

# Dark Matter and the invisible Universe

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<https://www.durhamcathedral.co.uk>



**PhD Paris ENS (France)**  
**Oxford University (UK)**  
**CERN Geneva (Switzerland)**  
**CNRS Staff (France)**  
**Durham Uni (UK)**  
**[Head of School, Sydney]**



# Questions AP physicists focus on

- What are our origins?
- What is the Universe made of?
- What is our future?

**Cosmology**

**Astronomy  
Astrophysics**

**Particle Physics**

*Astro Particle Physics*

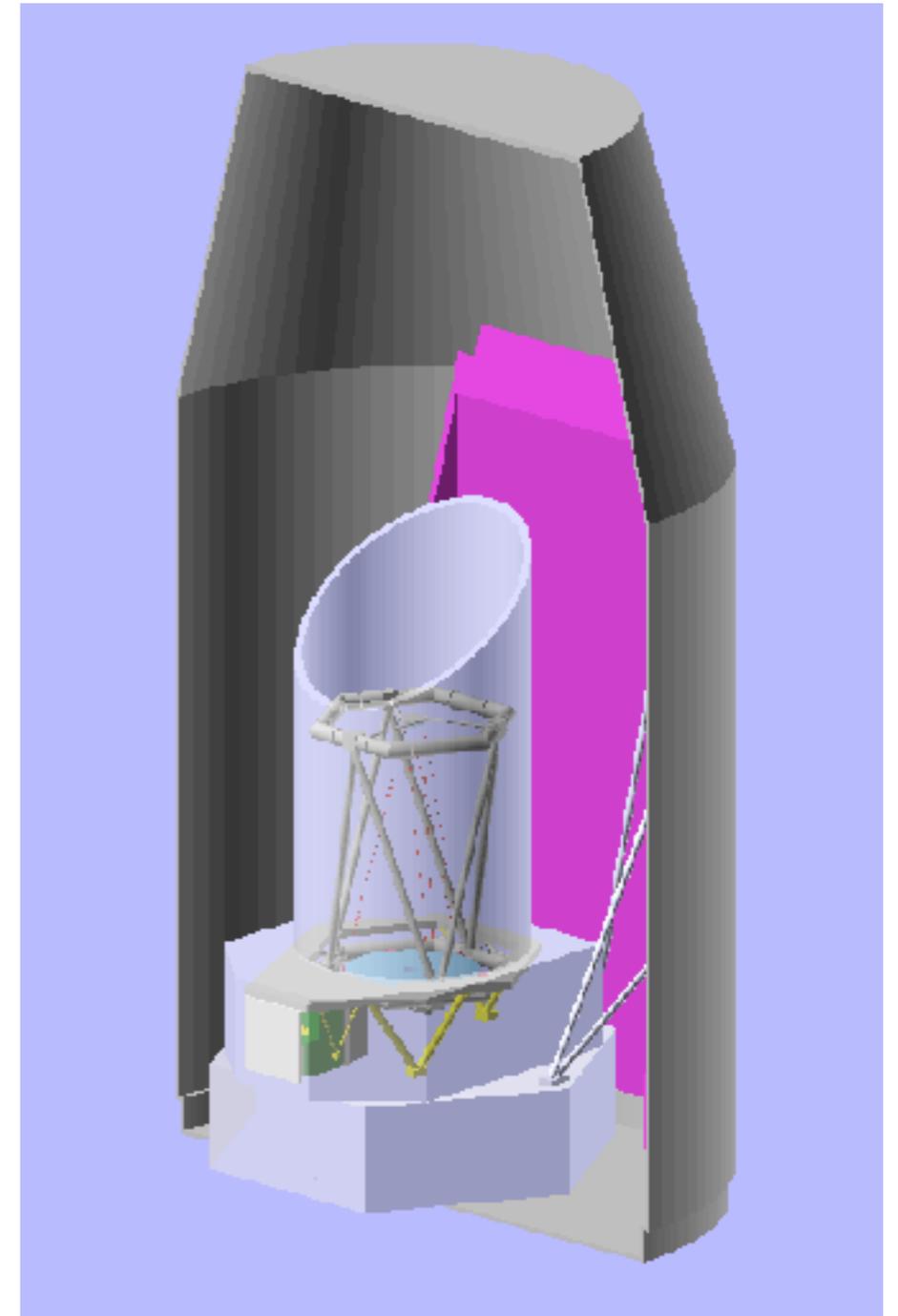
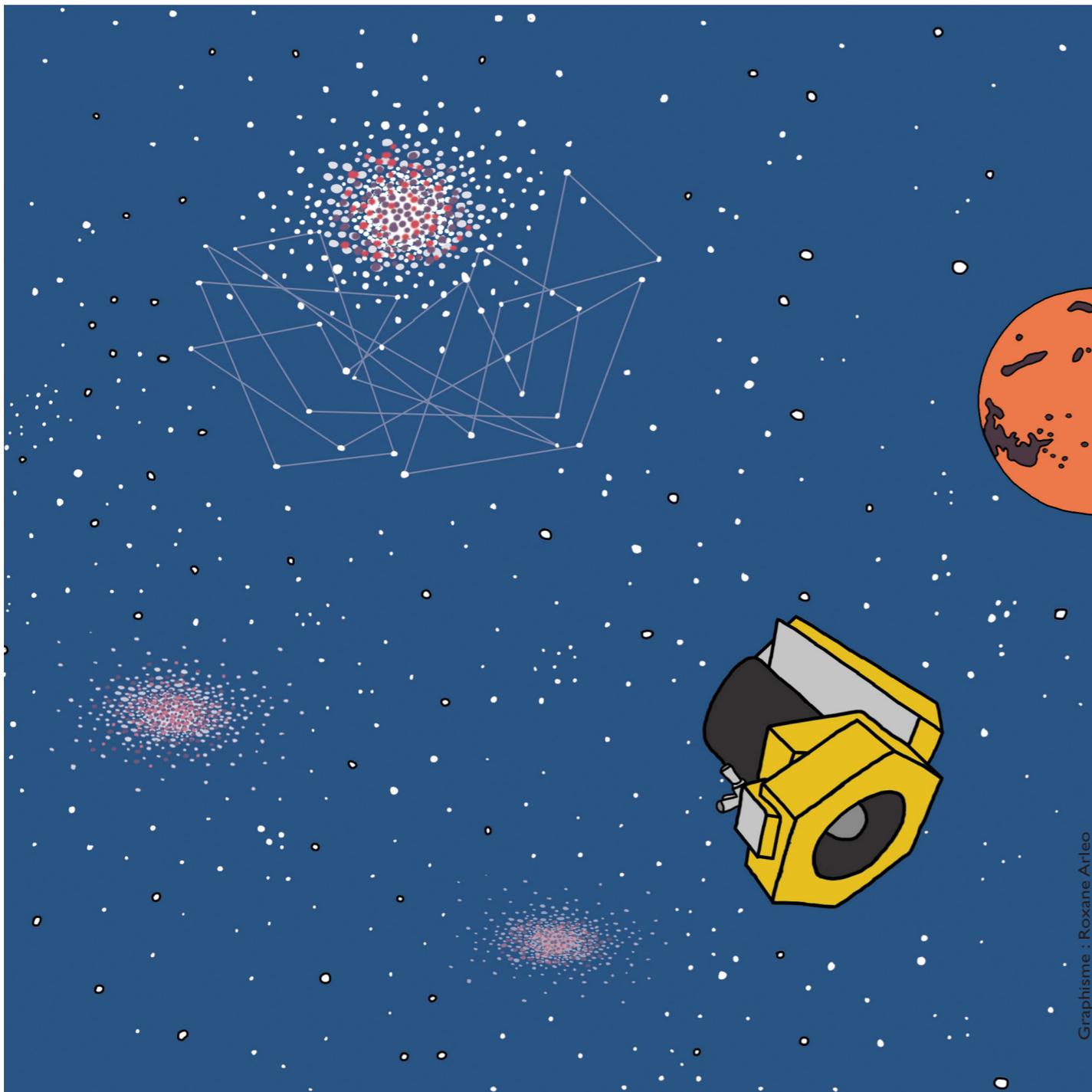
*Trying to determine the constituents of the Universe (95% unknown!)*



# THEIA

Microarcsecond Astrometric Observatory

*Proposed to ESA in 2017  
22 countries, +200 participants*



## **Faint objects in motion : the new astrometry frontier**

Proposal for a medium size mission opportunity in ESA's science programme (M5) mission

# Lectures organisation

**I. Introduction**

**II. Candidates**

**III. Signatures**



**V. Cosmology**

**VI. New research avenues**

**Please don't hesitate to interrupt me**

# I. Introduction

## Evidence for Dark Matter

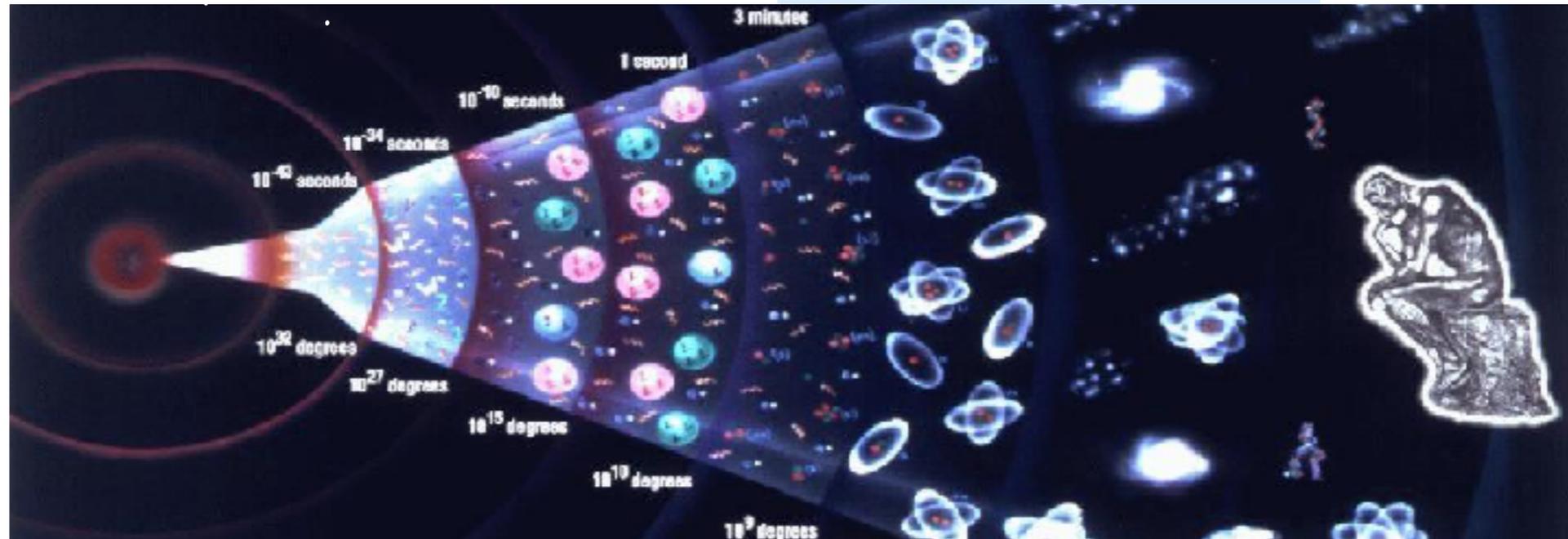
- \* **Current picture**
- \* **Rotation curves**
- \* **Gravitational lensing**
- \* **Early Universe and Large-Scale-Structures**

# Current picture

Radiation

Matter

Energy



**Particle  
Standard Model**

**Cosmology  
Astrophysics**

**dark matter** essential for galaxy formation

**dark energy** essential for accelerated expansion

# Brief history

1920s—30s — Evidence of missing mass in clusters of galaxies

1966—67 — Progress on primordial fluctuations

1970s — Discovery of flat galaxy rotation curves

*1977— 1982 — Neutrinos are (not) the dark matter; Birth of the WIMP concept*

1982—1984 — Birth of the cosmology of the Cold Dark Matter (CDM) scenario

*1985—1988 — DM particles can be detected in a lab and in the sky*

1992—2003 — DM only makes up 25% of the energy content of the Universe

**A lot of progress since then but no major discovery**

# Brief history

*(more people contributed!)*

**J. Oort, 1932** Doppler redshift values of stars moving near the galactic plane;  
The Galaxy needs to be twice as massive to prevent stars to escaping

**F. Zwicky 1933**

**more mass in the Coma Cluster than is visible**

1937 ApJ 86, 217

ON THE MASSES OF NEBULAE AND OF CLUSTERS OF NEBULAE

F. ZWICKY

The Coma cluster contains about one thousand nebulae. The average mass of one of these nebulae is therefore

$$\bar{M} > 9 \times 10^{43} \text{ gr} = 4.5 \times 10^{10} M_{\odot}. \tag{36}$$

Inasmuch as we have introduced at every step of our argument inequalities which tend to depress the final value of the mass  $\mathcal{M}$ , the foregoing value (36) should be considered as the lowest estimate for the average mass of nebulae in the Coma cluster. This result is somewhat unexpected, in view of the fact that the luminosity of an average nebula is equal to that of about  $8.5 \times 10^7$  suns. According to (36), the conversion factor  $\gamma$  from luminosity to mass for nebulae in the Coma cluster would be of the order

**Mass/Light =  $\gamma = 500$ ,** (37)

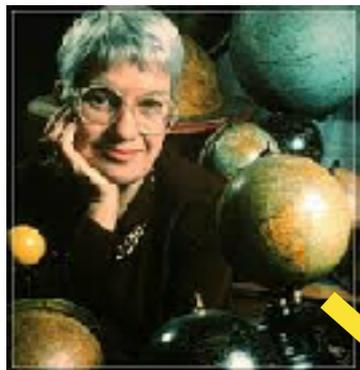
as compared with about  $\gamma' = 3$  for the local Kapteyn stellar system.

based on 21 radial velocities of galaxies in the Coma cluster

# I. Introduction

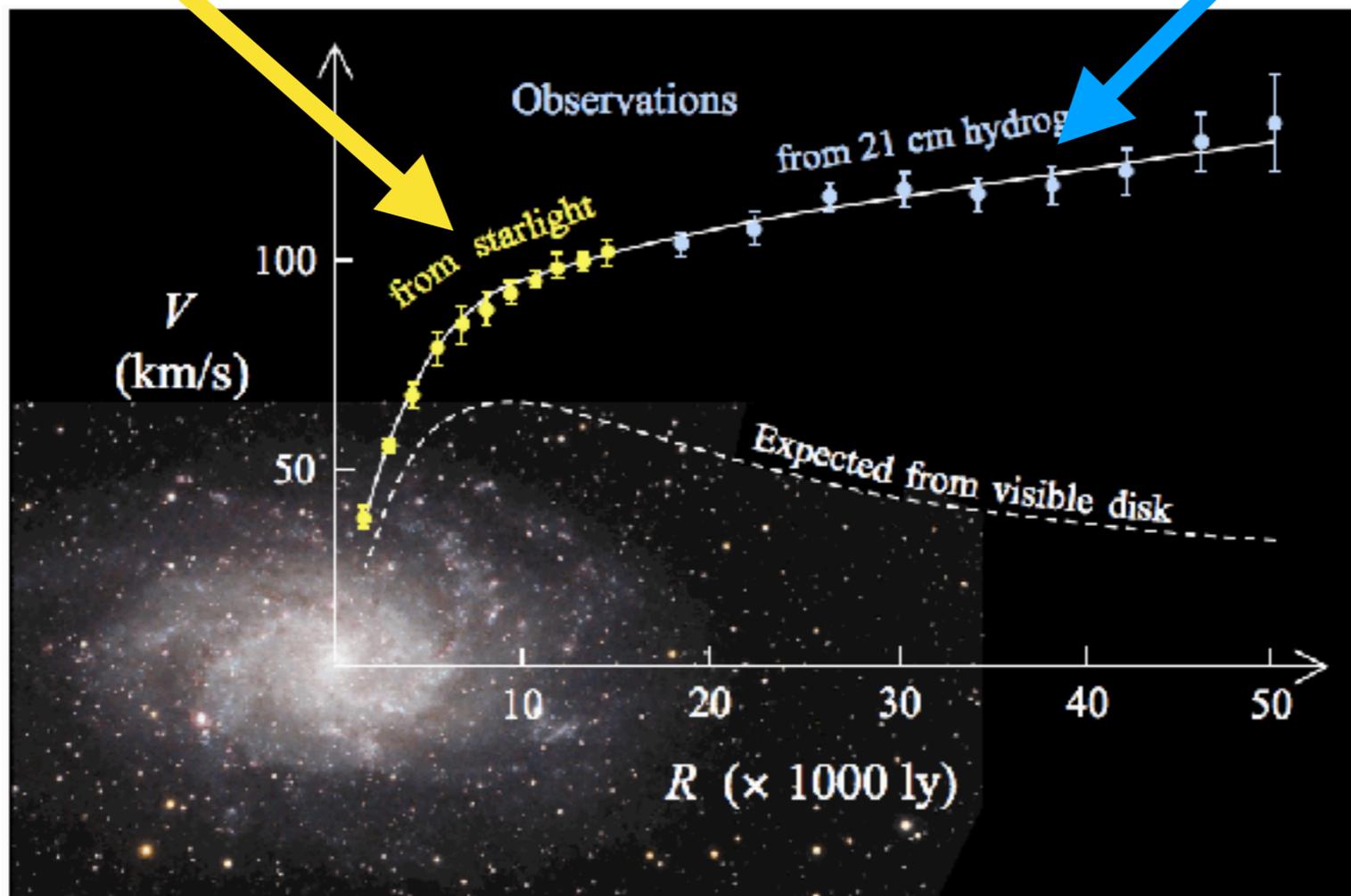
# Rotation curves *(many people contributed!)*

The rotation of galaxies was discovered in 1914 — Slipher (1914)



Freeman (1970) for M33 and NGC 300:  
rotation curve peaks at the edge of the optical disk  
so  $\sim 1/3$  of the mass outside the optical radius.

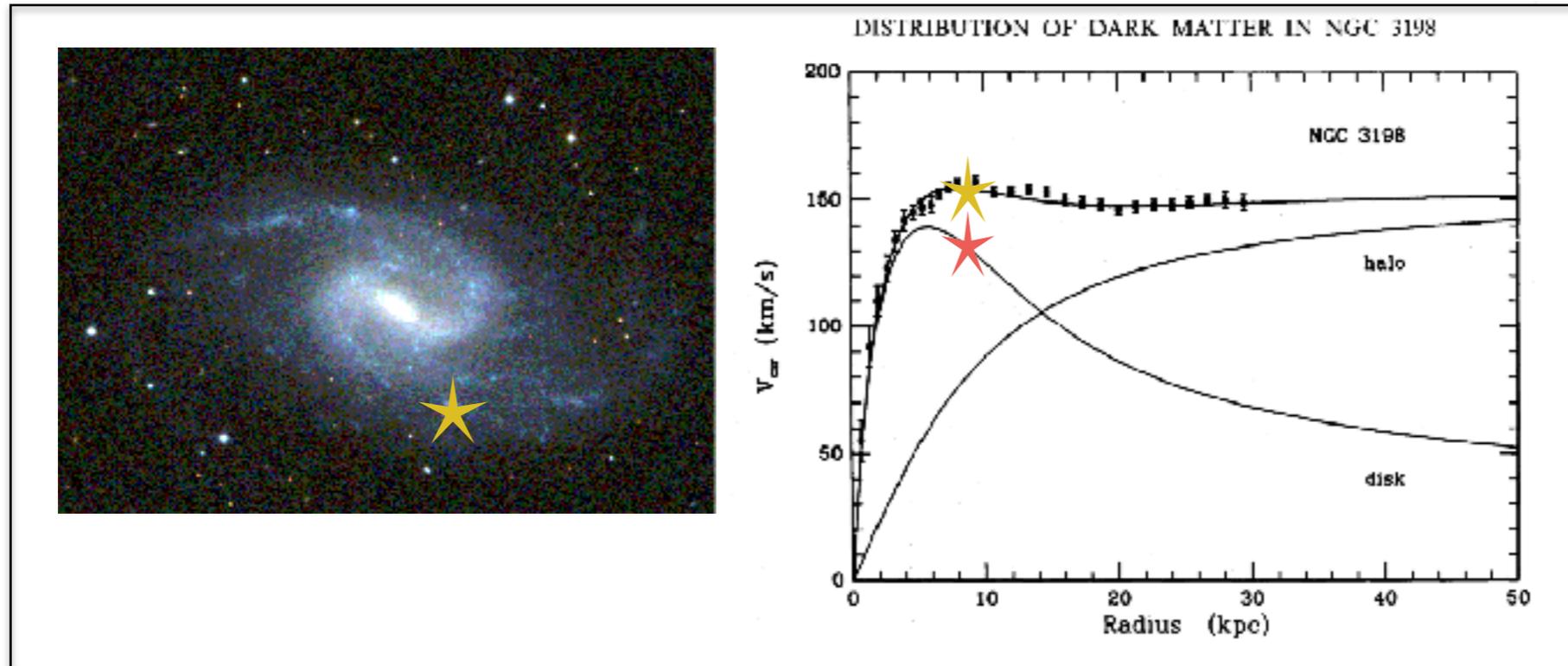
[Shostak & Rogstad \(1973\)](#),  
[Seielstad & Wright \(1973\)](#).  
M31: ([Roberts 1975a](#),  
[Roberts & Whitehurst 1975](#));  
Final straw: [Bosma \(1978\)](#)



1970ApJ...159..379R

# Key discovery

## Rotation curves of galaxies

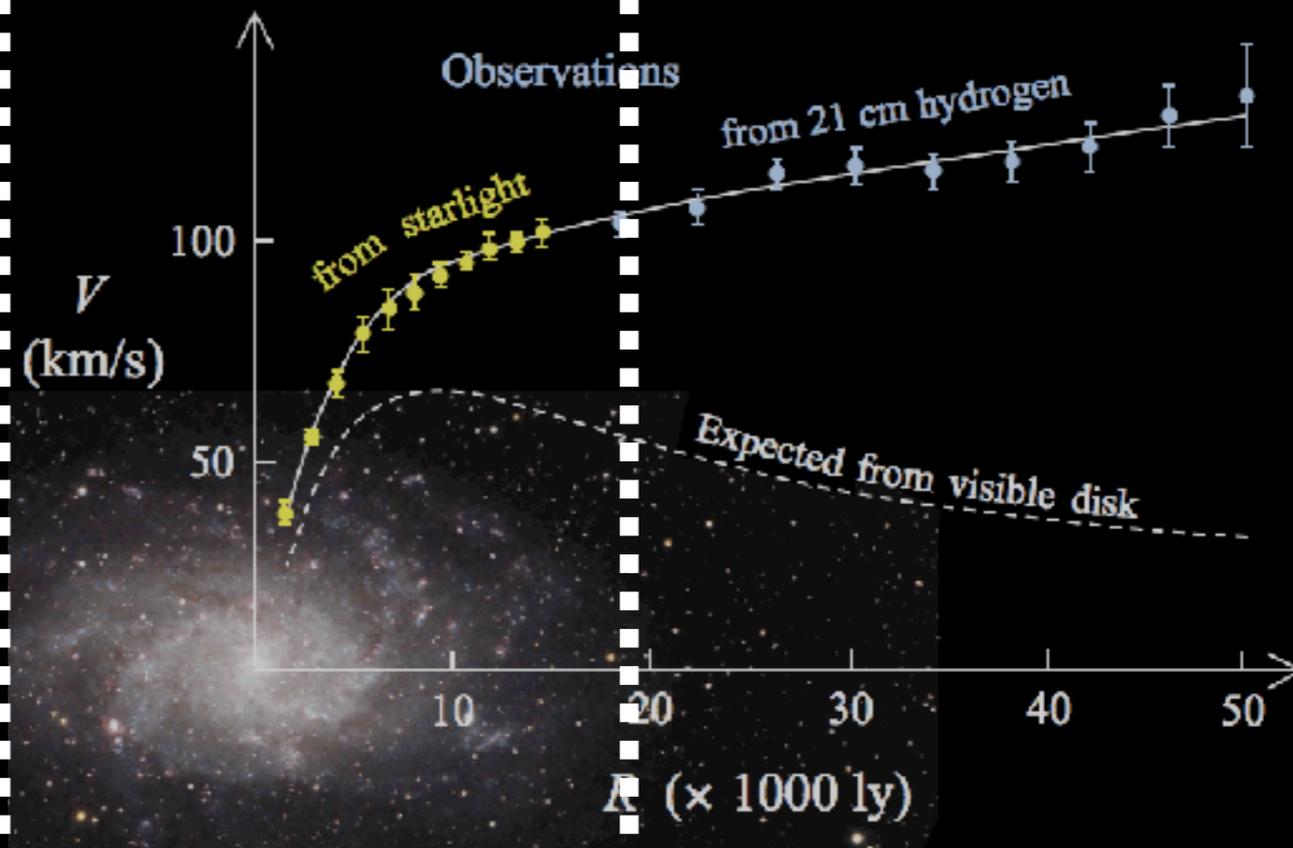


We need DM to explain the flat rotation curves **far from the GC**

$$v_c^2 = \frac{G M(r)}{r} \quad M(r) = \int 4\pi^2 \rho(r) dr^3$$



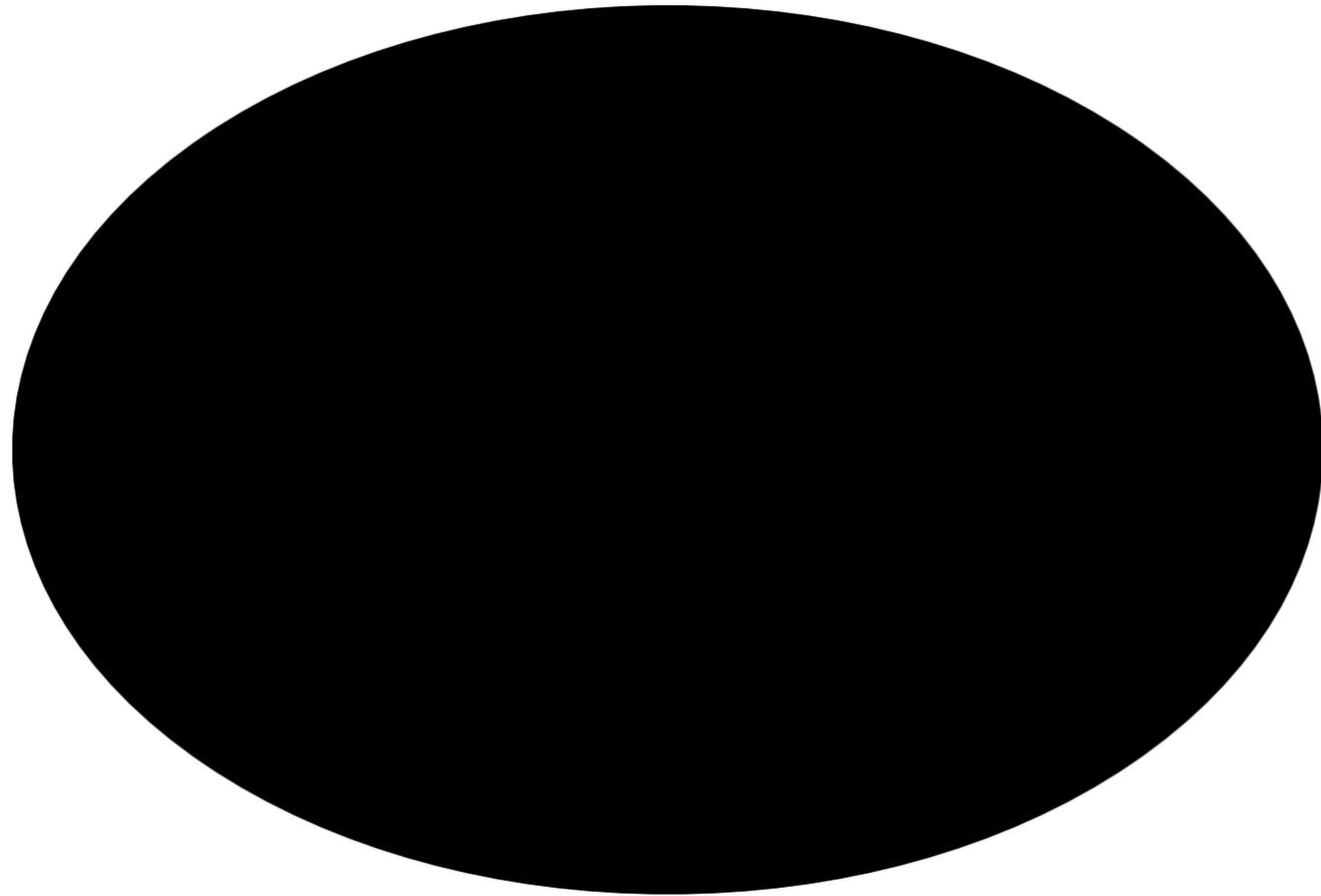
But the highest mass density would be in the inner part of the galaxy...



$\longleftrightarrow$   
**visible galaxy < 20 kpc**  
**we are located 10 kpc from the centre**

**Complexed structure ; much more extended**

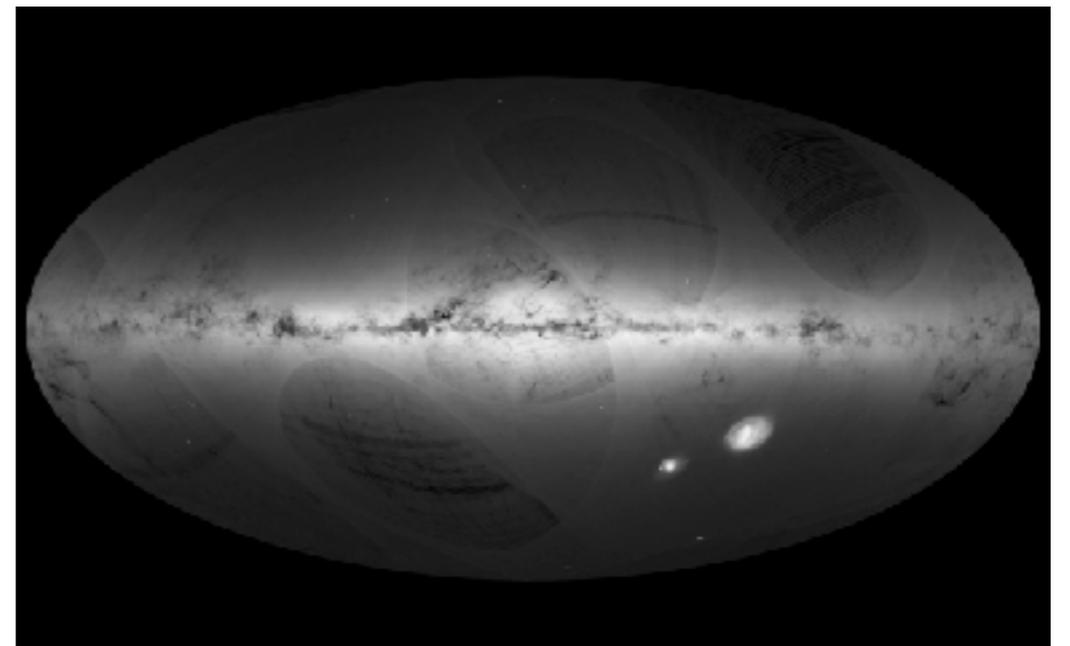
# The Milky Way



A “dark matter” halo

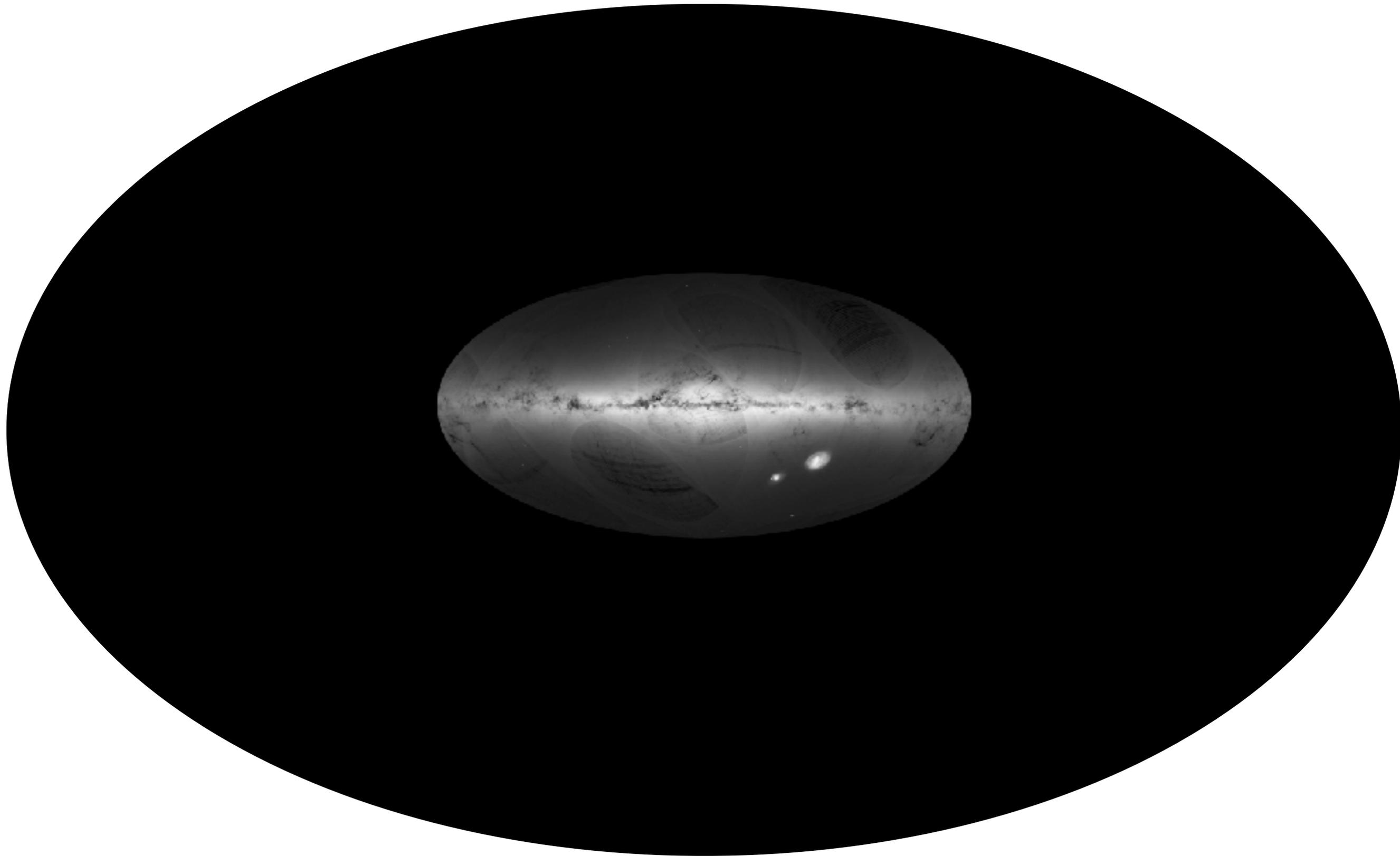


**A visible disc made of stars**



**MW seen by ESA/Gaia**

# The Milky Way



# Dark Matter is everywhere

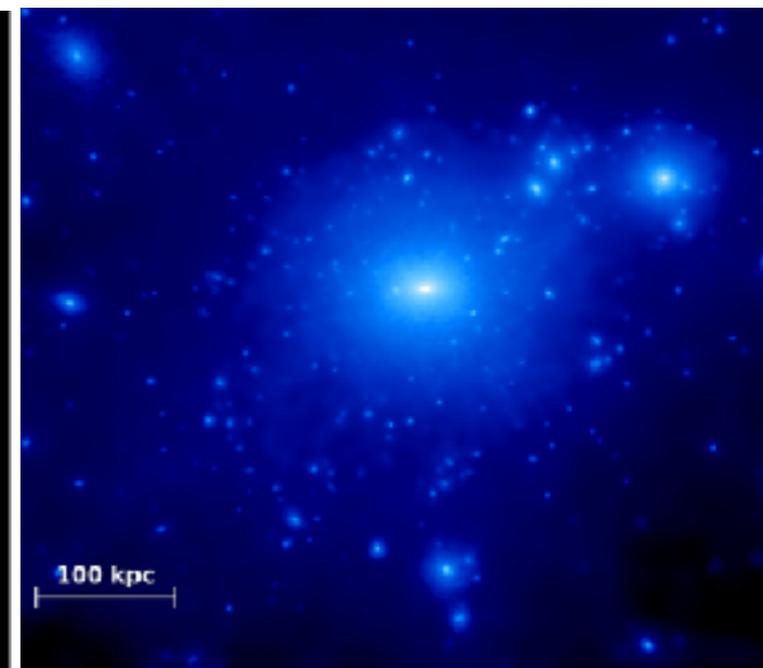
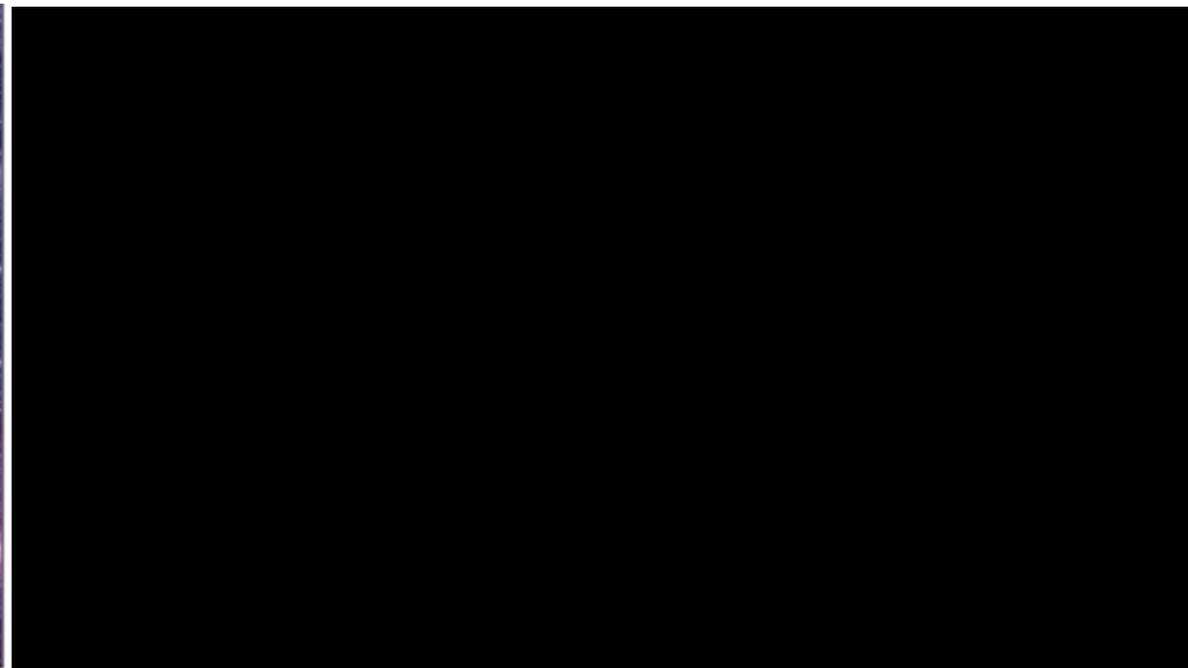
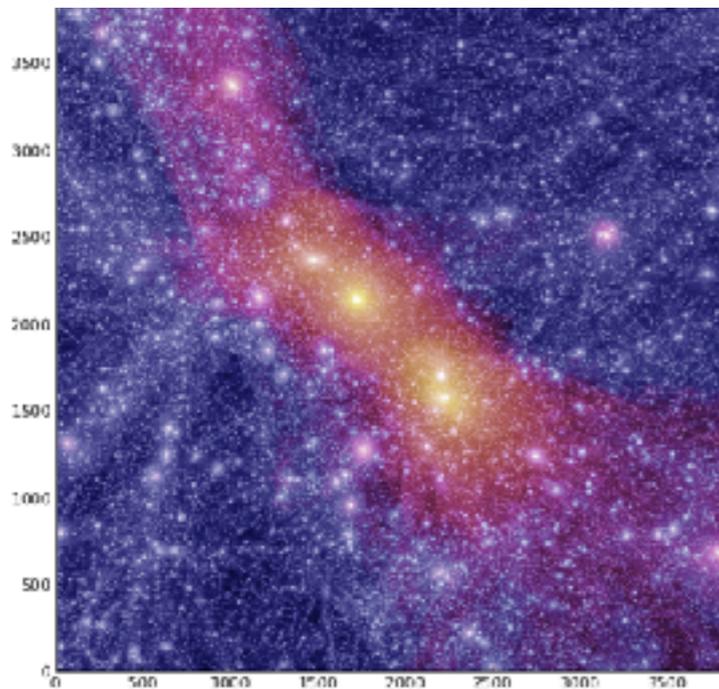
Cluster of galaxies



NGC 6814 Credit: NASA



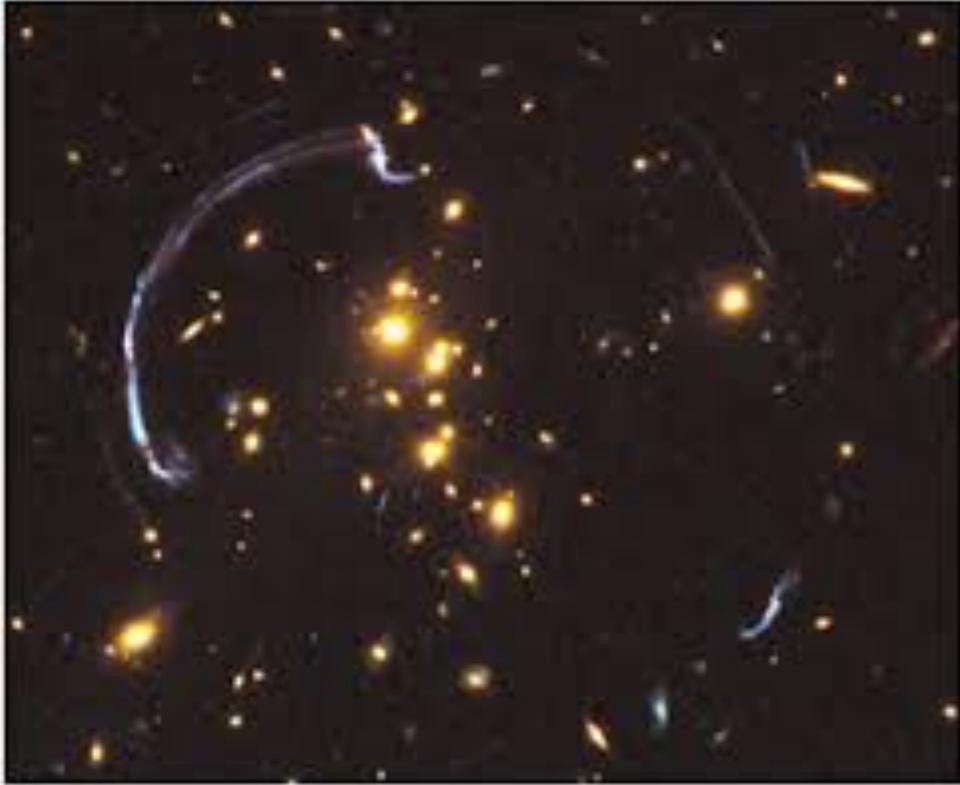
NGC 4621 Credit: WikiSky/SDSS



**But what is the DM?**

## I. Introduction

# Gravitational lensing evidence...

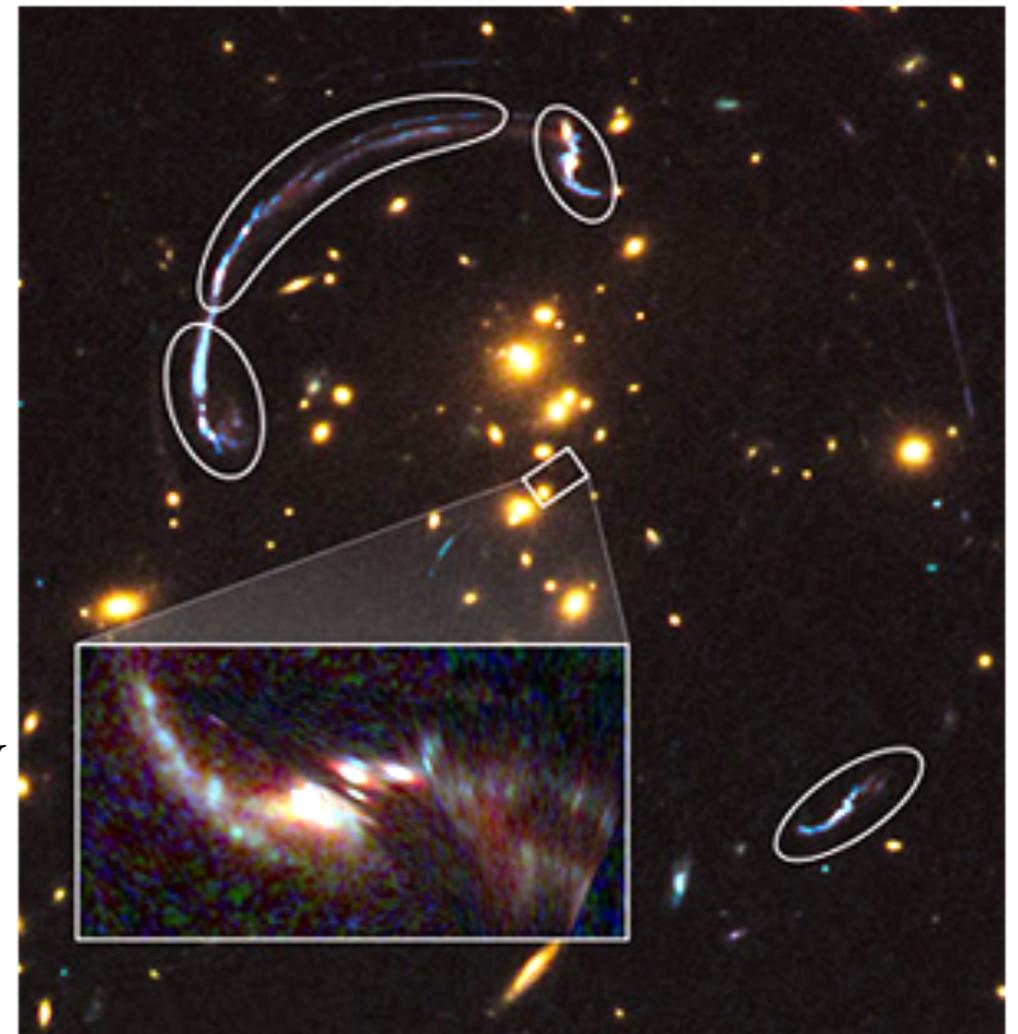


*Illustration Credit: NASA, ESA, and Z. Levay (STScI)  
Science Credit: NASA, ESA, J. Rigby  
(NASA Goddard Space Flight Center),  
K. Sharon (Kavli Institute for Cosmological Physics,  
University of Chicago), and M. Gladders & E. Wuyts  
(University of Chicago)*

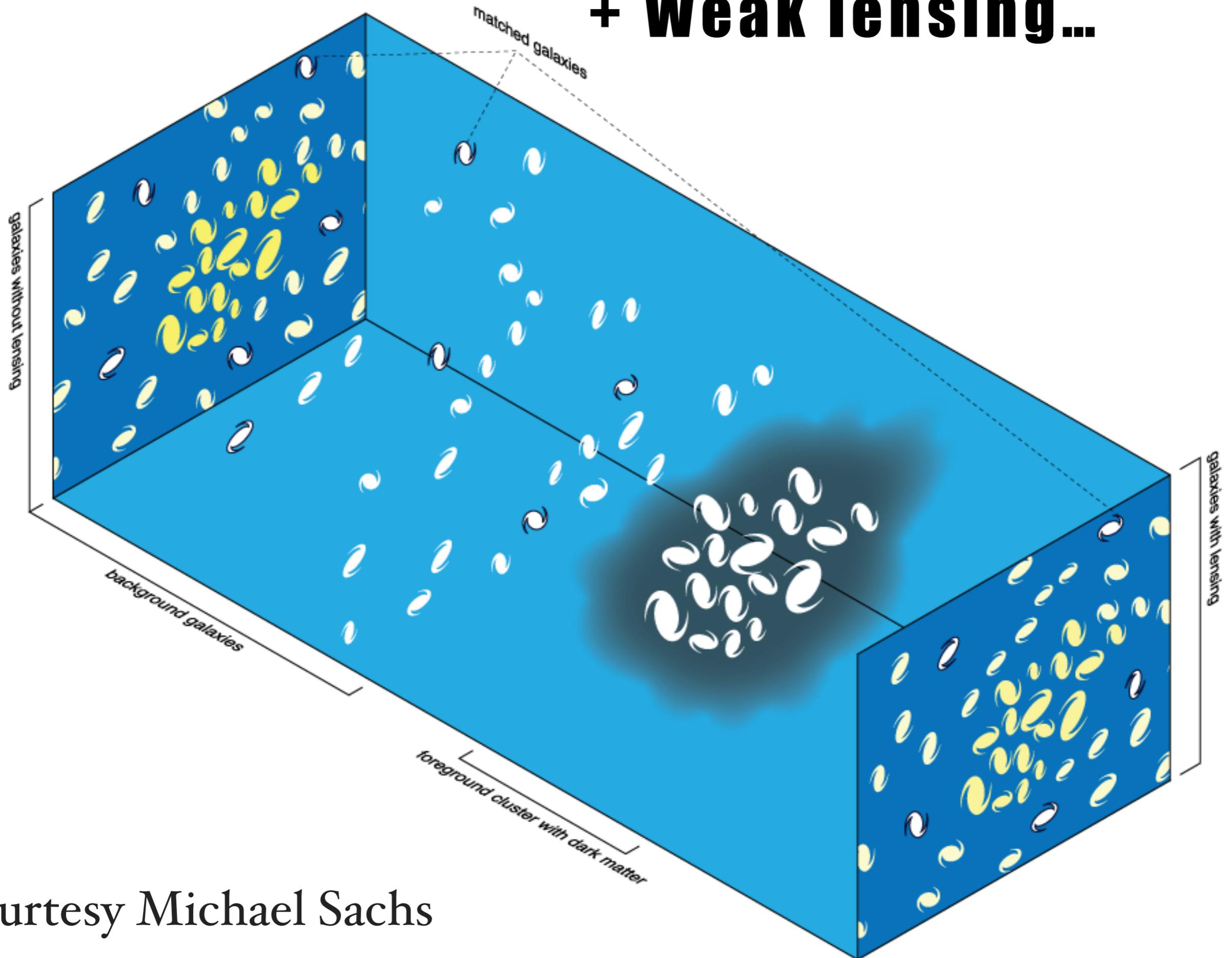
Reconstruction (lower left) of the brightest galaxy whose image has been distorted by the gravity of a distant galaxy cluster.

The small rectangle in the center shows the location of the background galaxy on the sky if the intervening galaxy cluster were not there. The rounded outlines show distinct, distorted images of the background galaxy resulting from lensing by the mass in the cluster.

The image at lower left is a reconstruction of what the lensed galaxy would look like in the absence of the cluster, based on a model of the cluster's mass distribution derived from studying the distorted galaxy images.

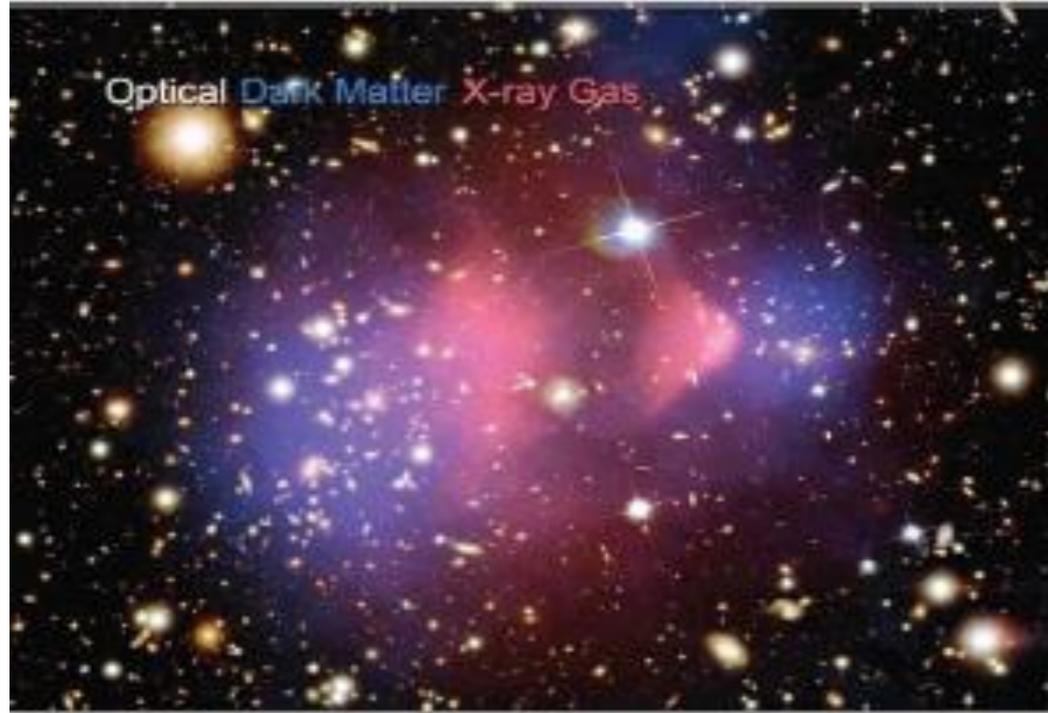


# + Weak lensing...

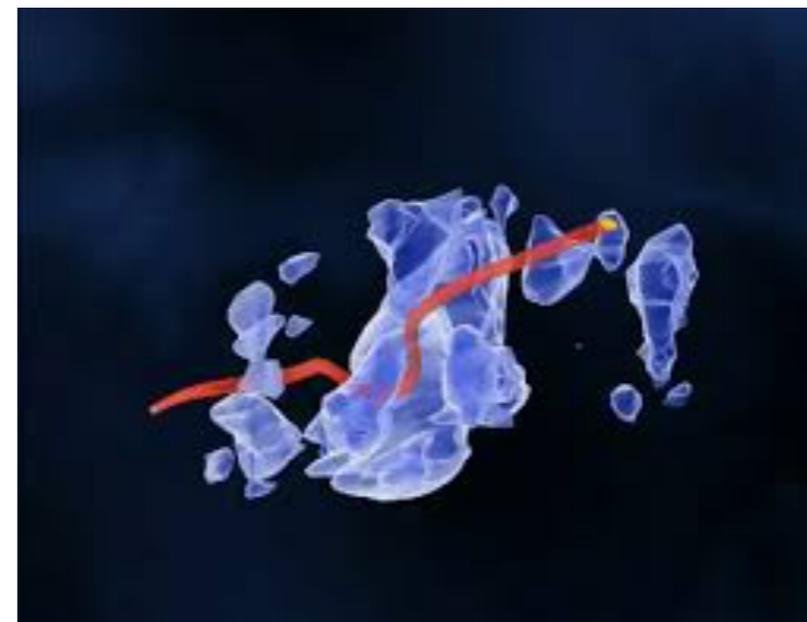
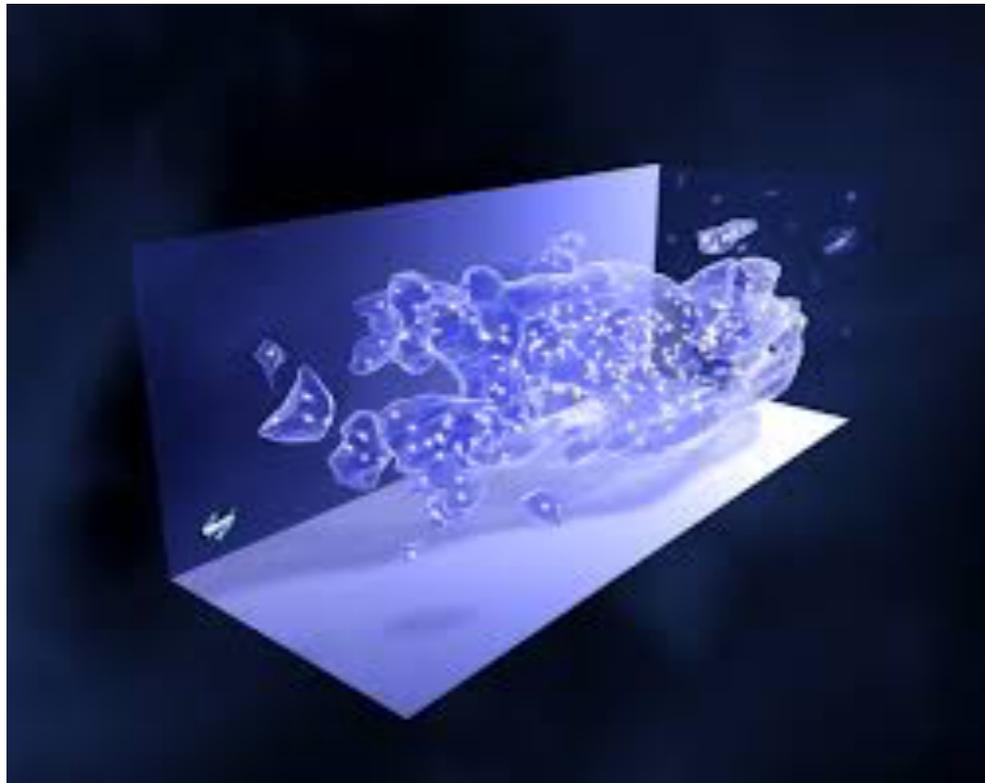


Courtesy Michael Sachs

# More lensing evidence...



X-ray emitted by gas  
(Thomson interactions, Bremsstrahlung,...)  
But the gravitational potential is dominant  
in the blue region where no light is emitted



# The cosmological evidence

## J. Peebles



- [Find Similar Abstracts](#) (with [default settings below](#))
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  - [Refereed Citations to the Article](#)
  - [Also-Read Articles](#) (Reads History)
  - [Translate This Page](#)
- Title:** The Gravitational Instability of the Universe  
**Authors:** [Peebles, P. J. E.](#)  
**Publication:** Astrophysical Journal, vol. 147, p.859 ([ApJ Homepage](#))  
**Publication Date:** 03/1967  
**Origin:** [ADS](#)  
**DOI:** [10.1086/149077](#)  
**Bibliographic Code:** [1967ApJ...147..859P](#)

### Abstract

It is argued that the expanding universe is unstable against the growth of gravitational perturbations. The argument is directed toward two problems, the physical conditions in the early, highly contracted phase of the expanding universe, and the formation of the galaxies.

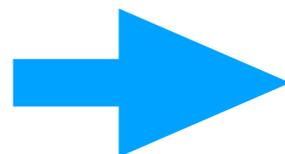
Followed Peebles, P. J. E., *Astrophys. J.*, **142**, 1317 (1965)

<http://adsabs.harvard.edu/abs/1970ApJ...162..815P>

Primordial fluctuations in the Early Universe grow under gravity (Peebles, 66)

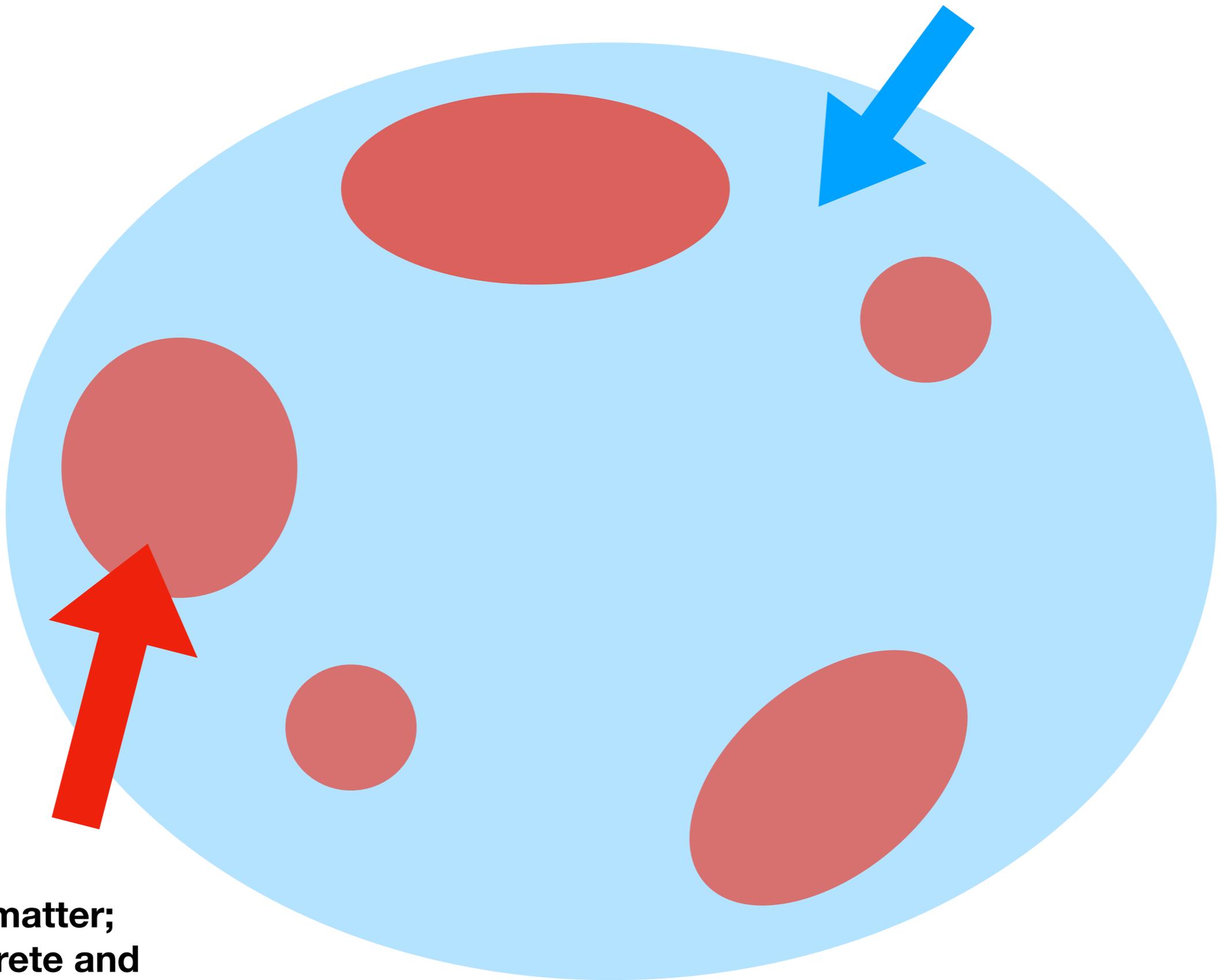
$$I(x) \propto \frac{x^3}{e^x - 1}$$

$$x = \frac{h\nu}{\kappa T}$$



$$\frac{\Delta T}{T} \simeq 10^{-5}$$

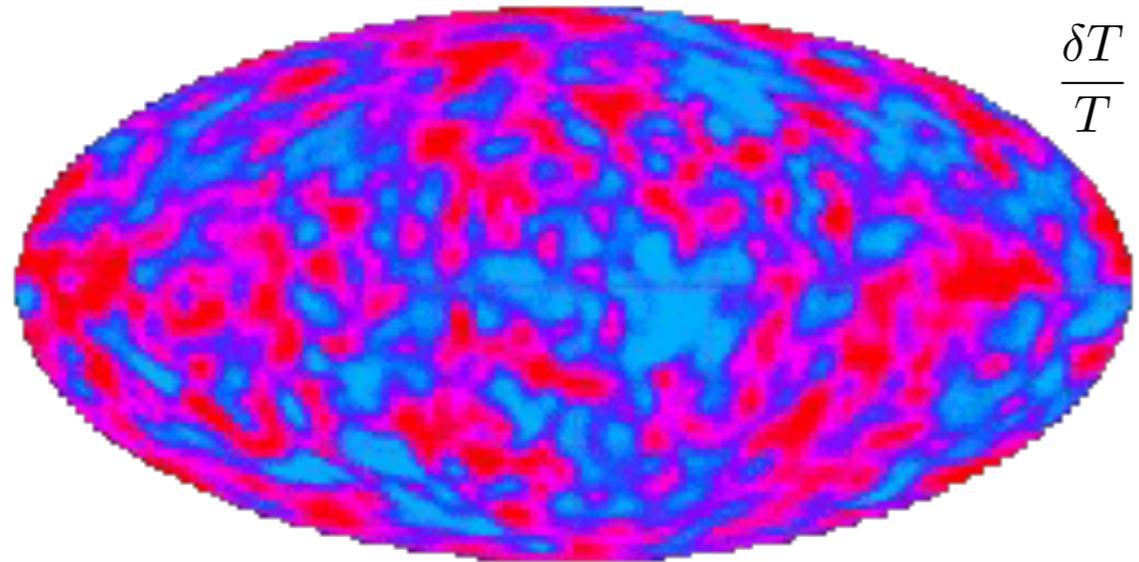
**less matter;  
will become even emptier with gravity**



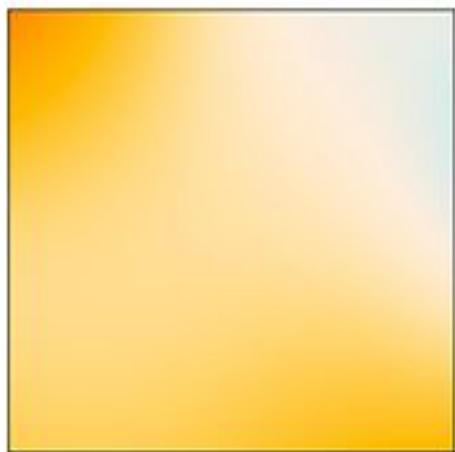
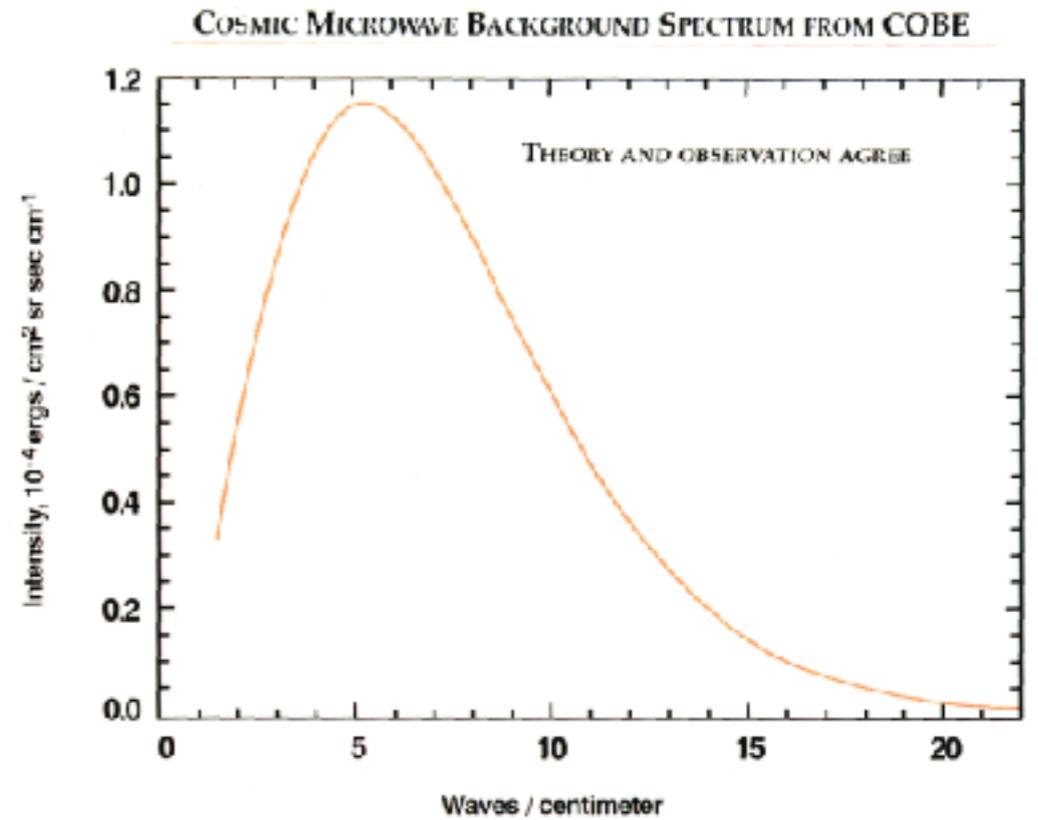
**more matter;  
will accrete and  
clump under gravity**

# The cosmological evidence

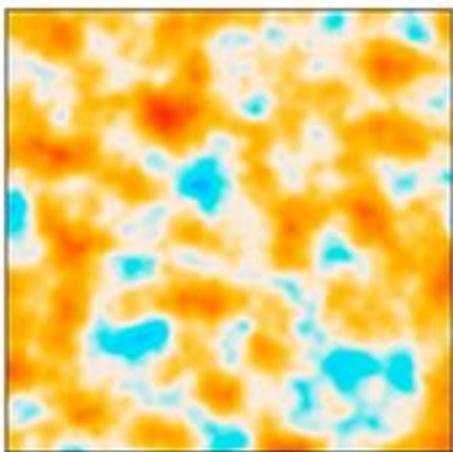
## Was Peebles right?



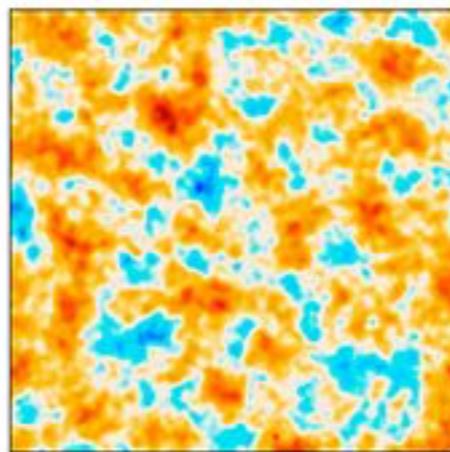
$$\frac{\delta T}{T} \approx 10^{-5}$$



COBE



WMAP



Planck

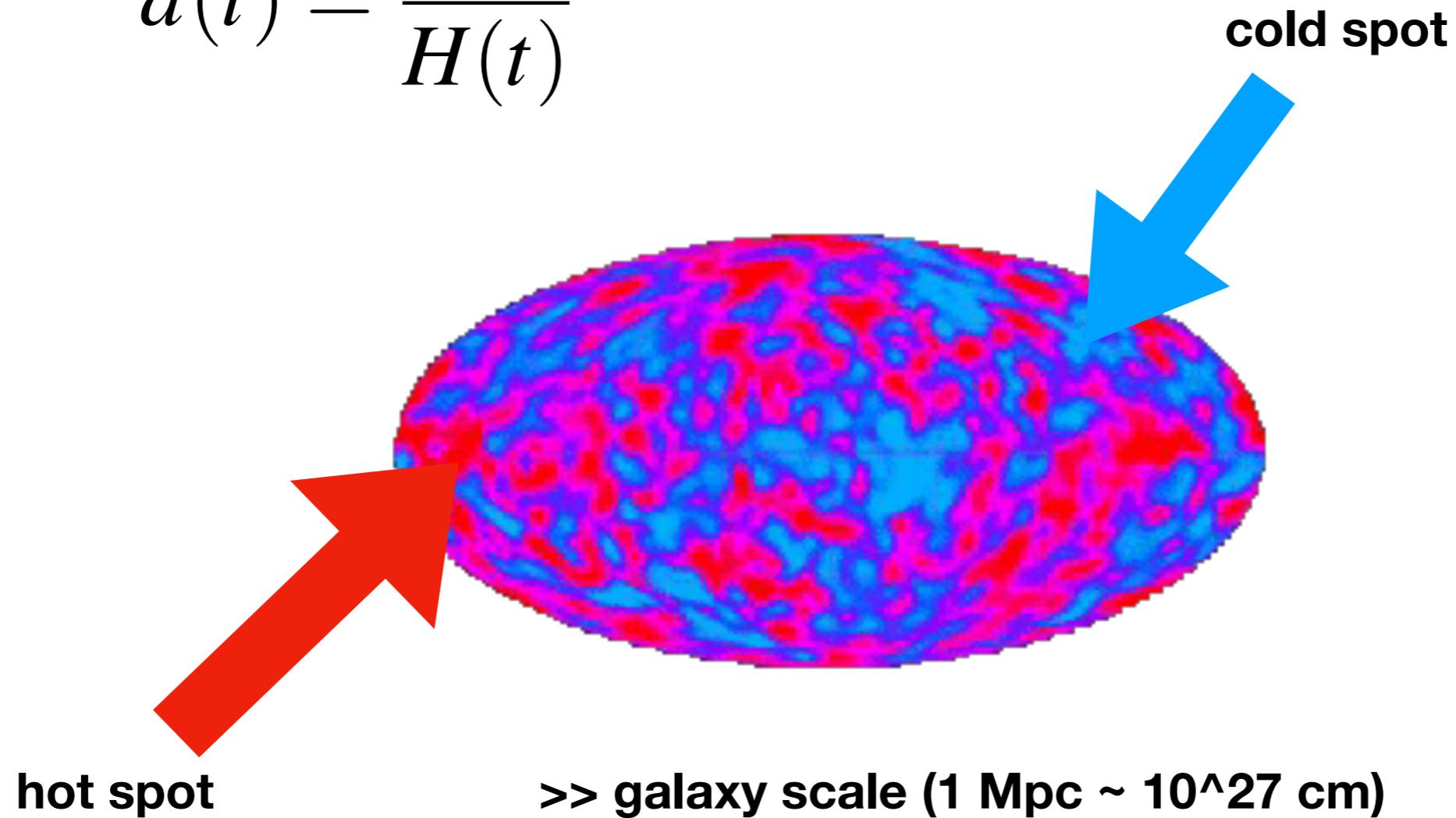
**YES!**

**so either Silk wrong or  
more matter than baryons**

courtesy wikipedia!

# The cosmological evidence

$$d(t) = \frac{c}{H(t)}$$

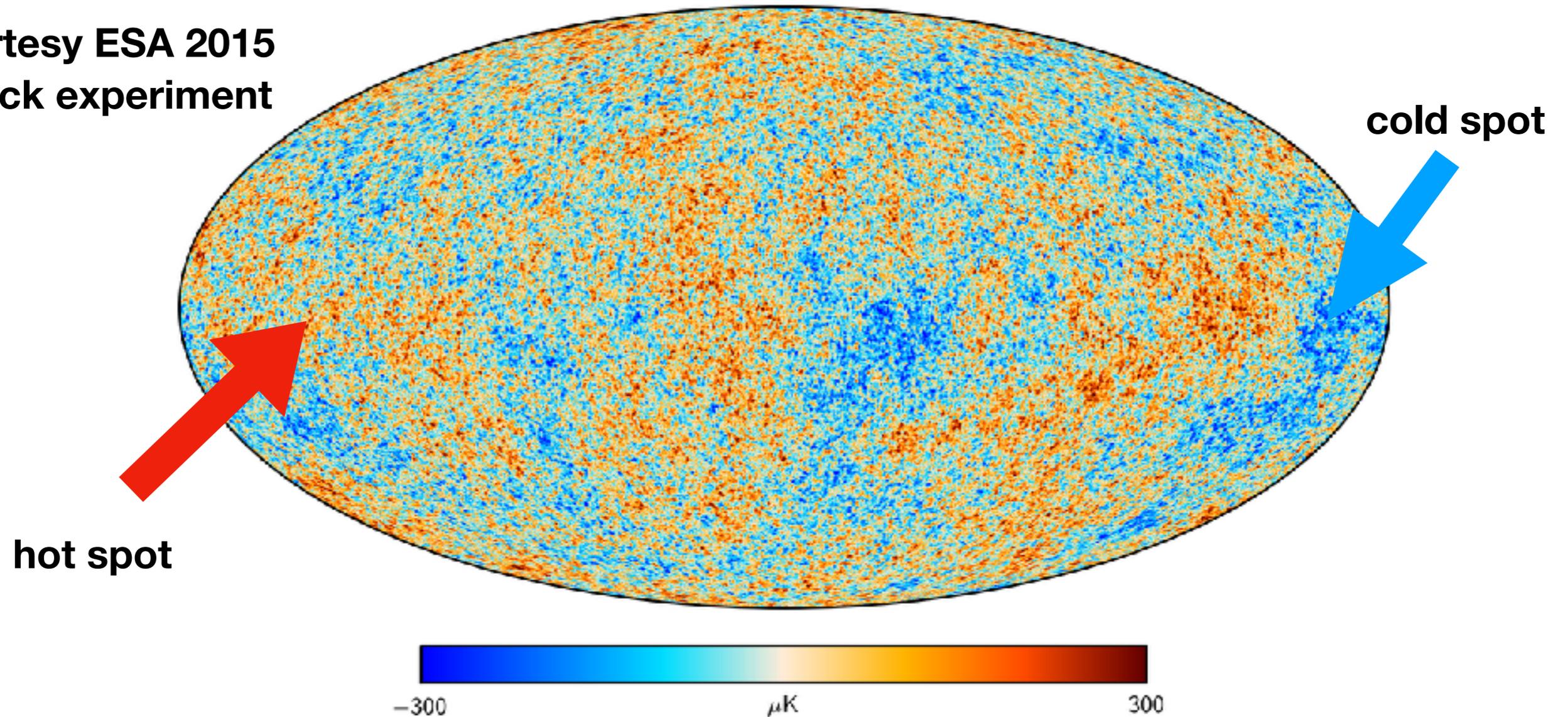


All regions of the sky have a temperature around 2.7k!  
How come?

$$\frac{\delta T}{T} \approx 10^{-5}$$

# The cosmological evidence

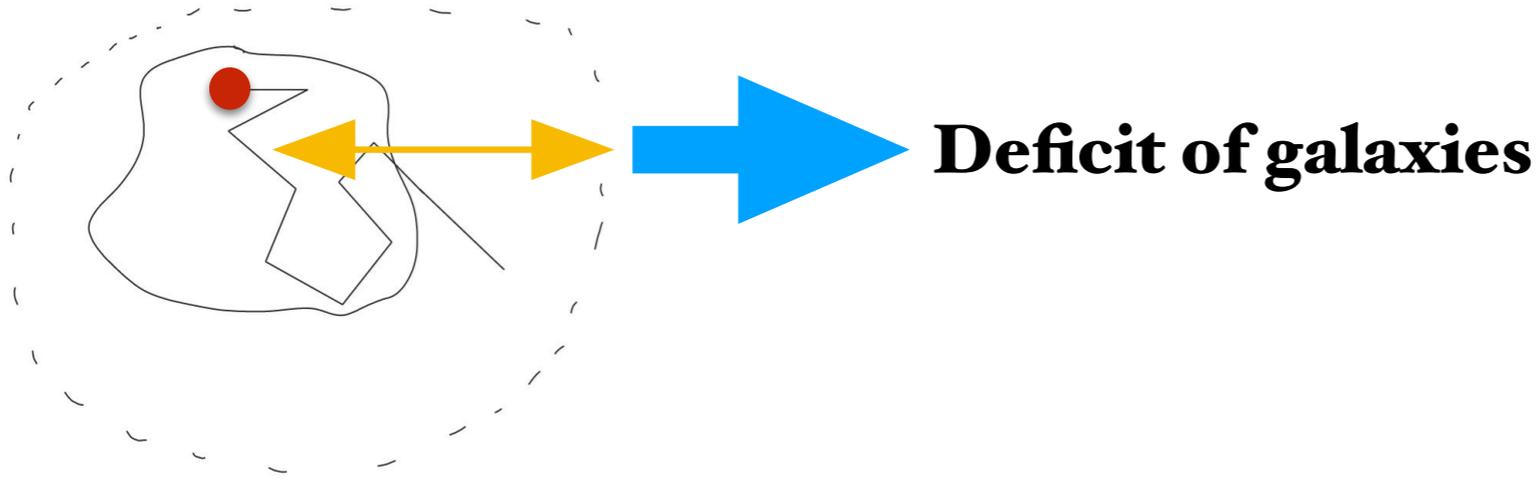
Courtesy ESA 2015  
Planck experiment



>> galaxy scale (1 Mpc  $\sim 10^{27}$  cm)

All regions of the sky have a temperature around  $2.7\text{k} + \frac{\delta T}{T} \simeq 10^{-5}$

How come such a tiny difference on such gigantic scales?



**baryonic** fluctuations do not survive the baryon scattering off the photon background.  
(Question first asked by Misner for neutrinos)

letters to nature

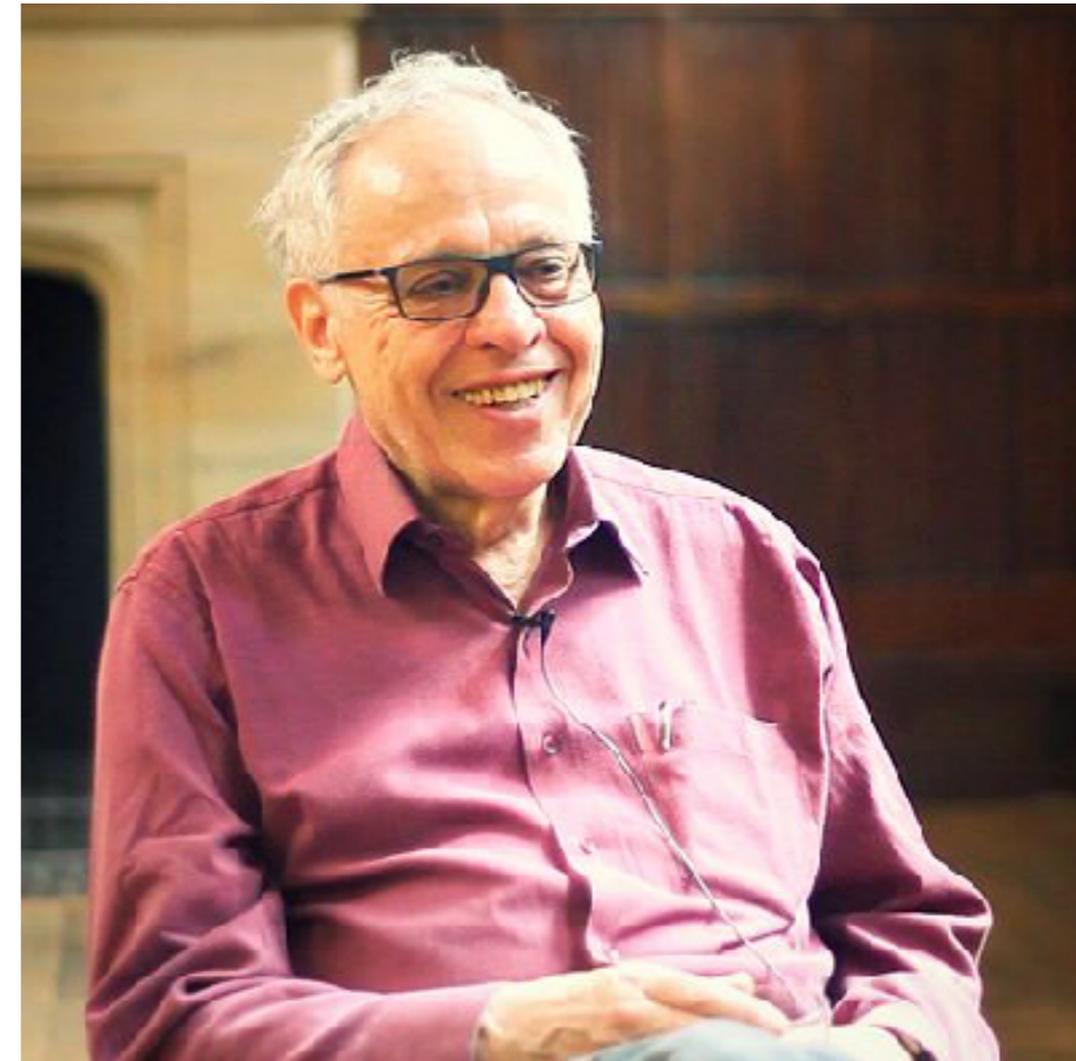
*Nature* 215, 1155 - 1156 (09 September 1967); doi:10.1038/2151155a0

## Fluctuations in the Primordial Fireball

JOSEPH SILK

Harvard College Observatory, Cambridge, Massachusetts.

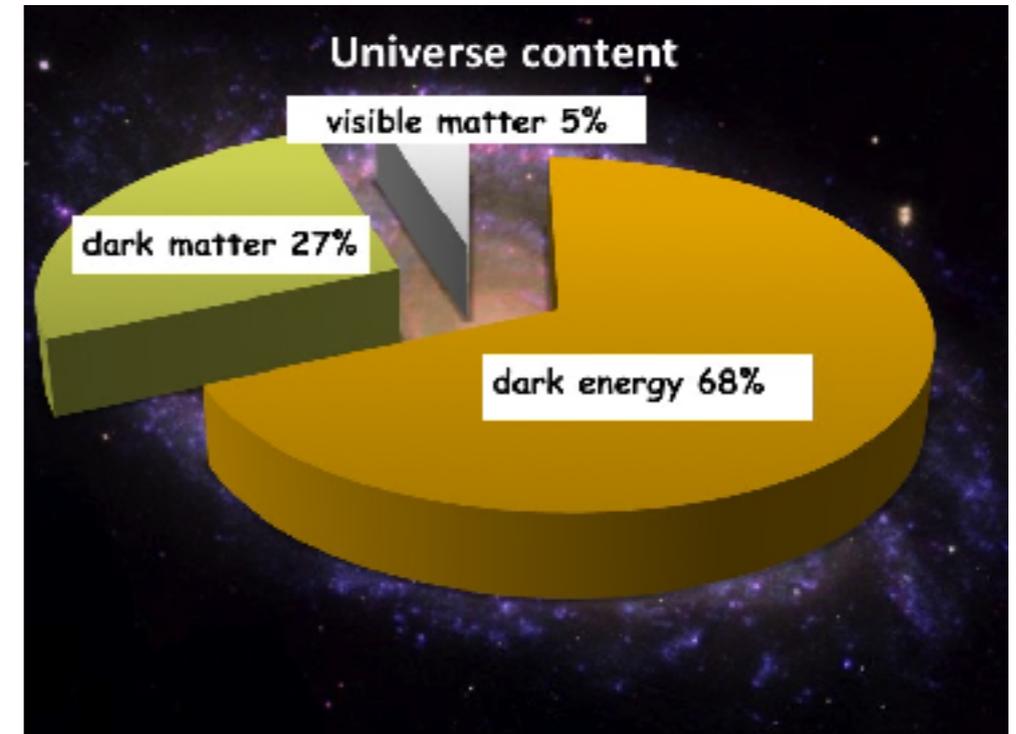
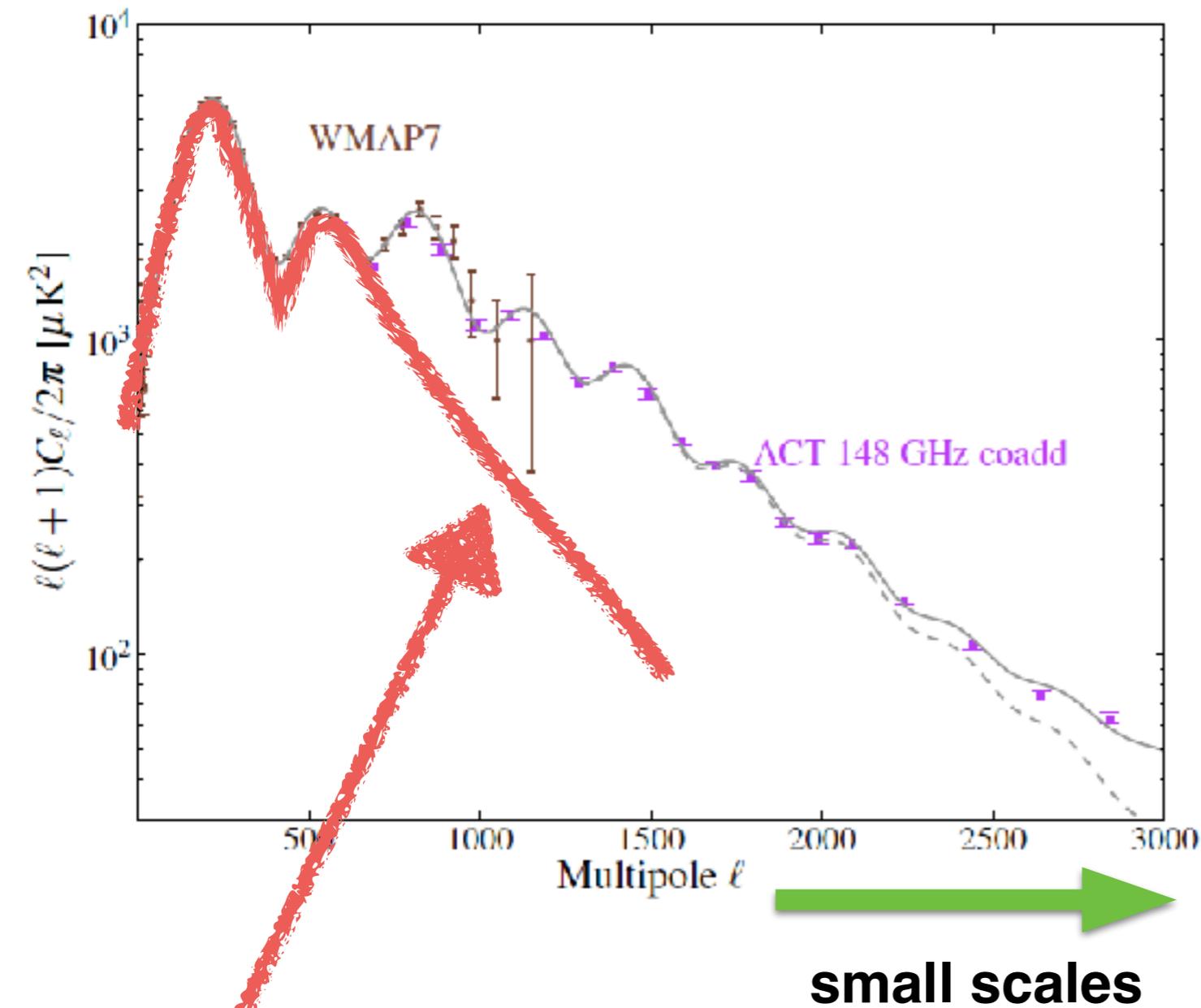
ONE of the overwhelming difficulties of realistic cosmological models is the inadequacy of Einstein's gravitational theory to explain the process of galaxy formation<sup>1-6</sup>. A means of evading this problem has been to postulate an initial spectrum of primordial fluctuations<sup>7</sup>. The interpretation of the recently discovered 3° K microwave background as being of cosmological origin<sup>8,9</sup> implies that fluctuations may not condense out of the expanding universe until an epoch when matter and radiation have decoupled<sup>4</sup>, at a temperature  $T_D$  of the order of 4,000° K. The question may then be posed: would fluctuations in the primordial fireball survive to an epoch when galaxy formation is possible ?



J. Silk

**Was Silk right?**

# The CMB evidence



the red curve = baryons only  
grey curve = baryons + DM

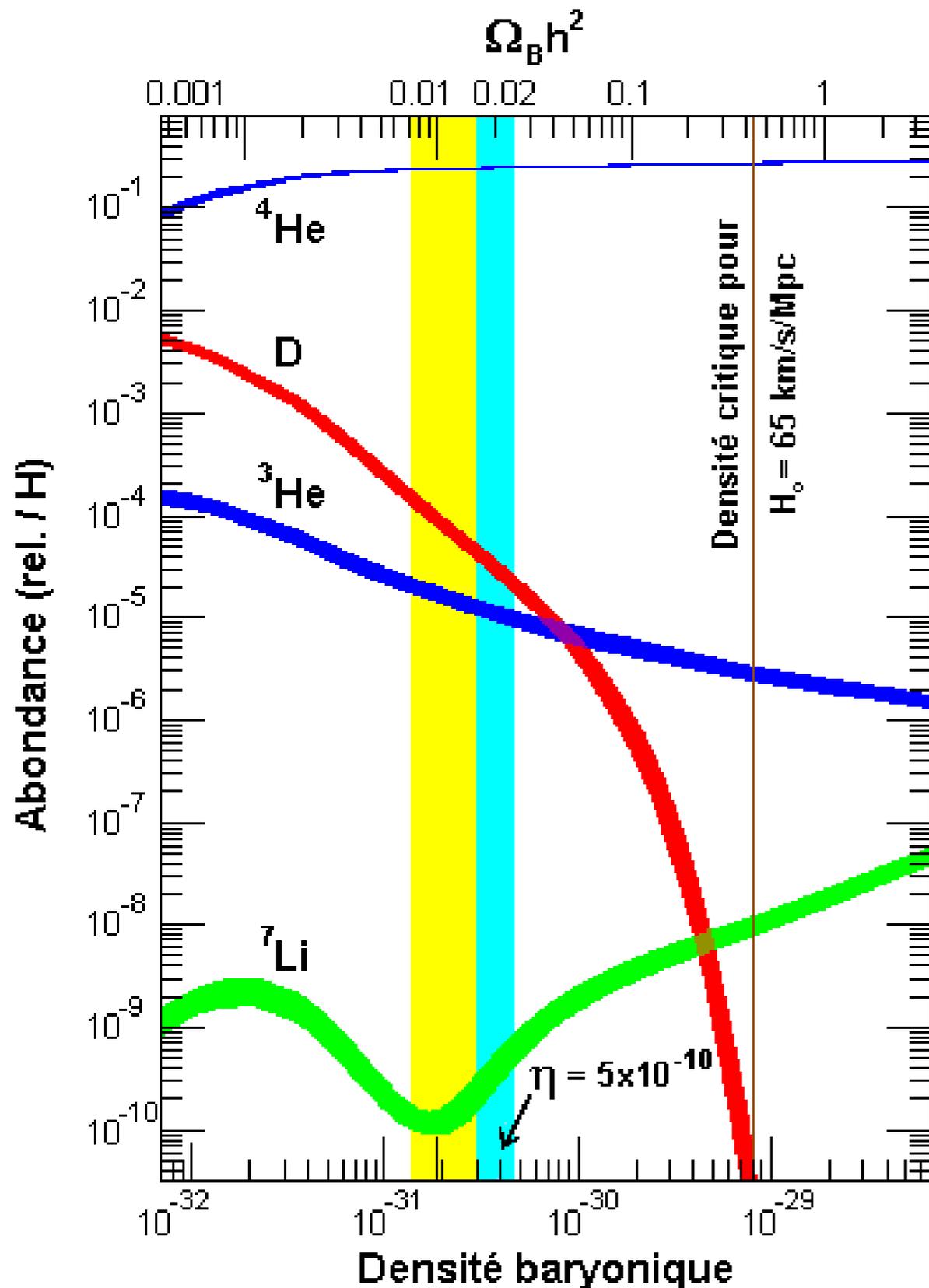
but also ... the suppression of small-scales  
is indicative of the presence of baryons

**Baryons scatters off photons** (which are relativistic and the most abundant particles in the early Universe). They diffuse on large scales, leading to a **deficit of small-scale fluctuations**.

**Based on the Silk damping  
we can conclude that ordinary matter  
cannot dominate the Universe's energy content.**

**yes, so only need 5% of baryons (!?)**

# Baryons in the Universe



**Baryons can be dark but cannot be (all) the dark matter.**

Only ***-5% max*** of baryons

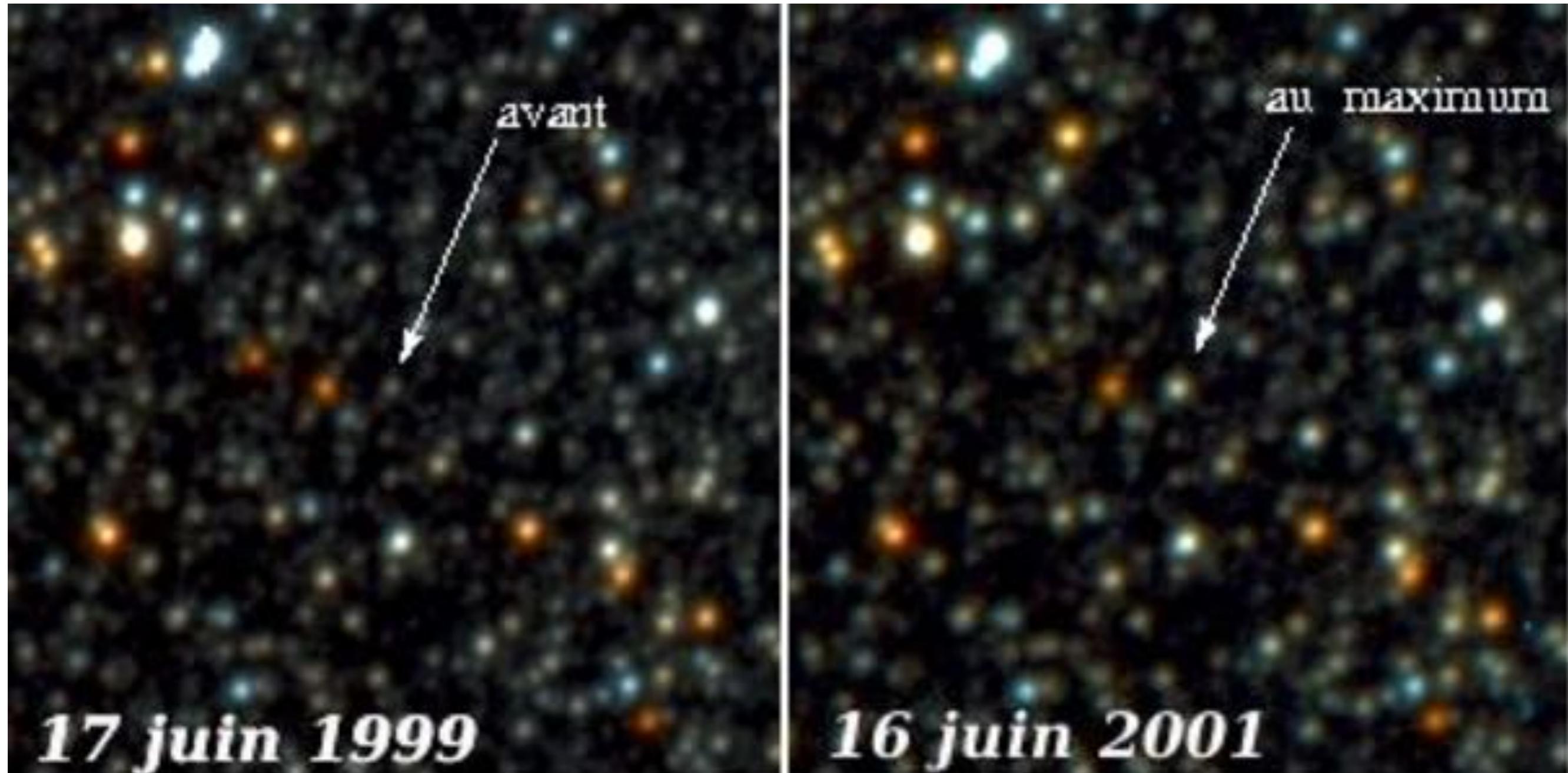
**Consistent with CMB!**

**Where are the baryons??**

# Baryons in the Universe

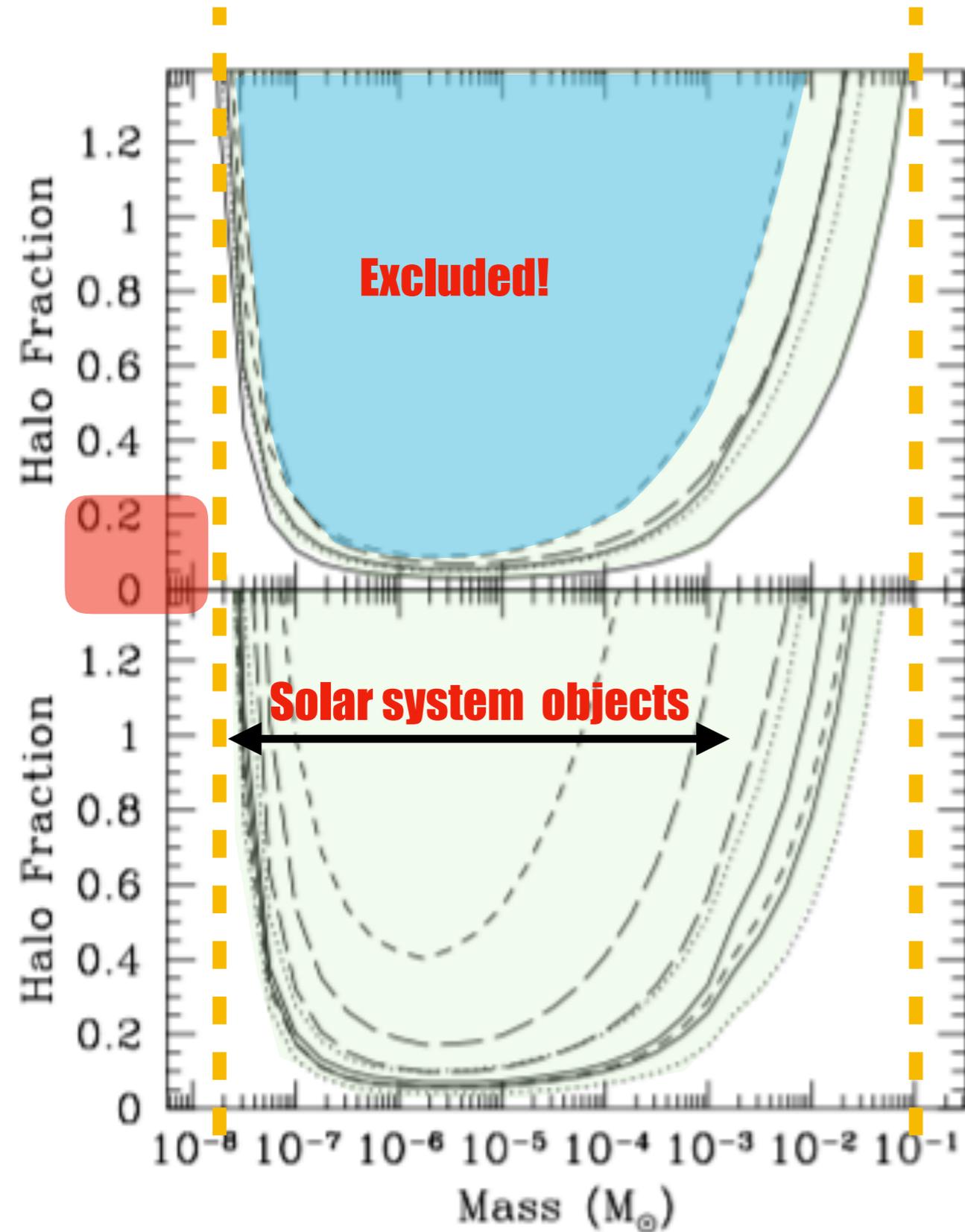
Microensing effect...

Before and two years after (during the maximum of amplification)



Courtesy: EROS experiment. They were looking for "brown dwarfs" or "MACHOs" which belong gravitationally to our Galaxy. This was made possible by their gravitational microlensing effects on stars in the Magellanic Clouds (two dwarf galaxies, Milky Way satellites).

# Is the dark matter made of planets?



## EROS and MACHO

(La Silla vs Mount Stromlo Observatory, Australia)

**Earth**  $3 \cdot 10^{-6} M_{\odot}$

**Jupiter**  $\simeq 10^{-3} M_{\odot}$

**Pluto**  $\simeq 6 \cdot 10^{-8} M_{\odot}$

**MACHO fraction < 10%**

Fig. 3.— Halo fraction upper limit (95% c.l.) versus lens mass for the five EROS models (top) and the eight MACHO models (bottom). The line coding is the same as in Figure 2.

**I.**

**Free (charged) baryons = 5% of the energy content of the Universe.**

**II.**

**We need a collisionless species to help forming structures**

# IS DM a neutrino?

1973

## GRAVITY OF NEUTRINOS OF NONZERO MASS IN ASTROPHYSICS

R. COWSIK\* AND J. MCCLELLAND

Department of Physics, University of California, Berkeley

*Received 1972 July 24*

### ABSTRACT

If neutrinos have a rest mass of a few  $eV/c^2$ , then they would dominate the gravitational dynamics of the large clusters of galaxies and of the Universe. A simple model to understand the virial mass discrepancy in the Coma cluster on this basis is outlined.

*Subject headings:* cosmology — galaxies, clusters of — neutrinos

1977 - Hut, Lee&Weinberg : massive neutrinos would work well

1980 - Zel'dovich et al develop Hot Dark Matter (HDM) theory

# MASSES AND MASS-TO-LIGHT RATIOS OF GALAXIES<sup>1</sup>

*S. M. Faber*<sup>2</sup>

Lick Observatory, Board of Studies in Astronomy and Astrophysics,  
University of California, Santa Cruz, California 95064

*J. S. Gallagher*

Department of Astronomy, University of Illinois, Urbana, Illinois 61801



ARAA 1979

After reviewing all the evidence, it is our opinion that the case for invisible mass in the Universe is very strong and getting stronger. Particularly encouraging is the fact that the mass-to-light ratio for binaries agrees so well with that for small groups. Furthermore, our detailed knowledge of the mass distribution of the Milky Way and Local Group is reassuringly consistent with the mean properties of galaxies and groups elsewhere. In sum, although such questions as observational errors and membership probabilities are not yet completely resolved, we think it likely that the discovery of invisible matter will endure as one of the major conclusions of modern astronomy.

# DM is dead, let us have DM again

.....

**1983** - White, Frenk, Davis: numerical simulations rule out HDM

.....

## Galaxy formation by dissipationless particles heavier than neutrinos

GEORGE F. BLUMENTHAL<sup>1</sup>, HEINZ PAGELS<sup>2</sup> & JOEL R. PRIMACK<sup>3</sup>

<sup>1</sup>Lick Observatory, Board of Studies in Astronomy and Astrophysics, <sup>2</sup>Board of Studies in Physics, University of California, Santa Cruz, California 95064, USA

<sup>3</sup>The Rockefeller University, New York, New York 10021, USA

**In a baryon dominated universe, there is no scale length corresponding to the masses of galaxies. If neutrinos with mass  $<50\text{eV}$  dominate the present mass density of the universe, then their Jeans mass  $M_J \sim 10^{16} M_\odot$ , which resembles supercluster rather than galactic masses. Neutral particles that interact much more weakly than neutrinos would decouple much earlier, have a smaller number density today, and consequently could have a mass  $>50\text{eV}$  without exceeding the observational mass density limit. A candidate particle is the gravitino, the spin 3/2 supersymmetric partner of the graviton, which has been shown<sup>1</sup> to have a mass  $\approx 1\text{keV}$  if stable<sup>2</sup>. The Jeans mass for a 1-keV noninteracting particle is  $\sim 10^{12} M_\odot$ , about the mass of a typical spiral galaxy including the nonluminous halo. We suggest here that the gravitino dominated universe can produce galaxies by gravitational instability while avoiding several observational difficulties associated with the neutrino dominated universe.**

---

## I. Introduction

# End of Brief history

- 1920s-30s — Evidence of missing mass in clusters of galaxies
- 1966s — Peebles&Yu: fluctuations seed structure formation;
- 1966 — Misner: neutrino dissipate on small scales
- 1967 — Silk: baryons also dissipate but on large scales.
- 1970s — Discovery of flat galaxy rotation curves
- 1970s — *Supersymmetry is proposed (1972/1974)*
- 1977 — *Hut, Lee&Weinberg: Relic density for thermal DM particles*
- 1978 — *Gunn, Lee, Lerche, Schramm, Steinman: Heavy stable neutral leptons (WIMPs)*
- 1981 — Davis, Lecar, Prior&Witten: light neutrinos can't make Milky Way-like galaxies
- 1982 — Blumenthal, Pagels&Primack/Peebles: Structure formation for WIMPs
- 1984 — Cosmological simulations of Cold Dark Matter (CDM)
- 1985 — *Goodman&Witten: birth of Direct detection*
- 1986 — *Frukier, Freese&Spergel: Annual modulation*
- 1988 — Indirect detection signatures of DM particles
- 1992 — COBE discovers CMB fluctuations, Peebles was right and so Silk damping...
- 1998 — Accelerated expansion of the Universe: DM only 25% of total
- 2001 — *Official end of LEP; LHC is coming — no Higgs found; no SUSY*
- 2001 — Boomerang measures the 1 peak of CMB. Universe is flat.
- 2003-08 — WMAP and LSS data confirm  $\Lambda$ CDM predictions

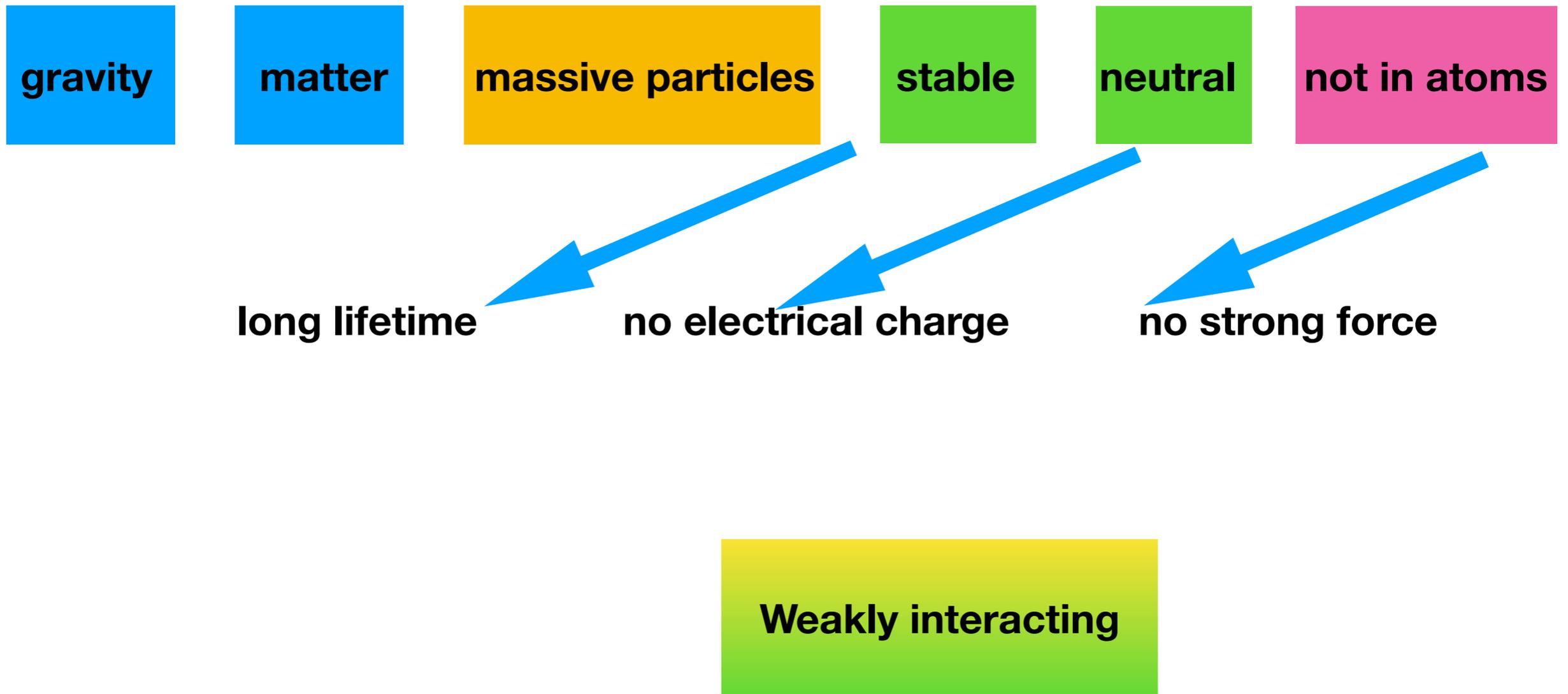
**Loads of progress since but no major discovery**

*From J. Primack's "History of dark matter" but slightly modified*

# Dark Matter and the invisible Universe

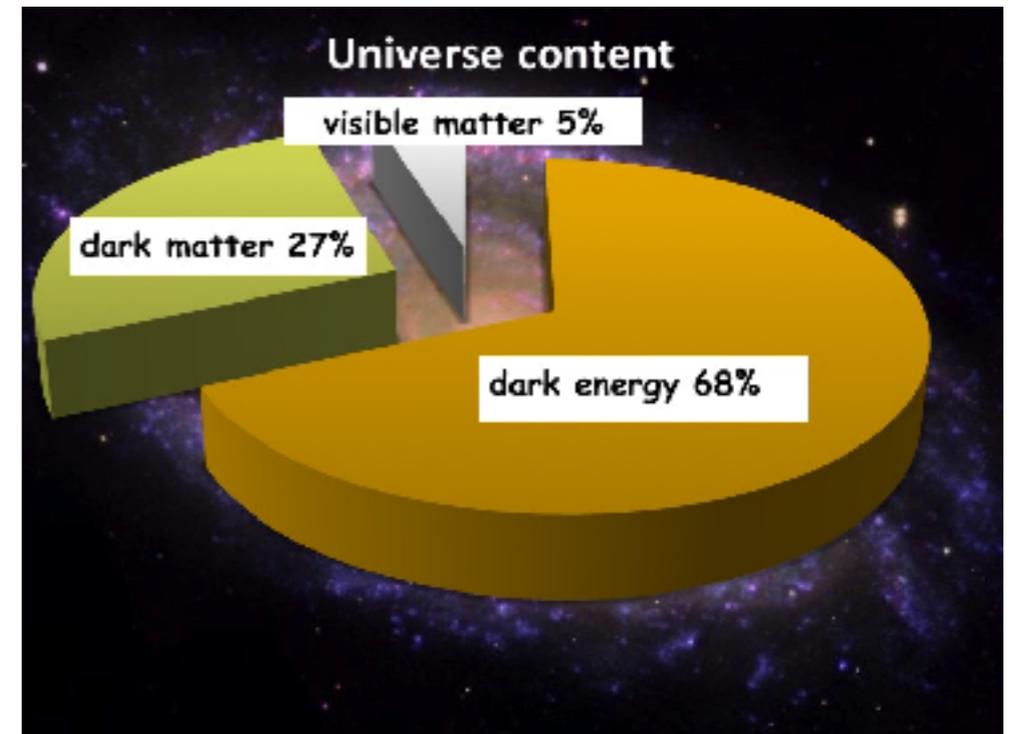
Céline Boehm

# II. A. Particles



# Relic density

Why 27%?



**How many DM particles were produced in the Early Universe?**

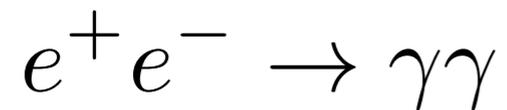
**How much should there be today if DM was made of particles?**

**Does it match observations?**

# Relic density

For the “baryons”

Thermal production



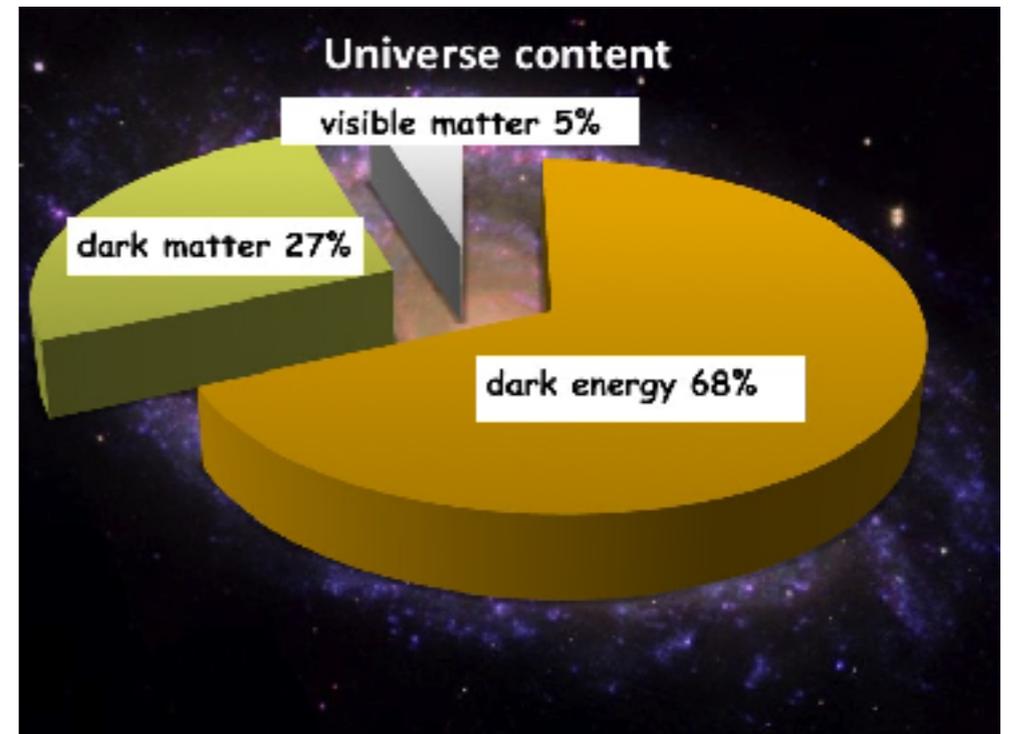
$$\sigma_T \sim 6 \cdot 10^{-25} \text{ cm}^2$$

The annihilation process is so efficient that there would be no electrons left at all

For the Dark Matter

Thermal production but ...

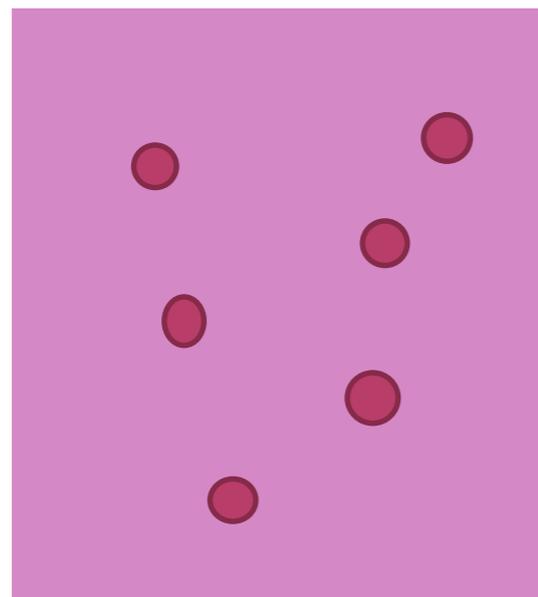
No asymmetry! but ...



Asymmetry

non-thermal, freeze-in

# Relic density



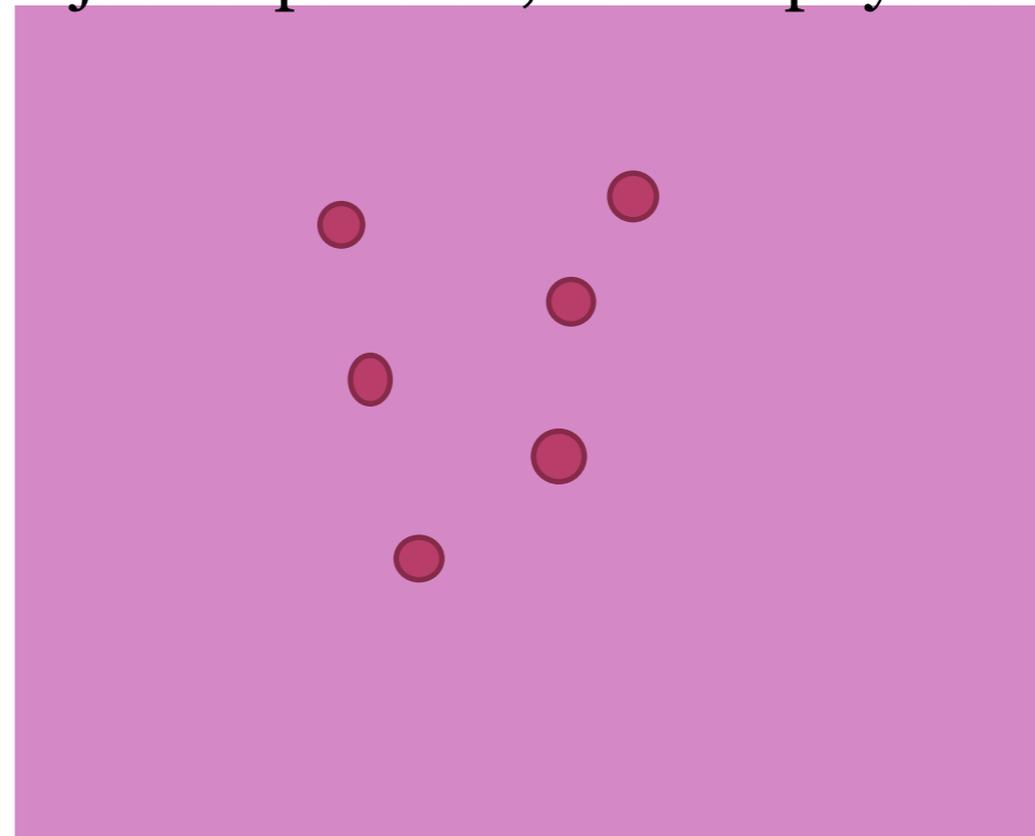
Early Universe

$$N = \#/\text{volume}$$

Expansion of the Universe



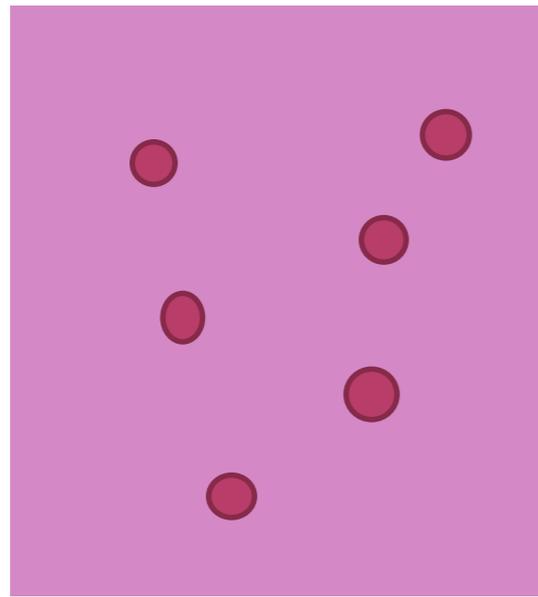
just expansion, no DM physics



Late Universe

**Massive DM particles can overclose the Universe!**

# Relic density

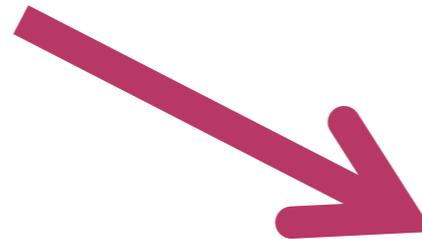


Early Universe

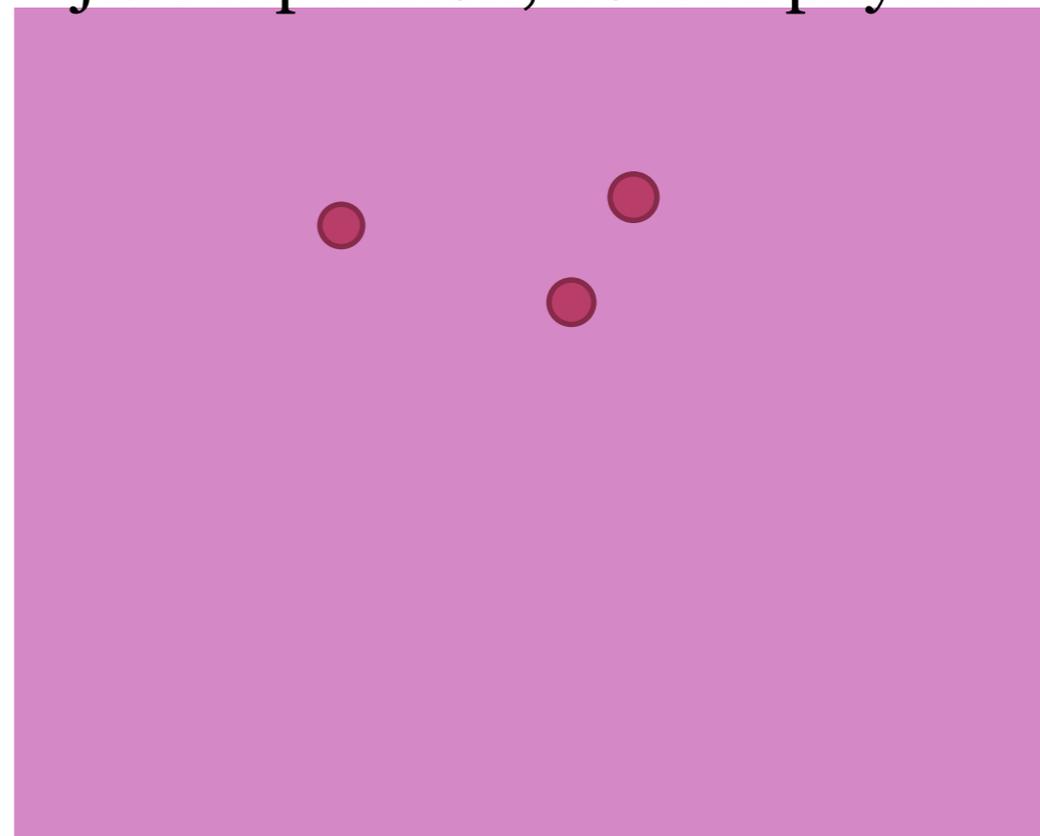
Expansion of the Universe



3 H



just expansion, no DM physics



Late Universe

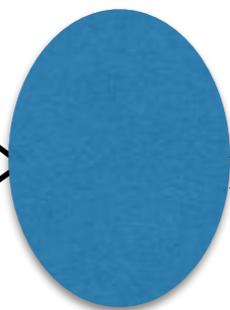
$$N = \#/\text{volume}$$

DM

$f^-$

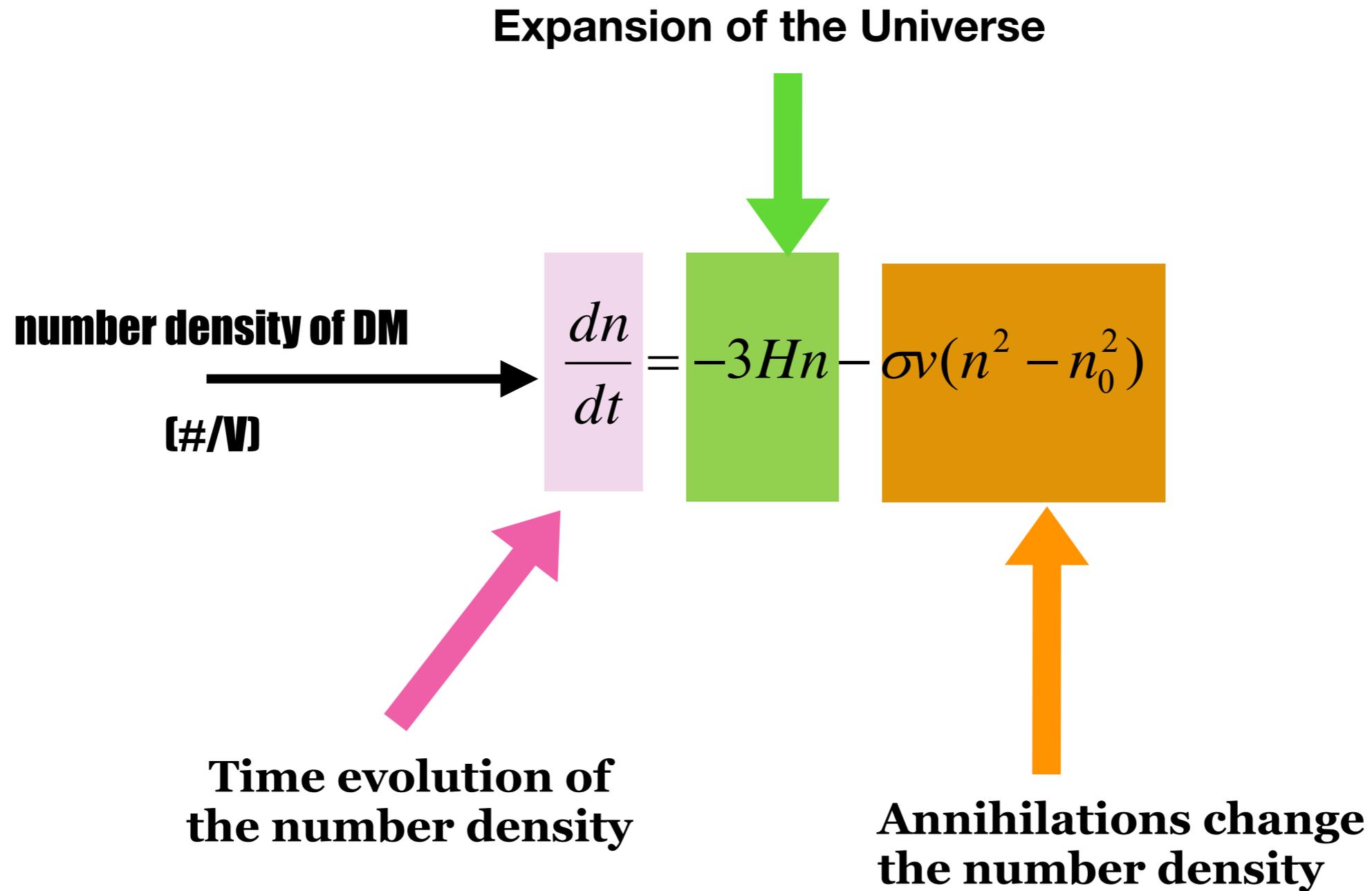
DM

$f^+$



**Number is reduced due to annihilations**

# The Boltzmann equation



# Deriving the Boltzmann equation

$$\frac{df}{d\lambda} = C(f)$$

$$\frac{df}{d\lambda} = \frac{\partial f}{\partial x^\mu} \frac{dx^\mu}{d\lambda} + \frac{\partial f}{\partial p^\nu} \frac{dp^\nu}{d\lambda} = p^\mu \frac{\partial f}{\partial x^\mu} - \Gamma^\nu_{\alpha\beta} p^\alpha p^\beta \frac{\partial f}{\partial p^\nu}$$

using  $\frac{dp^\nu}{d\lambda} + \Gamma^\nu_{\alpha\beta} p^\alpha p^\beta = 0$

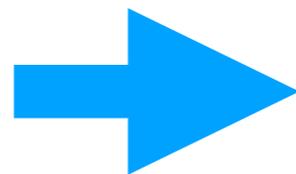
Isotropic Universe

$$p^i \frac{\partial f}{\partial x^i} = 0$$

$$\frac{df}{d\lambda} = E \frac{\partial f}{\partial t} - \Gamma^0_{\alpha\beta} p^\alpha p^\beta \frac{\partial f}{\partial E}$$

$$E \frac{\partial f}{\partial t} - \Gamma^0_{\alpha\beta} p^\alpha p^\beta \frac{\partial f}{\partial E} = C(f)$$

$$\frac{\partial f}{\partial t} - H \frac{E^2 - m^2}{E} \frac{\partial f}{\partial E} = \frac{1}{E} C(f)$$

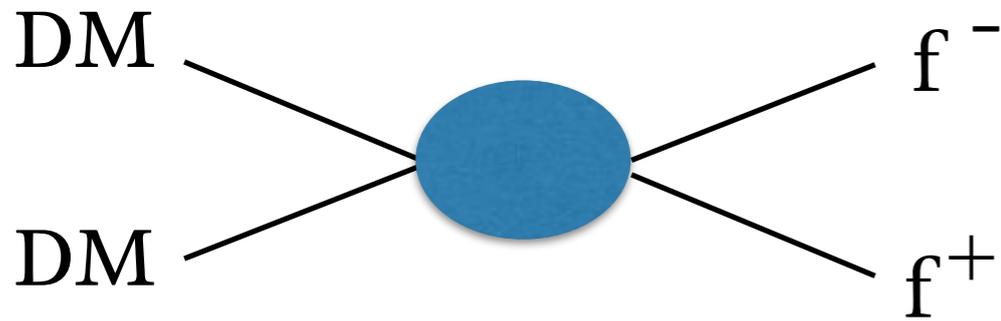


$$\frac{g}{(2\pi)^3} \int \left( \frac{\partial f}{\partial t} - H \frac{E^2 - m^2}{E} \frac{\partial f}{\partial E} \right) d^3 p = \frac{g}{(2\pi)^3} \int \frac{1}{E} C(f) d^3 p.$$

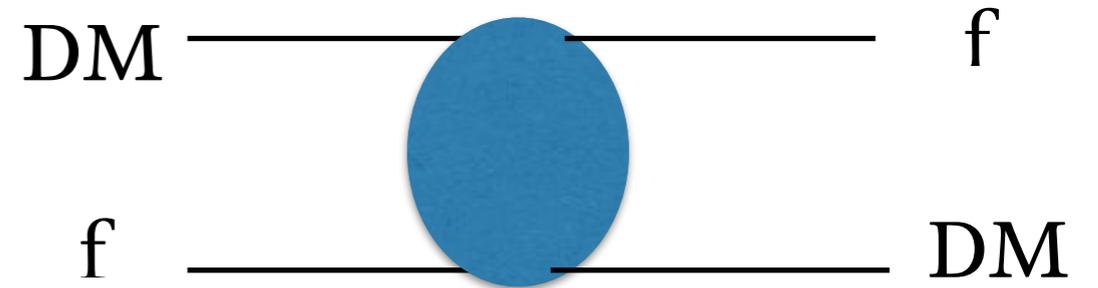
$$\frac{\partial n}{\partial t} + 3Hn = \frac{g}{(2\pi)^3} \int \frac{1}{E} C(f) d^3 p.$$

# Deriving the Boltzmann equation

$$\frac{\partial n}{\partial t} + 3Hn = \frac{g}{(2\pi)^3} \int \frac{1}{E} C(f) d^3 p.$$



annihilations; change the number density



elastic scattering; do not change density



Non-relativistic transition

expansion won

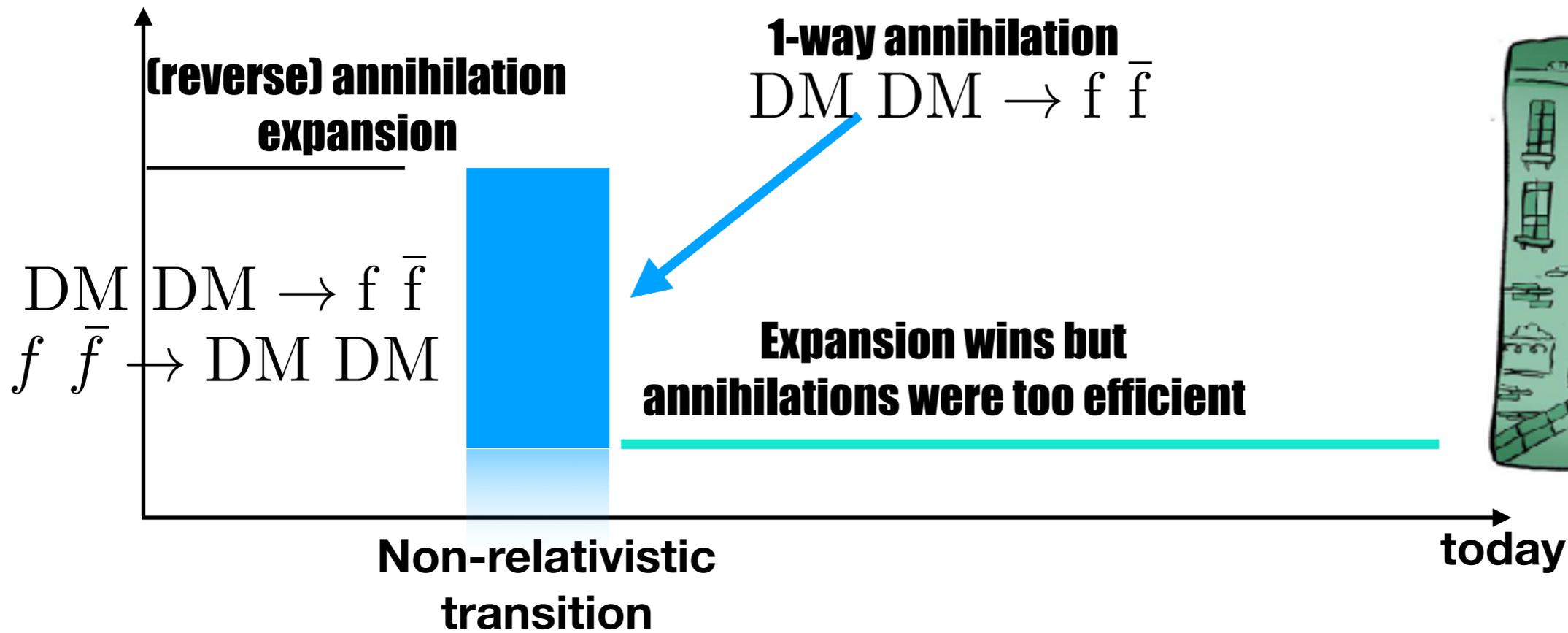
time

$$C(f) = -\frac{1}{2} \sum_{\text{spins}} \int \left[ f f_2 (1 \pm f_3) (1 \pm f_4) |\mathcal{M}_{12 \rightarrow 34}|^2 - f_3 f_4 (1 \pm f) (1 \pm f_2) |\mathcal{M}_{34 \rightarrow 12}|^2 \right] \\ (2\pi)^4 \delta^4(p + p_2 - p_3 - p_4) \frac{d^3 p_2}{(2\pi)^3 2E_2} \frac{d^3 p_3}{(2\pi)^3 2E_3} \frac{d^3 p_4}{(2\pi)^3 2E_4}$$

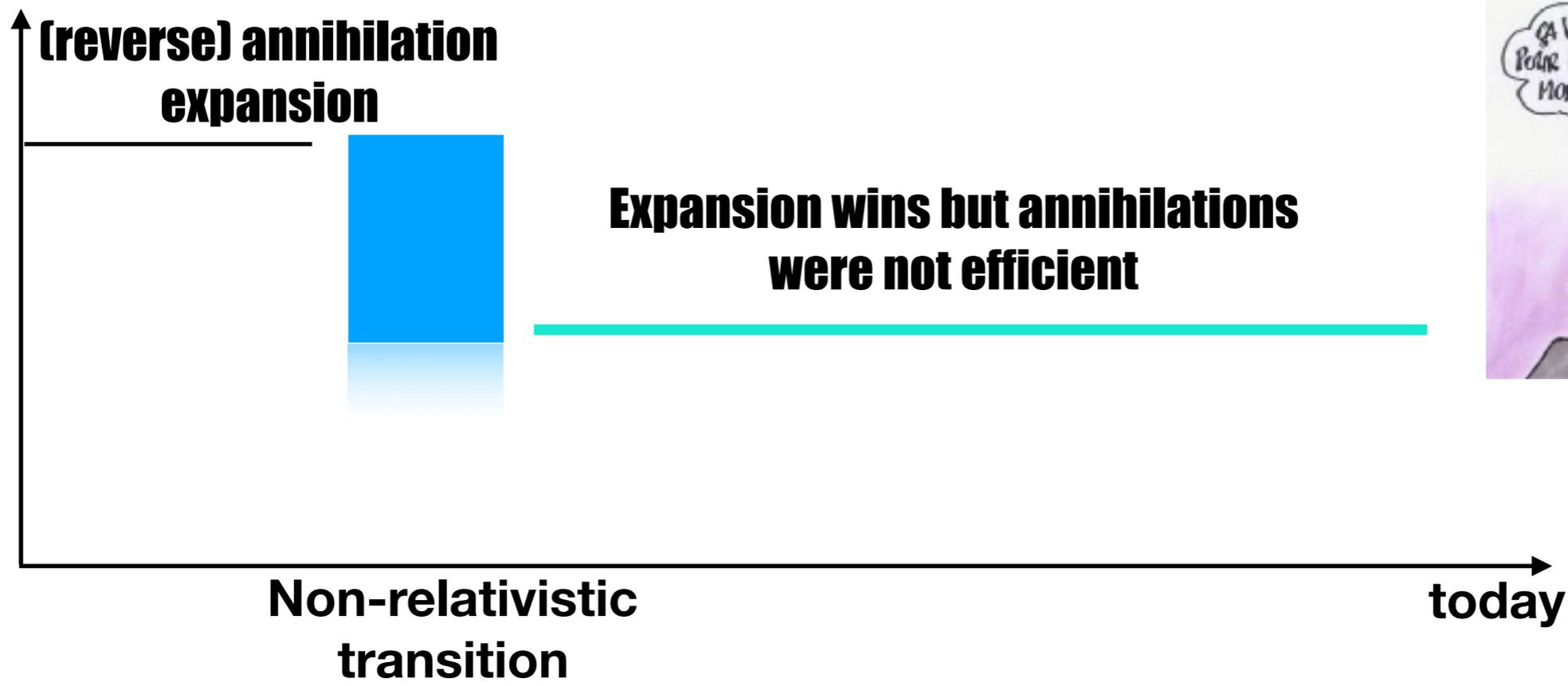
$$\dot{n} = -3Hn - \langle \sigma v \rangle (n^2 - n_{eq}^2)$$

# Boltzmann equation caught in the act

number of particles

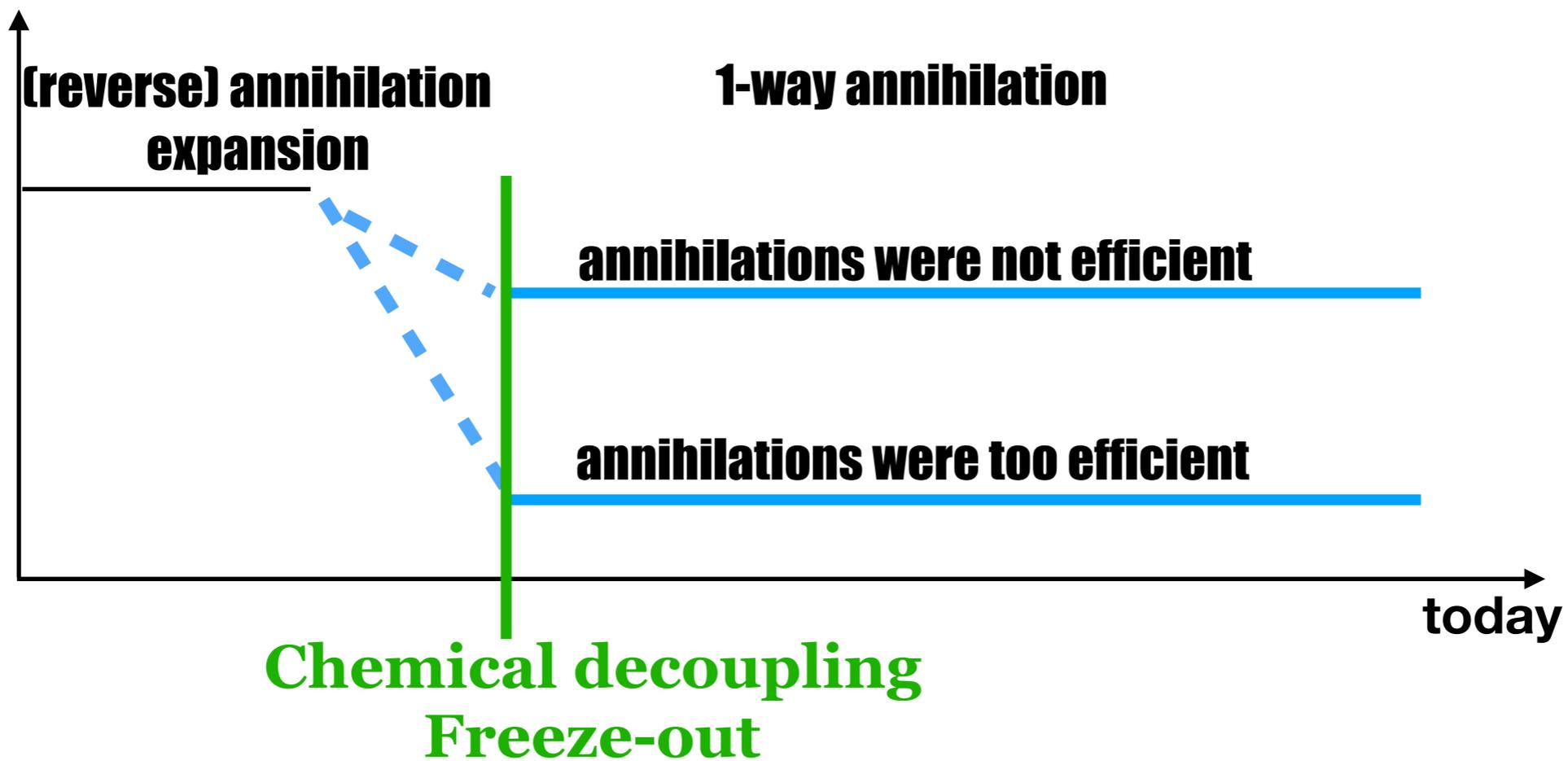


number of particles



# Boltzmann equation caught in the act

number of particles



**Only one cross section gives the observed number of DM particles!**

Interactions maintaining the **thermal equilibrium can continue**

$$\frac{dn}{dt} = -3Hn - \sigma v (n^2 - n_0^2)$$

$$\sigma v n_{DM}^2 \simeq H n_{DM}$$



$$\sigma v n_{DM} \simeq H$$

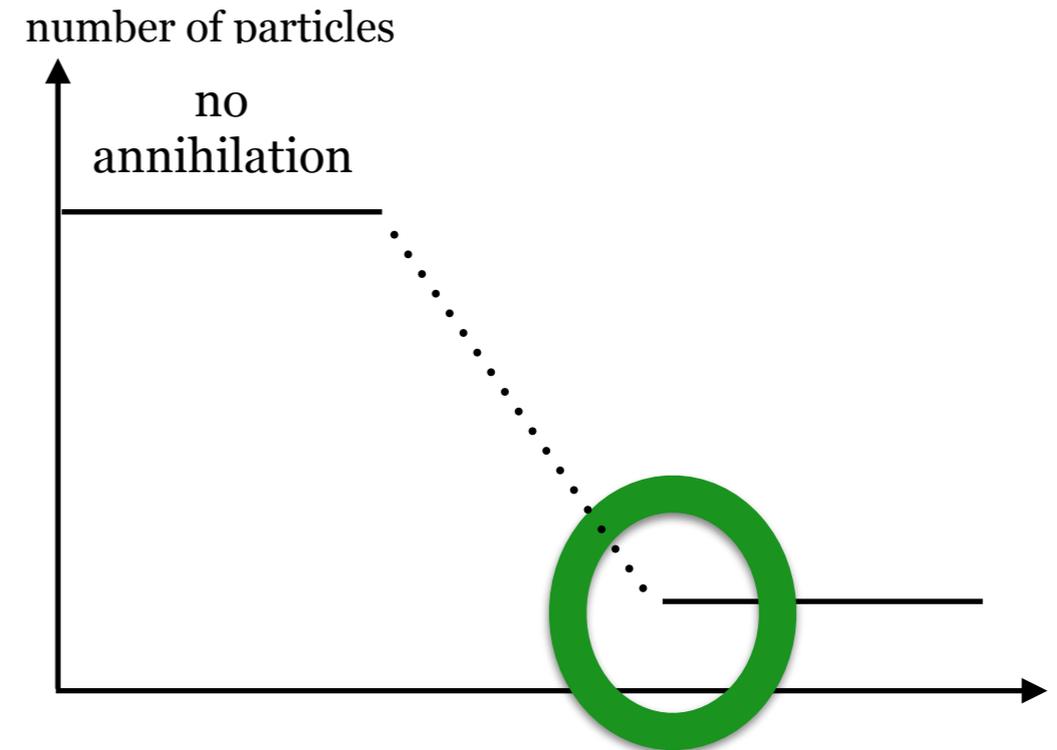
# Analytical solution

$$\langle \sigma v \rangle n_{\text{DM}} = H$$

$$n_{\text{DM}} a^3 = n_{\text{DM},0} a_0^3$$

$$a(T) = \frac{T_0}{T} \quad \text{and} \quad H = H_r T^2$$

$$n_{\text{DM},0} = \frac{H_r}{\langle \sigma v \rangle} \frac{T_0}{T_{fo}}$$



$$\Omega_0 = \frac{\rho_{\text{DM},0}}{\rho_{c,0}} \quad \longrightarrow \quad \Omega_0 = \frac{n_{\text{DM},0}}{\rho_{c,0}} m_{\text{DM}} \quad \longrightarrow \quad \Omega_0 = \frac{H_r}{\rho_{c,0}} \frac{T_0}{\langle \sigma v \rangle} \frac{m_{\text{DM}}}{T_{fo}}$$

$x_{fo}$

**At freeze-out, the density obeys Boltzmann statistics**

$$n(T) \propto (m_{\text{DM}} T)^{3/2} e^{-\frac{m_{\text{DM}}}{T}} \quad n_{\text{DM},0} = \frac{H_r}{\langle \sigma v \rangle} \frac{T_0}{T_{fo}} \quad x_{fo}^{-1} \simeq \ln \frac{\langle \sigma v \rangle T_0^2 m}{H_\alpha (2\pi)^{3/2} \sqrt{x_{fo}}}$$

$$x_{fo} \approx 12 + (\approx 2) \log \left( \frac{m_{dm}}{\text{MeV}} \times \frac{\sigma v}{3.10^{-26} \text{ cm}^3 / \text{s}} \right)$$

# Numerical solution

Numerically: ★ re-write Boltzmann to remove  $T^3$  factors in number density by using  $n = y T^3$

$$\frac{dy}{dt} = -\sigma v \times (y^2 - y_0^2) \times T^3$$

★ solve  $dy/dT$  instead of  $dy/dt$

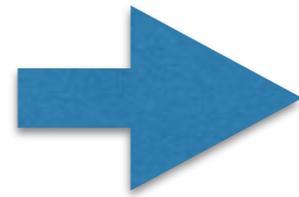
$$\frac{dy}{dT} = \frac{\sigma v}{2t_r T_0^2} \times (y^2 - y_0^2)$$

Tempted to use:  $\frac{y_{i+1} - y_i}{\Delta T} = \Lambda \times (y^2 - y_0^2)$  ???

$$\frac{y_{i+1} - y_i}{\Delta T} = \frac{\Lambda}{2} \times \left[ (y_i^2 - y_{0_i}^2) + (y_{i+1}^2 - y_{0_{i+1}}^2) \right]$$

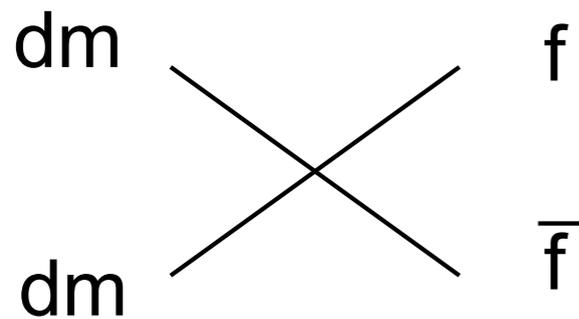
# The Hut, Lee&Weinberg argument

$$\frac{dn}{dt} = -3Hn - \sigma v (n^2 - n_0^2)$$

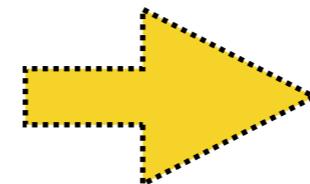


$$\Omega h^2 \simeq \frac{3 \times 10^{-27} \text{ cm}^3 / \text{s}}{\langle \sigma v \rangle}$$

$$\sigma v \sim 3 \times 10^{-26} \text{ cm}^3 / \text{s}$$



$$\sigma v \propto \frac{m_{\text{dm}}^2}{m_w^4}$$



$$\Omega_{\text{DM}} h^2 \propto m_{\text{DM}}^{-2}$$

**Dark Matter needs to be heavier than a proton to not over close the Universe**

