

Electroweak physics at low energy

(recent experimental results on the muon ($g-2$) and tau decays)

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Plan

- Muon (g-2) and R measurements
 - (g-2) experiment and theory
 - direct R measurements in e^+e^-
 - R measurement by ISR
- Search for LFV in tau decays
- Hadronic tau decays
 - $\tau^- \rightarrow \pi^- \pi^0 \nu_\tau$ decay and CVC
 - Search for 2-d class currents
 - V_{us} evaluation from τ hadronic decays
- Lepton universality and τ -lepton mass measurement
- Perspectives

Muon Anomalous Magnetic Moment

$$\vec{\mu} = g \frac{e}{2m} \vec{s}, \quad a = (g - 2)/2.$$

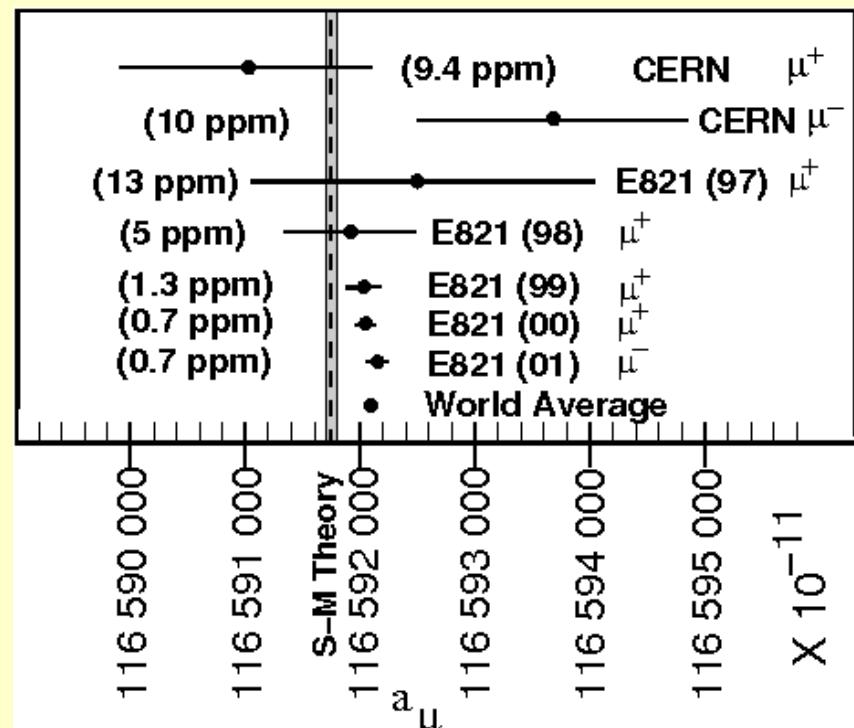
In Dirac theory for pointlike particles $g = 2$, higher-order effects (or new physics) $g \neq 2$

a_μ is measured with a 5×10^{-7} relative accuracy:

G.W. Bennett et al., 2004, 2006 $a_\mu = (11659208.0 \pm 6.3) \times 10^{-10}$.

a_e is measured with a 4.9×10^{-10} accuracy, but a_μ is much more sensitive to new physics effects: the gain is usually $\sim (m_\mu/m_e)^2 \approx 4.3 \times 10^4$.

Any significant difference of a_{exp} from a_{th} indicates new physics beyond the Standard Model.



Muon Anomalous Magnetic Moment

$$a_{\mu}^{SM} = a_{\mu}^{QED} + a_{\mu}^{EW} + a_{\mu}^{had}$$

Contribution	$a_{\mu}, 10^{-10}$
Experiment	11659208.0 ± 6.3
QED	11658471.8 ± 0.016
Electroweak	$15.4 \pm 0.1 \pm 0.2$
Hadronic	693.1 ± 5.6
Theory	11659180.3 ± 5.6
Exp. - Theory	$27.7 \pm 8.4 (3.3\sigma)$

By TAU-08

The difference between experiment and theory is 3.3σ !

QED and Electroweak contributions

QED

$$\begin{aligned} a_\mu^{\text{QED}} \cdot 10^{10} = \sum C_i \left(\frac{\alpha}{\pi}\right)^i = & 11614097.3 \text{ (1-loop)} \\ & + 41321.8 \text{ (2-loop)} \\ & + 3014.2 \text{ (3-loop)} \\ & + 38.1 \text{ (4-loop)} \\ & + 0.4 \text{ (5-loop)} \end{aligned}$$

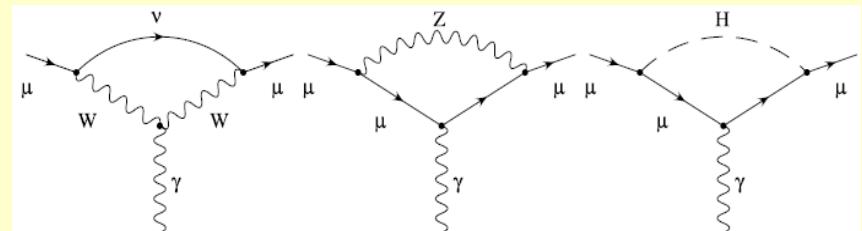
Terms up to α^3 are known analytically, a recent more accurate numerical calculation of the 4 terms and the leading $\log \alpha^5$ terms was done by (T. Kinoshita and M. Nio, 2005; A.L. Kataev, 2006):

From the latest value of a_e (G. Gabrielse et al., 2006; M. Passera, 2006): $\alpha^{-1} = 137.035999710(96)$,

$$a_{\text{QED}} = (116584718.09 \pm 0.14 \pm 0.08) \times 10^{-11}$$

The errors are due to: a/ $O(\alpha^5)$, b/ α

Electroweak



One-loop electroweak contributions

A.Czarnecki et al. 2002

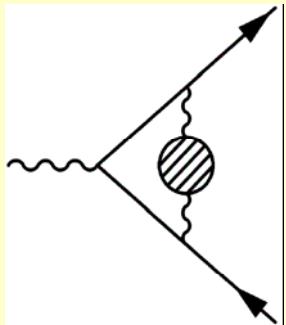
$$(15.4 \pm 0.1 \pm 0.2) \times 10^{-10}$$

The errors are due to: a/ hadr. loops, b/ M_H, M_t , 3-loop effects.

$$\text{LBL } (10.5 \pm 2.6) \times 10^{-10}$$

J. Prades, E. de Rafael, A. Vainshtein

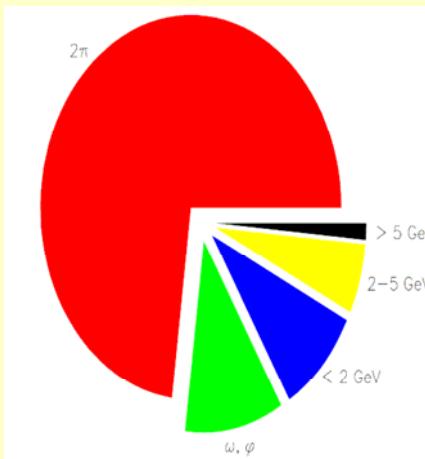
Hadronic contribution a_{had}



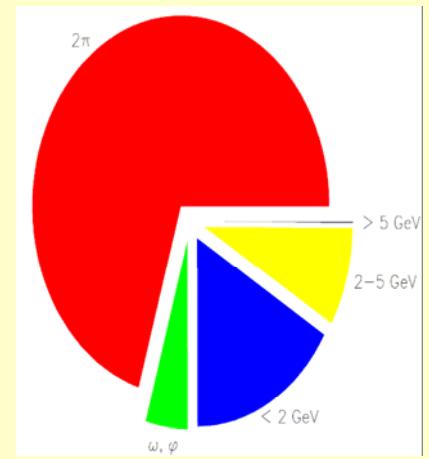
$$a_{\mu}^{\text{had}, LO} = \left(\frac{\alpha m_{\mu}}{3\pi} \right)^2 \int_{4m_{\pi}^2}^{\infty} ds \frac{R(s) \hat{K}(s)}{s^2}$$

$$R(s) = \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}, \quad \sigma_{\mu^+\mu^-} = \frac{85.86 \text{nb}}{s[\text{GeV}^2]}$$

Central values



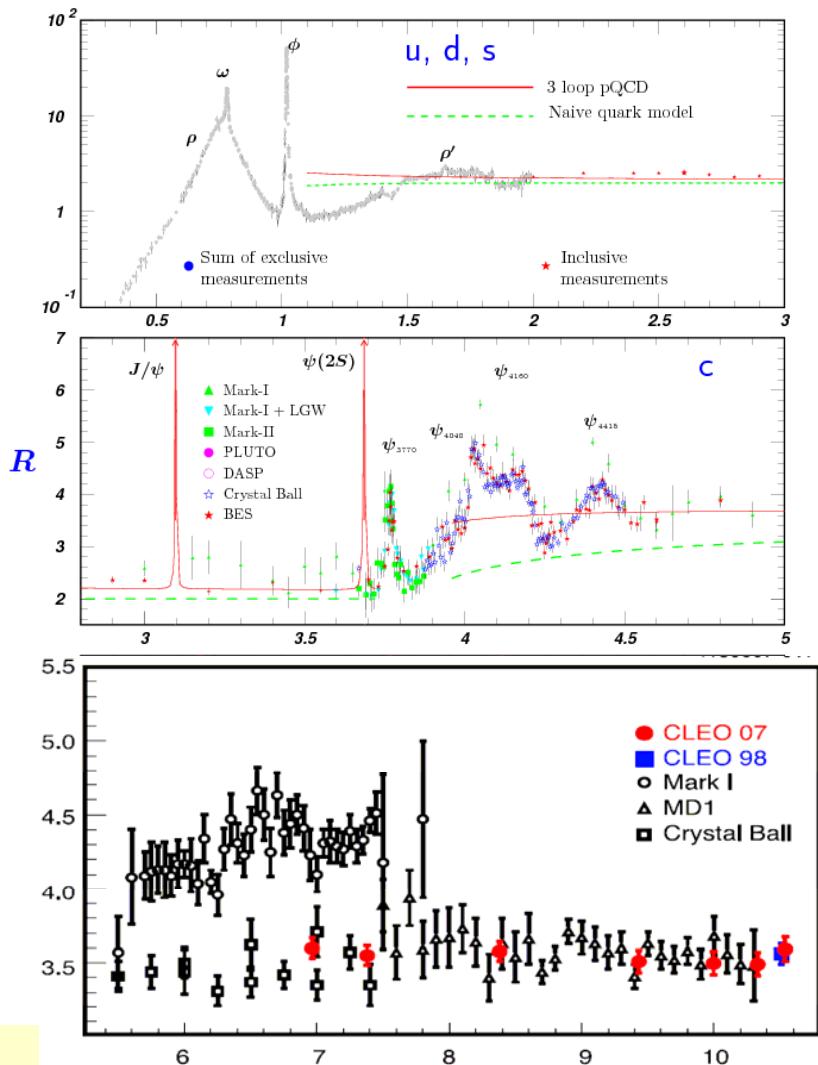
Uncertainties



\hat{K} grows from 0.63 at $s = 4m_{\pi}^2$ to 1 at $s \rightarrow \infty$, $1/s^2$ emphasizes the role of low energies, particularly important is the reaction $e^+e^- \rightarrow \pi^+\pi^-$ with a large cross section below 1 GeV.

R - measurements

R in Light-Flavor, Charm, and Beauty Threshold Regions



$$R_{QCD} = R^{(0)} \left[1 + \frac{\alpha_s}{\pi} + C_2 \left(\frac{\alpha_s}{\pi} \right)^2 + C_3 \left(\frac{\alpha_s}{\pi} \right)^3 + \dots \right]$$

$$R^{(0)} = 3 \sum_q e_q^2, \quad C_2 = 1.411, \quad C_3 = -12.8$$

The most surprising feature of this graph is that the simple quark model with pQCD corrections works down to 1.5 GeV!

Taking $R=R_{QCD}$ we can estimate the $a_{\mu, \text{had}}$ value with $\sim 30\%$ accuracy, but to obtain 1% level of the precision, $O(1000)$ man-years of effort were spent in the last two decades!

Why is R Measurement Interesting?

1. Tests of perturbative QCD QCD sum rules

-quark masses, quark and gluon condensates

-Higher order QCD corrections

- Λ_{QCD} , $\alpha(s)$

2. Hadronic corrections to fundamental parameters:

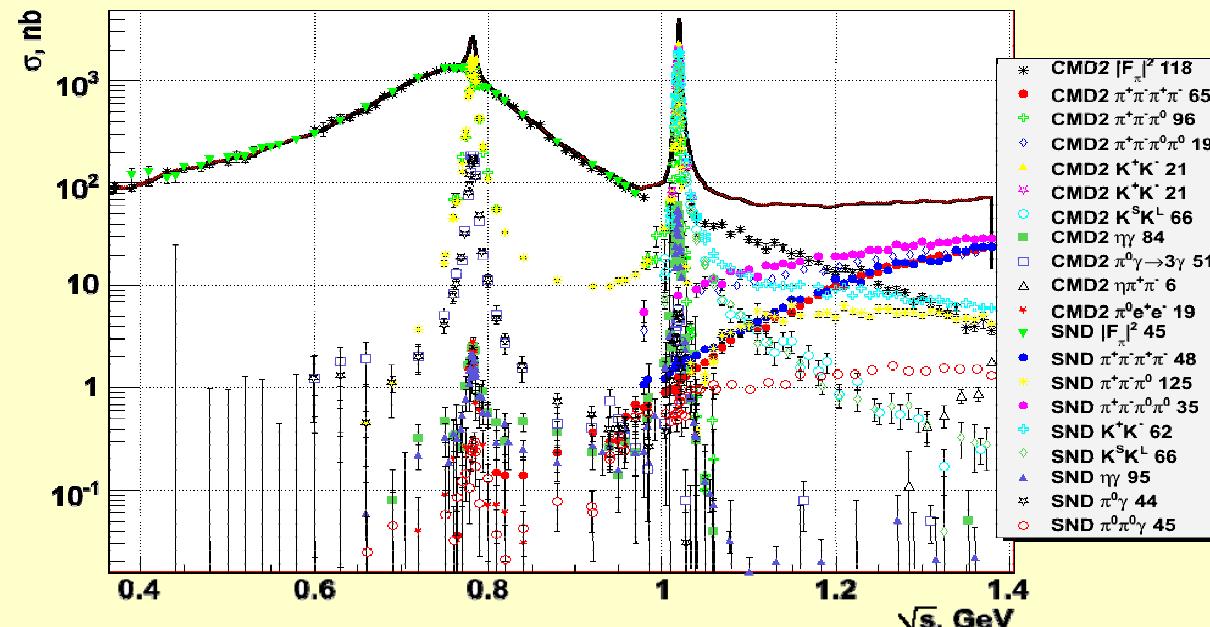
Running fine structure constant - $\alpha(M_Z^2)$

Anomalous magnetic moment of the muon

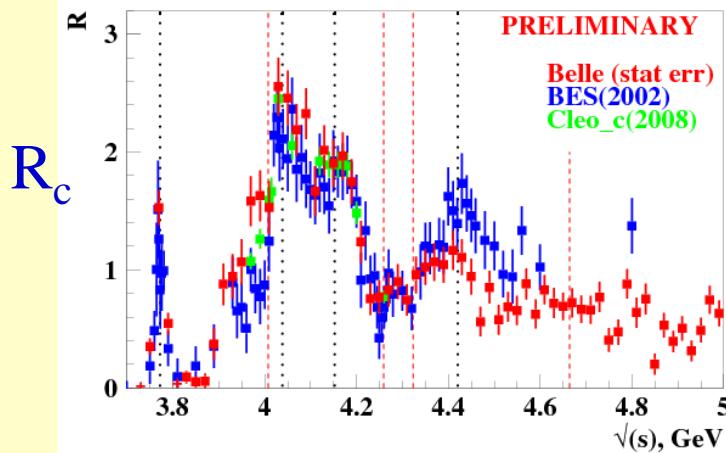
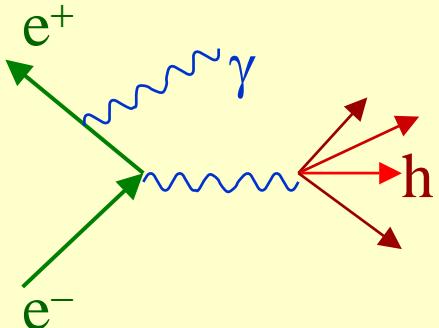
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Depending on the problem, different energy ranges are important.

In the energy range below 2 GeV the total hadronic cross section is obtained as a sum of the exclusive cross sections.

Overview of the results from VEPP-2M e^+e^- collider.

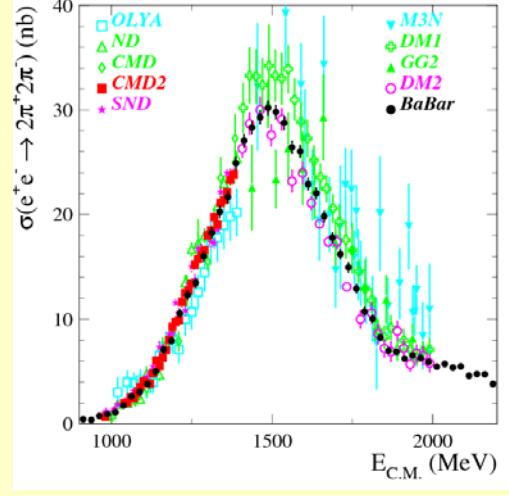
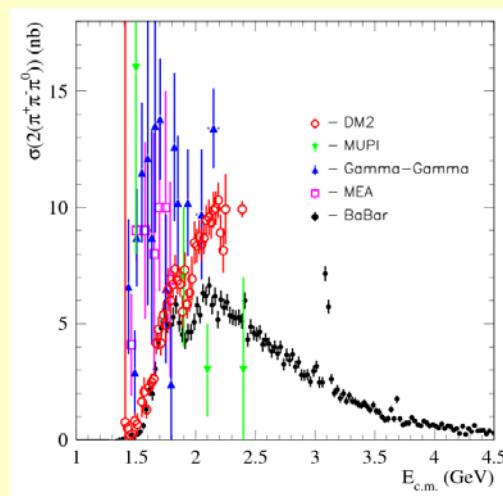
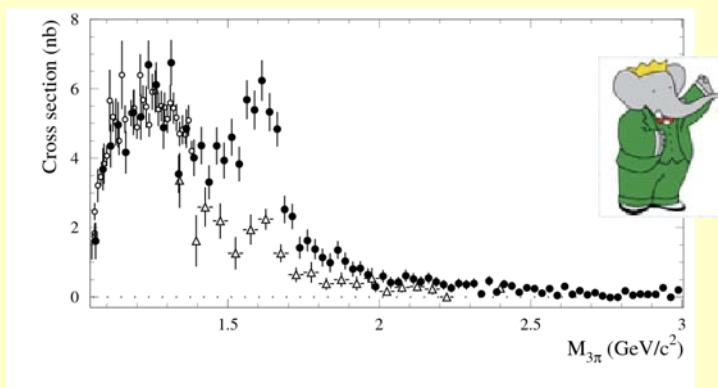


The last years a lot of new data were obtained in the ISR processes by BaBar, Belle and KLOE



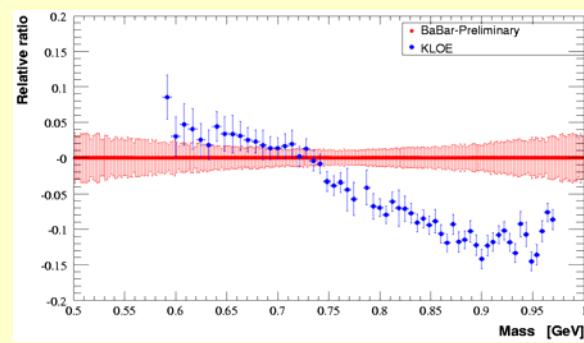
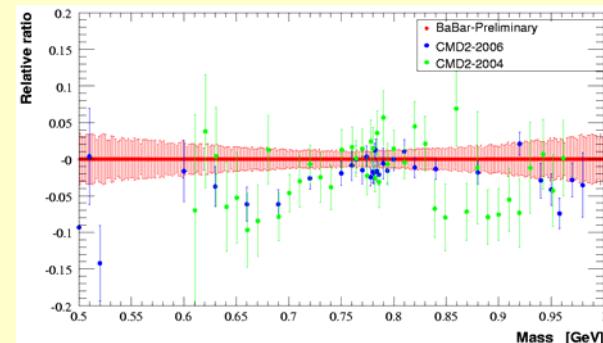
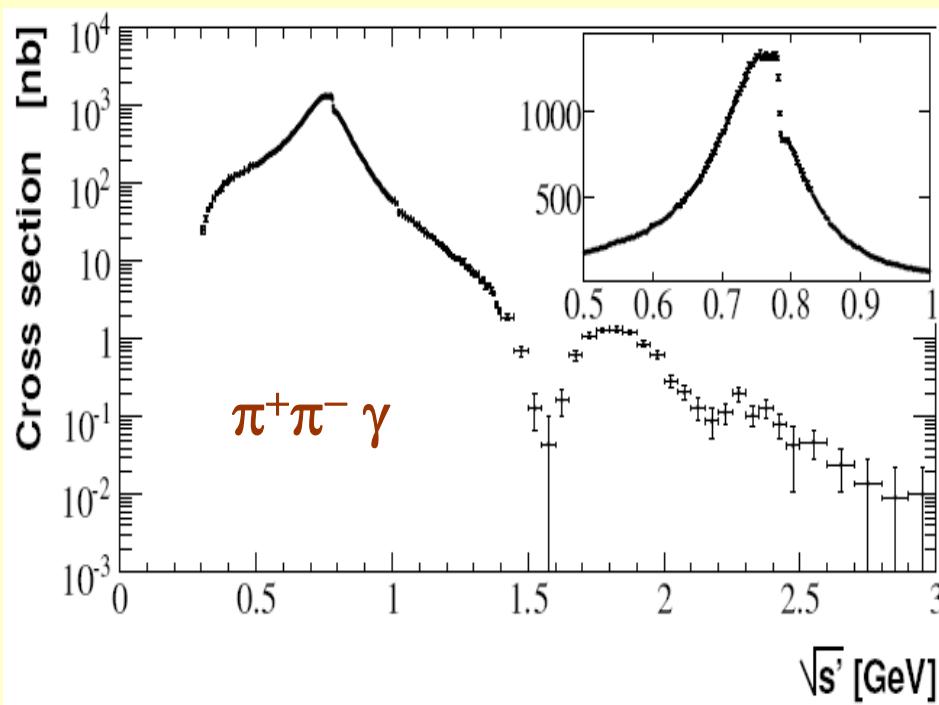
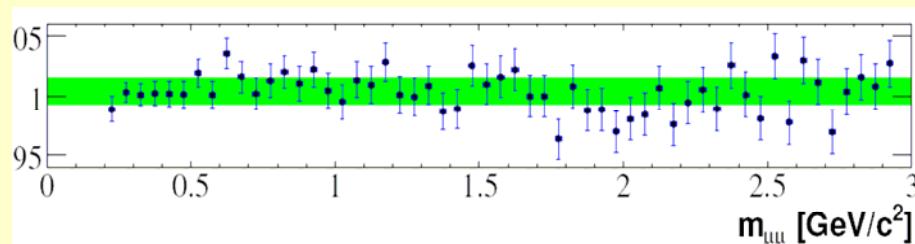
BES: $R_{\text{tot}} - R_{\text{uds}}$;

B,C : $\sum R_{\text{excl}}$



$\pi^+\pi^-\gamma$ - Last minute from BaBar

$\mu^+\mu^-\gamma$ - exp/QED





Computing $a_\mu^{\pi\pi}$

$$\frac{\sigma_{\mu\mu\gamma}^{data}}{\sigma_{\mu\mu\gamma}^{NLO QED}} = 1 + (4.0 \pm 2.0 \pm 5.5 \pm 9.4) \times 10^{-3}$$

From $\pi^+\pi^-$ threshold to 1.8 GeV

$$a_\mu^{\pi\pi(\gamma)} = (514.1 \pm 2.2 \pm 3.1) \times 10^{-10}$$

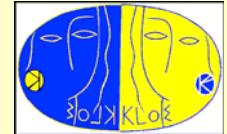
Previous e^+e^- data: $(502.8 \pm 3.2) \times 10^{-10}$

updated value from $\tau^- \rightarrow \pi^-\pi^0\nu_\tau$: $(514.3 \pm 3.0) \times 10^{-10}$

M.Davier et al., arXiv:0906.5443v1 (hep-ph)

According to these results $\Delta a_{\mu,\text{hadr}}$ reduces to $\sim 2\sigma$

Results from KLOE

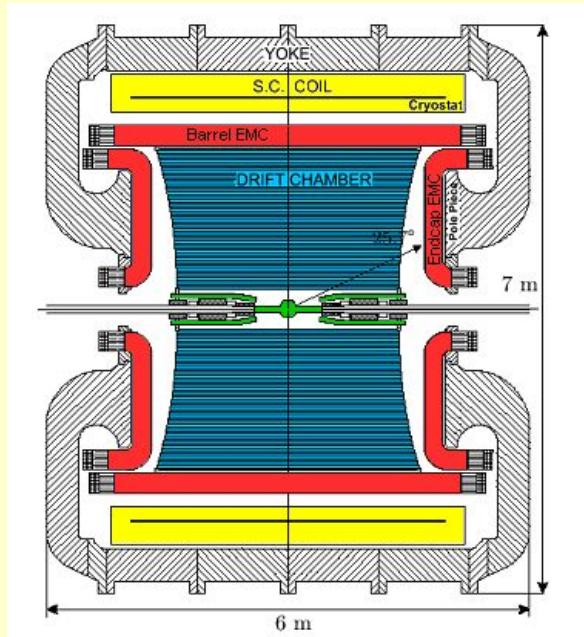
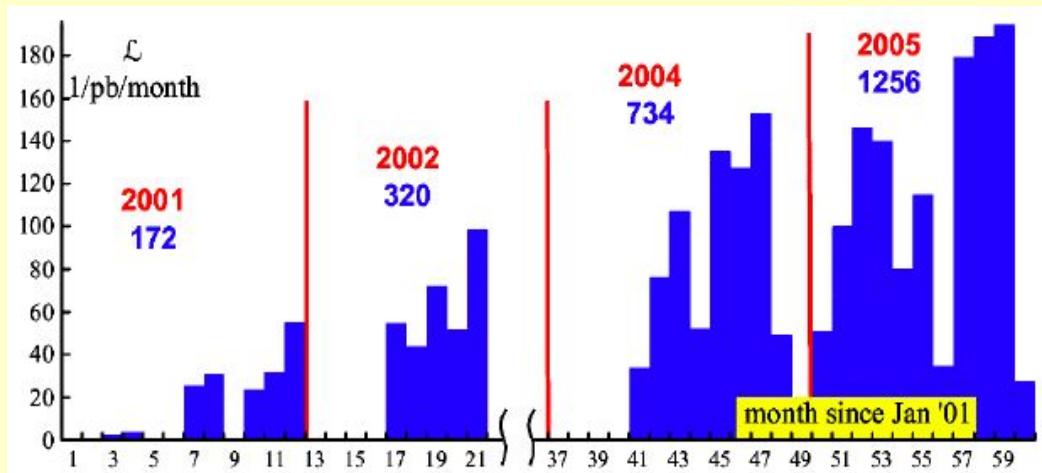


- e^+e^- collider at M_Φ : $\sqrt{s} \sim 1.019$ GeV
- angle btw the beams @ IP $\sim 2 \times 12.5$ mrad
- residual momentum in LAB ~ 13 MeV

2001-05: ~ 2.5 fb $^{-1}$ at M_Φ

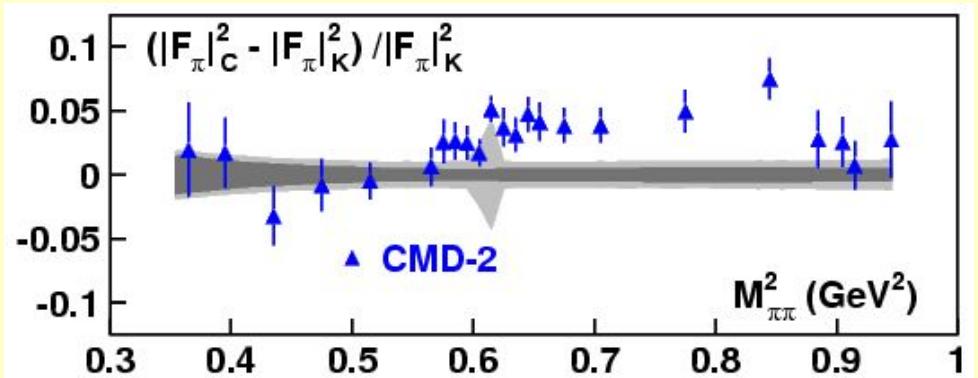
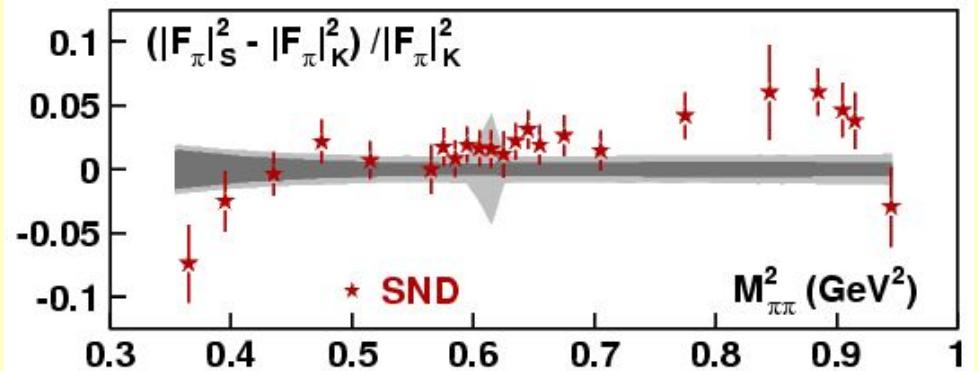
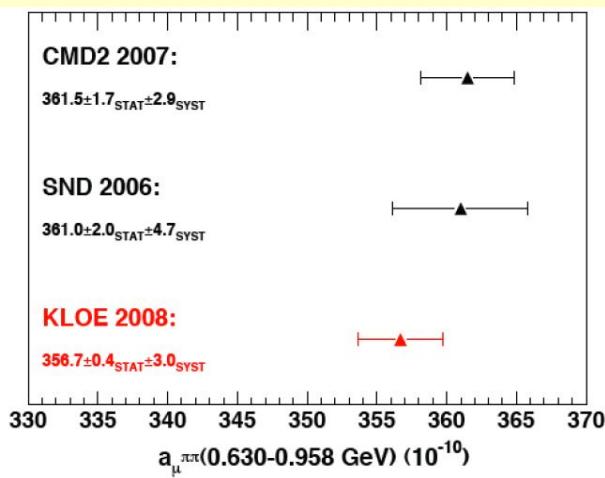
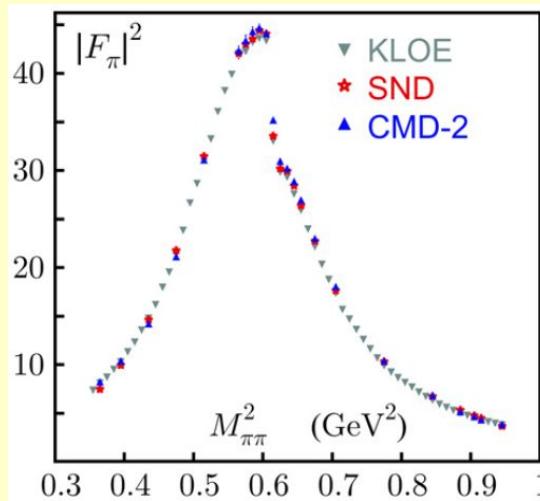
2006: ~ 250 pb $^{-1}$ at $\sqrt{s}=1$ GeV + scan

$$L_{\text{peak}} = 1.3 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$$





Results from KLOE

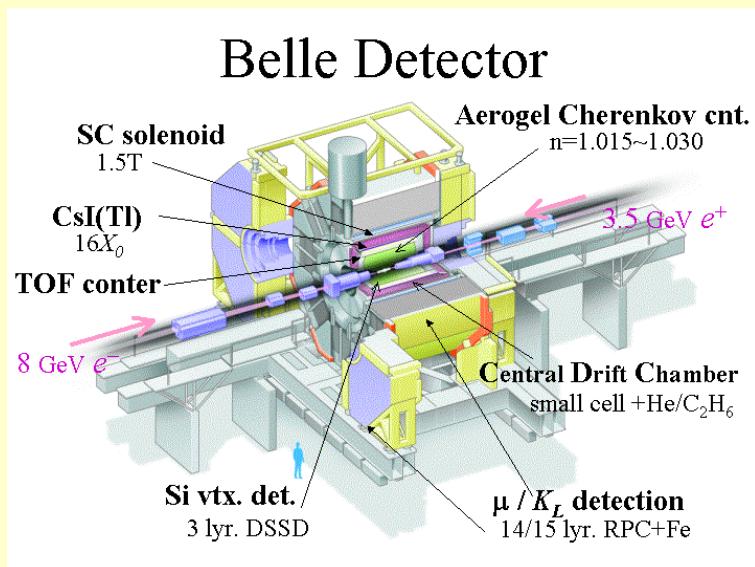


KLOE strengthens the discrepancy $\sim 3.4 \sigma$ between the SM prediction and the BNL measurements

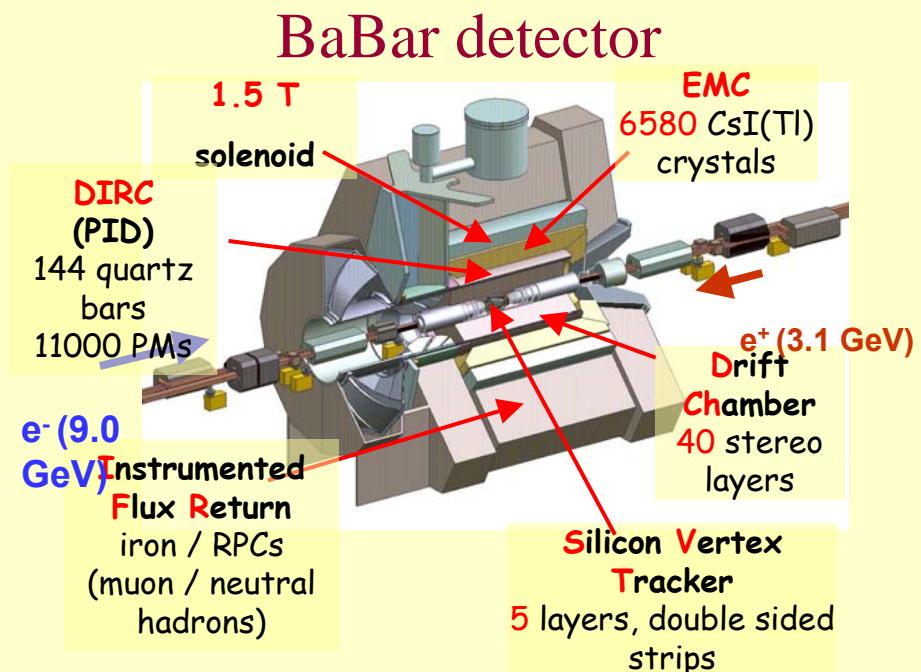
Tau decays study - last years the main contributions came from two B-factories – Belle and BaBar

F/B asymmetric detectors

High vertex resolution, magnetic spectrometry, excellent calorimetry and sophisticated particle ID ability



$$\sum_{\text{Belle } 2006} \int L dt \approx 1.5 ab^{-1}$$
$$\sum_{\text{BaBar } 1999}$$



Clear environment!

→ $\approx 1\ 400\ 000\ 000\ \tau^+\tau^-$

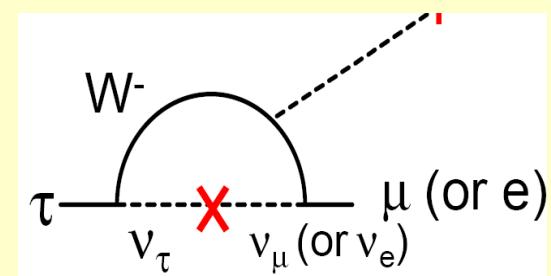
Decay Mode	Experiment	Reference	Result
$(\tau^- \rightarrow K^- \nu_\tau) / (\tau^- \rightarrow e^- \bar{\nu}e)$	BaBar	arXiv:0811.1429 [hep-ex]	$(0.03882 \pm 0.00032 \pm 0.00056)$
		$ g_{\text{tau}}/g_{\mu} = (0.9836 \pm 0.0087)$	
$\tau^- \rightarrow K^- \pi^0 \nu_\tau$	BaBar	Phys.Rev.D76:051104,2007	$(0.416 \pm 0.003 \pm 0.018) \times 10^{-2}$
$\text{tau-} \rightarrow K0\bar{\text{bar}} \pi^- \nu_\tau$	BaBar	arXiv:0808.1121 [hep-ex]	$(0.840 \pm 0.004 \pm 0.023) \times 10^{-2}$
	Belle	Phys.Lett.B654:65-73,2007	$(0.808 \pm 0.004 \pm 0.026) \times 10^{-2}$
$\text{tau-} \rightarrow K^- \pi^- \pi^+ \nu_\tau$ (excl. KS0)	BaBar	Phys.Rev.Lett.100:011801,2008	$(0.273 \pm 0.002 \pm 0.009) \times 10^{-2}$
$\text{tau-} \rightarrow K^- \pi^- K^+ \nu_\tau$	Belle	arXiv:0812.0480 [hep-ex]	$(0.325 \pm 0.002 {}^{+0.016}_{-0.015}) \times 10^{-2}$
	BaBar	Phys.Rev.Lett.100:011801,2008	$(1.346 \pm 0.010 \pm 0.036) \times 10^{-3}$
	Belle	arXiv:0812.0480 [hep-ex]	$(1.53 \pm 0.01 {}^{+0.06}_{-0.06}) \times 10^{-3}$
$\text{tau-} \rightarrow K^- K^- K^+ \nu_\tau$	BaBar	Phys.Rev.Lett.100:011801,2008	$(1.58 \pm 0.13 \pm 0.12) \times 10^{-5}$
	Belle	arXiv:0812.0480 [hep-ex]	$(2.60 \pm 0.23 {}^{+0.10}_{-0.10}) \times 10^{-5}$
$\text{tau-} \rightarrow K^- \phi \nu_\tau$	BaBar	Phys.Rev.Lett.100:011801,2008	$(3.39 \pm 0.20 \pm 0.28) \times 10^{-5}$
	Belle	Phys.Lett.B643:5-10,2006	$(4.05 \pm 0.25 \pm 0.26) \times 10^{-5}$
$\text{tau-} \rightarrow K^* K^- \nu_\tau$	Belle	arXiv:0808.1059 [hep-ex]	$(1.56 \pm 0.02 \pm 0.09) \times 10^{-3}$
$\text{tau-} \rightarrow K^* K^- \pi^0 \nu_\tau$	Belle	arXiv:0808.1059 [hep-ex]	$(2.39 \pm 0.46 \pm 0.26) \times 10^{-5}$
$\text{tau-} \rightarrow K^- \eta \nu_\tau$	Belle	Phys.Lett.B672:209-218,2009	$(1.58 \pm 0.05 \pm 0.09) \times 10^{-4}$
$\text{tau-} \rightarrow K^- \pi^0 \eta \nu_\tau$	Belle	Phys.Lett.B672:209-218,2009	$(4.6 \pm 1.1 \pm 0.4) \times 10^{-5}$
$\text{tau-} \rightarrow K\bar{S}0 \pi^- \eta \nu_\tau$	Belle	Phys.Lett.B672:209-218,2009	$(4.4 \pm 0.7 \pm 0.2) \times 10^{-5}$
$\text{tau-} \rightarrow K^* \eta \nu_\tau$	Belle	Phys.Lett.B672:209-218,2009	$(1.34 \pm 0.12 \pm 0.09) \times 10^{-4}$
$(\text{tau-} \rightarrow \pi^- \nu_\tau) / (\text{tau-} \rightarrow e^- \bar{\nu}e)$	BaBar	arXiv:0811.1429 [hep-ex]	$(0.5945 \pm 0.0014 \pm 0.006)$
		$ g_{\text{tau}}/g_{\mu} = (0.9859 \pm 0.0057)$	
$\text{tau-} \rightarrow \pi^- \pi^0 \nu_\tau$	Belle	Phys.Rev.D78:072006,2008	$(25.24 \pm 0.01 \pm 0.39) \times 10^{-2}$
$\text{tau-} \rightarrow \pi^- \pi^- \pi^+ \nu_\tau$ (excl. KS0)	BaBar	Phys.Rev.Lett.100:011801,2008	$(8.83 \pm 0.01 \pm 0.13) \times 10^{-2}$
	Belle	arXiv:0812.0480 [hep-ex]	$(8.41 \pm 0.00 {}^{+0.34}_{-0.33}) \times 10^{-2}$
$\text{tau-} \rightarrow \pi^- \pi^0 \eta \nu_\tau$	Belle	Phys.Lett.B672:209-,2009	$(1.35 \pm 0.03 \pm 0.07) \times 10^{-3}$
$\text{tau-} \rightarrow \pi^- \phi \nu_\tau$	BaBar	Phys.Rev.Lett.100:011801,2008	$(3.42 \pm 0.55 \pm 0.25) \times 10^{-5}$

Searches for lepton flavour violation in tau decays

In the SM the lepton flavour violation decays are extremely small:

$$\text{Br}(\tau \rightarrow l\gamma) \sim 10^{-54}$$

$$\text{Br}(\tau \rightarrow 3 \text{ leptons}) \sim 10^{-14}$$



Observation of LFV decays would be a clear signal of New Physics

- o Searches for $\mu - e$ LFV: $\mu - e$ conversion, $\mu^- \rightarrow e^- \gamma$ ($B < 1.2 \times 10^{-11}$), $\mu^- \rightarrow e^- e^+ e^-$ ($B < 1.0 \times 10^{-12}$) MEG, PRISM prepared.
- o Many models consider extensions of the Standard Model with enhanced LFV. Particularly popular are SUSY models, e.g. MSSM extension of SM, also discussed SUGRA, GUT, Higgs, little Higgs.

Predicted $B(\tau^- \rightarrow \mu^- \gamma)$ reach $10^{-8} - 10^{-7}$

- o At Belle and BaBar 44 different modes studied. The most stringent limit is

$B(\tau^- \rightarrow \mu^+ e^- e^-) < 1.5 \times 10^{-8}$. The sensitivity is limited by background suppression/statistics.

Example - results from Belle



$\tau^- \rightarrow \mu^-\gamma, e\gamma$ (PLB666, 16(2008))

Final state: 1-prong decays and others

Data: 535fb⁻¹

$\text{Br}(\tau^- \rightarrow \mu^-\gamma) < 4.5 \times 10^{-8}$ at 90% C.L.

$\text{Br}(\tau^- \rightarrow e^-\gamma) < 1.2 \times 10^{-7}$ at 90% C.L.

sensitivity is limited by the remaining background from $e^+e^- \rightarrow \tau^+\tau^-\gamma$

$\tau \rightarrow e/\mu(\eta, \eta', \pi^0)$ (PLB648, 341 2007))

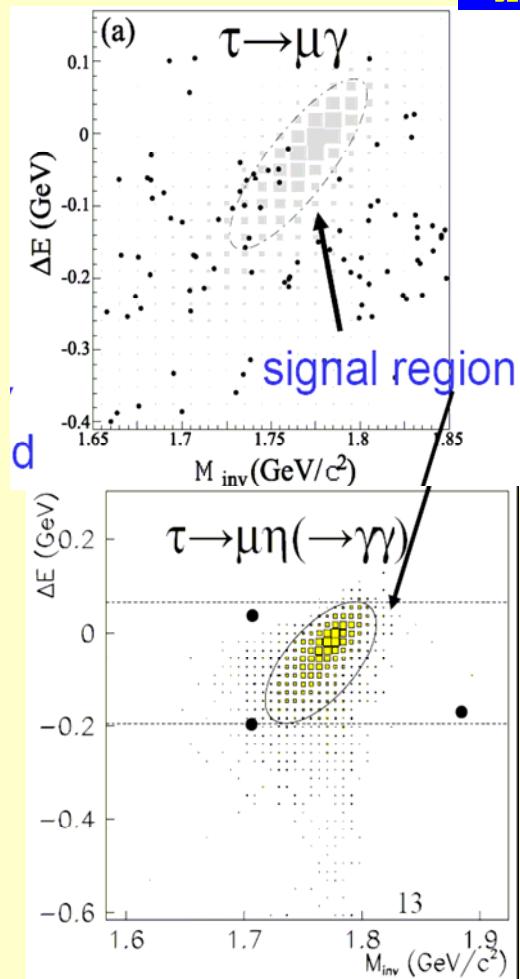
Data: 401fb⁻¹

Expected BG : (0.0-0.6) events

Nobs : 1 event

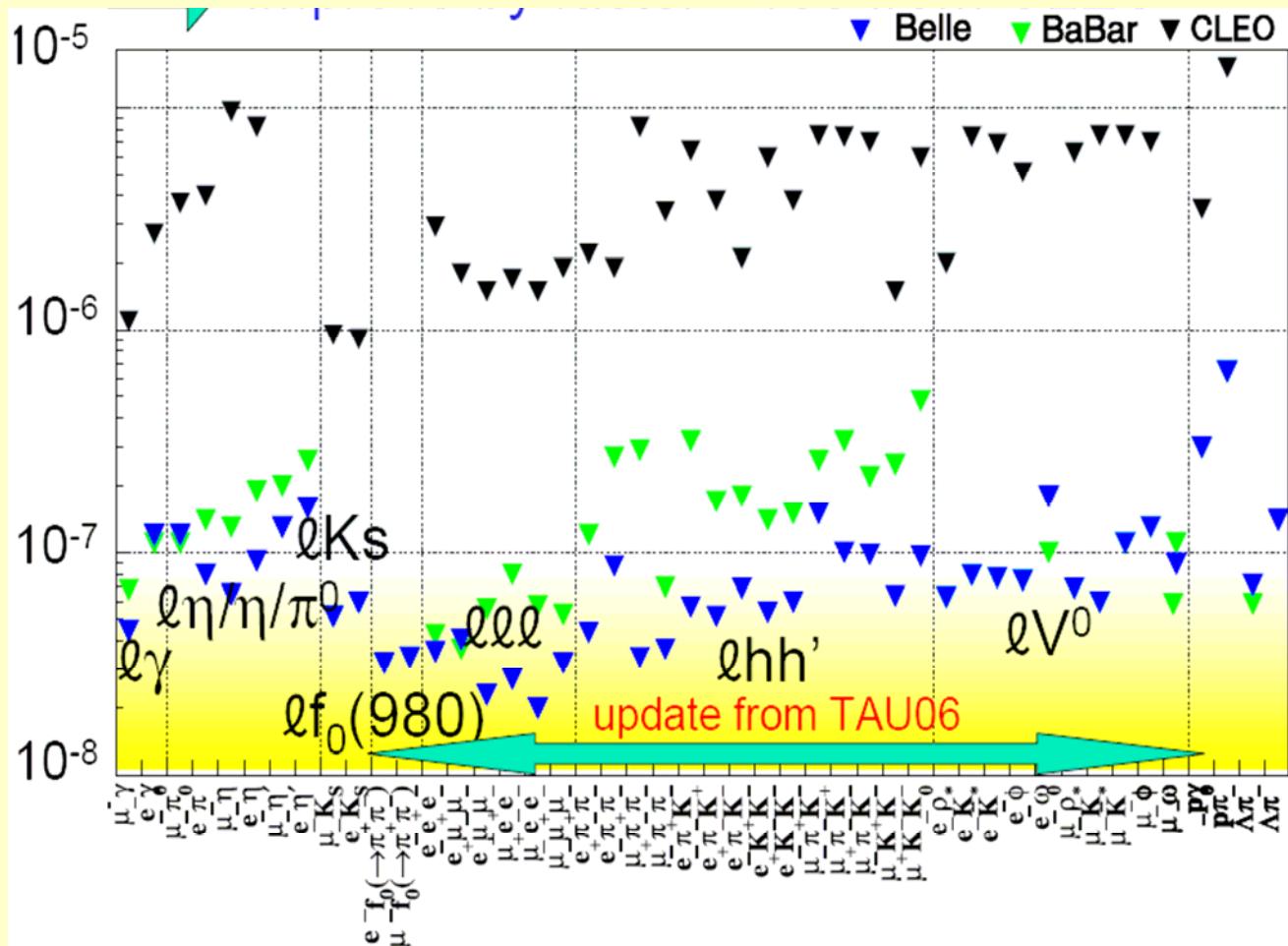
$\text{Br}(\tau \rightarrow \mu\eta, \mu\eta', \mu\pi^0) < (6.5-13) \times 10^{-8}$

$\text{Br}(\tau \rightarrow e\eta, e\eta', e\pi^0) < (8.0-16) \times 10^{-8}$

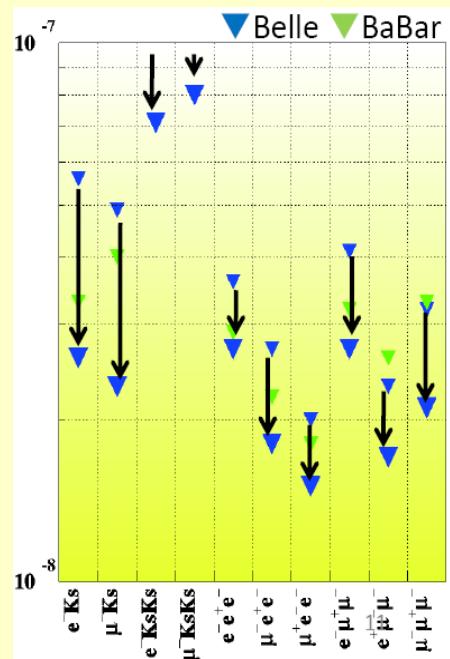


Points - data

Recent Upper limits on LFV τ decays

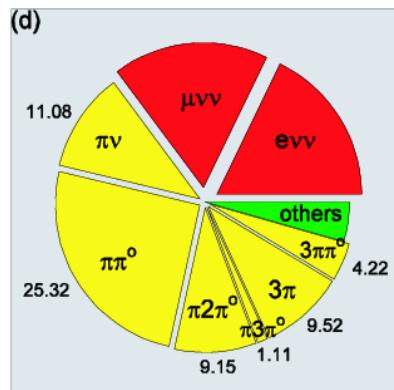
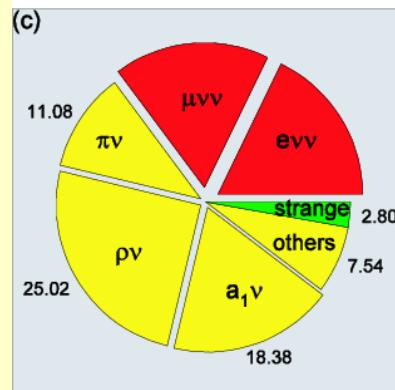
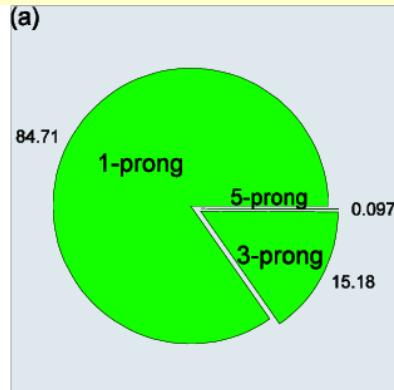
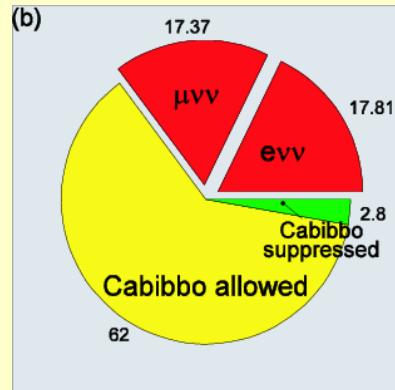


From
EPS 09



Improvement by factor ~ 100 from CLEO

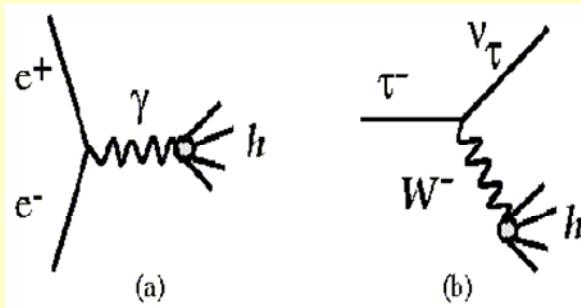
Main motivations to study tau hadronic decays



- ✓ τ -lepton decays provide an excellent laboratory to study hadron physics up to 1.8 GeV. The main attraction is quite clear initial state.
- ✓ Tests of CVC and evaluation of the a_μ from spectral functions.
- ✓ Search for CP violation effects in the hadronic decays in hope to find new physics.
- ✓ Improvement of the limits on the neutrino mass.

$\tau^- \rightarrow \pi^- \pi^0 \nu_\tau$ decay –important features:

- Largest branching fraction
- Connection to e^+e^- via CVC



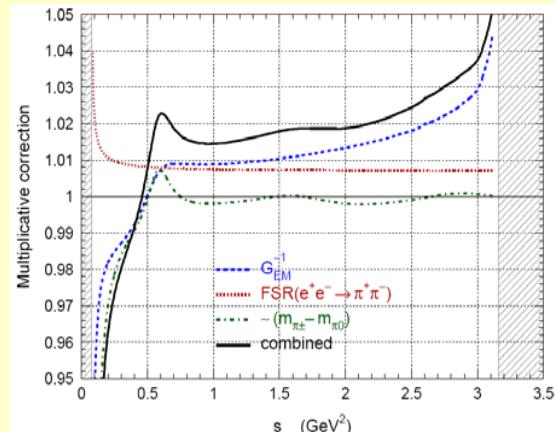
$$\frac{1}{N_{\pi\pi}} \frac{dN_{\pi\pi}}{ds} = \frac{6\pi |V_{ud}|^2 S_{EW}}{m_\tau^2} \times \frac{B_e}{B_{\pi\pi}} \left[\left(1 - \frac{s}{m_\tau^2}\right)^2 \left(1 + \frac{2s}{m_\tau^2}\right) \right] v^{\pi\pi}(s)$$

$$v^{\pi\pi^0}(s) = \frac{\beta^3(s)}{12\pi} |F_\pi(s)|^2$$

Corrections to the Spectral Functions

- $S_{EW} = 1.0233 \pm 0.0006$
- Real photons, loops
- FSR
- $m_{\pi^\pm} \neq m_{\pi^0}$ (phase space, $\Gamma\rho$)
- $m_{\rho^\pm} \neq m_{\rho^0}$
- $\rho - \omega$ interference
- Radiative decays ($\pi\pi\gamma$, $\pi(\eta)\gamma$, $l+l-$)
- $m_u \neq m_d$
- and 2 class currents

V. Cirigliano, G. Ecker,
H. Neufeld, 2002
M.Davier et al., 2002



$\tau^- \rightarrow \pi^-\pi^0\nu_\tau$ – recent results from Belle : Branching Fraction



updated results from Belle experiment based on 5.6×10^6 $\tau^- \rightarrow \pi^- \pi^0 \nu_\tau$ decays (72.2/fb). Presented at Tau-08.

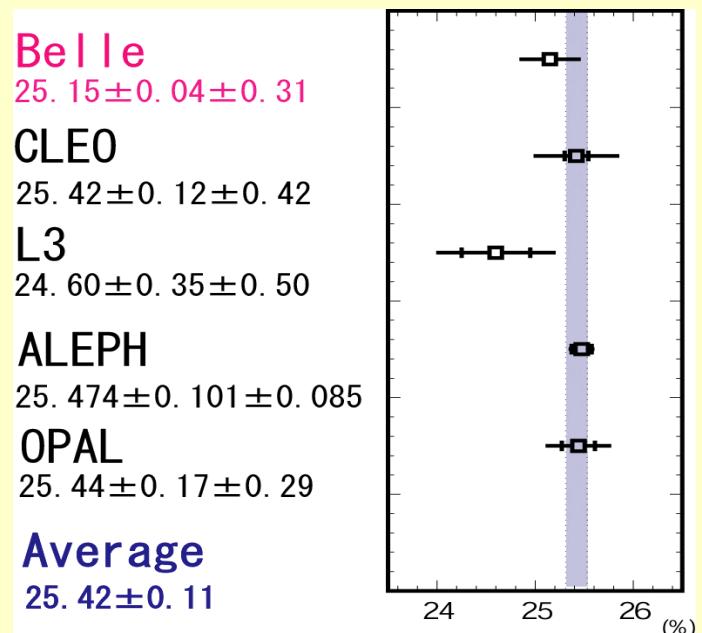
$$\text{Br}_{\gamma\pi} = (25.24 \pm 0.01(\text{stat}) \pm 0.39(\text{sys}))\%$$

Systematic uncertainties Source	$\Delta B/B, \%$
Tracking efficiency	0.47
π^0 efficiency	1.3
Background in τ -pair	0.59
Feed down background	0.16
Continuum background	0.20
γ veto	0.20
Trigger	0.32
MC statistics	0.08
Total	1.52

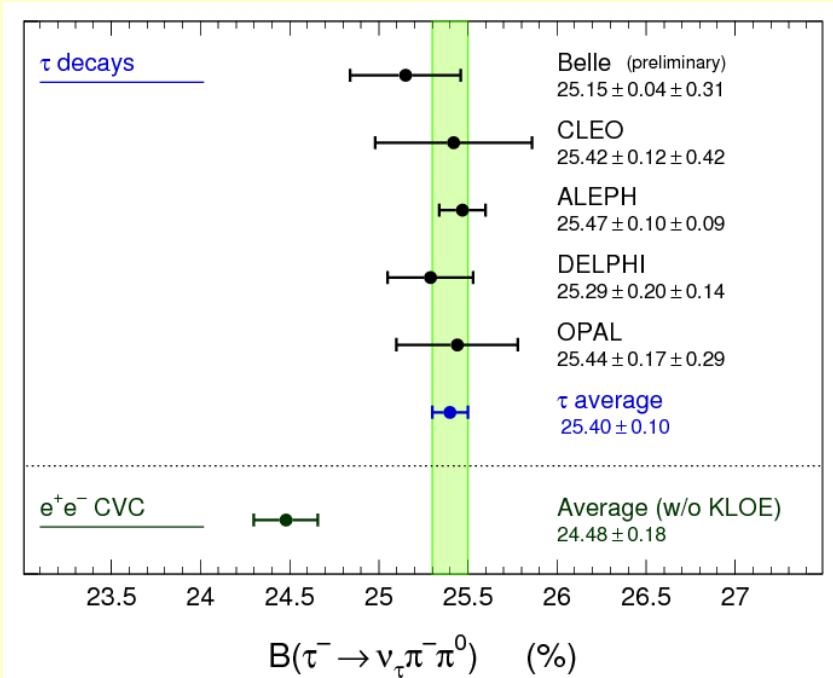
Systematic is dominated by the uncertainty of the π^0 efficiency and the BG in τ -pair

π^0 Calibrated by η signals ($\eta \rightarrow \pi^0\pi^0\pi^0/\eta \rightarrow \gamma\gamma$).

Checked by using electron tracks.



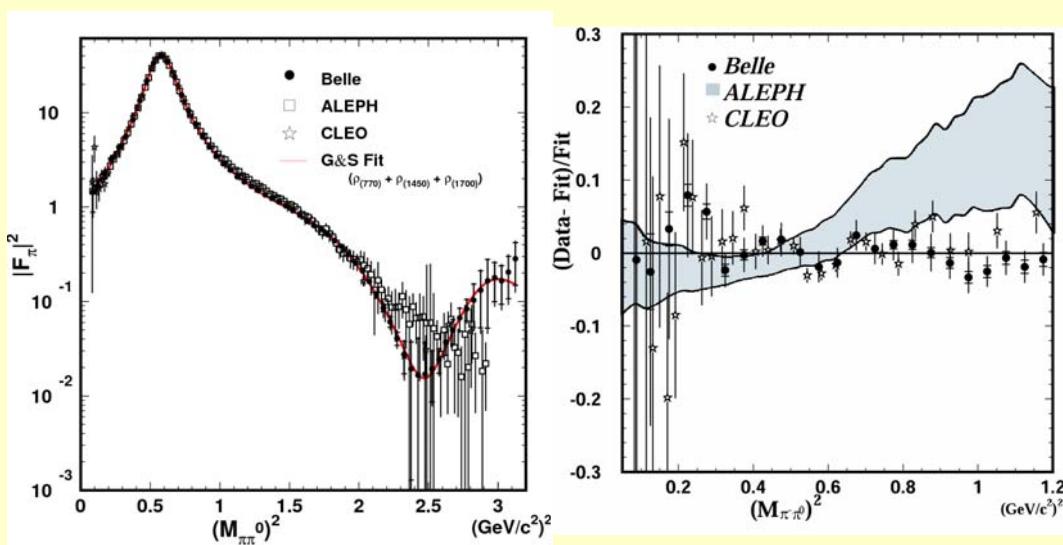
CVC in the 2π channel. e^+e^- vs. τ



The branching from all groups is systematically higher than the CVC prediction:

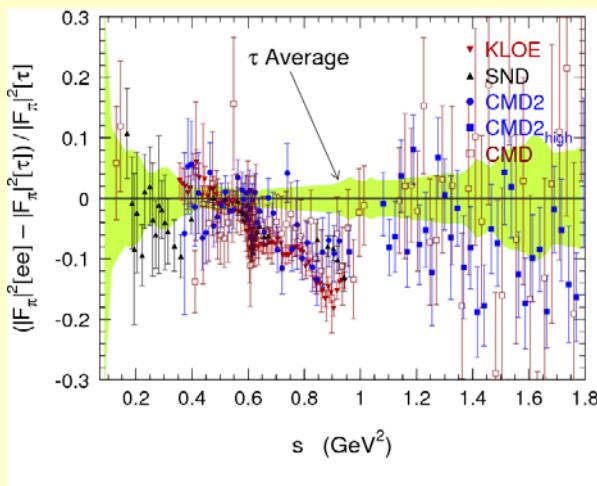
$B - Bee = (0.92 \pm 0.21)\%$ or 4.5σ from 0. The discrepancy is a 3.6% effect, about twice the SU(2) correction.

$\tau^- \rightarrow \pi^- \pi^0 \nu_\tau$ – recent results from Belle



Systematics, %

$M^2_{\pi\pi}$	threshold	ρ region	ρ'	ρ''
Total	5.3	0.7	1.8	11.4



Belle(τ)

$$a_\mu^{\pi\pi} = (523.5 \pm 1.5(\text{exp.}) \pm 2.6(\text{Br}) \pm 2.5(\text{isospin})) \times 10^{-10}$$

ALEPH, CLEO, OPAL (τ)

Ref. Eur. Phys. J. C27, 497 (2003)

$$a_\mu^{\pi\pi} = (520.1 \pm 2.4(\text{exp.}) \pm 2.7(\text{Br}) \pm 2.5(\text{isospin})) \times 10^{-10}$$

CMD2, SND (e^+e^-)

Ref. Nucl. Phys. Proc. Suppl. 169, 288 (2007)

$$a_\mu^{\pi\pi} = (504.6 \pm 3.1(\text{exp.}) \pm 0.9(\text{rad.})) \times 10^{-10}$$

Search for 2nd Class Currents

1CC – PG(-1)^J = +1: $J^{PG} = 0^-(\pi), 1^+(\rho), 1^+(a_1), \dots$

2CC – PG(-1)^J = -1: $J^{PG} = 0^+(a_0), 1^{++}(b_1), \dots$

S. Weinberg (Phys. Rev. **112**, 1375 (1958))

Experiment	$B(\tau^- \rightarrow \eta \pi^- \nu_\tau), 10^{-4}$
HRS, 1987	$510 \pm 100 \pm 120$
CLEO, 1987	< 100
ARGUS, 1988	< 90
CLEO, 1992	< 3.4
CLEO, 1996	< 1.4
ALEPH, 1997	< 6.2
experiment	$B(\tau^- \rightarrow \eta' \pi^- \nu_\tau), 10^{-5}$
CLEO, 1997	< 7.4
BaBar, 2006	< 1.2

2nd class currents suppressed

in SM: $\propto (m_u - m_d)$

$\tau^- \rightarrow \eta \pi^- \nu_\tau$ has $J^{PG} = 0^+$

Theory prediction:

$B(\tau^- \rightarrow \eta \pi^- \nu_\tau) \sim 10^{-6} - 10^{-5}$.

Large BG from $\tau^- \rightarrow \eta \pi^- \pi^0 \nu_\tau$

with $B = (1.77 \pm 0.24) \cdot 10^{-3}$

Up to now no SCC were not found in experiment

Recent results of a search for $\tau^- \rightarrow \eta \pi^- \nu_\tau$ at Belle

Studied sample contained $6.2 \times 10^8 \tau$ pairs

(EPS -09)

$$e^+ + e^- \rightarrow \tau^- + \tau^+$$

$$\tau^- \rightarrow \pi^- + \eta + \nu_\tau$$

$$\eta \rightarrow \pi^+ + \pi^- + \pi^0 (\rightarrow \gamma\gamma)$$

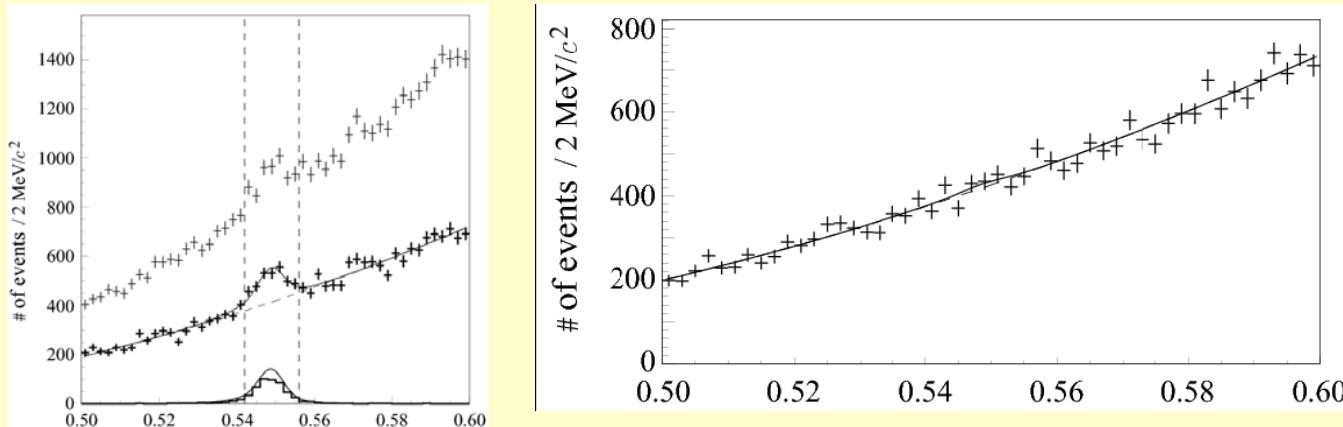
$$\tau^- \rightarrow l^+ + \nu_\tau + \nu_\lambda + n\gamma$$

signal side

tag side



Additional condition – $M(4\pi) < 1.2 \text{ GeV}$



After BG subtraction $N_{\eta, \text{sig}} = N_{\eta, \text{fit}} - N_{\eta, \text{BG}} = 190.9 \pm 68.6$

$$B(\tau^- \rightarrow \eta \pi^- \nu_\tau) = (4.4 \pm 1.6 \pm 0.8) \times 10^{-5}$$

$$B(\tau^- \rightarrow \eta \pi^- \nu_\tau) < 7.3 \times 10^{-5} \text{ @90%CL}$$

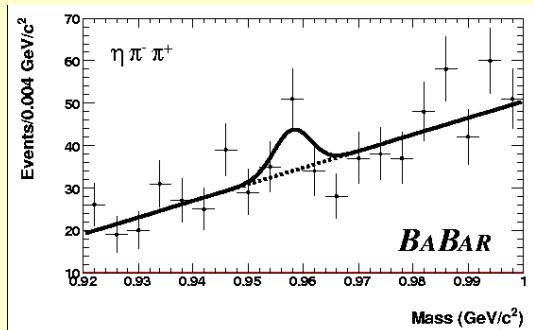
$$B(\tau^- \rightarrow \eta' \pi^- \nu_\tau) < 4.6 \times 10^{-6} \text{ @90%CL}$$



BaBar searches for SCC

$\tau^- \rightarrow \eta' \pi^- \nu_\tau$

Integrated luminosity of 384 fb^{-1} (706 million τ -decays)

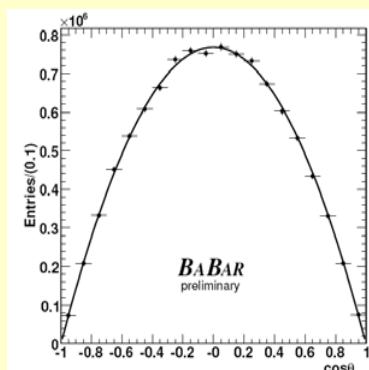


$M(\eta\pi\pi)$

Fit gives 19 ± 13 events

$B(\tau^- \rightarrow \eta'(958)\pi^- \nu_\tau) < 7.2 \times 10^{-6}$
at 90% confidence level

omega pi nu \Rightarrow vector (FCC) + axial-vector (SCC)



Integrated luminosity of 347 fb^{-1} (319 million τ -pairs)

$$\frac{N^{\omega\pi(\text{non-vector})}}{N^{\omega\pi(\text{vector})}}$$

< 0.69% at 90% C.L. and 0.85% at 95% CL

arXiv:0807.4900 [hep-ex].

▲ CLEO: < 6.4% at the 95% CL

K. E. Edwards et. al., Phys. Rev. D61, 072003 (2000),

▲ ALEPH: < 8.6% at the 95% CL

D. Buskulic et. al., Zeit. Phys. C74, 263 (1997).



$|V_{us}|$ from Tau Decays

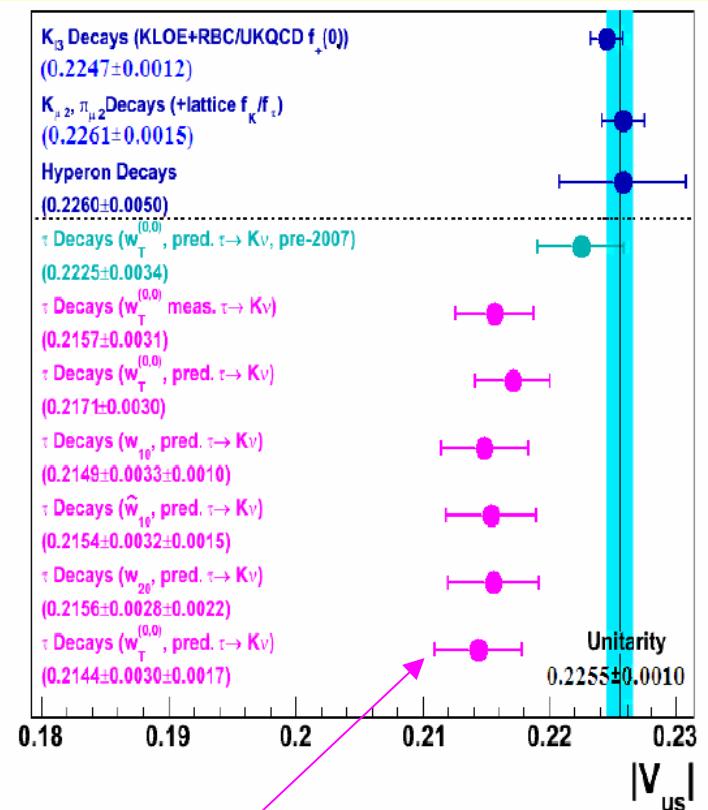
$$R_\tau = \frac{\Gamma(\tau^- \rightarrow h^- \bar{\nu}_\tau)}{\Gamma(\tau^- \rightarrow e^- \bar{\nu}_e \bar{\nu}_\tau)} = R_s + R_{ns}$$

$$|V_{us}|^2 = \frac{R_s}{R_{ns} / |V_{ud}|^2 - \delta R_\tau}$$

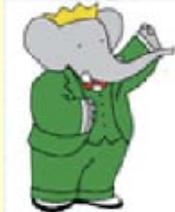
The branching fractions and invariant mass distributions are the experimental input to determine $|V_{us}|$ well measured from superallowed beta decays

This is determined from Finite Energy Sum Rules and is relatively small, so that even a large relative error can yield a precise measurement

of $|V_{us}|$ (e.g. ~6% of $R_{\text{non-strange}}/|V_{ud}|^2$ and known to better than 10%)



these points use same data, different weight functions in FESR

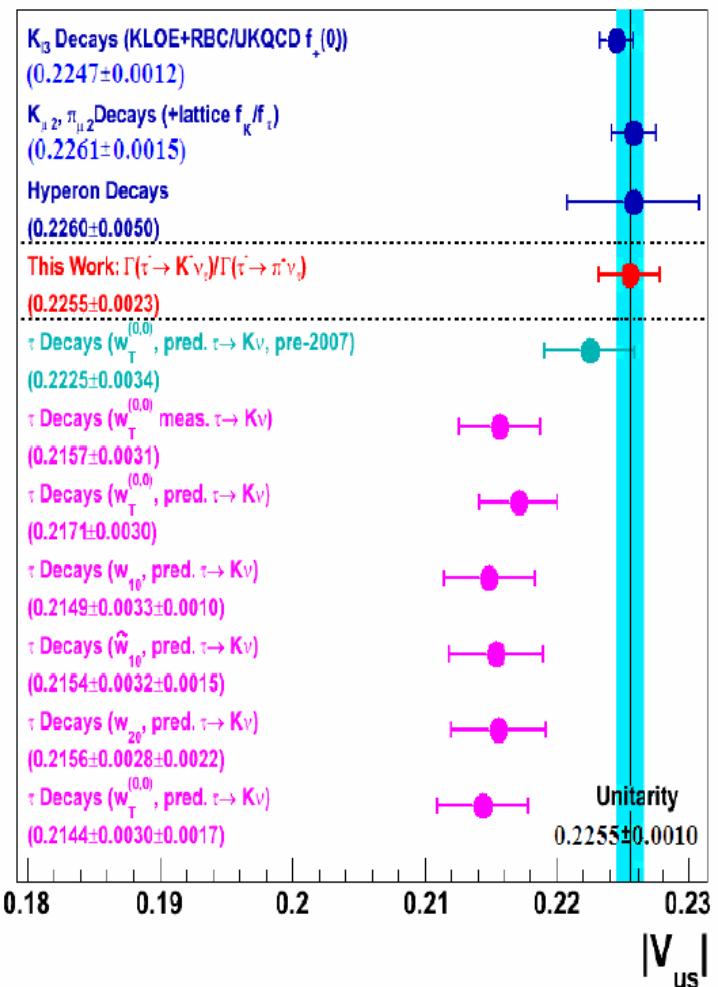


Independent determination of |V_{us}| in Tau Decays by Babar

$$\frac{\Gamma(\tau \rightarrow K \nu_\tau)}{\Gamma(\tau \rightarrow \pi \nu_\tau)} = \left| \frac{V_{us}}{V_{ud}} \right|^2 \frac{f_K^2}{f_\pi^2} \left(\frac{1 - m_K^2 / m_\tau^2}{1 - m_\pi^2 / m_\tau^2} \right)^2 (1 + \delta_{RC}^\tau)$$

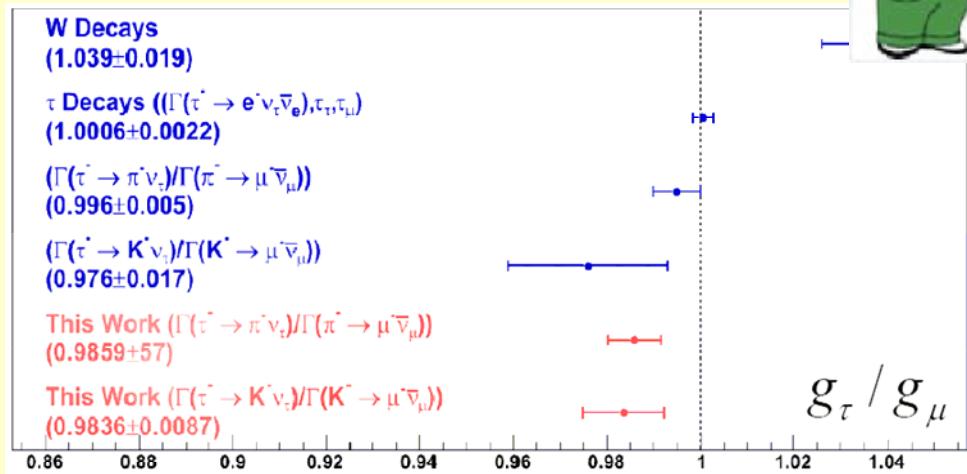
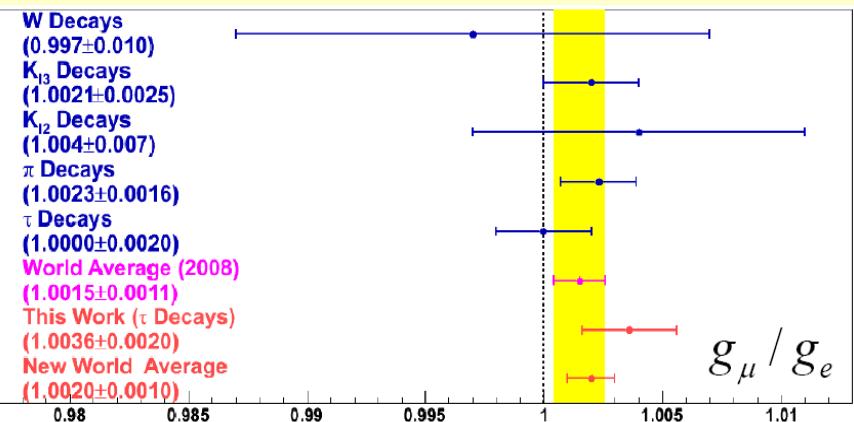
Measure $B(\tau \rightarrow K \nu_\tau)/B(\tau \rightarrow \pi \nu_\tau)$

- Take $f_K/f_\pi = 1.189 \pm 0.007$ from Lattice QCD
(E. Follana, et al. PRL 100, 062002 (2008))
- $\delta\tau RC = 0.03\%$
- $|V_{ud}| = 0.97408 \pm 0.00026$ from superallowed beta decays





Lepton universality and tau mass



From Standard Model

$$G_F = \frac{g^2}{4\sqrt{2}M_W^2}, \quad g = g_e = g_\mu = g_\tau$$

Experimental Measurements
W Decays:

ALEPH, DELPHI, L3, and OPAL

τ Decays:

ALEPH, DELPHI, L3, OPAL,
and CLEO

Kaon Decays:

KLOE

Pion Decays:

TRIUMF and PSI

$$r = \left(\frac{g_\tau}{g_\mu} \right)^2 = \left(\frac{m_\mu}{m_\tau} \right)^5 \left(\frac{\tau_\mu}{\tau_\tau} \right) B(\tau \rightarrow e \nu_\tau \bar{\nu}_e) \frac{F_{cor}(m_\mu, m_e)}{F_{cor}(m_\tau, m_e)}$$

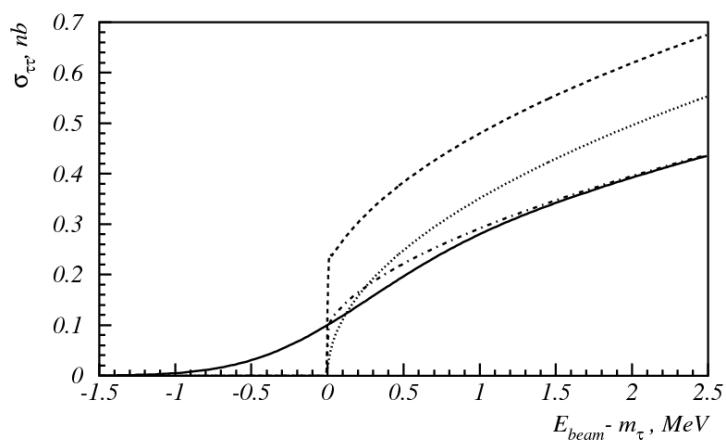
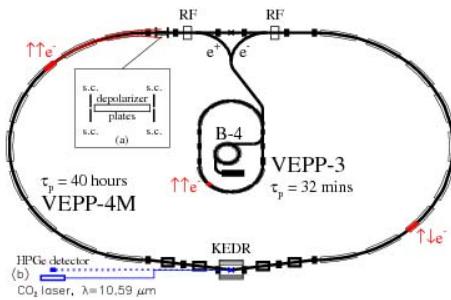
r	τ , fs	$B(\tau \rightarrow e \nu_\tau \bar{\nu}_e)$, %	m_τ , MeV
1.0020 ± 0.0051	290.6 ± 1.1 0.0038	17.84 ± 0.06 0.0034	$1776.99^{+0.29}_{-0.26}$ 0.0008

$$M_\tau = (1776.69 + 0.17 - 0.19 + -0.15) \text{ MeV} \quad \text{PDG 2004}$$

$$\text{Mass } m_\mu = 105.658367 \pm 0.000004 \text{ MeV}$$

$$\text{Mass } m_e = 0.510998910 \pm 0.000000013 \text{ MeV}$$

M_τ at KEDR: $\tau^+\tau^-$ cross section near threshold



$L_{max} = 2 \cdot 10^{30} \text{ cm}^{-2} \text{ s}^{-1}$ at 1.78 GeV/beam

Two independent methods of energy measurement

Resonant depolarization for absolute calibration (slow):

$$\Omega/\omega = 1 + \gamma \cdot \mu / \mu_0,$$

Ω - spin precession frequency,

ω - revolution frequency,

μ (μ_0) - anomalous (normal) emm

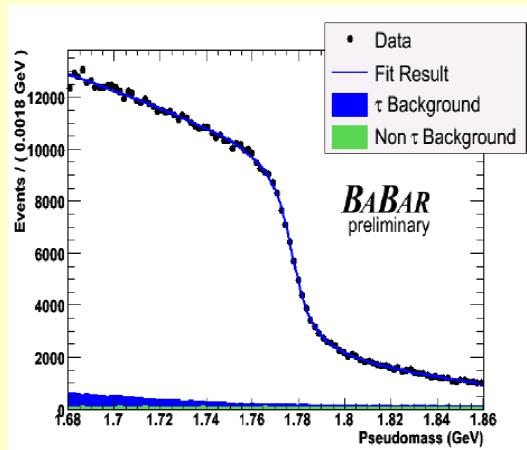
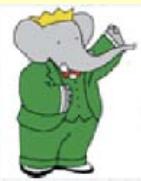
Compton backscattering of

laser 0.12 MeV photons (fast)

M_τ at Belle and BaBar: analysys of the hadronic decays by Pseudomass method

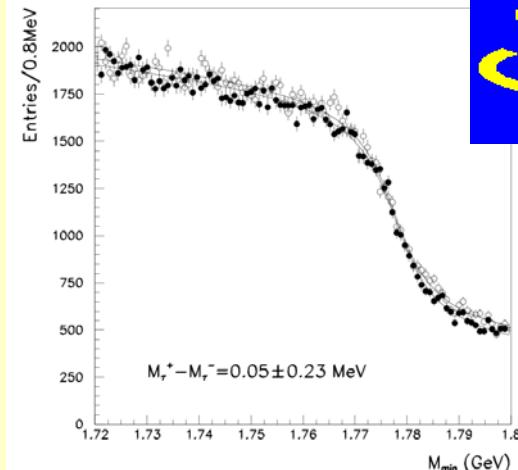
$$\begin{aligned}
 M_\tau^2 &= (E_h + E_\nu)^2 - (\vec{p}_h + \vec{p}_\nu)^2 = M_h^2 + 2(E_\tau - E_h)(E_h - p_h \cos \theta) \\
 &\geq M_p^2 = M_h^2 + 2(E_{beam} - E_h)(E_h - p_h)
 \end{aligned}$$

BaBar: ~389 million $\tau^+\tau^-$ pairs



Belle: 414 fb^{-1} or $370 \times 10^6 \tau^+\tau^-$ pairs

~ $5.8 \times 10^5 \tau^- \rightarrow \pi^+ \pi^- \pi^- \nu_\tau$ events



$$\Delta m = m_{\tau^+} - m_{\tau^-}$$

Group	OPAL, 2000	Belle, 2007	BaBar, 2008
$N_{\tau^+\tau^-}, 10^6$	0.16	370	389
$\Delta m/m_\tau, 10^{-4}$	0.0 ± 18.0	0.3 ± 1.5	-3.5 ± 1.3
$\Delta m/m_\tau, 10^{-4} 90\% CL$	< 30.0	$< 2.8 \times 10^{-4}$	$-5.6 < \dots < -1.4$

Group	M_τ , MeV
BES, 1996	$1776.96+0.18-021+0.25-0.17$
PDG, 2006	$1776.99+0.29-0.26$
KEDR, 2007	$1776.81+0.25-0.23\pm 0.15$
Belle, 2007	$1776.61 \pm 0.13 \pm 0.35$
PDG, 2008	1776.83 ± 0.18
KEDR, 2008	$1776.68+0.17-0.19\pm 0.15$
BaBar, 2008	$1776.68 \pm 0.12 \pm 0.41$

What is next?

Next 3 – 5 - years:

Intensive analysis of the ~1.5 ab⁻¹ data sample harvested by both B-factories;

New results from KLOE and KEDR;

First results from BES-III;

First results from LHC

.....

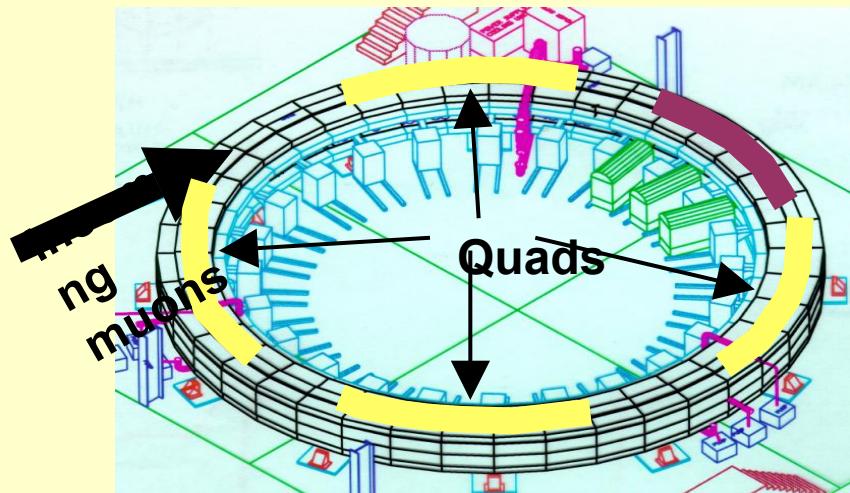
What's then? ⇒

Successor of the BNL E821

◆ **Experimental uncertainty = 63×10^{-11}
(0.54 ppm)**

- **0.46 ppm statistical**
- **0.28 ppm systematic**

The New ($g - 2$) Experiment: A Proposal to Measure the Muon Anomalous Magnetic Moment to ± 0.14 ppm Precision	
<p>New ($g - 2$) Collaboration: R.M. Carey¹, K.R. Lynch¹, J.P. Miller¹, B.L. Roberts¹, W.M. Morse², Y.K. Semertzidis², V.P. Druzhinin³, B.I. Khazin³, I.A. Koop³, I. Logashenko³, S.I. Redin³, Y.M. Shatunov³, Y. Orlov⁴, R.M. Talman⁴, B. Casey⁵, J. Johnstone⁵, D. Harding⁵, A. Klebaner⁵, A. Leveling⁵, J-F. Ostiguy⁵, N. Mokhov⁵, D. Neuffer⁵, M. Popovic⁵, S. Striganov⁵, M. Syphers⁵, G. Velev⁵, S. Werkema⁵, F. Happacher⁶, G. Venanzoni⁶, P. Debevec⁷, M. Grosse-Perdekamp⁷, D.W. Hertzog⁷, P. Kammler⁷, C. Polly⁷, K.L. Giovanetti⁸, K. Jungmann⁹, C.J.G. Onderwater⁹, N. Saito¹⁰, C. Crawford¹¹, R. Fatemi¹¹, T.P. Gorringe¹¹, W. Korsch¹¹, B. Plaster¹¹, V. Tishchenko¹¹, D. Kawall¹², T. Chupp¹³, C. Ankenbrandt¹⁴, M.A. Cummings¹⁴, R.P. Johnson¹⁴, C. Yoshikawa¹⁴, André de Gouvêa¹⁵, T. Itahashi¹⁶, Y. Kuno¹⁶, G.D. Alkhazov¹⁷, V.L. Golovtsov¹⁷, P.V. Neustroev¹⁷, L.N. Uvarov¹⁷, A.A. Vasilyev¹⁷, A.A. Vorobyov¹⁷, M.B. Zhalov¹⁷, F. Gray¹⁸, D. Stöckinger¹⁹, S. Baefler²⁰, M. Bychkov²⁰, E. Frlez²⁰, and D. Počanić²⁰</p>	



parameter	BNL	FNAL	gain factor	FNAL/BNL
Y_π pion/p into channel acceptance	$\approx 2.7\text{E}-5$	$\approx 1.1\text{E}-5$		0.4
L decay channel length	88 m	900 m		2
decay angle in lab system	3.8 ± 0.5 mr	forward		3
$\delta p_\pi / p_\pi$ pion momentum band	$\pm 0.5\%$	$\pm 2\%$		1.33
FODO lattice spacing	6.2 m	3.25 m		1.8
inflector	closed end	open end		2
total				11.5

Proposal for J-PARC experiment

New Muon g-2/EDM Experiment@J-PARC

Proposal in preparation

- Current result is 3.4 sigma above from the SM value
- New generation of muon g-2/EDM experiment is being explored at J-PARC
 - To improve the statistics and systematics
 - To further explore new physics
- With completely new technique
 - Off magic momentum with **ultra-cold muon beam** at 300 MeV/c
 - Stored in **ultra-precision B field** without E-field so that the $\vec{B} \times \vec{E}$ term drops
 - Separation of g-2 and EDM?

$$\vec{\omega}_a = -\frac{e}{m} \left[a_\mu \vec{B} + \frac{\eta}{2} (\vec{\beta} \times \vec{B}) \right]$$

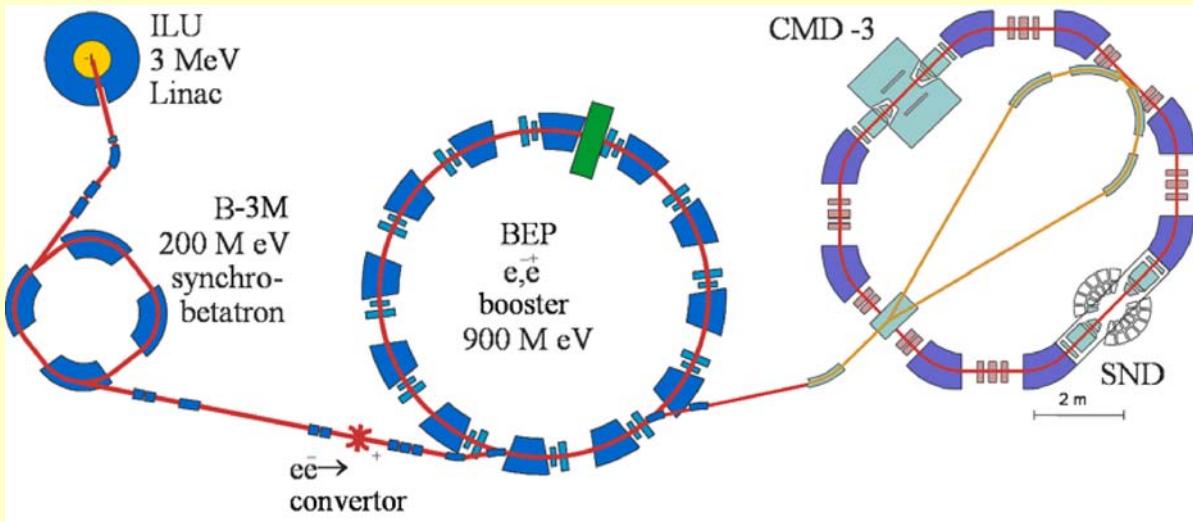
Proton beam (3 GeV, 1MW) Surface Muon (~ 30 MeV, 4×10^8 /s)



Muon Linac (300 MeV/c)



VEPP-2000 storage ring at BINP



$\approx 100 \text{ 1/pb per detector per year}$

Status:

construction is finished

had first beams and collisions

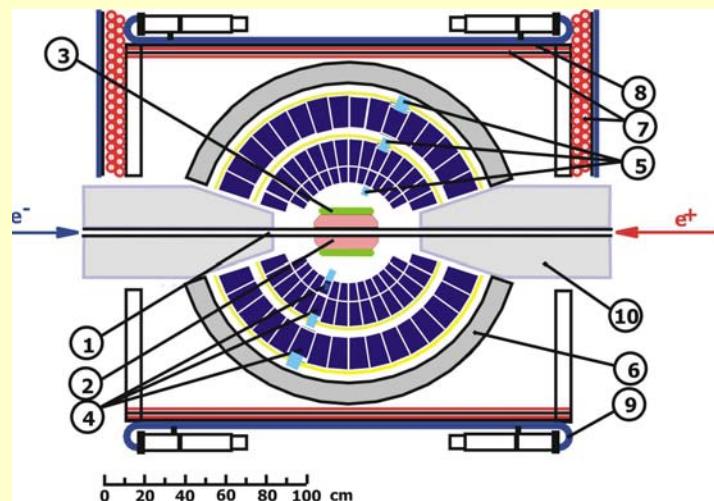
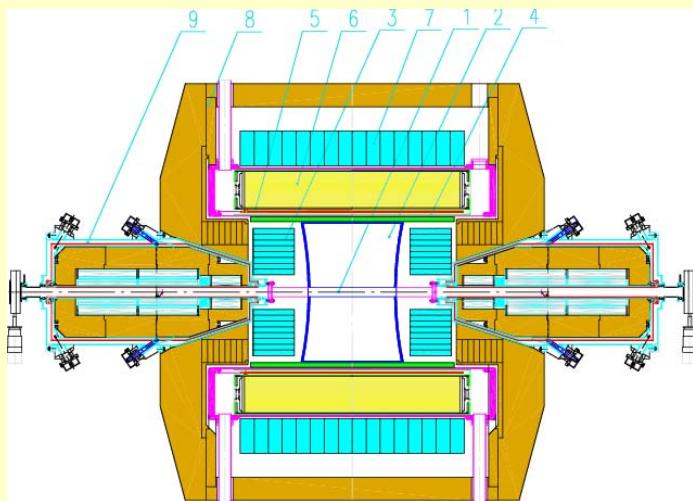
2009 - start of experiments

- Up to 2 GeV c.m. energy
- Factor >10 in luminosity

$L=10^{31} \text{ cm}^{-2}\text{c}^{-1}, \sqrt{s}=1.0 \text{ GeV}$

$L=10^{32} \text{ cm}^{-2}\text{c}^{-1}, \sqrt{s}=2.0 \text{ GeV}$

Detectors for VEPP-2000



Advantages compared to CMD-2:

- new drift chamber with x2 better resolution - better tracking
- thicker barrel calorimeter better separation
- LXe calorimeter
 - much better spatial resolution for γ 's
 - shower profile

Advantages compared to "old" SND:

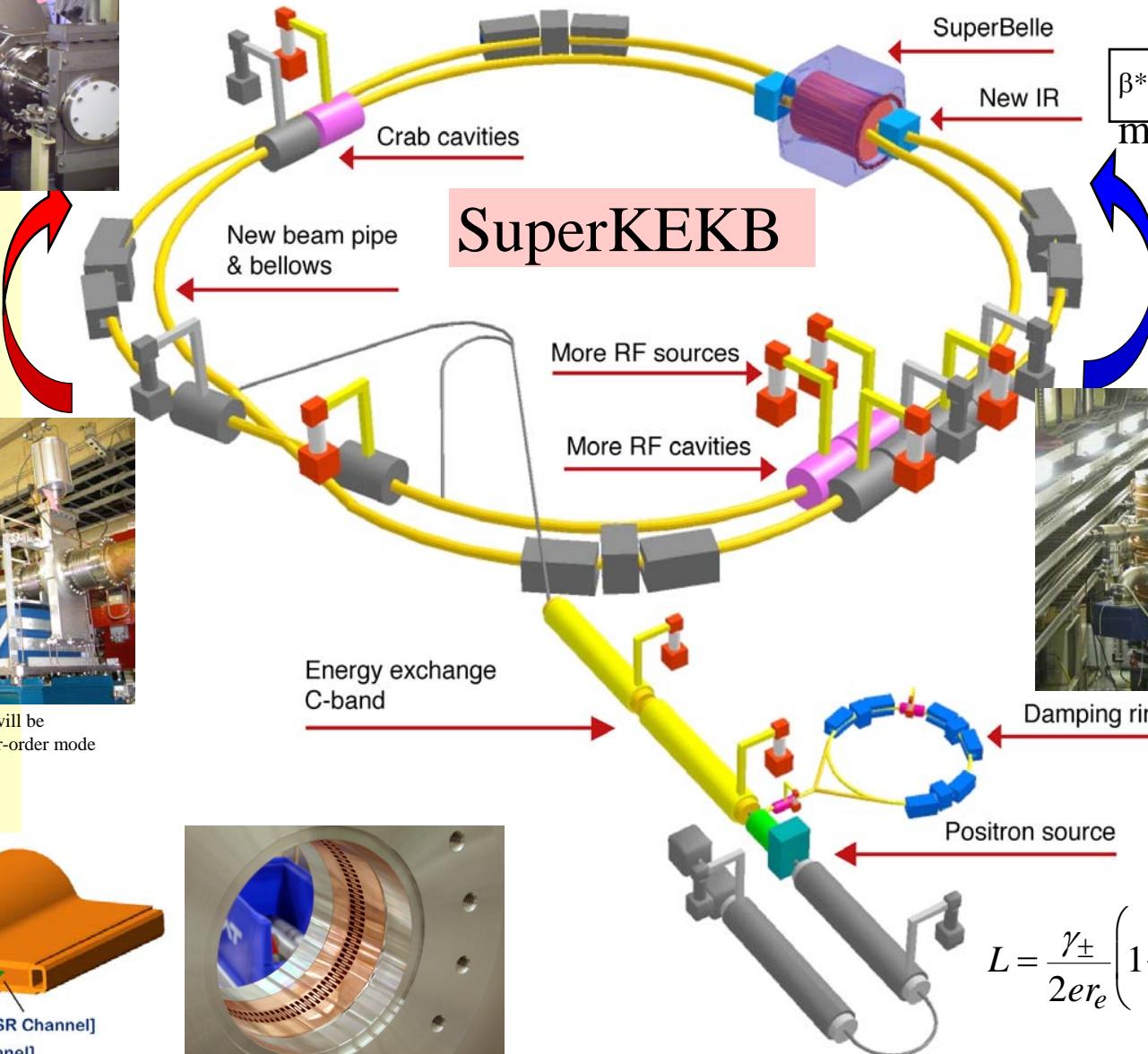
- new system - cherenkov counter ($n=1.05, 1.13$)
- e/π separation $E < 450$ MeV
- π/K separation $E < 1$ GeV
- new drift chamber
 - better tracking
 - better determination of solid angle

We expect to:

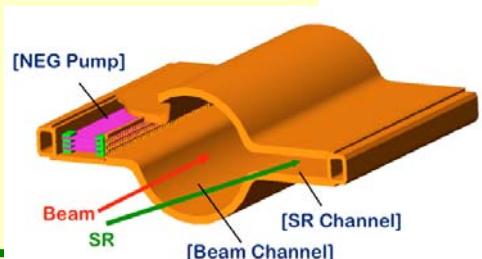
- measure 2π mode to 0.3-0.4%, 4π mode to 2%
- overall improvement in R precision by factor 2-3
- Efforts of theorists are highly needed!



Crab cavities will be installed and tested with beam in 2006.



The superconducting cavities will be upgraded to absorb more higher-order mode power up to 50 kW.



The beam pipes and all vacuum components will be replaced with higher-current-capacity ones.
21.08.2009



Lepton

will reach $8 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$.

$$L = \frac{\gamma_{\pm}}{2e r_e} \left(1 + \frac{\sigma_y^*}{\sigma_x^*} \right) \frac{I_{\pm} \xi_{\pm y}}{\beta_v^*} \left(\frac{R_L}{R_y} \right)$$

Super B-factory

Super (KEK)B-factory:(10~50) ab⁻¹

Expected sensitivity

$\tau \rightarrow \ell\gamma$ Br~O(10^{-8~9})

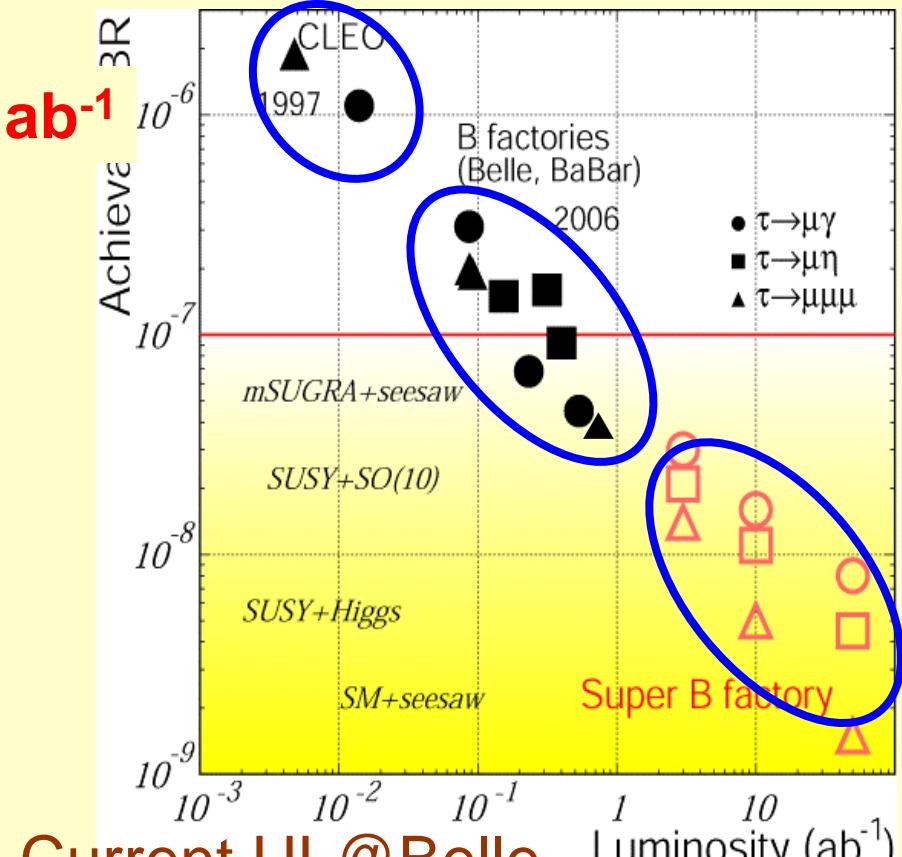
$\tau \rightarrow \ell\ell\ell$, l+meson Br~O(10^{-9~10})

● Super (KEK) B GOAL:

Improve the sensitivity by additional factor of 100 and achieve 10⁻¹⁰

● $\tau \rightarrow \mu\gamma$ and $\tau \rightarrow e\gamma$:

Background dominated



Current UL@Belle

$\text{Br}(\tau \rightarrow \mu\mu\mu) < 3.2 \times 10^{-8}$ @ 543 fb⁻¹

$\text{Br}(\tau \rightarrow \mu\mu\mu) < 3 \times 10^{-10}$ @ 50 ab⁻¹

Conclusion

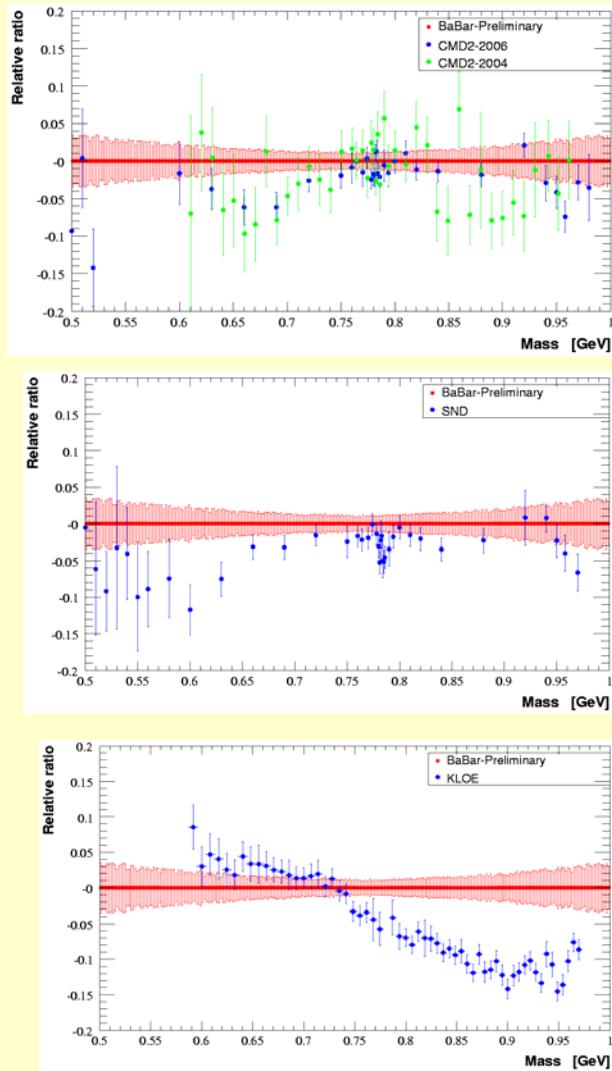
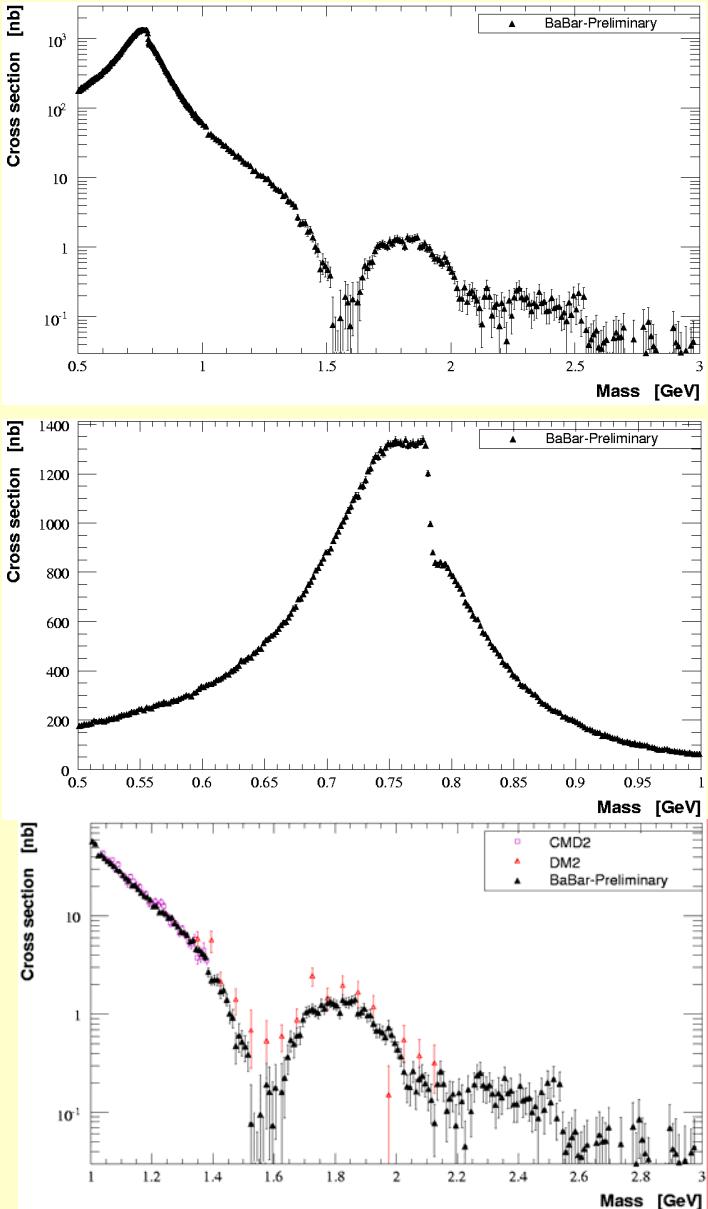
In the last three decades the Standard Model (SM) was successfully used to describe variety of physical phenomena in the wide energy range – from atomic transitions to the hundreds GeV scale. On the other hand, a word “model” in the title reflects the common feeling that some more fundamental theory can be hidden behind SM. At present many experiments are aimed to search for the SM boundaries.

In the considered class of experiments at low energies we can see some (illusive? real?) discrepancies with the calculations based on the SM. These can be barely taken as the indications of a NP, however, we have to apply new efforts to clarify this phenomena.

Hopefully, in the next 5-10 years we'll receive answers from new experiments and advanced theoretical approaches.

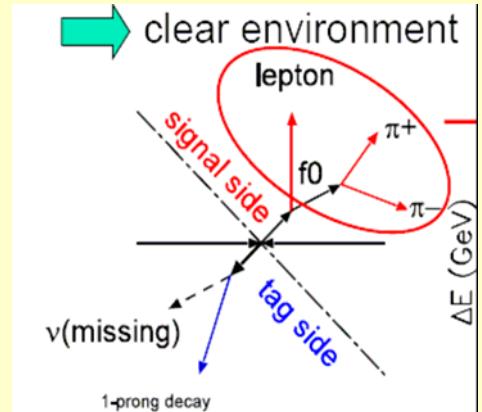
Back up

BaBar – $\pi^+\pi^-$, Tau-08



Analysis method

- ✓ At Y(4S) (10.58 GeV) $\sigma(e^+e^- \rightarrow \tau^+\tau^-) = 0.92 \text{ nb} \Rightarrow 100 \text{ fb}^{-1}$ provides $N = 92 \times 10^6$.
- ✓ We divide the event space by the plane perpendicular to the thrust axis into two hemispheres { “tag” side , in which some ordinary decay (usually
 - ✓ 1-prong modes are selected) is observed and “signal” side , in which we try to completely reconstruct a neutrinoless LFV decay.
 - ✓ Decays we are searching for are very rare ($P < 10^{-7}$) \Rightarrow mostly background (BG) is detected in the “signal” side. We apply various kinematical, topological and PID cuts to suppress BG.
 - ✓ We compare various distributions in data with MC to be sure that we completely understand BG.
 - ✓ We calculate the branching ratio or place an upper limit:
 $B = N_{\text{sig}} / 2N_{\tau^+\tau^-} \varepsilon$, where N_{sig} - signal yield, ε - acceptance



$$M_{\text{inv}} = \sqrt{E_{\text{sig}}^2 - p_{\text{sig}}^2}$$

$$\Delta E = E_{\text{sig}}^{\text{CM}} - E_{\text{beam}}^{\text{CM}}$$

Blind analysis:

Blind signal region in the $M_{\text{inv}}-\Delta E$ plain

number of BG is estimated
using sideband data

	Belle		BaBar		CLEO	
	B, 10^{-8}	$\int_{\text{Ldt}} \text{fb}^{-1}$	B, 10^{-8}	$\int_{\text{Ldt}} \text{fb}^{-1}$	B, 10^{-8}	$\int_{\text{Ldt}} \text{fb}^{-1}$
$\mu^-\gamma$	4.5	535	6.8	232	110	13.8
$e^-\gamma$	12	535	11	232	270	4.68
$e^-e^-e^+$	3.6	535	4.9	376	290	4.79
$e^-\mu^-\mu^+$	4.3	535	6.6	376	180	4.79
$e^+\mu^-\mu^-$	2.4	535	4.6	376	150	4.79
$\mu^-e^-e^+$	2.8	535	5.0	376	170	4.79
$\mu^-\mu^-\mu^+$	3.4	535	6.7	376	190	4.79
$\mu^+e^-e^-$	2.1	535	2.7	376	150	4.79
$e^-\pi^0$	8.0	401	13	339	370	4.68
$e^-\eta$	9.2	401	16	339	820	4.68
$e^-\eta'$	16	401	24	339	-	-
$\mu^-\pi^0$	12	401	11	339	400	4.68
$\mu^-\eta$	6.5	401	15	339	960	4.68
$\mu^-\eta'$	13	401	14	339	-	-