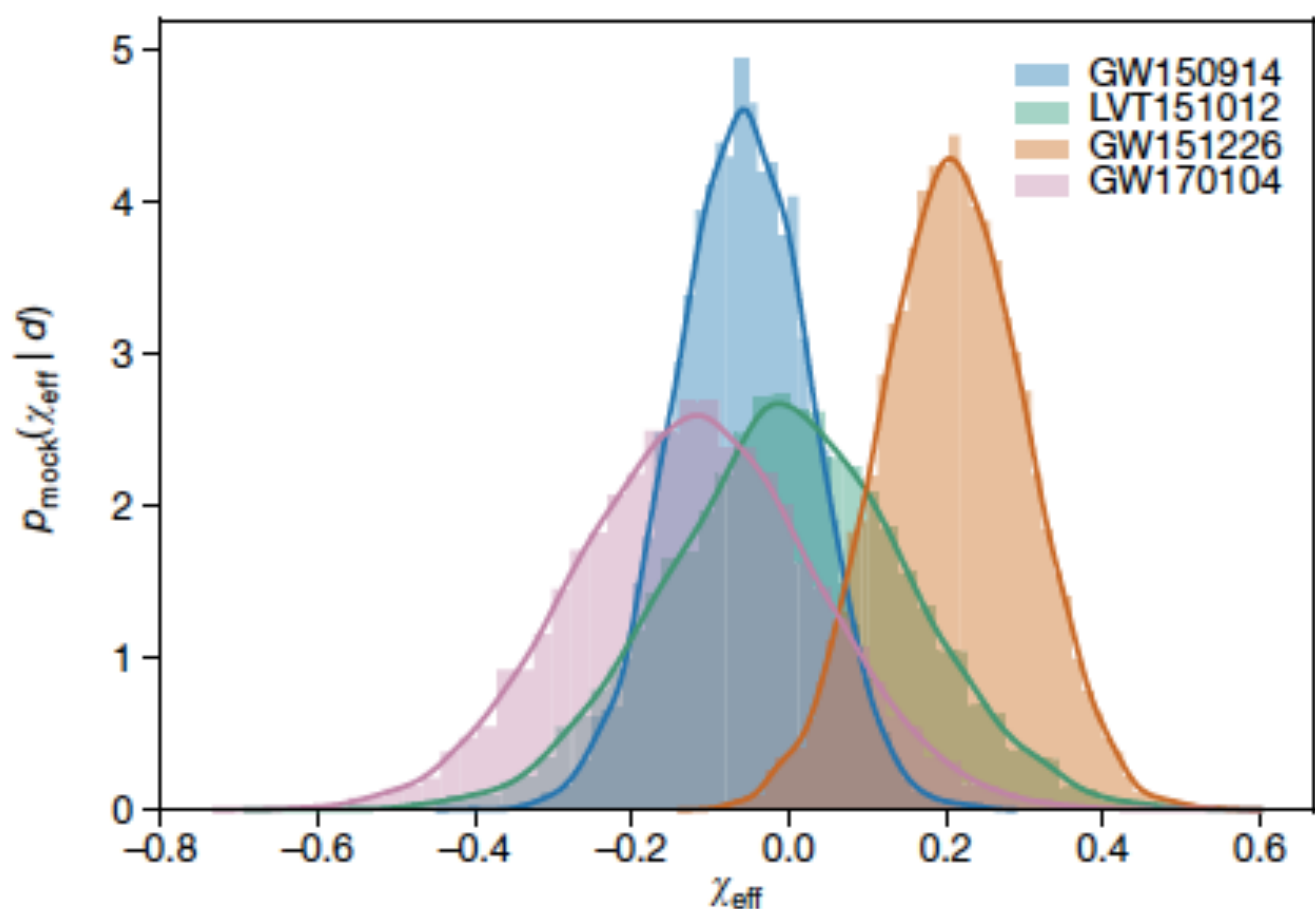


Vigna Gomez+, in prep.

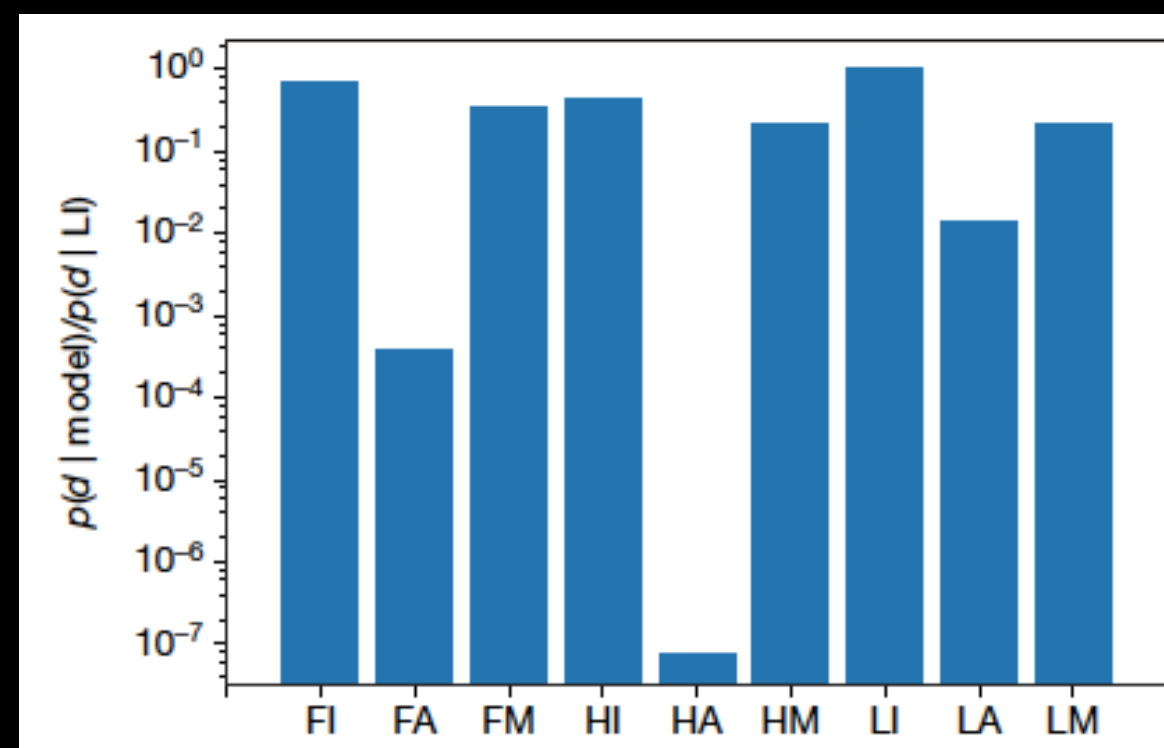
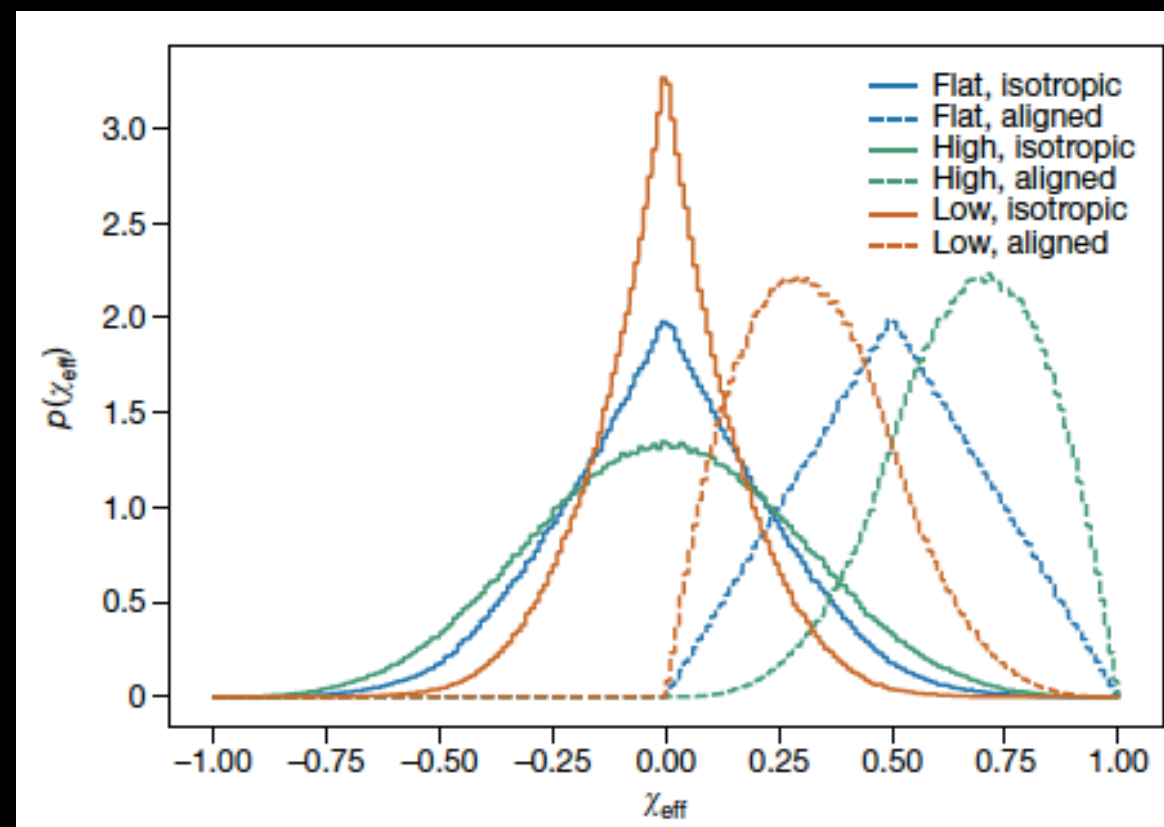
Population Synthesis

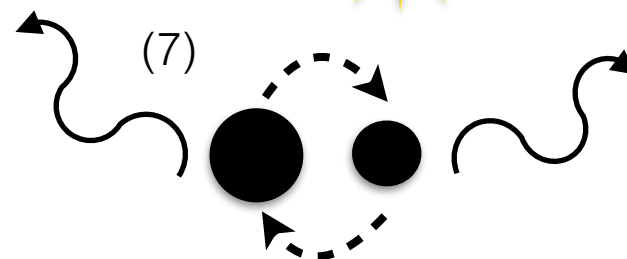
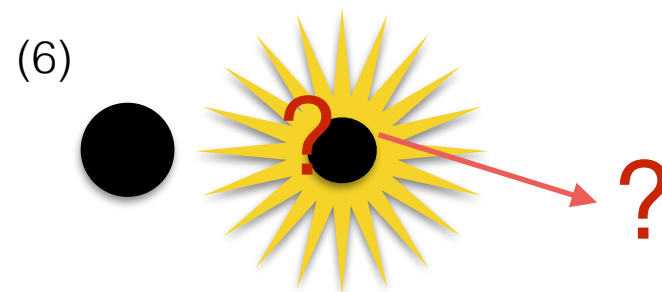
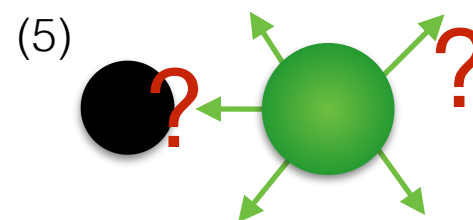
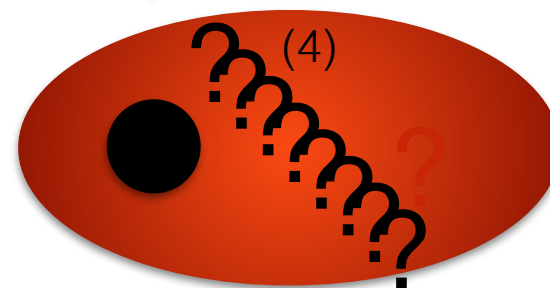
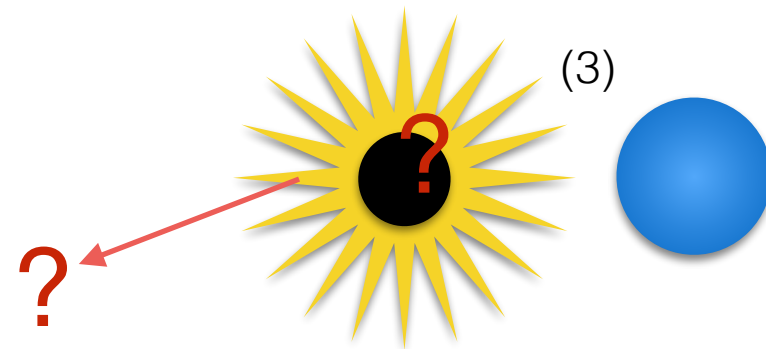
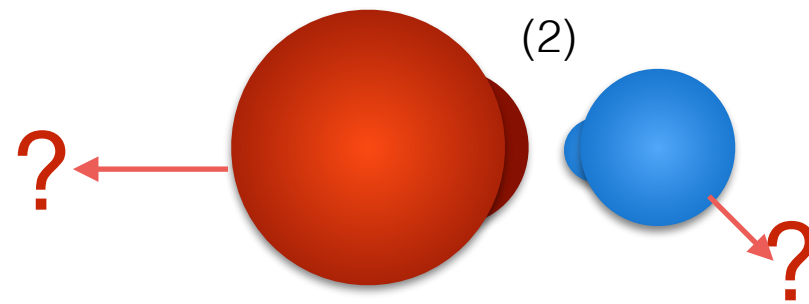
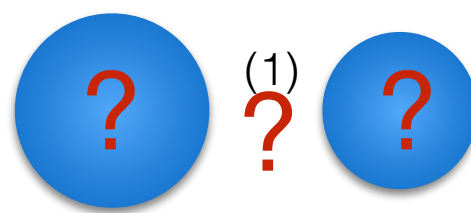


Learning from detections

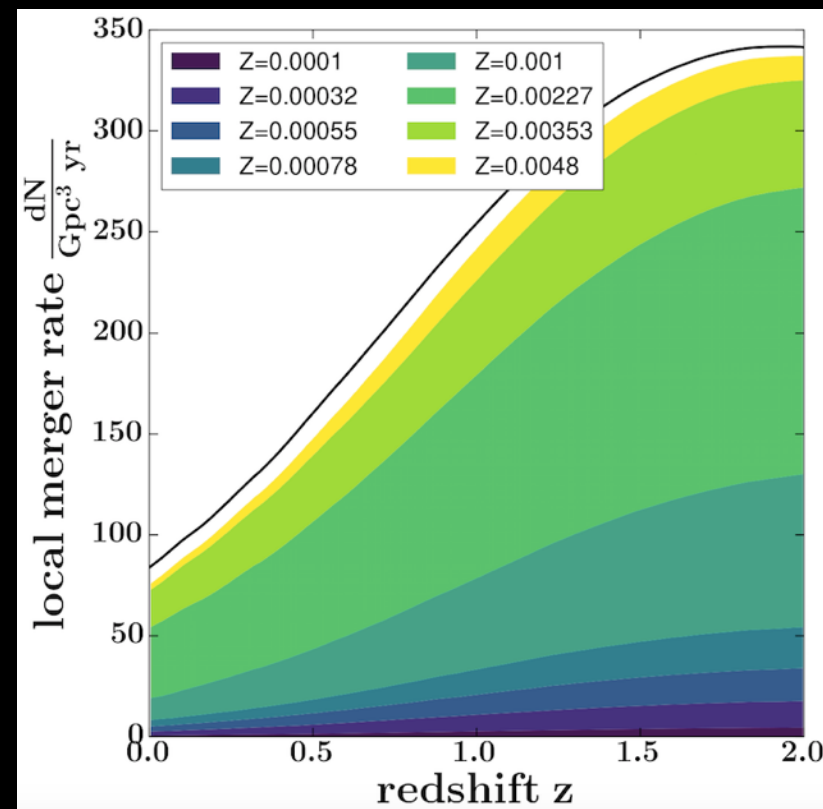
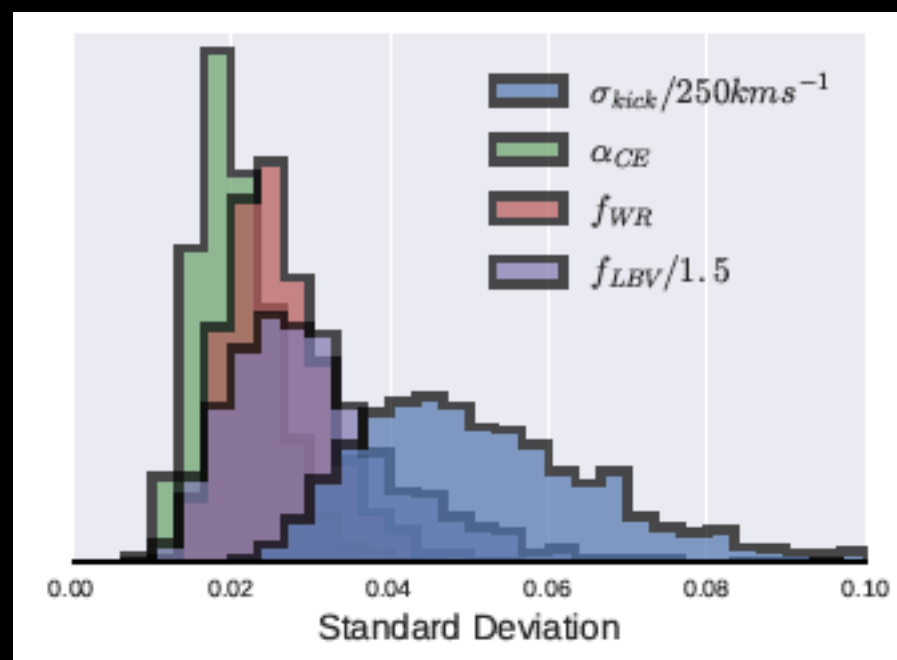
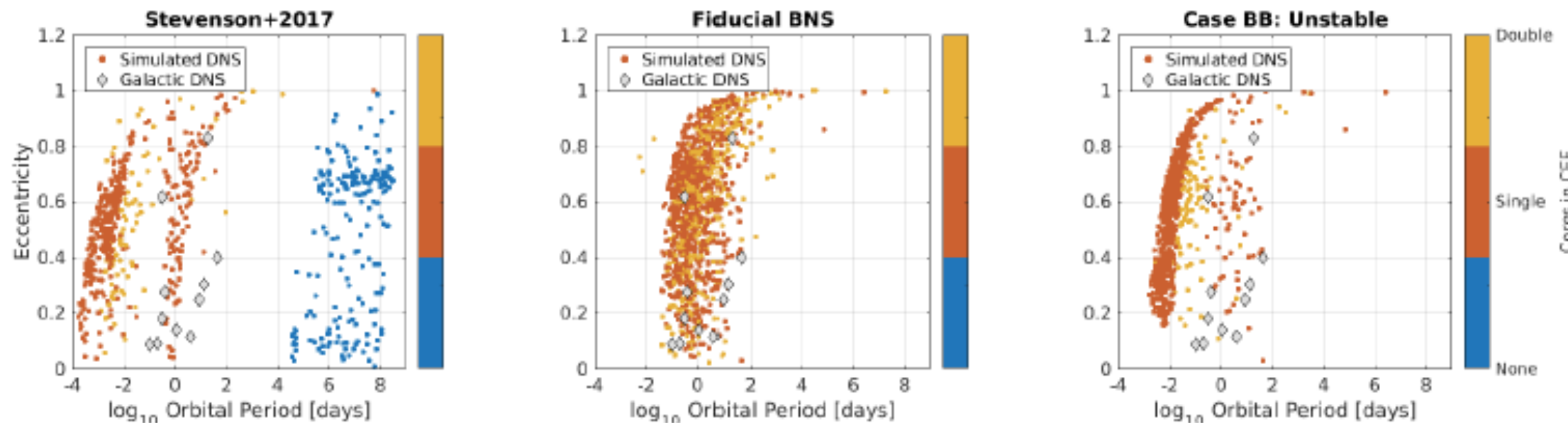


Farr+, Nature, 2017



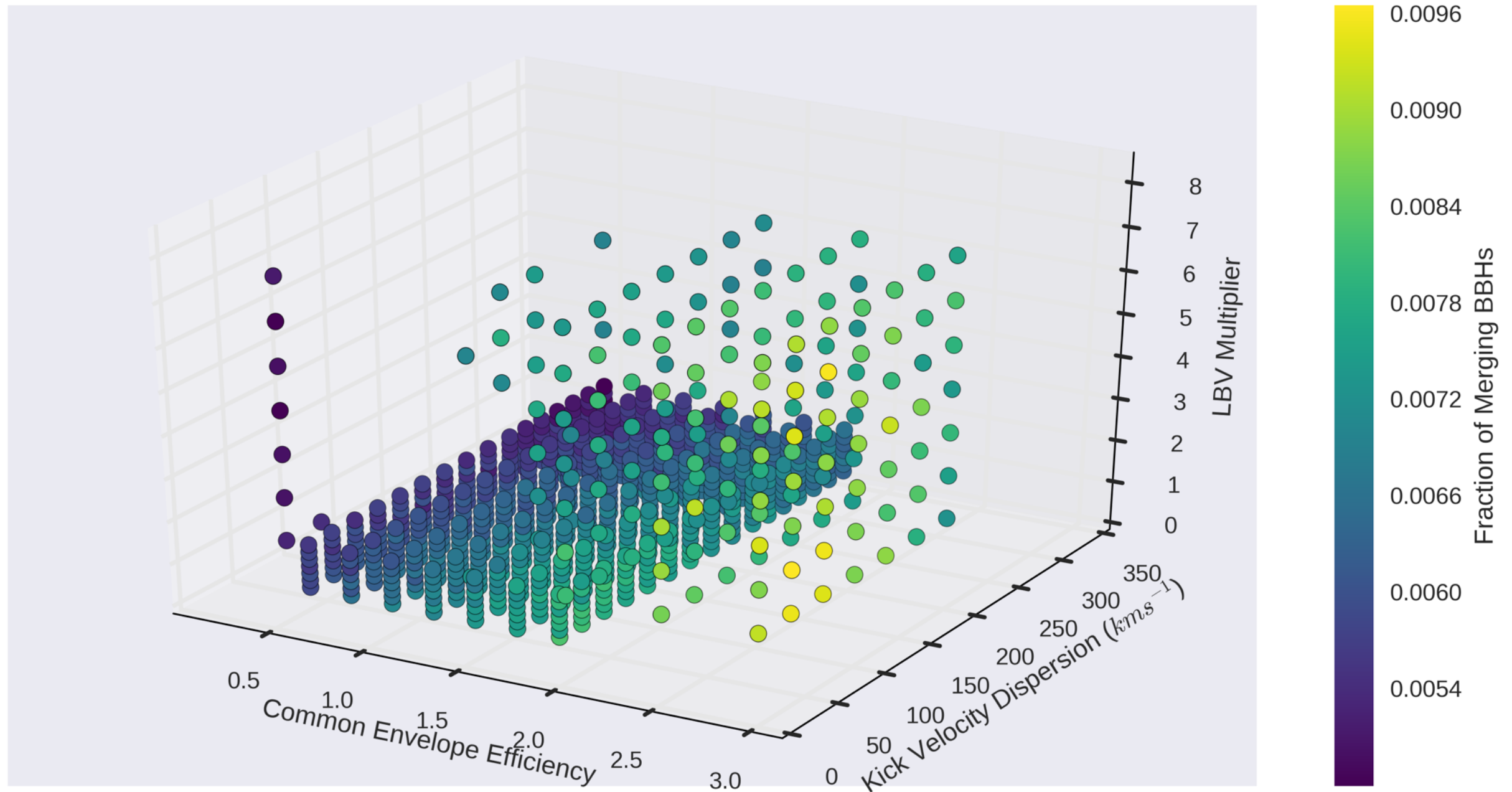


Predictions: what can we learn?

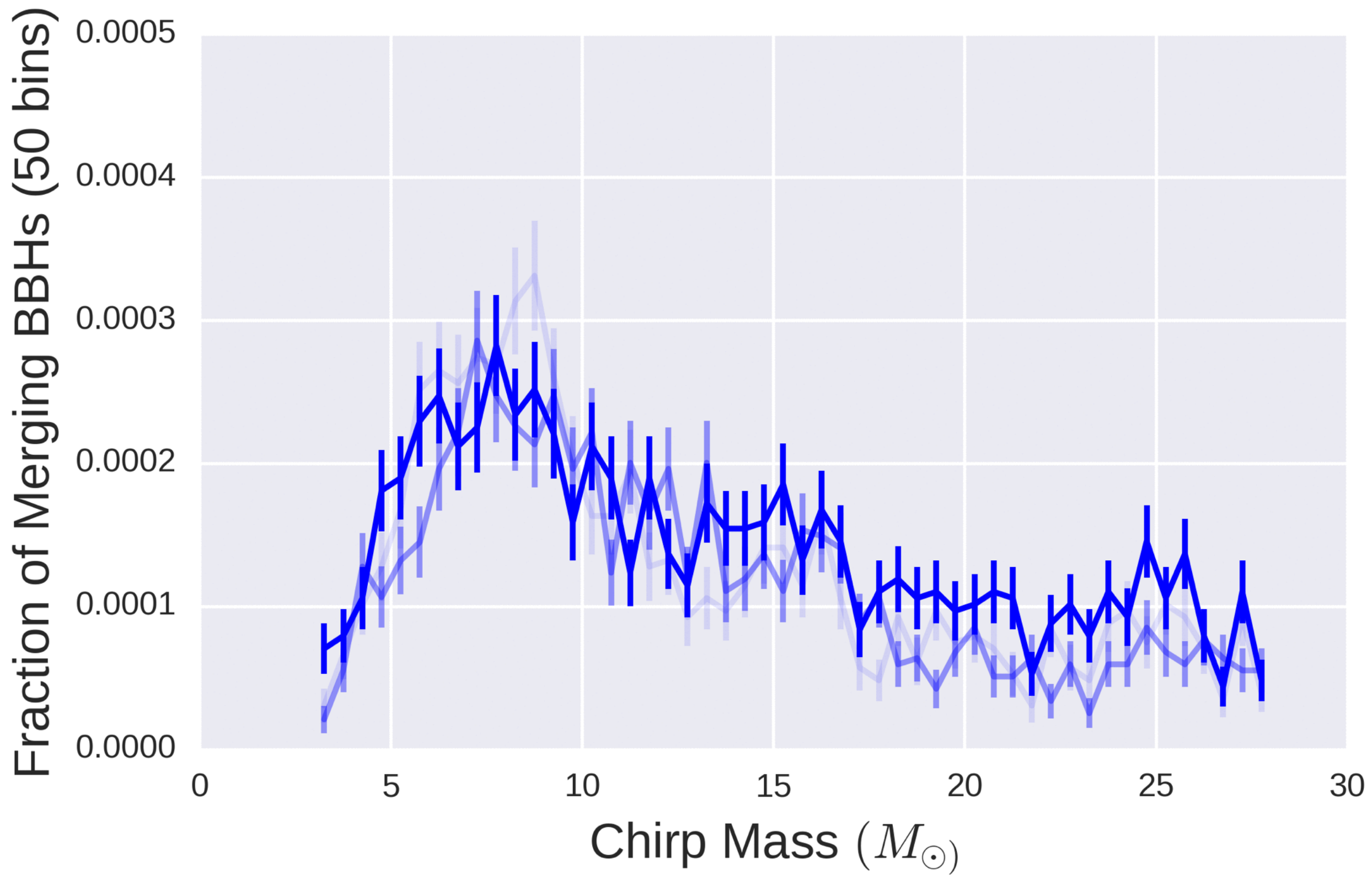


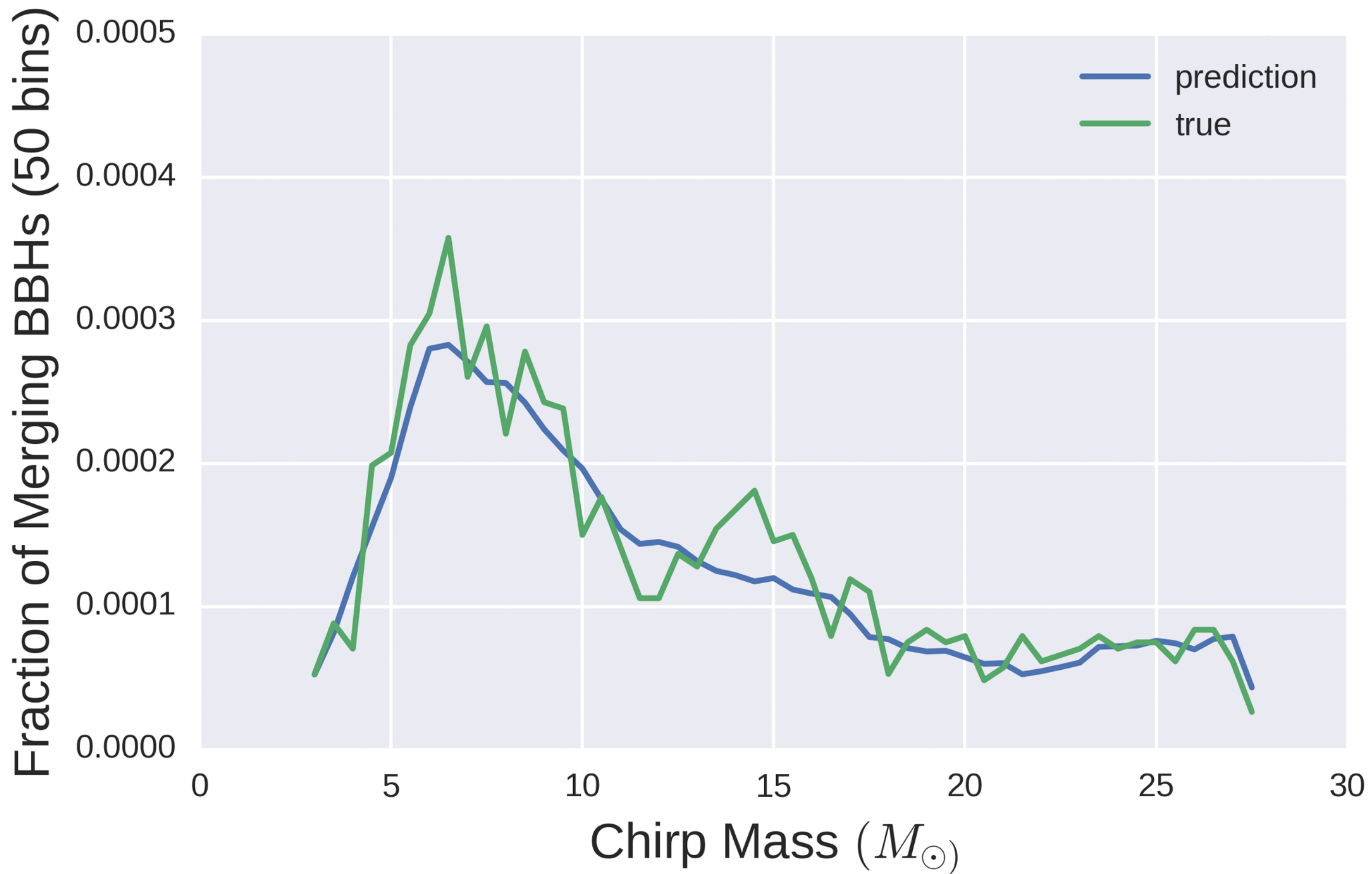
Vigna Gomez+;
Barrett+;
Neijssel+;
in prep.

Model interpolation



Barrett et al., in prep.





Population Reconstruction



- Selection effects and measurement uncertainty

$$p(\{\vec{d}^{(i)}\}|\vec{\lambda}) = \prod_{i=1}^k \frac{\int d\vec{\theta} p(\vec{d}^{(i)}|\vec{\theta}) p_{\text{pop}}(\vec{\theta}|\vec{\lambda})}{\int d\vec{\theta} p_{\text{det}}(\theta) p_{\text{pop}}(\vec{\theta}|\vec{\lambda})}$$

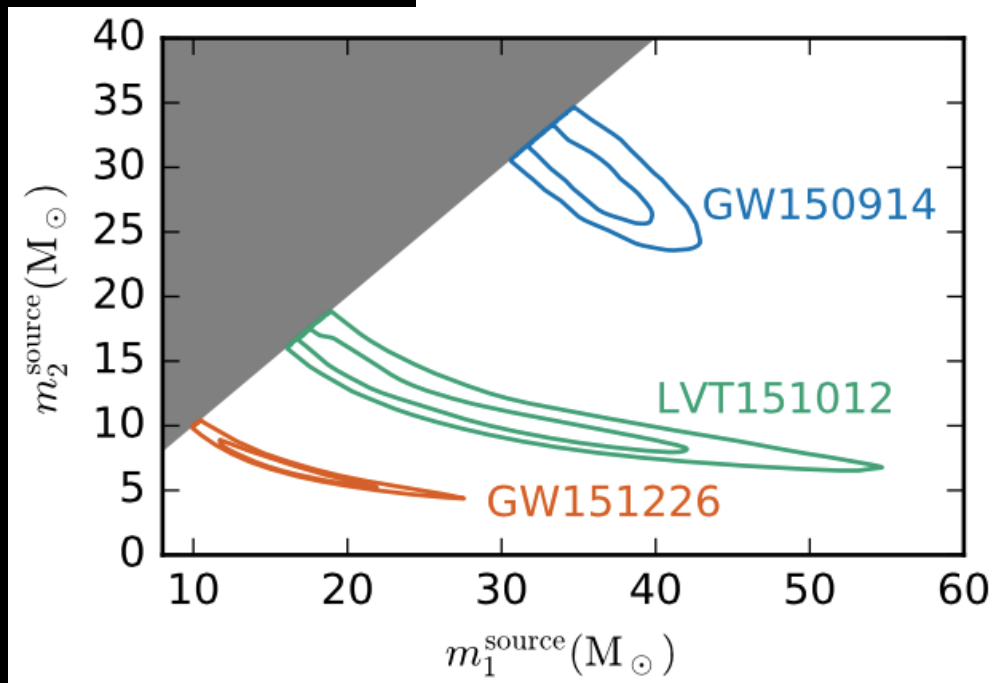
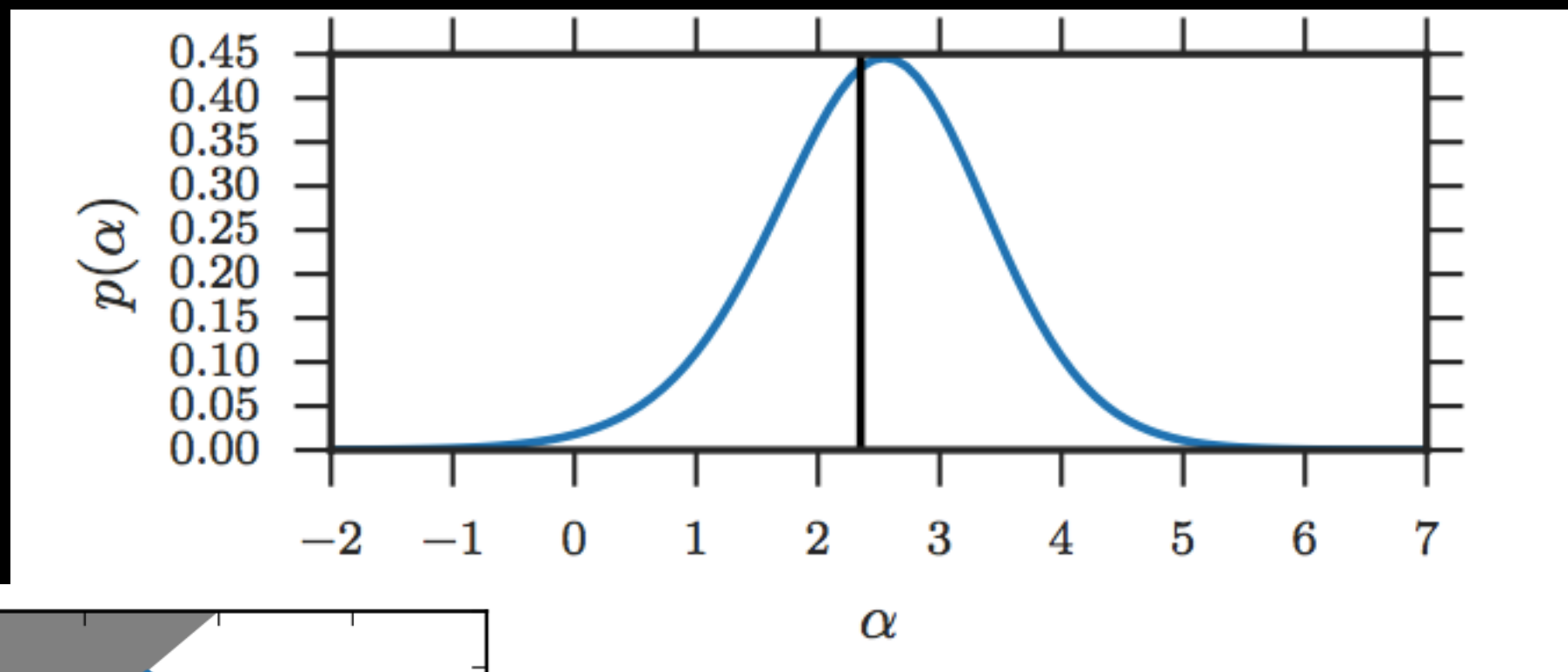
Mandel, Farr, Gair, in prep.

- [Counting and confusion — Farr, Gair, Mandel, Cutler, 2015]

Population Reconstruction



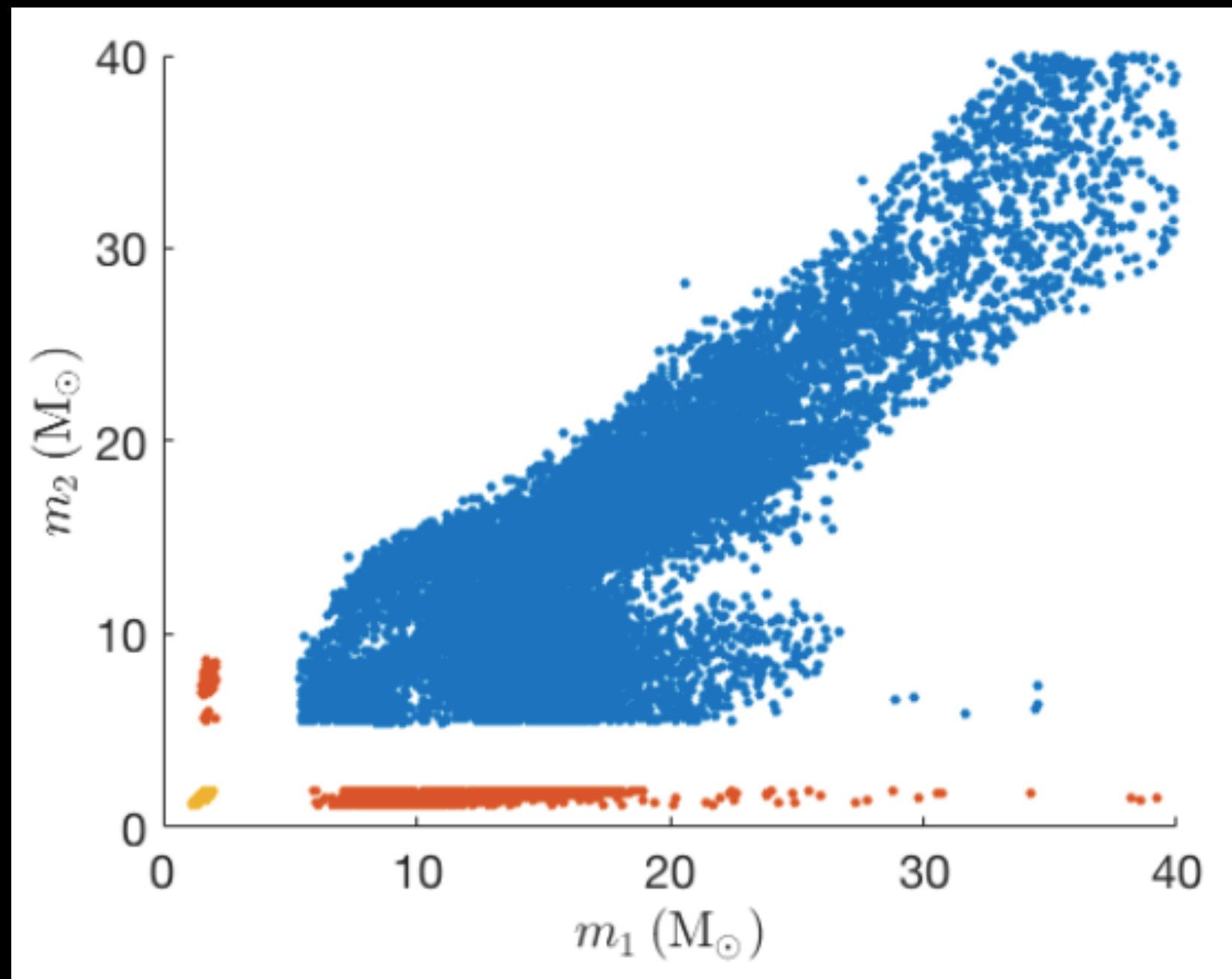
$$p(m_1) \propto m_1^{-\alpha} \quad \text{flat } q$$



Abbott+ (LVC), 2016

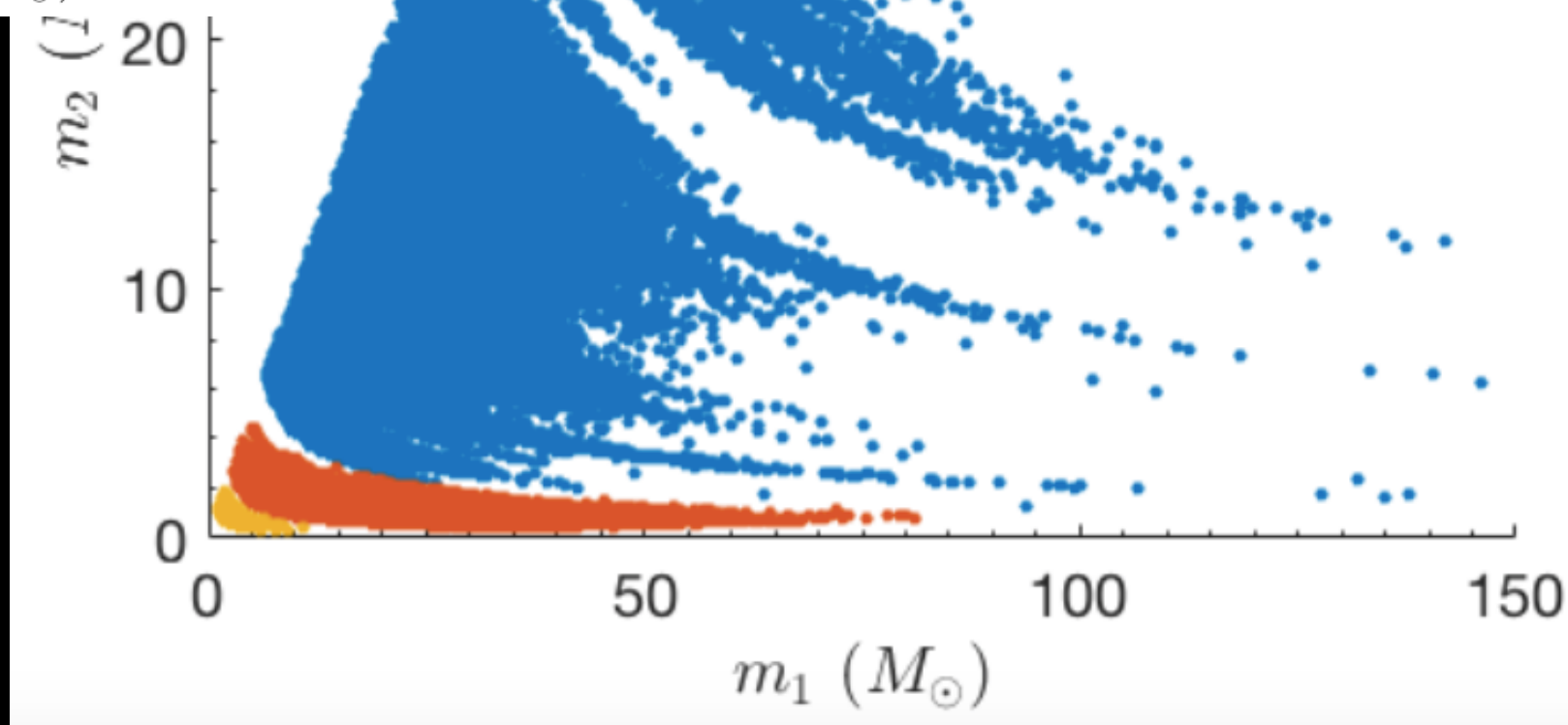
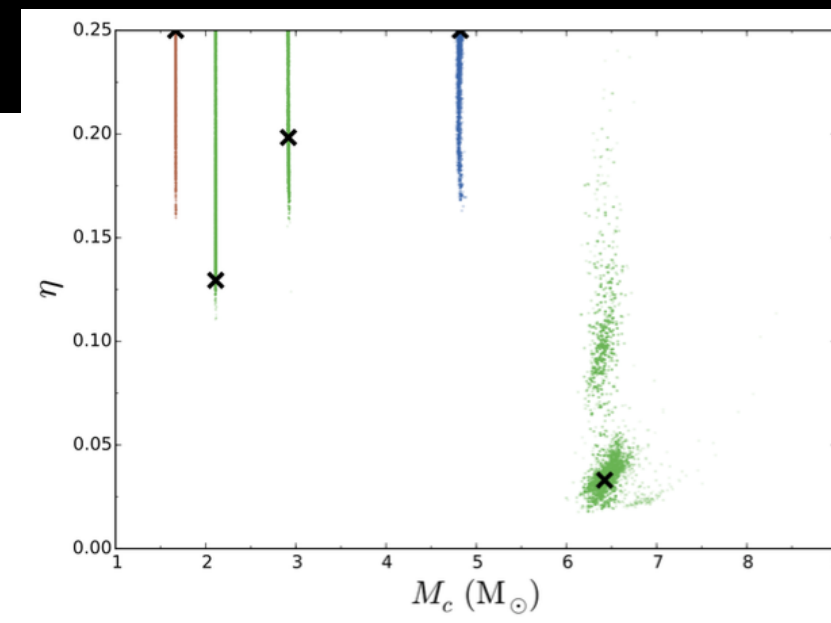
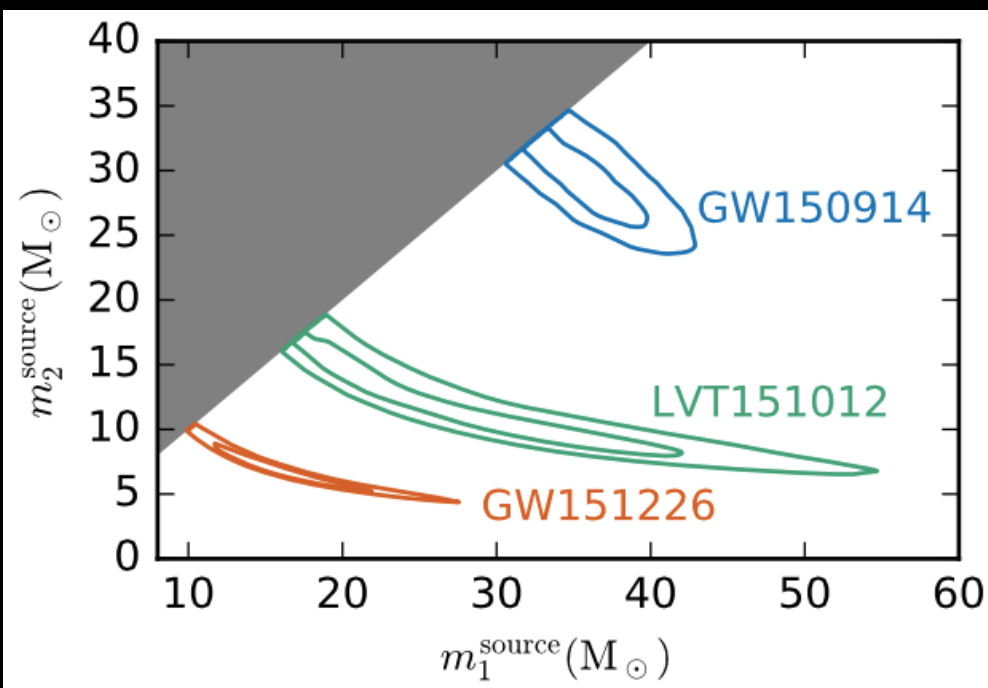
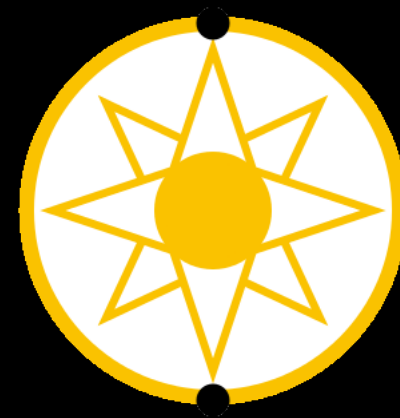
$$h(f) \sim M^{5/6} \Rightarrow V \sim M^{2.5}$$

Unmodeled Inference: Binary population clustering



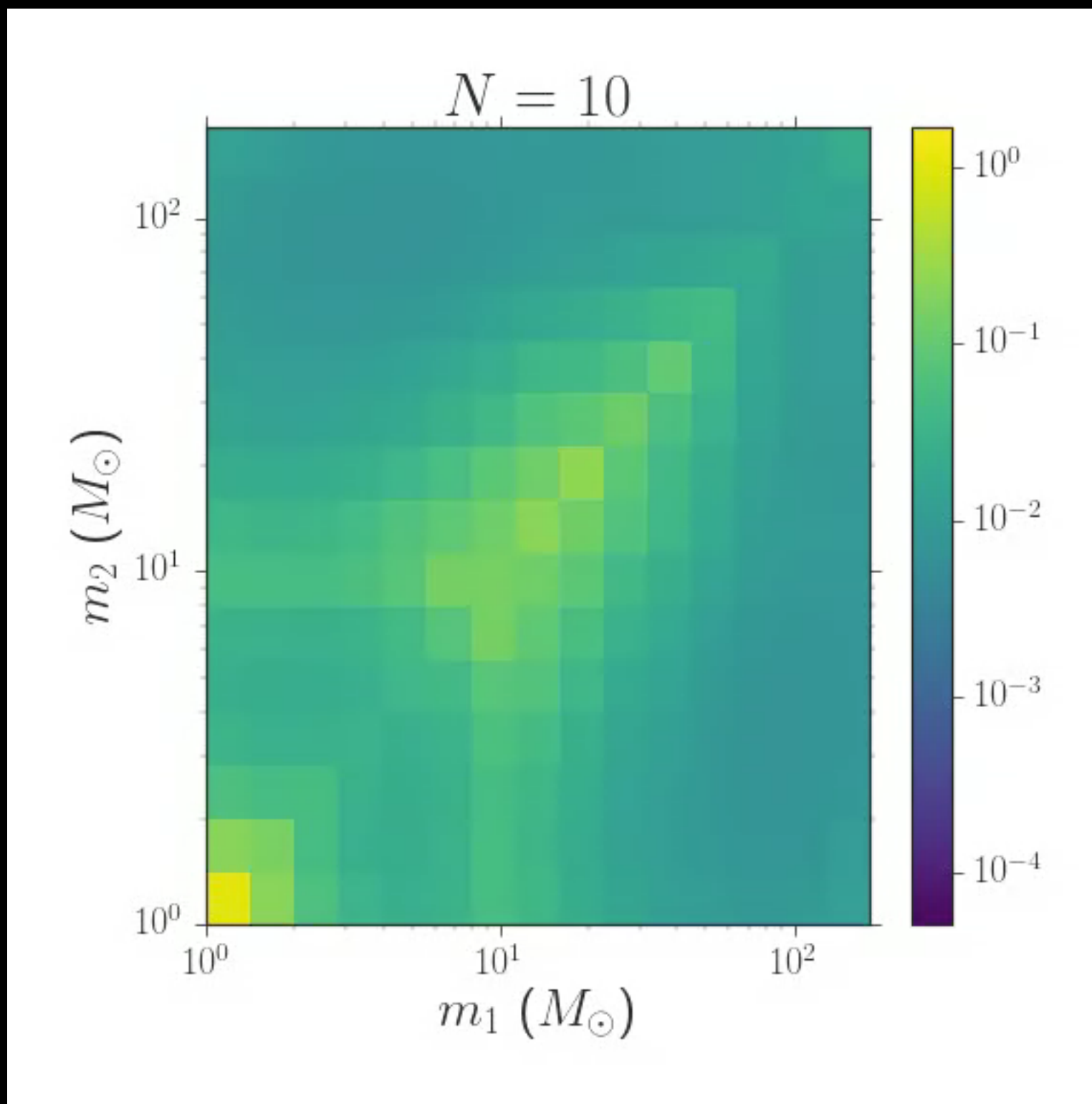
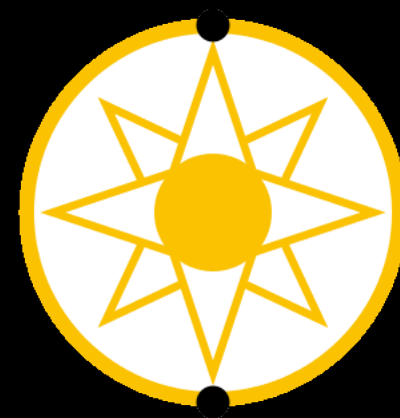
[Mandel et al., 2015 based on Dominik et al., 2015]

Measurement uncertainty

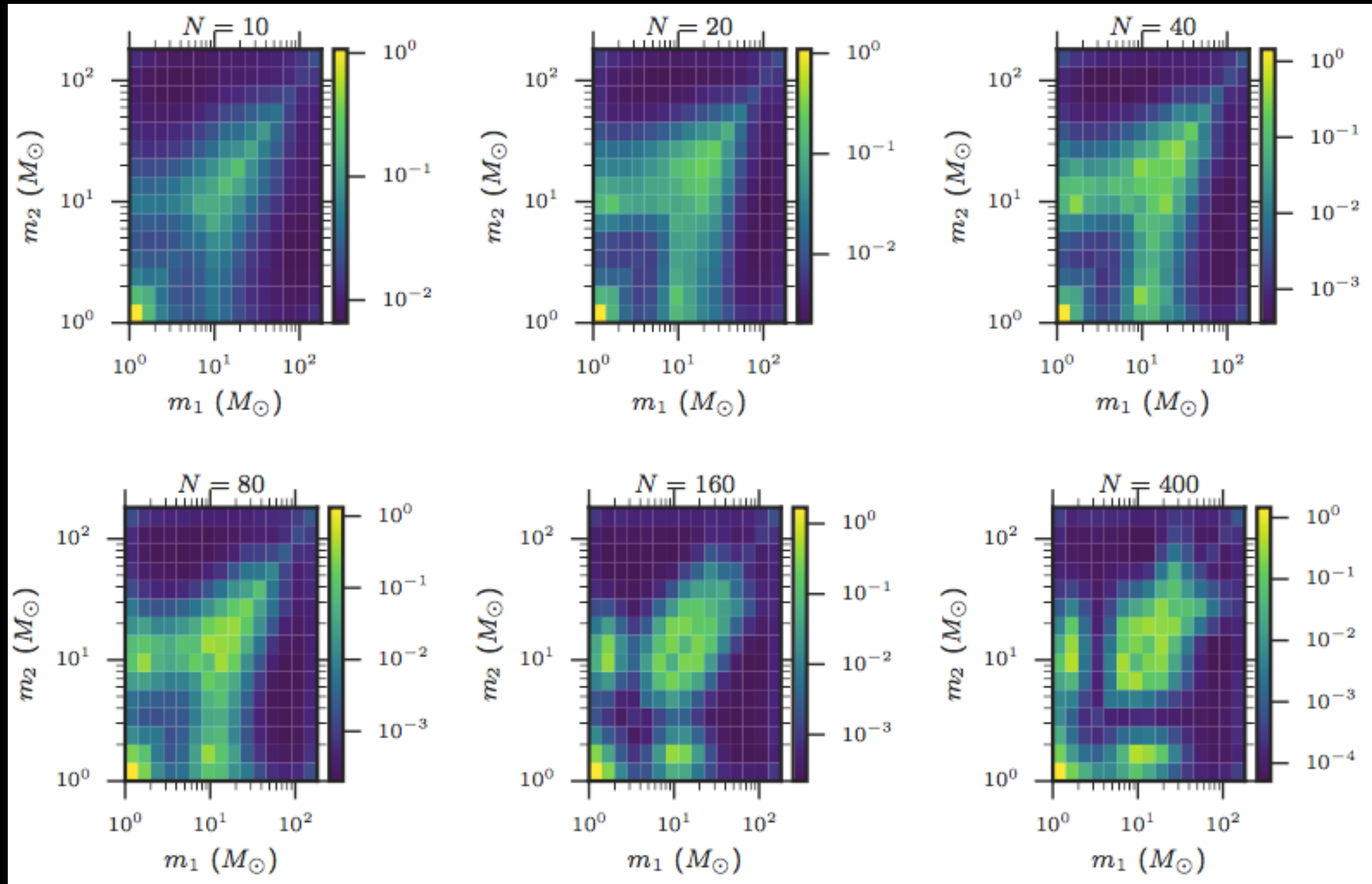
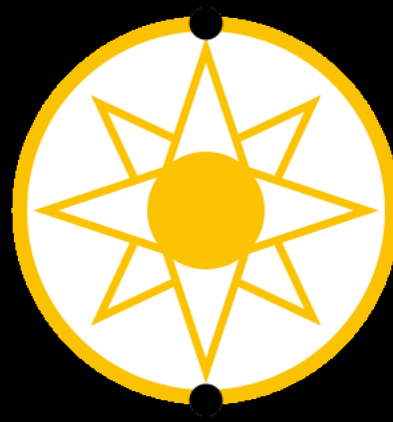


[Abbott et al., 2016; Mandel et al., 2015; see also Littenberg et al., 2015]

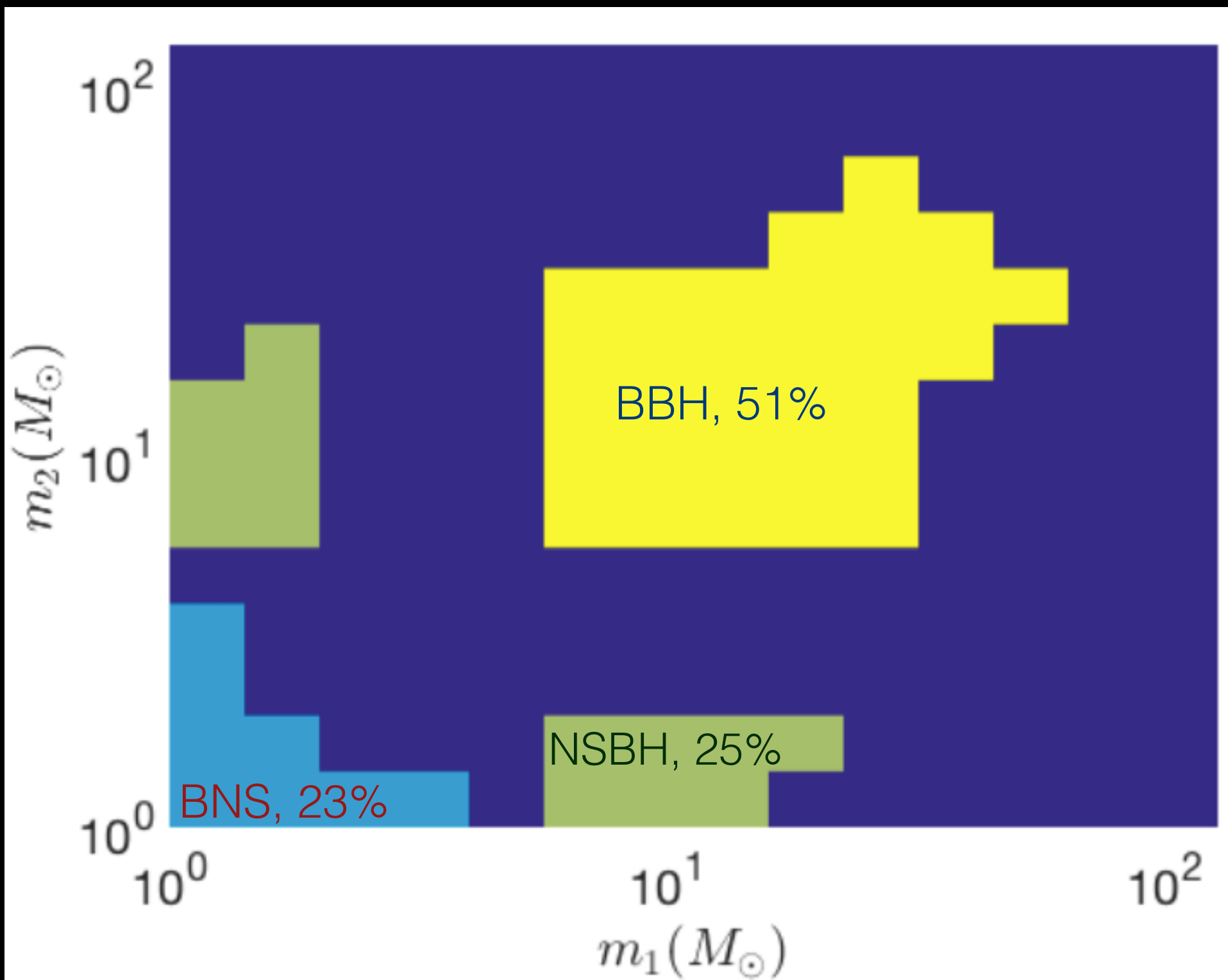
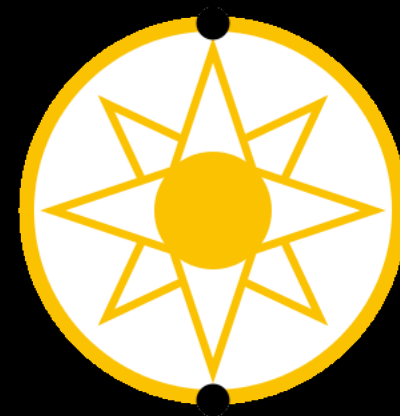
Mean inferred bin density



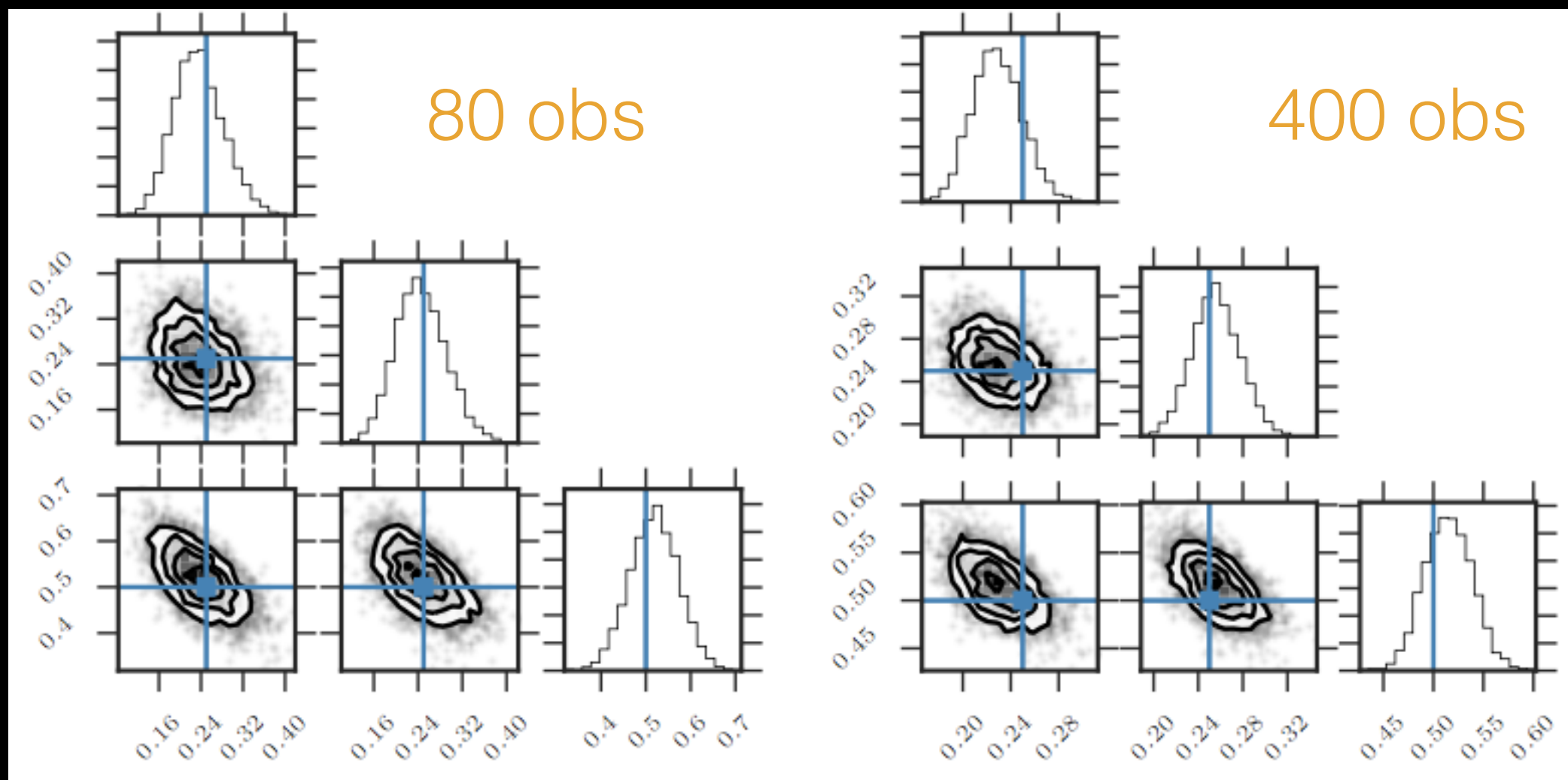
Mean inferred bin density



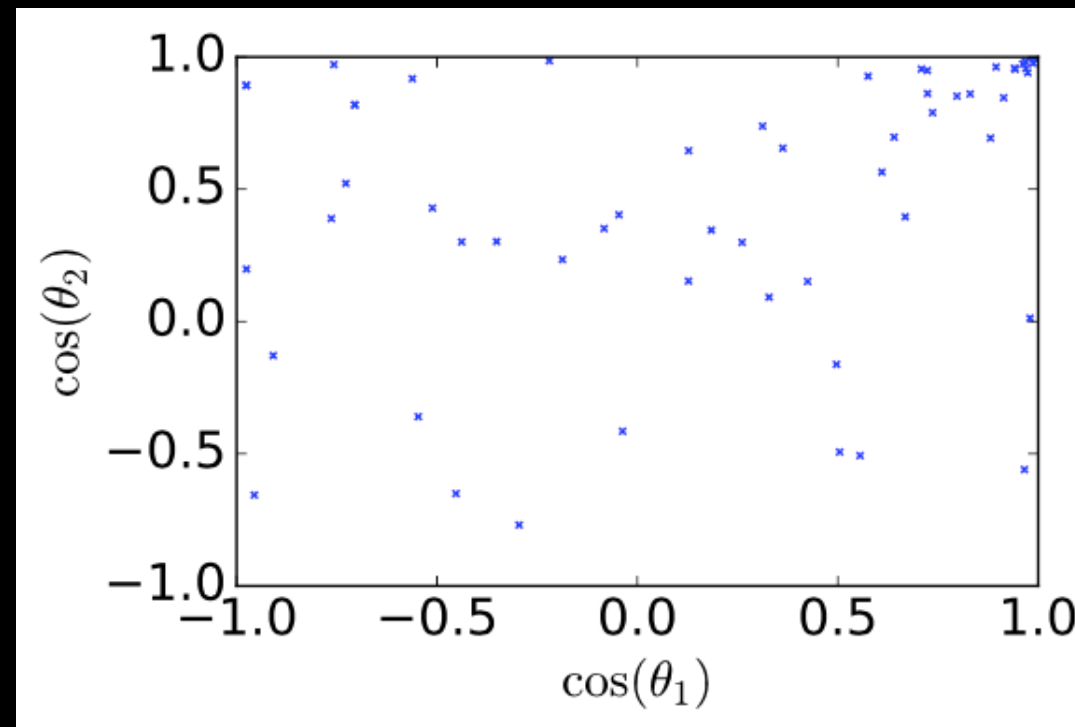
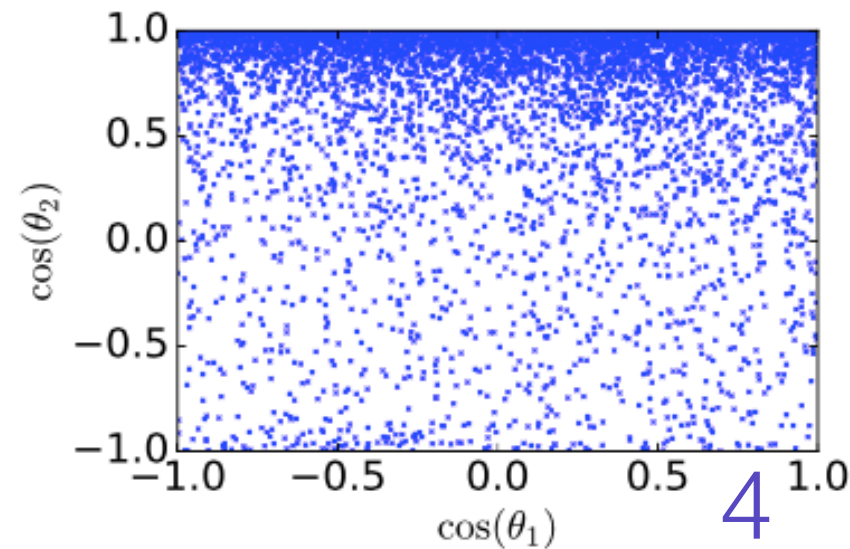
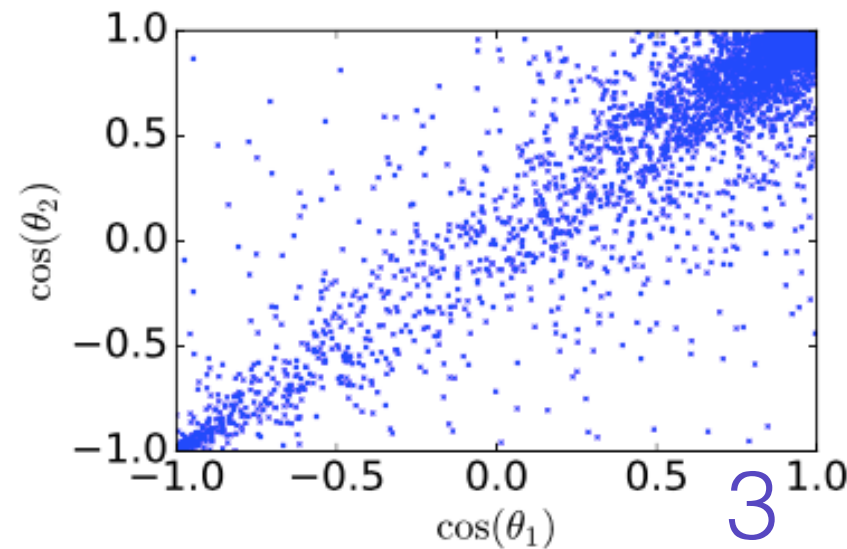
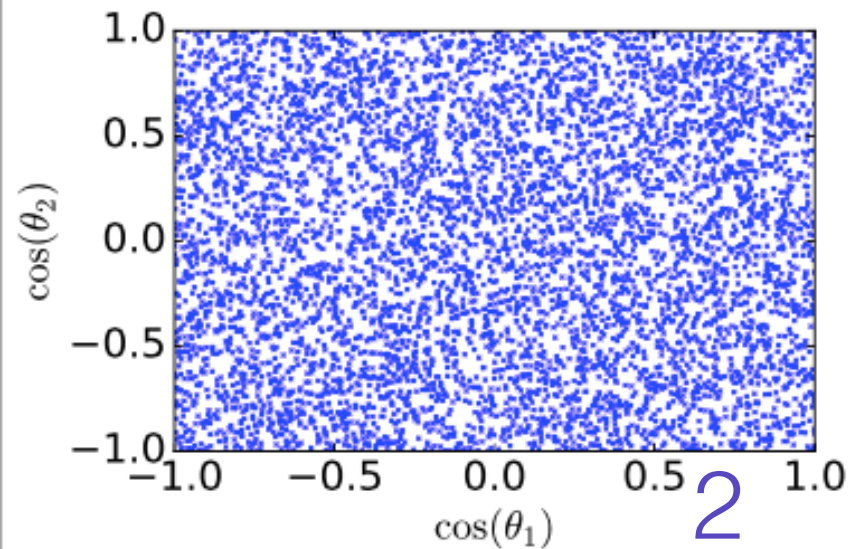
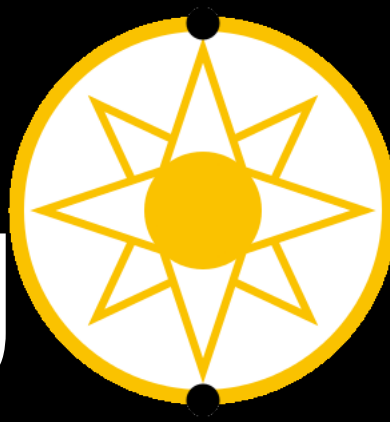
Water filling on mean density



Unmodeled Inference

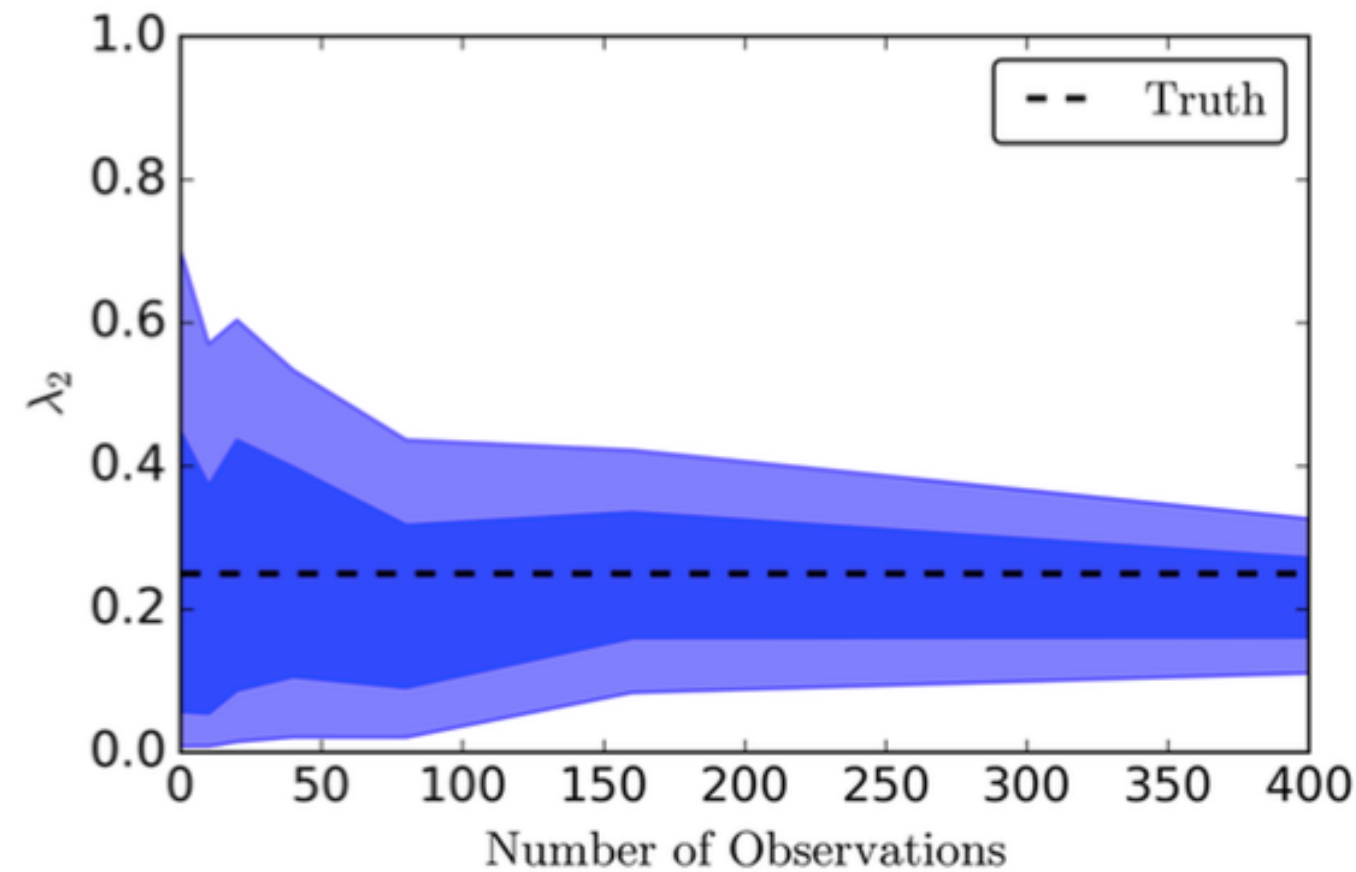
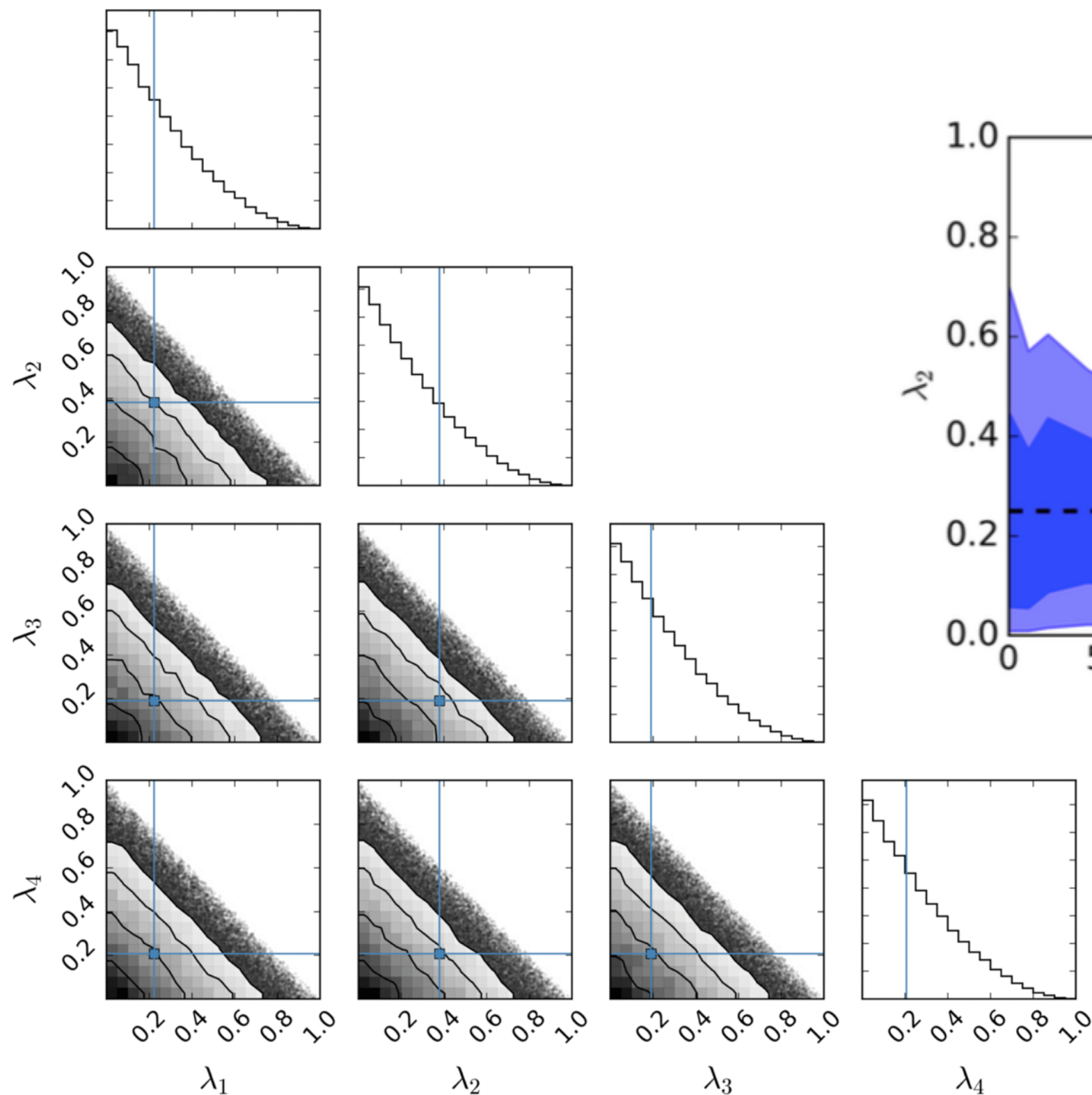
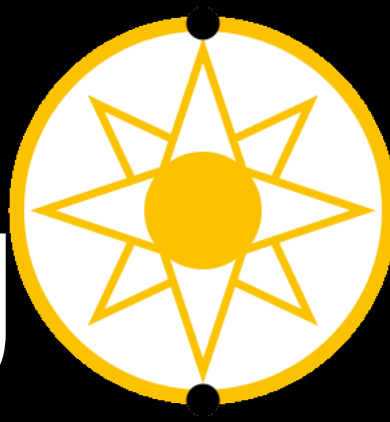


Hierarchical modeling



Stevenson, Berry, Mandel, 2017

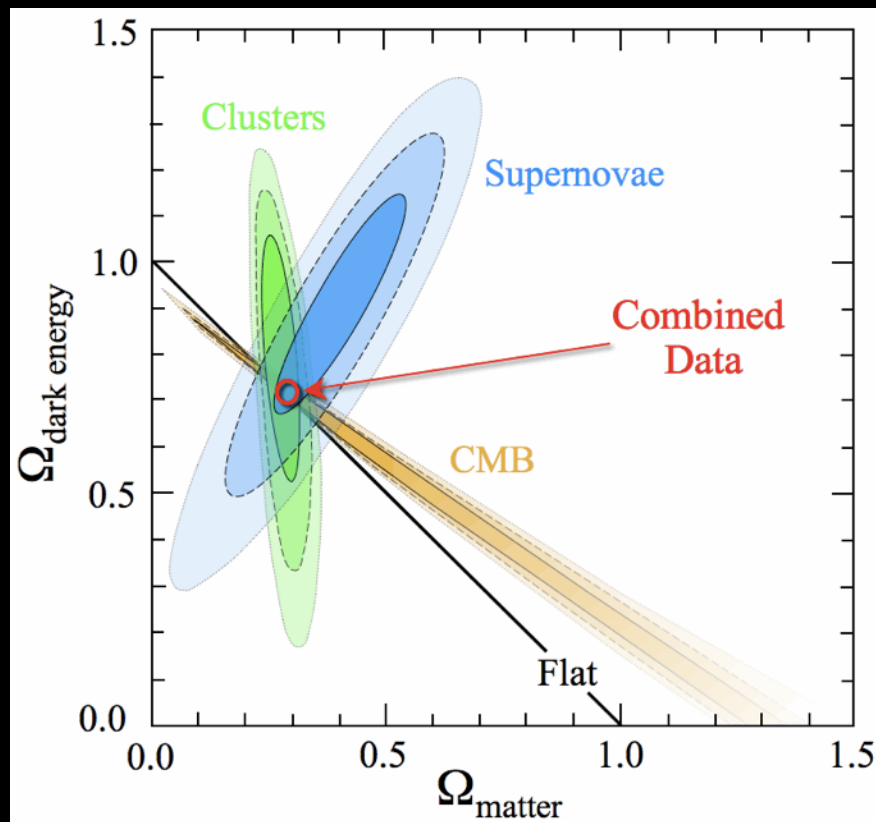
Hierarchical modeling



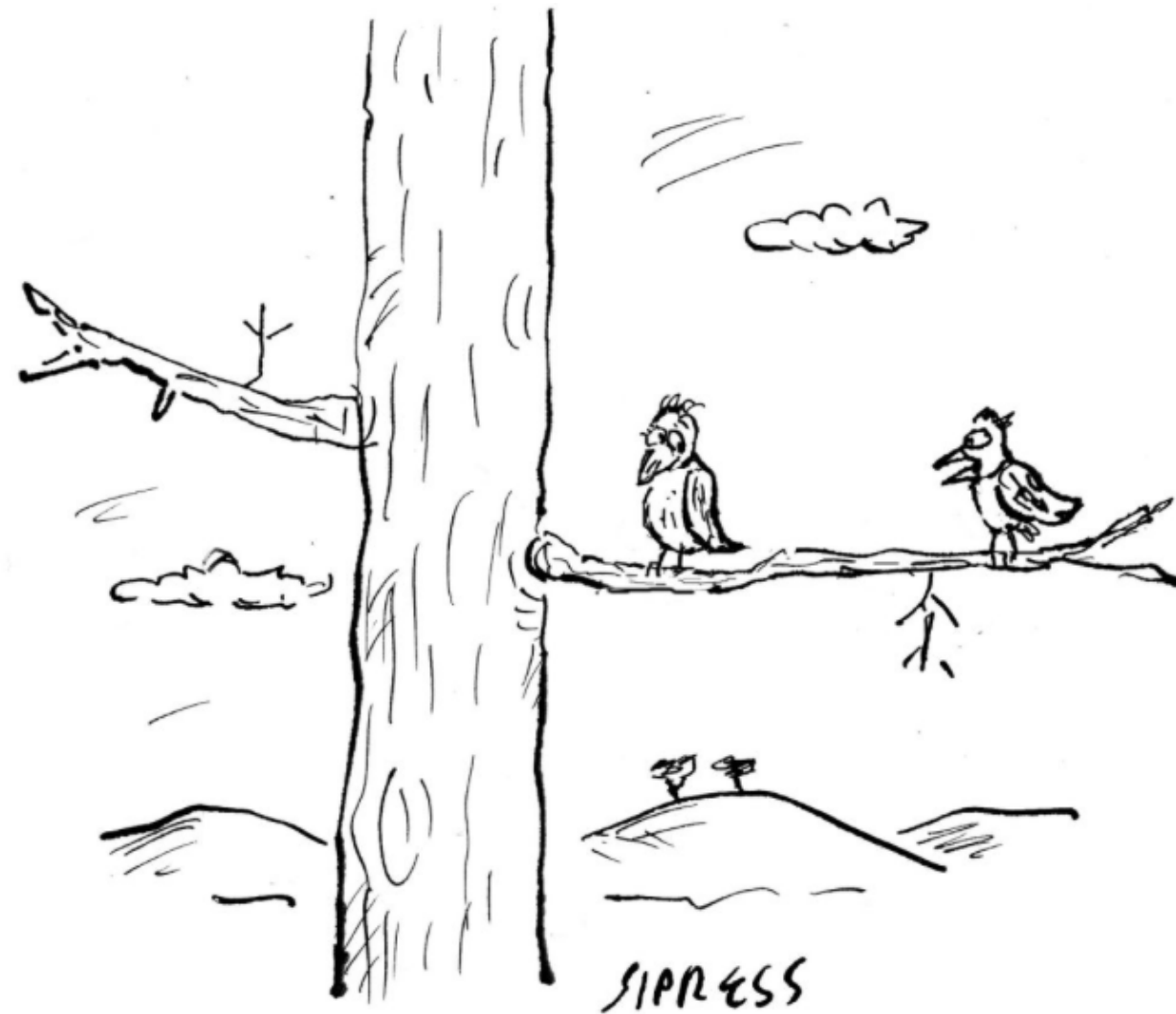


Future

- Bring together modelling and astrostatistics
- Figure out what questions we can realistically answer... and answer them!
- Use full observation set — concordance binary evolution?



Gravitational-wave astrophysics: the future is *now*



"Was that you I heard just now, or was it two black holes colliding?"

Ilya Mandel
University of Birmingham