

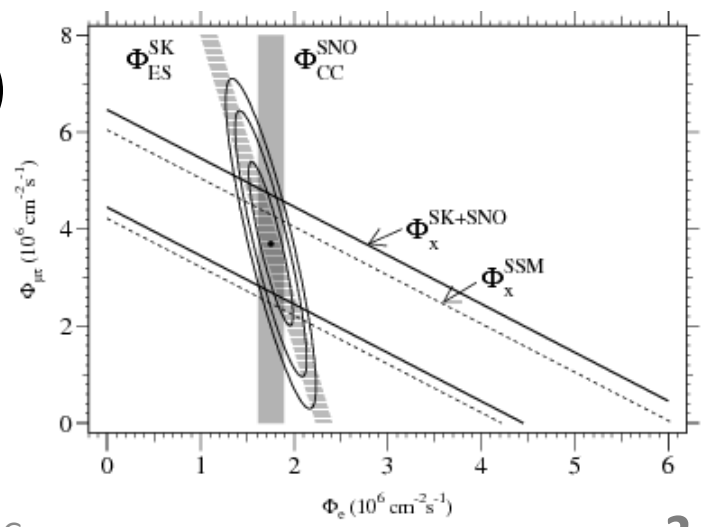
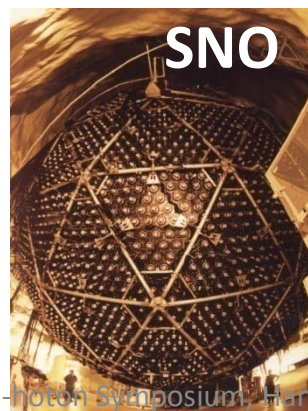
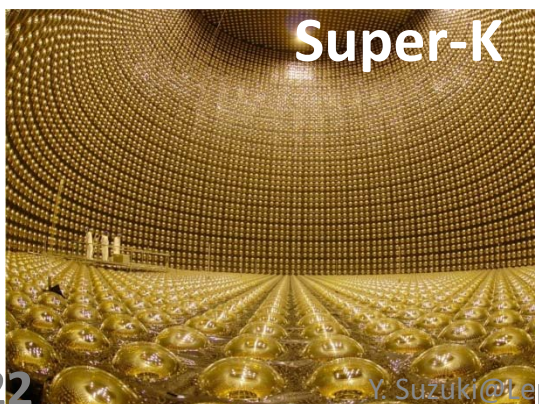
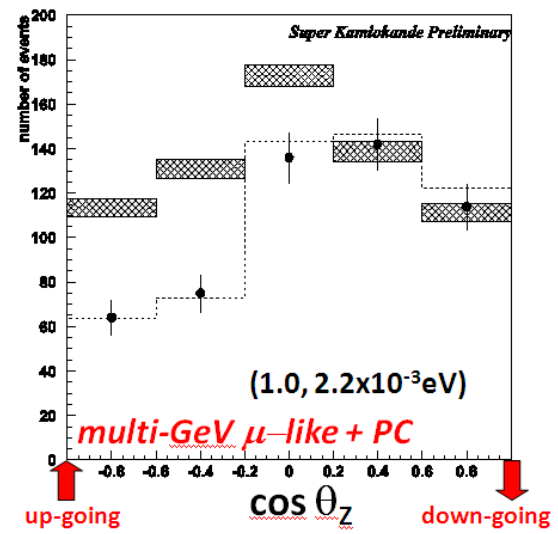
Solar and Atmospheric Neutrinos

Yoichiro Suzuki

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The University of Tokyo, and
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the Universe (IPMU), The University of Tokyo

Discovery of Neutrino Oscillation

- 1998: Atmospheric Neutrino Oscillation (*Super-Kamiokande*)
 - Asymmetry in zenith angle distribution
 - ν_μ deficits (up-going)
- 2001: Solar Neutrino Oscillation (*SNO+Super-Kamiokande*)
 - SNO: charged current $\rightarrow \nu_e$
 - SK: Electron Scattering $\rightarrow \nu_e + 0.15(\nu_\mu + \nu_\tau)$



Oscillation Parameters

~10 years after the discovery

mixing: $\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$

flavor eigenstates mass eigenstates

$$U_{\alpha i} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13} e^{-i\delta} \\ 0 & 1 & 0 \\ s_{13} e^{-i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Atmospheric ν
Long baseline
(θ_{23} : maximal?)

Reactor, LongBL
(θ_{13} : upper limit)
Not determined yet

Solar ν
Reactor LBL
(θ_{12} : large)

Current

Best parameter value from a single experiment (except solar ν)

$\Delta m_{12}^2 = 7.58_{-0.20}^{+0.21} \times 10^{-5} \text{ eV}^2$	(~ 3% @ $\Delta\chi^2 = 1$)	[KamLAND : PRL100 , 221803 (08)]
$\sin^2 \theta_{12} = 0.31_{-0.02}^{+0.02}$	(~ 7% @ $\Delta\chi^2 = 1$)	[All solar experiments] done by SNOGr.
$\Delta m_{23}^2 = 2.43_{-0.13}^{+0.13} \times 10^{-3} \text{ eV}^2$	(~ 5% @ $\Delta\chi^2 = 1$)	[MINOS : PRL101 , 131802 (2008)]
$= 2.19_{-0.13}^{+0.14} \times 10^{-3} \text{ eV}^2$	(~ 6% @ $\Delta\chi^2 = 1$)	[SuperK : Atmospheric ν L / E]
$\sin^2 \theta_{23} = 0.51_{-0.07}^{+0.05}$	(~ 14% @ $\Delta\chi^2 = 1$)	[SuperK : Atmospheric ν 3f]
$\sin^2 \theta_{13} < 0.04$	(@ 90% C.L.)	[CHOOZ]

- Solar – Atmospheric; better sensitivities for mixing angles
- Reactor; better sensitivities for solar mass difference
- Accelerator; will be better in atmospheric mass difference

Missing parameters: θ_{13} and CP phase

Oscillation Parameters

~10 years after the discovery

mixing:
$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

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(θ_{23} : maximal?)

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$\Delta m_{23}^2 = 2.43_{-0.13}^{+0.13} \times 10^{-5} \text{ eV}^2$

$= 2.19_{-0.13}^{+0.14} \times 10^{-3} \text{ eV}^2$

$\sin^2 \theta_{23} = 0.51_{-0.07}^{+0.05}$

$\sin^2 \theta_{13} < 0.04$

SK Atm- ν : $\sin^2 \theta_{13} < 0.06$

K2K: $\sin^2 \theta_{13} < 0.075$ PRL93(04)

MINOS: $\sin^2 \theta_{13} < 0.073$ PRL101(08)

($\sim 14\% @ \Delta\chi^2 = 1$) [SuperK • Atmospheric ν SJ]

(@ 90% C.L.) [CHOOZ]

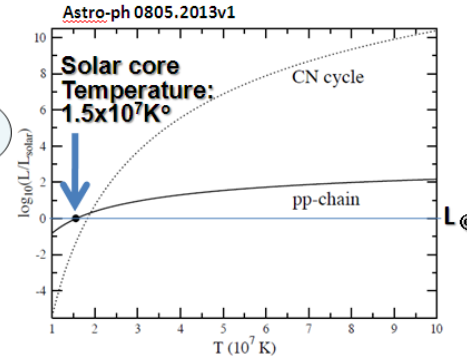
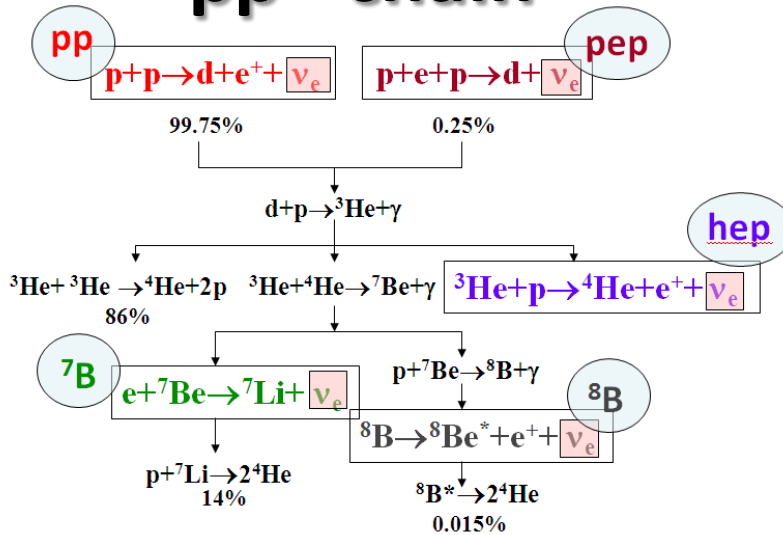
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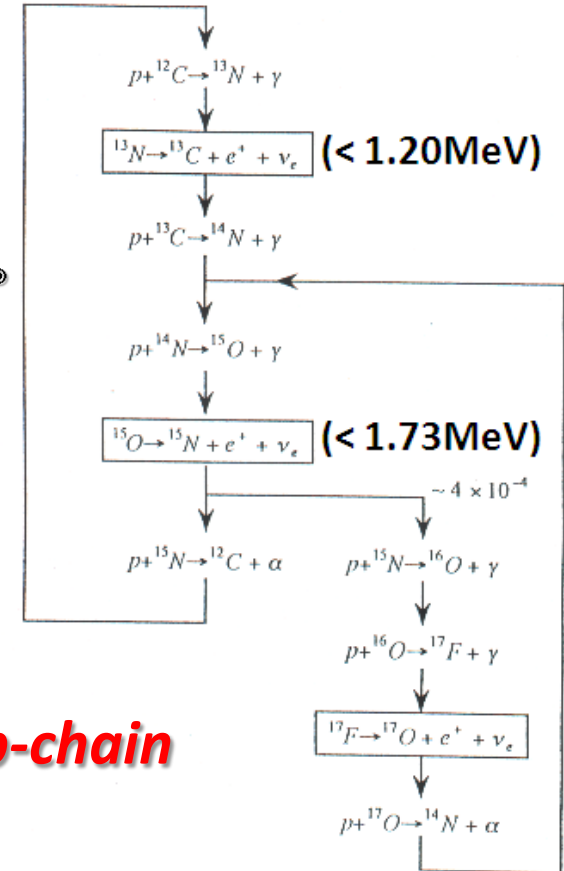
Solar Neutrinos

pp chain and CNO cycle

pp - chain



CNO cycle



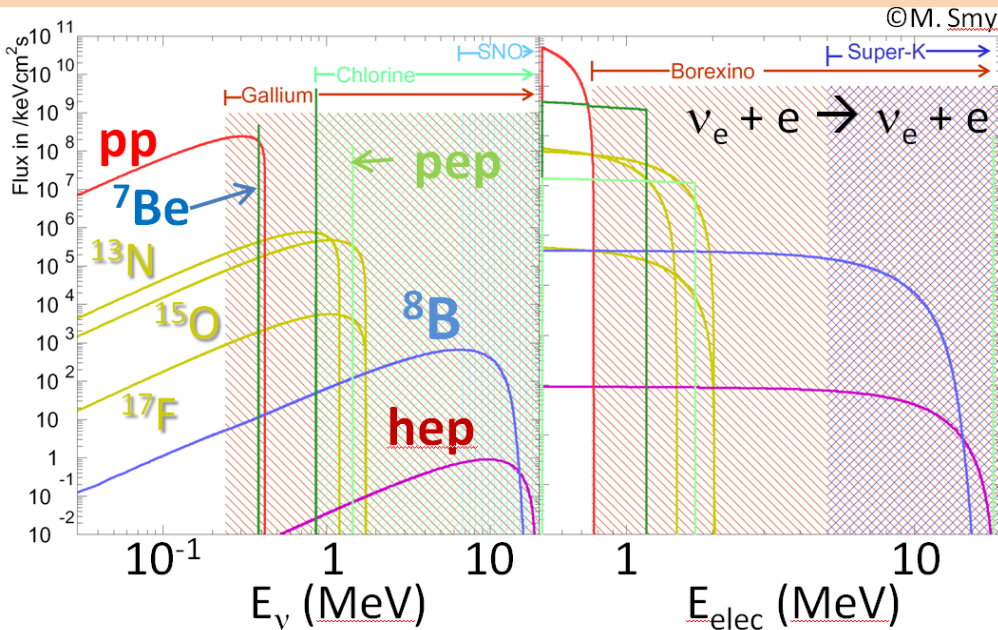
pp-chain

- Dominant process in the sun
- 5 processes produce neutrinos
- Detection of the ${}^8\text{B}$ neutrinos is a proof of pp-chain

CNO cycle

- Hydrogen is burned using a carbon as a catalyst
- < 1% of the solar energy production
- Relatively low energy neutrinos are produced

Neutrino Spectrum and Solar Neutrino Experiments



• Radio-Chemical

– Ga: **SAGE, GALLEX/GNO** (pp, ^7Be)

$\nu_e + ^{71}\text{Ga} \rightarrow e + ^{71}\text{Ge}: E_\nu > 235\text{keV}$
 Meas: 66.1 ± 3.1 SNU; $R=0.52$
 Pred: $127.9^{+8.1}_{-8.0}$ SNU_{BPS08(GS)}

– Cl: **Homestake** (^8B , ^7Be ,...)

$\nu_e + ^{37}\text{Cl} \rightarrow e + ^{37}\text{Cl}: E_\nu > 816\text{keV}$
 Meas: $2.56 \pm 0.16 \pm 0.16$ SNU
 Pred: $8.46^{+0.87}_{-0.88}$ SNU_{BPS08(GS)}

• Real time Counter

– H₂O: **Kamiokande(ES)** (^8B)

– H₂O: **Super-Kamiokande(ES)** (^8B)

$$\phi_{^8\text{B}}^{\text{SK-I}} = 2.35 \pm 0.02 \pm 0.08 \times 10^6 \text{cm}^2$$

$$\text{Pred: } 5.94(1 \pm 0.11) \times 10^6 \text{cm}^2_{\text{BPS08(GS)}}$$

– D₂O: **SNO(CC, NC, ES)** (^8B)

$$\phi_{^8\text{B}}^{\text{SNOIII(CC)}} = 1.67^{+0.05}_{-0.04} \text{ } ^{+0.07}_{-0.08} \times 10^6 \text{cm}^2$$

$$\phi_{^8\text{B}}^{\text{SNOIII(NC)}} = 5.54^{+0.33}_{-0.31} \text{ } ^{+0.36}_{-0.34} \times 10^6 \text{cm}^2$$

– Scinti: **Borexino** (ES) (^7Be , ^8B)

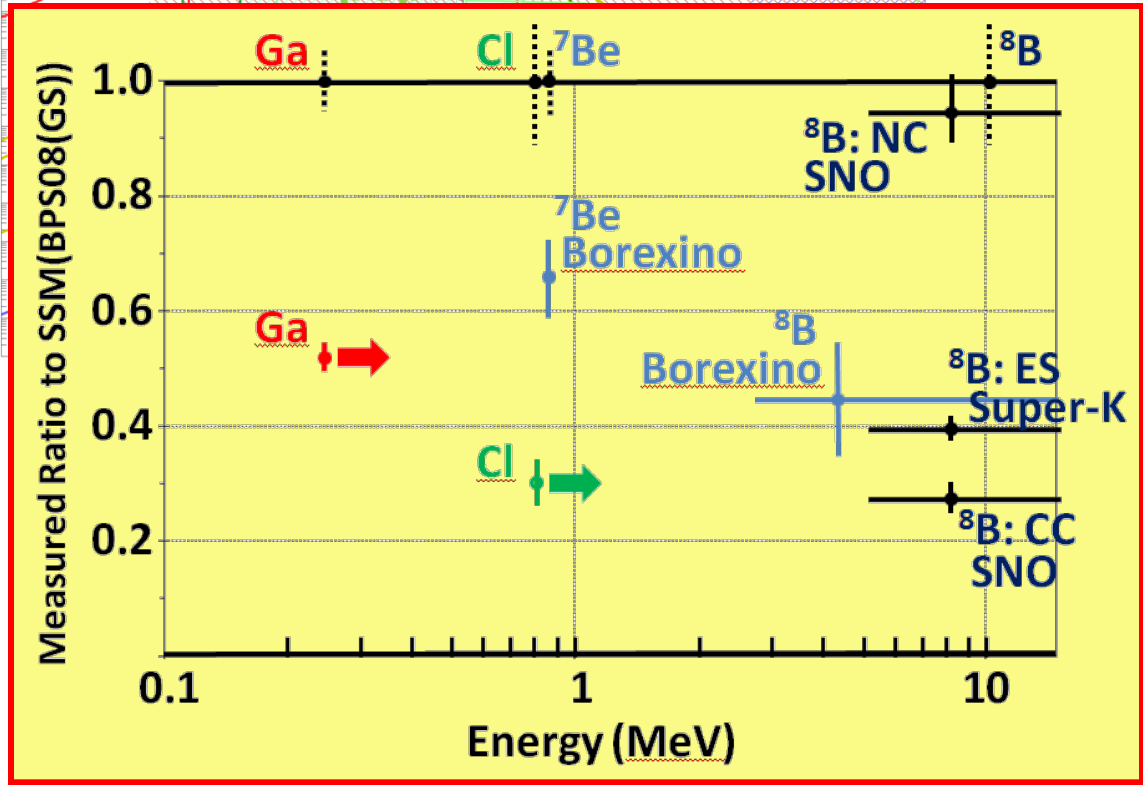
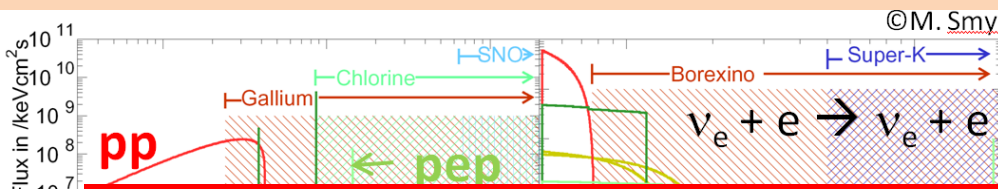
^7Be : Meas: $49 \pm 3_{\text{sta}} \pm 4_{\text{sys}}$ c/day/100ton

^7Be : Pred: 74 ± 4 c/day/100ton_{BPS08(GS)}:

^7Be : Pee($\nu_e \rightarrow \nu_e$) = $0.56 \pm 0.10(1\sigma)$

^8B : $\phi_{^8\text{B}}^{\text{Borexino}} = 2.65 \pm 0.44 \pm 0.18 \times 10^6 \text{cm}^2$

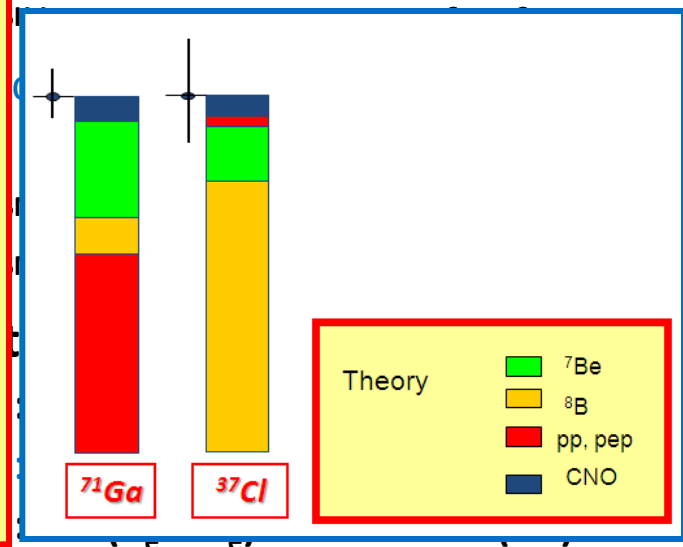
Neutrino Spectrum and Solar Neutrino Experiments



— Cl: Homestake

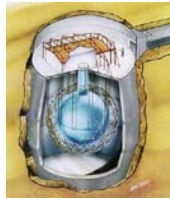
$\nu_e + {}^{37}\text{Cl} \rightarrow e + {}^{37}\text{Cl}; E_\nu > 816\text{keV}$
 Meas: $2.56 \pm 0.16 \pm 0.16$ SNU
 Pred: $8.46^{+0.87}_{-0.88}$ SNU_{BPS08(GS)}

Time Counter
 Kamiokande(ES)
 Super-Kamiokande(ES)

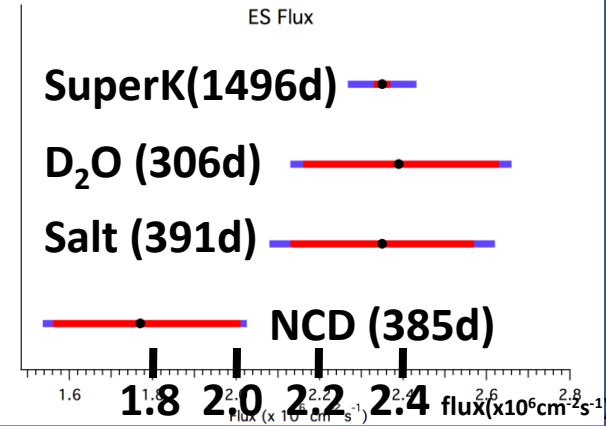
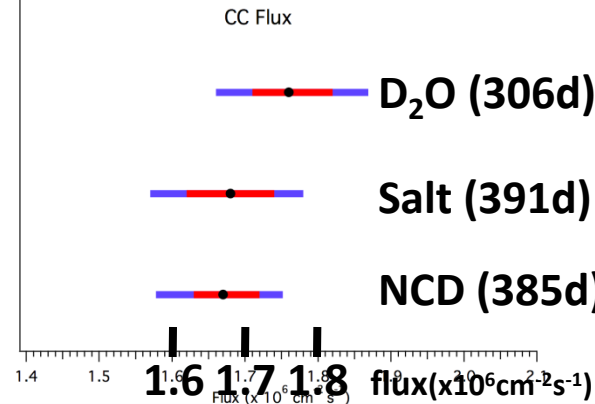
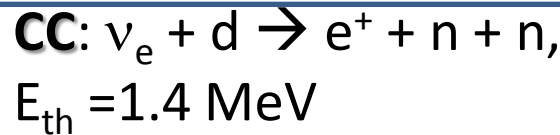
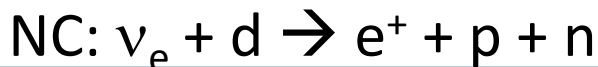


${}^8\text{B}: \phi_{8\text{B}}^{\text{Borexino}} = 2.65 \pm 0.44 \pm 0.18 \times 10^6 \text{cm}^2$

Neutral Current Measurements by SNO



SNO: 1000tons D₂O
Started in Nov-99, and
completed in Dec-06



NC: 3 neutron detection methods:

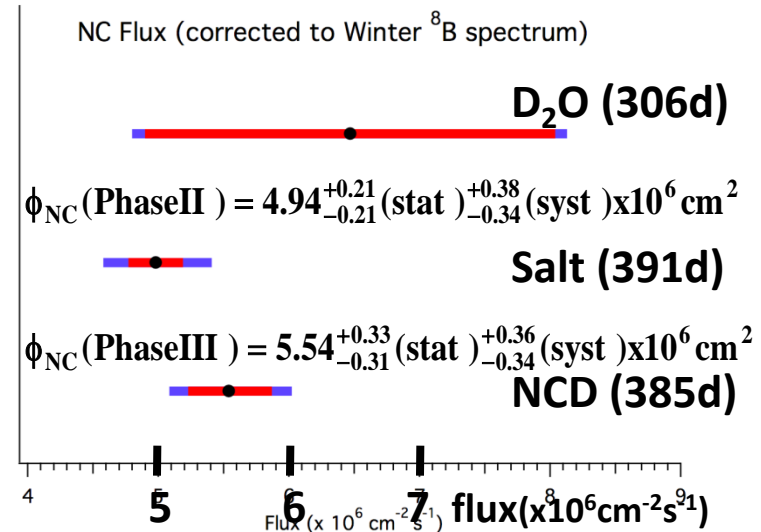
Phase I: D₂O, $^2\text{H}(n,\gamma)^3\text{H}$, 6.25 MeV γ
 Eff. ~14.4%

Phase II: Salt, $^{35}\text{Cl}(n,\gamma)^{36}\text{Cl}$, 8.6MeV γ
 Eff. ~40%

Phase III: ^3He neutron counters
 $n + ^3\text{He} \rightarrow p + ^3\text{H}$
 Eff. ~30%, but separated detection

Comb. Error (NC): ~5.4% by hand (not from SNO)

↔ ~11% SSM(⁸B)

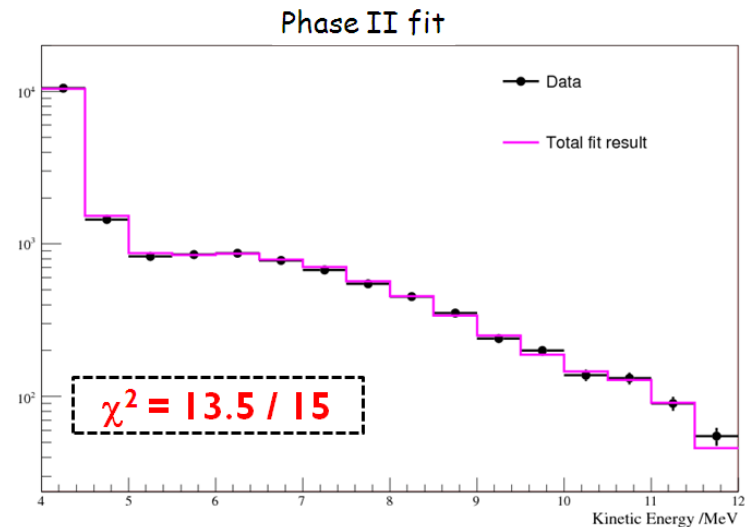
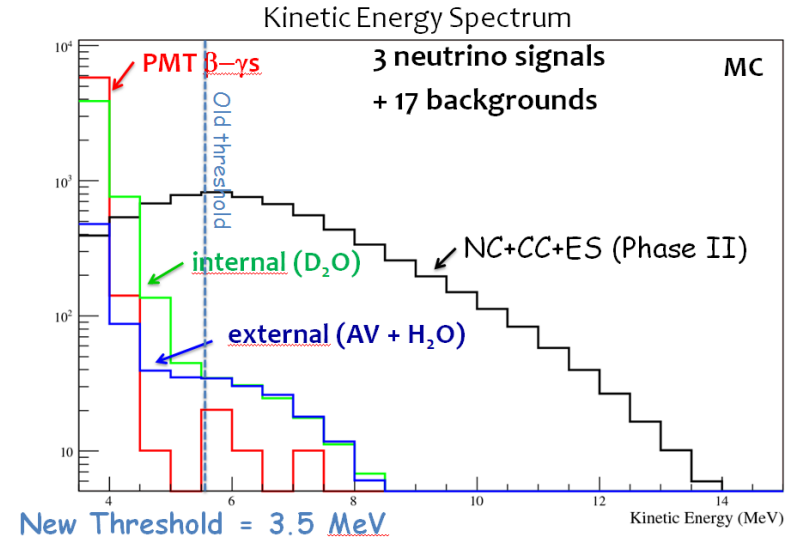


SNO LETA

- **Phase I (>5MeV)+II(5.5MeV) will be jointly analyzed down to $T_{\text{eff}} \sim 3.5 \text{ MeV}$**

- CC interaction down to $E_{\nu} \sim 6 \text{ MeV}$
- More than 50% increase of events for NC
- But many backgrounds (background dominates)
 - Reduce BG
 - Reduce systematics
 - Make pdf for signals and backgrounds

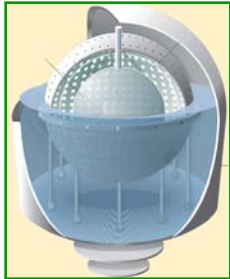
- **Expect significant improvements of the SNO results soon**



PRELIMINARY

Borexino ^7Be and CNO

- **270t liquid scintillator**



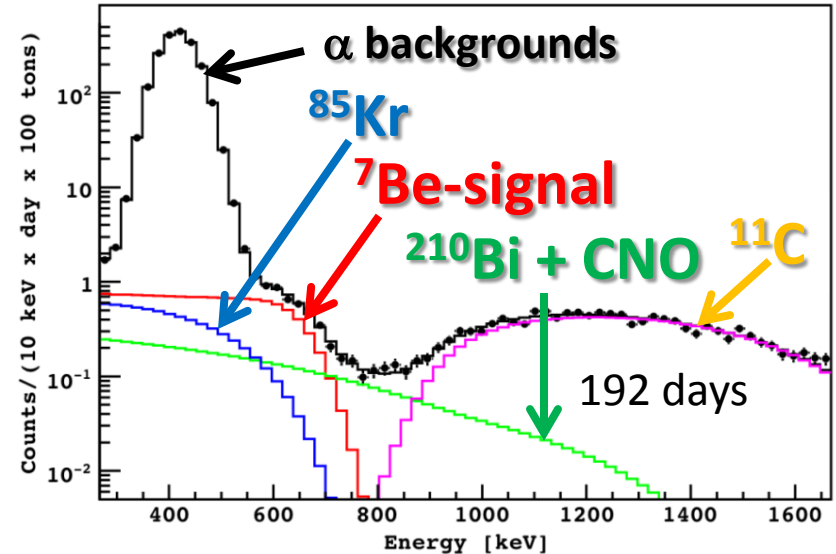
- PC + PPO in a 150mm thick nylon vessel
- Graded shielding
- Two oil layers and water shields

- **^7Be (192days):**

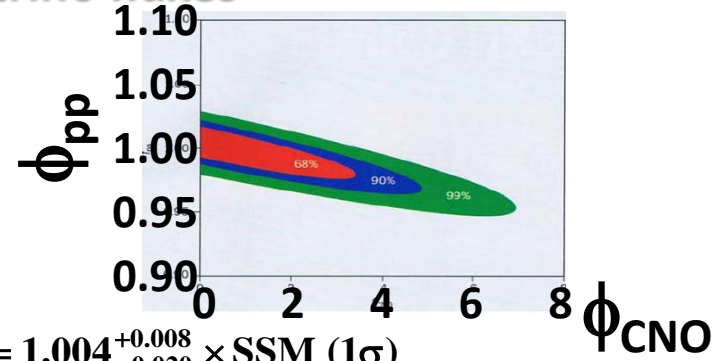
- Meas. $49 \pm 3_{\text{stat}} \pm 4_{\text{sys}}$ c/day/100ton
- Pred. 74 ± 4 c/day/100ton_{BPS08(GS)}
 - BPS08(GS): $5.07(1 \pm 0.06) \times 10^9 / \text{cm}^2$
 - BPS07(GS) = 5.08 (Borexino paper)
- P_{ee} : ν_e survival prob. assuming SSM

$$P_{ee} \sim (P_{\text{meas}} - \sigma(\nu_e) / \sigma(\nu_{\mu, \tau})) / (1 - \sigma(\nu_e) / \sigma(\nu_{\mu, \tau}))$$

→ $P_{ee} = 0.56 \pm 0.10$ (1 σ)
@0.862MeV



Solar Model(+luminosity constraint), LMA and Borexino data
→ improve constraints on other neutrino fluxes



$$\phi_{pp} = 1.004^{+0.008}_{-0.020} \times \text{SSM} \text{ (1}\sigma\text{)}$$

$$\phi_{\text{CNO}} < 4.8 \times \text{SSM} \text{ (90\% C.L.)}$$

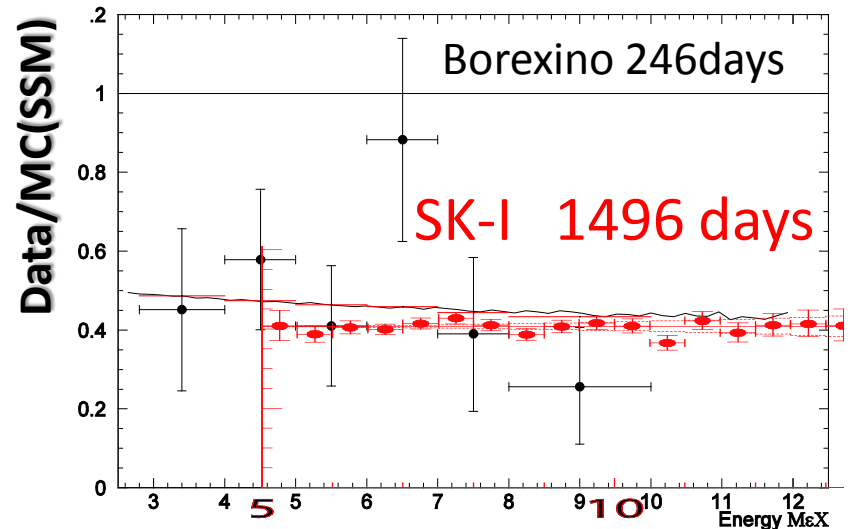
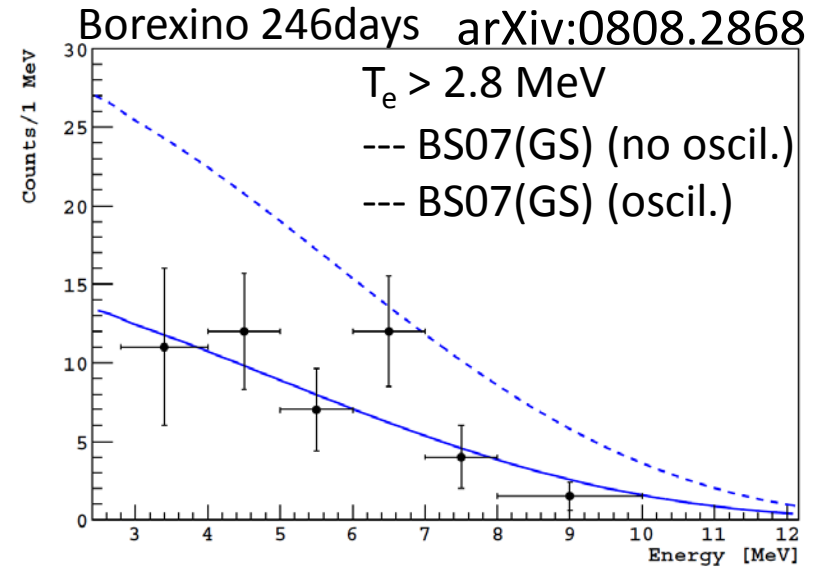
Borexino ^8B

- ^8B : $> 2.8 \text{ MeV}$
 - $\phi_{^8\text{B}}^{\text{Borexino}} = 2.65 \pm 0.44 \pm 0.18 \times 10^6 \text{ cm}^2$
- ^8B : $> 5 \text{ MeV}$ (SK: $> 4.5 \text{ MeV}$)
 - $\phi_{^8\text{B}}^{\text{Borexino}} = 2.75 \pm 0.54 \pm 0.17 \times 10^6 \text{ cm}^2$
 - $\phi_{^8\text{B}}^{\text{SK-I}} = 2.35 \pm 0.02 \pm 0.08 \times 10^6 \text{ cm}^2$
- $P_{ee} = 0.35 \pm 0.10$ at $\langle T_e \rangle = 8.6 \text{ MeV}$
(BPS07(GS) is used)

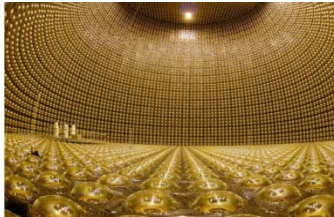
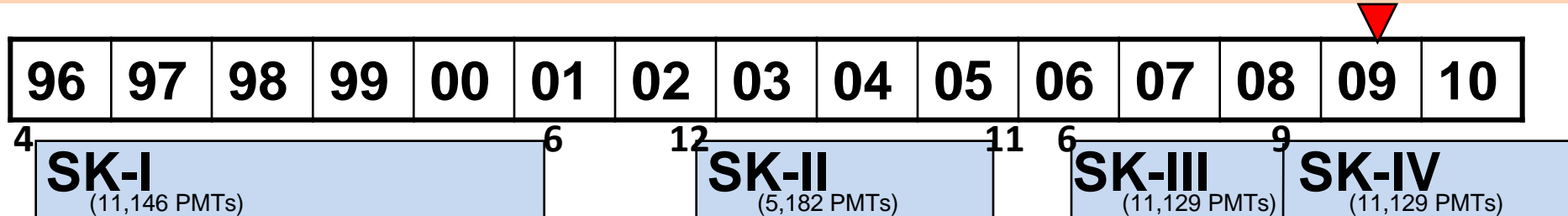
Note:

Super-K: Energy \leftarrow Total energy

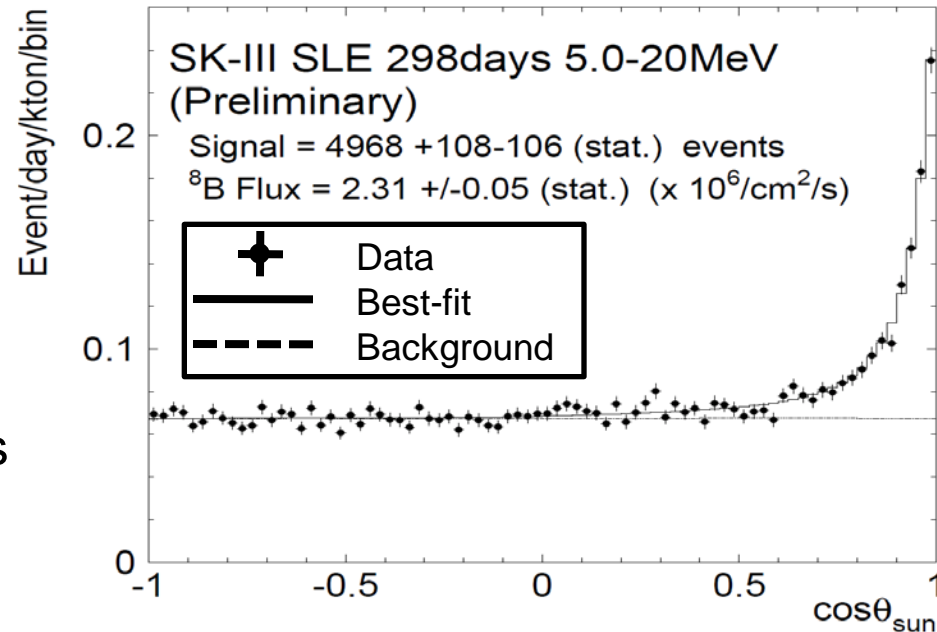
Borexino: Energy \leftarrow Kinetic energy



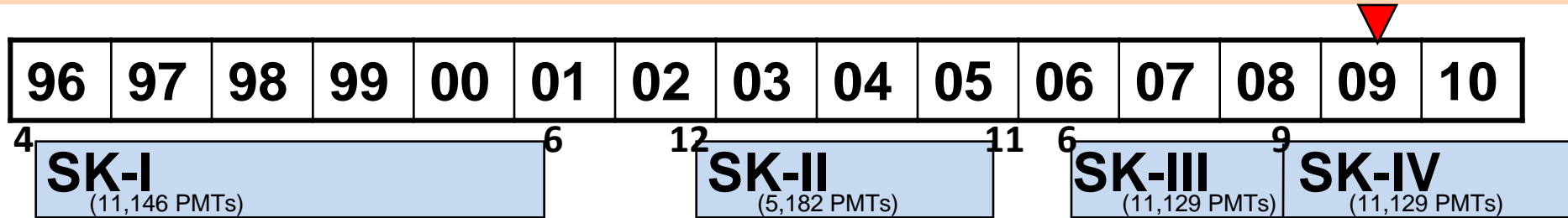
SK Solar ν is back on



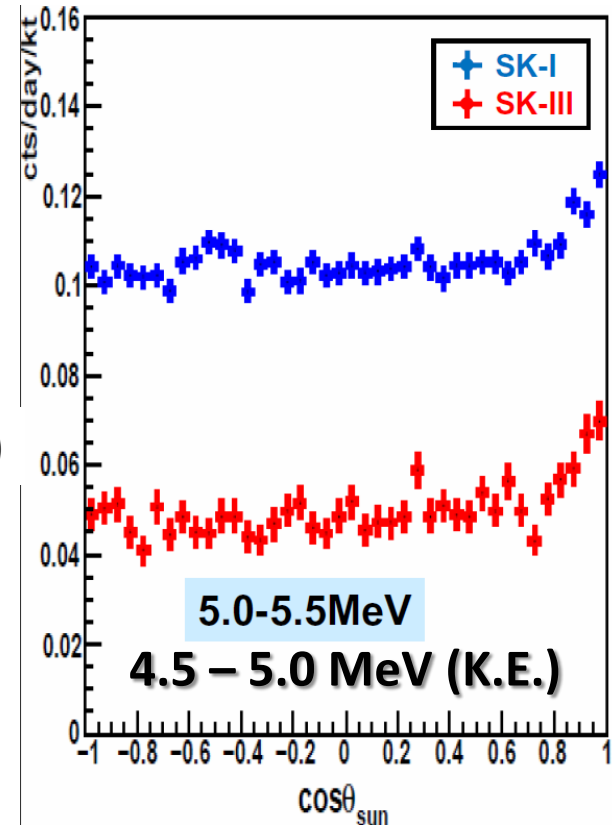
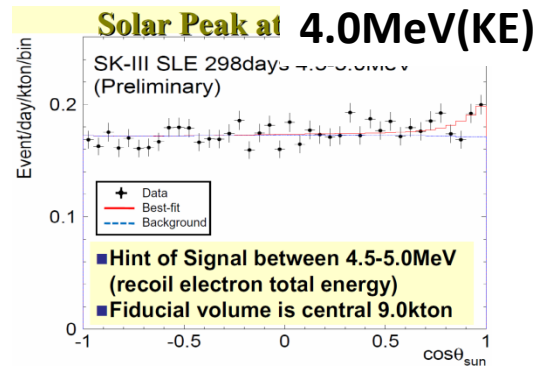
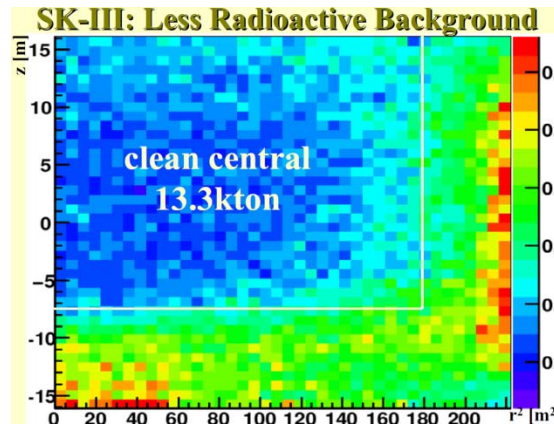
- **Full SK** was back on June-06
 → SK-III
 $2.31 \pm 0.05(\text{stat}) \times 10^6/\text{cm}^2\text{s}$
- SK-I ^8B flux:
 $2.35 \pm 0.02(\text{stat}) \pm 0.08(\text{sys}) \times 10^6/\text{cm}^2\text{s}$
- consistent with SK-I flux within statistical uncertainty
- SK is now back in solar neutrino business



SK Solar ν is back on



- New electronics on September 09 → SK IV
- Lower background was achieved
- Threshold: 4 MeV (KE)
- Aim to measure transition region down to 4 MeV or may be 3.5 MeV



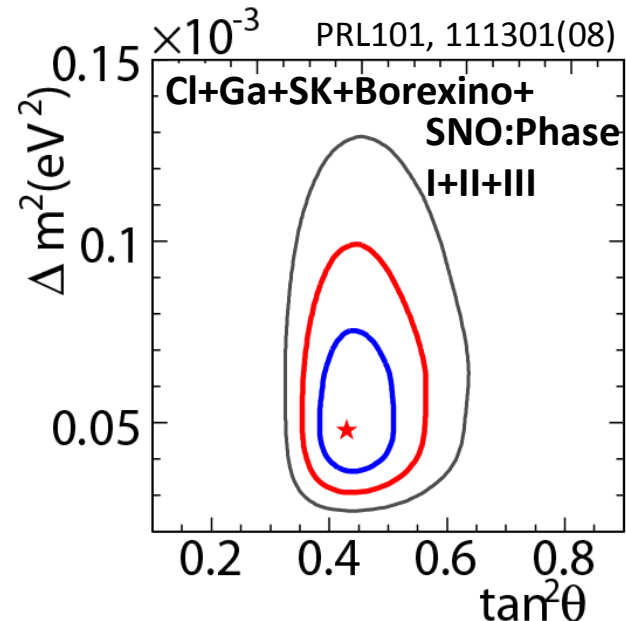
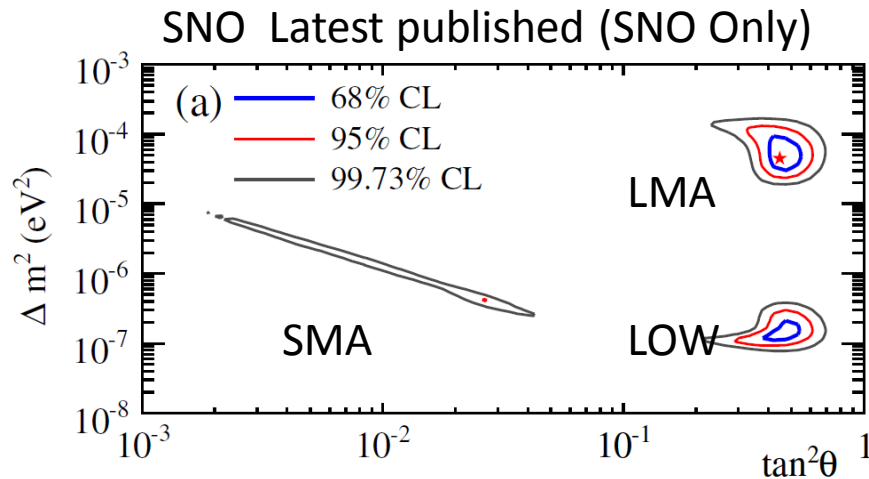
Solar Neutrino Oscillation (Global Analysis)

- **Need multiple solar neutrino experiments**
→ to obtain LMA
- No single solar neutrino experiment can single out LMA.

- **A GLOBAL Analysis^{Phase I+II+III}**
(Ref: SNO Group Ph.I+II+III)
[All solar neutrino experiments]

$$\Delta m^2 = 4.90_{-0.93}^{+1.64} \times 10^{-5} \text{ eV}^2$$

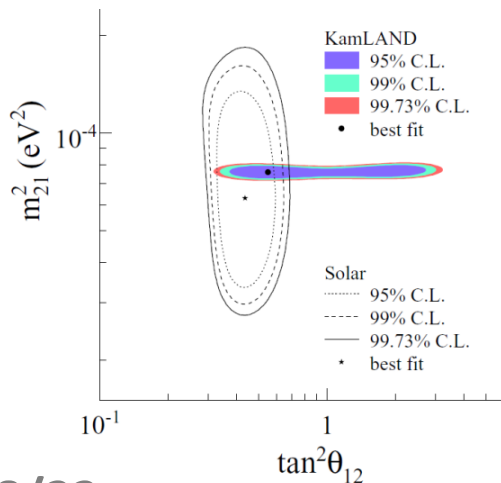
$$\tan^2 \theta = 0.437_{-0.040}^{+0.043}$$



KamLAND and Global Analysis (sol+KL)

KamLAND (KL)

- Reactor neutrino experiment
 - $L \sim 180$ km
 - $E \sim$ a few MeV
- Good Δm^2 determination:
 - better knowledge of L/E
- KL only
 - $\Delta m^2 = 7.58 \times 10^{-5} \text{ eV}^2$ (2.7%)
 - $\tan^2\theta = 0.56$ (~25%)



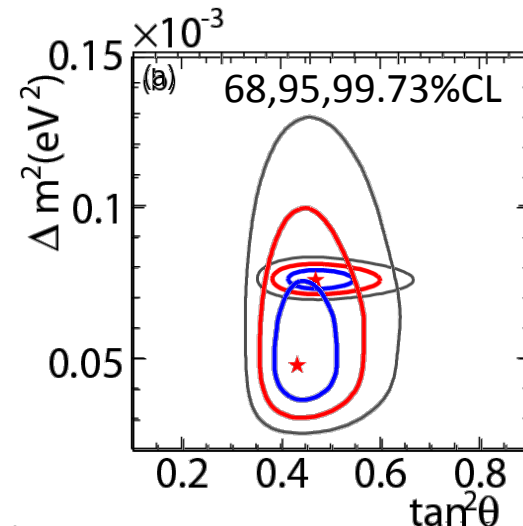
• Solar+KL

- Solar:
Cl+Ga+SK+BorexinoSNO(Phase-II-III) (SNO Analysis)

- $\Delta m^2 = 7.59 \times 10^{-5} \text{ eV}^2$ (~2.8%)
- $\tan^2\theta = 0.468$ (~10%)

(Sol Only)

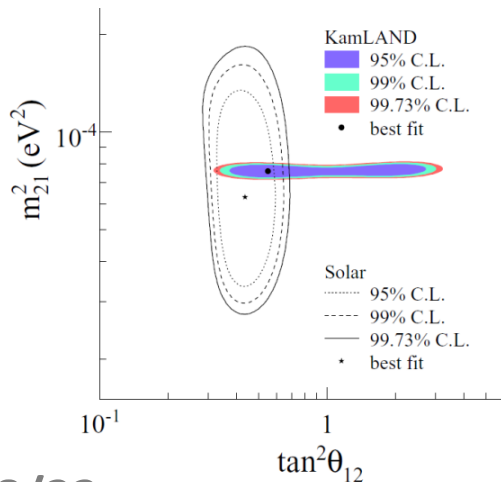
- $\Delta m^2 = 4.90 \times 10^{-5} \text{ eV}^2$ (~34%)
- $\tan^2\theta = 0.437$ (~10%)



KamLAND and Global Analysis (sol+KL)

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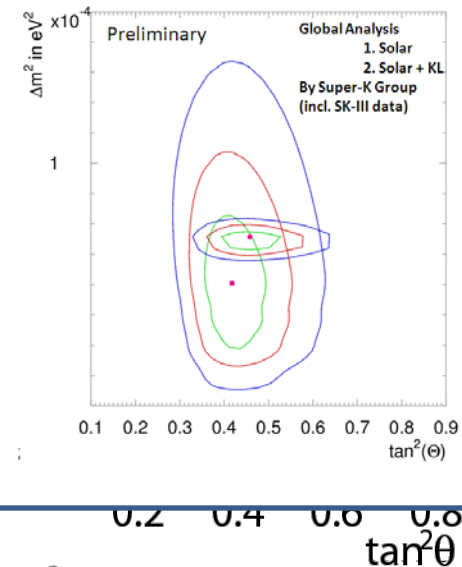
• Solar+KL

Global Analysis by SK-Group

- 1) All solar, 2) All solar + KL including SK-III

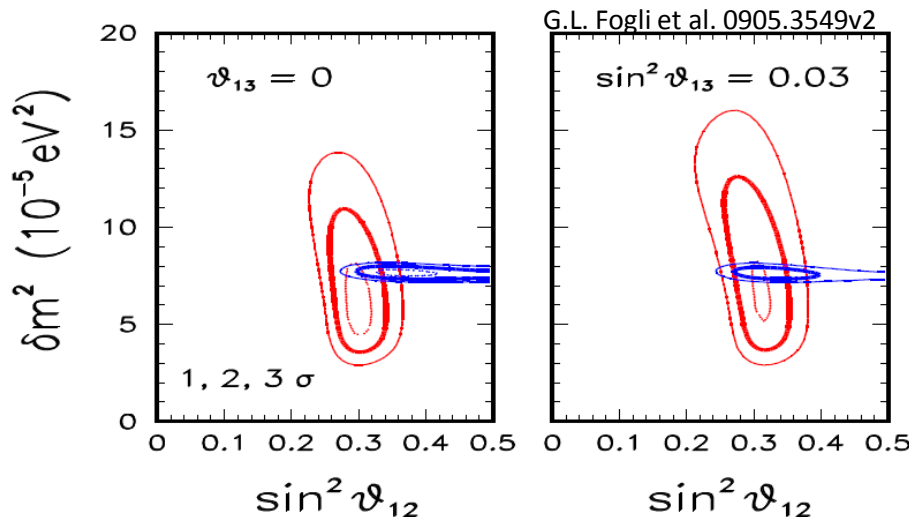
$$\Delta m^2 = 7.6 \times 10^{-5} \text{ eV}^2$$

$$\tan^2\theta = 0.47$$



KamLAND vs Solar Neutrinos

- Solar
 - Good for $\sin^2\theta_{12}$
 - KamLAND
 - Good for Δm^2
 - Getting better also on $\sin^2\theta_{12}$
- ➔ KamLAND vs Solar Neutrinos: slight tension
 good place to study on the small effect like $\sin^2\theta_{13}$ in future

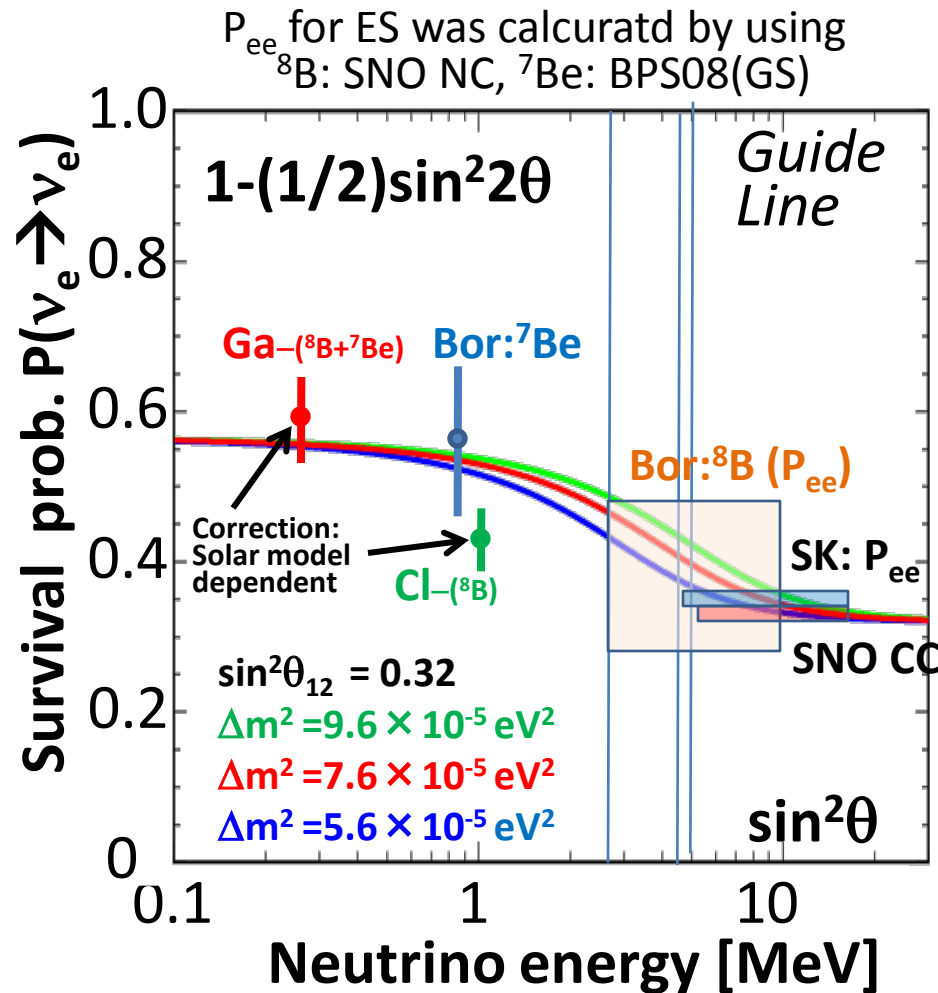


$$P_{ee}^{\text{KL}} \approx \cos^4 \theta_{13} \left(1 - \sin^2 2\theta_{12} \sin^2 \frac{\Delta m_{12}^2 L}{4E} \right)$$

$$P_{ee}^{\text{Sol}} \approx \cos^4 \theta_{13} \left(1 - \frac{1}{2} \sin^2 2\theta_{12} \right) \quad (\text{LowEnergy})$$

$$\approx \cos^4 \theta_{13} \sin^2 \theta_{12} \quad (\text{HighEnergy})$$

Large Mixing Angle Solution



LMA

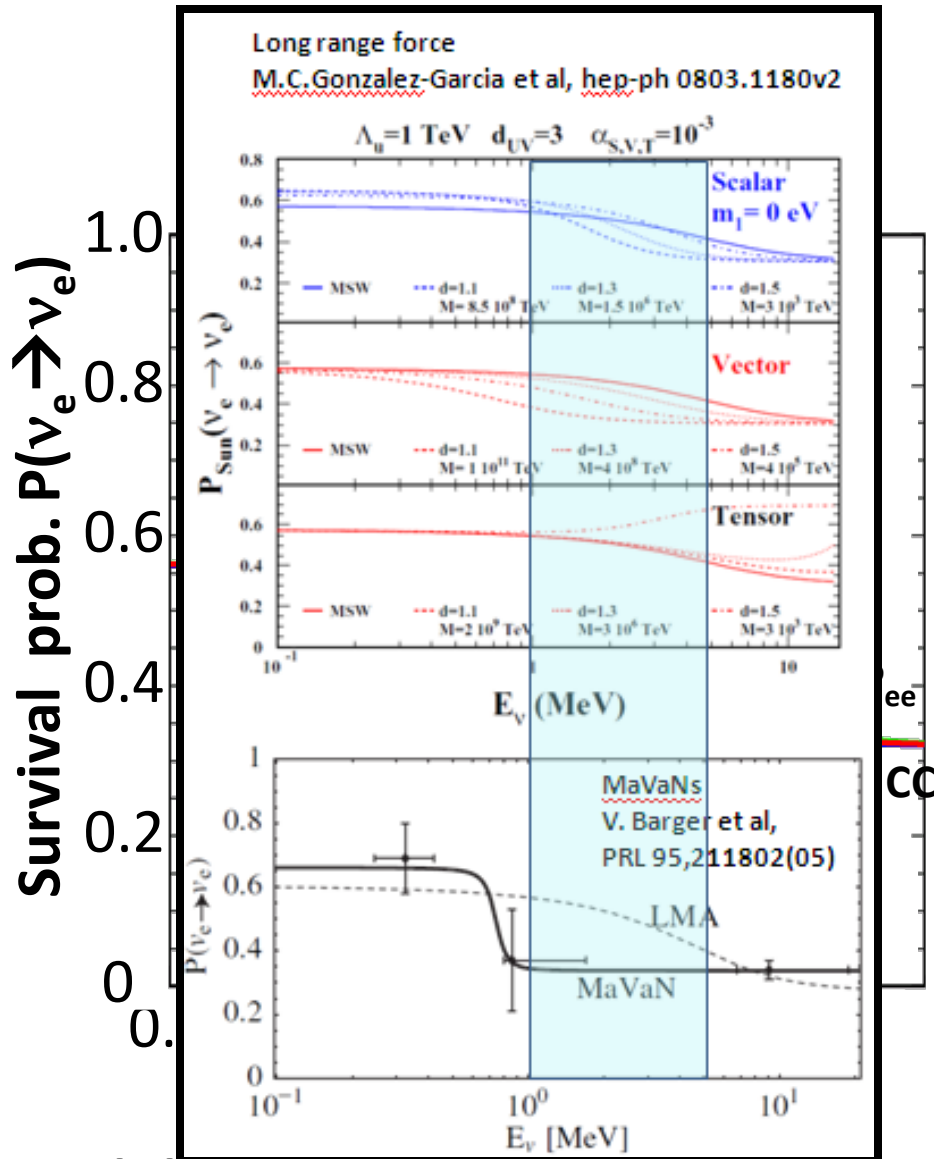
- **Vacuum in low energy:**
 - $P_{ee} = 1 - (1/2)\sin^2 2\theta$
- **Matter in high energy (>5 MeV):**
 - $P_{ee} = \cos^2 \theta \cos^2 \theta_m + \sin^2 \theta \sin^2 \theta_m$
 - $P_{ee} = \sin^2 \theta$ ($\theta_m \rightarrow \pi/2$)

$$\tan^2 2\theta_m = \frac{\tan^2 2\theta_v}{1 - (2p\sqrt{2G_F n_e}) / (\Delta m^2 \cos 2\theta_v)}$$

= 0 **Resonance condition**

- Δm^2 region 10^{-5} to 10^{-4} eV^2
 - $\Delta m^2 < 1.6 \times 10^{-4} \text{ eV}^2$ resonance $> 10 \text{ MeV}$
 - $\Delta m^2 > 1.6 \times 10^{-5} \text{ eV}^2$ no resonance $< 1 \text{ MeV}$
- **Transition Vac → Matter: 1~5 MeV**
 - sensitivity on Δm^2 from the experiment
 - good place to look for exotics

Large Mixing Angle Solution



LMA

- Vacuum in low energy:
 - $P_{ee} = 1 - (1/2)\sin^2 2\theta$
- Matter in high energy (>5 MeV):
 - $P_{ee} = \cos^2 \theta \cos^2 \theta_m + \sin^2 \theta \sin^2 \theta_m$
 - $P_{ee} = \sin^2 \theta$ ($\theta_m \rightarrow \pi/2$)

$$\tan^2 2\theta_m = \frac{\tan^2 2\theta_v}{1 - (2p\sqrt{2G_F n_e}) / (\Delta m^2 \cos 2\theta_v)}$$

→ = 0 Resonance condition

- Δm^2 region 10^{-5} to 10^{-4} eV^2
 - $\Delta m^2 < 1.6 \times 10^{-4} \text{ eV}^2$ resonance >10MeV
 - $\Delta m^2 > 1.6 \times 10^{-5} \text{ eV}^2$ no resonance <1MeV
- Transition Vac → Matter: 1~5 MeV
 - sensitivity on Δm^2 from the experiment
 - good place to look for exotics

Remaining Problems/Tasks

- **Precise determination of oscillation parameters! and small effects ?**

- Solar vs KamLAND
- Transition region

- Borexino
- SNO low energy analysis
- SK

Source	BPS08(GS)	BPS08(AGS)	Difference
<i>pp</i>	5.97(1 ± 0.006)	6.04(1 ± 0.005)	1.2%
<i>pep</i>	1.41(1 ± 0.011)	1.45(1 ± 0.010)	2.8%
<i>hep</i>	7.90(1 ± 0.15)	8.22(1 ± 0.15)	4.1%
⁷ Be	5.07(1 ± 0.06)	4.55(1 ± 0.06)	10%
⁸ B	5.94(1 ± 0.11)	4.72(1 ± 0.11)	21%
¹³ N	2.88(1 ± 0.15)	1.89(1 ^{+0.14} _{-0.13})	34%
¹⁵ O	2.15(1 ^{+0.17} _{-0.16})	1.34(1 ^{+0.16} _{-0.15})	31%
¹⁷ F	5.82(1 ^{+0.19} _{-0.17})	3.25(1 ^{+0.16} _{-0.15})	44%
Cl	8.46 ^{+0.87} _{-0.88}	6.86 ^{+0.69} _{-0.70}	
Ga	127.9 ^{+8.1} _{-8.2}	120.5 ^{+6.9} _{-7.1}	

- **SSM problem**

- Refined determination of the surface metallicity (AGS05)
- Different total metallicity
 - Z/X=0.0165(AGS05): Low Z
(BeforeAGS05:Z/X=0.0229 (GS98): High Z)
 - Especially, C,N,O, Ne, Mg are lower
 - → Solar model conflicts with helioseismology

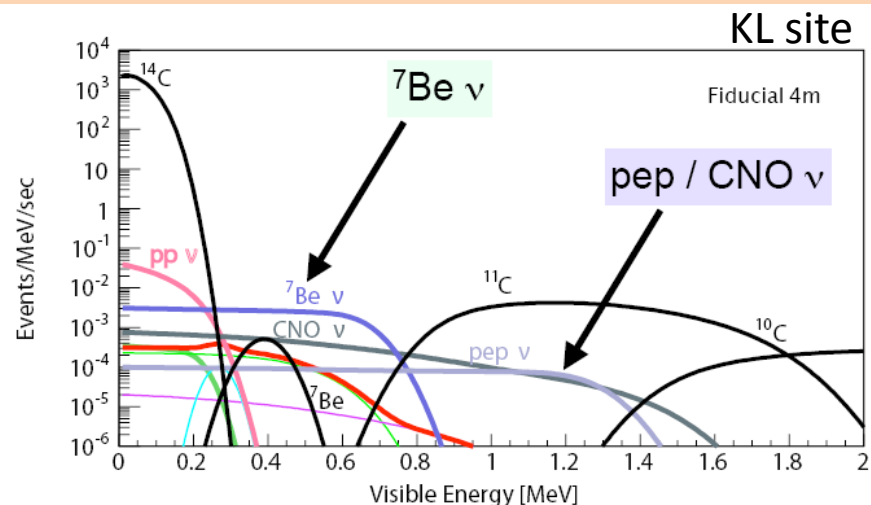
- **Does not change the global view of the solar ν oscillation, but affects on the search for small effects or precise study on the oscillation parameters.**

- **Can be tested by**

- ⁸B flux measurement
- CNO measurements

Future Experiments

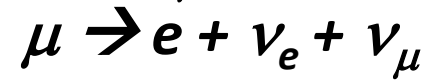
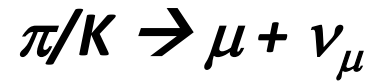
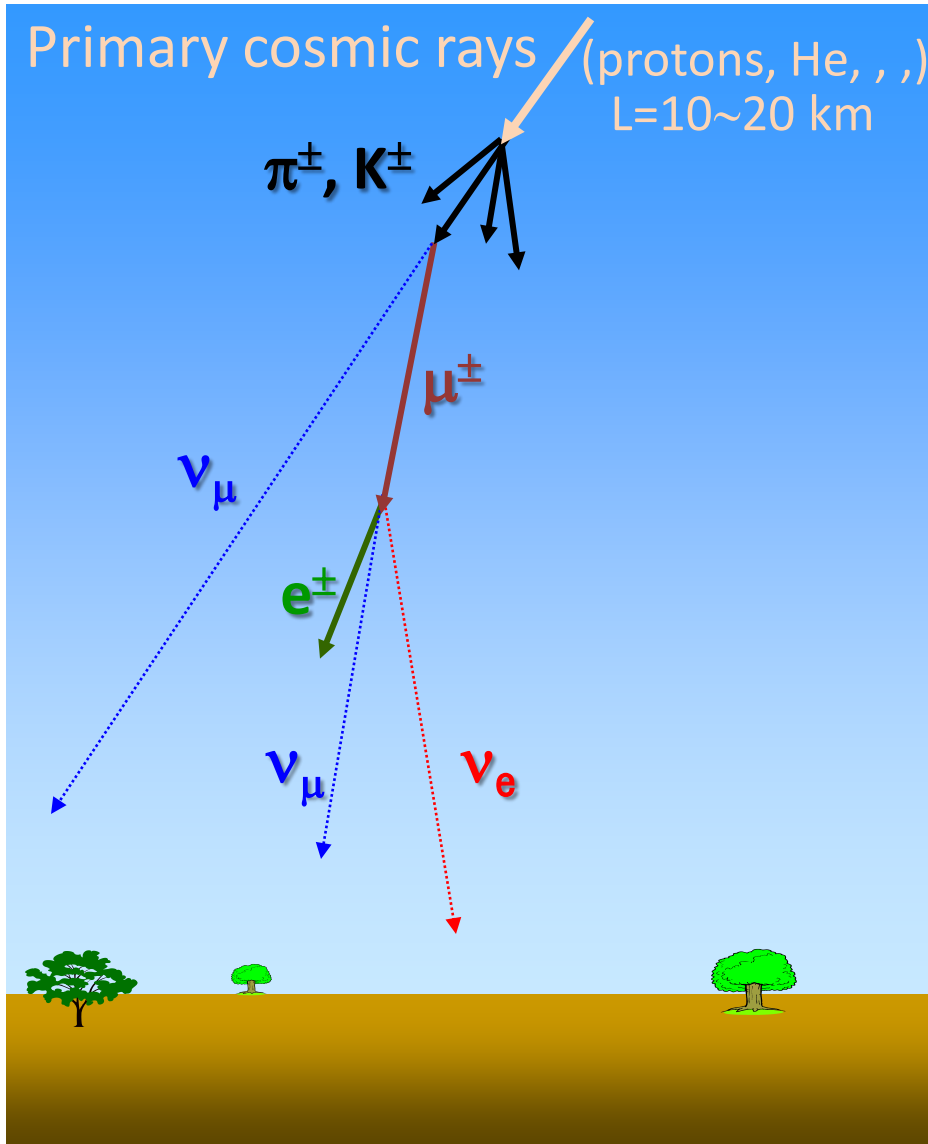
- SAGE(Ga), SK(ES), Borexino(ES)
 - will continue to be running
 - Low energy: below 5 MeV
- KamLAND(ES): liq. Scinti.
 - ${}^7\text{Be}$, CNO
 - ${}^7\text{Be}$? Purification test
 - move to double β
- SNO+(ES): liq. Scinti.
 - pep, CNO
 - Lower background @ deeper site



R&D/Proto-Type

Experiments	Aim	Technology	CC /ES
LENS	pp neutrino	In-loaded liq. Scinti.	CC
CLEAN	pp neutrino	Liq. Neon/Ar	ES
MOON	pp, ${}^7\text{Be}$ neutrino	Mo tracking calorimeter	CC
XMASS	pp neutrino	Liq. Xenon	ES

Atmospheric Neutrinos

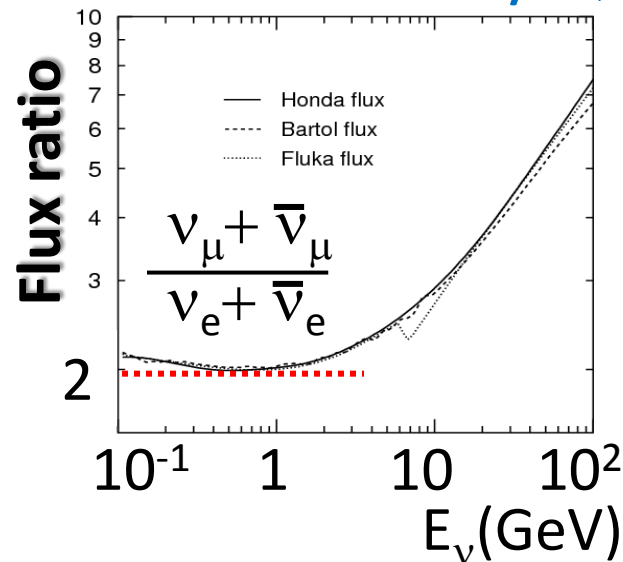


For the low energy limit

– μ 's decay before reaching the ground

– $\nu_\mu : \nu_e = 2 : 1$

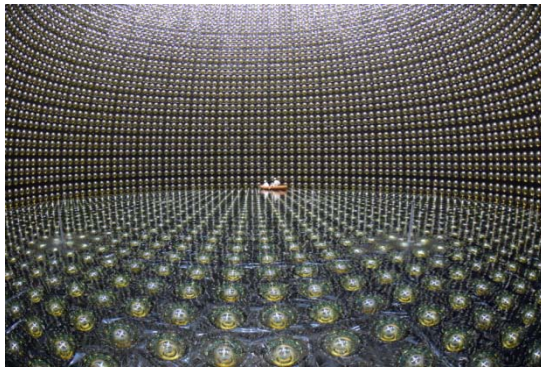
For higher energy:



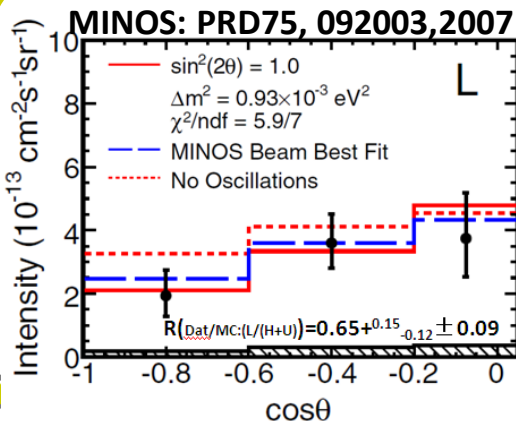
Experiments

Historical Experiments

– IMB	(Water Ch.	3.3kt)
– Frejus	(Calorimeter 0.7kt)	
– NUSEX	(Calorimeter 0.1kt)	
– Kamiokande	(Water Ch.	1.0kt)
– Soudan II	(Calorimeter)	1.0kt)
– MACRO	(Up- μ)



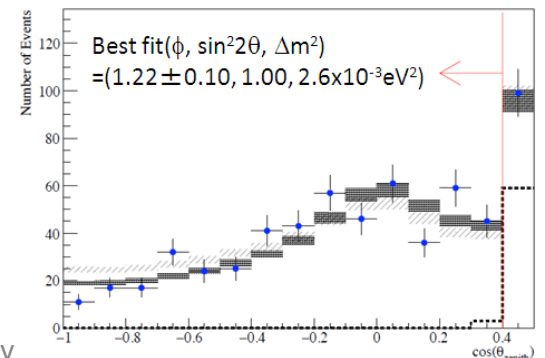
- **Super-Kamiokande (22.5kt)** provided the evidence and still provides largest statistics
 → today' report



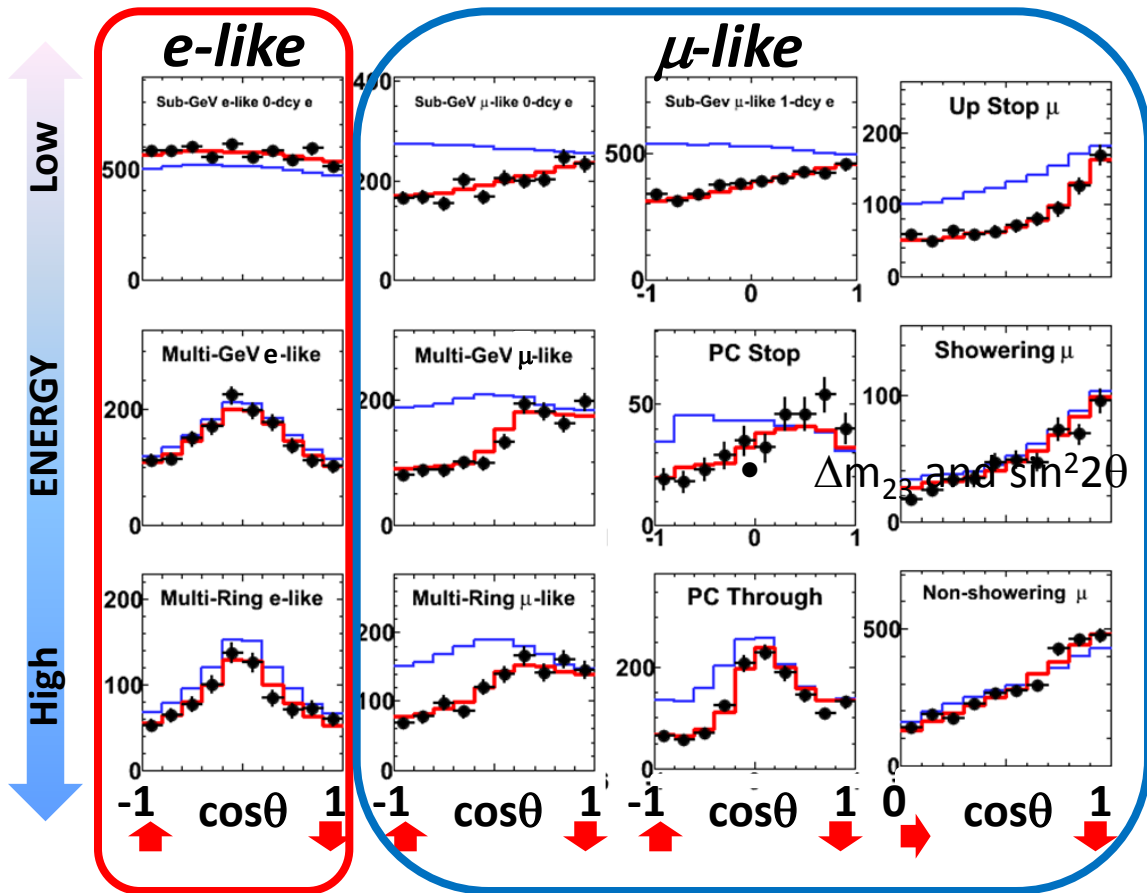
New Measurements

MINOS (Calorimeter	5.4 kt)
- Up- μ	
SNO (D ₂ O	1.0kt)
- Up- μ	

SNO: arXiv 0902.2776 (→PRD)



Experimental Results (Super-K)

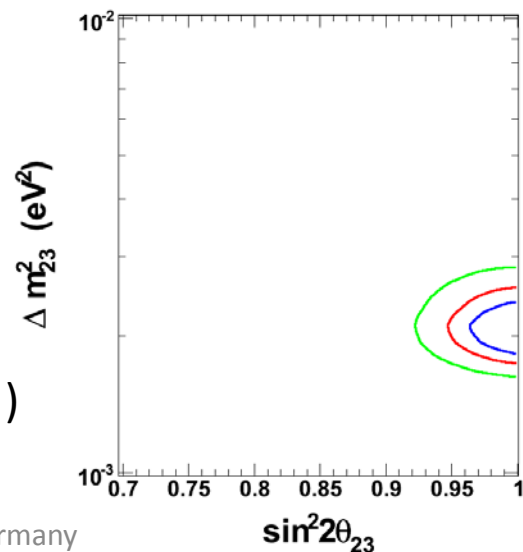


Physical Region

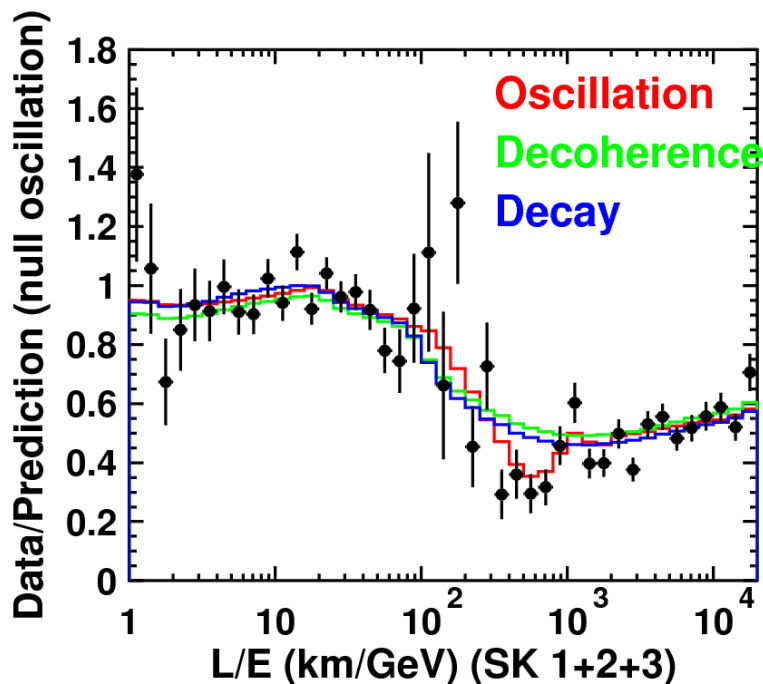
$$\Delta m_{23}^2 = 2.11^{+0.11}_{-0.19} \text{ (1}\sigma \text{ : } \Delta\chi^2=1)$$

$$\sin^2 2\theta = 1 \text{ (} > 0.96 \text{ (90\%C.L.))}$$

- Latest SK results
 - SK-I,II,III combined
 - 2806days (173ktyr) for FC+PC
 - 24841 events
 - 3109days for up- μ
 - 4238 events



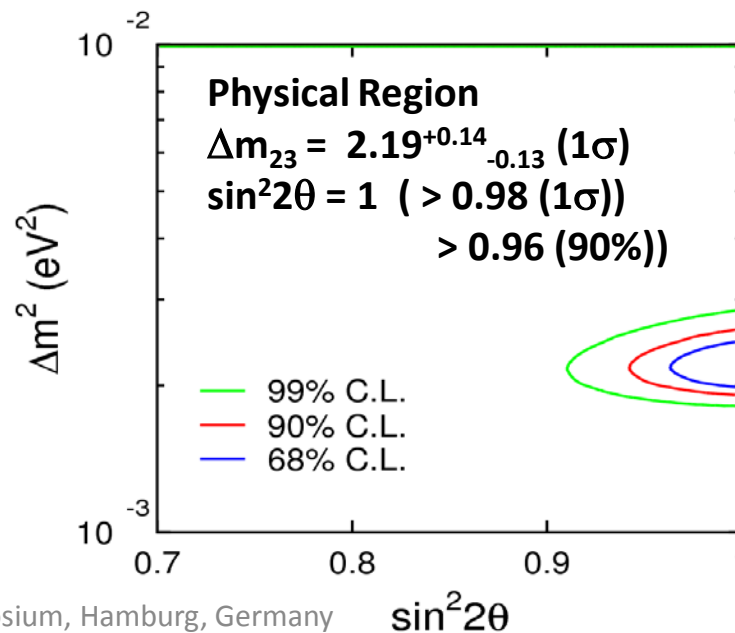
L/E plot



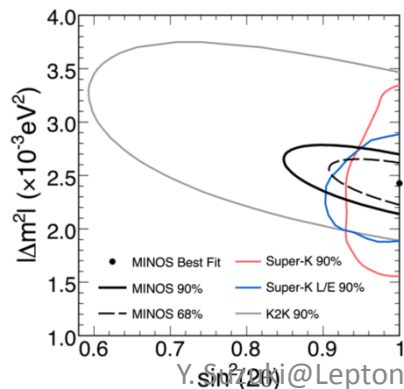
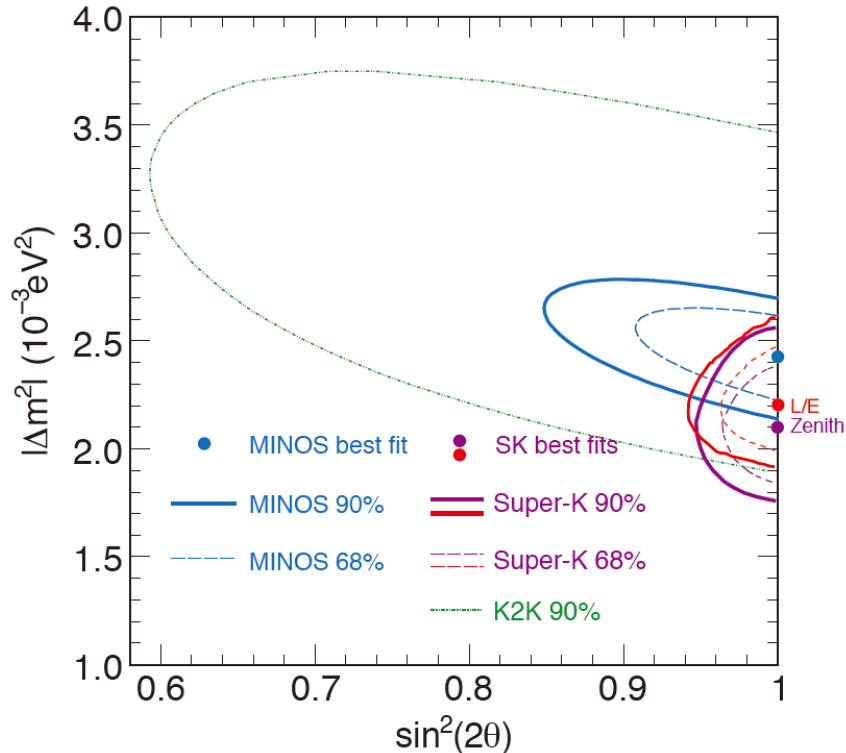
- Neutrino decay: 4.4σ
– $\Delta\chi^2 = 19.8/126\text{d.o.f.}$
- Decoherence: 5.4σ
– $\Delta\chi^2 = 29.0/126\text{d.o.f.}$

L/E analysis (SK I+II+III)

- Direct determination of $\Delta m^2 \leftarrow E/\lambda$
 - Position of the dip in L/E plot
- Select events with good L/E ($\Delta(L/E) < 70\%$)
- Better sensitivity on Δm^2
- The first dip at $\sim 500(\text{km}/\text{GeV})$



Oscillation Parameters



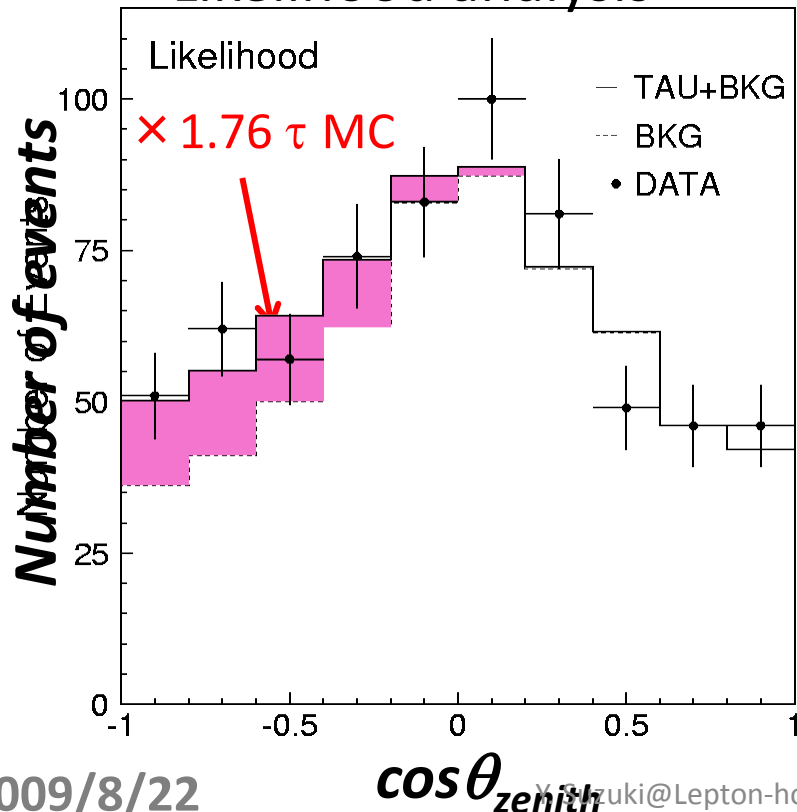
- $\Delta m_{23}^2 = 2.11^{+0.11}_{-0.19} \times 10^{-3} \text{ eV}^2$
(Atm- ν : Zenith)
- $\Delta m_{23}^2 = 2.19^{+0.14}_{-0.13} \times 10^{-3} \text{ eV}^2$
(Atm- ν : L/E)
- $\Delta m_{23}^2 = 2.43^{+0.13}_{-0.13} \times 10^{-3} \text{ eV}^2$
(MINOS)
- $\sin^2 2\theta > 0.96$ (90%) (Atm- ν)
- $\sin^2 2\theta > 0.90$ (90%) (MINOS)
- Δm^2 : comparable uncertainty
– Probably better in future LBLE
- $\sin^2 2\theta$: better in atm- ν

Tau appearance

OLD
Result

- Cannot: event-by-event analysis
→ need statistical analysis
- Not easy:
← $E_{th} > 3.5$ GeV, low rate (S/BG~1/140)
- select enriched sample
← likelihood and neural network
- Make zenith angle distribution

Likelihood analysis



Fit in zenith angle distribution to evaluate τ contribution:

$$N_{total}(\cos\theta) = \alpha N_{tau} + \beta N_{bkg}$$

$$\alpha = 1.76 \text{ and } \beta = 0.9$$

Fitted # of τ events $138 \pm 48(\text{stat.})^{+14.8}_{-31.6}$
(corr. for 43% efficiency)

Expected # of τ events $78.4 \pm 26(\text{syst.})$

Tau appearance : 2.4σ

Neural Network Method provides similar result

Tau appearance

OLD
Result

- Cannot: event-by-event analysis
→ need statistical analysis
- Not easy:
← $E_{th} > 3.5$ GeV, low rate (S/BG~1/140)
- select enriched sample
← likelihood and neural network
- Make zenith angle distribution

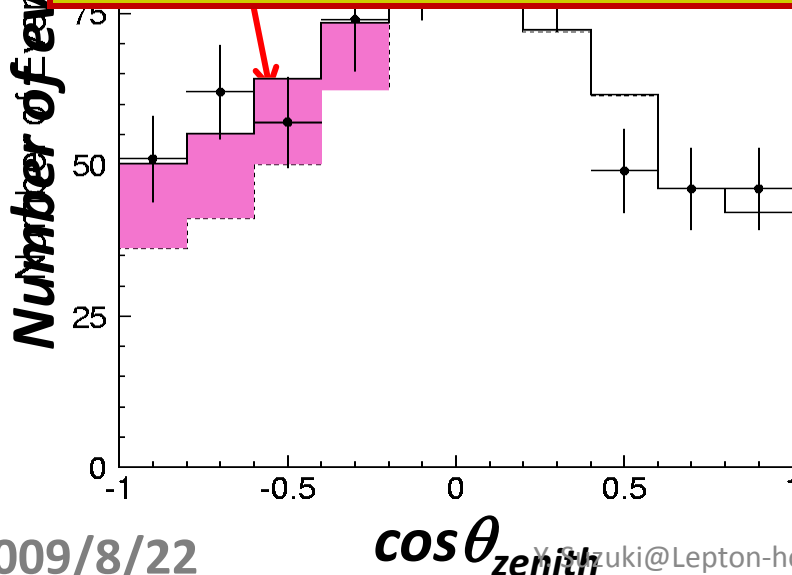
Likelihood analysis

Fit in zenith angle distribution

Direct tau appearance experiment (OPERA) is taking data

(1.25kt target; $\langle E_\nu \rangle \sim 17$ GeV, L=732km; $\langle L/E \rangle \sim 43$)

Expect ~ 10 events from 22.5×10^{19} POT exposure for $2.5 \times 10^{-3} \text{ eV}^2$



Fitted # of τ events $138 \pm 48(\text{stat.})^{+14.8}_{-31.6}$
 (corr. for 43% efficiency)
 Expected # of τ events $78.4 \pm 26(\text{syst.})$

Tau appearance : 2.4σ

Neural Network Method provides similar result

Remaining Problems of Atmospheric ν

- θ_{13} in atmospheric neutrinos
- Mass hierarchy
- Octant of θ_{23}
- CPV in atmospheric neutrinos

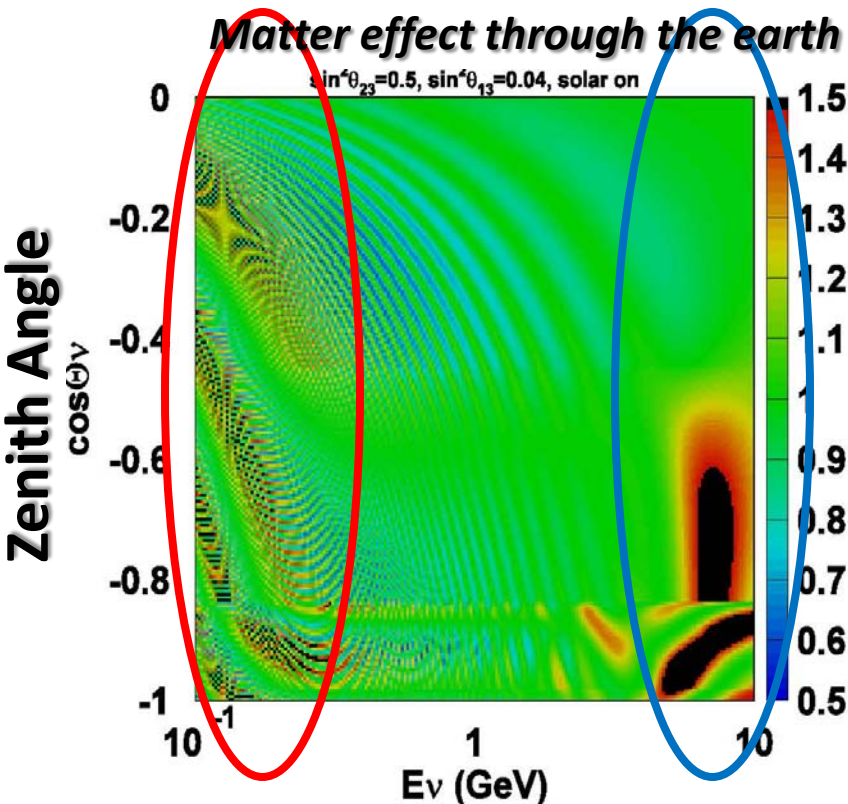
See subdominant effects in three flavour analysis

Three flavor analysis

ν_e appearance in atmospheric- ν

$$\frac{\Psi(\nu_e)}{\Psi_0(\nu_e)} - 1 \cong P_2(r \cdot c_{23}^2 - 1) - r \cdot \tilde{s}_{13} \cdot \tilde{c}_{13}^2 \cdot \sin 2\theta_{23} (\cos \delta_{CP} \cdot R_2 - \sin \delta_{CP} \cdot I_2) + 2\tilde{s}_{13}^2 (r \cdot s_{23}^2 - 1)$$

$\tilde{}$: mixing angle in matter
 $P_2 = |A_{e\mu}|^2$: $\nu_e \rightarrow \nu_{\mu\tau}$ in matter
 $R_2 = \text{Re}(A_{ee}^* A_{e\mu})$
 $I_2 = \text{Im}(A_{ee}^* A_{e\mu})$



1st term: solar term ($\theta_{12}, \Delta m_{12}$)
 mostly in low energy
 cancellation effect ($c_{23}^2=0.5, r=\nu_{\mu}/\nu_e=2@LE$)
 1~2% effect

3rd term: θ_{13} term
 > a few GeV (in multi-GeV data)
 10~15% effect

2nd term: Interference
CP-Phase

$s^2\theta_{12}=0.825, s^2\theta_{23}=0.4, s^2\theta_{13}=0.04$

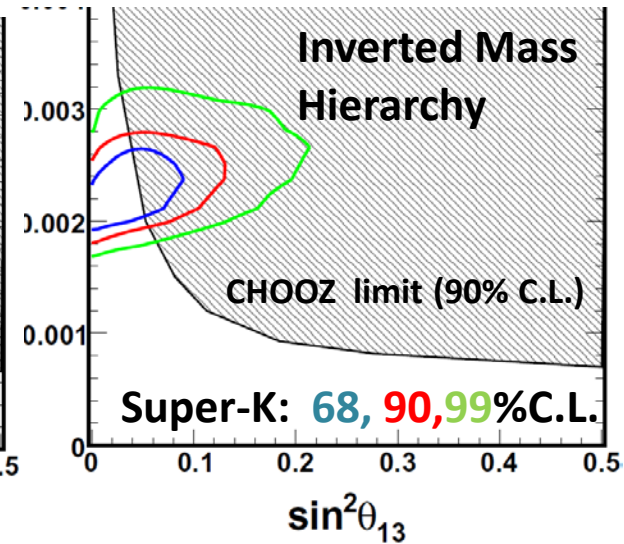
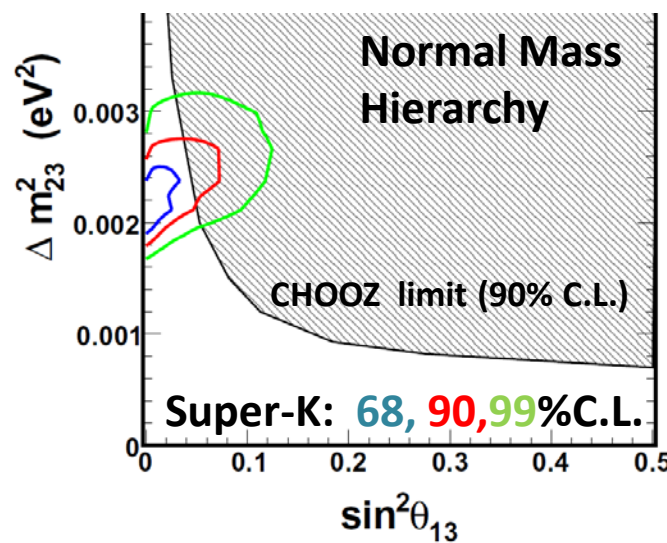
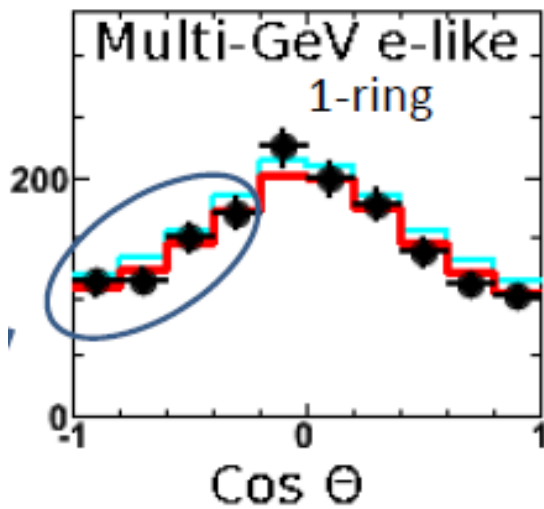
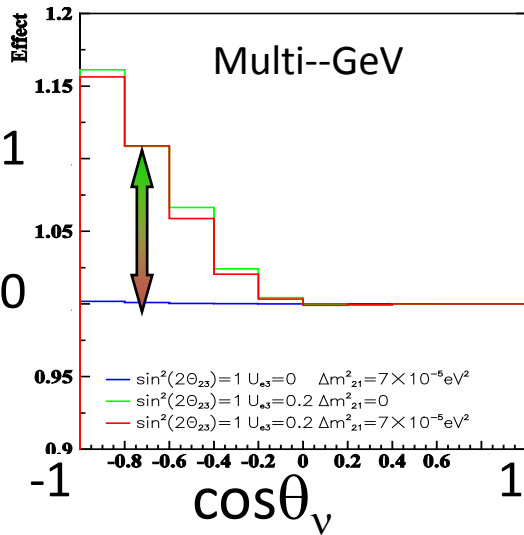
$\delta_{CP}=45^\circ, \Delta m^2_{12}=8.3 \times 10^{-5}, \Delta m^2_{23}=2.5 \times 10^{-3}$

θ_{13}

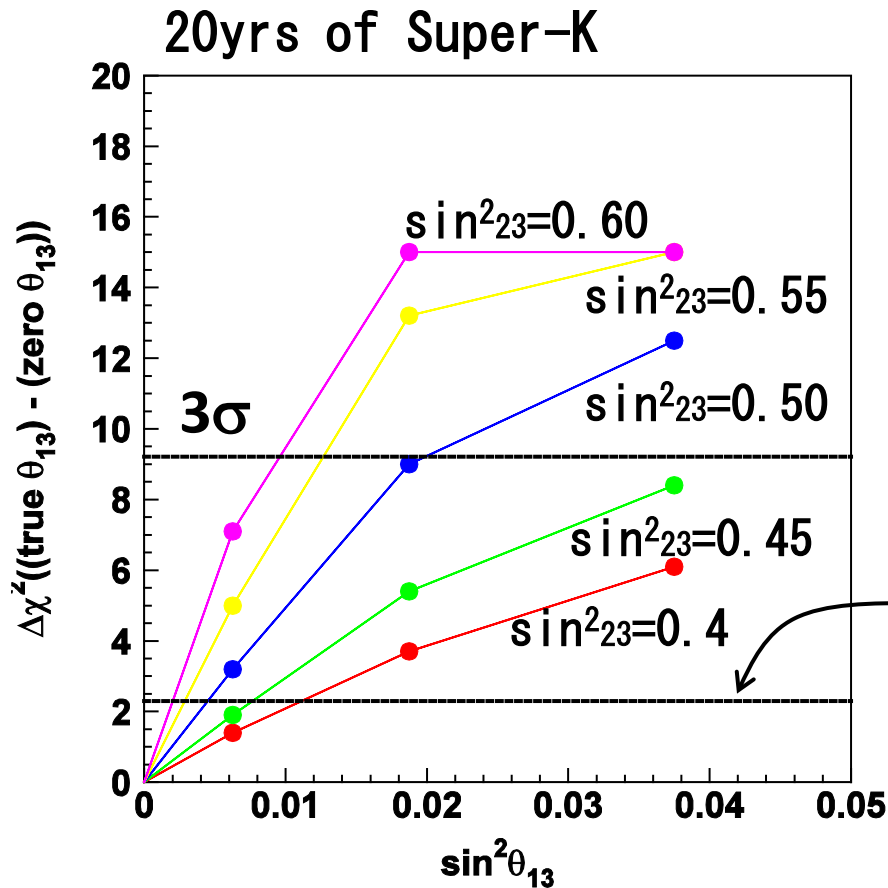
- Effect of θ_{13} can be seen in a few GeV electron data

For SK-I, II, III combined data

- $\sin^2\theta_{13} < 0.07$ (90% C.L.)
 - Normal Hierarchy
- $\sin^2\theta_{13} < 0.13$ (90% C.L.)
 - Inverted Hierarchy



θ_{13} in future

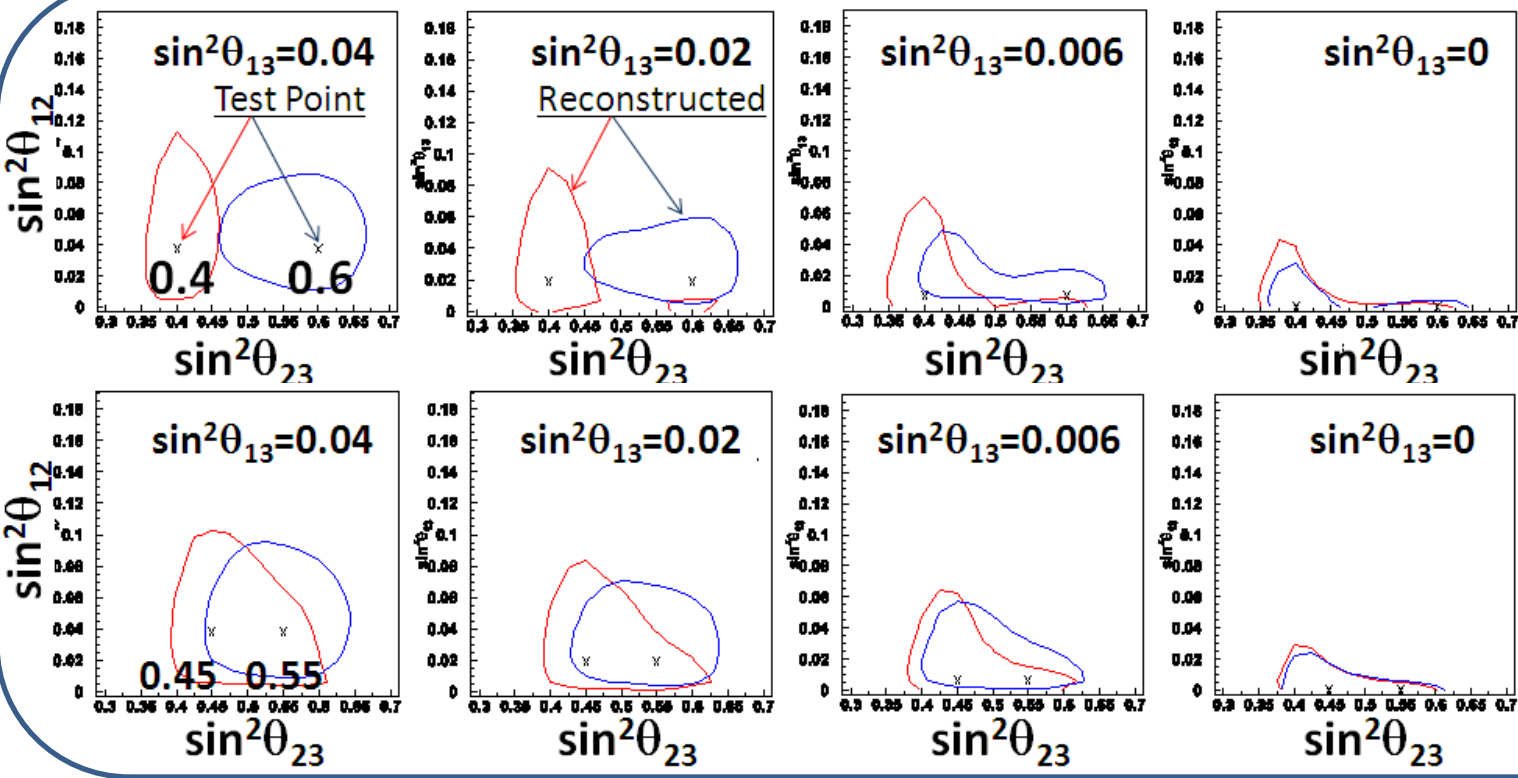
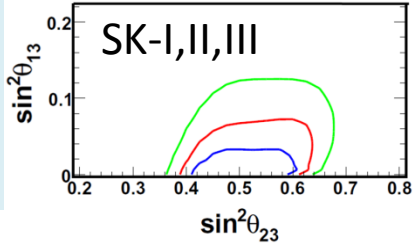


20yrs SK: Positive signal for nonzero θ_{13} can be seen if $\sin^2\theta_{13}$ is > 0.02 and $\sin^2\theta_{23} > 0.5$

3 σ for 80yrs SK
~4yrs HK

$s^2\theta_{12}=0.825$
 $s^2\theta_{23}=0.40 \sim 0.60$
 $s^2\theta_{13}=0.00 \sim 0.04$
 $\delta_{cp}=45^\circ$
 $\Delta m^2_{12}=8.3e-5$
 $\Delta m^2_{23}=2.5e-3$

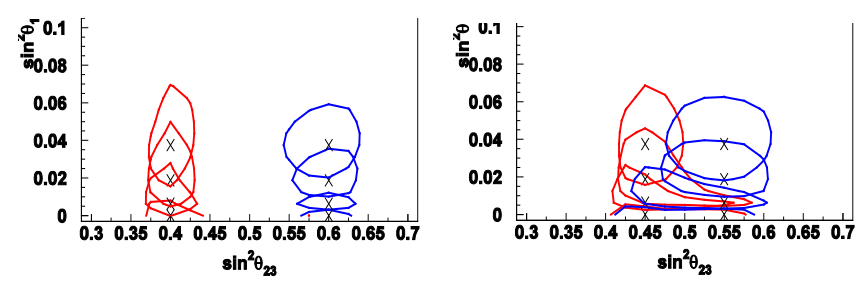
Octant (in future)



Monte Carlo
SK (22.5kt f.v.)
20 years

Can be seen:
for
 $\sin^2\theta_{13} > 0.02$ &
 $\sin^2\theta_{23} < 0.4$ or
 $\sin^2\theta_{23} > 0.6$

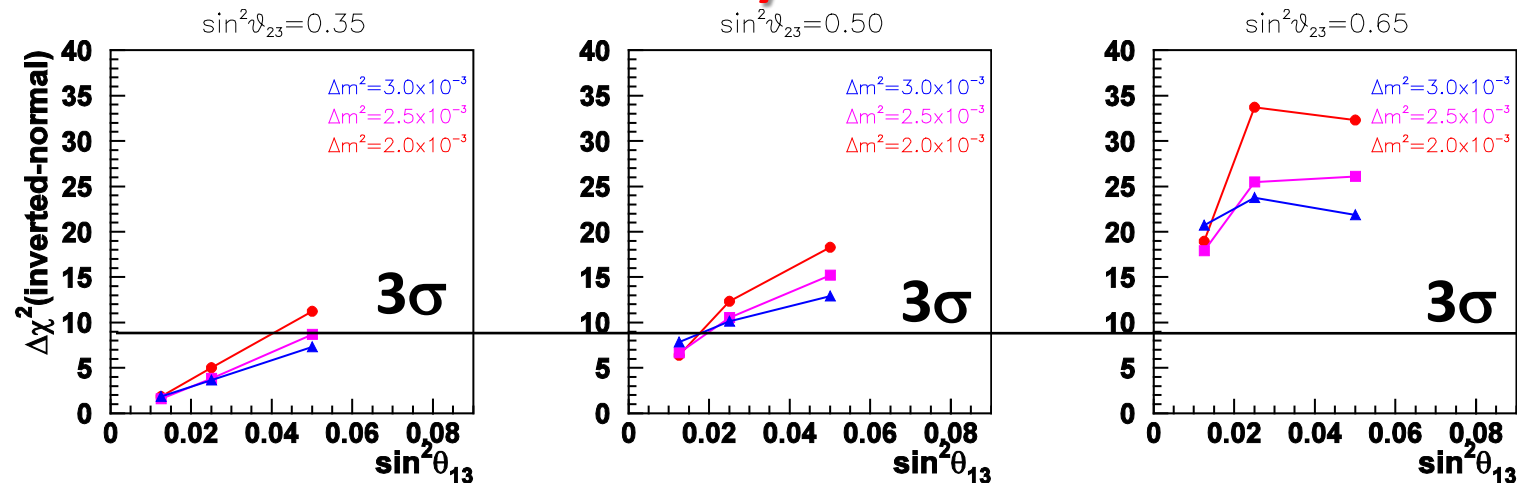
$s^2\theta_{12} = 0.825$
 $s^2\theta_{23} = 0.40 \sim 0.60$
 $s^2\theta_{13} = 0.00 \sim 0.04$
 $\delta_{cp} = 45^\circ$
 $\Delta m^2_{12} = 8.3 \times 10^{-5}$
 $\Delta m^2_{23} = 2.5 \times 10^{-3}$



Monte Carlo
0.5Mt f.v. det.
3.6 years

Mass Hierarchy

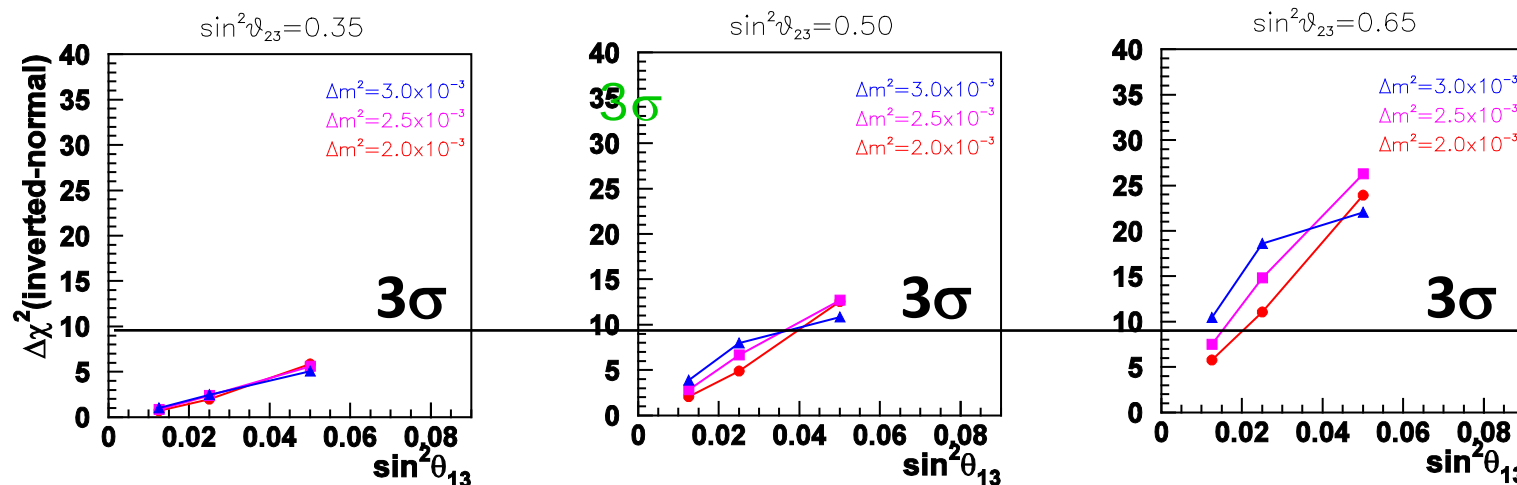
True : normal mass hierarchy



1.8 Mton \cdot yr
3.6yr HK

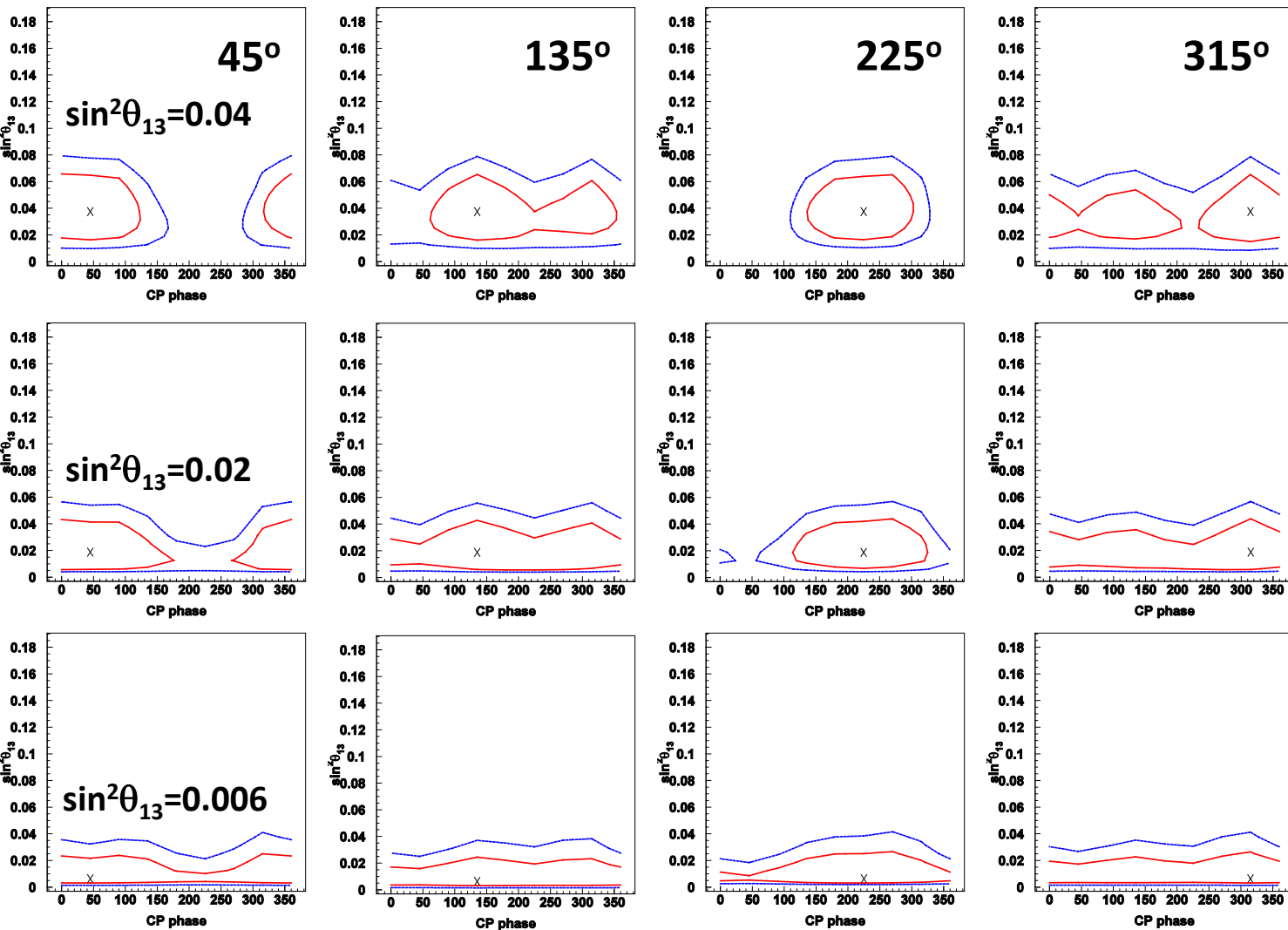
Can be seen
for
 $\sin^2\theta_{13} > 0.02$
 $\sin^2\theta_{23} > 0.5$
(normal)

True : inverted mass hierarchy

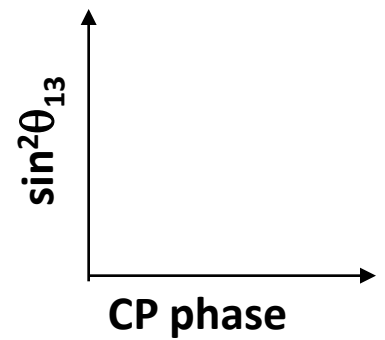


for
 $\sin^2\theta_{13} > 0.02$
 $\sin^2\theta_{23} > 0.65$
(inverted)

Sensitivity for CPV (3.6 yrs HK)

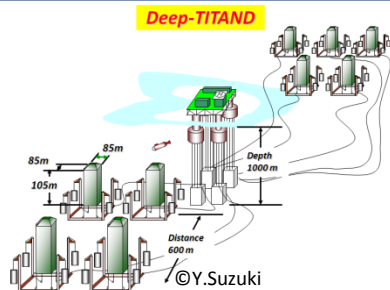
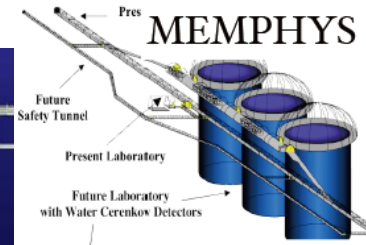
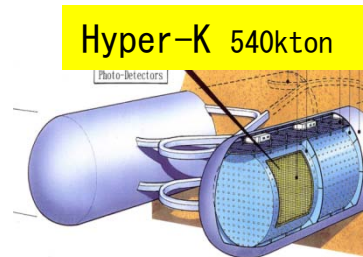
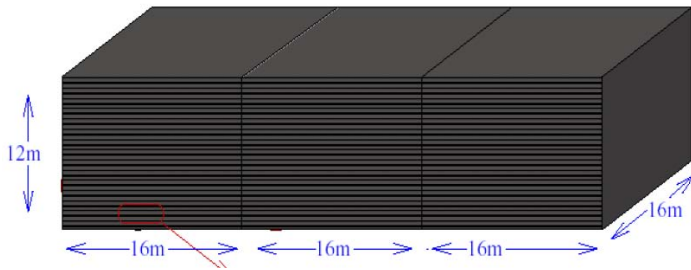


$s^2\theta_{12}=0.825$
 $s^2\theta_{23}=0.5$
 $s^2\theta_{13}=0.006\sim 0.04$
 $\delta_{cp}=0^\circ\sim 360^\circ$
 $\Delta m^2_{12}=8.3\times 10^{-5}$
 $\Delta m^2_{23}=2.5\times 10^{-3}$



Future atmospheric neutrino experiments beyond Super-K

- **INO**
 - 50 kt magnetized (1.2 Tesla) iron
 - 3 modules
 - Each module = 16x16x12m³
 - Can measure charge
 - ➔ Mass hierarchy
- **Megaton (0.5Mt fid.) detectors (HK, DUSEL,....)**
 - Water Cherenkov or Liquid Ar.
 - ➔ Octant
 - ➔ CP phase sensitivity
 - ➔ Mass hierarchy
 - Far detector of long baseline experiments



- **Multi-Megaton detectors (5-10Mt fid.) – Water Cherenkov**
 - Placed 1000m under water
 - Not only atmospheric
 - SN neutrino burst detection every year
 - Proton decay up to 10³⁶ yrs

Summary

- **~10 years after the discovery, oscillation parameters are now determined at a few % level**
- **Solar Neutrinos in future:**
 - **Transition region: low energy ^8B , CNO, pep, ^7Be**
 - **Sensitive to Δm^2**
 - **Deviation from LMA?**
 - **CNO is especially interest to resolving metallicity problem of the solar models.**
- **Atmospheric Neutrinos in future:**
 - **A complementary method to determine θ_{13} and other subdominant effects.**
 - **Future large detectors can be used for long baseline oscillation experiments, and can study proton decay as well as atmospheric neutrinos**